

Review on Kaon decays

Durham 14 years later

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Outline

- Beautiful decays: K_{l3} and related
- Interplay Long -Short : $K_L \rightarrow \pi^0 e e$
- Chiral Perturbation theory tests

Many thanks to B. Sciascia, M. Moulson and
Flavianet people

$K \rightarrow \pi l \nu$ and CKM unitarity

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 \quad V_{ub} \text{ negligible}$$

- Superallowed transitions $\implies |V_{ud}| = 0.9738 \pm 0.0003 \xrightarrow{\text{Unit.}}$

$$|V_{us}|^{\text{Unit.}} = 0.2275 \pm 0.0012$$

$$|V_{us}|^{\text{PDG04}} = 0.2196 \pm 0.0026$$

Leutwyler, Roos

$$|V_{us}|^{\text{PDG06}} = 0.2257 \pm 0.0021$$

$$|V_{us}|^{\text{Flavianet}} = 0.22461 \pm 0.00048$$

All K's

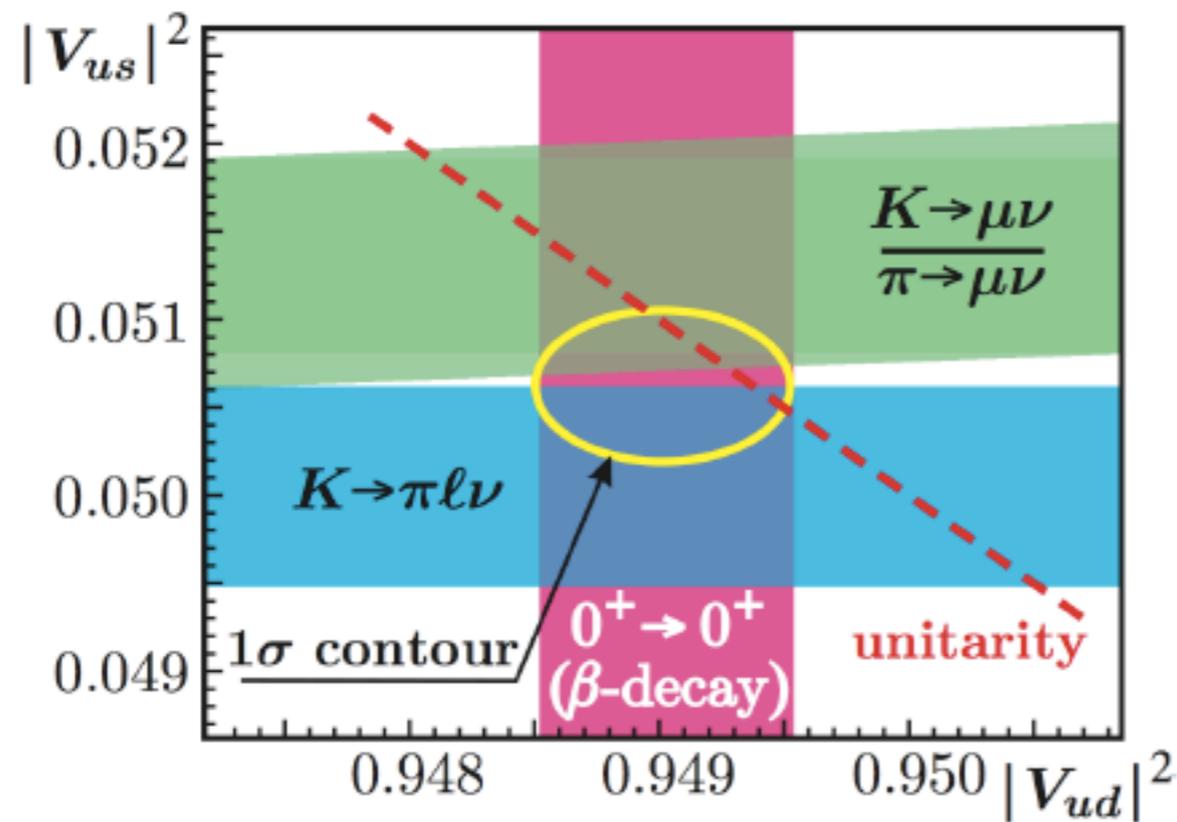
$$\Gamma(K_{l3}^i) = \mathcal{N}_i |V_{us}|^2 |f_+(0)|^2 (1 + \delta_{rad}^l) I(\lambda_+, \lambda_0)$$

- Kaon revolution in 2004-2005: BNL E865, ISTRA, KTeV, NA48, KLOE $\Gamma(K_{l3}^i)$ all increased by 6% All Major KL BRs Changed! ϵ_K changed by 3.7σ
- After 06 NA48, KLOE improvements in semileptonic BRs
- NA48, KLOE $R_K = \Gamma(K_{e2})/\Gamma(K_{\mu2})$
- Better understanding theoretically of the form factor $f_{+,0}(t) = f_+(0)(1 + \lambda_{+,0}t/m_\pi^2)$ (see [Passemar](#))
- Lattice $f_+(0) = 0.9644(49)$ RBC-UKQCD DW Lattice (see [Jüttner, Colangelo](#))

- TH radiat./isospin breaking corr. δ_{rad}^l known accurately **BUT** Chiral Pert Th. + Large N $\longrightarrow f_+(0) = 0.984(12)$ (see Neufeld)



CKM unitarity



V_{us} K_{l3}

$V_{us} V_{ud}$ $K_{\mu 2} / \pi_{\mu 2}$

V_{ud} $0^+ \rightarrow 0^+ \beta$ decay
(HardyTowner07)

New value available

$$|V_{us}| = 0.2249 \pm 0.0010$$

$$|V_{ud}| = 0.97418 \pm 0.00026$$

$$1 - |V_{us}|^2 - |V_{ud}|^2 = 0.0004 \pm 0.0007$$

Was 0.0031 ± 0.0015 in PDG04

KLOE-Sibidanov-CKM

Experimental evaluation of $f_+(0)$ and f_{K^*}/f_π

Matthew Moulson and Barbara Sciascia
LNF-INFN

for the FlaviaNet Working Group on Kaon decays

*prepared for the FlaviaNet meeting,
Durham, 22-26 September 2008*

- Use $K\mu^2/\pi\mu^2$ ratio to evaluate $f_K/f_\pi/f_+(0)$ by fitting with experimental inputs

$$\frac{\Gamma(K_{\mu^2(\gamma)})}{\Gamma(\pi_{\mu^2(\gamma)})} = \frac{|V_{us}|^2}{|V_{ud}|^2} \times \frac{f_K^2}{f_\pi^2} \times \frac{M_K(1-m_\mu^2/M_K^2)^2}{m_\pi(1-m_\mu^2/m_\pi^2)^2} \times (1+\alpha/\pi(C_K-C_\pi))$$

- use RBC-UKQCD07 $f_+(0) = 0.9644(49)$ as reference th. value;
- use HPQCD-UKQCD07 $f_K/f_\pi = 1.189(7)$ as reference th. value.
- Details of the experimental inputs:
 - $|V_{us} \times f_+(0)|$: FlaviaNet average;
 - Theoretical corrections entering $|V_{us} \times f_+(0)|$ value;
 - $|V_{ud}|$ from nuclear β -decays;
 - Theoretical corrections entering V_{ud} value;
 - Kinematical factor and its theoretical corrections.
- Definition of fit constraints.
- Outputs for different fit configurations.

Definition of the experimental inputs

$$\frac{\Gamma(K_{\mu 2}(\gamma))}{\Gamma(\pi_{\mu 2}(\gamma))} = \frac{|V_{us}|^2}{|V_{ud}|^2} \times \frac{f_K^2}{f_\pi^2} \times \frac{M_K(1-m_\mu^2/M_K^2)^2}{m_\pi(1-m_\mu^2/m_\pi^2)^2} \times (1+\alpha/\pi(C_K-C_\pi))$$

C: constant, including corrections.

$$\frac{\Gamma(K_{\mu 2}(\gamma))}{\Gamma(\pi_{\mu 2}(\gamma))} = \frac{|V_{us} f_+(0)|^2}{|V_{ud}|^2} \times \frac{1}{f_+(0)^2} \frac{f_K^2}{f_\pi^2} \times C$$

From decay rates

From K13

From nucl. β -decay

- $|V_{us} f_+(0)| = 0.2167(5)$
- $|V_{ud}| = 0.97425(23)$
- $\Gamma(K_{\mu 2}) / \Gamma(\pi_{\mu 2}) / C = 0.076197(322)$

Use FlaviaNet@CKM08 value:

$$|V_{us}| f_+(0) = 0.2167(5) \quad \chi^2/\text{ndf} = 2.83/4 \text{ (59\%)}$$

Only experimental inputs (BRs, lifetimes, form factors) with the exception of **theoretical estimations** of:

- **em corrections** from ChPT $O(e^2 p^2)$ with detailed error matrix (Cirigliano, Giannotti, and Neufeld, 0807.4507[hep-ph])
- **SU(2) breaking corrections.**

	$\delta_{\text{SU}(2)}^{\text{K}}(\%)$	$\delta_{\text{em}}^{\text{K}^\ell}(\%)$		$K^0 e3$	$K^0 \mu3$	$K^+ e3$	$K^+ \mu3$	
$K^0 e3$	0	+0.50(11)	$K^0 e3$	1	0.69	0.08	-0.15	values used to extract $ V_{us} f_+(0)$
$K^0 \mu3$	0	+0.70(11)	$K^0 \mu3$		1	-0.15	0.08	
$K^+ e3$	+2.36(22)	+0.05(13)	$K^+ e3$			1	0.76	
$K^+ \mu3$	+2.36(22)	+0.01(12)	$K^+ \mu3$				1	

V_{ud} from nuclear β -decay: $V_{ud} = 0.97425(23)$ presented by Towner at CKM08;
 - total fractional error at **0.2 per mil**;
 - new review paper in preparation [Hardy and Towner]

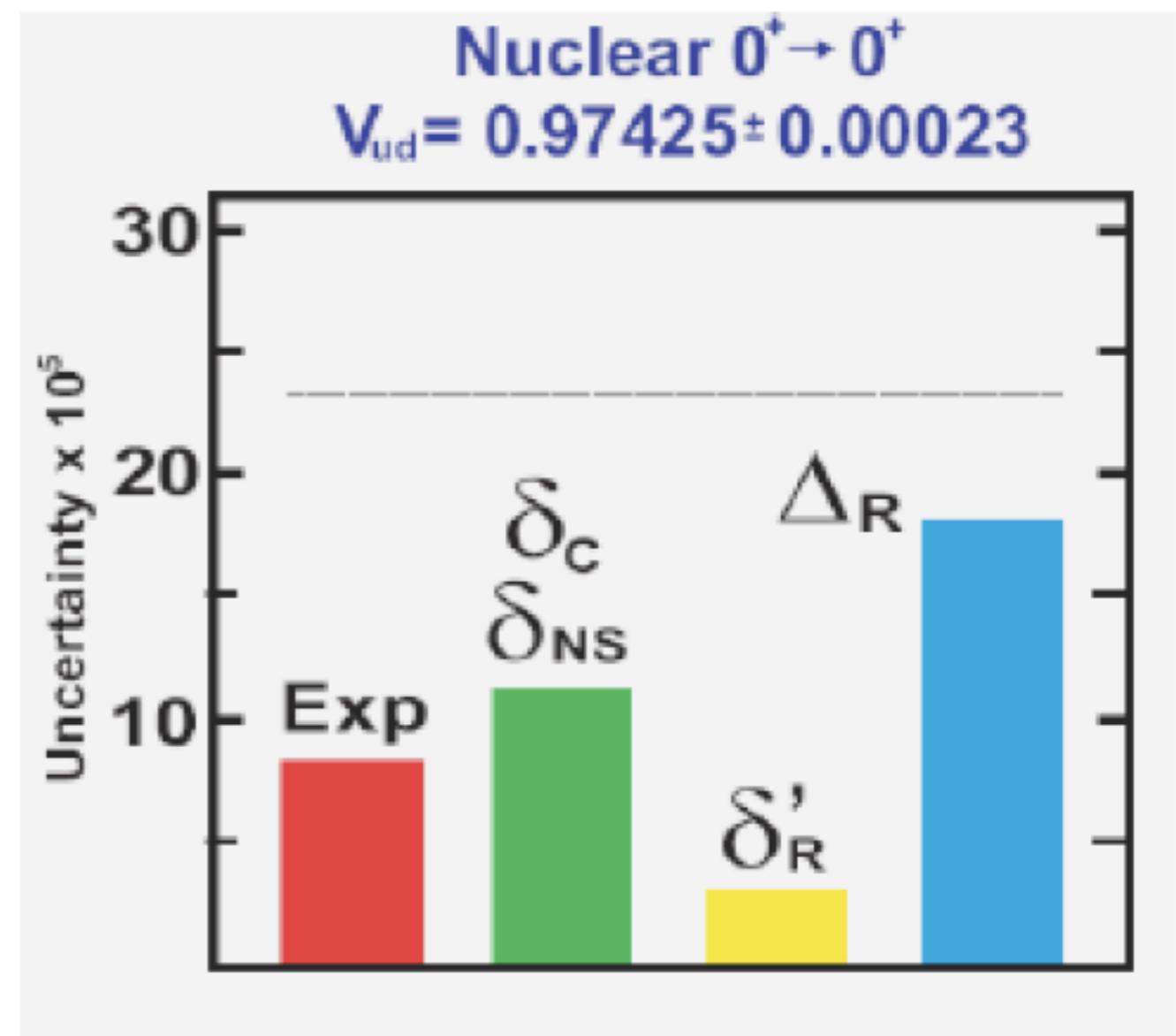
- **Theoretical contributions** to the V_{ud} determination:

δ_C : SU(2) breaking corrections

δ_{NS} : “small” nuclear-structure dependent component

δ'_R : “trivially” nucleus-dependent component

Δ_R : nucleus-independent component



$$\frac{\Gamma(K_{\mu 2(\gamma)})}{\Gamma(\pi_{\mu 2(\gamma)})} = \frac{|V_{us}|^2}{|V_{ud}|^2} \times \frac{f_K^2}{f_\pi^2} \times \frac{M_K(1-m_\mu^2/M_K^2)^2}{m_\pi(1-m_\mu^2/m_\pi^2)^2} \times (1+\alpha/\pi(C_K-C_\pi))$$

C: constant, including corrections.

$$\Gamma(K_{\mu 2})/\Gamma(\pi_{\mu 2})/C = 0.076197(322)$$

- K lifetime and BR(K μ 2) from FlaviaNet
- π lifetime and BR($\pi\mu$ 2) from PDG08
- masses from PDG08.

