

Note, that an excellent reference is PDG, specifically the chapters.

- Kinematics
- Electroweak Model and Constraints on New Physics

The notations in this appendix follow the book “An Introduction to Quantum Field Theory” by M. Peskin and D. Schroeder.

## Electroweak Feynman Rules in the Unitary Gauge (one fermionic generation)

Propagators:

$$\begin{array}{l}
 \mu \text{ --- } W^\pm \text{ --- } \nu \quad \frac{-i}{p^2 - m_W^2} \left( g_{\mu\nu} - \frac{p_\mu p_\nu}{m_W^2} \right) \\
 \mu \text{ --- } Z \text{ --- } \nu \quad \frac{-i}{p^2 - m_Z^2} \left( g_{\mu\nu} - \frac{p_\mu p_\nu}{m_Z^2} \right) \\
 \mu \text{ --- } \gamma \text{ --- } \nu \quad \frac{-i}{p^2} g_{\mu\nu} \\
 \text{--- } \psi \text{ ---} \quad \frac{i(\not{p} + m_\psi)}{p^2 - m_\psi^2} \quad \text{(for any fermion } \psi) \\
 \text{--- } h \text{ ---} \quad \frac{i}{p^2 - m_H^2}
 \end{array}$$

Initial and final lines

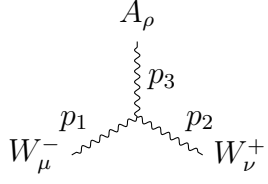
$$\begin{array}{l}
 \text{--- } \left| \begin{array}{l} \epsilon_\mu(p) \text{ incoming} \\ \xrightarrow{p} \end{array} \right. \\
 \left| \begin{array}{l} \epsilon_\mu^*(p) \text{ outgoing} \\ \xrightarrow{p} \end{array} \right.
 \end{array}$$

Summation over polarizations:

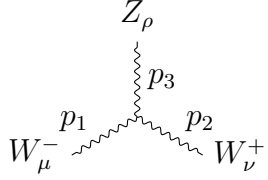
$$\begin{array}{l}
 \sum_{\text{polarizations}} \epsilon_\mu(p) \epsilon_\nu^*(p) = -g_{\mu\nu} \text{ for photons} \\
 \sum_{\text{polarizations}} \epsilon_\mu(p) \epsilon_\nu^*(p) = -g_{\mu\nu} + \frac{p_\mu p_\nu}{m^2} \text{ for massive vectors} \\
 \sum_{\text{spins}} u(p) \bar{u}(p) = \not{p} + m, \quad \sum_{\text{spins}} v(p) \bar{v}(p) = \not{p} - m
 \end{array}$$

Vertices (all momenta are incoming):

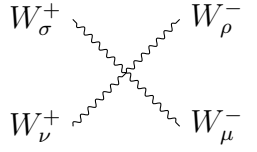
Gauge boson self interactions



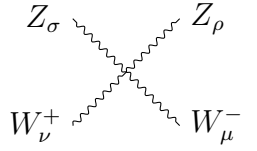
$$ig \sin \theta_W ((p_1 - p_2)_\rho g_{\mu\nu} + (p_2 - p_3)_\mu g_{\nu\rho} + (p_3 - p_1)_\nu g_{\rho\mu})$$



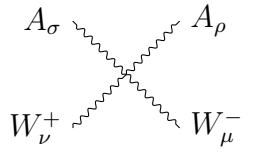
$$ig \cos \theta_W ((p_1 - p_2)_\rho g_{\mu\nu} + (p_2 - p_3)_\mu g_{\nu\rho} + (p_3 - p_1)_\nu g_{\rho\mu})$$



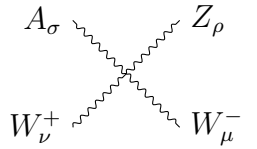
$$ig^2 (2g_{\mu\rho}g_{\nu\sigma} - g_{\mu\nu}g_{\rho\sigma} - g_{\mu\sigma}g_{\nu\rho})$$



$$ig^2 \cos^2 \theta_W (2g_{\mu\nu}g_{\rho\sigma} - g_{\mu\rho}g_{\nu\sigma} - g_{\mu\sigma}g_{\nu\rho})$$

