

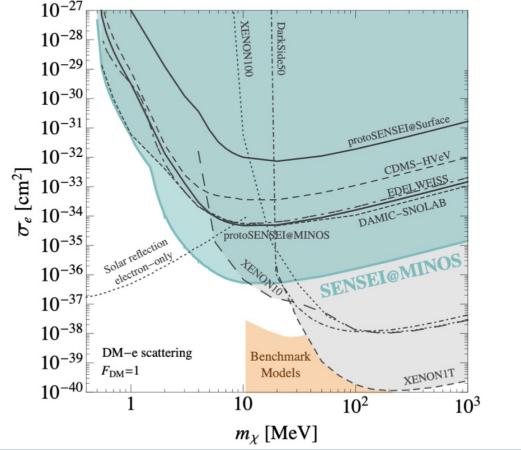
# **Motivating DM-electron searches with SPCs**

Louis Hamaide – UK HEP Forum

Based on arxiv 2110.02985

## **Why DM-Electron Searches?**

- DM-electron scattering opens searches for MeV-GeV DM
- Requires sensitivity to small number of electrons (<4e-)

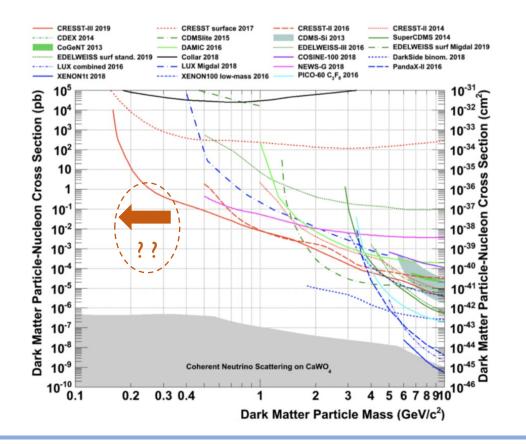


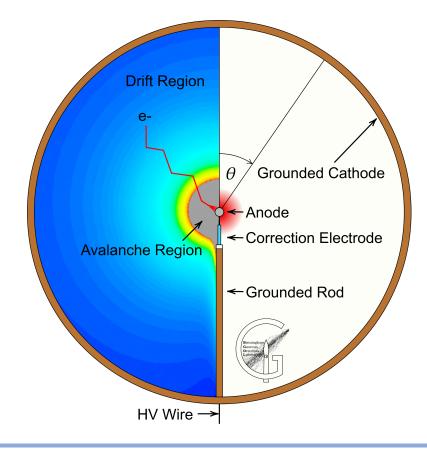
arxiv 2004.11378

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## What Are Spherical Proportional Counters (SPC)?

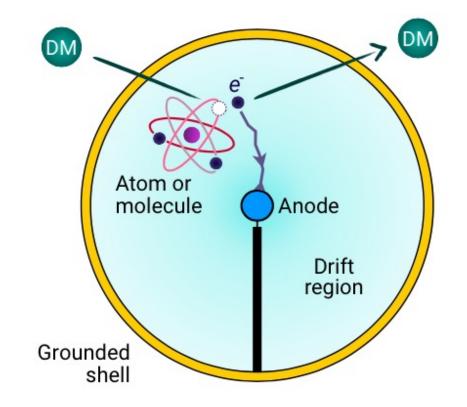
- SPCs consist of gas in a sphere, sensitive to Ie- events and exhibit low noise
- Used for nuclear scattering bounds on DM



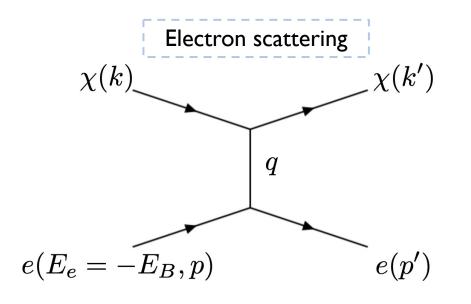


## Can SPCs be used for DM-electron searches?

• Electron gets kicked off by DM particle and drifts down, triggering an avalanche

