

High Energy Resummation for Higgs-plus-Jet(s) Production



Jennifer Smillie

Higgs Maxwell Meeting, Feb 2023

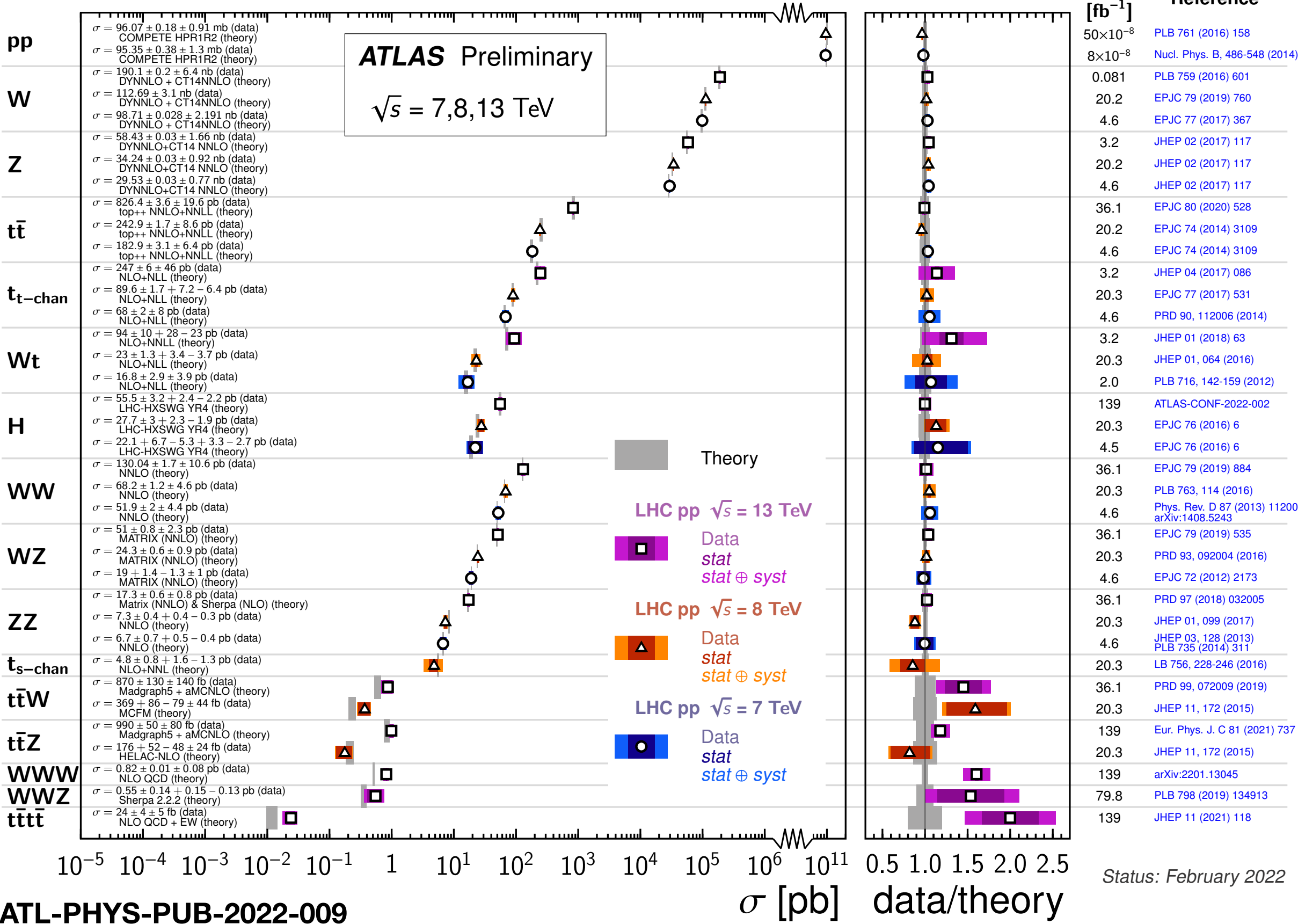




LHC Summary So Far...



Standard Model Total Production Cross Section Measurements



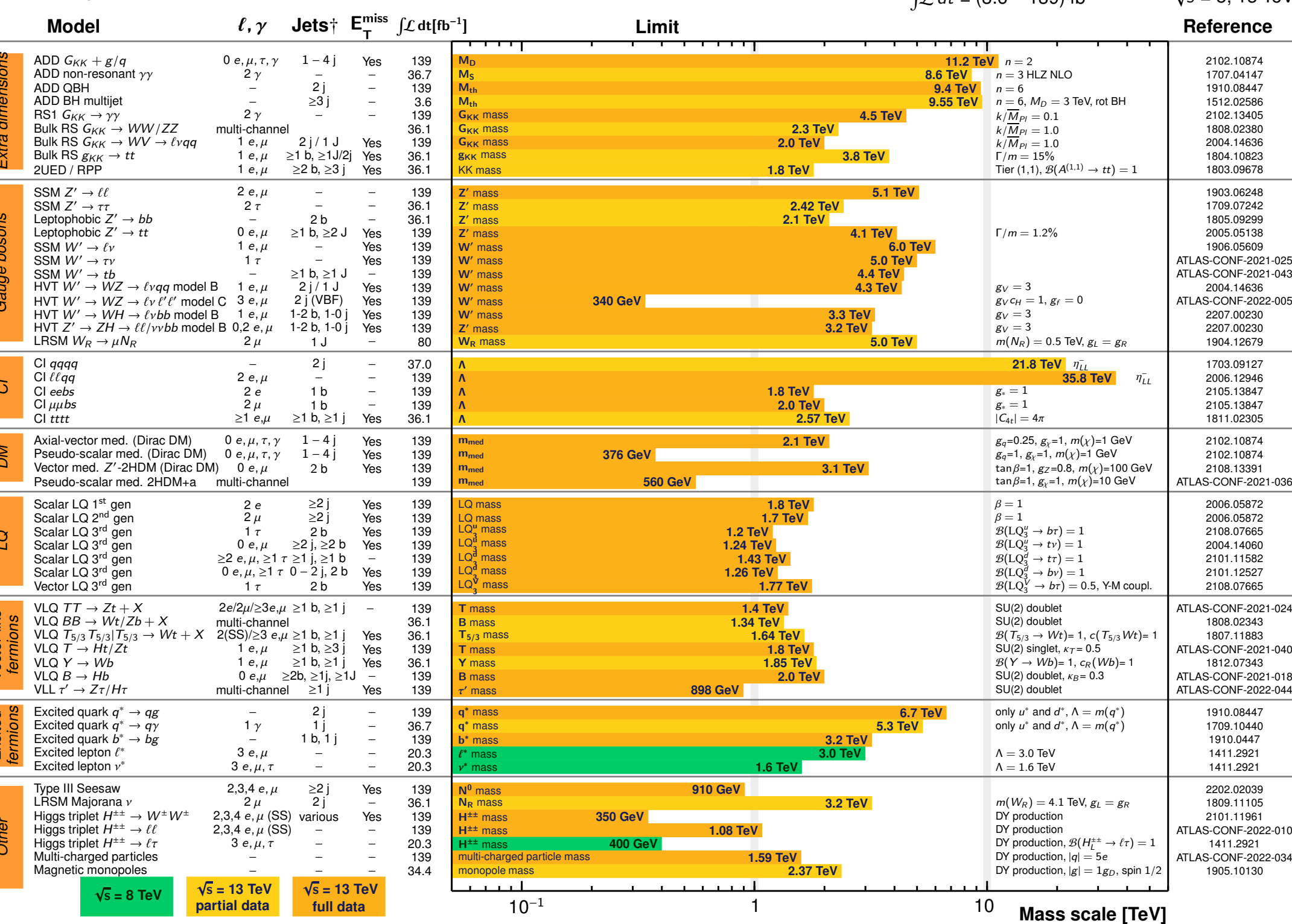
ATL-PHYS-PUB-2022-009

- Phenomenal agreement with theory so far
- Very sophisticated calculations, e.g. $t\bar{t}$ at NNLO+NNLL
Czakon, Mitov [arXiv:1112.5675](#)

New physics searches have generated many exclusion limits (huge range of models, very high limits)

ATLAS Heavy Particle Searches* - 95% CL Upper Exclusion Limits

Status: July 2022



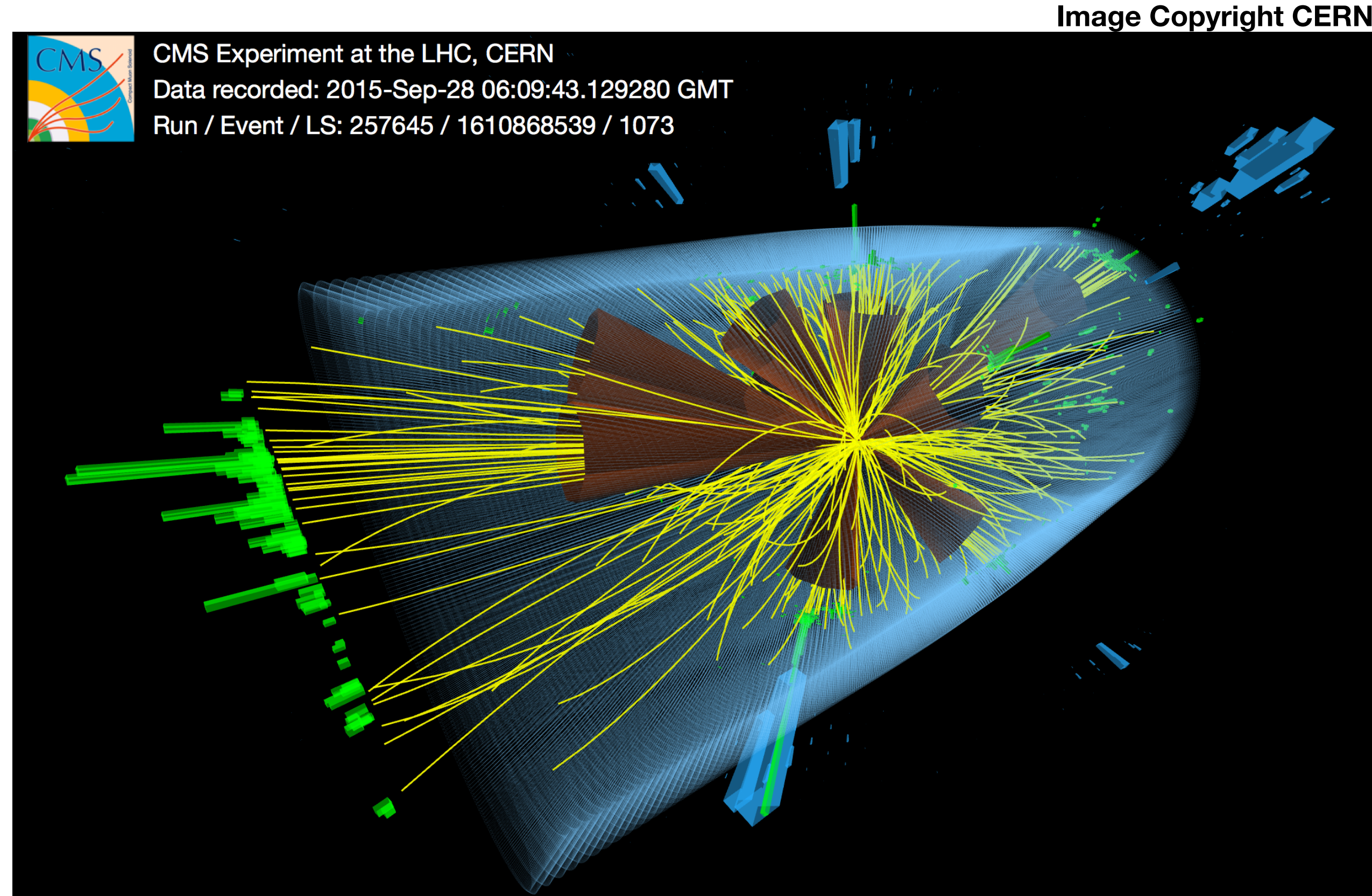
*Only a selection of the available mass limits on new states or phenomena is shown.

\dagger Small-radius (large-radius) jets are denoted by the letter j (J).

ATL-PHYS-PUB-2022-034

A Challenge at High Centre of Mass

12 jets with $p_T > 50 \text{ GeV}$
at CMS (13 TeV)

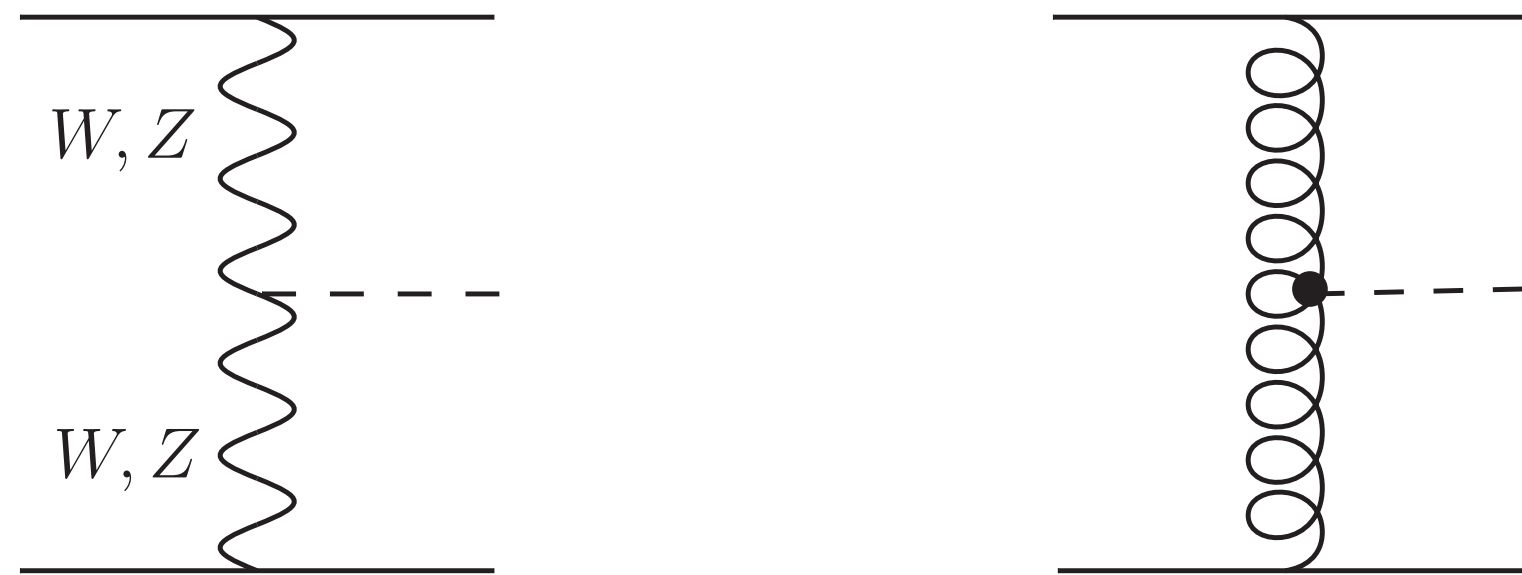


Many colour-charged, hard particles with p_T , s_{ij} , \hat{s}

Large logs in s_{ij}/p_T^2 damage convergence of pert. expansion

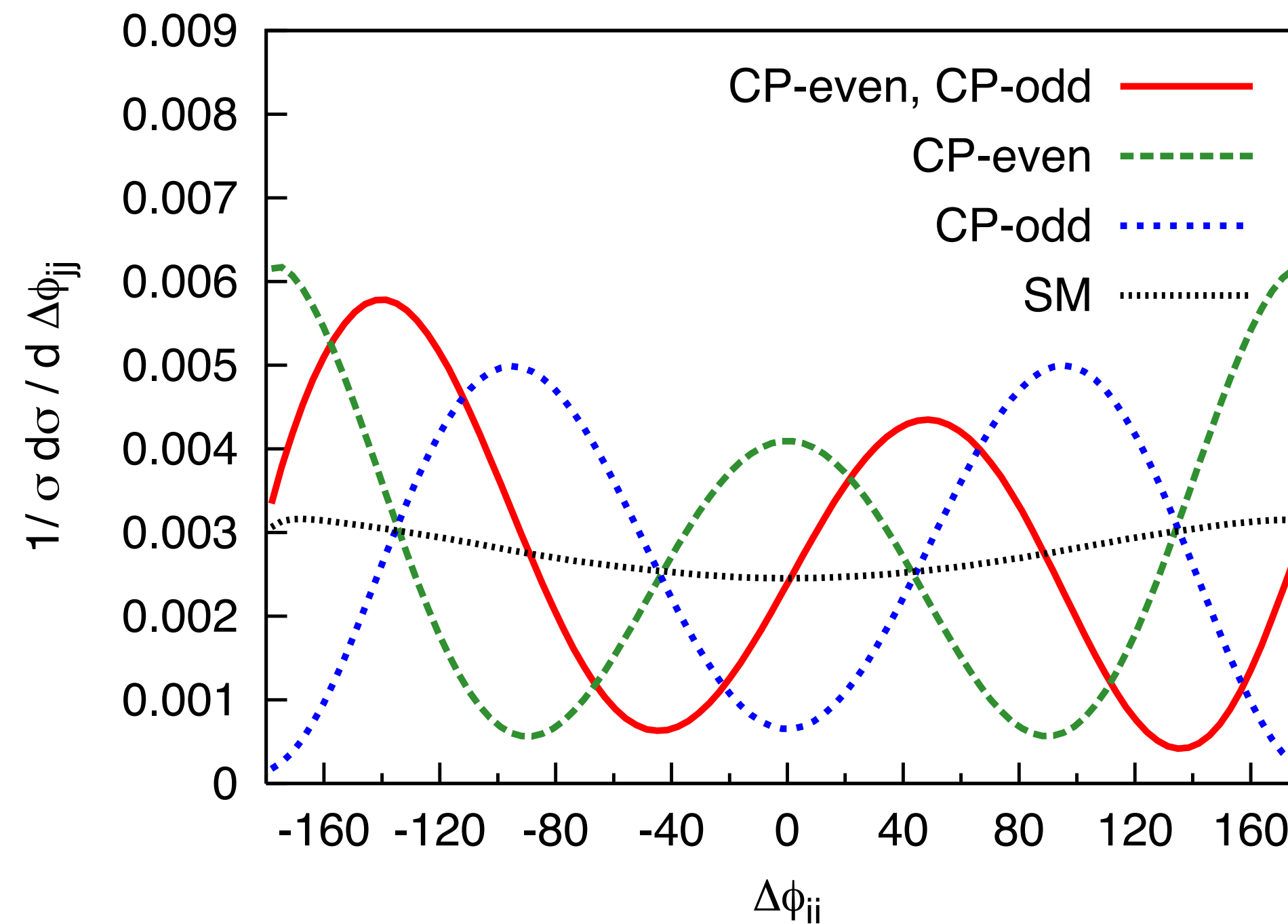
Higgs + Dijets

Higgs boson looks like SM so far, but critical to check CP structure of couplings to bosons



