

# Precision Physics for Single and Multi-Higgs Boson Production

Stephen Jones IPPP Durham / Royal Society URF



THE ROYAL SOCIETY

### The Standard Model



### The Standard Model and Beyond



### Higgs Couplings

The Higgs sector continues to yield impressive fundamental discoveries



**2018** ( $t\bar{t}H$ ): First direct observation of top-quark Yukawa coupling

CMS 1804.02610/ ATLAS 1806.00425

**2020** ( $H \rightarrow \mu\mu$ ): First direct evidence that Higgs field is responsible for mass of 2nd gen. leptons

CMS 2009.04363 / ATLAS 2007.07830

**2022** ( $H \rightarrow c\overline{c}$ ): First hints that Higgs field is responsible for mass of 2nd gen. quarks

CMS 2205.05550 / ATLAS 2201.11428

Imagine we had current experimental results for  $gg \rightarrow H$ , but only LO theory...



Imagine we had current experimental results for  $gg \rightarrow H$ , but only LO theory...



Imagine we had current experimental results for  $gg \rightarrow H$ , but only NLO theory...

![](_page_6_Figure_2.jpeg)

Much better with NNLO theory, but theory uncertainty is still quite large...

![](_page_7_Figure_2.jpeg)

Anastasiou, Melnikov 02; Harlander, Kilgore 02; Ravindran, Smith, van Neerven 03;

\*Warning: just a cartoon, don't trust data/theory from this plot!

**Reality:** we actually have N<sup>3</sup>LO theory, beautiful example of precision @ LHC

![](_page_8_Figure_2.jpeg)

Anastasiou, Duhr, Dulat, (Furlan), (Gehrmann), Herzog, Mistlberger 16; Mistlberger 18;

\*Warning: just a cartoon, don't trust data/theory from this plot!

![](_page_9_Figure_1.jpeg)

#### Figure: G. Zanderighi / M. Wiesemann Sigure: G. Zanderighi / M. Wiesemann

![](_page_10_Figure_1.jpeg)

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Figure: G. Zanderighi / M. Wiesemann

# \_\_\_\_\_

### Cartoon 2: How Important is Precision?

Precision theory can enhance the discovery potential of our experiments!

![](_page_11_Figure_3.jpeg)

Figure: G. Zanderighi / M. Wiesemann

### Upcoming Experiments: Precision

![](_page_12_Figure_1.jpeg)

![](_page_12_Picture_2.jpeg)

HL-LHC construction underway ~10x integrated luminosity of LHC (LHC 0.3 ab<sup>-1</sup>, HL-LHC: 3 ab<sup>-1</sup>)

 Experimental projection is pessimistic considering current performance

**2)** Plot shown assumes reduction by factor 2 of today's uncertainties

# Theory uncertainty is expected to dominate HL-LHC Higgs physics

→ See next talk! (Harald Fox)

### Outline

#### **Higgs Boson Production**

#### **Gluon Fusion**

Theory uncertainties in gluon fusion

Boosted Higgs boson production & the top-quark mass

#### **ZH** Production

Impact of the gluon channel

Remaining uncertainties and open questions

#### **Di-Higgs Boson Production**

Current status and open questions

\*All of these areas are very active, apologies for my very biased topic selection

### How do we Improve Precision?

![](_page_14_Figure_1.jpeg)

$$d\sigma = \int dx_a dx_b f(x_a) f(x_b) d\hat{\sigma}_{ab}(x_a, x_b) F_J + \mathcal{O}\left((\Lambda/Q)^m\right)$$
Parton Distribution Hard Scattering Non-perturbative Functions (PDFs) Matrix Element effects ~ few %

### Higgs Production & Decay

![](_page_15_Figure_1.jpeg)