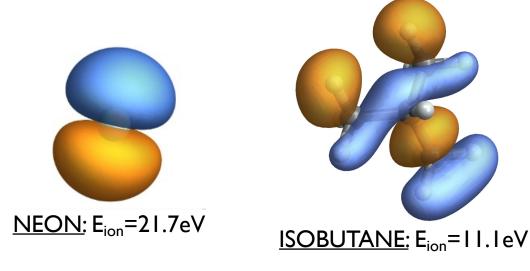


## **Developing the theory**



Rates 
$$\boldsymbol{\alpha} \quad \left| \int d^3x \, \tilde{\psi}^*_{p'l'm'}(\mathbf{x}) e^{i\mathbf{q}\cdot\mathbf{x}} \psi_{nlm}(\mathbf{x}) \right|^2$$

- Look at Helium, Neon (lighter), Xenon (traditional) and CH<sub>4</sub> & C<sub>4</sub>H<sub>10</sub> (quenchers)
- $\rightarrow$  **PySCF** : Quantum chemistry package that solves HF eqs. self-consistently for atoms and molecules



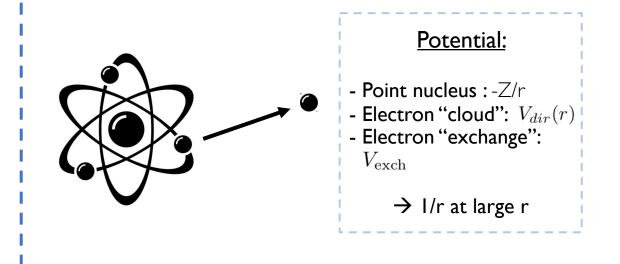
#### **Unbound Electron Wavefunctions**

• **Atoms:** Continuum limit: Hartree-Fock + frozen core:

 $-\frac{1}{2}\frac{d^2P_{n_al_a}}{dr^2} + \frac{l_a(l_a+1)}{2r^2}P_{n_al_a}(r) - \frac{Z}{r}P_{n_al_a}(r) + V_{eff}(r) = \epsilon_{n_al_a}P_{n_al_a}(r) + V_{$ 

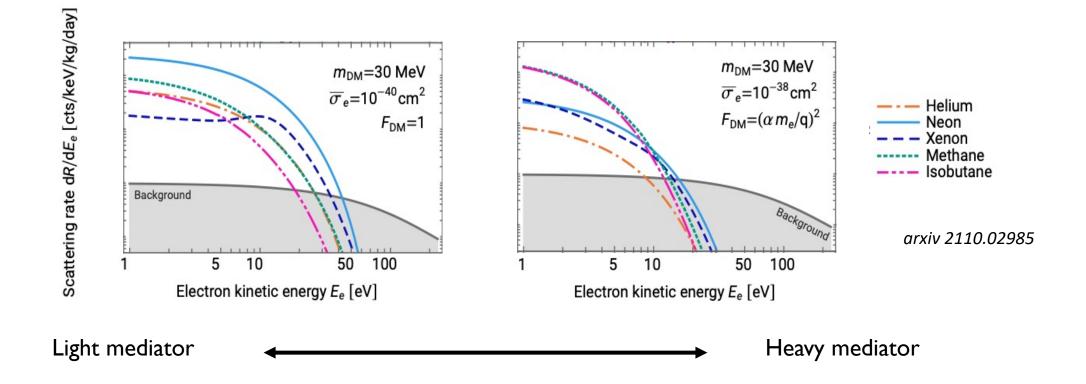
Molecules: Coulomb potential/wavefunction:

$$-\frac{1}{2}\frac{d^2 P_{n_a l_a}}{dr^2} + \frac{l_a(l_a+1)}{2r^2}P_{n_a l_a}(r) - \frac{Z}{r}P_{n_a l_a}(r) + \frac{Z_{eff}}{r} = \epsilon_{n_a l_a}P_{n_a l_a}(r)$$

