

Role of a triangular singularity in the $\gamma p \rightarrow p \pi^0 \eta$ reaction

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for the CBELSA/TAPS Collaboration

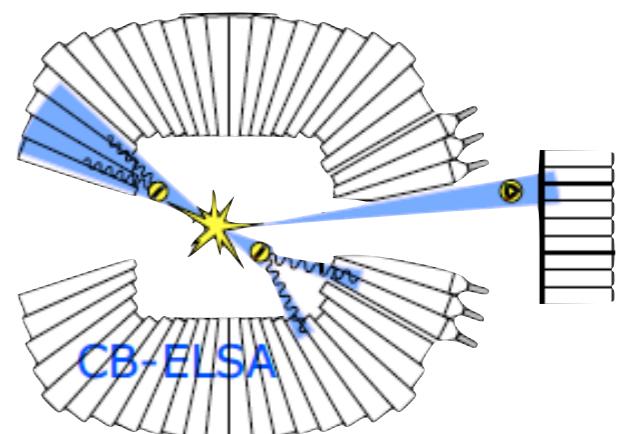
Outline:

- ❖ observation and characterisation of a structure at $M_{p\eta} \approx 1710$ MeV
- ❖ interpretation: triangular singularity at opening of the $\gamma p \rightarrow p a_0$ channel
- ❖ summary and conclusions



Experimental Physics II

Exotic Hadron Spectroscopy 2023
April 19-21, 2022
Durham University, United Kingdom



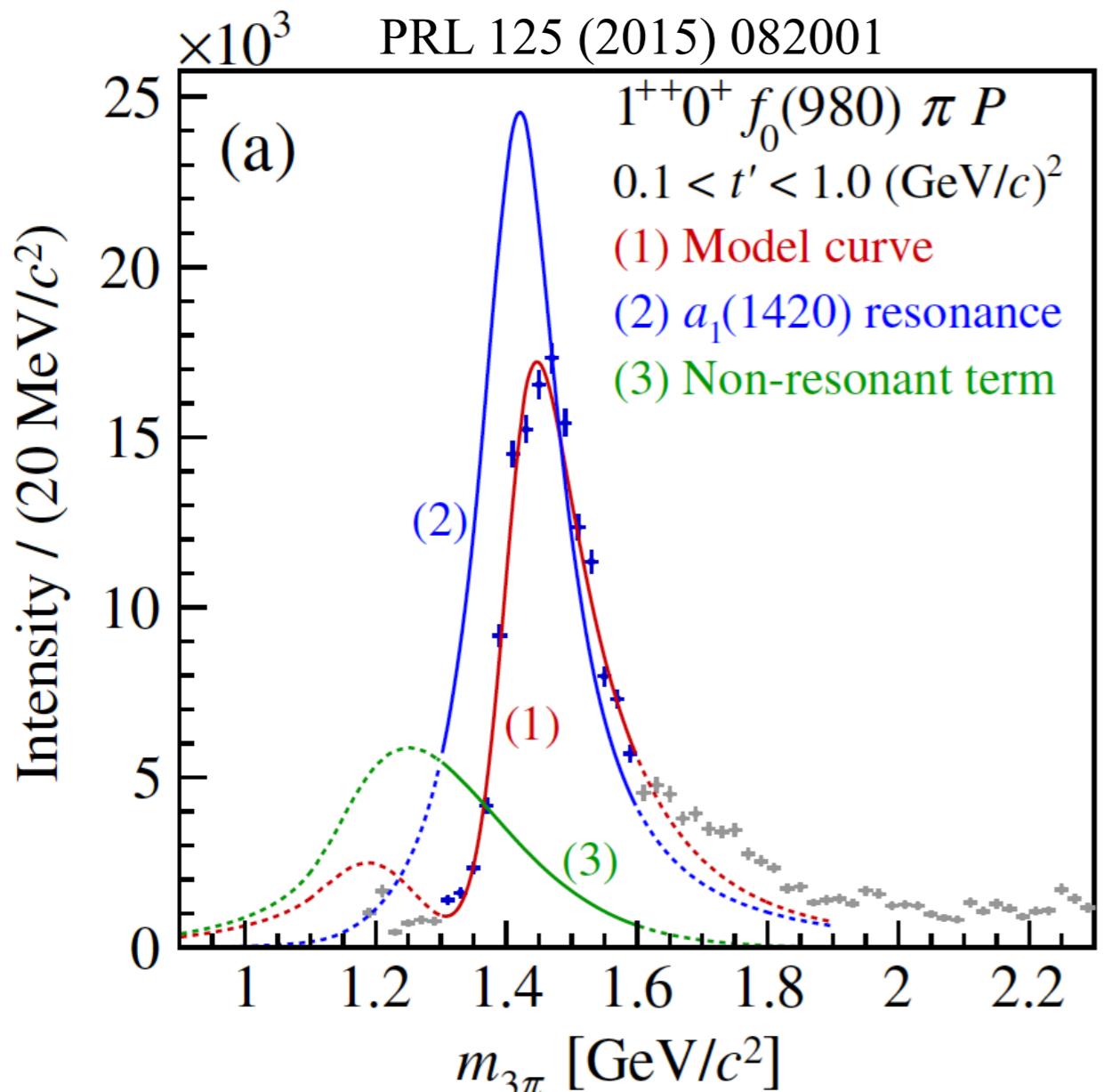
triangular singularities in hadronic reactions

diffractive $\pi^- p$ scattering at 190 GeV



COMPASS collaboration

PRL 125 (2015) 082001



resonance like signal in $\pi^- \pi^- \pi^+$ final state

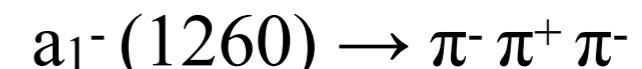
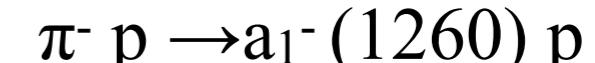
genuine new state: $a_1(1420)$??
difficult to explain within quark model
tetra-quark resonance ??

M. Mikhasenko, B. Ketzer, A Sarantsev

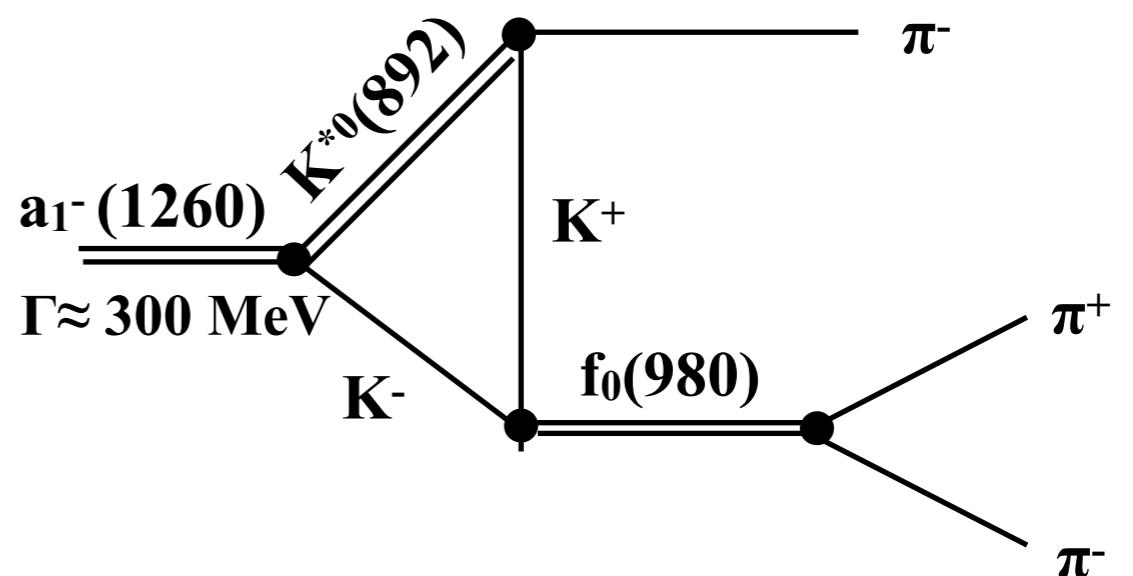
PRD 91 (2015) 094105

COMPASS collaboration

PRL 127 (2021) 082501



triangular diagram

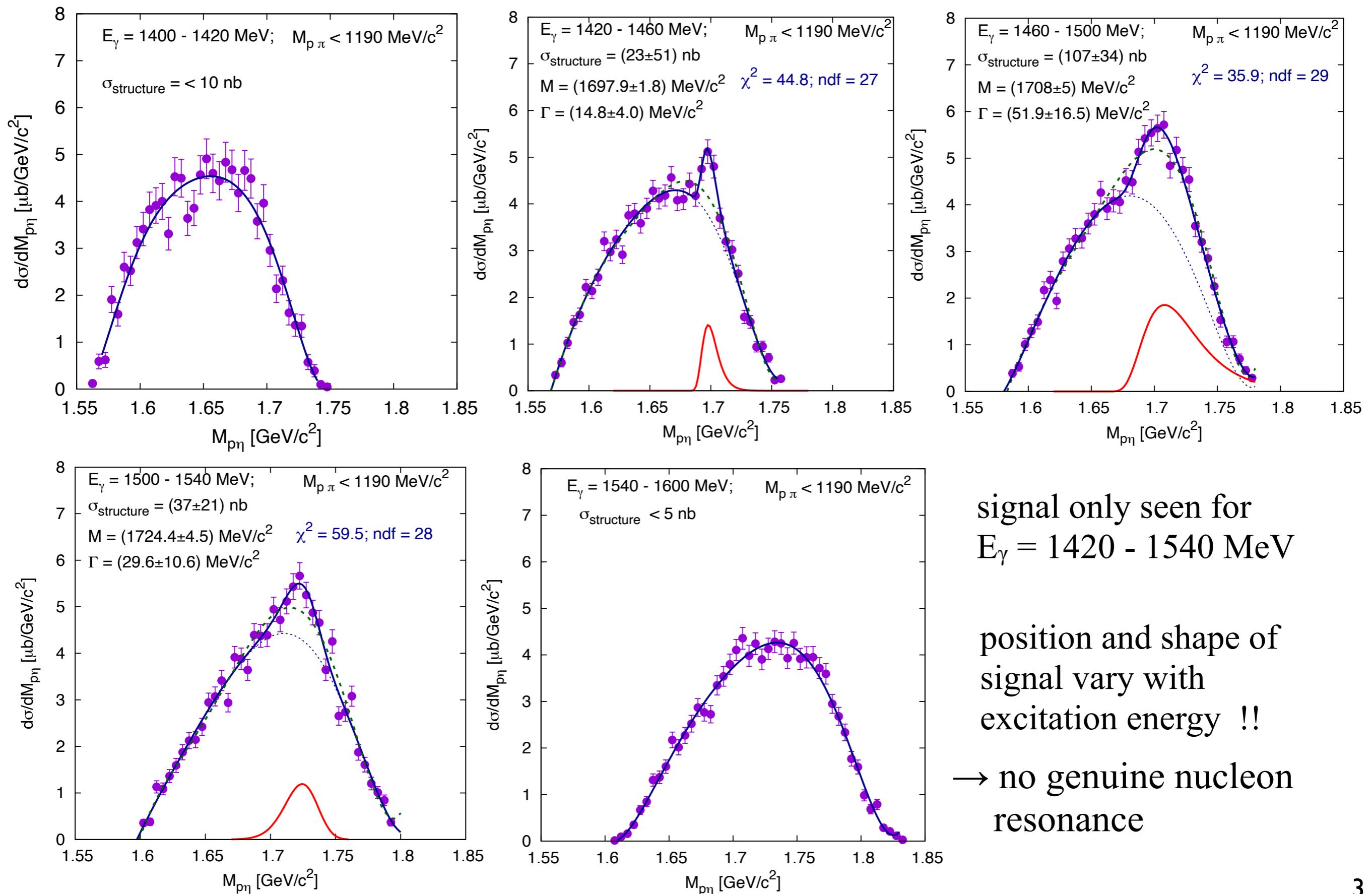


three point (triangular) loop generates structure (singularity) at $\sqrt{s} = 1420 \text{ MeV}$

many other cases in meson sector:

F-K.Guo, X-H.Liu, S.Sakai
Prog. Part. Nucl. Phys. 112 (2020) 103757

properties of structures as function of the incident photon energy



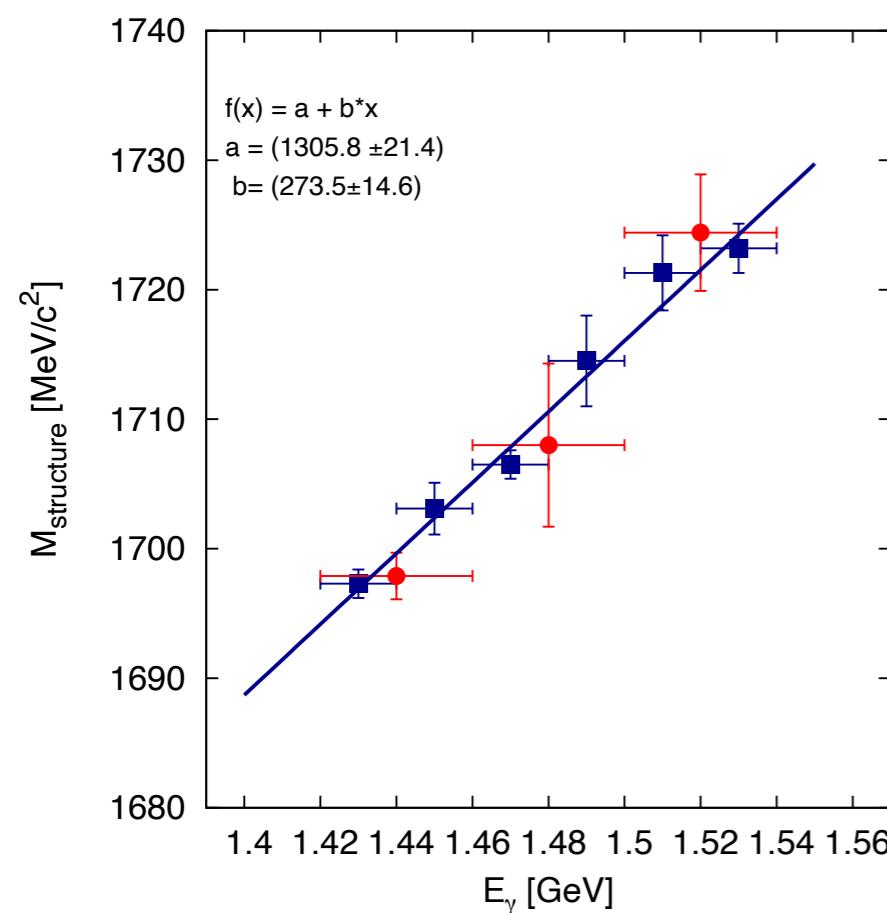
properties of the structure as function of the excitation energy

signal fitted with Novosibirsk function

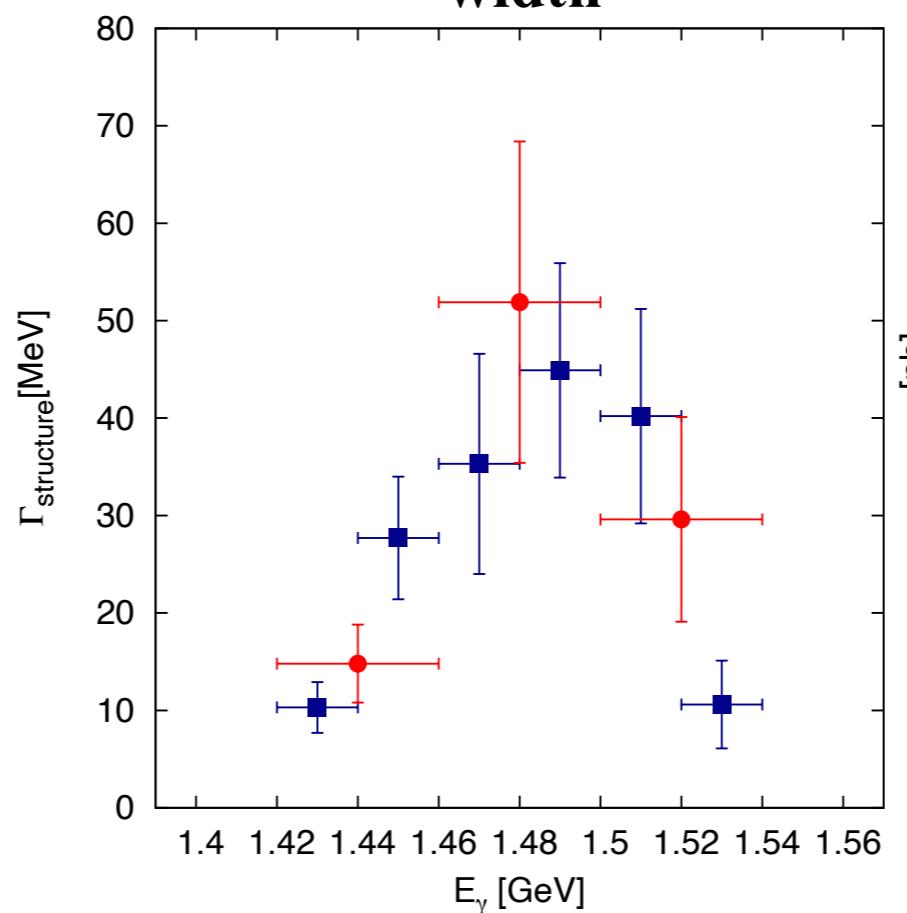
signal fitted with Gaussian function

systematic error of fits (different fit functions): $\leq 15\%$

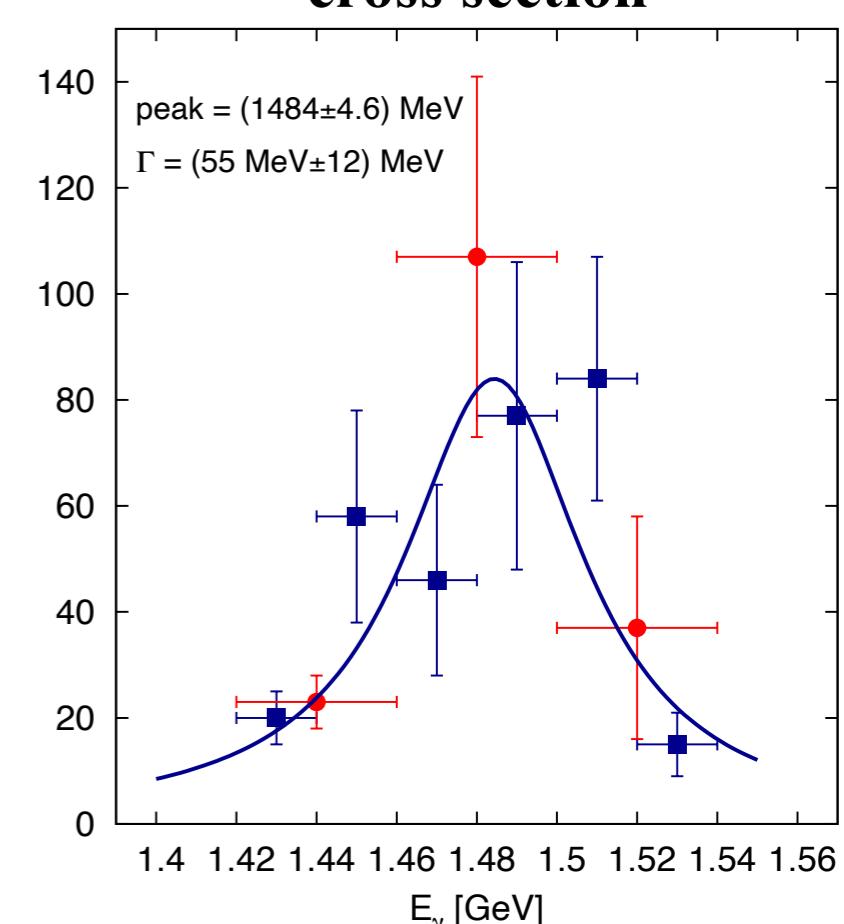
peak position



width



cross section



I. peak shifts with incident energy

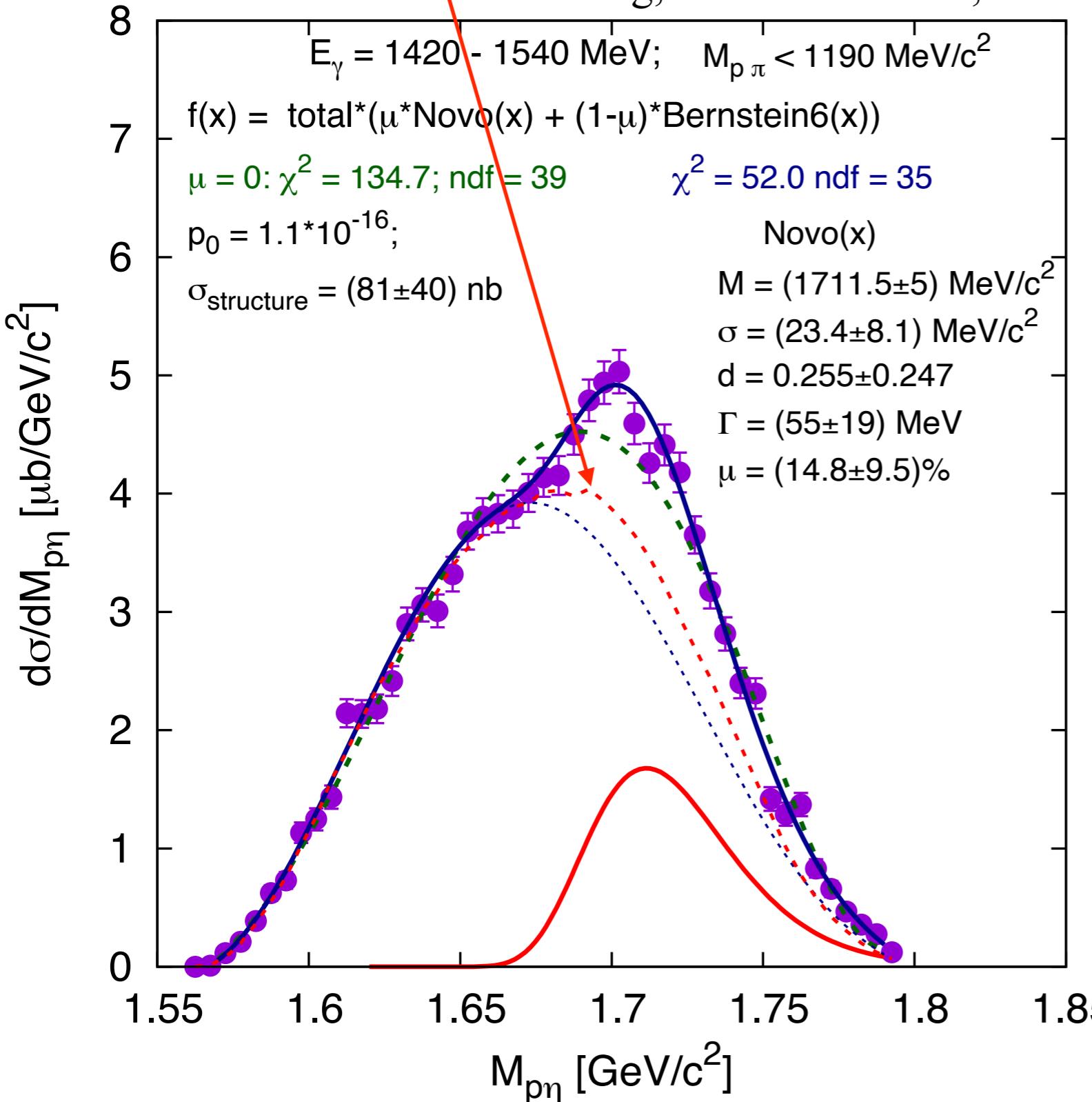
II. width: $\Gamma \leq 50 \text{ MeV}$

III. resonance-like cross section peaking at
 $E_\gamma = 1490 \text{ MeV} (\gamma p \rightarrow p a_0 \rightarrow p \pi^0 \eta \text{ threshold})$

observation of a structure at $M_{p\eta} \approx 1710$ MeV in the $\gamma p \rightarrow p \pi^0 \eta$ reaction

comparison to PWA: BnGa 2016-02 (normalized to data in $1550 \text{ MeV} < M_{p\eta} < 1680 \text{ MeV}$)

