

$Wb\bar{b}$ production at NNLO QCD

Heribertus Bayu Hartanto

based on work with: Simon Badger, Rene Poncelet,
Andrei Popescu and Simone Zoia

arXiv:2102.02516, arXiv:2205.01687, arXiv:2209.03280

QCD@LHC 2023, Durham
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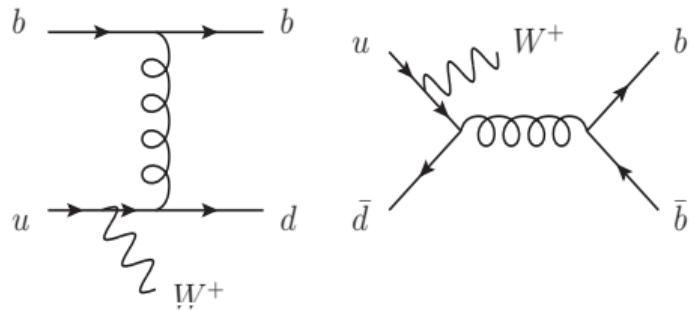


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$W + b$ jets



- ⇒ test perturbative QCD
- ⇒ modelling of flavoured jets
- ⇒ theoretical approach: 4FS vs 5FS
- $W + 1b$ jet: probe b quark PDFs
- $W + 2b$ jets: backgrounds for
 - Higgs-strahlung $pp \rightarrow WH(H \rightarrow b\bar{b})$
 - single top $pp \rightarrow bt(t \rightarrow bW)$

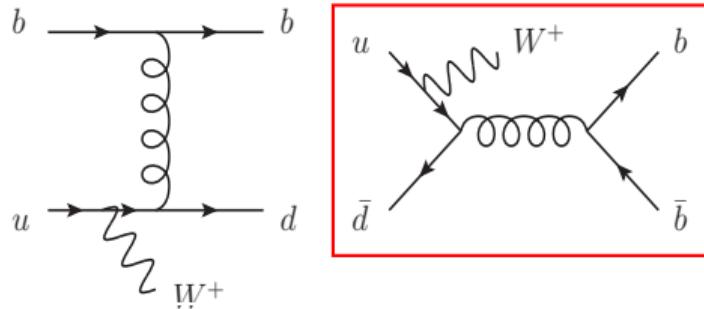
Measured at [Tevatron](#)_{[hep-ex/0410062][arXiv:1210.0627]} and [LHC](#)_{[arXiv:1109.1470][arXiv:1302.2929][arXiv:1312.6608][arXiv:1608.07561]}
talk by Vieri Candelise on Friday

Theoretical predictions available at NLO:

$W + 1b$: [Campbell,Ellis,Maltoni,Willenbrock(2006)][Campbell,Ellis,Febres Cordero,Maltoni,Reina,Wackerlo,Willebroek(2008)]
[Caola,Campbell,Febres Cordero,Reina,Wackerlo(2011)]

$W + 2b$: $m_b = 0$ [Ellis,Veseli(1999)], onshell W [Febres Cordero,Reina,Wackerlo(2006,2009)], $W(\ell\nu)b\bar{b}$ [Badger,Campbell,Ellis(2010)]
NLO+PS [Oleari,Reina(2011)][Frederix et al(2011)], $W(\ell\nu)b\bar{b}j$ [Luisoni,Oleari,Tramontano(2015)]
 $W(\ell\nu)b\bar{b} + \leq 3j$ [Anger,Febres Corder,Ita,Sotnikov(2018)]

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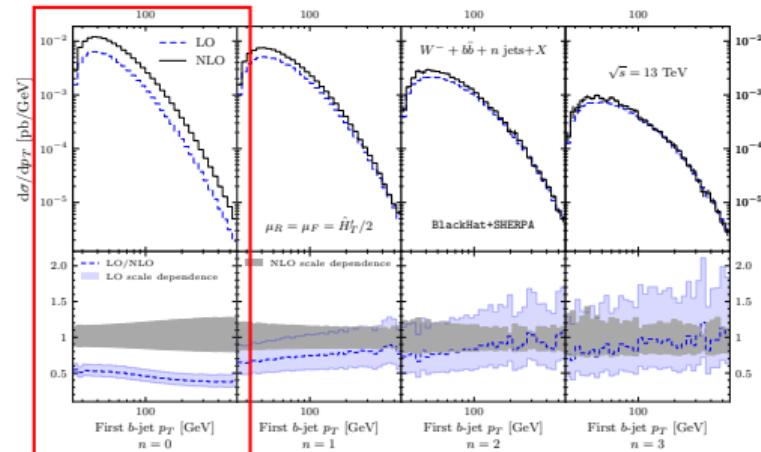
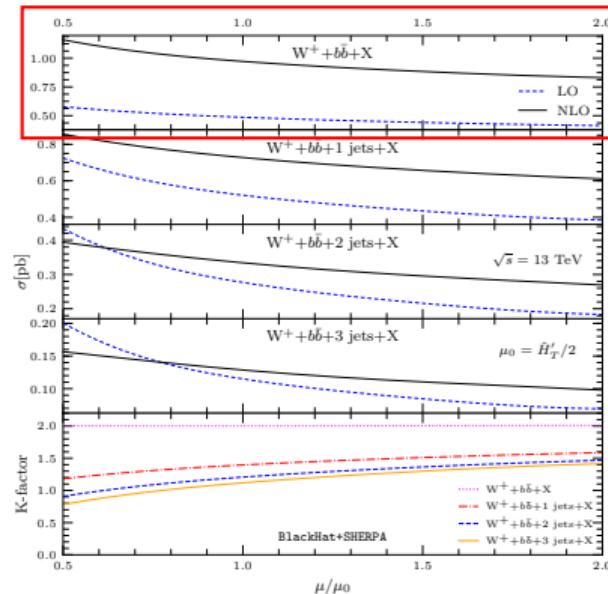
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$Wb\bar{b} + \text{jets}$ production at NLO QCD