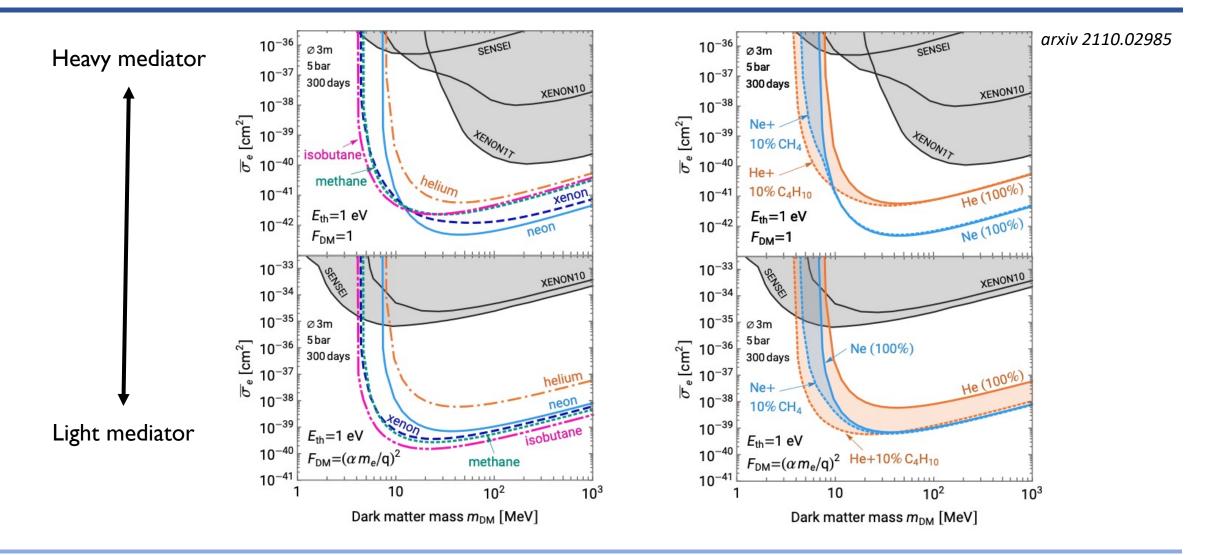


### **Event Rates**

- Event rates higher for lighter states, but also for states spread in momentum space: Neon best overall
- Molecules can be used for the lightest dark matter bounds