Azimuthal angle between the dijets is sensitive to this

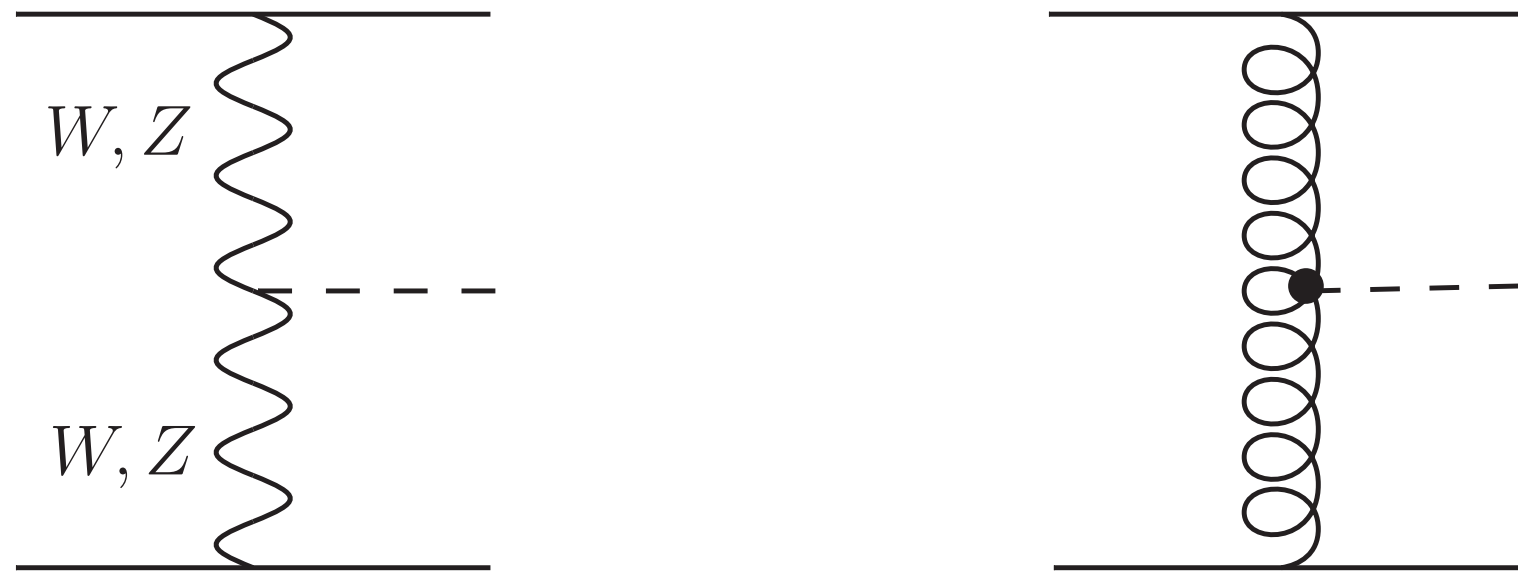
Figy et al [hep-ph/0609075](https://arxiv.org/abs/hep-ph/0609075)



ggH

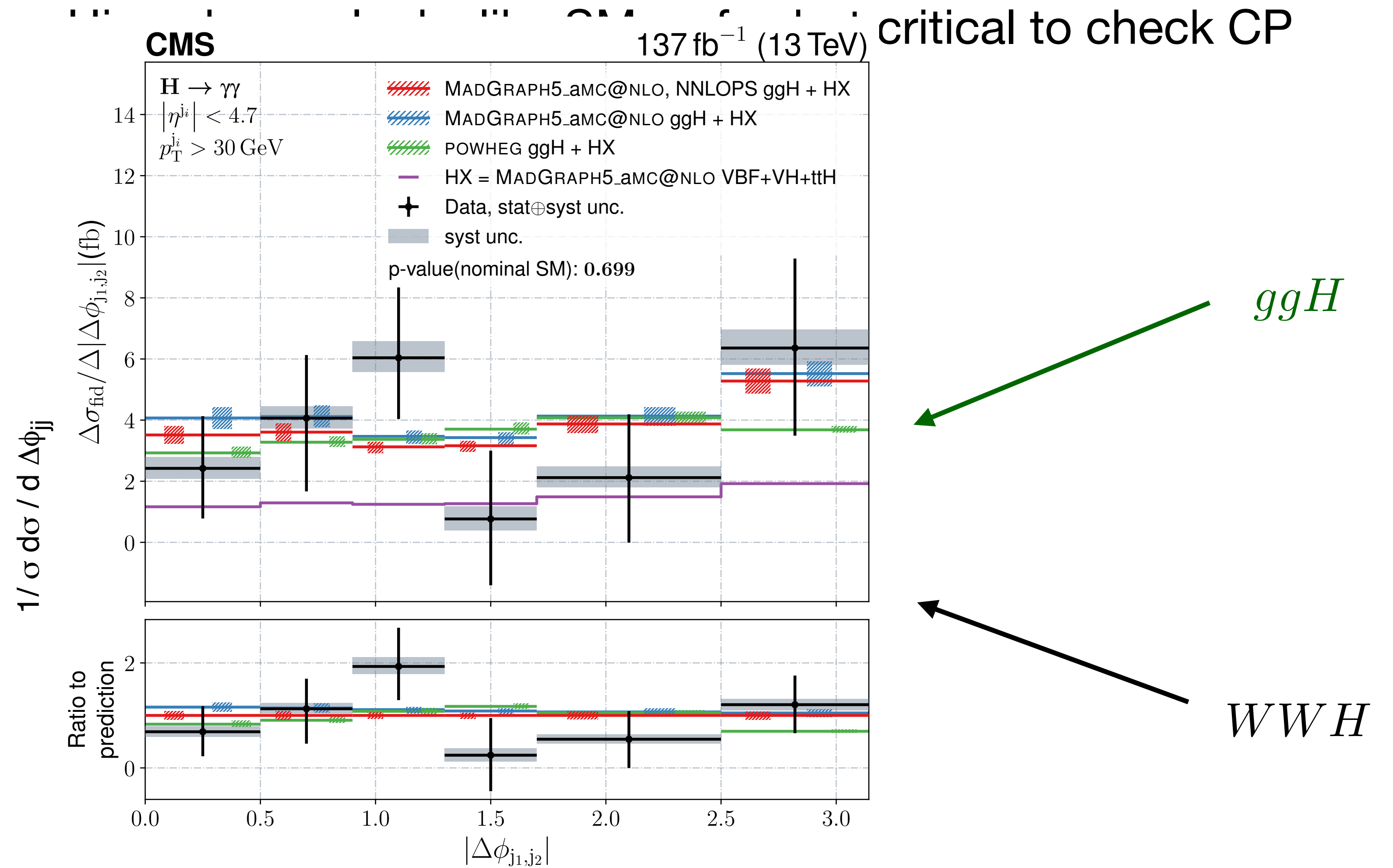
WWH

Higgs + Dijets



Azimuthal angle between the dijets is sensitive to this

Figy et al [hep-ph/0609075](https://arxiv.org/abs/hep-ph/0609075)



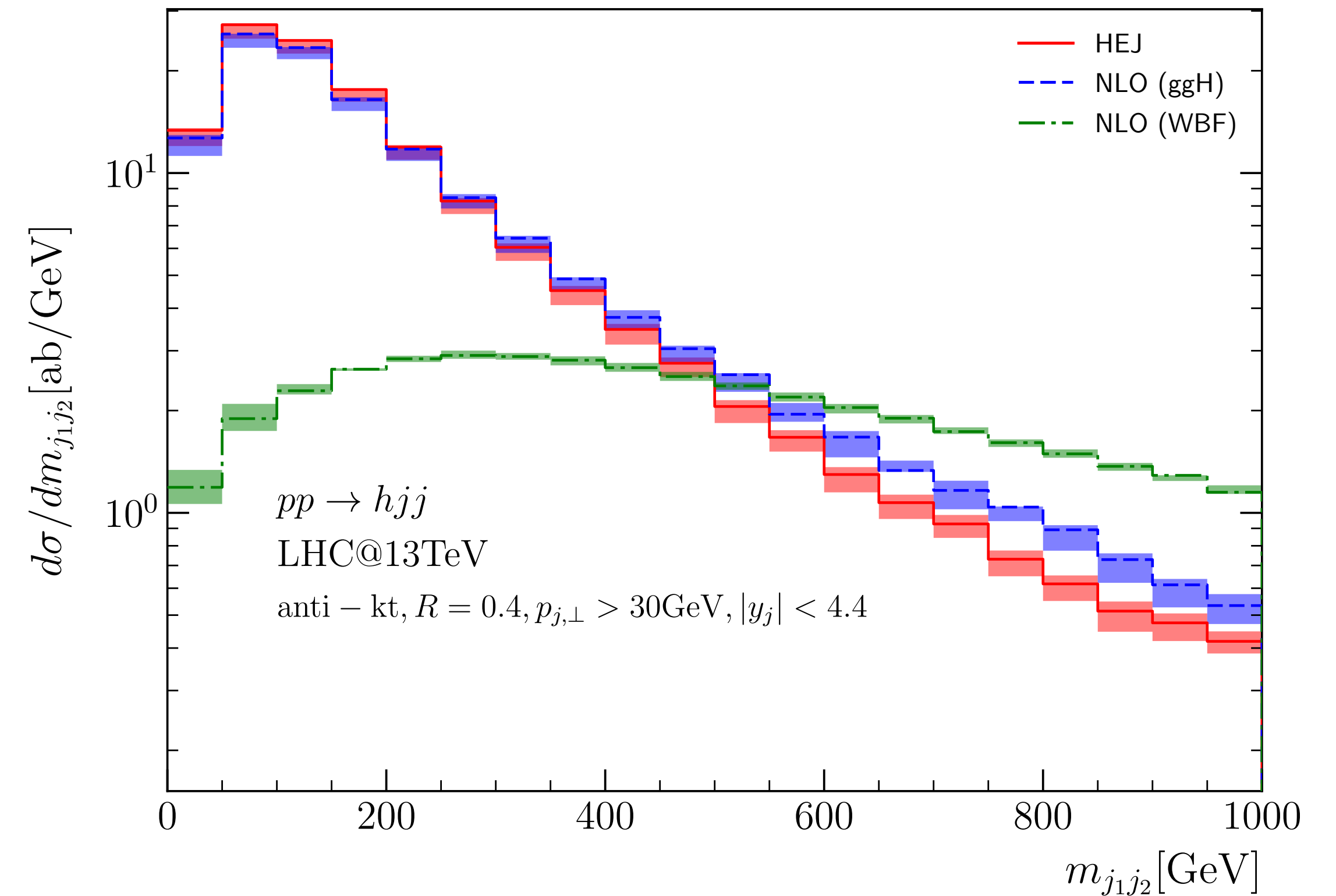
CMS [arXiv:2208.12279](https://arxiv.org/abs/2208.12279)

Higgs + Dijets

Use distinctive event shape to separate channels with “VBF cuts”

e.g. $\Delta y_{jj} > 2.8, m_{jj} > 400 \text{ GeV}$

BUT this precisely enhances higher orders in pert. expansion



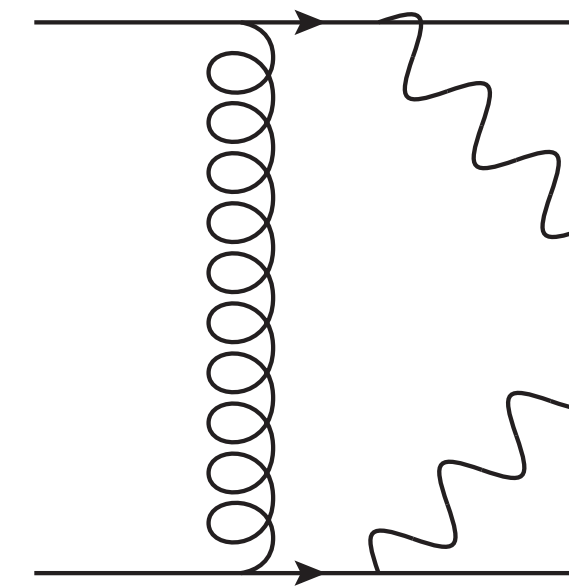
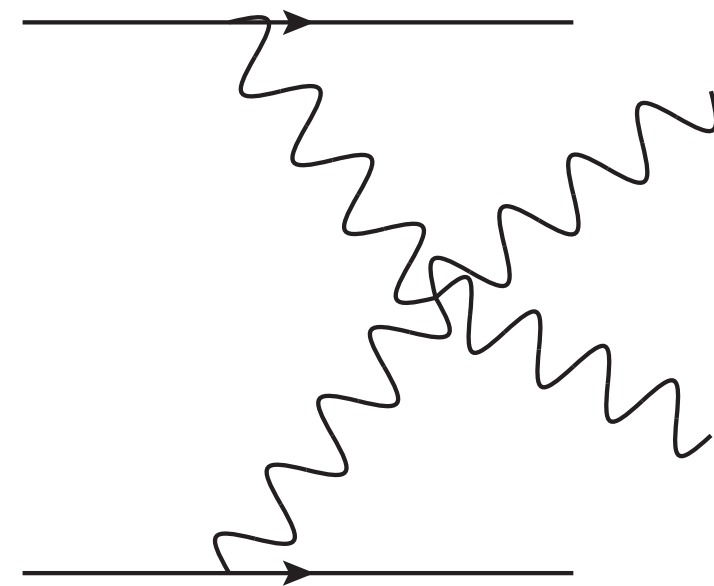
Andersen, Heil, Maier & JMS, in [arXiv:1803.07977](https://arxiv.org/abs/1803.07977)

Vector Boson Scattering

Vector Boson Scattering (VBS) sensitive probe of EWSB

$pp \rightarrow W^+ W^+ jj$ proceeds through various diagrams including

$$\text{EW} = O(\alpha_W^4)$$

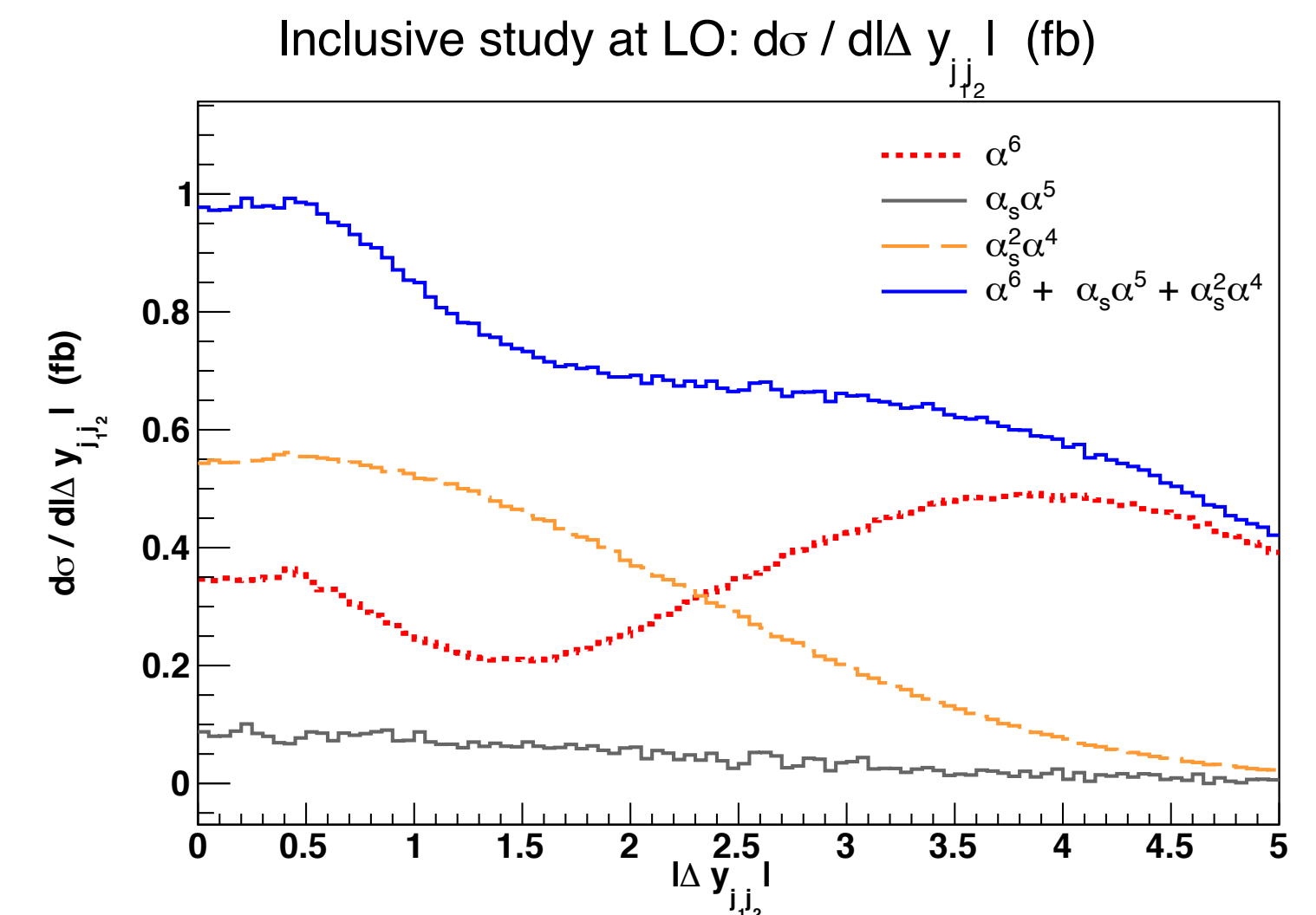


$$\text{QCD} = O(\alpha_W^2 \alpha_s^2)$$

We would like to separate the EW and QCD channels, justified by assessing interference between the two to be small

To isolate EW component, typically apply VBS cuts of large rapidity and/or large invariant mass on the jets.

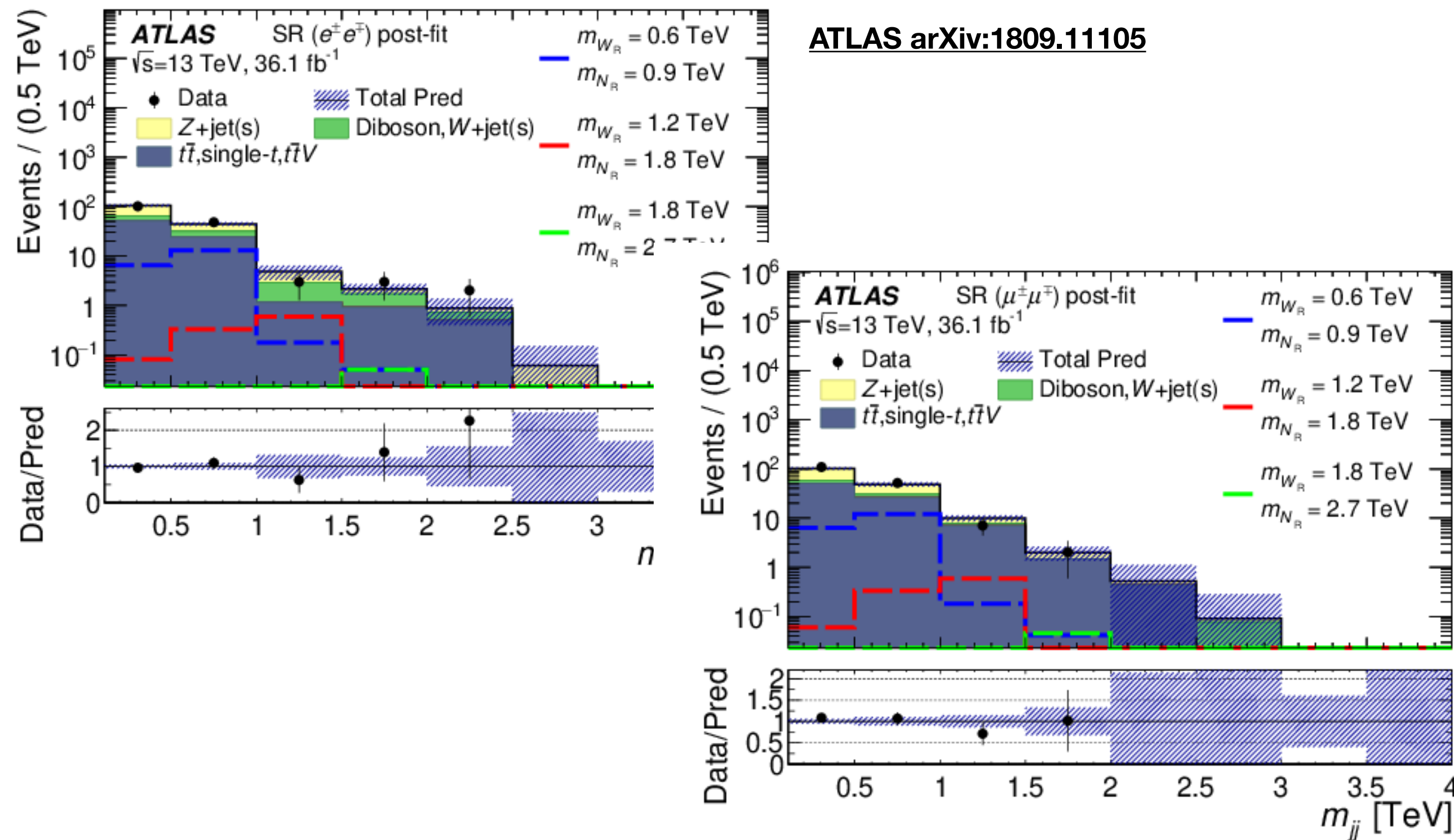
Very similar to $pp \rightarrow Hjj$



Ballestrero et al arXiv:1803.07943

We want to exploit high centre-of-mass energy to search for new heavy particles at large invariant mass