[Anger, Febres Cordero, Ita, Sotnikov(2017)]



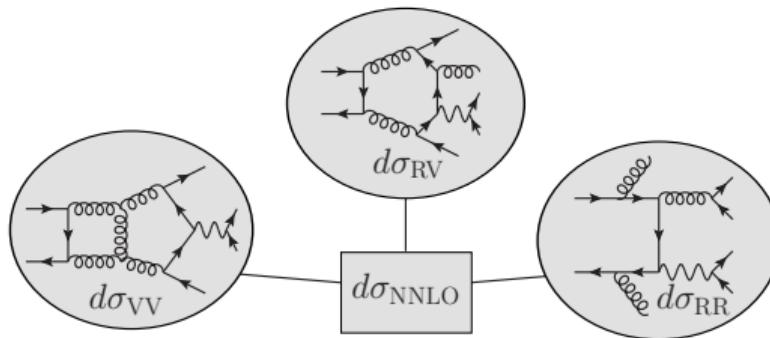
- ⇒ $Wb\bar{b} + X$ (inclusive, $n = 0$): large NLO corrections, large NLO scale dependence
- ⇒ due opening of qg channel at NLO

NNLO QCD corrections to $Wb\bar{b}$ production is required!

NNLO QCD corrections to $W(\rightarrow \ell\nu)b\bar{b}$ production

NNLO QCD calculation for $W + 2b$ -jets: massless b (5FS) [HBH, Poncelet, Popescu, Zoia(2022)]

massive b (4FS) [Buonocore, Devoto, Kallweit, Mazzitelli, Rottoli, Savoini(2022)]

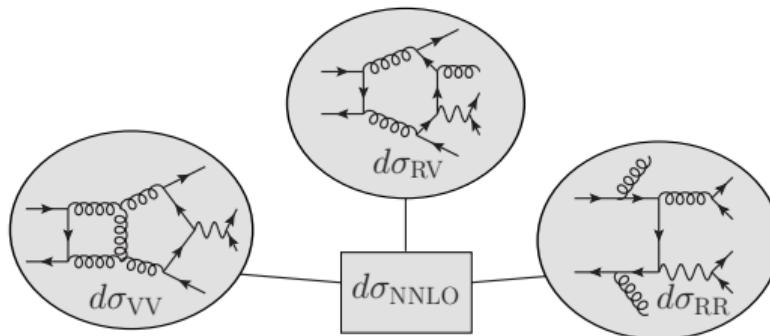


- Amplitudes:
 - ▶ Tree-level $pp \rightarrow W(\rightarrow \ell\nu)b\bar{b}jj$: AvH [Bury, van Hameren(2015)]
 - ▶ 1-loop $pp \rightarrow W(\rightarrow \ell\nu)b\bar{b}j$: OPENLOOPs [Bucionni, Lang, Lindert, Maierhoefer, Pozzorini, Zhang, Zoller(2018,2019)]
 - ▶ 2-loop $u\bar{d} \rightarrow W(\rightarrow \ell\nu)b\bar{b}$: [Abreu, Febres Cordero, Ita, Klinkert, Page(2021)][HBH, Poncelet, Popescu, Zoia(2022)]
- NNLO subtraction scheme: Sector Improved Residue Subtraction Scheme (STRIPPER)
[Czakon(2010)][Czakon, Heymes(2014)]

NNLO QCD corrections to $W(\rightarrow \ell\nu)b\bar{b}$ production

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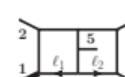
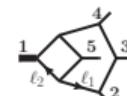
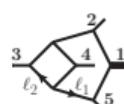
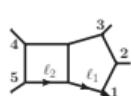
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Two-Loop Scattering Amplitude

$2 \rightarrow 3$ scattering with an off-shell leg at two loops

talk by Federica Devoto on Monday on massless 2-loop 5-point amplitudes

- ▶ Multi-loop scattering amplitude: $A^{(2)} = c(\epsilon, \{p\}) \text{ MI}(\epsilon, \{p\})$
- ▶ All two-loop master integrals are known!!!