#### SPCs can reach very encouraging cross sections

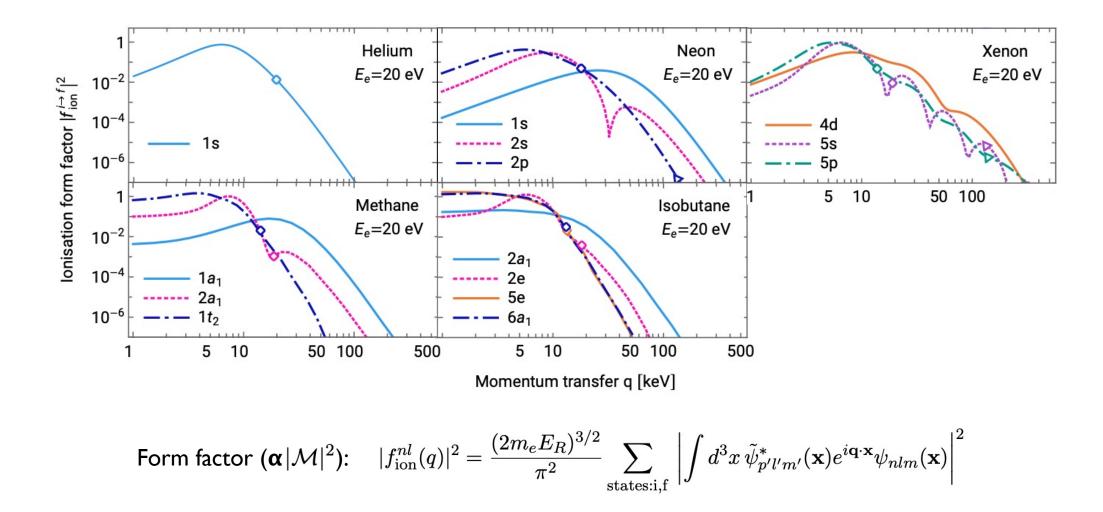


## Summary

- Dedicated direct detection of DM-electron scattering good probe of light DM (<IGeV)
- Developed theory for DM-electron scattering in atoms and molecules in SPCs
- Seems promising  $\rightarrow$  more sensitive than current bounds / comparable to other proposed experiments
- SPC good probe of light DM-electron scattering !

## Thank you!

#### **Form Factors**



## **Bound Electron Wavefunctions**

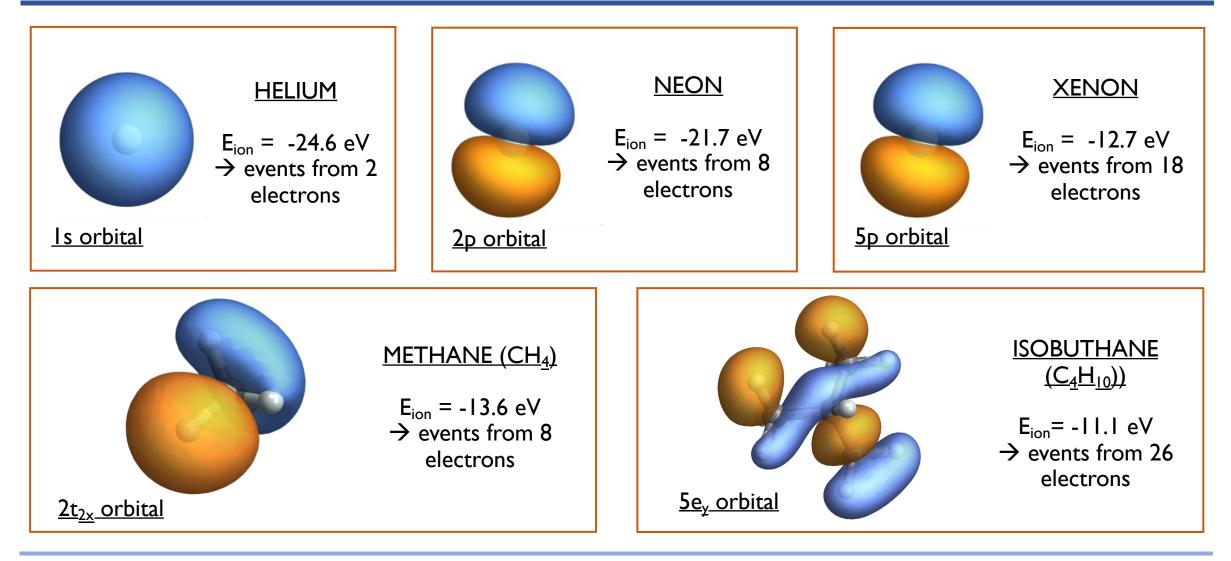
• Hartree-Fock approximation: mean field self consistent bound states:

$$\begin{split} -\frac{1}{2}\frac{d^{2}P_{n_{a}l_{a}}}{dr^{2}} + \frac{l_{a}(l_{a}+1)}{2r^{2}}P_{n_{a}l_{a}}(r) - \frac{Z}{r}P_{n_{a}l_{a}}(r) + \sum_{n_{b}l_{b}}(4l_{b}+2)\left(v_{0}(n_{b}l_{b},r)P_{n_{a}l_{a}}(r) - \sum_{l}\Lambda_{l_{a}ll_{b}}v_{l}(n_{b}l_{b},n_{a}l_{a},r)P_{n_{b}l_{b}}(r)\right) \\ &= \epsilon_{n_{a}l_{a}}P_{n_{a}l_{a}}(r) + \sum_{n_{b}\neq n_{a}}\epsilon_{n_{a}l_{a},n_{b}l_{a}}P_{n_{b}l_{a}}(r) \end{split}$$