#### ATLAS-CONF-2021-053

ATLAS Preliminary	<b>⊢</b> •-1	Total	
$V_s = 13 \text{ TeV}, 36.1 - 139 \text{ fb}^{-1}$		Stat. Svst	
$m_H = 125.09 \text{ GeV}$		SM	
$p_{SM} = 79\%$		-	
ggF γγ	1.02	Total + 0.11 - 0.11	Stat. Syst. ( + 0.08 , + 0.07 - 0.08 , - 0.07 )
ggF ZZ	0.95	+ 0.11 - 0.11	$\left(\begin{array}{cc} +0.10 & +0.04 \\ -0.10 & -0.03 \end{array}\right)$
ggF WW	1.13	+ 0.13 - 0.12	$(\begin{array}{ccc} +0.06 & +0.12 \\ -0.06 & , & -0.10 \end{array})$
ggF ττ 📫	0.87	+ 0.28 - 0.25	$\left( \begin{array}{cc} + \ 0.15 \\ - \ 0.15 \end{array} \right. , \begin{array}{c} + \ 0.23 \\ - \ 0.20 \end{array} \right)$
ggF+ttH μμ 📕 💶 🖬	0.52	+ 0.91 - 0.88	$\left( \begin{array}{cc} +0.77 & +0.49 \\ -0.79 & , & -0.38 \end{array} \right)$
VBF γγ 🔎	1.47	+ 0.27 - 0.24	$\left(\begin{array}{ccc} +0.21 & +0.17 \\ -0.20 & , & -0.14 \end{array}\right)$
VBF ZZ	1.31	+ 0.51 - 0.42	$\left(\begin{array}{cc} +0.50 & +0.11 \\ -0.42 & , & -0.06 \end{array}\right)$
VBFWW	1.09	+ 0.19 - 0.17	$\left(\begin{array}{ccc} +0.15 & +0.11 \\ -0.14 & -0.10 \end{array}\right)$
VBF ττ 🙀	0.99	+ 0.20 - 0.18	$\begin{pmatrix} +0.14 & +0.15 \\ -0.14 & -0.12 \end{pmatrix}$
VBF+ggF bb	0.98	+ 0.38 - 0.36	$\left( \begin{array}{cc} + 0.31 & + 0.21 \\ - 0.33 & - 0.15 \end{array} \right)$
VBF+VH μμ	2.33	+ 1.34 - 1.26	$\left(\begin{array}{cc} + 1.32 & + 0.20 \\ - 1.24 & , & - 0.23 \end{array}\right)$
VH γγ	1.33	+ 0.33 - 0.31	$\left( \begin{array}{ccc} +0.32 & +0.10 \\ -0.30 & -0.08 \end{array} \right)$
VH ZZ	1.51	+ 1.17 - 0.94	$\left(\begin{array}{cc} +1.14 & +0.24 \\ -0.93 & -0.16 \end{array}\right)$
	0.98	+ 0.59 - 0.57	$\left( \begin{array}{cc} + \ 0.49 \\ - \ 0.49 \end{array} \right.$ , $\begin{array}{c} + \ 0.33 \\ - \ 0.29 \end{array} \right)$
WH bb	1.04	+ 0.28 - 0.26	$\left( \begin{array}{ccc} + \ 0.19 \\ - \ 0.19 \end{array} \right. , \begin{array}{c} + \ 0.20 \\ - \ 0.18 \end{array} \right)$
ZH bb	1.00	+ 0.24 - 0.22	$\left( \begin{array}{ccc} + 0.17 & + 0.17 \\ - 0.17 & - 0.14 \end{array} \right)$
ttH+tH γγ	0.93	+ 0.27 - 0.25	$\left( \begin{array}{cc} + \ 0.26 \\ - \ 0.24 \end{array} \right.$ , $\begin{array}{c} + \ 0.08 \\ - \ 0.06 \end{array} \right)$
ttH+tH WW	1.64	+ 0.65 - 0.61	$\left( \begin{array}{cc} + 0.44 \\ - 0.43 \end{array} , \begin{array}{c} + 0.48 \\ - 0.43 \end{array} \right)$
ttH+tH ZZ	1.69	+ 1.69 - 1.10	$\left( \begin{array}{cc} +1.65 & +0.37 \\ -1.09 \end{array} \right)$ , $\begin{array}{c} -0.16 \end{array} \right)$
ttH+tH TT F	1.39	+ 0.86 - 0.76	$\left( \begin{array}{cc} +0.66 & +0.54 \\ -0.62 \end{array} \right)$ , $\begin{array}{c} -0.44 \end{array} \right)$
ttH+tH bb	0.35	+ 0.34 - 0.33	$( \begin{array}{c} +0.20 \\ -0.20 \end{array}, \begin{array}{c} +0.28 \\ -0.27 \end{array} )$
-4 -2 0 2 4	<u> </u>	6	8
. <u> </u>	× B n	ormal	lised to SM

### **Gluon Fusion**

![](_page_16_Figure_1.jpeg)

### A Useful Approximation: Heavy Top Limit

Heavy Top Limit (HTL): integrate out top quarks ( $m_T \rightarrow \infty$ ) Introduces couplings  $c_h \& c_{hh}$  between gluons and Higgs Removes dependence on  $m_T$  and decreases the number of loops by 1

![](_page_17_Figure_2.jpeg)

### Gluon Fusion: Error Budget

![](_page_18_Figure_1.jpeg)

#### Progress

 $\delta(1/m_t)$ : Known to NNLO, removed

 $\delta(t, b, c)$ : Challenging but possible

 $\delta(\mathrm{EW})$ : gg known, reduced from ~1% to 0.6%

 $\delta(PDF - TH)$ : Progress but uncertainty persists

 $\delta(\text{scale}):$  Some ingredients known

Czakon, Harlander, Klappert, Niggetiedt 21

Becchetti, Bonciani, Del Duca, Hirschi, Moriello, Schweitzer 20; + Bonetti, Panzer, Smirnov, Tancredi, Melnikov, ...