V. Metag, M. Nanova et al., EPJA 57 (2021) 325



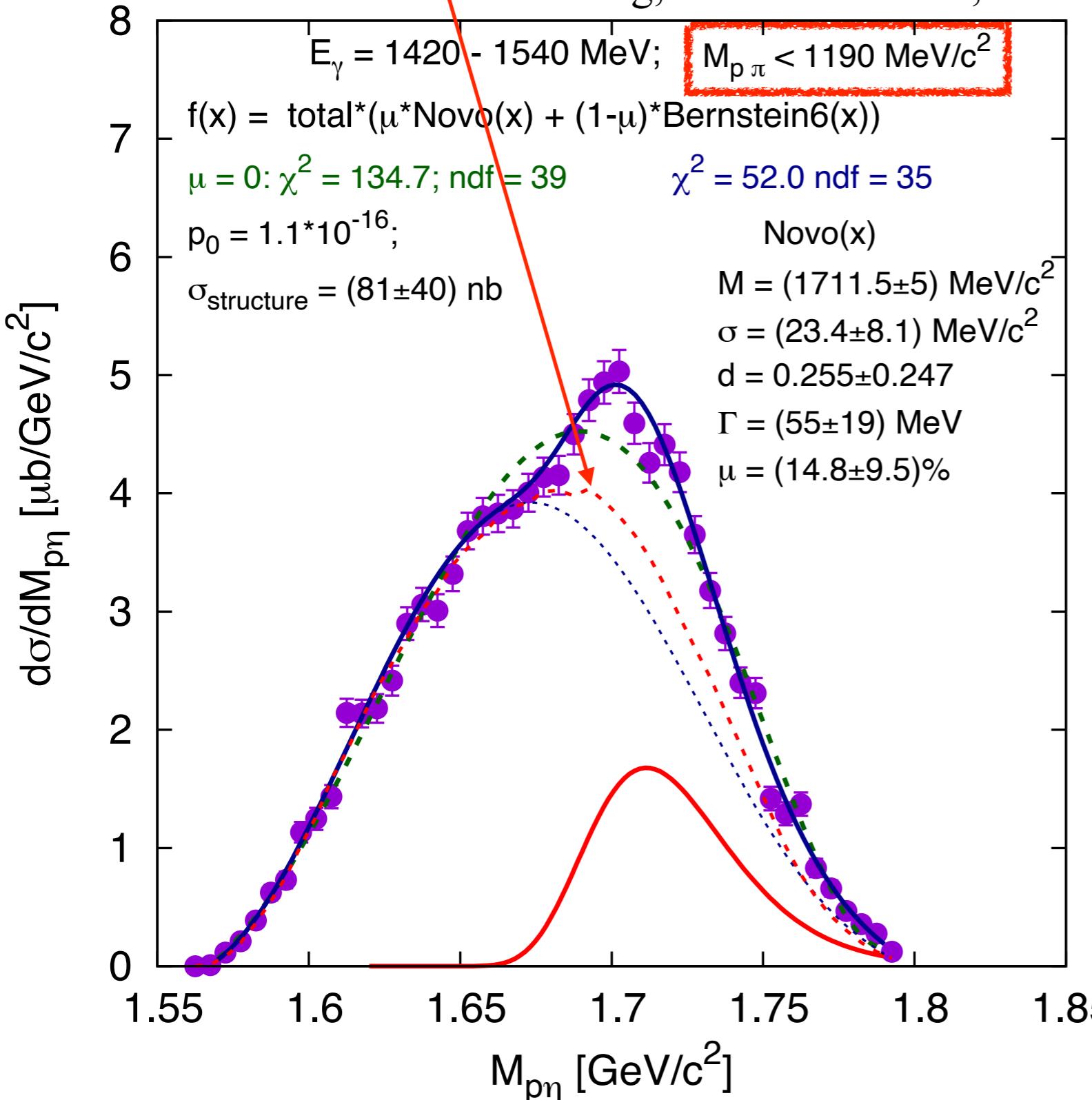
structure established with 6σ

characterisation of structure: { 1.) by fit of signal
2.) by deviation from PWA

observation of a structure at $M_{p\eta} \approx 1710$ MeV in the $\gamma p \rightarrow p \pi^0 \eta$ reaction

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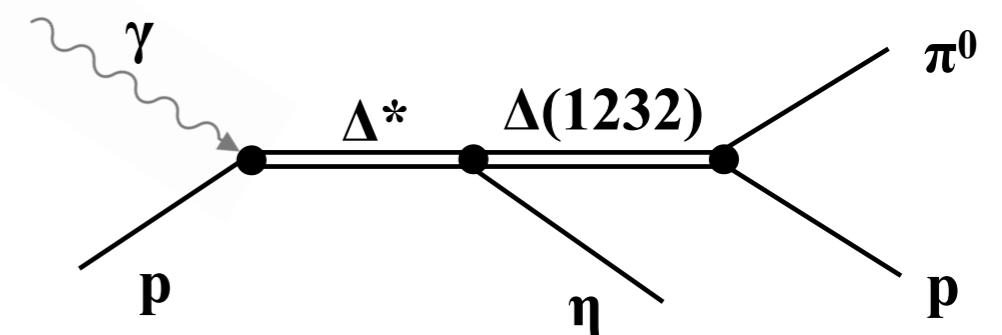
V. Metag, M. Nanova et al., EPJA 57 (2021) 325



structure established with 6σ

$M_{p\pi}$ cut applied to suppress dominant decay chain via the $\Delta(1232)$ resonance

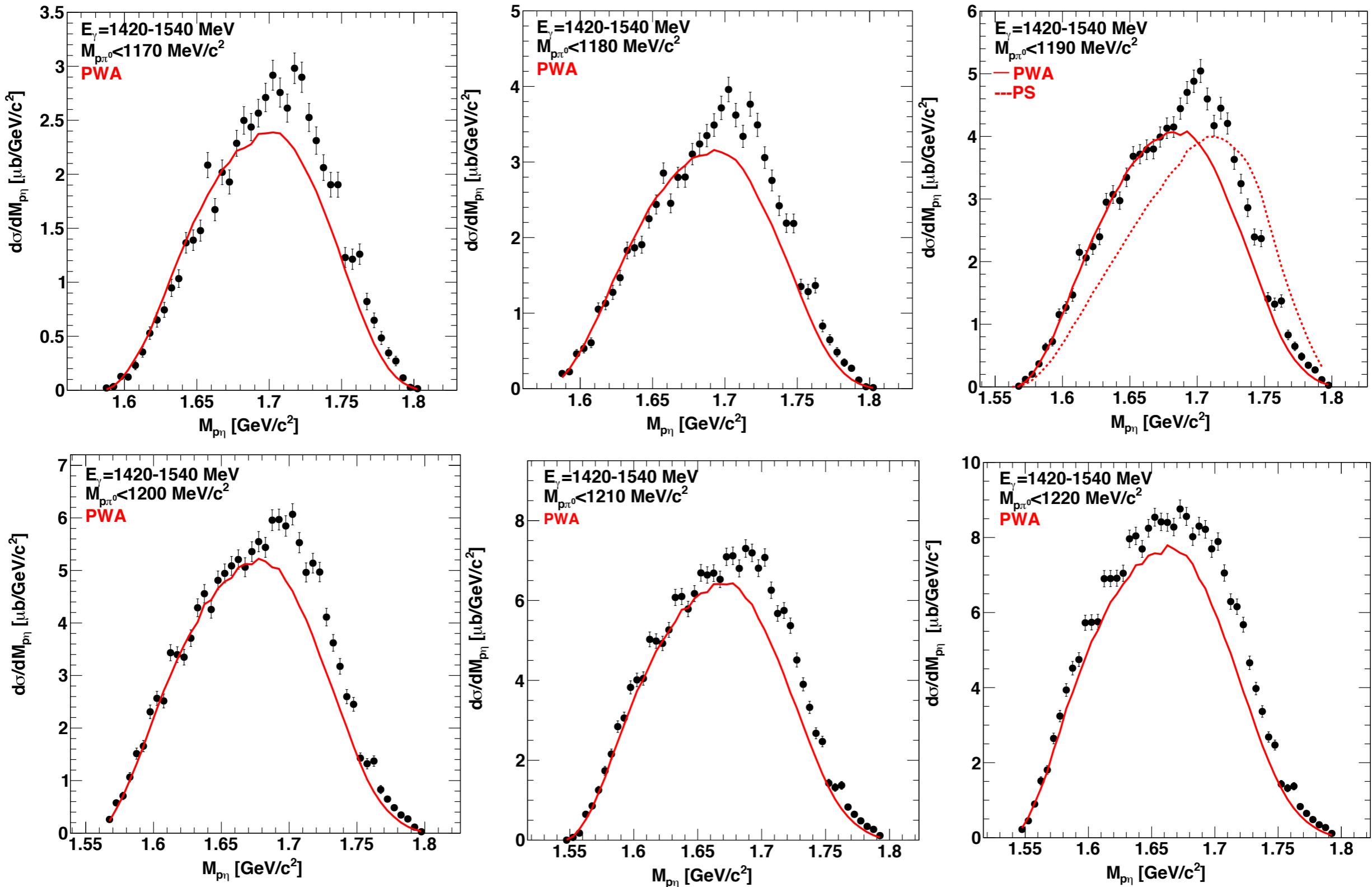
tree level diagram:



characterisation of structure: { 1.) by fit of signal
2.) by deviation from PWA

$\gamma p \rightarrow p \pi^0\eta; E_\gamma = 1420 - 1540 \text{ MeV}$

comparison to partial wave analysis (PWA) /and phase space distribution (PS)



structure not reproduced by PWA; excess also seen for different $M_{p\pi^0}$ cuts

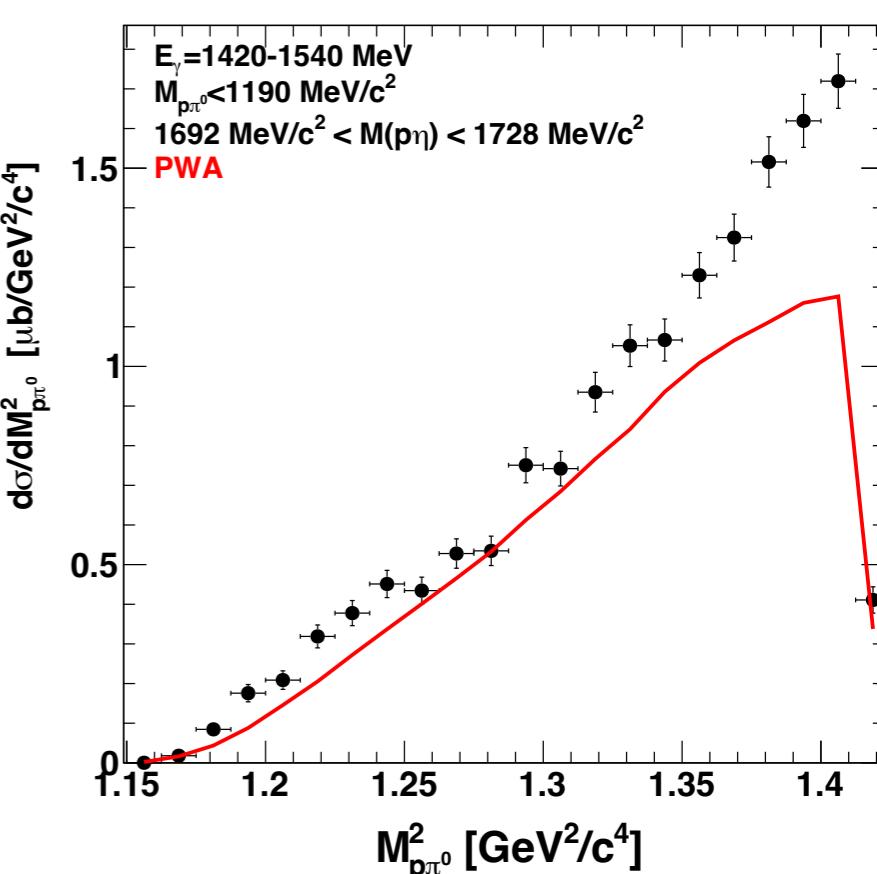
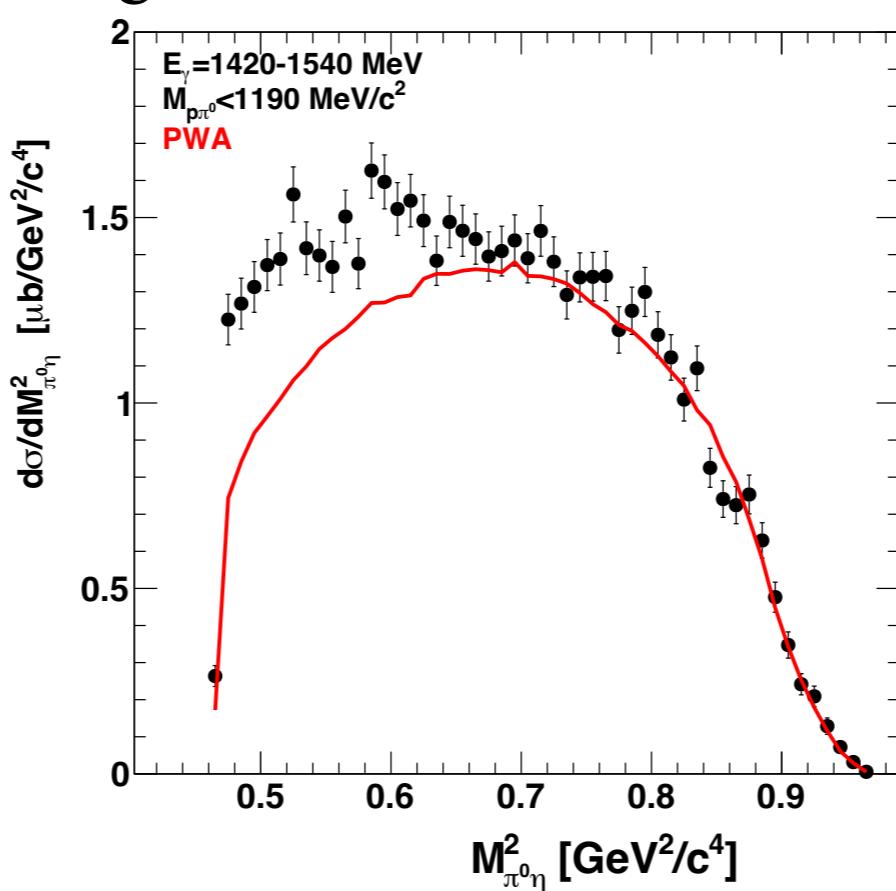
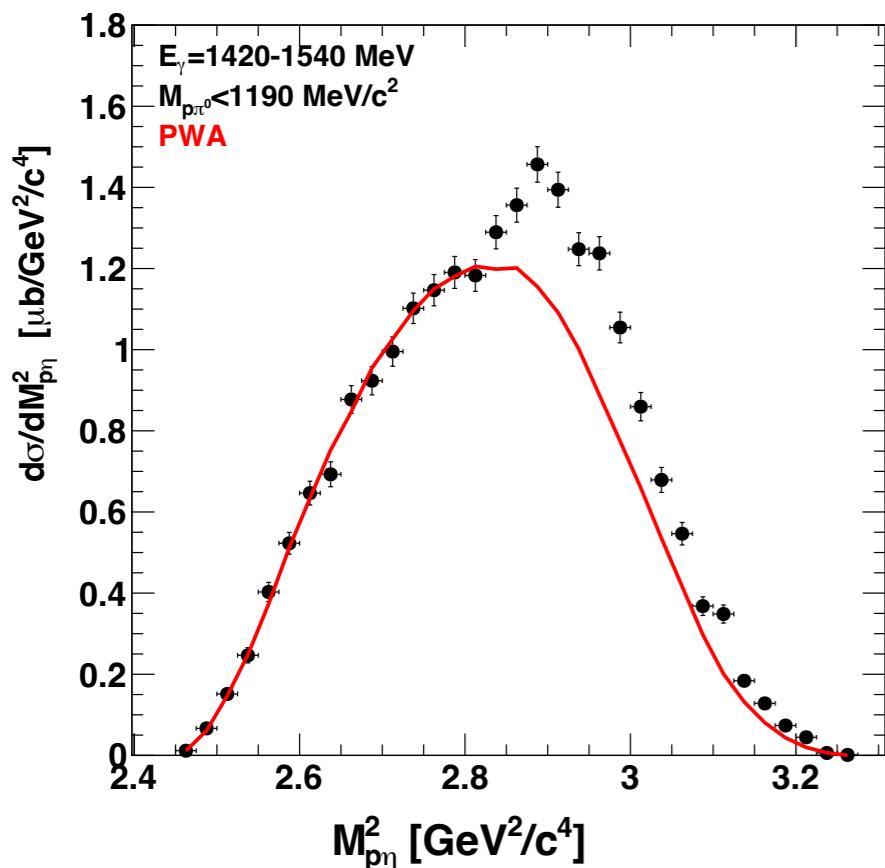
structure not caused by cut $M_{p\pi^0} < 1190 \text{ MeV}$

$M_{p\pi^0} < 1190 \text{ MeV}$

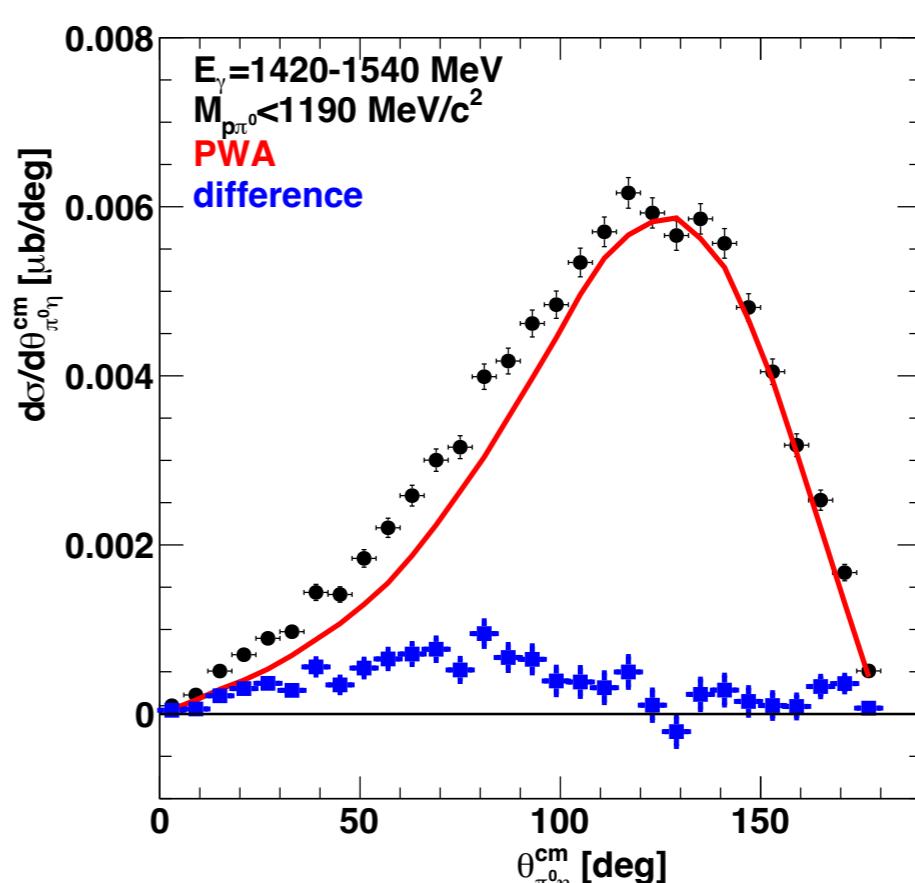
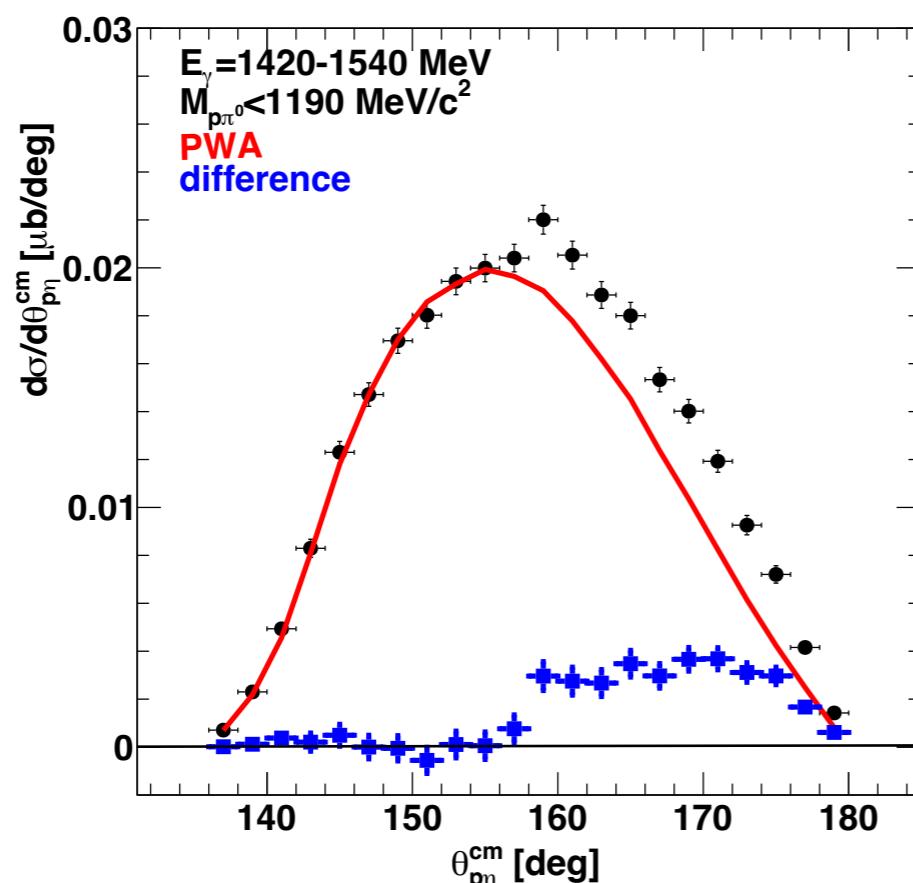
$\gamma p \rightarrow p \pi^0 \eta; E_\gamma = 1420 - 1540 \text{ MeV}$

$(1190 \text{ MeV})^2$

signal = deviation from PWA

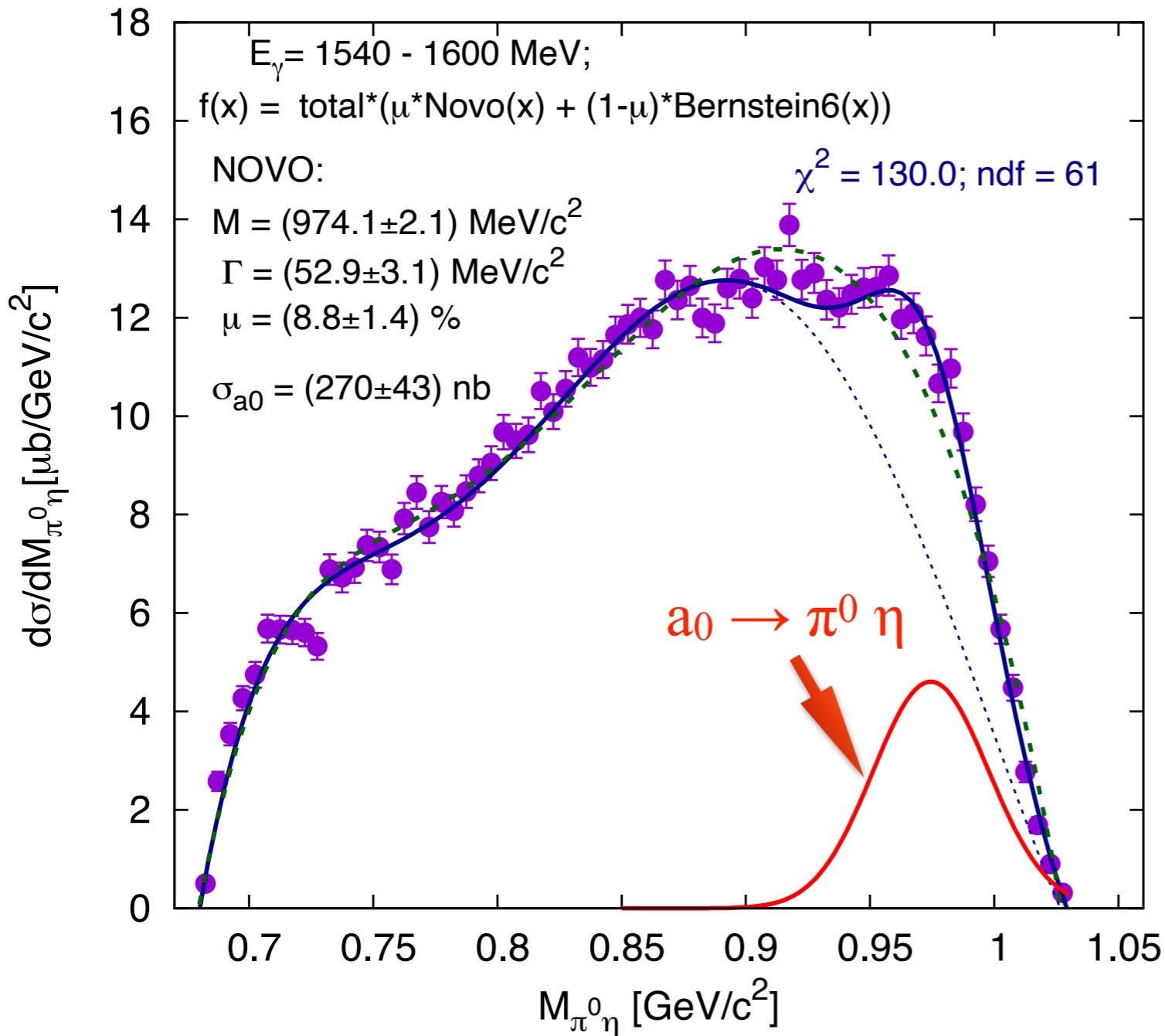


predominant
back-to-back
emission in
 γp -cm-system



deviation for
 $\theta_{\pi^0\eta} \approx 20^\circ - 90^\circ$
 γp -cm-system

γ p \rightarrow p $\pi^0\eta$; direct observation of an a₀ signal



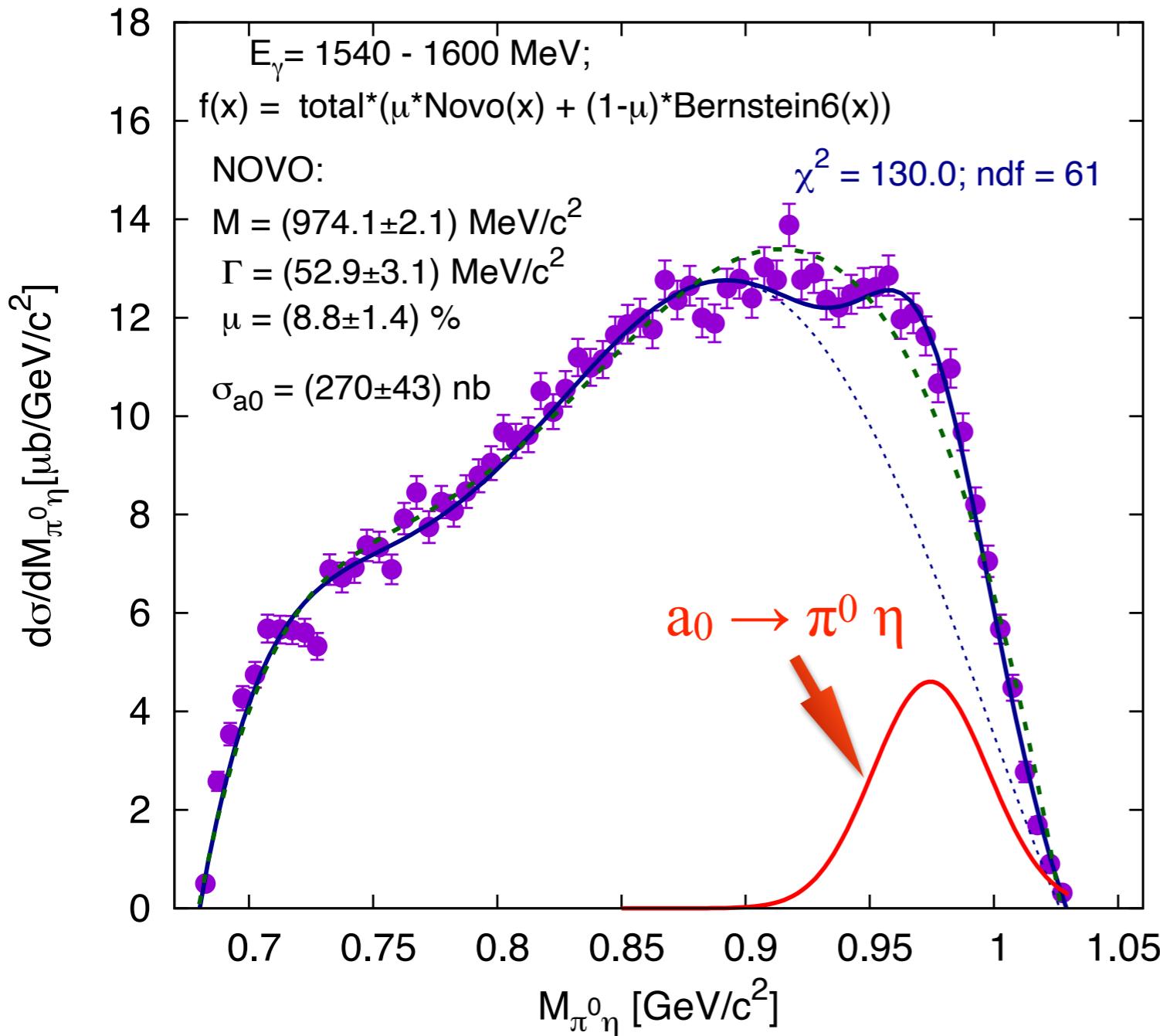
$$m_{a_0} = 974 \pm 2 \text{ MeV}; \quad \Gamma_{a_0} = 53 \pm 3 \text{ MeV}$$

