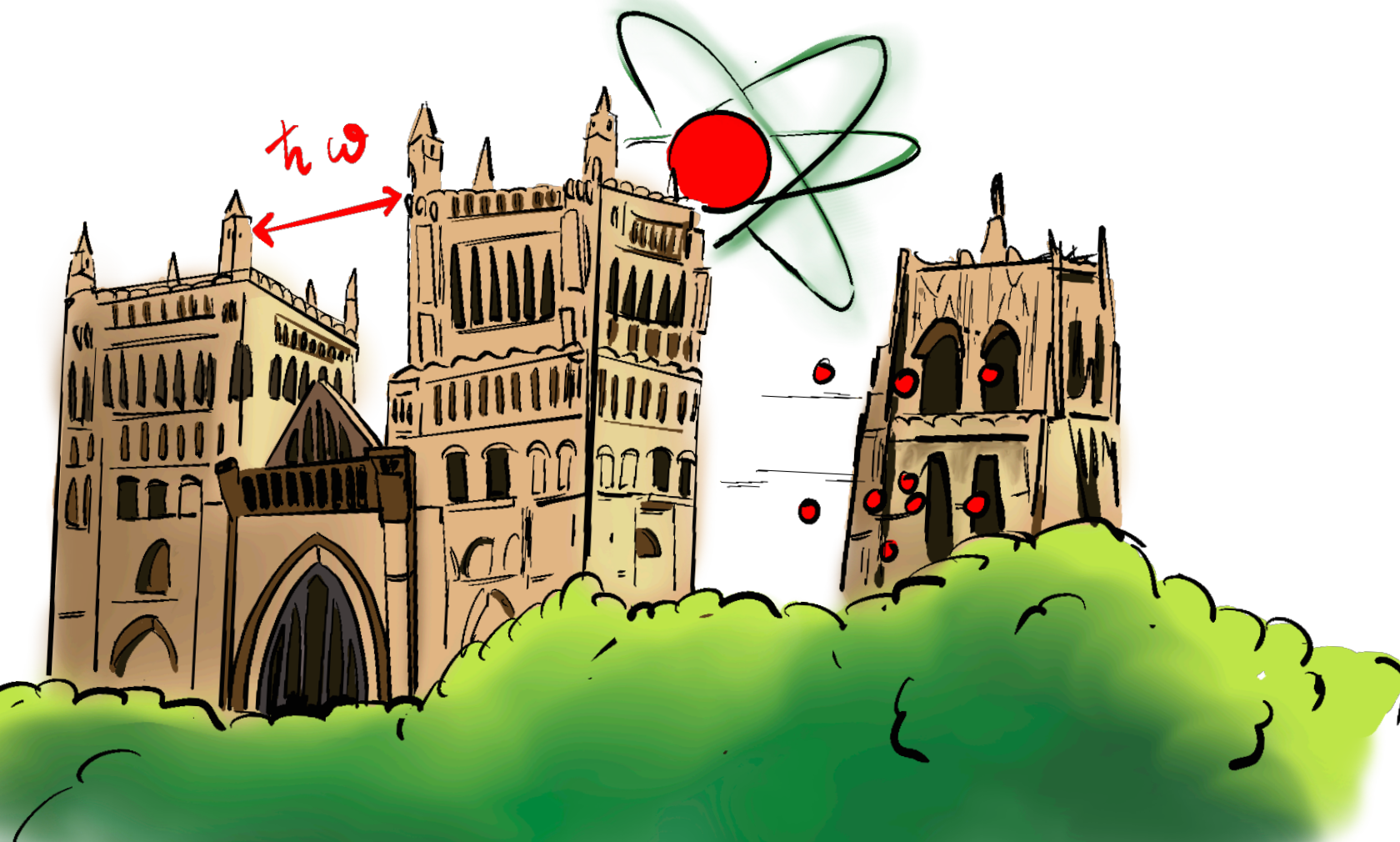


12th Desember 2023
Annual Theory Meeting
Durham

Quantum Sensing

Clara Murgui (UAB/IFAE)



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UAB
Universitat Autònoma
de Barcelona

IFAE
Institut de Física
d'Altes Energies

Quantum Sensing

“Use of a quantum system, quantum properties or quantum phenomena to perform a measurement of a physical quantity”

[Degen, Reinhard, Cappellaro, 2017]

Quantum Sensing: classification

“Use of a quantum system, quantum properties or quantum phenomena to perform a measurement of a physical quantity”

[Degen, Reinhard, Cappellaro, 2017]

1 Quantum object

2 Quantum coherence

3 Quantum entanglement

Quantum Sensing: requirements

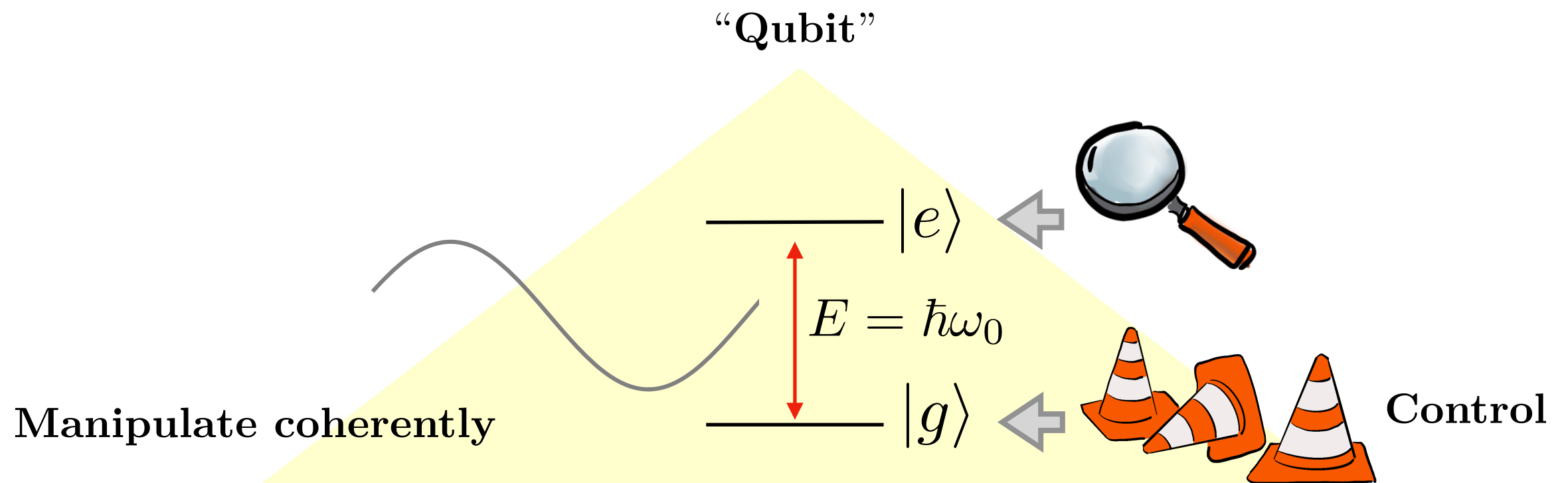
“Use of a quantum system, quantum properties or quantum phenomena to perform a measurement of a physical quantity”

[Degen, Reinhard, Cappellaro, 2017]

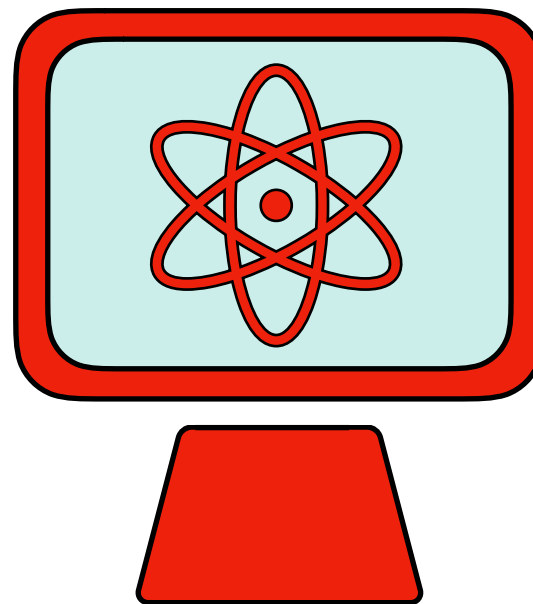
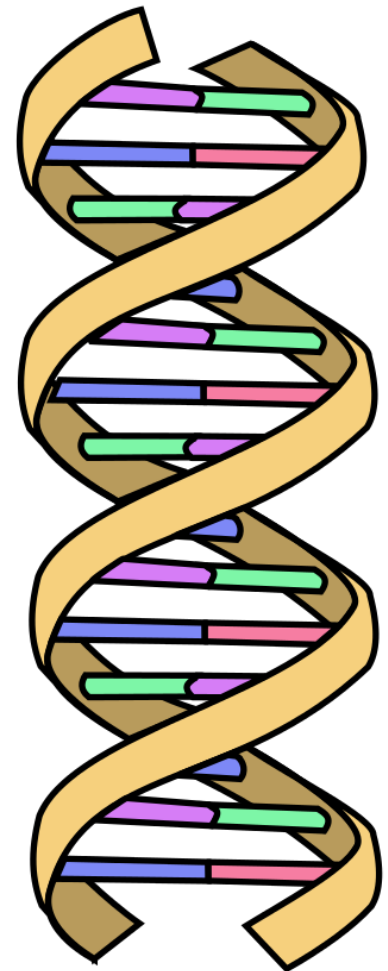
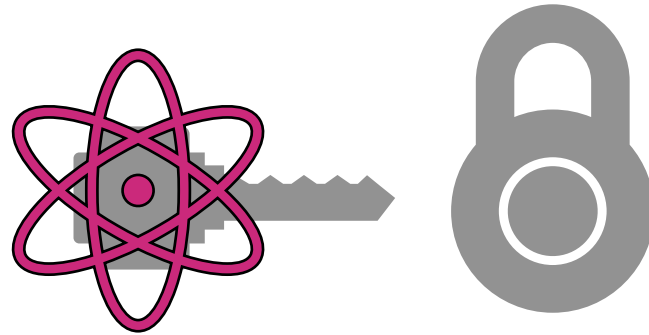
1 Quantum object

2 Quantum coherence

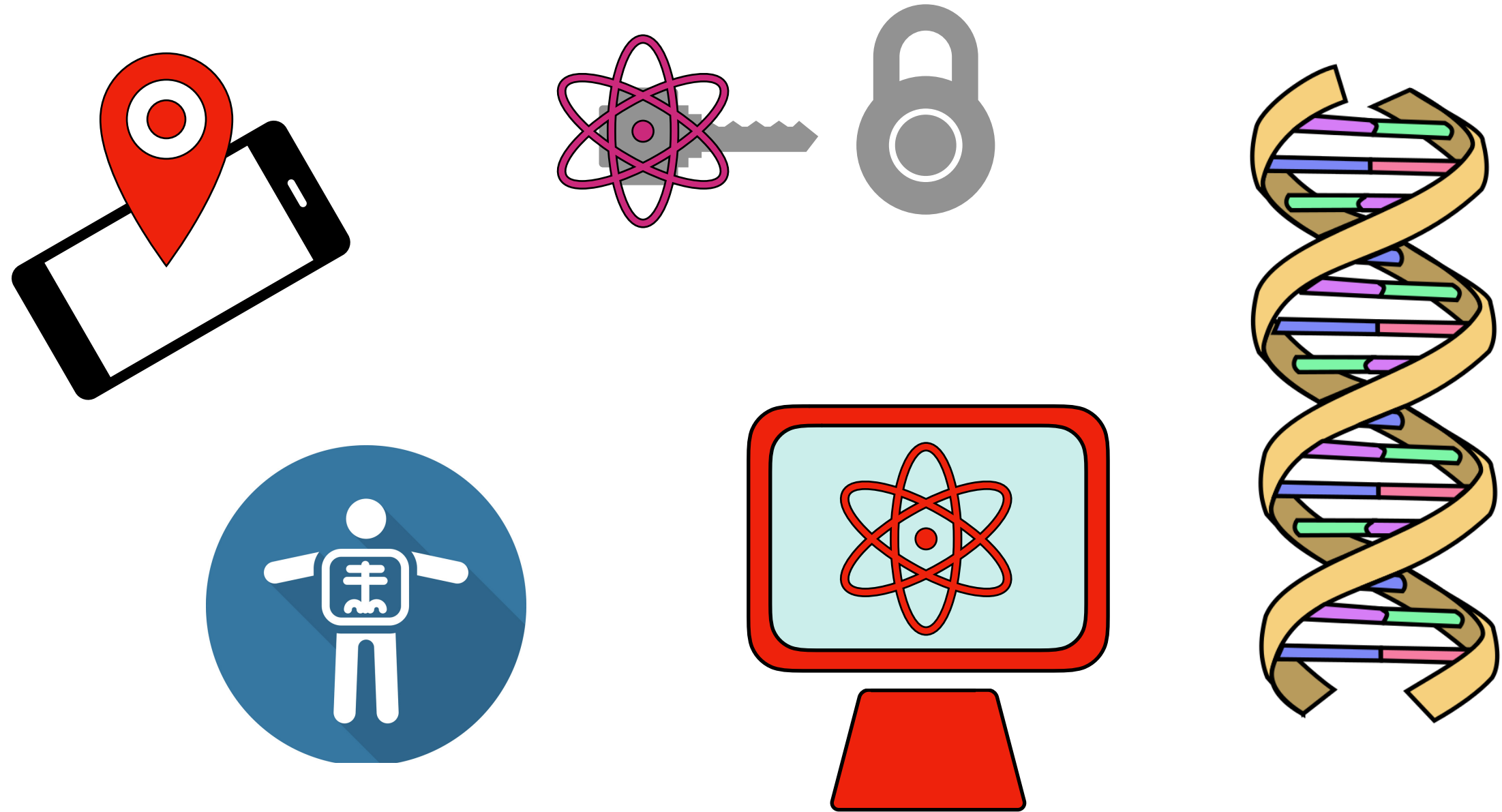
3 Quantum entanglement



Quantum Sensing: applications

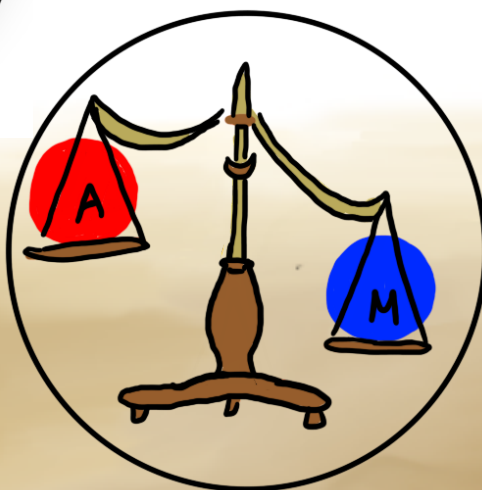
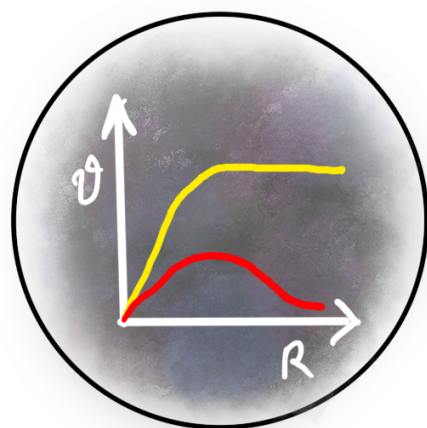
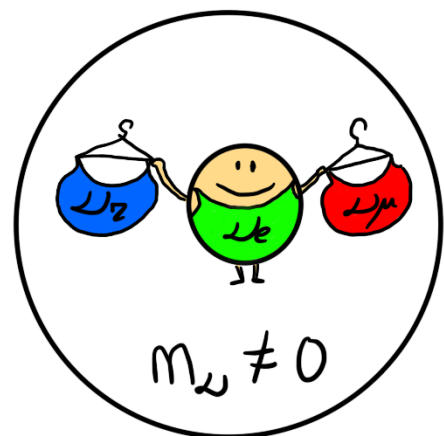


Quantum Sensing: applications

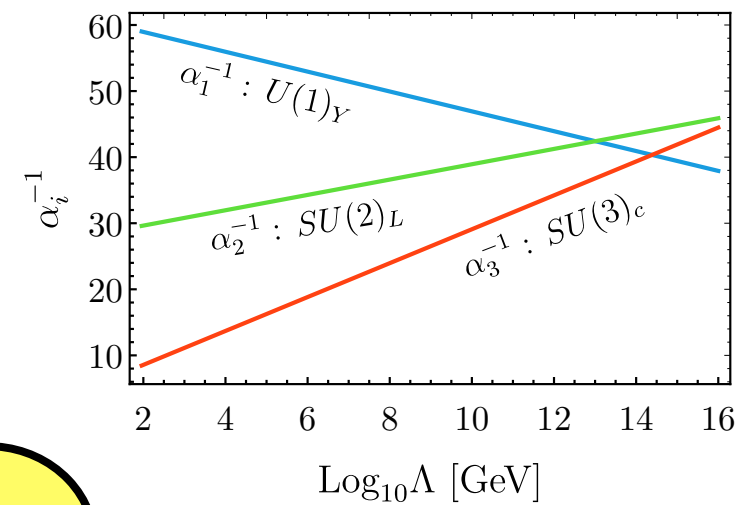
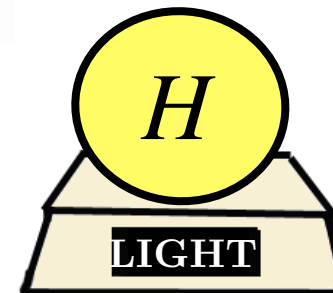
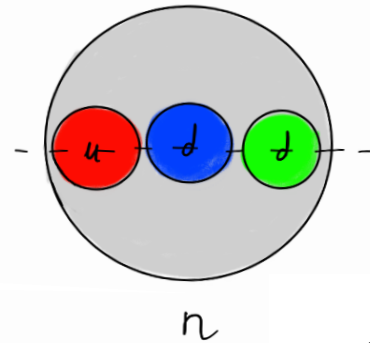
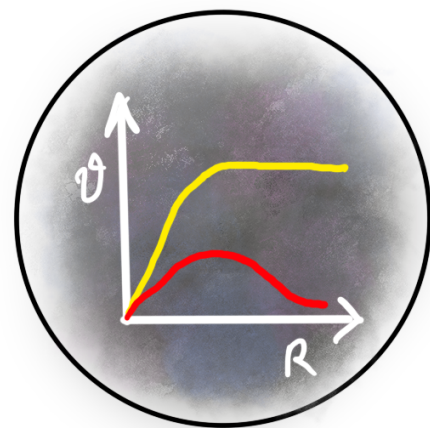
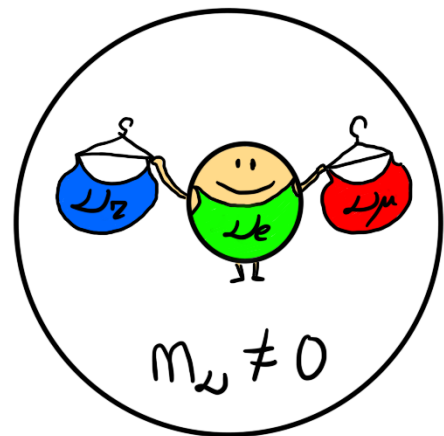


“Why a phenomenologist is given me this talk?”

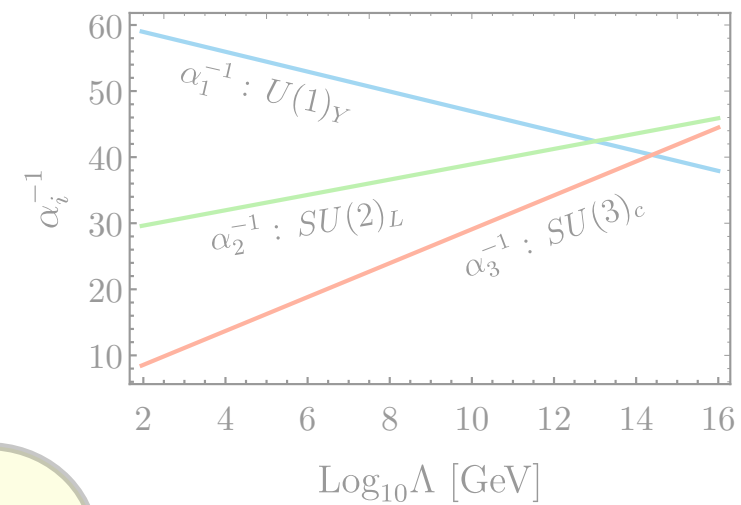
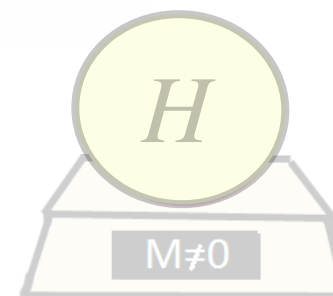
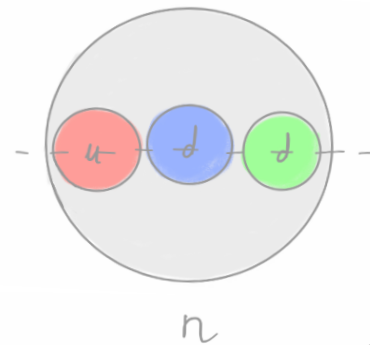
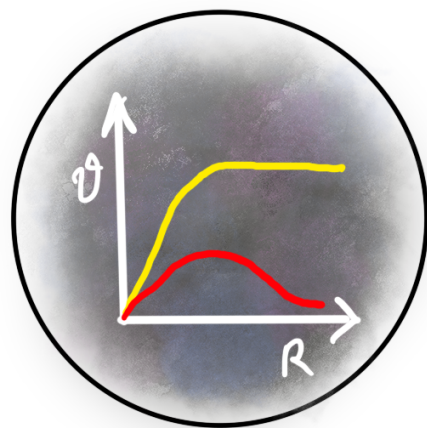
The Need for New Physics



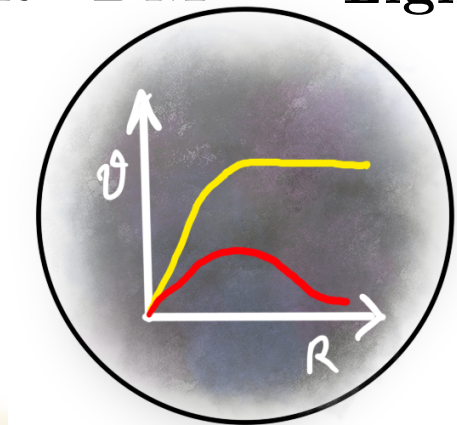
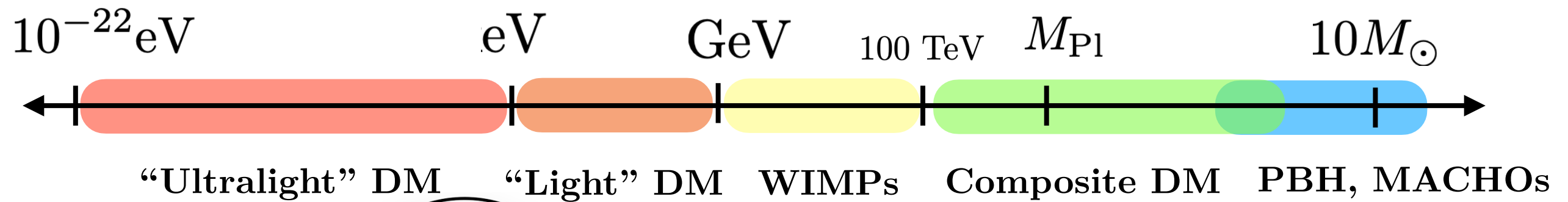
The Need for New Physics



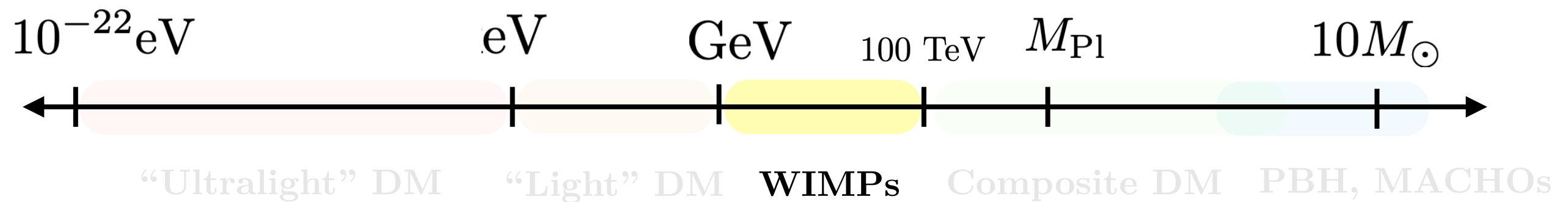
The Need for New Physics



Beyond the SM: where to look?



