

QSFP 2021 – Experimental Neutrino Physics

Lecture 2

September 16, 2021

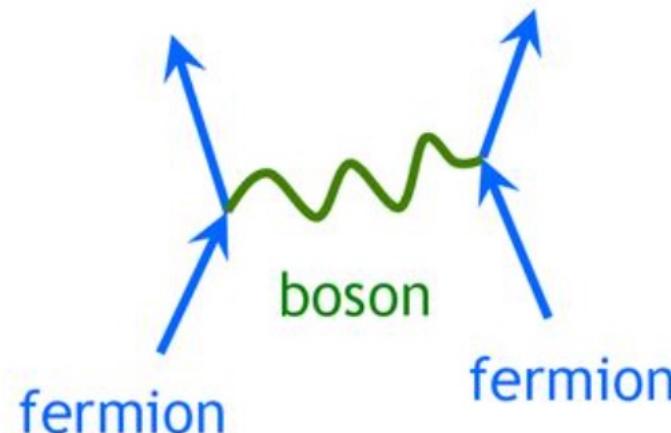
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Selected facts about
neutrinos in the Standard Model...

The Standard Model

- The Standard Model combines the electromagnetic, weak, and strong interactions
- Bosons with spin 1 communicate the forces between Fermion of spin $\frac{1}{2}$
- Mass of Fermions (but neutrinos?) is generated through the Higgs boson (spin 1)



The Nobel Prize in Physics 1979



Sheldon Lee
Glashow
Prize share: 1/3



Abdus Salam
Prize share: 1/3



Steven Weinberg
Prize share: 1/3

The Standard Model

- The Standard Model includes all known elementary fermions

<u>Quarks</u> (spin 1/2)		
Bottom Quark (Charge -1/3)	b	Up Quark (Charge 2/3)
Down Quark (Charge -1/3)	d	Top Quark (Charge 2/3)
Strange Quark (Charge -1/3)	s	Charm Quark (Charge 2/3)

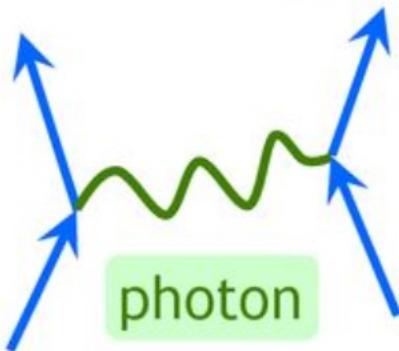
<u>Leptons</u> (spin 1/2)		
Electron (Charge -1)	e⁻	Electron Neutrino (Charge 0)
Tau (Charge -1)	T	Tau Neutrino (Charge 0)
Muon (Charge -1)	μ	Muon Neutrino (Charge 0)

- Matter particles are grouped into three families
- Each fermion has a corresponding antiparticle

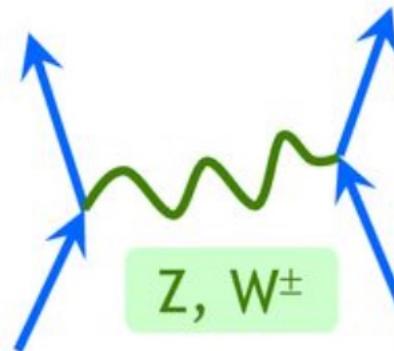
The Standard Model: Weak Interaction

- Three sets of bosons mediate three interactions

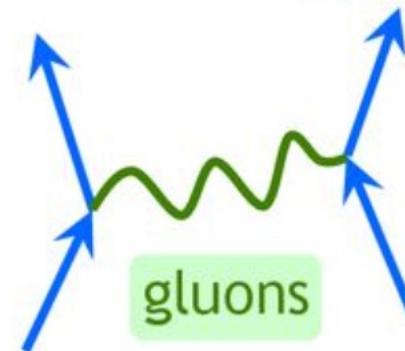
electromagnetism



weak interaction

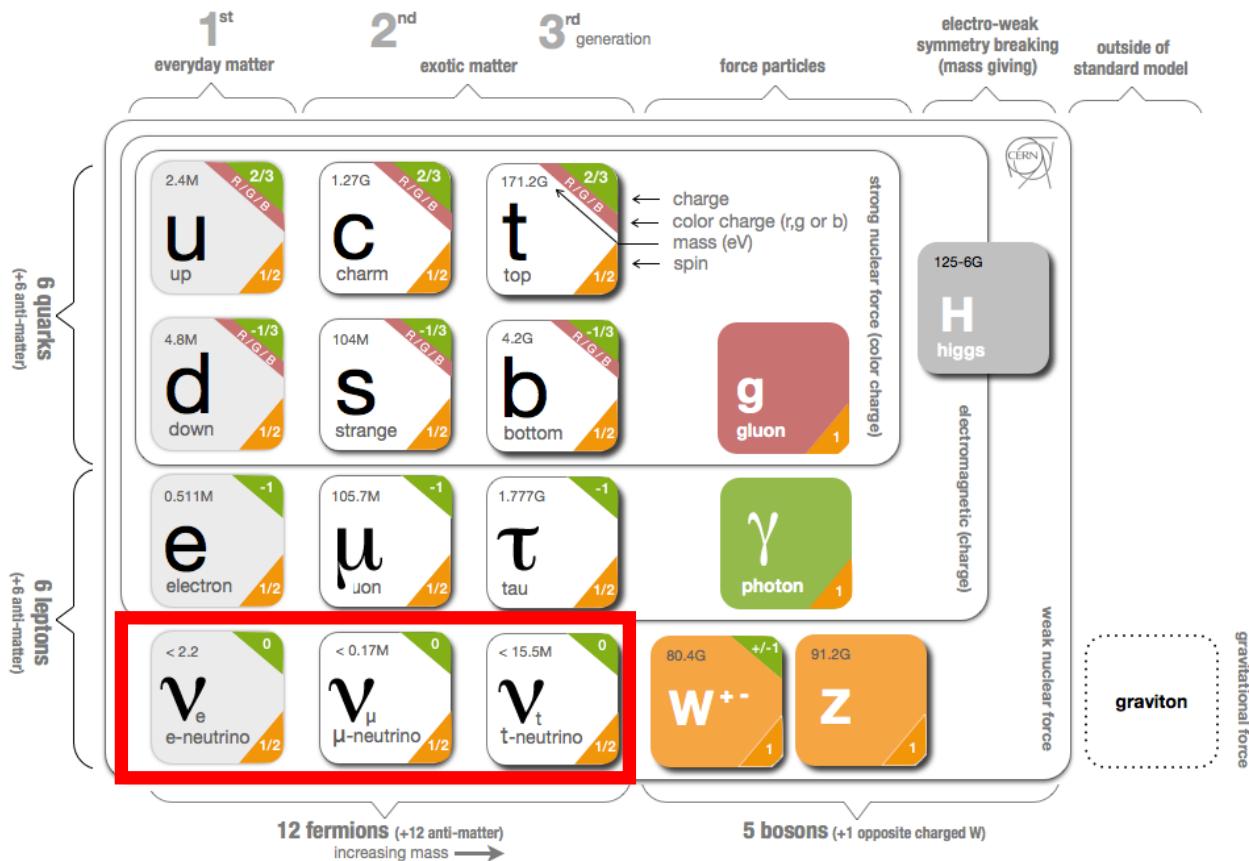


strong interaction



- Each interaction has its characteristic set of boson
- Neutrinos are only involved in weak interactions

Standard Model: 3 types of neutrinos



- Three neutrino flavors
- Neutrinos only interact via weak interaction (and gravity)

Interaction Rules

- Electric charge conservation
- Lepton number conservation
- Energy / Momentum conservation

Neutrino Production

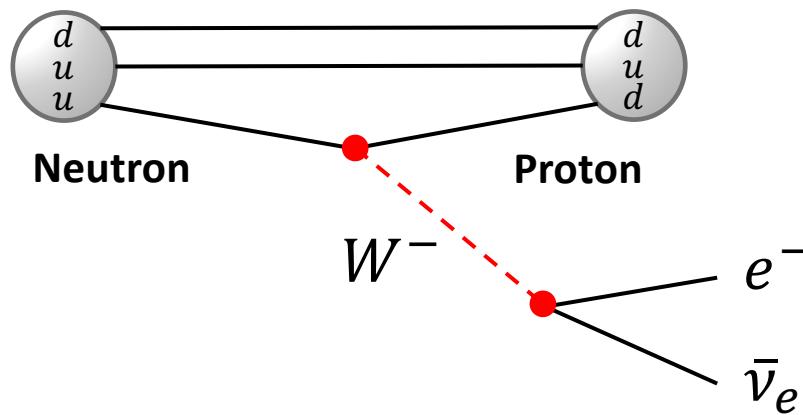
$$m_p = 938.3 \text{ MeV}$$

$$m_n = 939.6 \text{ MeV}$$

Semi-leptonic decay: β -decay's

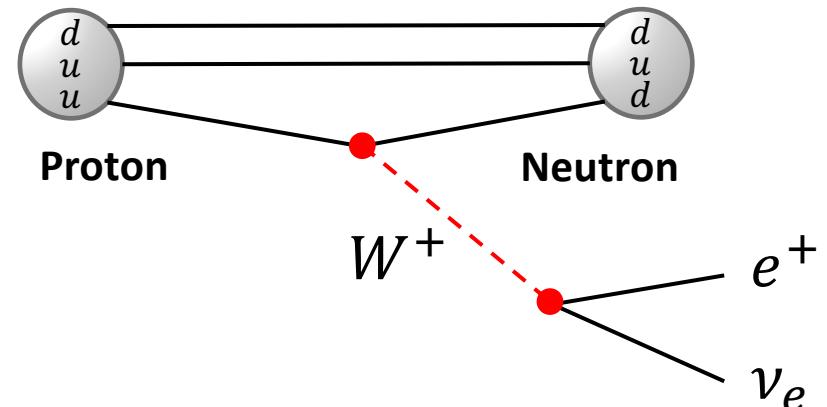
β^- -decay

- Lifetime neutron: 15 minutes (887 s)
- Occurs in reactors, fission explosions



β^+ -decay

- Free proton decay has never been observed



Energy balance has to be fulfilled

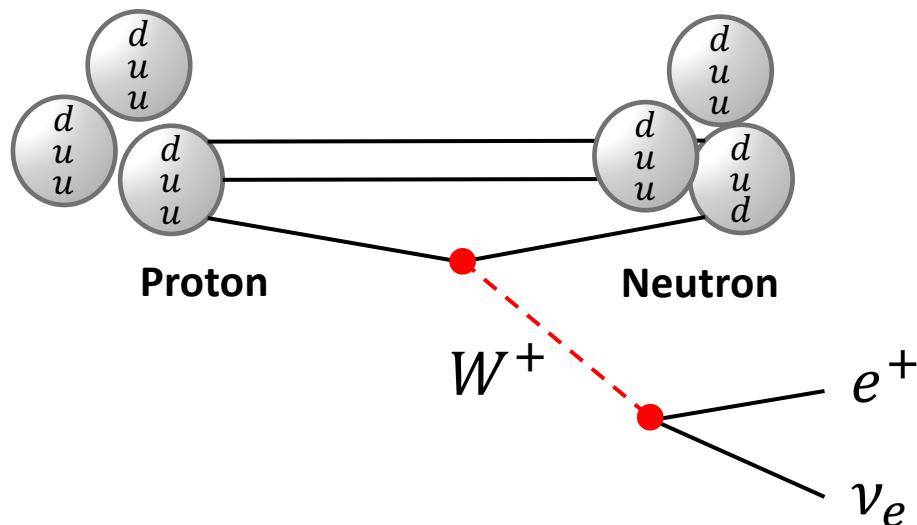
$$X \rightarrow Y + e + \nu$$

$$E_0 = M(X) - M(Y) - m_e - m_\nu > 0$$

Semi-leptonic decay: β^+ and Electron capture

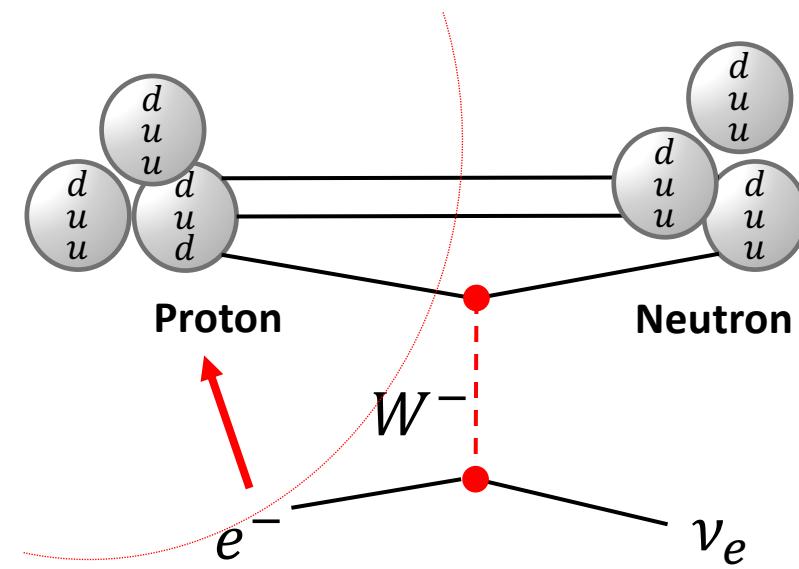
β^+ -decay

- Free proton decay has never been observed
- β^+ decay only occurs in proton-rich nuclei



Electron capture:

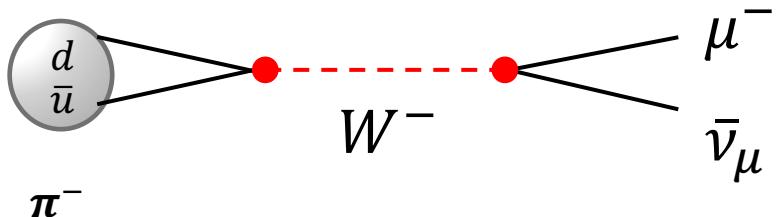
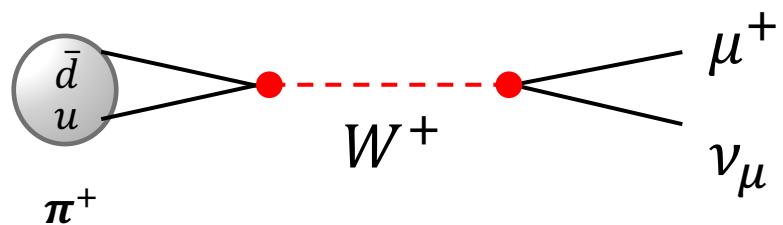
- Electron captured from atomic shell
- Occurs when released energy is not enough to create a positron



Semi-leptonic decay: e.g. Pion decay

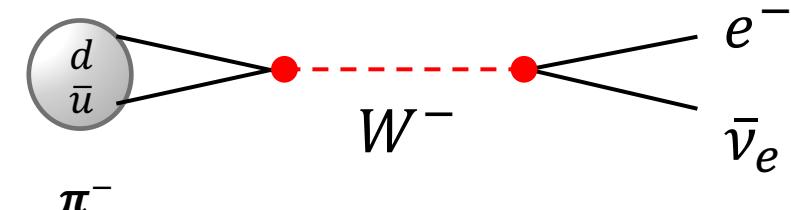
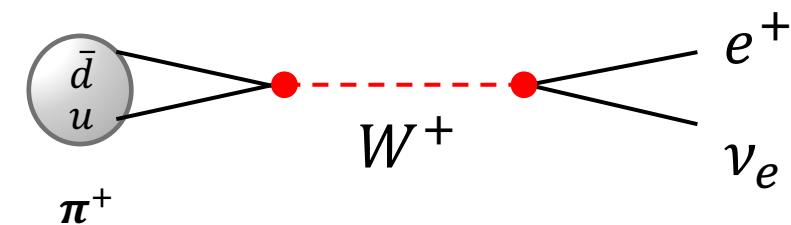
Pion (quark and an antiquark) to muons

- Pion lifetime: 2.6×10^{-8} s
- Decays with 99.99% probability to muons
- Atmospheric / Accelerator neutrinos



Pion to electrons

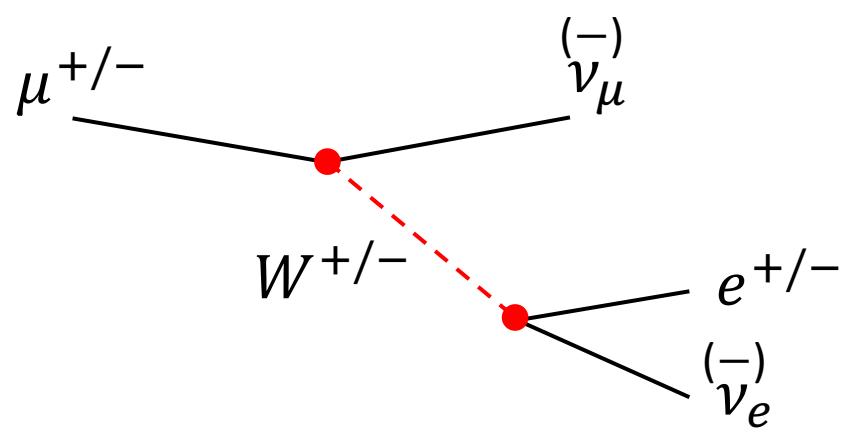
- Suppressed due to smaller mass of electron (compared to muon) → helicity suppression



Leptonic Decay: muon and tau decay

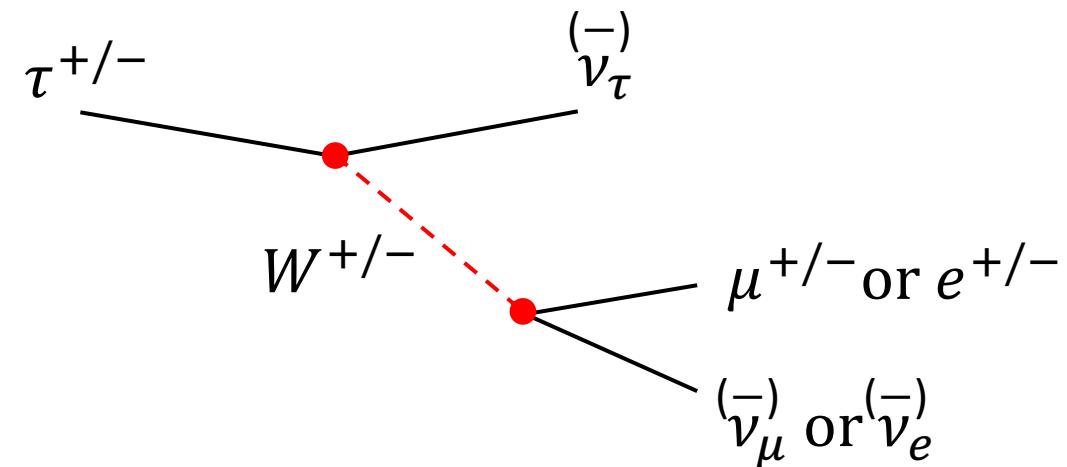
Muon decay

- Muon lifetime: 2.2 ms
- Decays to muon-neutrino, electron, and electron-neutrino of known spectrum
- Atmospheric / Accelerator neutrinos



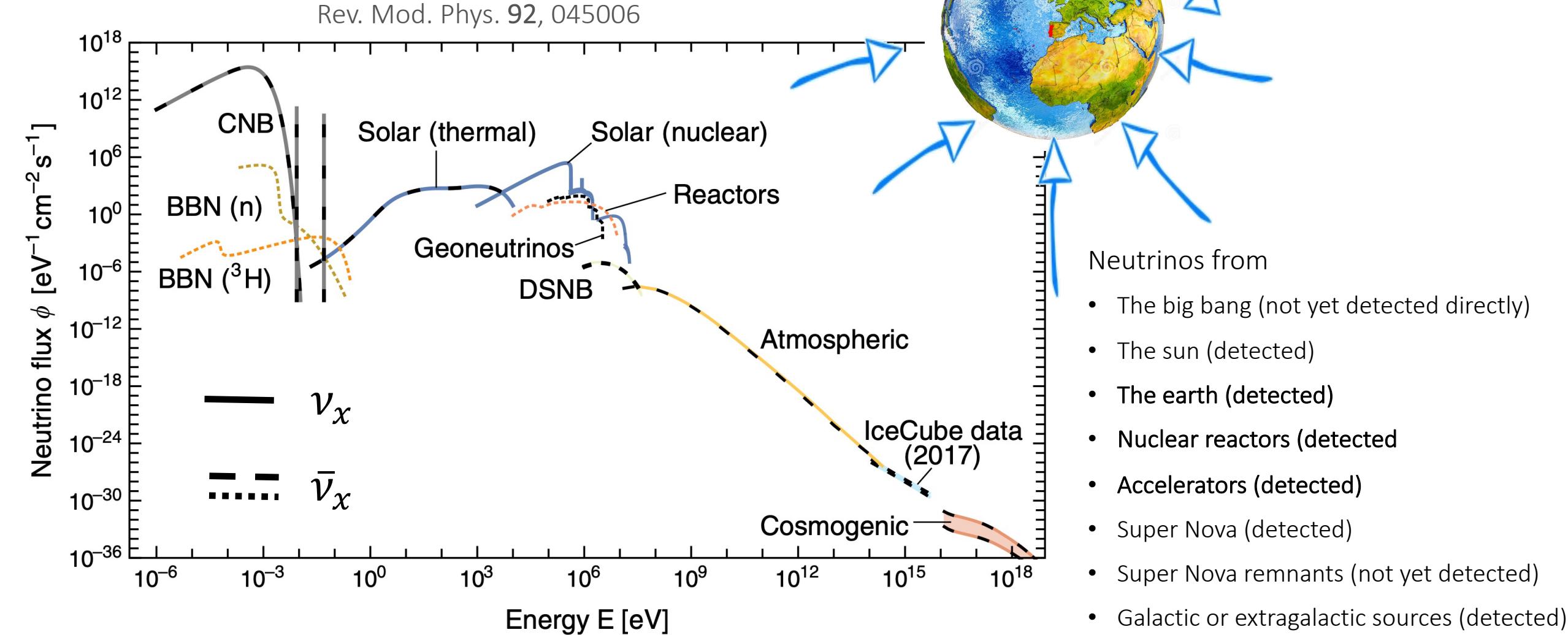
Tau decay

- Tau lifetime: 2.3×10^{-13} s
- Decays to neutrinos + muon (17%) or electron (17%)
- Accelerator neutrinos