Theoretical contributions: radiative corrections [Marciano, hep-ph/0402299]

- C_K and C_π include short-distance EW effects and long-distance radiative corrections.
- use the difference: $C_K - C_\pi = 3.0 \pm 1.5$ [e.g. Finkemeier, hep-ph/9412267]
- conservative estimate of the error;
- dominant error contribution from hadronic structure dependent radiative corrections.

$$\frac{\Gamma(K_{\mu 2(\gamma)})}{\Gamma(\pi_{\mu 2(\gamma)})} = \frac{|V_{us} f_+(0)|^2}{|V_{ud}|^2} \times \frac{1}{f_+(0)^2} \frac{f_K^2}{f_\pi^2} \times C$$

From decay rates

From Kl3

From nucl. β -decay

Straight calculation from $K\mu 2/\pi\mu 2$ relation and **assuming SM**:

- $f_K/f_\pi / f_+(0) = 1.2409(46)$
- using $f_+(0) = 0.9644(49)$ [RBC-UKQCD07] obtain $f_K/f_\pi = 1.1967(75)$
- using $f_K/f_\pi = 1.189(7)$ [HPQCD-UKQCD07] obtain $f_+(0) = 0.9582(67)$

Experimental and theoretical evaluations agree to within $\sim 1\sigma$.

$$\frac{\Gamma(K_{\mu 2(\gamma)})}{\Gamma(\pi_{\mu 2(\gamma)})} = \frac{|V_{us} f_+(0)|^2}{|V_{ud}|^2} \times \frac{1}{f_+(0)^2} \frac{f_K^2}{f_\pi^2} \times C$$

Assuming SM

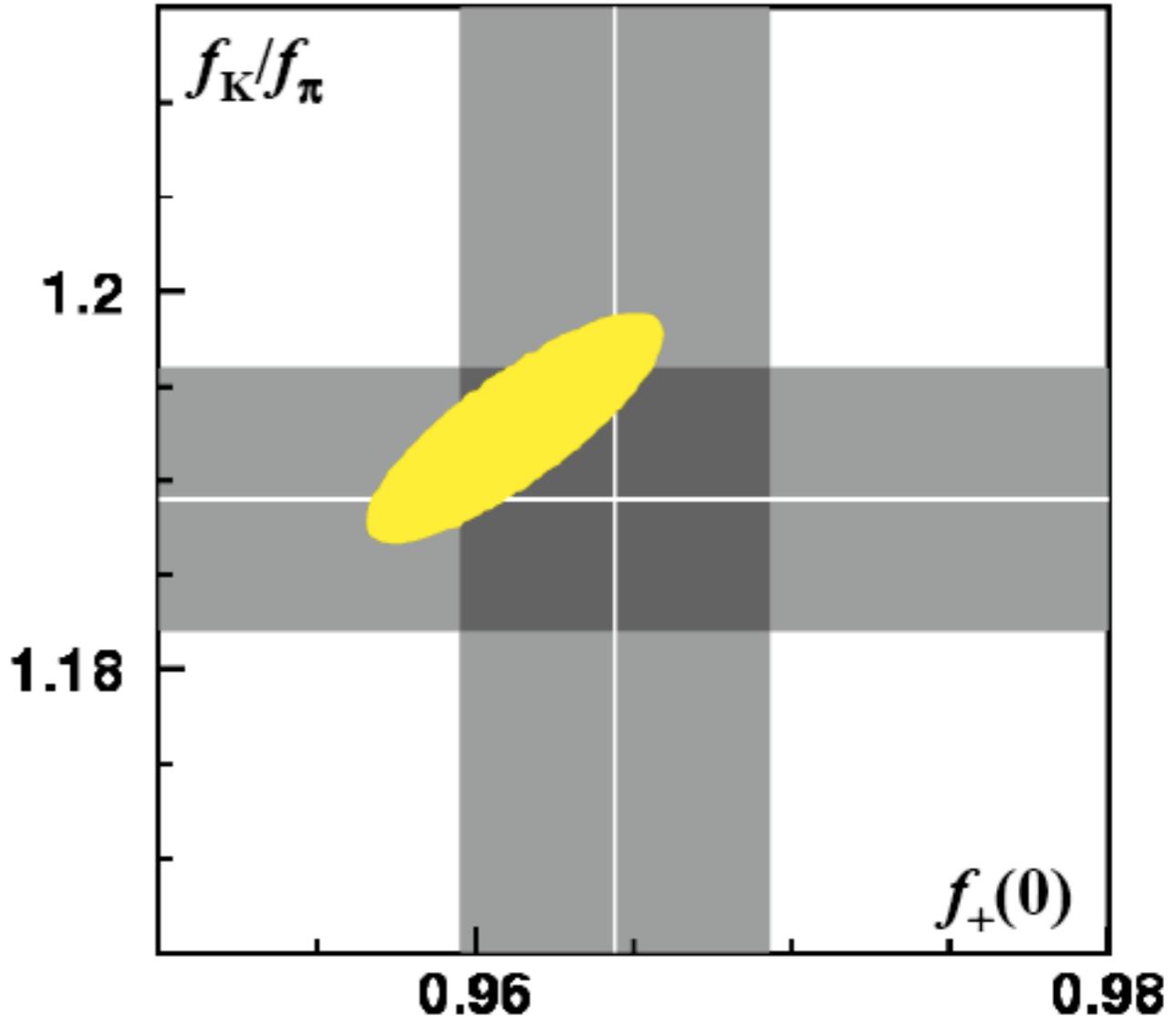
From decay rates From Kl3 From nucl. β -decay

- Obtain f_K/f_π and $1/f_+(0)$ values from a fit.
- 5 parameters: V_{ud} , $V_{us}f_+(0)$, $\Gamma(K_{\mu 2}/\pi_{\mu 2})/C$, f_K/f_π and $f_+(0)$.
 - 3 inputs: V_{ud} , $V_{us}f_+(0)$, $\Gamma(K_{\mu 2}/\pi_{\mu 2})/C$
 - 2 constraints:

$\Gamma(K_{\mu 2})/\Gamma(\pi_{\mu 2})$ relation and Unitarity

- Obtain:
 - $f_K/f_\pi = 1.1928(61)$ and $f_+(0) = 0.9612(47)$
 with a correlation of 0.82 (complete correlation matrix available)

- Very good agreement with th. estimations:
 - $f_K/f_\pi = 1.189(7)$ and $f_+(0) = 0.9644(49)$.



$$\frac{\Gamma(K_{\mu 2(\gamma)})}{\Gamma(\pi_{\mu 2(\gamma)})} = \frac{|V_{us} f_+(0)|^2}{|V_{ud}|^2} \times \frac{1}{f_+(0)^2} \frac{f_K^2}{f_\pi^2} \times C$$

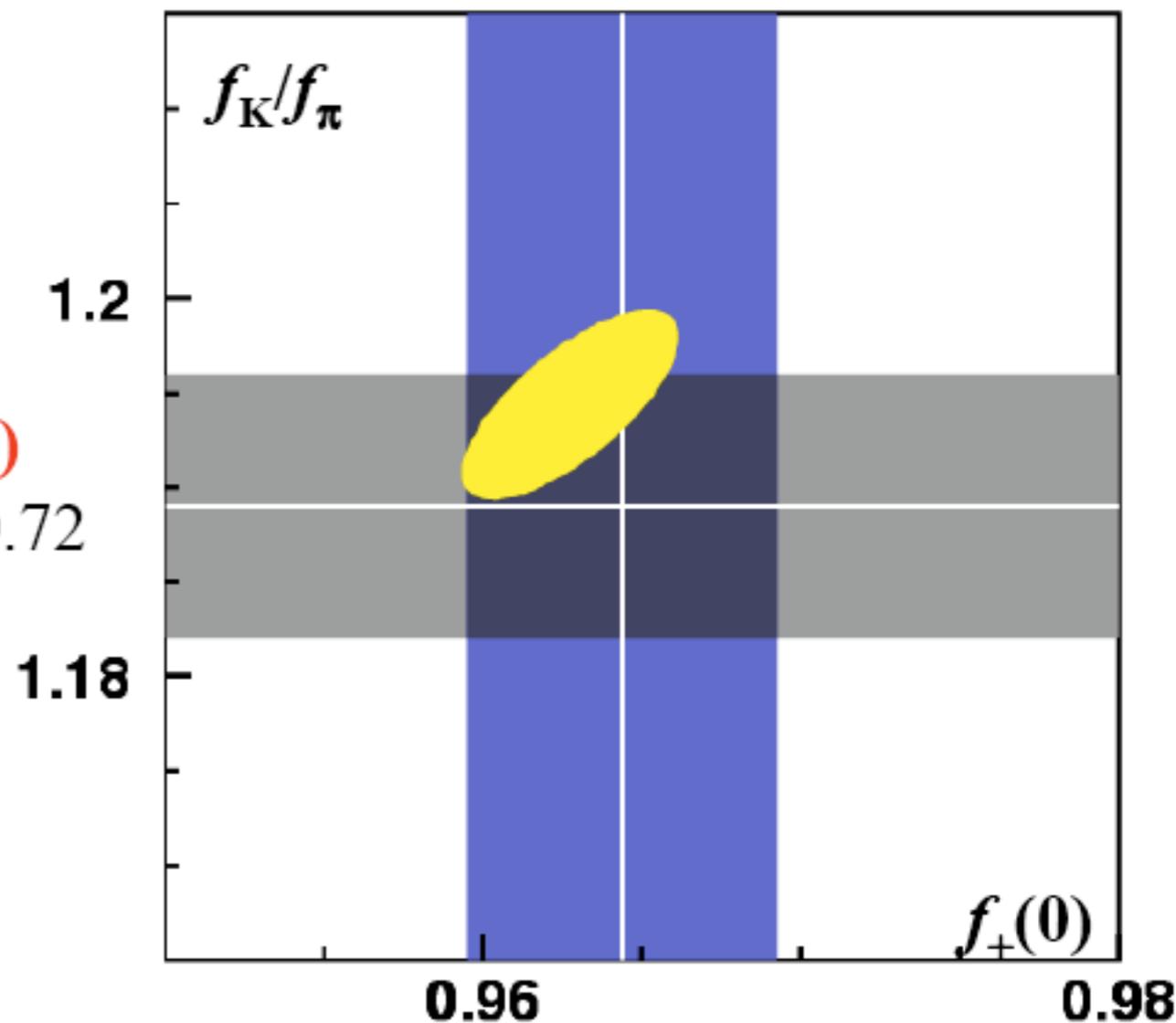
Assuming SM

From decay rates From Kl3 From nucl. β -decay

- Obtain f_K/f_π and $f_+(0)$ values from a fit:
 - one more input: $f_+(0) = 0.9644(49)$
 - 2 constraints:
 - $\Gamma(K\mu 2)/\Gamma(\pi\mu 2)$ relation and Unitarity.

- Obtain:
 - $f_K/f_\pi = 1.1944(50)$ and $f_+(0) = 0.9628(34)$
 - with $\chi^2=0.22/1$ (64%) and a correlation of 0.72 (complete correlation matrix available)

- Again very good agreement with th. estimations: $f_K/f_\pi = 1.189(7)$ and $f_+(0) = 0.9644(49)$ (used as fit input).



0C FIT

[no theory input for f_K/f_π or $f_+(0)$]

$$f_K/f_\pi = 1.1928(61)$$

$$f_+(0) = 0.9612(47)$$

1C FIT

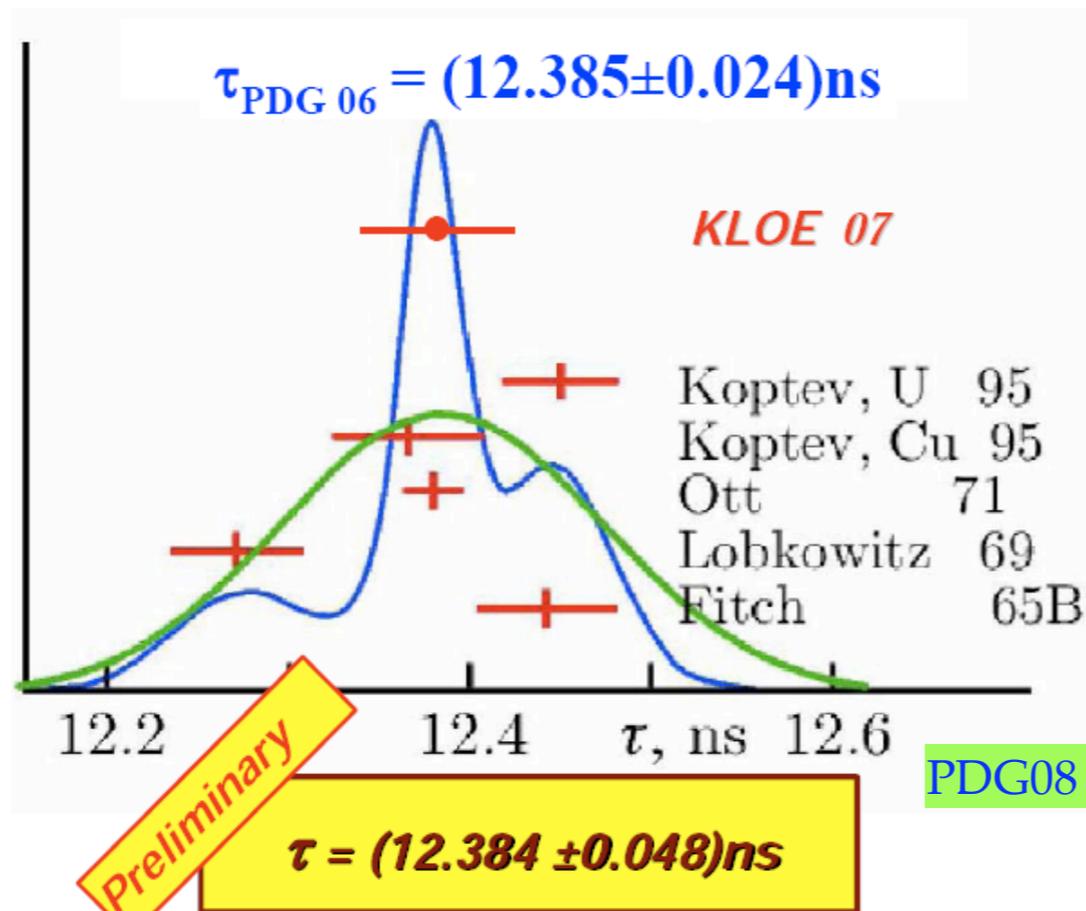
[$f_+(0) = 0.9644(49)$ used as input]