Dark Matter: where to look?



The WIMP miracle

A Feynman diagram showing two incoming lines labeled "DM" and two outgoing lines labeled "SM" meeting at a central shaded circle, representing an interaction.

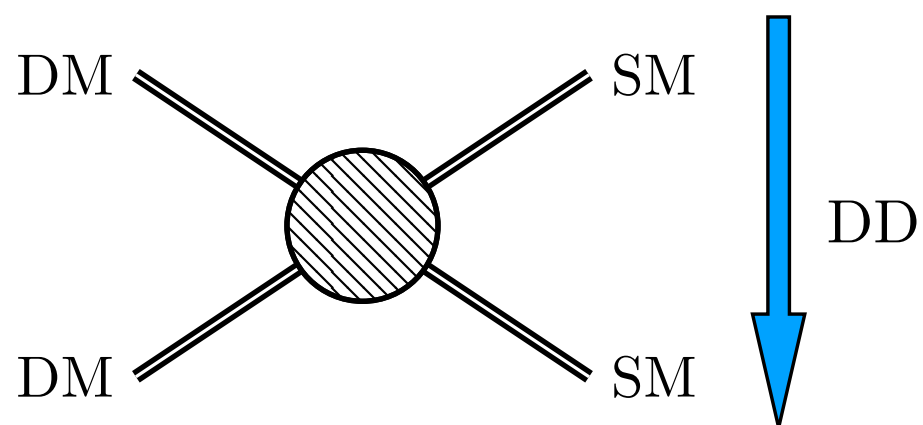
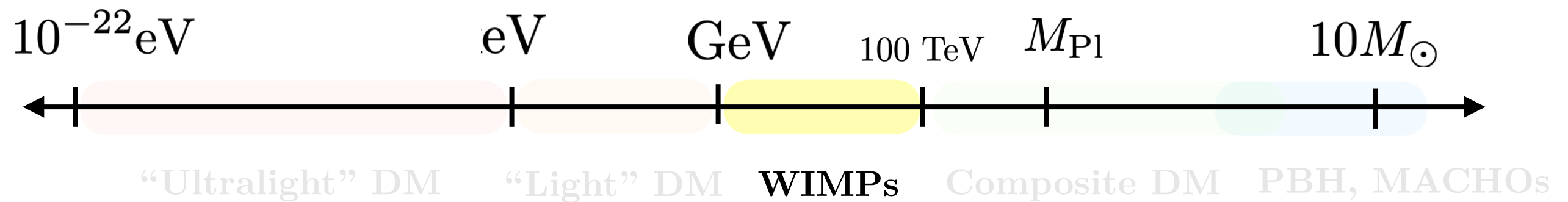
$\Rightarrow \langle \sigma v \rangle \sim \frac{G_F^2}{8\pi} m_{\chi}^2 \frac{c}{3} \sim 10^{-24} \text{ cm}^3/\text{s} \left(\frac{m_{\chi}}{100 \text{ GeV}} \right)^2$

An arrow points from the text "weak coupling" to the G_F^2 term in the equation.

Three colorful party hats with streamers and confetti.

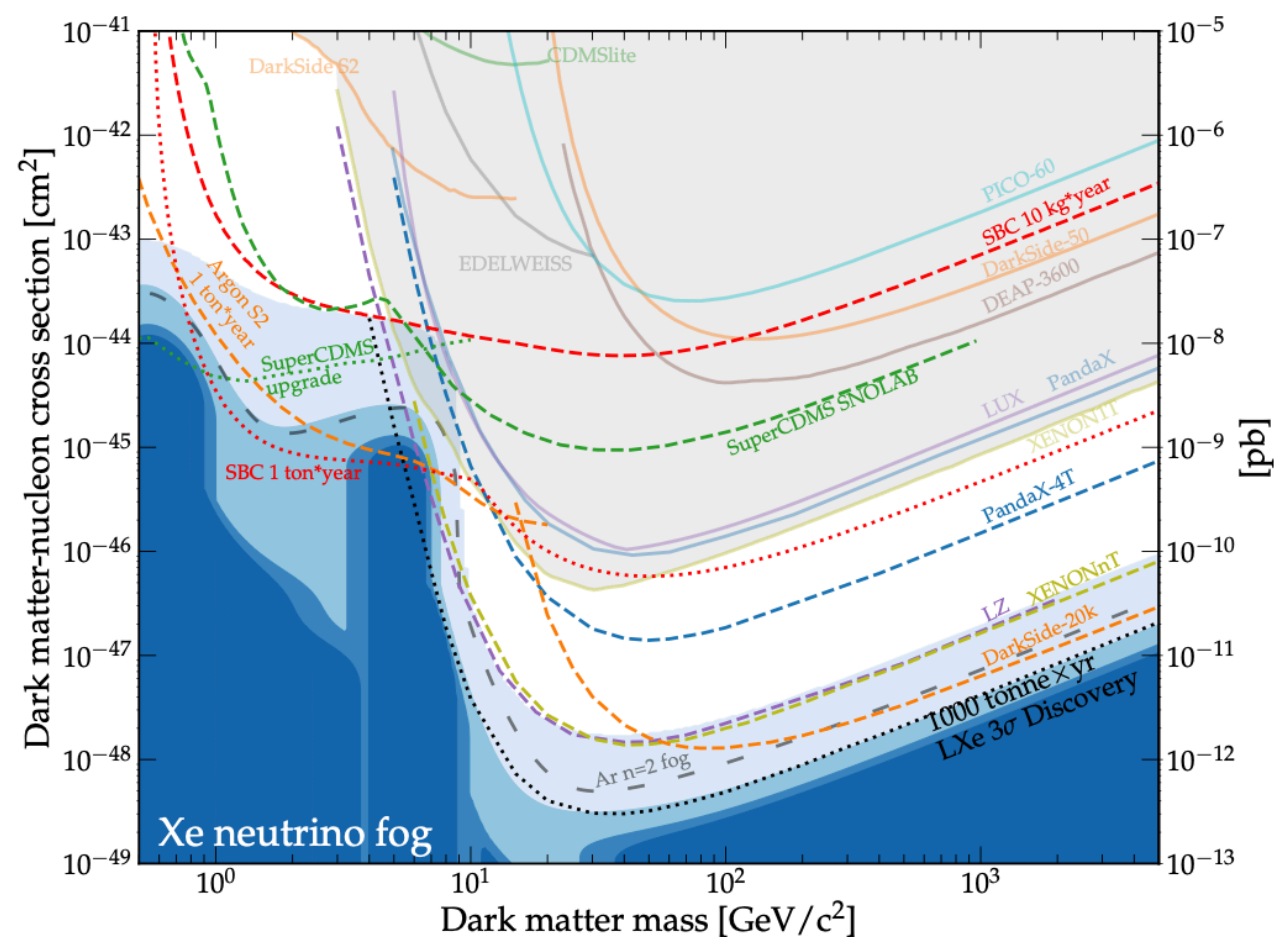
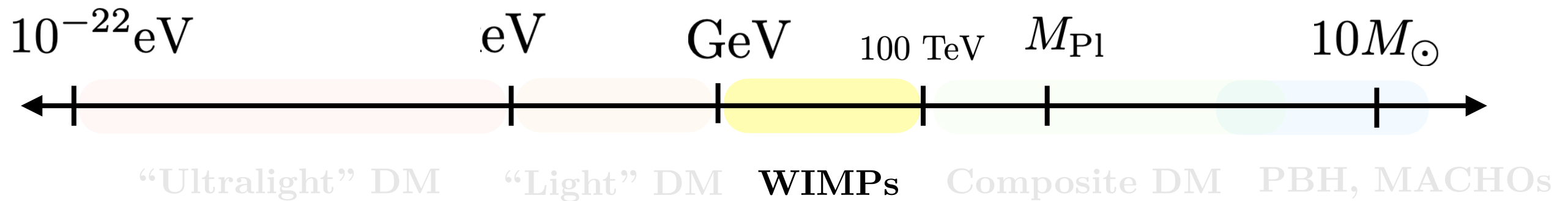
$\Omega_{\text{DM}} \sim 0.1 \times \left(\frac{3 \times 10^{-26} \text{ cm}^3/\text{s}}{\langle \sigma v \rangle} \right)$

Dark Matter: where to look?



$$\sigma \sim 10^{-34}\text{cm}^2 \left(\frac{m_{\chi}}{100\text{ GeV}} \right)^2$$

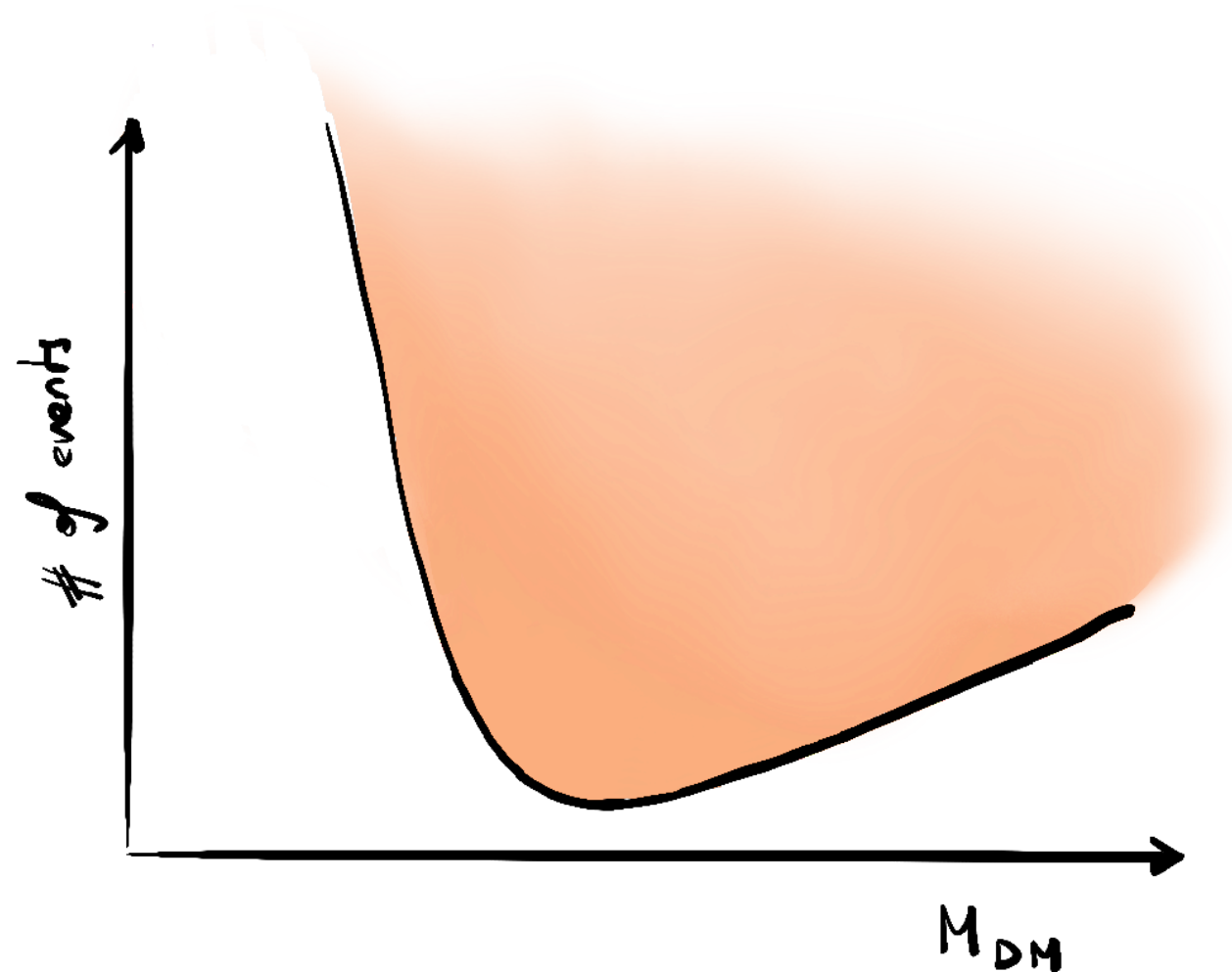
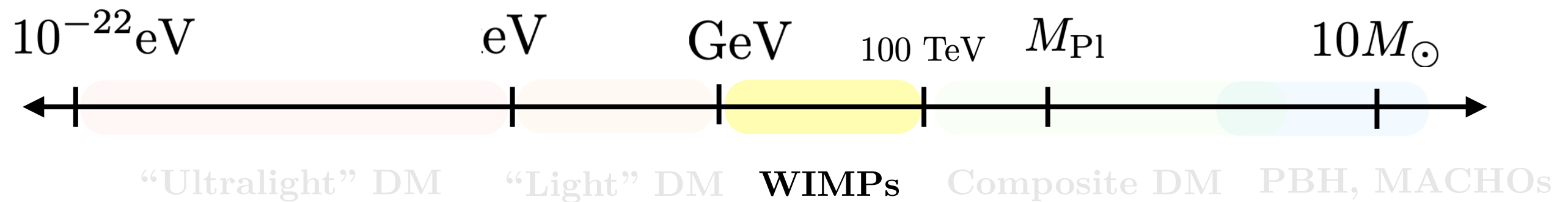
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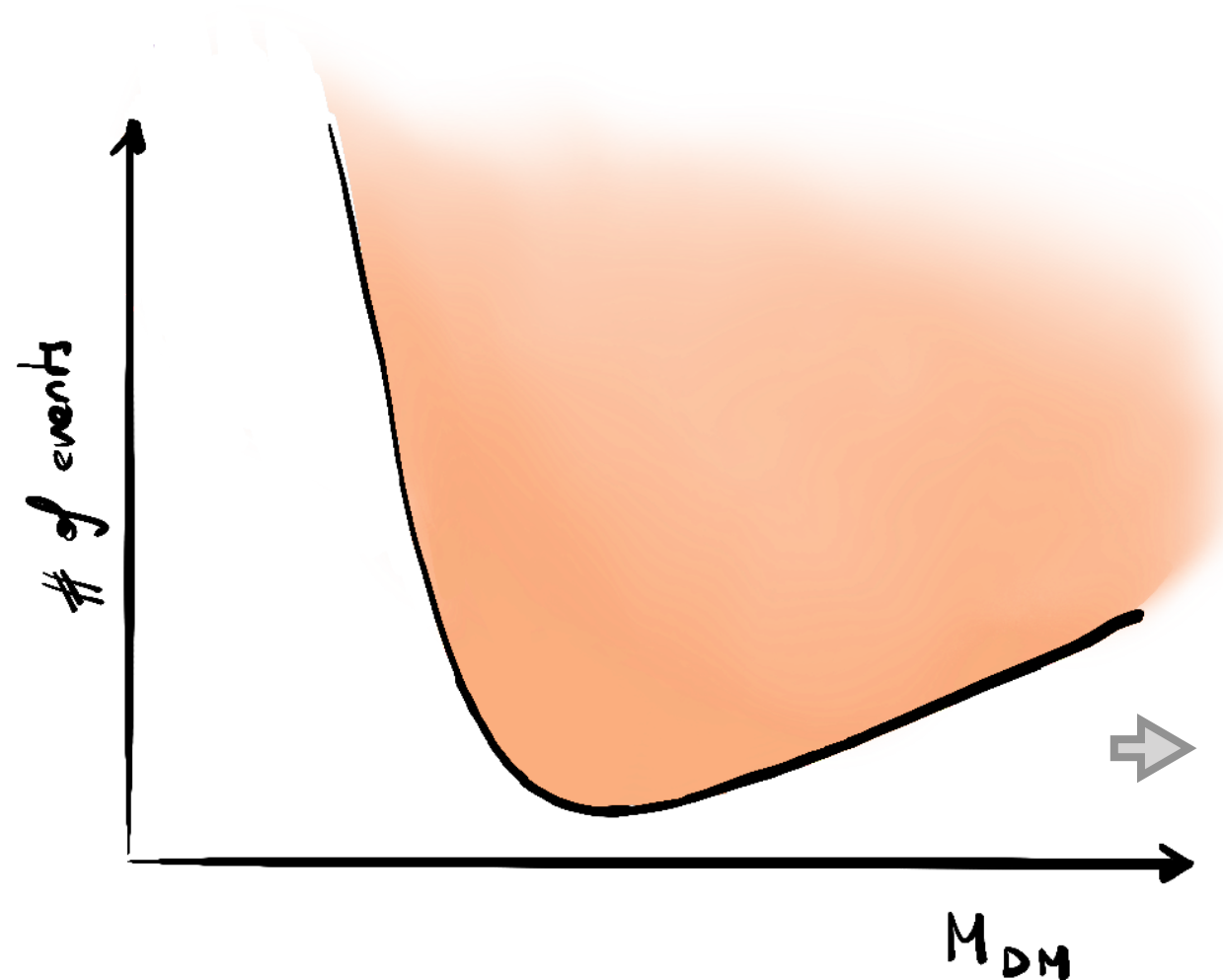
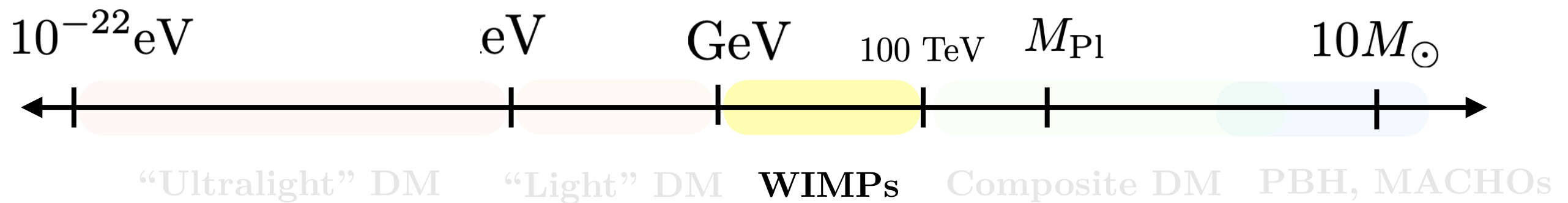
[Akerib, D. S., et al., Snowmass2021, 2203.08084]

Dark Matter: where to look?



$$\sigma \sim 10^{-34} \text{cm}^2 \left(\frac{m_{\chi}}{100 \text{ GeV}} \right)^2$$

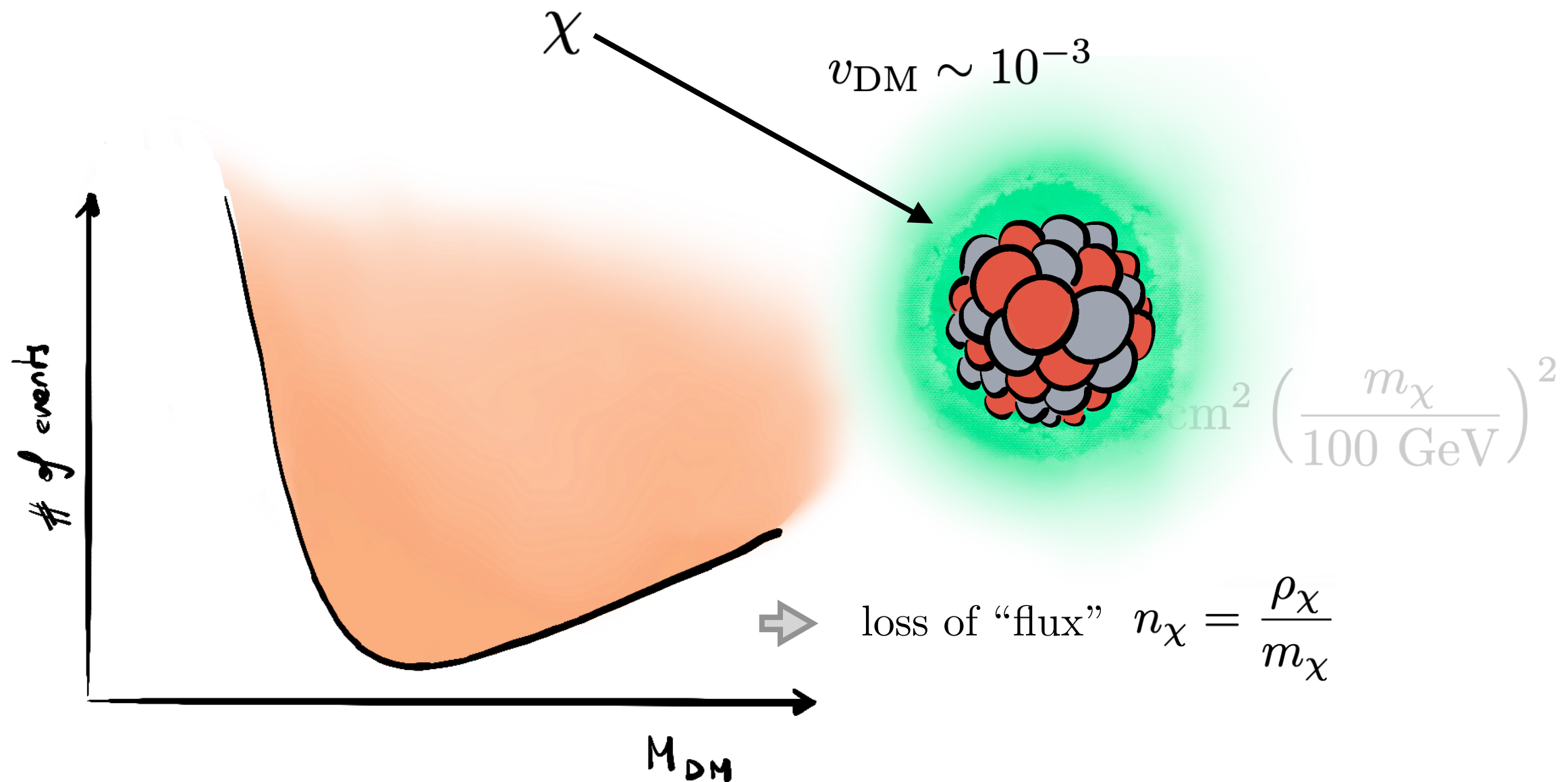
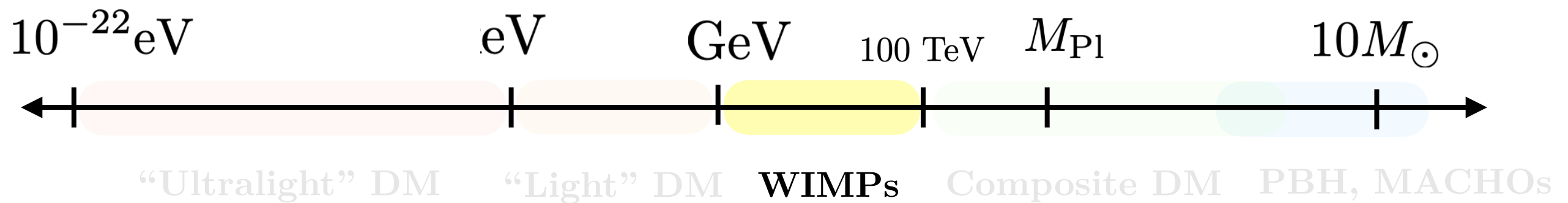
Dark Matter: where to look?



