

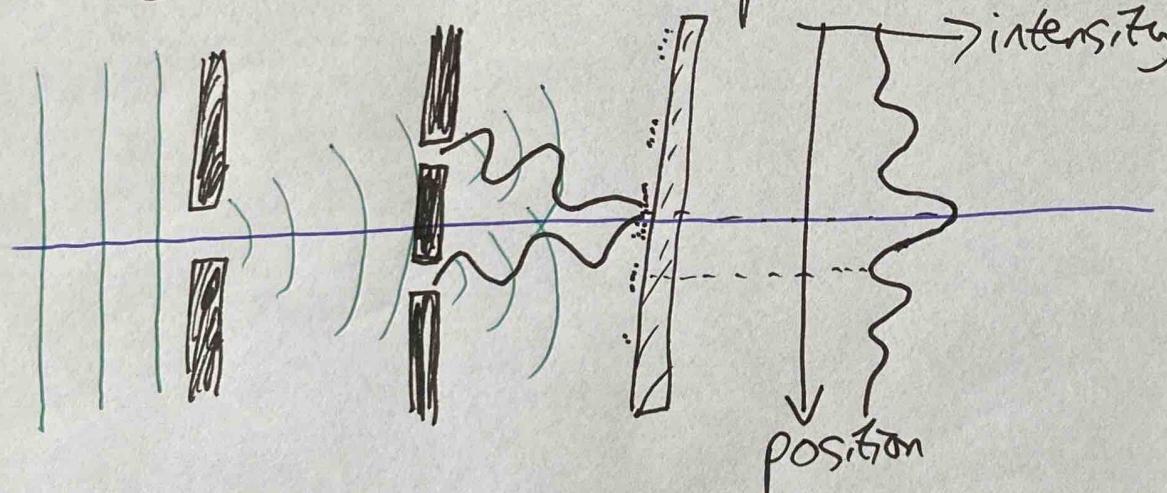
CAN WE TEST THE EFFECT OF A MASS IN A SUPERPOSITION?
GRAVITATIONAL

MACROSCOPIC QUANTUM SUPERPOSITIONS
TO TEST QUANTUM GRAVITY

QUANTUM MECHANICS

- INTERFEROMETRY

- Quantum 2-slit experiment



phase
 $\rightarrow \sin$

- WAVEFUNCTION

↓

SPATIAL
SUPERPOSITION

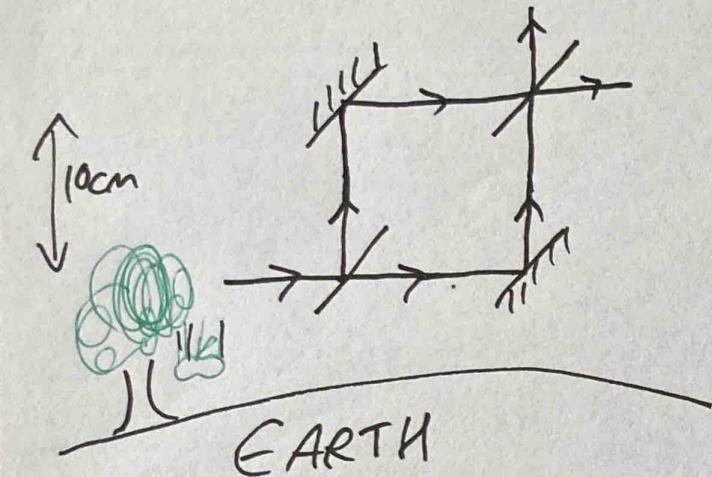
$$|Y\rangle = \frac{1}{\sqrt{2}}(|L\rangle + |R\rangle)$$

★ MOLECULES
OF 2000 ATOMS [1]

$$S.E.: \left[\frac{\hat{p}^2}{2m} + \hat{V} \right] |Y\rangle = i\hbar \frac{\partial}{\partial \epsilon} |Y\rangle$$

