



A grayscale background image showing a complex array of detector components, likely the LHCb experiment's silicon vertex detector, with various wires and chambers visible.

# Latest exotic spectroscopy results from LHCb

Chen Chen

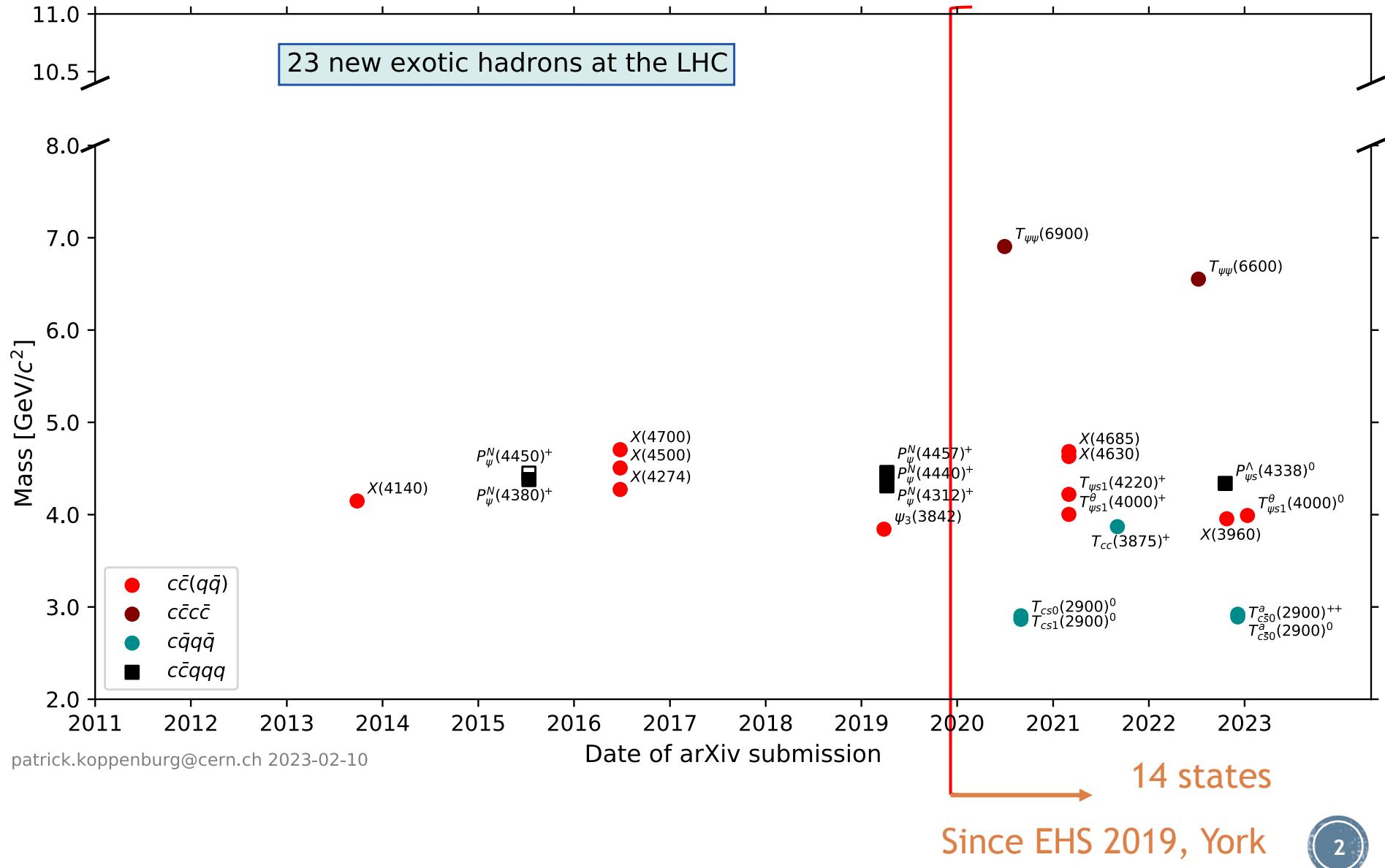
Aix Marseille Univ, CNRS/IN2P3, CPPM, Marseille, France



Exotic Hardon Spectroscopy 2023

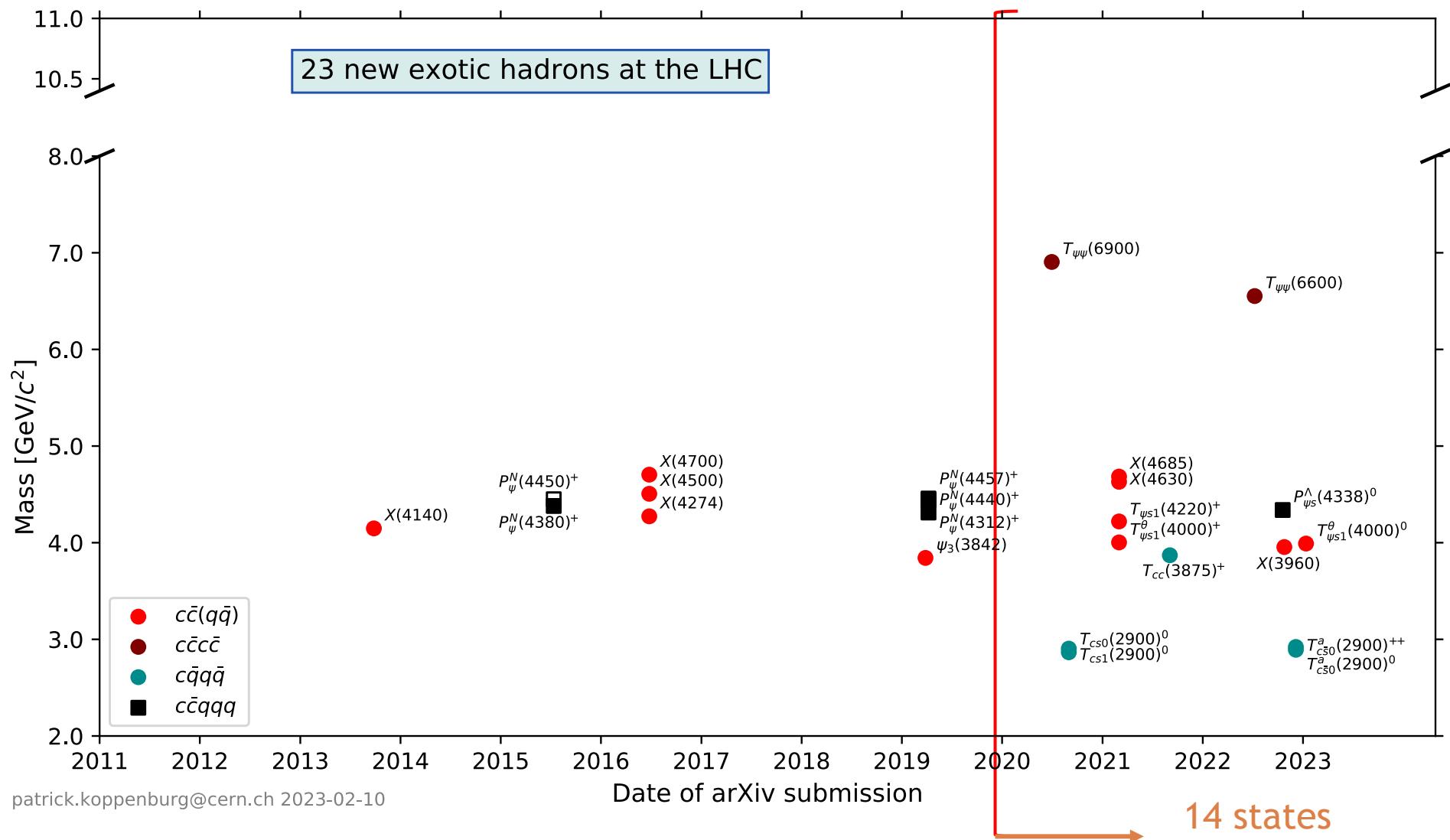
20 Apr. 2023, Durham

# Exotic hadrons at LHC

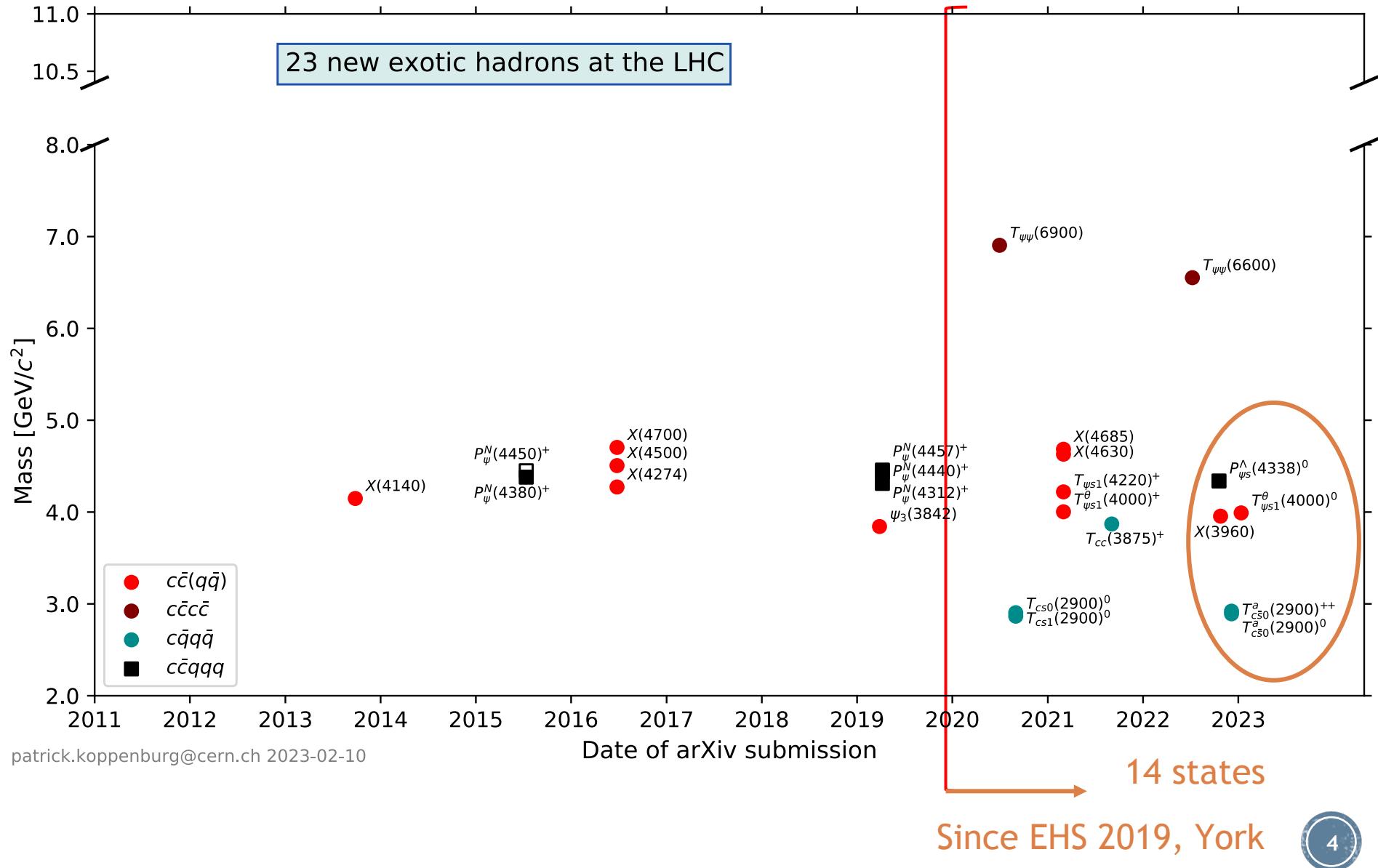


# Exotic hadrons at LHC

I'd like to cover all the 14 states,  
which this talk is too short to contain



# Exotic hadrons at LHC

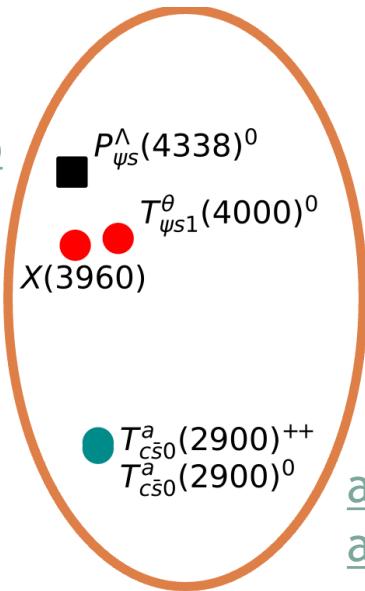


# LHCb results in this talk

- New exotic hadrons

[arXiv:2210.10346](https://arxiv.org/abs/2210.10346)

[arXiv:2210.15153](https://arxiv.org/abs/2210.15153)  
[arXiv:2211.05034](https://arxiv.org/abs/2211.05034)



[arXiv:2301.04899](https://arxiv.org/abs/2301.04899)

[arXiv:2212.02717](https://arxiv.org/abs/2212.02717)  
[arXiv:2212.02716](https://arxiv.org/abs/2212.02716)

- Observations of new decays

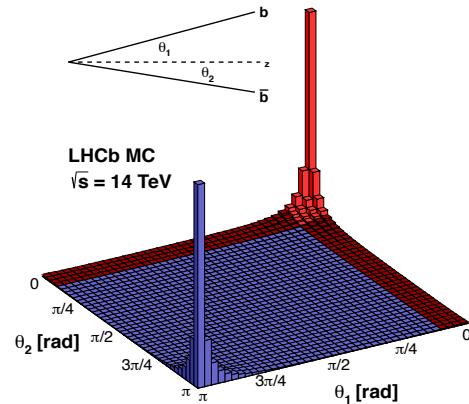
- $B^+ \rightarrow J/\psi \eta' K^+$  [[arXiv:2303.09443](https://arxiv.org/abs/2303.09443)]
- $B_s^0 \rightarrow \chi_{c1}(3872) \pi^+ \pi^-$  [[arXiv:2302.10629](https://arxiv.org/abs/2302.10629)]

# LHCb experiment

JINST 3 (2008) S08005, Int.J.Mod.Phys. A30 (2015) 1530022

- Dedicated for precise and efficient heavy-hadron reconstruction
  - Single-arm and forward design

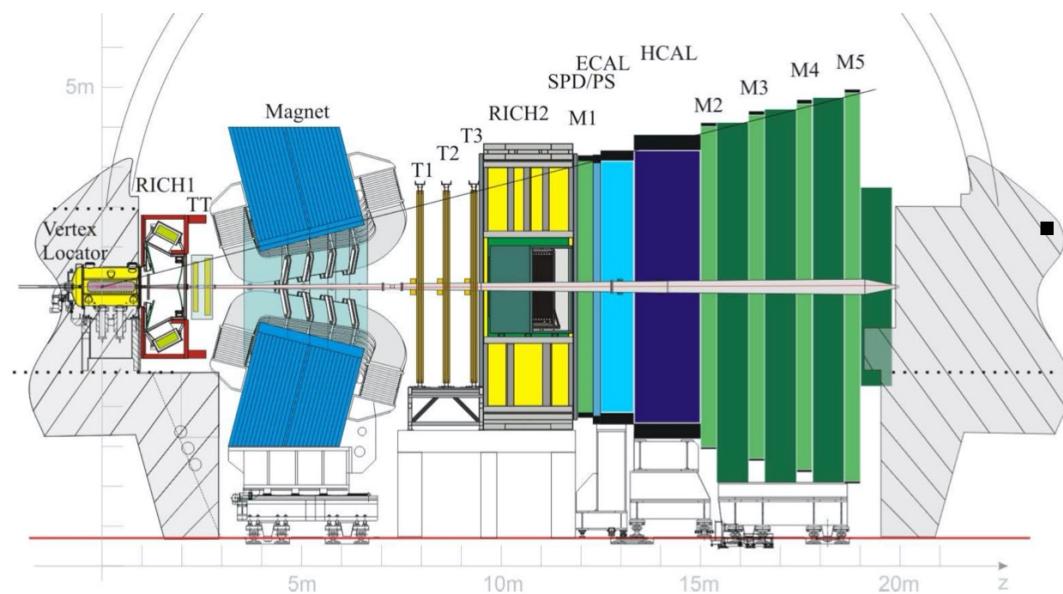
$2 < \eta < 5$  range:  $\sim 25\%$   $b\bar{b}$  pairs in LHCb acceptance