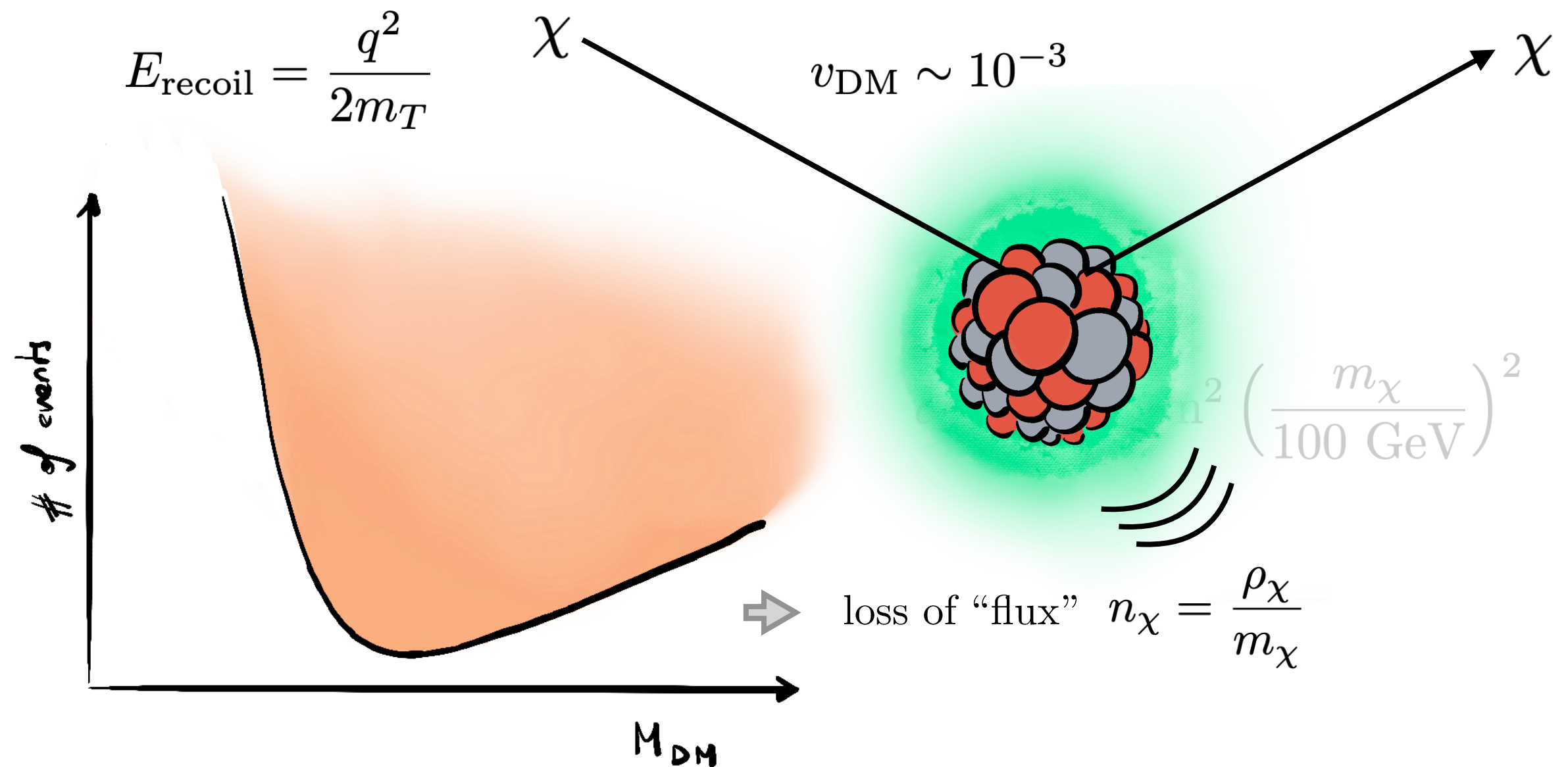
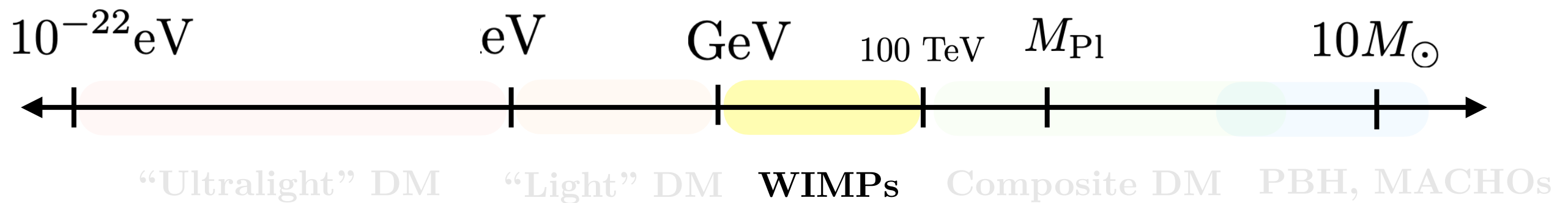
$$\sigma \sim 10^{-34}\text{cm}^2 \left(\frac{m_{\chi}}{100\text{ GeV}} \right)^2$$

⇒ loss of "flux" $n_{\chi} = \frac{\rho_{\chi}}{m_{\chi}}$

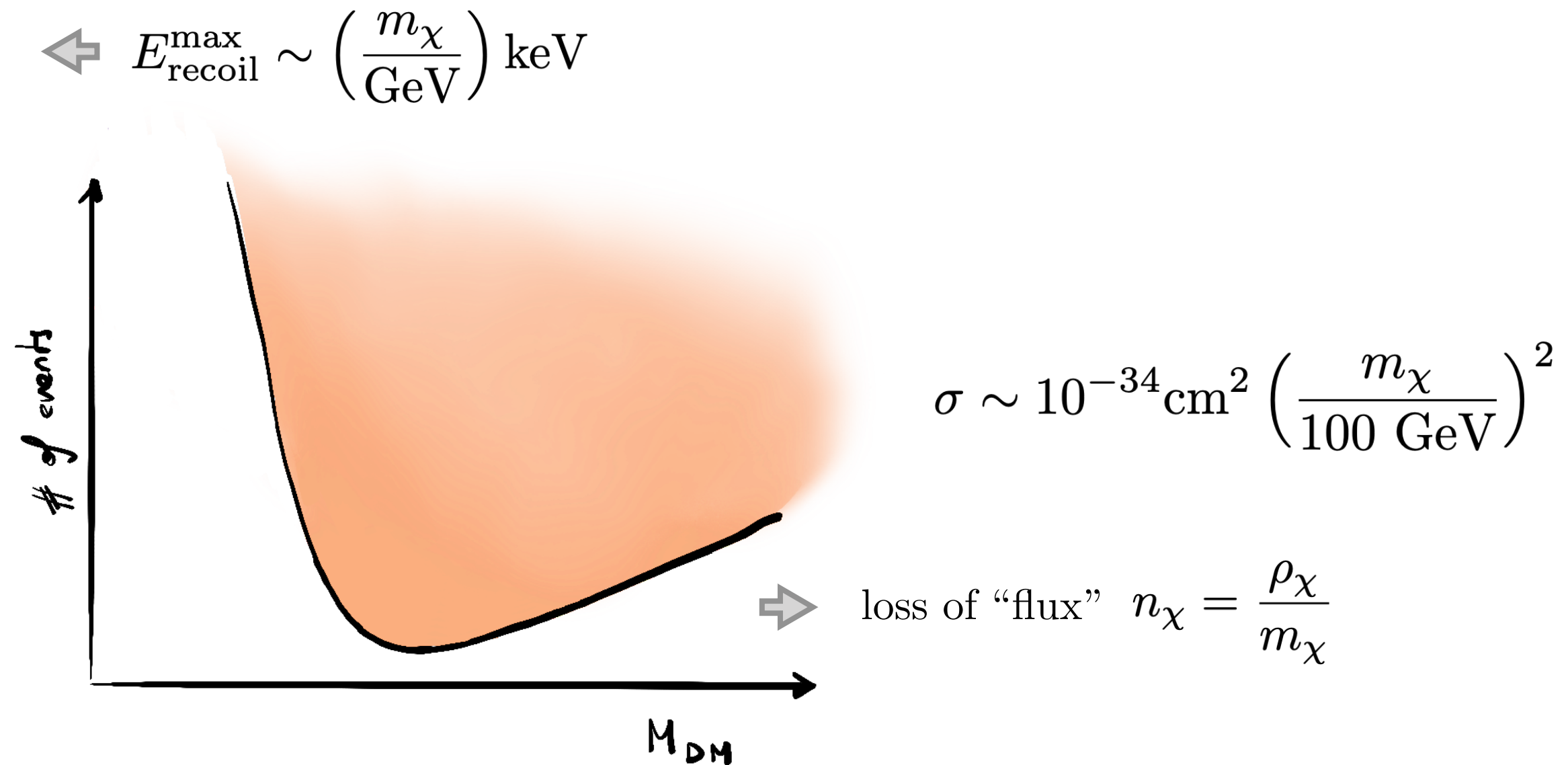
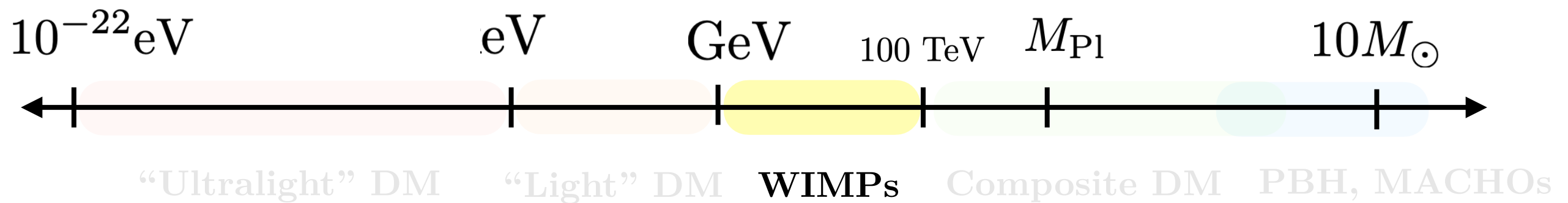
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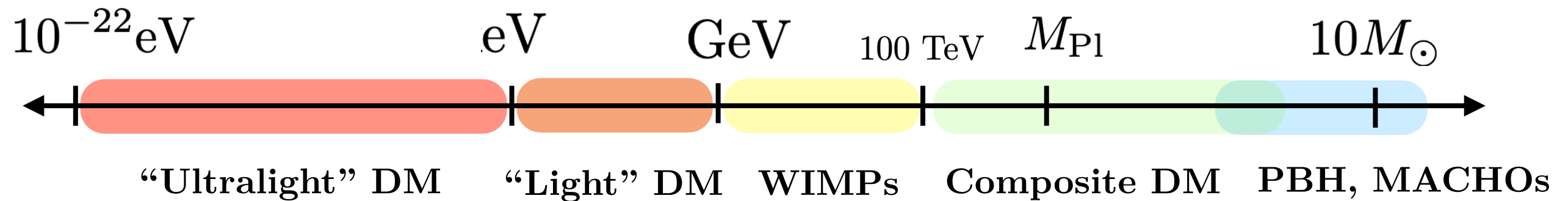
Dark Matter: where to look?



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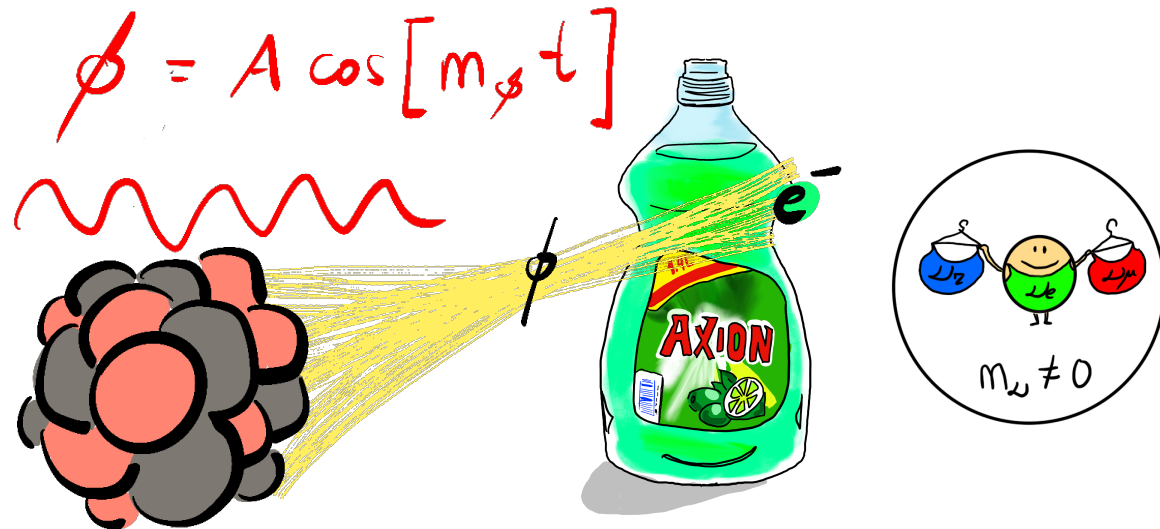
Beyond the SM: “how” to look?



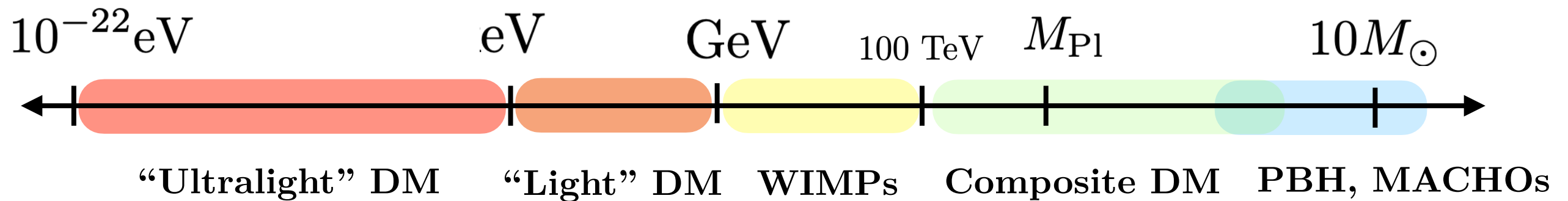
Nuclear recoil exp.

Colliders

...



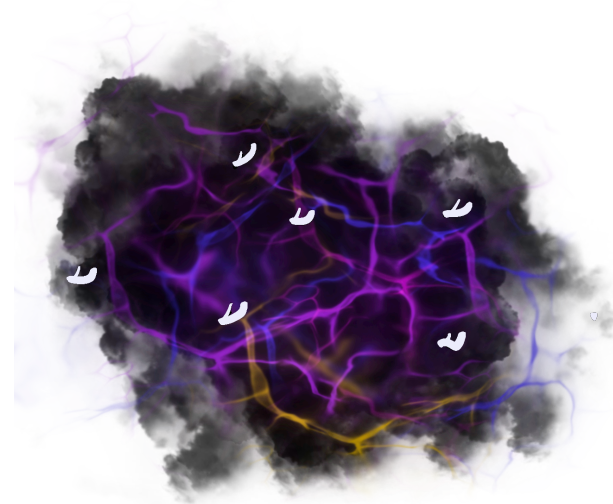
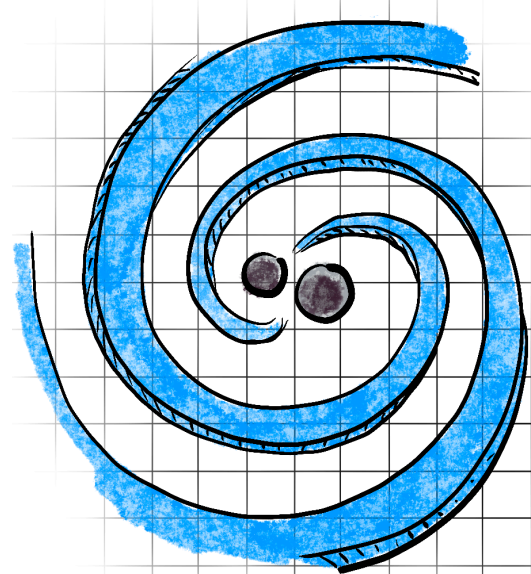
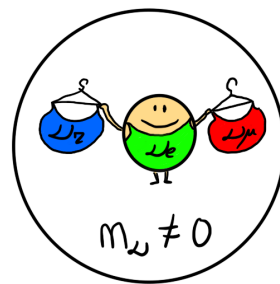
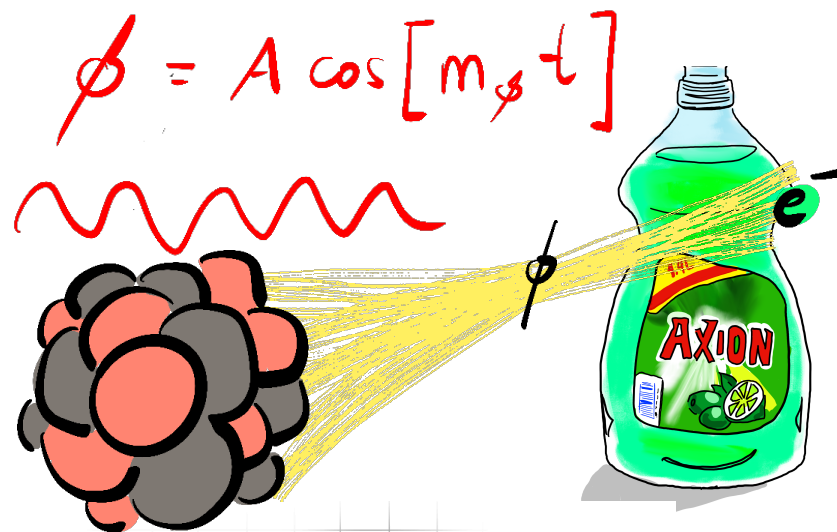
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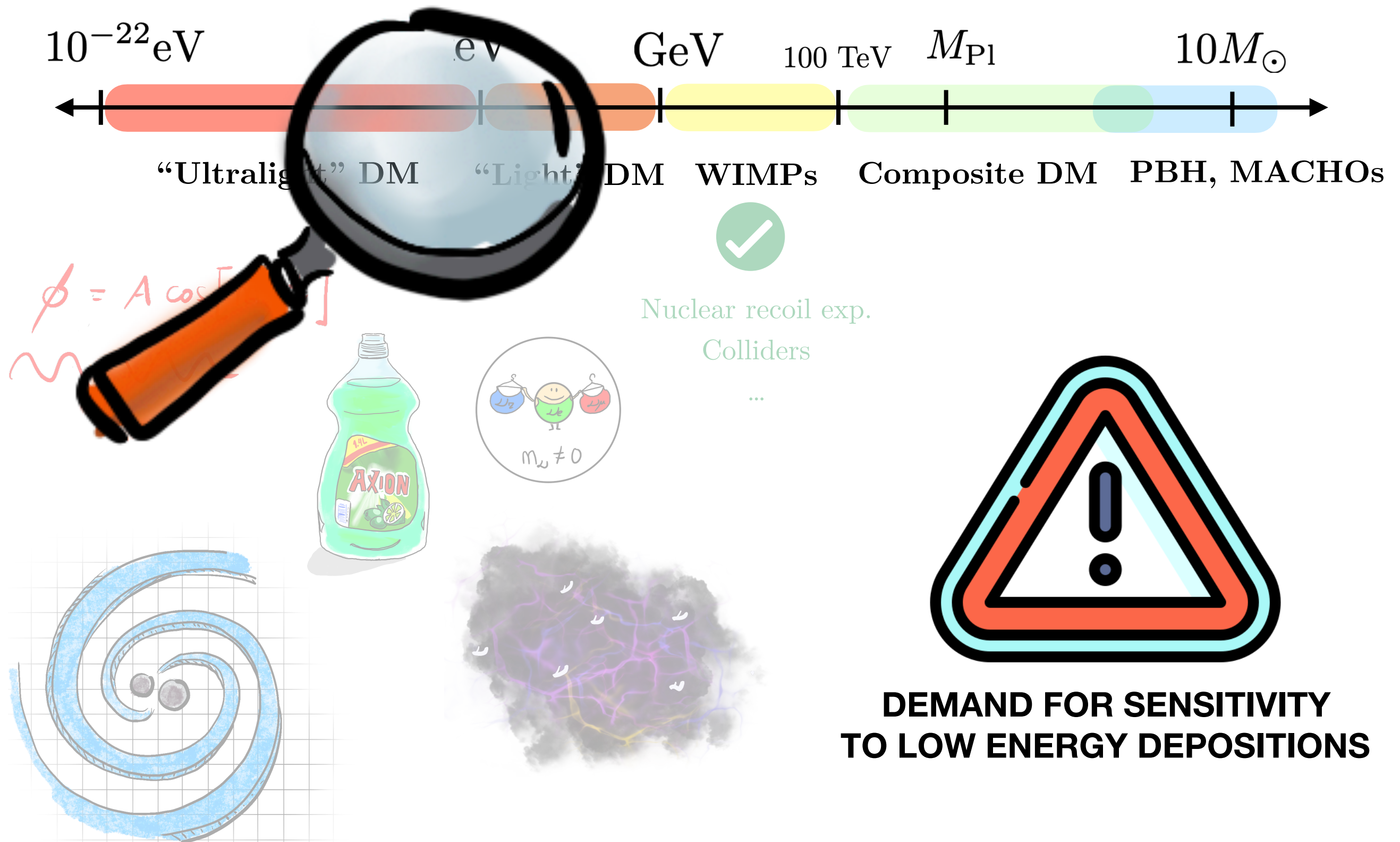
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Colliders

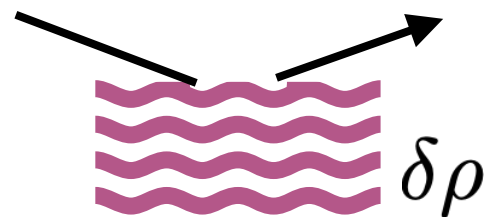
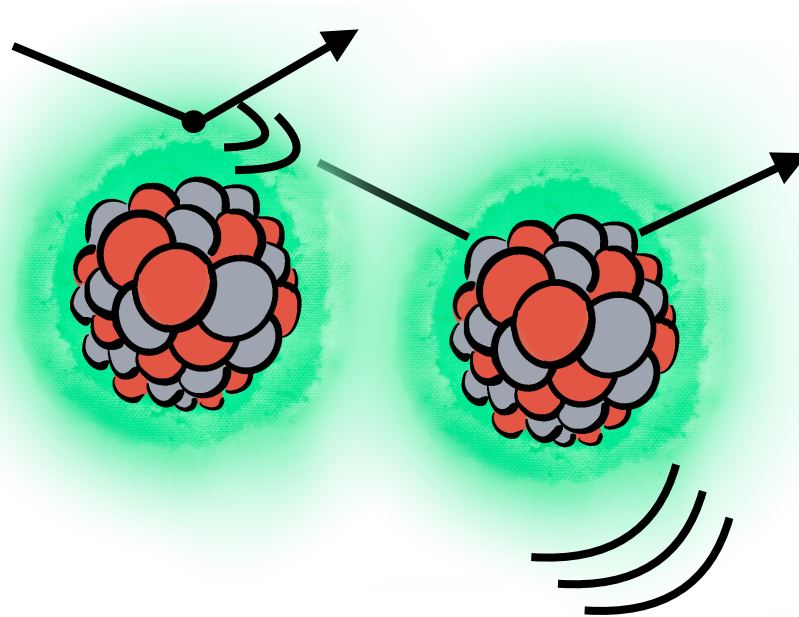
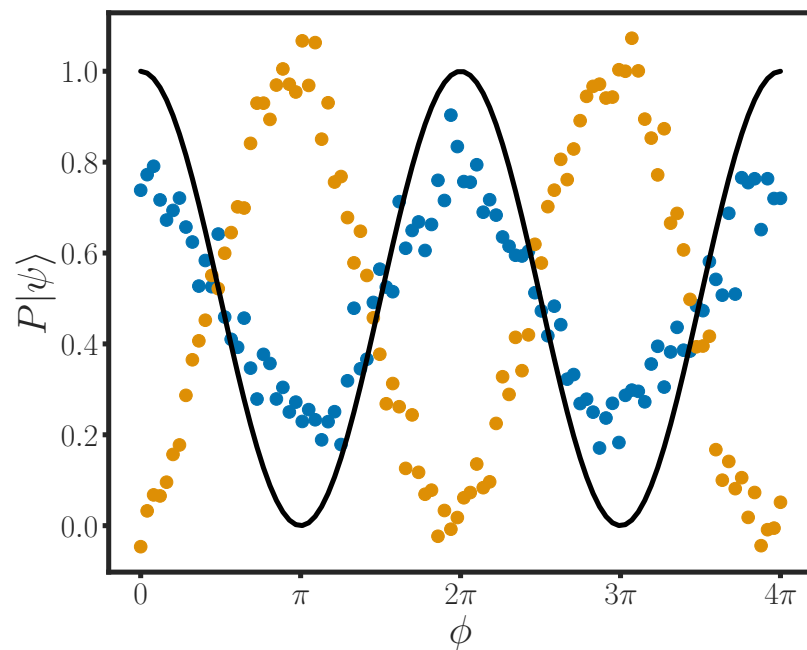
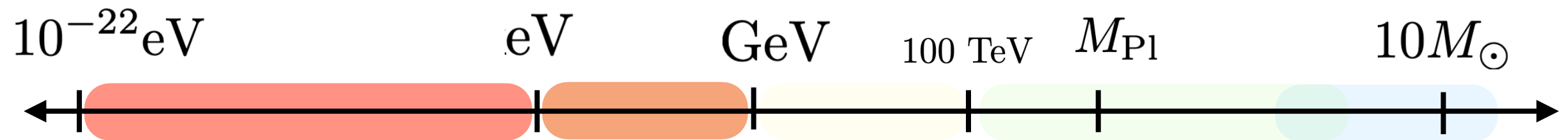
...