McGowan, Cridge, Harland-Lang, Thorne 22

Lee, von Manteuffel, Schabinger, Smirnov, Smirnov, Steinhauser 22

### Boosted Higgs: NLO H+jet

To attack  $\delta(1/m_T)$  need amplitudes with  $m_T$  included  $pp \rightarrow Hjj @$  LO (1-loop)  $pp \rightarrow Hj @$  NLO (2-loop)  $pp \rightarrow H @$  NNLO (3-loop)

![](_page_19_Figure_2.jpeg)

 $gg \rightarrow H + j$ 

The ppHj amplitude is itself interesting Predicts **boosted** (high- $p_T$ ) Higgs

Challenging calculation ( $s, t, m_H, m_T$ ) completed with various techniques:

#### Small $m_T$ approximation

Kudashkin, (Lindert), Melnikov, Wever 17, (18); Neumann 18;

#### Numerical evaluation of integrals

SPJ, Kerner, Luisoni 18, 21

The HTL alone is a very poor approximation of the large- $p_T$  behaviour

### Boosted Higgs: NLO H+jet

Recently,  $pp \rightarrow Hj$  was calculated including full  $m_B, m_T$  dependence using the series expansion of differential equations

Bonciani, Del Duca, Frellesvig, Hidding, Hirschi, Moriello, Salvatori, Somogyi, Tramontano 22;

![](_page_20_Figure_3.jpeg)

Confirm earlier results that indicated NLO corrections are large  $K_{\rm NLO/LO} \approx 2$ Bottom and top/bottom interference effects relevant only for low- $p_T$ Result very flexible: allows quark masses to be renormalised in different schemes

### Boosted Higgs: NLO H+2jet

Interestingly, a particular approximation (FT<sub>approx</sub>) works quite well for H+j Use exact Born + Reals Approximate 2-loop Virtuals with  $|\mathscr{M}_4^2(m_t,\mu_R^2;\{p\})|^2 \rightarrow |\mathscr{M}_4^1(\infty,\mu_R^2;\{p\})|^2 \frac{|\mathscr{M}_4^1(m_t;\{p\})|^2}{|\mathscr{M}_4^0(\infty;\{p\})|^2}$ 

![](_page_21_Figure_2.jpeg)

Chen, Huss, SPJ, Kerner, Lang, Lindert, Zhang 21

Assuming approximation works similarly well for higher jet multiplicity, can produce improved H+2j predictions just by computing full reals

### Gluon Fusion: NNLO with Full top-quark Mass

![](_page_22_Figure_1.jpeg)

Decreases  $\sigma_{\rm tot}$  by -0.26% @ 13 TeV compared to heavy top limit (HTL)

Intricate interplay between mass effects gg (+0.62%), qg (-16%), qq (-15%) Complete NNLO results obtained using STRIPPER framework

### **Gluon Fusion: Mixed QCD-EW Corrections**

![](_page_23_Figure_1.jpeg)

Increases  $\sigma_{tot}$  by +5.1 % @ 13 TeV, reduces residual uncertainty  $\delta(EW) \sim 0.6$  % Favouring factorisation of EW corrections:  $\sigma = \sigma_{LO} (1 + \delta_{OCD}) \times (1 + \delta_{EWK})$ 

Compatible with previous estimates:

Soft approx: +5.4%,  $M_H \ll M_V$ : +5.2%,  $M_H \gg M_V$ : +5.4%

Bonetti, Melnikov, Tancredi 18;

Anastasiou, Boughezal, Petriello 09:

Anastasiou, Del Duca, Furlan, Mistlberger, Moriello, Schweitzer, Specchia 19

### **ZH** Production

![](_page_24_Figure_1.jpeg)

### $pp \rightarrow ZH$ : Role of ggZH Channel

![](_page_25_Figure_1.jpeg)

Drell-Yan-like contribution recently computed @ N<sup>3</sup>LO Baglio, Duhr, Mistlberger, Szafron 22

Gluon channel contributes to

- $pp \rightarrow ZH @ NNLO$
- ~10% of the total cross section at LHC (due to large gluon luminosity)
- 2) Has large uncertainty >100%
- 3) A dominant TH uncertainty on ZH analyses

This motivates calculating ggZH @ NLO (2-loop)

### $gg \rightarrow ZH$ : 2-loop Virtual Amplitude

![](_page_26_Figure_1.jpeg)

#### A challenging calculation ( $s, t, m_H, m_T, m_Z$ ), completed with various techniques

(Small  $m_Z, m_H$ ) Wang, Xu, Xu, Yang 21; (Small  $m_T \& 1/m_T$  Expansions) Davies, Mishima, Steinhauser 20; (Numerical) Chen, Heinrich, SPJ, Kerner, Klappert, Schlenk 20; ( $p_T \& 1/m_T$  Expansions) Alasfar, Degrassi, Giardino, Gröber, Vitti 21; Bellafronte, Degrassi, Giardino, Gröber, Vitti 22; Degrassi, Gröber, Vitti, Zhao 22; (Small  $m_T \&$  Numerical) Chen, Davies, Heinrich, SPJ, Kerner, Mishima, Schlenk, Steinhauser 22