Neutrino Sources

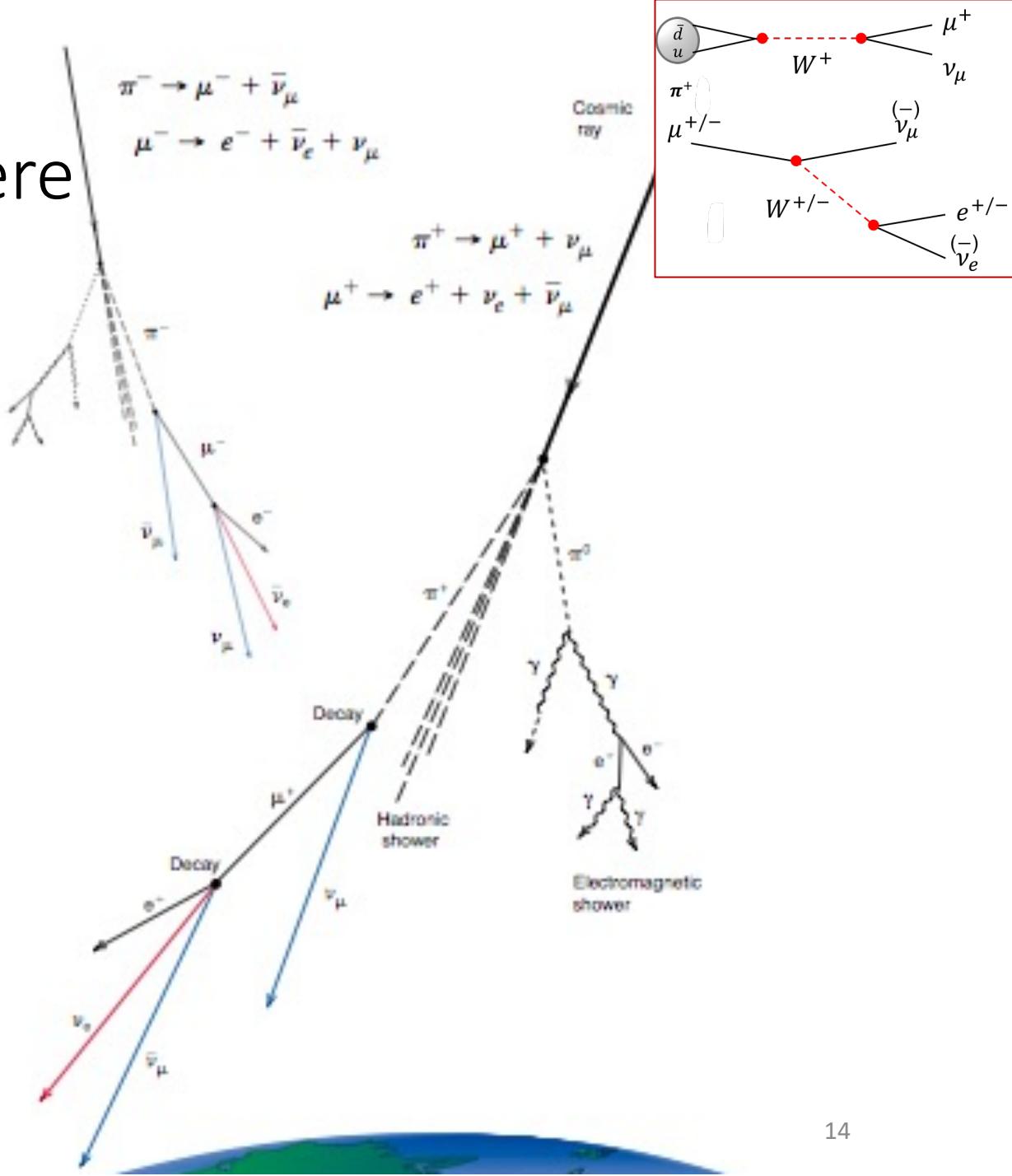
Grand unified neutrino spectrum



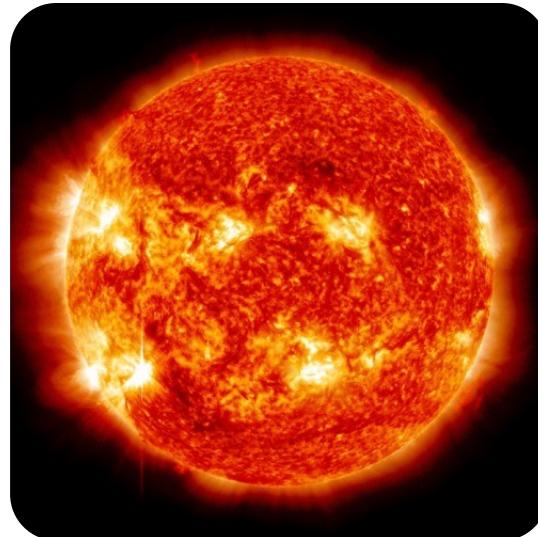
Neutrinos from the atmosphere



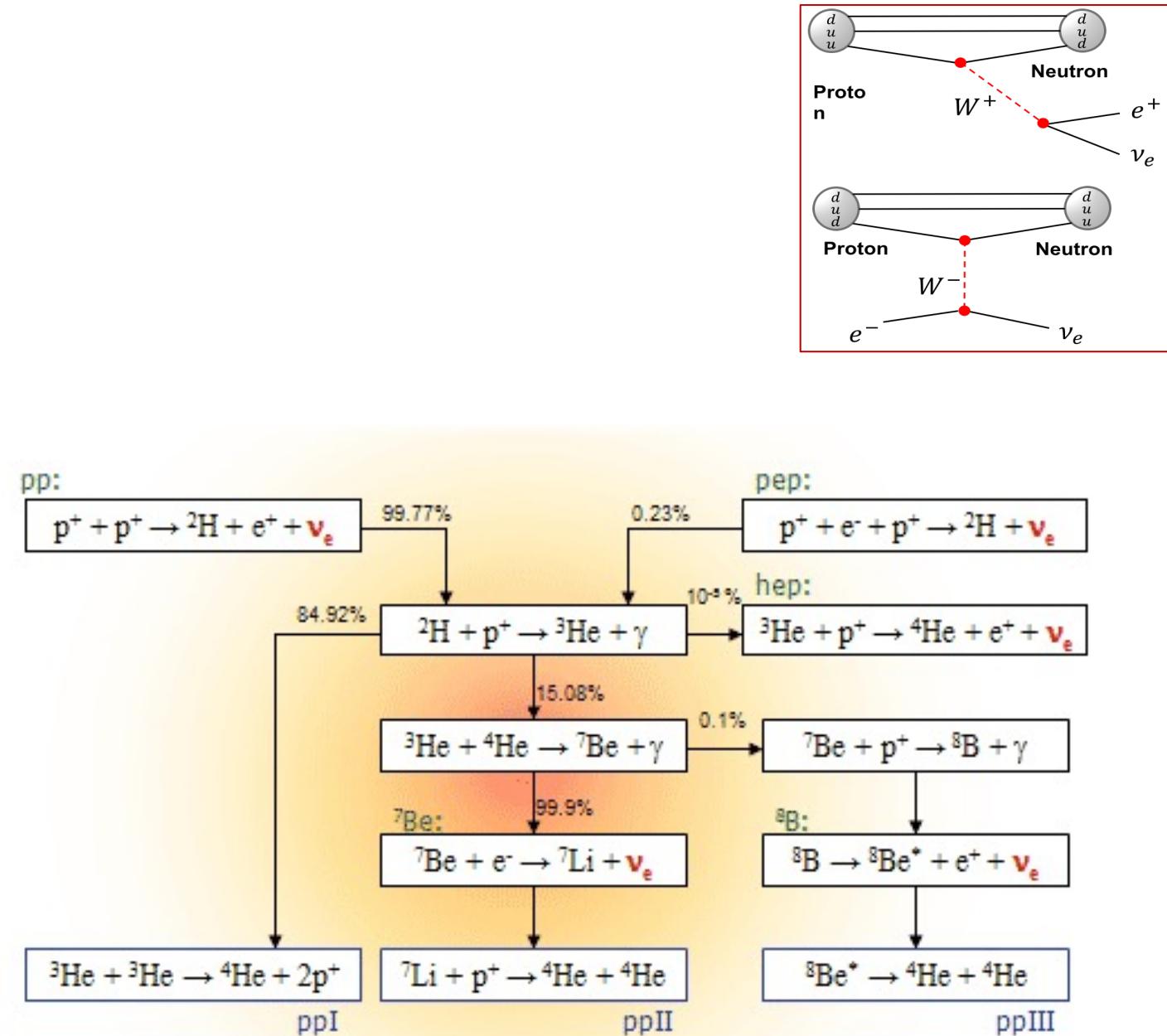
- Collision of cosmic rays (protons) with atmosphere
- Generation of showers of pions = ud quark
- Muon- and electron-neutrinos are produced in 2:1 ratio
- Used to detect neutrino oscillations (1998)



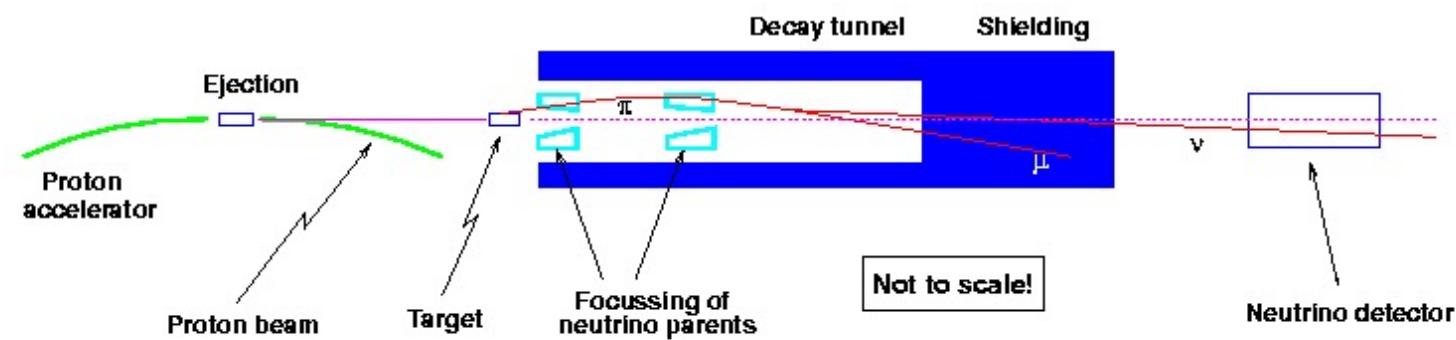
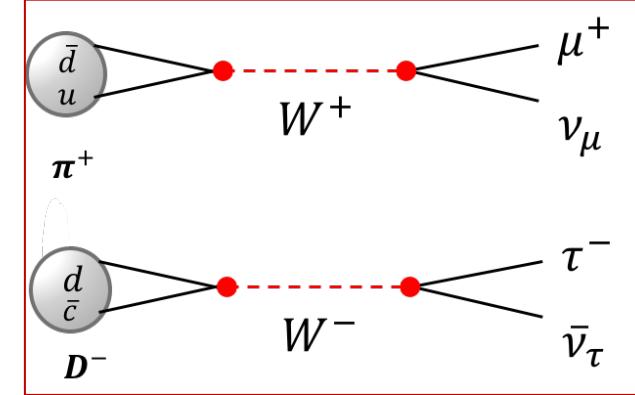
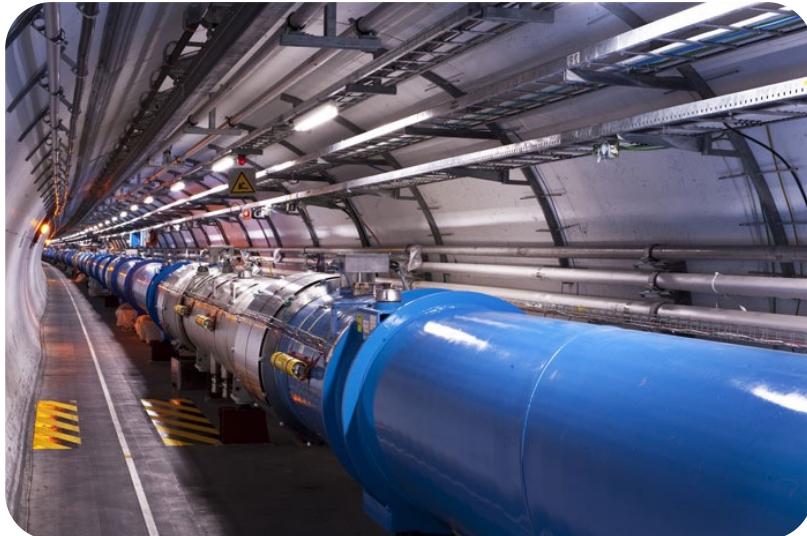
Neutrinos from the sun



- Nuclear fusion in the sun
- Only electron neutrinos are created
- @Earth: 66 Billion neutrinos /cm²/s



Neutrinos from accelerators



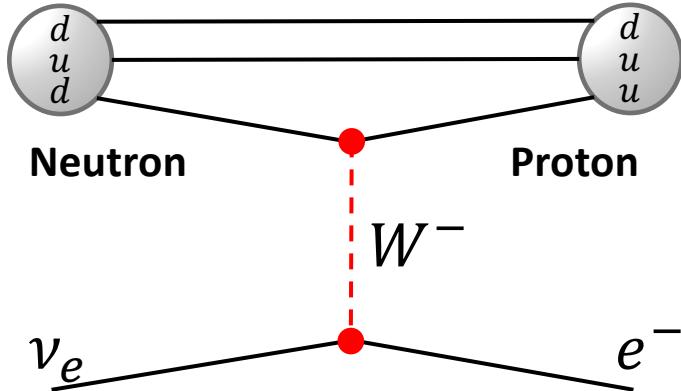
- Protons hit a target (e.g. made of beryllium)
- Generation of pions, kaons, and charmed mesons
- Mesons decay and produce neutrinos

Neutrino Interactions

Inverse beta decay

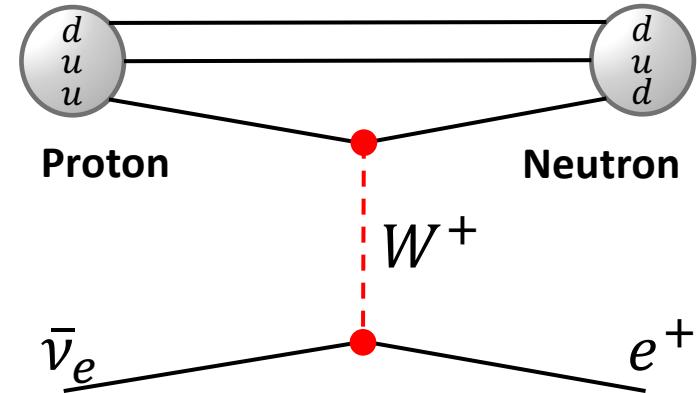
Inverse β^- -decay

- Capture of electron neutrino
- High-enough energy muon/tau-neutrinos would be needed to create a muon/tau



Inverse β^+ -decay

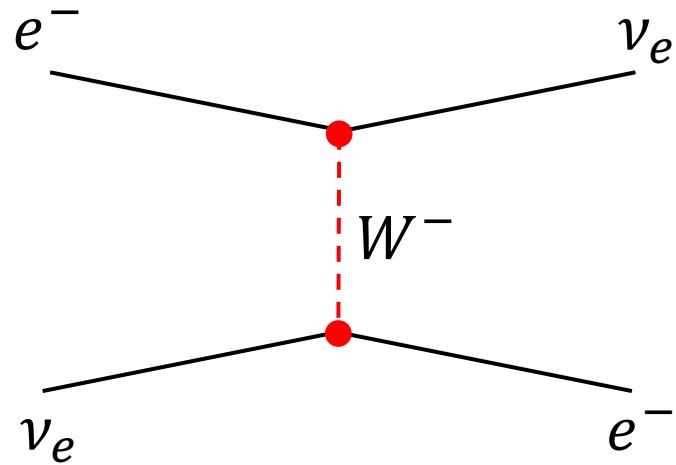
- Capture of electron anti-neutrino
- Important detection reaction !



Electron scattering

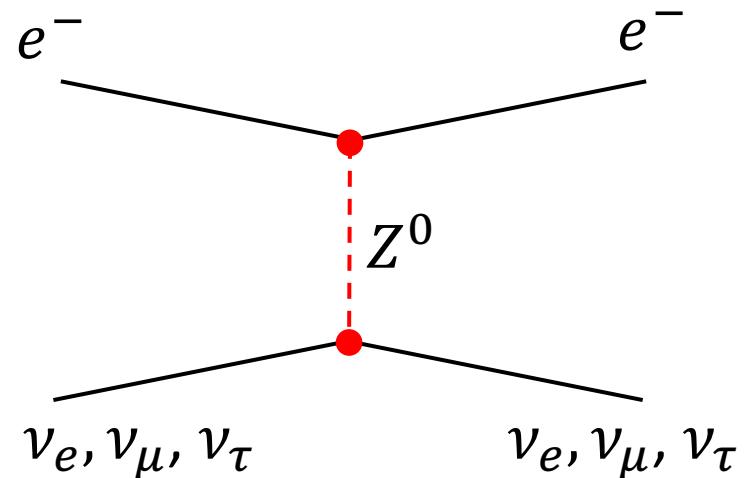
Charged-current

- Neutrino-electron scattering via the exchange of a charged current
- High-enough energy muon/tau-neutrinos would be needed to create a muon/tau



Neutral current:

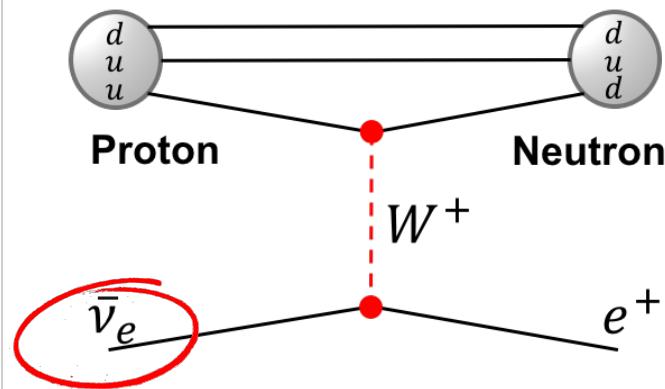
- Identical coupling of the neutral current to all flavors
- Very important for all-flavor neutrino detection



For all flavors, Charged Current interactions

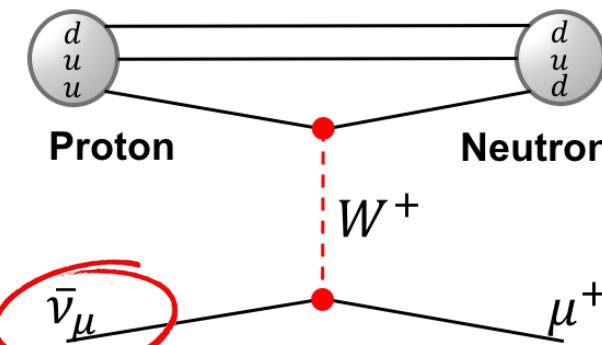
Electron ν :

... inverse beta decay (IBD)



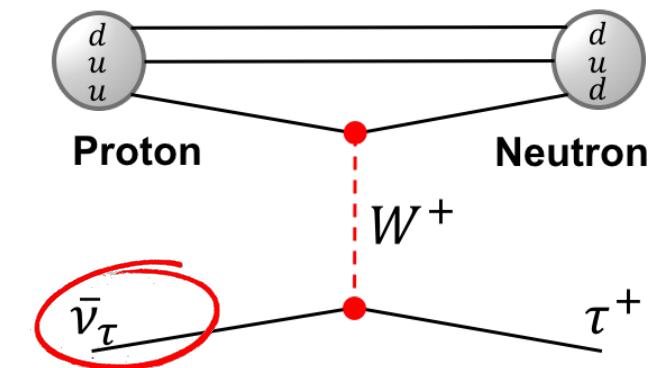
Muon ν :

... CC nuclear reaction
(dominant)

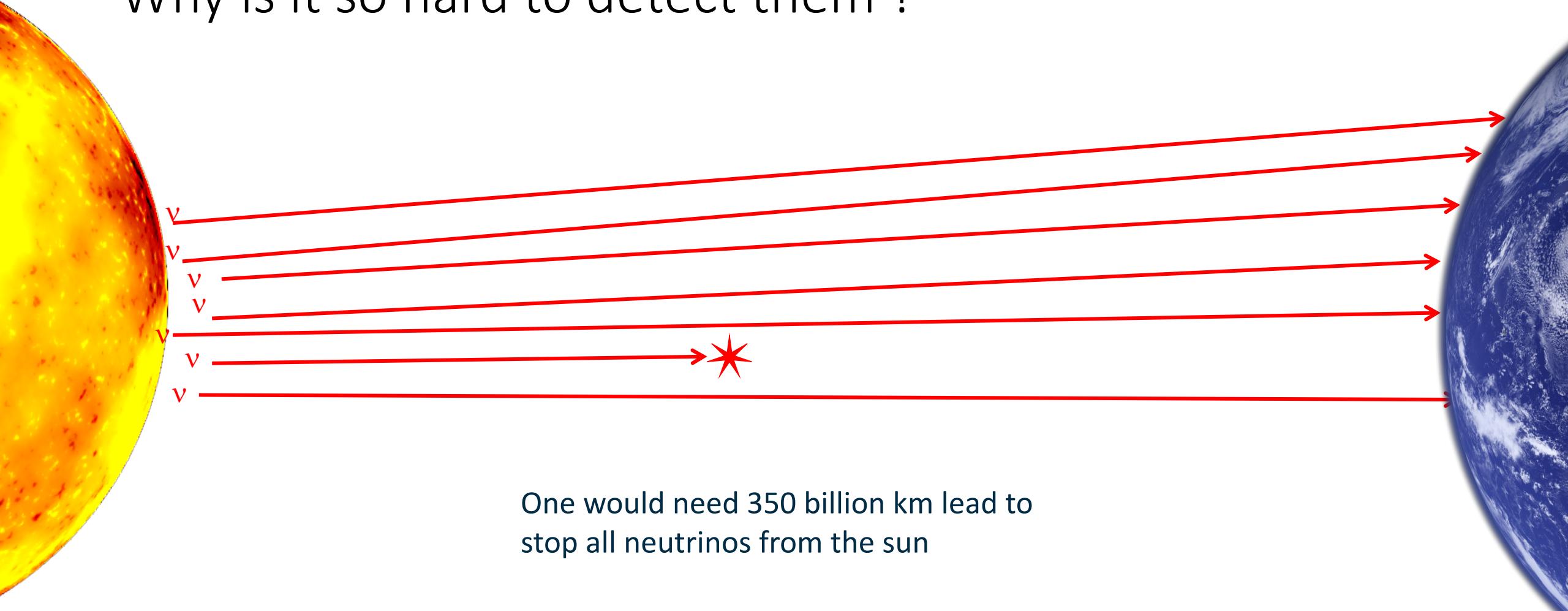


Tau ν :

