## PDFs and their Nuclear Modifications





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- Carlos A. Salgado IGFAE - Santiago de Compostela
- Physics Opportunities at the Electron-Ion Collider 2021 on-line







# Why nuclear PDFs

Short answer - same reasons as for proton PDFs

- □ Partonic structure of the nuclei universality of nuclear PDFs?



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Benchmarking in search for new phenomena (saturation of partonic densities and hot matter effects).







# Why nuclear PDFs



- □ Benchmarking in sea
- □ Partonic structure of



[Eskola, Hon



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Example











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EKS98 [Eskola, Kolhinen, Ruuskanen, Salgado] HKM01, HKN04 [Hirai, Kumano, Miyama, Nagai] HKN04 - first Hessian error analysis de Florian, Sassot 2004 **First NLO analysis** 









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EPS09 [Eskola, Paukkunen, Salgado] **RHIC data included for 1st time** DSSZ-2012 [de Florian, Sassot, Stratmann, Zurita] Neutrino data included in fit nCTEQ - 2015 [Kovarik et al.]









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EPPS16 [Eskola, Paakkinen, Paukkunen, Salgado] LHC data included for first time

KA15, KSASG20 [Khanpour, Soleymaninia, Tehrani, Spiesberger, Guzey] TUJU19 [Walt, Helenius, Vogelsang] nNNPDF1.0/2.0 [Abdul Khalek, Ethier, Rojo, van Weelden]









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# Recall DGLAP

## **Collinear factorization - perturbative cross sections**

$$\frac{d}{dk} \stackrel{AB \to x}{dk} = \int_{i}^{A} (x_{i} \mu^{2}) \otimes \int_{j}^{B} (y_{i} \mu^{2}) \otimes \frac{de^{ij \neq x}}{dk}$$
Parton distribution functions are universal-  
evolution given by DGLAP
$$\stackrel{P}{=} Non-perturbative (long-distance)$$

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$$\stackrel{P}{=} Differential equations need initial conditions$$

$$\stackrel{P}{=} We cannot compute I.C. - fit from data$$

$$\stackrel{P}{=} DGLAP predicts (perturbative) scale evolution$$

$$\stackrel{P}{=} Vs = \left[ \begin{array}{c} Pq \otimes q + Pq \otimes q \\ Pq \otimes q + Pq \otimes q \end{array}\right]$$

$$\stackrel{P}{=} \frac{ds}{dt} \left[ \begin{array}{c} Pq \otimes q + Pq \otimes q \\ Pq \otimes q +$$

### Knowledge about PDFs reflects used/available experimental data in the fit







# Global PDF fits

One of the most standardized procedures in High-Energy Physics. Main goal: provide a set of Parton Distribution Functions (PDFs)

$$f_{i}(x_{i}a_{i}; \{a_{i}\})$$

$$f_{i}(x_{i}a_{i})$$

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Different sets differ mostly on how I.C. are parametrized and how to treat the error analysis







# Global PDF fits

One of the most standardized procedures in High-Energy Physics. Main goal: provide a set of Parton Distribution Functions (PDFs)

## Input is a set of PDFs at at initial scale Q<sub>0</sub>

This is the fitting function



Different sets differ mostly on how I.C. are parametrized and how to treat the error analysis

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# (Hessian) Error analysis

Define chi2 in terms of the initial parameters **a** (N-dim vector)

$$\sum_{i,j} \left[ T_i(\mathbf{a}) - D_i \right] C_{ij}^{-1} \left[ T_j(\mathbf{a}) - D_j \right].$$

$$\chi^2(\mathbf{z}) \approx \chi_0^2 + \sum_i z_i^2 \,.$$

## vectors z are linear combinations of original a now uncorrelated

## **Tolerance factor for EPPS16** $^{2} = 52$

$$\exp\left(-\chi^2/2\right) = 0.90,$$















# Nuclear PDFs



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## Main historical disadvantage - Lack of data

- No collider DIS data only fixed target from 90's
- Data taken with different nuclei nPDFs have an extra variable: A-dependence
- ▶ however... nPDFs known to differ from proton PDFs







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## Solution - use ratios with proton PDFs

Advantage: huge amount of data included for proton **Disadvantage:** inherits problems from proton PDF / lack of freedom / treatment of correlations in error analyses