Our full result has 452 ``master integrals'' and ~5GB amplitude

Using (IBP) relations between the integrals we found a much simpler ~1GB expression for amplitude

Largest coefficient (double-tadpole) 150 MB  $\rightarrow$  5 MB

Chen, Heinrich, SPJ, Kerner, Klappert, Schlenk 20;

![](_page_26_Figure_8.jpeg)

### Aside: Evaluating Feynman Integrals

One of the biggest challenges for processes like this is computing the integrals We evaluate them numerically on CPUs & GPUs using **pySecDec** 

Try it now at: <a href="https://github.com/gudrunhe/secdec">https://github.com/gudrunhe/secdec</a>

#### Previous update (v1.5):

# Expansion by Regions & Amplitude Evaluation

Heinrich, Jahn, SPJ, Kerner, Langer, Magerya, Põldaru, Schlenk, Villa 21

#### Upcoming (wip->v1.6):

Significant speed improvements, flexible amplitude input, smaller generated code, ...

![](_page_27_Figure_8.jpeg)

\* v1.5: adaptive sampling, automatic contour deformation adjustment;

- \* *dev*: separation of real and complex variables in the integrand code;
- \* *wip*: simlification of the integrand code, vectorization on CPU (AVX2).

The latest release is fast; the next release will be faster.

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### $gg \rightarrow ZH$ : Results

Putting all pieces together (Born + reals + virtual) can obtain full NLO results

Chen, Davies, Heinrich, SPJ, Kerner, Mishima, Schlenk, Steinhauser 22

#### **Total Cross-section**

$\sqrt{S}$	LO [fb]	NLO [fb]
$13 { m TeV}$	$52.42^{+25.5\%}_{-19.3\%}$	$103.8(3)^{+16.4\%}_{-13.9\%}$
$13.6 { m TeV}$	$58.06^{+25.1\%}_{-19.0\%}$	$114.7(3)^{+16.2\%}_{-13.7\%}$
$14 { m TeV}$	$61.96^{+24.9\%}_{-18.9\%}$	$122.2(3)^{+16.1\%}_{-13.6\%}$

#### **Invariant Mass**

![](_page_28_Figure_6.jpeg)

NNPDF31\_nlo\_pdfas  $m_t^{OS} = 173.21 \text{ GeV}$   $\mu = m_{ZH}$  $\mu_{R,F} \in \left[\frac{\mu}{2}, 2\mu\right]$  (7 - point)

NLO corrections are large and lie outside the usual LO scale uncertainties

NLO/LO somewhat\* flat except at production & top thresholds

\*Starts to rise above ~1 TeV (also depends on what real diagrams are included)

### $gg \rightarrow ZH$ : Transverse Momentum

**H** Transverse Momentum

![](_page_29_Figure_1.jpeg)

#### Z Transverse Momentum

Z  $p_T$ : Large NLO corrections, rising sharply at large  $p_{T,Z}$ H  $p_T$ : Extremely large NLO corrections, rising very sharply at large  $p_{T,H}$ Placing cuts on soft Z or H emission slightly tames growth

Radiating an additional jet opens up an important new region of phase-space Very important to include higher order corrections in this region

### $gg \rightarrow ZH$ : Z vs H

The different behaviour of  $p_{T,Z}$  and  $p_{T,H}$  was observed previously in  $gg \rightarrow ZH + j$ Hespel, Maltoni, Vryonidou 15; Les Houches 19

![](_page_30_Figure_2.jpeg)

Traced to configurations where Higgs recoils against a hard jet, with a soft Z

 $p \cdot p_Z$ 

#### **One observation**

![](_page_30_Figure_5.jpeg)

Maltoni et al. attributed this to *t*-channel gluon exchange

If we apply an eikonal approximation to such diagrams, the enhancement of soft Z bosons can be understood (Soft Z emission):  $\frac{p^{\mu}}{2}$ 

(Soft *H* emission):  $\frac{m_t}{p \cdot p_H}$  P Ratio for large radiator (transverse) momentum  $\sim p_T/m_t \gg 1$ 

### $gg \rightarrow ZH$ : Mass Scheme Uncertainty

![](_page_31_Figure_1.jpeg)

![](_page_31_Figure_2.jpeg)

#### **Observations @** $m_{ZH} = 1$ TeV

Large difference between different schemes LO: OS result ~2.9x  $\overline{\text{MS}}$  result NLO: Difference reduced ~1.9x If taken as a theoretical uncertainty, this is larger than the scale uncertainty!