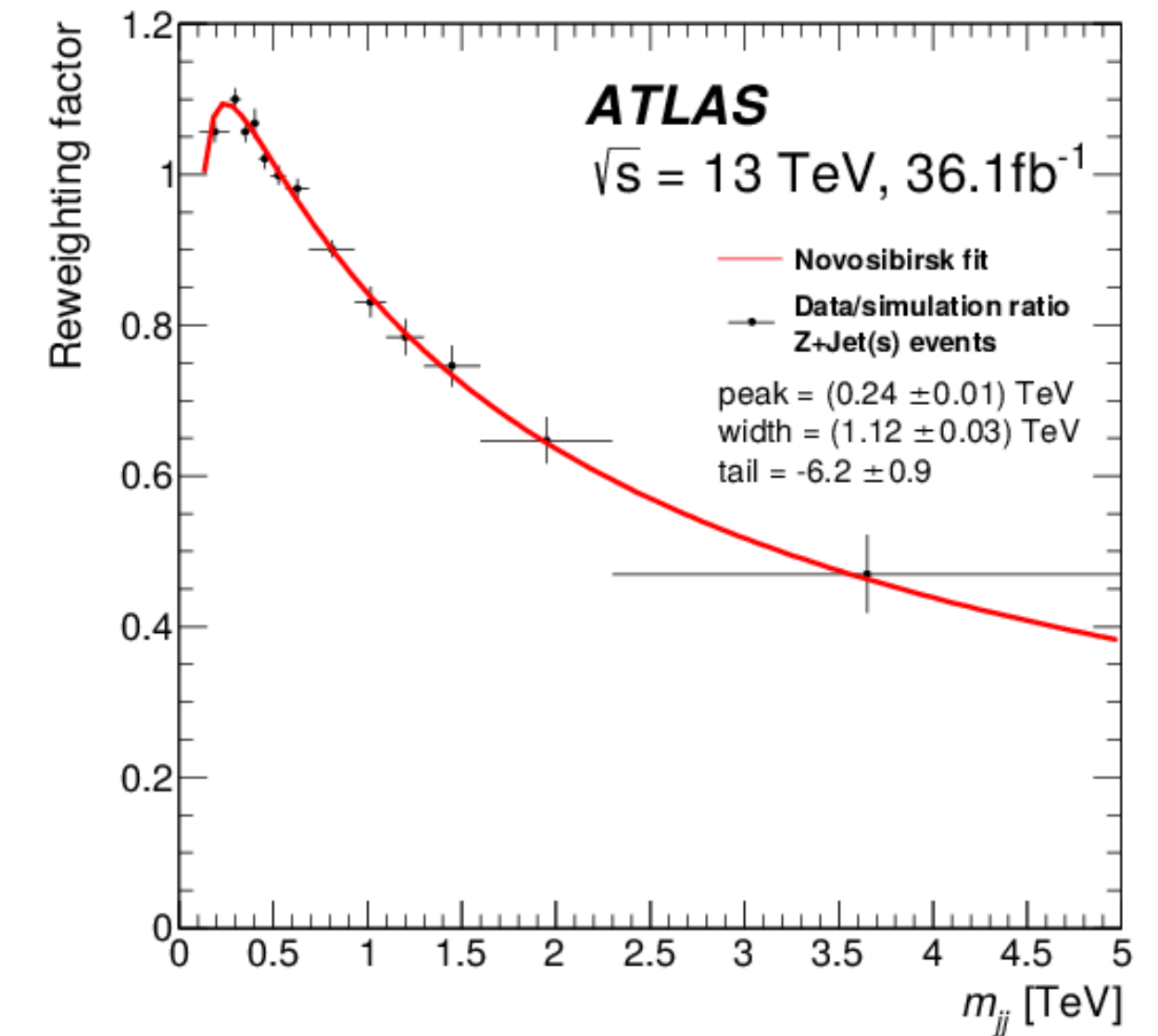
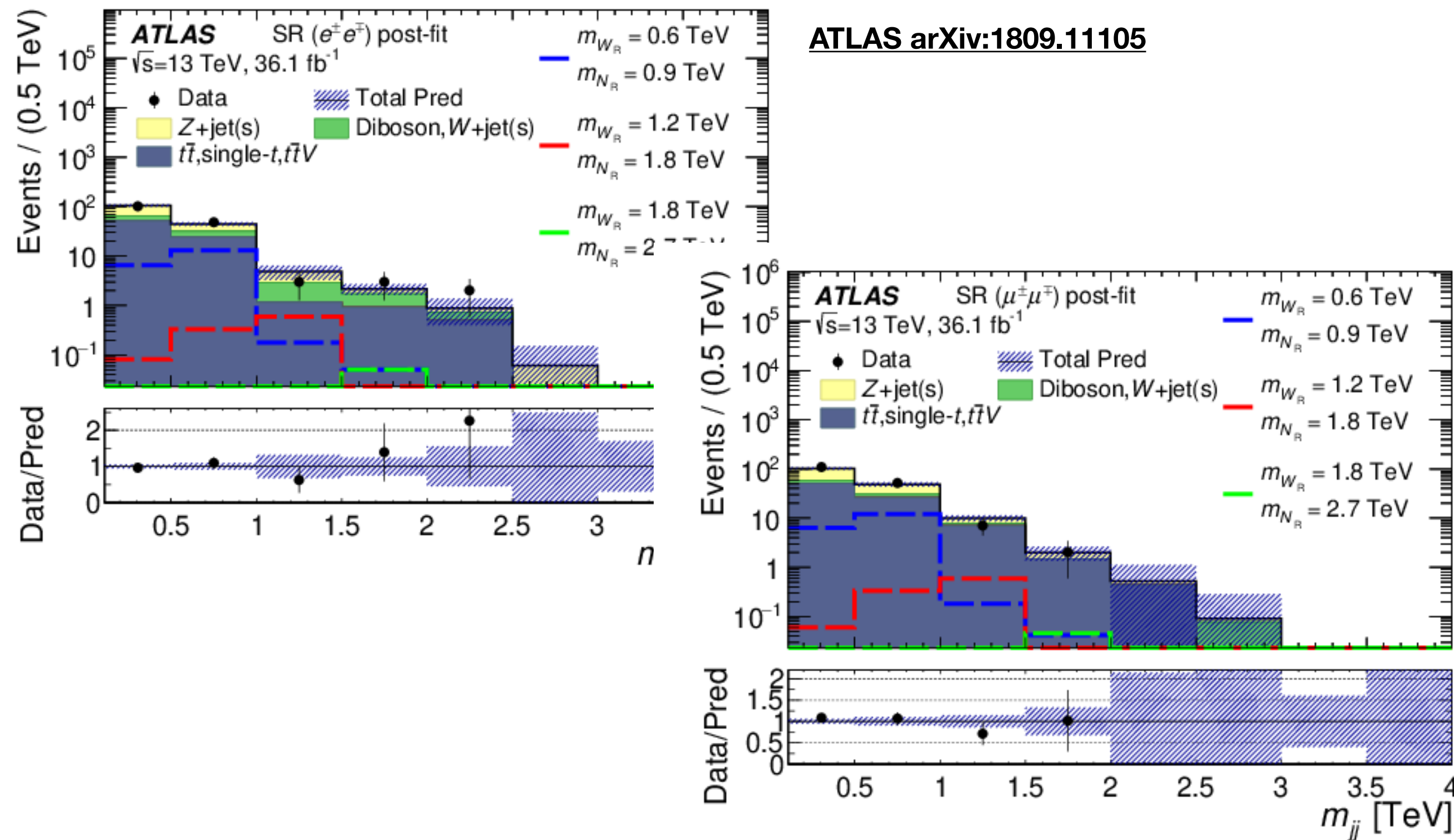
e.g. a search for heavy right-handed neutrinos or right-handed Ws



Exotics Searches

We want to exploit high centre-of-mass energy to search for new heavy particles at large invariant mass

e.g. a search for heavy right-handed neutrinos or right-handed Ws



BUT needed to scale the MC background by this much

Which Logs in s/t?

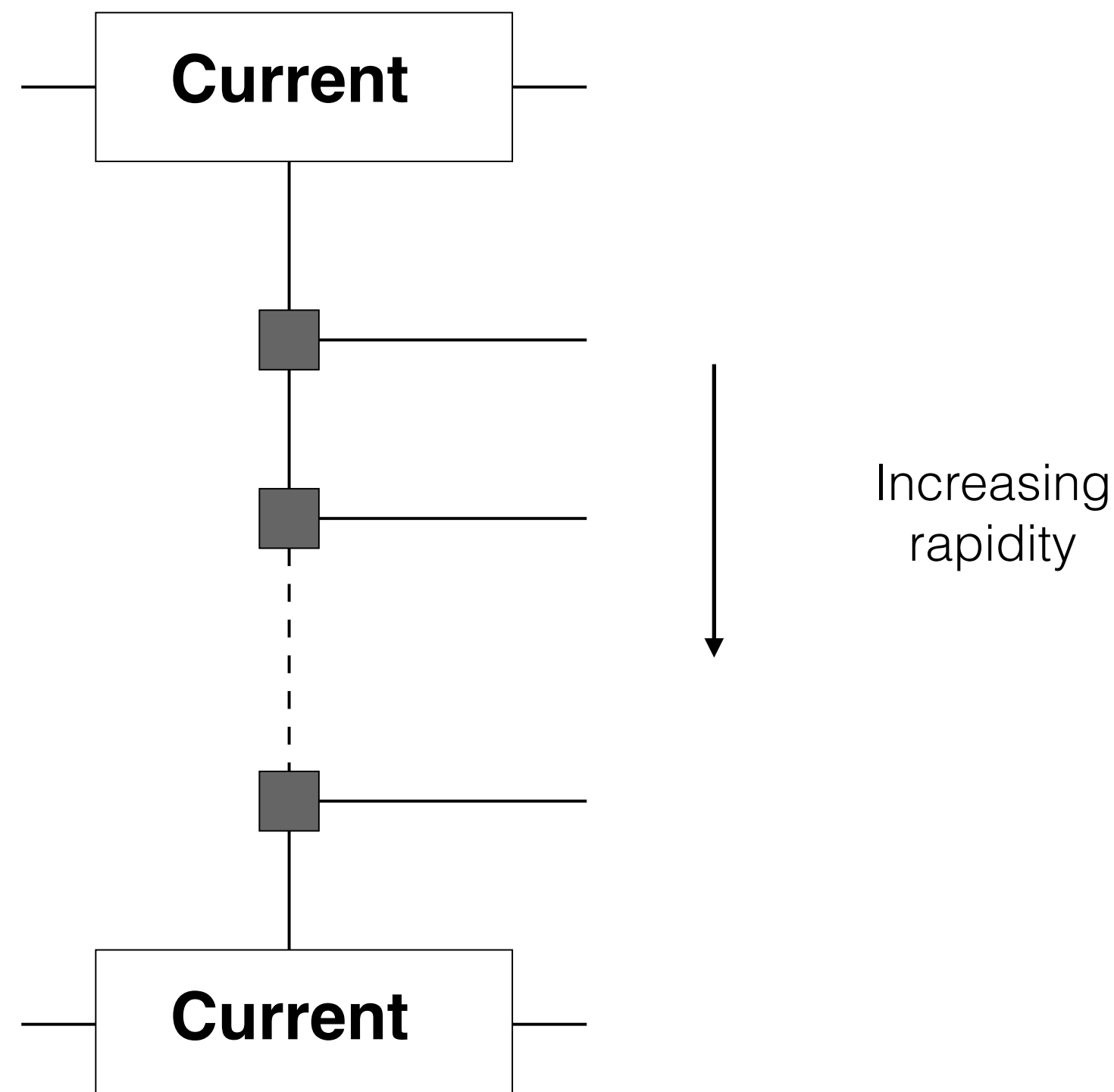
Inclusive 2-jet cross section given by $\int dPS_2 |M_{2j+}|^2$, with

$$\begin{aligned} |M_{2j+}|^2 = & \alpha_s^2 \left(a_2(s^2/t^2) + b_2 \right) \\ & + \alpha_s^3 \left(a_3(s^2/t^2) \log(s/t) + b_3(s^2/t^2) + c_3 \right) \\ & + \alpha_s^4 \left(a_4(s^2/t^2) \log^2(s/t) + b_4(s^2/t^2) \log(s/t) + \dots \right) \\ & + \dots \end{aligned}$$

- LO = first line, NLO = first two lines
- Leading logs = the 'a'-terms: $\alpha_s^{2+k} \log^k(s^2/t^2)$
- Logs arise from integrals over loop momenta in virtuals and from integrals over reals
- Our description = **LO + LL + ...**

Amplitudes in the High Energy Limit

Fortunately, the matrix elements of these processes simplify in the High Energy limit: $s_{ij} \rightarrow \infty$, $|p_{Ti}|$ finite



Local pieces, independent of the rest of the process

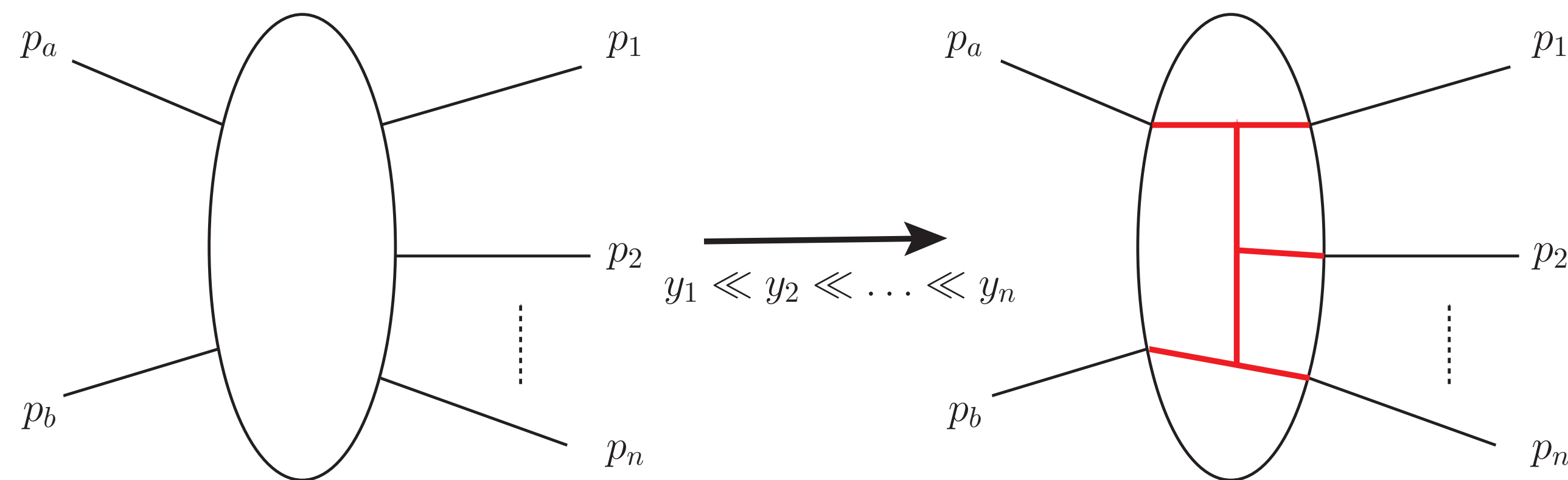
Applies to loop diagrams too, and generates leading logs in s_{ij}/p_T^2

Can use this simpler structure to make an efficient event generator for arbitrary numbers of quarks/gluons.

High Energy limit of amplitudes also many theory applications...

Regge Scaling of Amplitudes

Regge scaling dictates the scaling of an amplitude with s_{ij} for a given process

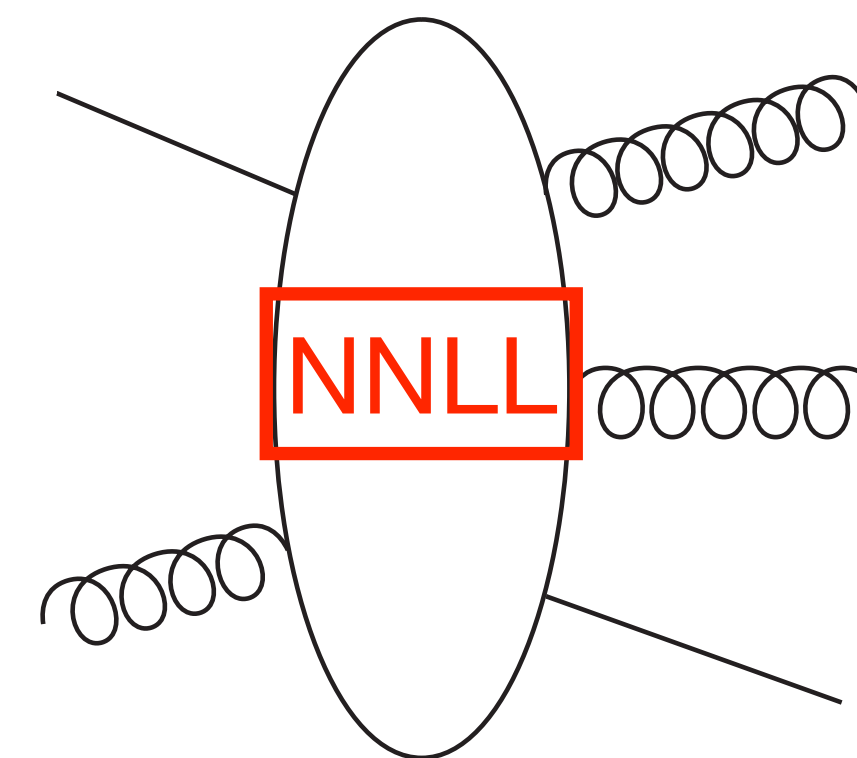
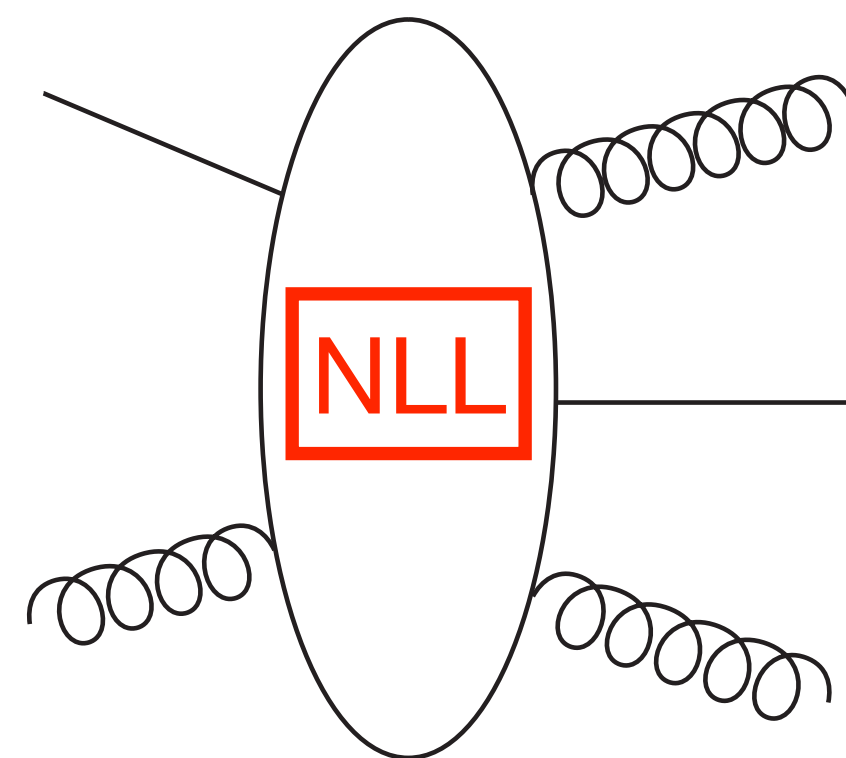
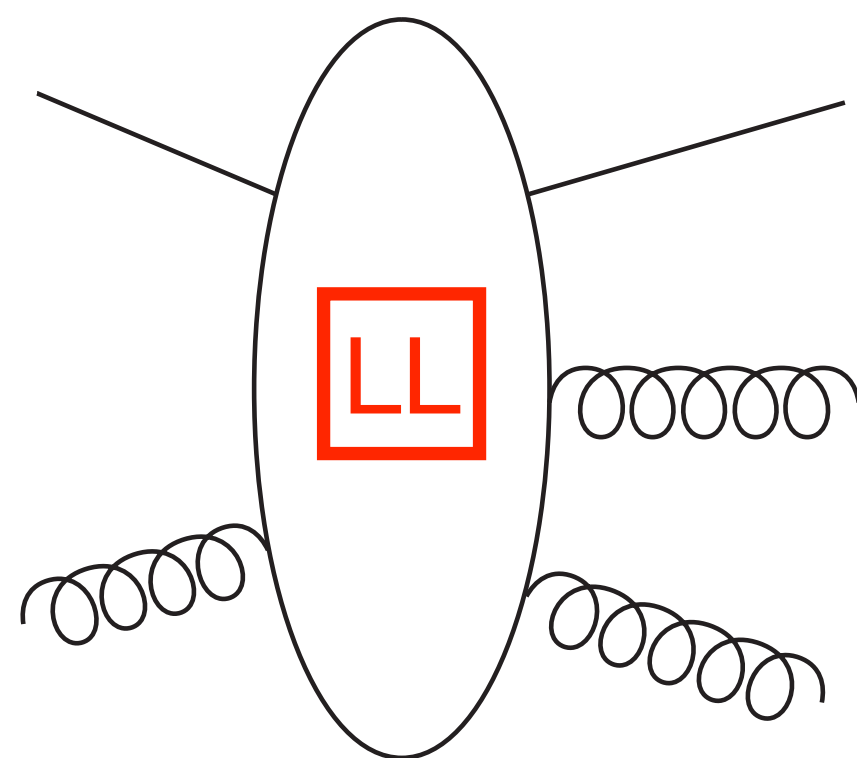


$$\mathcal{M} \propto s_{12}^{\alpha_{12}} \dots s_{n-1,n}^{\alpha_{n-1,n}} f(\{p_{T,i}\})$$

where α_{ij} is the spin of that particle in **effective t-channel**

Brower, DeTar, Weis Phys Rept. 14:257, 1974

Powers of s_{ij} in the real matrix elements match powers of log in the inclusive matrix element.