Beyond the SM: “how” to look?



Beyond the SM: “how” to look?



$$\text{SNR} \propto \frac{\sigma}{\Delta\sigma}$$

A red arrow points to the denominator $\Delta\sigma$ in the equation.

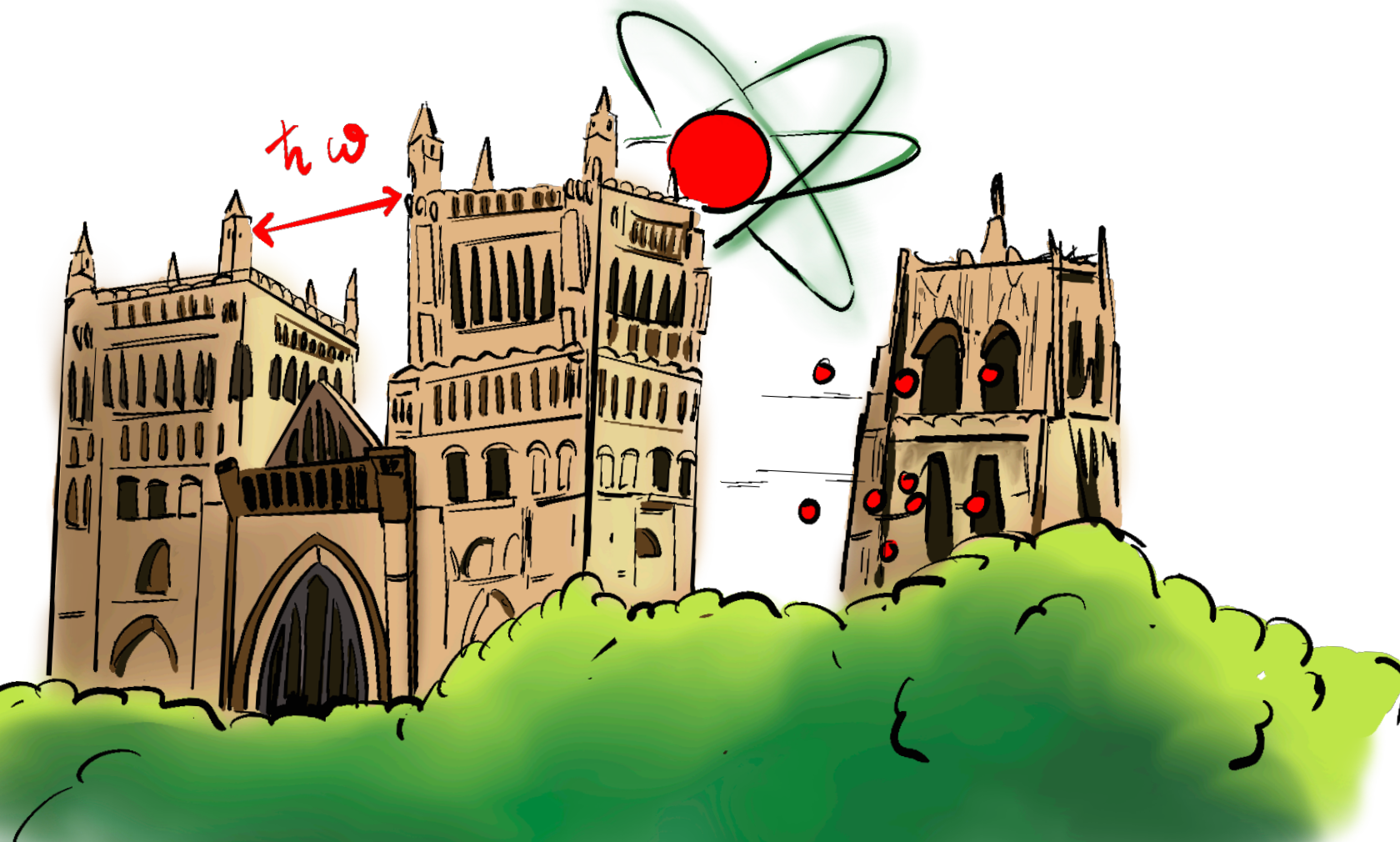
1 Quantum object

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Quantum Sensors as Particle(-wave) detectors



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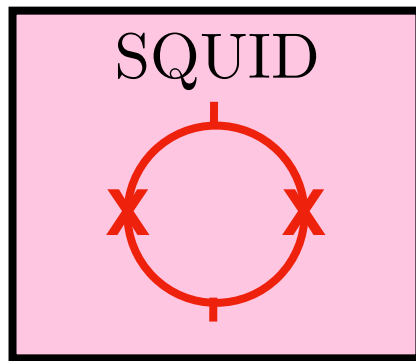


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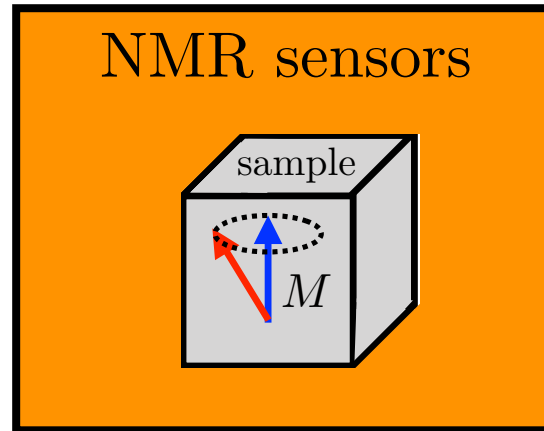
IFAE
Institut de Física
d'Altes Energies

Quantum Sensing: examples

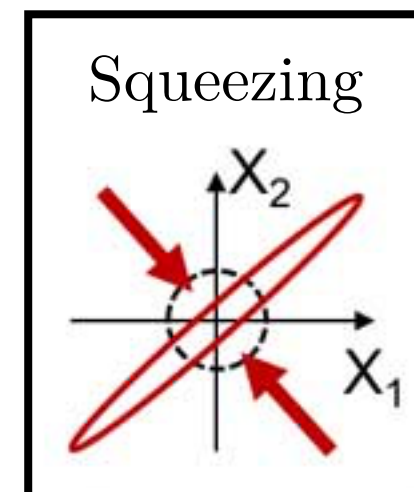
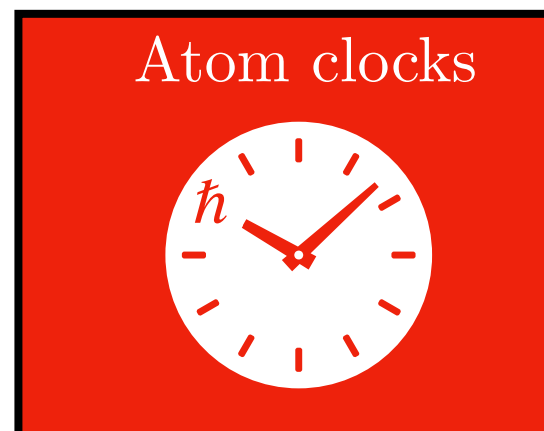
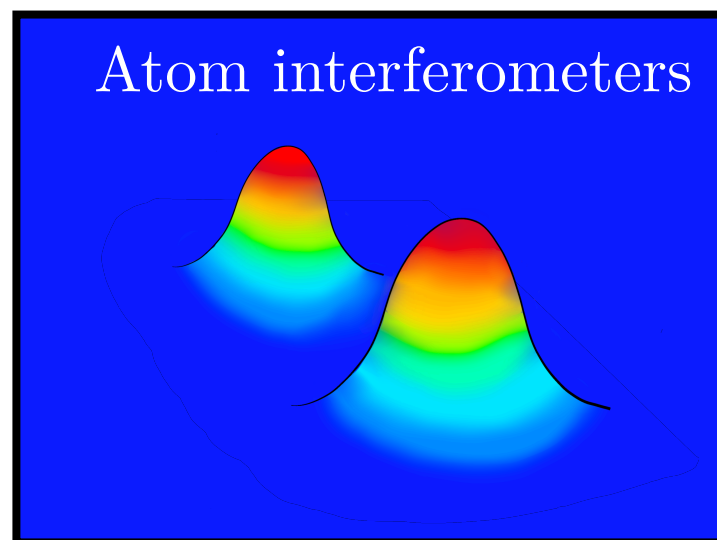
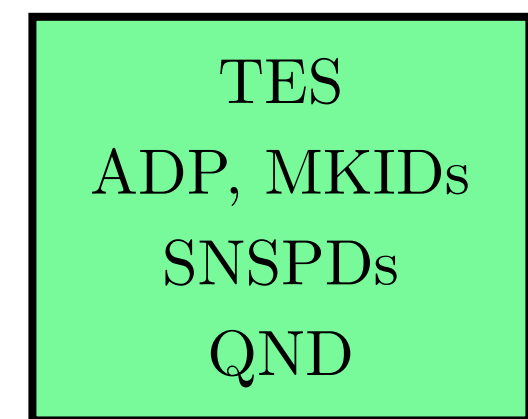
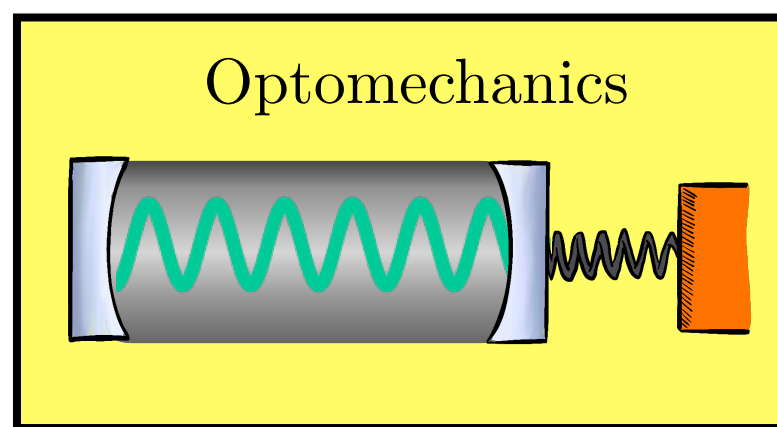
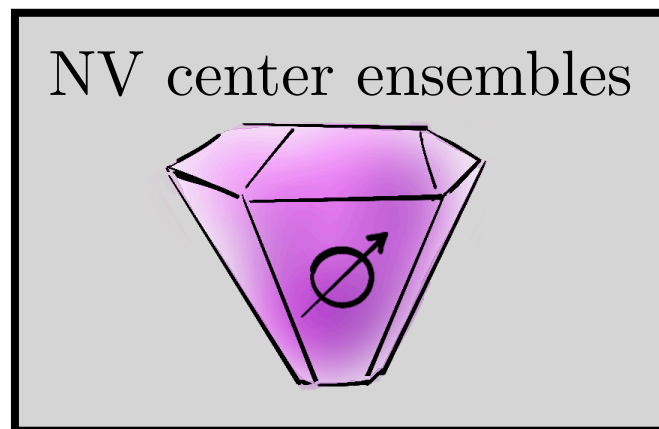
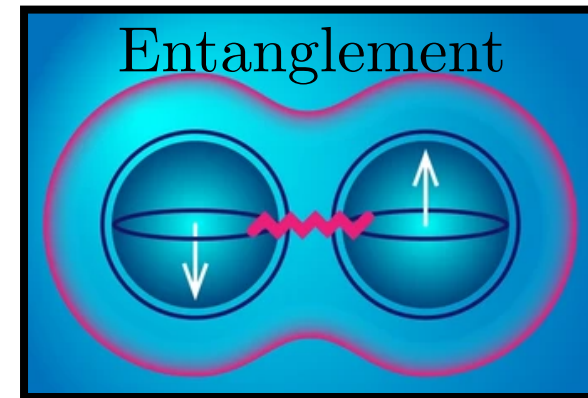
[van Bibber et al., 1803.11306]



[Chou et al., 2311.01930]



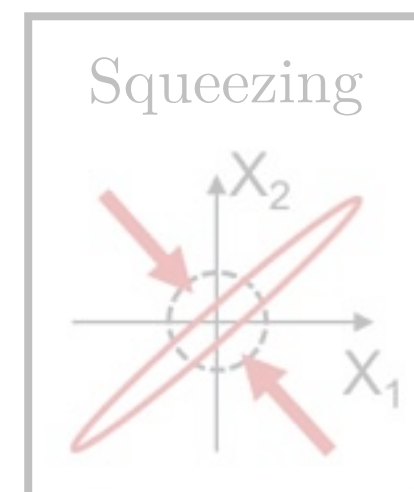
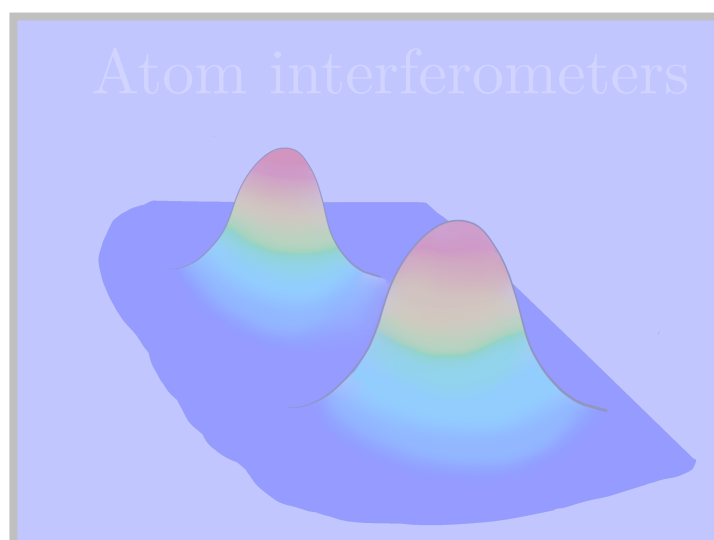
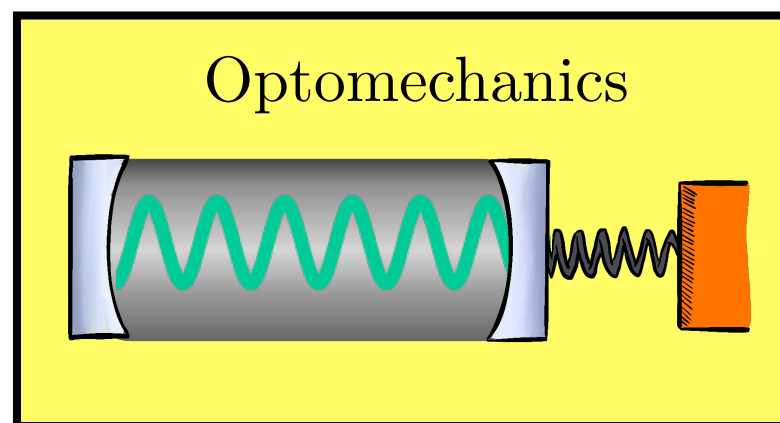
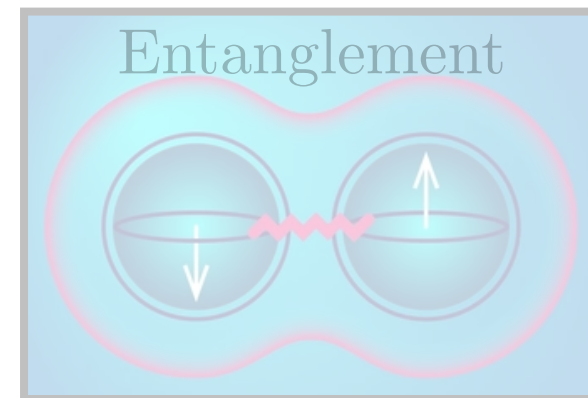
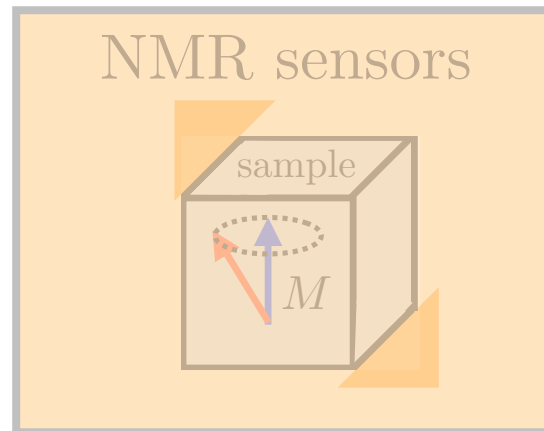
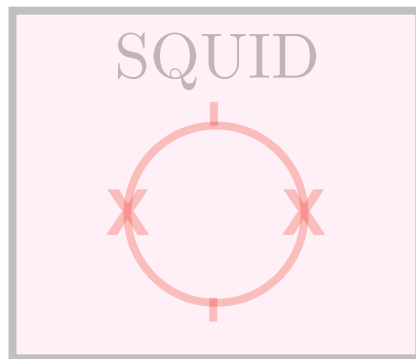
[Blas, 2311.10187]



[Buchmuller et al., 2203.07250]

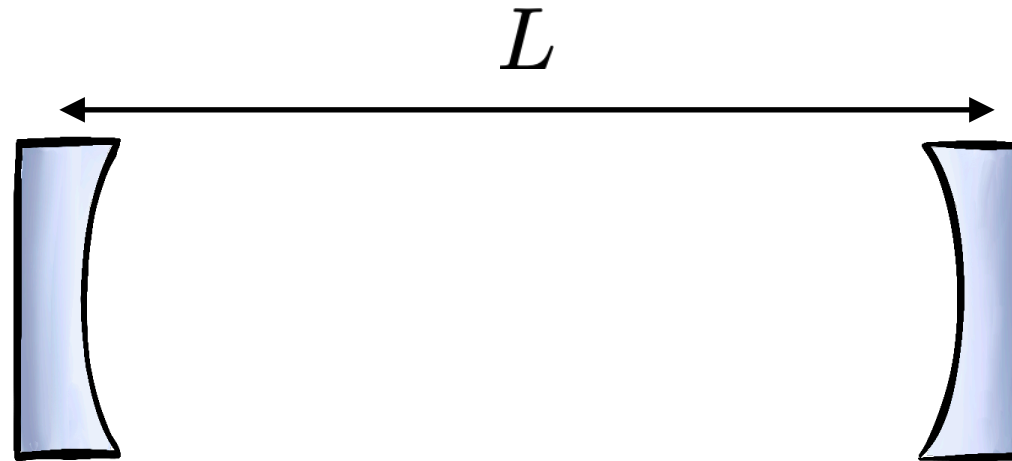
[Golwala and Figueroa-Feliciano, 2203.07250]

Quantum Sensing: examples



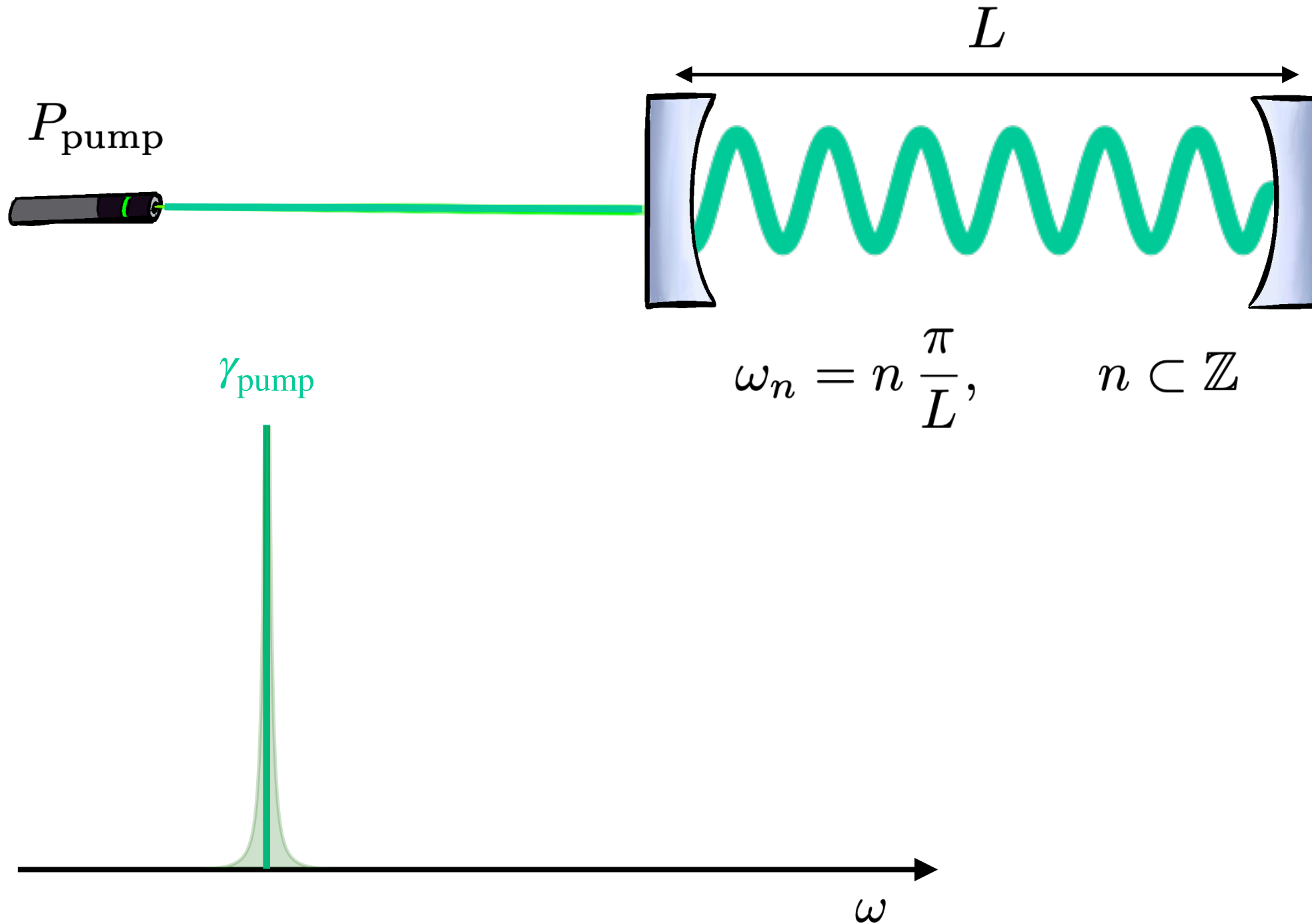
Standard Optomechanics

[Review: M. Aspelmeyer, T. J. Kippenberg, F. Marquardt, 2013. Thesis at J. Harris lab.]