$$\text{PDG: } m_{a_0} = 980 \pm 20 \text{ MeV}; \quad \Gamma_{a_0} = 50 - 100 \text{ MeV}$$

$$\sigma_{a_0} = 270 \pm 43 \text{ nb}; \quad \sigma_{a_0} (\text{PWA}) = 250 \text{ nb}$$

for $m_{a_0} > 990 \text{ MeV}$ $a_0 \rightarrow K^+K^-$ dominant

$\gamma p \rightarrow p \pi^0 \eta$; direct observation of an a_0 signal



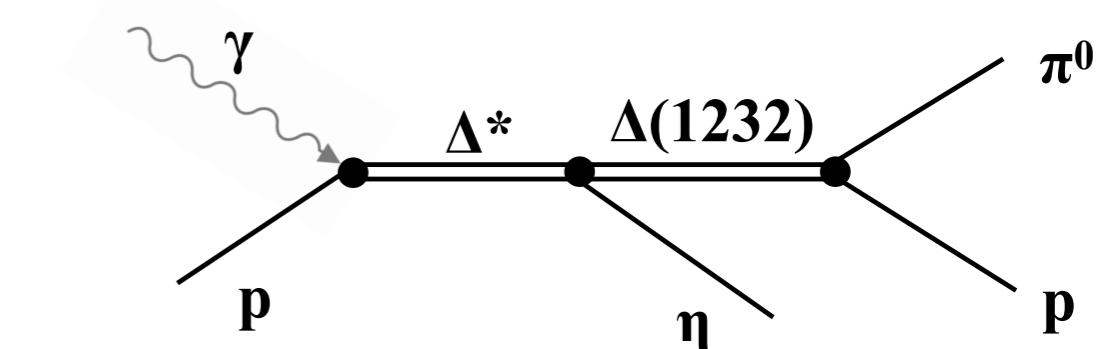
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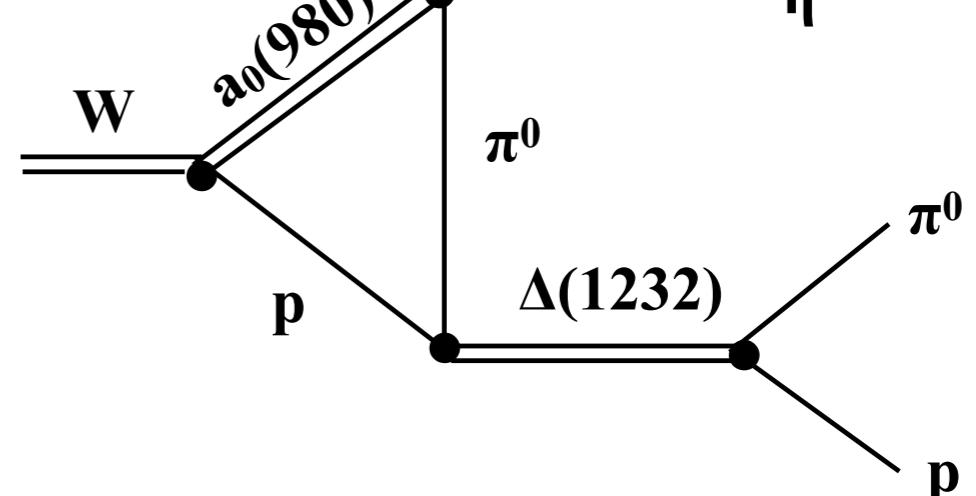
$$\sigma_{a_0} = 270 \pm 43 \text{ nb}; \quad \sigma_{a_0} (\text{PWA}) = 250 \text{ nb}$$

for $m_{a_0} > 990 \text{ MeV}$ $a_0 \rightarrow K^+K^-$ dominant

tree level diagram:
(suppressed by $M_{p\pi} < 1190 \text{ MeV}$ cut)

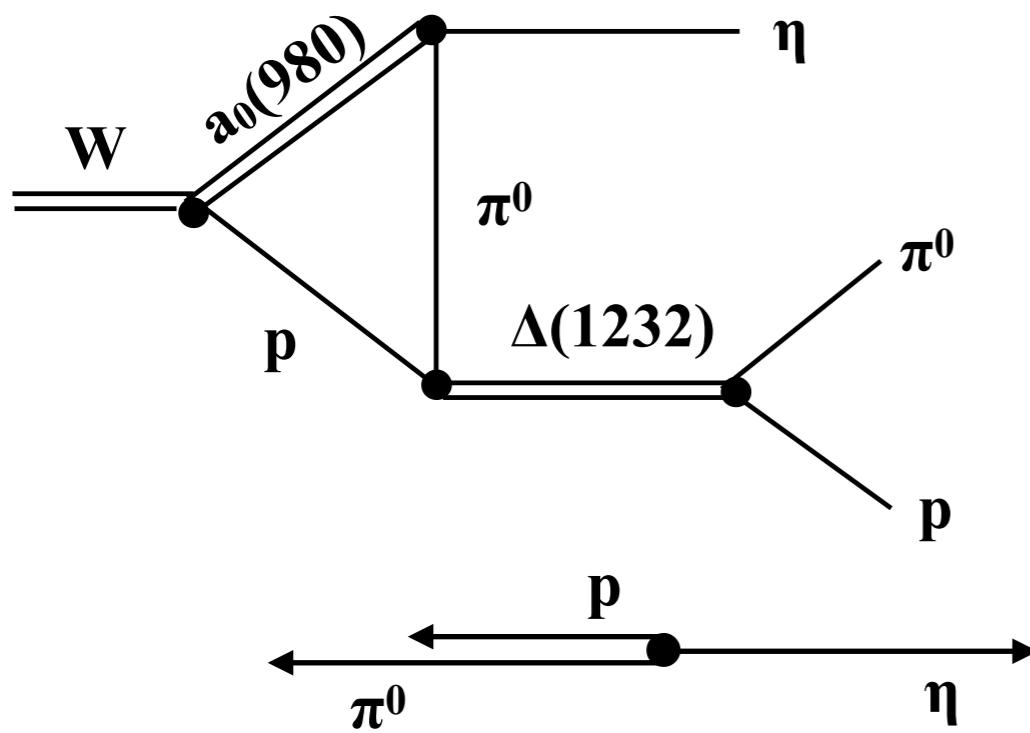


triangular diagram:



calculating triangular singularities

triangular diagram:



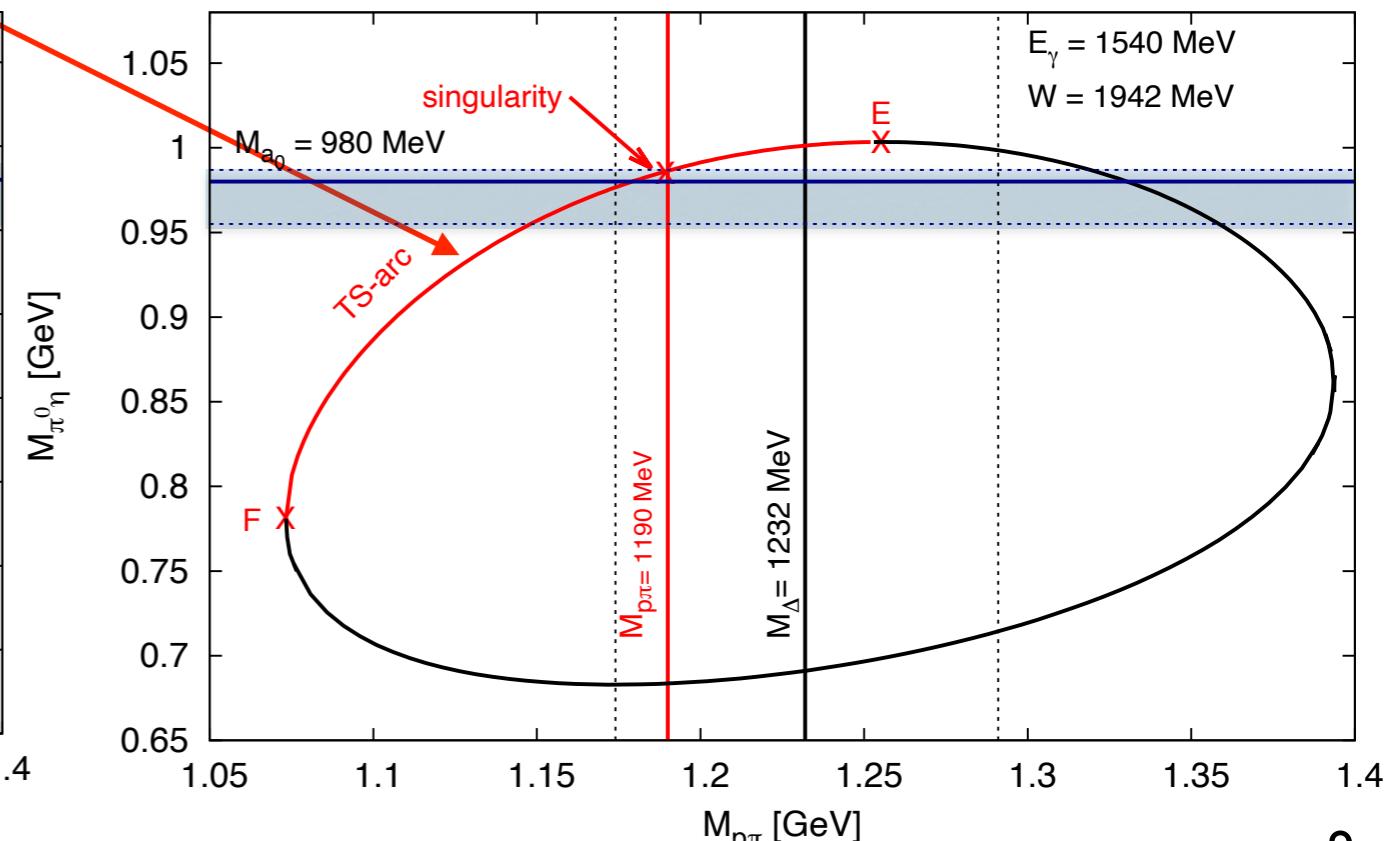
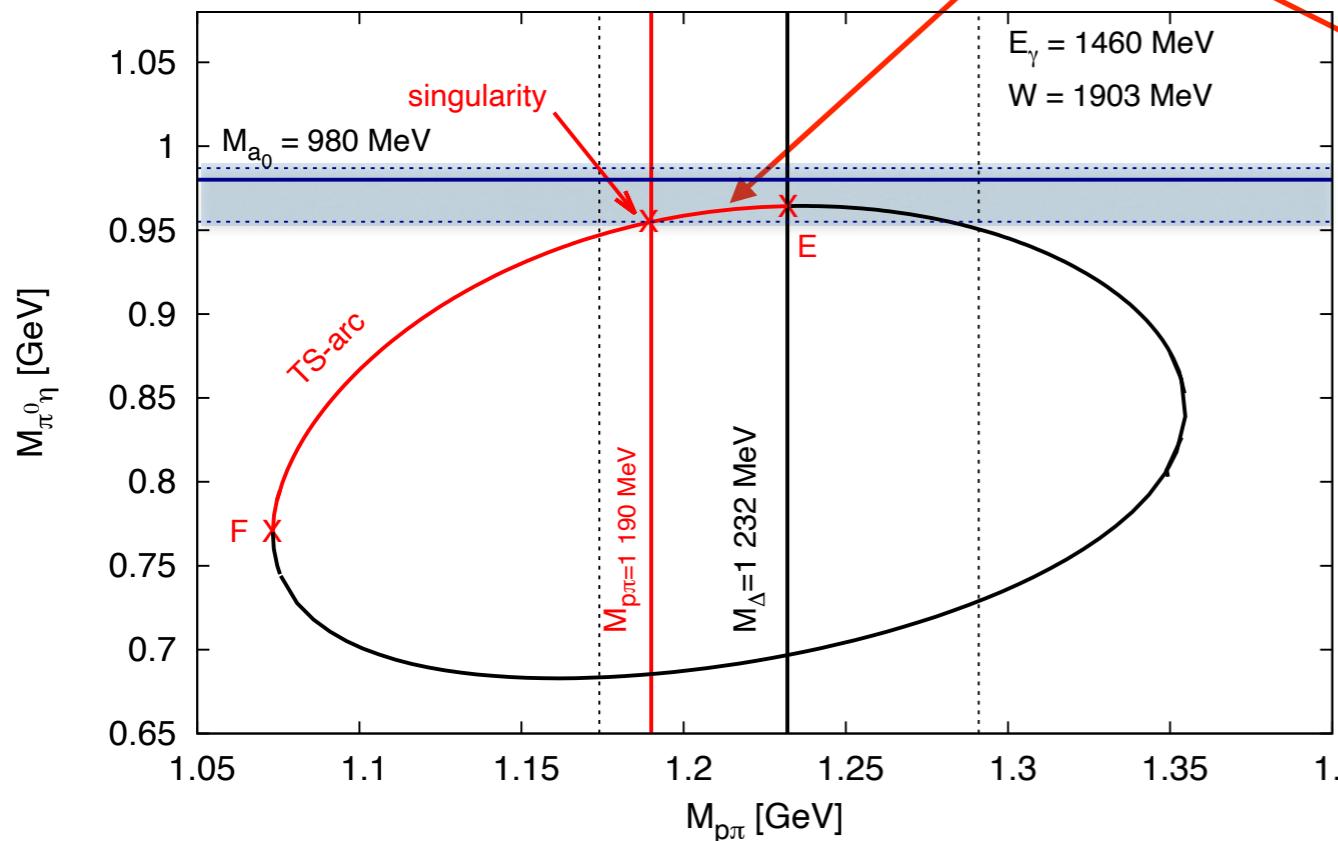
Bayar et al. PRD 94 (2016) 074039

the triangular diagram leads to an enhancement at the a_0 threshold;

- 1.) energy/mom. balance: internal \leftrightarrow external
- 2.) all internal particles almost on mass shell
- 3.) p, π^0, η collinear:

F-K.Guo, X-H.Liu, S.Sakai

Prog. Part. Nucl. Phys. 112 (2020) 103757



Calculation of triangular singularity strength

$$m_p + m_{a0} = 1918 \text{ MeV}$$

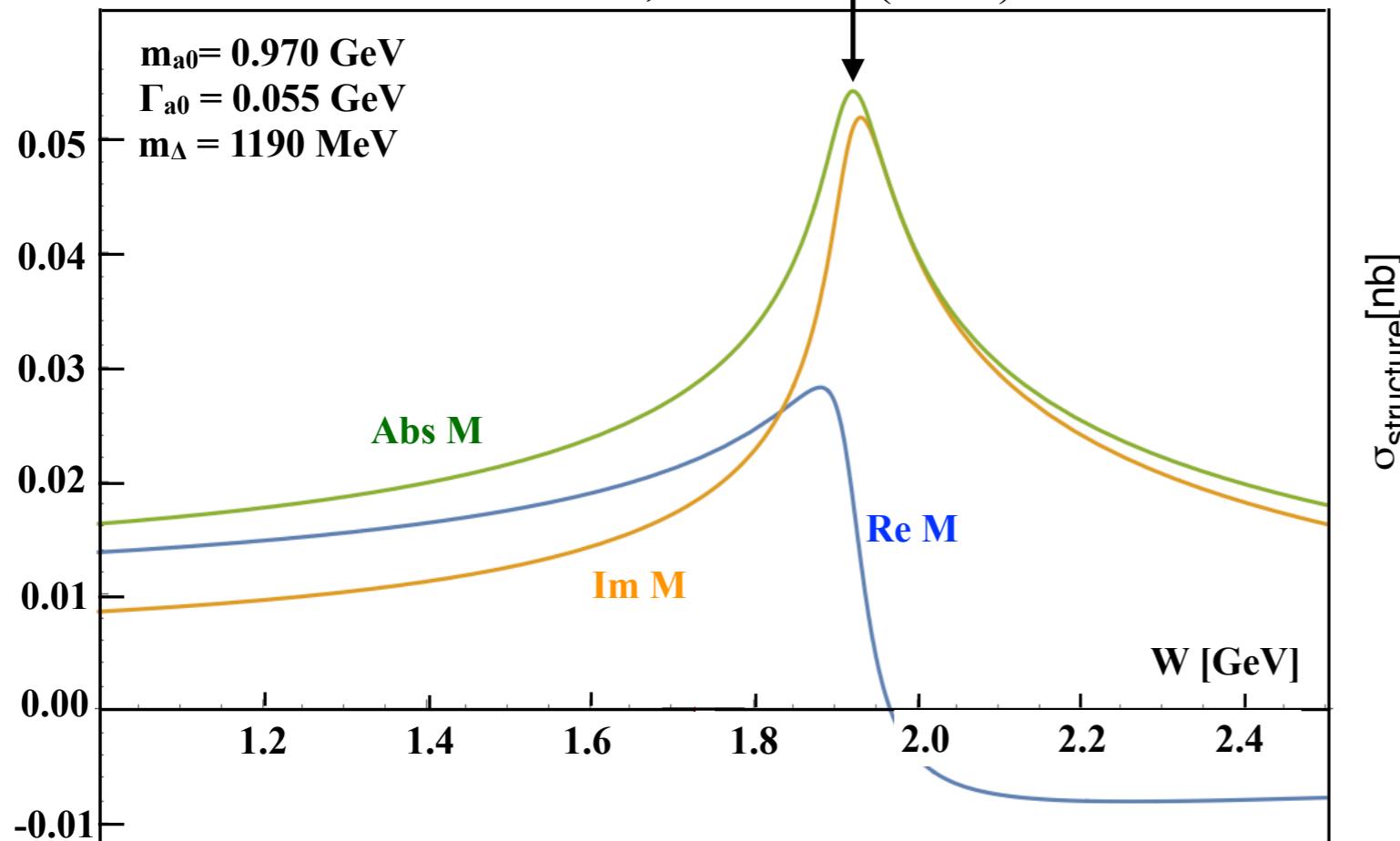
$$W = 1918 \text{ MeV}$$

$$E_\gamma = 1492 \text{ MeV}$$

thanks to Mathias Wagner and Bernhard Ketzer (Univ. Bonn)

M. Mikhasenko et al., PRD 91 (2015) 094015

G.D. Alexeev et al., PRL 127 (2021) 082501

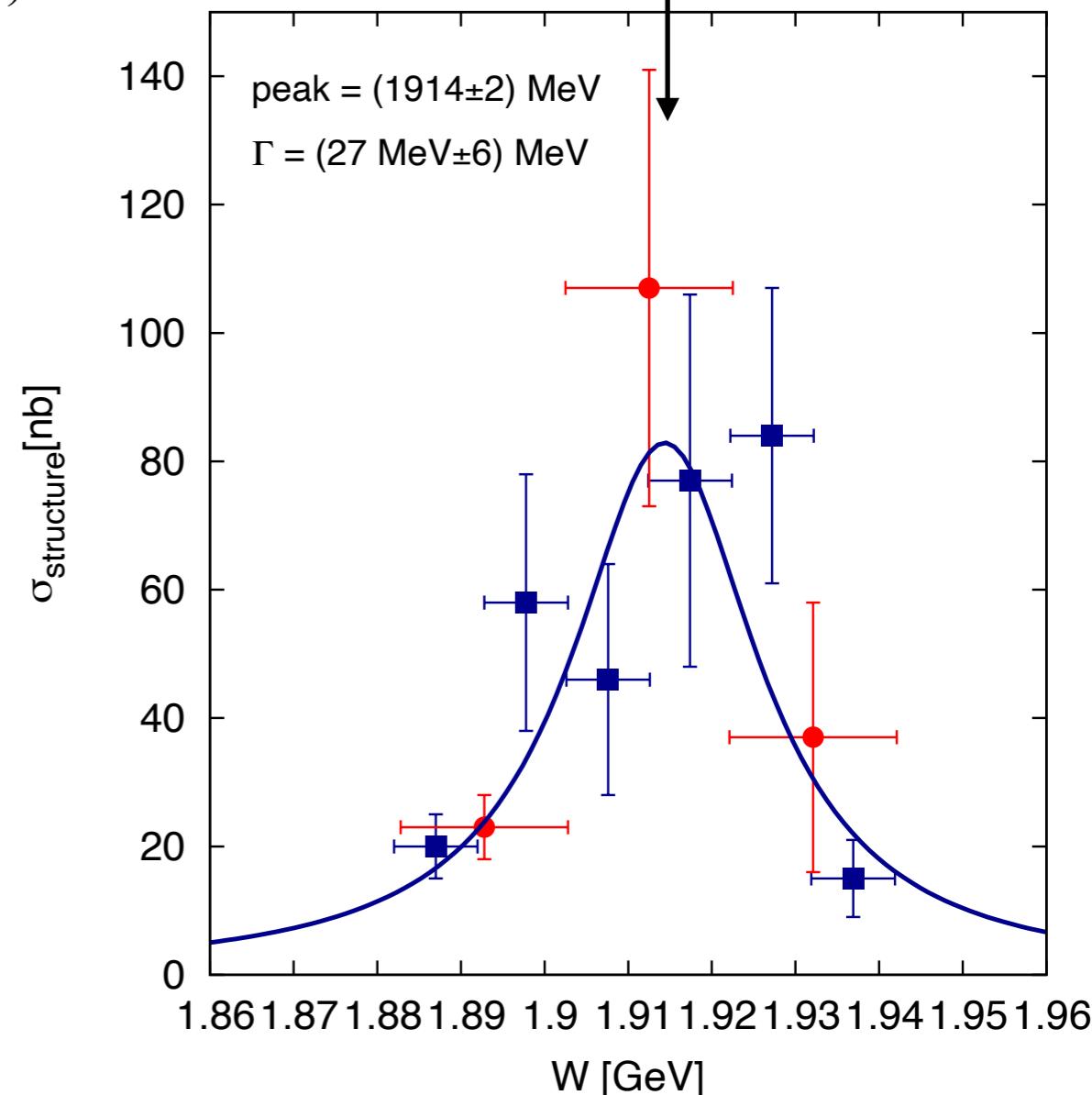


comparison to data:

$$m_p + m_{a0} = 1918 \text{ MeV}$$

$$W = 1918 \text{ MeV}$$

$$E_\gamma = 1492 \text{ MeV}$$

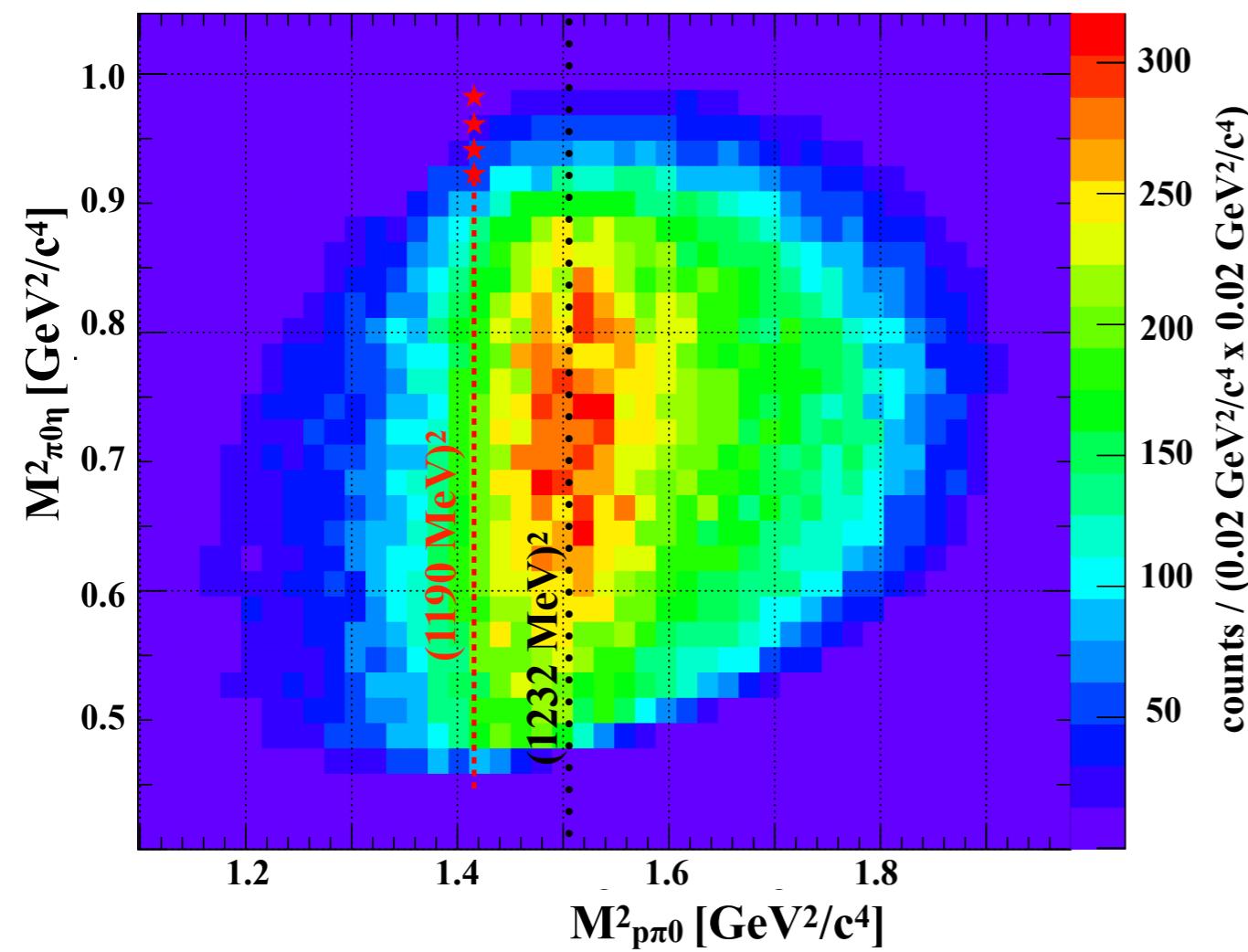


calculation shows enhancement at $W = 1918 \text{ MeV}; E_\gamma = 1492 \text{ MeV}$
as observed experimentally

calculating triangular singularities

calculation of singularities for 4 incident energies near the a_0 threshold,
following Bayar et al. PRD 94 (2016) 074039

| E_γ [MeV] | $M_{\pi^0\eta}$ [MeV] | $M_{p\eta}$ [MeV] | $M_{p\pi^0}$ [MeV] |
|------------------|-----------------------|-------------------|--------------------|
| 1549 | 990 | 1609 | 1190 |
| 1524 | 980 | 1601 | 1190 |
| 1498 | 970 | 1591 | 1190 |
| 1473 | 960 | 1583 | 1190 |



calculating triangular singularities

calculation of singularities for 4 incident energies near the a_0 threshold,
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| 1549 | 990 | 1609 | 1190 |
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| 1473 | 960 | 1583 | 1190 |