The High Energy Jets (HEJ) framework is

- exact for simple processes (2 to 2 (+X))
- accurate to leading logarithm in s/t
- constructed event-by-event
- sufficiently fast for numerical integration (up to 30 gluons)

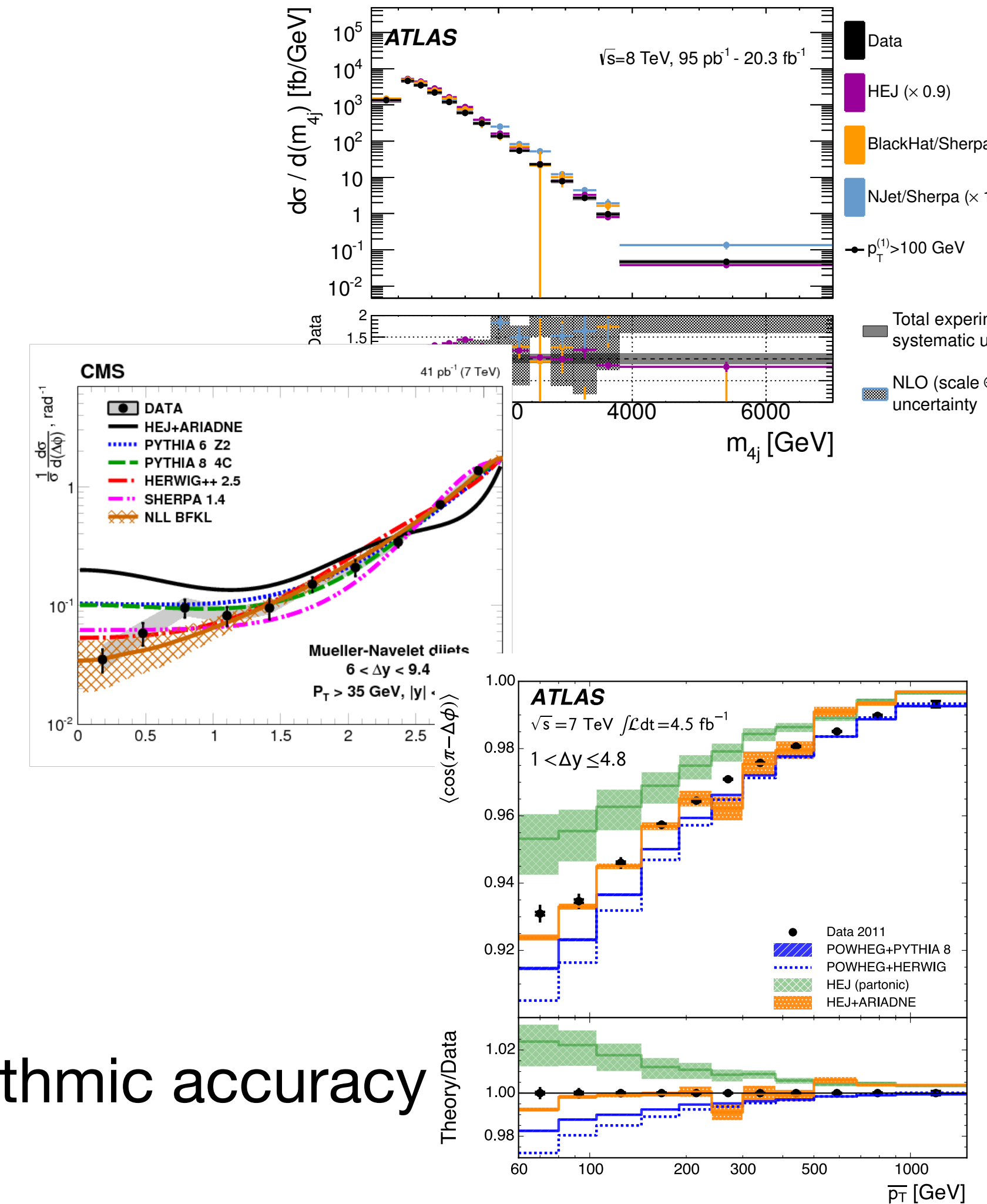
HEJ2 event generator: <https://hej.hepforge.org>

Andersen, Hapola, Heil, Maier & JMS [arXiv:1902.08430](https://arxiv.org/abs/1902.08430)

Extra colour-neutral bosons can be added without affecting the logarithmic accuracy

HEJ2.1 includes: $\geq 2j, H+ \geq 2j, W(\rightarrow \ell\nu)+ \geq 2j, Z/\gamma^*(\rightarrow \ell\bar{\ell})+ \geq 2j$

Andersen, Black, Brooks, Ducloué, Heil, Maier & JMS [arXiv:2110.15692](https://arxiv.org/abs/2110.15692)



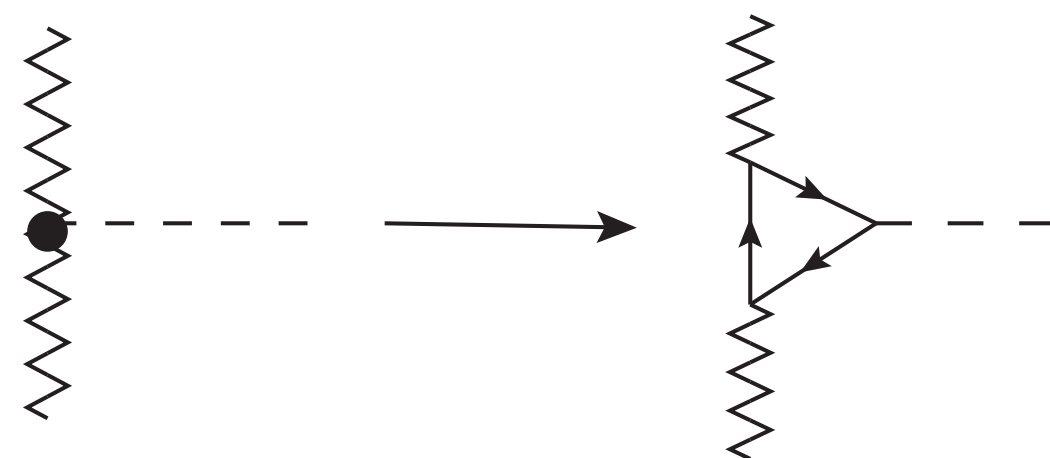
Finite Quark Masses in H+2j

Fixed-order stalled for full quark mass effects because LO = 1-loop.
LO results only for 2 and 3 jets (no NLO for 2j+)

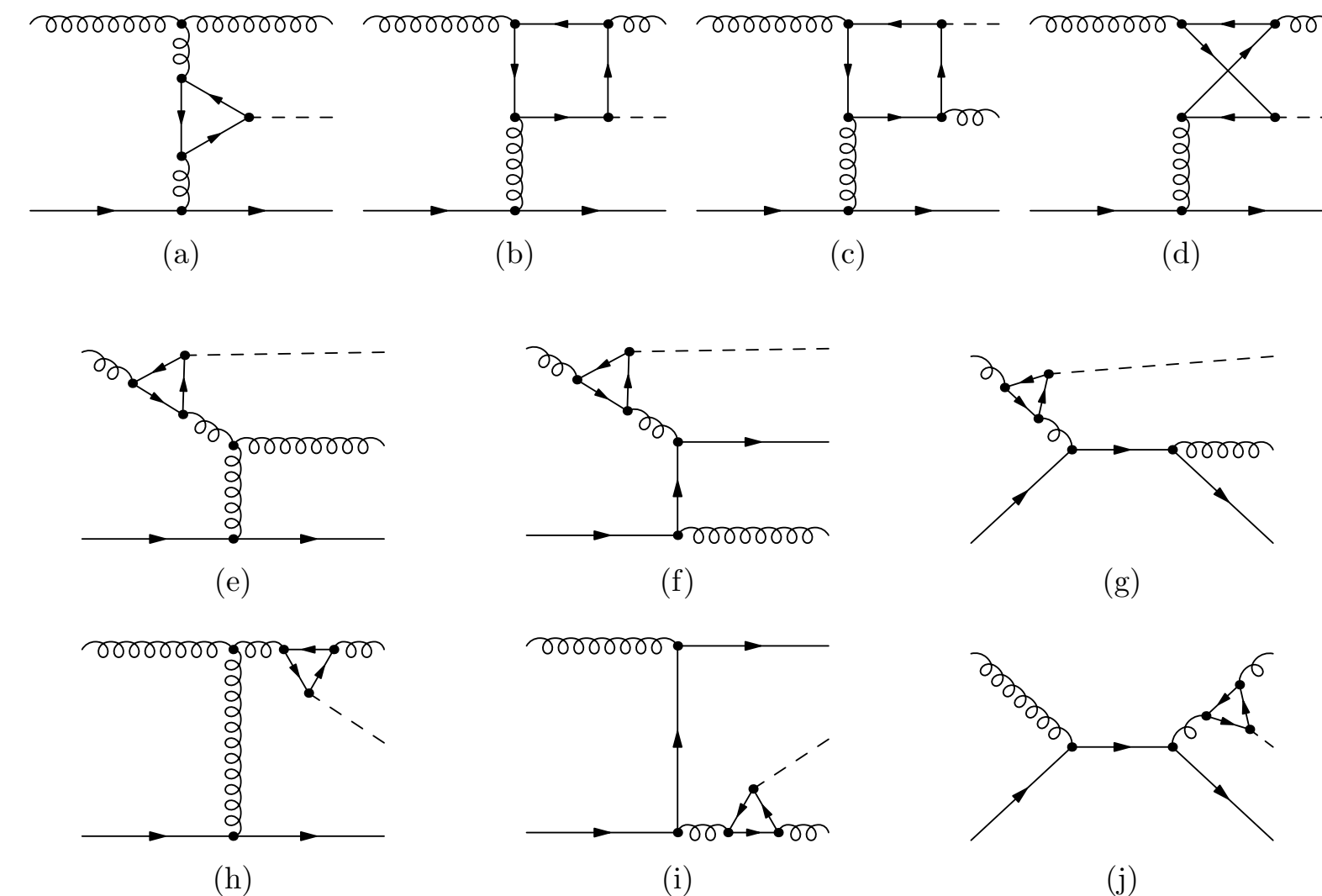
Del Duca et al [hep-ph/0105129](#), [hep-ph/0108030](#)
Greiner et al [arXiv:1608.01195](#)

In HEJ, factorised structure removes complexity from increasing number of jets

Del Duca, Kilgore, Oleari, Schmidt & Zeppenfeld [hep-ph/0301013](#)
Andersen, Cockburn, Heil, Maier & JMS [arXiv:1812.08072](#)



Straight-forward
e.g. $qQ \rightarrow qHQ$



Outer Higgs more involved but calculated

Finite Quark Masses in HEJ

HEJ can include finite quark mass and loop propagator effects for any number of jets
 Performed at amplitude level so we include mass effects from top quark, bottom quark and the interference between the two

Fixed-order matching performed to highest-available accuracy

Here use Sherpa and OpenLoops

Gleisberg et al arXiv:[0811.4622](#); Cascioli, Maierhöfer, Pozzorini arXiv:[1111.5206](#)



Highest available =

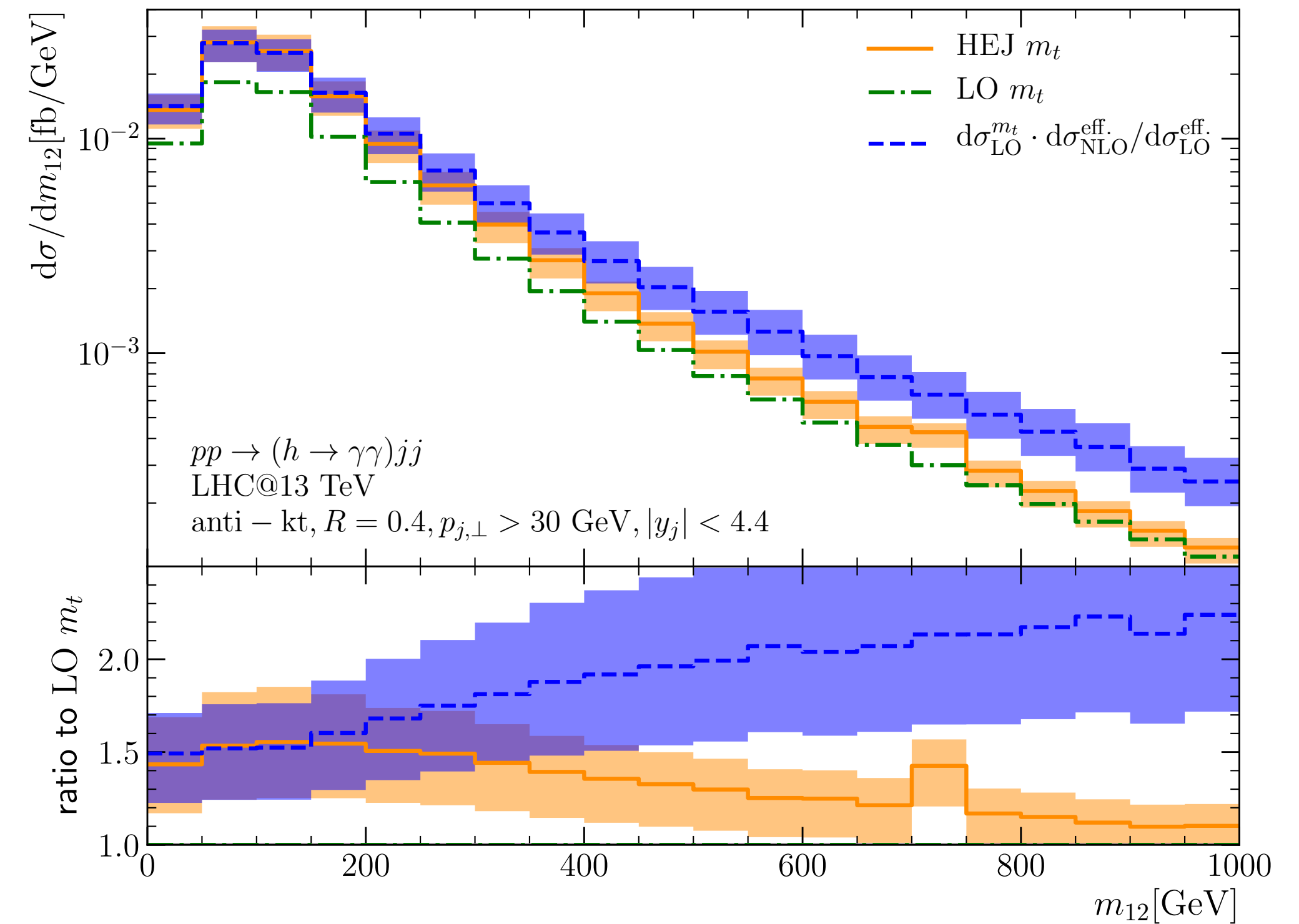
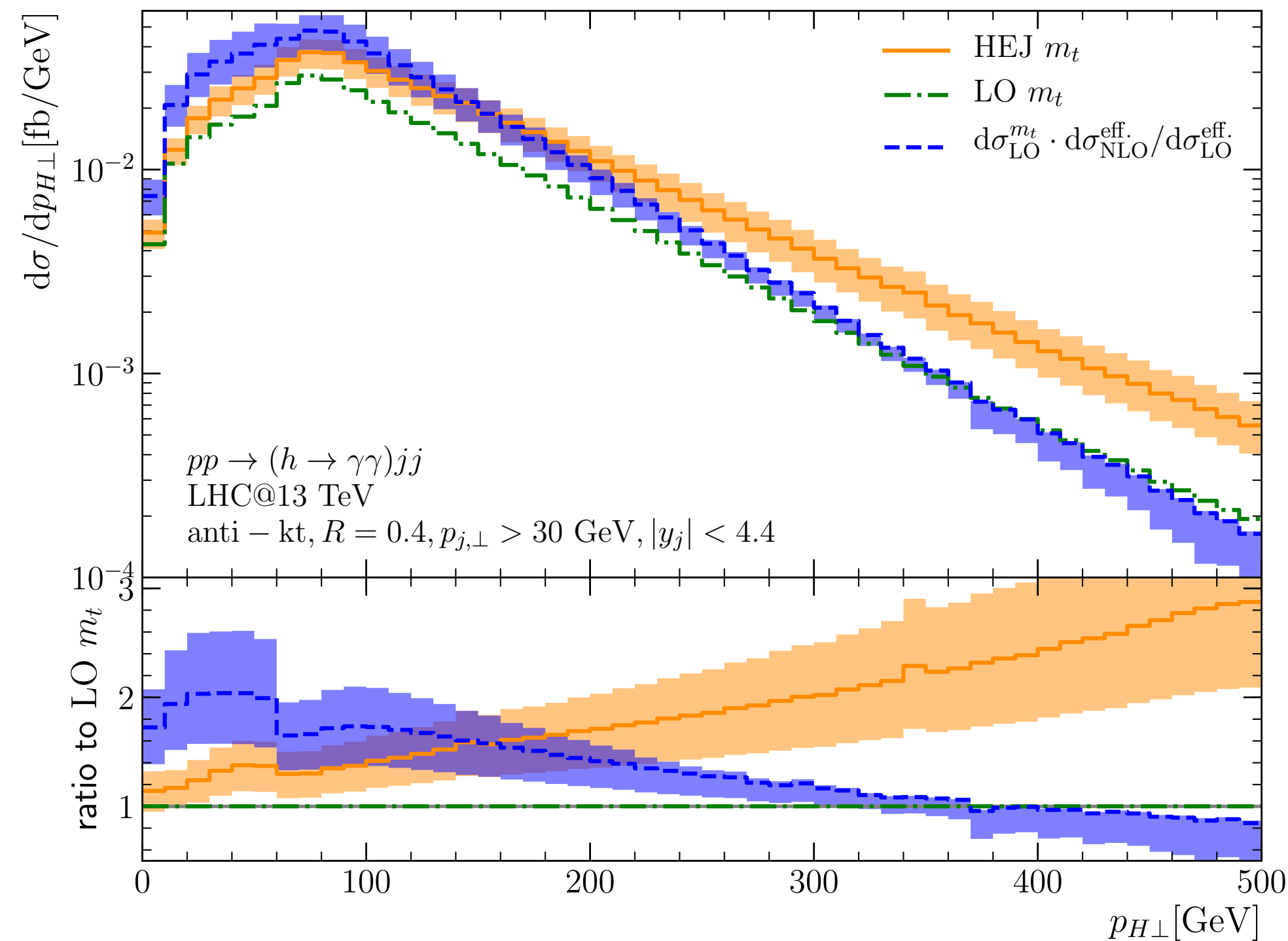
finite m_t	$H + 2j$ at LO	($3j$ results exist, but events not available)
infinite m_Q	$H + 2j$ at NLO	
	$H + 5j$ at LO	