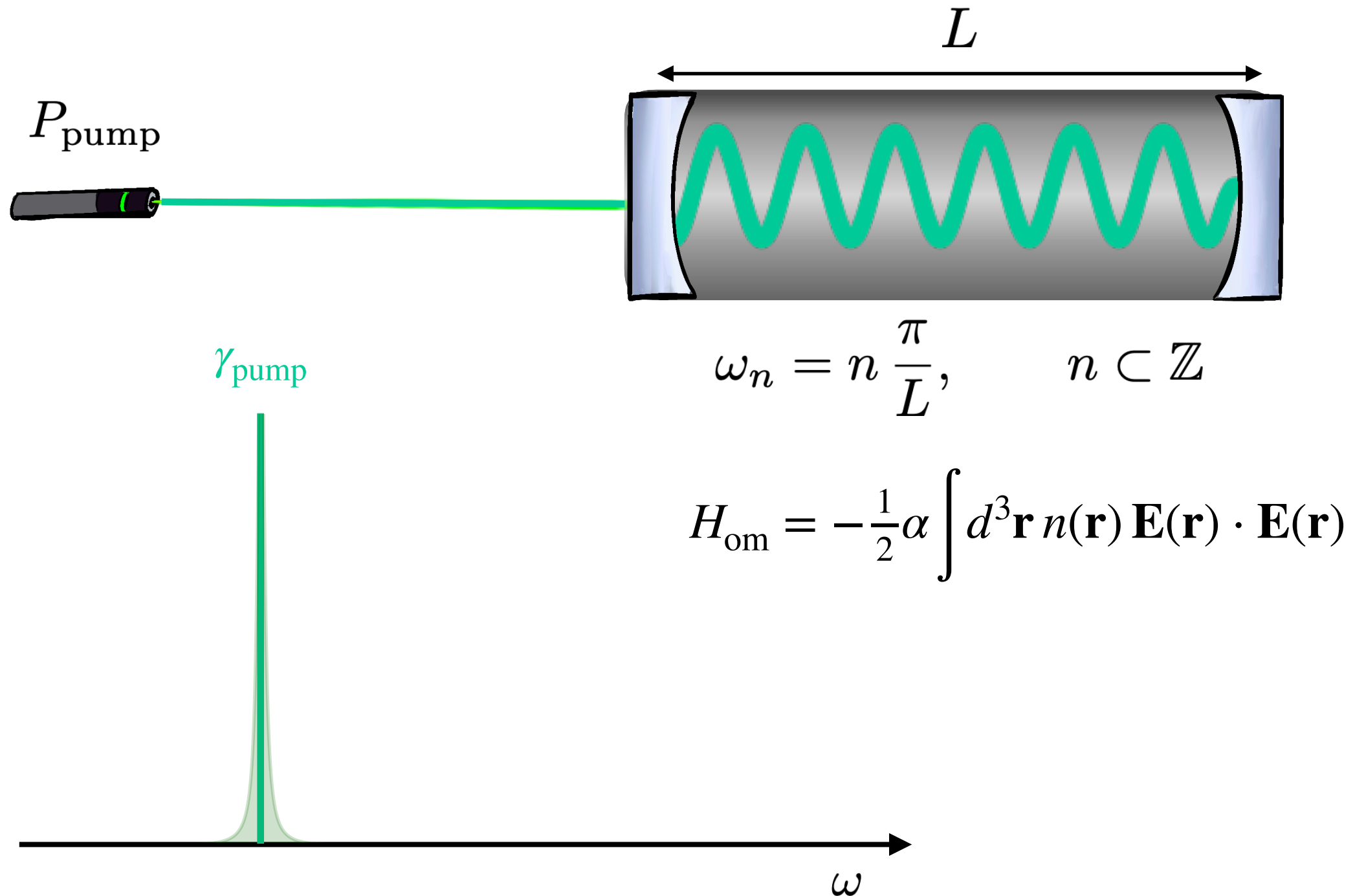
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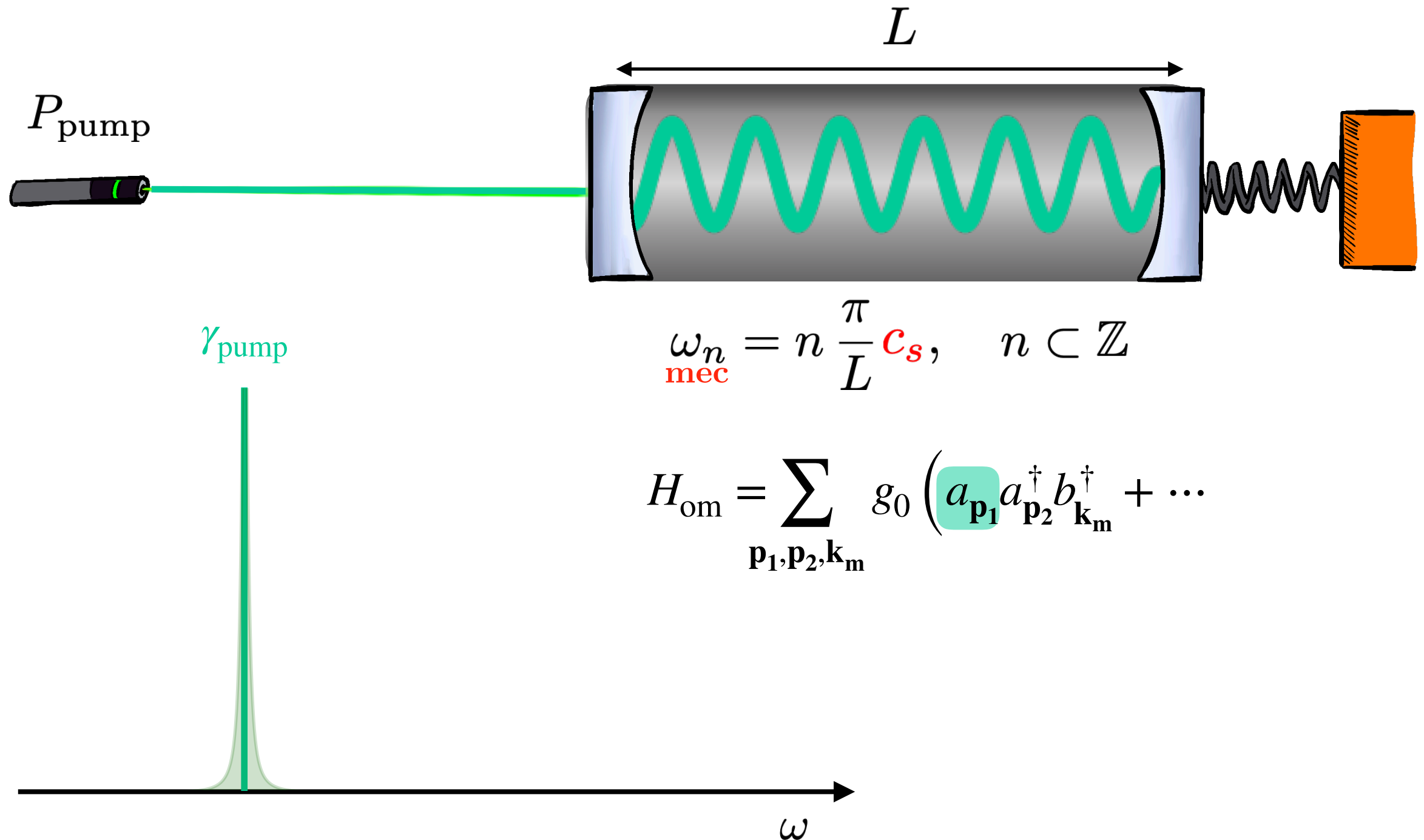
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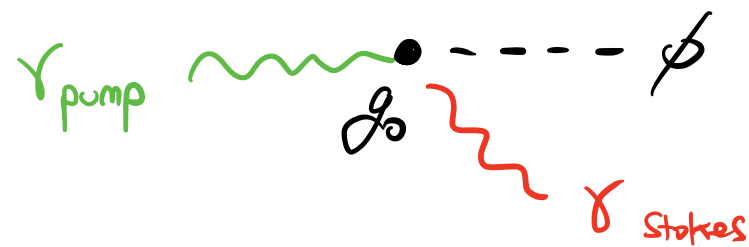


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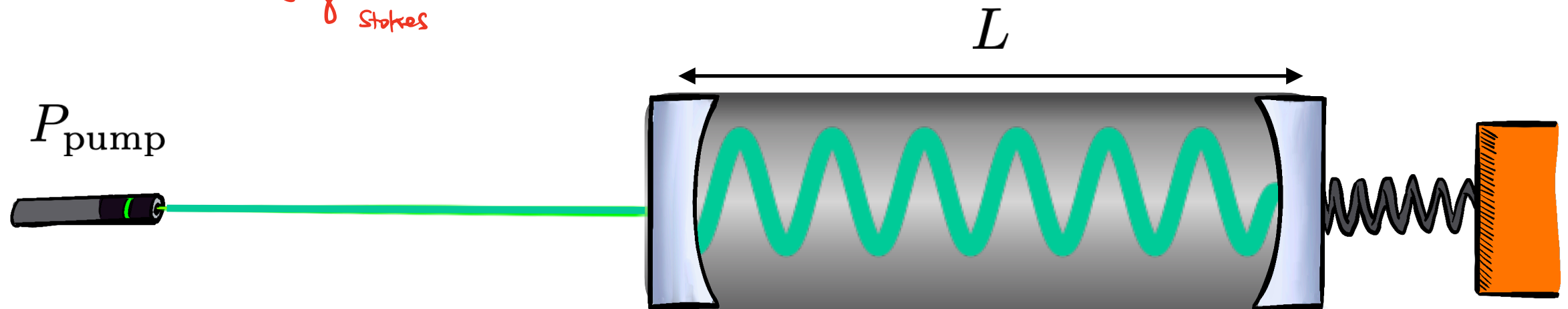


Standard Optomechanics



$$\vec{p}_{\gamma 1} = \vec{p}_{\phi} + \vec{p}_{\gamma 2}$$

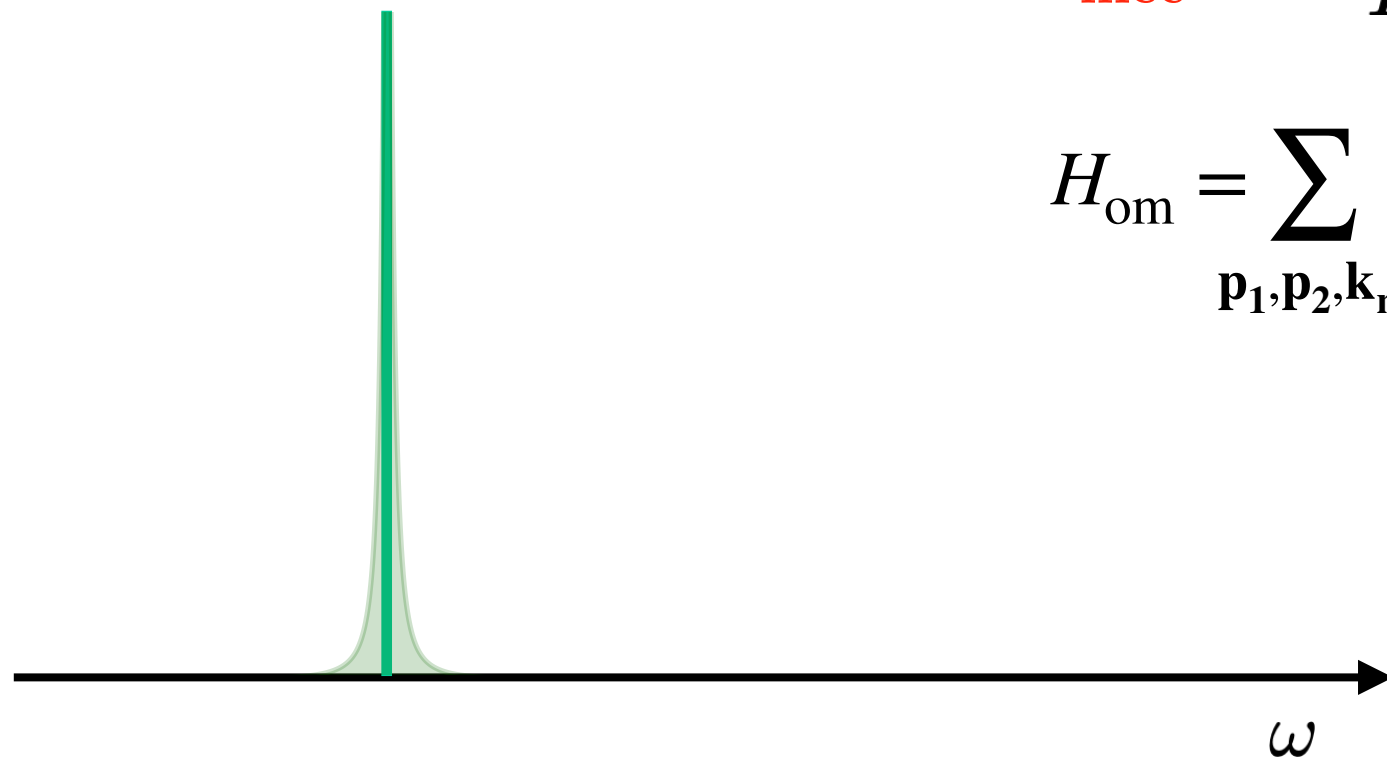
$$\omega_{\gamma 1} = \omega_m + \omega_{\gamma 2}$$



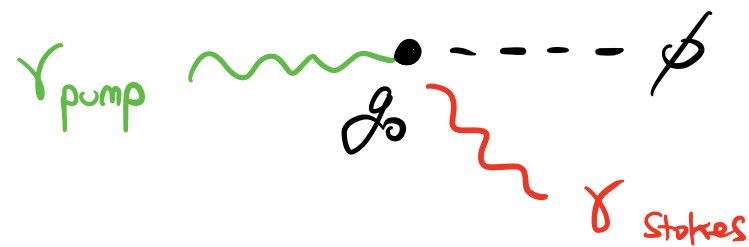
γ_{pump}

$$\omega_{\text{mec } n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^{\dagger} b_{\mathbf{k}_m}^{\dagger} + \dots \right)$$

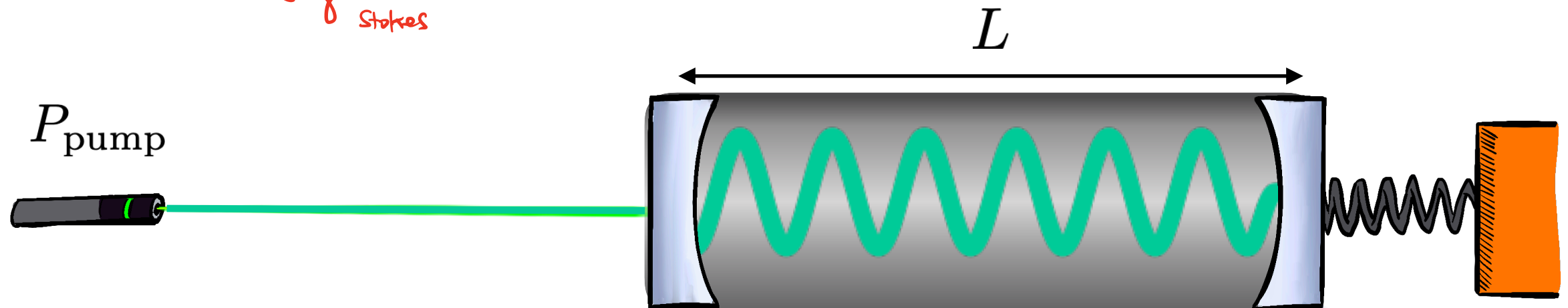


Standard Optomechanics



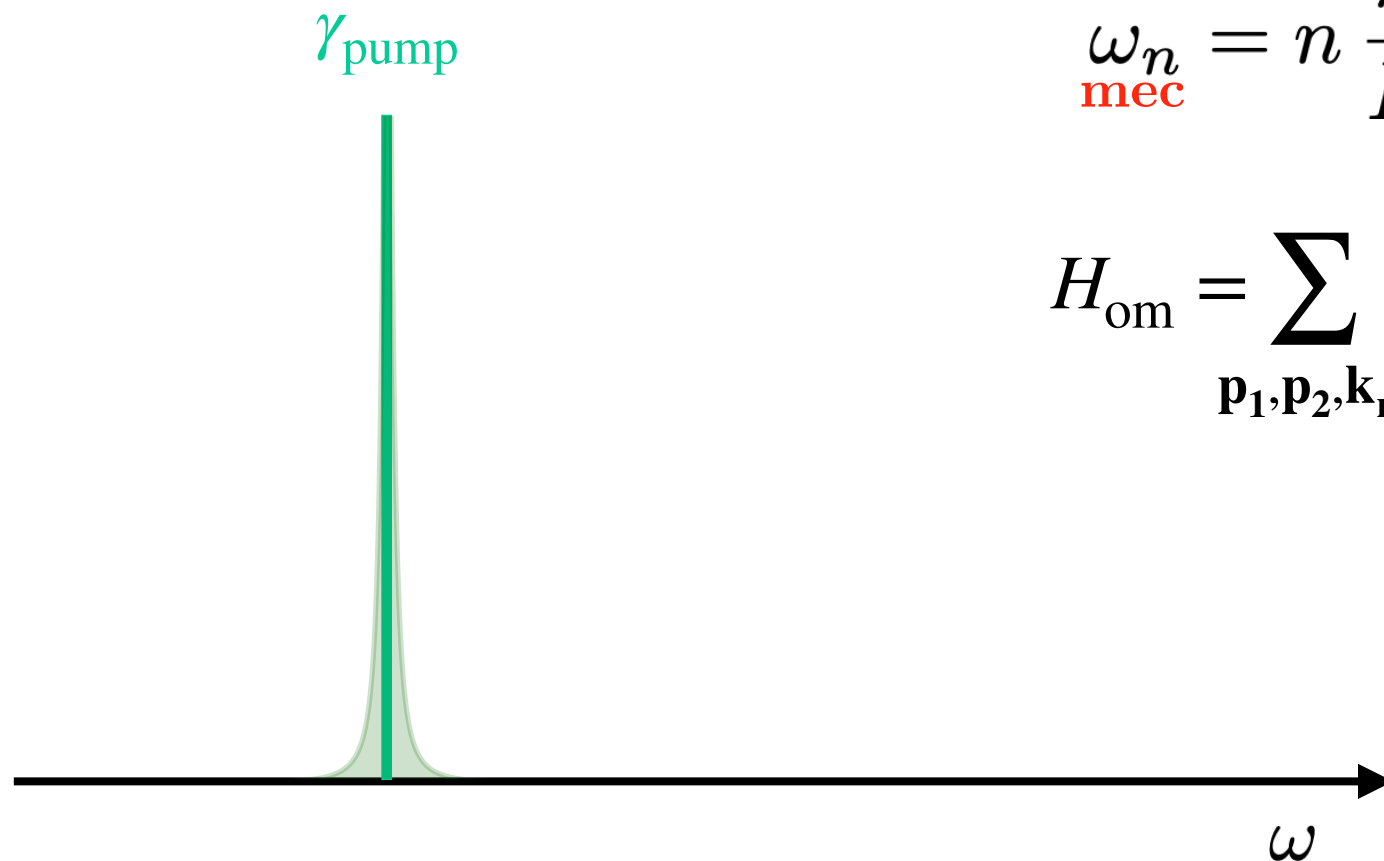
$$p_\phi = 2p_\gamma$$

$$\Omega_m = 2c_s\omega_{\text{opt}}$$

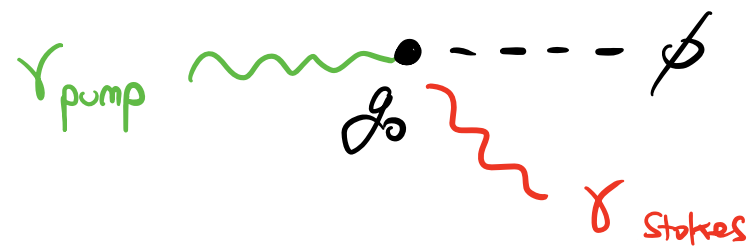


$$\omega_{\text{mec } n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

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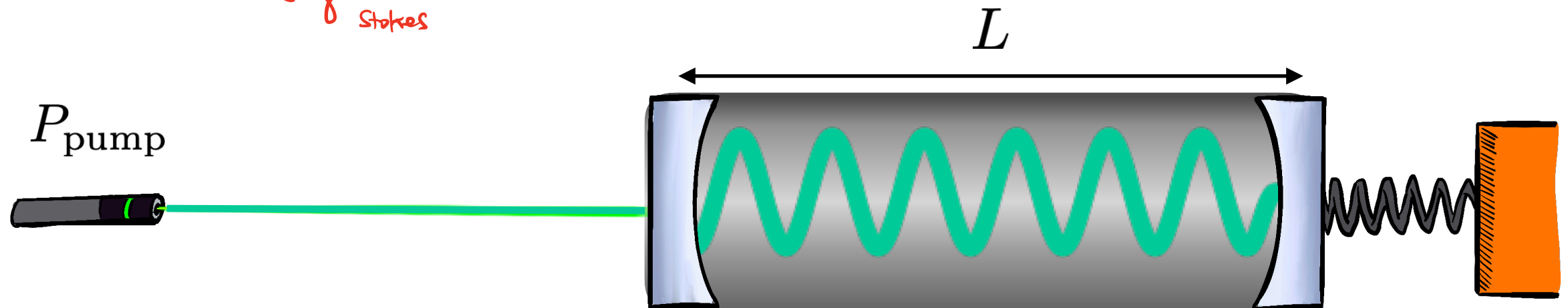


Standard Optomechanics



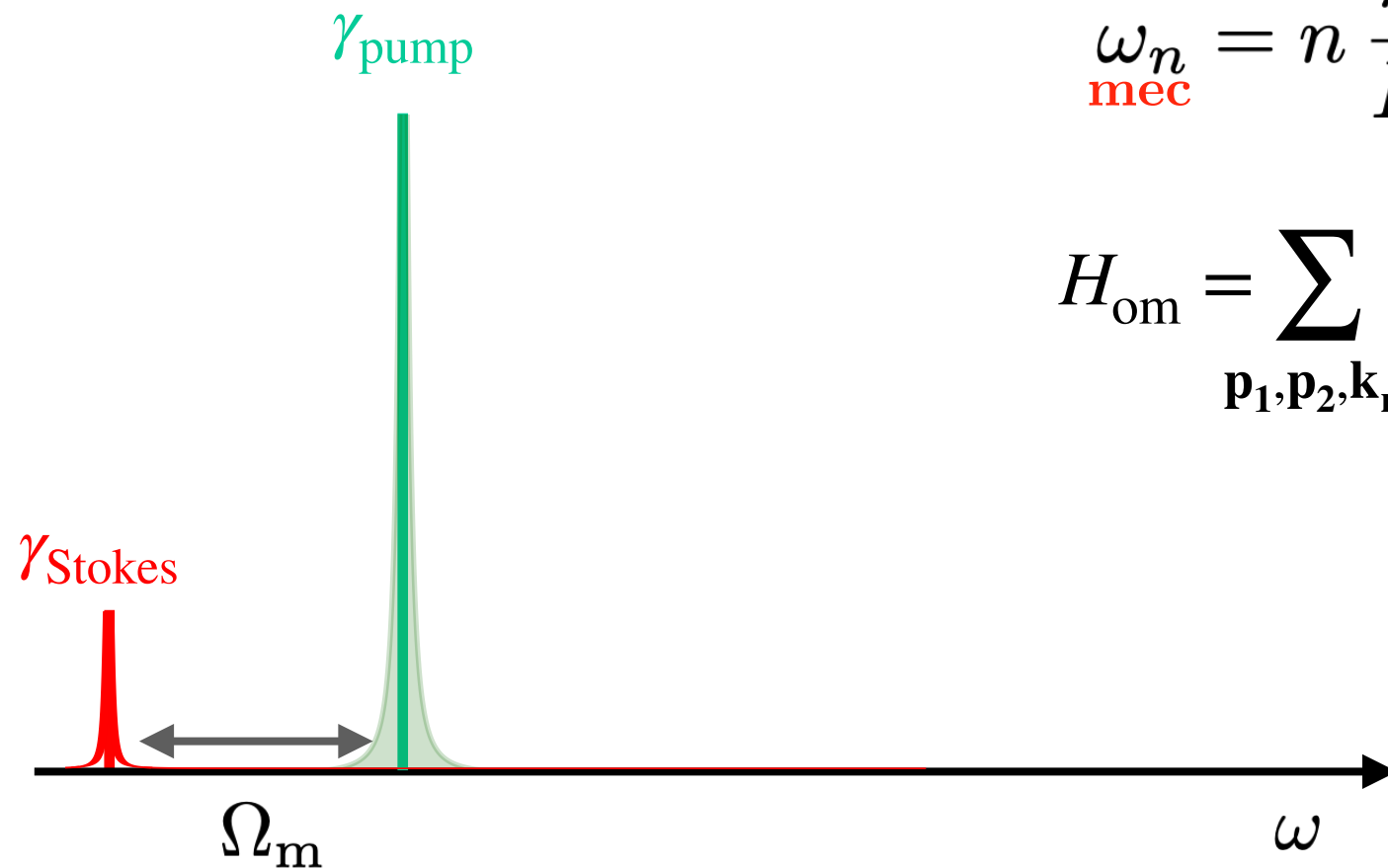
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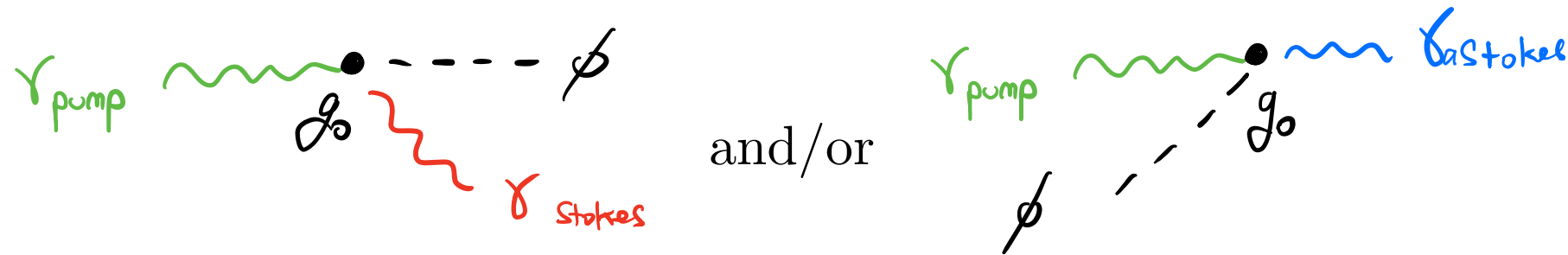