- Powerful particle identification
  - $\epsilon(K \rightarrow K) \sim 95\%$  with  $\epsilon(\pi \rightarrow K) \sim 5\%$
  - $\epsilon(\mu \rightarrow \mu) \sim 97\%$  with  $\epsilon(\pi \rightarrow \mu) \sim 1 - 3\%$

- High momentum resolution
  - $\Delta p/p = 0.4 \sim 0.6\%$  ( $5 - 100\text{GeV}/c$ )
  - $\sigma_{m_B} \sim 10\text{MeV}$  for  $B \rightarrow D\bar{D}K$

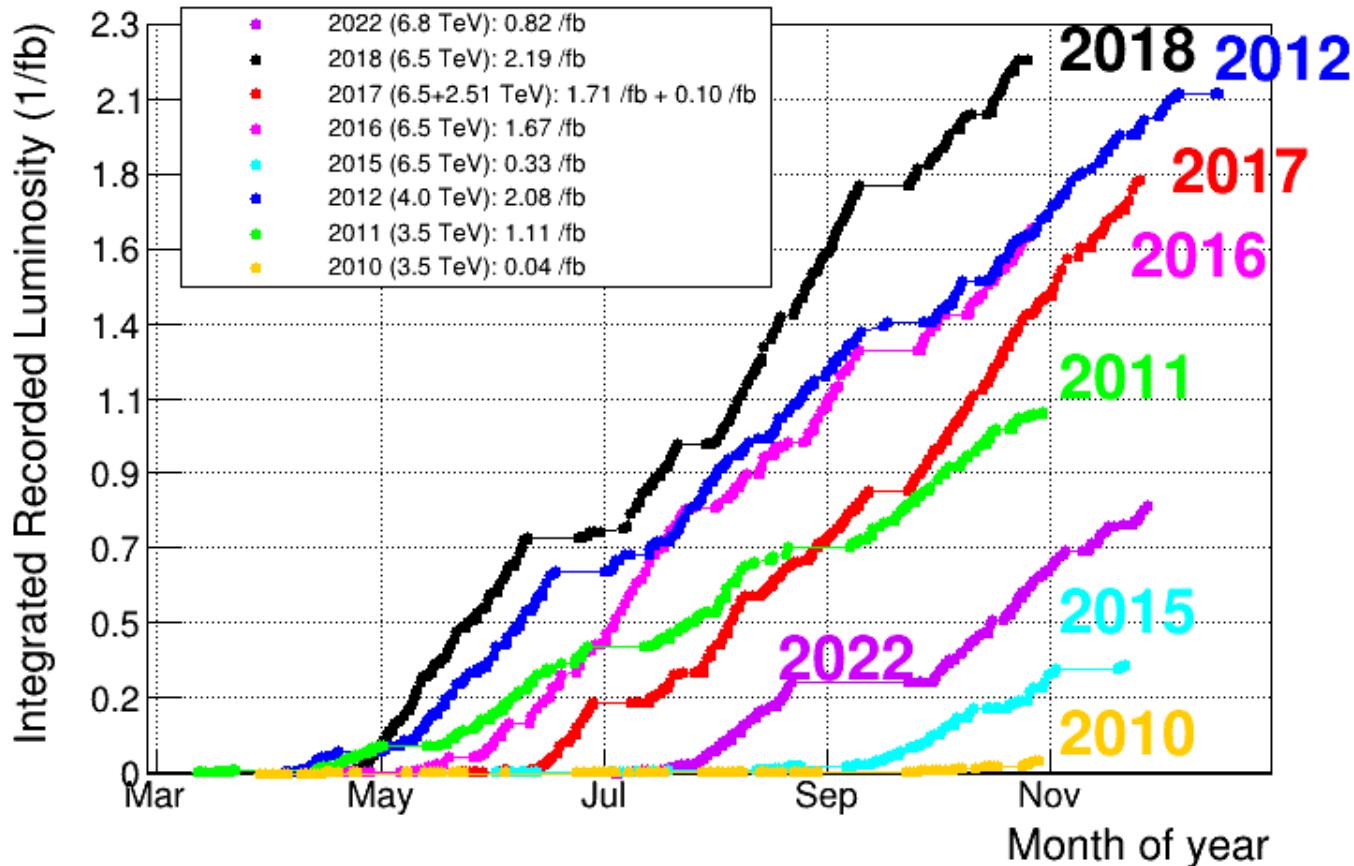
- High spatial resolution
  - $\sigma_{IP} \sim 20\mu\text{m}$ ;  $\sigma_{PV,x/y} \sim 10\mu\text{m}$ ;  $\sigma_{PV,z} \sim 60\mu\text{m}$



# LHCb dataset

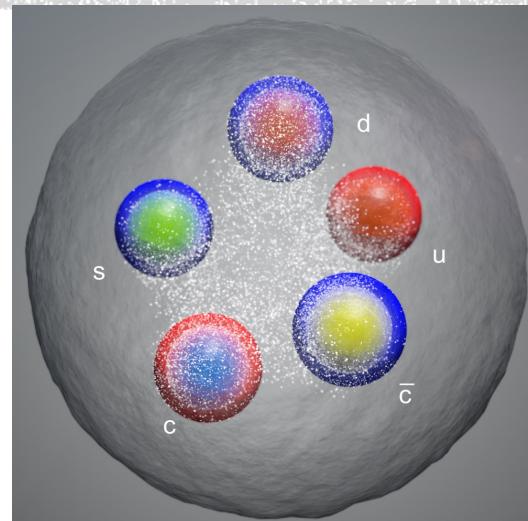
- Run1:  $3 \text{ fb}^{-1}$   $pp$  collision @ 7, 8 TeV
- Run2:  $6 \text{ fb}^{-1}$   $pp$  collision @ 13 TeV
- Run3: started in 2022

All analyses in this talk used the Run1 + Run2 dataset



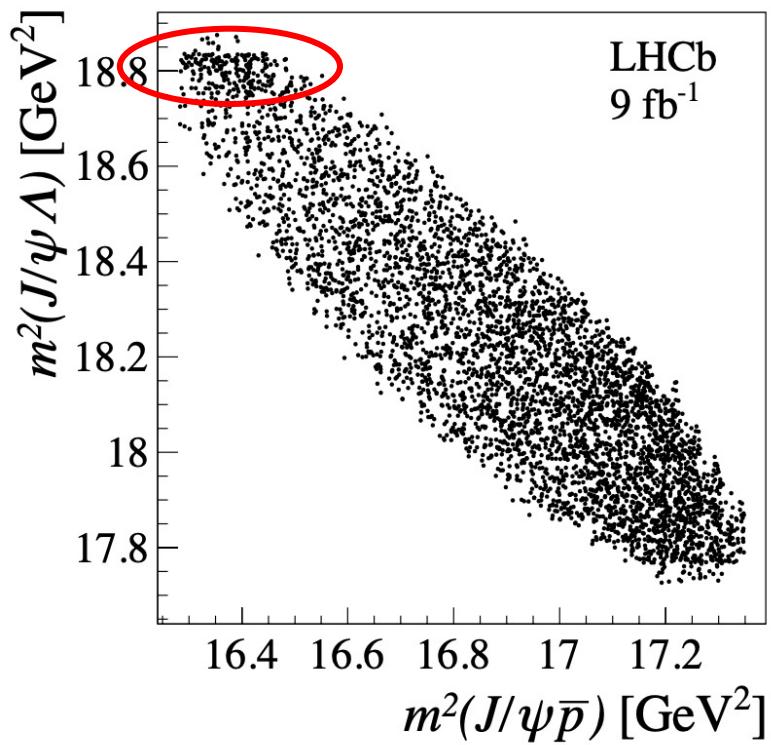
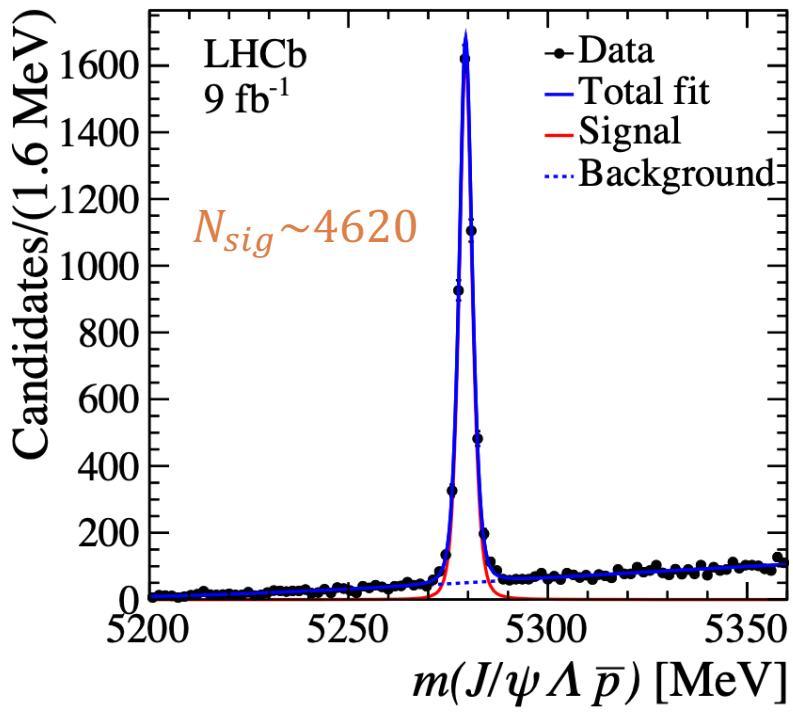
# Observation of pentaquark $P_{\psi S}^{\Lambda}(4338)$ in $B^- \rightarrow J/\psi \Lambda \bar{p}$

[arXiv:2210.10346](https://arxiv.org/abs/2210.10346)



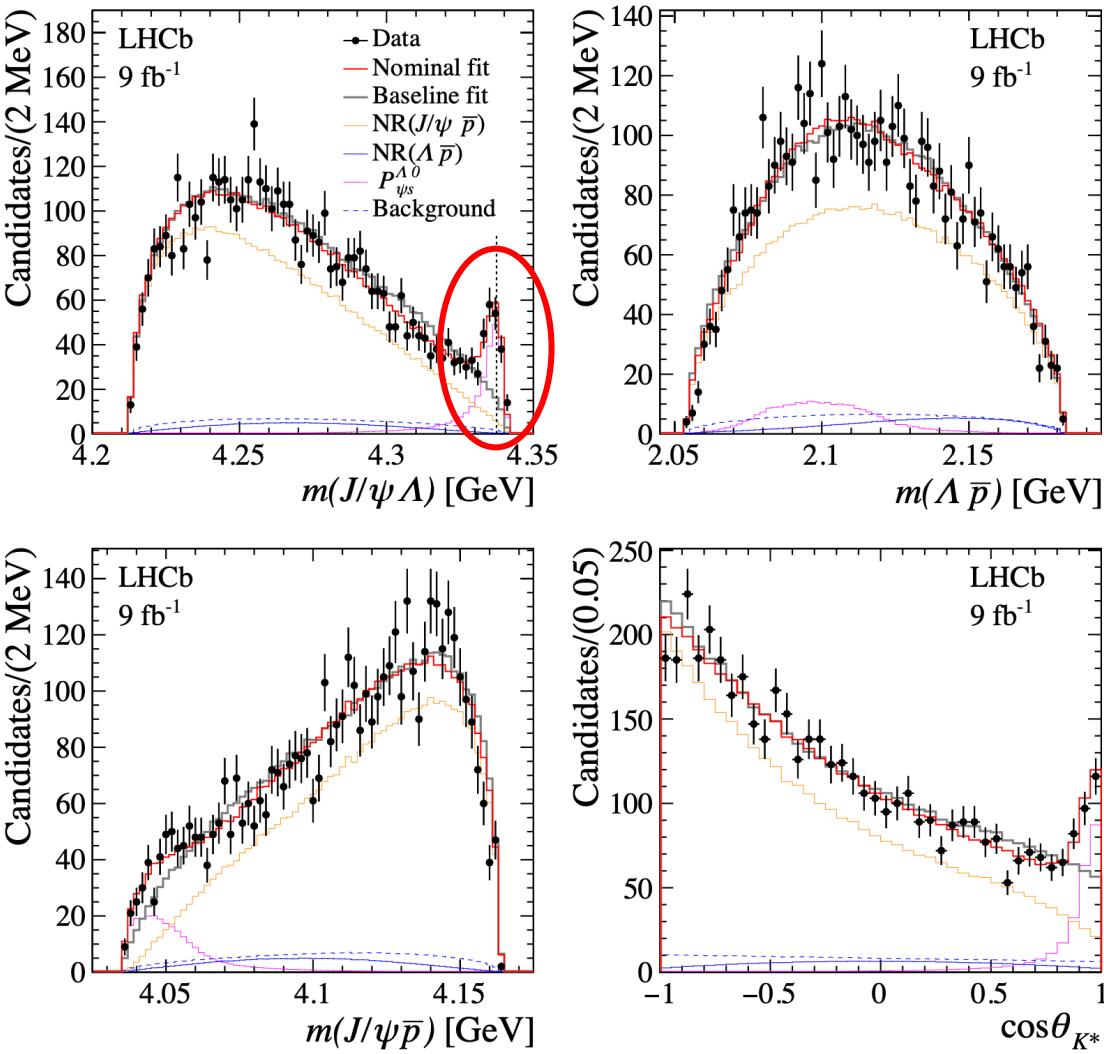
# $B^- \rightarrow J/\psi \Lambda \bar{p}$ dataset

- $J/\psi \rightarrow \mu^+ \mu^-$ ,  $\Lambda \rightarrow p \pi^-$



# Observation of $P_{\psi S}^{\Lambda}(4338)^0$

- $P_{\psi S}^{\Lambda}(4338)^0: > 10\sigma$ 
  - $M_0 = 4338.2 \pm 0.7 \pm 0.4$  MeV
  - $\Gamma_0 = 7.0 \pm 1.2 \pm 1.3$  MeV
  - $J = \frac{1}{2}$
  - $P = -1$  is favored  
(+1 excluded at 90% CL)



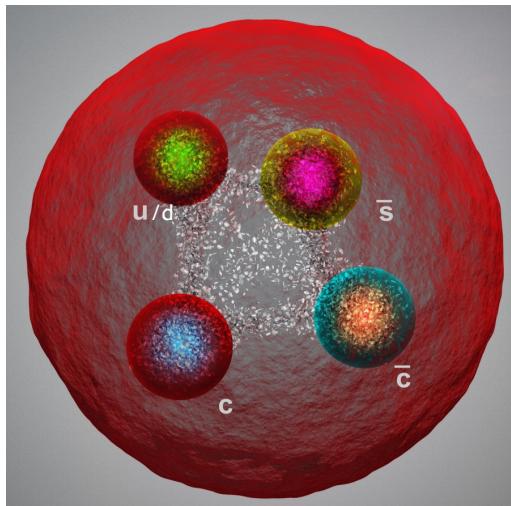
## Interesting facts:

- Mass close to  $\Xi_c^+ D^-$  threshold and in  $S$ -wave
- Mass similar to  $P_{\psi}^N(4337)$ 
  - Same pattern as  $P_{\psi S}^{\Lambda}(4459)$  &  $P_{\psi}^N(4457)$

Can fit in SU(3) flavor multiplets or are more likely a molecular state?