... CC nuclear reaction
(dominant)



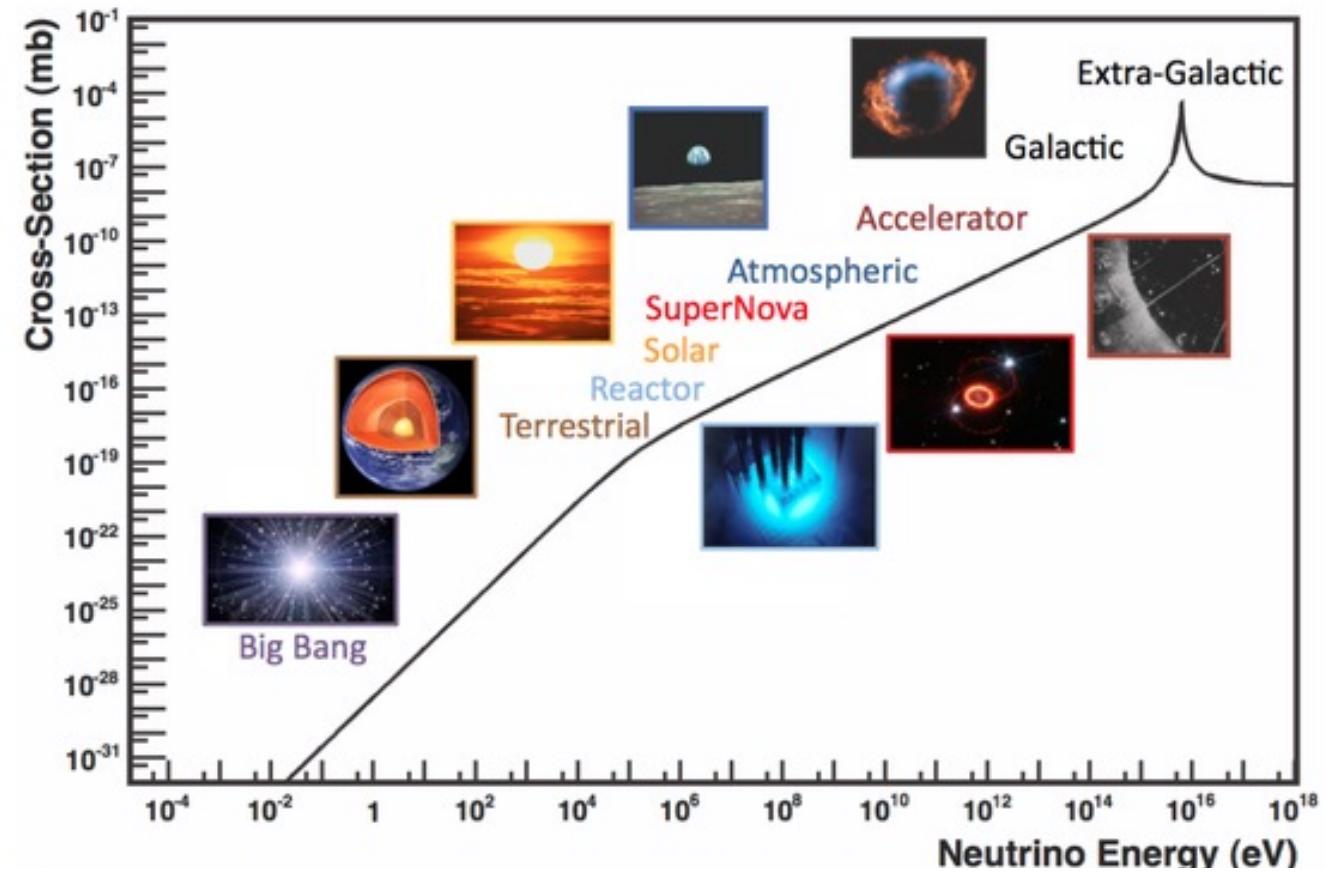
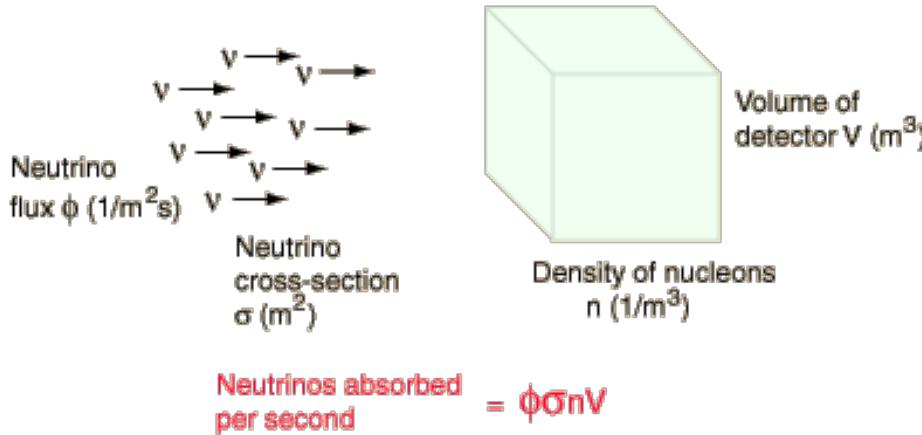
Why is it so hard to detect them ?



One would need 350 billion km lead to
stop all neutrinos from the sun

Neutrino cross section (on nucleons)

- 1 barn = 10^{-24} cm^2
- @1 MeV (solar, radioactive decay):
 $\sigma = 10^{-44} \text{ cm}^2$
- Comparison to electro-weak interaction:
 $e^+ + e^- \rightarrow \gamma \gamma$ (1 MeV): $\sigma = 10^{-25} \text{ cm}^2$



Neutrino cross section (on nucleons)

- 1 barn = 10^{-24} cm^2
- @1 GeV (accelerator, atmospheric):
 $\sigma = 10^{-38} \text{ cm}^2$
- Comparison to p-p interaction (1 GeV):
 $\sigma = 10^{-26} \text{ cm}^2$

Diagram illustrating the calculation of neutrino absorption:

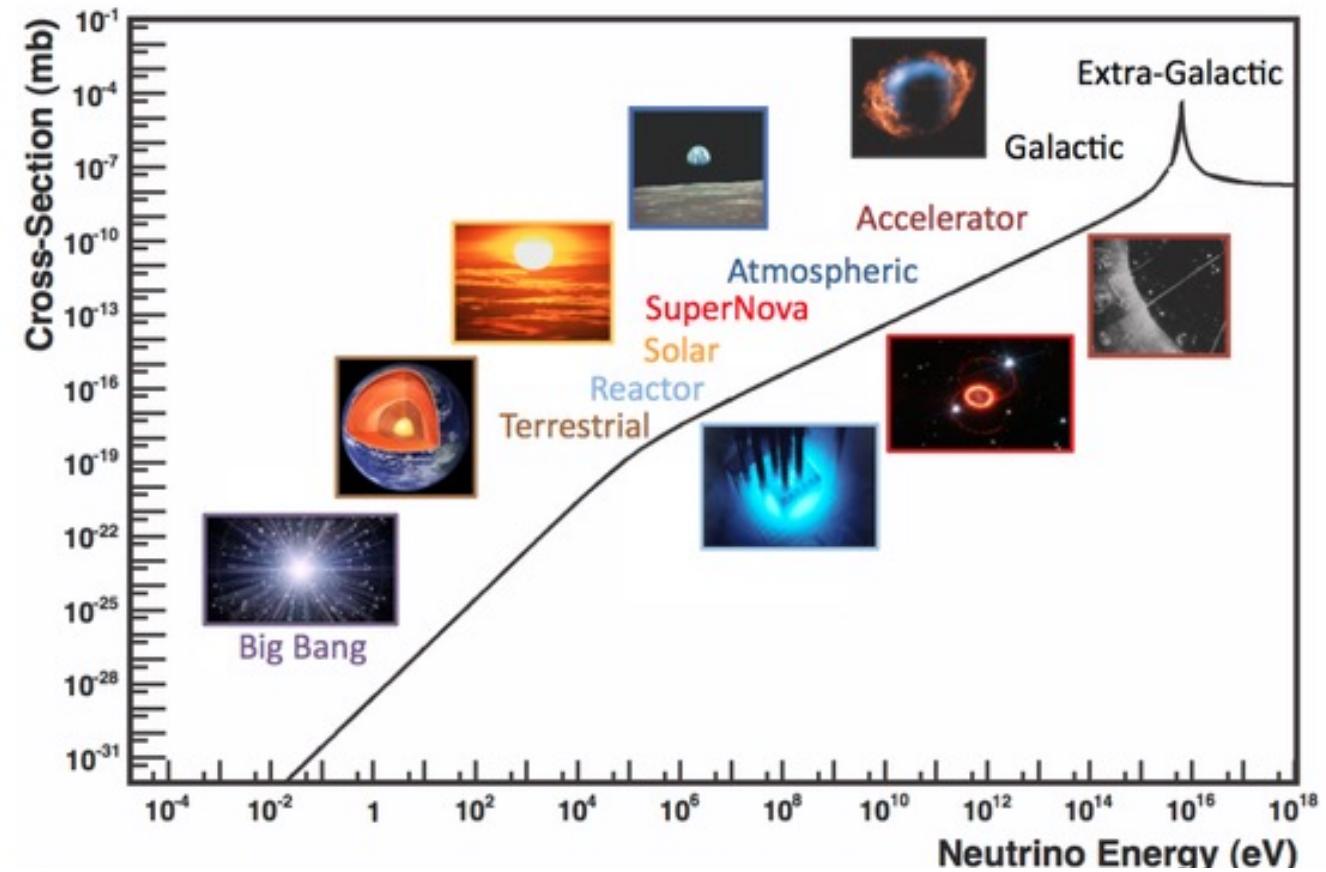
Neutrino flux ϕ ($1/\text{m}^2\text{s}$)

Neutrino cross-section σ (m^2)

Volume of detector V (m^3)

Density of nucleons n ($1/\text{m}^3$)

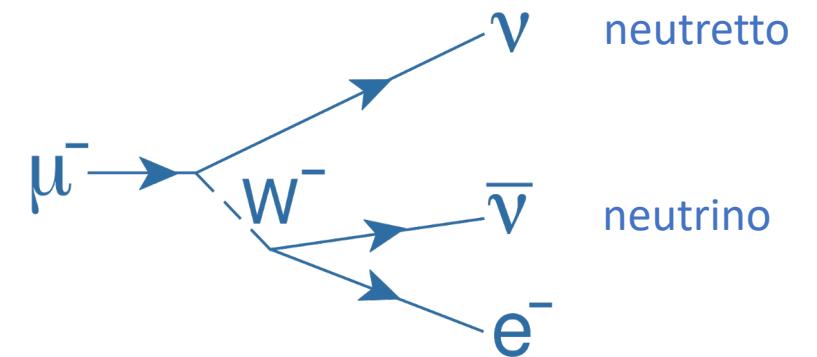
Neutrons absorbed per second = $\phi \sigma n V$



Muon neutrinos

A bit of history

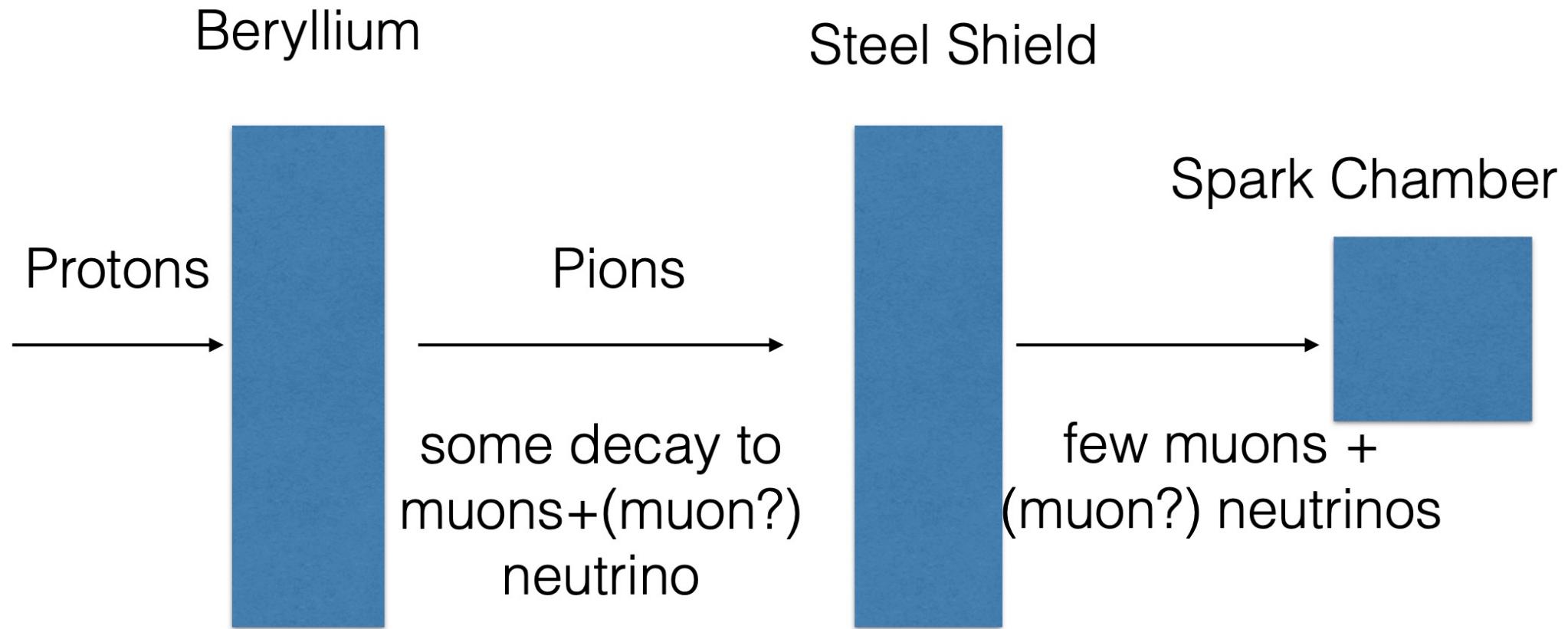
- 1930: Neutrino Predicted
- 1937: Muon Discovered
- 1941: Muon shown to decay into electron + neutrino(s)
- 1948: Energy spectrum of Muon decay shown to be continuous: there must be 2 neutrinos in the decay



Most people felt that the neutrinos should be different, and they named them : [neutrino](#) and [neutretto](#)

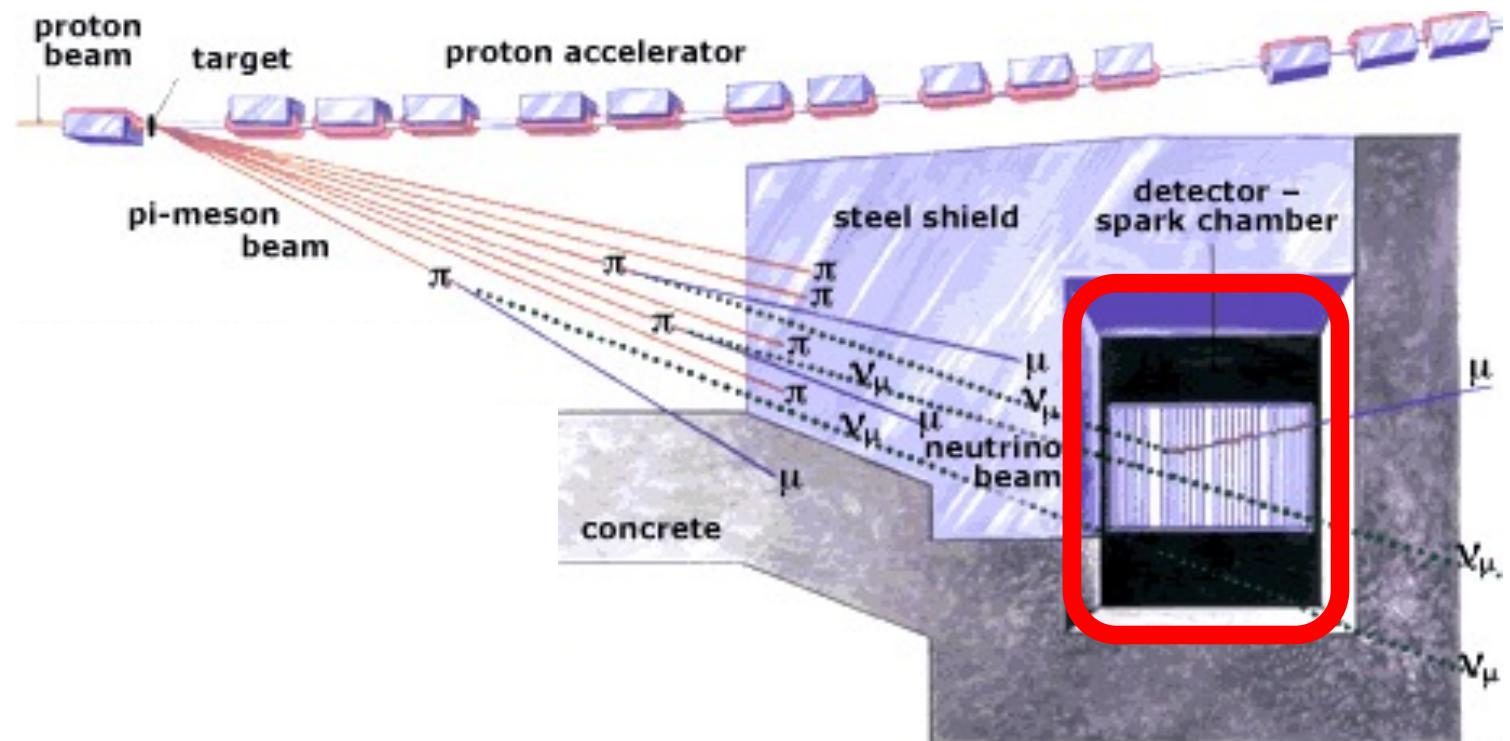
- 1955: (electron) antineutrino directly observed
- 1962: direct observation of muon neutrino

Muon neutrino discovery: experimental concept



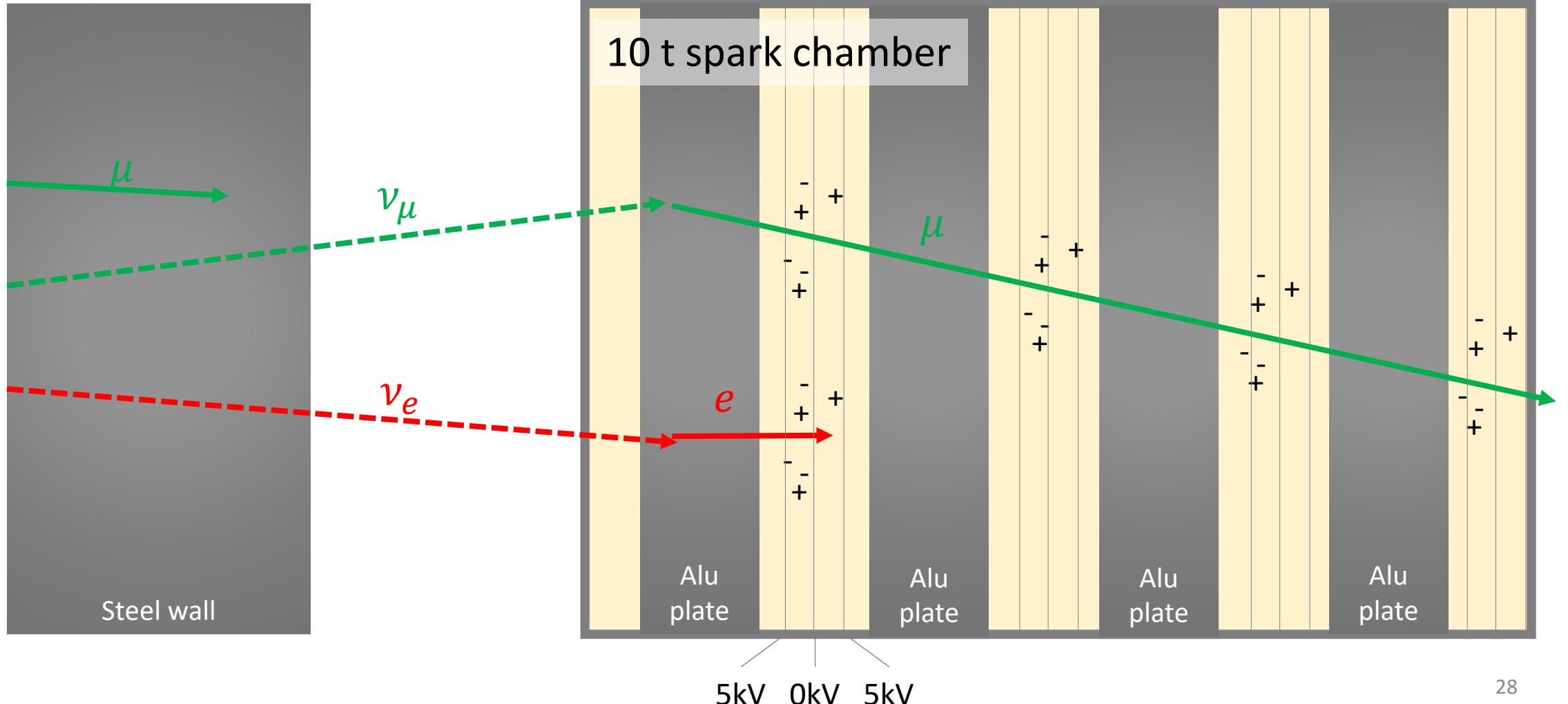
Muon neutrino discovery (ν_μ – detection)

- Brookhaven National Laboratory Alternating Gradient Synchrotron (AGS) generates protons of 15 GeV
- Proton beam hits beryllium target, producing pions
- Pions decay into muons and muon-neutrinos
- Neutrinos, Pions, muons, etc. pass through a wall of 13.5 meters thick steel: only neutrinos pass
- Neutrinos detected in 10-ton spark chamber
- Muon and electron neutrino creates different signature