All predictions shown with $\mu_F = \mu_R = \max(m_H, m_{12})$ with indt variations by 1/2,2

Finite Quark Mass Results

First probe the impact of higher orders in α_s

HEJ here temporarily without m_b



NLO K-factors clearly not flat, very scale-dependent, all choices have problems

HEJ harder $p_{H\perp}$ spectrum

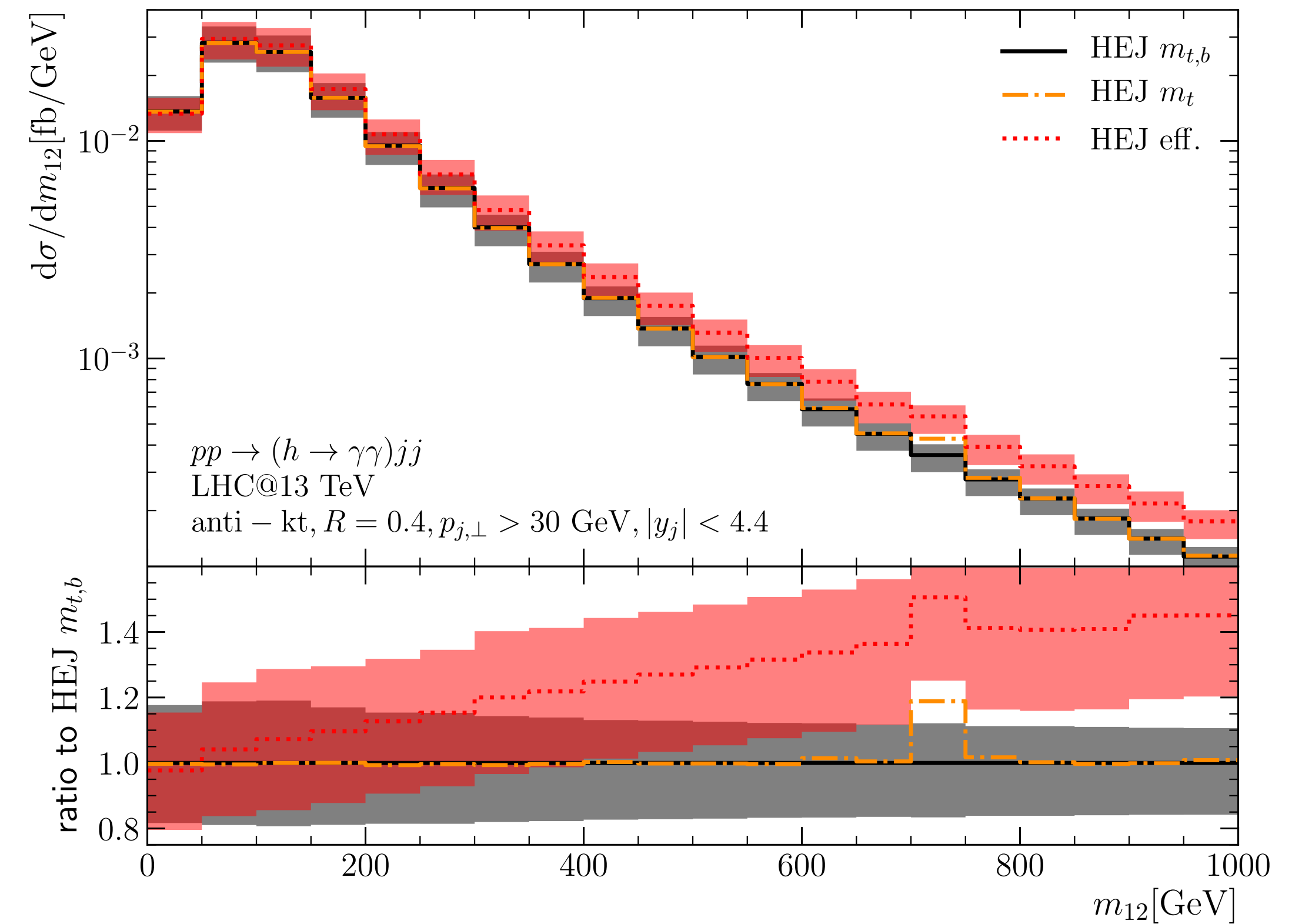
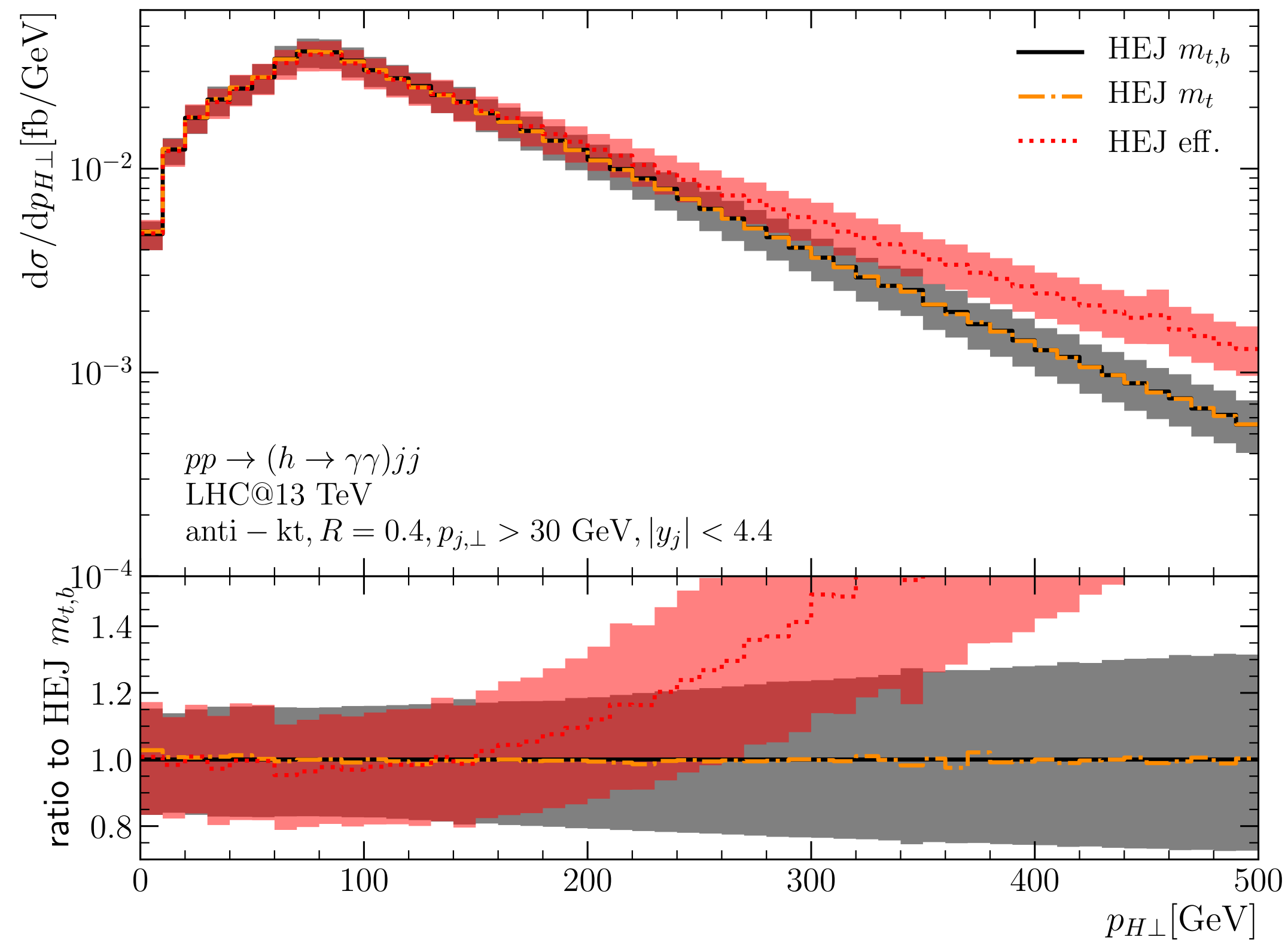
HEJ much steeper drop with m_{12}

Andersen, Cockburn, Heil, Maier & JMS arXiv:1812.08072

Finite Quark Mass Results

Now probe the impact of quark masses

Andersen, Cockburn, Heil, Maier & JMS arXiv:1812.08072

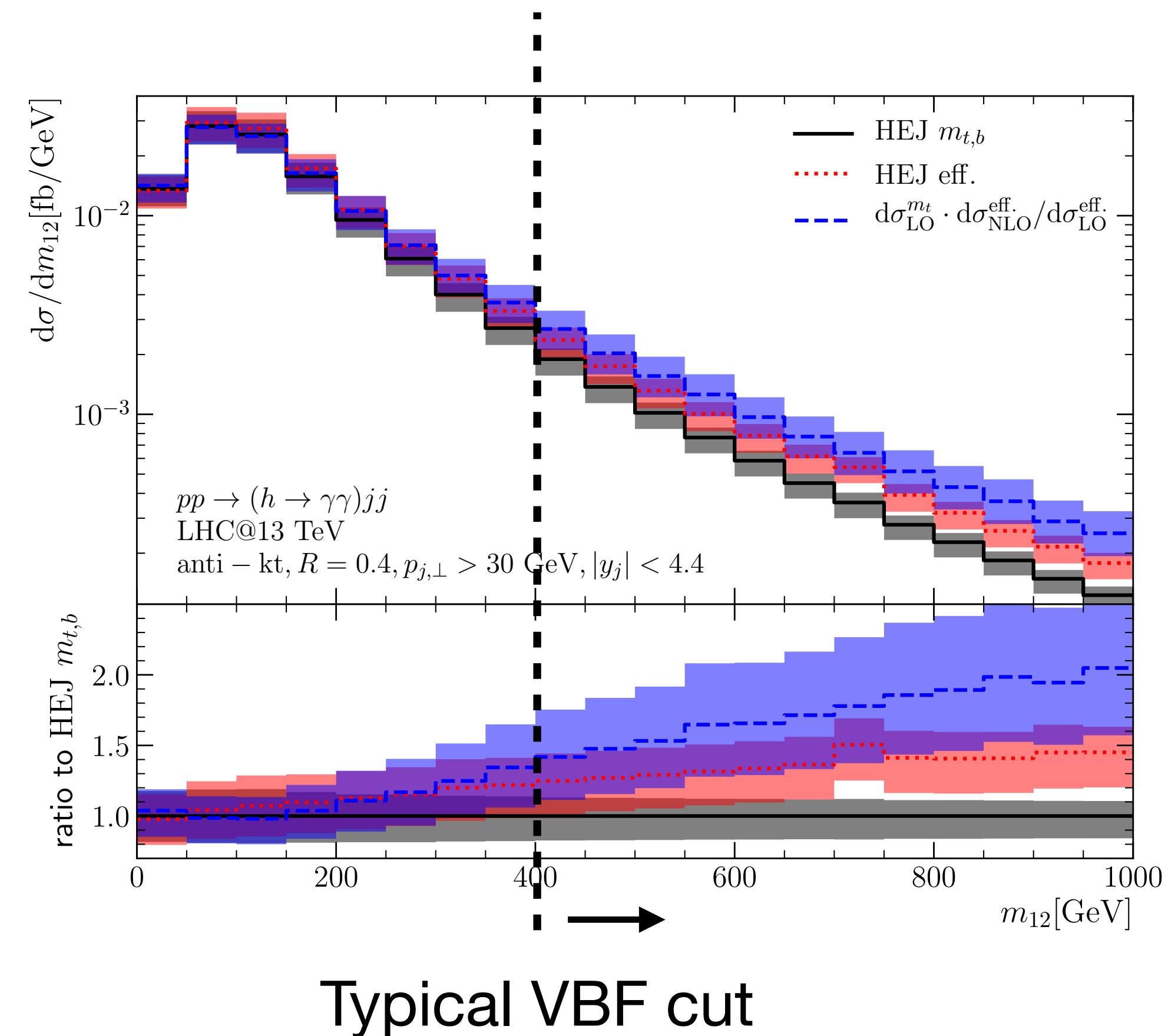


- Importance of finite quark mass increases with $p_{H\perp}$
- Relatively small impact of m_b , finite m_t lowers predictions at large m_{12}
- Therefore finite quark mass effects make VBF cuts more effective

Full HEJ Prediction vs “best” fixed-order

- Resummation alone reduces cross section at large values of m_{12}
- Finite quark mass/loop effects reduce x-section in VBF cuts by *further* 11%

Prediction	xs after VBF cuts
Fixed order	9%
HEJ	4%

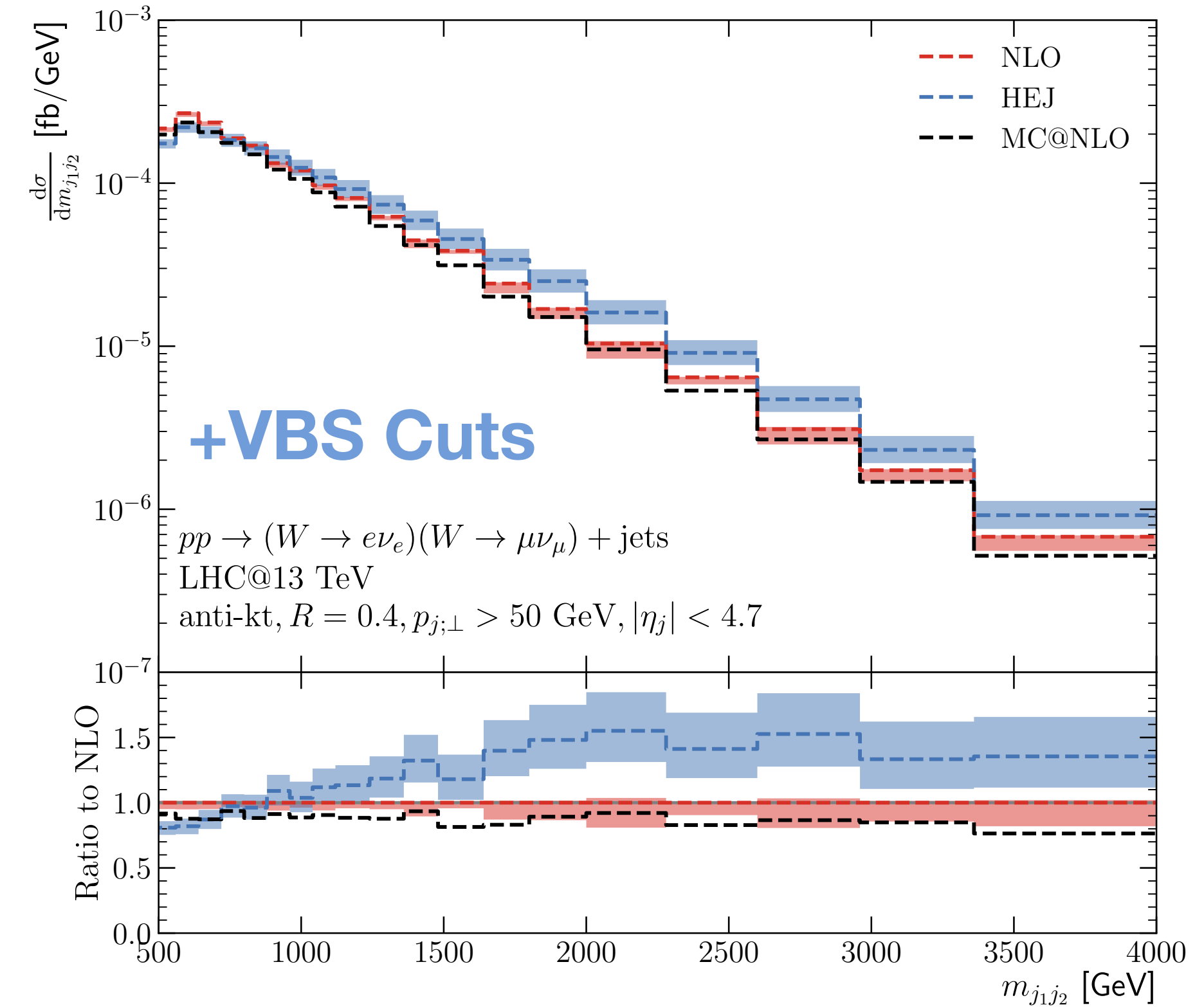
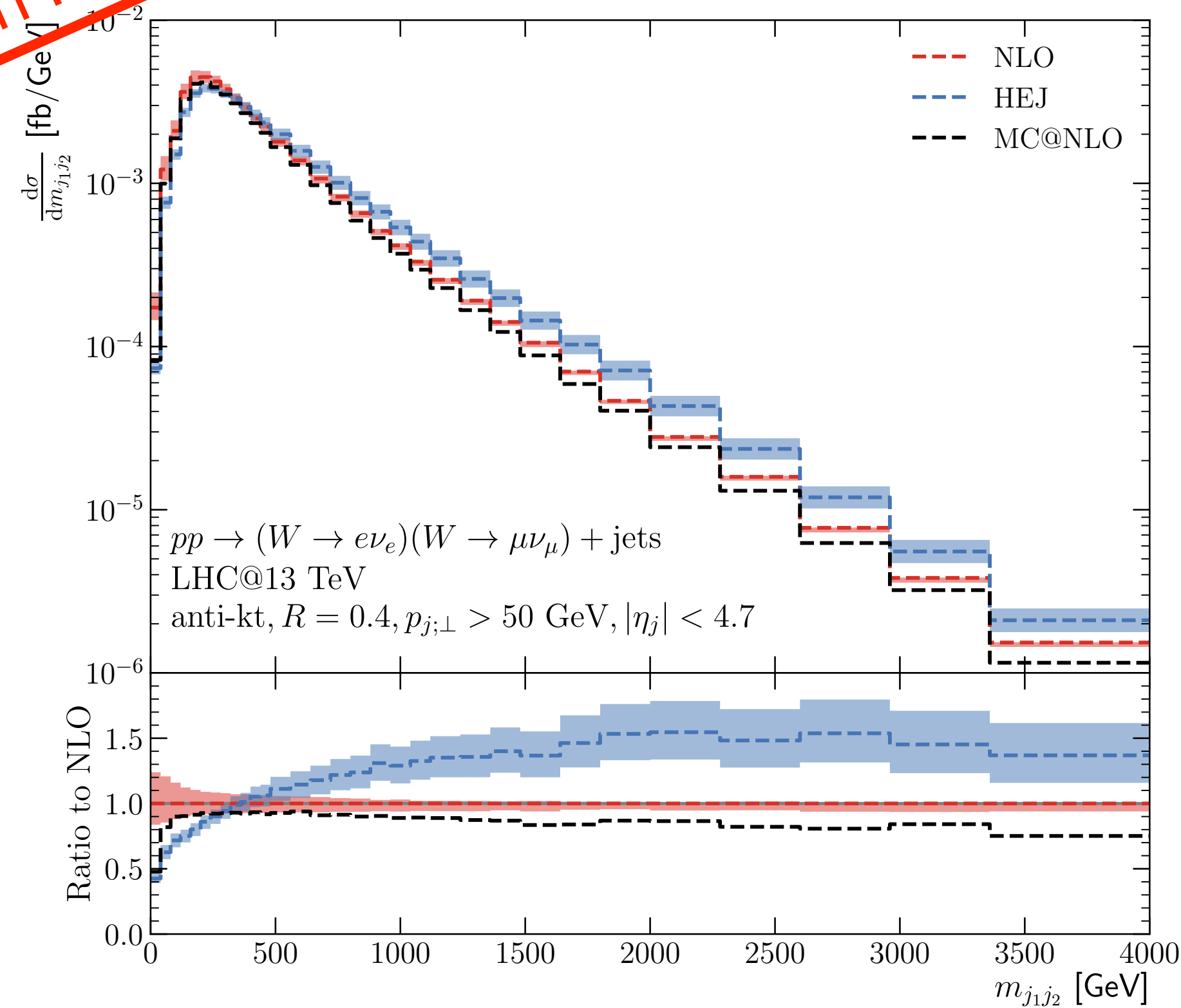