# Evidence of tetraquark $T_{\psi s1}^\theta(4000)^0$ in $B^0 \rightarrow J/\psi K_S^0 \phi$

[arXiv:2301.04899](https://arxiv.org/abs/2301.04899)

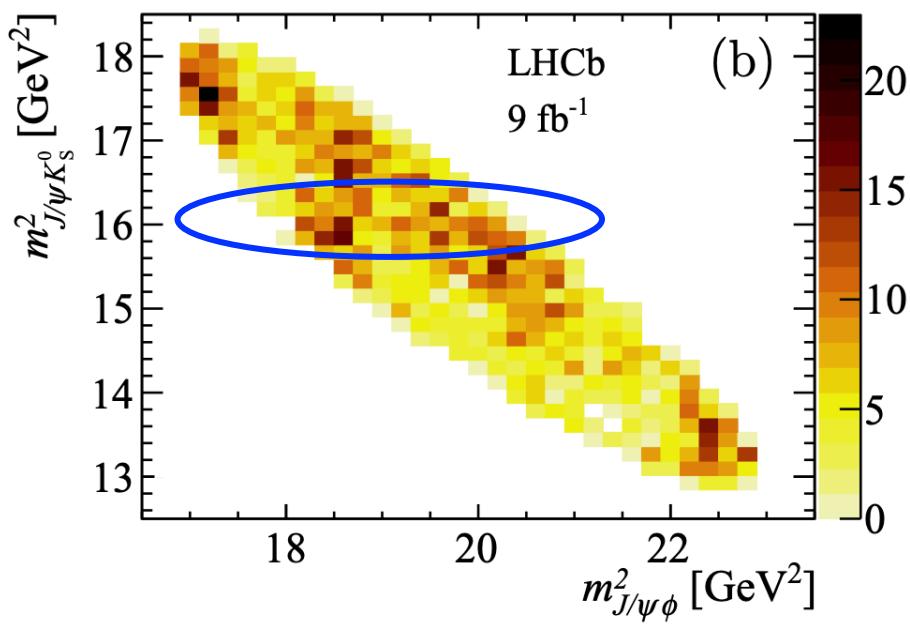
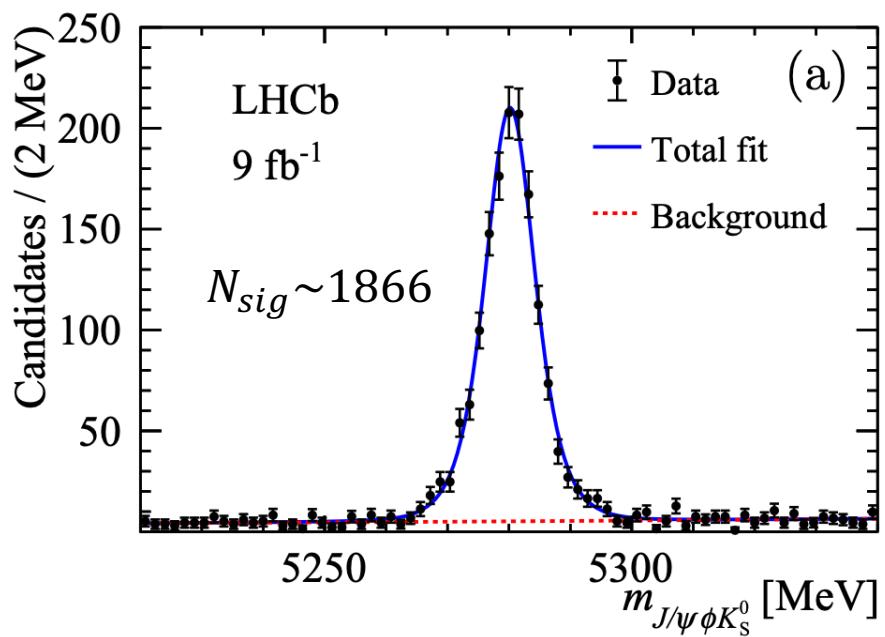


Isospin extention of  $B^+ \rightarrow J/\psi K^+ \phi$  analysis  
where  $c\bar{c}u\bar{s}$  tetraquarks  $T_{\psi s1}^\theta(4000)^+$  and  
 $T_{\psi s1}(4220)^+$  were observed

[Phys. Rev. Lett. 127 \(2021\) 082001](https://doi.org/10.1103/PhysRevLett.127.082001)

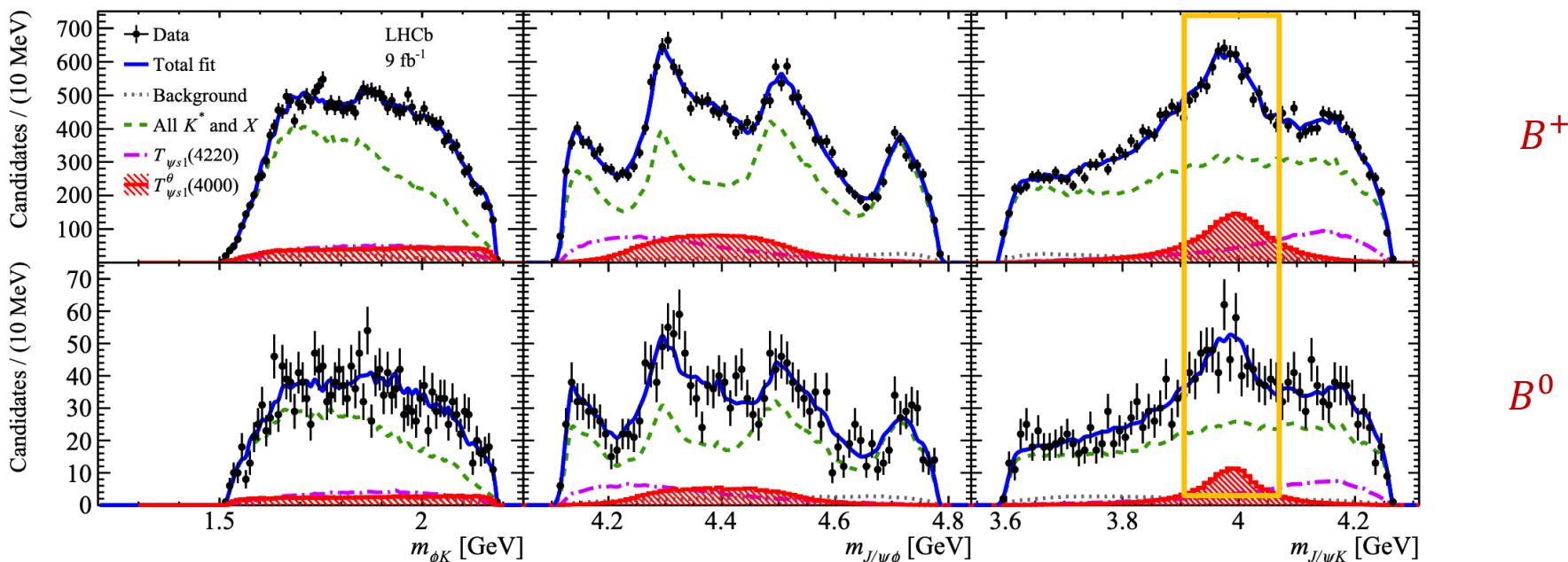
# $B^0 \rightarrow J/\psi K_S^0 \phi$ dataset

- $J/\psi \rightarrow \mu^+ \mu^-$ ;  $\phi \rightarrow K^+ K^-$ ;  $K_S^0 \rightarrow \pi^+ \pi^-$



# Amplitude analysis

- $B^0 \rightarrow J/\psi K_S^0 \phi$  &  $B^+ \rightarrow J/\psi K^+ \phi$  connected by isospin symmetry
- Combined fit to  $B^+$  &  $B^0$  decays
  - All components except  $T_{\psi s1}^\theta(4000)^0$  in  $B^0$  decay are constrained by those in  $B^+$  decay

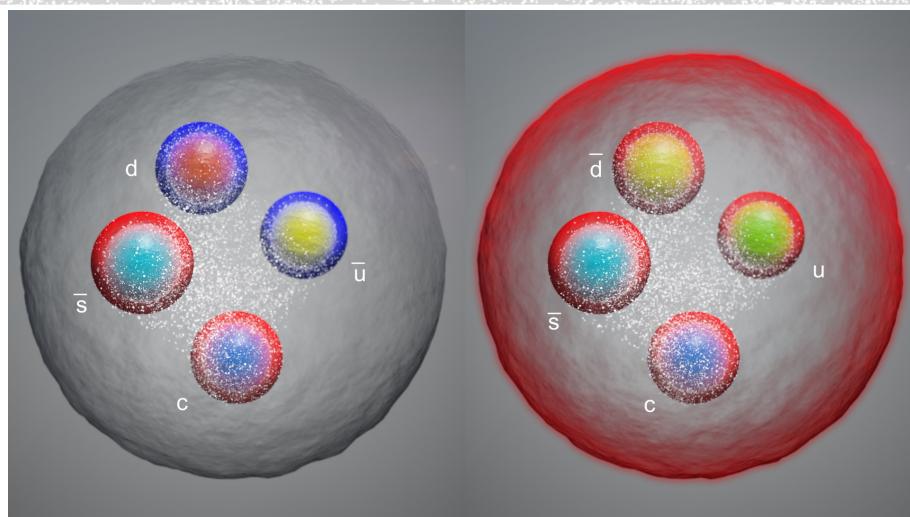
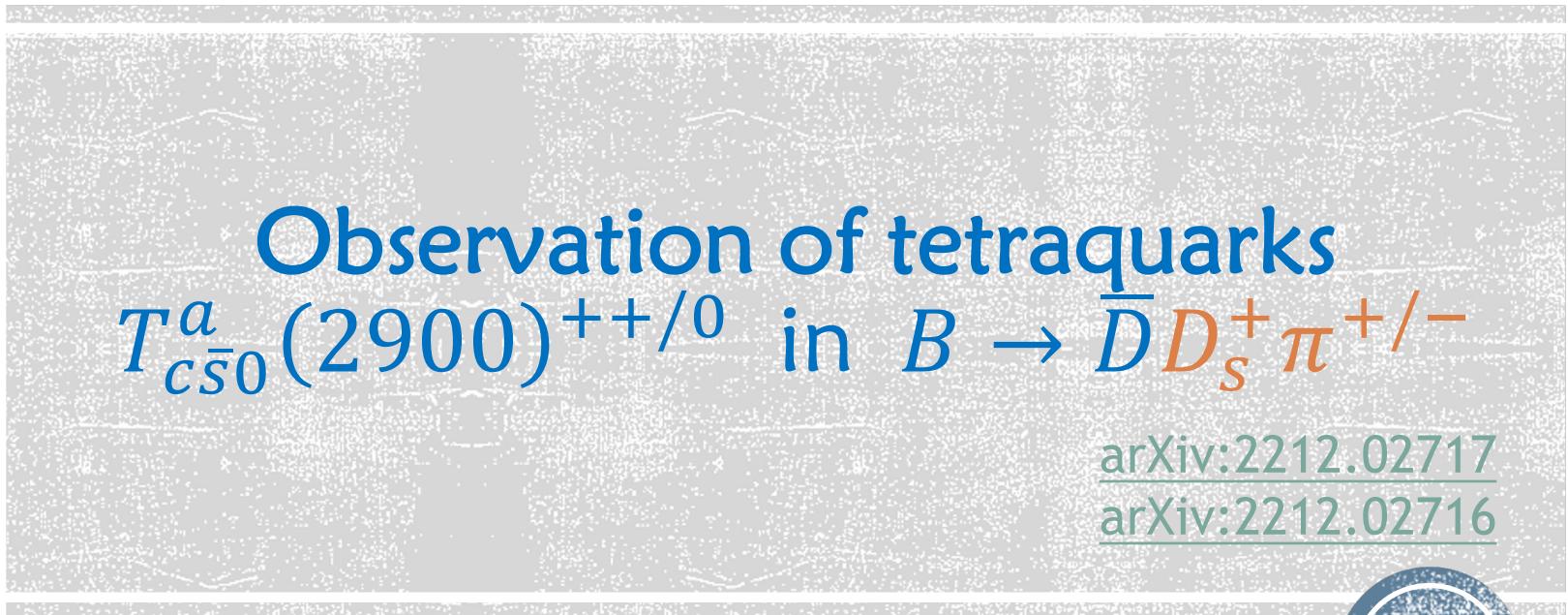


$$M(T_{\psi s1}^\theta(4000)^0) = 3991^{+12}_{-10}{}^{+9}_{-17} \text{ MeV}$$

$$\Gamma(T_{\psi s1}^\theta(4000)^0) = 105^{+29}_{-25}{}^{+17}_{-23} \text{ MeV}$$

**Significance: 4 $\sigma$**

(would be 5.4 $\sigma$  if assuming isospin symmetry for  $T_{\psi s1}^\theta(4000)^0$ )



# $B \rightarrow \bar{D} D_s^+ \pi^{+/-}$ dataset

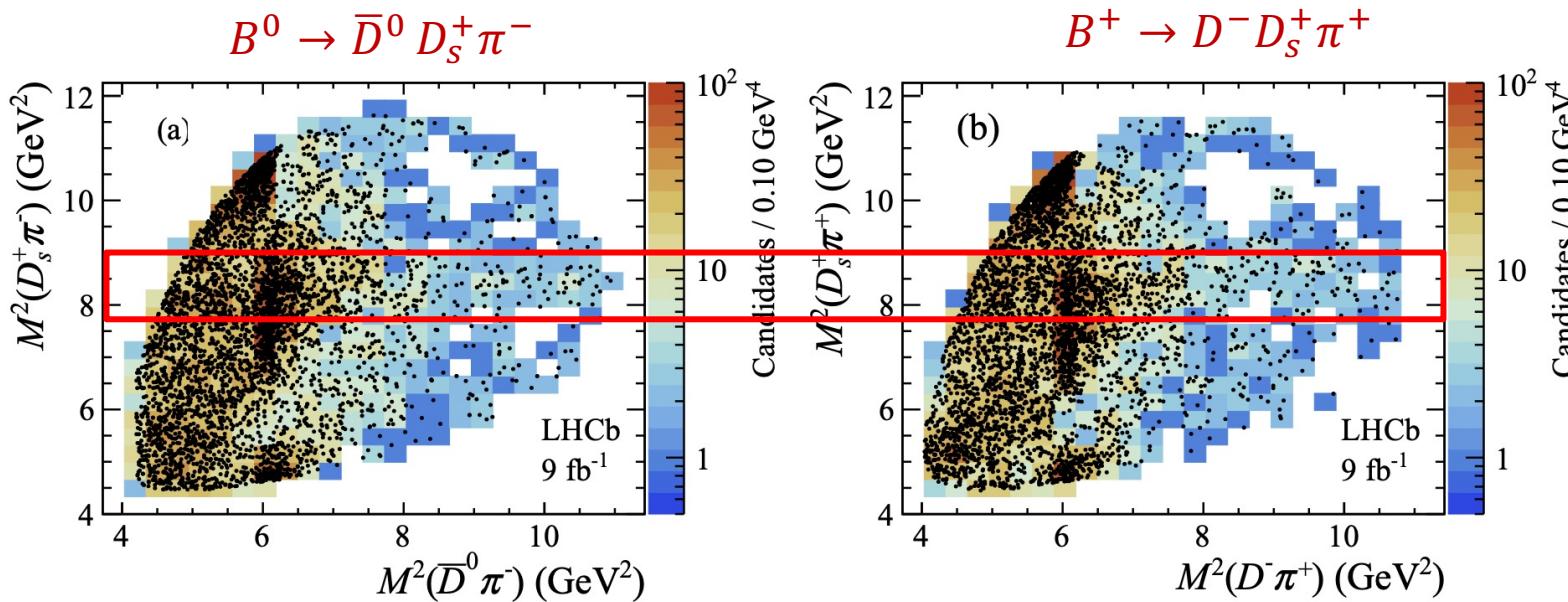
arXiv:2212.02717

arXiv:2212.02716

- $D^- \rightarrow K^+ \pi^- \pi^-$ ;      -  $\bar{D}^0 \rightarrow K^+ \pi^-, K^+ \pi^- \pi^+ \pi^-$ ;      -  $D_s^+ \rightarrow K^+ K^- \pi^+$