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### For neutrons - use isospin symmetry

bound-proton PDF bound-neutron PDF  $f_i^A(x,Q^2) = Z f_i^{p/A}(x,Q^2) + (A-Z) f_i^{n/A}(x,Q^2),$ 

and assume  $f_i^{p/A} \stackrel{\text{isospin}}{\longleftrightarrow} f_j^{n/A}$ 







	A-	1.0 0.7	mal-snadwing OEV	ACC minimum			
All sets of r	PDFs have A-deper	0.6 ndence,	but e.g. LHC hav	e only collic	mr⊾ y₀ ded Pb	o (and	some Xe
	CERN NMC 96 CERN CMS* CERN CMS* CERN ATLAS* CERN CMS*	0.4 DIS <sup>10-4</sup> W <sup>±</sup> Z Z dijet	$\mu^{-}Pb(207), \mu^{-}C(192)$ pPb(208) pPb(208) pPb(208) pPb(208) pPb(208) pPb(208)	$\begin{array}{cccc} x & 10^{-1} & 15 \\ & 10 & 6 \\ & 6 & 7 \\ & 7 & 7 \end{array}$	14.1 8.8 5.8 9.6 5.5	[72] [43] [45] [46] [34]	
(	CERN CHORUS $\star$	DIS	$\nu Pb(208), \overline{\nu}Pb(208)$	824	998.6	$\begin{bmatrix} 47 \end{bmatrix}$	

## Before the LHC basically only 15 data points for Pb!

> Other nuclei are interesting for phenomenological reasons (e.g. benchmarking in heavy-ion experiments) but data is still very limited - old data from the 90's in fixed target DIS or Drell-Yan

> A-dependence included in the parameters but some needs to be fixed by hand to ensure convergence.

E.g. EPPS16 
$$y_i(A) = y_i(A_{ref}) \left(\frac{A}{A_{ref}}\right)^{\gamma_i[y_i(A_{ref})-1]}$$









## Parametrization bias reduced with new data

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## Pre-LHC constraints

## Parametrization bias reduced with new data





























## Latest and next generation NLO nPDF global fits

	EPPS16	nNNPDF
la NC DIS	$\checkmark$	$\checkmark$
+ JLab NC DIS		
$\nu$ A CC DIS	$\checkmark$	$\checkmark$
pA DY	$\checkmark$	
$\pi A DY$	$\checkmark$	
RHIC dAu/pp $\pi^0$	$\checkmark$	
LHC pPb dijet $R_{ m FB}$	$\checkmark$	
$ ightarrow$ dijet $R_{ m pPb}$		
LHC pPb $D^0$		
LHC pPb W,Z Run 1	$\checkmark$	$\checkmark$
+ Run 2 pPb W		$\checkmark$
Q cut in DIS	1.3 GeV	1.87 Ge
Data points	1811	1467
Free parameters	20	256
Error analysis	Hessian	Monte Ca
Error tolerance $\Delta\chi^2$	52	N/A
Free-proton PDFs	CT14	
HQ treatment	S-ACOT	FONL
Indep. flavours	6	6
Reference	EPJC 77, 163	JHEP 09,

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Paakkinen - Hadrons2021] [Slide from P.

# EPPS16 - results



## Best fit + 40 error sets. Large uncertainties, **decrease with evolution**





# EPPS16 - results



## Best fit + 40 error sets. Large uncertainties, **decrease with evolution**





# Computing errors



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## A comment on neutrino DIS

In conclusion, we have demonstrated that disposing the overall normalization by dividing the data by the integrated cross section in each neutrino energy bin separately, all large- $Q^2$  neutrino data show practically identical nuclear effects, consistent with the present nuclear PDFs. Our numerical consistency test based on the Hessian method of propagating uncertainties confirms that these data could be included in a global fit without causing disagreement with the other data.

## CONCLUSIONS

Incompatibility of neutrino DIS with charged lepton DIS (?)

- conclusions heavily rely on only NuTeV data most precise
- incompatibility a "precision" effect the result changes e.g. when using uncorrelated errors
- tension in NuTeV data  $\rightarrow$  high  $\chi^2$  of the fit to NuTeV alone  $\rightarrow$  problem of NuTeV data ?
- NOMAD data can help decide

[Slide from K. Kovari's talk at DIS 2012]

[Paukkunen, Salgado arXiv:1302.2001 / PRL110 (2013) 212301]

D-DIS with Pb/Fe included in prote PDF analyses tactorization!









Salgado / arXiv:1004.3140,1302.2001] [Paukkunen,



# EPPS16 vs LHC



Dijet data constrains gluon distributions - only FB ratios used in the analysis.

Good description of heavy boson production but limited constraining power on the fit



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No nuclear effects EPPS16









## Including LHC Run2 - nNNPDF













## [slides shamelessly stolen from P. Paakkinen talk at DIS21]

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## Need to mitigate free-proton PDF uncertainty

Absolute cross sections carry large proton-PDF uncertainty!

Should not be neglected when fitting the nPDFs!



