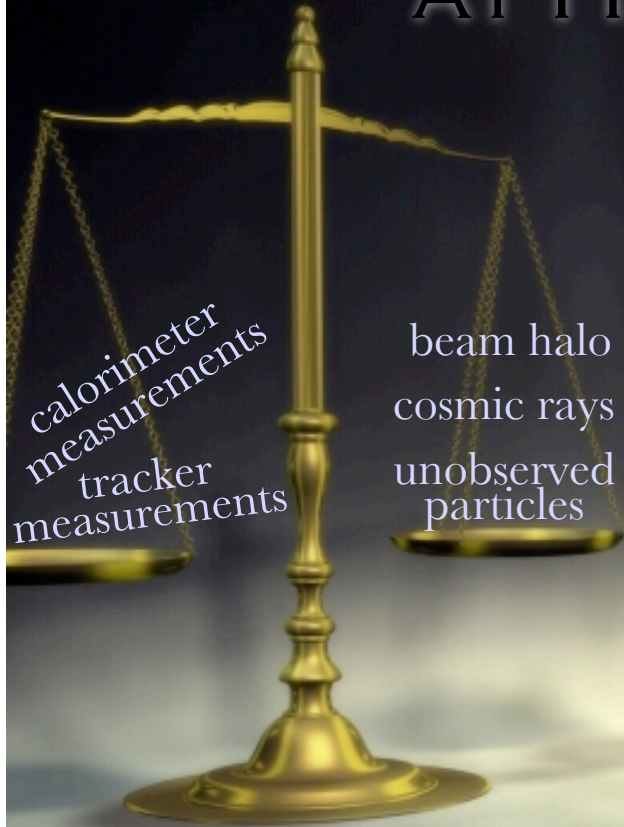


“MISSING” MOMENTUM MEASUREMENT AT HADRON COLLIDERS



Motivation
Measurement
Mismeasurement
Modelling

**(Event
selection)**

Chris Hays,
Oxford University

YETI 2008, Durham



Motivation

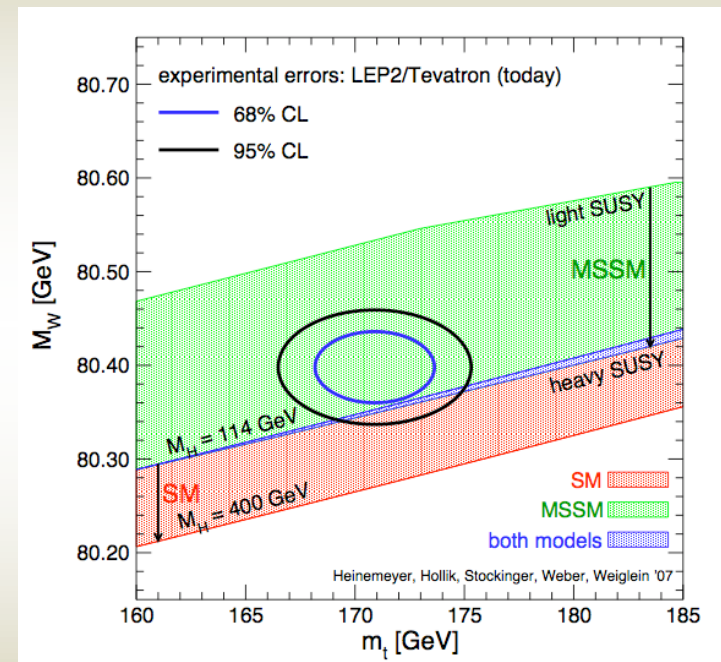
- *Unobserved particles crucial to standard model measurements and future discoveries*

– Neutrinos:

- W and top mass measurements
 - *constrain the Higgs mass and the existence of supersymmetric particles*
- Higgs decay to WW
 - *discovery channel if Higgs mass is ~ 160 GeV*

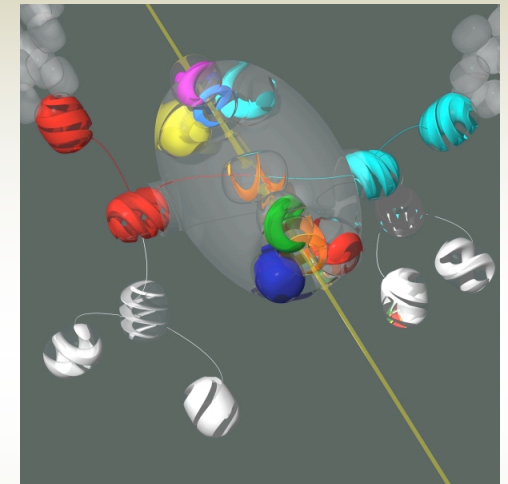
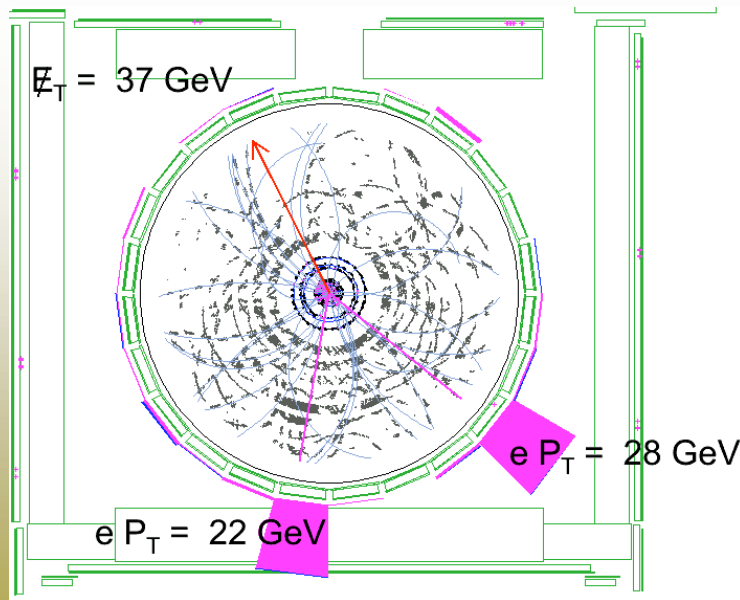
– Dark matter:

- Heavy neutral particles such as the lightest supersymmetric particle
 - *Inferred by excess of events with large momentum imbalance of observed particles*



Measurement

- *Initial state z -momentum not known, can only infer momentum imbalance in the direction transverse to the beam line*
- *Momentum imbalance measured primarily using calorimeter energy and a vertex*
 - Hence the jargon “missing transverse energy” or \cancel{E}_T



Jan Henrik-Andersen

WW decay to a pair of
electrons and neutrinos
(CDF)

Measurement

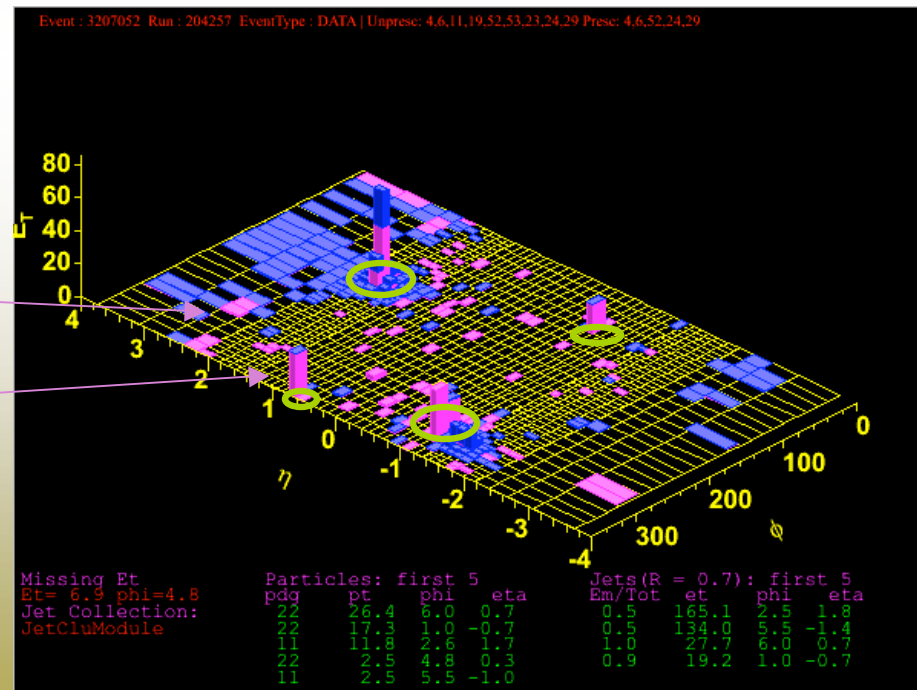
- *Correct for particles not measured well by calorimeter*
 - **Muons:** use track momentum, subtract energy in calorimeter
 - **Jets:** apply calibrations to correct for lost particles and calorimeter response
- *The end result is an accurate measurement of momentum imbalance*

$$\sum_i \vec{p}_i + \overrightarrow{\text{uncl}} + \vec{p} = \vec{0}$$

Unclustered energy

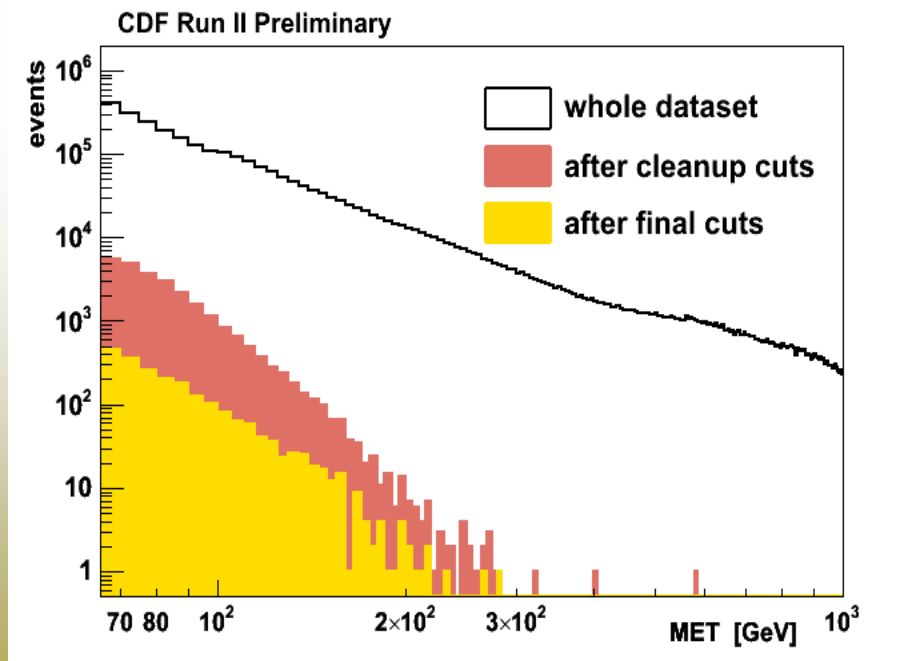
Object

Diphoton plus dijet event
(CDF)