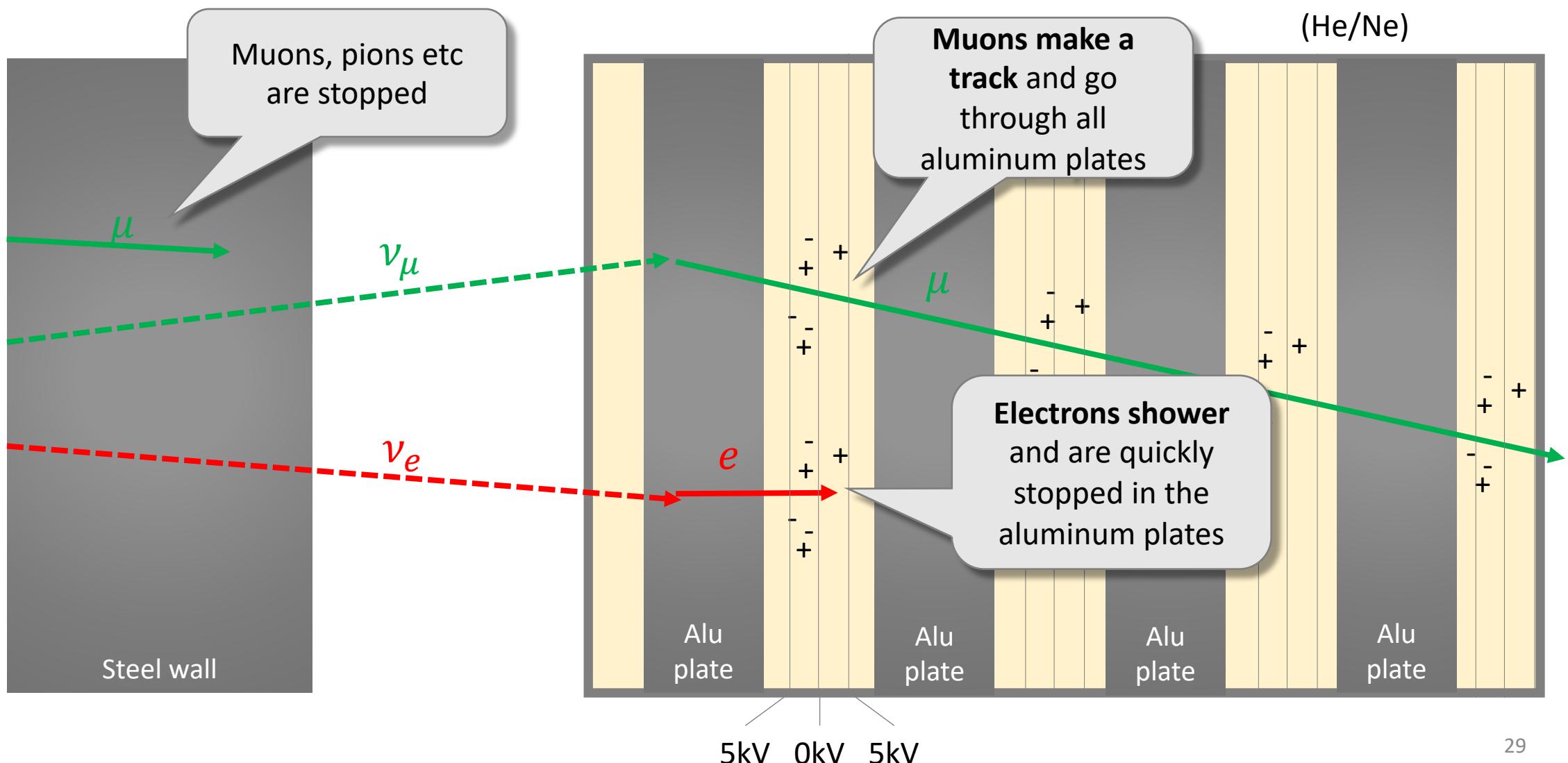


Muon neutrino discovery (ν_μ – detection)

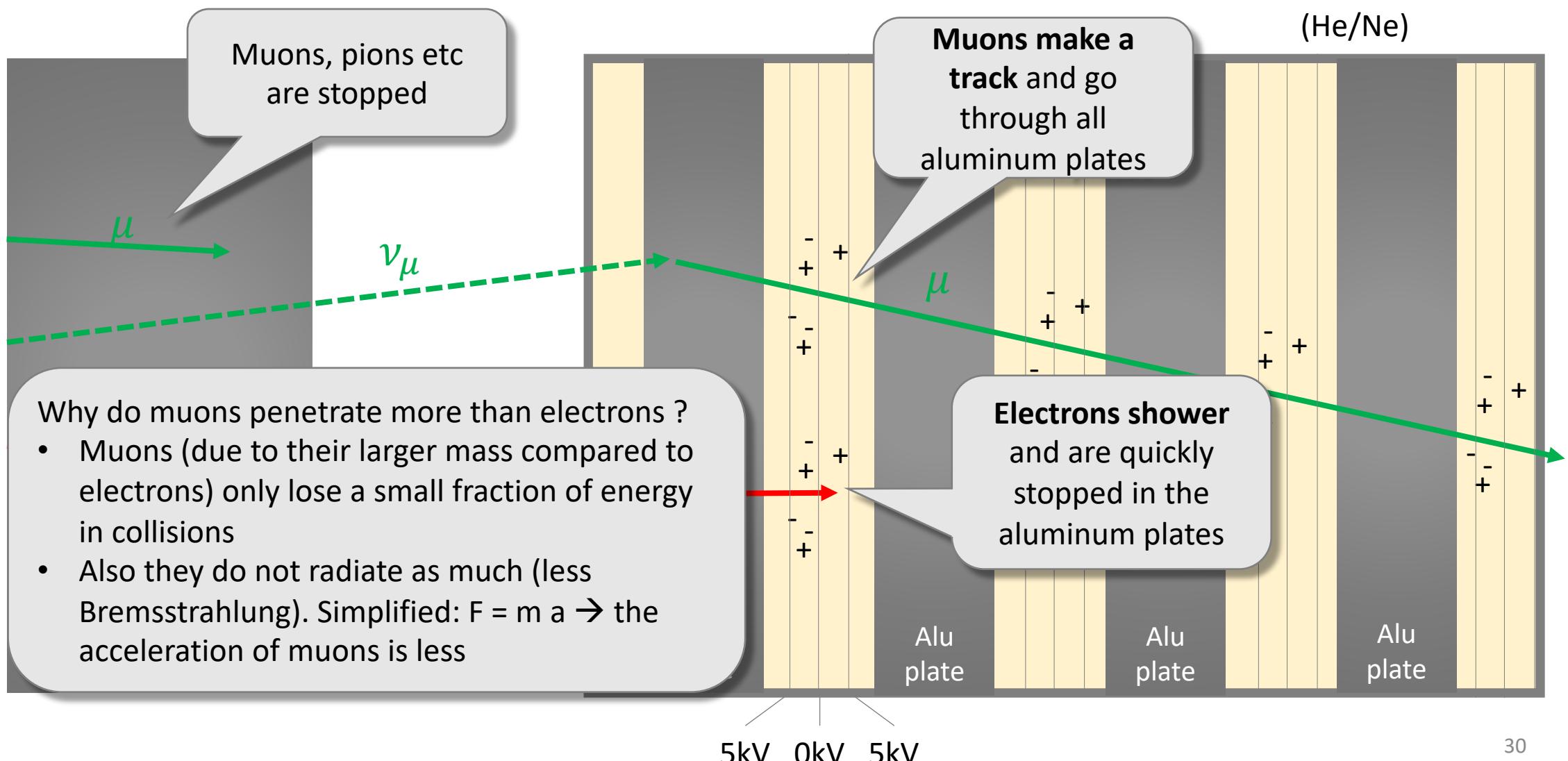
Gas enclosure
(He/Ne)



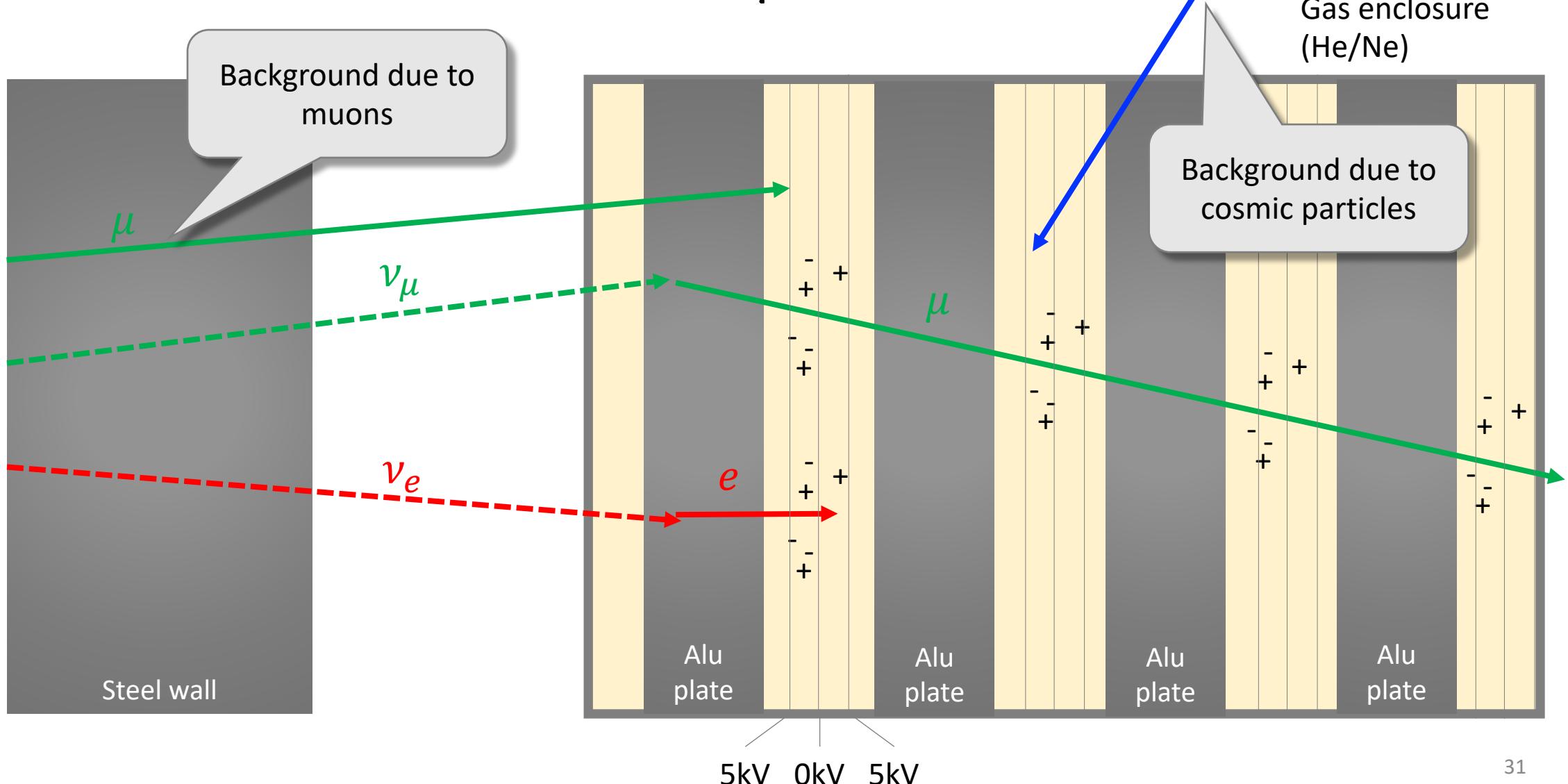
Muon neutrino discovery (ν_μ – detection)



Muon neutrino discovery (ν_μ – detection)



Muon neutrino discovery (ν_μ – detection)



Muon neutrino discovery

- DAQ = 
- Detected 113 events (with 3.48×10^{17} protons on target)
- Of these, 34 were single muon events
- Only 6 electron neutrinos (showers) observed
- If there was no difference between muon neutrinos and electron neutrinos, we would expect a similar number of electron showers

FIG. 8. 400-MeV electrons from the Cosmotron.

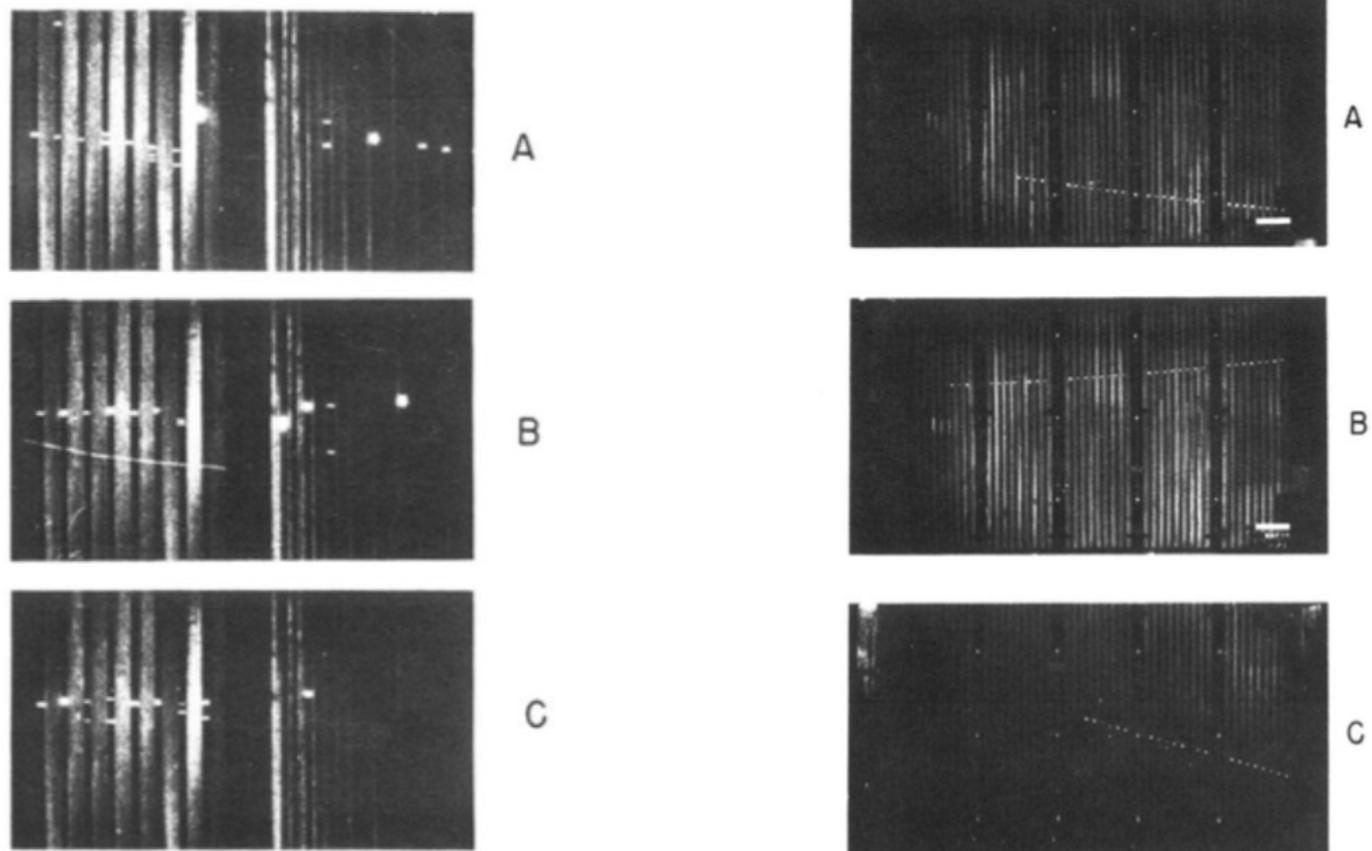


FIG. 5. Single muon events. (A) $p_\mu > 540$ MeV and δ ray indicating direction of motion (neutrino beam incident from left); (B) $p_\mu > 700$ MeV/c; (C) $p_\mu > 440$ with δ ray.

Muon neutrino discovery



The Nobel Prize in Physics 1988: Leon M. Lederman, Melvin Schwartz and Jack Steinberger *"for the neutrino beam method and the demonstration of the doublet structure of the leptons through the discovery of the muon neutrino"*.



Jakob Steinberger,
Born 1921

Melvin Schwartz,
1921 - 2006

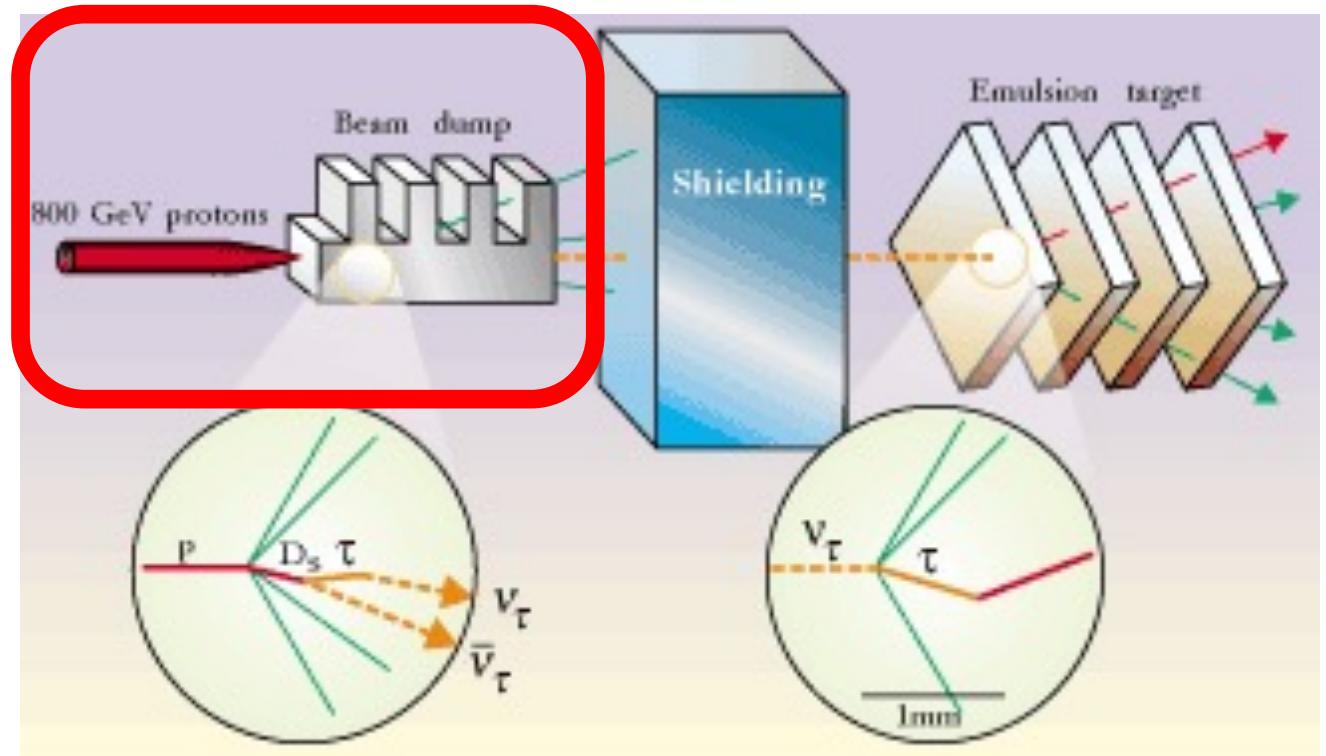
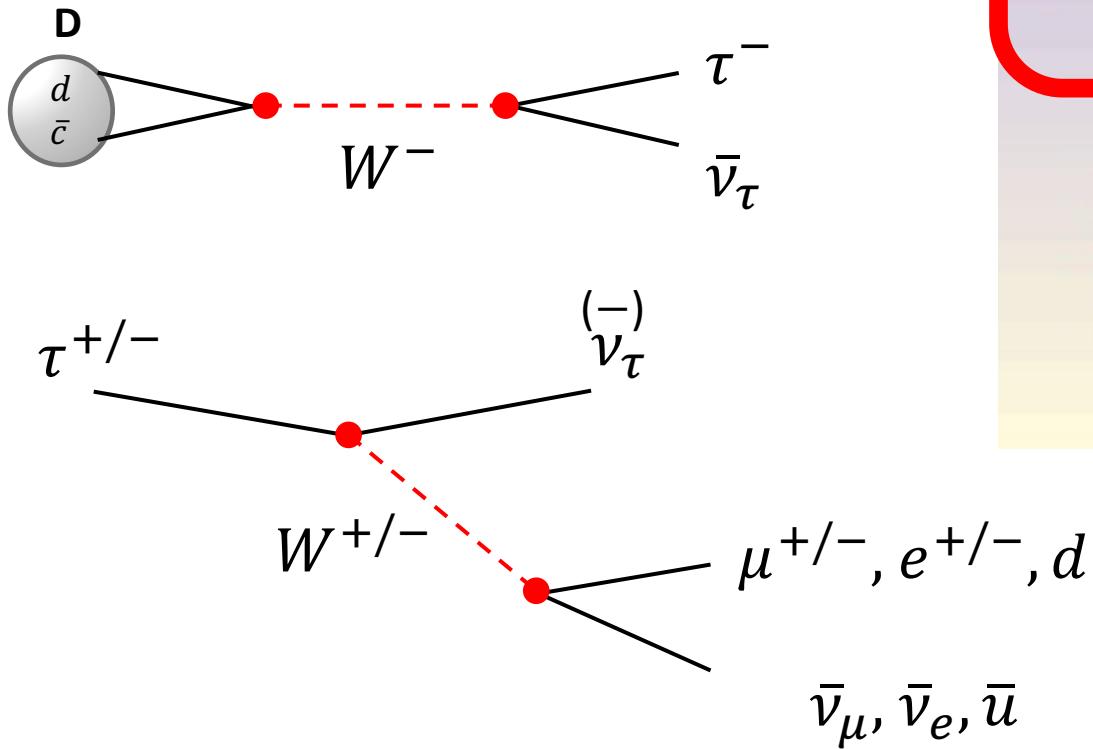