- **Signal yields:**

- $B^+ \rightarrow D^- D_s^+ \pi^+ : \sim 3751$
- $B^0 \rightarrow \bar{D}^0 D_s^+ \pi^- : \sim 4008$

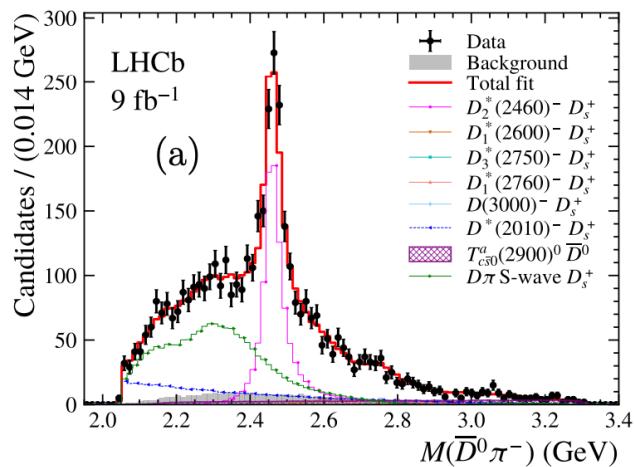


- Clear vertical band at  $M^2(\bar{D}\pi) \sim 6 \text{ GeV}^2$ :  $D_2^*(2460)$
- Faint horizontal band at  $M^2(D_s\pi) \sim 8.5 \text{ GeV}^2$ : new tetraquark candidates

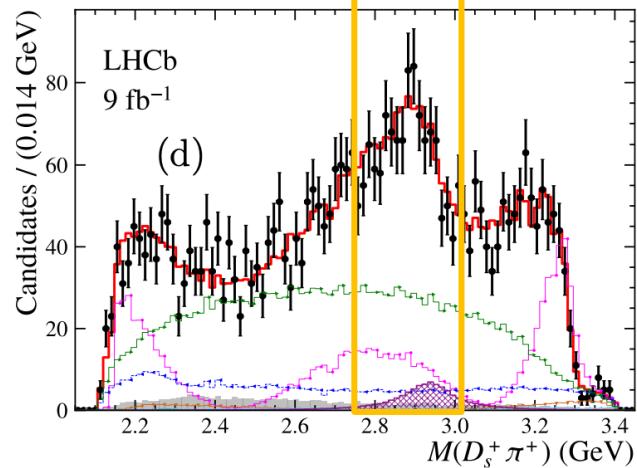
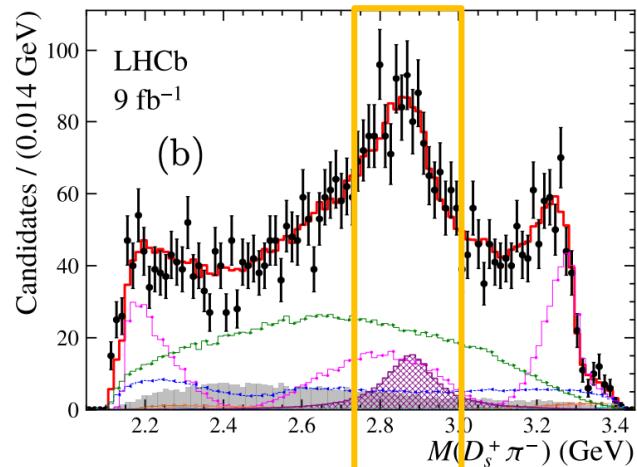
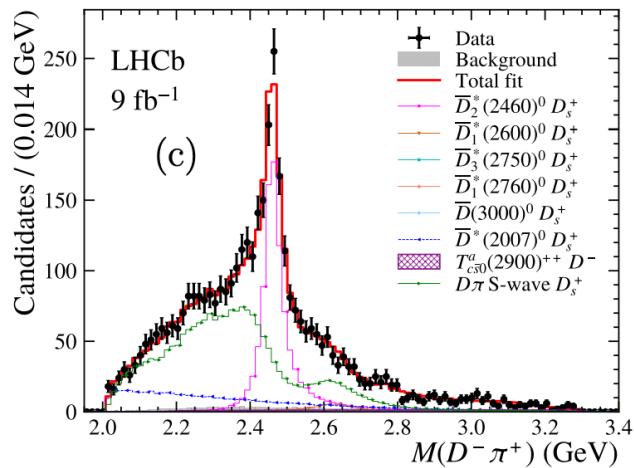
# $T_{c\bar{s}0}^a(2900)^{++/0}$ in $B \rightarrow \bar{D} D_s^+ \pi^{+/-}$

arXiv:2212.02717  
arXiv:2212.02716

$$B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$$



$$B^+ \rightarrow D^- D_s^+ \pi^+$$



- Isospin symmetry -> combined amplitude analysis to the two channels

$T_{c\bar{s}0}^a(2900)^{++/0}$  :  $> 9\sigma$ ;  $J^P = 0^+$      $M = 2.908 \pm 0.011 \pm 0.020$  GeV

$\Gamma = 0.136 \pm 0.023 \pm 0.011$  GeV

# Discussions on $T_{c\bar{s}0}^a(2900)^{++/0}$

arXiv:2212.02717

[arXiv:2212.02716](#)

- $T_{c\bar{s}0}^a(2900)^{++}$  &  $T_{c\bar{s}0}^a(2900)^0$  in isospin triplet
  - Where is  $T_{c\bar{s}0}^a(2900)^+?$  -> be searched for in  $D_s^+\pi^0$

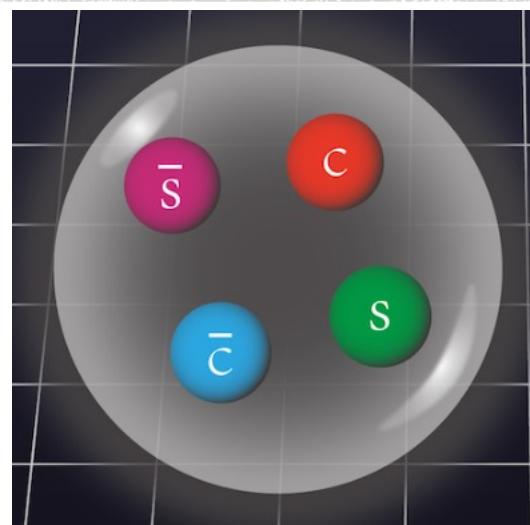
- $T_{c\bar{s}0}^a(2900)$  &  $T_{cs0}(2900)$  have similar masses
  - Are they SU(3) flavor partners?
  - Where are other states in the SU(3) multiplets?

$$T_{cs0}(2900) \equiv X_0(2900)$$

Remain to be revealed in future studies

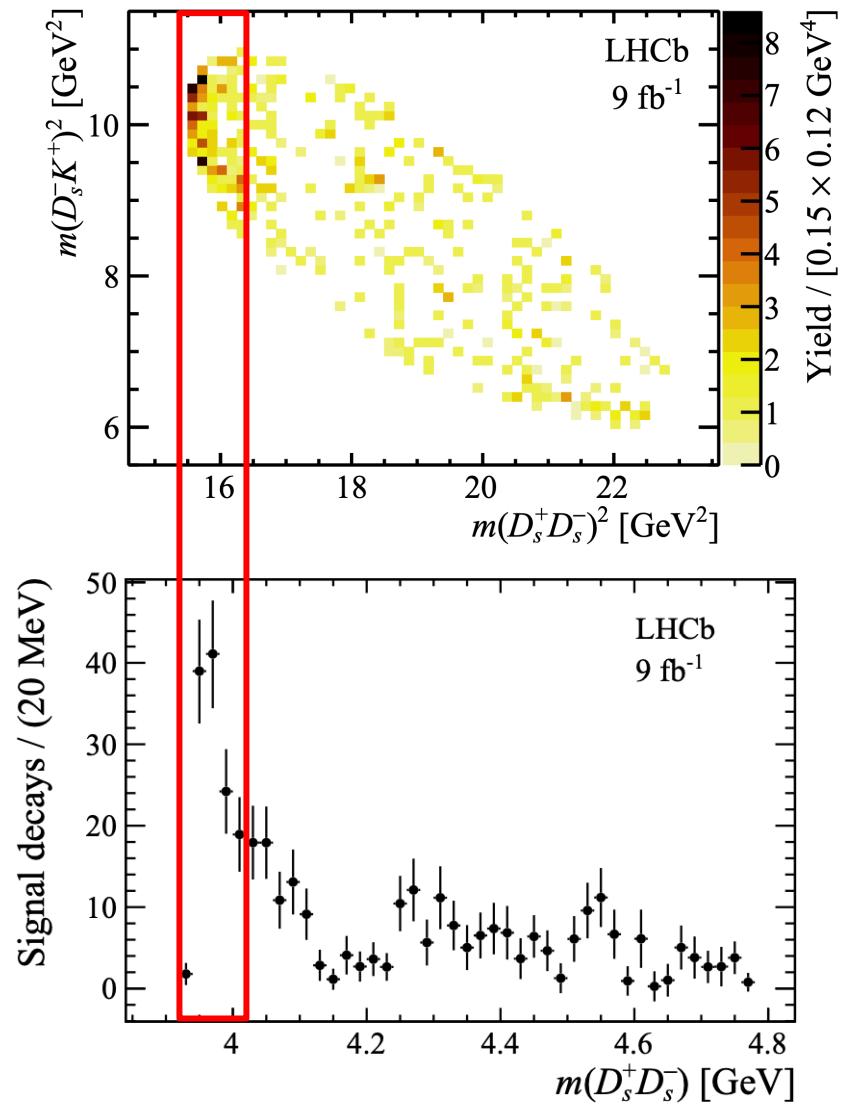
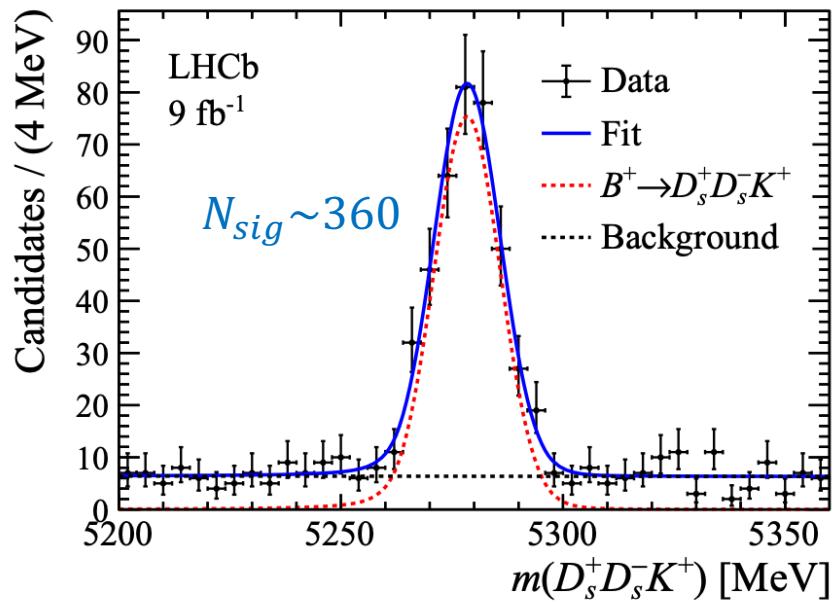
# A near-threshold $D_s^+ D_s^-$ structure in $B^+ \rightarrow D_s^+ D_s^- K^+$

[arXiv:2210.15153](https://arxiv.org/abs/2210.15153)  
[arXiv:2211.05034](https://arxiv.org/abs/2211.05034)



# Observation of $B^+ \rightarrow D_s^+ D_s^- K^+$

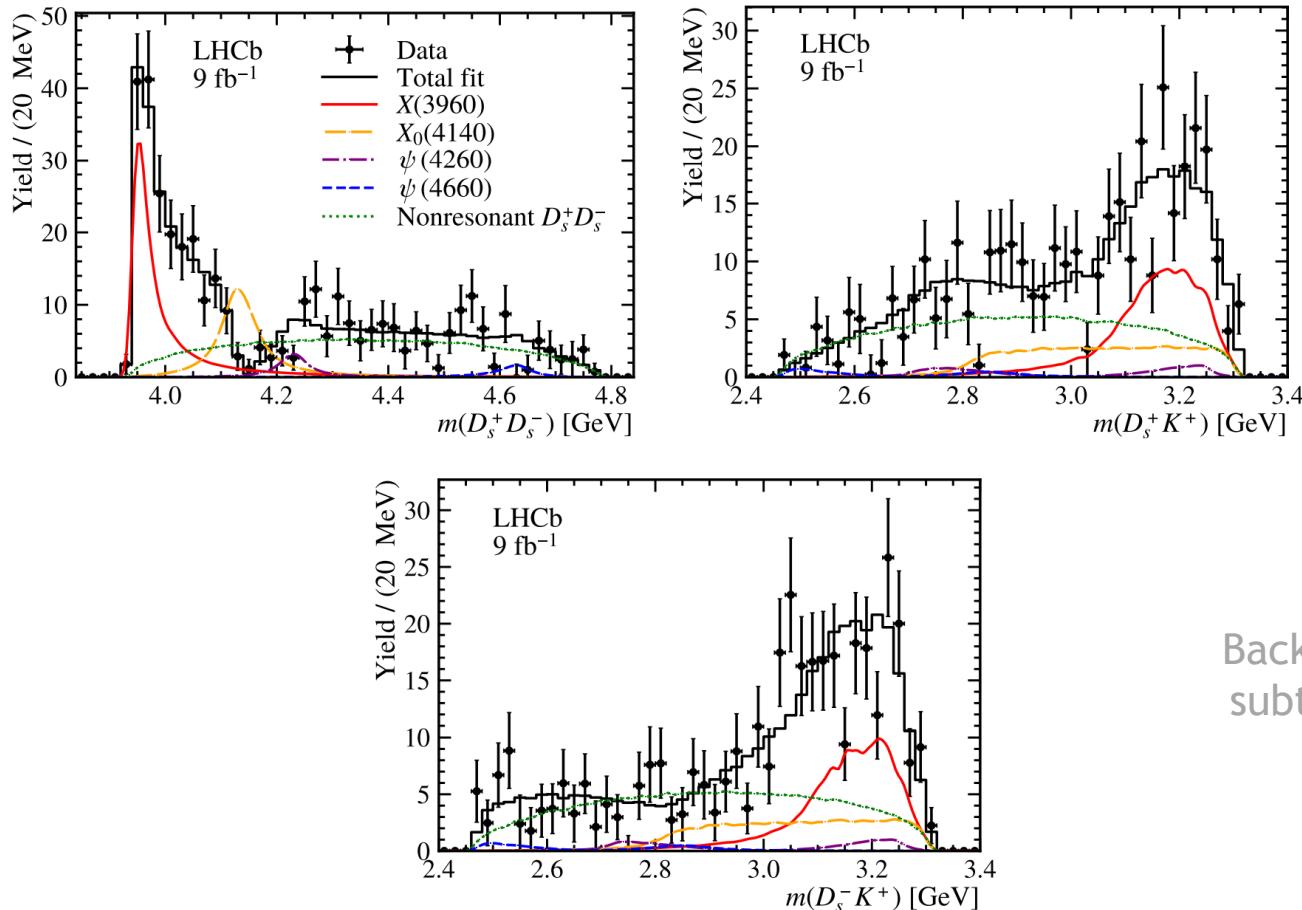
$$D_s^\pm \rightarrow K^\mp K^\pm \pi^\pm$$



$$\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+) = (1.15 \pm 0.07 \pm 0.06 \pm 0.38) \times 10^{-4}$$