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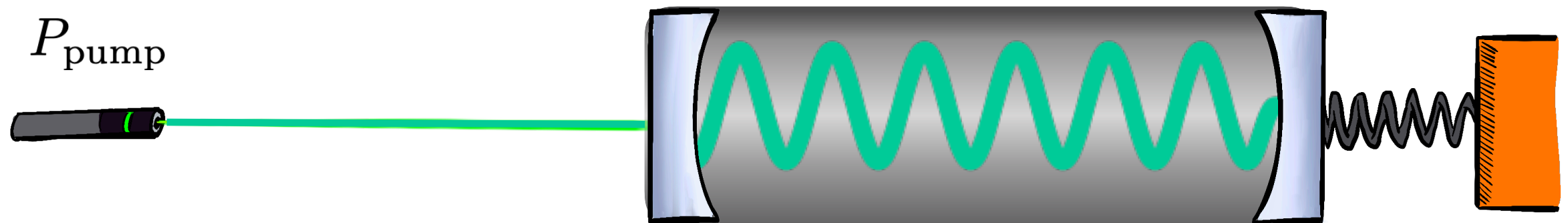


Standard Optomechanics



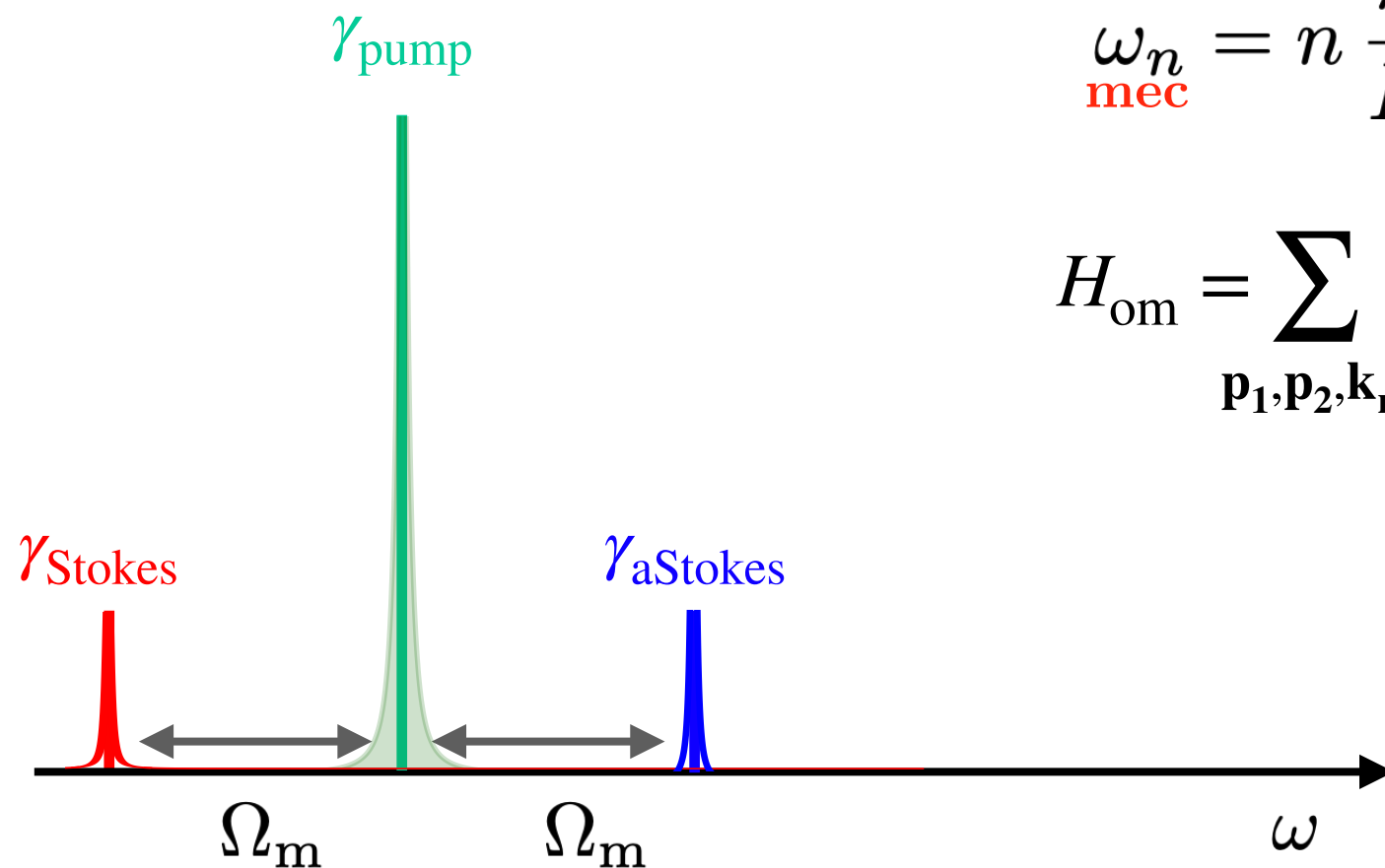
$$p_\phi = 2p_\gamma$$

$$\Omega_m = 2c_s\omega_{\text{opt}}$$

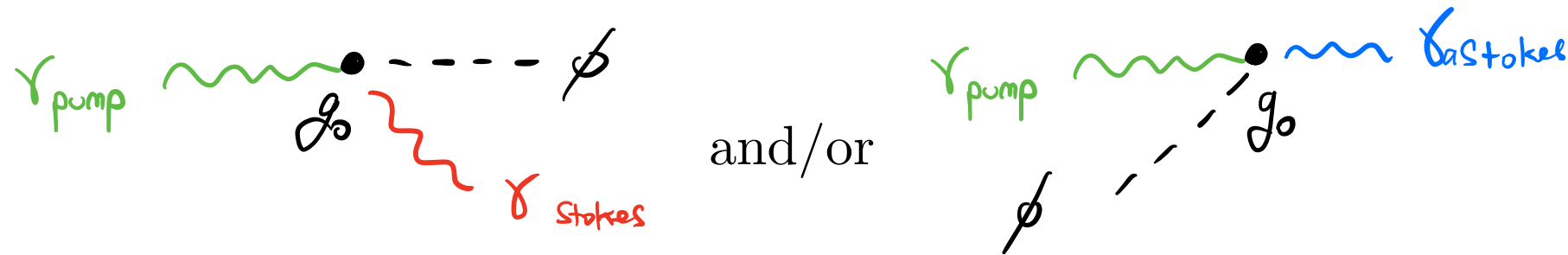


$$\omega_{\text{mec } n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger + a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m} \right)$$

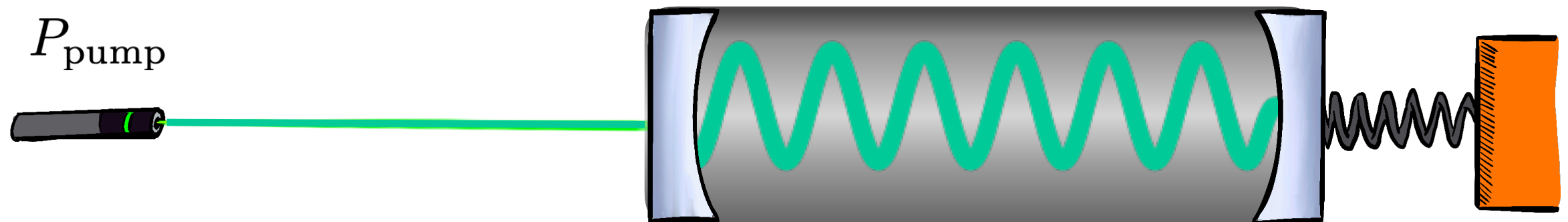


Standard Optomechanics



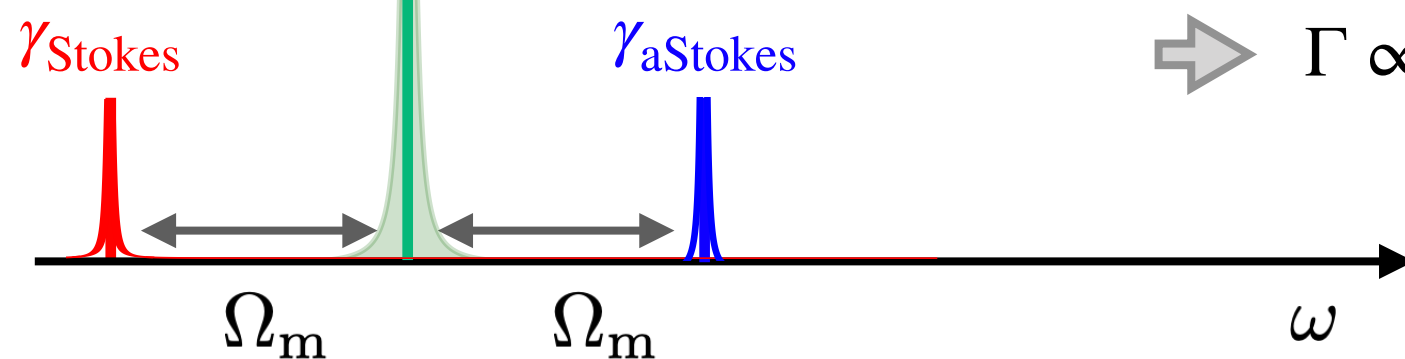
$$p_\phi = 2p_\gamma$$

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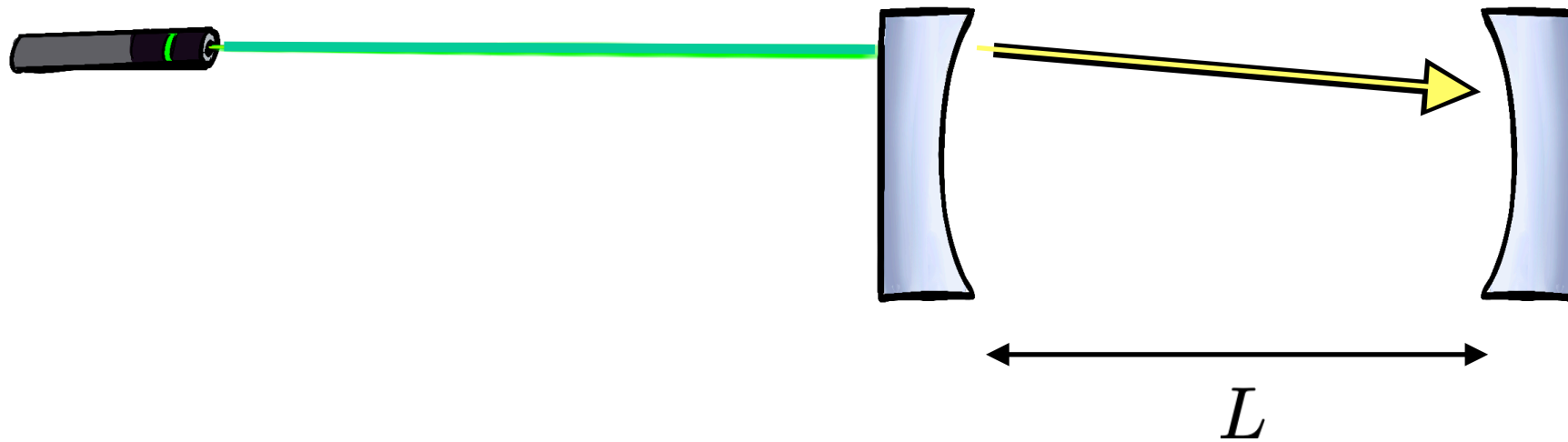
$$\omega_{\text{mec},n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger + a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m} \right)$$

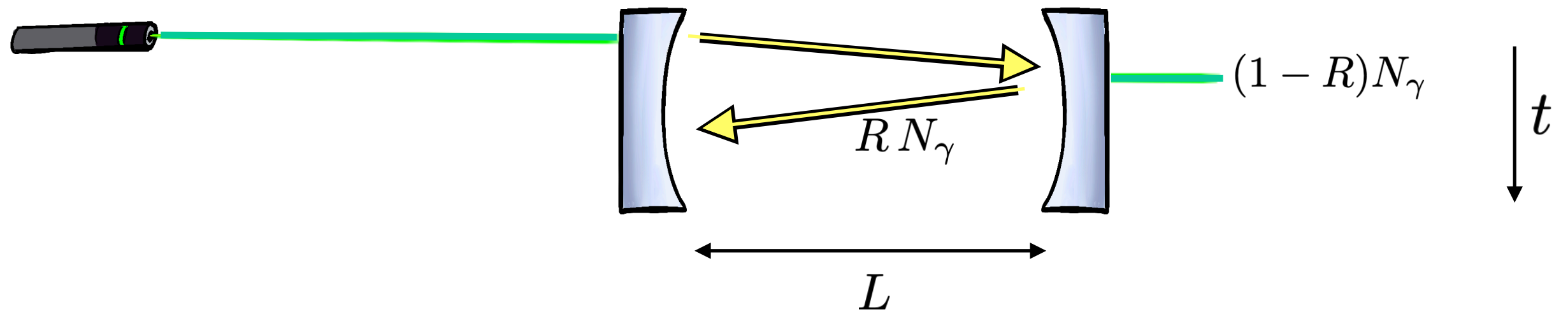


$$\Rightarrow \Gamma \propto |g_0|^2 N_{\gamma, \text{pump}}^{\text{circ}} [\Delta_{\text{pump}}]$$

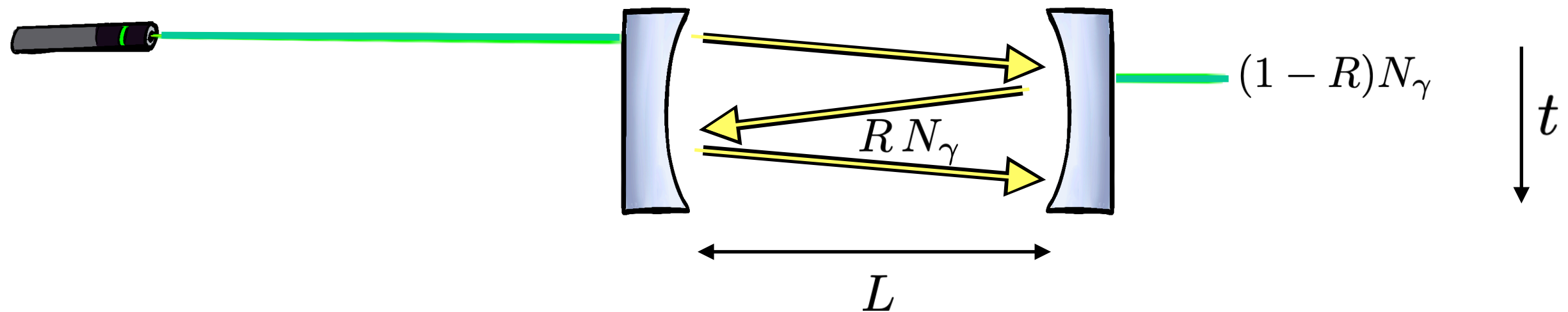
Standard Optomechanics



Standard Optomechanics



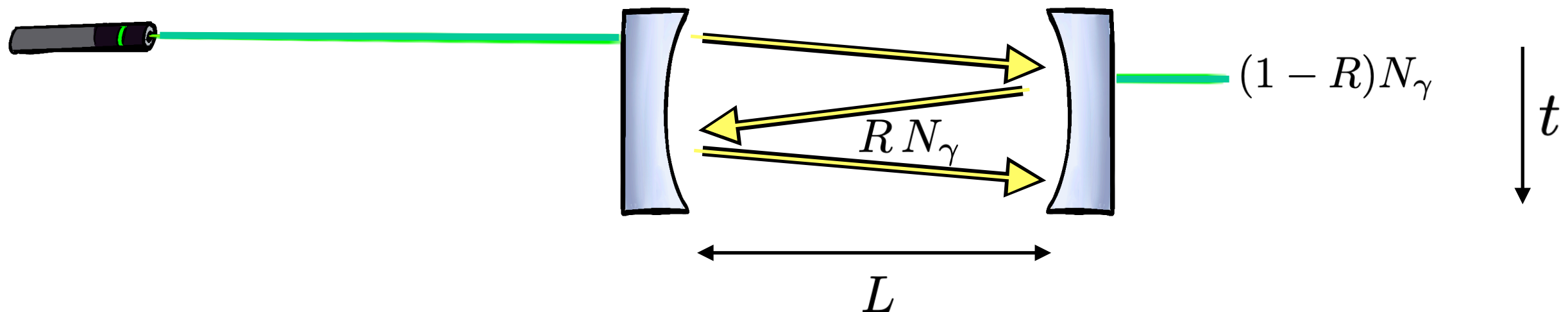
Standard Optomechanics



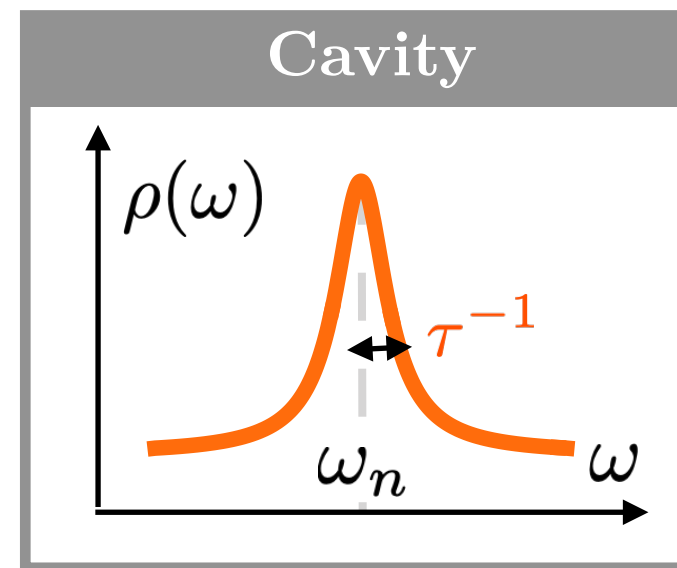
$$\frac{dN_\gamma}{dt} \simeq \frac{\Delta N_\gamma}{L/c} = \frac{c(1 - R)}{L} N_\gamma \quad \Rightarrow \quad \tau_\gamma^{-1} \equiv \kappa \simeq \frac{c}{(1 - R)^{-1} L}$$

$\mathcal{F}_{\text{opt}}$

Standard Optomechanics



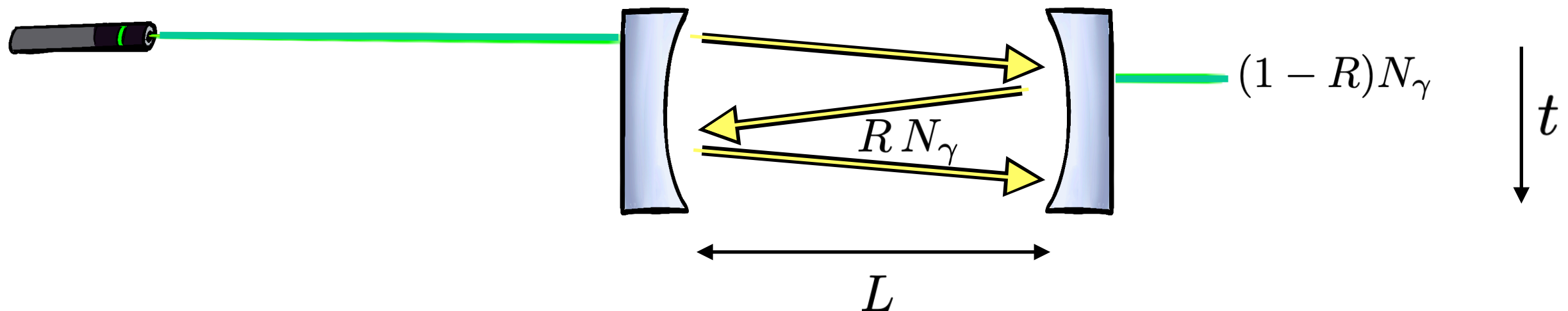
$$\frac{dN_\gamma}{dt} \simeq \frac{\Delta N_\gamma}{L/c} = \frac{c(1 - R)}{L} N_\gamma \quad \Rightarrow \quad \tau_\gamma^{-1} \equiv \kappa \simeq \frac{c}{(1 - R)^{-1} L}$$



$\mathcal{F}_{\text{opt}}$

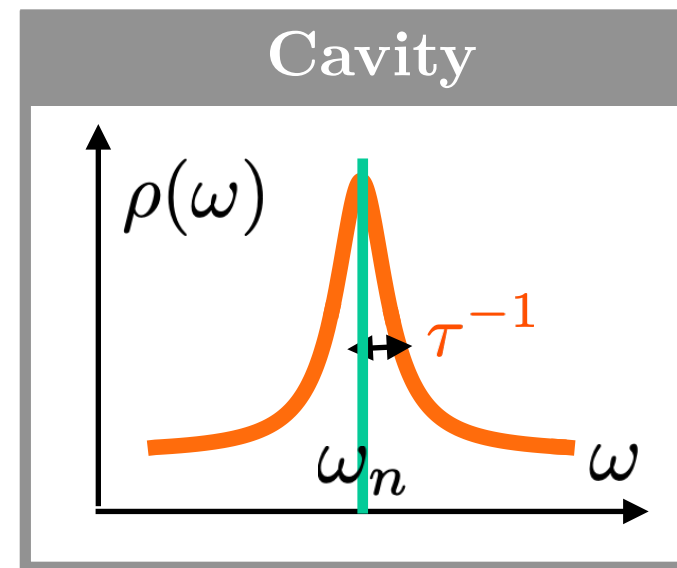
$$\rho(\omega) = \sum_i \delta(\omega - \omega_i) = \sum_n \frac{1}{2\pi} \int dt e^{i(\omega - \omega_n)t} e^{-t/(2\tau)} = \sum_n \frac{\tau^{-1}/2}{(\omega - \omega_n)^2 + (\tau^{-1}/2)^2}$$