Leon M. Lederman,
Born 1922

Tau neutrinos

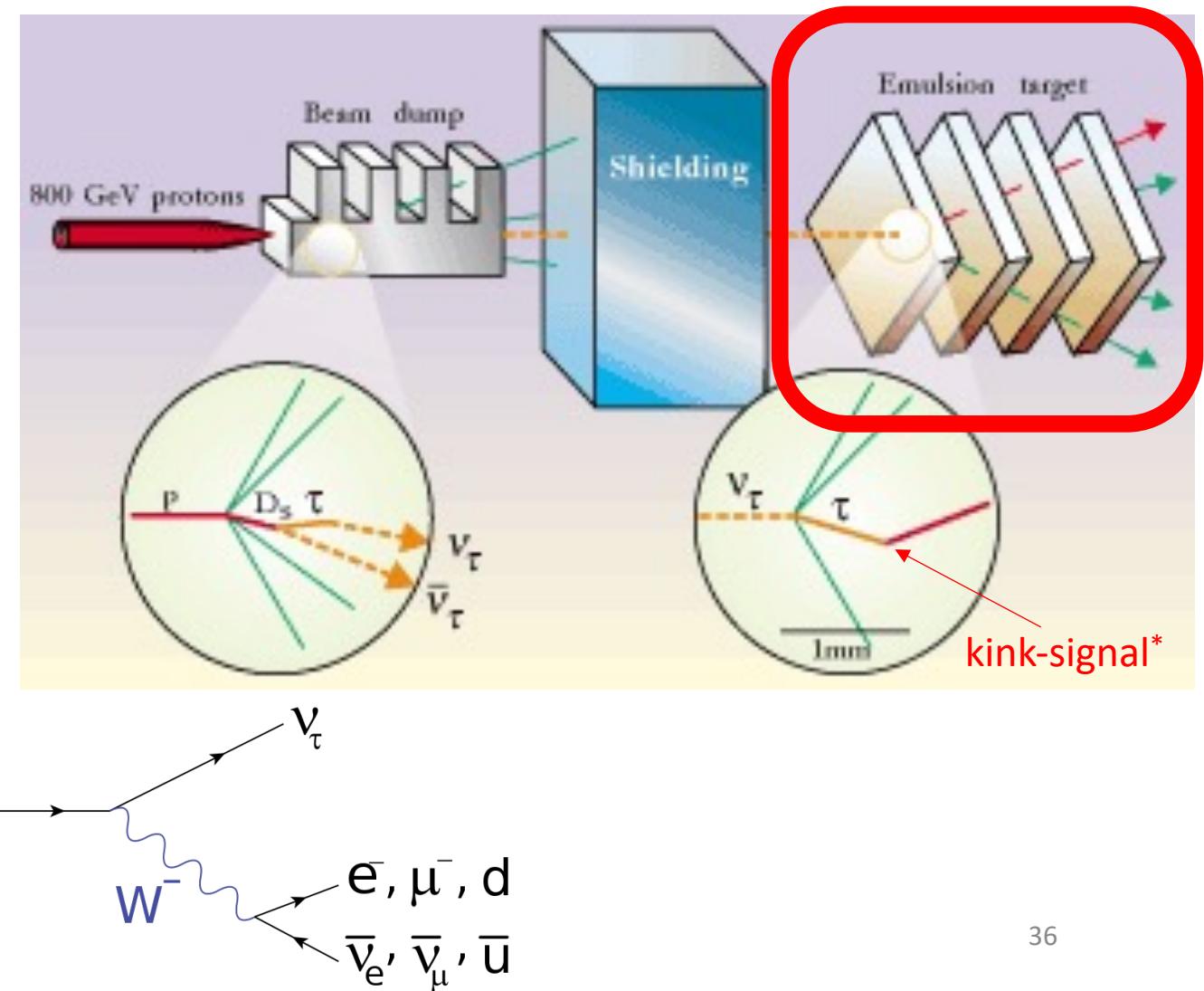
Tau neutrino discovery

- Protons accelerated by the Tevatron (Fermilab) produce tau neutrinos via decay of charmed mesons

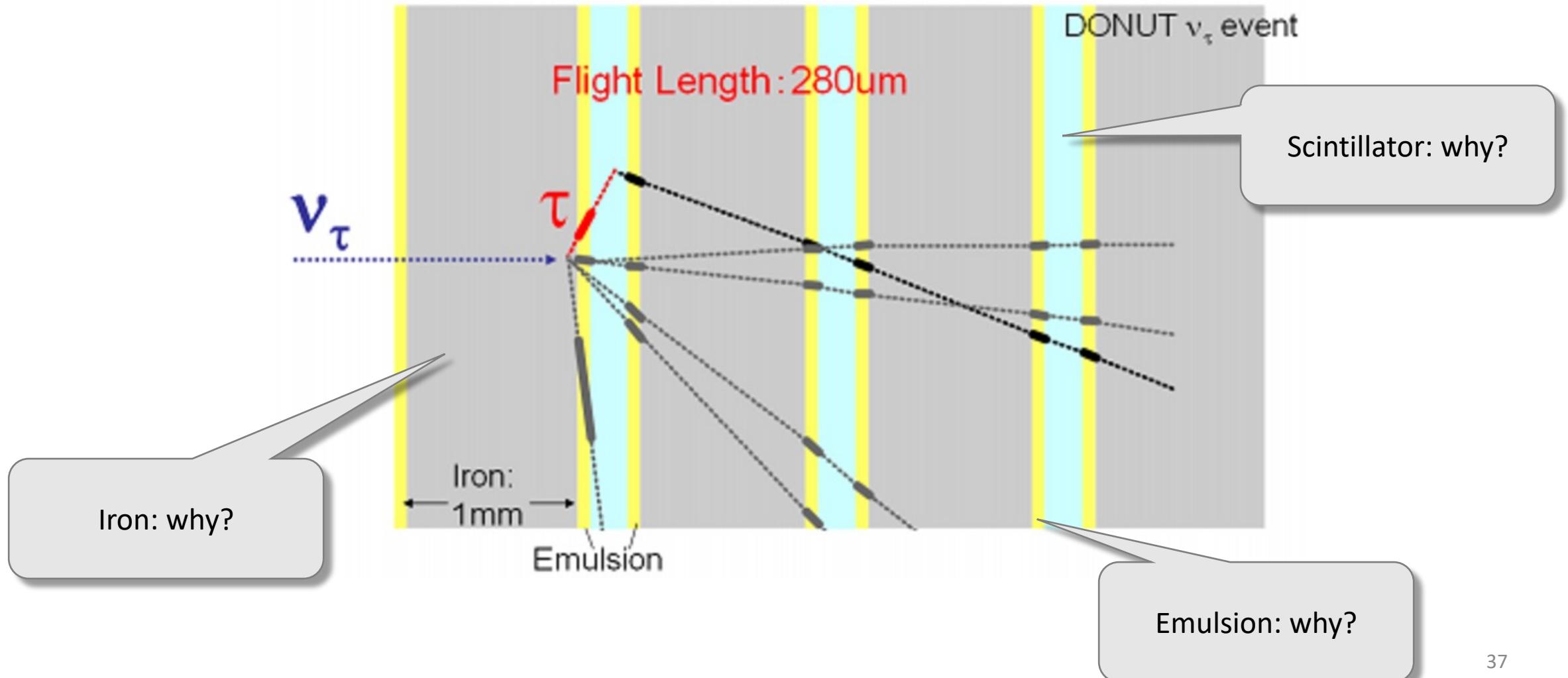


Tau neutrino discovery

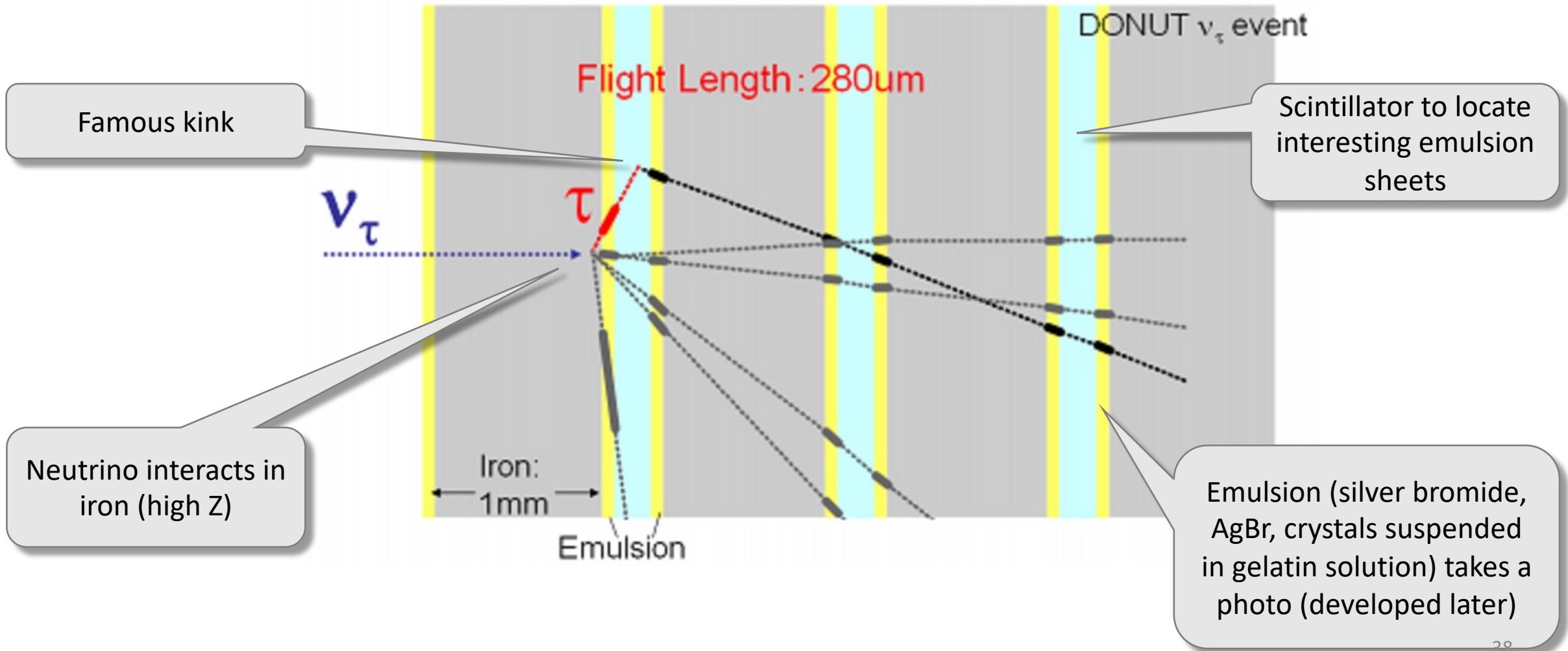
- Protons accelerated by the Tevatron produce tau neutrinos via decay of charmed mesons
 - Shielding and magnetic deflection stops/removes all particles but the neutrinos
 - Tau neutrino interacts in steel target and produces a tau
 - Tau travels for 1mm, leaves a track in the emulsion, then decays into a neutrino and charged particles
 - Charged particles leave a track in the emulsion
- Famous kink-signal*



Tau neutrino discovery

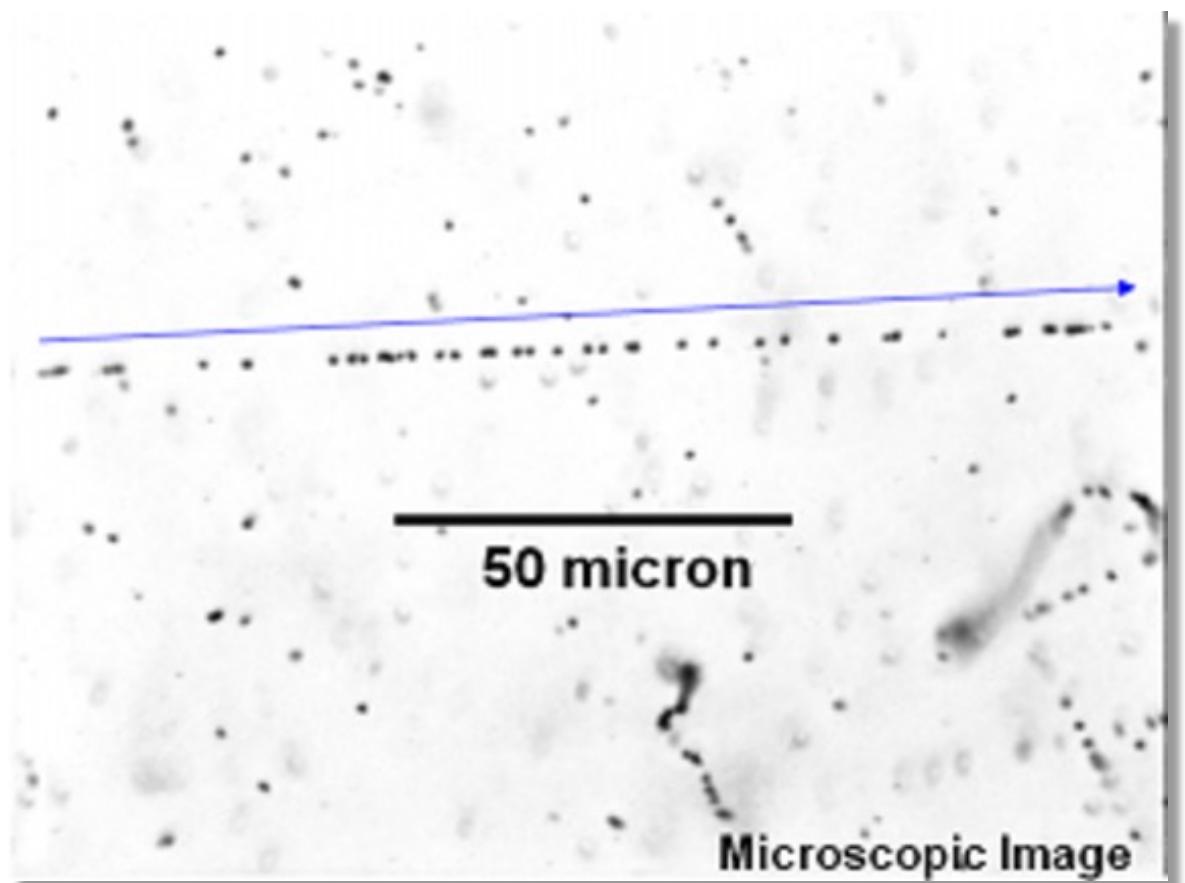


Tau neutrino discovery



Tau neutrino discovery

- The DONUT (Direct Observation of the Nu Tau) experiment recorded a total of six million potential interactions.
- Four events provided evidence for the tau neutrino in 2000
- Last particle to be discovered before the Higgs boson in 2012



Discovery of the neutrinos (Overview)

	Electron ν	Muon ν	Tau ν
Source	Reactor: Electron Anti-neutrinos	Accelerator: Pions \rightarrow Muon neutrinos	Accelerator: Charmed mesons \rightarrow tau neutrinos
Detector	Water with Cadmium + Scintillator	Aluminum Plates + Spark Chamber	Lead + Scintillator + Emulsion sheet layers
Signature	Coincidence signal	Long tracks	Kink
Location	Hanford reactor site, USA	Brookhaven, USA	Tevatron @ Fermilab, USA
People/Group	Reines, Cowan	Ledermann, Schwartz, Steinberger	DONUT Collaboration
Year	1957 	1962 	2000

Neutrino Oscillation

Neutrino Flavours und Masses

Key ingredient 1:

- A neutrino with a specific **mass** has no specific **flavor**
- A neutrino with a specific **flavor** has no specific **mass**

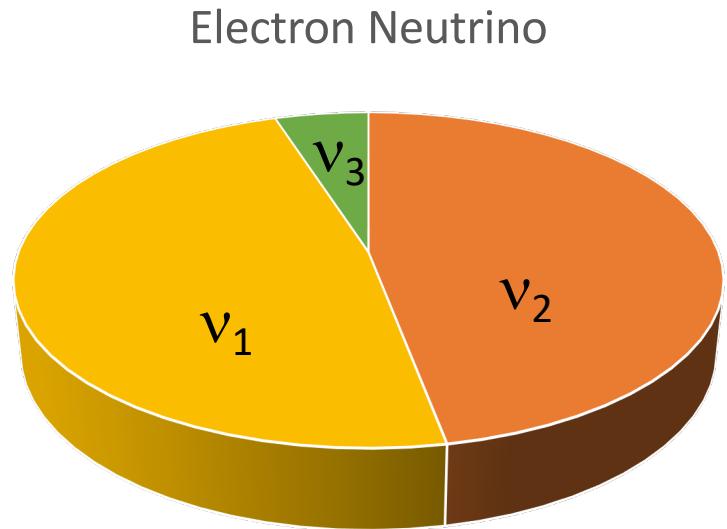
Key ingredient 2:

- Neutrino is born in a flavor eigenstate, but propagates as mass eigenstate
- Neutrino mass eigenstates evolve differently with time

$$e^{-i\hat{H}t/\hbar} |\nu_e\rangle = U_{e1} \cdot e^{-iE_1 t/\hbar} |\nu_1\rangle + U_{e2} \cdot e^{-iE_2 t/\hbar} |\nu_2\rangle + U_{e3} \cdot e^{-iE_3 t/\hbar} |\nu_3\rangle$$

Flavor	Mass
Electron Neutrino	 m_1 Neutrino1
Muon Neutrino	 m_2 Neutrino2
Tau Neutrino	 m_3 Neutrino3

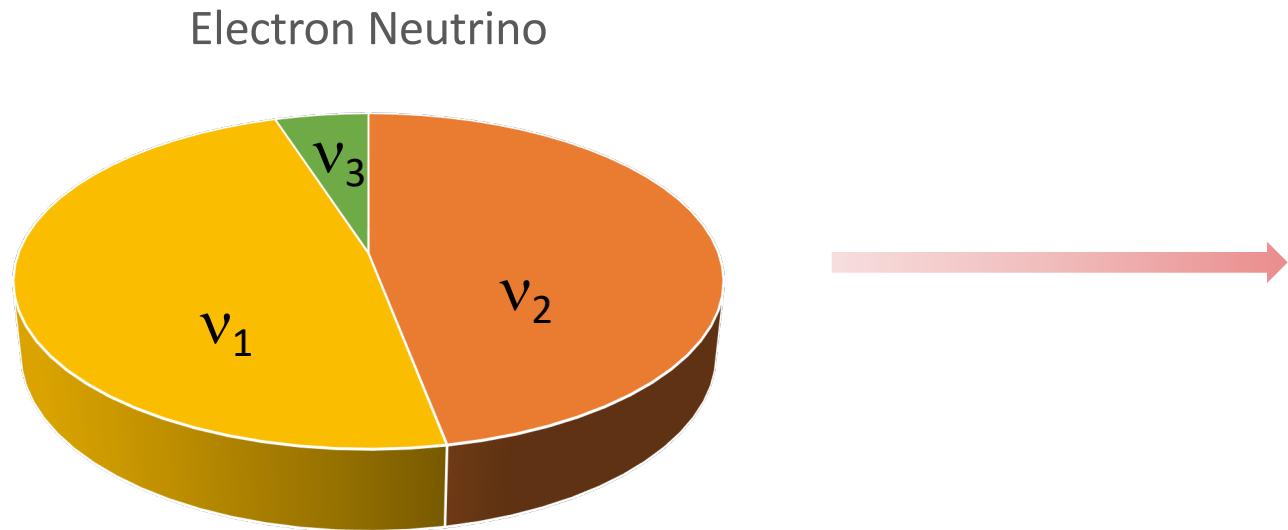
Neutrino Oscillations



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

t=0 $|\nu_e\rangle = U_{e1} \cdot |\nu_1\rangle + U_{e2} \cdot |\nu_2\rangle + U_{e3} \cdot |\nu_3\rangle$

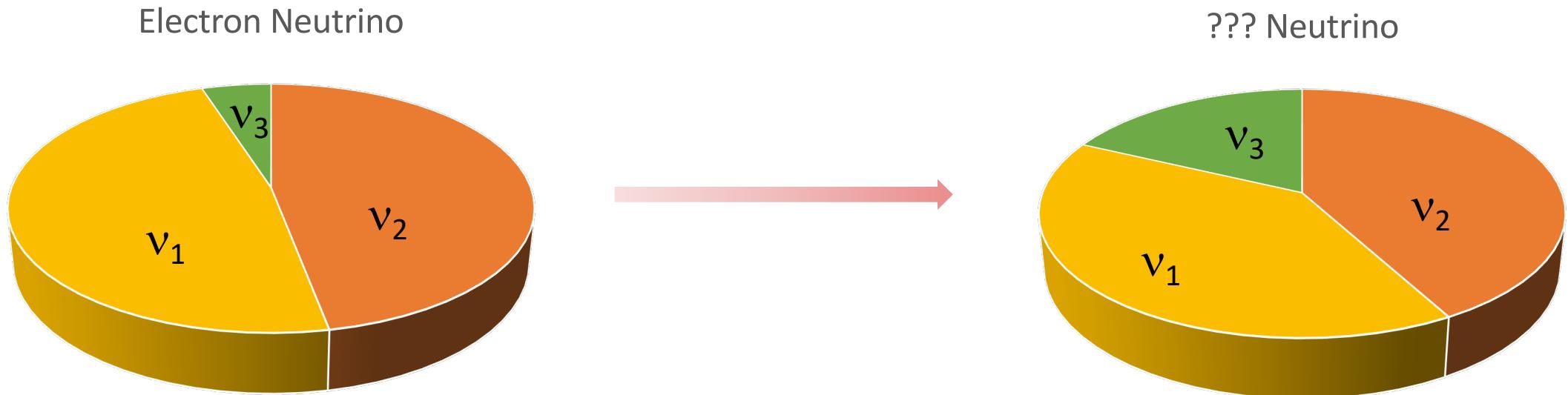
Neutrino Oscillations



t=0 $|\nu_e\rangle = U_{e1} \cdot |\nu_1\rangle + U_{e2} \cdot |\nu_2\rangle + U_{e3} \cdot |\nu_3\rangle$

t>0 $e^{-i\hat{H}t/\hbar} |\nu_e\rangle = U_{e1} \cdot e^{-i\hat{H}t/\hbar} |\nu_1\rangle + U_{e2} \cdot e^{-i\hat{H}t/\hbar} |\nu_2\rangle + U_{e3} \cdot e^{-i\hat{H}t/\hbar} |\nu_3\rangle$