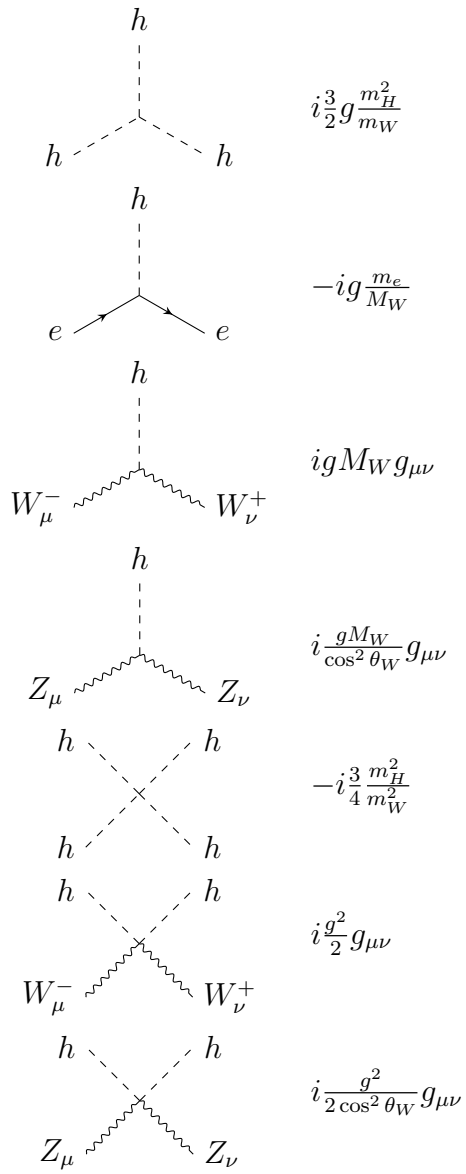


$$ig^2 \sin^2 \theta_W (2g_{\mu\nu}g_{\rho\sigma} - g_{\mu\rho}g_{\nu\sigma} - g_{\mu\sigma}g_{\nu\rho})$$

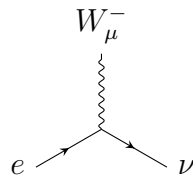


$$ig^2 \cos \theta_W \sin \theta_W (2g_{\mu\nu}g_{\rho\sigma} - g_{\mu\rho}g_{\nu\sigma} - g_{\mu\sigma}g_{\nu\rho})$$

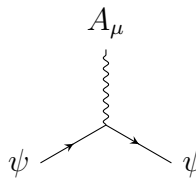
Higgs interactions



Fermion interactions with gauge bosons

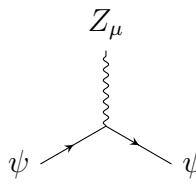


$$-i\frac{g}{2\sqrt{2}}\gamma_\mu(1-\gamma^5)$$



$$+iQg\sin\theta_W\gamma_\mu$$

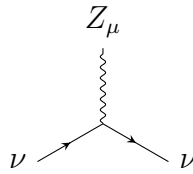
$Q$  is the fermion charge in units of  $e$



$$+i\frac{g}{2\cos\theta_W}\gamma_\mu(T^3(1-\gamma^5) - 2Q\sin^2\theta_W)$$

$T^3 = 1/2$  for up quarks and neutrinos,

$-1/2$  for down quarks and charged leptons



$$-i\frac{g}{4\cos\theta_W}\gamma_\mu(1-\gamma^5)$$

## Some formulas for traces of gamma matrices

$$\text{tr}(\mathbf{1}) = 4$$

$$\text{tr}(\text{odd number of } \gamma \text{ matrices}) = 0$$

$$\text{tr}(\gamma^\mu \gamma^\nu) = 4g^{\mu\nu}$$

$$\text{tr}(\gamma^\mu \gamma^\nu \gamma^\rho \gamma^\sigma) = 4(g^{\mu\nu} g^{\rho\sigma} - g^{\mu\rho} g^{\nu\sigma} + g^{\mu\sigma} g^{\nu\rho})$$

$$\text{tr}(\gamma^5) = 0$$

$$\text{tr}(\gamma^5 \gamma^\mu \gamma^\nu) = 0 \text{ (proove it!)}$$

$$\text{tr}(\gamma^5 \gamma^\mu \gamma^\nu \gamma^\rho \gamma^\sigma) = -4i\epsilon^{\mu\nu\rho\sigma}$$

$$\epsilon^{\alpha\beta\gamma\delta} \epsilon_{\alpha\beta\gamma\delta} = -24$$

$$\epsilon^{\alpha\beta\gamma\mu} \epsilon_{\alpha\beta\gamma\nu} = -6\delta_\nu^\mu$$

$$\epsilon^{\alpha\beta\mu\nu} \epsilon_{\alpha\beta\rho\sigma} = -2(\delta_\rho^\mu \delta_\sigma^\nu - \delta_\sigma^\mu \delta_\rho^\nu)$$