[Papadopoulos, Tommasini, Wever(2015)] [Papadopoulos, Wever(2019)] [Abreu, Ita, Moriello, Page, Tschernow, Zeng(2020)]

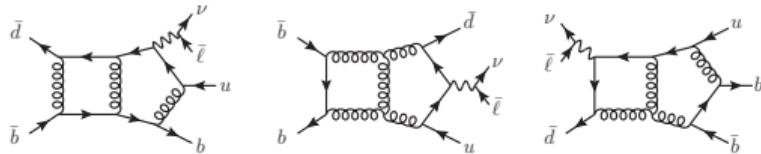
[Canko, Papadopoulos, Syrrakos(2020)] [Syrrakos(2020)][[Abreu, Ita, Page, Tschernow(2021)] [Kardos, Papadopoulos, Smirnov, Syrrakos, Wever(2022)]
[Abreu, Chicherin, Ita, Page, Sotnikov, Tschernow, Zoia(2023)]]

⇒ Pentagon function basis ⇒ fast numerical evaluation available
[Chicherin, Sotnikov, Zoia(2021)][[Abreu, Chicherin, Ita, Page, Sotnikov, Tschernow, Zoia(2023)]]

- ▶ Several two-loop QCD amplitudes known analytically at **leading colour**
 - $pp \rightarrow W b\bar{b}$, $pp \rightarrow W^+ (\rightarrow \ell\nu) b\bar{b}$, $pp \rightarrow H b\bar{b}$ (massless b)
[Badger, HBH, Zoia(2021)][Badger, HBH, Krys, Zoia(2021)][HBH, Poncelet, Popescu, Zoia(2022)]
 - $pp \rightarrow W/Z + jj$ [Abreu, Febres Cordero, Ita, Klinkert, Page(2021)] $pp \rightarrow W^+ (\rightarrow \ell\nu) \gamma j$ [Badger, HBH, Krys, Zoia(2022)]
- Towards full colour amplitudes: determination of **coefficients** extremely complicated
⇒ extremely large algebraic expressions and huge integral reduction tables!!!

$u\bar{d} \rightarrow W^+(\rightarrow \ell\nu) b\bar{b}$ at two loops

[Badger,HBH,Zoia(2021)][HBH,Poncelet,Popescu,Zoia(2022)]

⇒ leading colour approximation and massless b quark

⇒ compute squared matrix element

$$\sum \mathcal{M}^{(0)*} \mathcal{M}^{(2)} = M_{\text{even}}^{(2)} + \text{tr}_5 M_{\text{odd}}^{(2)}$$

$$\text{tr}_5 = 4i\epsilon_{\mu\nu\rho\sigma} p_1^\mu p_2^\nu p_3^\rho p_4^\sigma$$

employ CDR+Larin scheme to treat γ_5 .⇒ Incorporating $W \rightarrow \ell\nu$ decay

$$M_6^{(L)} = \sum_{\text{spin}} A_6^{(0)\dagger} A_6^{(L)} = M_5^{(L)\mu\nu} \mathcal{D}_{\mu\nu} |P(s_{56})|^2$$

$$M_5^{(L)\mu\nu} = \sum_{i=1}^{16} a_i^{(L)} v_i^{\mu\nu} \quad v_i^{\mu\nu} \in \{p_1^\mu, p_2^\mu, p_3^\mu, p_W^\mu\}$$

Derive analytic expressions of the finite remainders using finite-field reconstruction method

talk by Xiao Liu on Tuesday on analytic reconstruction method

QGRAF[Nogueira], FORM[Vermaseren], LiteRed[Lee],
FiniteFlow[Peraro], Mathematica

$$M_k^{(2)}(\{p\}, \epsilon) = \sum_i c_{k,i}(\{p\}, \epsilon) \mathcal{I}_{k,i}(\{p\}, \epsilon)$$

↓ IBP reduction

$$M_k^{(2)}(\{p\}, \epsilon) = \sum_i d_{k,i}(\{p\}, \epsilon) \text{MI}_{k,i}(\{p\}, \epsilon)$$

↓ map to pentagon function basis

↓ subtract UV/IR poles

↓ ϵ expansion

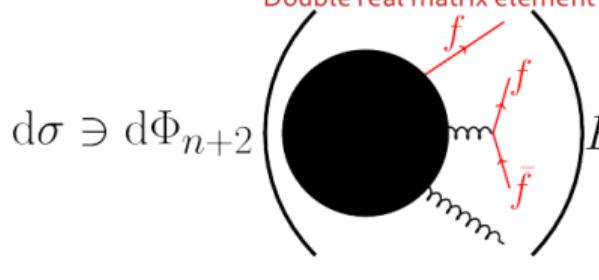
$$F_k^{(2)}(\{p\}) = \sum_i e_{k,i}(\{p\}) m_{k,i}(f) + \mathcal{O}(\epsilon)$$

Numerical Results

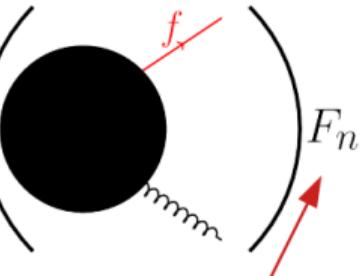
Fixed-order flavoured jets beyond NLO

Example NNLO: double real radiation and subtraction

Double real matrix element



Double soft subtraction term:
Double soft function * tree ME



Mistreatment of flavour pair in $F_{n+2} \Rightarrow$ mismatch w.r.t $F_n \Rightarrow$ double soft singularity not subtracted

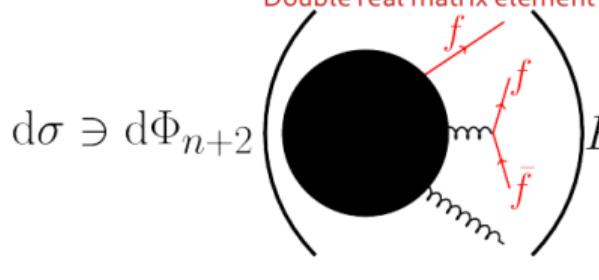
Solutions:

- ▶ Flavour- k_T jet algorithm [Banfi,Salam,Zanderighi(2006)] → data/theory comparison requires unfolding
- ▶ Practical jet flavour through NNLO [Caletti,Larkoski,Marzani,Reichelt(2022)]
- ▶ Infrared-safe flavoured anti- k_T jets [Czakon,Mitov,Poncelet(2022)]
- ▶ A dress of flavour to suit any jet [Gauld,Huss,Stagnitto(2022)]
- ▶ Flavoured jets with exact anti- k_T kinematics [Caola,Grabarczyk,Hutt,Salam,Scyboz,Thaler(2023)]

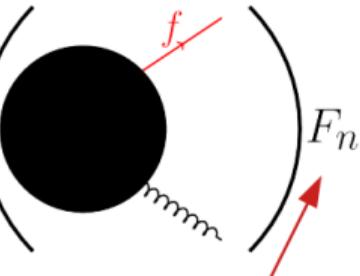
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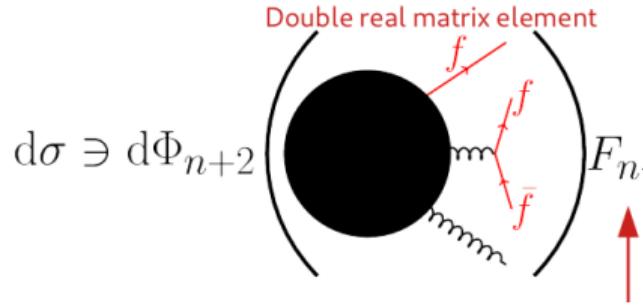
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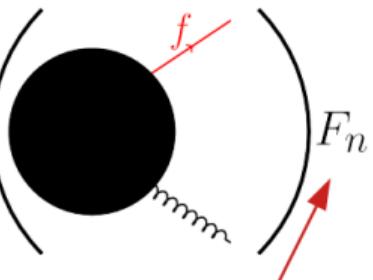
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Example NNLO: double real radiation and subtraction



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Infrared-safe flavoured anti- k_T jet algorithm [Czakon, Mitov, Poncelet (2022)]

\Rightarrow introduce damping function to the standard anti- k_T

$$S_{ij} = 1 - \Theta(1 - x) \cdot \cos\left(\frac{\pi}{2}x\right) \leq 1 \quad x \equiv \frac{1}{a} \frac{k_{T,i}^2 + k_{T,j}^2}{2k_{T,\max}^2}$$

if i, j have the same non-zero flavour of opposite sign, a : tunable softness parameter

\Rightarrow minimize the effect of unfolding

Setup (follows CMS measurement [arXiv:1608.07561])

- ⇒ **5FS**, LHC 8 TeV, PDFs: NNPDF31, cuts: $p_{T,\ell} > 30 \text{ GeV}$, $|\eta_\ell| < 2.1$, $p_{T,j} > 25 \text{ GeV}$, $|\eta_j| < 2.4$
- ⇒ **jet algorithm**: flavour- k_T [Banfi, Salam, Zanderighi (2006)] and flavour anti- k_T [Czakon, Mitov, Poncelet (2022)] with $R = 0.5$
- ⇒ central scale: $\mu_R = \mu_F = \mu_0$, where $H_T = E_T(\ell\nu) + p_T(b_1) + p_T(b_2)$.
- ⇒ final states: **inclusive** (at least 2 b jets) and **exclusive** (exactly two b jets and no other jets).
- ⇒ scale uncertainties: **inclusive** → 7-pt variation $1/2 \leq \mu_R/\mu_F \leq 2$
exclusive → 7-pt variation and uncorrelated prescription [Stewart, Tackmann (2012)]

Uncorrelated scale variation $\sigma_{Wb\bar{b},\text{exc}} = \sigma_{Wb\bar{b},\text{inc}} - \sigma_{Wbbj,\text{inc}}$ $\Delta\sigma_{Wb\bar{b},\text{exc}} = \sqrt{\left(\Delta\sigma_{Wb\bar{b},\text{inc}}\right)^2 + \left(\Delta\sigma_{Wbbj,\text{inc}}\right)^2}$

Leading colour approximation is only applied to **scale independent** double virtual finite remainder

$$\mathcal{V}^{(2)}(\mu_R^2) = \mathcal{V}_{\text{LC}}^{(2)}(s_{12}) + \sum_{i=1}^4 c_i \ln^i \left(\frac{\mu_R^2}{s_{12}} \right)$$

Double virtual contributions to σ : **5% (inc)** and **10% (exc)**, expected SLC: **0.5% (inc)** and **1% (exc)**