Mismeasurement

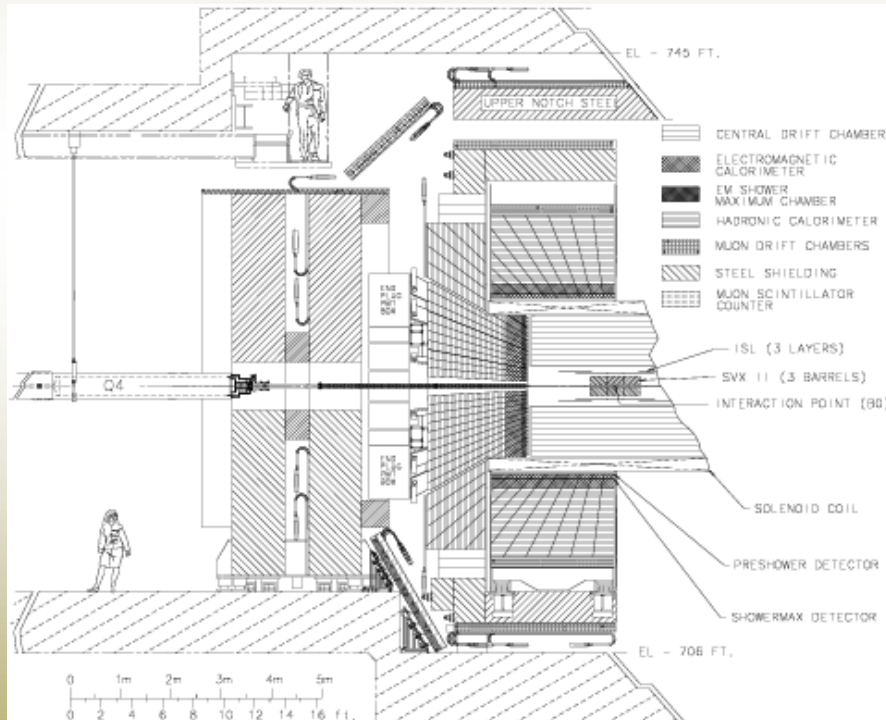
- *Background to events with large \cancel{E}_T results predominantly from pathological mismeasurements*
 - **Beam-induced background**
 - **Cosmic-ray muons**
 - **Jet energy lost in detector cracks**



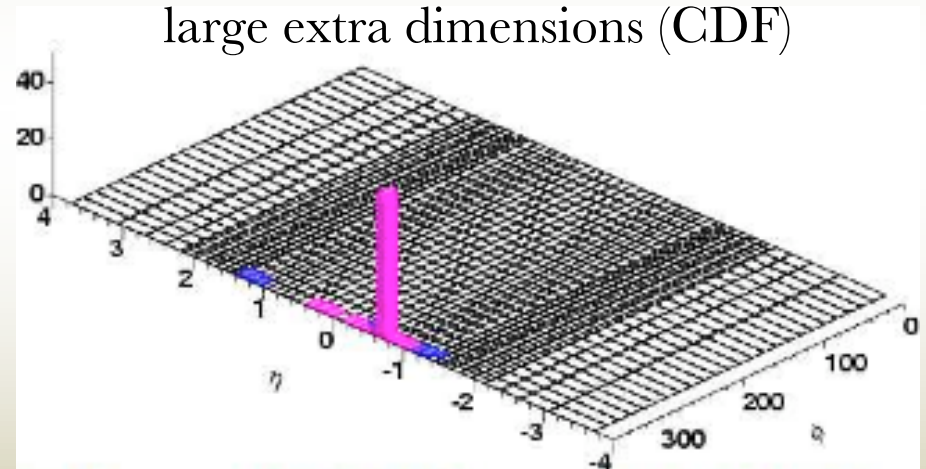
Jets plus \cancel{E}_T search
for squarks and gluinos
(CDF)

Beam Halo

- *Beam interactions with pipe produce showers upstream of detector*
 - **CDF: shielding significantly attenuates shower**
 - **Muons can penetrate shielding and deposit energy in calorimeter**



Photon plus \cancel{E}_T search for large extra dimensions (CDF)

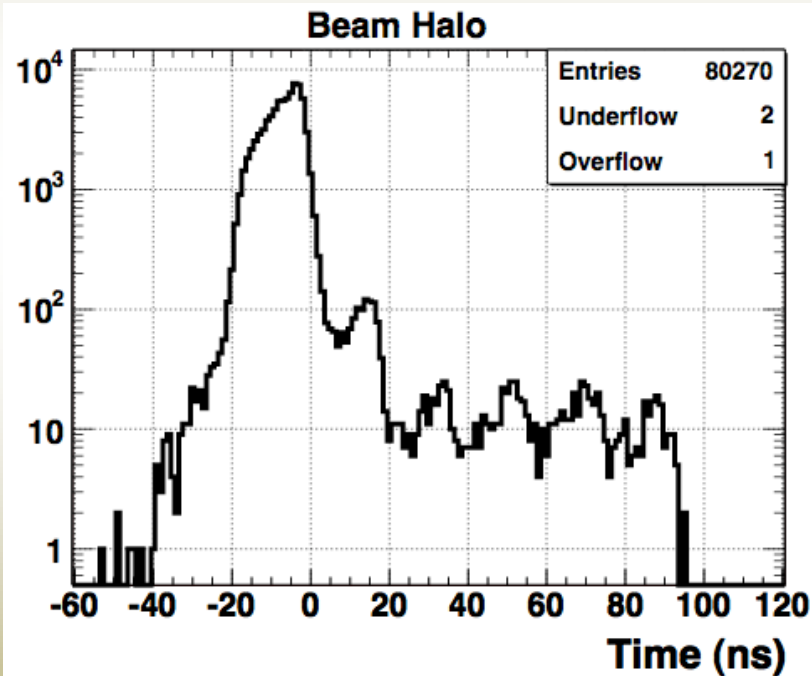


Line of minimum-ionizing energy deposition

Bremsstrahlung results in single high-momentum photon

Beam Halo

- *Halo observable in timing distribution of photon candidates*
 - **18 ns beam bunch structure**
 - **Width due to size of central calorimeter**



Timing cut reduces background

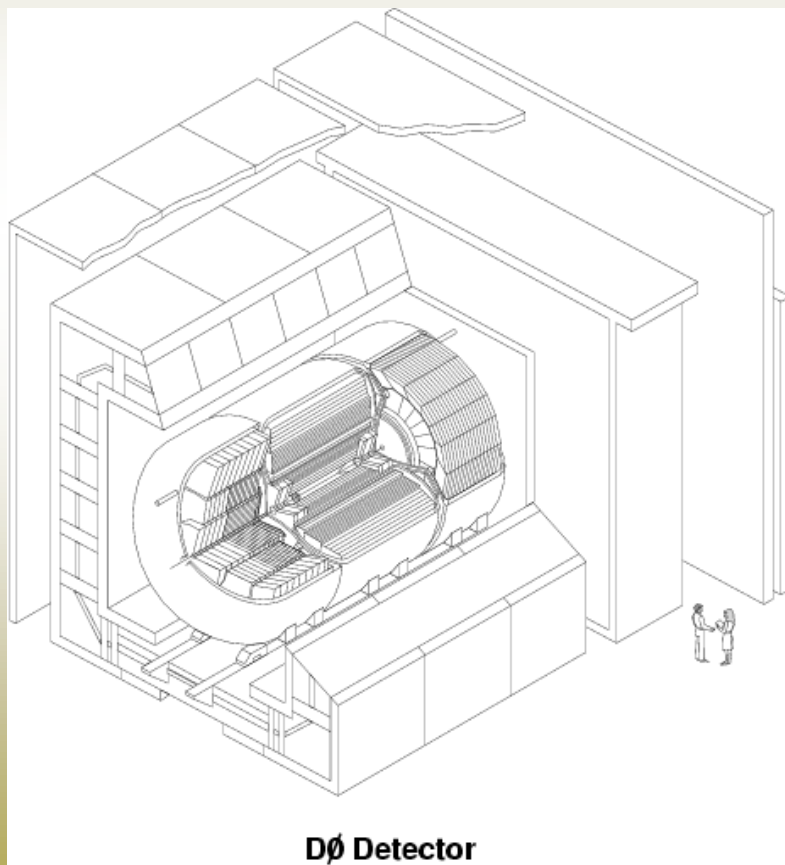
Residual background removed with calorimeter requirements:

No more than 8 central EM and 2 forward hadronic towers with energy along the line of the candidate photon

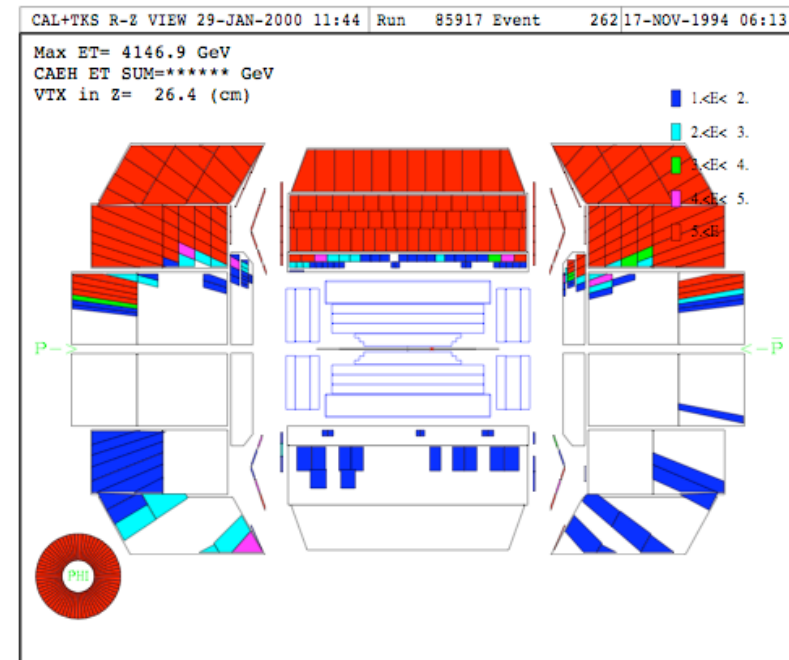
Photon plus \cancel{E}_T searches (CDF)

Beam Splash

- *Tevatron Run 1: Two accelerator rings, one went through top of DØ calorimeter*
 - Beam interactions with pipe produced showers inside detector
 - **Vetoed events collected while beam passed through top ring**

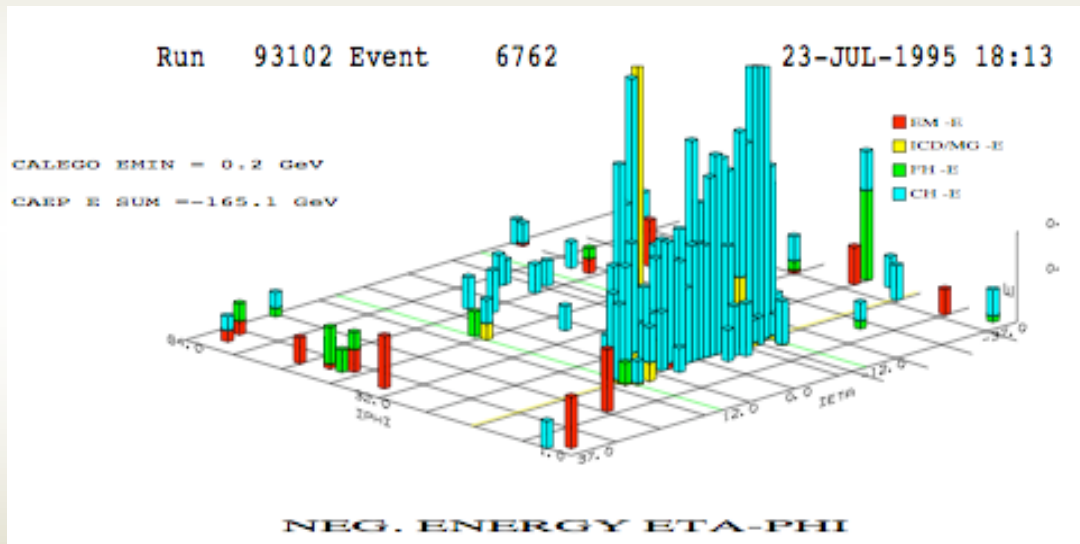


Two jets plus \cancel{E}_T search for leptoquarks (DØ)