# Observation of $X(3960)$ in $D_s^+ D_s^-$

- Two new states with  $J^{PC} = 0^{++}$ :
  - $X(3960)$  : to describe the near-threshold peak  $> 12\sigma$
  - $X_0(4140)$ : to account for the dip at  $\sim 4.14$  GeV via interference  $> 3\sigma$



RBW mass lineshape for all resonances

# $X(3960)$ vs $\chi_{c0}(3930)$

- $X(3960)$ :  $M_0 = 3955 \pm 6 \pm 11$  MeV;  $\Gamma_0 = 48 \pm 17 \pm 10$  MeV;  $J^{PC} = 0^{++}$
- $\chi_{c0}(3930)$ :  $M_0 = 3924 \pm 2$  MeV;  $\Gamma_0 = 17 \pm 5$  MeV;  $J^{PC} = 0^{++}$

[Phys.Rev.D102\(2020\) 112003](#), [Phys. Rev. Lett. 125 \(2020\) 242001](#)

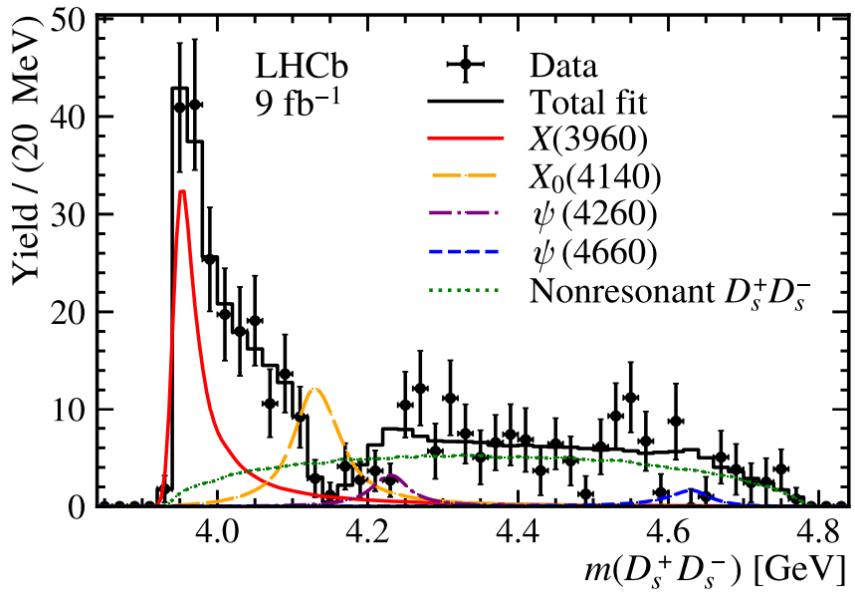
- Are they the same particle? If yes

$$\frac{\Gamma(X \rightarrow D^+ D^-)}{\Gamma(X \rightarrow D_s^+ D_s^-)} = \frac{\mathcal{B}(B^+ \rightarrow D^+ D^- K^+) \mathcal{FF}_{B^+ \rightarrow D^+ D^- K^+}^X}{\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+) \mathcal{FF}_{B^+ \rightarrow D_s^+ D_s^- K^+}^X} = 0.29 \pm 0.09 \text{ (stat)} \pm 0.10 \text{ (syst)} \pm 0.08 \text{ (ext)}$$

$\mathcal{FF}$ : Fit fractions in the two  $B^+$  decays

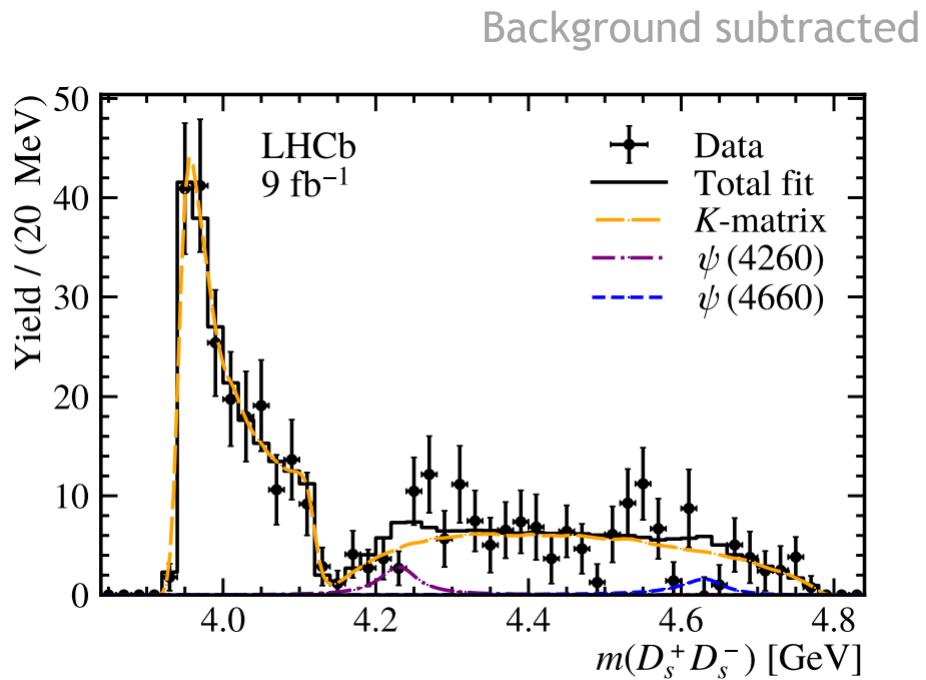
- $\Gamma(X \rightarrow D^+ D^-) < \Gamma(X \rightarrow D_s^+ D_s^-)$  -> exotic  $T_{\psi\phi 0}^f(39xx)$ 
  - Conventional charmonium predominantly decays into  $D^{(*)}\bar{D}^{(*)}$ 
    - It is harder to excite an  $s\bar{s}$  pair from vacuum compared with  $u\bar{u}(d\bar{d})$
- What can we do in the future?
  - Precision measurements of  $X(3960)/\chi_{c0}(3930)$  properties -> to see if they are really the same particle
    - $X(3960)/\chi_{c0}(3930)/\chi_{c0}(3915) \rightarrow J/\psi\omega$  -> more input to help reveal the nature of this state
      - E.g.  $B \rightarrow J/\psi\omega K$

# Look again at $X_0(4140)$



The default model:  
dip@4.14GeV modelled  
by a new resonance,  
 $X_0(4140)$

No definitive conclusion on existence of  $X_0(4140)$



Can also be described by  
considering  $J/\psi\phi \rightarrow D_s^+ D_s^-$   
rescattering in the  $K$ -matrix  
formula

# Observation of $B^+ \rightarrow J/\psi\eta' K^+$

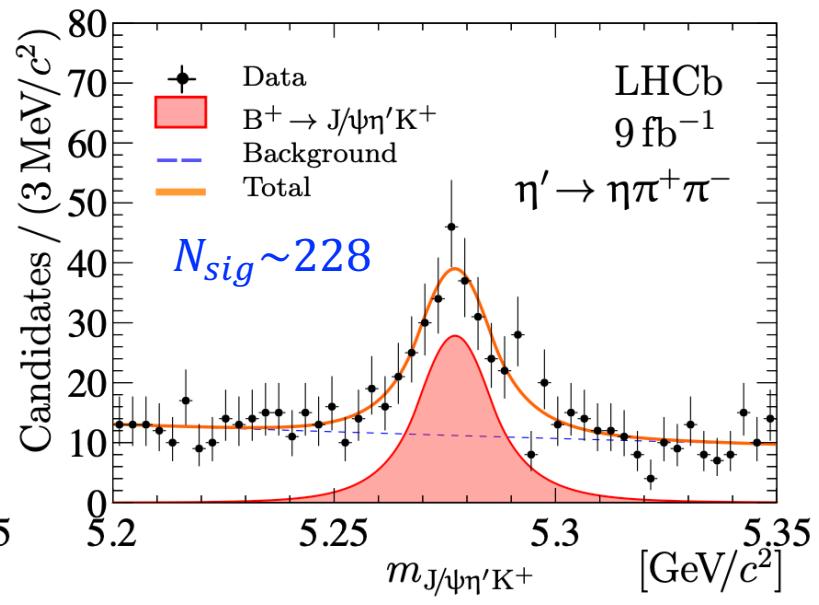
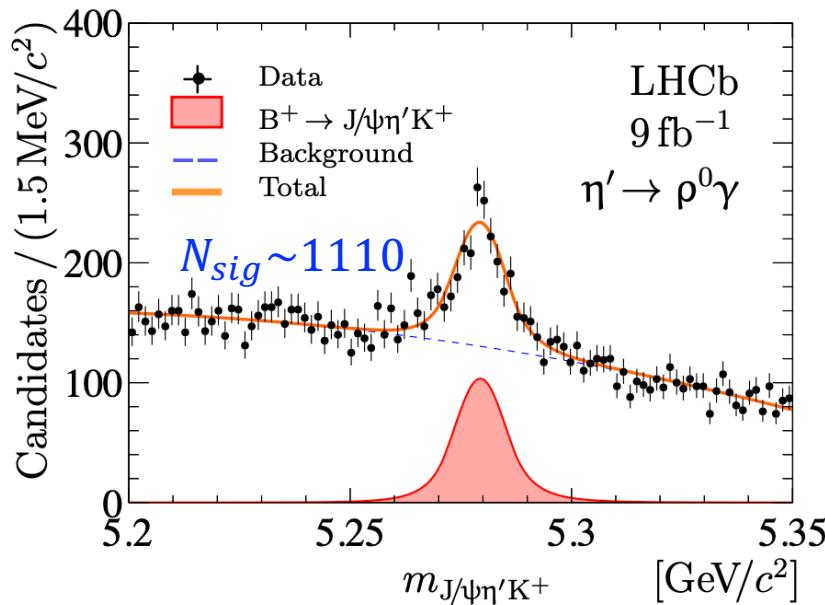
[arXiv:2303.09443](https://arxiv.org/abs/2303.09443)

Opportunity to investigate exotic resonances in  
 $J/\psi\eta'$  and  $J/\psi K^+$  systems



# Observation of $B^+ \rightarrow J/\psi\eta'K^+$

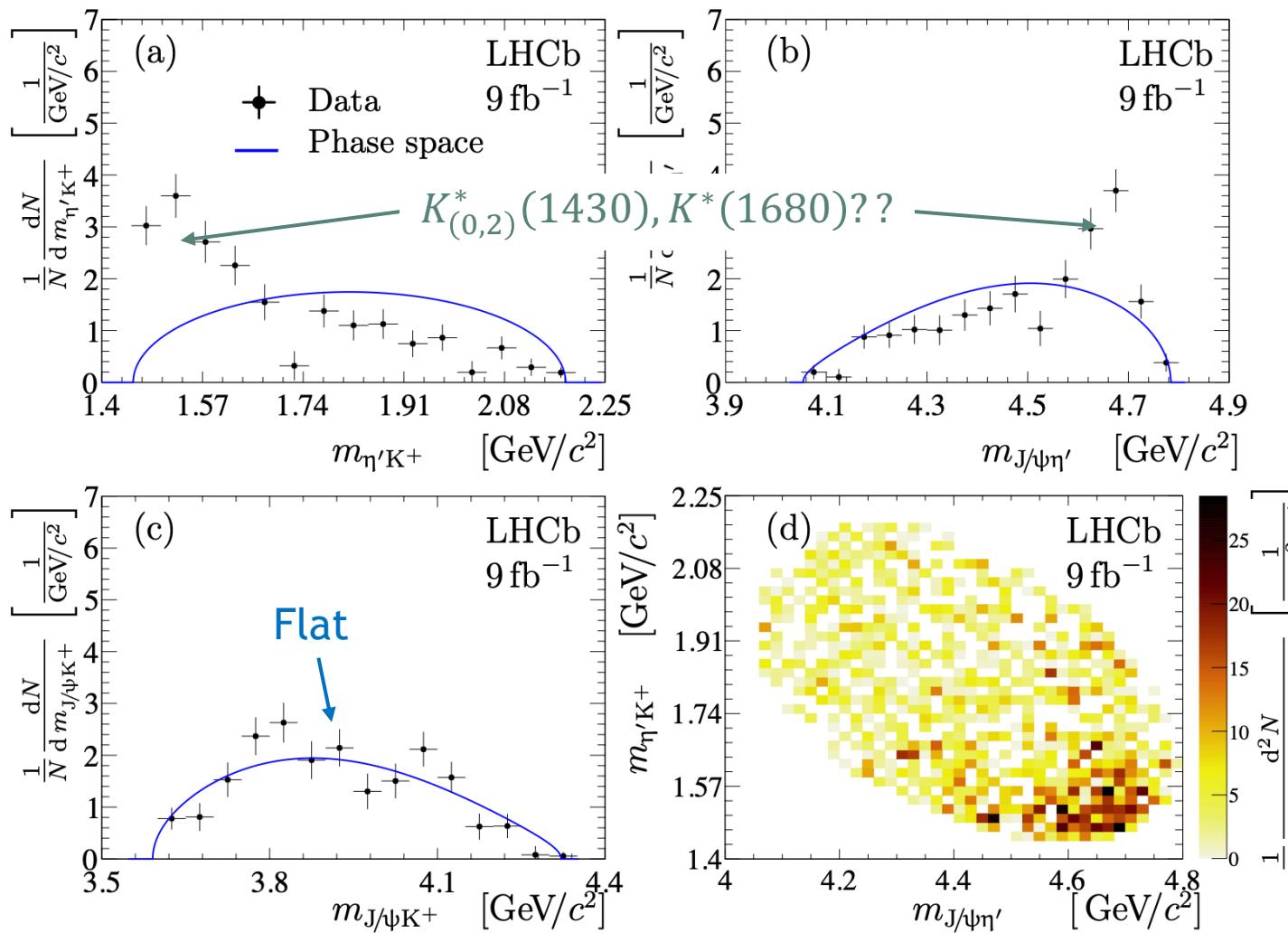
- $B^+ \rightarrow J/\psi\eta'K^+, J/\psi \rightarrow \mu^+\mu^-$ 
  - $\eta' \rightarrow \rho^0(\rightarrow \pi^+\pi^-)\gamma$
  - $\eta' \rightarrow \eta(\rightarrow 2\gamma)\pi^+\pi^-$



$$\mathcal{B}(B^+ \rightarrow J/\psi\eta'K^+) = (3.06 \pm 0.29 \pm 0.18 \pm 0.04) \times 10^{-5}$$