Neutrino Oscillations



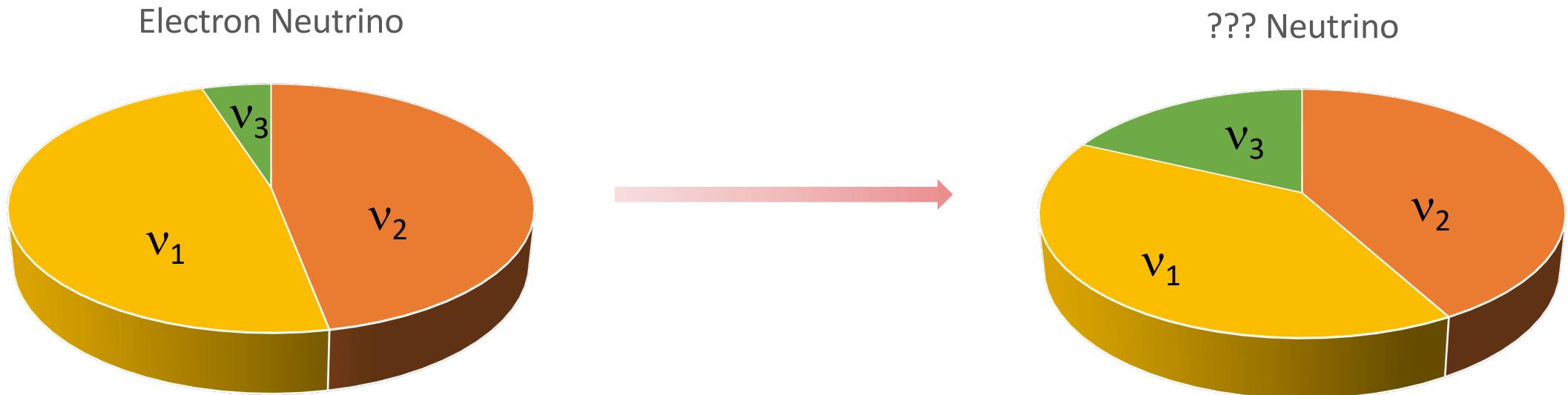
$$t=0 \quad |\nu_e\rangle = U_{e1} \cdot |\nu_1\rangle + U_{e2} \cdot |\nu_2\rangle + U_{e3} \cdot |\nu_3\rangle$$

$$t>0 \quad e^{-i\hat{H}t/\hbar}|\nu_e\rangle = U_{e1} \cdot e^{-i\hat{H}t/\hbar}|\nu_1\rangle + U_{e2} \cdot e^{-i\hat{H}t/\hbar}|\nu_2\rangle + U_{e3} \cdot e^{-i\hat{H}t/\hbar}|\nu_3\rangle$$

$$e^{-i\hat{H}t/\hbar}|\nu_e\rangle = U_{e1} \cdot e^{-iE_1 t/\hbar}|\nu_1\rangle + U_{e2} \cdot e^{-iE_2 t/\hbar}|\nu_2\rangle + U_{e3} \cdot e^{-iE_3 t/\hbar}|\nu_3\rangle$$

The three mass eigenstates evolve differently in time

Neutrino Oscillations



$$t=0 \quad |\nu_e\rangle = U_{e1} \cdot |\nu_1\rangle + U_{e2} \cdot |\nu_2\rangle + U_{e3} \cdot |\nu_3\rangle$$

$$t>0 \quad e^{-i\hat{H}t/\hbar} |\nu_e\rangle = U_{e1} \cdot e^{-i\hat{H}t/\hbar} |\nu_1\rangle + U_{e2} \cdot e^{-i\hat{H}t/\hbar} |\nu_2\rangle + U_{e3} \cdot e^{-i\hat{H}t/\hbar} |\nu_3\rangle$$

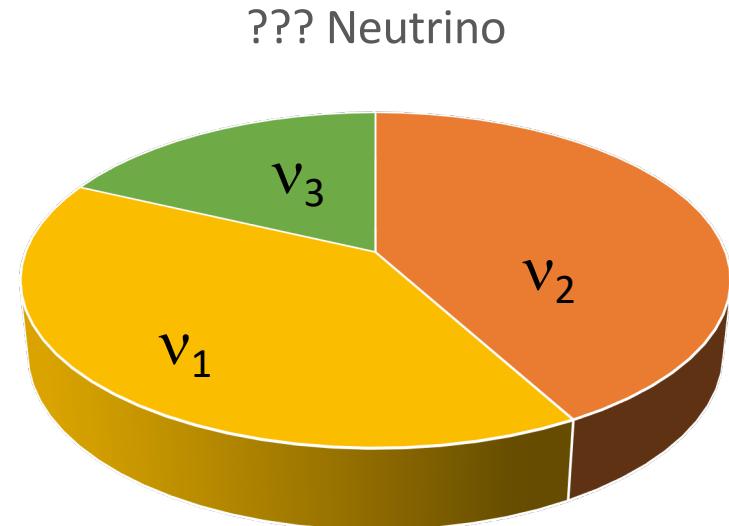
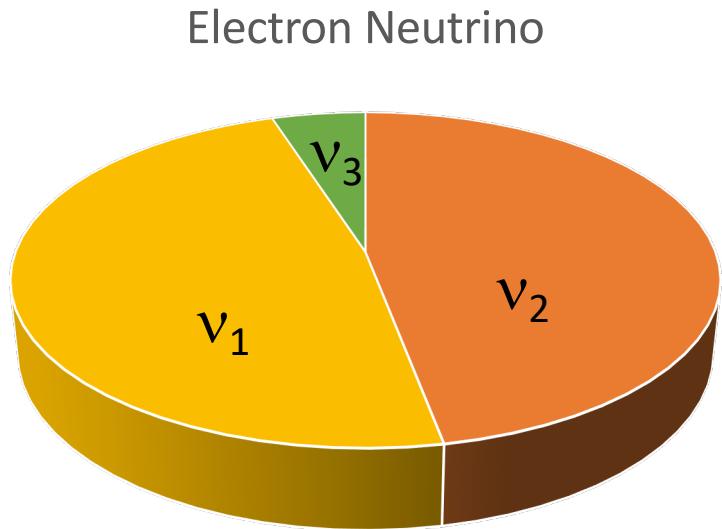
$$|\nu_x\rangle = U_{e1} \cdot e^{-iE_1 t/\hbar} |\nu_1\rangle + U_{e2} \cdot e^{-iE_2 t/\hbar} |\nu_2\rangle + U_{e3} \cdot e^{-iE_3 t/\hbar} |\nu_3\rangle$$

The neutrino is no longer a pure electron neutrino

Neutrino Oscillations

Projection onto the electron flavor gives us the probability to detect an electron neutrino

$$P = |\langle \nu_e | \nu_x \rangle|^2$$



$t=0$ $|\nu_e\rangle = U_{e1} \cdot |\nu_1\rangle + U_{e2} \cdot |\nu_2\rangle + U_{e3} \cdot |\nu_3\rangle$

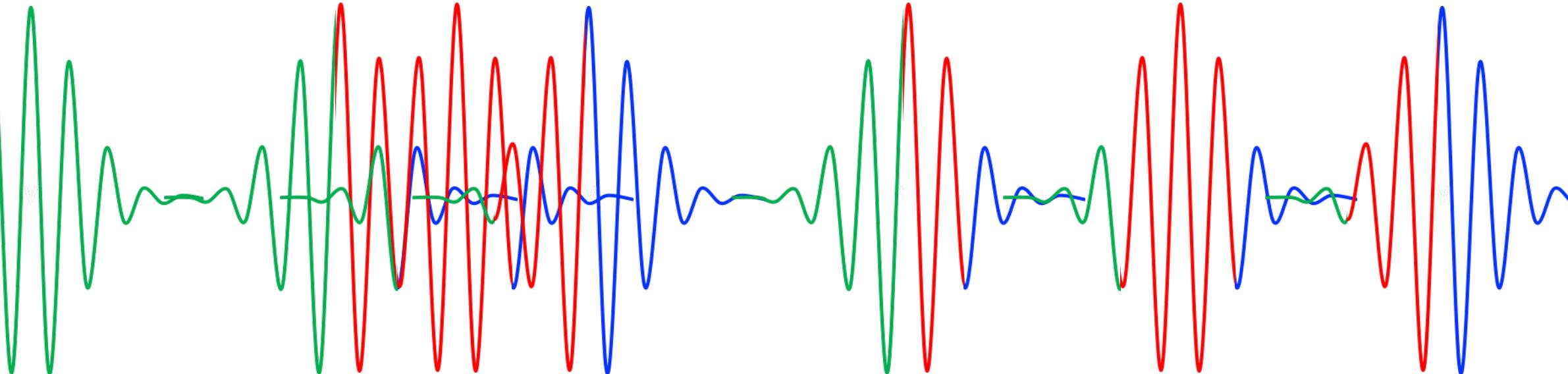
$t>0$ $e^{-i\hat{H}t/\hbar} |\nu_e\rangle = U_{e1} \cdot e^{-i\hat{H}t/\hbar} |\nu_1\rangle + U_{e2} \cdot e^{-i\hat{H}t/\hbar} |\nu_2\rangle + U_{e3} \cdot e^{-i\hat{H}t/\hbar} |\nu_3\rangle$

$$|\nu_x\rangle = U_{e1} \cdot e^{-iE_1 t/\hbar} |\nu_1\rangle + U_{e2} \cdot e^{-iE_2 t/\hbar} |\nu_2\rangle + U_{e3} \cdot e^{-iE_3 t/\hbar} |\nu_3\rangle$$

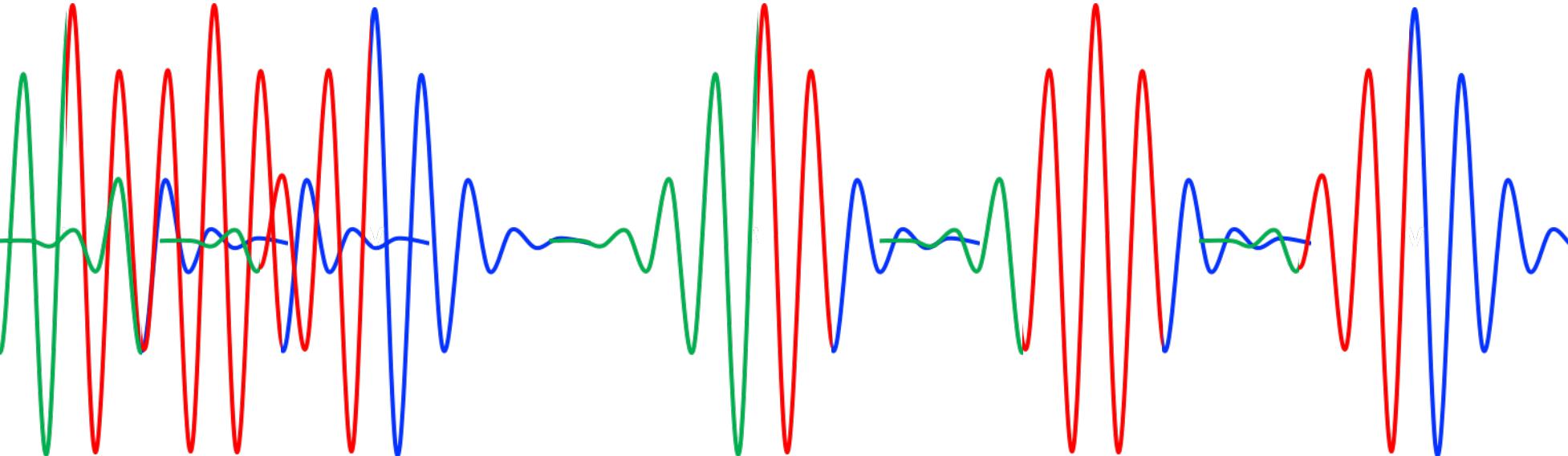
The neutrino is no longer a pure electron neutrino

Another view...

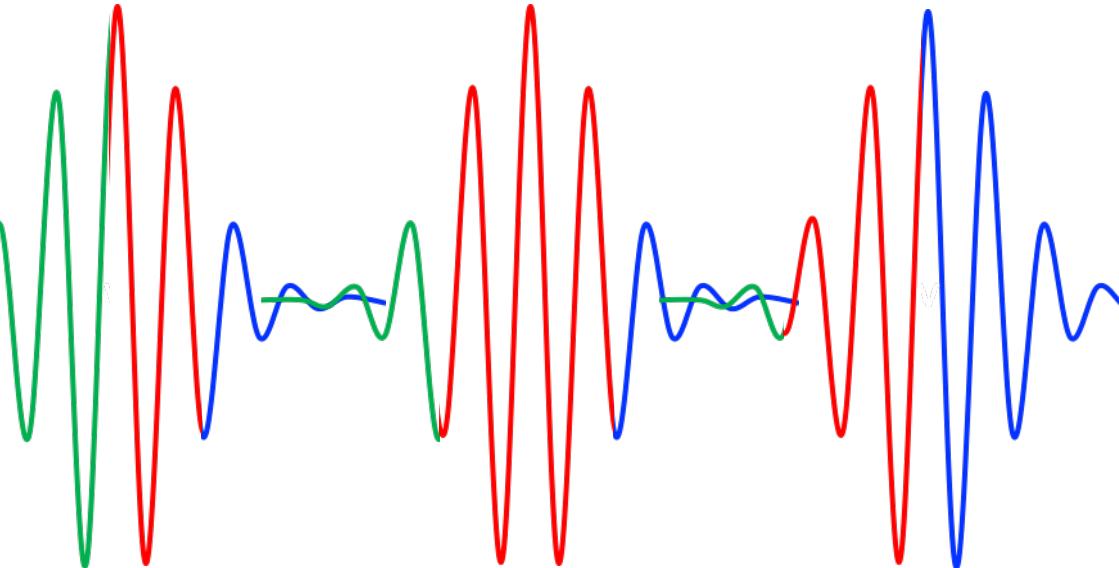
Production



Interference → oscillations



Dehoherence

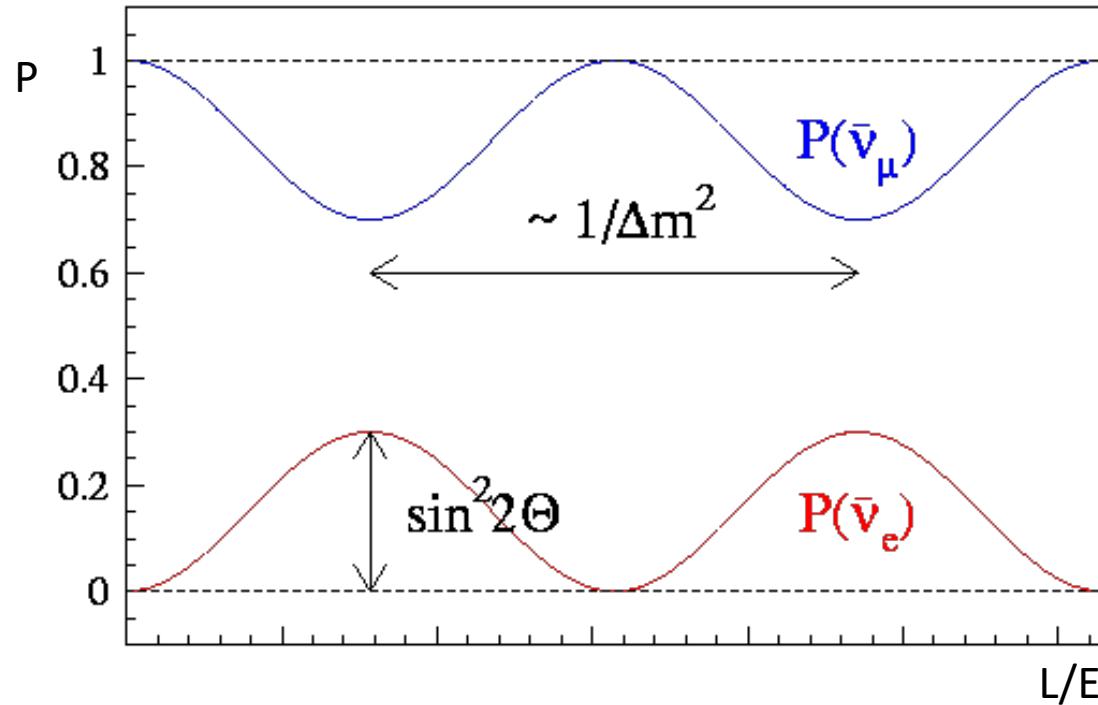


Neutrino produced as flavor eigenstate

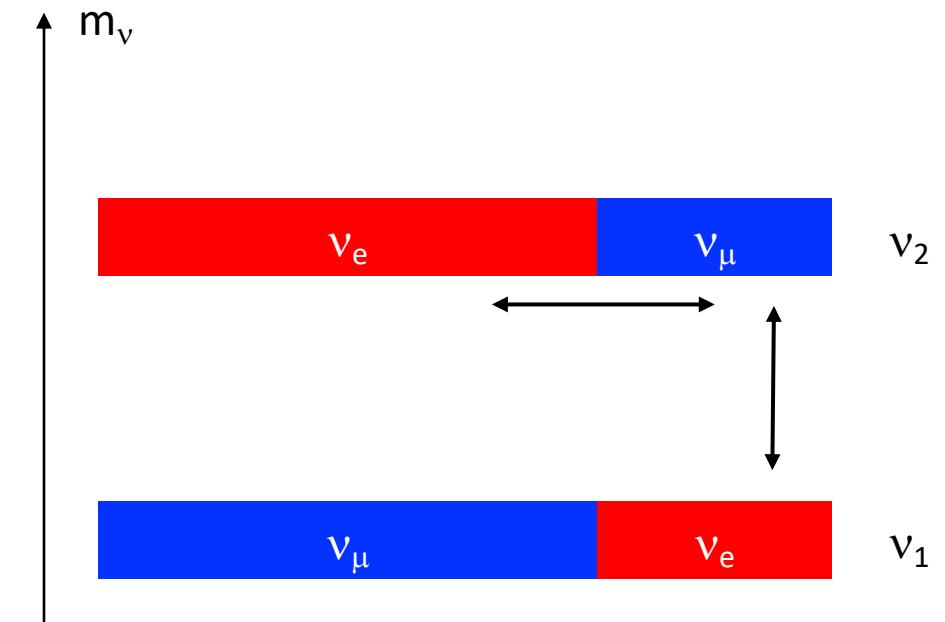
Neutrino mass eigenstates propagate. Interference pattern determines probability to detect a specific neutrino flavor

Neutrino mass eigenstates are well separated. No more neutrino oscillations

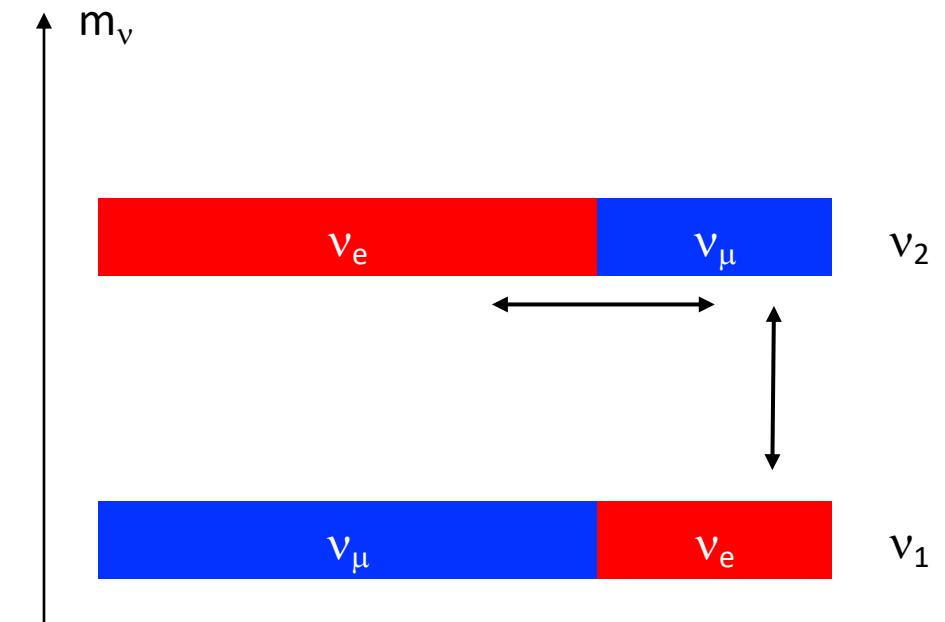
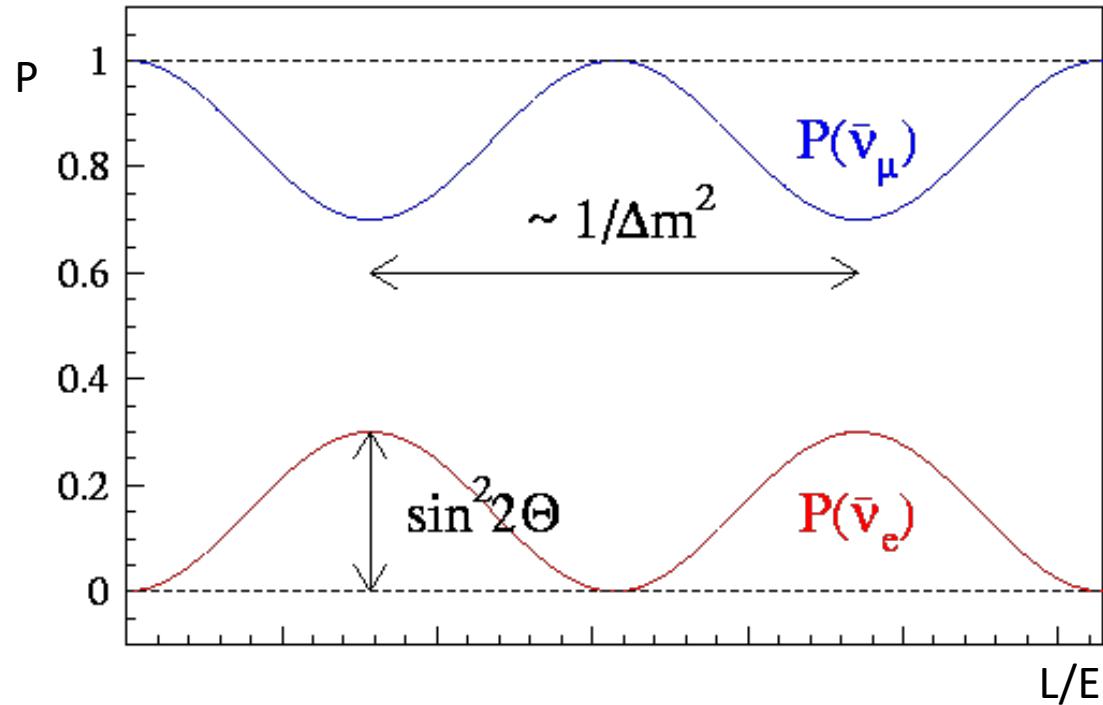
Neutrino Oscillations (for 2 Flavour)



$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \cdot \sin^2(\Delta m^2 \cdot L_\nu / E_\nu)$$



Neutrino Oscillations (for 2 Flavour)