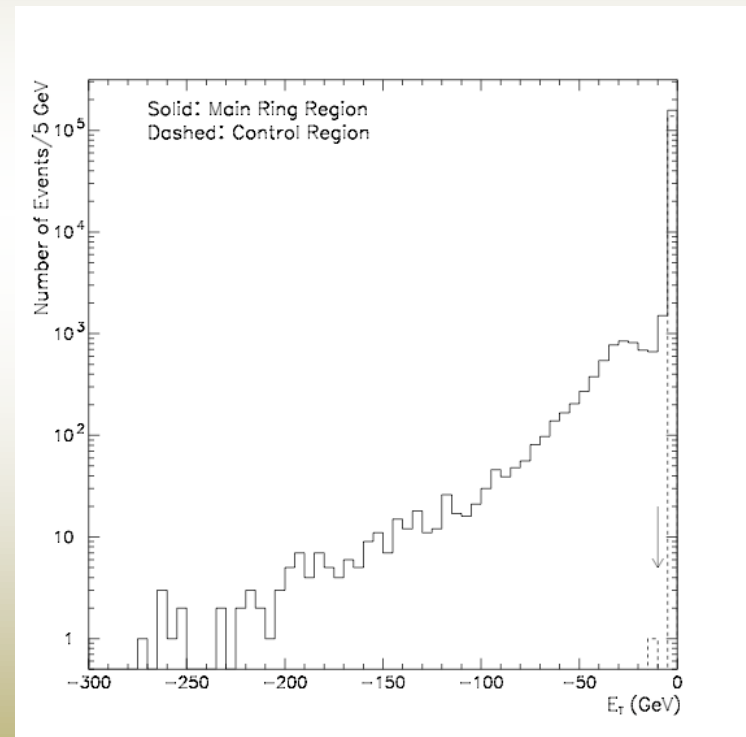


Beam Splash

- *Events collected in crossings after beam splash also had large \cancel{E}_T*
 - Charge dissipation from readout resulted in negative observed energies
 - **Charge at end of bunch lower than at start of bunch**



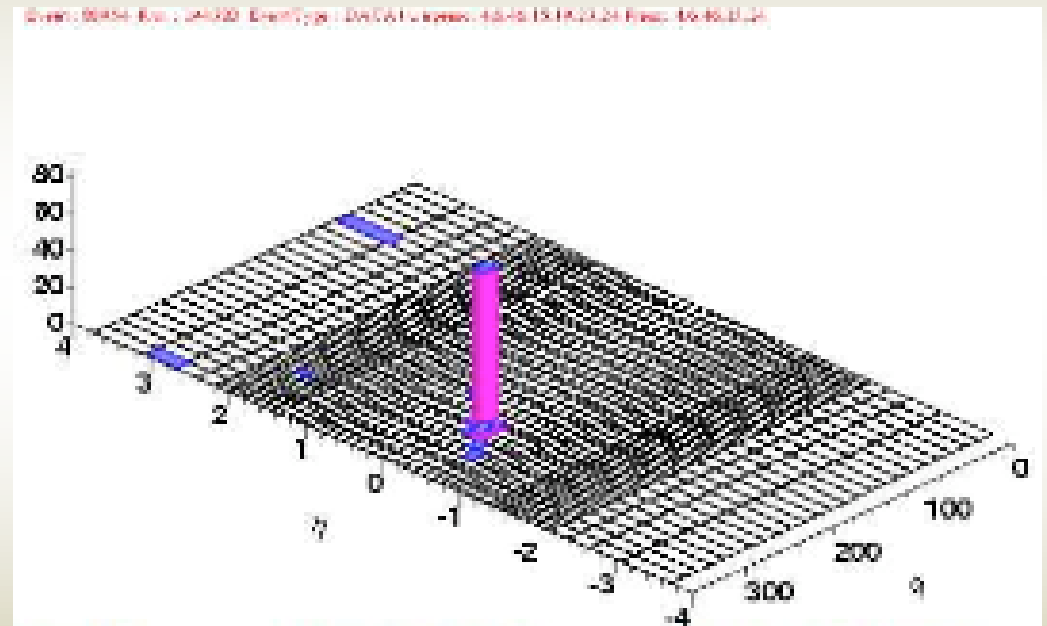
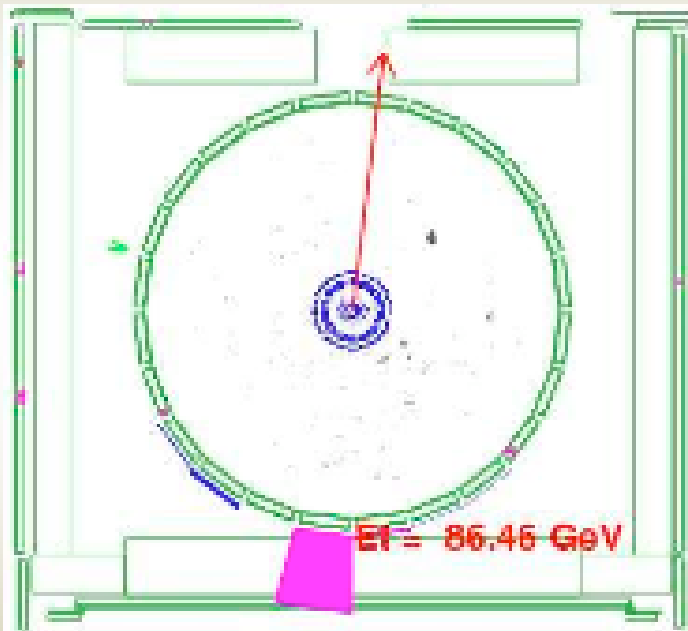
Remove events with either positive or negative energy resulting from beam splash ($|E_T| > 10$ GeV)



Two jets plus \cancel{E}_T search for leptoquarks (DØ)

Cosmic-Ray Muons

- *Cosmic-ray muon bremsstrahlung contributes to \cancel{E}_T*
 - Predominantly single-photon and single-jet events

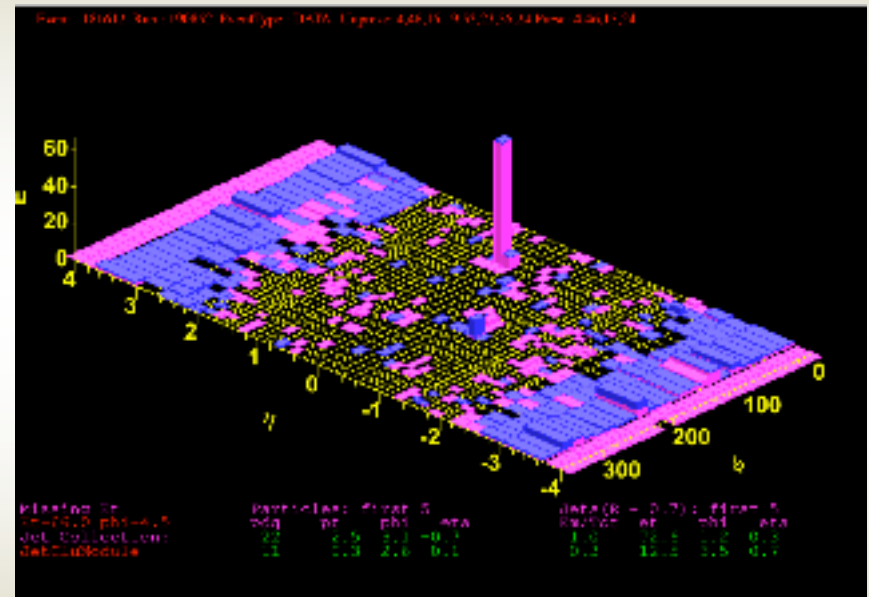
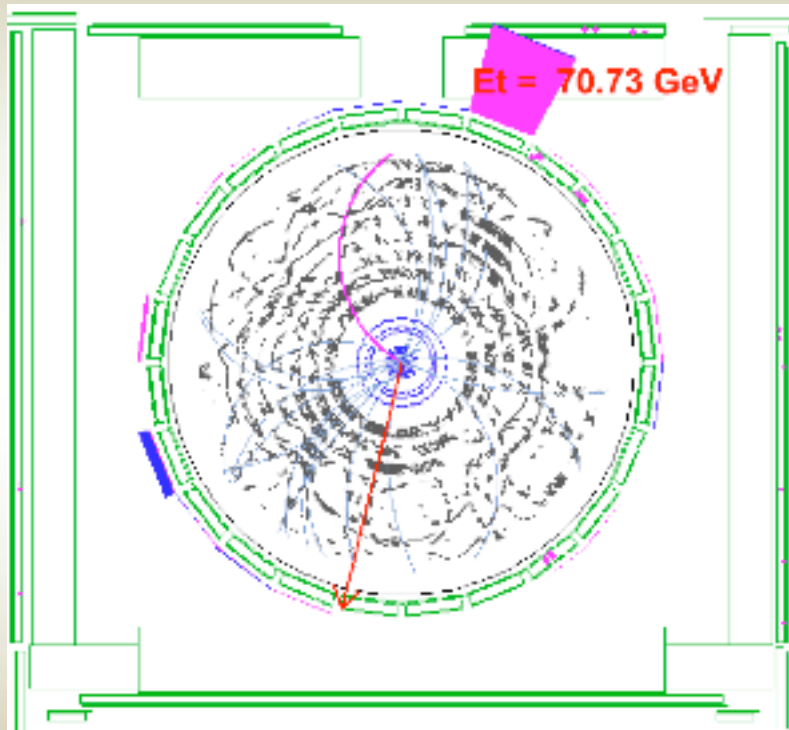


Remove events with fewer than 3 central tracks

Photon plus \cancel{E}_T search for large extra dimensions (CDF)

Cosmic-Ray Muons

- *Cosmic-ray muons can overlap collision events*

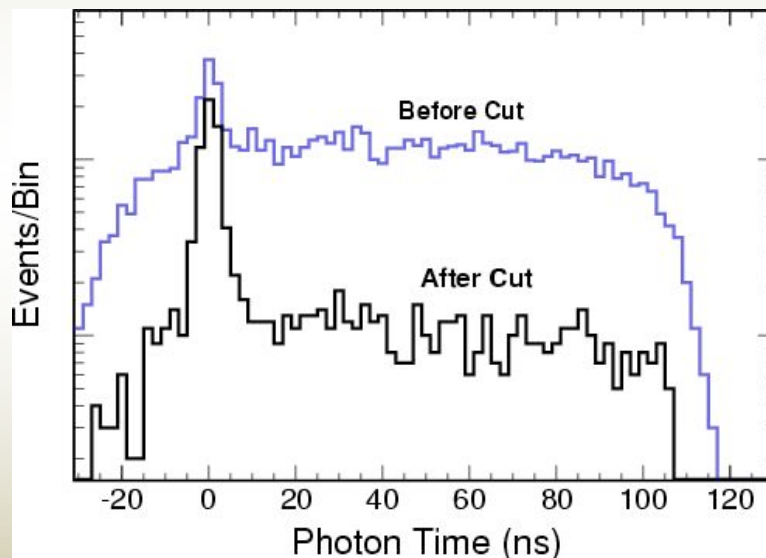


Use EM timing system to remove cosmic overlaps with collisions

Photon plus \cancel{E}_T search for large extra dimensions (CDF)