Wherever possible, we use nuclear modification ratios to cancel the free-proton PDF uncertainty

For Ws at 8.16 TeV, we formulate a mixed-energy nuclear modification ratio

$$R_{\rm pPb} = \frac{\mathrm{d}\sigma_{8.16 \ \mathrm{TeV}}^{\mathrm{pPb}}/\mathrm{d}\eta_{\mu}}{\mathrm{d}\sigma_{8.0 \ \mathrm{TeV}}^{\mathrm{pp}}/\mathrm{d}\eta_{\mu}}$$



### Cancel proton-PDF uncertainty ↓ **↓**





### Charting the baseline proton-PDF uncertainty new!

We study baseline-PDF sensitivity by fitting nuclear modifications separately for each CT18A error set



Baseline error mostly subdominant in the observables we fit, but shows up e.g. in the fixed-target DY



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### 5/13





Dijets at 5.02 TeV new!



### data from: [CMS Collaboration, Phys.Rev.Lett. 121 (2018) 062002]

### 7/13

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 $D^0$ s at 5.02 TeV – backward new!

Excellent fit!

Results in line with the reweighting study [Eskola, Helenius, PP & Paukkunen, JHEP 05 (2020) 037]

Using the NLO pQCD S-ACOT- $m_{\rm T}$  GM-VFNS [Helenius & Paukkunen, JHEP 05 (2018) 196]

Using a  $p_{\rm T} > 3 {
m ~GeV}$  cut to reduce theoretical uncertainties





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### data from: [LHCb Collaboration, JHEP 10 (2017) 090]





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### Ws at 8.16 TeV new!



Fully consistent with the dijets and  $D^0s$ 

Important check on the nPDF universality & factorization

These data do not appear to give additional flavour-separation constraints on top of those we had already in EPPS16

Looking forward to increased precision at LHC Run 3

data from: [CMS Collaboration, Phys.Lett.B 800 (2020) 135048, Eur.Phys.J.C 76 (2016) 469]





## Fit results – valence



 $\frac{10}{13}$  PDFs and their nuclear modifications 28





### Fit results – sea



10/13 PDFs and their nuclear modifications 29





## Fit results – strange and glue



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## Comparison with EPPS16



Better control over gluon (anti)shadowing  $\rightarrow$  sub-10% level uncertainties at mid-x! Flavour separation (esp. strangeness) remains a difficult beast to tame

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## Comparison with nNNPDF2.0 and nCTEQ15WZ



• All three consistent within uncertainties, but significant differences in the uncertainty estimates Best constrained gluons in the (prelim.) EPPS21 fit!

prelim





## Data availability w.r.t. A



 $\sim 50\%$  of the data points are for Pb!

 $\bigcirc$  Good coverage of DIS measurements for different A

○ DY data more scarce, but OK A coverage

Hadronic observables available only for heavy nuclei! 

Light-ion runs at LHC could:

- Complement other light-nuclei DY data with W and Z production (strangeness!)
- Give first direct constraints (e.g. dijets, D-mesons) on light-nuclei gluon distributions!

Paakkinen OO-pO Workshop 2021] 





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Paakkinen 00-p0 Workshop 2021] 









# EIC for nPDFs



EIC extends the range to lower-x and lower-Q2







# EIC for nPDFs



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# EIC for nPDFs



EIC extends the range to lower-x and lower-Q2







# EIC - Expected impact







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### [From the EIC yellow report]



## Notice that no LHC Run2 data has been included in EPPS16 (EPPS21 has more constraints for gluons)

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**Figure 7.69:** Left: Relative uncertainty bands of the gluon for Au at  $Q^2 = 1.69 \text{ GeV}^2$  for EPPS16\* (light blue), EPPS16\*+EIC  $\sigma$  (green) and EPPS16\*+EIC  $\sigma^{charm}$  (orange). Right: same as left panel but for Fe at  $Q^2 = 2 \text{ GeV}^2$  for EPPS16 (yellow) and EPPS16+EIC  $\sigma^{charm}$  (red).





# Conclusions

## Nuclear PDFs had strong progress in the last years after LHC data becomes available □ Rather good control on gluons with dijet and D meson data $\Box$ Large uncertainties at the IC rapidly get smaller with evolution. Some problems still persist □ Flavour decomposition □ A-dependence □ Lack of constraints in strange quarks... EIC should have a big impact □ Not clearly seen in re-weighting studies IMHO □ But... fills the gap from small to large virtualities (LHC kinematics) - **checks of universality** □ Flexibility for A-dependence Proton PDF - nucleus PDF joint analyses. DIS observables are THE observables for PDF studies - many years with very limited data