$$f_K/f_\pi = 1.1944(50)$$

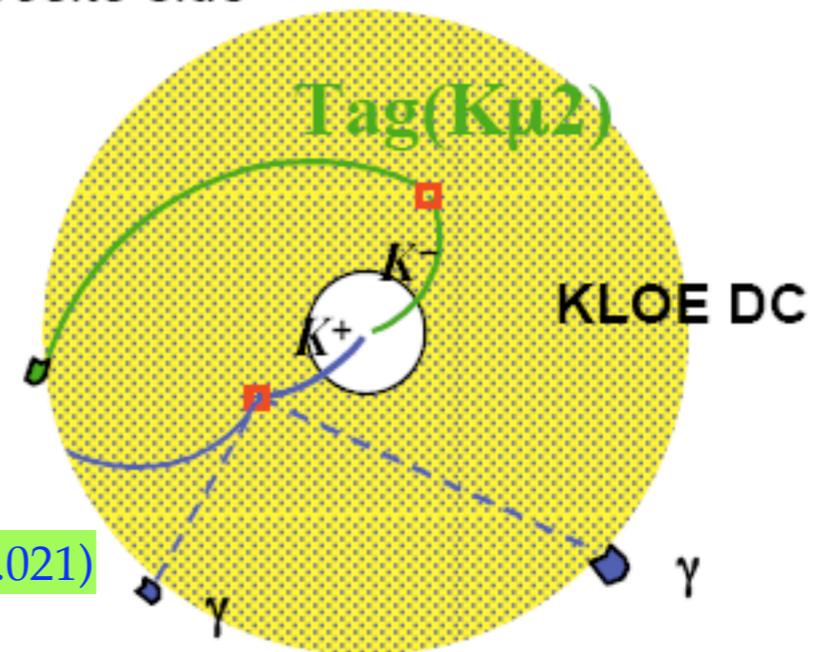
$$f_+(0) = 0.9628(34)$$

Good agreement of current world results on $|V_{ud}|$
and $|V_{us}|$ with first-row unitarity constraint
translates into expected values for f_K/f_π and $f_+(0)$
in agreement with recent lattice estimates.

K^\pm lifetime from KLOE



- Tag events with $K^\pm \rightarrow \mu\nu$ decay
- Identify a kaon decay on the opposite side



KLOE preliminary, 2 different methods:

τ_\pm from the K decay length, using tagged vertices in DC

$$\tau_\pm = 12.367(44)(65) \text{ ns}$$

τ_\pm from the K decay time, using γ from $K^\pm \rightarrow \pi^\pm \pi^0$ decays

$$\tau_\pm = 12.391(49)(25) \text{ ns}$$

Combined result ($\rho = 0.34$): $\tau_\pm = 12.384(48) \text{ ns}$

The ratio R_K

R_K accurately predicted within the SM:

$$R_K = \frac{\Gamma(K^\pm \rightarrow e^\pm \nu_e)}{\Gamma(K^\pm \rightarrow \mu^\pm \nu_\mu)} = \frac{m_e^2}{m_\mu^2} \left(\frac{m_K^2 - m_e^2}{m_K^2 - m_\mu^2} \right)^2 (1 + \delta R_{QED}) = (2.477 \pm 0.001) \cdot 10^{-5}$$

[V. Cirigliano and I Rosell, JHEP 0710:005 (2007)]

ChPT, $O(e^2 p^4)$

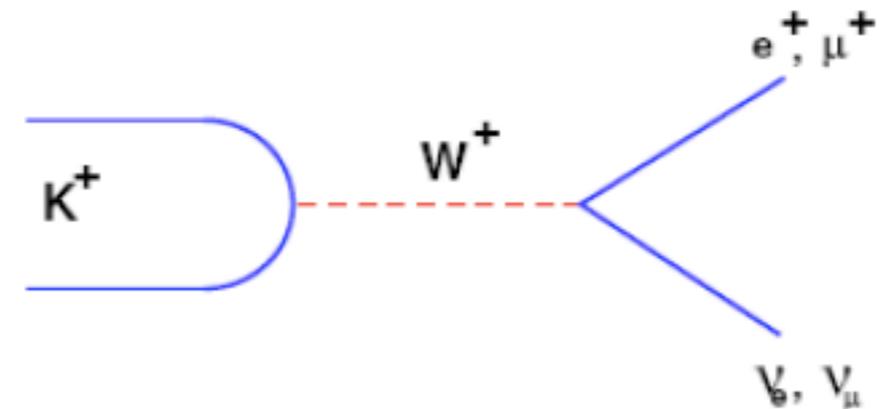
Helicity suppression

Radiative corrections

Adronic contributions cancel in the ratio



R_K is sensitive to New Physics due to the helicity suppression



A precise measurement of R_K probes μ - e universality and provides a stringent test of the SM.

$$\delta R_K = -3.8\%$$

($K_{l2\gamma}$ and virtual photons)

compared to

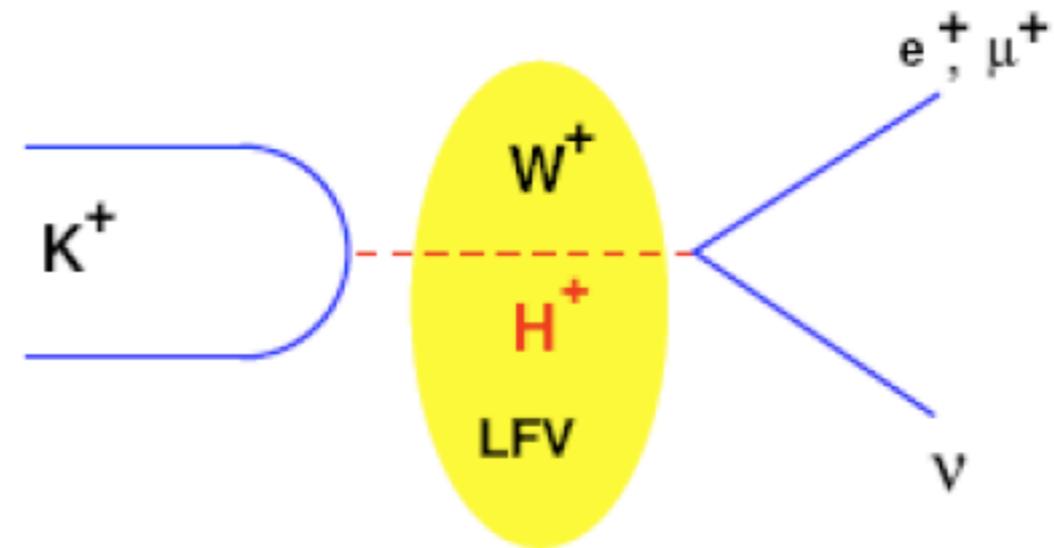
$$\Delta R_K / R_K \sim 0.04\%$$

R_K beyond the SM

SUSY effects (MSSM framework) can modify R_K wrt SM up to 3%

(Masiero, P. Paradisi, R. Petronzio hep-ph/0511289 PRD74 (2006))

R-parity is the source of new physics effect on R_K



Yukawa LFV effective couplings:

$$lH^{\pm}\nu_{\tau} \rightarrow \frac{g_2}{\sqrt{2}} \frac{m_{\tau}}{M_W} \Delta_R^{3l} \tan^2 \beta \quad l = e, \mu$$

Δ^{3l} is the LFV term connected to helicity suppression in $Ke2$

R_K in SUSY

The measurement of R_K produces limits to the value of $\Delta_{31} = \Delta_{31}(m_{H^\pm}, \tan\beta)$



$$R_K^{LFV} \approx R_K^{SM} \left[1 + \left(\frac{m_K^4}{m_{H^\pm}^4} \right) \left(\frac{m_\tau^2}{m_e^2} \right) |\Delta_{31}|^2 \tan^6 \beta \right]$$

- Loop diagrams mainly contribute
- LFC contributions $O((\tan\beta)^2)$ suppressed
- For large $\tan\beta$ values (still not experimentally excluded) LFV contributions $O(\tan\beta)^6$ dominate producing sizable effects on R_K
- Destructive interference between SM and SUSY LFC (arising from double LFV Mass Insertions) can give negative correction to R_K^{SM}

$$\tan\beta=40 \text{ e } M_H=500 \text{ GeV}/c^2$$

$$R_K^{LFV} = R_K^{SM} (1 + 0.013)$$

M Piccini

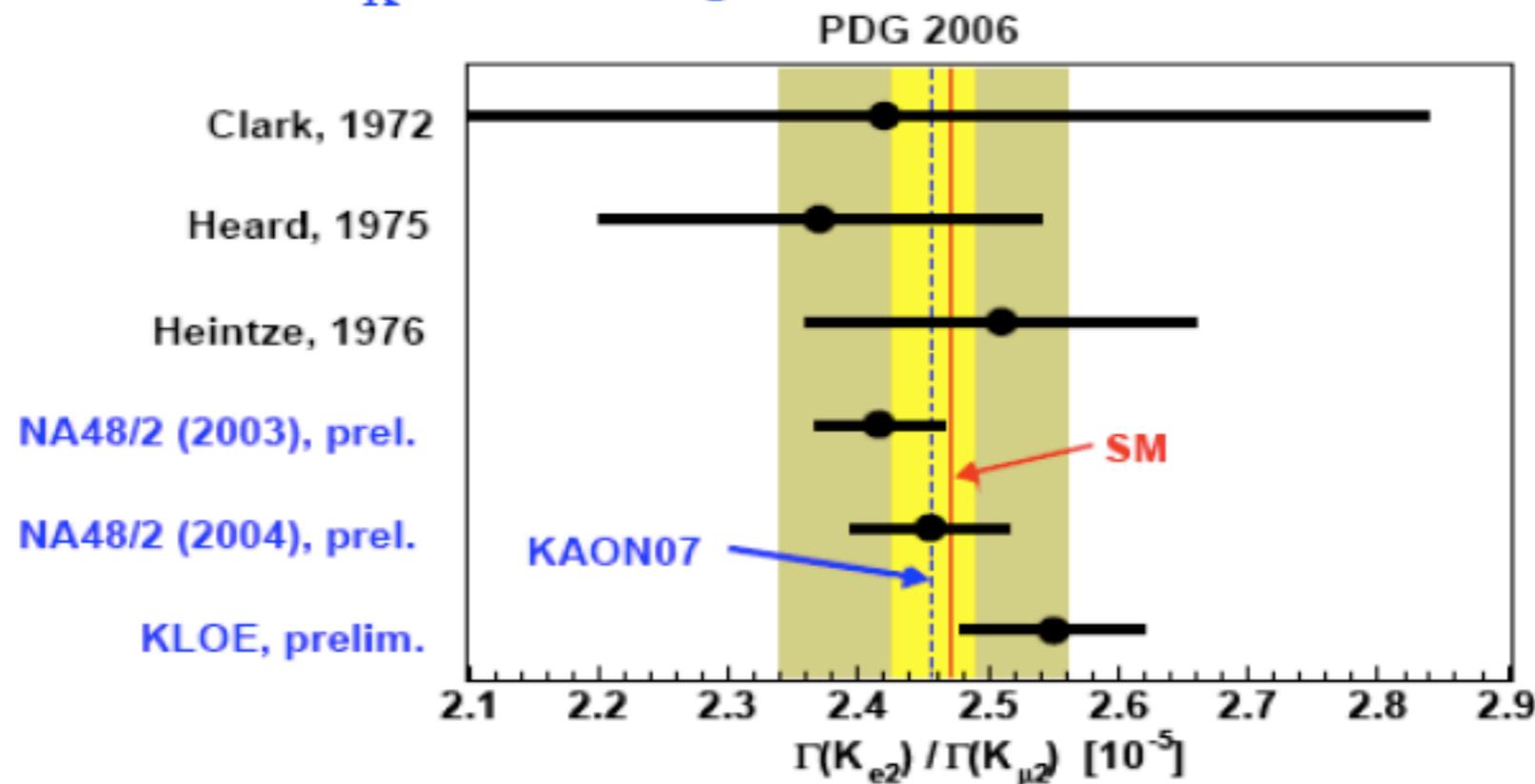
Flavianet fit to R_K

Before NA48/2
and Kloe results



$$R_K^{PDG} = (2.45 \pm 0.11) \cdot 10^{-5} \quad \delta R_K / R_K = 4.5\%$$

Flavianet fit to R_K combining PDG 2006, NA48/2 and KLOE results:



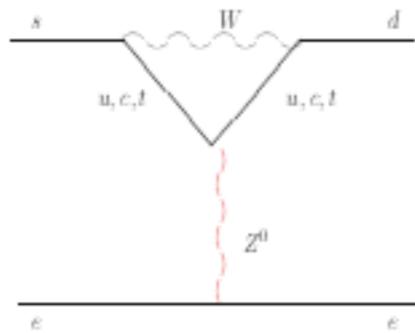
$$R_K = (2.457 \pm 0.032) \cdot 10^{-5} \quad (\chi^2 / ndf = 2.44 / 3)$$

- ✓ Big improvement wrt PDG \rightarrow now $\delta R_K / R_K \sim 1.3\%$
- ✓ Good agreement with SM prediction

Motivations

SM at short distance predicts the **current** \otimes **current** structure for $K \rightarrow \pi e^+ e^-$

$$\mathcal{H} \sim \frac{G_F \alpha}{\sqrt{2} M_W^2} \bar{s}_L \gamma_\mu d_L \bar{e}_L \gamma^\mu e_L \left[\sum_q V_{qs}^* V_{qd} m_q^2 \right] + h.c.$$



$$\left[A^2 \lambda^5 (1 - \rho - i\eta) m_t^2 + \lambda m_c^2 \right]$$

Gilman,Wise; Buchalla,Buras, Lautenbacher

$$K_L \rightarrow \pi^0 e^+ e^- \quad \left\{ \begin{array}{l} \text{CP violating} \\ \text{sensitivity to new physics} \\ \text{Im} \lambda_t = \Im(V_{ts}^* V_{td}) \end{array} \right.$$

$$K_L \rightarrow \pi^0 e^+ e^- \text{ vs. } K_L \rightarrow \pi^0 \nu \bar{\nu}$$

$$\bullet K_L \rightarrow \pi^0 \nu \bar{\nu} \quad \overbrace{(2.76 \pm 0.40) \cdot 10^{-11}}^{\text{SM}} \quad \overbrace{< 6.7 \cdot 10^{-8}}^{\text{E391a}} \quad \text{no e.m. bck.}$$