Cosmic-Ray Muons

- *Large residual background of cosmic-ray muons overlapping collision events*
 - Create discriminant using:
 - Track stubs in muon chamber in the same direction as photon candidate
 - Energy in hadronic calorimeter and in strip chamber at nominal shower maximum



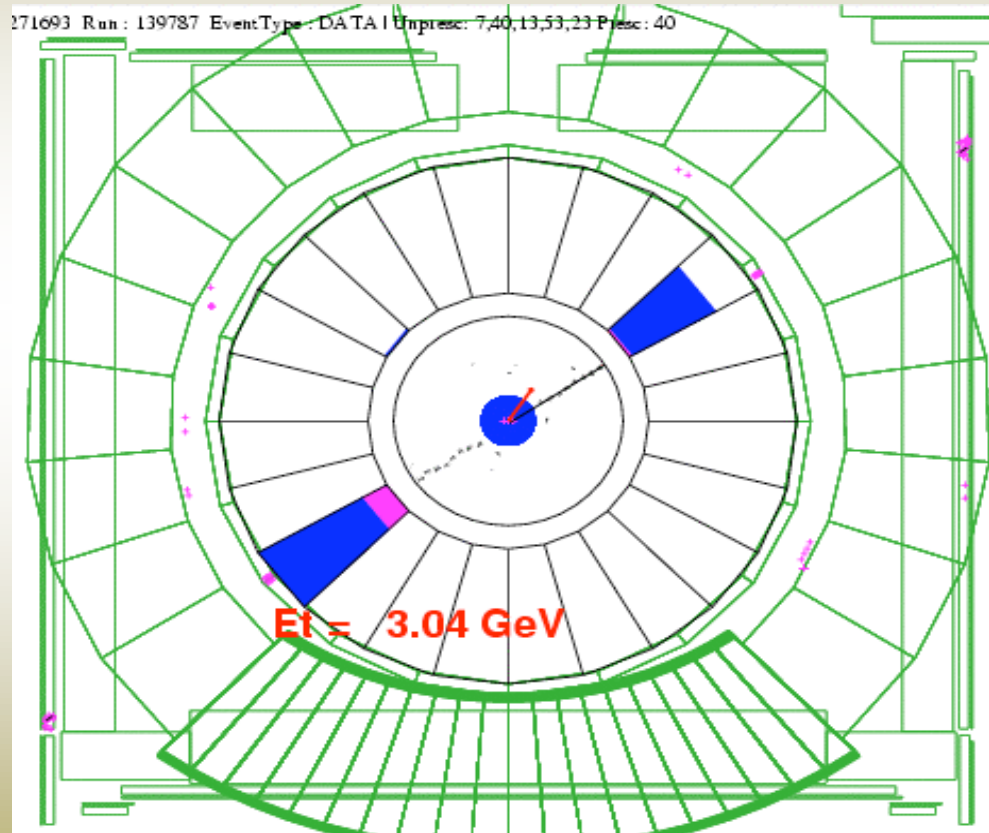
Photon plus \cancel{E}_T search for large extra dimensions (CDF)

- *Cosmics can also produce jets if bremsstrahlung is in hadronic calorimeter*
 - Remove by requiring jets to have EM fraction between 0.1 and 0.95

Two jets plus \cancel{E}_T search for leptoquarks (DØ)

Cosmic-Ray Muons

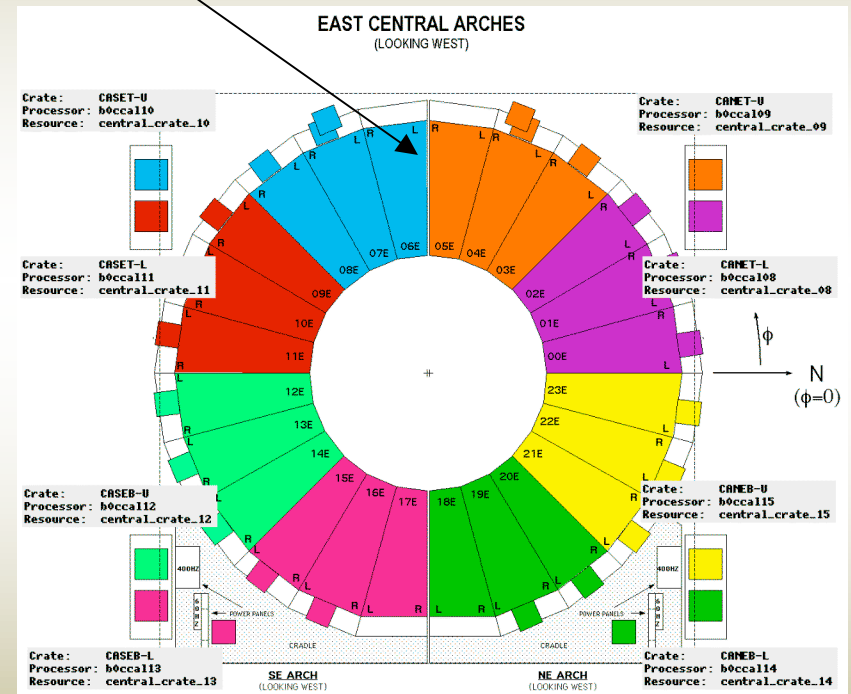
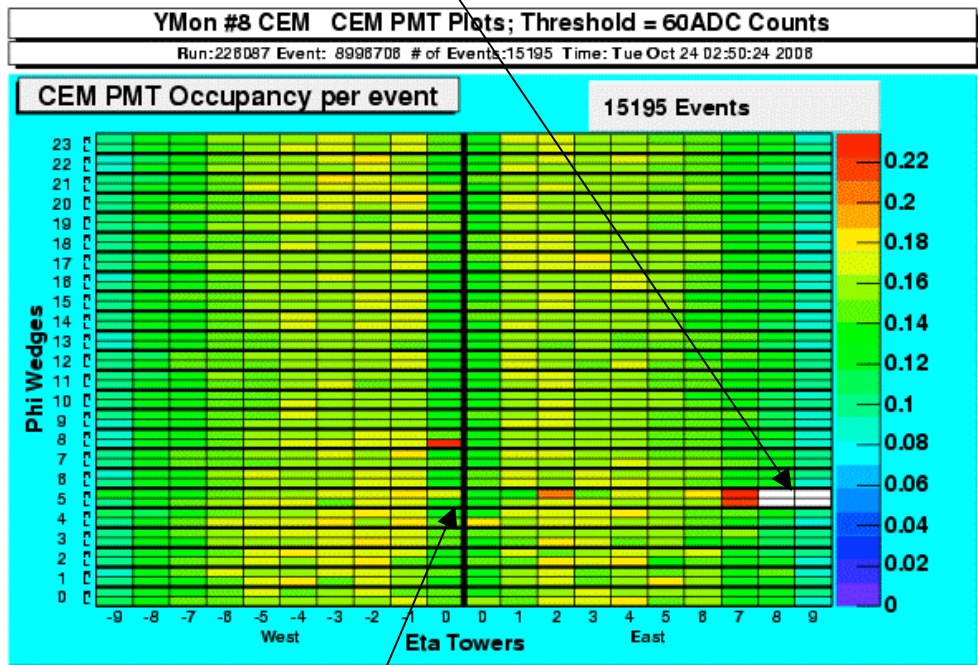
- *A cosmic-ray muon reconstructed on only one side of detector results in \cancel{E}_T*
 - Search for muon track opposite to reconstructed muon



All final states with muons (CDF)

Lost Particles in Jets

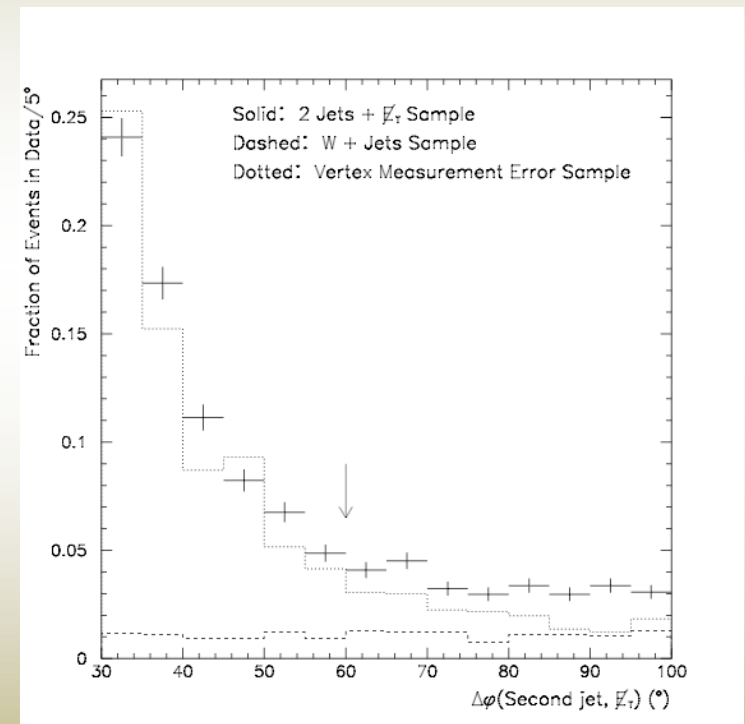
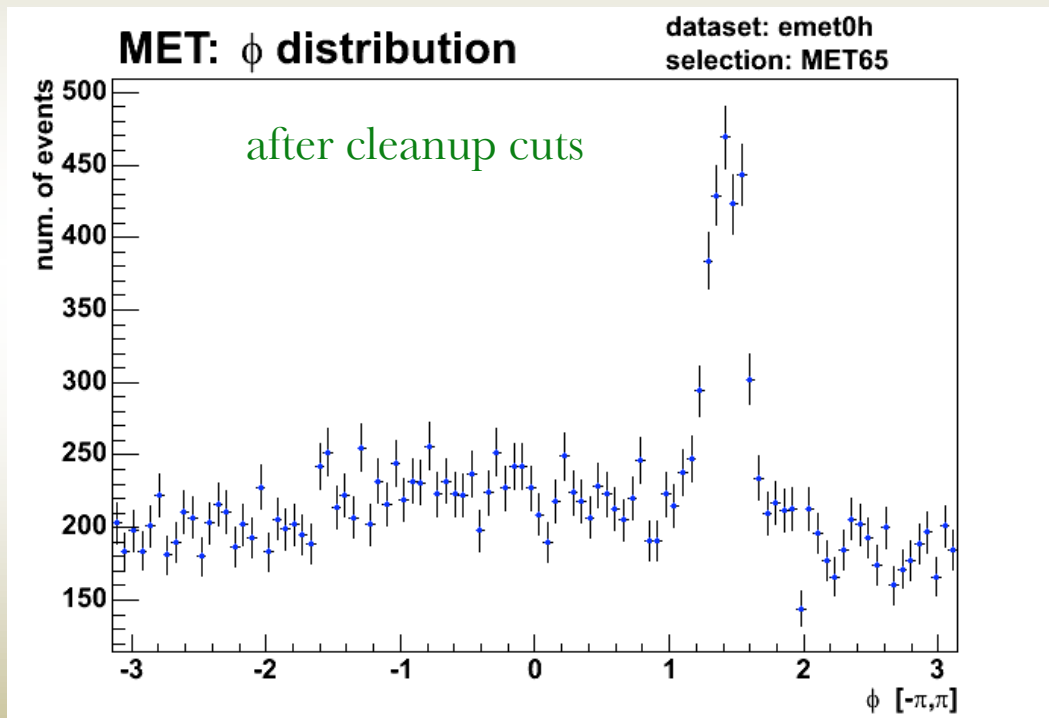
- *Detector cracks a significant source of \cancel{E}_T*
 - CDF: “Chimney” for cables at top of calorimeter