- **PySCF** : Quantum chemistry package that solves HF eqs. for atoms and molecules:
  - > HF equations solved self-consistently using gaussian basis
  - > Includes relativistic treatments, molecular dipoles, and more
  - $\succ$  Expect accuracy of O(30%) in event rates/bounds

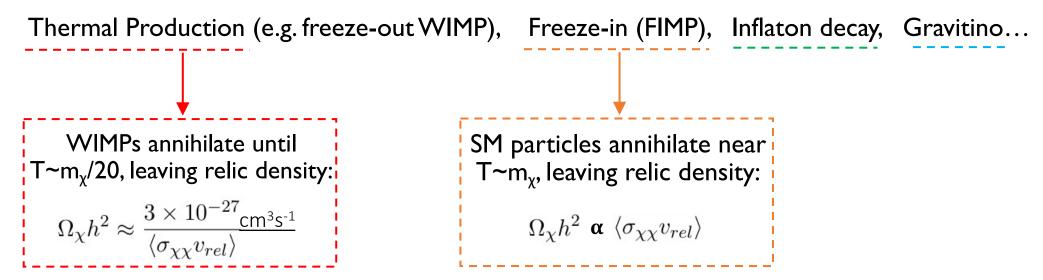


#### **Bound Electron Wavefunctions - Results**



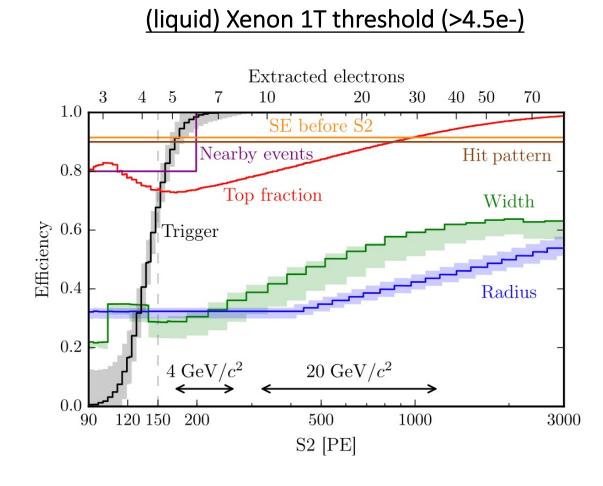
## Back up - Motivation for Light(er) Dark Matter

• Dark matter has many ways of appearing in the present day universe:

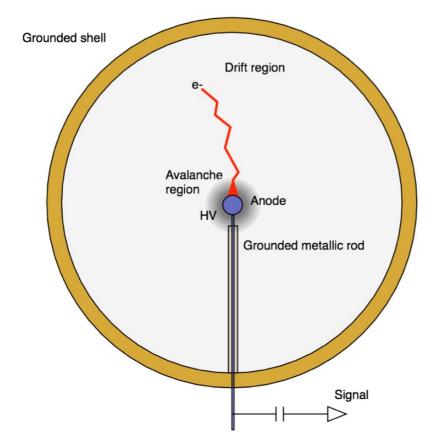


- Individual models of freeze-out and or freeze-in DM can be fully tested (even for unknown details of UV cosmology).
- Without knowledge of  $T_R$ , we cannot fully test inflaton decay or gravitino