γ p-cm-system:

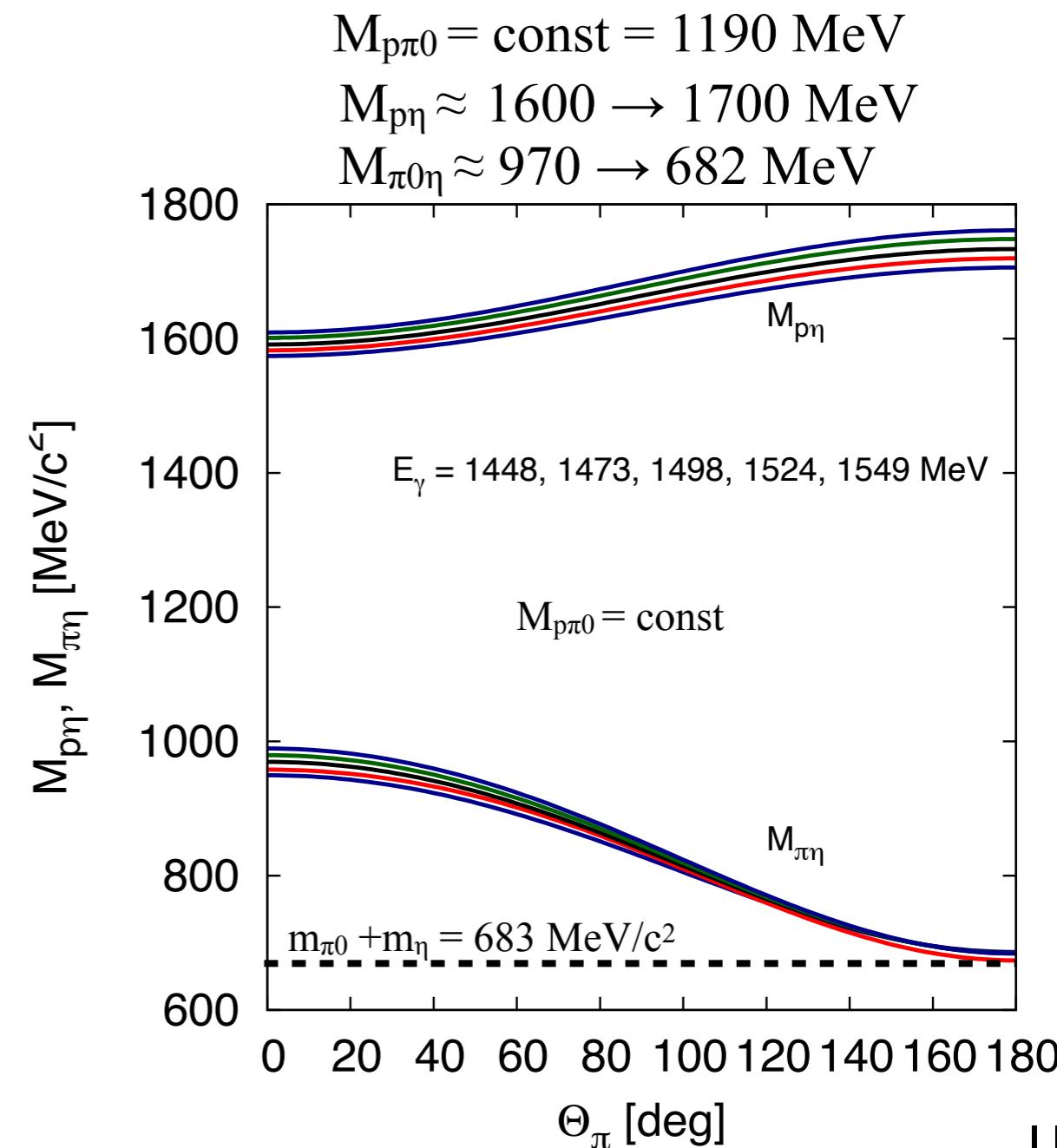
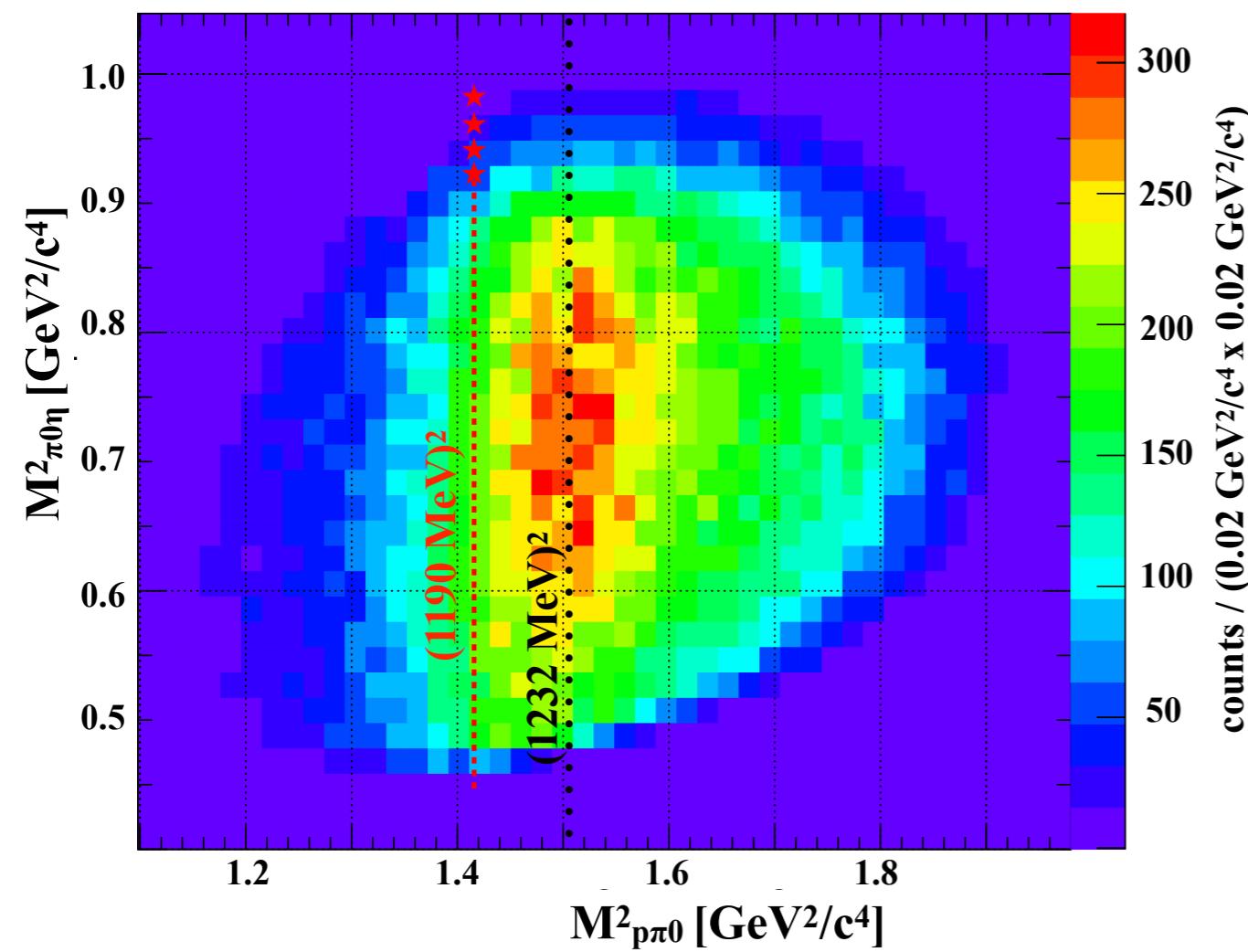
$$p_p = 122.9 \text{ MeV}; \beta_p = 0.130$$

$$p_\pi = 277.8 \text{ MeV}; \beta_\pi = 0.899 \quad p_\eta = -400.7 \text{ MeV}$$

$$\beta_\eta = -0.590$$

π^0 faster than p
 π^0 -p rescattering:

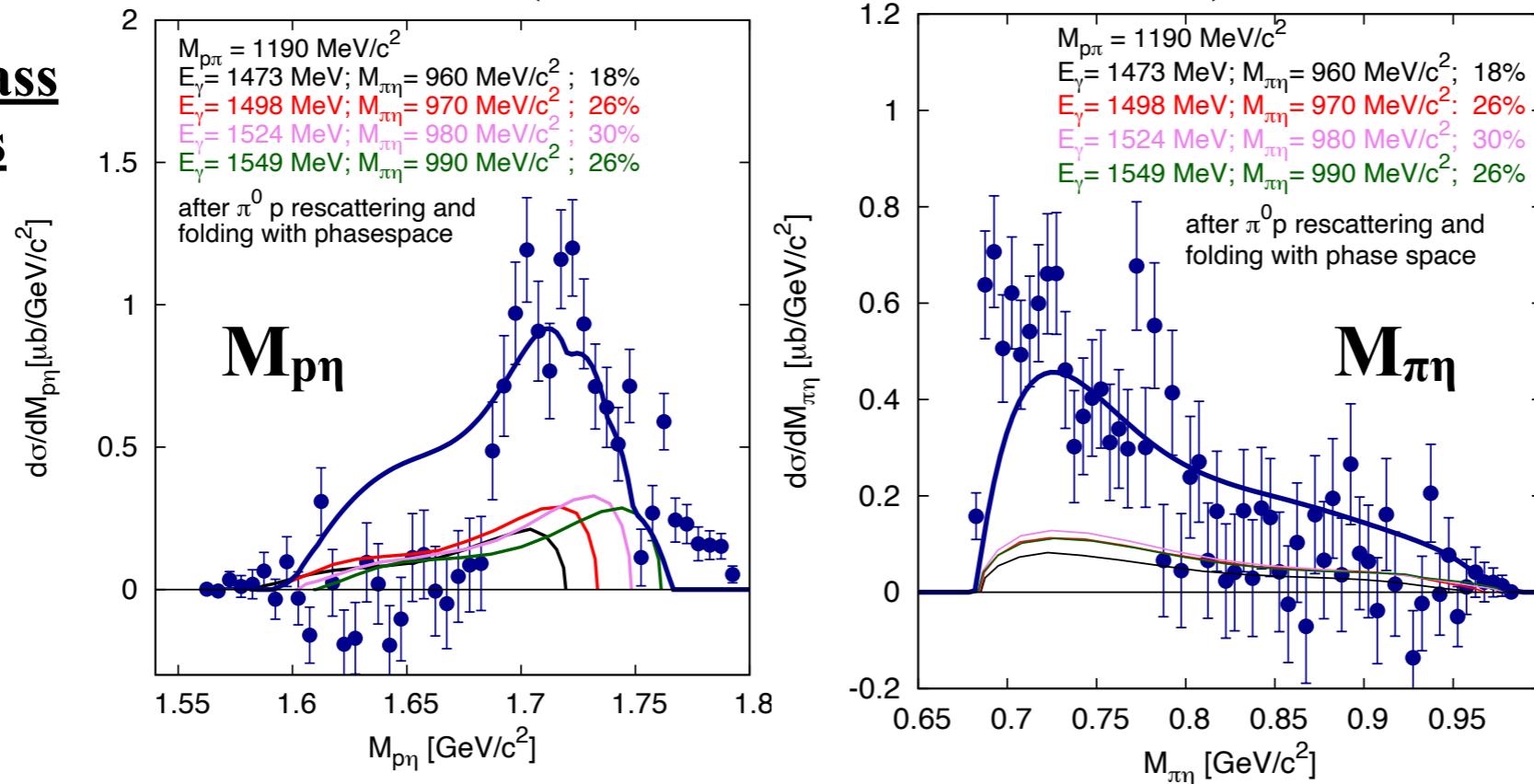
singularity events are re-distributed along
the dashed red line by **π^0 -p - rescattering**



Comparison data (difference to PWA) \longleftrightarrow calculation

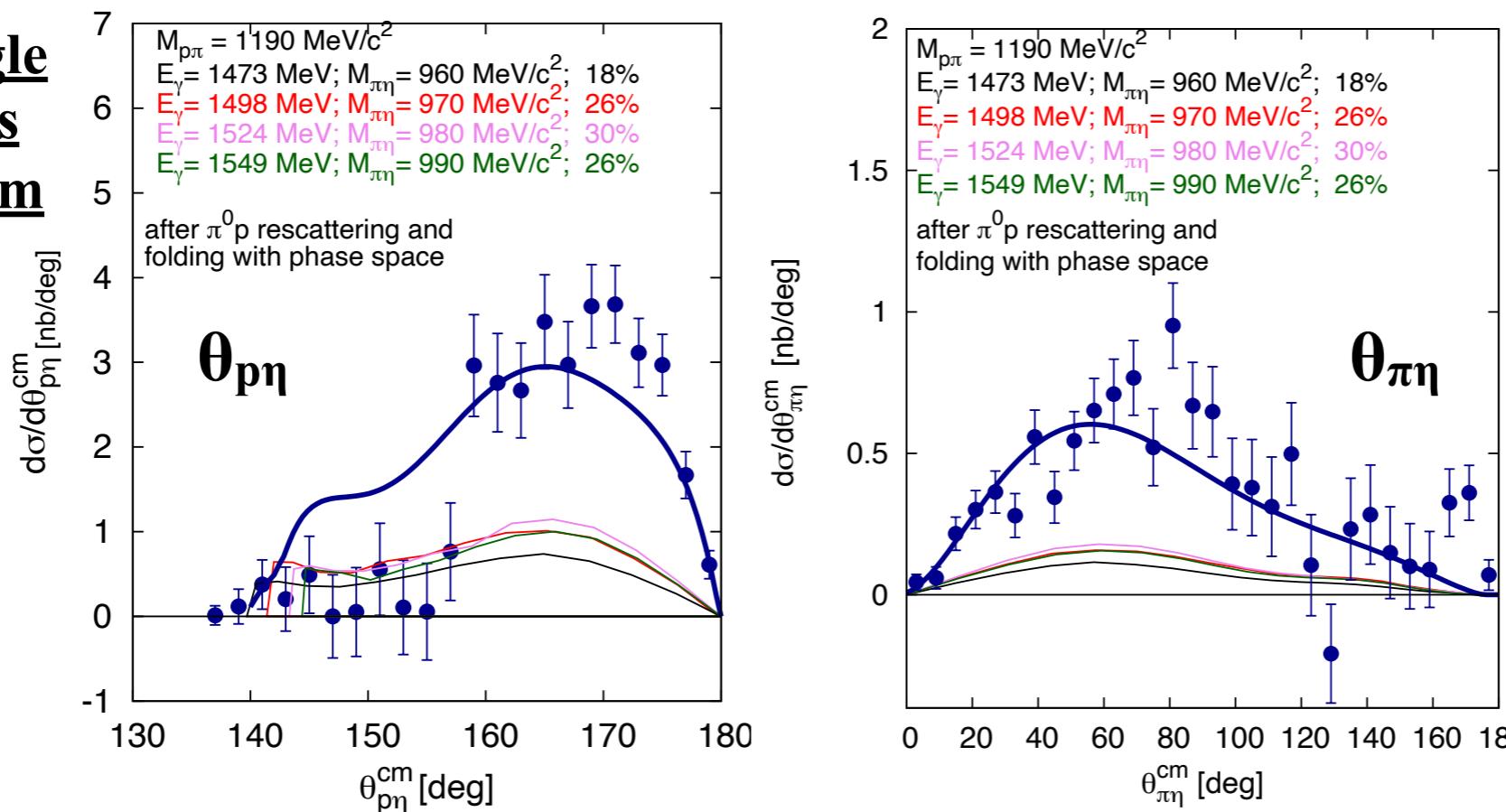
contributions of the 4 selected singularity points with weight given by a_0 line shape
 blue curve (sum of the 4 contributions) fitted to the data

invariant mass distributions



data qualitatively reproduced by calculations !!

opening angle distributions yp-cm-system



Interference of loop- (triangular) and tree-level amplitudes

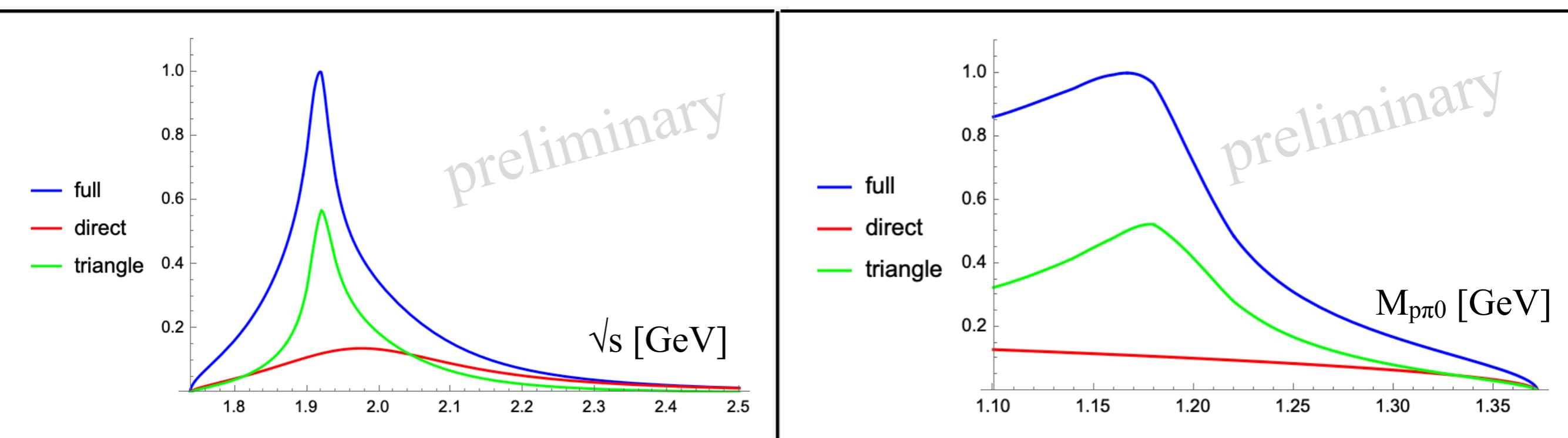
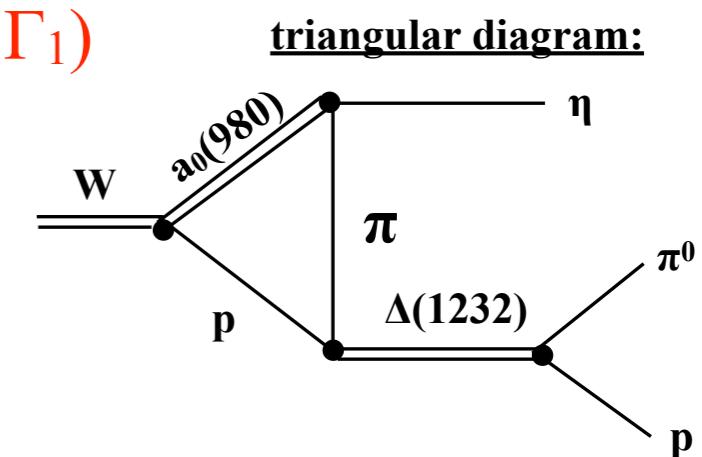
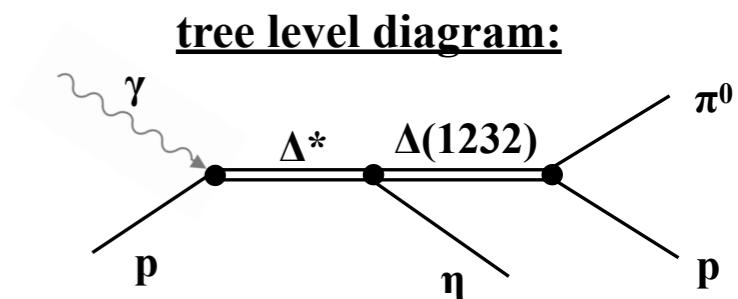
thanks to Mathias Wagner (Univ. Bonn)

initially populated nucleon resonance (source of p, a_0):
 $m_1 = 1.95 \text{ GeV}$; $\Gamma_1 = 0.350 \text{ GeV}$

$$f_{\text{tot}} = f_{\text{tree}} + f_{\text{loop}} = (\text{rel} + e^{i\varphi} * f_{\text{triangle}}(\sqrt{s}; \Gamma_{a_0}, m_{a_0}, m_\Delta)) * \text{BW}(\sqrt{s}; m_1, \Gamma_1)$$

intensity = $|M|^2 * \text{phasespace}$

experimentally observed excitation function and
 $M_{p\pi^0}$ distribution reproduced for $\text{rel} = 0.036$; $\varphi = -0.5$



