

$$\mathfrak{S}_6 = \text{Tr}(\text{Tr}^{a_1} \text{Tr}^{a_4}) \text{Tr}(\text{Tr}^{a_2} \text{Tr}^{a_3})$$