Numerical results: cross sections

$$K_{\text{NLO}} = \frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}}$$

$$K_{\text{NNLO}} = \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}$$

Inclusive $W^+(\rightarrow \ell^+ \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{LO} [fb]	σ_{NLO} [fb]	K_{NLO}	σ_{NNLO} [fb]	K_{NNLO}
flavour- k_T	$213.24(8)^{+21.4\%}_{-16.1\%}$	$362.0(6)^{+13.7\%}_{-11.4\%}$	1.70	$445(5)^{+6.7\%}_{-7.0\%}$	1.23
flavour anti- k_T ($a = 0.05$)	$262.52(10)^{+21.4\%}_{-16.1\%}$	$500.9(8)^{+16.1\%}_{-12.8\%}$	1.91	$690(7)^{+10.9\%}_{-9.7\%}$	1.38
flavour anti- k_T ($a = 0.1$)	$262.47(10)^{+21.4\%}_{-16.1\%}$	$497.8(8)^{+16.0\%}_{-12.7\%}$	1.90	$677(7)^{+10.4\%}_{-9.4\%}$	1.36
flavour anti- k_T ($a = 0.2$)	$261.71(10)^{+21.4\%}_{-16.1\%}$	$486.3(8)^{+15.5\%}_{-12.5\%}$	1.86	$647(7)^{+9.5\%}_{-8.9\%}$	1.33

Exclusive $W^\pm(\rightarrow \ell^\pm \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{LO} [fb]	σ_{NLO} [fb]	K_{NLO}	σ_{NNLO} [fb]	K_{NNLO}
flavour- k_T	$345.97(9)^{+21.4\%}_{-16.2\%}$	$408.4(5)^{+4.2\% \ (41\%)}_{-6.2\% \ (28\%)}$	1.18	$434(8)^{+1.7\% \ (16\%)}_{-2.5\% \ (16\%)}$	1.06
flavour anti- k_T ($a = 0.05$)	$425.71(12)^{+21.5\%}_{-16.2\%}$	$540.3(7)^{+6.2\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$636(11)^{+5.4\% \ (23\%)}_{-5.0\% \ (20\%)}$	1.18
flavour anti- k_T ($a = 0.1$)	$425.63(12)^{+21.5\%}_{-16.2\%}$	$538.7(7)^{+6.1\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$630(10)^{+5.0\% \ (22\%)}_{-4.8\% \ (20\%)}$	1.17
flavour anti- k_T ($a = 0.2$)	$424.37(12)^{+21.5\%}_{-16.2\%}$	$530.6(7)^{+5.8\% \ (42\%)}_{-7.2\% \ (29\%)}$	1.25	$606(10)^{+4.2\% \ (21\%)}_{-4.2\% \ (19\%)}$	1.14

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flavour anti- k_T ($a = 0.05$)	425.71(12) $\begin{array}{l} +21.5\% \\ -16.2\% \end{array}$	540.3(7) $\begin{array}{l} +6.2\% \ (42\%) \\ -7.4\% \ (29\%) \end{array}$	1.27	636(11) $\begin{array}{l} +5.4\% \ (23\%) \\ -5.0\% \ (20\%) \end{array}$	1.18
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flavour anti- k_T ($a = 0.2$)	$261.71(10)^{+21.4\%}_{-16.1\%}$	$486.3(8)^{+15.5\%}_{-12.5\%}$	1.86	$647(7)^{+9.5\%}_{-8.9\%}$	1.33

Exclusive $W^\pm(\rightarrow \ell^\pm \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{LO} [fb]	σ_{NLO} [fb]	K_{NLO}	σ_{NNLO} [fb]	K_{NNLO}
flavour- k_T	$345.97(9)^{+21.4\%}_{-16.2\%}$	$408.4(5)^{+4.2\% \ (41\%)}_{-6.2\% \ (28\%)}$	1.18	$434(8)^{+1.7\% \ (16\%)}_{-2.5\% \ (16\%)}$	1.06
flavour anti- k_T ($a = 0.05$)	$425.71(12)^{+21.5\%}_{-16.2\%}$	$540.3(7)^{+6.2\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$636(11)^{+5.4\% \ (23\%)}_{-5.0\% \ (20\%)}$	1.18
flavour anti- k_T ($a = 0.1$)	$425.63(12)^{+21.5\%}_{-16.2\%}$	$538.7(7)^{+6.1\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$630(10)^{+5.0\% \ (22\%)}_{-4.8\% \ (20\%)}$	1.17
flavour anti- k_T ($a = 0.2$)	$424.37(12)^{+21.5\%}_{-16.2\%}$	$530.6(7)^{+5.8\% \ (42\%)}_{-7.2\% \ (29\%)}$	1.25	$606(10)^{+4.2\% \ (21\%)}_{-4.2\% \ (19\%)}$	1.14

Numerical results: cross sections

$$K_{\text{NLO}} = \frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}}$$

$$K_{\text{NNLO}} = \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}$$

Inclusive $W^+(\rightarrow \ell^+ \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{LO} [fb]	σ_{NLO} [fb]	K_{NLO}	σ_{NNLO} [fb]	K_{NNLO}
flavour- k_T	$213.24(8)^{+21.4\%}_{-16.1\%}$	$362.0(6)^{+13.7\%}_{-11.4\%}$	1.70	$445(5)^{+6.7\%}_{-7.0\%}$	1.23
flavour anti- k_T ($a = 0.05$)	$262.52(10)^{+21.4\%}_{-16.1\%}$	$500.9(8)^{+16.1\%}_{-12.8\%}$	1.91	$690(7)^{+10.9\%}_{-9.7\%}$	1.38
flavour anti- k_T ($a = 0.1$)	$262.47(10)^{+21.4\%}_{-16.1\%}$	$497.8(8)^{+16.0\%}_{-12.7\%}$	1.90	$677(7)^{+10.4\%}_{-9.4\%}$	1.36
flavour anti- k_T ($a = 0.2$)	$261.71(10)^{+21.4\%}_{-16.1\%}$	$486.3(8)^{+15.5\%}_{-12.5\%}$	1.86	$647(7)^{+9.5\%}_{-8.9\%}$	1.33