Such mass scheme uncertainties show up in other processes (e.g. HH, H\*, HJ)

Baglio, Campanario, Glaus, Mühlleitner, (+Ronca) Spira, Streicher 18, (20); SPJ, Spira (Les Houches 19)

### HH Production

![](_page_32_Figure_1.jpeg)

$$\sigma(pp \to HH) \sim \frac{\sigma(pp \to H)}{1000}$$

### HH: Why Measure it?

$$\mathcal{L} \supset -V(\phi), \quad V(\Phi) = -\mu^2 (\Phi^{\dagger} \Phi) + \lambda (\Phi^{\dagger} \Phi)^2$$
  
EW symmetry breaking  

$$\mu^2 = \lambda v^2$$

$$m_H^2 = 2\lambda v^2$$

$$V(H) = \frac{1}{2}m_H^2 H^2 + \lambda v H^3 + \frac{\lambda}{4} H^4,$$
SM: self-couplings  
determined by  $m_H, v$   

$$\mu$$

$$V(H) = \frac{1}{2}m_H^2 H^2 + \frac{\lambda v H^3}{4} + \frac{\lambda}{4} H^4,$$
EXP: need measurements  
to confirm/refute this  

$$V(H) = \frac{1}{2}m_H^2 H^2 + \frac{\lambda}{4} V H^3 + \frac{\lambda}{4} H^4,$$
EXP: need measurements  
to confirm/refute this  

$$V(H) = \frac{1}{2}m_H^2 H^2 + \frac{\lambda}{4} V H^3 + \frac{\lambda}{4} H^4,$$
EXP: need measurements  
to confirm/refute this

g

g

### HH: Experimental Bounds

#### Very impressive experimental results

Combining 3 decay channels

+ using H and HH information CERN-EP-2022-149

> $\mu_{HH} < 2.4 @ 95\% cl$  $-0.4 < \kappa_{\lambda} < 6.3 @ 95\% cl$

#### **HL-LHC** projection

Using HH data from 3 channels Assuming TH uncertainty is halved ATL-PHYS-PUB-2022-053

#### Current

![](_page_34_Figure_9.jpeg)

#### **HL-LHC Projection**

![](_page_34_Figure_11.jpeg)

### HH: Theory History

![](_page_35_Figure_1.jpeg)

[1] Glover, van der Bij 88; [2] Dawson, Dittmaier, Spira 98; [3] Shao, Li, Li, Wang 13; [4] Grigo, Hoff, Melnikov, Steinhauser 13; [5] de Florian, Mazzitelli 13; [6] Grigo, Melnikov, Steinhauser 14; [7] Grigo, Hoff 14; [8] Maltoni, Vryonidou, Zaro 14; [9] Grigo, Hoff, Steinhauser 15; [10] de Florian, Grazzini, Hanga, Kallweit, Lindert, Maierhöfer, Mazzitelli, Rathlev 16; [11] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Schubert, Zirke 16; [12] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Zirke 16; [13] Ferrera, Pires 16; [14] Heinrich, SPJ, Kerner, Luisoni, Vryonidou 17; [15] SPJ, Kuttimalai 17; [16] Gröber, Maier, Rauh 17; [17] Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher 18; [18] Grazzini, Heinrich, SPJ, Kallweit, Kerner, Lindert, Mazzitelli 18; [19] de Florian, Mazzitelli 18; [20] Bonciani, Degrassi, Giardino, Gröber 18; [21] Davies, Mishima, Steinhauser 19; [26] Chen, Li, Shao, Wang 19, 19; [27] Davies, Herren, Mishima, Steinhauser 19, 21; [28] Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira 21; [29] Bellafronte, Degrassi, Giardino, Gröber, Vitti 22; [30] Davies, Mishima, Steinhauser, Zhang 22;

### HH: NLO

#### Results including $m_T$ are known up to NLO

(Numerical) Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Schubert, Zirke 16; Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Zirke 16; Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher 18;

(Small  $m_T$ ) Davies, Mishima, Steinhauser, Wellmann 18, 18;

(Numerical & Small  $m_T$ ) Davies, Heinrich, SPJ, Kerner, Mishima, Steinhauser, Wellmann 19

![](_page_36_Figure_5.jpeg)

![](_page_36_Figure_6.jpeg)

#### For HH production:

The NLO corrections are again large NLO/LO  $\approx$  1.7 and scale uncertainties ~halved

 $FT_{approx}$  does not work so well above the the top-quark threshold

This is exactly the sort of situation depicted in our ``Cartoon 2''

### HH: N<sup>3</sup>LO Heavy Top Limit

![](_page_37_Figure_1.jpeg)

Chen, Li, Shao, Wang 19

![](_page_37_Figure_3.jpeg)

#### Ingredients: N<sup>3</sup>LO H calculation

Anastasiou, Duhr, Dulat, Herzog, Mistlberger 15; Dulat, Lazopoulos, Mistlberger 18