Vector Boson Scattering — Distributions

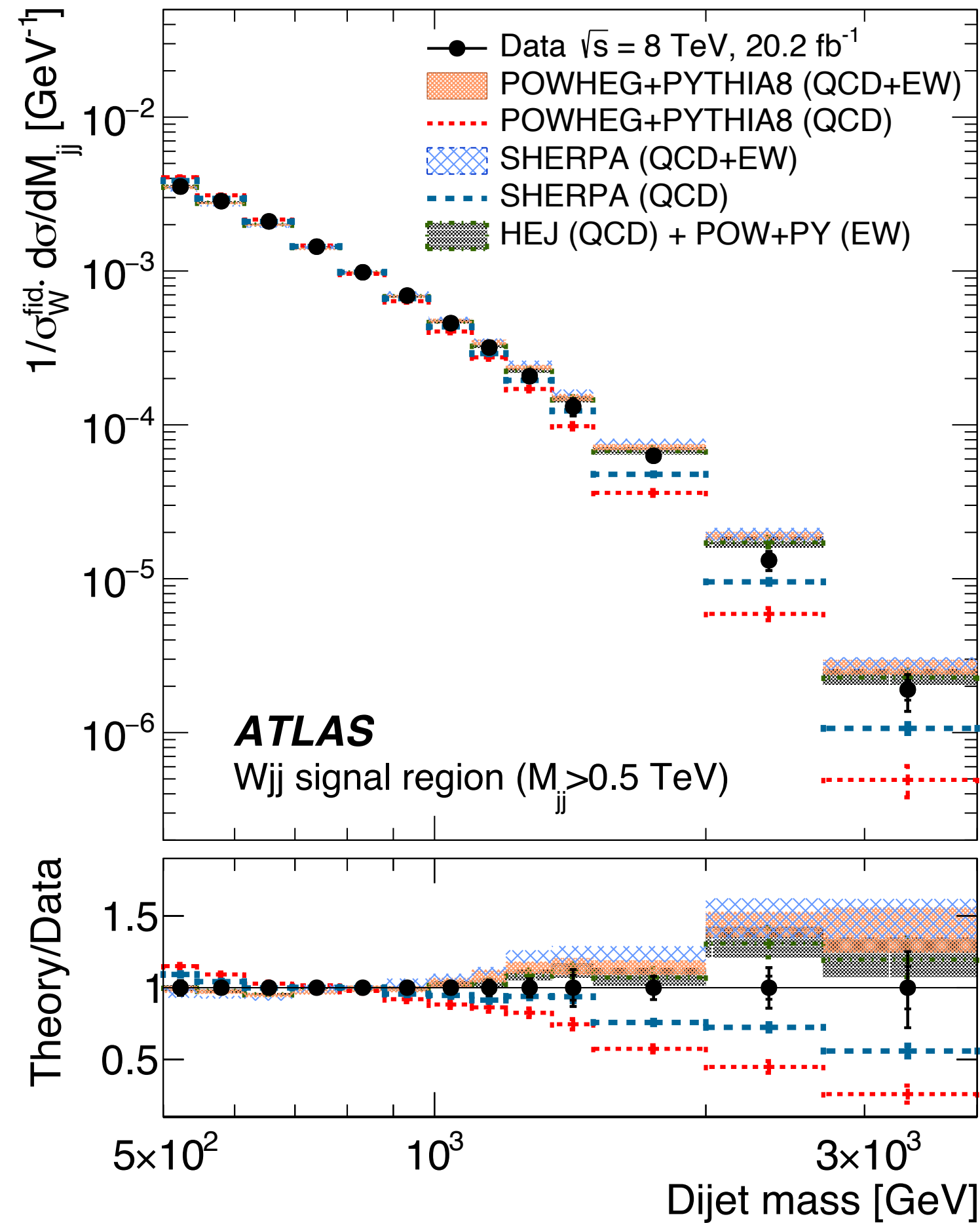
Impact on cross sections much reduced here (central scale choice) due to cancellation across phase space, not agreement throughout

Andersen, Ducloué, Elrick, Nail, Maier, JMS [arXiv:2107.06818](https://arxiv.org/abs/2107.06818)

New in HEJ 2.2!



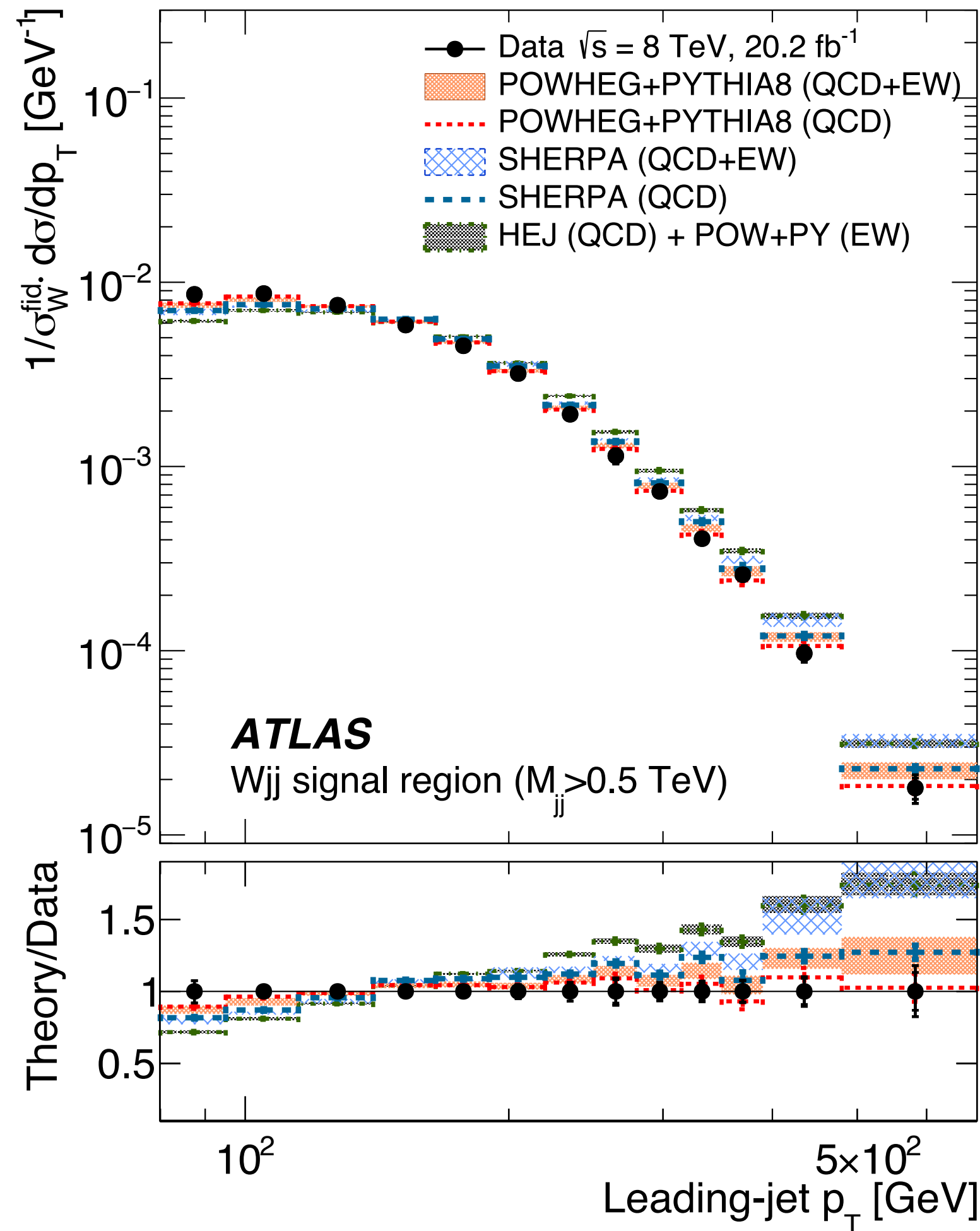
Shape of distributions significantly changed by the all-order resummation



W+2j study to investigate separation of QCD/EW contributions compared to NLO+PS (Powheg/Sherpa) and HEJ+EW from Powheg

- 8 TeV data probing out to 3 TeV already
- QCD contribution decreases at large dijet mass, but remains significant
- NLO+PS slightly overshoot, and increasing

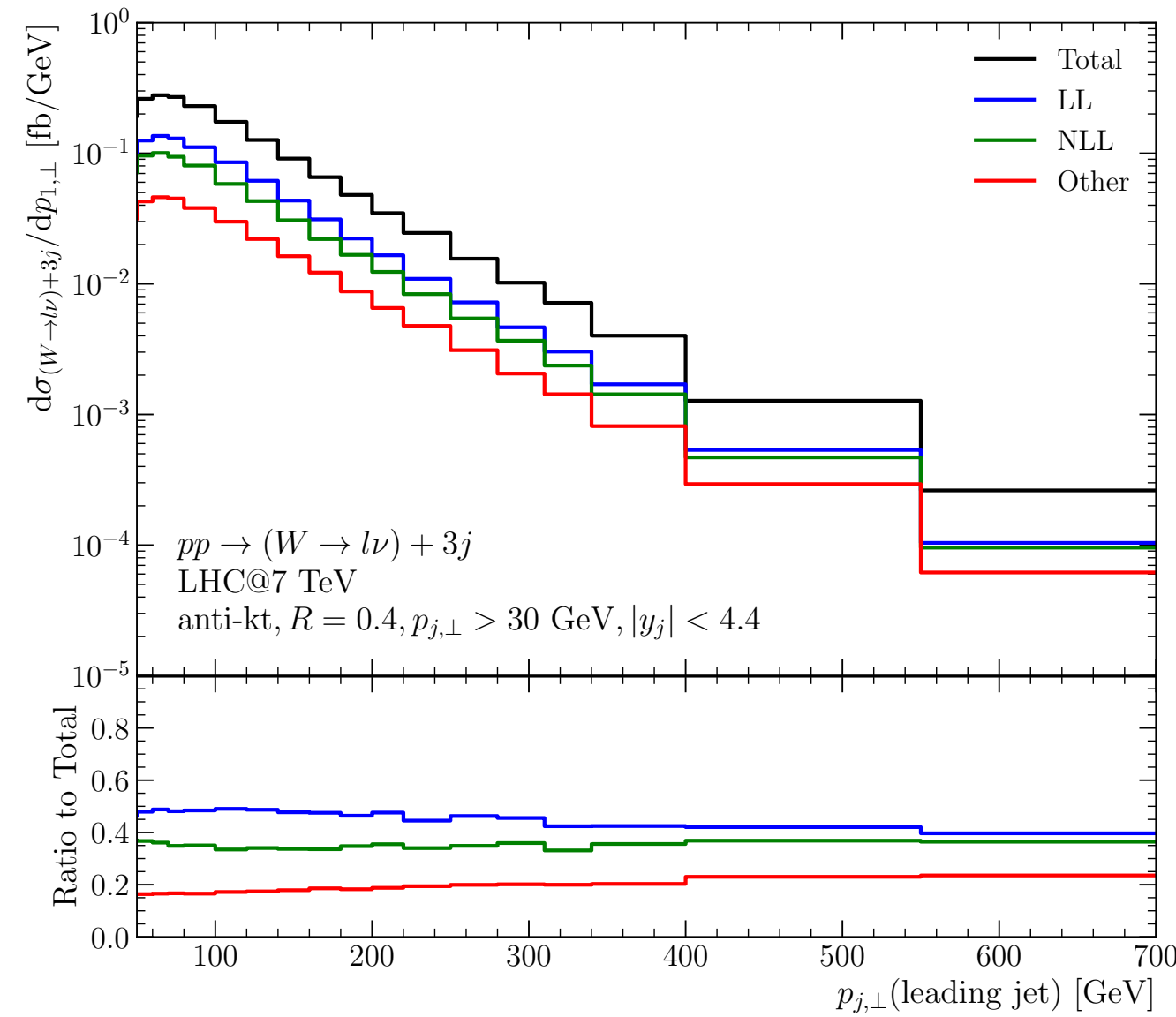
Similar for e.g. delta-y



- Different picture when plotted versus p_T as no systematic evolution in p_T in HEJ.
- QCD contribution no longer suppressed compared to EW
- Subleading corrections and NLO matching improve this (see later)
- Can also combine with a parton shower

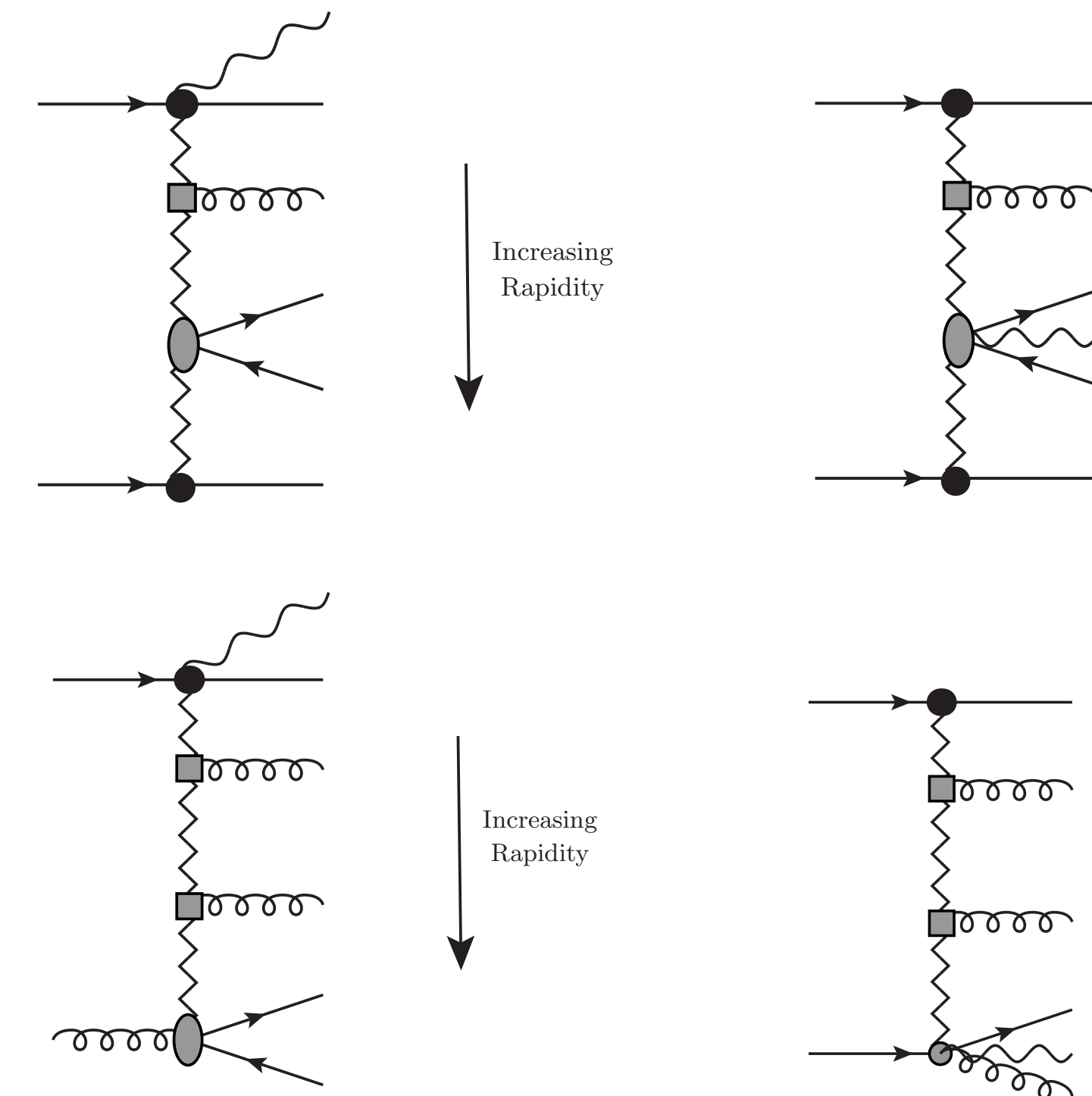
Andersen, Brooks & Lönnblad [arXiv:1712.00178](https://arxiv.org/abs/1712.00178)
Andersen, Hassan, Jaskiewicz [arXiv:2210.06898](https://arxiv.org/abs/2210.06898)

Improvements at Large p_T : NLL



Observed that particle channels which are formally next-to-leading log, contribute significantly at large p_T

Can consistently apply resummation to all such channels (part of full NLL, and step towards it)



Improvements at Large p_T : NLO Matching

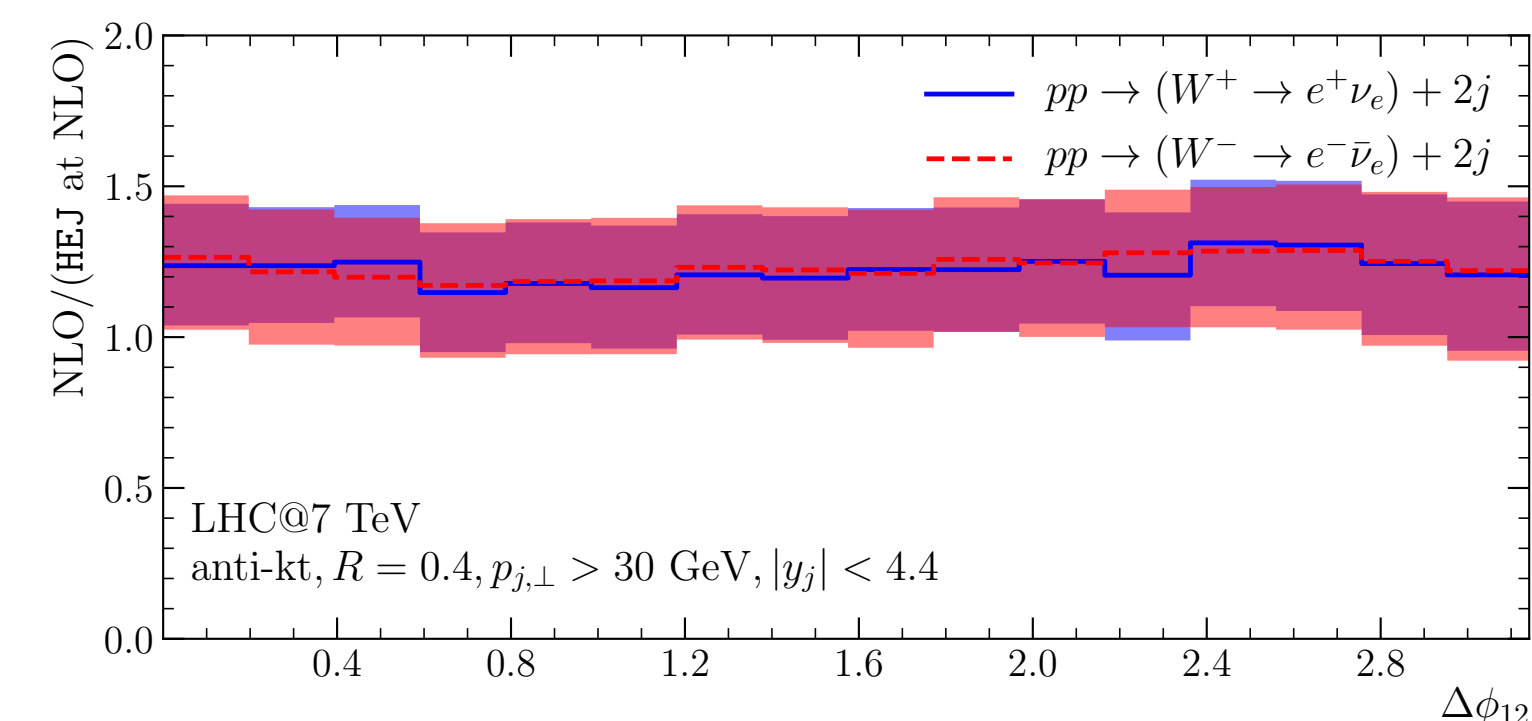
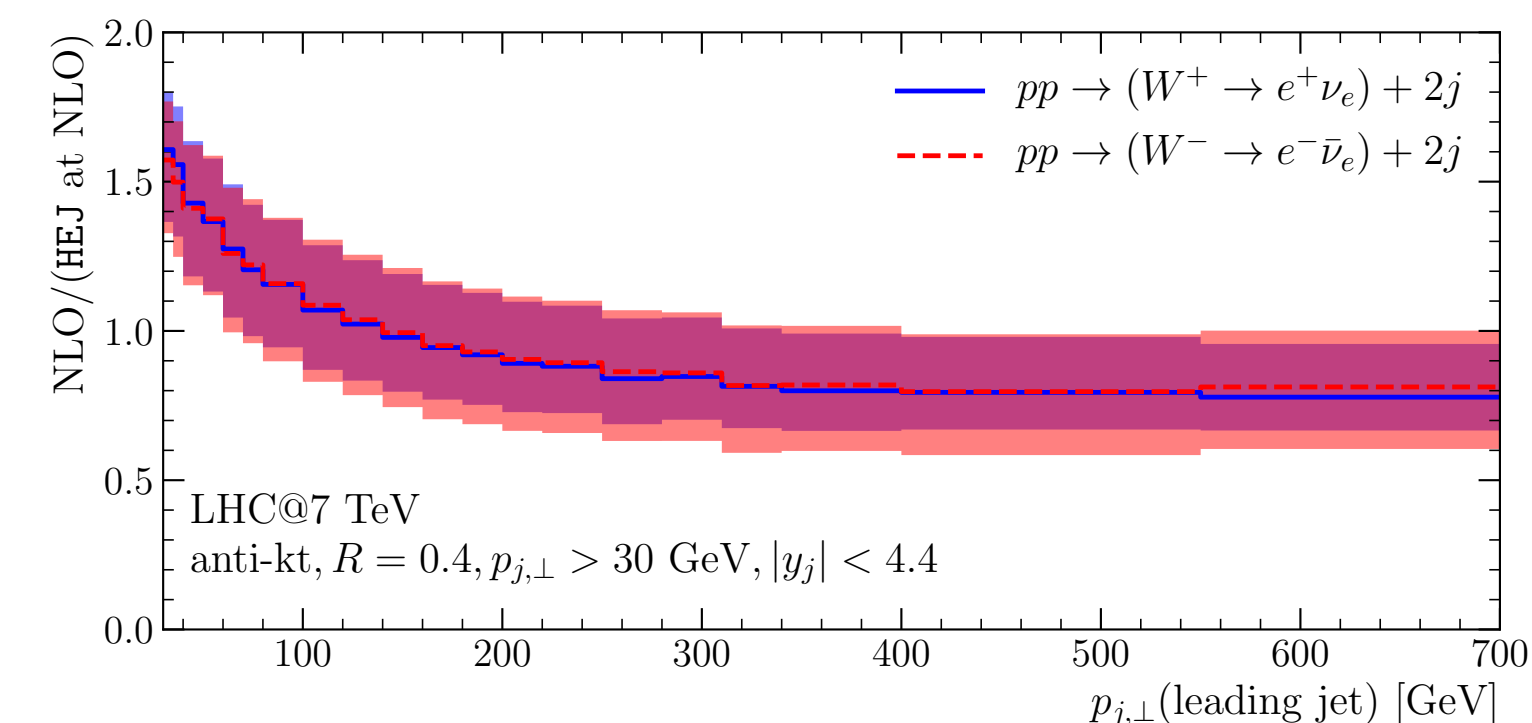
Not able yet to match to NLO event-by-event, but can do better than a k-factor by matching bin-by-bin