Exclusive $W^\pm(\rightarrow \ell^\pm \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{LO} [fb]	σ_{NLO} [fb]	K_{NLO}	σ_{NNLO} [fb]	K_{NNLO}
flavour- k_T	$345.97(9)^{+21.4\%}_{-16.2\%}$	$408.4(5)^{+4.2\% \ (41\%)}_{-6.2\% \ (28\%)}$	1.18	$434(8)^{+1.7\% \ (16\%)}_{-2.5\% \ (16\%)}$	1.06
flavour anti- k_T ($a = 0.05$)	$425.71(12)^{+21.5\%}_{-16.2\%}$	$540.3(7)^{+6.2\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$636(11)^{+5.4\% \ (23\%)}_{-5.0\% \ (20\%)}$	1.18
flavour anti- k_T ($a = 0.1$)	$425.63(12)^{+21.5\%}_{-16.2\%}$	$538.7(7)^{+6.1\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$630(10)^{+5.0\% \ (22\%)}_{-4.8\% \ (20\%)}$	1.17
flavour anti- k_T ($a = 0.2$)	$424.37(12)^{+21.5\%}_{-16.2\%}$	$530.6(7)^{+5.8\% \ (42\%)}_{-7.2\% \ (29\%)}$	1.25	$606(10)^{+4.2\% \ (21\%)}_{-4.2\% \ (19\%)}$	1.14

Numerical results: cross sections

$$K_{\text{NLO}} = \frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}}$$

$$K_{\text{NNLO}} = \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}$$

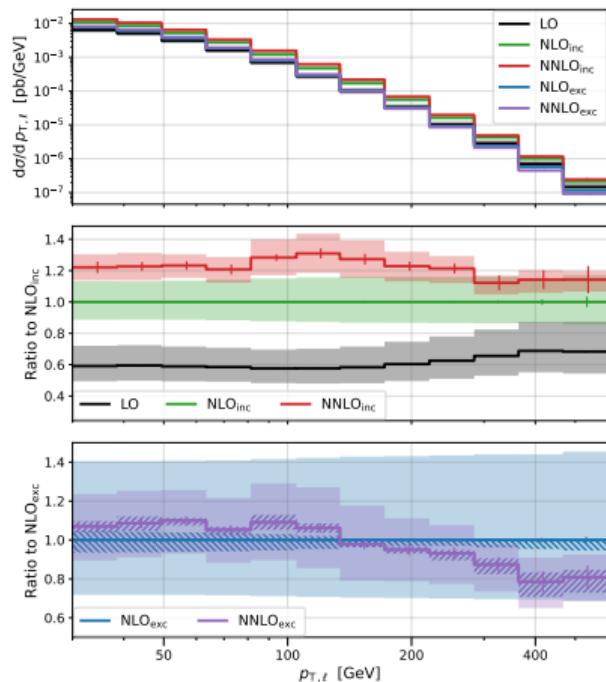
Inclusive $W^+(\rightarrow \ell^+ \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{LO} [fb]	σ_{NLO} [fb]	K_{NLO}	σ_{NNLO} [fb]	K_{NNLO}
flavour- k_T	$213.24(8)^{+21.4\%}_{-16.1\%}$	$362.0(6)^{+13.7\%}_{-11.4\%}$	1.70	$445(5)^{+6.7\%}_{-7.0\%}$	1.23
flavour anti- k_T ($a = 0.05$)	$262.52(10)^{+21.4\%}_{-16.1\%}$	$500.9(8)^{+16.1\%}_{-12.8\%}$	1.91	$690(7)^{+10.9\%}_{-9.7\%}$	1.38
flavour anti- k_T ($a = 0.1$)	$262.47(10)^{+21.4\%}_{-16.1\%}$	$497.8(8)^{+16.0\%}_{-12.7\%}$	1.90	$677(7)^{+10.4\%}_{-9.4\%}$	1.36
flavour anti- k_T ($a = 0.2$)	$261.71(10)^{+21.4\%}_{-16.1\%}$	$486.3(8)^{+15.5\%}_{-12.5\%}$	1.86	$647(7)^{+9.5\%}_{-8.9\%}$	1.33