•

$$K_L \rightarrow \pi^0 e^+ e^- : \overbrace{\sim 1 \cdot 10^{-11}}^{\text{SM}} \quad \text{But} \left\{ \begin{array}{l} K_L \rightarrow \pi^0 \gamma \gamma \rightarrow \pi^0 e^+ e^- \\ K_L = K_2 + \epsilon K_1 \rightarrow \pi^0 e^+ e^- \end{array} \right.$$

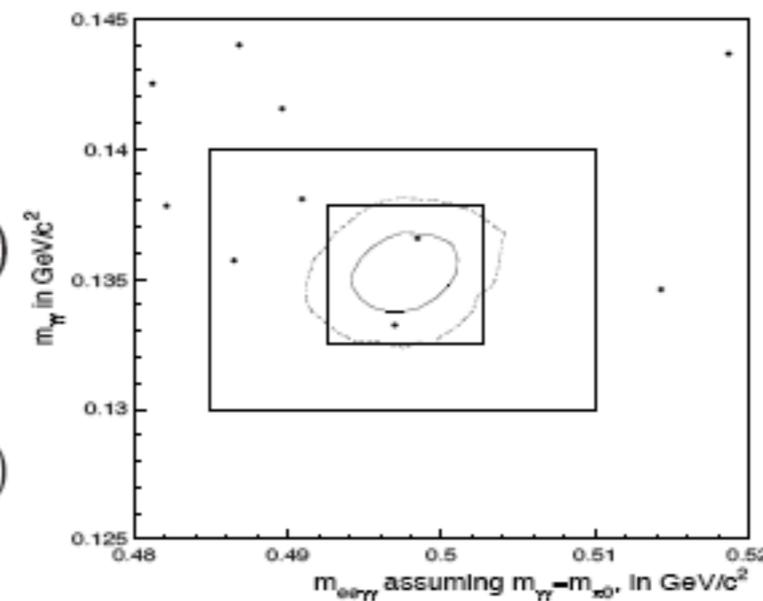
• – Greenlee bck.

$$Br(K_L \rightarrow e^+ e^- \gamma \gamma) \quad \left\{ \begin{array}{ll} (5.8 \pm 0.3) \cdot 10^{-7} & \text{No kin. cut} \\ 1 \cdot 10^{-10} & \text{kin. cut} \end{array} \right.$$

• $\frac{\text{signal}}{\text{bck.}} \sim 0.1$ But bck. can be known accurately (QED) \implies statistics

$$Br(K_L \rightarrow \pi^0 e^+ e^-) \text{ KTeV}$$

- '97('99) $2.6 \cdot 10^{11} K_L$
- expected bck. 1 evt. '97 ('99)
2 evt. (1)
- $Br < 5.1 \cdot 10^{-10}$ (3.5)
combined $< 2.8 \cdot 10^{-10}$



KTeV

Foreseen statistics to measure the Direct- CP-violating part in the SM $\Im\lambda_t$
at 30% : 1.000 more K_L

Control over three contributions

- Direct CP violation in $K_L \rightarrow \pi^0 e^+ e^-$
- CP conserving $K_L \rightarrow \pi^0 e^+ e^-$
- $K_L = K_2 + \epsilon K_1 \rightarrow \pi^0 e^+ e^-$

Short distance contribution to $K_L \rightarrow \pi^0 e^+ e^-$

$K_2 \rightarrow \pi^0 (e^+ e^-)_{J=1}$ dominated by the s.d.

$$Q_{7V} = \bar{s} \gamma^\mu (1 - \gamma_5) d \bar{\ell} \gamma_\mu \ell, \quad Q_{7A} = \bar{s} \gamma^\mu (1 - \gamma_5) d \bar{\ell} \gamma_\mu \gamma_5 \ell$$

$$\begin{aligned} B(K_L \rightarrow \pi^0 e^+ e^-)_{\text{CPV-dir}} &= \frac{\tau(K_L)}{\tau(K^+)} \frac{B(K_{e3}^+)}{|V_{us}|^2} (y_{7A}^2 + y_{7V}^2) [\Im(V_{ts}^* V_{td})]^2, \\ &= (2.45 \pm 0.22) \times 10^{-12} \left[\frac{\Im \lambda_t}{10^{-4}} \right]^2 \end{aligned}$$

where

$$\Im \lambda_t = \Im(V_{ts}^* V_{td}) \text{ from Buchalla et al, CKM}$$

$$K_L(p) \rightarrow \pi^0(p_3)\gamma(q_1)\gamma(q_2)$$

$$\text{Lorentz + gauge invariance} \Rightarrow M \sim \begin{array}{cc} A(y, z) & B(y, z) \\ \gamma\gamma & \gamma\gamma \\ J=0 & \text{D-wave too} \\ F^{\mu\nu}F_{\mu\nu} & F^{\mu\nu}F_{\mu\lambda}\partial_\nu K_L\partial^\lambda\pi^0 \end{array}$$

$$y = p \cdot (q_1 - q_2) / m_K^2, \quad z = (q_1 + q_2)^2 / m_K^2$$

$$r_\pi = m_\pi / m_K$$

- $\frac{d^2\Gamma}{dydz} \sim z^2 |A + B|^2 + \left(y^2 - \left(\frac{(1 + r_\pi^2 - z)^2}{4} - r_\pi^2 \right) \right)^2 |B|^2$ S, B
- Different gauge structure $\Rightarrow B \neq 0$ at $z \rightarrow 0$ (collinear photons).

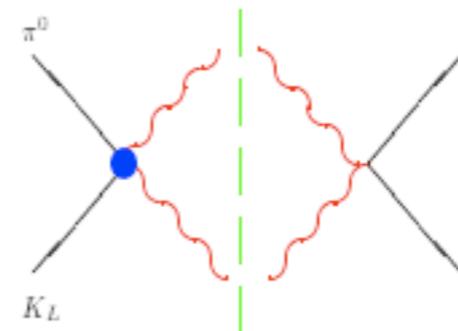
Crucial role in $K_L \rightarrow \pi^0 e^+ e^-$

A suppressed by m_e/m_K

B is not

Morozumi et al, Flynn Randall

Sehgal Heiliger, Ecker et al., Donoghue et al.



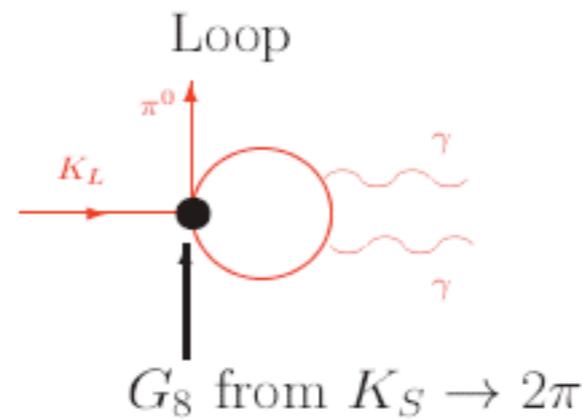


Ecker, Pich, de Rafael; Capiello, G.D

- $O(p^4)$

CT

0



only A

But

$$\frac{\Gamma(K_L \rightarrow \pi^0 \gamma \gamma)_{p4}}{\Gamma(K_L \rightarrow \pi^0 \gamma \gamma)_{\text{exp}}} \sim \frac{1}{2.5}$$

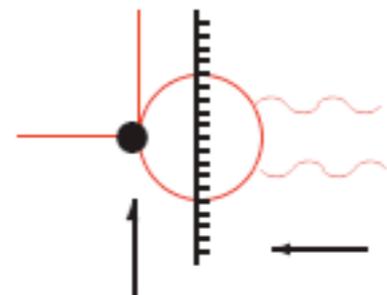
- $O(p^6)$ A, B from:

3 CT's

$$F_{\mu\nu} F^{\mu\alpha} \partial_\alpha K_L \partial^\nu \pi^0$$

$$F^2 \partial K_L \partial \pi^0$$

$$F^2 m_K^2 K_L \pi^0$$



Capiello, G.D., Miragliuolo
Cohen, Ecker, Pich

Full description of unitarity cut

$$A(K \rightarrow 3\pi) = a + b Y + c Y^2 + d X^2$$

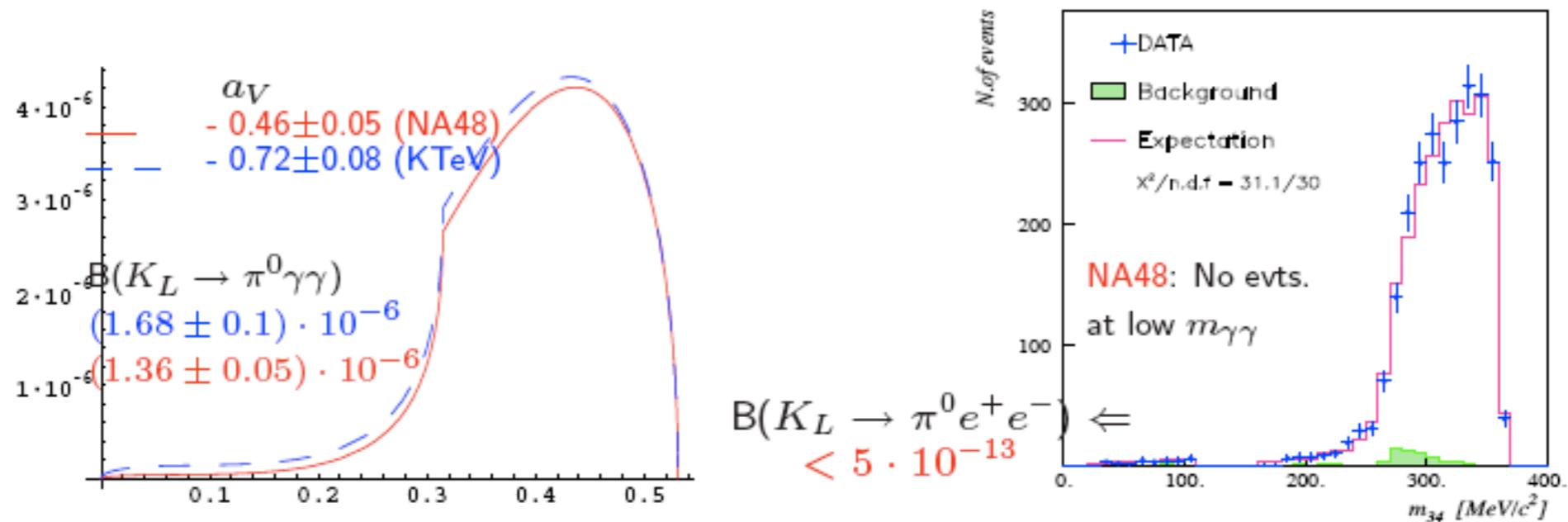
$$A_{CT} = \alpha_1(z - r_\pi^2) + \alpha_2$$

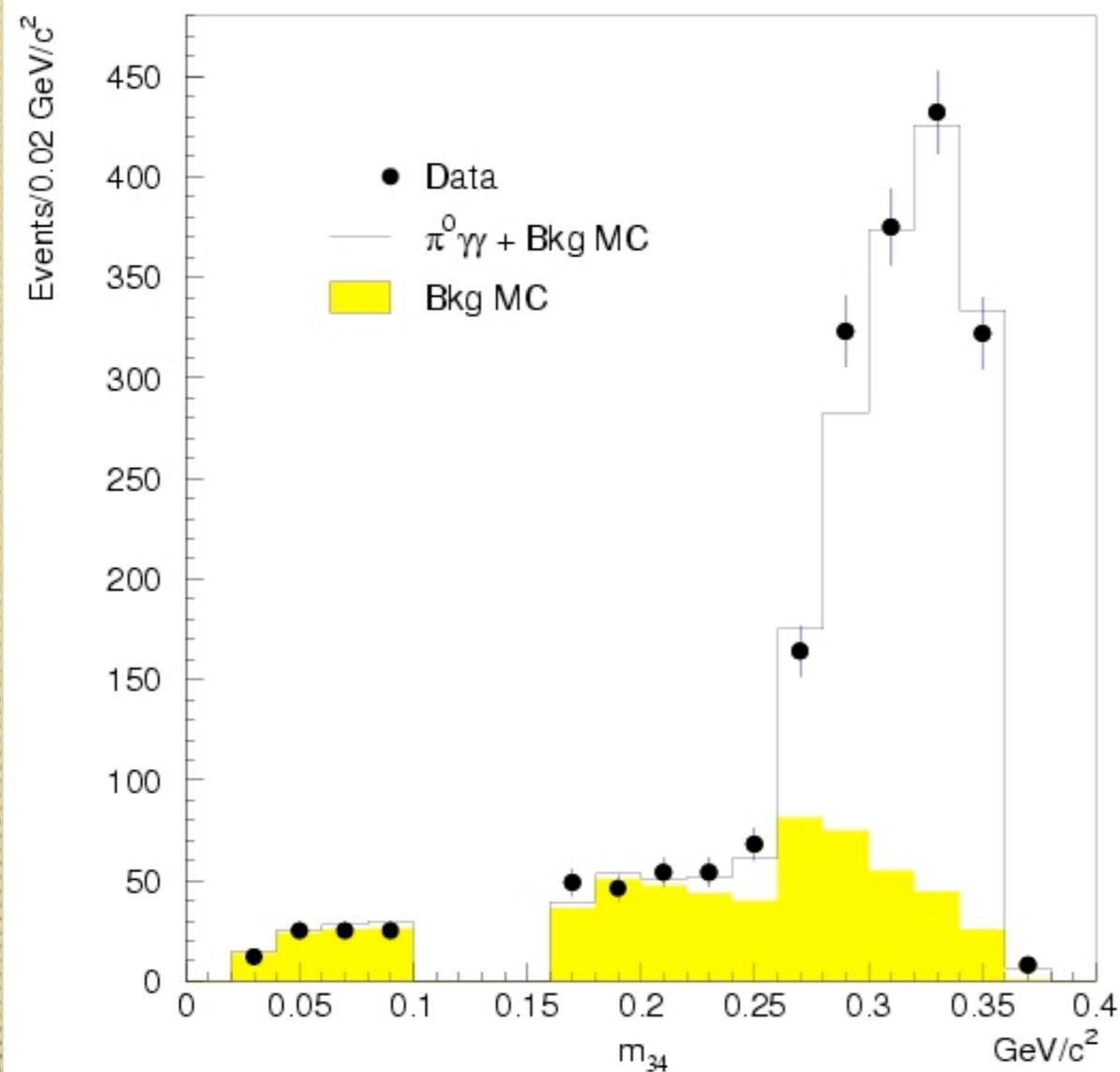
$$B_{CT} = \beta$$

VMD \Rightarrow 1 coupling a_V (~ -0.6 G.D., Portoles)
(Ecker, Pich, de Rafael; Sehgal et al.)