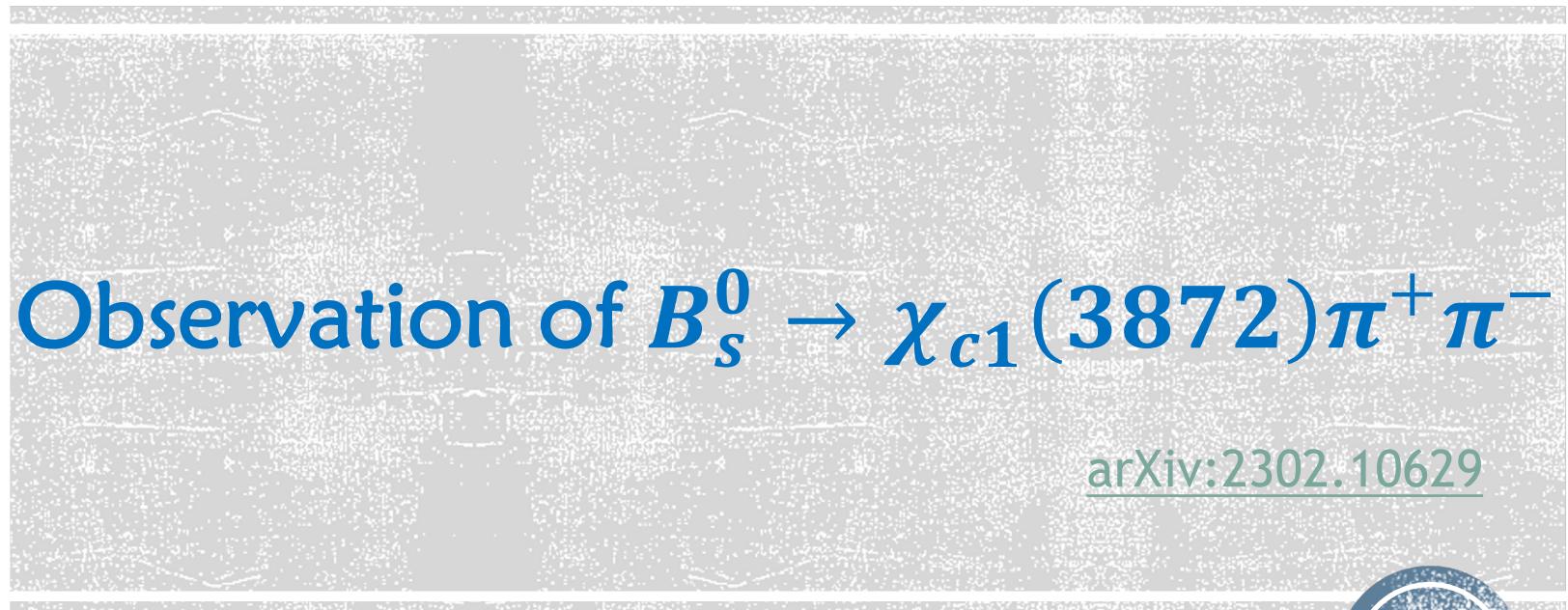
# Investigation of phase space

Background subtracted



No hint of exotic in  $m(J/\psi\eta')$  or  $m(J/\psi K^+)$

But let's wait for more data !!



# Observation of $B_s^0 \rightarrow \chi_{c1}(3872)\pi^+\pi^-$

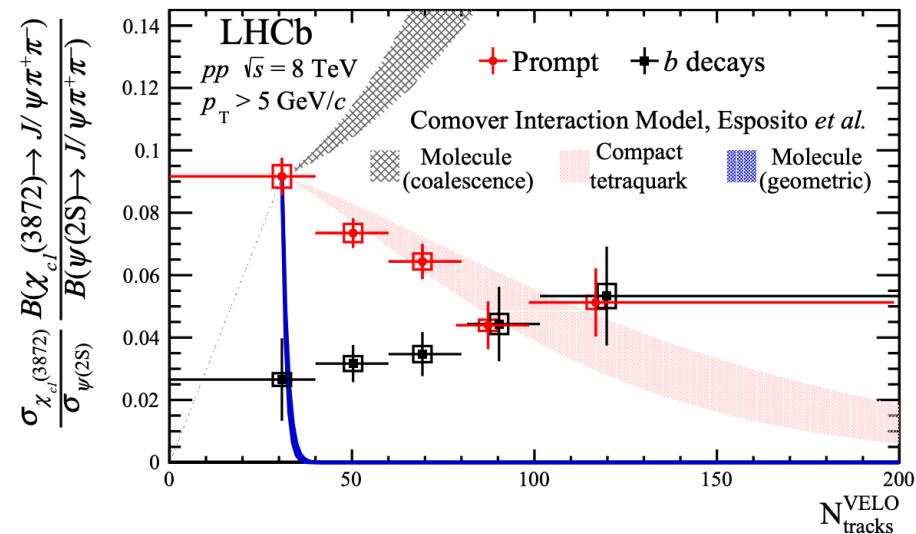
[arXiv:2302.10629](https://arxiv.org/abs/2302.10629)



# Probing $\chi_{c1}(3872)$ nature via production

- Prompt: multiplicity dependence
  - Compact scheme is favored by the  $\sigma(\chi_{c1}(3872))/\sigma(\psi(2S))$  trend

Phys. Rev. Lett. 126 (2021) 092001



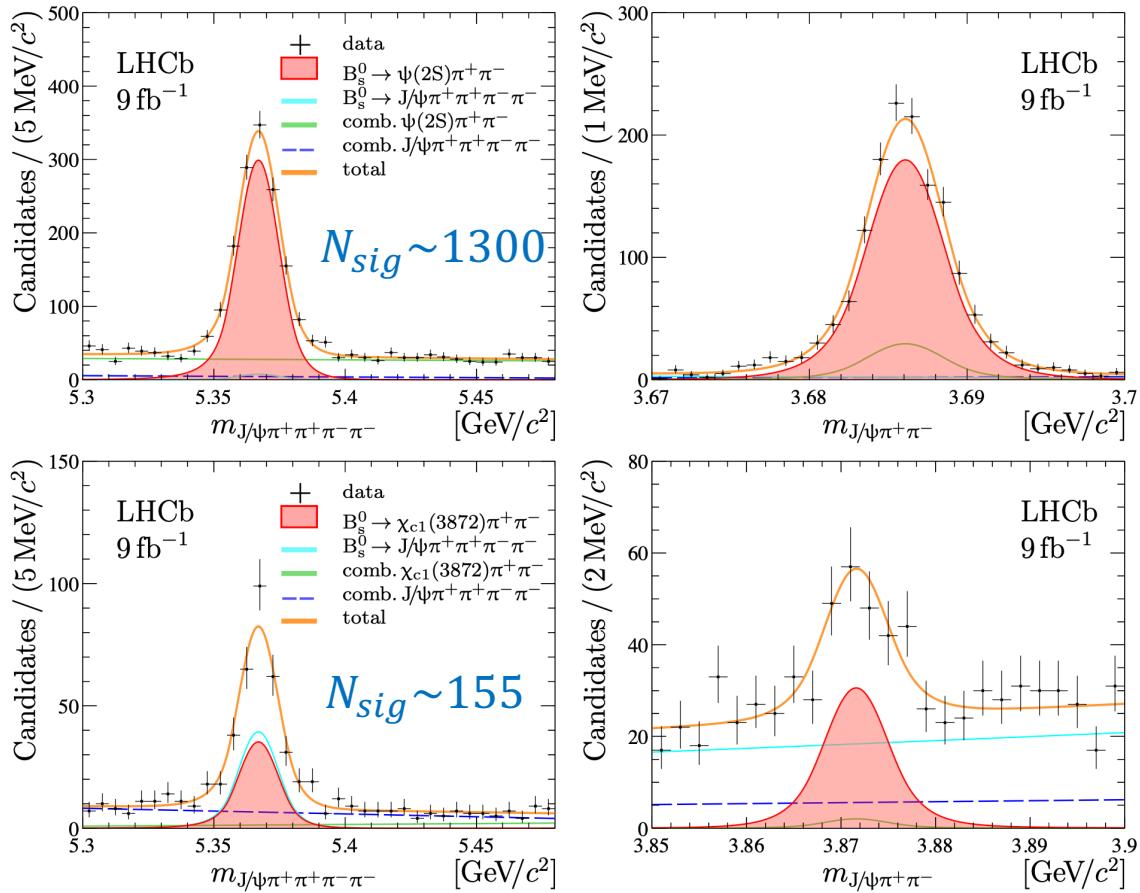
- B decays:
  - Puzzling difference in  $\mathcal{B}(B^+ \rightarrow \chi_{c1}(3872)K^+)$  and  $\mathcal{B}(B^0 \rightarrow \chi_{c1}(3872)K^0)$   
 $(2.1 \pm 0.7) \times 10^{-4}$        $(1.1 \pm 0.4) \times 10^{-4}$
  - But similar  $\mathcal{B}(B^0 \rightarrow \chi_{c1}(3872)K^0)$  and  $\mathcal{B}(B_s^0 \rightarrow \chi_{c1}(3872)\phi)$   
 $(1.1 \pm 0.4) \times 10^{-4}$
- The above two phenomena could be explained by a compact-tetraquark interpretation

Phys. Rev. D102 (2020) 034017

Let's investigate more  $B$ -hadron decays!

$$B_s^0 \rightarrow \chi_{c1}(3872)(\rightarrow J/\psi \pi^+ \pi^-) \pi^+ \pi^-$$

- Signal yield determined from 2D mass fit

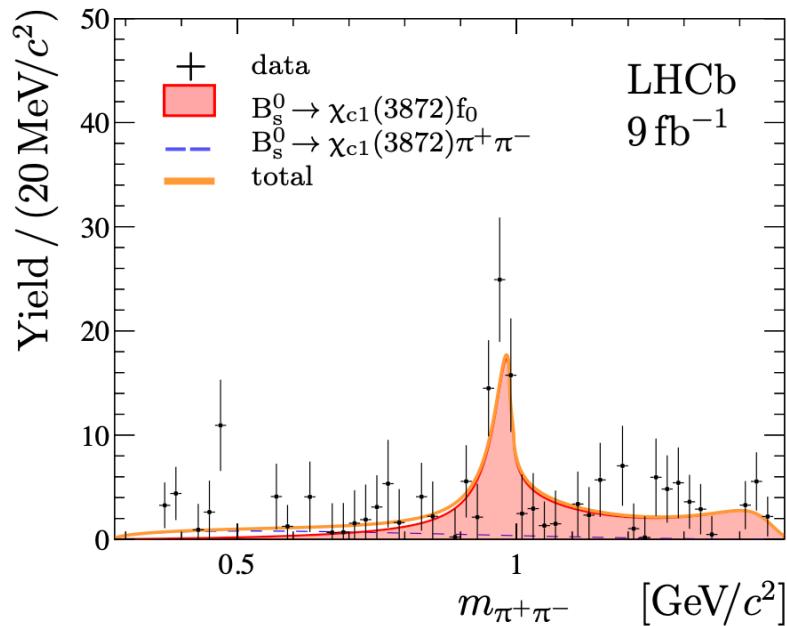
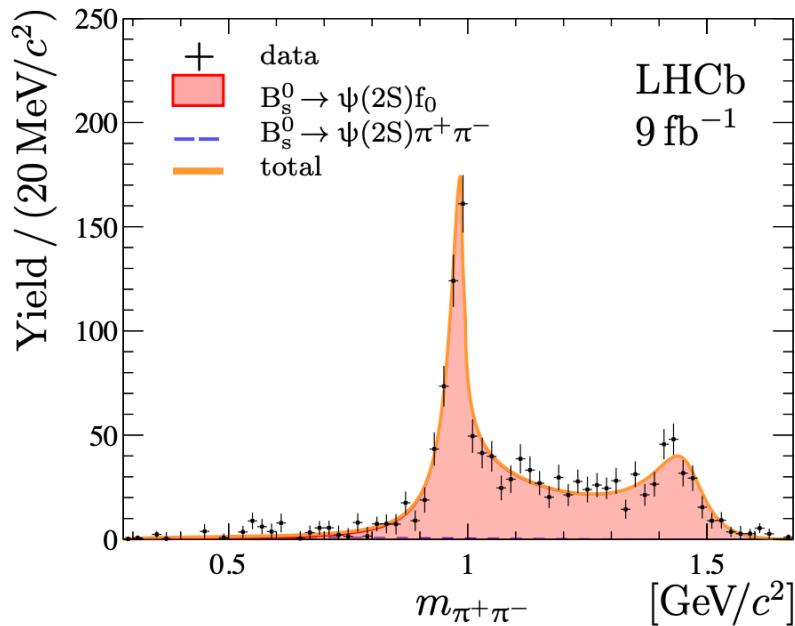


$$\frac{\mathcal{B}(B_s^0 \rightarrow \chi_{c1}(3872)\pi^+\pi^-) \times \mathcal{B}(\chi_{c1}(3872) \rightarrow J/\psi \pi^+\pi^-)}{\mathcal{B}(B_s^0 \rightarrow \psi(2S)\pi^+\pi^-) \times \mathcal{B}(\psi(2S) \rightarrow J/\psi \pi^+\pi^-)} = (6.8 \pm 1.1 \pm 0.2) \times 10^{-2}$$

Three times of the ratio:  $\mathcal{R}_{\psi(2S)\phi}^{\chi_{c1}(3872)\phi} = (2.42 \pm 0.23 \pm 0.07) \times 10^{-2}$

# The recoiled $\pi^+\pi^-$ mass

Background subtracted



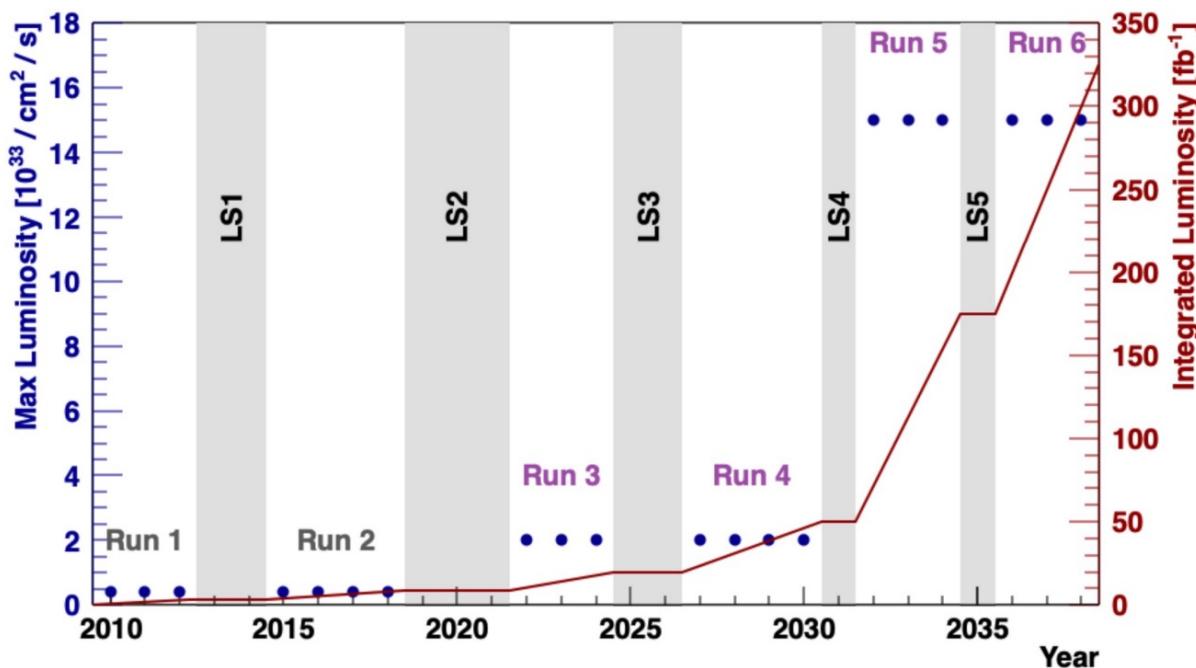
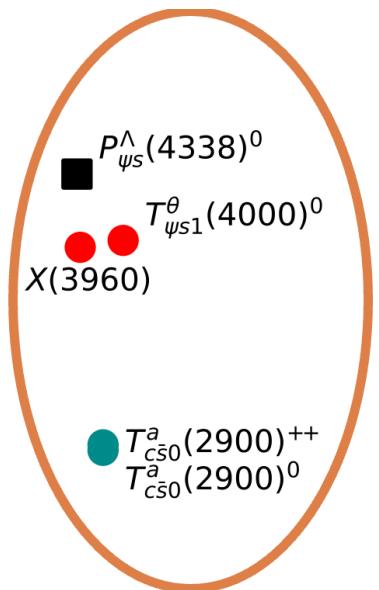
$$F(m) \propto mq p^3 \left| f \mathcal{A}_{f_0(980)}(m) + e^{i\varphi} \mathcal{A}_{f_0(1500)}(m) \right|^2 + \text{Phase space contribution}$$

- Similar to  $B_s^0 \rightarrow J/\psi\pi^+\pi^-$  and  $B_s^0 \rightarrow \psi(2S)\pi^+\pi^-$
- Observation of  $B_s^0 \rightarrow \chi_{c1}(3872)f_0(980)$ :  $> 7\sigma$

Amplitude measurement urges for more data !!