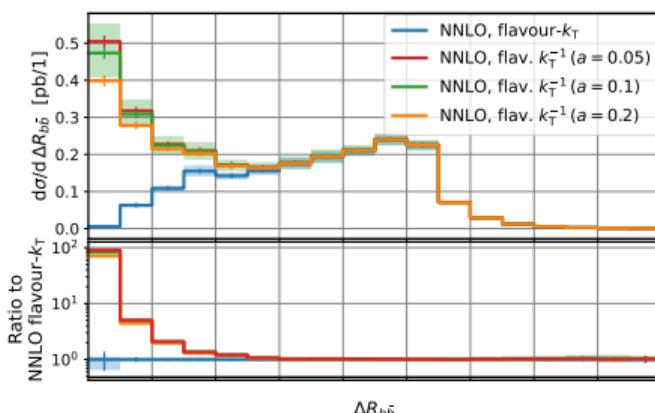
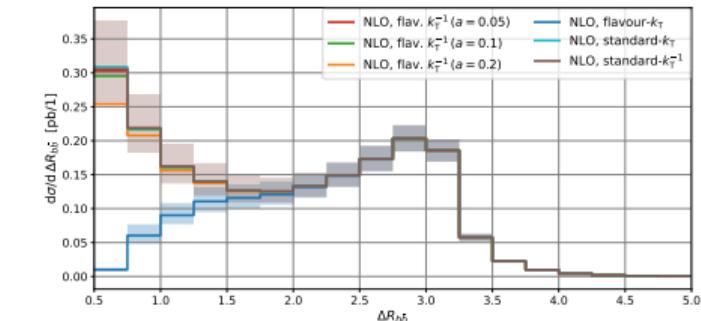
Exclusive $W^\pm(\rightarrow \ell^\pm \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{LO} [fb]	σ_{NLO} [fb]	K_{NLO}	σ_{NNLO} [fb]	K_{NNLO}
flavour- k_T	$345.97(9)^{+21.4\%}_{-16.2\%}$	$408.4(5)^{+4.2\% \ (41\%)}_{-6.2\% \ (28\%)}$	1.18	$434(8)^{+1.7\% \ (16\%)}_{-2.5\% \ (16\%)}$	1.06
flavour anti- k_T ($a = 0.05$)	$425.71(12)^{+21.5\%}_{-16.2\%}$	$540.3(7)^{+6.2\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$636(11)^{+5.4\% \ (23\%)}_{-5.0\% \ (20\%)}$	1.18
flavour anti- k_T ($a = 0.1$)	$425.63(12)^{+21.5\%}_{-16.2\%}$	$538.7(7)^{+6.1\% \ (42\%)}_{-7.4\% \ (29\%)}$	1.27	$630(10)^{+5.0\% \ (22\%)}_{-4.8\% \ (20\%)}$	1.17
flavour anti- k_T ($a = 0.2$)	$424.37(12)^{+21.5\%}_{-16.2\%}$	$530.6(7)^{+5.8\% \ (42\%)}_{-7.2\% \ (29\%)}$	1.25	$606(10)^{+4.2\% \ (21\%)}_{-4.2\% \ (19\%)}$	1.14

Numerical results: differential distributions



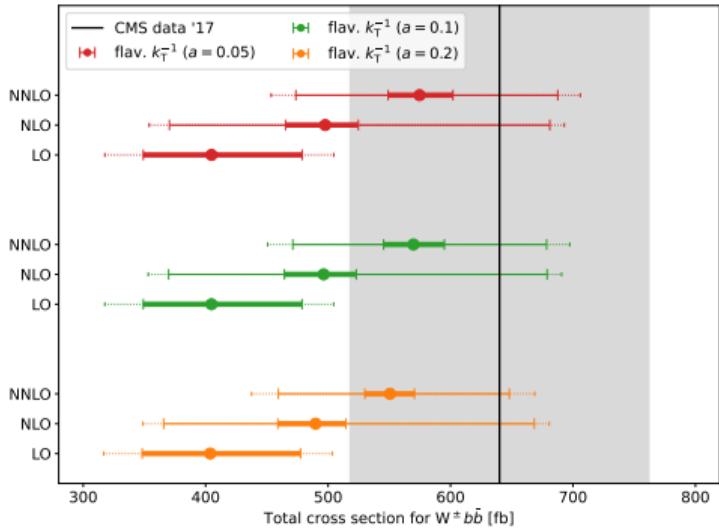
$W^+ \rightarrow \ell^+ \nu b\bar{b}$ with flavour- k_T



inclusive $W^+ \rightarrow \ell^+ \nu b\bar{b}$

Comparison to CMS data [arXiv:1608.07561]

- ▶ CMS measurement is done for exclusive final state configuration
- ▶ The use of flavour anti- k_T algorithm in theoretical calculation allows for close comparison with CMS data (standard anti- k_T)
⇒ unfolding corrections expected to be small
- ▶ Correction factors included:
hadronisation (multiplicative) = 0.81 ± 0.07
DPI (additive) = 0.06 ± 0.06 pb
- ▶ **Thick bands:** 7-pt scale variation (without DPI error)
thin bands: uncorrelated prescription (without DPI error),
dotted bands: uncorrelated prescription (with DPI error)



[HBH,Poncelet,Popescu,Zoia;arXiv:2209.03280]

$Wb\bar{b}$: 4FS vs 5FS comparison

NNLO QCD calculation for W $b\bar{b}$ with massive b quark (4FS) [Buonocore,Devoto,Kallweit,Mazzitelli,Rottoli,Savoini(2022)]

- ▶ main bottleneck: two-loop matrix element is still out of reach \Rightarrow use massification procedure
[Mitov,Moch(2007)]

$$\mathcal{M}^{Wb\bar{b},(m)} = \prod_{i \in b,\bar{b}} \left(Z_{[i]}^{(m|0)} \right)^{\frac{1}{2}} \mathcal{M}^{Wb\bar{b},(m=0)} + \mathcal{O}(m^k)$$