$$\alpha_1 = \frac{\beta}{2} = -\frac{\alpha_2}{3} = -4a_V \sim 2 \quad \text{n.d.a.} \sim 0.2$$

- **KTeV** and **NA48**: 1 parameter fit (a_V) with all the unitarity corrections





KTeV

**New KTeV result on full dataset
1982 events**

**Normalization to $K_L \rightarrow \pi^0\pi^0$
30% background ($K_L \rightarrow 3\pi^0$)**

$$BR = (1.29 \pm 0.03 \pm 0.05) \times 10^{-6}$$

**Supersedes previous KTeV result
(half dataset)**

$$BR = (1.55 \pm 0.07 \pm 0.08) \cdot 10^{-6}$$

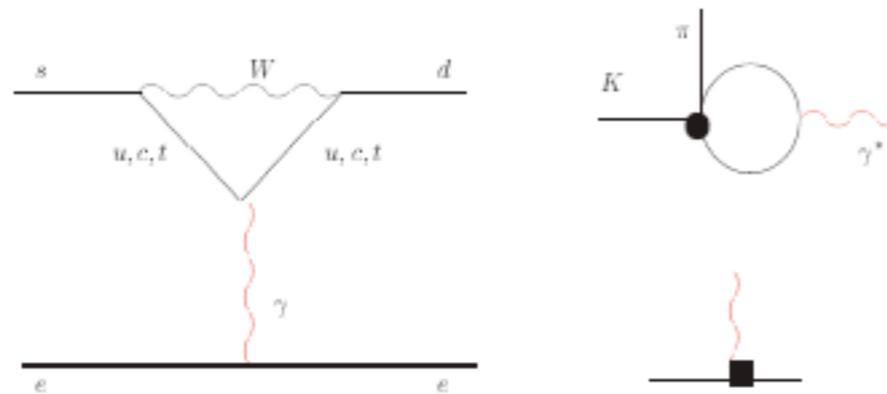
Agrees with NA48 2002 result:

$$BR = (1.27 \pm 0.04 \pm 0.01) \cdot 10^{-6}$$

$$K^\pm(K_S) \rightarrow \pi^\pm(\pi^0)\ell^+\ell^-$$

- short distance \ll long distance

LD described by form factor W



$$W^i = G_F m_K^2 (a_i + b_i z) + W_{\pi\pi}^i(z)$$

$$i = \pm, S$$

$$a_i, b_i \sim O(1), \quad z = \frac{q^2}{m_K^2}$$

- Observables $\Gamma(K^+ \rightarrow \pi^+ e^+ e^-)$, $\Gamma(K^+ \rightarrow \pi^+ \mu \bar{\mu})$, slopes

- $a_i \sim O(p^4)$

- $b_i \sim O(p^6)$

Ecker, Pich, de Rafael

G.D., Ecker, Isidori, Portoles

- a_+, b_+ in general not related to a_S, b_S

- **Expt. E865**

$$K^+ \rightarrow \pi^+ e^+ e^- : a_+ = -0.586 \pm 0.010 \quad b_+ = -0.655 \pm 0.044$$

confirmed by NA48/2 (1.4 σ 's away) also in $K^+ \rightarrow \pi^+ \mu \bar{\mu}$

- **HyperCP** has confirmed **E865** (02) ($K^+ \rightarrow \pi^+ \mu \bar{\mu}$) and put a bound on the CP asymmetry (≤ 0.1)

Problems: $\frac{a_i}{p^4}$ $\frac{b_i}{p^6}$ same phenomenological size
different theoretical order

Probably explained by large VMD. Then we can just parameterize

$$\text{Br}(K_S \rightarrow \pi^0 e^+ e^-) = 4.6 \times 10^{-9} a_S^2$$

not predicted but dynamically interesting: $a_S \sim \mathcal{O}(1)$: **NA48** Great expt!

$K_S \rightarrow \pi^0 e^+ e^-$ at NA48/1 Collaboration at CERN

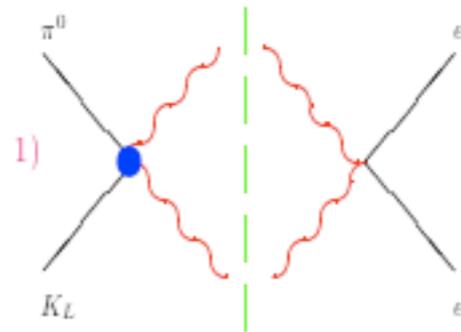
- 7 events observed (with 0.15 expected background events)

$$B(K_S \rightarrow \pi^0 e^+ e^-)_{m_{ee} > 165 \text{ MeV}} = (3.0_{-1.2}^{+1.5} \pm 0.2) \times 10^{-9}$$

$$|a_S| = 1.08_{-0.21}^{+0.26}$$

$K_L \rightarrow \pi^0 e^+ e^-$: summary

$$\text{Br}(K_L \rightarrow \pi^0 e^+ e^-) \leq 5 \cdot 10^{-10} \quad \text{KTeV}$$



CP conserving NA48

$$\text{Br}(K_L \rightarrow \pi^0 e^+ e^-) < 3 \cdot 10^{-12}$$

$V-A \otimes V-A \Rightarrow \langle \pi^0 e^+ e^- | (\bar{s}d)_{V-A} (\bar{e}e)_{V-A} | K_L \rangle$ violates CP



Possible large interference: $a_S < -0.5$ or $a_S > 1$; short distance probe even for a_S large

$$|2) + 3)|^2 = \left[15.3 a_S^2 - 6.8 \frac{\text{Im} \lambda_t}{10^{-4}} a_S + 2.8 \left(\frac{\text{Im} \lambda_t}{10^{-4}} \right)^2 \right] \cdot 10^{-12}$$

$$[17.7 \pm \quad 9.5 + \quad 4.7] \cdot 10^{-12}$$

- The large slope for $K^+ \rightarrow \pi^+ e^+ e^-$ calls for large VMD
- $K^+ \rightarrow \pi^+ e^+ e^-$ receives substantial $\pi\pi$ -loop, **contrary** to $K_S \rightarrow \pi^0 e^+ e^-$ (~ 0),
- if we split

$$\left(\frac{a_i^{\text{VMD}}}{1 - z m_K^2 / m_V^2} + a_i^{\text{nVMD}} \right) \approx \left[(a_i^{\text{VMD}} + a_i^{\text{nVMD}}) + a_i^{\text{VMD}} \frac{m_K^2}{m_V^2} z \right]$$

Then we can determine both terms from expt.

$$a_+^{\text{VMD}} = \frac{m_V^2}{m_K^2} b_+^{\text{exp}} = -1.6 \pm 0.1, \quad a_+^{\text{nVMD}} = a_+^{\text{exp}} - a_+^{\text{VMD}} = 1.0 \pm 0.1$$

- Also we can hope a_i^{VMD} obey a short distance relation since i) VMD is a larger scale and ii) NOT affected by $\pi\pi$ -loop
- The only operator at short distances is $Q_7 = \bar{s}\gamma^\mu(1 - \gamma_5)d\bar{\ell}\gamma_\mu\ell$,

$$\mathcal{H}_{eff}^{|\Delta S|=1} = \frac{G_F}{\sqrt{2}} V_{us}^* V_{ud} \left[\sum_{i=1}^{6,7V} (z_i(\mu) + \tau y_i(\mu)) Q_i(\mu) + \tau y_{7A}(M_W) Q_{7A}(M_W) \right]$$

$\tau = -V_{ts}^* V_{td} / V_{us}^* V_{ud}$. The Wilson coefficients $z_7(\mu)$ and $\tau y_7(\mu)$ determine the CPC CPV amplitudes and their relative sign. The isospin structure of Q_{7V} leads

$$(a_S)_{\langle Q_{7V} \rangle} = -(a_+)_{\langle Q_{7V} \rangle}$$

- If this relation is obeyed by the full VMD amplitude

$$(a_S^{\text{VMD}})_{\langle Q_{7V} \rangle} = -a_+^{\text{VMD}} = 1.6 \pm 0.1$$

in good agreement with NA48

$$(|a_S| = 1.08_{-0.21}^{+0.26})$$

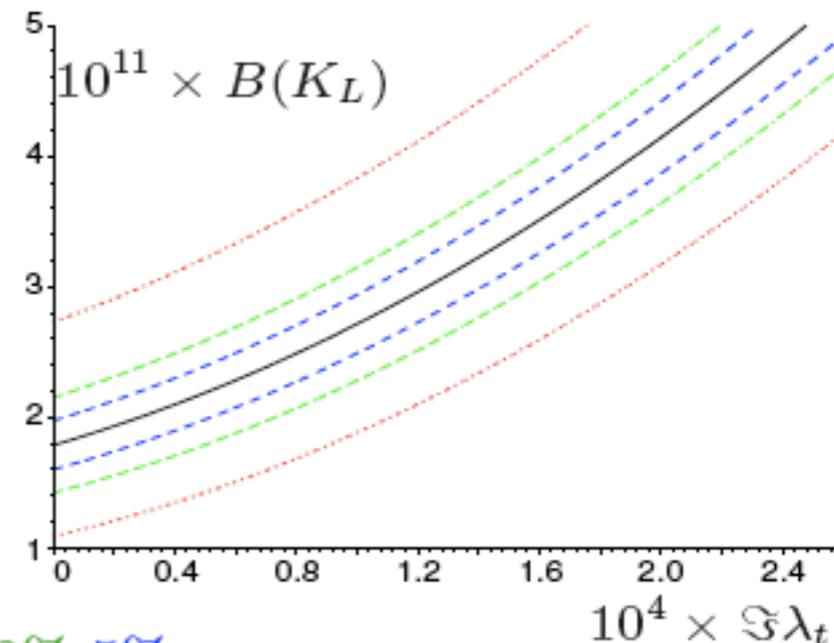
- Having i) **separated** the contribution better suited to comparison with **s.d. (VMD)** and ii) **realized** that this dominates **Theoret.** and **Phenom.(NA48)** a_S
- we believe the **positive interference** of **s.d.**

$$B(K_L \rightarrow \pi^0 e^+ e^-)_{\text{SM}} = (3.1^{+1.2}_{-0.9}) \times 10^{-11} a_S$$

$$\text{KTeV } B(K_L \rightarrow \pi^0 e^+ e^-) < 2.8 \times 10^{-10} \text{ at } 90\% \text{C.L.}$$

Present error on $a_S = 1.08, 10\% 5\%$, no error

K -physics bound: $-1.2 \times 10^{-3} < \Im\lambda_t < 1.0 \times 10^{-3}$ at 90% C.L.



see Mescia et al. for updated CKM

Chiral Perturbation Theory

χPT effective field theory based on the two assumptions

- π 's are the Goldstone boson of $SU(3)_L \otimes SU(3)_R \rightarrow SU(3)_V$
- (*chiral*) *power counting* i.e. the theory has a small expansion parameter: $p^2 / \Lambda_{\chi SB}^2$:
 $\Lambda_{\chi SB} \sim 4\pi F_\pi \sim 1.2 \text{ GeV}$

$$\mathcal{L}_{\Delta S=0} = \mathcal{L}_{\Delta S=0}^2 + \mathcal{L}_{\Delta S=0}^4 + \dots = \frac{F_\pi^2}{4} \overbrace{\langle D_\mu U D^\mu U^\dagger + \chi U^\dagger + U \chi^\dagger \rangle}^{\pi \rightarrow l\nu, \pi\pi \rightarrow \pi\pi, K \rightarrow \pi..} + \sum_i \overbrace{L_i O_i}^{K \rightarrow \pi..} + \dots$$

Fantastic chiral prediction $A_{\pi\pi} \sim (s - m_\pi^2) / F_\pi^2$

Weinberg, Colangelo *et al*

$$\mathcal{L}_{\Delta S=1} = \mathcal{L}_{\Delta S=1}^2 + \mathcal{L}_{\Delta S=1}^4 + \dots = G_8 F^4 \underbrace{\langle \lambda_6 D_\mu U^\dagger D^\mu U \rangle}_{K \rightarrow 2\pi/3\pi} + \underbrace{G_8 F^2 \sum_i N_i W_i}_{K^+ \rightarrow \pi^+ \gamma\gamma, K \rightarrow \pi l^+ l^-} + \dots$$

Vector Meson Dominance in the strong sector

Ecker, Gasser, de Rafael, Pich

i	$L_i^r(M_\rho)$	V	A	Total	Total ^{c)}
1	0.4 ± 0.3	0.6	0	0.6	0.9
2	1.4 ± 0.3	1.2	0	1.2	1.8
3	-3.5 ± 1.1	-3.6	0	-3.0	-4.9
4	-0.3 ± 0.5	0	0	0.0	0.0
5	1.4 ± 0.5	0	0	1.4	1.4
6	-0.2 ± 0.3	0	0	0.0	0.0
7	-0.4 ± 0.2	0	0	-0.3	-0.3
8	0.9 ± 0.3	0	0	0.9	0.9
9	6.9 ± 0.7	$6.9^{a)}$	0	6.9	7.3
10	-5.5 ± 0.7	-10.0	4.0	-6.0	-5.5

c) uses QCD "inspired" relations

$$F_V = 2G_V = \sqrt{2}f_\pi,$$

$$F_A = f_\pi$$

$$M_A = \sqrt{2}M_V$$

$$L_1^V = \frac{L_2^V}{2} = -\frac{L_3^V}{6} = \frac{G_V^2}{8M_V^2}, \quad L_9^V = \frac{F_V G_V}{2M_V^2}, \quad L_{10}^{V+A} = -\frac{F_V^2}{4M_V^2} + \frac{F_A^2}{4M_A^2}$$

Theoretical motivations of success of VMD

- VMD improves the matching with QCD

Ecker, Gasser, Leutwyler, Pich, de Rafael

$$F_V^{\pi^\pm}(t) \approx \frac{M_\rho^2}{M_\rho^2 - t},$$

$$L_1^V = L_2^V/2 = -L_3^V/6 = L_9^V/8 = -L_{10}^{V+A}/6 = f_\pi^2/(16M_V^2).$$

- Picture consolidated by in the chiral quark model χ QM Georgi-Manohar, Espriu, de Rafael, Taron
This is a dynamical interpretation (in CHPT) of the success of the non-relativistic quark model. In this model

$$L_i^{\chi\text{QM}} \sim L_i^{\text{VMD}}$$

- Also Large N
- Strong consolidated picture: **Must work also in the WEAK sector** in some way: **WHICH WAY?**

- Many CT's (37)

Ecker, Kambor, Wyler; G.D. Portoles

$$\mathcal{L}_{|\Delta S|=1}^{(4)} = G_8 F^2 \sum_{i=1}^{37} N_i W_i$$

- There are **tests**
- $K^+ \rightarrow \pi^+ \pi^0 \gamma$ and $K_S \rightarrow \pi^+ \pi^- \gamma$ same CT combination
- $K \rightarrow \pi l^+ l^-$, $K^+ \rightarrow \pi^+ \pi^0 \gamma$, $K^+ \rightarrow \pi^+ \gamma \gamma$ (observed or close to observation) and others probe the the same CT's \implies **CHPT tests**
- We need desperately some dynamical info and also some theory prejudice
- VMD must work and it is easy testable: form factor

Weak interactions in CHPT and VMD

- We know is tough: see $\Delta I = 1/2$ -rule
- Actually even in the strong sector: $V^{\mu\nu}$ better than V^μ
- $\mathcal{L}_{\Delta S=1}^{(4)}$: $V^{\mu\nu}$ and V^μ similar results (+) but important differences

Is there any chance that VMD works in CHPT weak?