- CDF: Central crack between calorimeters

Lost Particles in Jets

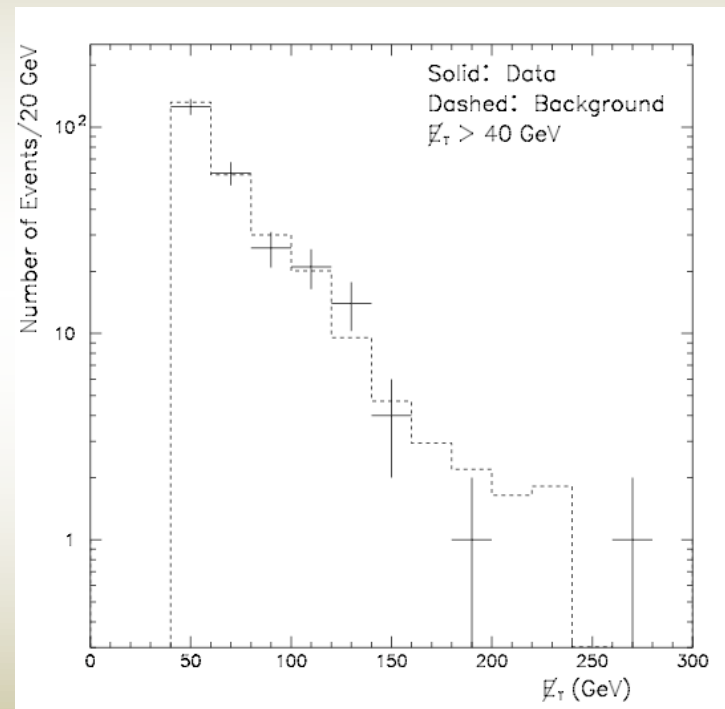
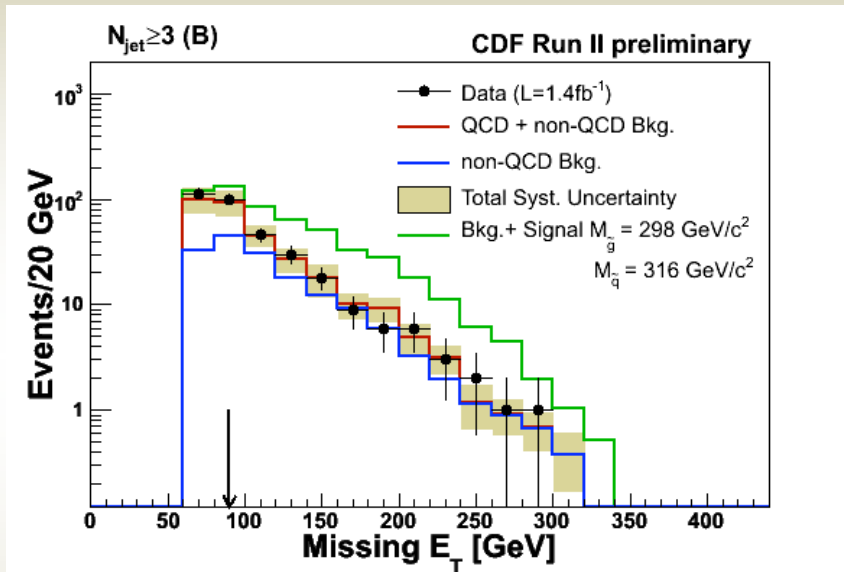
- *Chimney observable in ϕ distribution of \cancel{E}_T*
 - Reduce background by requiring separation between \cancel{E}_T and jet directions



Jets plus \cancel{E}_T final states (CDF and DØ)

Physics Results

- After removing pathological events a good description of \cancel{E}_T is achieved



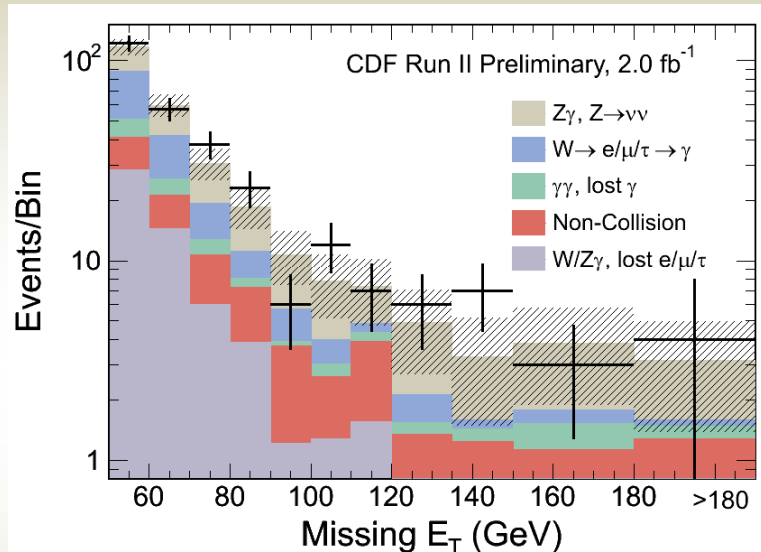
Events in 1.4 fb ⁻¹	Observed	Total + statistics + systematics
4-jets	29	27 ± 2 ± 9
3-jets(A)	616	607 ± 16 ± 146
3-jets(B)	166	154 ± 7 ± 44
3-jets(C)	22	25 ± 2 ± 8
2-jets	13	11 ± 2 ± 3

Jets plus \cancel{E}_T squark/gluino search (CDF)

Two jets plus \cancel{E}_T
leptoquark search (DØ)

Physics Results

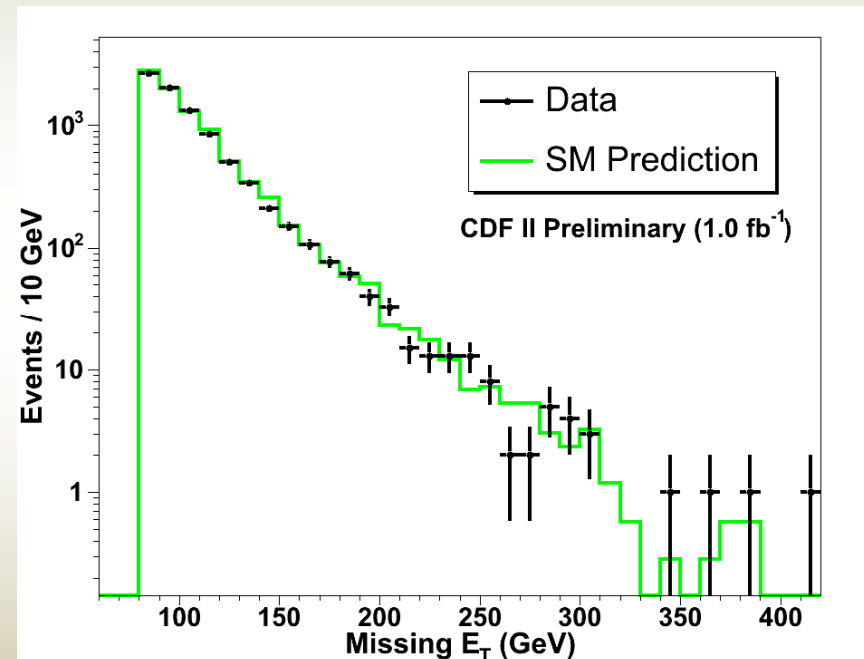
- After removing pathological events a good description of \cancel{E}_T is achieved



CDF RunII Preliminary, 2.0 fb⁻¹

Channel	$\gamma E_T > 50$ GeV	$\gamma E_T > 90$ GeV
$W \rightarrow e \rightarrow \gamma$	47.3 ± 5.1	2.6 ± 0.4
$W \rightarrow \mu/\tau \rightarrow \gamma$	19.1 ± 4.2	1.0 ± 0.2
$W\gamma \rightarrow \mu\gamma \rightarrow \gamma$	33.1 ± 10.2	1.7 ± 1.2
$W\gamma \rightarrow e\gamma \rightarrow \gamma$	8.0 ± 3.0	0.8 ± 0.7
$W\gamma \rightarrow \tau\gamma \rightarrow \gamma$	17.6 ± 1.6	2.5 ± 0.2
$\gamma\gamma \rightarrow \gamma$	18.9 ± 2.3	2.3 ± 0.6
cosmics	36.4 ± 2.5	9.8 ± 1.3
$Z\gamma \rightarrow \nu\nu\gamma$	84.4 ± 8.0	20.9 ± 2.0
Total	264.8 ± 14.8	42.4 ± 2.9
Data	280	40

One photon
plus \cancel{E}_T
large extra
dimensions
search (CDF)



One jet plus \cancel{E}_T
large extra dimensions search
(CDF)

Modelling Momentum Imbalance

- *Given understanding of pathologies, \cancel{E}_T can be modelled by understanding scale and resolution of collision products*

$$\sum_i \vec{p}_i + \overrightarrow{\text{uncl}} + \vec{p} = \vec{0}$$

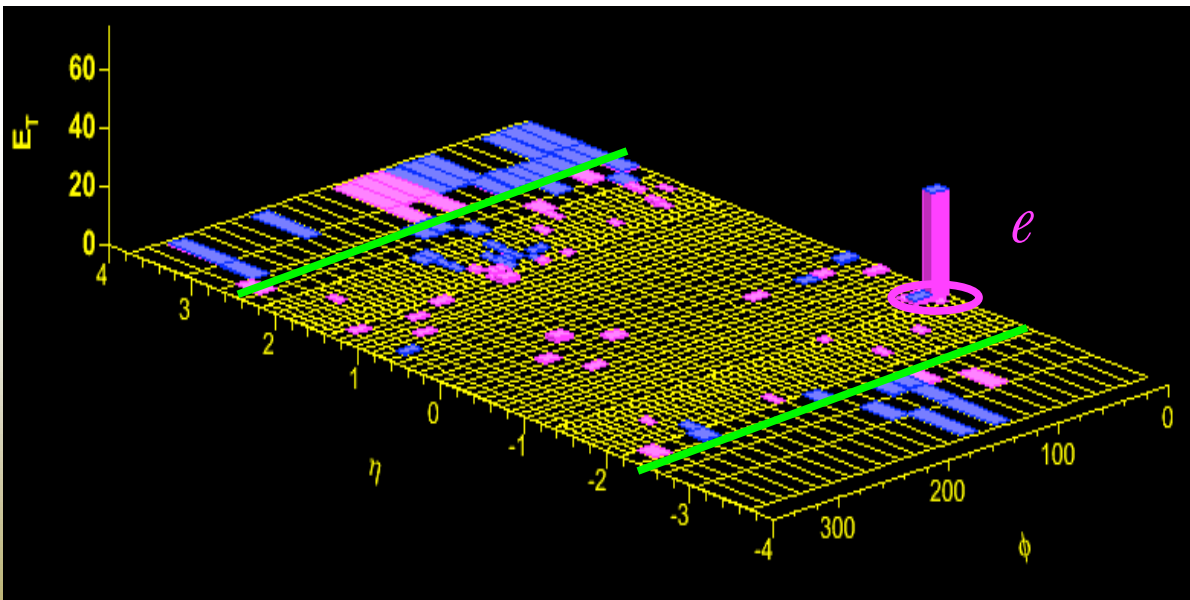
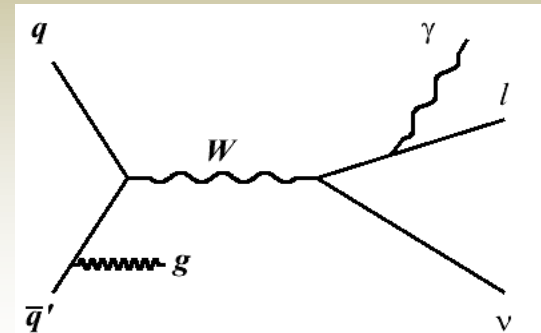
muons
electrons & photons
taus
jets

underlying event
extra interactions

- *Approaches to modelling \cancel{E}_T*
 - **Data-based** 2 jets + \cancel{E}_T search (DØ), 2 photons + \cancel{E}_T search (CDF)
 - **Fast simulation tuned to data** W mass measurement (CDF & DØ)
 - **Full GEANT simulation tuned to data** Jets + \cancel{E}_T search (CDF)