Total

## List of experimental data in EPPS16

Experiment	Observable	Collisions	Data points	$\chi^2$	Ref.
SLAC E139	DIS	$e^{-}$ He(4), $e^{-}$ D	21	12.2	[69]
CERN NMC 95, re.	DIS	$\mu^-\text{He}(4), \ \mu^-\text{D}$	16	18.0	[70]
	<b>DI</b> C				
CERN NMC 95	DIS	$\mu^{-}Li(6), \mu^{-}D$	15	18.4	[71]
CERN NMC 95, $Q^2$ dep.	DIS	$\mu^{-}$ Li(6), $\mu^{-}$ D	153	161.2	[71]
SLAC E139	DIS	$e^{-}\mathrm{Be}(9) e^{-}\mathrm{D}$	20	12.9	[69]
CERN NMC 96	DIS	$\mu^{-}Be(9), \mu^{-}C$	15	4.4	[05] [72]
		$\mu$ $Do(0); \mu$ $O$	10	1.1	[•2]
SLAC E139	DIS	$e^{-}C(12), e^{-}D$	7	6.4	[69]
CERN NMC 95	DIS	$\mu^{-}C(12), \ \mu^{-}D$	15	9.0	[71]
CERN NMC 95, $Q^2$ dep.	DIS	$\mu^{-}C(12), \mu^{-}D$	165	133.6	[71]
CERN NMC 95, re.	DIS	$\mu^{-}C(12), \mu^{-}D$	16	16.7	[70]
CERN NMC 95, re.	DIS	$\mu^{-}C(12), \mu^{-}Li(6)$	20	27.9	[70]
FNAL E772	DY	pC(12), pD	9	11.3	[73]
SLAC E139	DIS	$e^{-} Al(27), e^{-} D$	20	13.7	[69]
CERN NMC 96	DIS	$\mu^{-} Al(27),  \mu^{-} C(12)$	15	5.6	[72]
SLAC E120	DIC	$-C_{2}(40) = D_{2}$	7	1 0	[60]
SLAC E139 ENAL E779	DIS	e Ca(40), e D	1	4.0	[09]
FNAL EIIZ		pCa(40), pD	9	3.33 97.0	[70]
CERN NMC 95, re.	DIS	$\mu Ca(40), \mu D$	15	27.0	$\begin{bmatrix} 1 \\ 7 \end{bmatrix}$
CERN NMC 95, re.	DIS	$\mu Ca(40), \mu Ll(6)$	20	19.5	[70]
CERN NMC 96	DIS	$\mu$ Ca(40), $\mu$ C(12)	15	6.4	[72]
SLAC E139	DIS	$e^{-}$ Fe(56). $e^{-}$ D	26	22.6	[69]
FNAL E772	DY	$e^{-}$ Fe(56). $e^{-}$ D	9	3.0	[73]
CERN NMC 96	DIS	$\mu^{-}$ Fe(56), $\mu^{-}$ C(12)	15	10.8	[72]
FNAL E866	DY	pFe(56), pBe(9)	$\frac{13}{28}$	20.1	[74]
CERN EMC	DIS	$\mu^-$ Cu(64), $\mu^-$ D	19	15.4	[75]
SLAC E139	DIS	$e^{-}$ Ag(108), $e^{-}$ D	7	8.0	[69]
CERN NMC 96	DIS	$\mu^{-}$ Sn(117), $\mu^{-}$ C(12)	15	12.5	[72]
CERN NMC 96. $Q^2$ dep.	DIS	$\mu^{-}$ Sn(117), $\mu^{-}$ C(12)	144	87.6	[76]
, <b>, , ,</b>					
FNAL E772	DY	pW(184), pD	9	7.2	[73]
FNAL E866	DY	pW(184), pBe(9)	28	26.1	[74]
CERN NA10 $\star$	DY	$\pi^{-}W(184), \pi^{-}D$	10	11.6	[49]
FNAL E615 $\star$	DY	$\pi^+ W(184), \pi^- W(184)$	11	10.2	[50]
CERN NA3★	DY	$\pi^{-}$ Pt(195), $\pi^{-}$ H	7	4.6	[48]
$\mathbf{SIACE120}$	DIC	$-\Delta u(107) = D$	01	Q 1	[60]
SLAC E139 DUIC DUENIY	-0	e Au(197), e D	21 20	8.4 6.0	[09]
MIIIO FIIEMIA	76 -	uAu(197), pp	20	0.9	[20]
CERN NMC 96	DIS	$\mu^{-}$ Pb(207), $\mu^{-}$ C(12)	15	4.1	[72]
CERN CMS $\star$	$\mathrm{W}^{\pm}$	pPb(208)	10	8.8	[43]
CERN CMS $\star$	$\mathbf{Z}$	pPb(208)	6	5.8	[45]
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