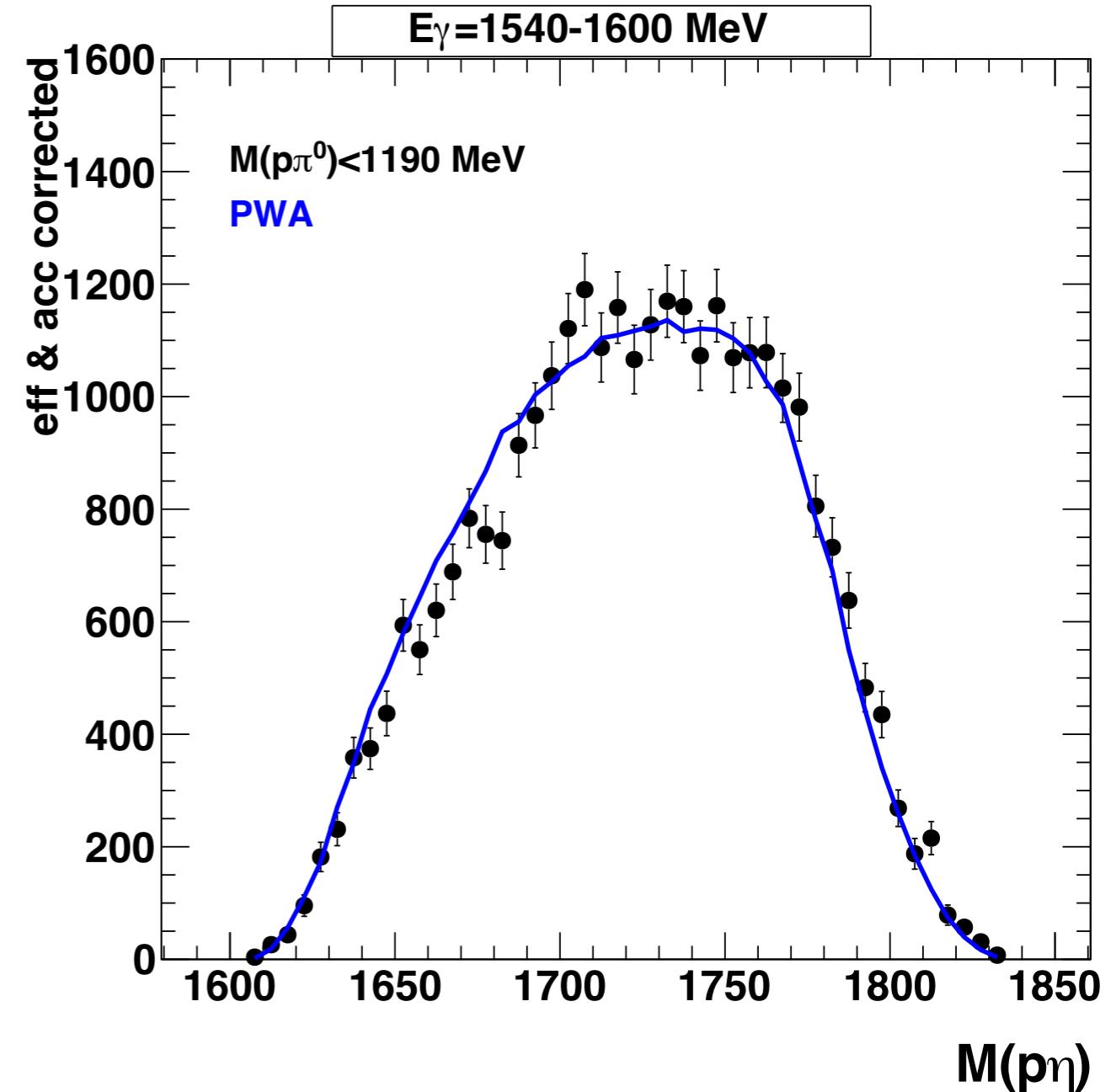
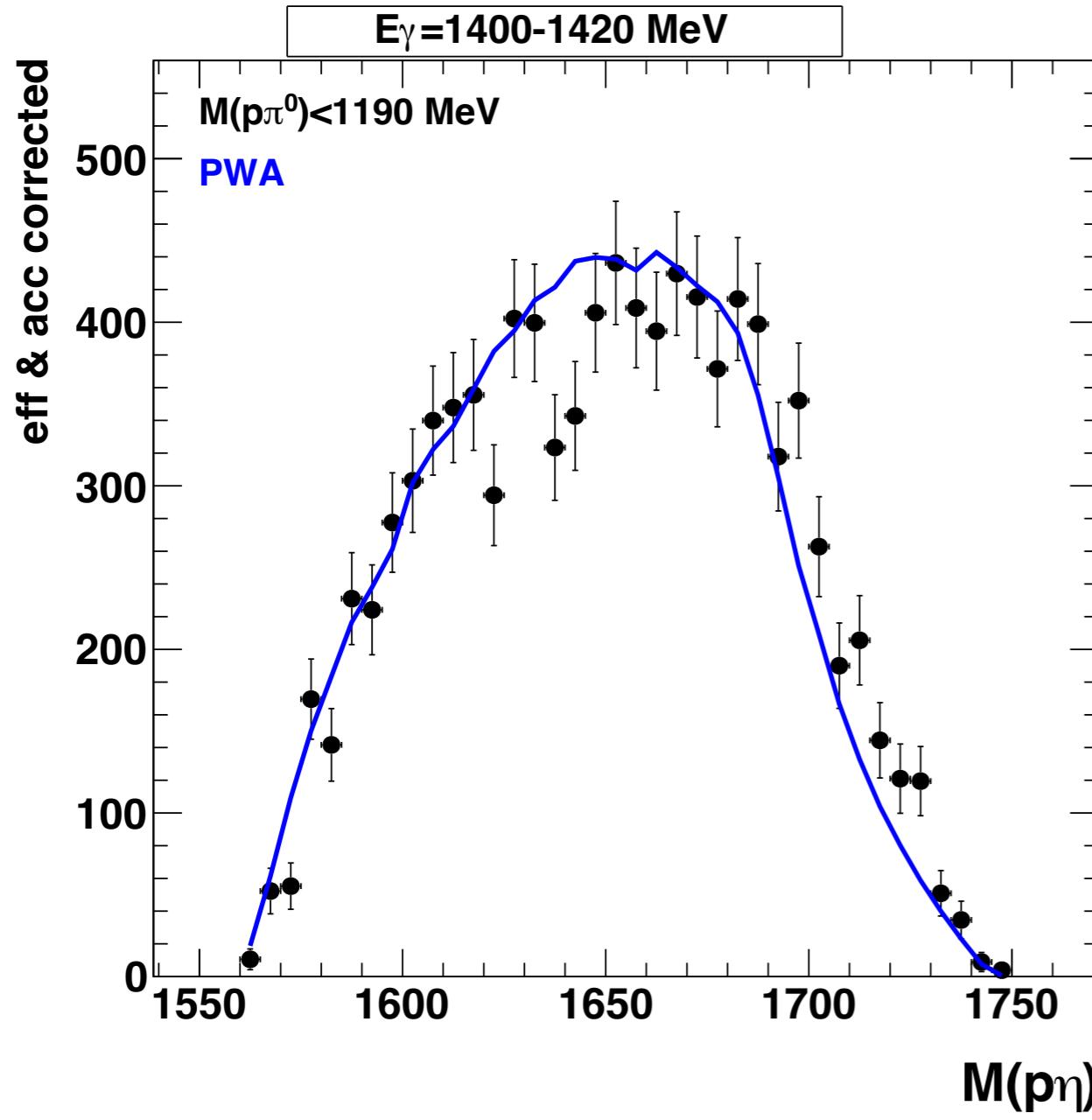
more detailed studies require partial wave analysis !!

summary and conclusions

- structure at $M_{p\eta} \approx 1710$ MeV established in $\gamma p \rightarrow p \pi_0 \eta$ reaction for $E_\gamma = 1400 - 1600$ MeV
- structure moves and changes shape with incident photon energy
→ no genuine nucleon resonance
- characteristics of structure qualitatively reproduced by calculation based on the triangular loop in the $\gamma p \rightarrow p a_0 \rightarrow p \pi_0 \eta$ reaction;
(EPJA 57 (2021) 325)
- loop diagrams and rescattering effects play an important role also in the **baryon sector** in the interpretation of structures in the excitation spectrum of the nucleon; important to distinguish kinematical singularities from genuine resonances
- not every bump in an invariant mass spectrum is a resonance !
- **improvements:**
calculation not only for 4 selected singularity points
→ **full partial wave analysis required including the present data**

backup

comparison data \longleftrightarrow PWA outside signal region



PWA describes data very well outside the signal region ($E_\gamma = 1420 - 1540$)

calculating triangular singularities

Bayar et al. PRD 94 (2016) 074039

energy-momentum balance within the loop has to match the energy-momentum balance of the initial and final state particles:

$$W = E_p(q) + E_\pi(q) + E_\eta$$

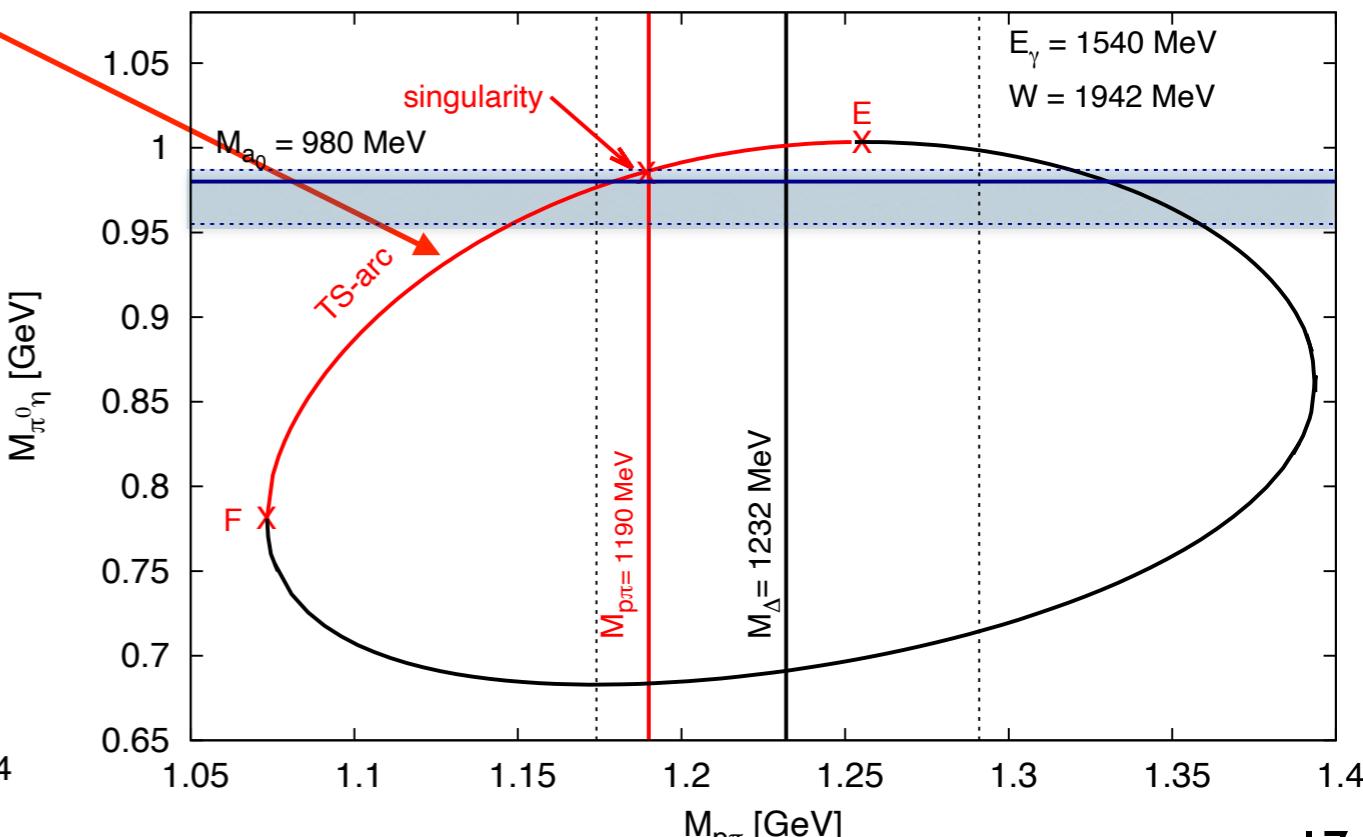
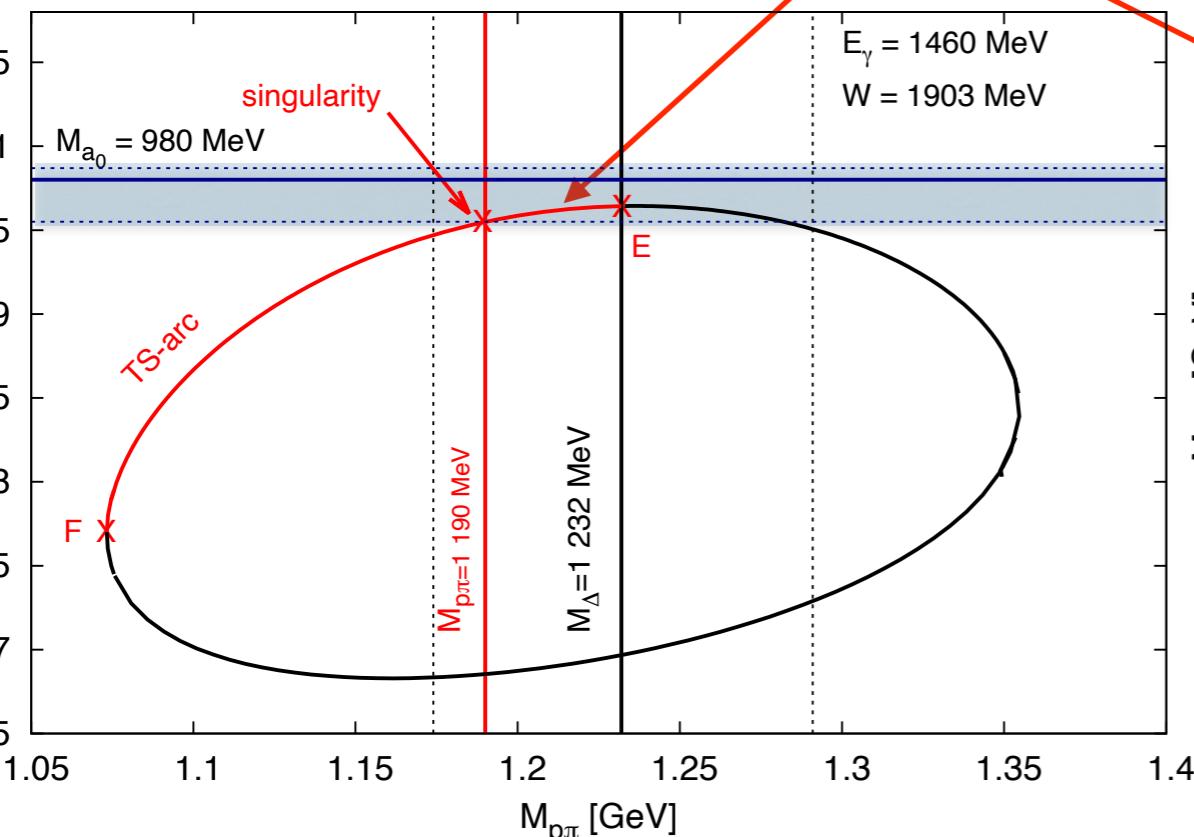
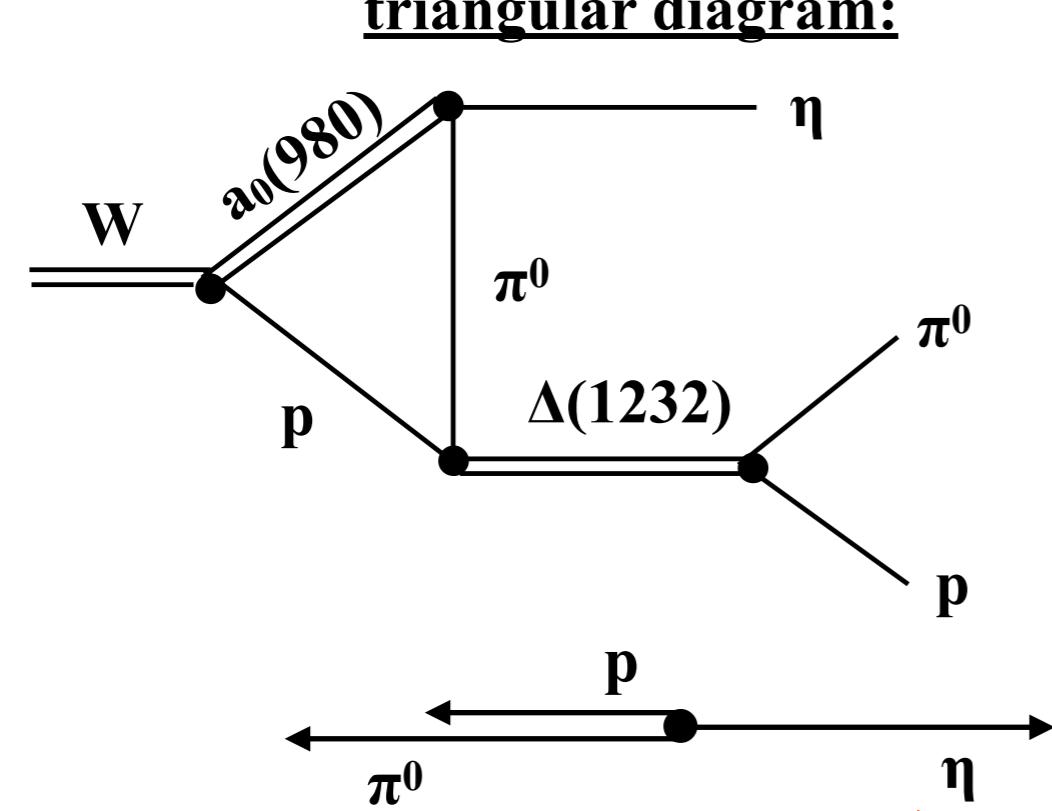
$$\underline{W = E_p(q) + E_{a0}(p_\eta - q)}$$

$$E_\eta + E_\pi(q) - E_{a0}(p_\eta - q) = 0$$

$$E_\eta + E_\pi(q) - \sqrt{m_{a0}^2 + (p_\eta - q)^2} = 0$$

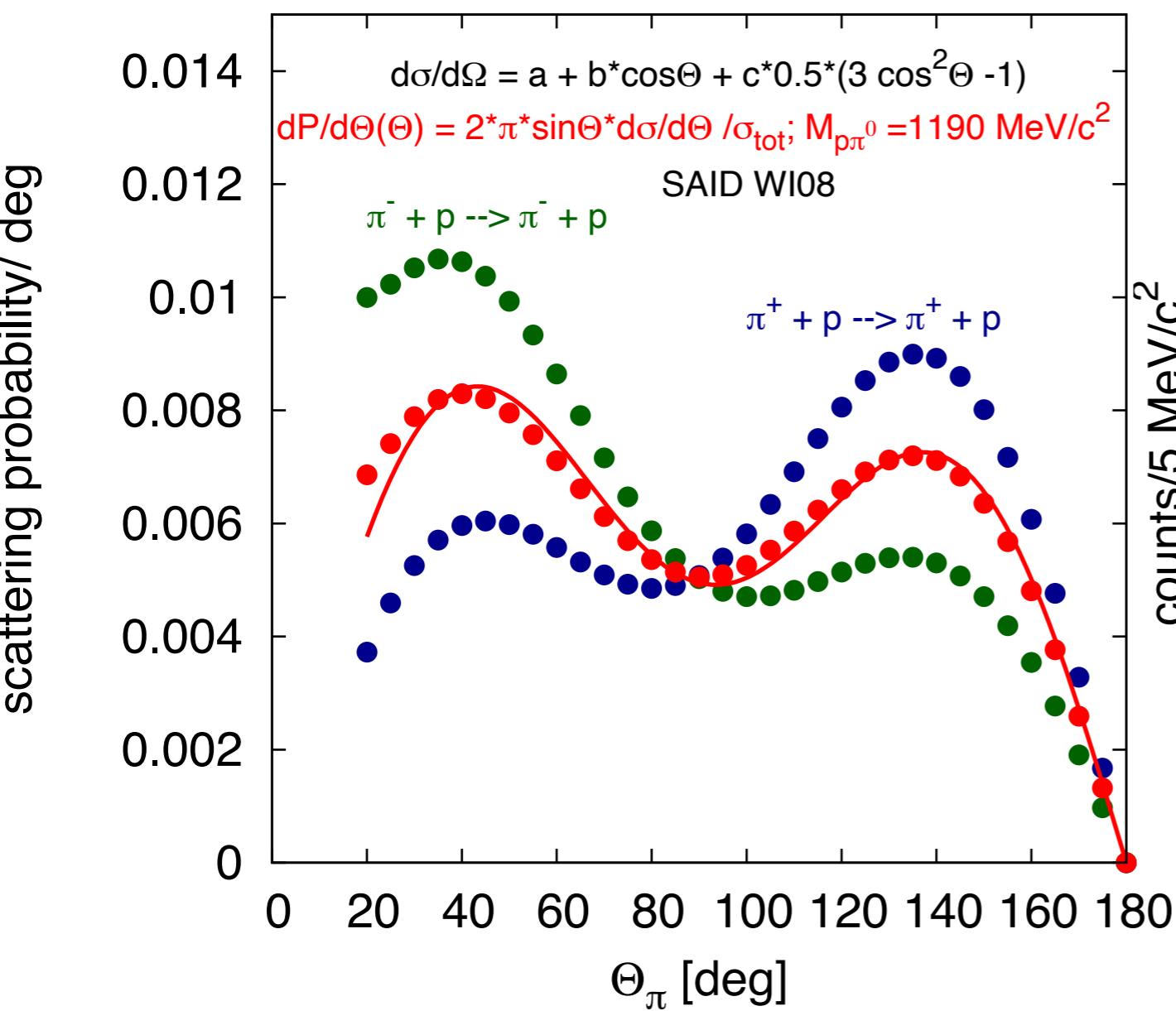
q = proton momentum in loop

for given excitation energy W solutions only for certain $(M_{\pi^0\eta}, M_{p\pi^0})$ values and if all particles are almost on-mass shell and p, π^0, η are collinear