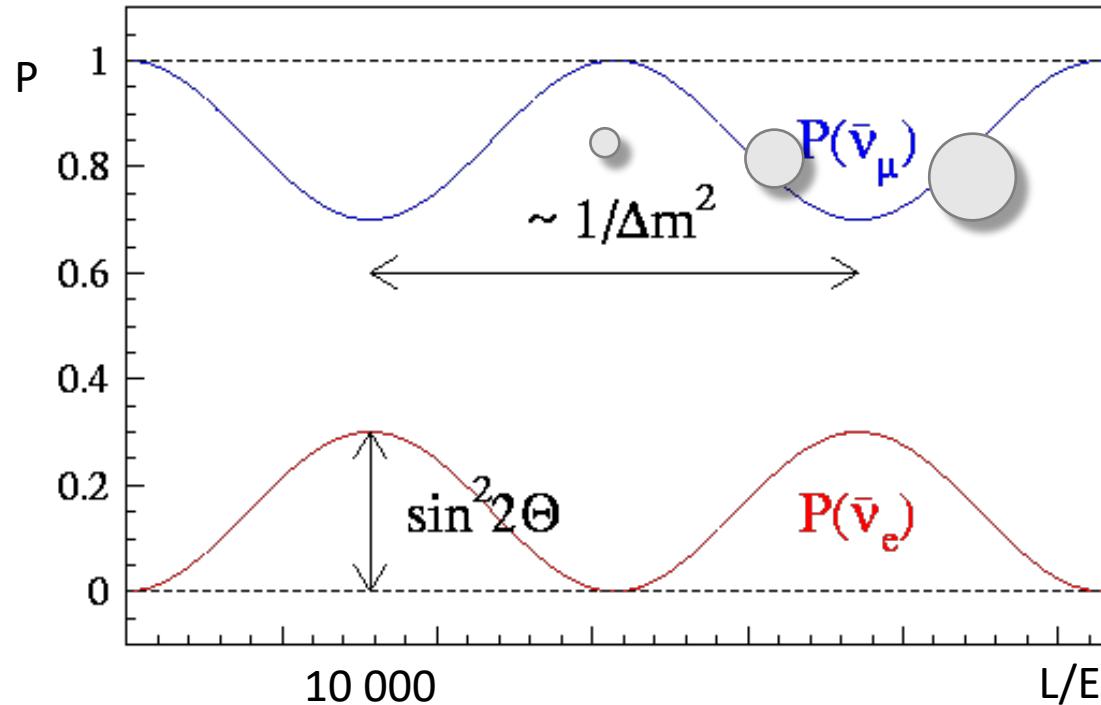


$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \sin^2 (\Delta m^2 \cdot L_\nu / E_\nu)$$

Amplitude Frequency

$$\Delta m^2 = m_1^2 - m_2^2$$

Neutrino Oscillations (for 2 Flavour)



In numbers (example):

For $\Delta m^2 = 10^{-4} \text{ eV}^2$:
 $1.27 \times 10^{-4} \times 10\,000 \approx \pi/2$
 $\rightarrow L/E \sim 10\,000 \text{ m/MeV}$

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \sin^2(\Delta m^2 \cdot L_\nu / E_\nu)$$

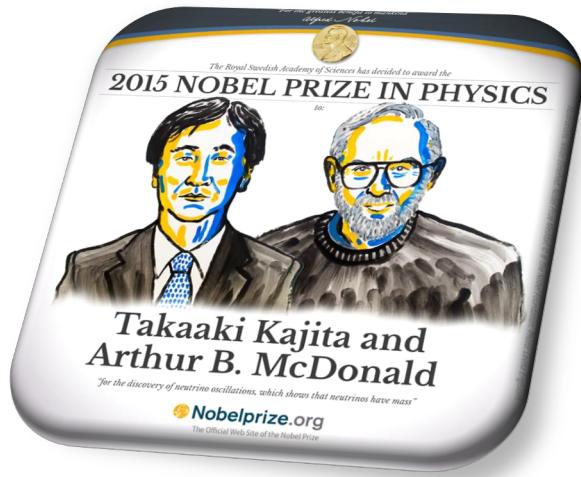
Amplitude Frequency

$$= \sin^2 2\theta \sin^2(1.27 \Delta m^2 L_\nu(\text{km}) / E_\nu(\text{GeV}))$$

Nobel Prize in Physics 2015



*Takaaki Kajita and Arthur B. McDonald:
“for the discovery of neutrino
oscillations, which shows that neutrinos
have mass”*

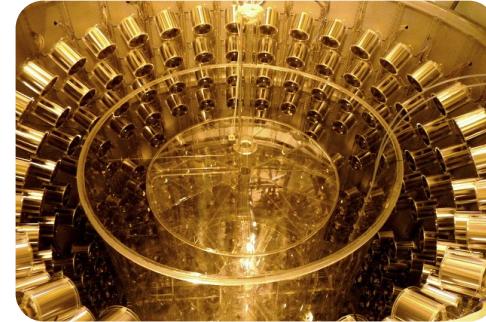


3-Flavour mixing, historically referred as:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{atmospheric mixing (45°)}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{\text{reactor mixing (small } \theta_{13} \approx 9^\circ \text{)}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{solar mixing (34°)}} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



e.g. Super Kamiokande



e.g. Double Chooz



e.g. SNO

3v Oscillation Formalism

$$U = \begin{matrix} \text{Atmospheric} \\ \left[\begin{array}{ccc} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{array} \right] \times \begin{matrix} \text{Cross-Mixing} \\ \left[\begin{array}{ccc} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{array} \right] \times \begin{matrix} \text{Solar} \\ \left[\begin{array}{ccc} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{array} \right] \times \begin{matrix} \text{Majorana CP phases} \\ (\text{L violating processes}) \\ \left[\begin{array}{ccc} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{array} \right] \end{matrix} \end{matrix} \end{matrix} \end{matrix}$$

PMNS mixing matrix

$\theta_{23} \sim 45^\circ$: "atm." angle $\theta_{13} \sim 9^\circ$ $\theta_{12} \sim 34^\circ$: "solar" angle

δ dirac CP phase

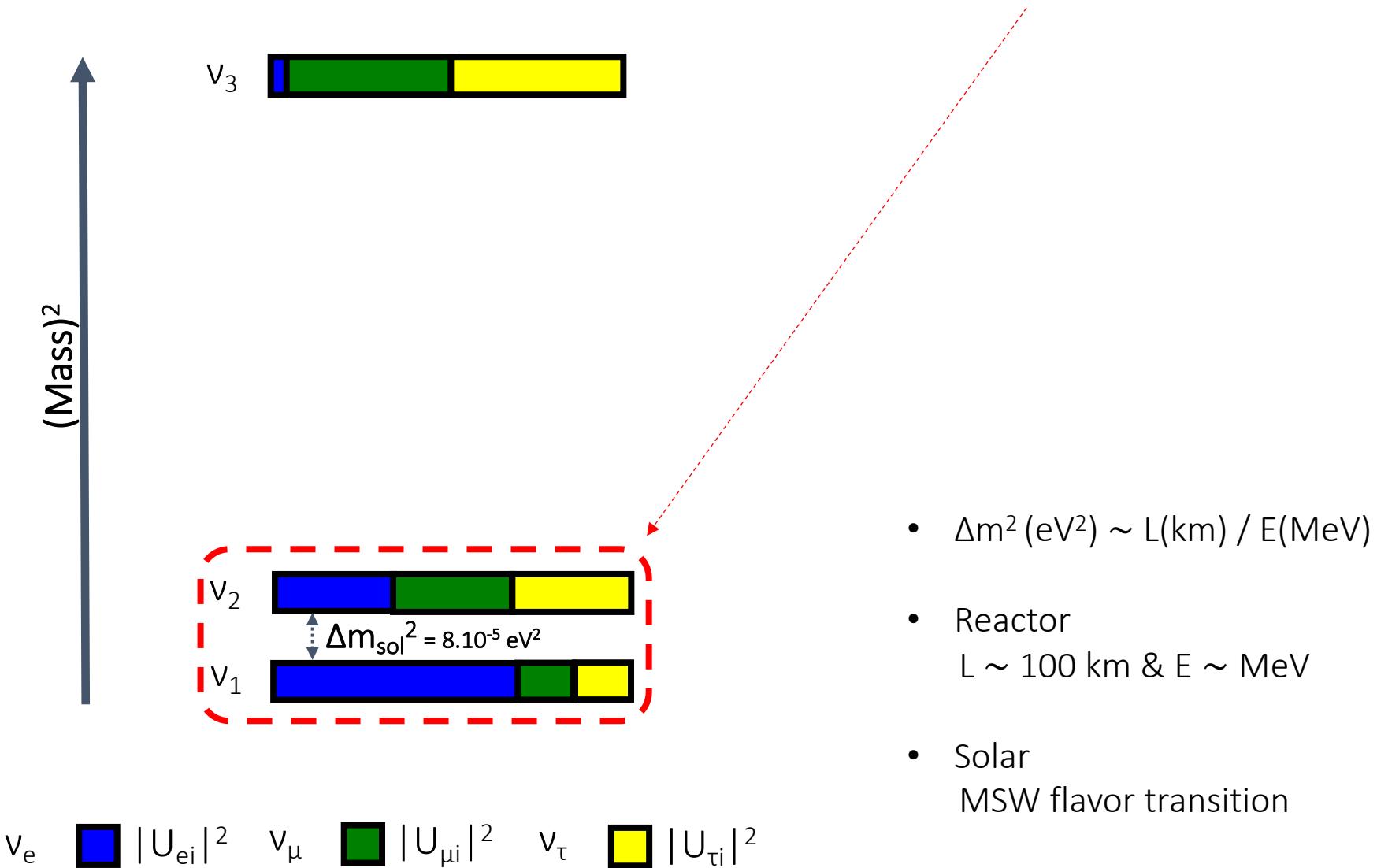
- 3 masses $m_{1,2,3}$: $\Delta m_{sol}^2 = m_2^2 - m_1^2 \sim 8 \cdot 10^{-5} \text{ eV}^2$ & $\Delta m_{atm}^2 = |m_3^2 - m_1^2| \sim 2 \cdot 10^{-3} \text{ eV}^2$
- Oscillation in vacuum : $P(v_x \rightarrow v_x) \approx 1 - \sin^2(2\theta_i) \times \sin^2\left(1.3 \cdot \Delta m_i^2 \cdot \frac{L}{E}\right)$

tunable

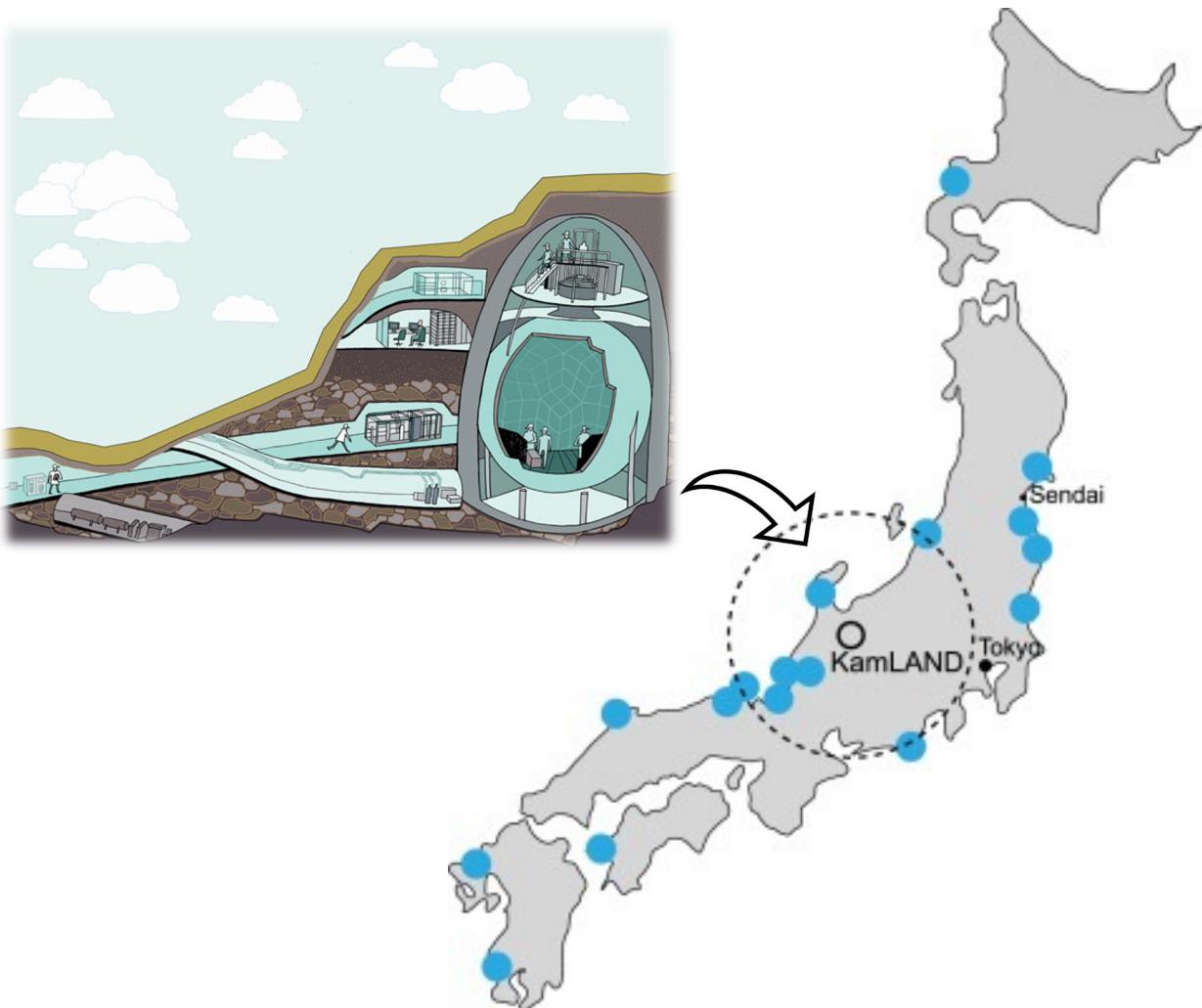
What are the leptonic mixing parameters?



Δm^2_{21} & θ_{12}

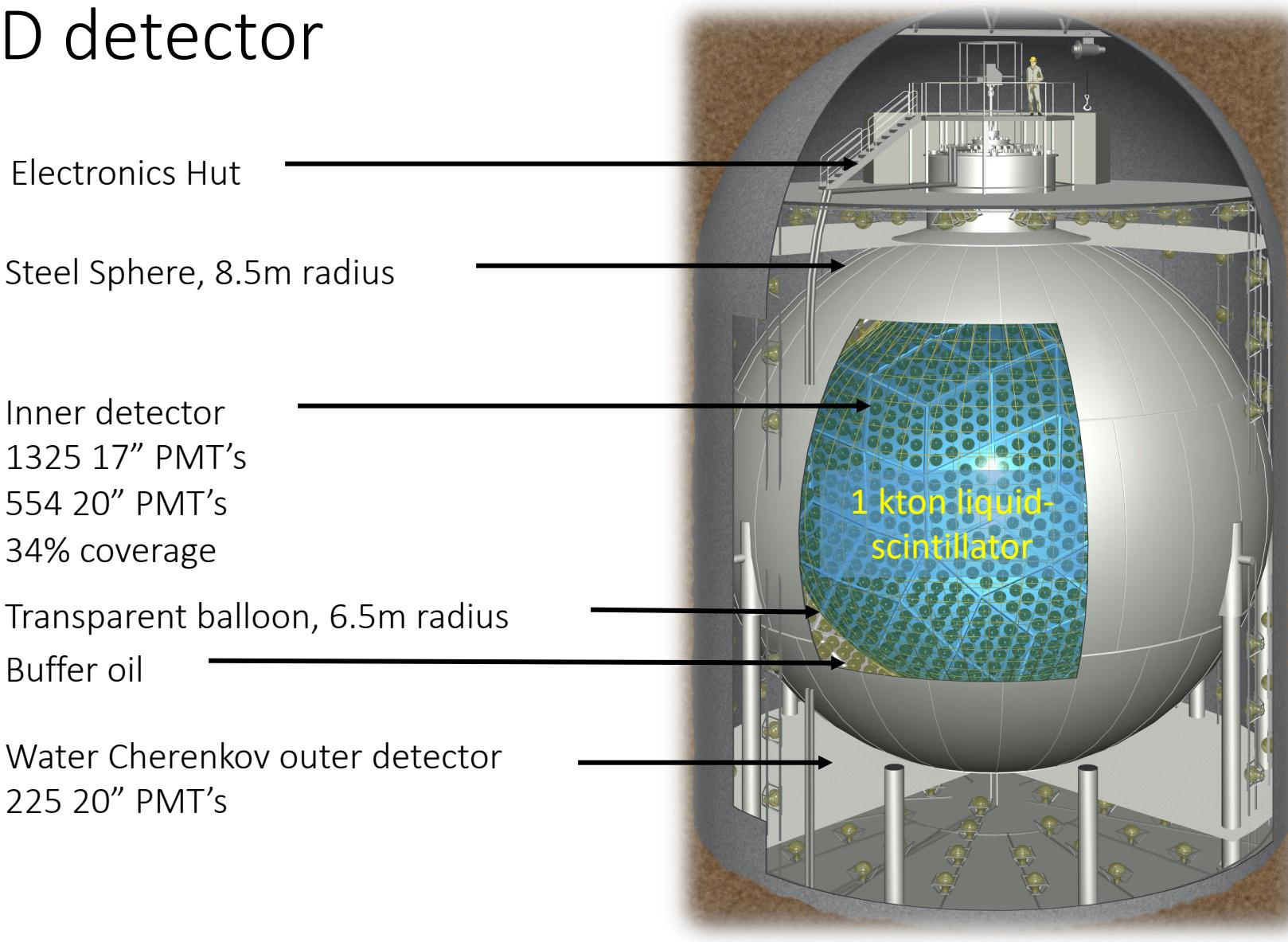
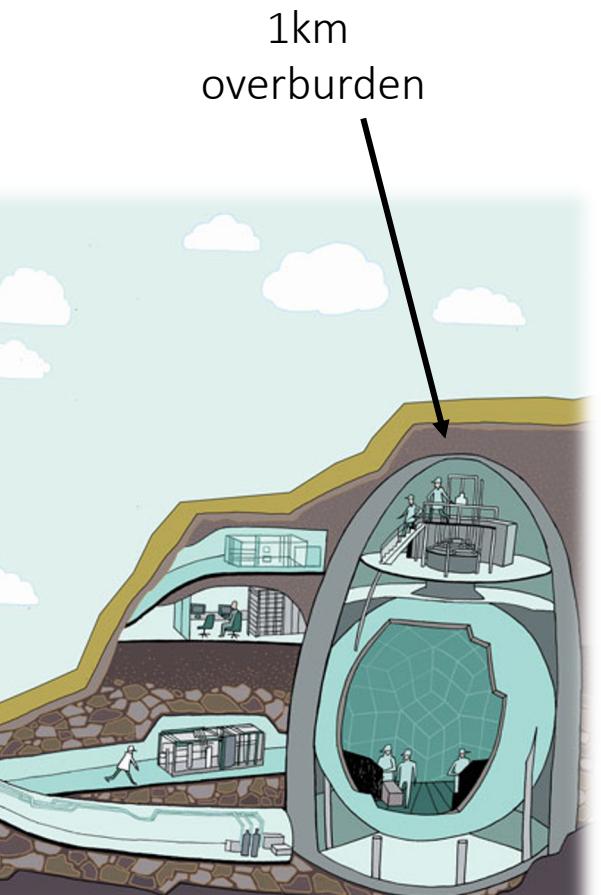


The KamLAND experiment

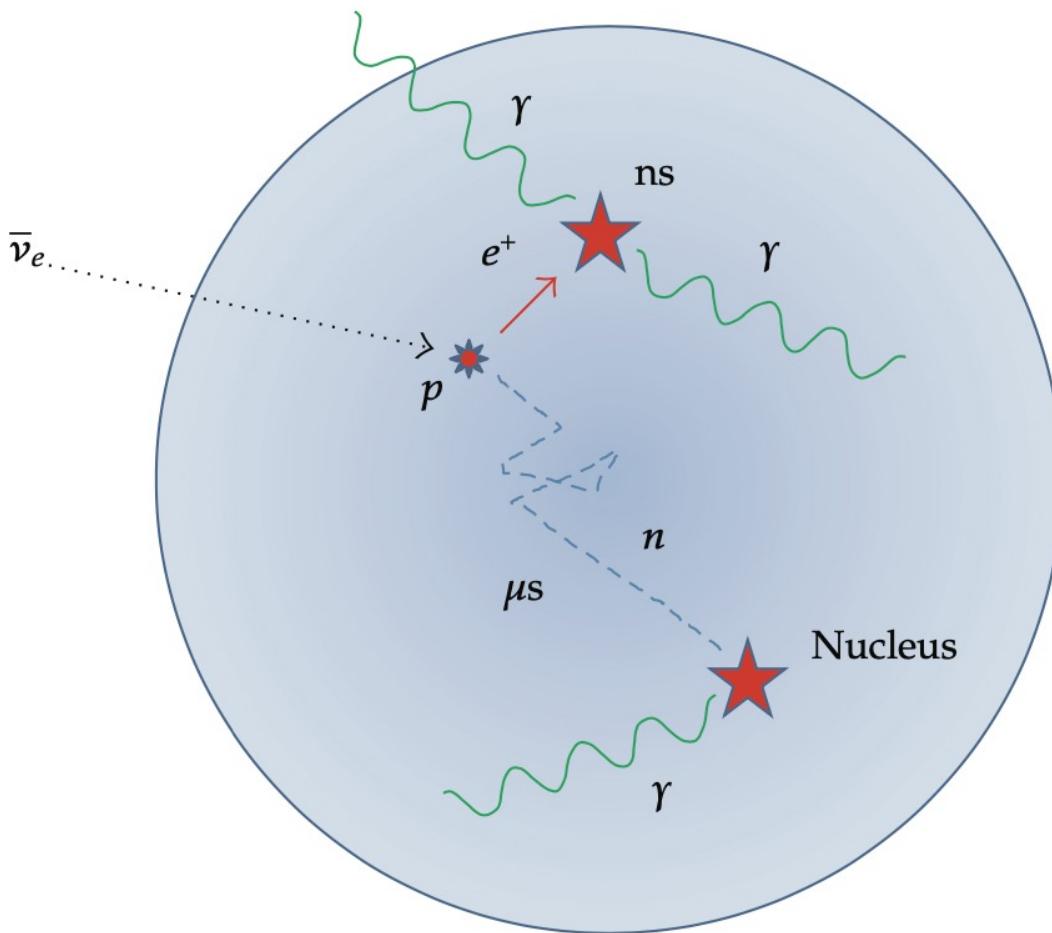


- KamLAND (Kamioka Liquid scintillator Anti-Neutrino Detector) is so far the largest low-energy antineutrino
- Located on the island of Honshu in Japan, since 2002
- Built to detect hundreds of anti-neutrinos per year from nuclear reactors hundreds of kilometers away