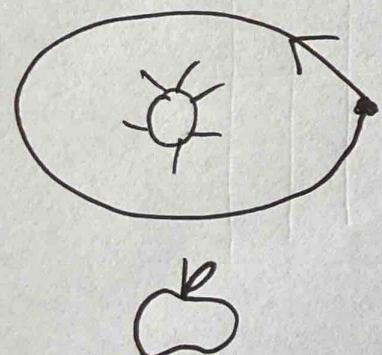
$$(p = \hbar/k) \quad \text{INTERFERENCE}$$

①



Interferometer
1975
COW [2]

NEWTON



GRAVITY

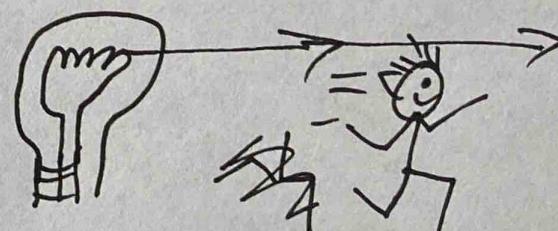
$$F = \frac{GMm}{r^2} \approx mg$$

$$V = -\frac{GMm}{r} \quad \leftarrow \text{GRAVITATIONAL POTENTIAL ENERGY}$$

$$V_{\text{Earth}} \approx mgh$$

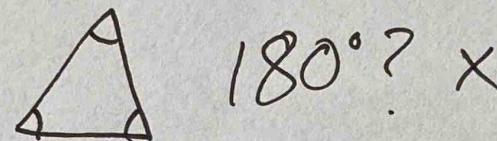
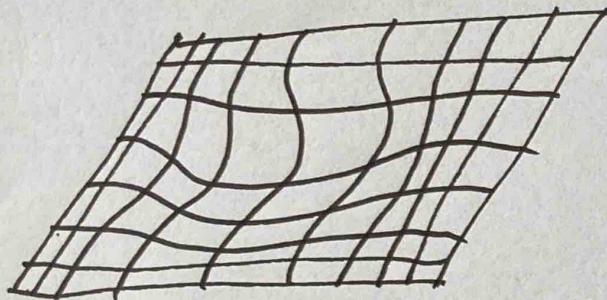
PROBLEMS

- mediator? X
- instantaneous? X



GENERAL RELATIVITY

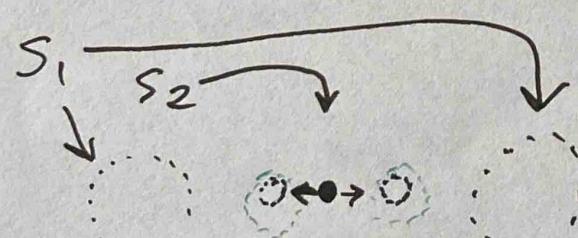
MASS CURVES SPACETIME



1936
BRONSTEIN
[3, 4, 5]

1957 CHAPEL HILL
FEYNMAN [6]

NANOPARTICLE: $10^8 - 10^{12}$ atoms



$$|4,\rangle = \frac{1}{\sqrt{2}} (|L\rangle + |R\rangle)$$

$$|4,\rangle |4_2\rangle = \frac{1}{\sqrt{2}} (|L\rangle + |R\rangle) |4_2\rangle$$