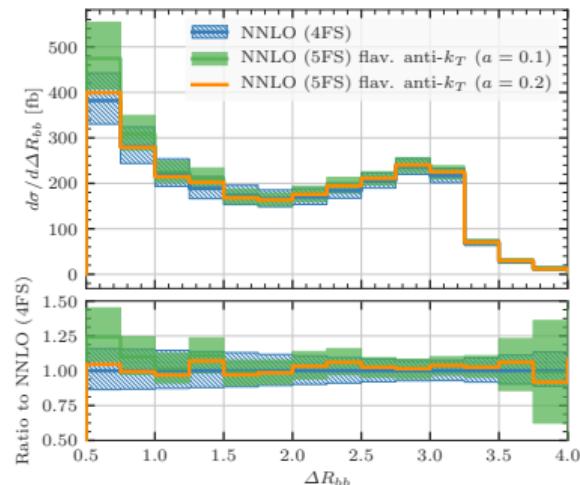
predicts poles, $\log(m)$ and mass independent terms but not m^k and heavy quark loops

talk by Simone Devoto on Friday

- ▶ b -quark mass regulates IR divergencies in the double soft limit
 \Rightarrow can use standard anti- k_T jet algorithm
- ▶ massless (5FS) vs massive (4FS) comparison

order	$\sigma^{4\text{FS}}$ [fb]	$\sigma_{a=0.05}^{5\text{FS}}$ [fb]	$\sigma_{a=0.1}^{5\text{FS}}$ [fb]	$\sigma_{a=0.2}^{5\text{FS}}$ [fb]
LO	210.42(2) $^{+21.4\%}_{-16.2\%}$	262.52(10) $^{+21.4\%}_{-16.1\%}$	262.47(10) $^{+21.4\%}_{-16.1\%}$	261.71(10) $^{+21.4\%}_{-16.1\%}$
NLO	468.01(5) $^{+17.8\%}_{-13.8\%}$	500.9(8) $^{+16.1\%}_{-12.8\%}$	497.8(8) $^{+16.0\%}_{-12.7\%}$	486.3(8) $^{+15.5\%}_{-12.5\%}$
NNLO	636.4(1.6) $^{+11.9\%}_{-10.5\%}$	690(7) $^{+10.9\%}_{-9.7\%}$	677(7) $^{+10.4\%}_{-9.4\%}$	647(7) $^{+9.5\%}_{-9.4\%}$

Table and Figure from [Buonocore,Devoto,Kallweit,Mazzitelli,Rottoli,Savoini(2022)]



Summary

Summary & Outlooks

Summary:

- ✓ NNLO QCD predictions for $W(\rightarrow \ell\nu)b\bar{b}$ production at the LHC
 - ⇒ improved perturbative convergence
 - ⇒ better agreement with CMS measurements
- ✓ Comparison between 4FS and 5FS calculations
- ✓ Two-loop amplitude for 5-point process with one external mass (at leading colour)

Outlooks:

- ▶ Full colour two-loop amplitude
- ▶ $W + 1b$ jet at NNLO QCD ⇒ comparison with data, 4FS vs 5FS
- ▶ NNLO+PS matching for the massive $Wb\bar{b}$ calculation [talk by Emanuele Re on Monday](#)

Back-up Slides

NNLO vs NLO-merged calculation

$$K_{\text{NNLO}} = \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}$$

$$K_{\text{NLO+}} = \frac{\sigma_{\text{NLO+}}}{\sigma_{\text{NLO}}}$$

Inclusive $W^+(\rightarrow \ell^+ \nu) b\bar{b}$ cross sections

Jet algorithm	σ_{NLO} [fb]	σ_{NNLO} [fb]	K_{NNLO}	$\sigma_{\text{NLO+}}$ [fb]	$K_{\text{NLO+}}$
flavour- k_T	$362.0(6)^{+13.7\%}_{-11.4\%}$	$445(5)^{+6.7\%}_{-7.0\%}$	1.23	$426(5)^{+7.6\%}_{-8.9\%}$	1.18
flavour anti- k_T ($a = 0.05$)	$500.9(8)^{+16.1\%}_{-12.8\%}$	$690(7)^{+10.9\%}_{-9.7\%}$	1.38	$635(6)^{+11.2\%}_{-11.1\%}$	1.27
flavour anti- k_T ($a = 0.1$)	$497.8(8)^{+16.0\%}_{-12.7\%}$	$677(7)^{+10.4\%}_{-9.4\%}$	1.36	$626(6)^{+10.8\%}_{-10.9\%}$	1.26
flavour anti- k_T ($a = 0.2$)	$486.3(8)^{+15.5\%}_{-12.5\%}$	$647(7)^{+9.5\%}_{-8.9\%}$	1.33	$602(6)^{+10.2\%}_{-10.5\%}$	1.24

Large corrections and scale dep at NLO

$\Rightarrow qg(\bar{q}g) \rightarrow Wb\bar{b}q(\bar{q})$ subprocess

\Rightarrow upgrade $pp \rightarrow Wb\bar{b}j$ to NLO

[Luisoni,Oleari,Tramontano(2015)]

Combine $Wb\bar{b}$ and $Wb\bar{b}j$ NLO cross sections using *exclusive sums* method

[The SM and NLO Multileg and SM MC Working Groups:

Summary Report(2012)]

[Anger,Febres Cordero,Ita,Sotnikov(2017)]

$$\sigma_{\text{NLO+}, Wb\bar{b}, \text{inc}} = \sigma_{\text{NLO}, Wb\bar{b}, \text{exc}} + \sigma_{\text{NLO}, Wb\bar{b}j, \text{inc}}$$