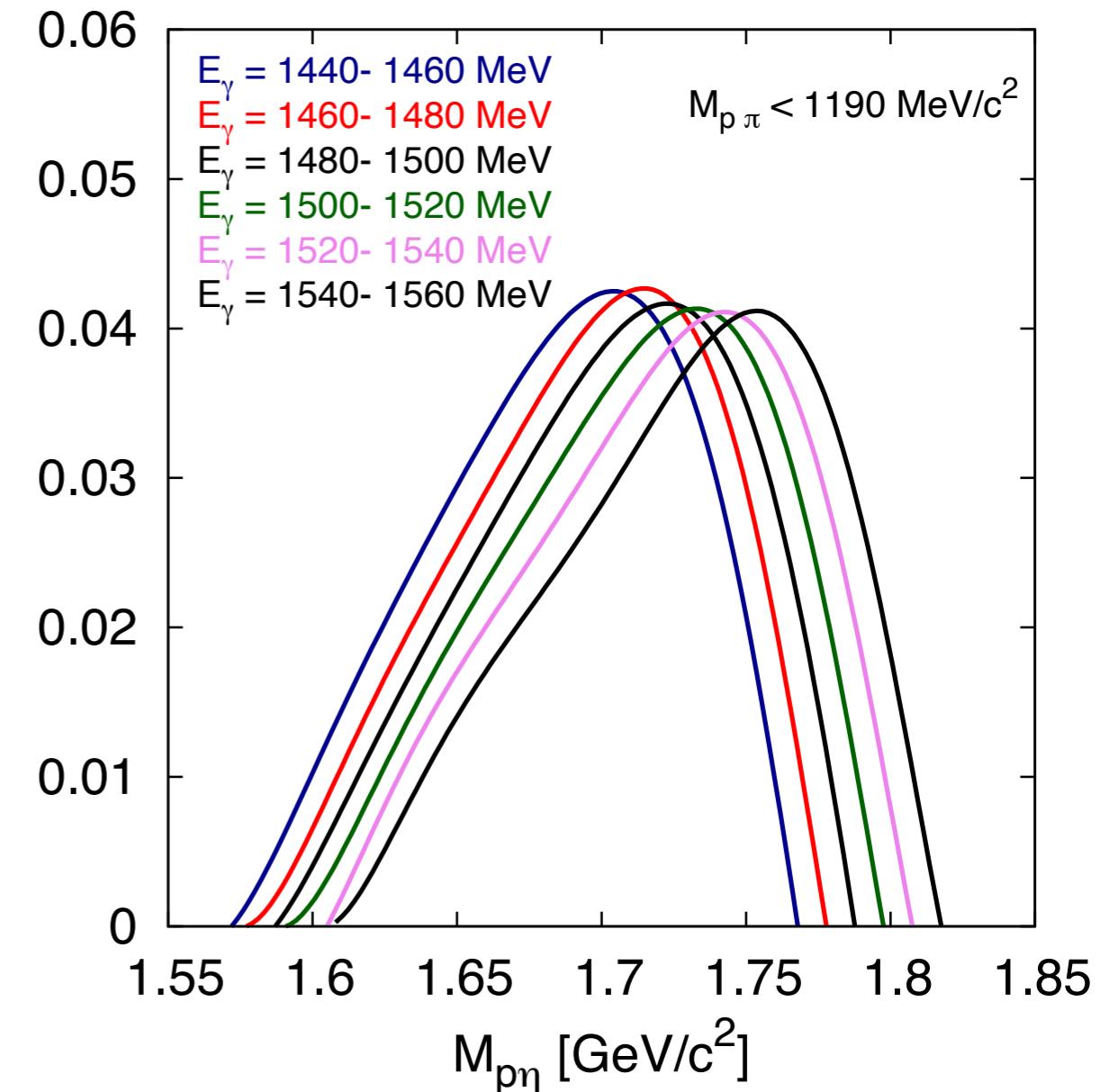


probability of π^0 - p rescattering

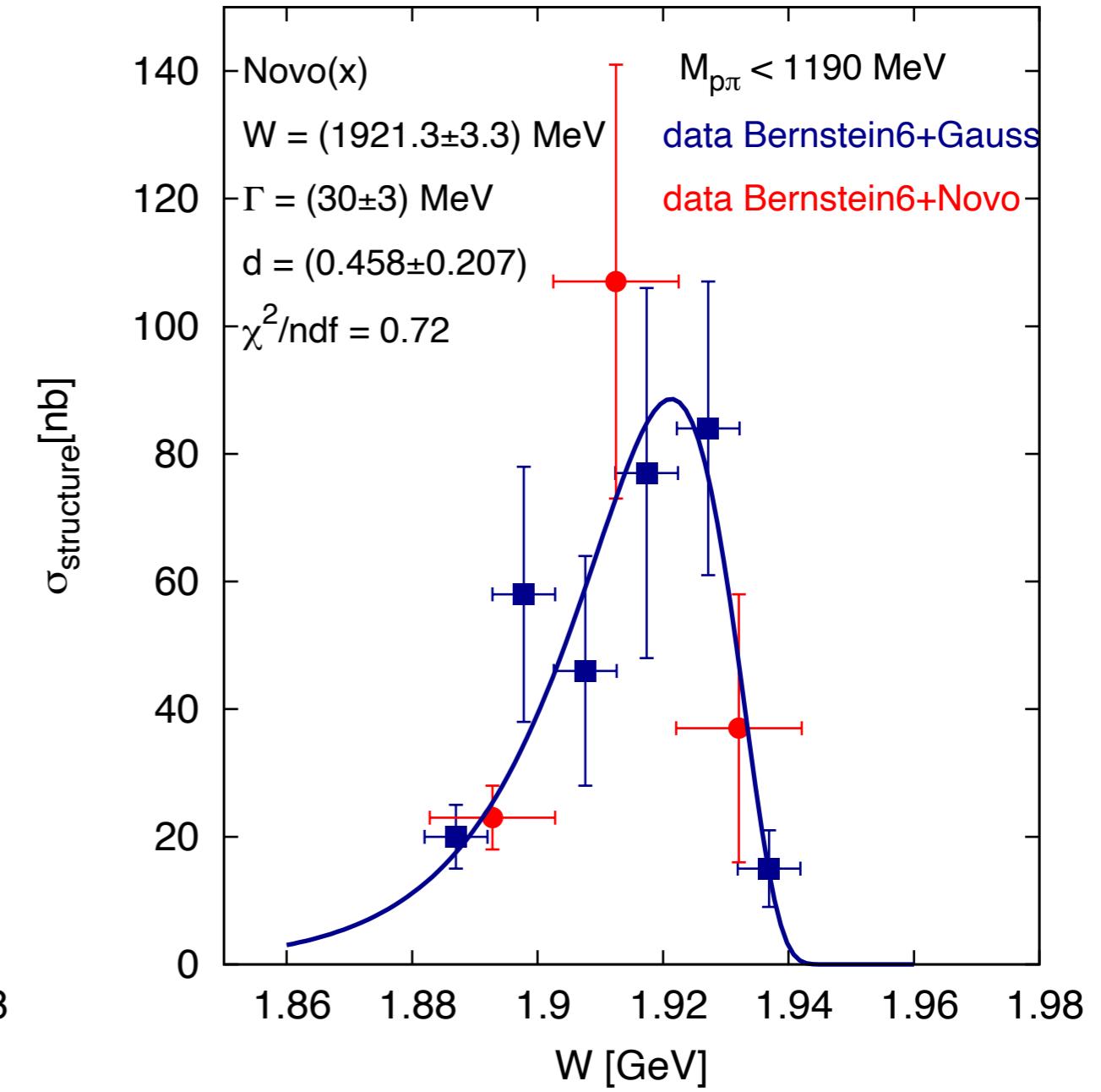
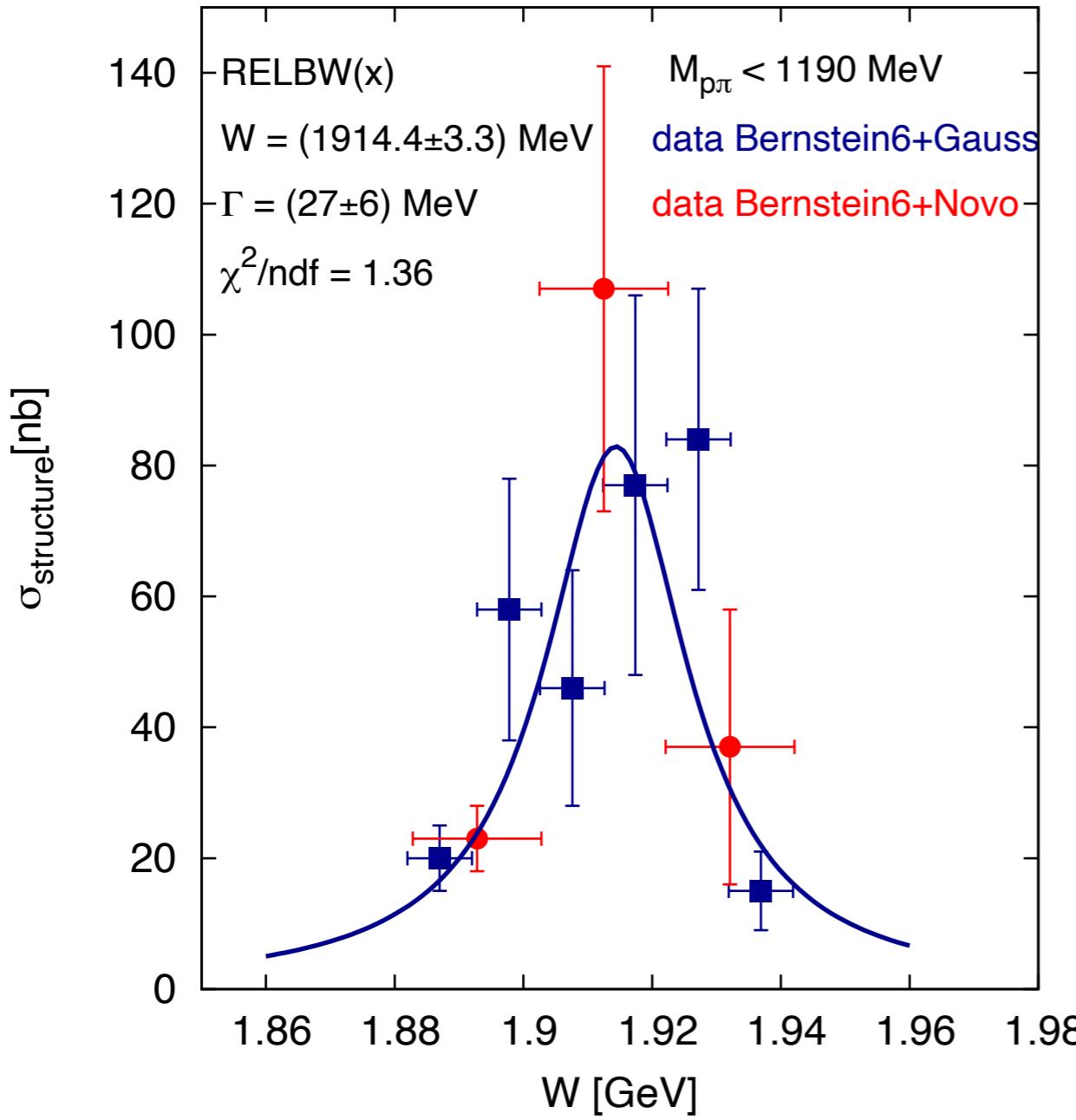
re-scattering probability



phase-space distribution

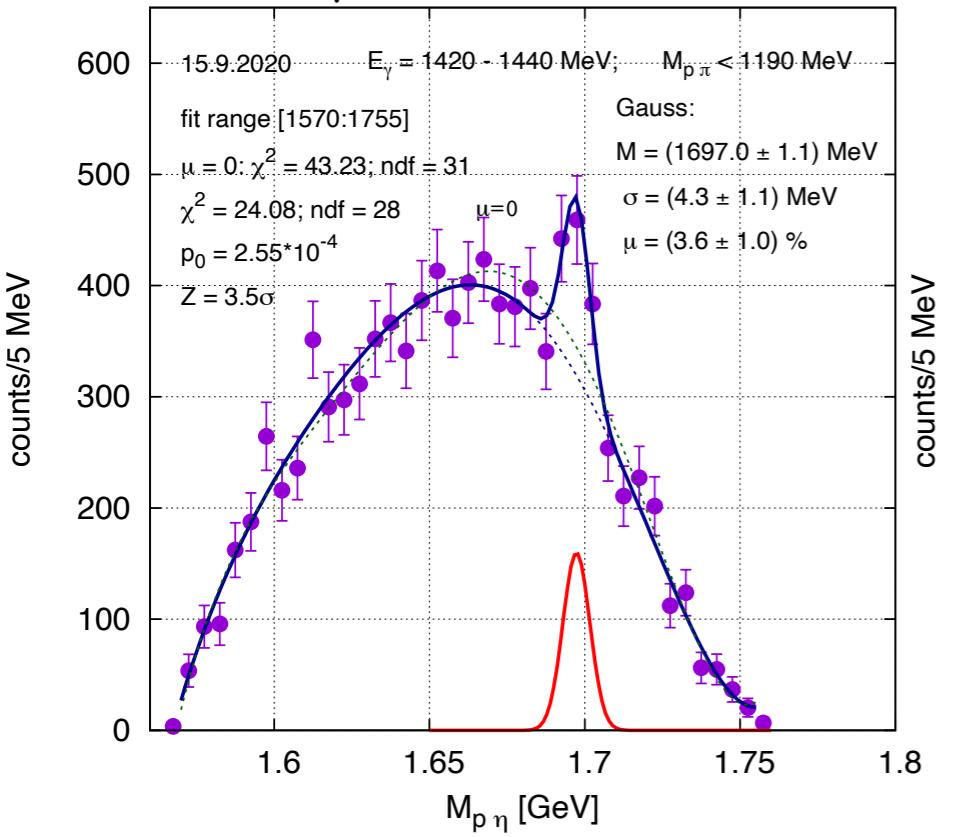


θ_π = scattering angle of π^0
in the π^0 -p cm system

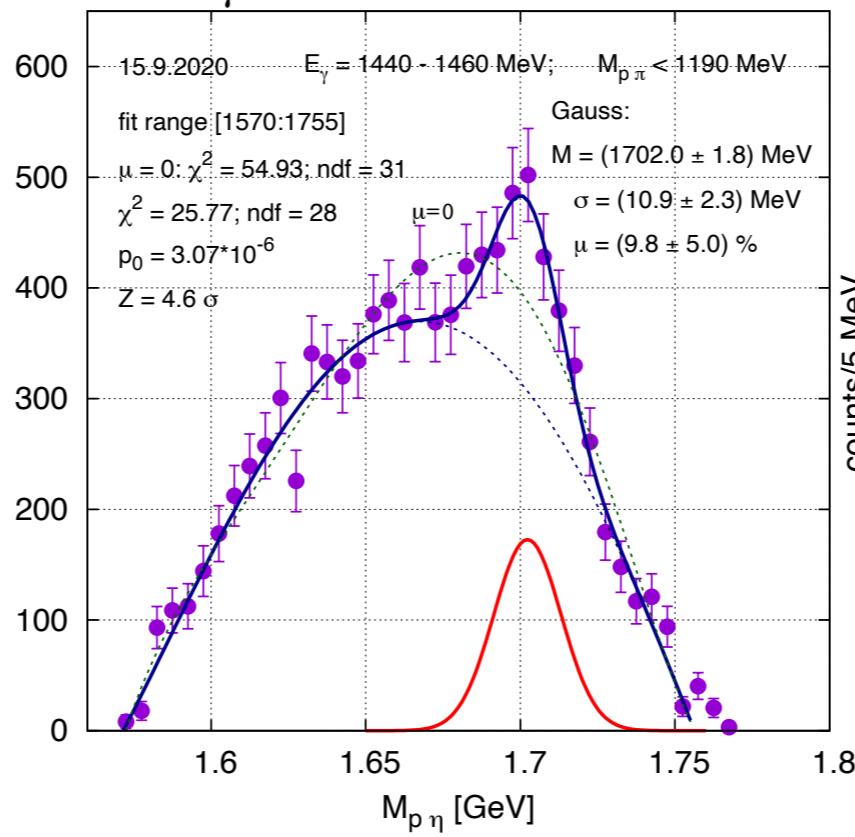


properties of structure as function of the incident photon energy; fit: Gauss

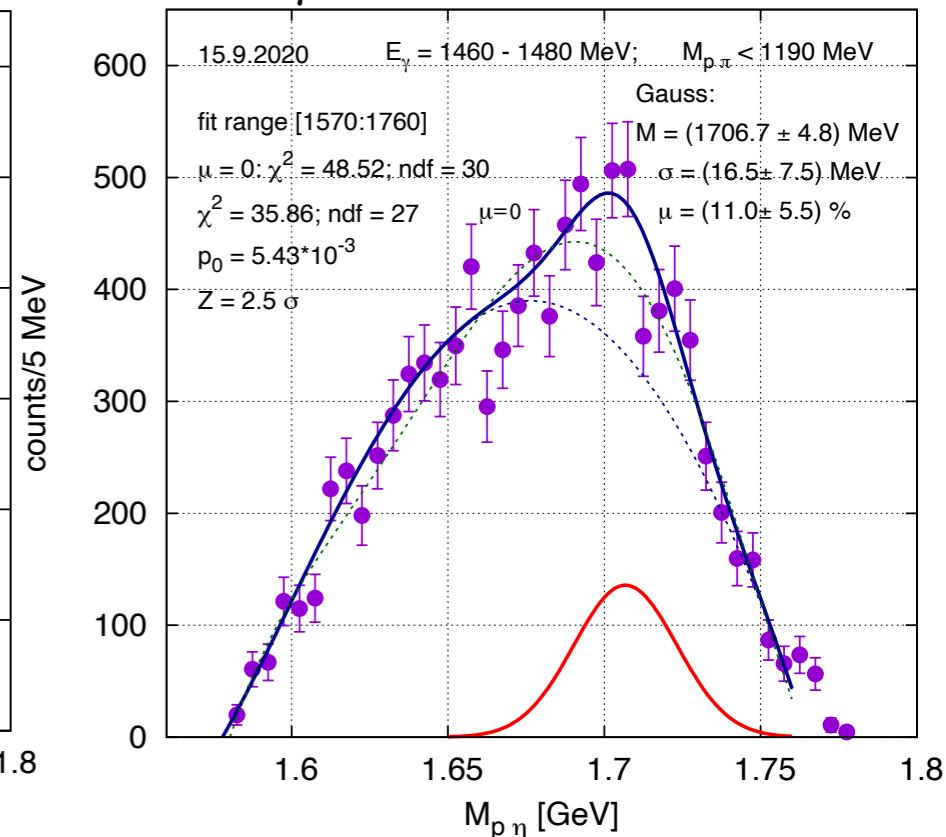
$E_\gamma = 1420 - 1440 \text{ MeV}$



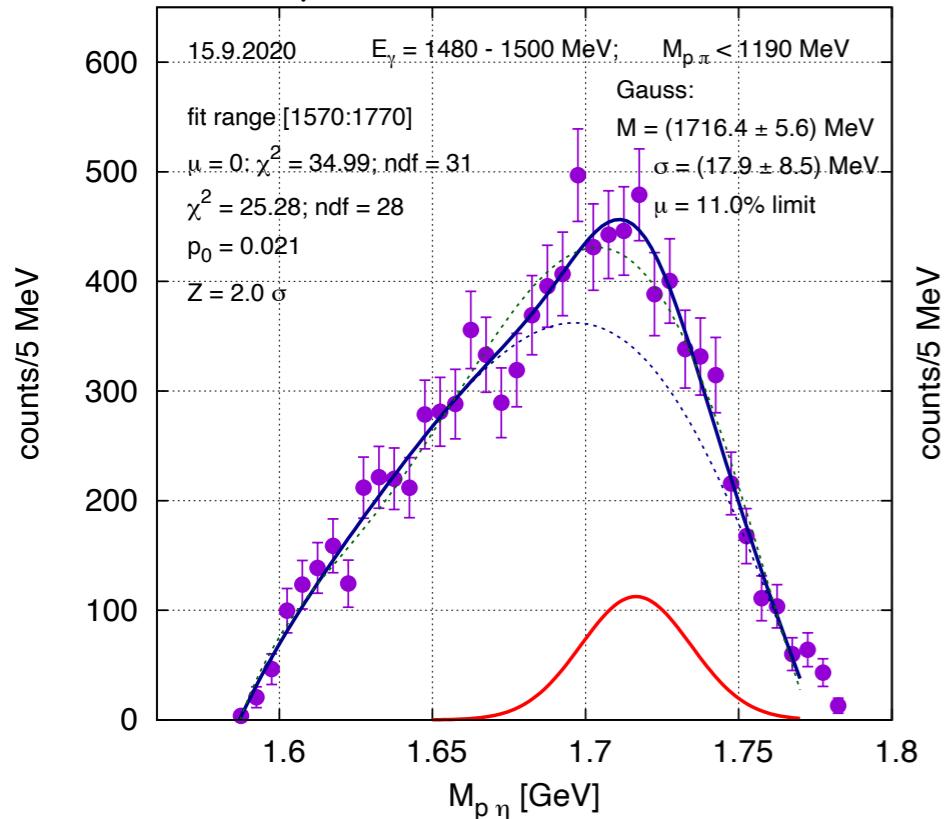
$E_\gamma = 1440 - 1460 \text{ MeV}$



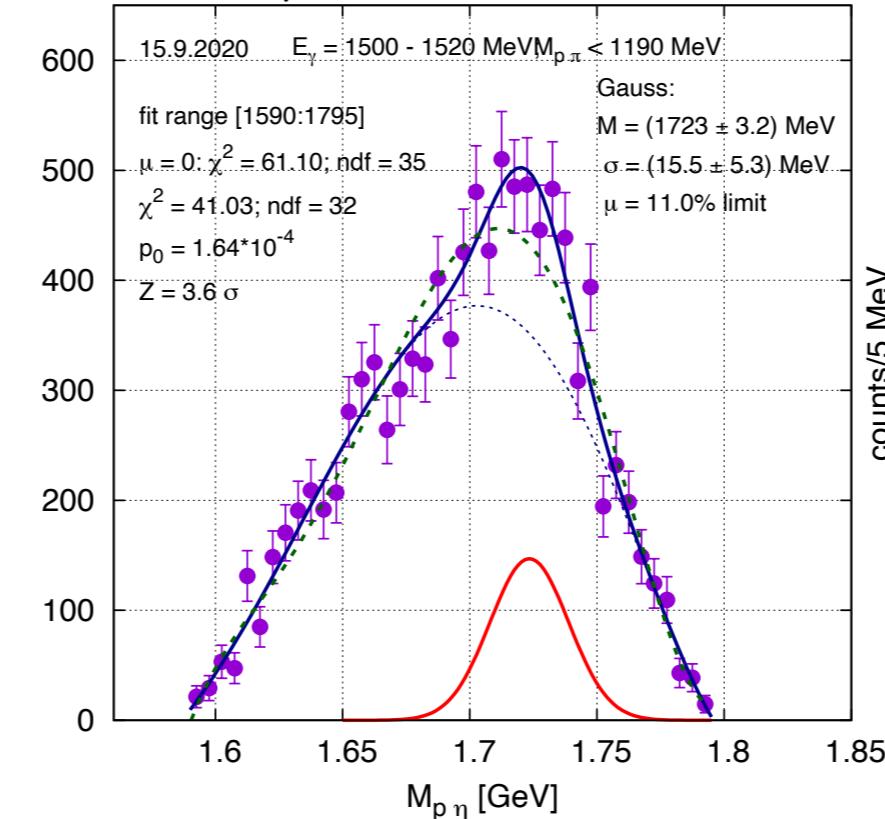
$E_\gamma = 1460 - 1480 \text{ MeV}$



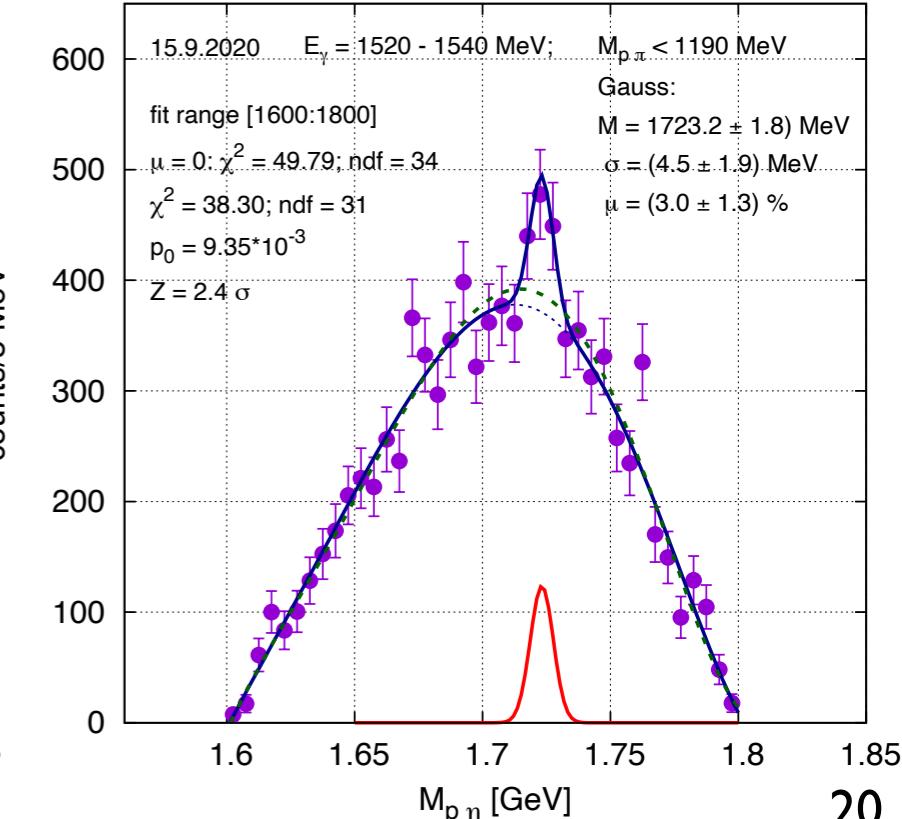
$E_\gamma = 1480 - 1500 \text{ MeV}$



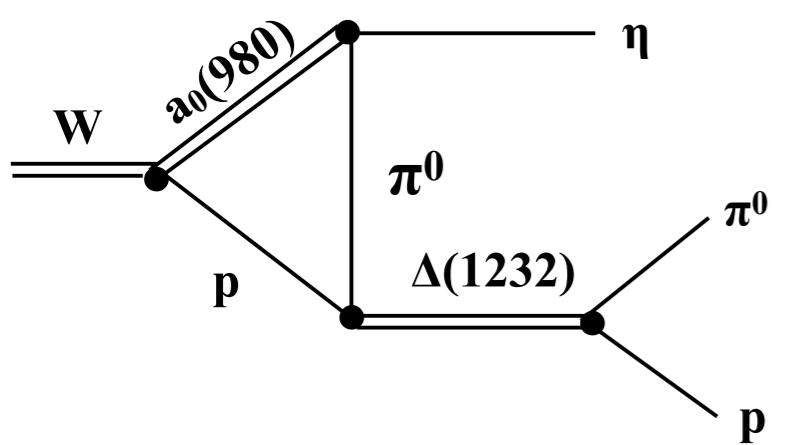
$E_\gamma = 1500 - 1520 \text{ MeV}$



$E_\gamma = 1520 - 1540 \text{ MeV}$

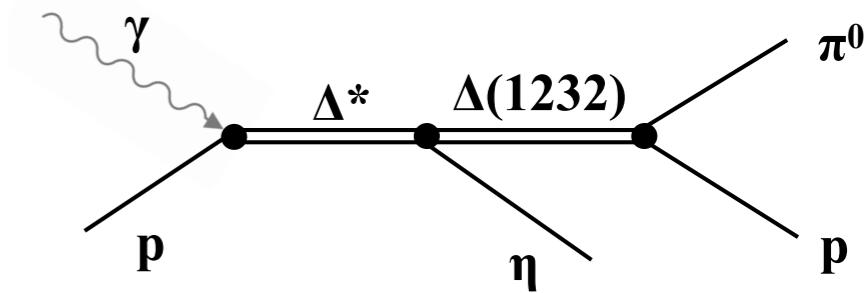


triangular diagram:



**interference of
tree-level and
triangular amplitudes**

tree level diagram:



| resonance | I | J ^P | mass[MeV] | width [MeV] | br(p a0) | br(η Δ(1232)) | reference |
|-----------|-----|------------------|-----------|-------------|----------|---------------|-----------|
| N(1880) | 1/2 | 1/2 ⁺ | 1860 | 230 | (3±2)% | — | Gutz/PDG |
| Δ(1910) | 3/2 | 1/2 ⁺ | 1900 | 300 | ? | (5-13)% | Gutz/PDG |
| Δ(1920) | 3/2 | 3/2 ⁺ | 1920 | 300 | (4±2)% | (5-17)% | Horn/PDG |
| Δ(1940) | 3/2 | 3/2 ⁻ | 2000 | 400 | (2±1)% | (4-16)% | Horn/PDG |

$$N(1880)1/2^+ (1/2, 1/2^+) \rightarrow a_0(1, 0^+) + p(1/2, 1/2^+); L = 0$$

$$\Delta(1910)1/2^+ (3/2, 1/2^+) \rightarrow a_0(1, 0^+) + p(1/2, 1/2^+); L = 0$$

$$\Delta(1920)3/2^+ (3/2, 3/2^+) \rightarrow a_0(1, 0^+) + p(1/2, 1/2^+); L = 2$$

$$\Delta(1940)3/2^- (3/2, 3/2^-) \rightarrow a_0(1, 0^+) + p(1/2, 1/2^+); L = 1$$

W = N(1880)1/2⁺ (I=1/2) would imply isospin violation since η Δ(1232) has I=3/2 !!!

if W = Δ(1910)1/2⁺ I=3/2 interference with dominating tree level (L_{ηΔ}= 1; I=3/2); L_{pa0} = 0