The KamLAND detector



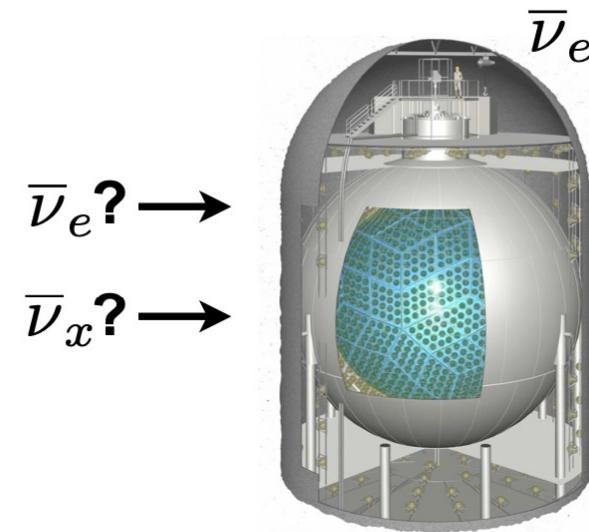
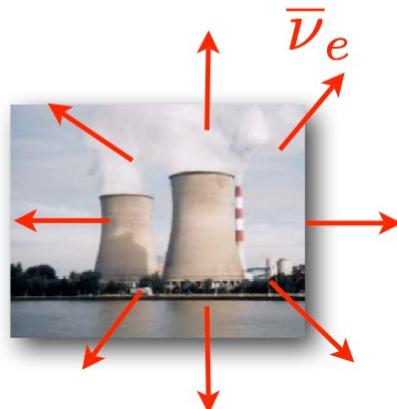
The KamLAND detection principle



- Inverse beta decay (IBD) reaction
- Prompt signal comes from positron annihilation
- Delayed signal occurs when neutron captures a proton
- Challenge: reduce background
 - Cosmic rays (overburden)
 - Natural radioactivity (pure materials)

The KamLAND reactor neutrino measurement

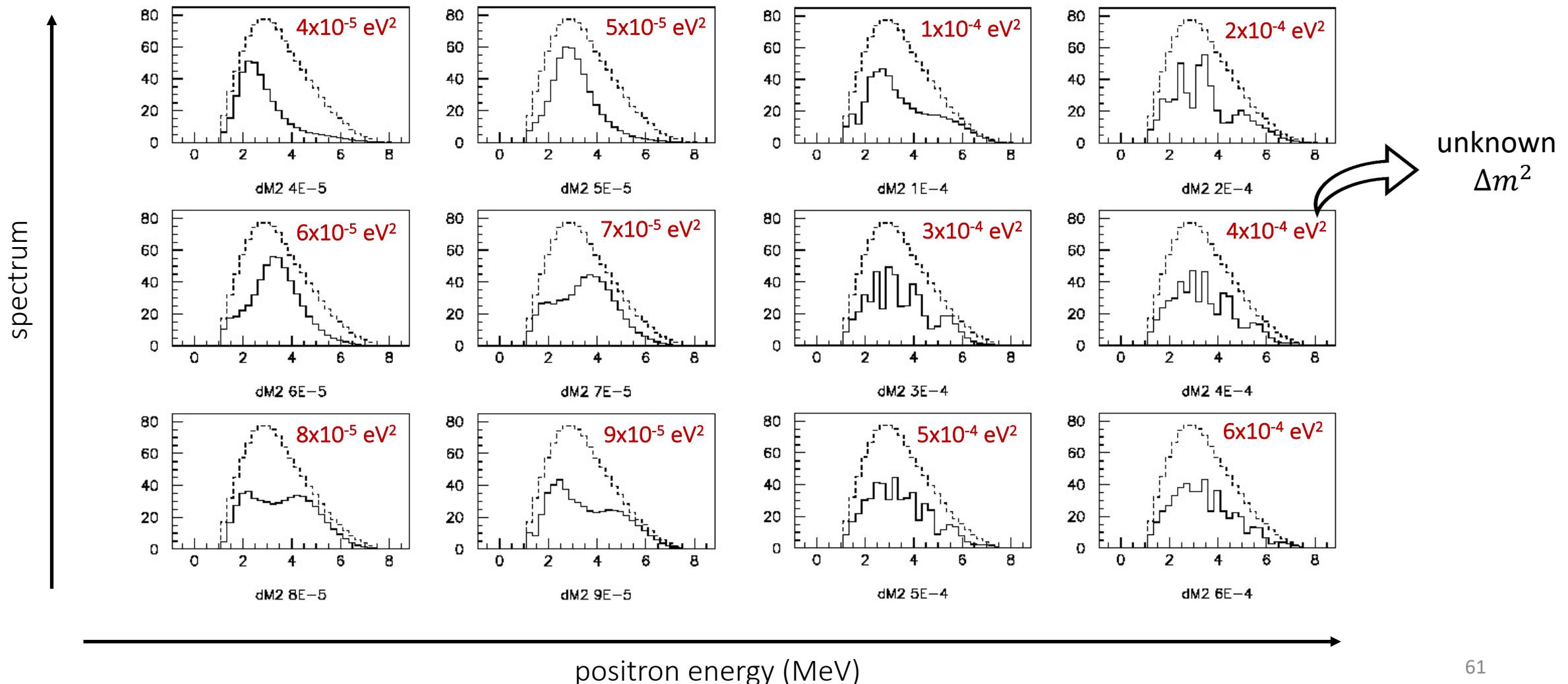
Question before the year 2001: are there reactor neutrino (MeV) oscillation at a distance >100 km?



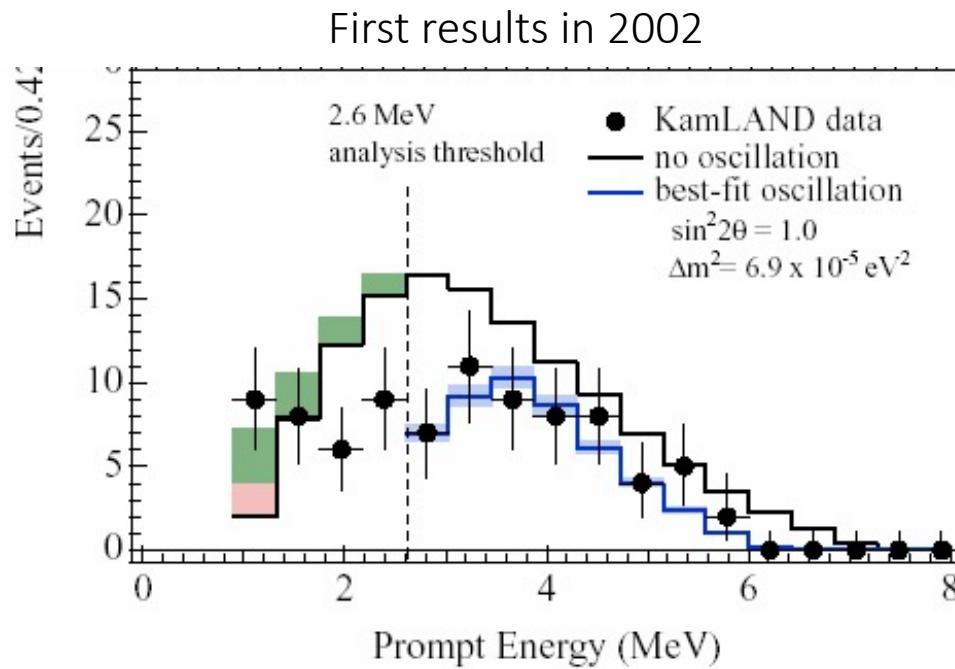
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta \sin^2 \frac{1.27 \Delta m^2 L}{E}$$

$$\begin{array}{c|c} \hline & \\ \hline \end{array} \quad L = 200 \text{ km} \quad \begin{array}{c|c} \hline & \\ \hline \end{array}$$

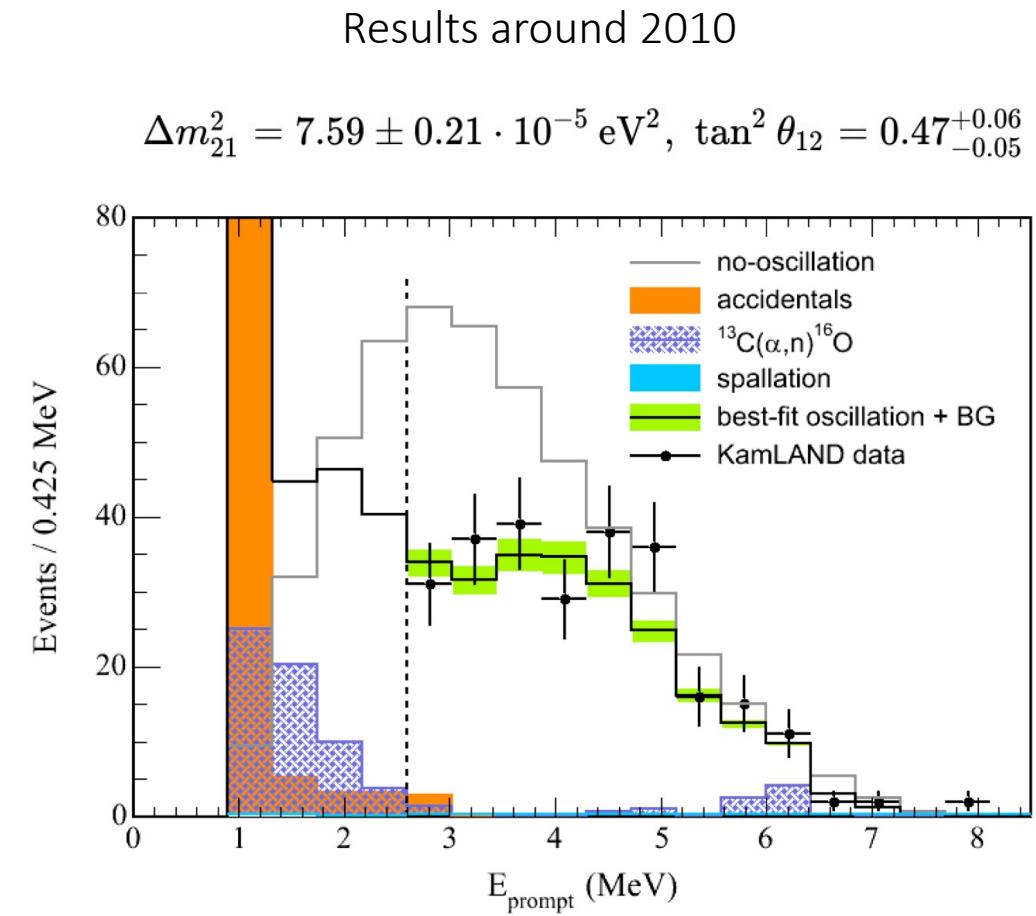
What KamLAND did we expect in 2001?



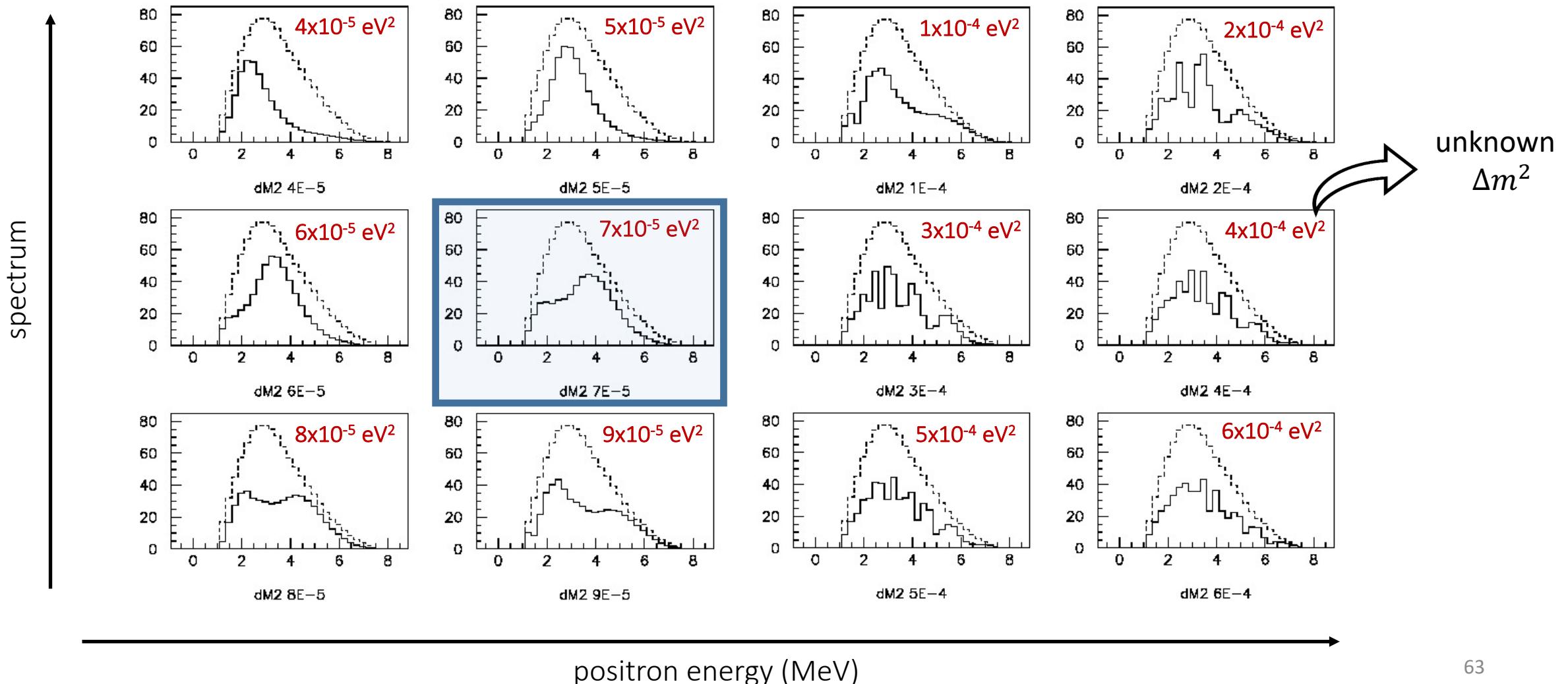
The KamLAND reactor neutrino measurement



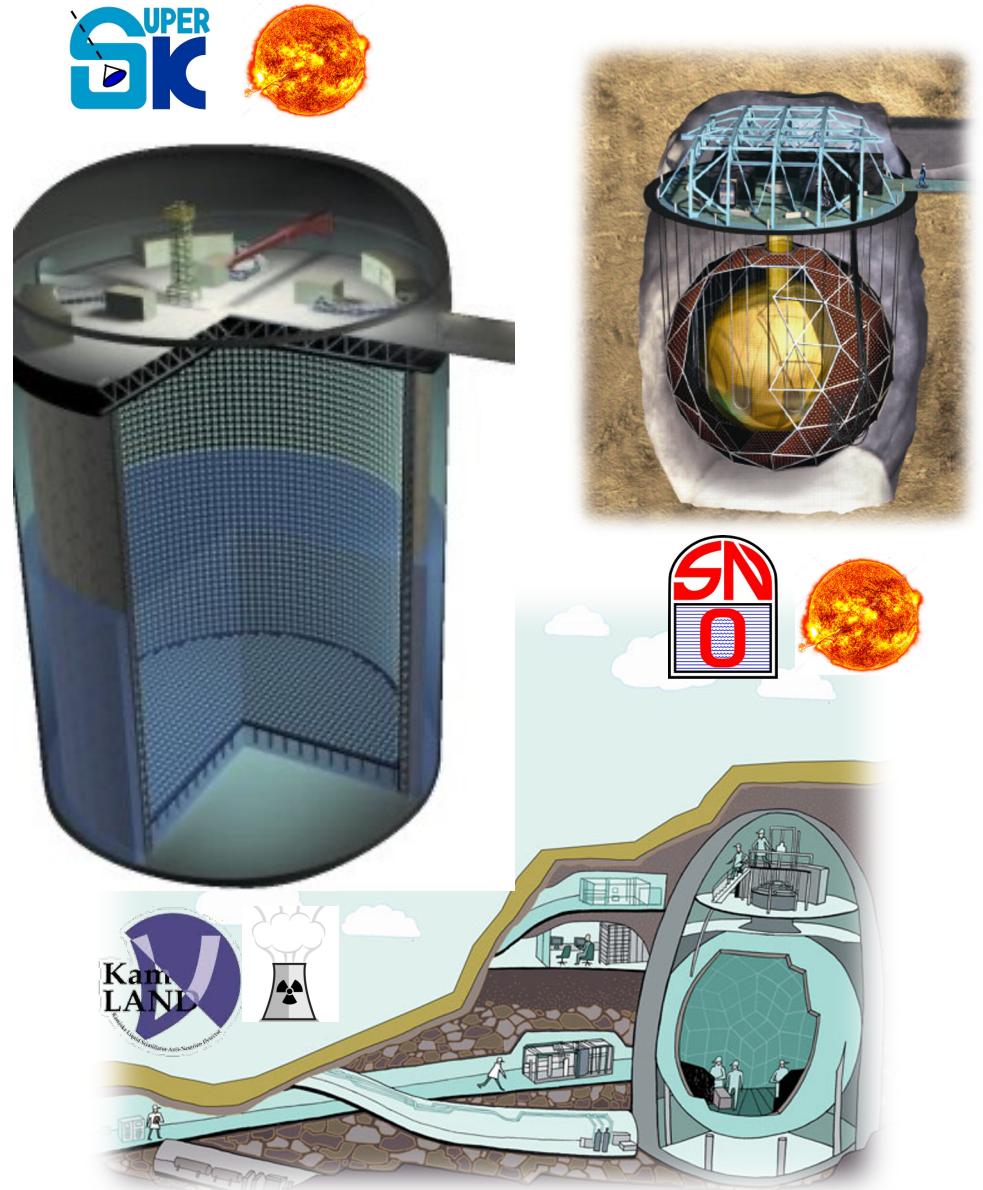
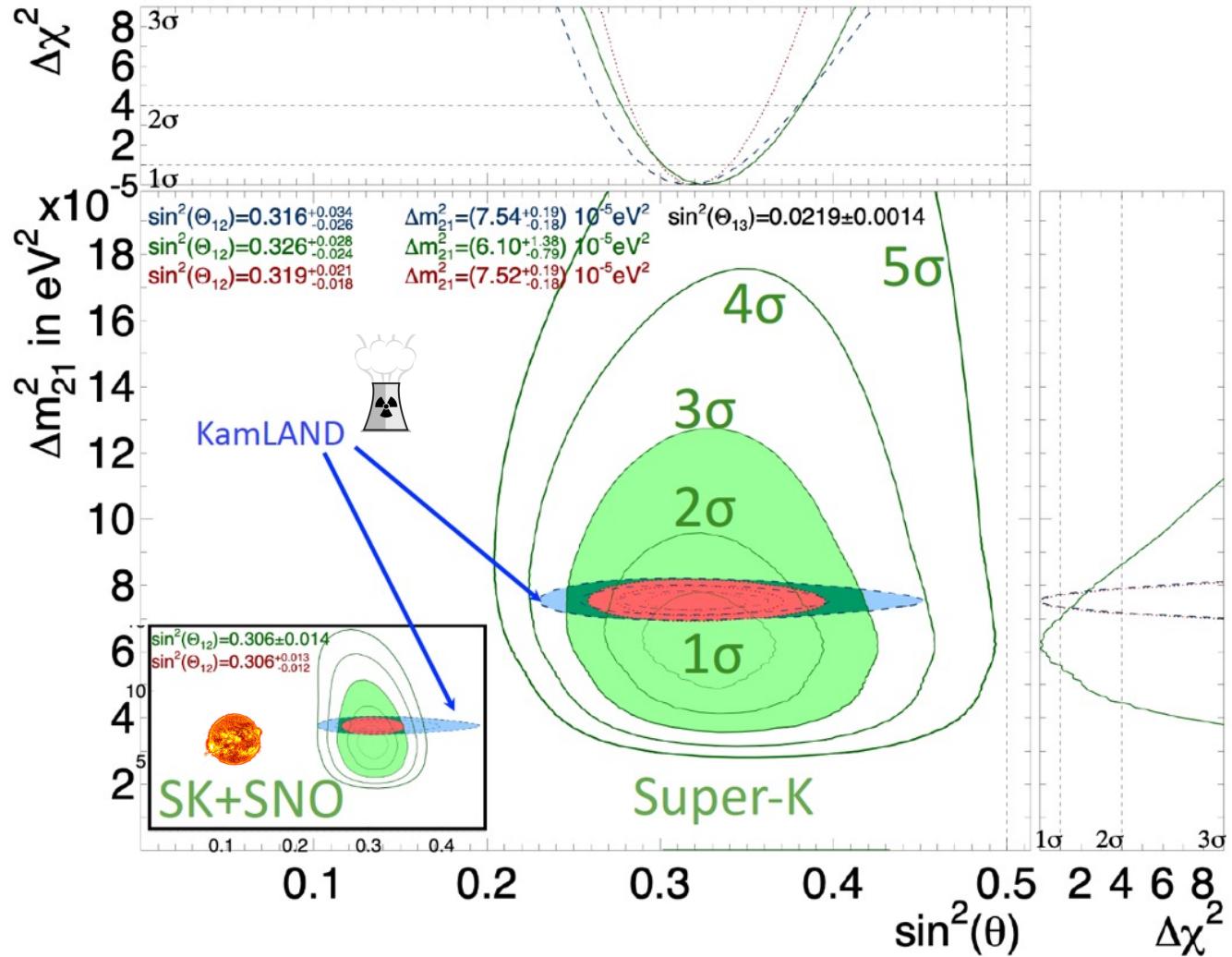
- established reactor antineutrino disappearance, $L >> 100 \text{ km}$, at high significance
- Energy threshold at 2.6 MeV
 - Backgrounds at low energy
 - Geoneutrinos!



What KamLAND did we expect in 2001?



Solar + Reactor Experiments



- Consistent Solar/Reactor Δm^2_{21} & θ_{12}