Standard Optomechanics



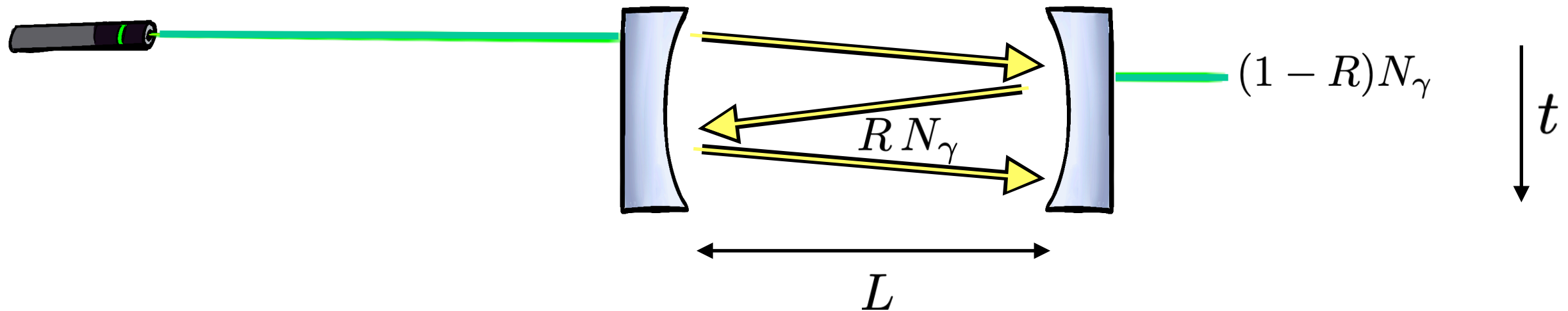
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$$N_{\gamma,L}^{\text{circ}} \sim \frac{4P_L \tau}{\omega_L}$$



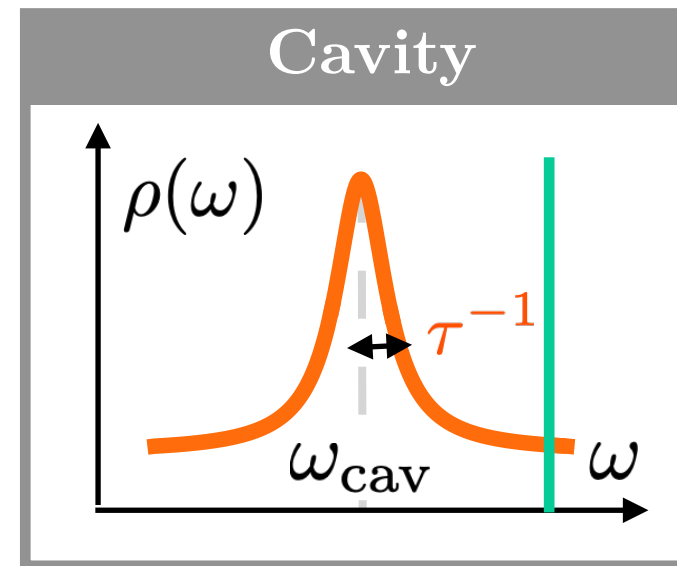
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Standard Optomechanics



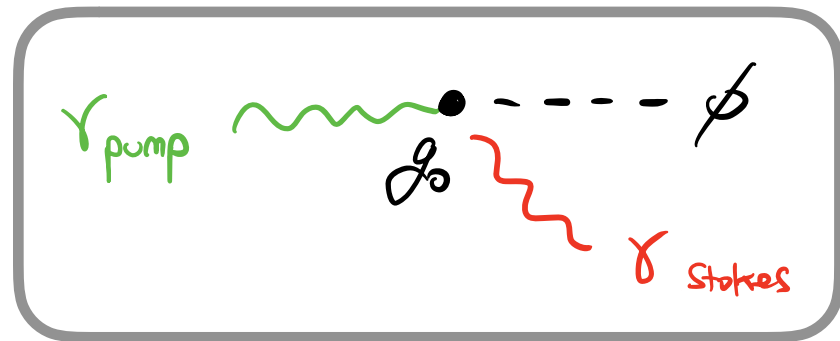
$$\frac{dN_\gamma}{dt} \simeq \frac{\Delta N_\gamma}{L/c} = \frac{c(1-R)}{L} N_\gamma \quad \Rightarrow \quad \tau_\gamma^{-1} \equiv \kappa \simeq \frac{c}{(1-R)^{-1}L}$$

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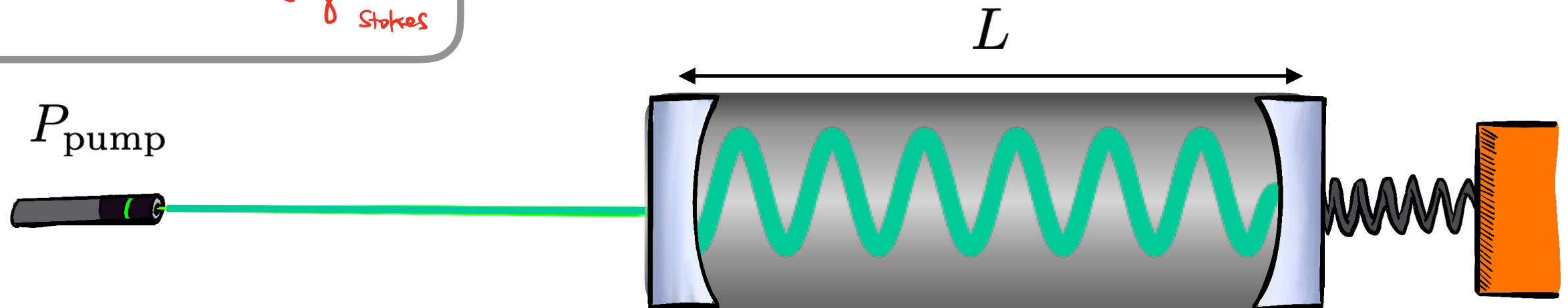
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Standard Optomechanics



$$p_\phi = 2p_\gamma$$

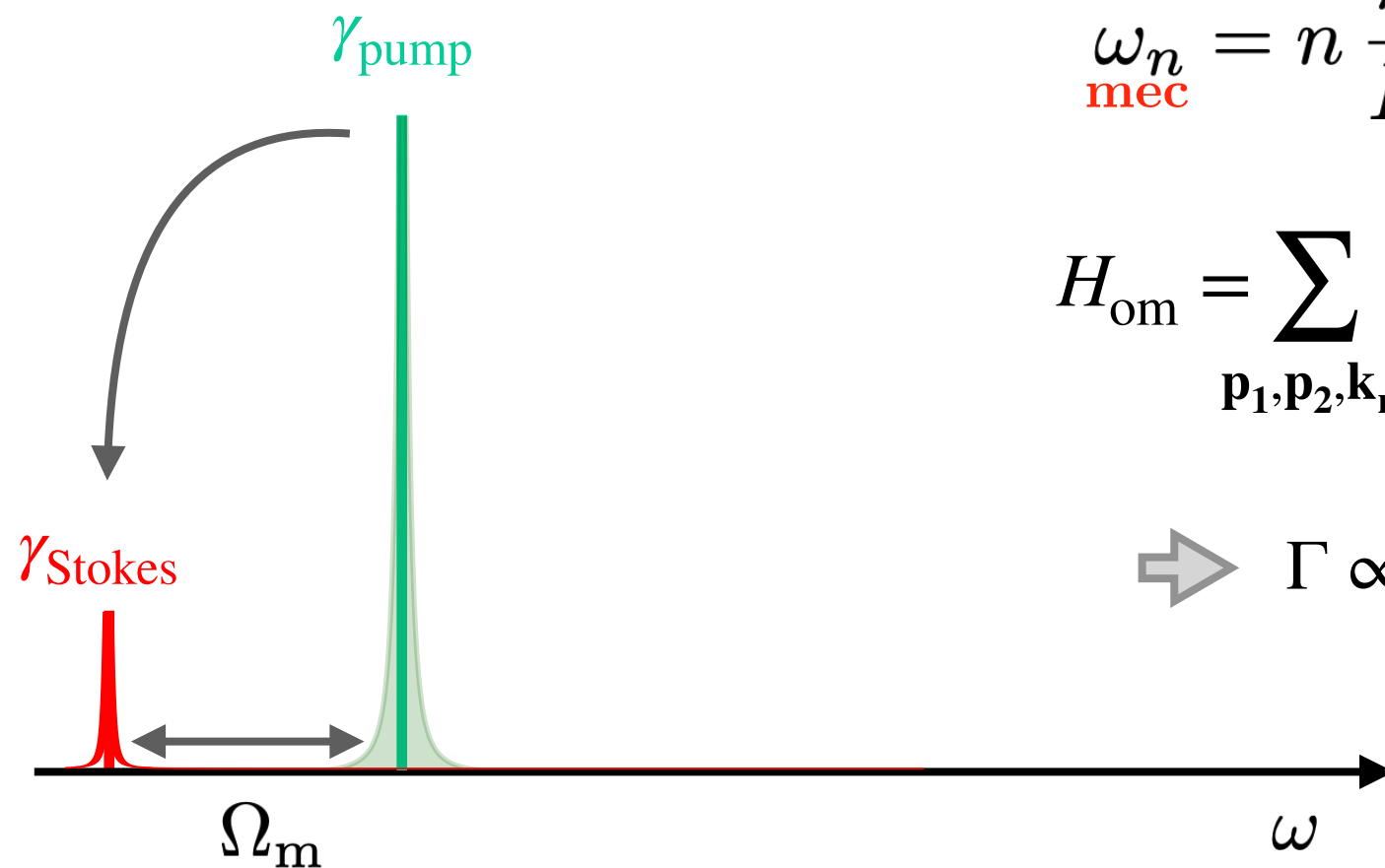
$$\Omega_m = 2c_s \omega_{\text{opt}}$$



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$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger \right)$$

$$\Rightarrow \Gamma \propto |g_0|^2 N_{\gamma, \text{pump}}$$



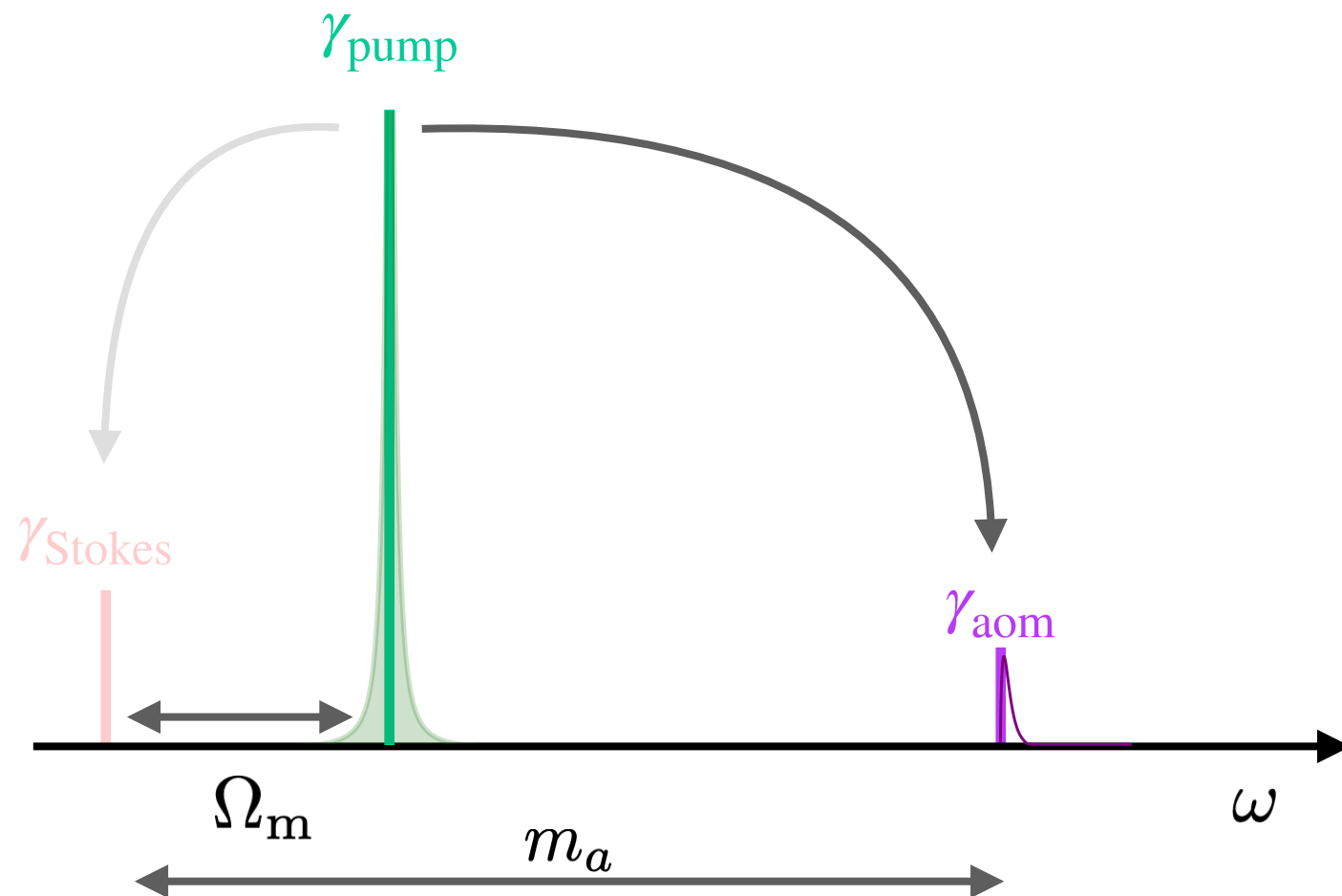
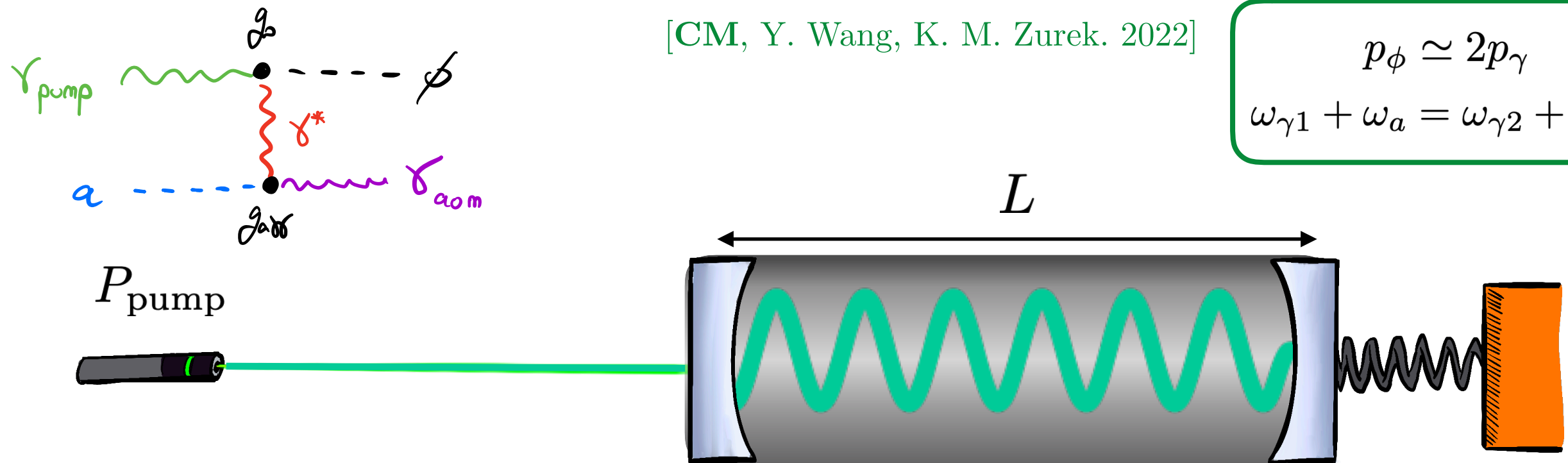
[Kashkanova et al., 2017]
[Reningner et al., 2017]

Standard Axioptomechanics

[CM, Y. Wang, K. M. Zurek. 2022]

$$p_\phi \simeq 2p_\gamma$$

$$\omega_{\gamma 1} + \omega_a = \omega_{\gamma 2} + \omega_\phi$$

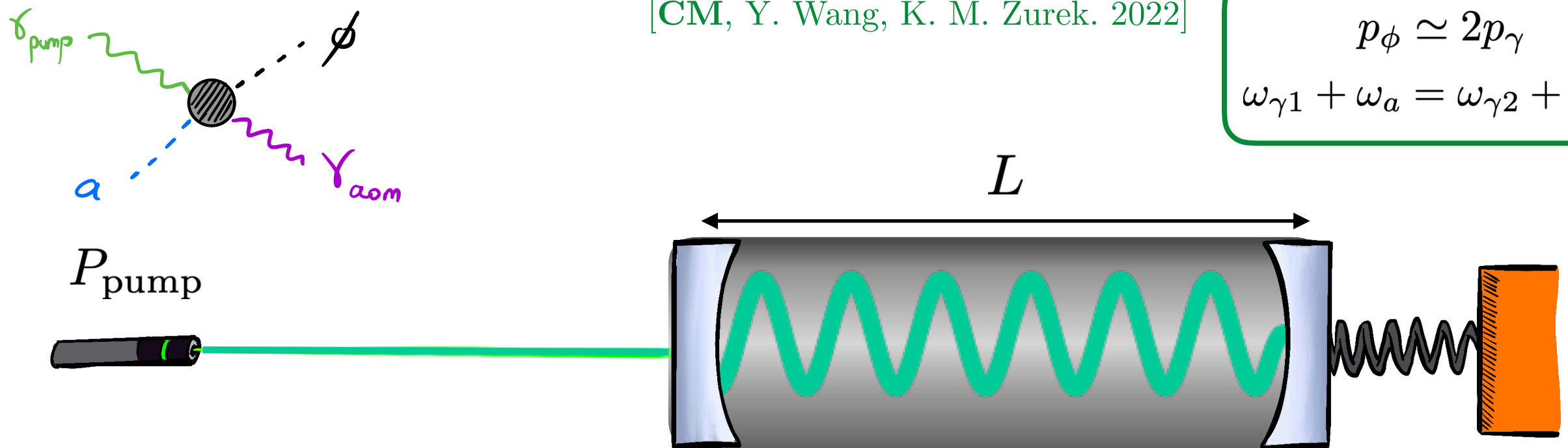


Standard Axioptomechanics

[CM, Y. Wang, K. M. Zurek. 2022]

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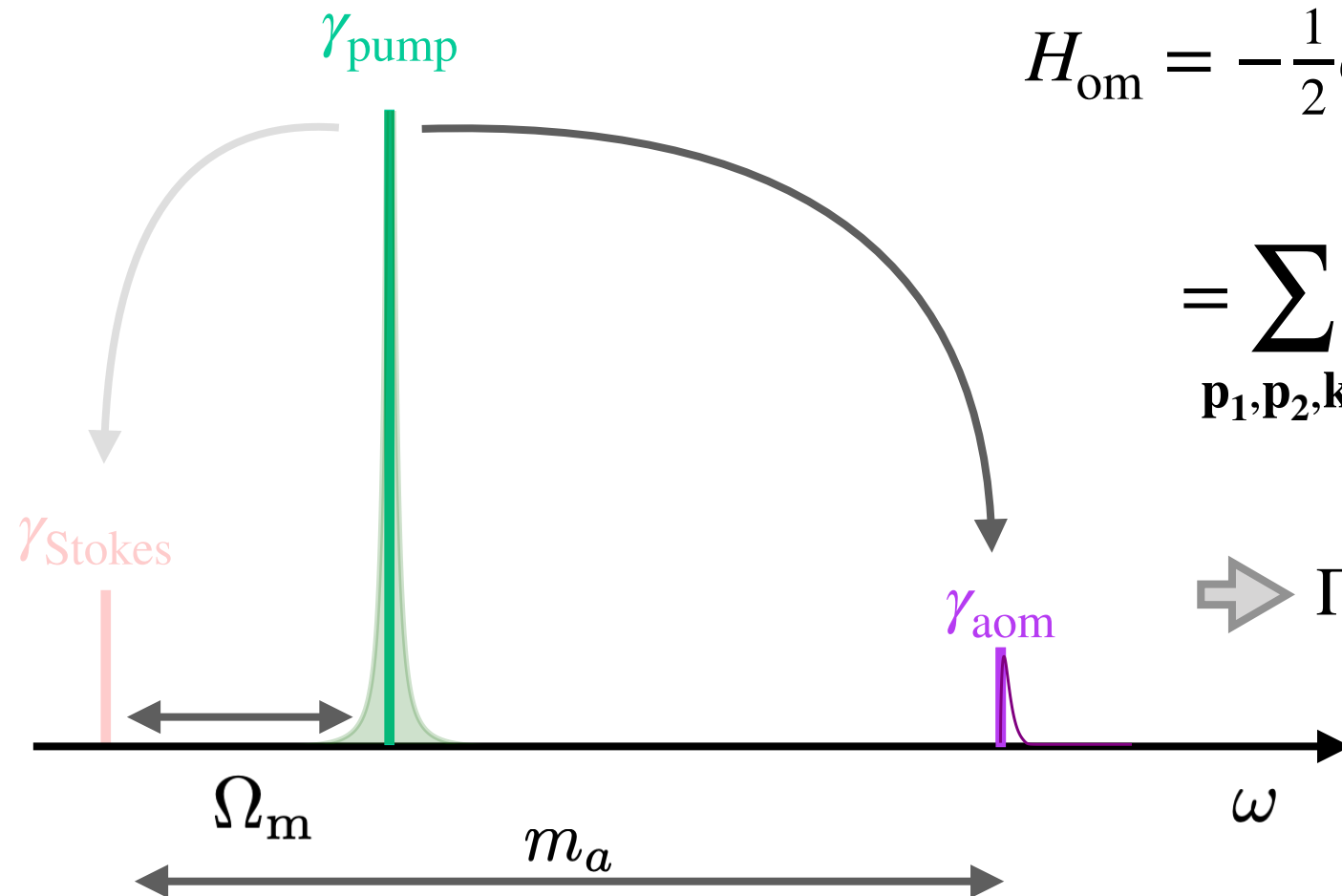
$$\omega_{\gamma 1} + \omega_a = \omega_{\gamma 2} + \omega_\phi$$



$$H_{\text{om}} = -\frac{1}{2}\alpha g_{a\gamma\gamma} \int d^3\mathbf{r} a(\mathbf{r}) n(\mathbf{r}) \mathbf{E}(\mathbf{r}) \cdot \mathbf{B}(\mathbf{r})$$

$$= \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0^{(a)} \left(g_{a\gamma\gamma} \frac{\sqrt{2\rho_a}}{m_a} \right) \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger \right)$$

$$\Rightarrow \Gamma \propto |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \times N_{\gamma, \text{pump}}$$