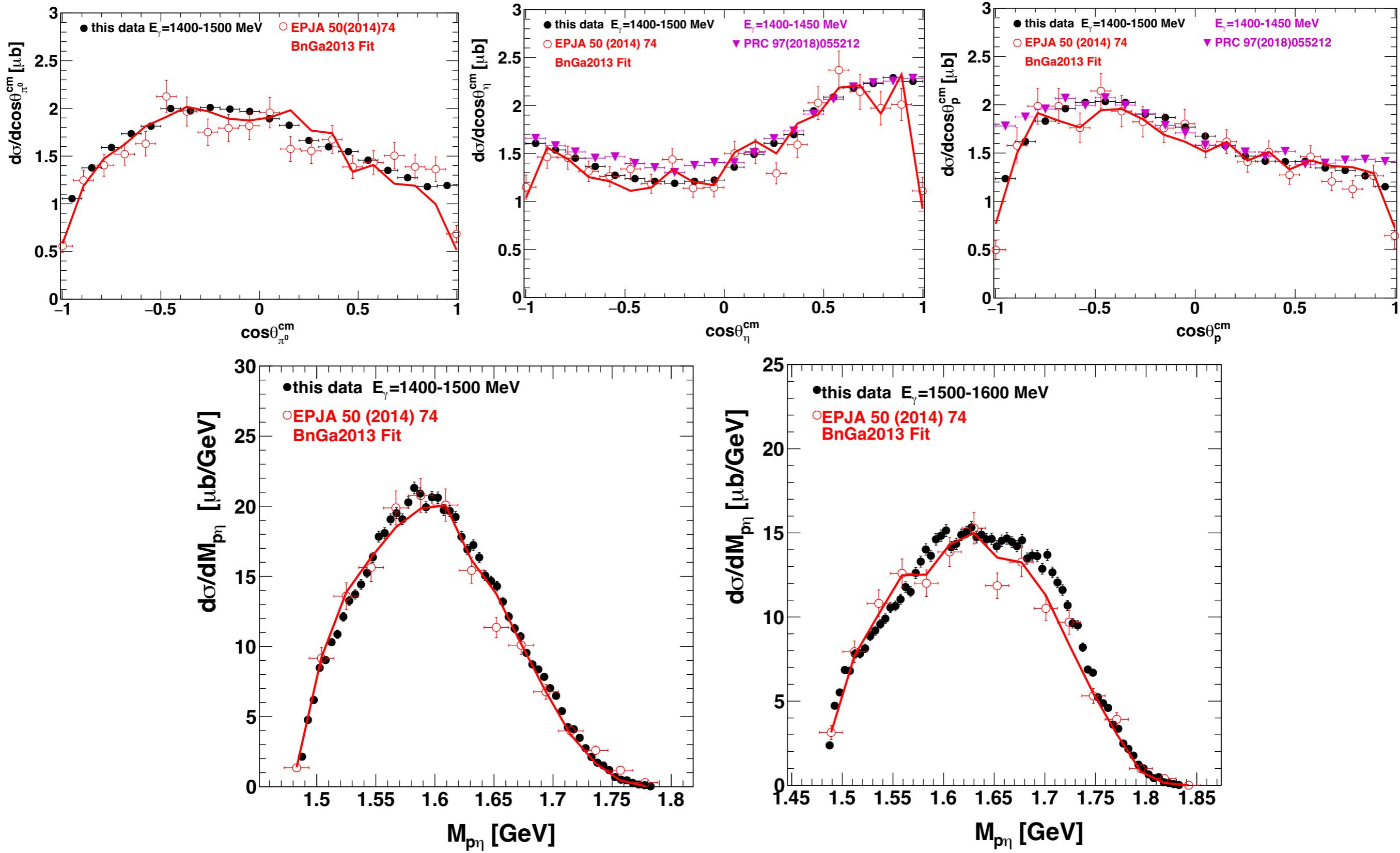
if W = Δ(1920)3/2⁺ I=3/2 interference with dominating tree level (L_{ηΔ}= 1; I=3/2); L_{pa0} = 2

if W = Δ(1940)3/2⁻ I=3/2 interference with dominating tree level (L_{ηΔ}= 0,2; I =3/2); L_{pa0}= 1

comparison to previous results

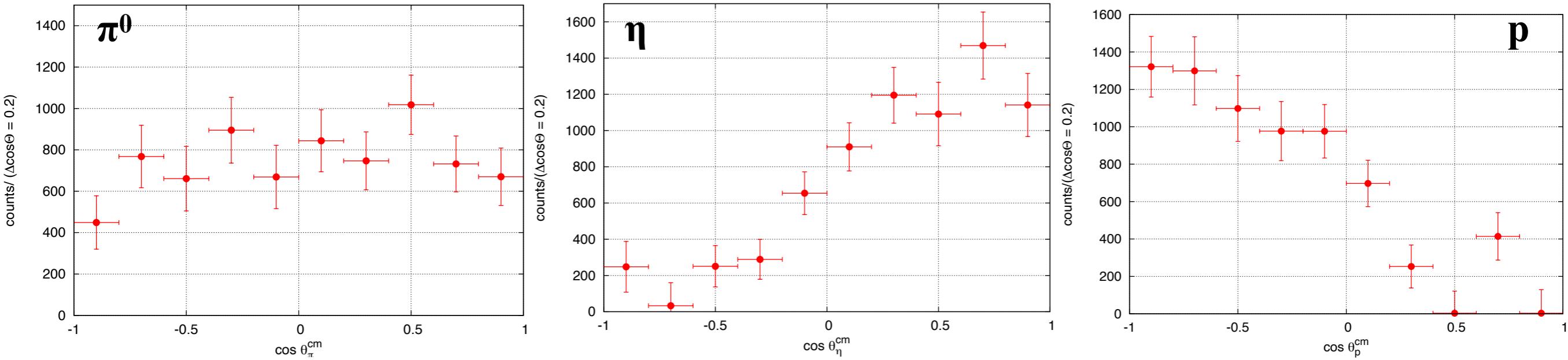
$\gamma p \rightarrow p \pi^0 \eta$

$E_\gamma = 1400 - 1500 \text{ MeV}$

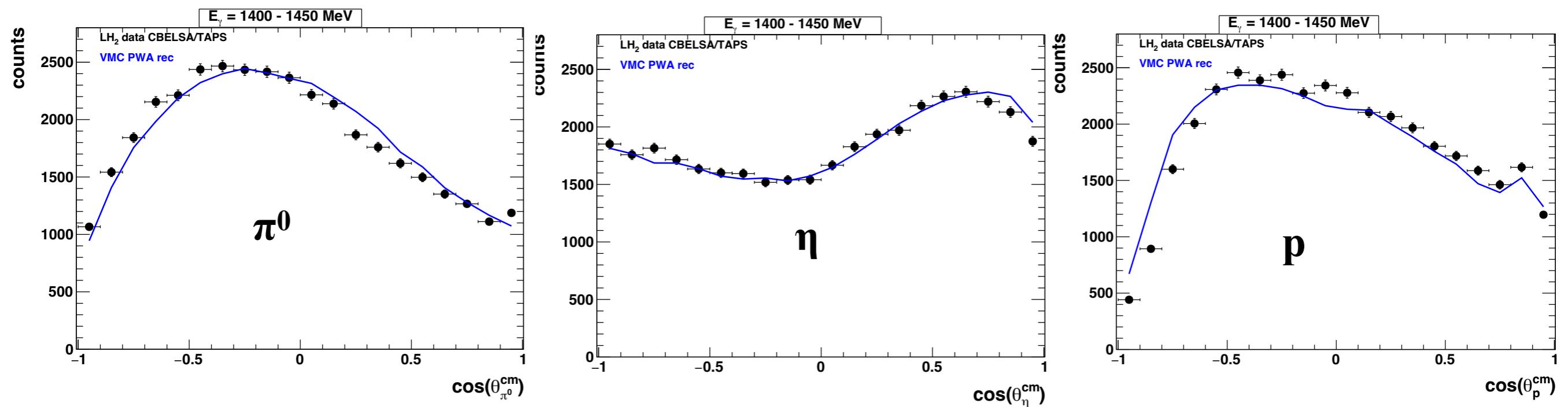


$$\gamma p \rightarrow p \pi^0 \eta$$

**angular distributions of events in structure for $E_\gamma = 1420 - 1540$ MeV and $M_{p\pi} < 1190$ MeV
in γp cm system**



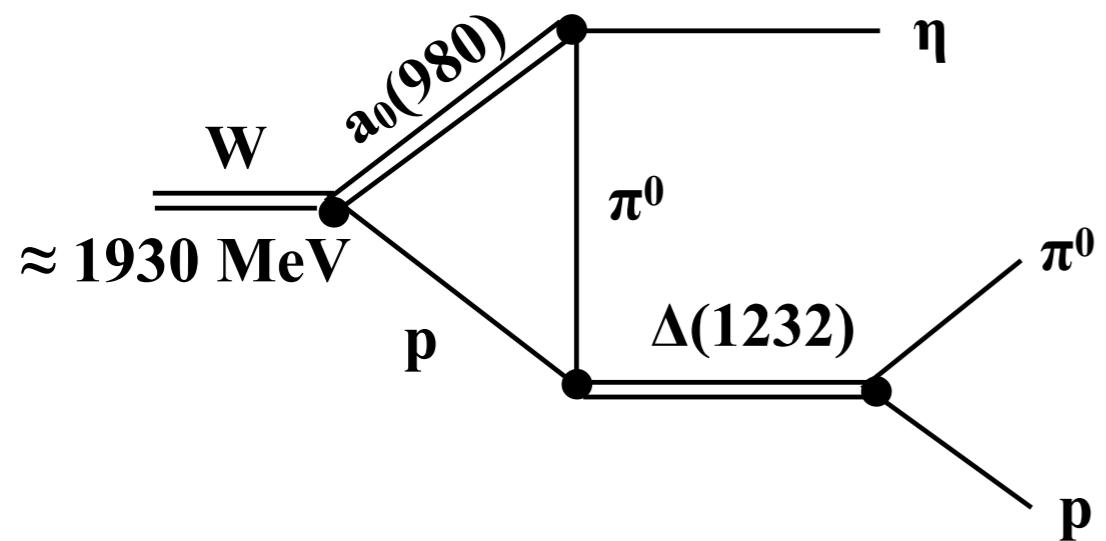
angular distributions for $E_\gamma = 1400 - 1450$ MeV without $M_{p\pi}$ cut



CBELSA/TAPS

$$\gamma p \rightarrow p \pi^0 \eta$$

triangular diagram:



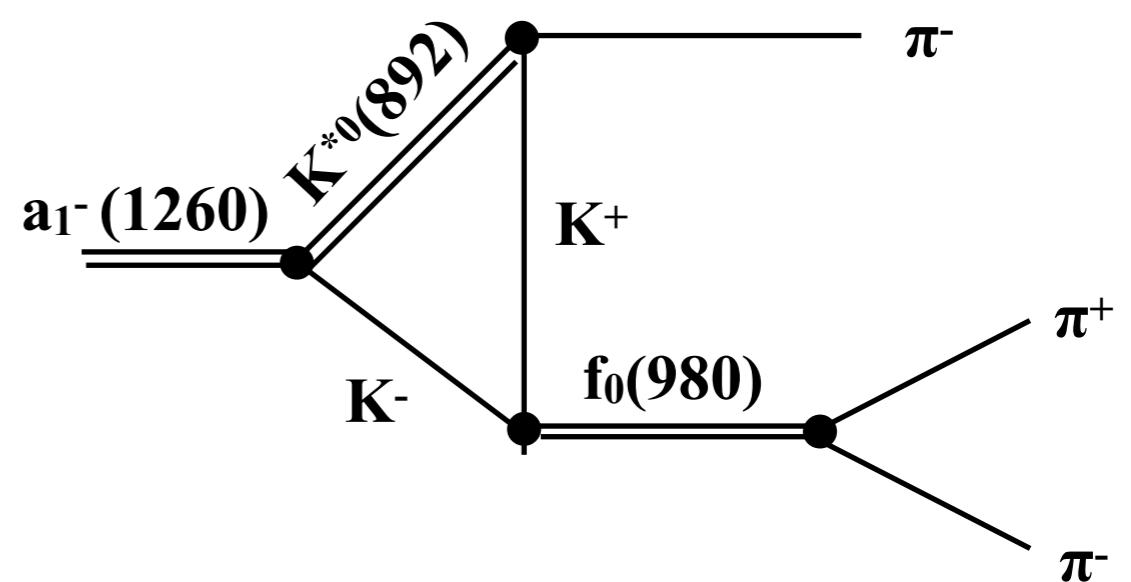
$a_0(980); \Gamma \approx 50 - 100 \text{ MeV}$

$\Delta(1232); \Gamma \approx 117 \text{ MeV}$

COMPASS

$$\begin{aligned} \pi^- p &\rightarrow a_1^-(1260) p \\ a_1^-(1260) &\rightarrow \pi^- \pi^+ \pi^- \end{aligned}$$

triangular diagram



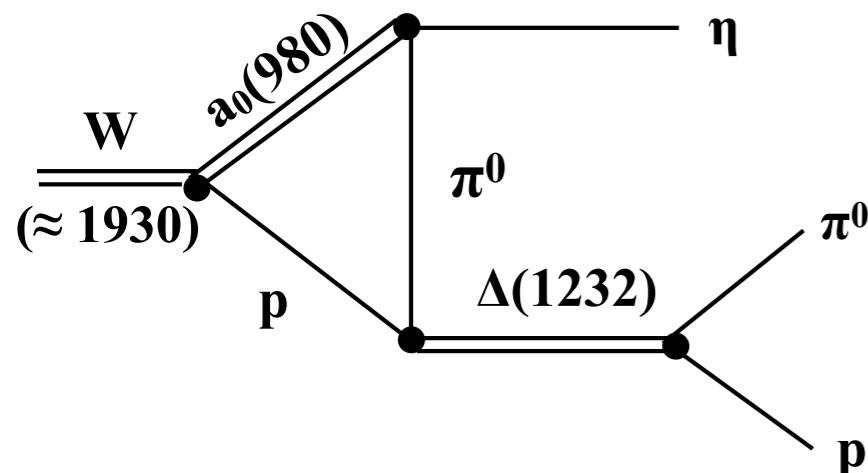
$K^{*0}(892); \Gamma = 47.3 \pm 0.5 \text{ MeV}$

$f_0(980); \Gamma \approx 10 - 100 \text{ MeV}$

triangular diagrams

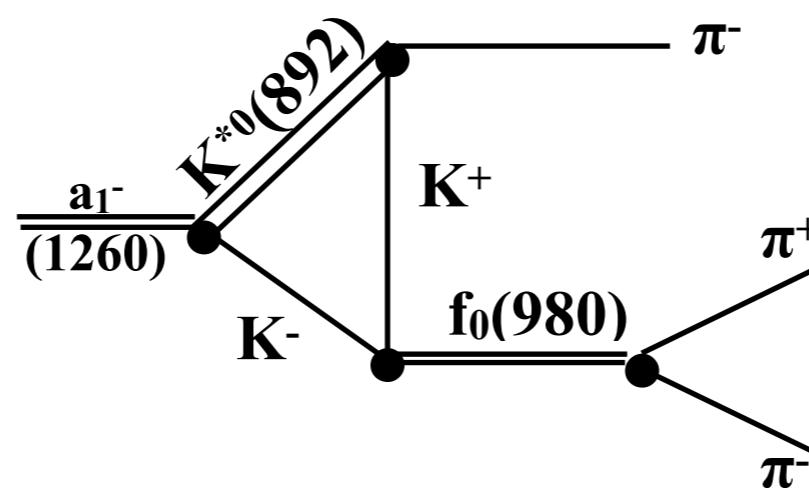
CBELSA/TAPS

$$\gamma p \rightarrow p \pi^0 \eta$$



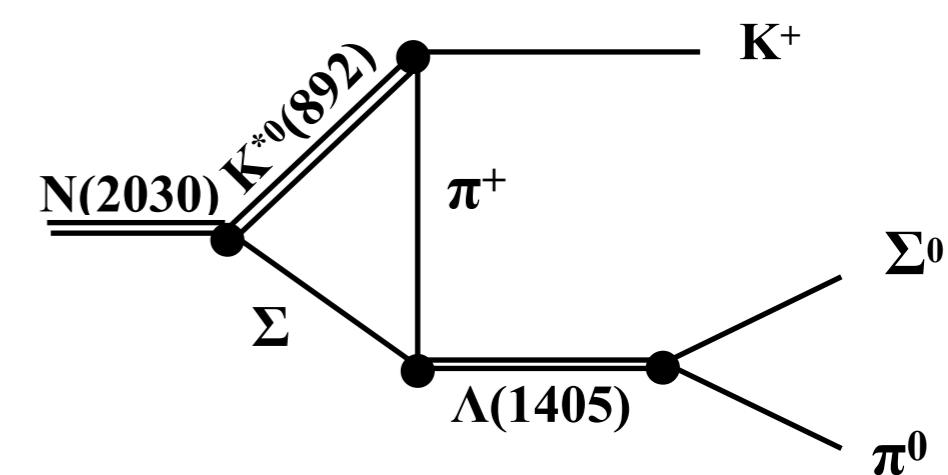
COMPASS

$$\begin{aligned} \pi^- p &\rightarrow a_1^- (1260) p \\ a_1^- (1260) &\rightarrow \pi^- \pi^+ \pi^- \end{aligned}$$



BGOOD

$$\gamma p \rightarrow K^+ \pi^0 \Sigma^0$$



kinematics: singularity

$a_0(980); \Gamma \approx 50 - 100 \text{ MeV}$

$\Delta(1232); \Gamma \approx 117 \text{ MeV}$

$K^{*0}(892); \Gamma = 47.3 \pm 0.5 \text{ MeV}$

$f_0(980); \Gamma \approx 10 - 100 \text{ MeV}$

$K^{*0}(892); \Gamma = 47.3 \pm 0.5 \text{ MeV}$

$\Lambda(1405); \Gamma = 50.5 \pm 2.0 \text{ MeV}$

motivation:

observation of narrow N(1685) resonances in $\gamma N \rightarrow \eta \pi N$ reactions

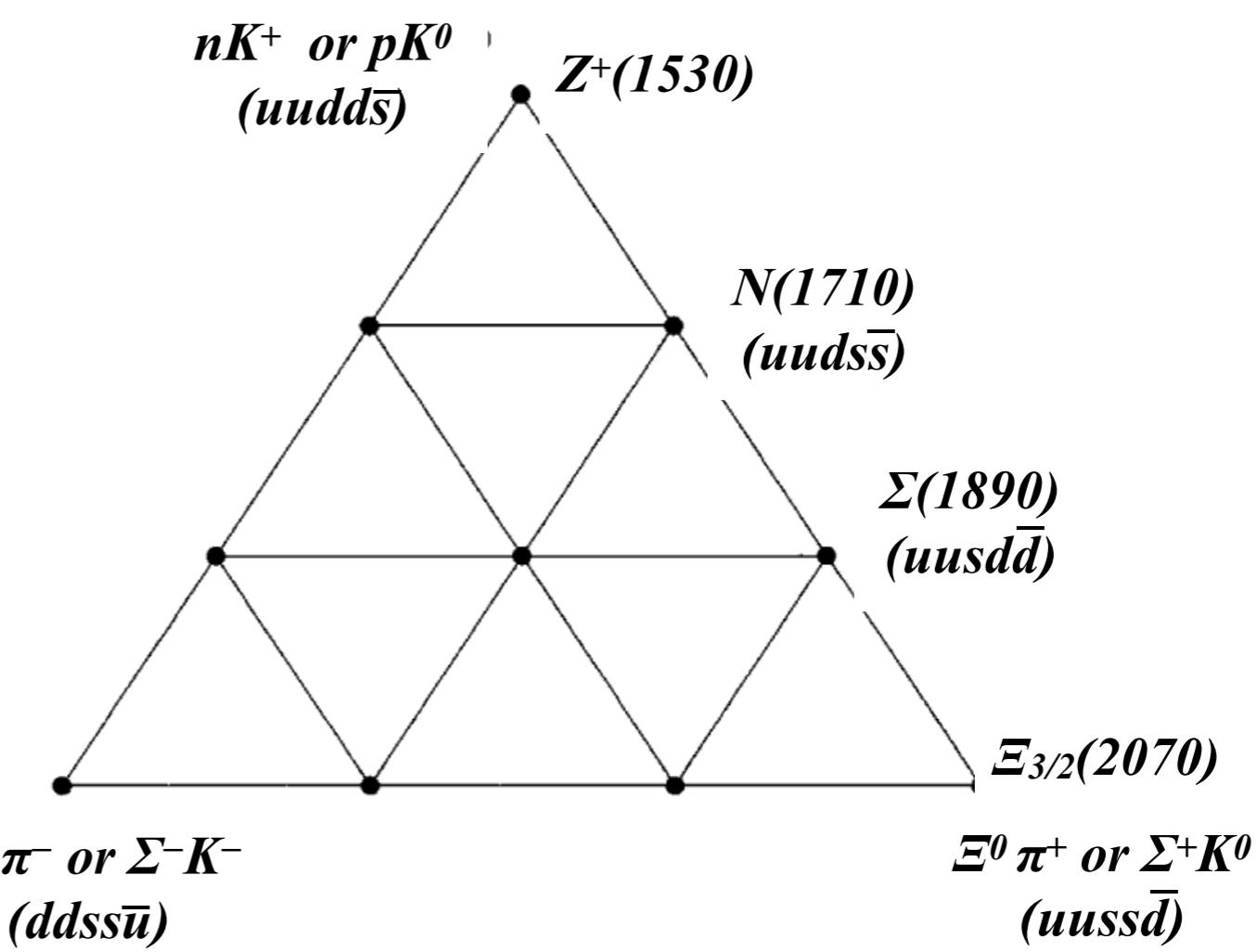
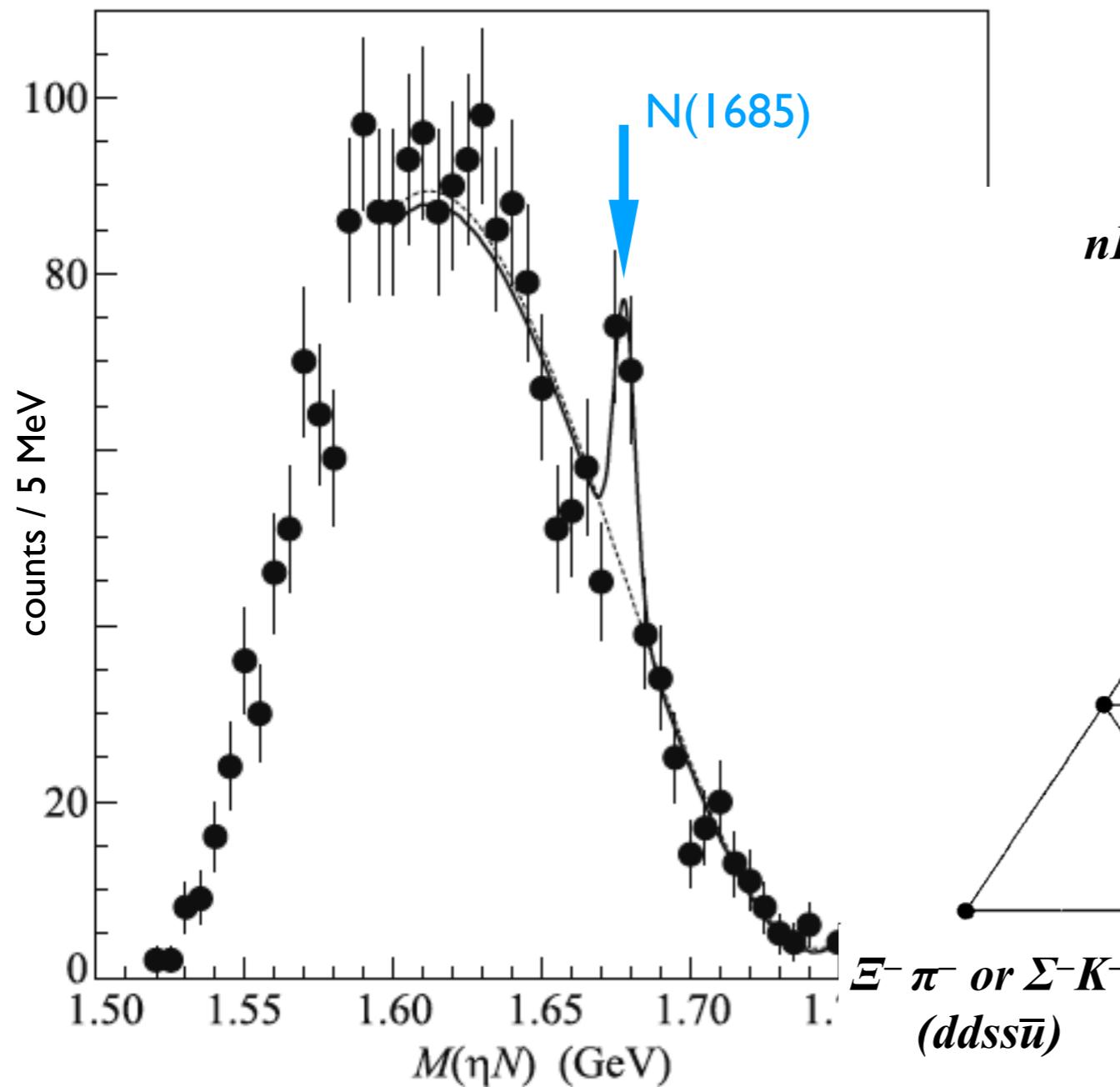
V. Kuznetsov et al., JETP Letters 106 (2017) 69

$E_\gamma = 1400 - 1500$ MeV

Anti-Decuplet of baryons
in the Chiral Soliton Model

$\gamma N \rightarrow \pi \eta N$ - sum of all channels

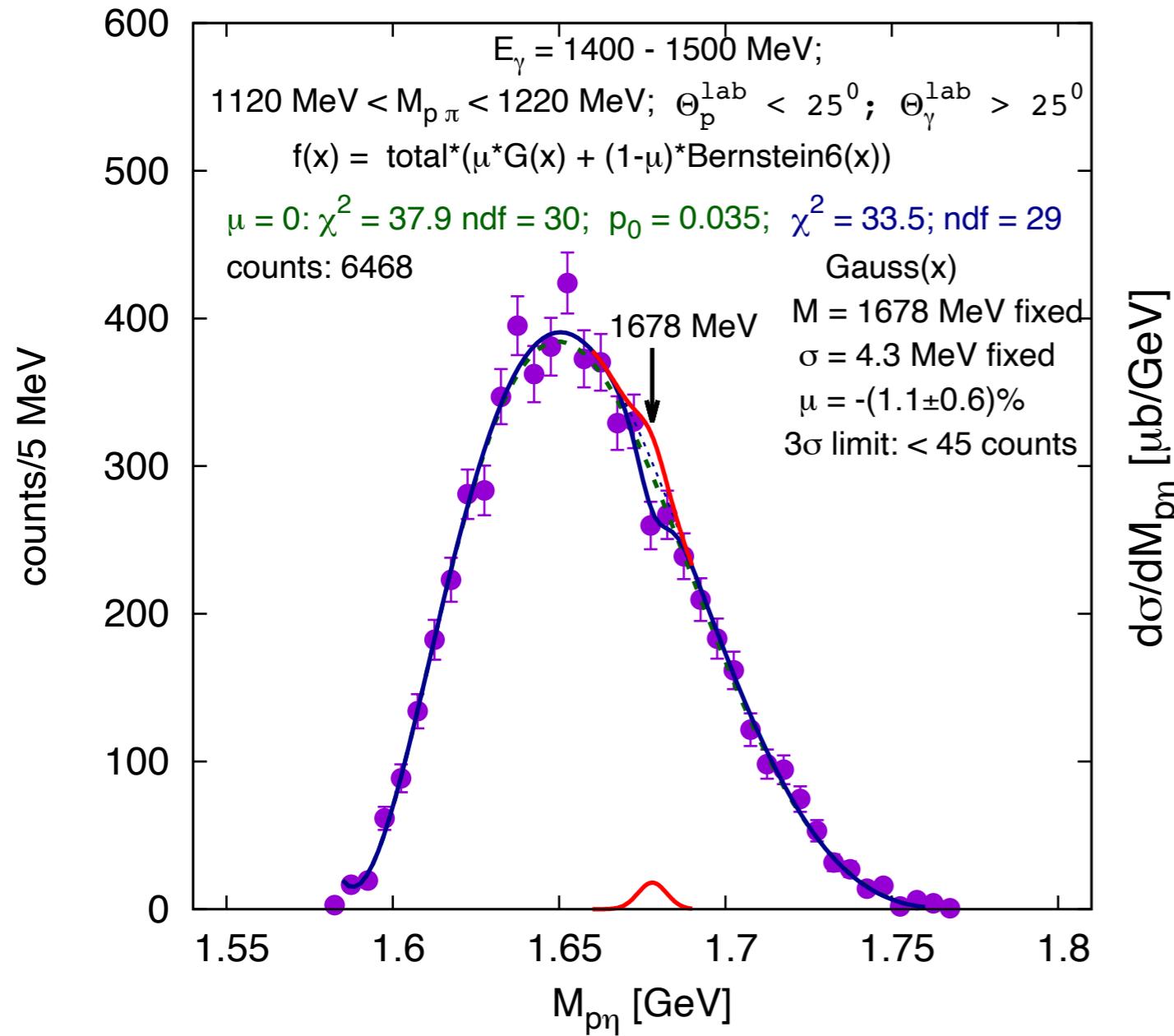
D. Diakonov, V. Petrov, and M.V. Polyakov,
Z. Phys. A 359 (1997) 305