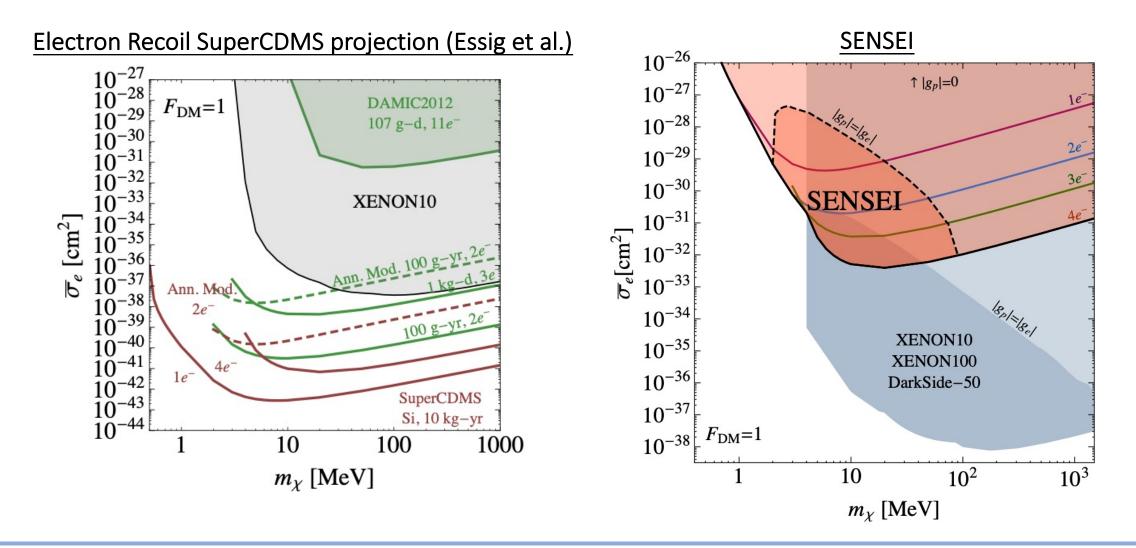
### **Back up – More On Detector**



# Spherical Proportional Counter (SPC, as proposed in DarkSPHERE)

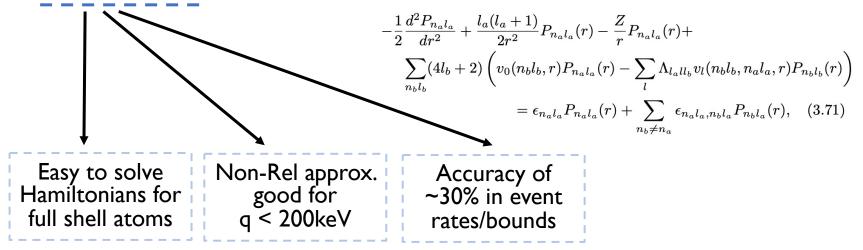


## Back up – More On Constraints



## Back up – Hartree Fock choice

• Hartree-Fock approximation: self-consistent bound states with energies correct to first order:



- Sensitivities of bounds to choices:
  - > ~30-50% Gaussian basis choice
  - > ~50-100% exchange potential choice, orthogonalization
  - $\geq$  ~10-20% analysis of recoil energy profile vs. deposited energies
  - > ~30% astrophysical parameter choices
  - Linear with background

## **Bound electron wavefunctions (3/4)**

Hartree-Fock approximation: mean field self consistent bound states: ٠

$$-\frac{1}{2}\frac{d^{2}P_{n_{a}l_{a}}}{dr^{2}} + \frac{l_{a}(l_{a}+1)}{2r^{2}}P_{n_{a}l_{a}}(r) - \frac{7}{r}P_{n_{a}l_{a}}(r) + \sum_{n_{b}l_{b}}(4l_{b}+2)\left(v_{0}(n_{b}l_{b},r)P_{n_{a}l_{a}}(r) - \sum_{l}\Lambda_{l_{a}ll_{b}}v_{l}(n_{b}l_{b},n_{a}l_{a},r)P_{n_{b}l_{b}}(r)\right)$$

$$= \epsilon_{n_{a}l_{a}}P_{n_{a}l_{a}}(r) + \sum_{n_{b}\neq n_{a}}\epsilon_{n_{a}l_{a},n_{b}l_{a}}P_{n_{b}l_{a}}(r)$$

$$= \epsilon_{n_{a}l_{a}}P_{n_{a}l_{a}}(r) + \sum_{n_{b}\neq n_{a}}\epsilon_{n_{b}l_{a}}P_{n_{b}l_{a}}(r)$$