- Evidence that VMD form factor describes better the photon energy distribution in $K_L \rightarrow \pi^+ \pi^- \gamma$
- size and sign of a_V in $K_L \rightarrow \pi^0 \gamma \gamma$ were postdicted in VMD
- the large slope in $K^+ \rightarrow \pi^+ l^+ l^-$ maybe explained by the large size of VMD
- It is not a lot ...We need more infos

i	W_i	Vectors	Axials
14	$i\langle\Delta\{f_+^{\mu\nu}, u_\mu u_\nu\}\rangle$	$\frac{1}{2}f_V^2\eta_V$	
15	$i\langle\Delta u_\mu f_+^{\mu\nu} u_\nu\rangle$	$f_V^2\eta_V$	
16	$i\langle\Delta\{f_-^{\mu\nu}, u_\mu u_\nu\}\rangle$		$\frac{1}{2}f_A^2\eta_A$
17	$i\langle\Delta u_\mu f_-^{\mu\nu} u_\nu\rangle$		$f_A^2\eta_A$
18	$\langle\Delta(f_{+\mu\nu}^2 - f_{-\mu\nu}^2)\rangle$	$-\frac{1}{4}f_V^2\eta_V$	$\frac{3}{4}f_A^2\eta_A$

η_V Weak Vector coupling

η_A Weak Axial coupling

we have used $f_V = 2 g_V$
 This approx. too drastic
 (when V -contributions cancel)

$K^+ \rightarrow \pi^+ \pi^0 \gamma$
 $N_{14} - N_{15} - N_{16} - N_{17}$

$K^+ \rightarrow \pi^+ \gamma \gamma$
 $N_{14} - N_{15} - 2N_{18}$
 size and sign from Axials
 $f_V \stackrel{?}{=} 2 g_V$

Counterterm combination	Processes	VMD weak coupling
$N_{14}^r - N_{15}^r$	$K^+ \rightarrow \pi^+ \gamma^*$ $K^+ \rightarrow \pi^+ \pi^0 \gamma^*$	$-0.020 \eta_V + 0.004 \eta_A$
$2N_{14}^r + N_{15}^r$	$K_S \rightarrow \pi^0 \gamma^*$	$0.08 \eta_V$
$N_{14} - N_{15} - 2N_{18}$	$K^+ \rightarrow \pi^+ \gamma \gamma$ $K^+ \rightarrow \pi^+ \pi^0 \gamma \gamma$	$-0.01 \eta_A$
$N_{14} - N_{15} - N_{16} - N_{17}$	$K^+ \rightarrow \pi^+ \pi^0 \gamma$ $K_S \rightarrow \pi^+ \pi^- \gamma$	$-0.010 \eta_A$
$N_{14}^r - N_{15}^r - 3(N_{16}^r - N_{17})$	$K_L \rightarrow \pi^+ \pi^- \gamma^*$	$-0.004 \eta_V + 0.018 \eta_A$
$N_{14}^r - N_{15}^r - 3(N_{16}^r + N_{17})$	$K_S \rightarrow \pi^+ \pi^- \gamma^*$	$0.05 \eta_V - 0.04 \eta_A$
$N_{14}^r + 2N_{15}^r - 3(N_{16}^r - N_{17})$	$K^+ \rightarrow \pi^+ \pi^0 \gamma^*$	$0.12 \eta_V + 0.01 \eta_A$
$N_{29} + N_{31}$	$K_L \rightarrow \pi^+ \pi^- \gamma$	$0.005 \eta_V + 0.003 \eta_A$
$3N_{29} - N_{30}$	$K^+ \rightarrow \pi^+ \pi^0 \gamma$	$-0.005 \eta_V - 0.003 \eta_A$

Observation hidden by other effects: different analysis maybe useful (Kaon charge radius)
NA48 has a good chance

$K_S \rightarrow \gamma\gamma$

- No short distance contributions, No $O(p^2)$
- Neutral particles (K_S) \Rightarrow No $O(p^4)$ CT : $F_{\mu\nu}F^{\mu\nu} \langle \lambda_6 Q U^+ Q U \rangle$

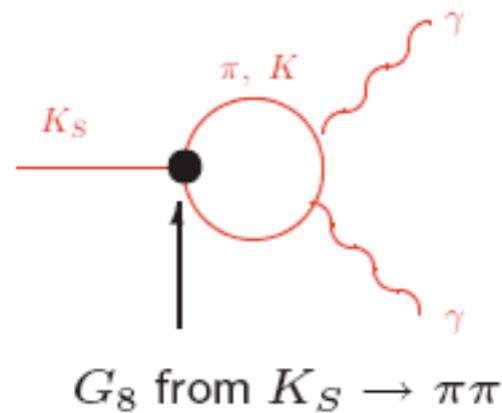
- Loop contribution finite **scale independent** and **unambiguous χ PT prediction**

$$\text{Br}_{\chi\text{PT}}(K_S \rightarrow \gamma\gamma) = 2.1 \cdot 10^{-6}$$

(G.D. and Espriu 86, Goity 87)

$$(2.78 \pm 0.072) \cdot 10^{-6} \text{ (NA48 '02)}$$

$$(2.26 \pm 0.12 \pm 0.06) \cdot 10^{-6} \text{ (KLOE08)}$$



- $O(p^6)_{CT}$ $F^{\mu\nu} F_{\mu\nu} \langle \lambda_6 Q^2 \mu M U^+ \rangle$

No VMD $\Rightarrow \frac{A^{(6)}}{A^{(4)}} \sim \frac{m_K^2}{(4\pi F_\pi)^2} \sim 0.2$

(No terms $\sim \frac{m_K^2}{m_\rho^2} \sim 0.4$)

- NA48 $\Rightarrow \frac{A^{(6)}}{A^{(4)}} \sim 15\%$

↓

- The error in the amplitude, is smaller than the naive expectation, 20-30%

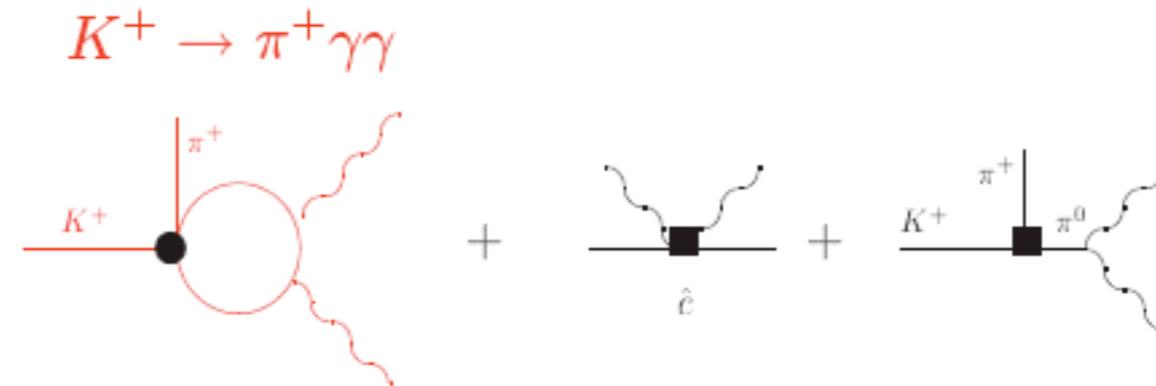
$$K^+ \rightarrow \pi^+ \gamma \gamma$$

$\gamma \gamma$ in $\underbrace{\begin{matrix} J = 0 & J = 2 \\ \overbrace{F_{\mu\nu} F^{\mu\nu}} & \overbrace{F \tilde{F}} \\ P = +1 & P = -1 \\ A & C \end{matrix}} + \dots$

Lorentz + gauge invariance

$$\frac{d^2\Gamma}{dydz} \sim \left[z^2 (|A + B|^2 + |C|^2) + \left(y^2 - \left(\frac{(1 + r_\pi^2 - z)^2}{4} - r_\pi^2 \right) \right)^2 |B|^2 \right]$$

- $O(p^4)$



Ecker, Pich, de Rafael

In factorization $\hat{c} = 2.3(1 - 2k_f)$

spin-1 contributions (axials)

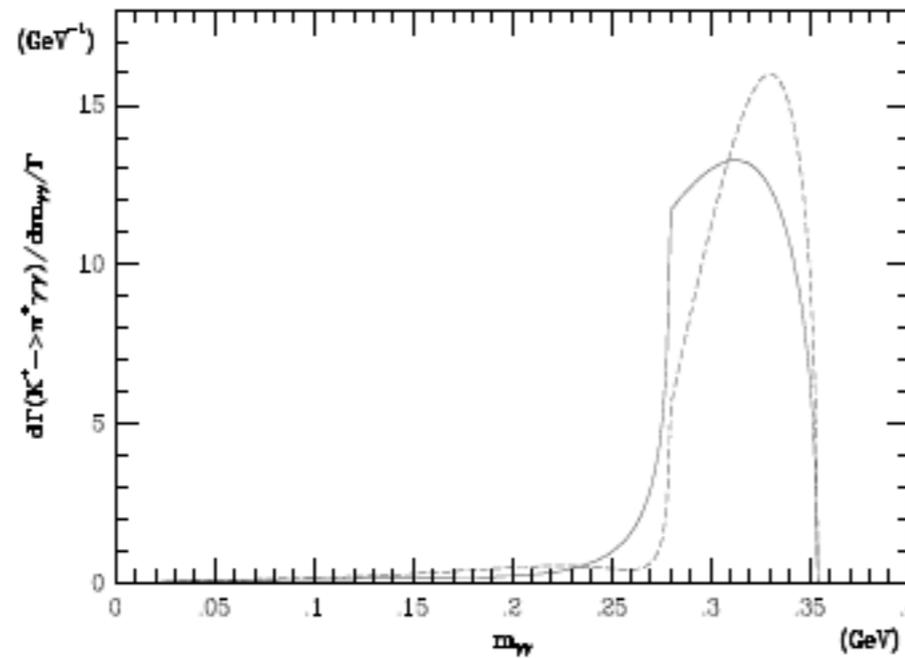
to \hat{c}

- $O(p^6)$

Unitarity corrections: 30%-40%

a_{V^+} negligible

G.D., Portoles 96



$$\begin{array}{r} \text{---} \\ \text{---} \end{array} \quad \begin{array}{l} \hat{c} \\ 0 \\ -2.3 \end{array}$$

NA48 preliminary

$$B = (1.07 \pm 0.04 \pm 0.08) \cdot 10^{-6}$$

assuming $c=2$

BNL 787 (96) got 31 events:

- i) confirm $O(p^6)$
- ii) $Br \sim (6 \pm 1.6) \cdot 10^{-7}$
- iii) $\hat{c} = 1.8 \pm 0.6$

E949 no events at low $m_{\gamma\gamma}$, work for NA48/2,

NA48 publ. $K^+ \rightarrow \pi^+ \gamma e^+ e^-$

first observation $O(10^{-8})$

$$c = 0.90 \pm 0.45$$

see Smith

$$K(p_K) \rightarrow \pi(p_1)\pi(p_2)\gamma(q)$$

- Lorentz + gauge invariance \Rightarrow Electric (E) and Magnetic (M) amplitude

$$A(K \rightarrow \pi\pi\gamma) = F^{\mu\nu} [E \partial_\mu K \partial_\nu \pi + M \varepsilon_{\mu\nu\rho\sigma} \partial^\rho K \partial^\sigma \pi]$$

- Unpolarized photons

$$\frac{d^2\Gamma}{dz_1 dz_2} \sim |E|^2 + |M|^2$$

$$|E^2| = |E_{IB}|^2 + 2\text{Re}(E_{IB}^* E_D) + |E_D|^2$$

↓

$$\text{Low Theorem} \Rightarrow E_{IB} \sim \frac{1}{E_\gamma^*} + c \quad E_D, M \text{ chiral tests}$$

We need FIGHT $DE/IB \sim 10^{-3}$

	<i>IB</i>	<i>DE_{exp}</i>	
$K_S \rightarrow \pi^+ \pi^- \gamma$	10^{-3}	$< 9 \cdot 10^{-5}$	<i>E1</i>
$K^+ \rightarrow \pi^+ \pi^0 \gamma$	10^{-4} ($\Delta I = \frac{3}{2}$)	$(0.44 \pm 0.07) 10^{-5}$ PDG	<i>M1, E1</i>
$K_L \rightarrow \pi^+ \pi^- \gamma$	10^{-5} (CPV)	$(2.92 \pm 0.07) 10^{-5}$ KTeVnew	<i>M1,</i> VMD

CPV is **only** from IB K_L (also measured in $K_L \rightarrow \pi^+ \pi^- e^+ e^-$)

BUT IB suppressed in K^+ and K_L .

$$K_L \rightarrow \pi^+ \pi^- \gamma$$

M1 transitions clearly measured KTeV (00) with large slope

form factor measured

$$\mathcal{F} = 1 + \frac{a}{1 - \frac{m_k^2}{m_\rho^2} + \frac{2m_K E_\gamma^*}{m_\rho^2}} \quad E_\gamma^* \text{ photon energy}$$

KTeV:

- $a = -1.243 \pm 0.057$

- χ^2/DOF

linear slope	quadratic slope	\mathcal{F}
43.2/27	37.6/26	38.8/27

\Rightarrow Large VMD: ρ -pole

$$p^4$$

$$\text{Theory } M1 \sim a_2 + 2a_4 + h.o.$$



Large VMD in the a_i . Not automatic in all spin-1 formulations

[G.D. Portoles, G.D. Gao]

Consistent with **M1** in $K^+ \rightarrow \pi^+ \pi^0 \gamma$ and predictive for spectrum (work for **NA48/2**)

$$K^+ \rightarrow \pi^+ \pi^0 \gamma$$

$$A(K \rightarrow \pi \pi \gamma) = F^{\mu\nu} [E \partial_\mu K \partial_\nu \pi + M \varepsilon_{\mu\nu\rho\sigma} \partial^\rho K \partial^\sigma \pi]$$

$E1$ and $M1$ are measured with Dalitz plot

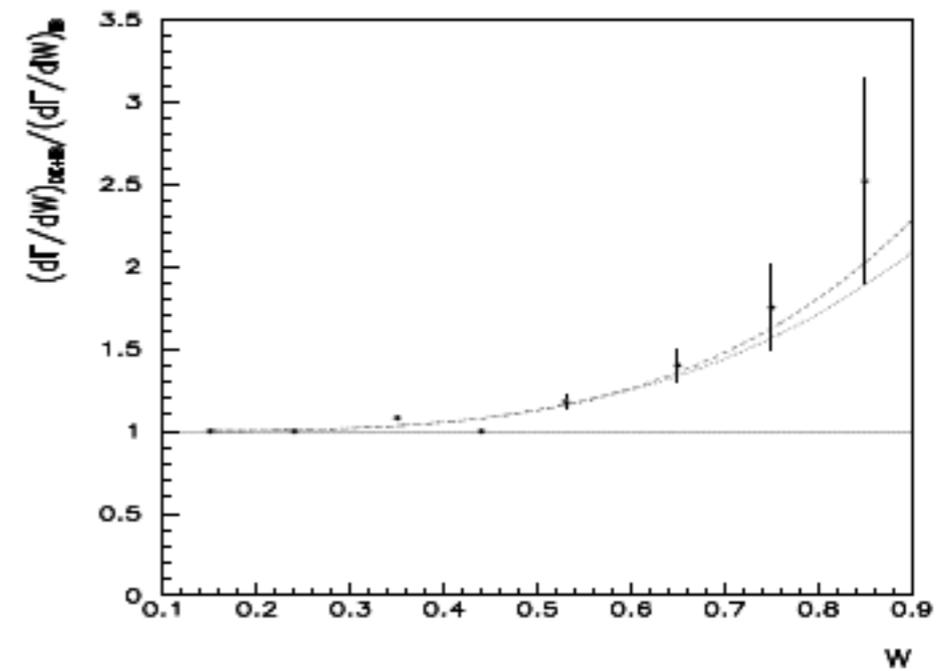
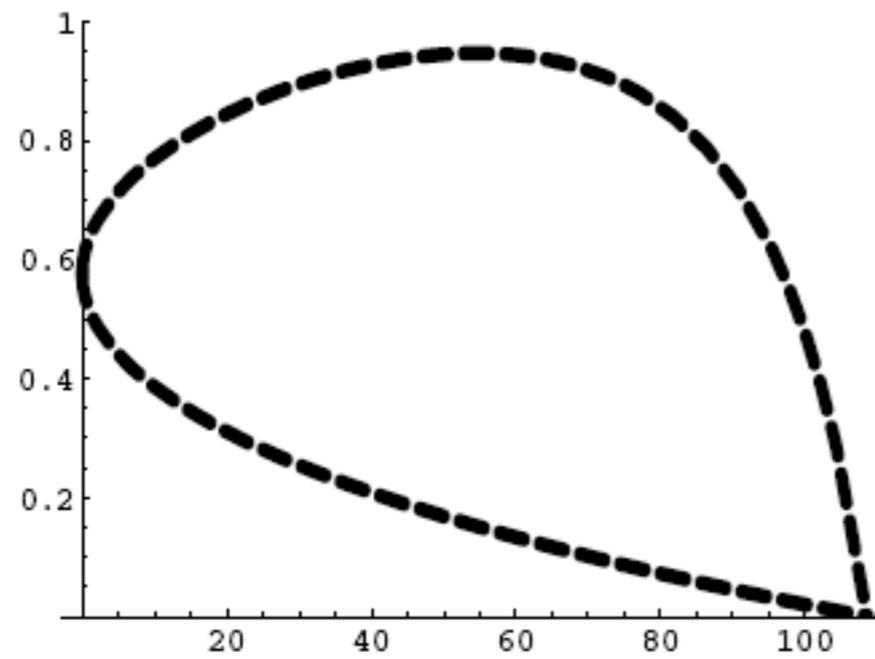
$$\frac{\partial^2 \Gamma}{\partial T_c^* \partial W^2} = \frac{\partial^2 \Gamma_{IB}}{\partial T_c^* \partial W^2} \left[1 + \frac{m_{\pi^+}^2}{m_K} 2 \operatorname{Re} \left(\frac{E1}{eA} \right) W^2 + \frac{m_{\pi^+}^4}{m_K^2} \left(\left| \frac{E1}{eA} \right|^2 + \left| \frac{M1}{eA} \right|^2 \right) W^4 \right]$$

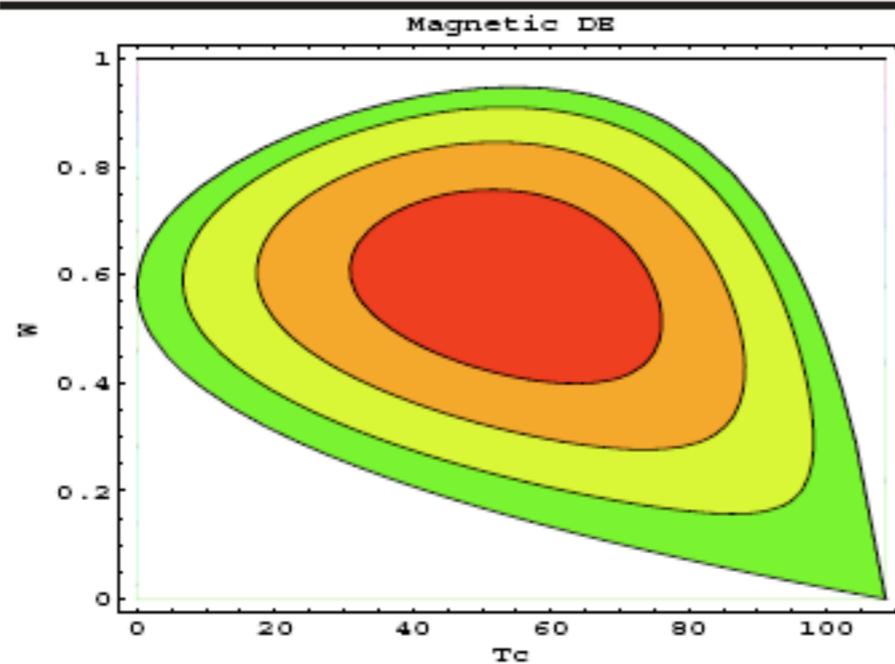
$$W^2 = (q \cdot p_K)(q \cdot p_+) / (m_\pi^2 m_K^2)$$

$$A = A(K^+ \rightarrow \pi^+ \pi^0)$$

$K^+ \rightarrow \pi^+ \pi^0 \gamma$ $W - T_c$ Dalitz plot

Integrating over T_c deviations from IB measured





- $M1 \sim (-2 + 3a_2 - 6a_3)$

\uparrow
Wess Zumino

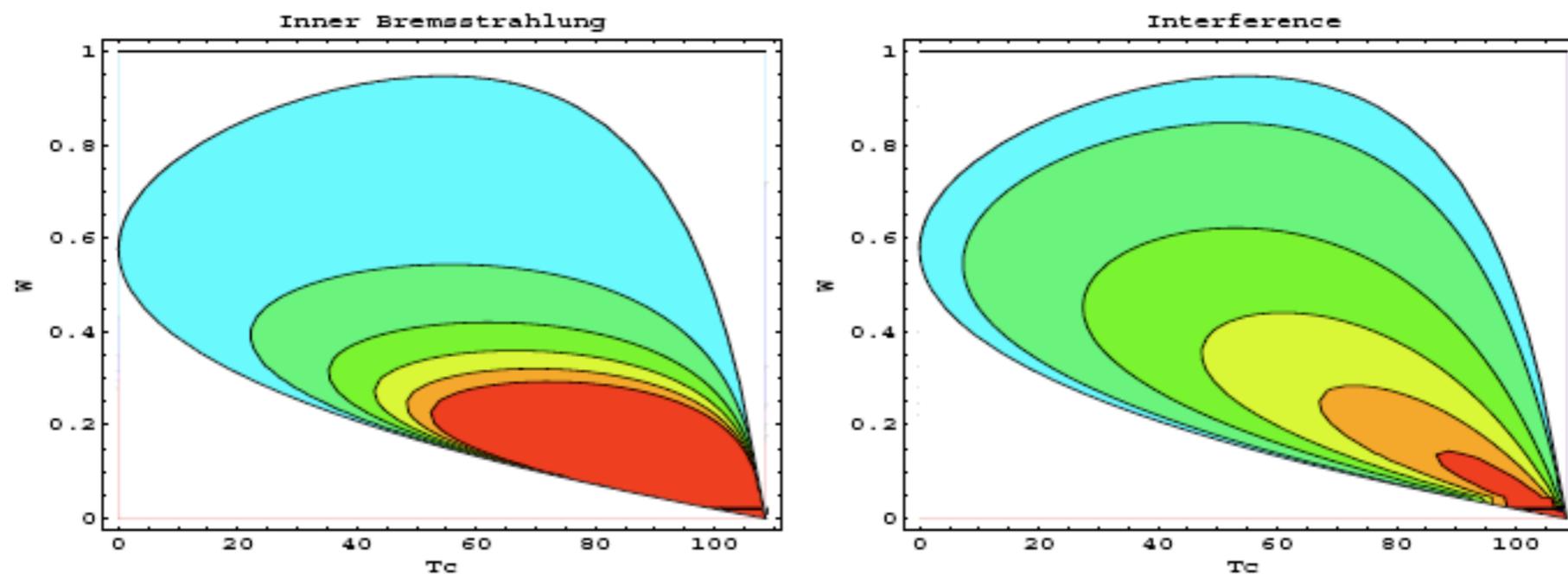
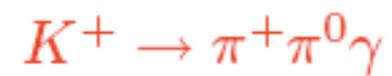
\uparrow
 p^4 CT's (VMD)

$$-2.5$$

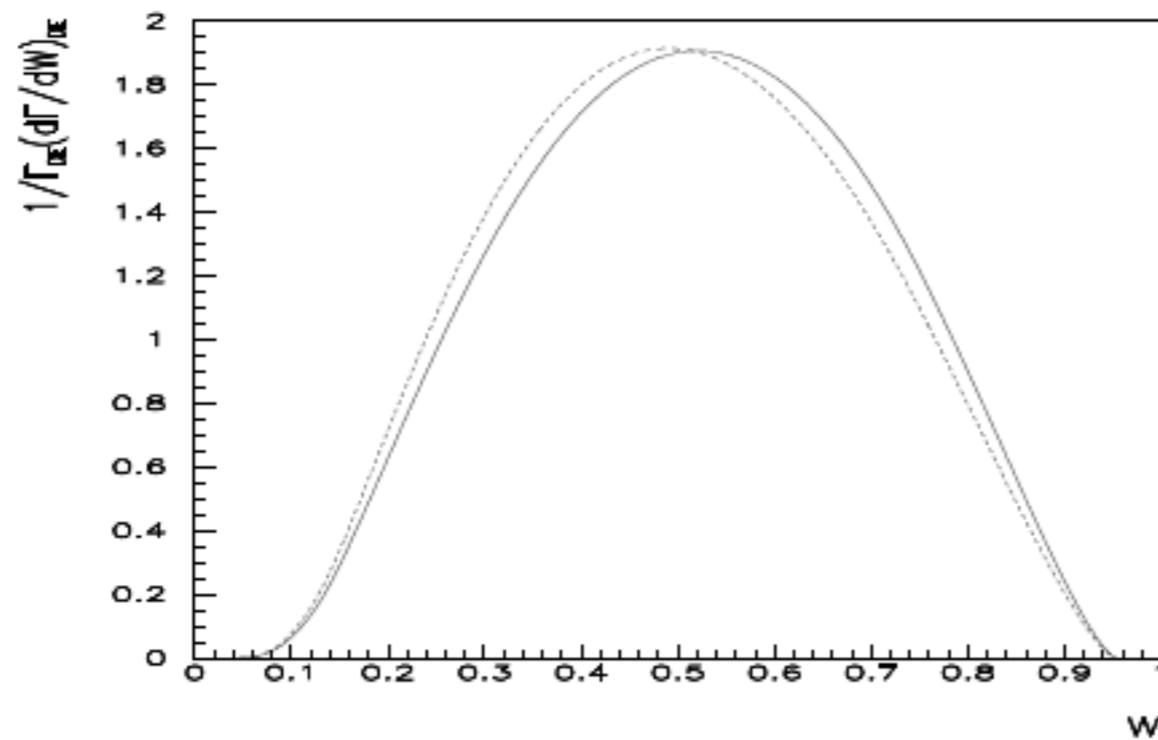
$$\Downarrow$$

$$a_i \text{ small?}$$

Cheng
Bijnens, Ecker, Pich; G.D., Gao



- E787 has measured $M1$ and $\text{Re}\left(\frac{E1}{E_{IB}}\right) \sim (-0.4 \pm 1.6)\%$
- ↓
- E1 dominated by CT \Rightarrow E787 constrains models ($k_f < 1$)



- $\frac{d\Gamma}{dW}$ may be **crucial** to study well the form factor

$$W^2 = (q \cdot p_K)(q \cdot p_+) / (m_\pi^2 m_K^2)$$

- to establish VMD

CP asymmetry

- In the asymmetry in the slope, $\frac{\partial^2 \Gamma^\pm}{\partial T_c^* \partial W^2}$ select a favourable kin. region (large W^2)
- This asymm., Ω , in extensions of SM $\sim \mathcal{O}(10^{-4})$ Colangelo et al.
- SM $\leq \mathcal{O}(10^{-5})$ Paver et al.
- Assuming the expts. are almost seeing the CP conserving [E1 Statistics](#) seems tough but previous limit ([Smith eta I. 76](#)) weak
- Similar analysis for **CPV** in K_L : but time interf. required