#### + 2-loop 4-point functions

Banerjee, Borowka, Dhani, Gehrmann, Ravindran 18

$\sqrt{s}$ order	$13 { m TeV}$	$14 { m TeV}$	$27 { m TeV}$	100 TeV
LO	$13.80^{+31\%}_{-22\%}$	$17.06^{+31\%}_{-22\%}$	$98.22^{+26\%}_{-19\%}$	$2015^{+19\%}_{-15\%}$
NLO	$25.81^{+18\%}_{-15\%}$	$31.89^{+18\%}_{-15\%}$	$183.0^{+16\%}_{-14\%}$	$3724_{-11\%}^{+13\%}$
NNLO	$30.41^{+5.3\%}_{-7.8\%}$	$37.55^{+5.2\%}_{-7.6\%}$	$214.2^{+4.8\%}_{-6.7\%}$	$4322_{-5.3\%}^{+4.2\%}$
$N^{3}LO$	$31.31^{+0.66\%}_{-2.8\%}$	$38.65^{+0.65\%}_{-2.7\%}$	$220.2^{+0.53\%}_{-2.4\%}$	$4438^{+0.51\%}_{-1.8\%}$

#### T Very mild scale dependence

### HH: Beyond HTL @ N<sup>3</sup>LO

Top quark mass effects included in N<sup>3</sup>LO HTL (up to NLO)

![](_page_38_Figure_2.jpeg)

Chen, Li, Shao, Wang 19

Results agree with NNLO result but with smaller scale uncertainty Results recently computed at  $N^{3}LO + N^{3}LL$  Ajjath, Shao 22

### HH: EFT

Can leverage SM calculations @ NLO (NNLO,...) to compute also EFT results (... though EFTs can be tricky HEFT/SMEFT,  $O_6/O_6^2$ ,  $O_{8, ...}$ )

![](_page_39_Figure_2.jpeg)

![](_page_39_Figure_3.jpeg)

Related in SMEFT

#### EFT results available in various approximations:

NLO (HEFT) Buchalla, Capozi, Celis, Heinrich, Scyboz 18;
+ PS Heinrich, SPJ, Kerner, Scyboz 20;
NLO + NNLO' de Florian, Fabre, Heinrich, Mazzitelli, Scyboz 21
NLO (SMEFT) Heinrich, Lang, Scyboz 22;

### HH: Mass Scheme Uncertainty

Comparing  $gg \rightarrow HH$  and  $gg \rightarrow ZH$  we see a different high-energy behaviour

 $A_i^{\text{fin}} = a_s A_i^{(0),\text{fin}} + a_s^2 A_i^{(1),\text{fin}} + \mathcal{O}(a_s^3) \quad \text{with} \ a_s = \alpha_s/4\pi$ 

 Davies, Mishima, Steinhauser, Wellmann 18;
 Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira, Streicher 20

$$\begin{split} A_{i}^{(0)} &\sim m_{t}^{2} f_{i}(s,t) \\ A_{i}^{(1)} &\sim 6 C_{F} A_{i}^{(0)} \log \left[ \frac{m_{t}^{2}}{s} \right] \end{split}$$

LO:  $m_t^2$  from  $y_t^2$ NLO: leading  $log(m_t^2)$  from mass c.t. **ZH** Davies, Mishima, Steinhauser 20

$$\begin{split} A_i^{(0)} &\sim m_t^2 f_i(s,t) \; \log^2 \left[ \frac{m_t^2}{s} \right] \\ A_i^{(1)} &\sim \frac{(C_A - C_F)}{6} A_i^{(0)} \; \log^2 \left[ \frac{m_t^2}{s} \right] \end{split}$$

LO: one  $m_t$  from  $y_t$ NLO: leading  $log(m_t^2)$  not coming from mass c.t. ( $C_A$ )

Would be interesting to further understand these structures, similar powersuppressed mass logarithms were studied in single H  $\frac{\text{Liu, Modi, Penin 22}}{\text{Liu, Neubert, Schnubel, Wang 22}}$ 

### HH: EW Corrections

It is also interesting to explore the impact of EW corrections (in single Higgs for off-shell Higgs have  $\pm 5\%$  impact) Actis, Passarino, Sturm, Uccirati 08

Richer structure in the SM and much richer structure in the context of EFT

#### Partial 2-loop EW corrections known:

![](_page_41_Figure_4.jpeg)

![](_page_41_Figure_5.jpeg)

Borowka, Duhr, Maltoni, Pagani, Shivaji, Zhao 18

Leading top-Yukawa contributions

![](_page_41_Figure_8.jpeg)

(Small  $m_T$ ) Davies, Mishima, Schönwald, Steinhauser, Zhang 22 + (EFT approach) Mühlleitner, Schlenk, Spira 22

# Complete EW corrections will modify distributions and bounds in the SM & EFT frameworks

### Summary

Great progress in theory precision over the last few years

Uncertainties beyond scale variations are becoming increasingly relevant

Still plenty to do if you are bored!