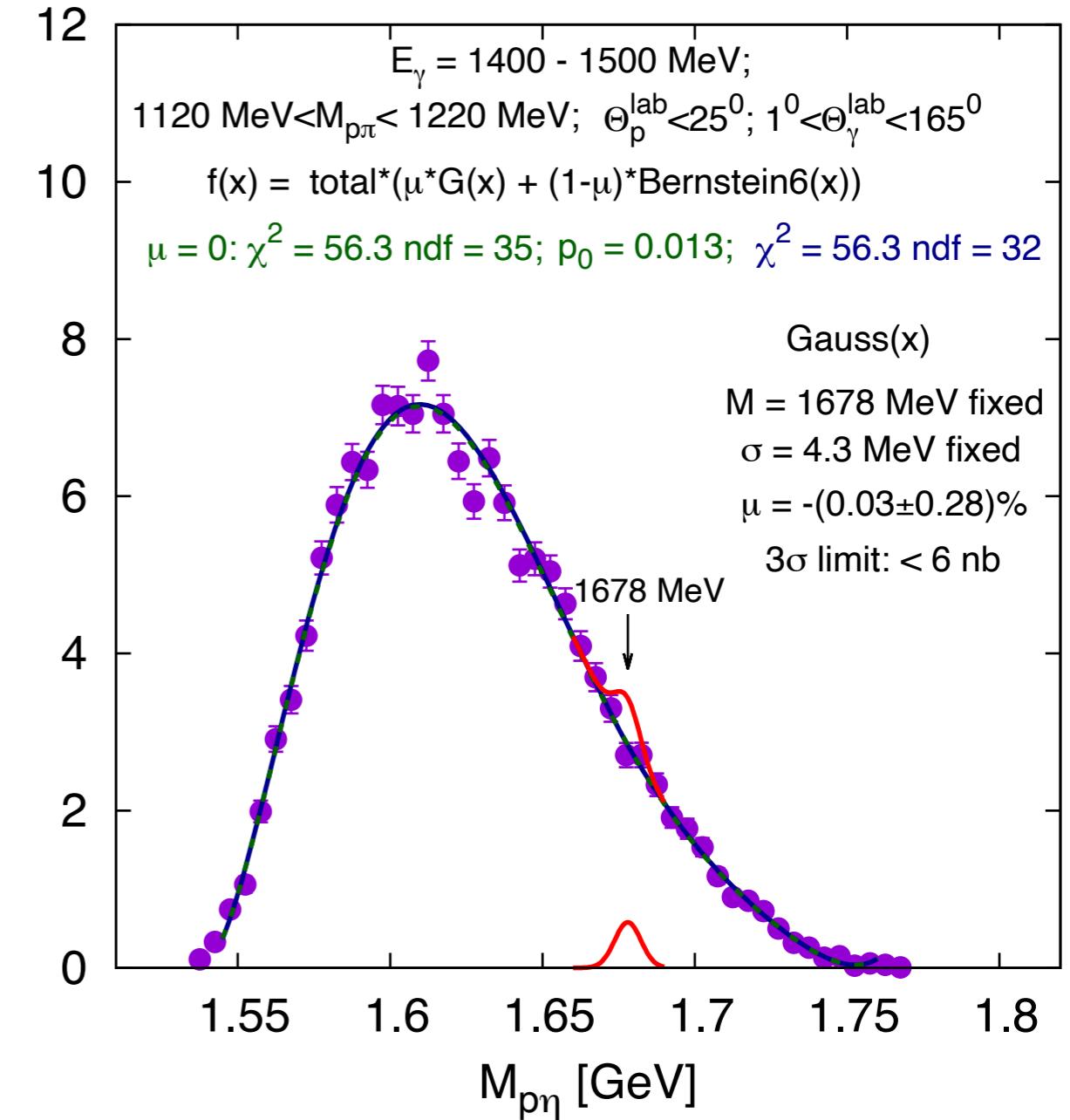
is the narrow structure in $M(\eta N)$ real?

search for a narrow structure in $M(p\eta)$ distribution around 1678 MeV

identical cuts as in JETP 106



acceptance corrected; $\theta_\gamma > 1^\circ$



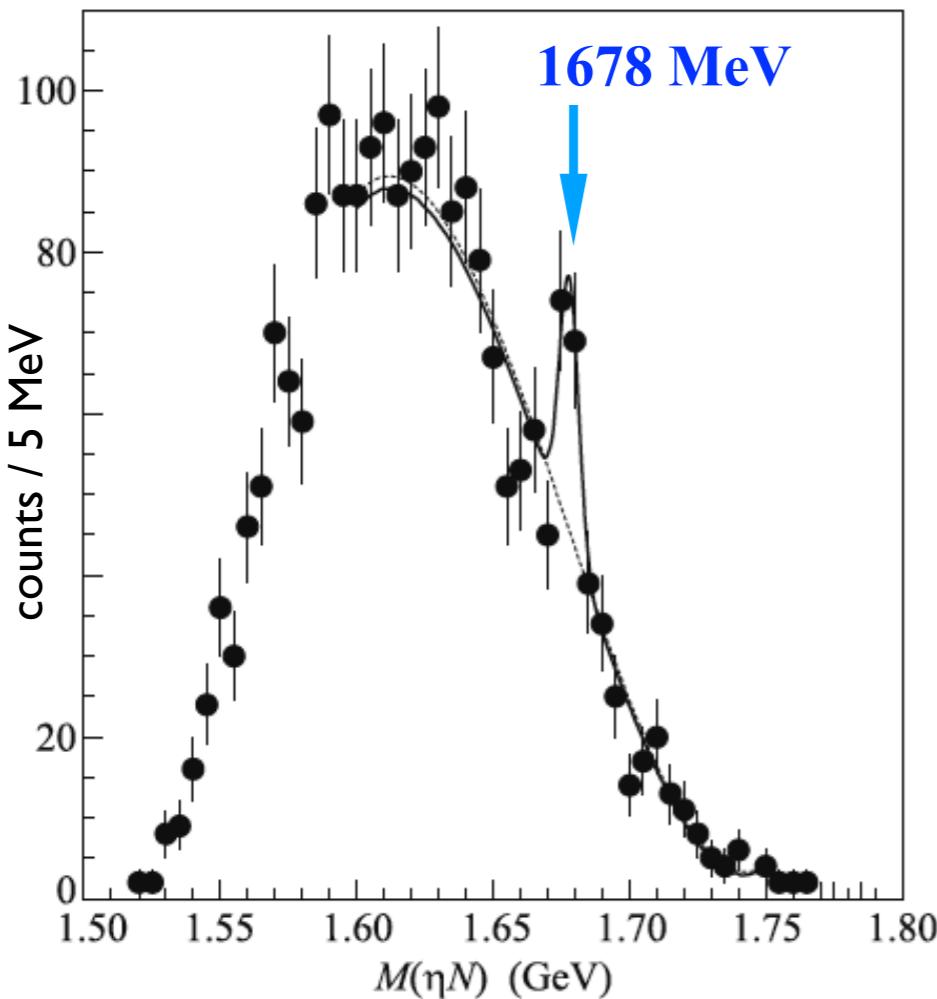
3σ limit: < 45 counts

≈ 4 times higher statistics

motivation: observation of narrow N(1685) resonances in $\gamma N \rightarrow \eta\pi N$ reactions

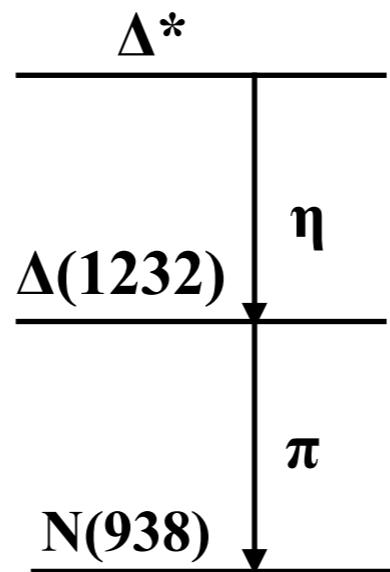
V. Kuznetsov et al.,
JETP Lett. 106 (2017) 693
exotic state predicted by
Chiral Soliton Model

D. Diakonov, V. Petrov, and M.V. Polyakov,
Z. Phys. A 359 (1997) 305



$E_\gamma = 1400 - 1500$ MeV
 $\theta_p < 25^\circ$; $25^\circ < \theta_\gamma < 155^\circ$

$1120 < M_{p\pi} < 1220$ MeV
to suppress
dominant decay

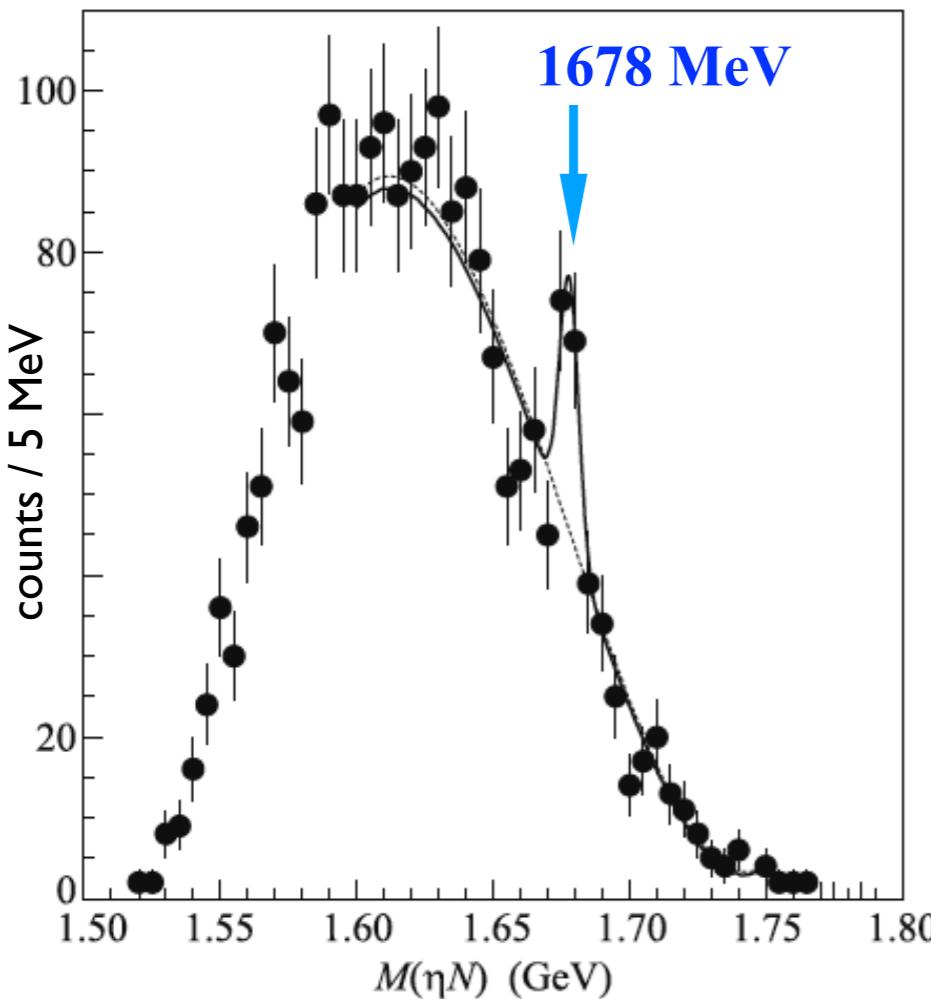


$M_{\eta N} = (1678 \pm 0.8(\text{stat}) \pm 10(\text{syst}))$ MeV;
 $\Gamma \approx 10$ MeV; significance 4.6σ

motivation: observation of narrow N(1685) resonances in $\gamma N \rightarrow \eta\pi N$ reactions

V. Kuznetsov et al.,
 JETP Lett. 106 (2017) 693
 exotic state predicted by
 Chiral Soliton Model

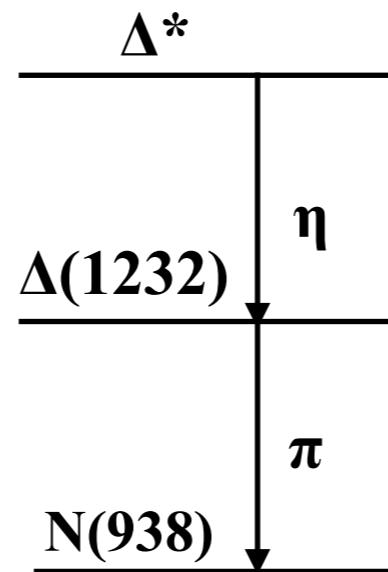
D. Diakonov, V. Petrov, and M.V. Polyakov,
 Z. Phys. A 359 (1997) 305



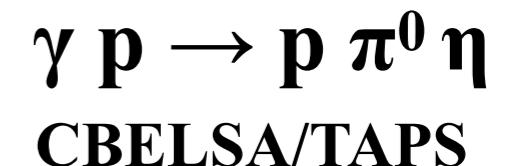
$M_{\eta N} = (1678 \pm 0.8(\text{stat}) \pm 10(\text{syst})) \text{ MeV};$
 $\Gamma \approx 10 \text{ MeV};$ significance 4.6σ

$E_\gamma = 1400 - 1500 \text{ MeV}$
 $\theta_p < 25^\circ; 25^\circ < \theta_\gamma < 155^\circ$

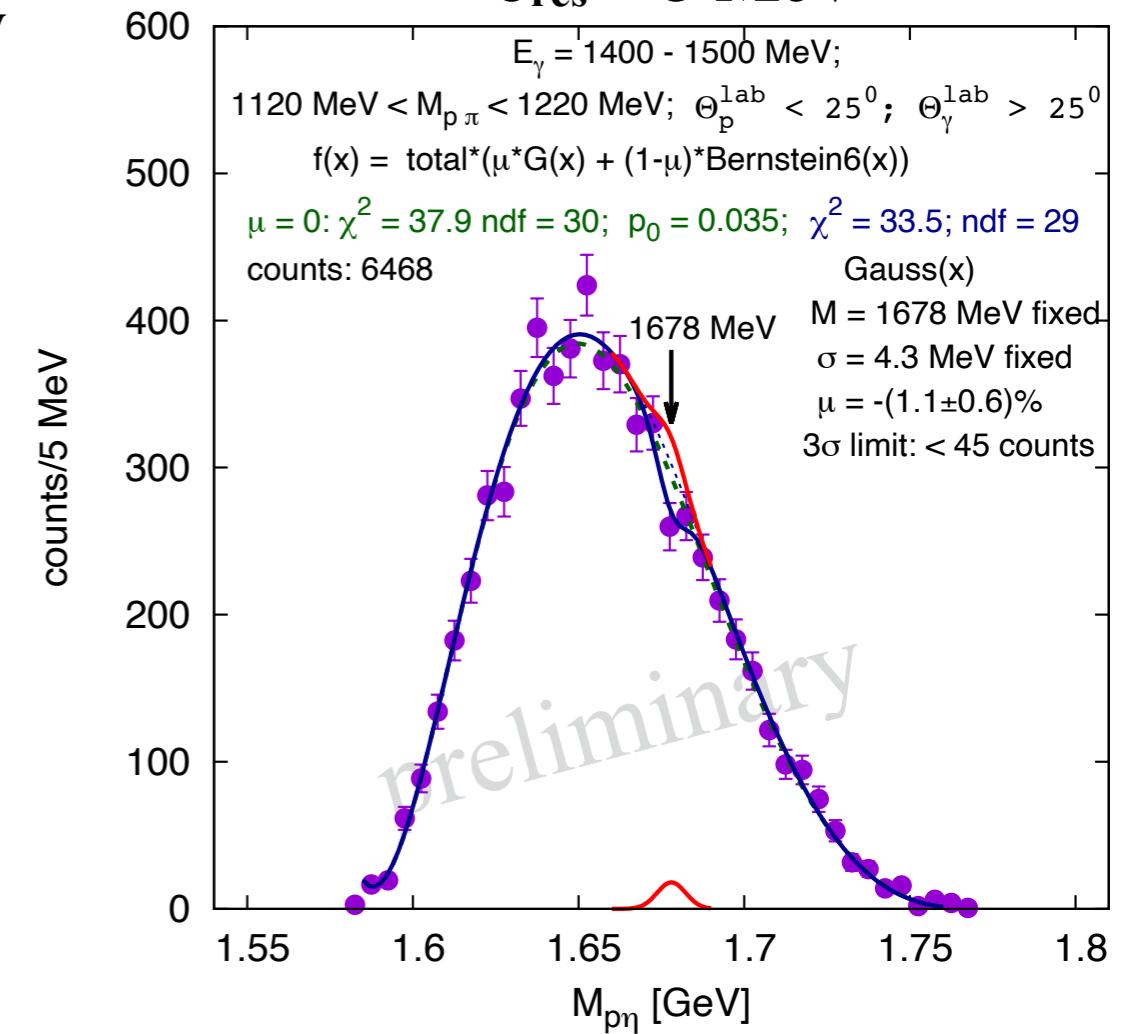
$1120 < M_{p\pi} < 1220 \text{ MeV}$
 to suppress
 dominant decay



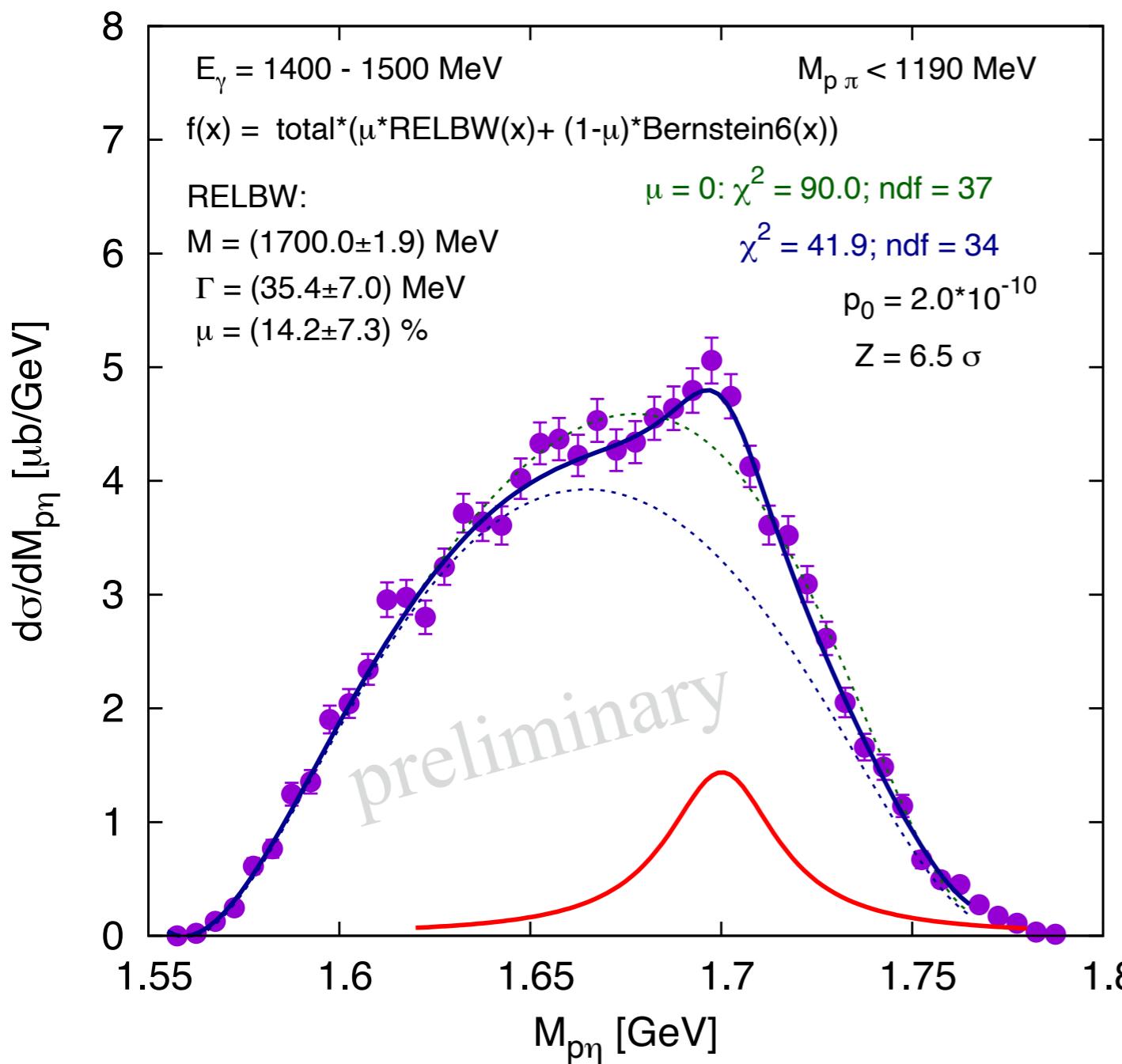
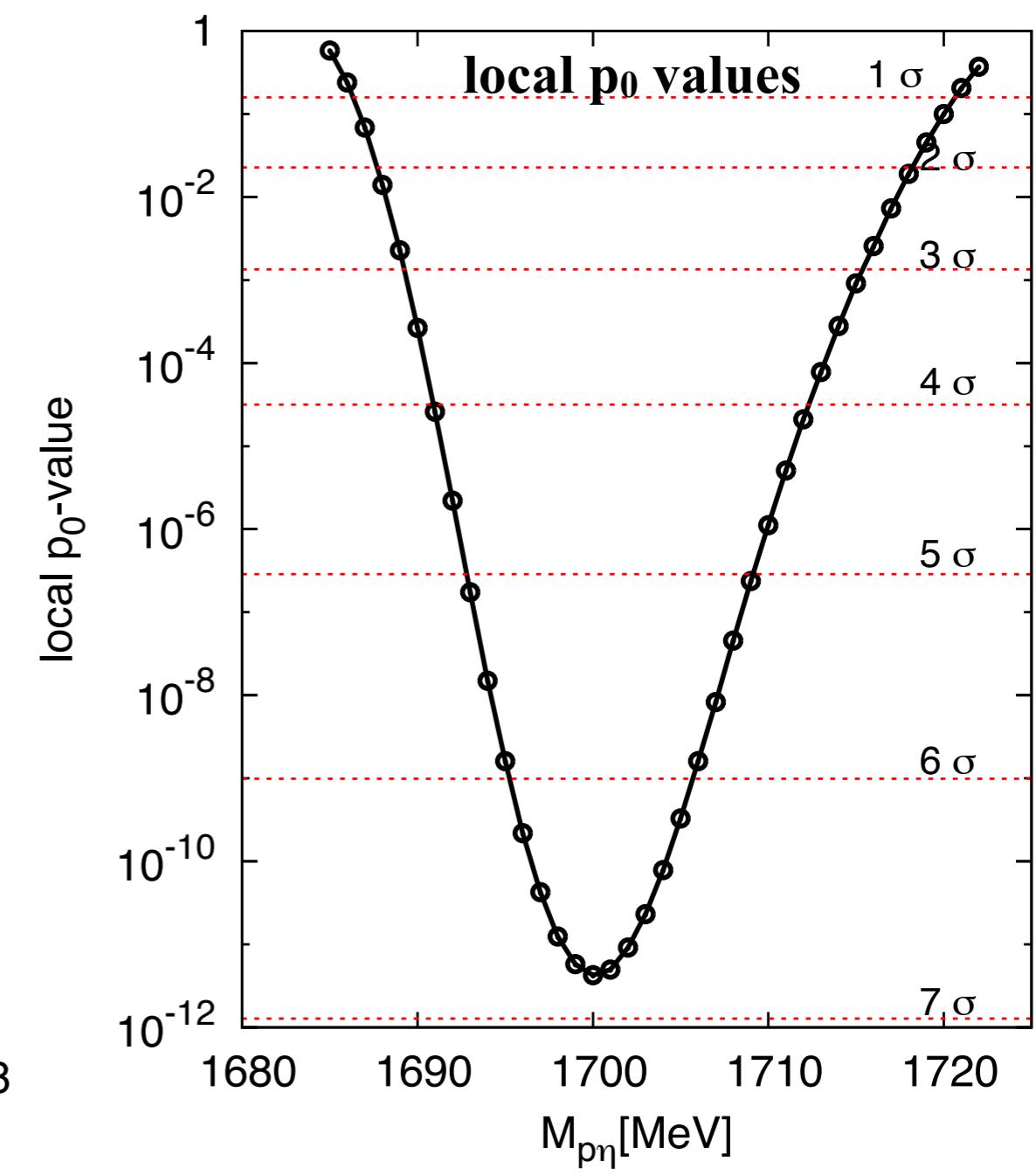
identical conditions:



4.5 times higher statistics;
 $\sigma_{\text{res}} = 5 \text{ MeV}$



< 45 counts: $\sigma_{\text{structure}} < 6 \text{ nb (3}\sigma\text{)}$
structure cannot be confirmed !!!

$E_\gamma = 1400 - 1500 \text{ MeV}$ $M_{p\pi} < 1190 \text{ MeV}$ **statistical significant structure observed at $M_{p\eta} \approx 1700 \text{ MeV}$**  $M_{p\eta} = (1700 \pm 1.9) \text{ MeV}; \Gamma = (35.4 \pm 7.0) \text{ MeV}$ **structure established at 6.8σ**