

$$\mathfrak{S}_5 = \text{Tr}(\text{Tr}^{a_1} \text{Tr}^{a_3}) \text{Tr}(\text{Tr}^{a_2} \text{Tr}^{a_4})$$