We derive predictions from HEJ, truncated to NLO and take the ratio to full NLO for each distribution.

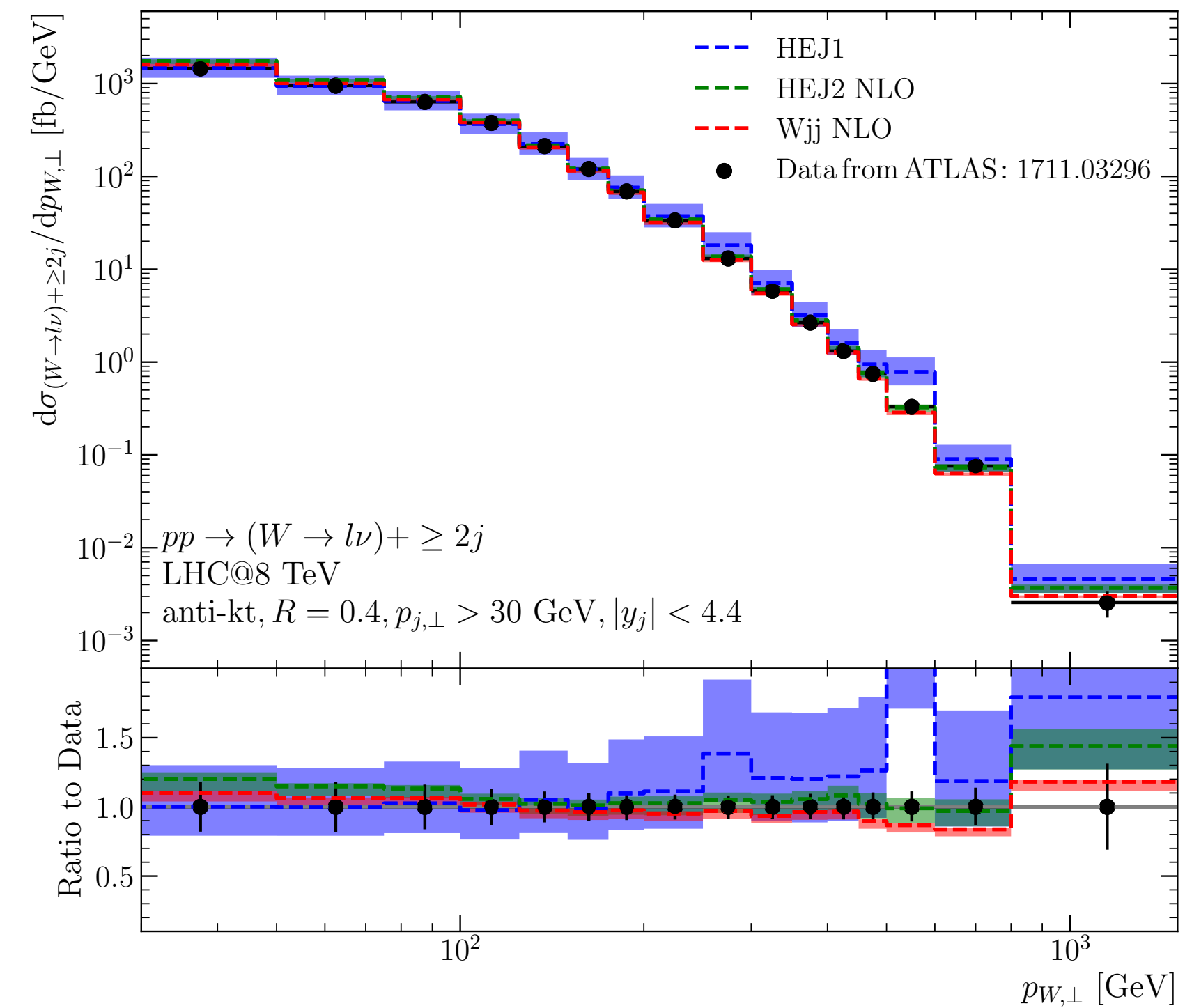
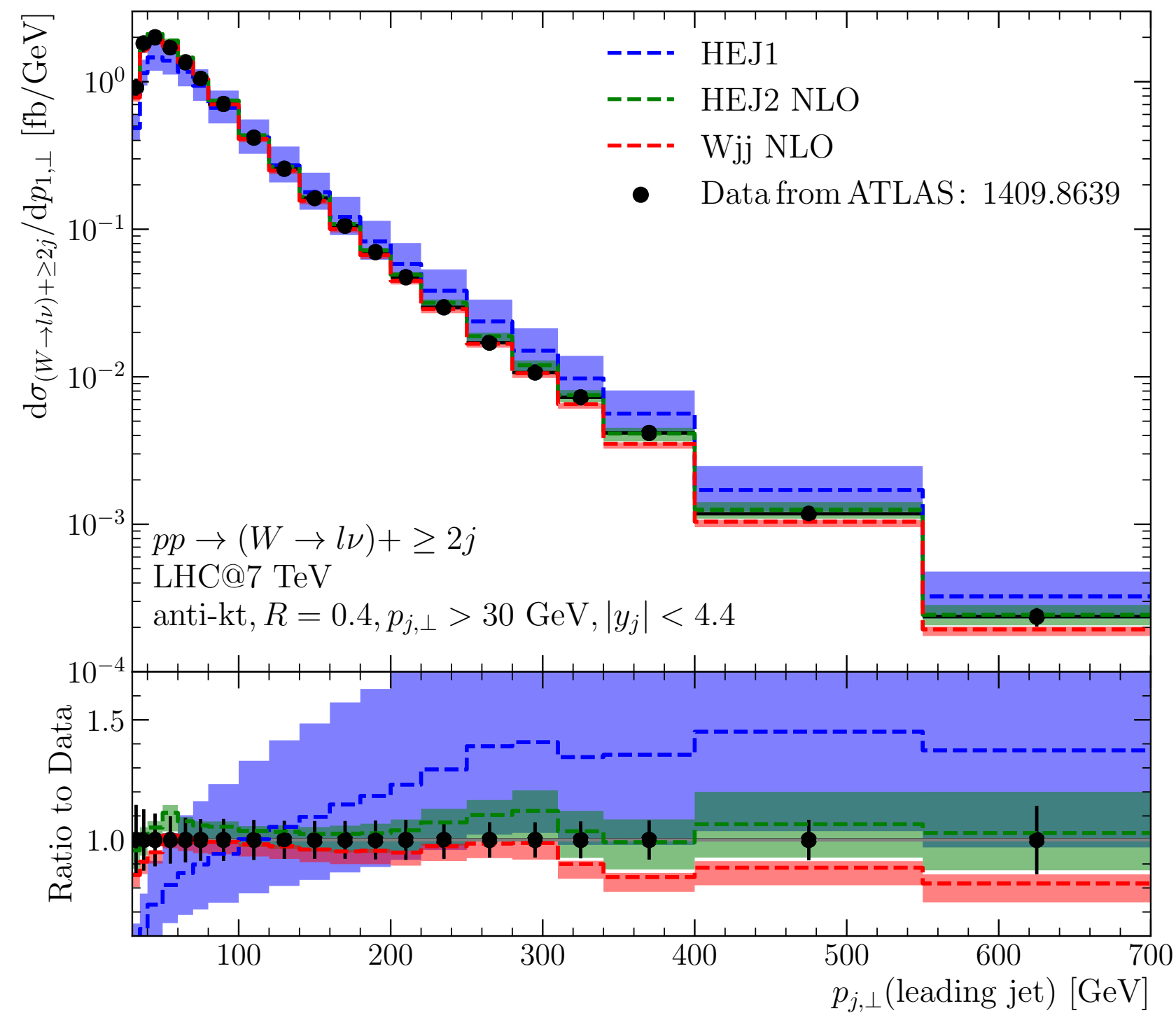
Final predictions are then given by

$$w_{\text{HEJ2 NLO}} = w_{\text{HEJ2}} \frac{w_{\text{NLO}}}{w_{\text{HEJ at NLO}}} + w_{\text{FO } W+\geq 4j}$$

Can check by expansion that each bin is accurate to NLO+LL



Improved W-Plus-Dijets



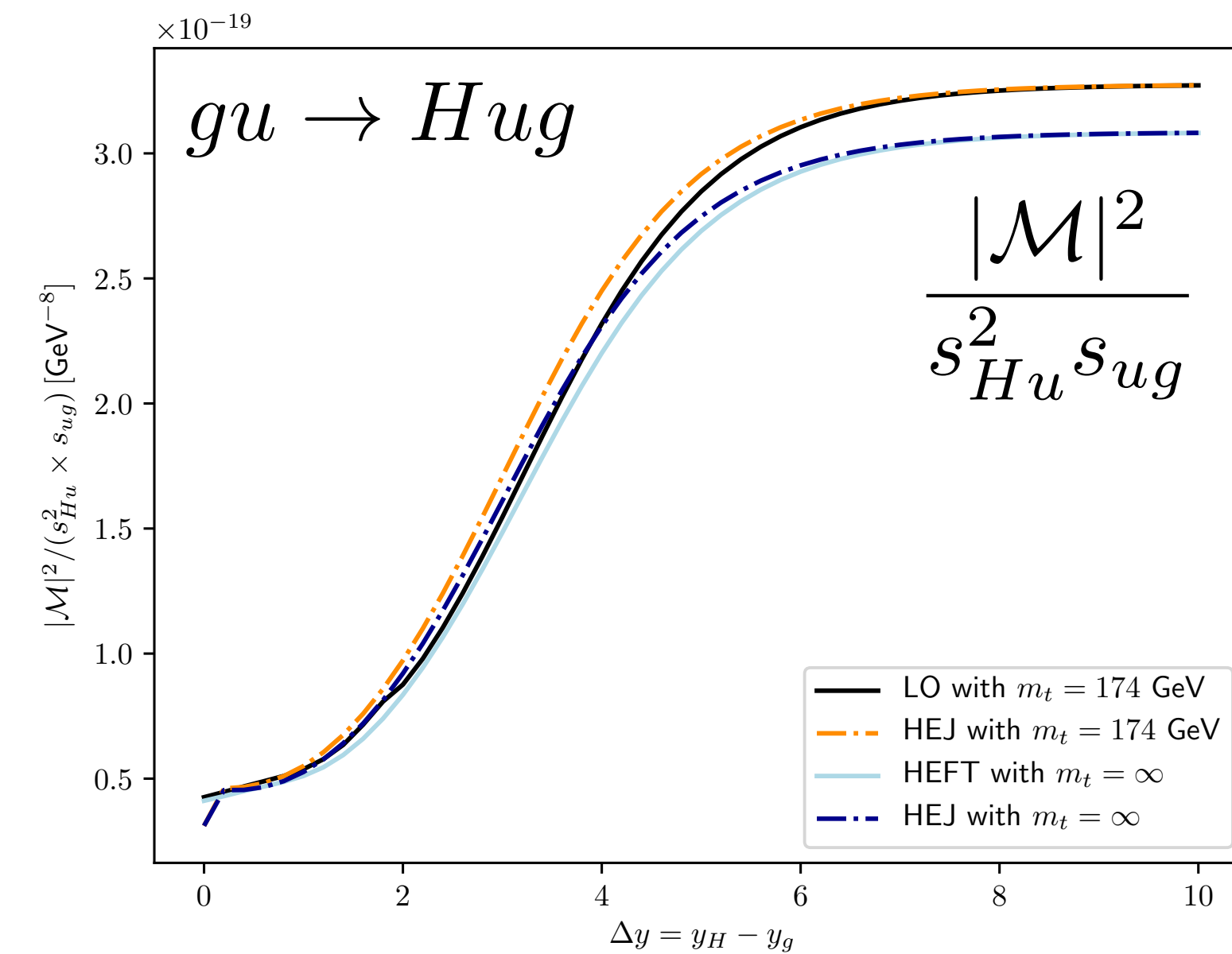
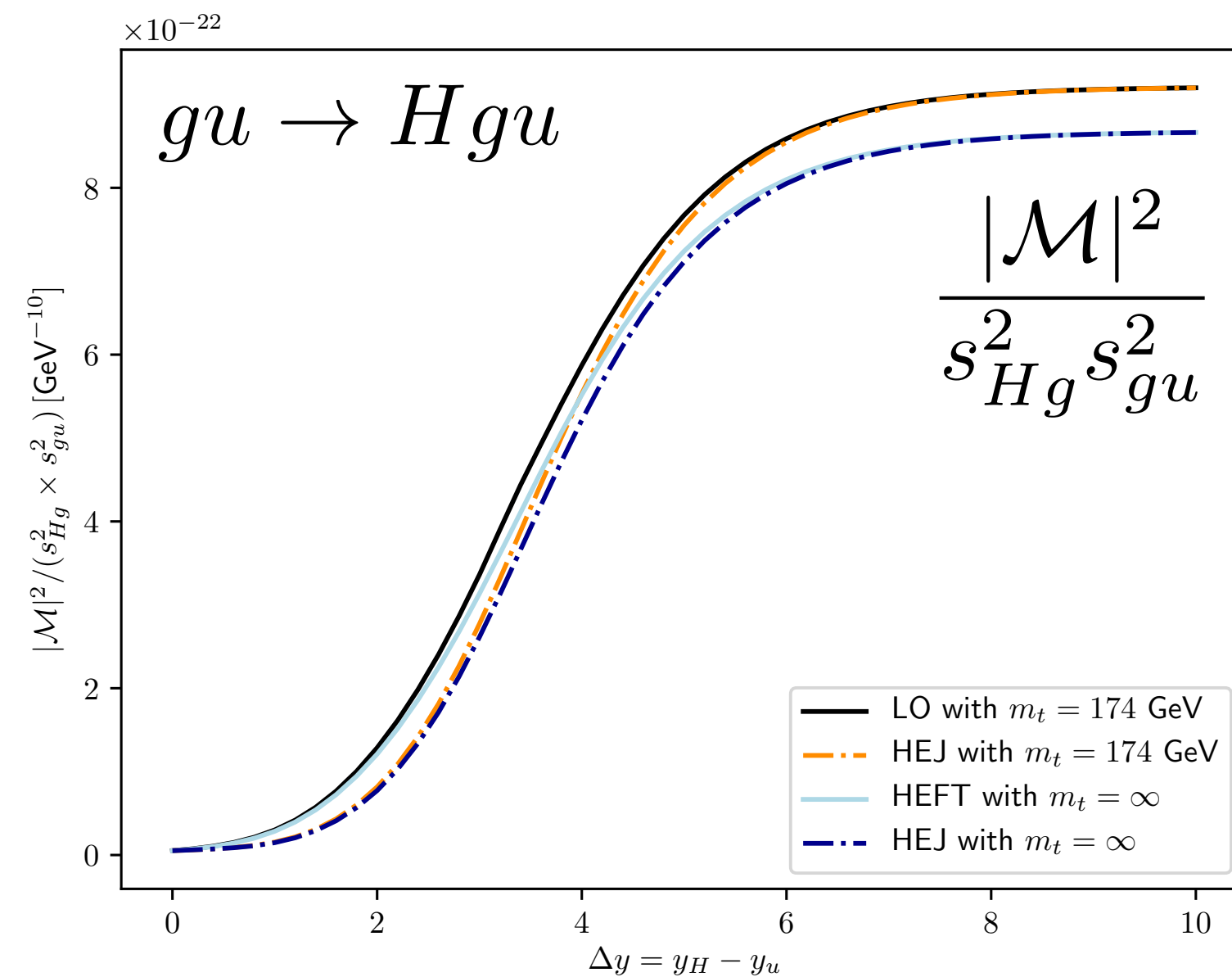
- HEJ2 NLO prediction lies between the previous two
- Scale variation reduced — larger than NLO due to higher multiplicities

- At large p_T values, require $\geq 4j$ events to obtain good agreement

Higgs + 1j in HEJ

- HEJ has always resummed logarithms in the region between the outer jets in rapidity, hence always for processes with at least two jets
- Observed in H+2j studies, that scaling with an intermediate Higgs boson was as in QCD

Andersen, Hapola, Maier, JMS [arXiv:1706.01002](#)



- The same (Regge) scaling applies in the amplitude if the Higgs boson is external in rapidity
- Hence the same framework can be applied to H+1j

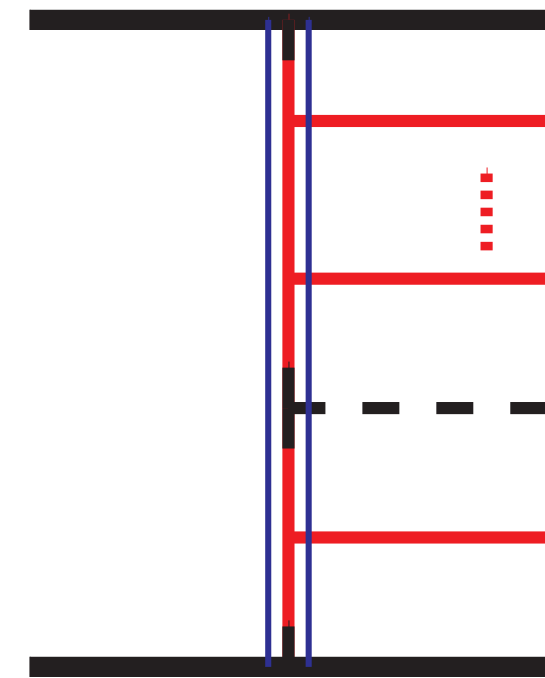
Andersen, Hassan, Maier, Paltrinieri, Papaefstathiou, JMS [arXiv:2210.10671](#)