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$$= \epsilon_{n_{a}l_{a}}(r) + \sum_{n_{b}l_{a}}(r)$$

$$= \epsilon_{n_{a}l_{a}}(r) + \sum_{n_{b}l_{a$$

Gaussian dasis choice important at small/large r

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## **Back up - Bound electron wavefunction symmetry**

• Molecular orbitals are no longer eigenfunctions (spherical harmonics) of the SO(3) generators.

$$\psi(\mathbf{r}) = \frac{P(r)}{r} Y_{lm}(\theta, \phi) \quad \to \quad \psi(x, y, z)$$

• We need new classification of orbitals :

irreducible representations of SO(3)  $\rightarrow$  irreducible representation of point group

T <sub>d</sub>	E	8C <sub>3</sub>	3C <sub>2</sub>	6S <sub>4</sub>	6σ <sub>d</sub>	linear functions, rotations	quadratic functions	cubic functions
A <sub>1</sub>	+1	+1	+1	+1	+1	-	$x^2+y^2+z^2$	xyz
A <sub>2</sub>	+1	+1	+1	-1	-1	-	-	-
E	+2	-1	+2	0	0	-	$(2z^2-x^2-y^2, x^2-y^2)$	-
T <sub>1</sub>	+3	0	-1	+1	-1	$(\mathbf{R}_{\mathbf{X}},\mathbf{R}_{\mathbf{y}},\mathbf{R}_{\mathbf{z}})$	-	$[x(z^2-y^2), y(z^2-x^2), z(x^2-y^2)]$
T <sub>2</sub>	+3	0	-1	-1	+1	(x, y, z)	(xy, xz, yz)	$\boxed{(x^3, y^3, z^3) [x(z^2+y^2), y(z^2+x^2), z(x^2+y^2)]}$

Tetrahedral group (Methane): T<sub>d</sub>

#### **Back-up - bound electron energies**

Helium (He)	Neon (Ne)	Methane (CH <sub>4</sub> )	Isobutane $(C_4H_{10})$	Xenon (Xe)	
Basis: aug-cc-pV5Z Total energy: -2.8616	Basis: aug-cc-pV5Z Total energy: -128.5467	Basis: $6-31G(d,p)$ Total energy: $-40.2016$	Basis: $6-31G(d,p)$ Total energy: $-157.3123$	Basis: Jorge-QZP Total energy: -7229.7195	
$\begin{array}{c c} \text{Orbital} & I_{\text{HF}} & I_{\text{exp}} \\ 1s^2 & 24.98 & 24.6 \end{array}$	$\begin{array}{c cccc} \text{Orbital} & I_{\text{HF}} & I_{\text{exp}} \\ 2p^6 & 23.14 & 21.7 \\ 2s^2 & 52.53 & 48.5 \\ 1s^2 & 891.79 & 870.2 \end{array}$	$\begin{array}{c cccc} \text{Orbital} & I_{\text{HF}} & I_{\text{exp}} \\ 1t_2^6 & 14.80 & 13.6 \\ 2a_1^2 & 25.66 & 22.9 \\ 1a_1^2 & 304.96 & 290.8 \end{array}$	$\begin{array}{c ccccc} \mbox{Orbital} & I_{\rm HF} & I_{\rm exp} \\ 6a_1^2 & 12.34 & 11.13 \\ 5e^4 & 12.44 & 11.75 \\ 1a_2^2 & 13.86 & 12.85 \\ 4e^4 & 14.54 & 13.71 \\ 3e^4 & 16.04 & 15.03 \\ 5a_1^2 & 17.15 & 15.91 \\ 4a_1^2 & 20.62 & 18.58 \\ 2e^4 & 25.17 & 21.83 \\ 3a_1^2 & 29.44 & 24.83 \\ 2a_1^2 & 305.01 & - \\ 1e^4 & 305.01 & - \\ 1a_1^2 & 305.30 & - \\ \end{array}$	$\begin{array}{c ccccc} \text{Orbital} & I_{\text{HF}} & I_{\text{exp}} \\ 5p^6 & 12.45 & 12.7 \\ 5s^2 & 25.54 & 23.3 \\ 4d^{10} & 75.72 & 68.5 \\ 4p^6 & 163.56 & 146.1 \\ 4s^2 & 212.69 & 213.2 \\ 3d^{10} & 711.26 & 682.7 \\ 3p^6 & 958.02 & 971.4 \\ 3s^2 & 1087.7 & 1149 \\ 2p^6 & 4839.8 & 4947 \\ 2s^2 & 5132.0 & 5453 \\ 1s^2 & 33321 & 34561 \end{array}$	

