# **Neutrino Physics**

**Neutrino Oscillations in vacuum** 

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# Summary of what we learned from the last lecture

- Neutrinos are very weakly interacting fermions and are part of the SU2L doublet
- There are three "types" of neutrinos:  $u_e \, 
  u_\mu \, 
  u_ au$
- Electrically neutral fermion of the SM and there are no right-handed neutrinos in SM
- While we don't understand neutrinos very well they are omnipresent!



## Atmospheric neutrinos

 Neutrinos get produced via cosmic rays (accelerated protons, He) interacting with the atmosphere



## Atmospheric neutrinos

 1998 Super-Kamiokande experiment: 40 kton water cherenkov experiment detected atmospheric neutrinos



#### Atmospheric neutrinos





Exercise: What is the minimum energy a neutrino must have to create a charged lepton when it interactions with a neutron i.e.  $\nu_{\alpha}n \rightarrow p\ell_{\alpha}$  calculate this for each neutrino flavour

T2K could not "see" the tau neutrinos so it appears there is a deficit of muon neutrinos

Two neutrino oscillation

massive states: V, , V2, V3 interaction states: Ve, Vu, Ve

Neutrino Escillations Wet ye correct interaction Charged we can't know which wt ligentate was podued =) supton is described by Ue1\* N, NZ; N3 alinar superposition of Uez' V1, V2, V3 Uez\* Le presider i=1,2,3 flavor index X = R, H, Z

$$\begin{pmatrix} Ve \\ Vu \\ Ve \\ Ve \\ Ve \\ Ve \\ \end{pmatrix} = \begin{pmatrix} lle_1 \\ llu_2 \\ llu_2$$

1ve7= lle 1vi7+ lle21v27+ lle21v37

· IVe? propagates as a linear superposition until it is masured. then wou function collapses ) nections on measured as a flavour state. · the wave friction evolves in time due to the phone shift and this allow for v-oscillations is the phononenon of neutino flavour transformation.



$$\begin{array}{l} \left( \begin{array}{c} \text{Weutrino fscillations} \\ \left( \begin{array}{c} \text{W}_{1} \right) &= \left( \begin{array}{c} \text{Co} & -s \\ s & \text{Co} \end{array} \right) \left( \begin{array}{c} \text{W}_{1} \right) & \text{rewrite massive stats in terms of } \\ \text{flavor stats} \\ \text{flavor stats} \\ 14(L,t)^{2} &= \text{co} \left[ \left( \text{co} | \text{Ve} \right) - s \\ \text{o} | \text{Vu} \right) \right] e^{-i \left( 0 \right)} \\ &+ s \\ \text{so} \left[ s \\ \text{o} | \text{Ve} \right] + \left[ s \\ \text{so} | \text{co} | \text{ve} \right] + \left[ s \\ \text{so} | \text{co} | \text{ve} \right] \\ &+ \left[ s \\ \text{so} | \text{co} | \text{ve} \right] \\ \text{flux} \\ \text{flux}$$

$$P(Ve \rightarrow Vu) = |\langle Vu | \Psi(L_{+}) \rangle|^{2}$$

$$\langle vu | ve \rangle = 0 \qquad \langle vu | vu \rangle = 1$$

$$P(ve \rightarrow Vu) = co^{2} so^{2} (e^{-i\Delta q_{12}} - 1) (e^{i\Delta q_{12}} - 1)$$

$$use \quad 2\cos s \sin \theta = \sin 2\theta$$

$$P(ve \rightarrow vu) = \frac{\sin^{2} 2\theta}{4} (1 - e^{-i\Delta q_{12}}) (1\tau e^{i\Delta q_{12}})$$

$$use \quad e^{ix} = \cos x + i \sin x + s + \kappa uvrite;$$

$$P(ve \rightarrow vu) = \frac{\sin^{2} 2\theta}{4} sin^{2} (\Delta q_{12})$$

 $= [\vec{p}] \left( \frac{m_{1}^{2} - m_{1}^{2}}{2|\vec{p}|^{2}} \right) = \frac{m_{1}^{2} - m_{2}^{2}}{2|\vec{p}|^{2}}$ Since neutrinos are relativistic,  $E \approx |\vec{p}| \gg m_{1}, m_{2} \Rightarrow \Delta q_{12} = \left(\frac{m_{1}^{2} - m_{2}^{2}L}{2E}\right)$ P(Ve = vin 20 sin2 ( Drun L)

$$P(ve \rightarrow ve) = 1 - P(ve \rightarrow vn) = 1 - sin^2 20 sin^2 (\frac{0m_{12}^2L}{4E})$$

$$\begin{array}{rcl} P(Ve \Rightarrow Ve) &= \sin^{2} 20 & \sin^{2} \left( \frac{D^{2}nnL}{4E} \right) \\ P(Ve \Rightarrow Ve) &= 1 - P(Ve \Rightarrow Ven) = 1 - \sin^{2} 20 \sin^{2} \left( \frac{Dm^{2}nL}{4E} \right) \\ P(Ve \Rightarrow Ve) & is the probability Ve oscillate to  $v_{11} \\ P(Ve \Rightarrow Ve) & is the survival probability E consequence of unitarity of quantum mechanics] \\ The wave length of an oscillation is given by \\ Aosc [km] &= \frac{\pi}{16E} \frac{E[GeV]}{16F} \\ \end{array}$$$





Neutrino Escillations In general we can write an arbitrary unitary 3×3 matrix as:  $U = e \operatorname{diag}(e, e, l) CKU(\theta_{12}, \theta_{13}, \theta_{27}, \delta)$  $\operatorname{diag}(e^{ipe}, e^{ipu}, l)$  $\begin{array}{c} CEM = \left( \begin{array}{c} 1 & 0 & 0 \\ 0 & C_{23} & S_{23} \\ 0 & -S_{73} & C_{13} \end{array} \right) \left( \begin{array}{c} C_{13} & 0 & S_{13}e^{-i\delta} \\ 0 & ( & 0 \\ -S_{17}e^{i\delta} & 0 & C_{13} \end{array} \right) \left( \begin{array}{c} C_{12} & S_{12} & 0 \\ -S_{12} & C_{12} & 0 \\ 0 & 0 & 1 \end{array} \right) \end{array}$ ⇒ 9 real parameters: φ1, φ2, 0,2, 0,3, 023, δ ρε, ρμ, 4

The only "place" where U appears is in CC interactions (in neutral current interactions Ut & U appear one for V & V and by unitarity give the identity matrix)  $dc = -q \left[ \overline{v}_i \ U_{xi} \ \delta^{\mu} \left( 1 - \delta^{5} \right) d_{x} \ \omega_{\mu}^{\dagger} + h \cdot c \right]$ We can "rephase" ie just  $\begin{pmatrix} e \\ H \\ T \end{pmatrix}$ rotate by a global each generation of the charged lepsters -i(pe+4) -i(pu+4) $e \rightarrow e$   $\mu \rightarrow e$  M  $T \rightarrow Te^{-i4}$ 

This remove 3 of the 9 parametes and a further 2 phases can be removed by the Dirac neutrino man ferm 4 m 4 - If y Majorana particle cannot remove any phases & Q,, pr are physical phases. ie trey have an effect on physical observables.