Higgs + 1j in HEJ

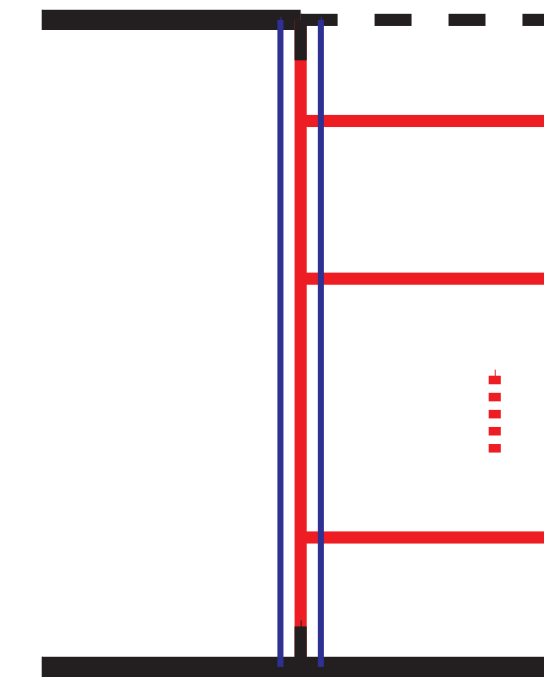
Black = Born/skeleton function

Red = Range of resummation

Previous 2jet+



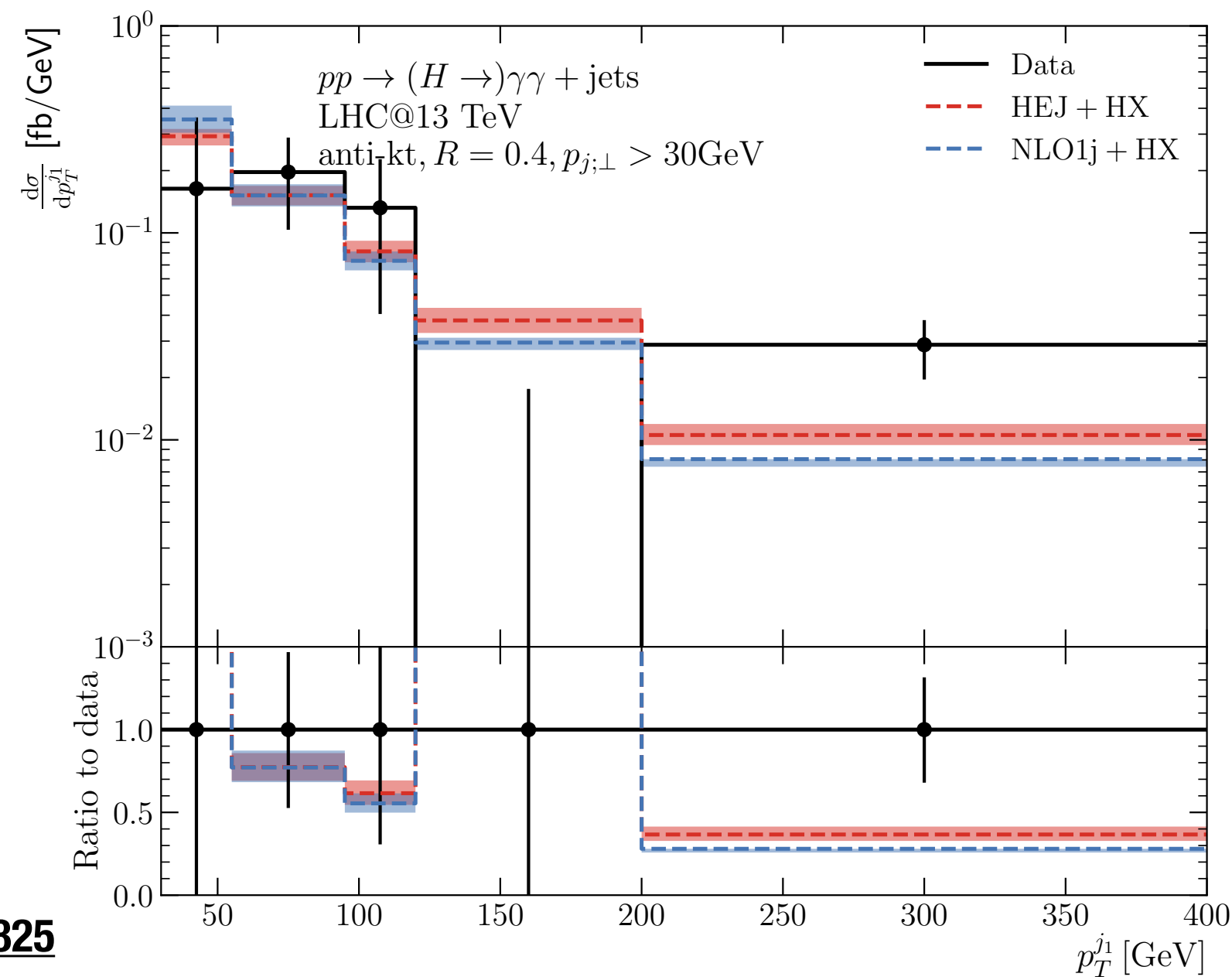
Increasing rapidity



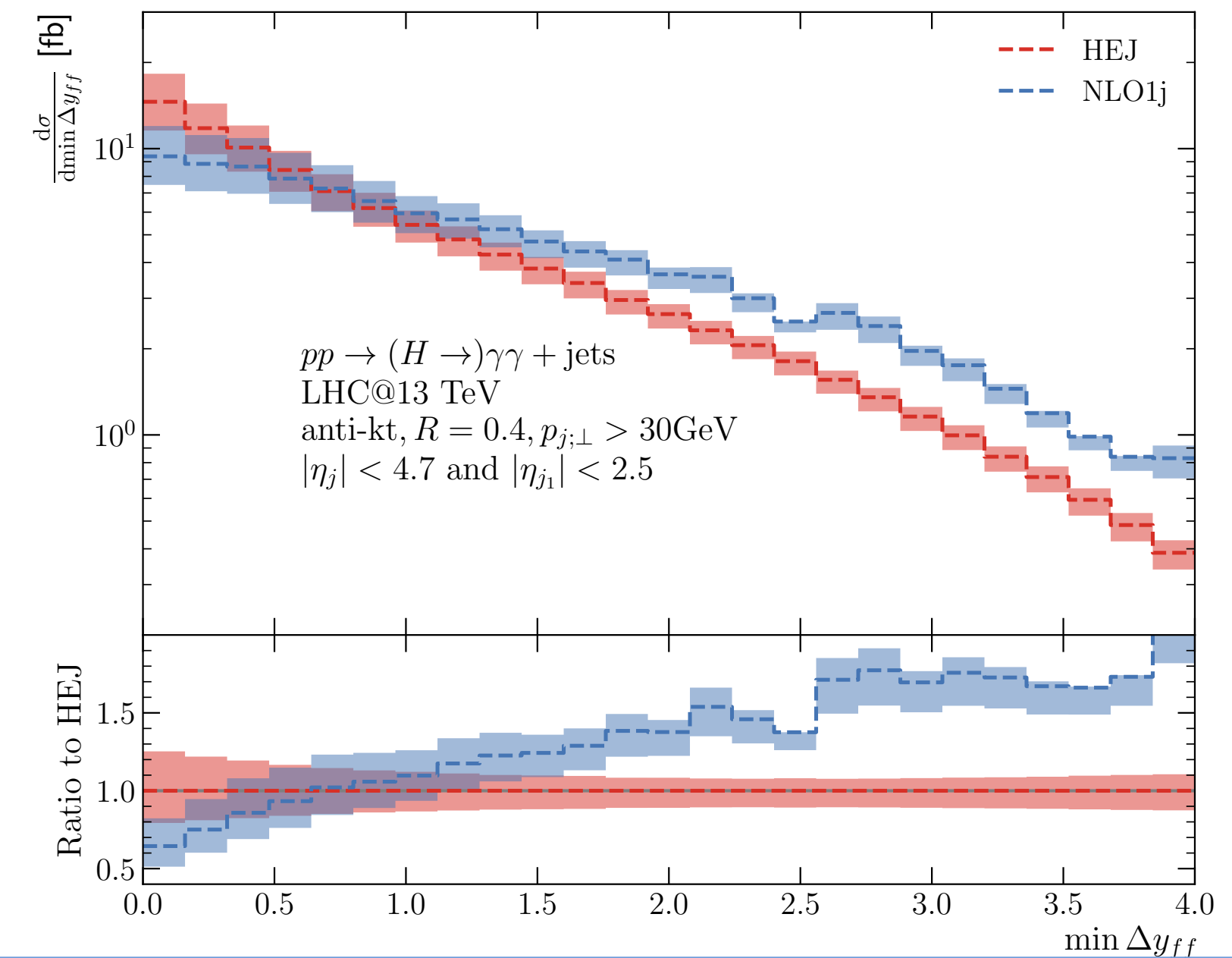
New 1jet+

Similar effects on distributions

Andersen, Hassan, Maier, Paltrinieri, Papaefstathiou, JMS [arXiv:2210.10671](https://arxiv.org/abs/2210.10671)

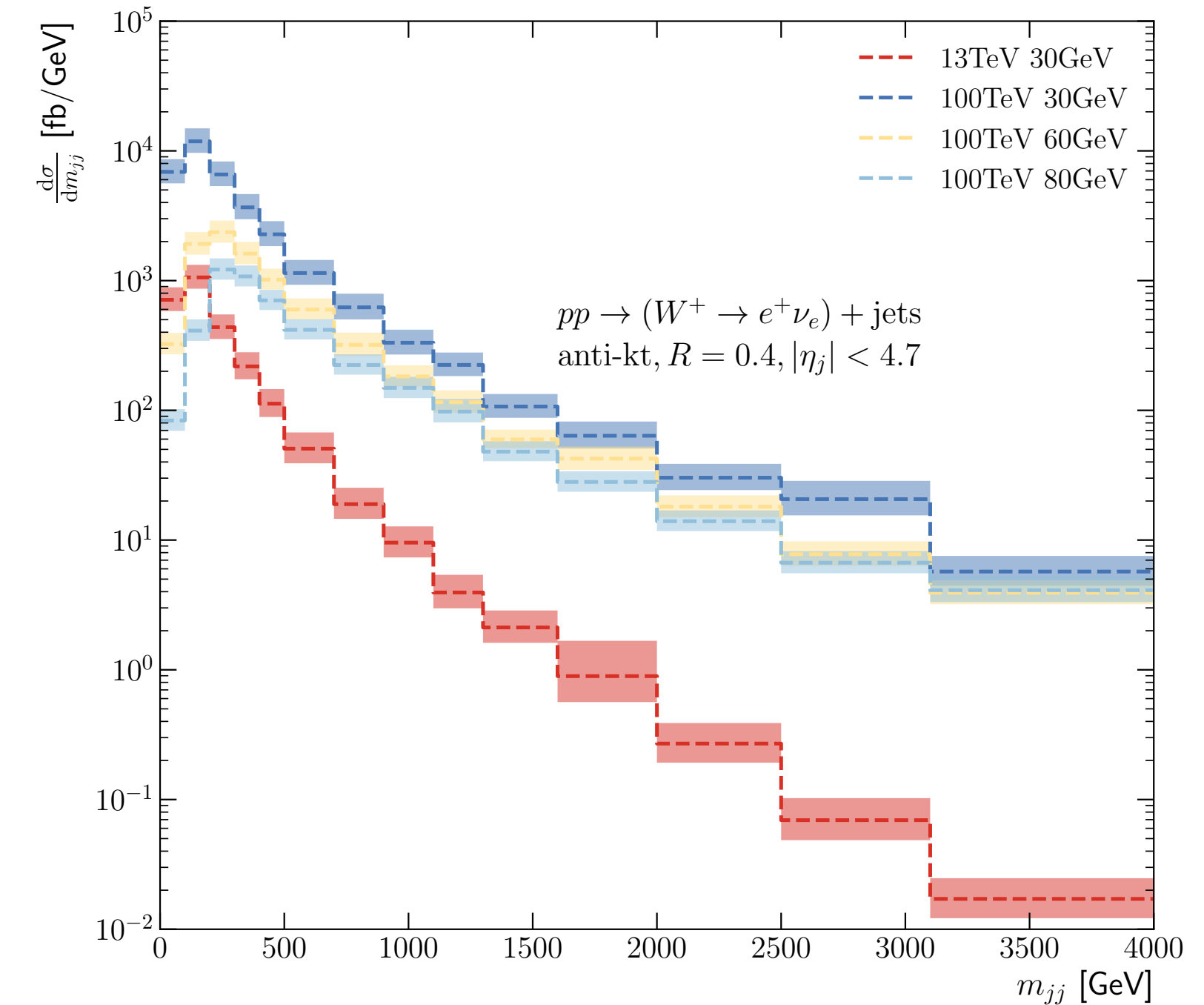
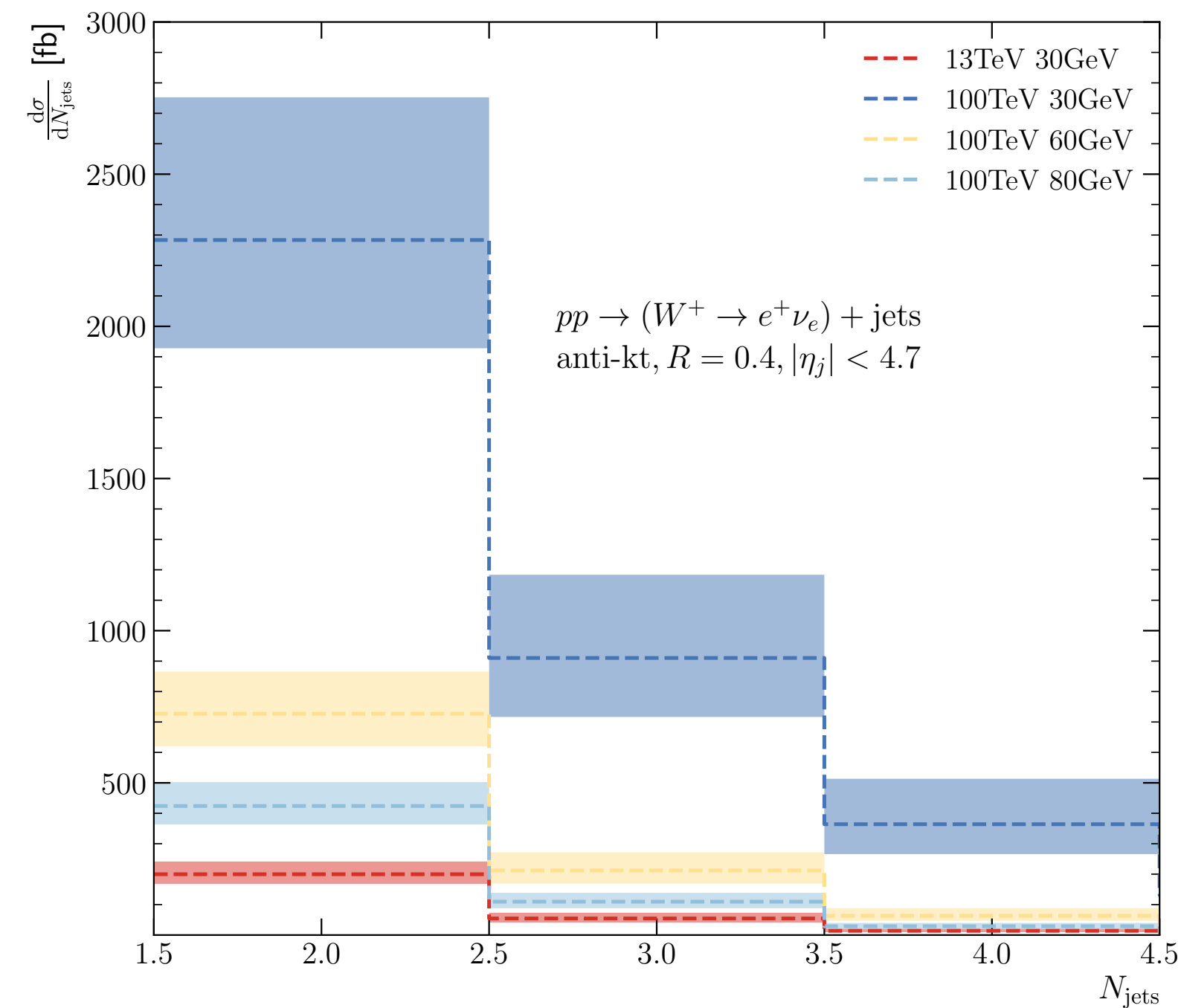


CMS data [arXiv:1807.03825](https://arxiv.org/abs/1807.03825)



Looking Forward

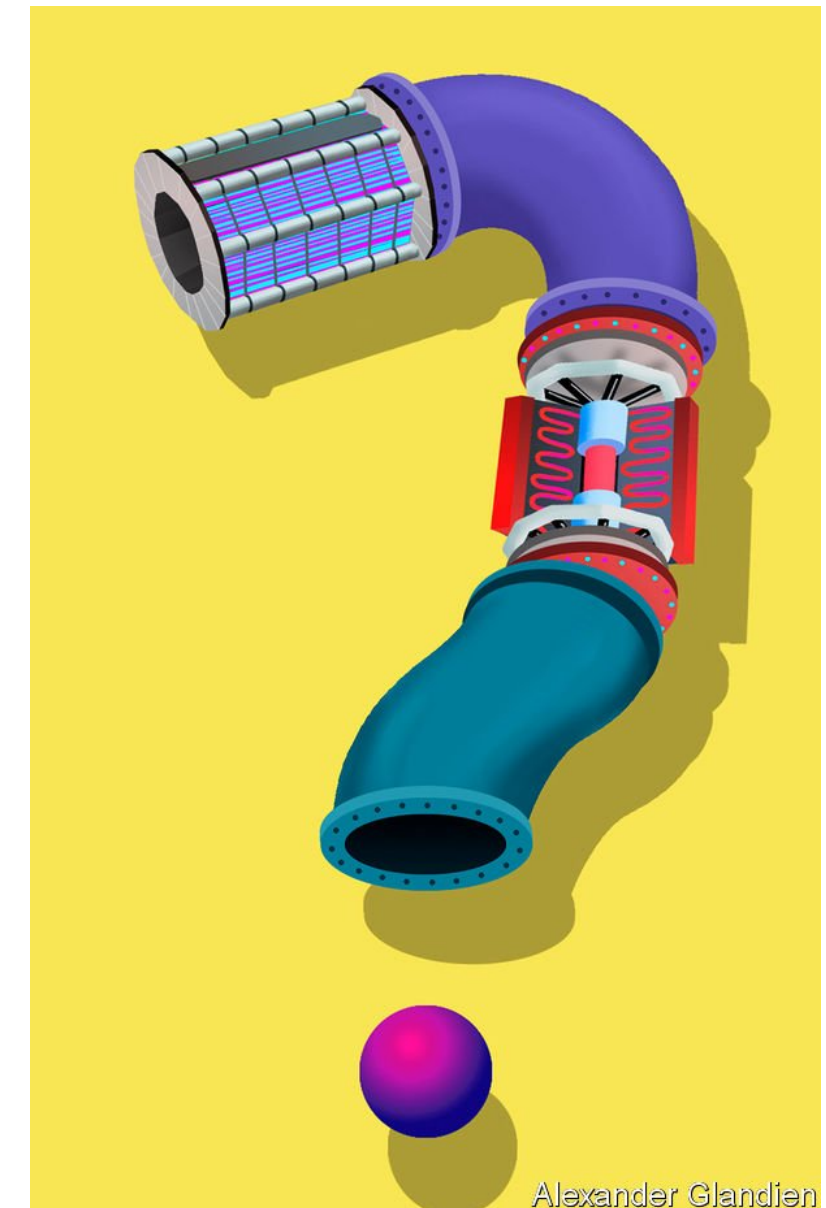
What about a 100 TeV collider? Even larger centre-of-mass energy will give even larger logs!



Higher pT cuts can control the jet rates, but impact of logs on shapes of distributions will be large

Summary & Outlook

- Current and future data demand higher precision predictions...
- ... and demand calculation of new effects
- High Energy Jets allows the description of high energy logs in a fully flexible framework
- High Energy Jets provides alternative way to include finite quark mass effects



HEJ2 event generator: <https://hej.hepforge.org>