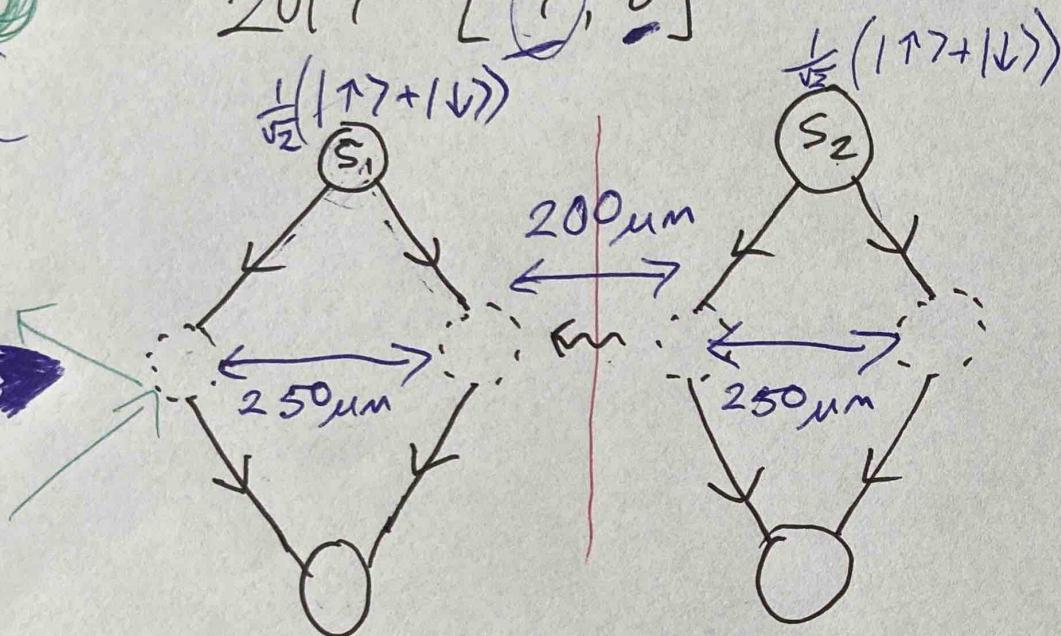
↓

IF WE HAVE
QUANTUM GRAVITY: $|4_{\text{entangled}}\rangle = \frac{1}{\sqrt{2}} (|L,L\rangle + |R,R\rangle)$ ③

Schrodinger Cats Proposal

2017

[7, 8]



cat 1



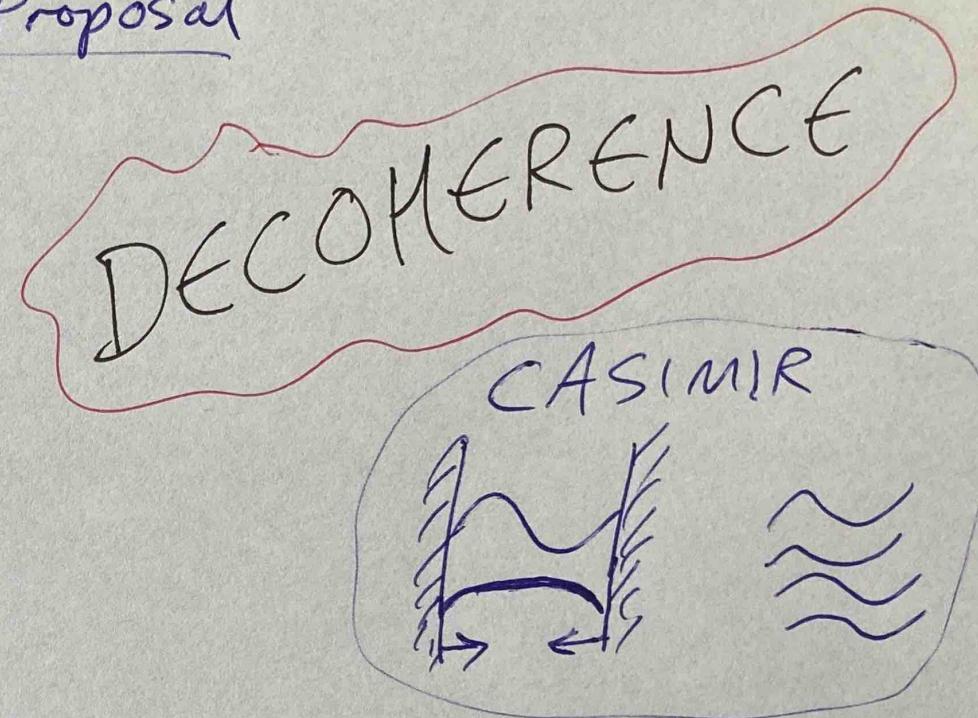
- 2 mm across
- 10^{-14} kg
- 10^{12} atoms



cat 2

* ONLY A QUANTUM THING CAN ENTANGLE THINGS

- 1 s coherence time



Lecture 2

Decoherence & Experimental Progress

Decoherence is:

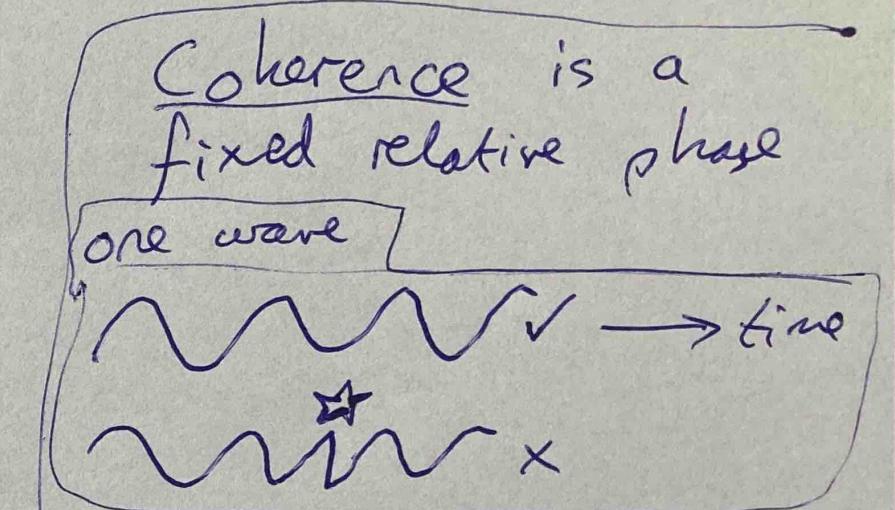
- quantum noise
- entanglement you don't like [9-12]

Entanglement

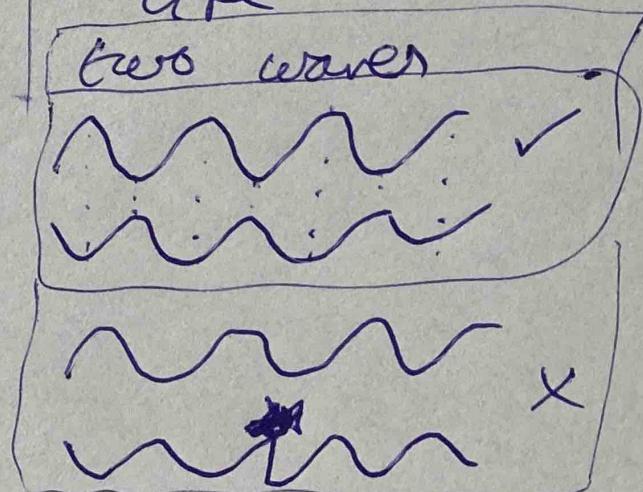
Coin 1	Coin 2
H	T
T	T
T	H
H	H

Spin 1	Spin 2
↑	↑
↓	↓
↓	↑
↑	↓
↓	↑
↑	↓

$$|4\rangle = \frac{1}{\sqrt{2}}(|TT\rangle + |LL\rangle)$$



Noise is an interaction you don't like



Decoherence for nanoparticles

- potential energy noise
- collisions - gas atoms
 - photons (blackbody radiation - emission, absorption, scattering)
 - collapse models (CSL, DP...)