Case Study: CDF Run II W Mass Measurement

- \cancel{E}_T calibrated to 0.1% accuracy
 - Procedure:
 - **Calibrate electrons and muons**
 - **Define unclustered energy measurement**
 - **Calibrate unclustered energy**

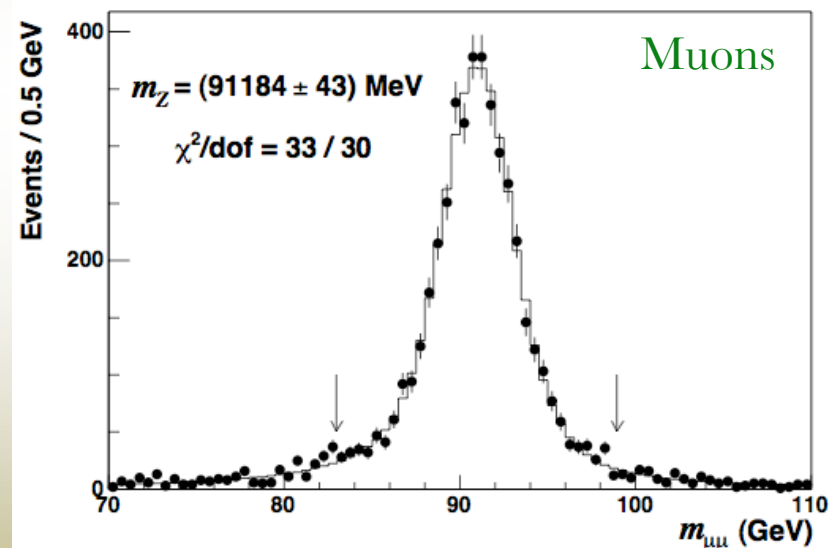
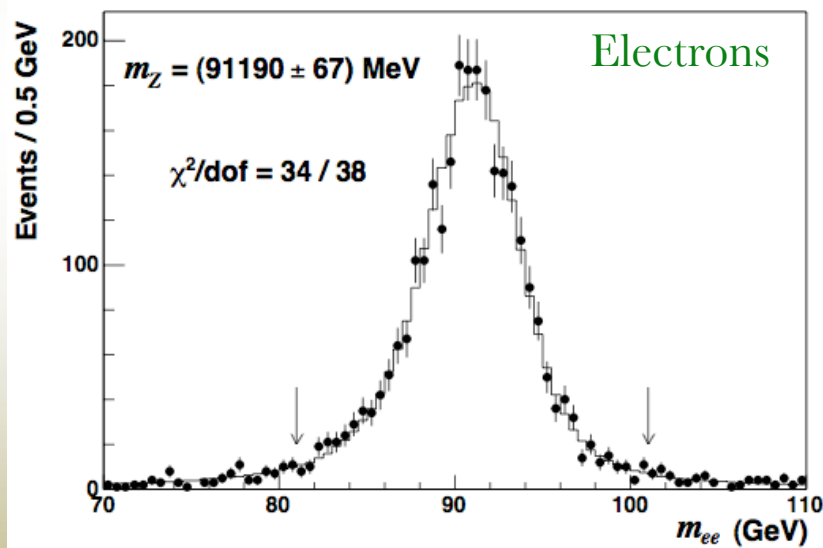


$$\vec{\cancel{p}}_T = -(\vec{p}_T^l + \vec{u}_T)$$

unclustered energy:
“recoil”

Electron and Muon Calibration

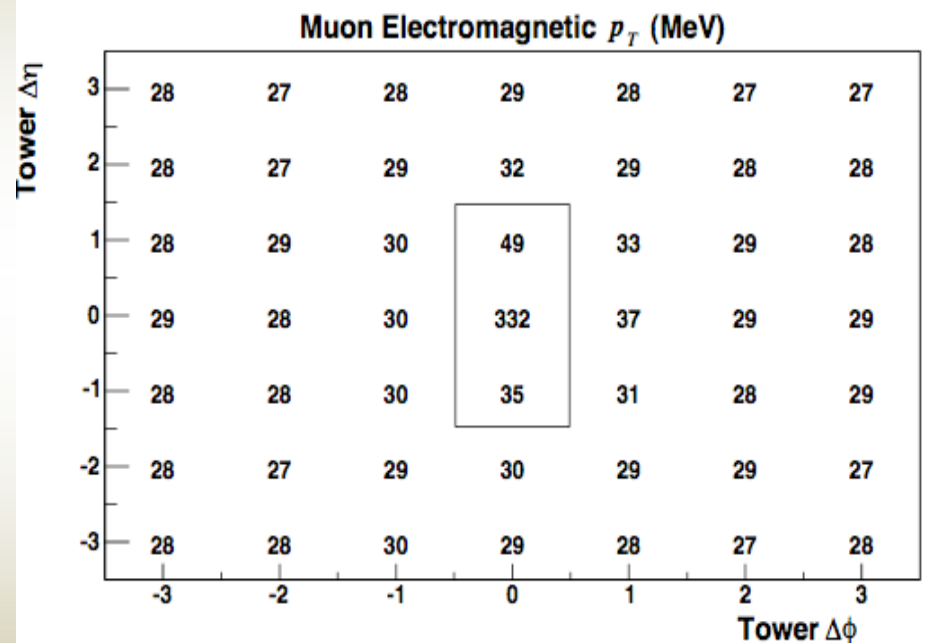
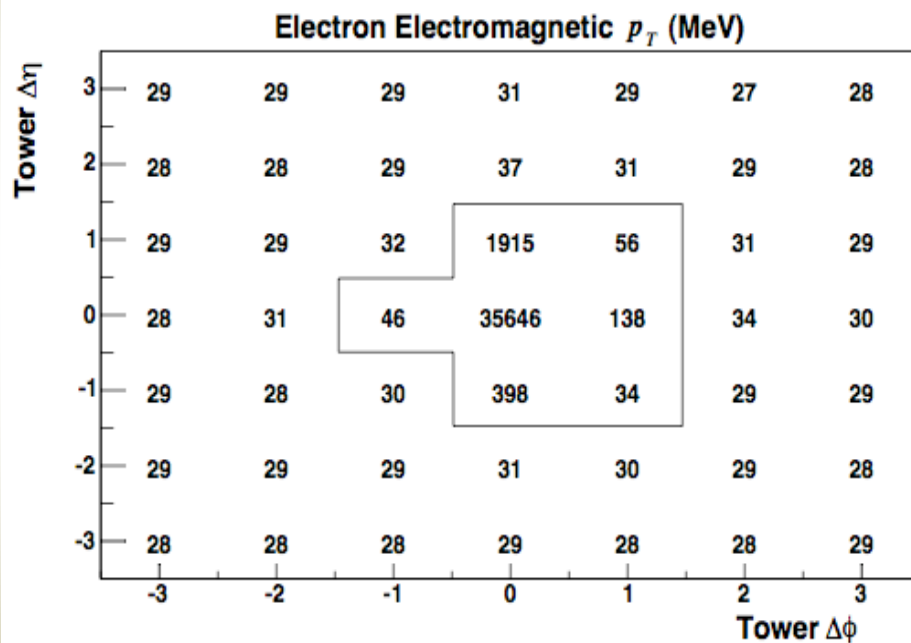
- *Calibrate electron and muon momenta using masses of well-known resonances and ratio of calorimeter to tracker measurements*
- *Z mass measurement validates the calibration*



$$m_Z^{PDG} = 91188 \text{ MeV}$$

Electron and Muon Removal

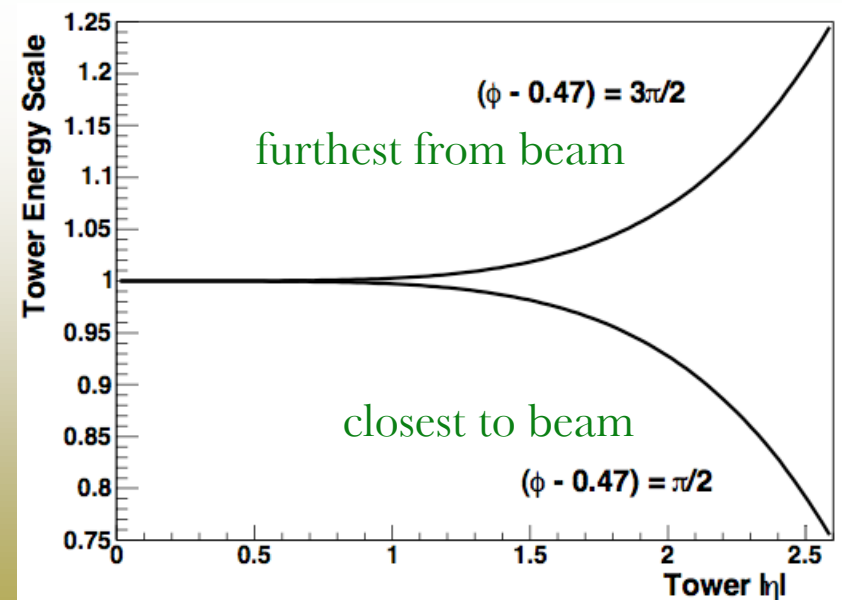
- *Remove calorimeter towers with energy from electron or muon*