#### **Event rates – Back up**

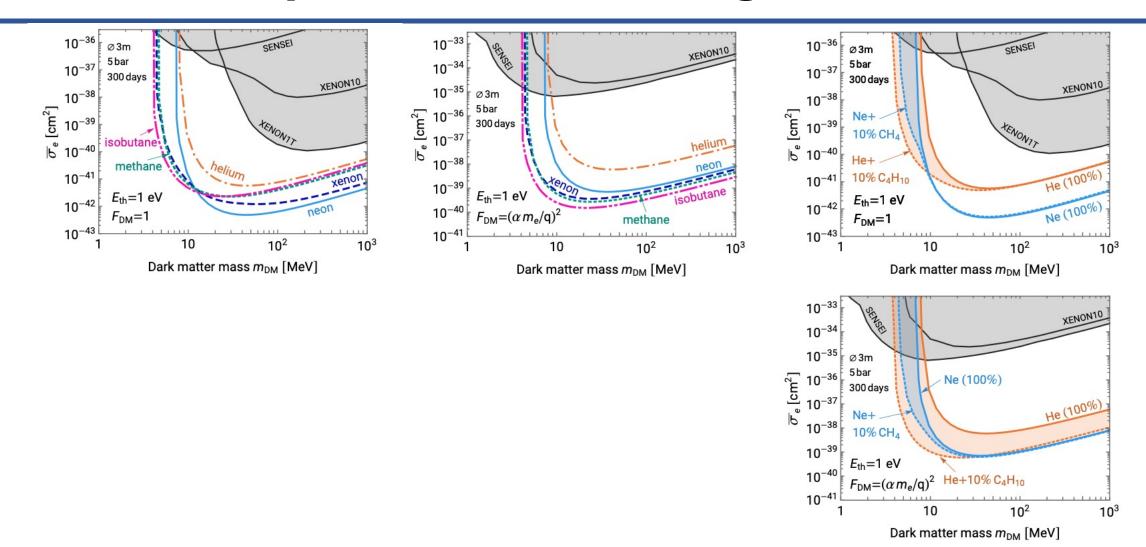
• The dark event rate can be calculated using:

- Assume phenomenological background provided by NEWS-G,  $F_{DM}$ =1
- 10% Methane (plane wave) contribution

• Likelihood analysis: 
$$\Lambda = \frac{\mathcal{L}(0)}{\mathcal{L}(\sigma_e)} \quad -2\ln(\Lambda) \sim \chi^2_{\mathsf{I}} \qquad \mathcal{L}(\sigma_e) = \prod_{i=0}^{N_{bins}} \mathcal{P}\left(N_{obs}^i \mid N_{\chi}^i(\sigma_e) + N_{bg}^i\right)$$

- With exposure 5atm.300days in sphere of radius 1.5m DarkSPHERE sensitivity below Xenon IT
- Molecular contribution seen as setting own bounds → potential for molecular bounds on DM-e scattering

#### **Back-up – Sensitivities to higher threshold**



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