[13]

★ $\sim 2\mu\text{m}$ particle: if we want
 $\sim 1\text{s}$ coherence time
 \Rightarrow need $\sim 10^{-16}$ mbar
need $\sim 5\text{K}$ internal temperature

more details: [14, 15]

Quantum Harmonic Oscillator

$$E = KE + PE$$

$$= \frac{(\Delta p)^2}{2m} + \frac{1}{2} m\omega^2 (\Delta x)^2$$

$$\frac{dE}{d(\Delta x)} = 0$$

$$\Delta x = \sqrt{\frac{\hbar}{2m\omega}}$$

Zero
Point
notion

~~$$E_0 = \frac{\hbar\omega}{2}$$~~

+ HUP
 $\Delta x \Delta p = \frac{\hbar}{2}$

Experiments

Ⓐ Ground-state cooling of nanoparticles

[16-18]

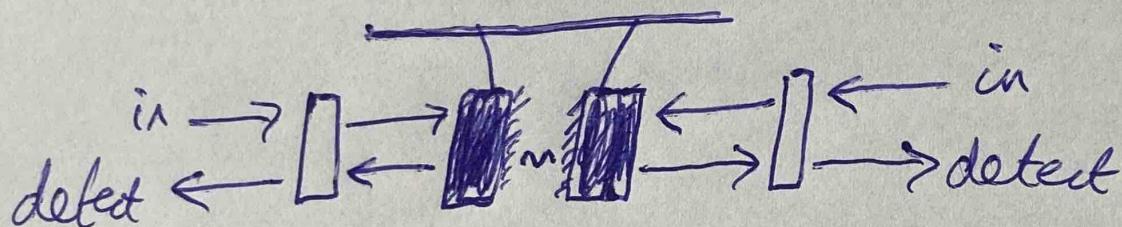
Ⓑ Feedback cooling of LIGO mirror [19]

Ⓒ Gravitational interaction between two 90mg masses

Lecture 3

Extensions to the Schrodinger Cat's Proposal

- Use a LIGO [21]



NEEDS:

- * 2 mirrors back-to-back

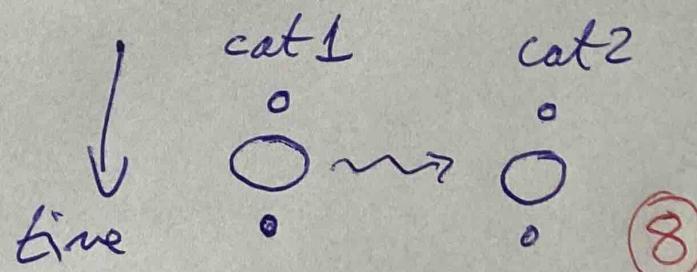
- * Needs more COM cooling ($\times 1000?$) than ref [19]

- Control potential to expand wavefunction [22]
[instead of creating $\frac{1}{\sqrt{2}}(|L\rangle + |R\rangle)$]

potential: $V \rightarrow \Lambda \rightarrow V \rightarrow \Lambda \rightarrow V$

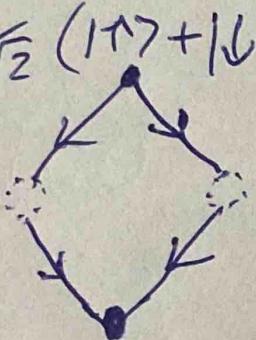
— \rightarrow time

'squeezing'



- Experiments with a closed-loop Stern-Gerlach interferometer with atoms

[23, 24] $\frac{1}{\sqrt{2}}(|\uparrow\rangle + |\downarrow\rangle)$



BEC: $\sim 10^7$ atoms
in one
quantum
state

$$|\Psi\rangle_{\text{cat}} = \frac{1}{\sqrt{2}}(|\text{all left}\rangle + |\text{all right}\rangle)$$

$$|\Psi\rangle = \left[\frac{1}{\sqrt{2}}(|L\rangle + |R\rangle) \right] \left[\frac{1}{\sqrt{2}}(|L\rangle + |R\rangle) \right]$$

.... +

- Motional dynamic decoupling [25]

... based on

spin dynamic decoupling

... based on

spin echo

Summary: Macroscopic Superposition could test the gravitational effect of matter, testing quantum gravity. ①