See: Les Houches Wishlist 21

#### Thank you for listening

process	known	desired
	N <sup>3</sup> LO <sub>HTL</sub>	
$pp \to H$	$\mathrm{NNLO}_{\mathrm{QCD}}^{(t)}$	$N^4LO_{HTL}$ (incl.)
	$\mathrm{N}^{(1,1)}\mathrm{LO}^{(\mathrm{HTL})}_{\mathrm{QCD}\otimes\mathrm{EW}}$	$\mathrm{NNLO}_\mathrm{QCD}^{(b,c)}$
	$\rm NLO_{QCD}$	
	$\mathrm{NNLO}_{\mathrm{HTL}}$	
$pp \to H+j$	$\rm NLO_{QCD}$	$\mathrm{NNLO}_{\mathrm{HTL}} \otimes \mathrm{NLO}_{\mathrm{QCD}} + \mathrm{NLO}_{\mathrm{EW}}$
	$\rm N^{(1,1)}LO_{QCD\otimes EW}$	
	$\rm NLO_{\rm HTL} \otimes \rm LO_{\rm QCD}$	NNLO $\otimes$ NLO $+$ NLO
$m \rightarrow H + 2i$	$ m N^{3}LO_{QCD}^{(VBF^{*})}$ (incl.)	$\mathbf{N}^{3}\mathbf{LO}_{\mathrm{HTL}} \otimes \mathbf{N}^{2}\mathbf{LO}_{\mathrm{QCD}} + \mathbf{N}^{2}\mathbf{LO}_{\mathrm{EW}}$
$pp \neq m \neq 2j$	$\mathrm{NNLO}_{\mathrm{QCD}}^{(\mathrm{VBF}^*)}$	$N LO_{QCD}$
	$\mathrm{NLO}_{\mathrm{EW}}^{(\mathrm{VBF})}$	NNLOQCD
$pp \rightarrow H + 3j$	$\mathrm{NLO}_{\mathrm{HTL}}$	
	$\mathrm{NLO}_{\mathrm{QCD}}^{\mathrm{(VBF)}}$	$NLO_{QCD} + NLO_{EW}$
$m \rightarrow VH$	$\mathrm{NNLO}_{\mathrm{QCD}} + \mathrm{NLO}_{\mathrm{EW}}$	
$pp \rightarrow v \Pi$	$\text{NLO}_{gg \to HZ}^{(t,b)}$	
$pp \rightarrow VH + j$	$NNLO_{QCD}$	$NNLO_{OCD} + NLO_{DW}$
	$\rm NLO_{QCD} + \rm NLO_{EW}$	THEOGCD + HEOEW
$pp \to HH$	$\rm N^{3}LO_{HTL} \otimes \rm NLO_{QCD}$	$\rm NLO_{EW}$
	$N^{3}LO_{QCD}^{(VBF^{*})}$ (incl.)	
$pp \to HH + 2j$	$\mathrm{NNLO}_{\mathrm{QCD}}^{(\mathrm{VBF}^*)}$	
	$\mathrm{NLO}_{\mathrm{EW}}^{(\mathrm{VBF})}$	
$pp \rightarrow HHH$	NNLO <sub>HTL</sub>	
$pp \to H + t\bar{t}$	$\rm NLO_{QCD} + \rm NLO_{EW}$	
	$\rm NNLO_{\rm QCD}$ (off-diag.)	ININLOQCD
$pp \to H + t/\bar{t}$	$\rm NLO_{QCD} + \rm NLO_{EW}$	NNLO <sub>QCD</sub>

## Backup

### $gg \rightarrow ZH$ : Real Emission Diagrams

There is some **freedom** regarding which real diagrams we include in gg vs  $q\bar{q}$ Must be careful not to double count when combining all channels for  $pp \rightarrow ZH$ Our reals are evaluated using **GoSam** Cullen et al. 11,14

**Diagrams excluded in our work** 

![](_page_44_Picture_3.jpeg)

**Left class of diagrams**: separately UV/IR finite & gauge invariant Previously studied in detail See e.g. Brein, Harlander, Wiesemann, Zirke 12

**Right class of diagrams:** belongs to real corrections to Drell-Yan (i.e.  $q\bar{q}$ ) Included in DY calculations Brein, Djouadi, Harlander 03;

Ferrera, Grazzini, Tramontano 14; See also: Kumara, Mandal, Ravindran 14

#### HH: Mass Scheme Uncertainty

Combination of scale ( $\mu_R$ ,  $\mu_F$ ) and top mass scheme (OS / MS) studied Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira 20

If we wish to take the **envelope** of the predictions as the uncertainty, then the two uncertainties should be added **linearly** (validated at NLO)