Need to simulate underlying event energy removed from towers

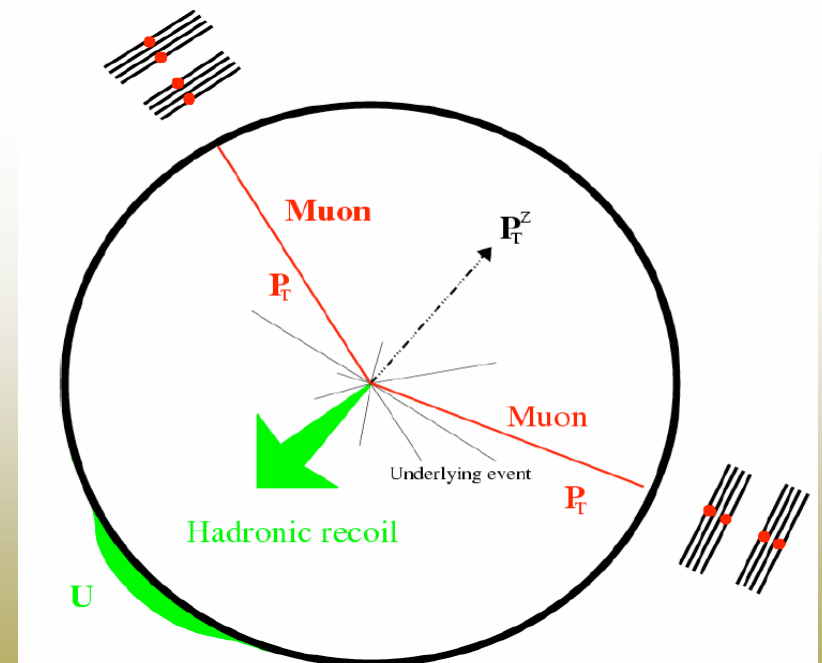
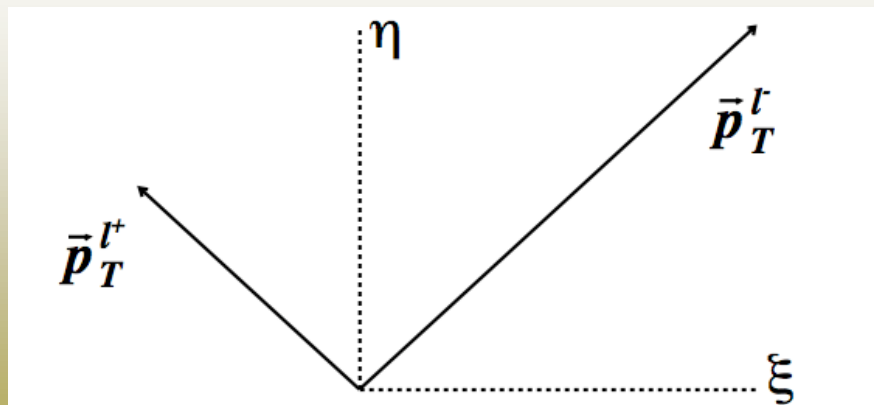
Unclustered Energy Measurement

- *Apply large (5 GeV) threshold to calorimeter towers closest to beam*
 - Reduces bias from beam splash and low-momentum central particles
 - Maintains measurement of high-energy jets
- *Apply 12% relative scale between central and forward calorimeter towers*
 - Determined by comparing calorimeter and tracker measurements for isolated charged pions
 - Improves resolution of unclustered energy measurement
- *Correct measured energy for acceptance variations from beam radial offset*
 - Towers closest to beam have highest acceptance: scale down measured energy



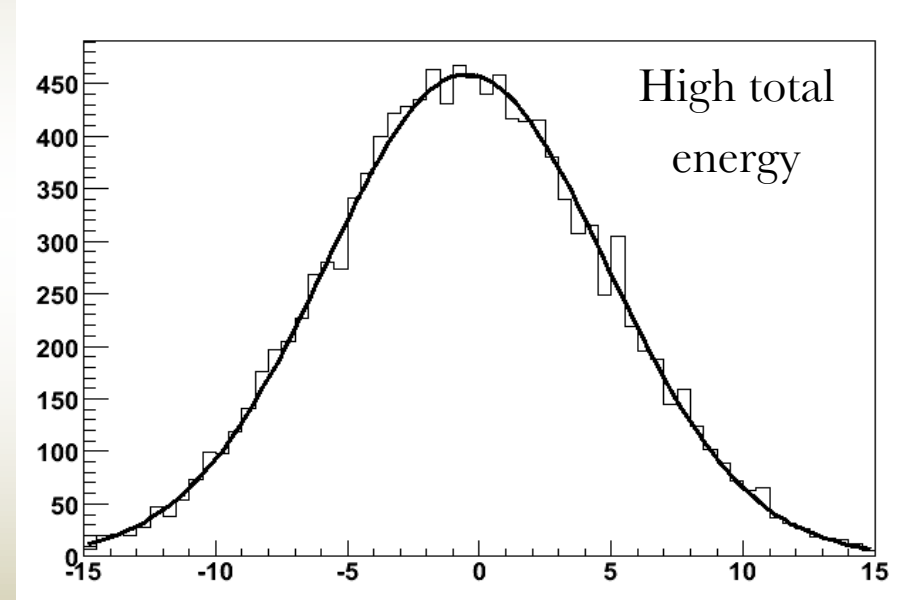
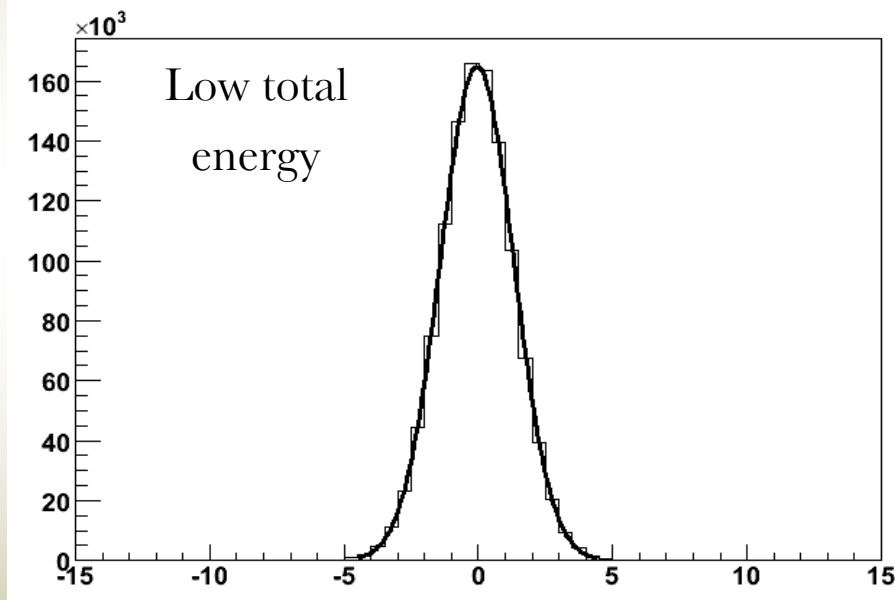
Unclustered Energy Calibration

- *Recoil model components*
 - Radiation in production of W boson
 - Radiation from “spectator” partons (underlying event) and additional $p\bar{p}$ collisions
- *Calibrate radiation and measurement with events where all particles are observable*
 - Generic inelastic $p\bar{p}$ collisions
 - Z boson decays to charged leptons
 - Define coordinate system (η, ξ) such that net radiation lies along $-\eta$ direction



Underlying Event Energy Calibration

- *Underlying event and additional interactions*
 - Resolution depends on energy in calorimeter

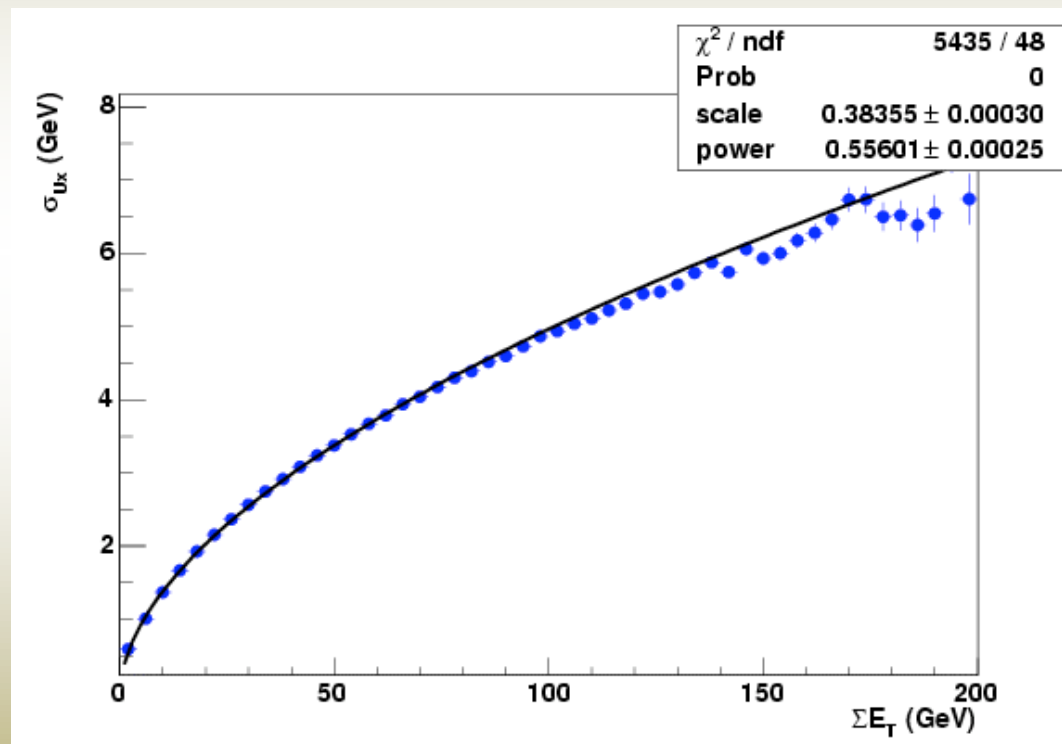


Net energy in x -direction (GeV)

Underlying event resolution gaussian for a given ΣE_T

Underlying Event Energy Calibration

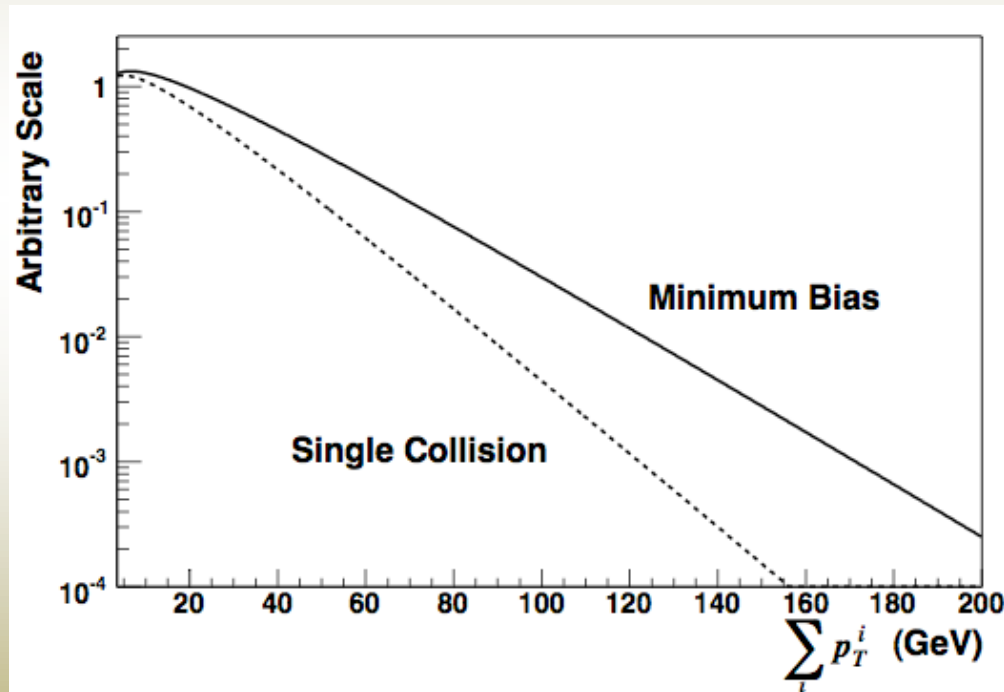
- *Calorimeter samples energy deposited by particle showers*
 - Statistical fluctuations on the number of sampled particles result in $\sqrt{\Sigma E_T}$ dependence to resolution