G. D'Ambrosio, N. Paver, A. Pugliese, G. Pancheri and P. Gensini during the
EUROPEAN Collaboration Meeting, in Durham, 10-15 December, 1994

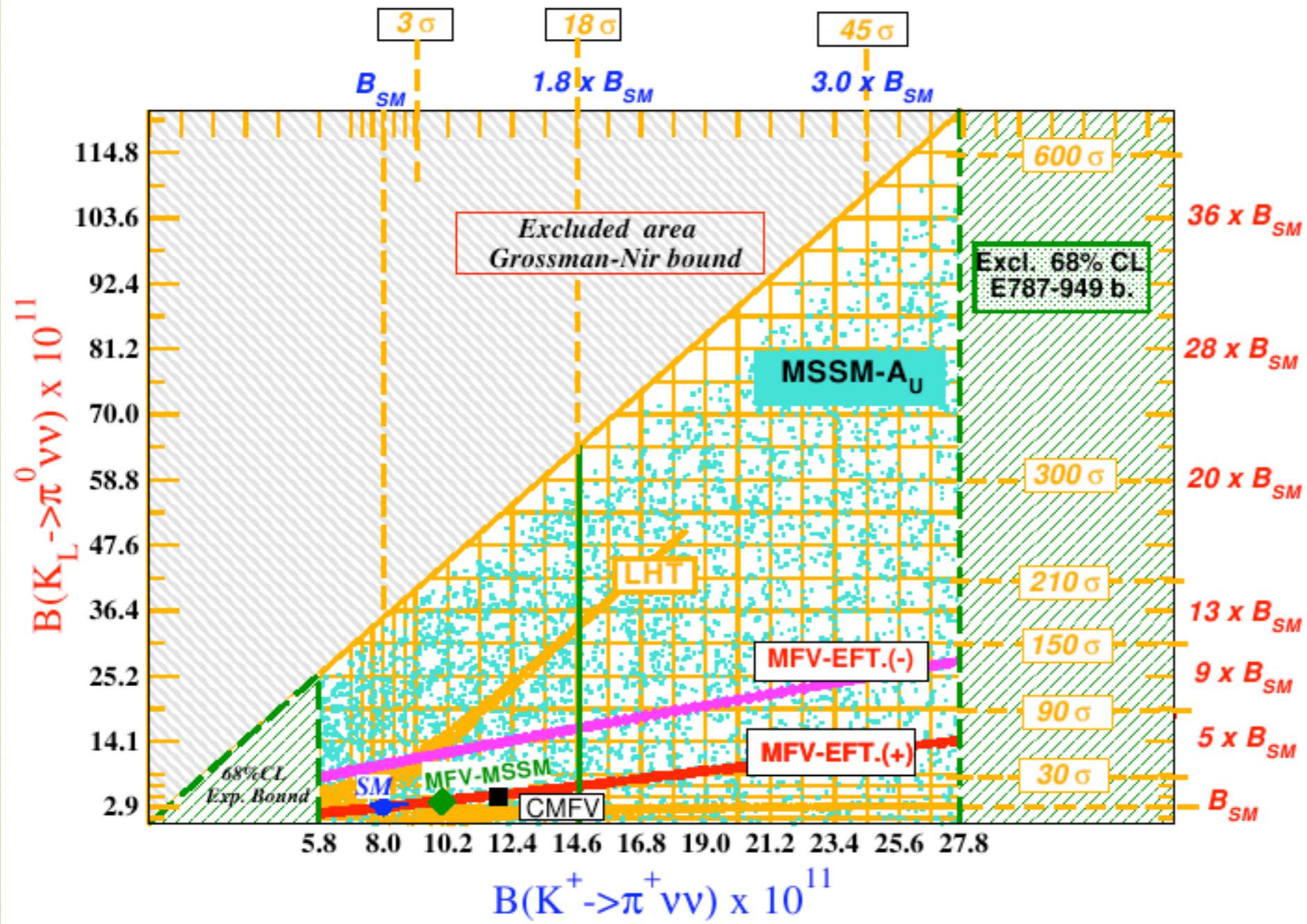


PHOTOGRAPH BY [unreadable]

Conclusions

- We have reached a precision in golden decays making worthy to check the less clean ones
- Many kaon decays still to explore
i.e. $K_L \rightarrow \pi^+ \pi^- e e$ $K^+ \rightarrow \pi^+ \pi^0 e e$
- Sorry not discussing the cusp and $K \rightarrow \pi \pi \pi$

NA62 Fantastic attack



Mescia

A. The New Physics flavor puzzle

- Most New Physics (NP) models have either *new flavored particles*, or *new flavor-breaking interactions* between quarks and leptons.

→ *New contributions to FCNC's!*

- At the same time, there is *no signal of NP in low-energy experiments*.

↳ Experiments ~ SM predictions

$$\left\{ \begin{array}{l} b \rightarrow s: \\ |V_{tb}^* V_{ts}| \sim \lambda^2 \end{array} \right. \quad \left\{ \begin{array}{l} b \rightarrow d: \\ |V_{tb}^* V_{td}| \sim \lambda^3 \end{array} \right.$$

$$\left\{ \begin{array}{l} s \rightarrow d: \\ |V_{ts}^* V_{td}| \sim \lambda^5 \end{array} \right.$$

- New Physics cannot be *both light and generic*:

$$\mathcal{L}_{\text{eff}} = \frac{c_{bs}}{\Lambda^2} (\bar{b} \Gamma s)(\bar{\nu} \Gamma \nu) + \frac{c_{bd}}{\Lambda^2} (\bar{b} \Gamma d)(\bar{\nu} \Gamma \nu) + \frac{c_{sd}}{\Lambda^2} (\bar{s} \Gamma d)(\bar{\nu} \Gamma \nu) + \dots$$

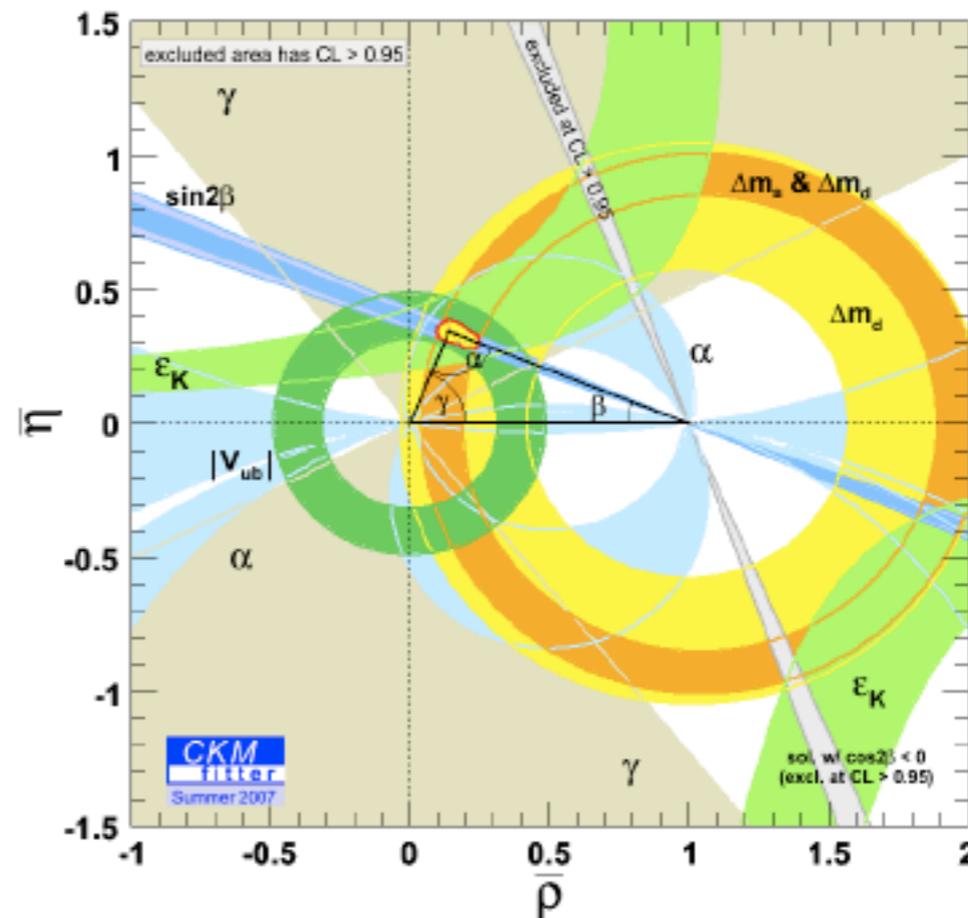
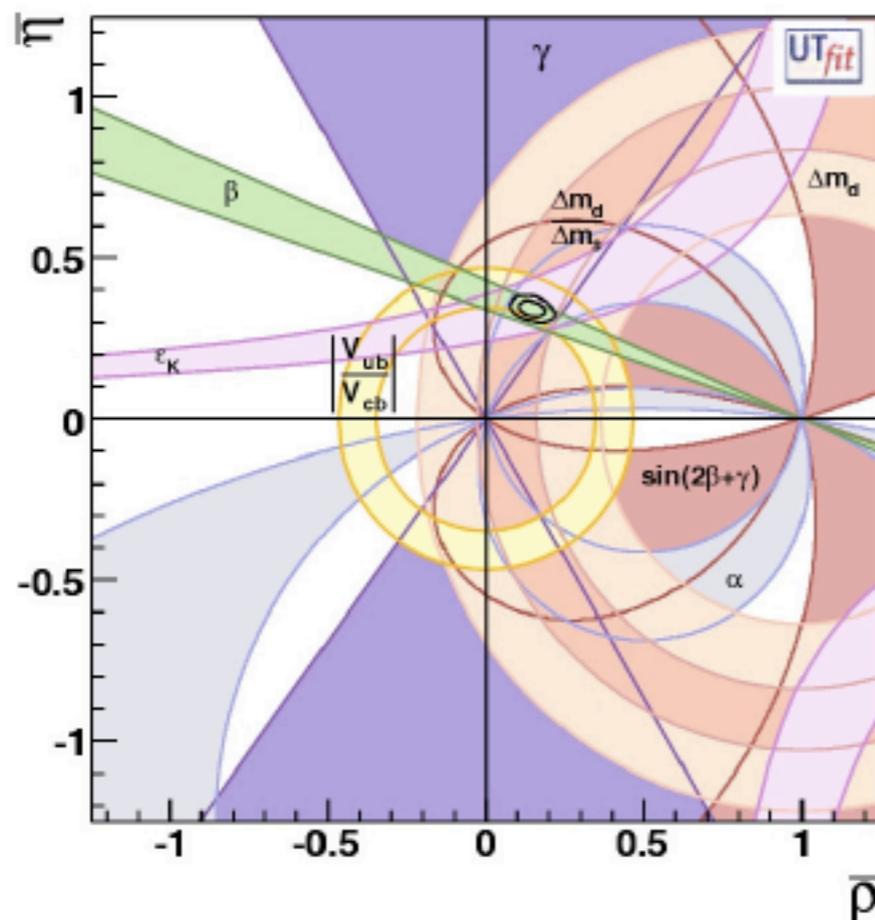
$c_{sd} \approx 1$, $\Lambda \gtrsim 75 \text{ TeV}$: NP very massive, beyond the reach of LHC,

$\Lambda \approx 1 \text{ TeV}$, $c_{sd} \lesssim V_{ts}^* V_{td}$: NP flavor structures highly non-generic.

Most constraining!

B. Global CKM fits and constraints on New Physics

Flavianet members contribute to CKMfitter and UTfit analyses:



Bayesian vs. frequentist?

Charles, Hocker, Lacker, Le Diberder, T'Jampens '06

Hint of a large new physics phase in $b \rightarrow s$ transitions?

Bona et al. '08

C. Bottom-up approach to the New Physics flavor puzzle

Minimal Flavor Violation: New Physics scale as in the SM.

$$\mathcal{L}_{\text{eff}} = \frac{c_{qq'}}{\Lambda^2} (\bar{q}\Gamma q')(\bar{\nu}\Gamma\nu) + \dots \quad \text{with} \quad c_{qq'} \sim |V_{tq}^* V_{tq'}| \Rightarrow \Lambda \leq 1 \text{ TeV}$$

“Constrained” MFV: No new phase, no new operator.

“Symmetric” MFV: Only the Yukawas can break the $SU(3)^5$ flavor-symmetry.

- MSSM at large $\tan \beta \equiv v_u / v_d$ *Freitas, Gasser, Haisch '07*
Isidori, Mescia, Paradisi, Temes '07
- MSSM: UT fit in the B sector *Altmannshofer, Buras, Guadagnoli '07*
Altmannshofer, Buras, Guadagnoli, Wick '07
- MSSM: running MFV *Paradisi, Ratz, Schieren, Simonetto '07*
- MFV as an alternative to R-parity *Nikolidakis, CS '07*
- Extra quarks: connection with LHC *Grossman, Nir, Thaler, Volansky, Zupan '07*
- Generic: constraints from $Z \rightarrow b\bar{b}, \dots$ *Haisch, Weiler '07*
- Lepton sector & leptogenesis *Cirigliano, De Simone, Isidori, Masina, Riotto '07*

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D. Top-down approach to the New Physics flavor puzzle

Specific New Physics models: identifying interesting scenarios, and studying their impact on flavor physics, including their correlation with LHC observables.

- Supersymmetry:*
- Generic MSSM
 - with MFV
 - with large $\tan \beta$
 - with RPV

(see e.g. Refs. on the previous slide)

Supersymmetric *GUT scenarios*

Dorsner, Fileviez Perez, Rodrigo '06

Cuichini, Masiero, Paradisi, Silvestrini, Vempati, Vives '07

Albrecht, Altmannshofer, Buras, Guadagnoli, Straub '07

Altmannshofer, Guadagnoli, Raby, Straub '08

Alternatives: - *Little Higgs*

Blanke, Buras, Recksiegel, Tarantino, Uhlig '07

Blanke, Buras, Recksiegel, Tarantino '08

- *Higgsless*

Bernard, Oertel, Passemar, Stern '07

Barbieri, Isidori, Rychkov, Trincherini '08

- *Extra-dimensions*

Davidson, Isidori, Uhlig '07, Haisch, Weiler '07

Colangelo, De Fazio, Ferrandes, Pham '06

- *Unparticles*

Zwicky '07, Freitas, Wyler '07

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