# Summary and prospects

- Recent exotic candidates at LHCb
- Observations of new  $B$  decays show potential for future exotic studies
  - $B^+ \rightarrow J/\psi \eta' K^+$
  - $B_s^0 \rightarrow \chi_{c1}(3872) \pi^+ \pi^-$
- More LHCb data will provide new opportunities



Thank you for your attention!

# Backup slides



# New exotic naming scheme

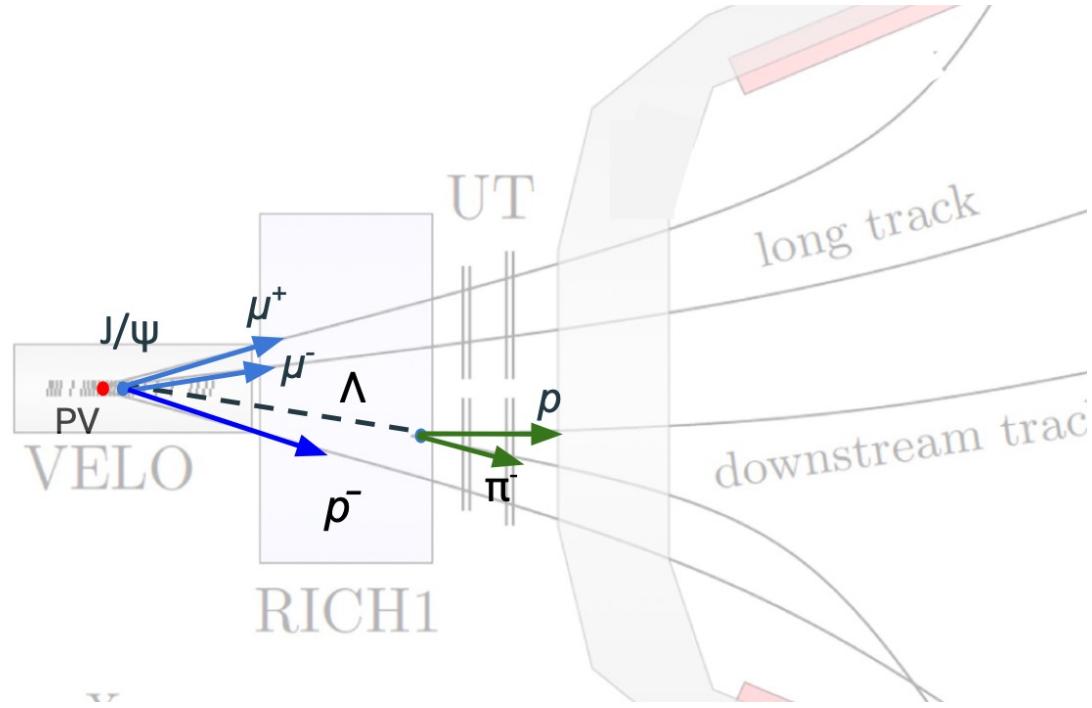
- **$T$**  for tetraquark
- **$P$**  for pentaquark
- **superscript:** based on existing symbols, to indicate isospin, parity and G-parity
- **subscript:** heavy quark content

T states				T states			
zero net $S, C, B$				non-zero net $S, C, B$			
$(P, G)$	$I = 0$	$I = 1$		$(P)$	$I = 0$	$I = \frac{1}{2}$	$I = 1$
$(-, -)$	$\omega$	$\pi$		$(-)$	$\eta$	$\tau$	$\pi$
$(-, +)$	$\eta$	$\rho$		$(+)$	$f$	$\theta$	$a$
$(+, +)$	$f$	$b$					
$(+, -)$	$h$	$a$					

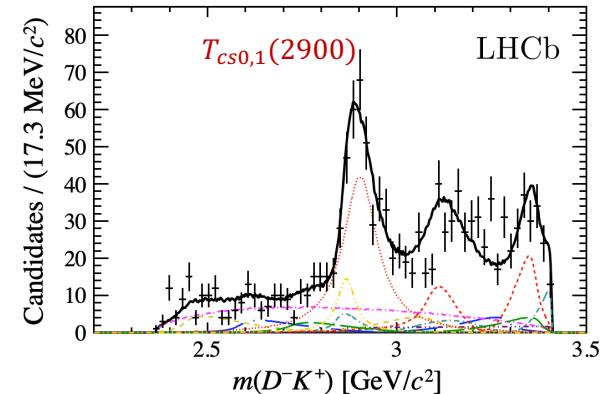
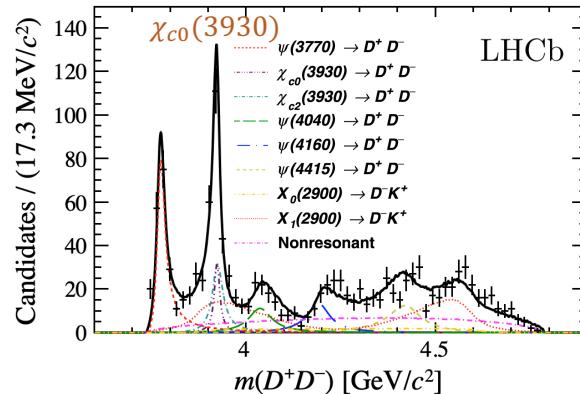
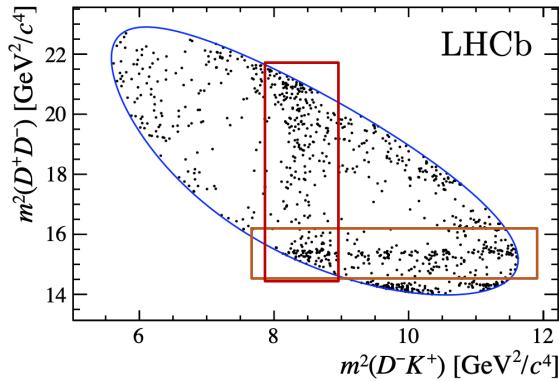
P states			
$I = 0$	$I = \frac{1}{2}$	$I = 1$	$I = \frac{3}{2}$
$\Lambda$	$N$	$\Sigma$	$\Delta$

Minimal quark content	Current name	$I^{(G)}, J^{P(C)}$	Proposed name	Reference
$c\bar{c}$	$\chi_{c1}(3872)$	$I^G = 0^+, J^{PC} = 1^{++}$	$\chi_{c1}(3872)$	[24, 25]
$c\bar{c}u\bar{d}$	$Z_c(3900)^+$	$I^G = 1^+, J^P = 1^+$	$T_{\psi 1}^b(3900)^+$	[26–28]
$c\bar{c}u\bar{d}$	$X(4100)^+$	$I^G = 1^-$	$T_\psi(4100)^+$	[29]
$c\bar{c}u\bar{d}$	$Z_c(4430)^+$	$I^G = 1^+, J^P = 1^+$	$T_{\psi 1}^b(4430)^+$	[30, 31]
$c\bar{c}(s\bar{s})$	$\chi_{c1}(4140)$	$I^G = 0^+, J^{PC} = 1^{++}$	$\chi_{c1}(4140)$	[32–35]
$c\bar{c}u\bar{s}$	$Z_{cs}(4000)^+$	$I = \frac{1}{2}, J^P = 1^+$	$T_{\psi s1}^\theta(4000)^+$	[7]
$c\bar{c}u\bar{s}$	$Z_{cs}(4220)^+$	$I = \frac{1}{2}, J^P = 1^?$	$T_{\psi s1}(4220)^+$	[7]
$c\bar{c}c\bar{c}$	$X(6900)$	$I^G = 0^+, J^{PC} = ?^?+$	$T_{\psi\psi}(6900)$	[4]
$c\bar{s}u\bar{d}$	$X_0(2900)$	$J^P = 0^+$	$T_{cs0}(2900)^0$	[5, 6]
$c\bar{s}u\bar{d}$	$X_1(2900)$	$J^P = 1^-$	$T_{cs1}(2900)^0$	[5, 6]
$c\bar{c}\bar{u}\bar{d}$	$T_{cc}(3875)^+$		$T_{cc}(3875)^+$	[8, 9]
$b\bar{b}u\bar{d}$	$Z_b(10610)^+$	$I^G = 1^+, J^P = 1^+$	$T_{\gamma 1}^b(10610)^+$	[36]
$c\bar{c}uud$	$P_c(4312)^+$	$I = \frac{1}{2}$	$P_\psi^N(4312)^+$	[3]
$c\bar{c}uds$	$P_{cs}(4459)^0$	$I = 0$	$P_{\psi s}^A(4459)^0$	[20]



# Story of $B^+ \rightarrow D^+ D^- K^+$

Phys. Rev. D102(2020) 112003  
Phys. Rev. Lett. 125 (2020) 242001



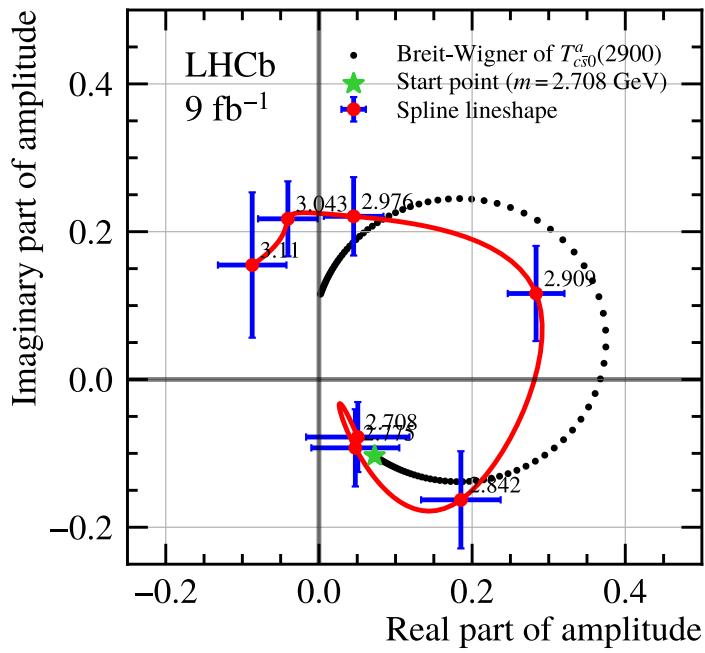
$T_{c\bar{s}0,1}(2900) \rightarrow D^- K^+$ : first  $c\bar{s}\bar{u}\bar{d}$  tetraquarks [arXiv:2204.02649](https://arxiv.org/abs/2204.02649)

- Some models predict its SU(3) flavour partners, e.g.  $T_{c\bar{s}} \rightarrow D_s \pi?$  Searched for in  $B \rightarrow \bar{D} D_s \pi$
- $\chi_{c0}(3930) \rightarrow D^+ D^-$ :  
  - It is suggested to be the same particle as  $\chi_{c0}(3915) \rightarrow J/\psi \omega$  [PDG 2020](https://pdg.lbl.gov/2020/reviews/surveys.html)
  - Some theories suggest that it is a  $c\bar{c} s\bar{s}$  tetraquark candidate

[JHEP 06 \(2021\) 035](https://doi.org/10.1007/JHEP06(2021)035)  
[Sci. Bull., 2021, 66: 1413](https://doi.org/10.1007/s41365-021-00143-1)