Fit to function $\sigma = \text{scale } \Sigma E_T^{\text{power}}$

Underlying Event Energy Calibration

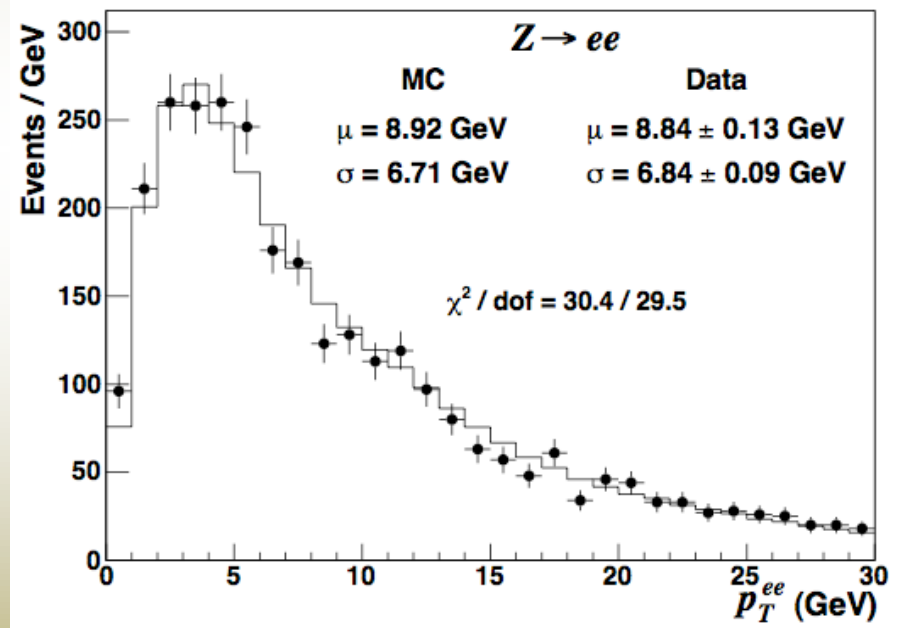
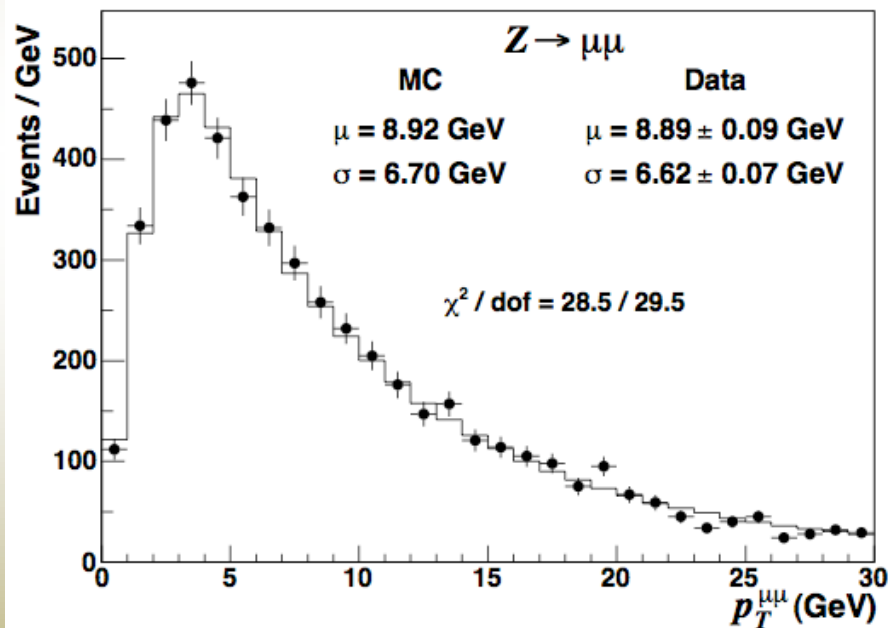
- *Model underlying event and additional interactions using a per-event ΣE_T distribution*
 - Take distribution from generic $\bar{p}p$ interactions (“minimum bias”)
 - Use expected number of interactions per $\bar{p}p$ crossing to extract a single-interaction distribution



Scale single-collision energy according to Z data fit

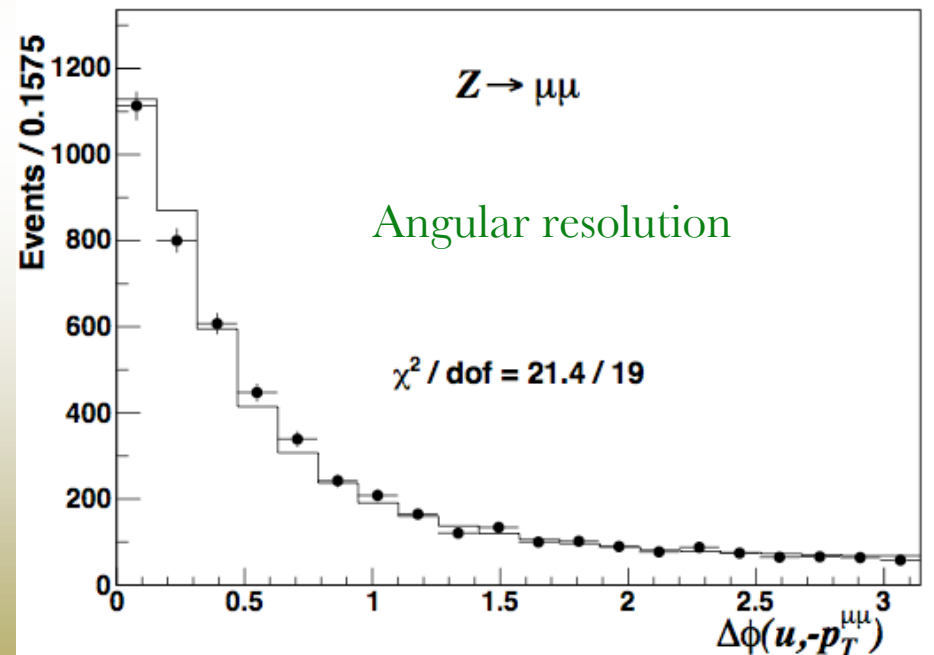
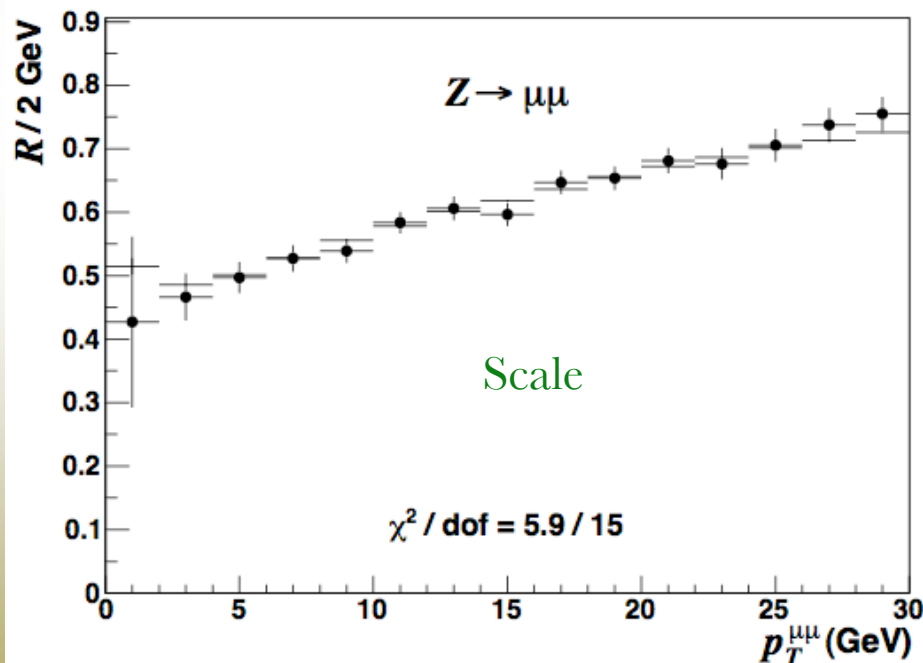
Radiated Energy Calibration

- *Net radiation in W production calibrated using Z production*
 - Small theoretical correction due to difference between W and Z masses



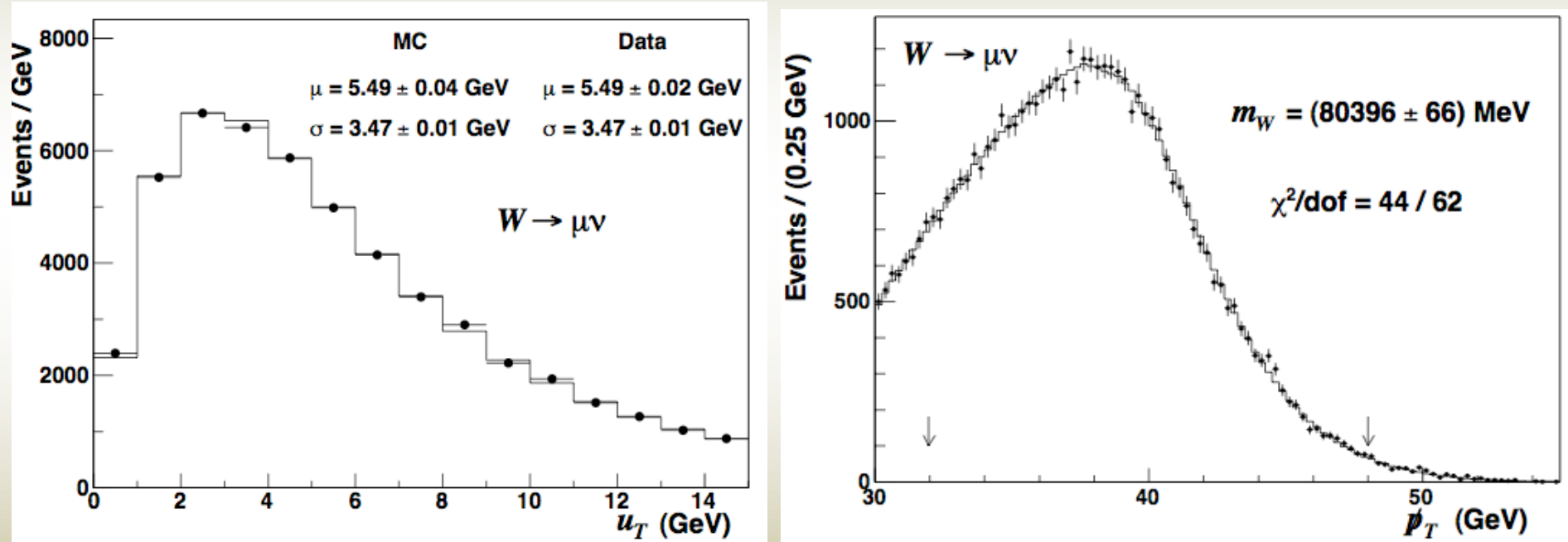
Radiated Energy Calibration

- *Fraction of measured radiation (“scale”) and resolution calibrated using Z data*
 - Scale has logarithmic dependence on radiated energy
 - Resolution has quadratic dependence on radiated energy
 - Apply angular resolution to radiated momentum



Results

- *Net radiation in W events well modelled*
- *Missing momentum fit gives 0.1% accuracy on m_W*



Missing momentum fit in muon channel:

45 MeV systematic uncertainty

80 MeV total uncertainty

Summary

- *Missing transverse energy a part of many discovery and measurement signatures*
- *Two aspects to understanding missing momentum:*
 - **Determine and reduce pathologies**
 - **Model residual pathological events with data using discriminating variables**
 - **Calibrate detector response to high- p_T particles and unclustered energy**
 - **Results can be used in tuned fast simulation or full GEANT simulation**
- *Expect new challenges with the new collider and detectors at the LHC!*