#### Scale $(\mu_R, \mu_F)$

#### $\kappa_{\lambda} = -10: \quad \sigma_{tot} = 1680^{+3.0\%}_{-7.7\%} \text{ fb}, \qquad \kappa_{\lambda} = -10: \quad \sigma_{tot} = 1438(1)^{+10\%}_{-6\%} \text{ fb},$ $\kappa_{\lambda} = -5: \quad \sigma_{tot} = 598.9^{+2.7\%}_{-7.5\%} \text{ fb}, \qquad \kappa_{\lambda} = -5: \quad \sigma_{tot} = 512.8(3)^{+10\%}_{-7\%} \text{ fb},$ $\kappa_{\lambda} = -1: \quad \sigma_{tot} = 131.9^{+2.5\%}_{-6.7\%} \text{ fb}, \qquad \kappa_{\lambda} = -1: \quad \sigma_{tot} = 113.66(7)^{+8\%}_{-9\%} \text{ fb},$ $\kappa_{\lambda} = 0: \quad \sigma_{tot} = 70.38^{+2.4\%}_{-6.1\%} \text{ fb}, \qquad \kappa_{\lambda} = 0: \quad \sigma_{tot} = 61.22(6)^{+6\%}_{-12\%} \text{ fb},$ $\begin{aligned} \kappa_{\lambda} &= 1: \quad \sigma_{tot} &= 31.05^{+2.2\%}_{-5.0\%} \text{ b}, \\ \kappa_{\lambda} &= 2: \quad \sigma_{tot} &= 13.81^{+2.1\%}_{-4.9\%} \text{ fb}, \end{aligned} \qquad \textbf{+} \qquad \begin{aligned} \kappa_{\lambda} &= 1: \quad \sigma_{tot} &= 27.73(7^{+4\%}_{-18\%} \text{ fb}, \\ \kappa_{\lambda} &= 2: \quad \sigma_{tot} &= 13.2(1)^{+1\%}_{-23\%} \text{ fb}, \end{aligned}$ $\kappa_{\lambda} = 2.4: \quad \sigma_{tot} = 13.10^{+2.3\%}_{-5.1\%} \text{ fb}, \qquad \kappa_{\lambda} = 2.4: \quad \sigma_{tot} = 12.7(1)^{+4\%}_{-22\%} \text{ fb},$ $\kappa_{\lambda} = 3: \quad \sigma_{tot} = 18.67^{+2.7\%}_{-7.3\%} \text{ fb}, \qquad \kappa_{\lambda} = 3: \quad \sigma_{tot} = 17.6(1)^{+9\%}_{-15\%} \text{ fb},$ $\kappa_{\lambda} = 5: \quad \sigma_{tot} = 94.82^{+4.9\%}_{-8.8\%} \text{ fb}, \qquad \kappa_{\lambda} = 5: \quad \sigma_{tot} = 83.2(3)^{+13\%}_{-4\%} \text{ fb},$ $\kappa_{\lambda} = 10: \quad \sigma_{tot} = 672.2^{+4.2\%}_{-8.5\%} \text{ fb} \qquad \kappa_{\lambda} = 10: \quad \sigma_{tot} = 579(1)^{+12\%}_{-4\%} \text{ fb}$

#### NLO Mass Scheme Unc.

#### **Proposed Combination**

$\kappa_{\lambda} = -10$ :	$\sigma_{tot}$	=	$1680^{+13\%}_{-14\%}$ fb,
$\kappa_{\lambda} = -5:$	$\sigma_{tot}$	=	$598.9^{+13\%}_{-15\%}$ fb,
$\kappa_{\lambda} = -1:$	$\sigma_{tot}$	=	$131.9^{+11\%}_{-16\%}$ fb,
$\kappa_{\lambda} = 0$ :	$\sigma_{tot}$	=	$70.38_{-18\%}^{+8\%}$ fb,
$\kappa_{\lambda} = 1$ :	$\sigma_{tot}$	=	$31.05_{-23\%}^{+6\%}$ b,
$\kappa_{\lambda} = 2$ :	$\sigma_{tot}$	=	$13.81_{-28\%}^{+3\%}$ fb,
$\kappa_{\lambda} = 2.4$ :	$\sigma_{tot}$	=	$13.10^{+6\%}_{-27\%}$ fb,
$\kappa_{\lambda} = 3$ :	$\sigma_{tot}$	=	$18.67^{+12\%}_{-22\%}$ fb,
$\kappa_{\lambda} = 5:$	$\sigma_{tot}$	=	94.82 <sup>+18%</sup> <sub>-13%</sub> fb,
$\kappa_{\lambda} = 10$ :	$\sigma_{tot}$	=	$672.2^{+16\%}_{-13\%}$ fb

#### @13 TeV

### Tackling Mass Scheme Uncertainties

![](_page_46_Figure_1.jpeg)

#### Low invariant mass:

expand in  $1/m_t^2$ known to NNLO Grigo, Hoff, Steinhauser 15;

**Around Peak:** threshold expansion Gröber, Maier, Rauh 17

#### High energy:

small-*m*<sub>t</sub> expansion known at NLO Davies, Mishima, Steinhauser, Wellmann 18, 19

#### **Options:**

1) Try to understand structure of mass logarithms

- 2) Keep calculating
- 3) Other ideas (?)