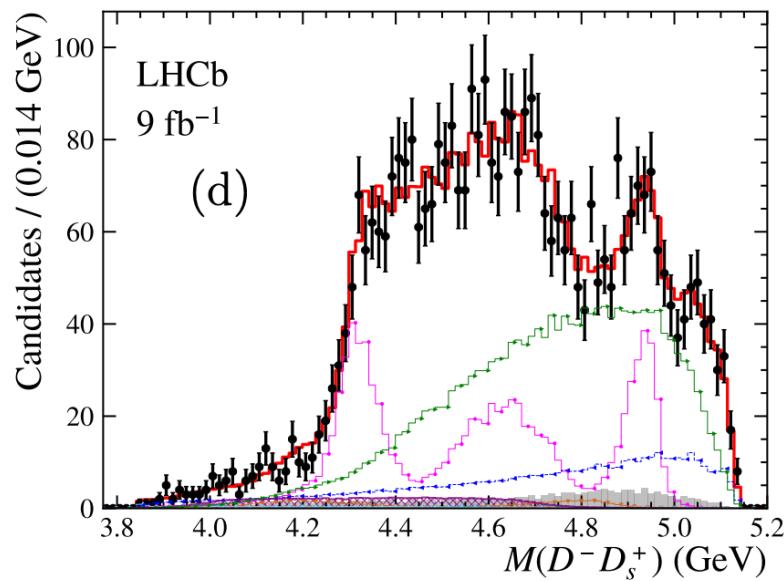
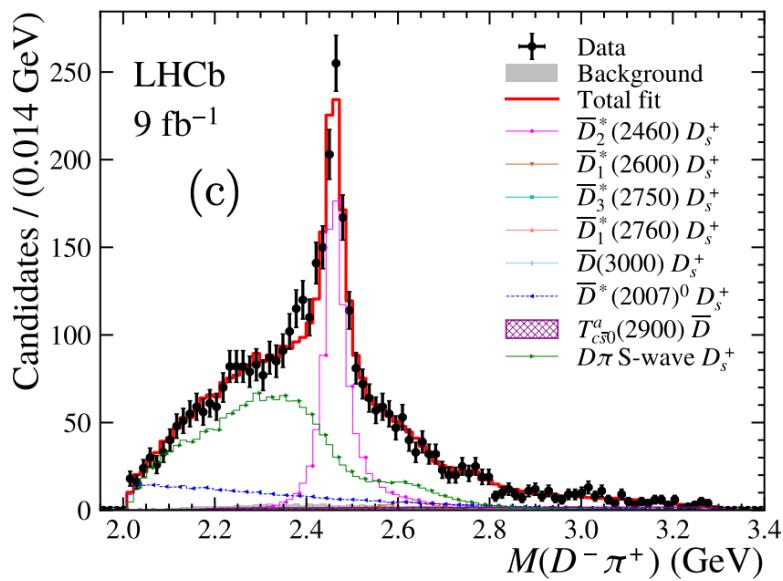
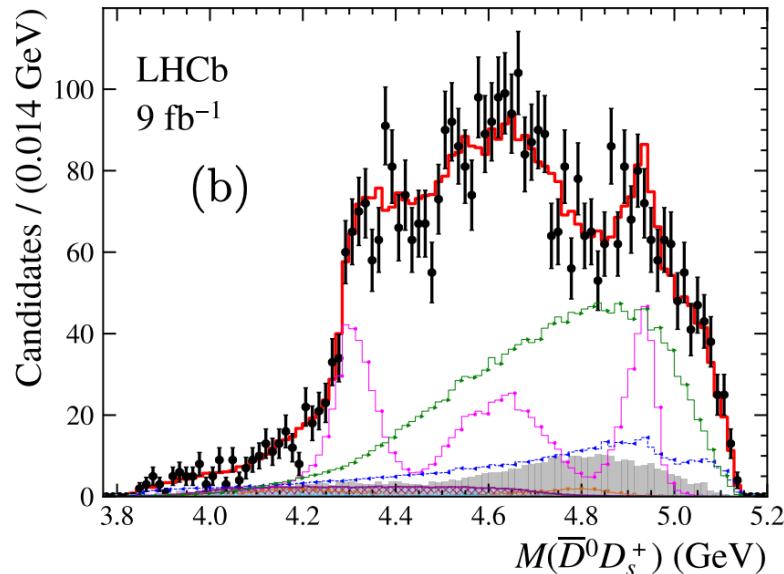
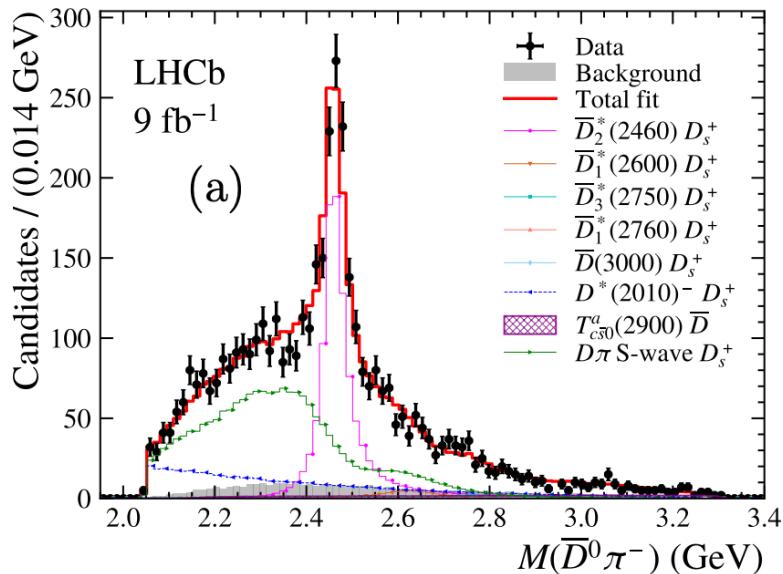
Search for  $\chi_{c0}(3930) \rightarrow D_s^+ D_s^-$  in  $B^+ \rightarrow D_s^+ D_s^- K^+$

# $T_{c\bar{s}0}^a(2900)$ Argand plot



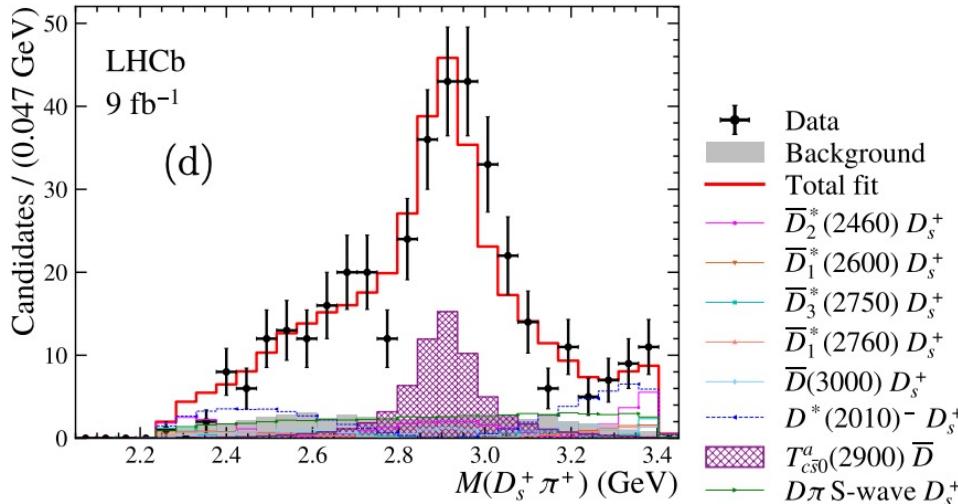
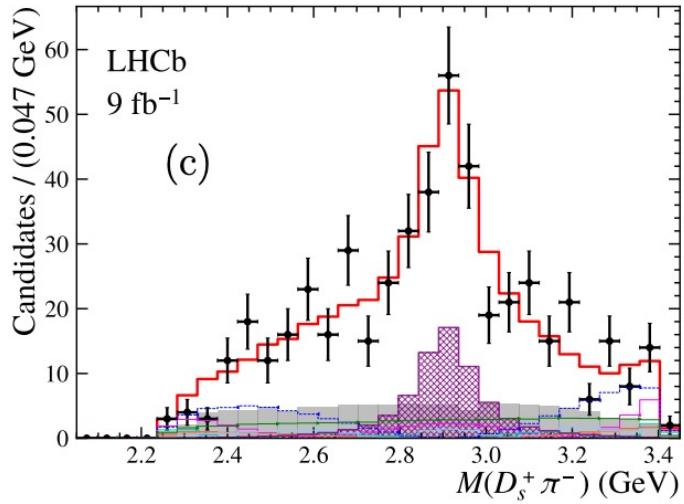
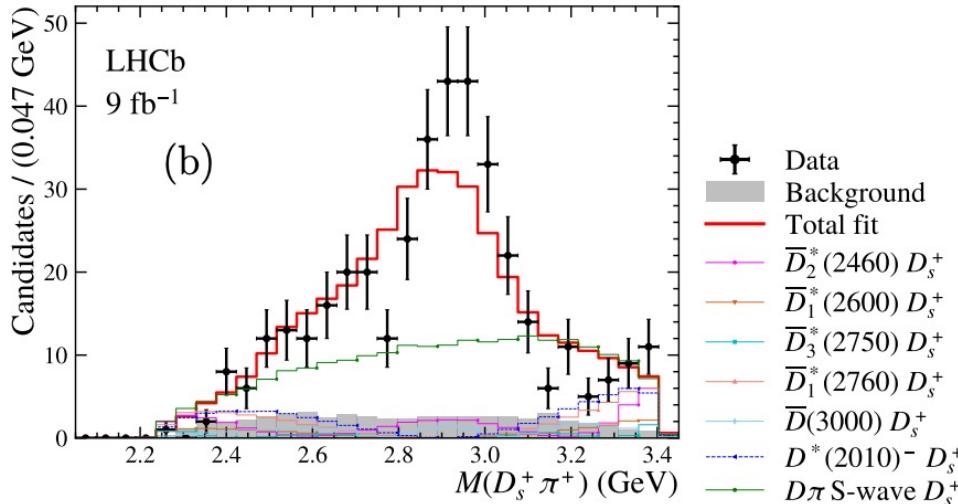
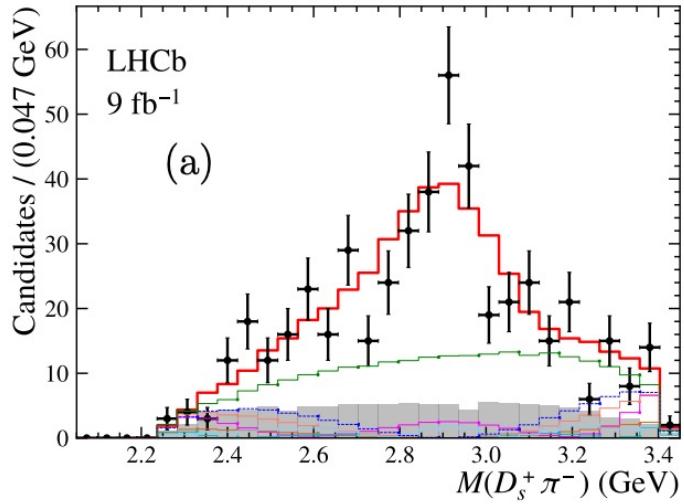
Spline and BW models both go anticlockwise  
 ->  
 Support the resonant nature of  $T_{c\bar{s}0}^a(2900)$

# Other projections



# Other projections

$m(\bar{D}\pi) > 2.7 \text{ GeV}$



# $B^+ \rightarrow D_s^+ D_s^- K^+$ fit results

arXiv:2210.15153

arXiv:2211.05034

- $\mathcal{F}$ : fit fraction
- $\mathcal{S}$  : significance

(numbers in brackets don't include systematic effect)

Component	$J^{PC}$	$M_0$ (MeV)	$\Gamma_0$ (MeV)	$\mathcal{F}$ (%)	$\mathcal{S}$ ( $\sigma$ )
$X(3960)$	$0^{++}$	$3956 \pm 5 \pm 10$	$43 \pm 13 \pm 8$	$25.4 \pm 7.7 \pm 5.0$	$12.6$ (14.6)
$X_0(4140)$	$0^{++}$	$4133 \pm 6 \pm 6$	$67 \pm 17 \pm 7$	$16.7 \pm 4.7 \pm 3.9$	$3.8$ (4.1)
$\psi(4260)$	$1^{--}$	4230	55	$3.6 \pm 0.4 \pm 3.2$	$3.2$ (3.6)
$\psi(4660)$	$1^{--}$	4633	64	$2.2 \pm 0.2 \pm 0.8$	$3.0$ (3.2)
NR	$0^{++}$	-	-	$46.1 \pm 13.2 \pm 11.3$	$3.1$ (3.4)

- Fixed parameters taken from PDG 2018/2020  
( $\psi(4260)$  is  $\psi(4230)$  in PDG2022)
- Spin-parity tests:
  - $X(3960)$ :  $0^{++}$  favored;  $1^{--}$  and  $2^{++}$  rejected by at least  $9\sigma$
  - $X_0(4140)$ :  $0^{++}$  favored;  $1^{--}$  and  $2^{++}$  rejected by at least  $3.5\sigma$

# K-matrix model for $X(3960)$

$$\begin{pmatrix} \mathcal{M}_{D_s^+ D_s^- \rightarrow D_s^+ D_s^-} & \mathcal{M}_{D_s^+ D_s^- \rightarrow J/\psi \phi} \\ \mathcal{M}_{J/\psi \phi \rightarrow D_s^+ D_s^-} & \mathcal{M}_{J/\psi \phi \rightarrow J/\psi \phi} \end{pmatrix} \equiv \begin{pmatrix} \mathcal{K}_{11} & \mathcal{K}_{12} \\ \mathcal{K}_{21} & \mathcal{K}_{22} \end{pmatrix}$$

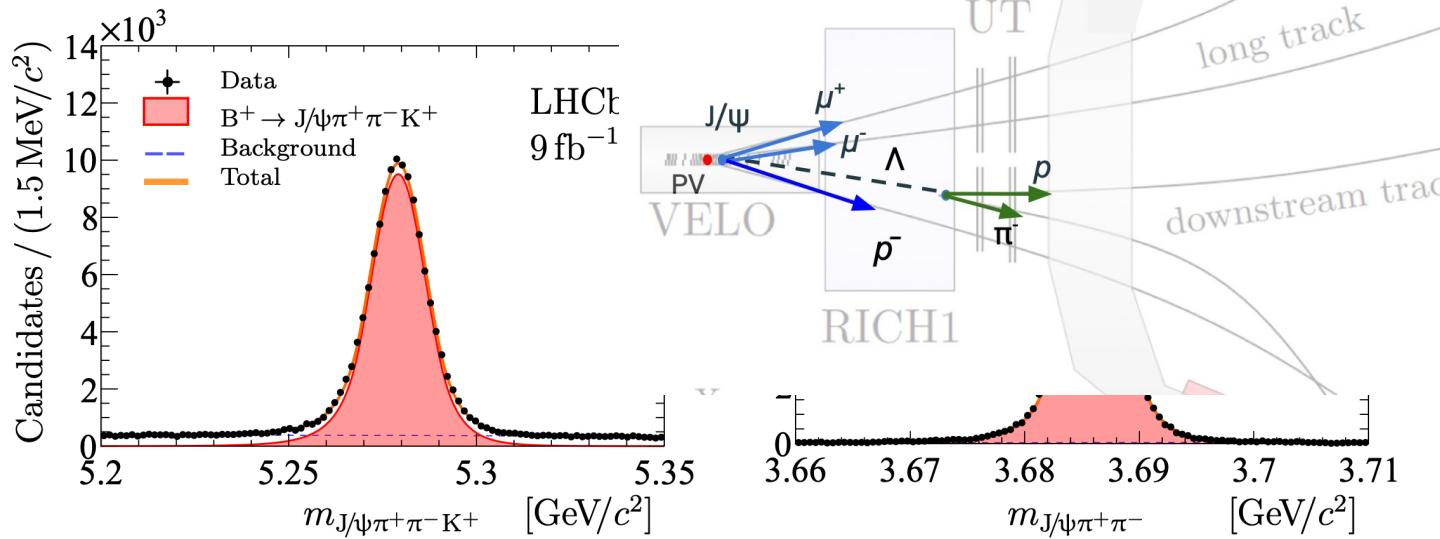
$$\mathcal{K}_{ab}(m) = \sum_R \frac{g_b^R g_a^R}{M_R^2 - m^2} + f_{ab}$$

$$\mathcal{P}_b(m) = \sum_R \frac{\beta_R g_b^R}{M_R^2 - m^2} + \beta_b$$

$$\mathcal{M}_a = \sum_b (I - i\rho\mathcal{K})_{ab}^{-1} \mathcal{P}_b$$

Contribution	$J^{PC}$	$M_R$ (MeV)	$g_1^R$ (MeV)	$\Gamma_\psi$ (MeV)	$\mathcal{F}$ (%)
$ \mathcal{M}_1 ^2$	$0^{++}$	$3957 \pm 14$	$1350 \pm 344$		$94.7 \pm 0.4$
$\psi(4260)$	$1^{--}$	$4230$ [59]		$55$ [59]	$3.2 \pm 0.5$
$\psi(4660)$	$1^{--}$	$4633$ [31]		$64$ [31]	$2.1 \pm 0.2$
$\beta_R$		$(1, 0i)$	$\beta_1$	$(-1.2, 2.5i) \pm (4.5, 3.1i)$	
$\beta_2$		$(-137.2, -1.5i) \pm (2.7, 218.6i)$	$f_{11}$		$0.8 \pm 1.2$
$f_{12} = f_{21}$		$0.1 \pm 0.1$	$f_{22}$		$8.0 \pm 5.1$

Large  
uncertainties.  
Larger data  
sample is  
needed

$B^+ \rightarrow J/\psi \eta' K^+$ 


$$\frac{\mathcal{B}(B^+ \rightarrow J/\psi \eta' K^+)}{\mathcal{B}(B^+ \rightarrow \psi(2S) K^+)} = (4.91 \pm 0.47 \pm 0.29 \pm 0.07) \times 10^{-2}$$

Source	Value [%]
$B^+$ kinematics	0.1
$B^+$ decay model	1.1
Tracking efficiency correction	0.7
Photon reconstruction correction	3.6
Kaon identification	2.8
Trigger efficiency	1.1
Data-simulation agreement	3.0
Fit model	1.6
Simulation sample size	0.9
Total	6.0