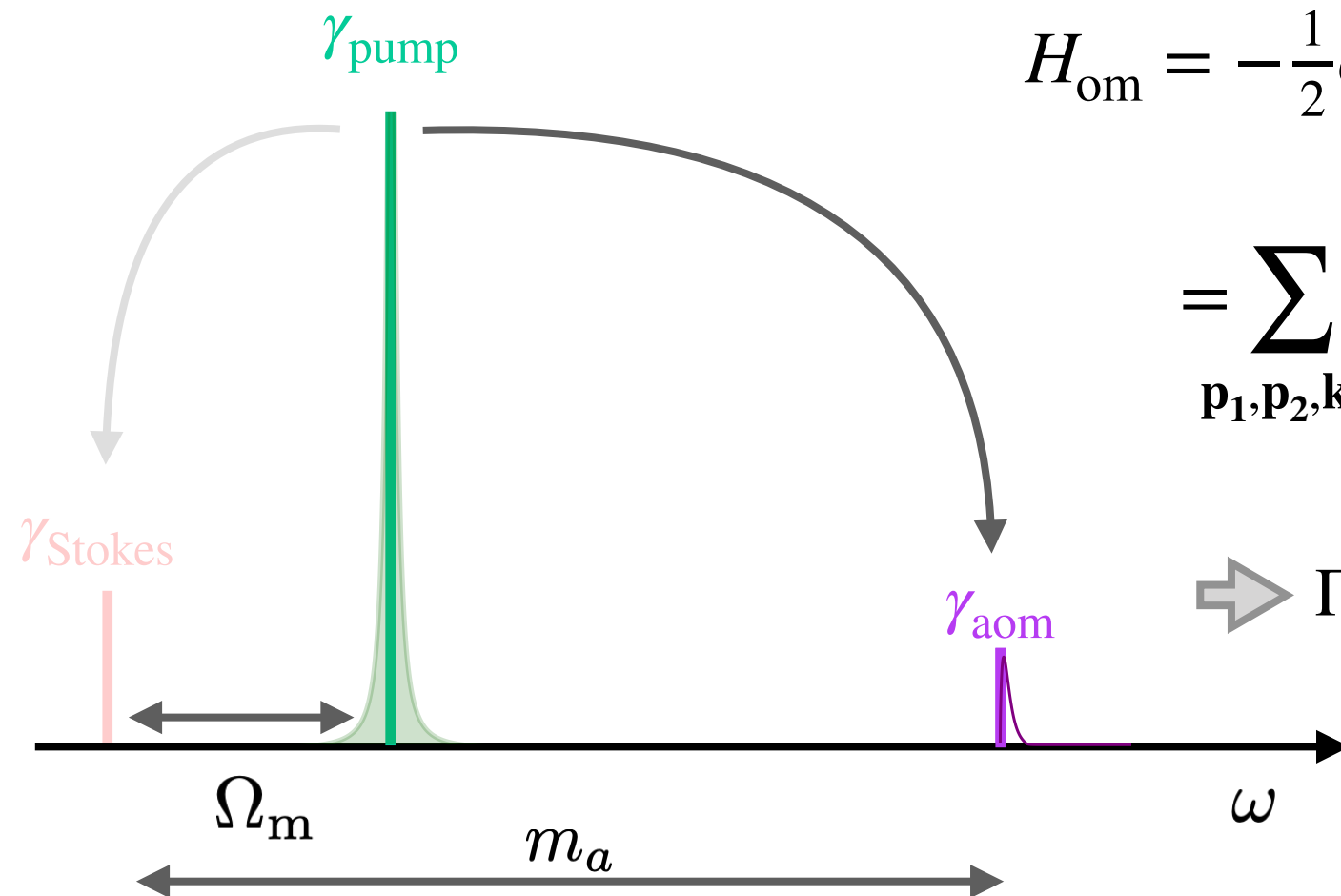
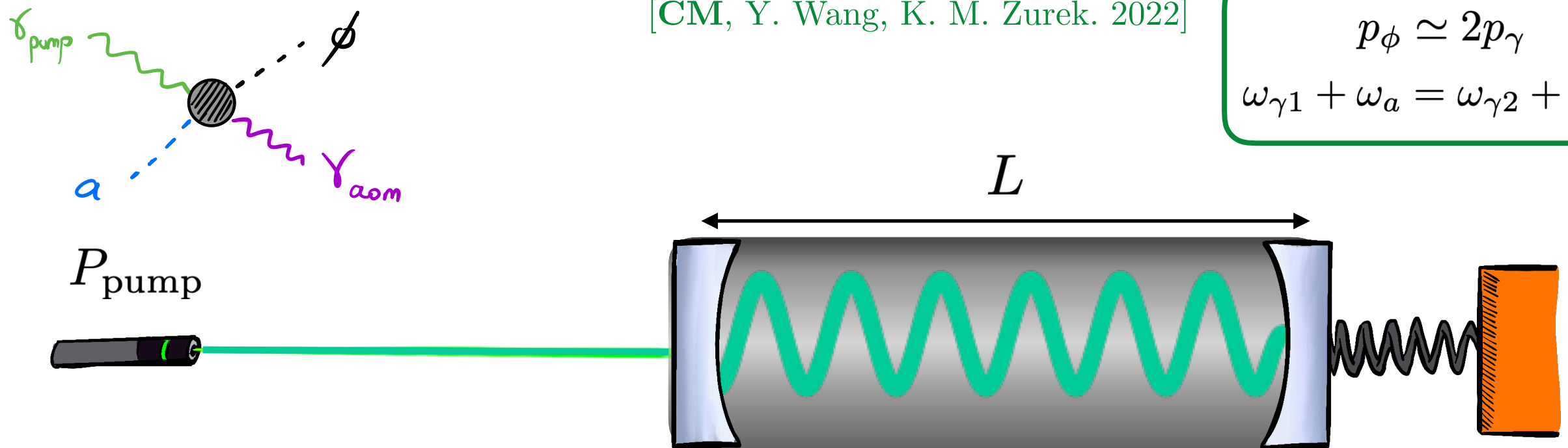


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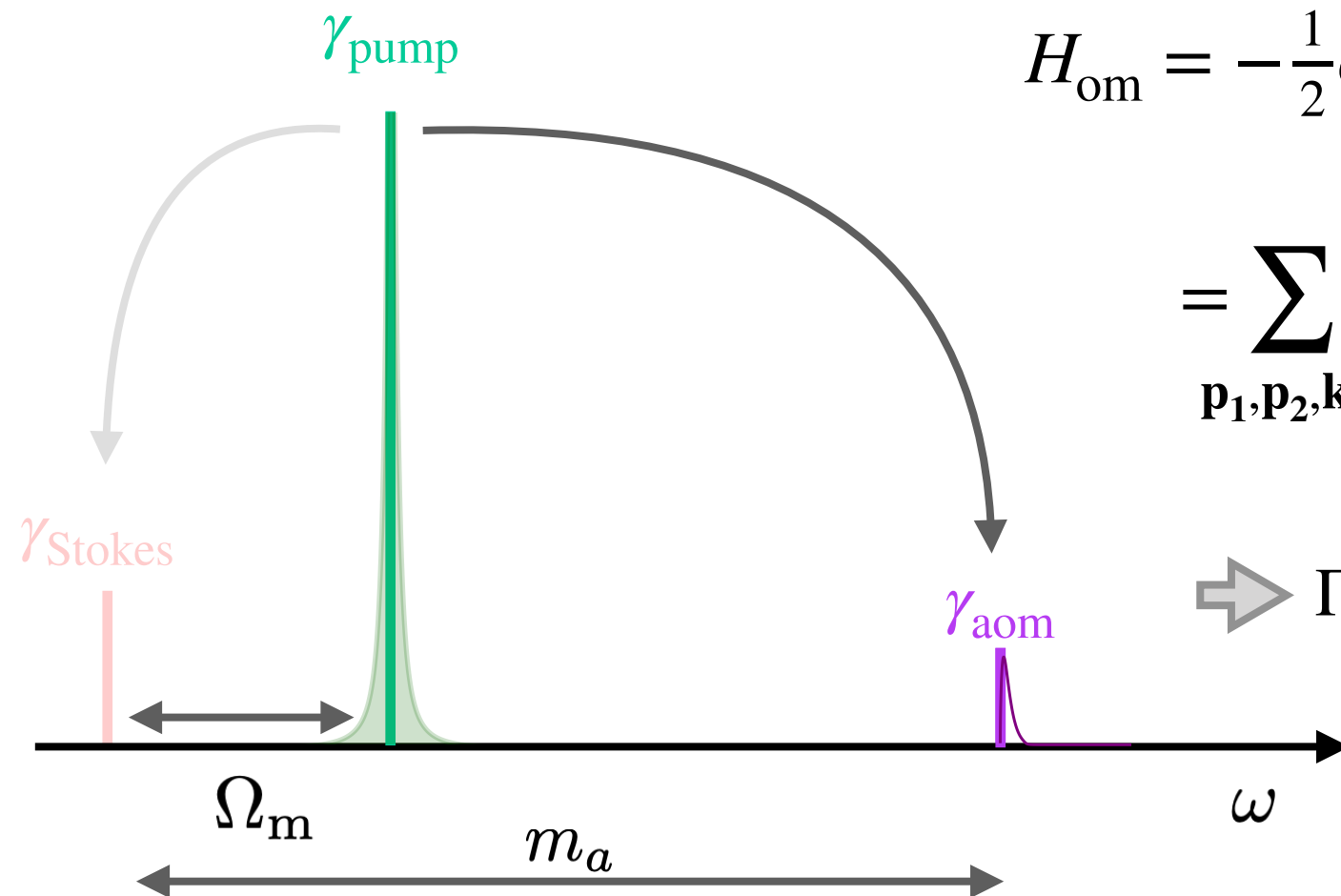
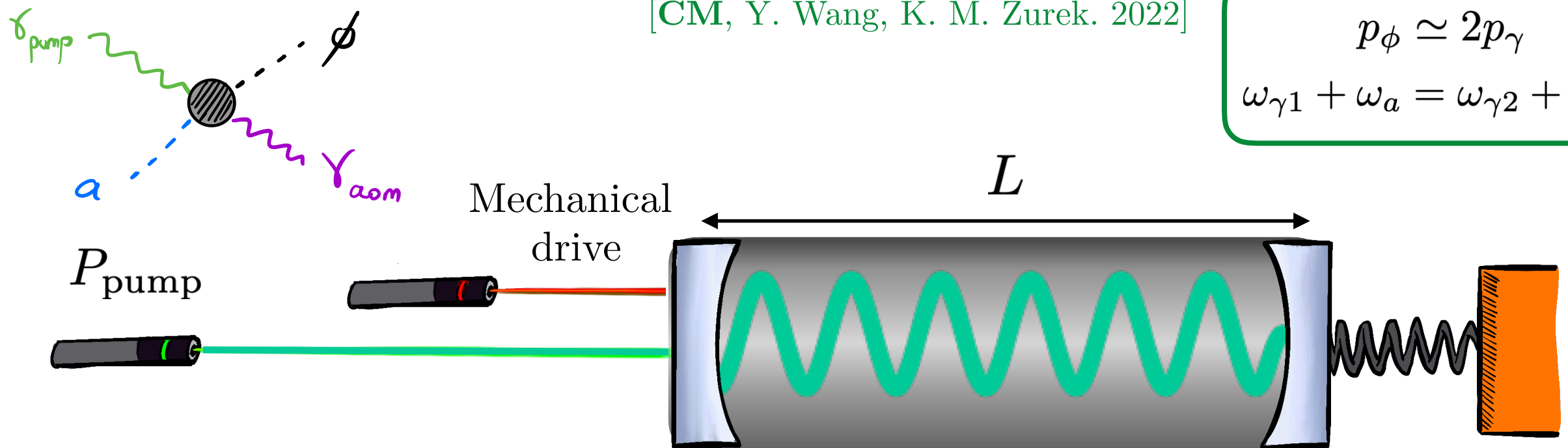
$\sim 10^{-22}$ for QCD axion

Coherent enhancement: Phonons

[CM, Y. Wang, K. M. Zurek. 2022]

$$p_\phi \simeq 2p_\gamma$$

$$\omega_{\gamma 1} + \omega_a = \omega_{\gamma 2} + \omega_\phi$$



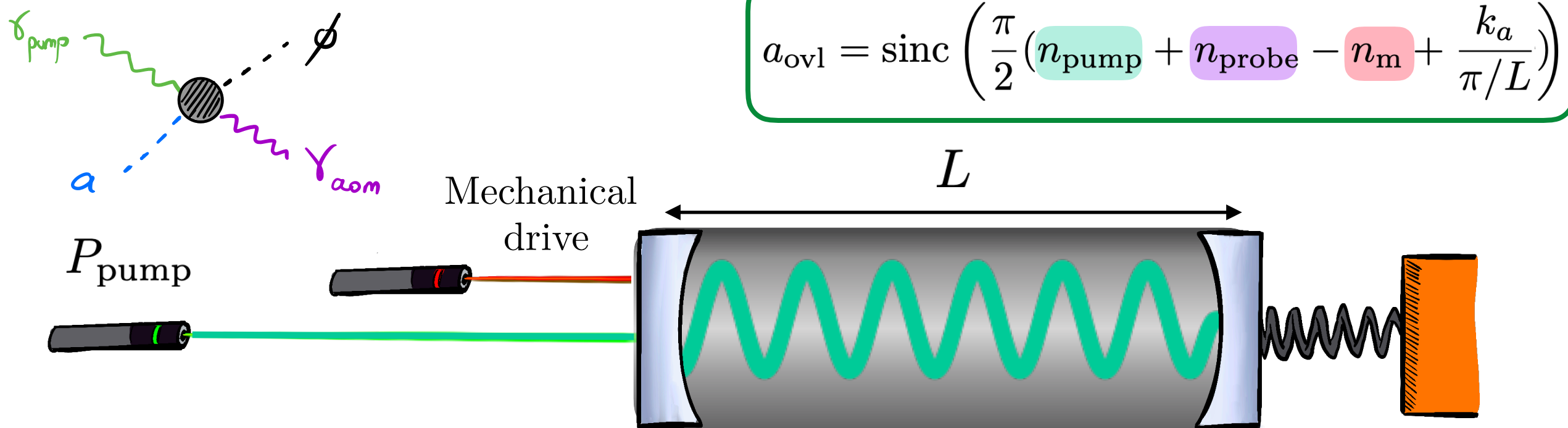
$$H_{\text{om}} = -\frac{1}{2}\alpha g_{a\gamma\gamma} \int d^3\mathbf{r} a(\mathbf{r}) n(\mathbf{r}) \mathbf{E}(\mathbf{r}) \cdot \mathbf{B}(\mathbf{r})$$

$$= \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0^{(a)} \left(g_{a\gamma\gamma} \frac{\sqrt{2\rho_a}}{m_a} \right) (a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger)$$

$$\Rightarrow \Gamma \propto |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \times N_{\gamma, \text{pump}} N_\phi^{\text{circ}} [\Delta_m]$$

$\sim 10^{-22}$ for QCD axion

Axiptomechanics: Rates



$$a_{\text{ovl}} = \text{sinc} \left(\frac{\pi}{2} (n_{\text{pump}} + n_{\text{probe}} - n_{\text{m}} + \frac{k_a}{\pi/L}) \right)$$

$$H_{\text{om}} = -\frac{1}{2} \alpha g_{a\gamma\gamma} \int d^3\mathbf{r} a(\mathbf{r}) n(\mathbf{r}) \mathbf{E}(\mathbf{r}) \cdot \mathbf{B}(\mathbf{r})$$

$$= \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0^{(a)} \left(g_{a\gamma\gamma} \frac{\sqrt{2\rho_a}}{m_a} \right) (a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger)$$

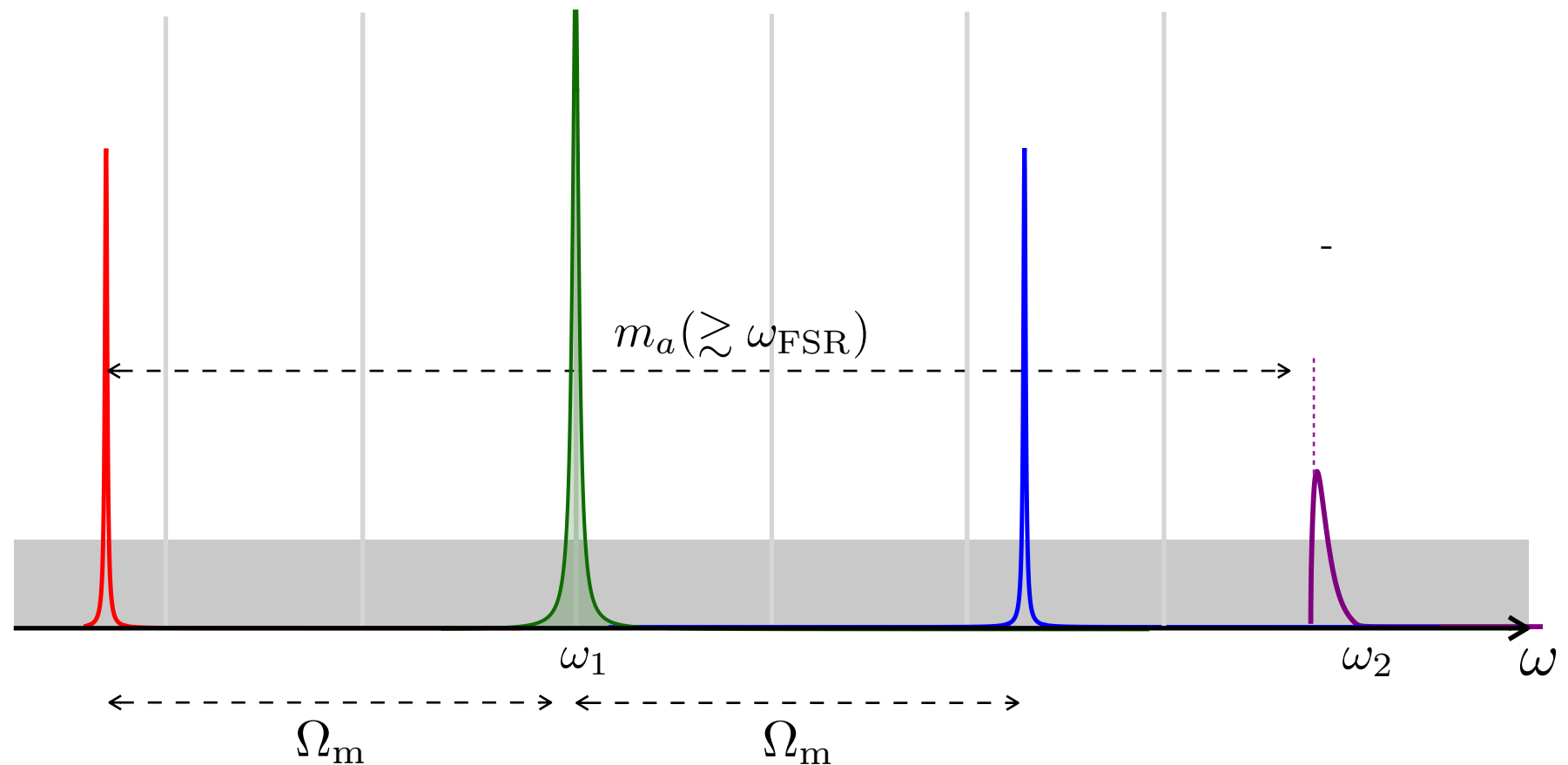
Phonon populated

$$\Rightarrow \Gamma = (2\pi) |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \int d\omega_{\gamma_{\text{aom}}} B_{m_a}(\omega_{\gamma_{\text{aom}}} + \Omega_m - \omega_{\text{pump}}) L(\omega_{\gamma_{\text{aom}}} - \omega_{\text{res}}, \kappa) \times N_{\gamma, \text{pump}} N_{\phi}^{\text{circ}} [\Delta_m]$$

[CM, Y. Wang, K. M. Zurek. 2022]

Axioptomechanics: Sensitivity

$$\text{SNR} = \frac{\Gamma_{\text{sig}} (t_{\text{int}}/\tau_a)}{\Gamma_{\text{back}}} > 3$$



Phonon populated

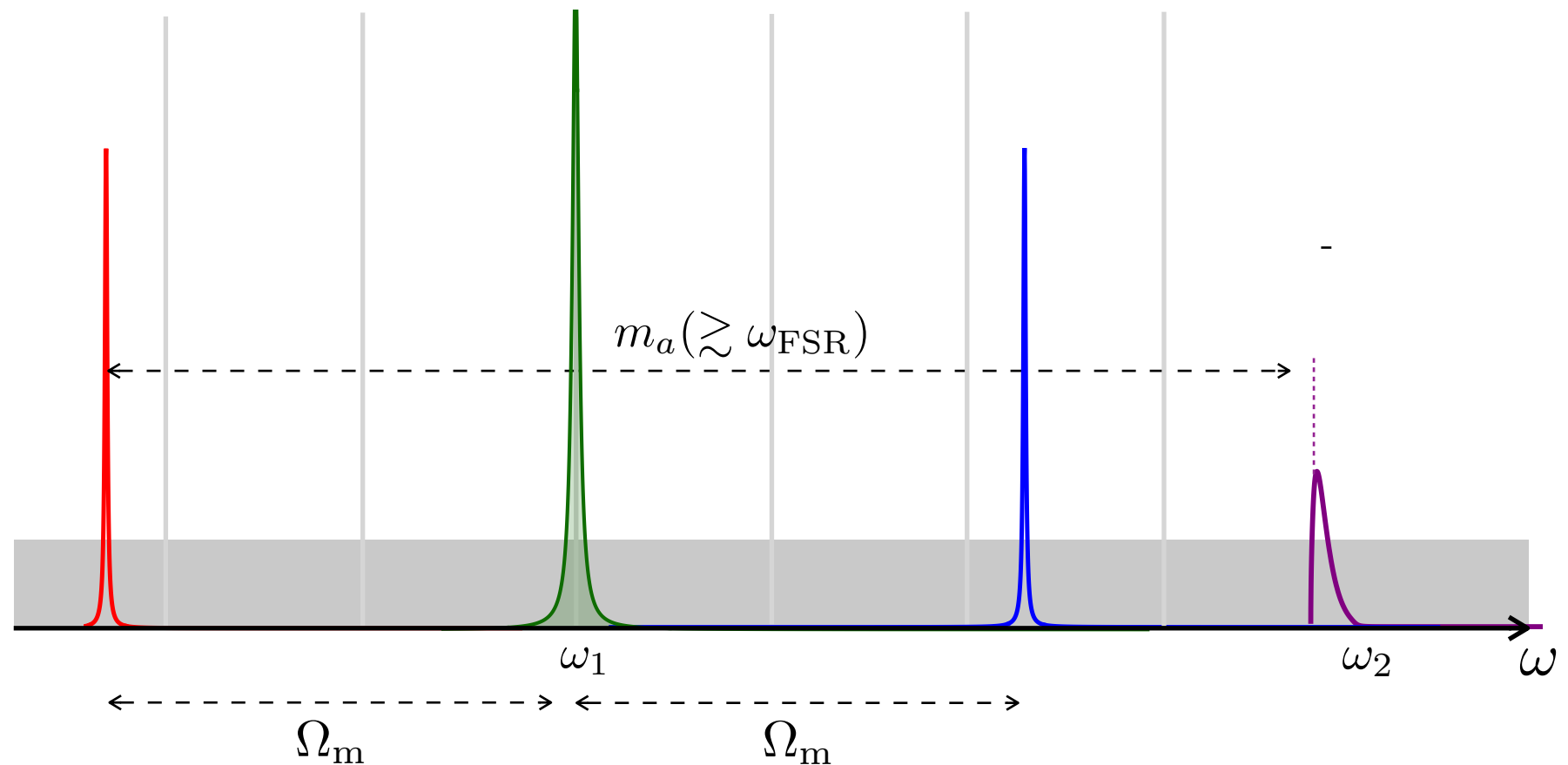
$$\Rightarrow \Gamma = (2\pi) |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \int d\omega_{\gamma_{\text{aom}}} B_{m_a}(\omega_{\gamma_{\text{aom}}} + \Omega_m - \omega_{\text{pump}}) L(\omega_{\gamma_{\text{aom}}} - \omega_{\text{res}}, \kappa) \times N_{\gamma, \text{pump}} N_{\phi}^{\text{circ}} [\Delta_m]$$



[CM, Y. Wang, K. M. Zurek. 2022]

Axioptomechanics: Sensitivity

$$\text{SNR} = \frac{\Gamma_{\text{sig}} (t_{\text{int}}/\tau_a)}{\Gamma_{\text{back}}} > 3 \Rightarrow g_{a\gamma\gamma} > f(m_a, \text{cavity, lasers, material})$$



Phonon populated

$$\Rightarrow \Gamma = (2\pi) |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \int d\omega_{\gamma_{\text{aom}}} B_{m_a}(\omega_{\gamma_{\text{aom}}} + \Omega_m - \omega_{\text{pump}}) L(\omega_{\gamma_{\text{aom}}} - \omega_{\text{res}}, \kappa) \times N_{\gamma, \text{pump}} N_{\phi}^{\text{circ}} [\Delta_m]$$



[CM, Y. Wang, K. M. Zurek. 2022]

Axioptomechanics: Numbers

[A.D. Kashkanova, A.B. Shkarin, C.D. Brown, et al. , 2017]

He For usual experiments in their lab:

$$\Rightarrow N_{\text{pump}} \simeq 10^6$$

$$P_{\text{pump}} \sim 1 \mu\text{W}$$

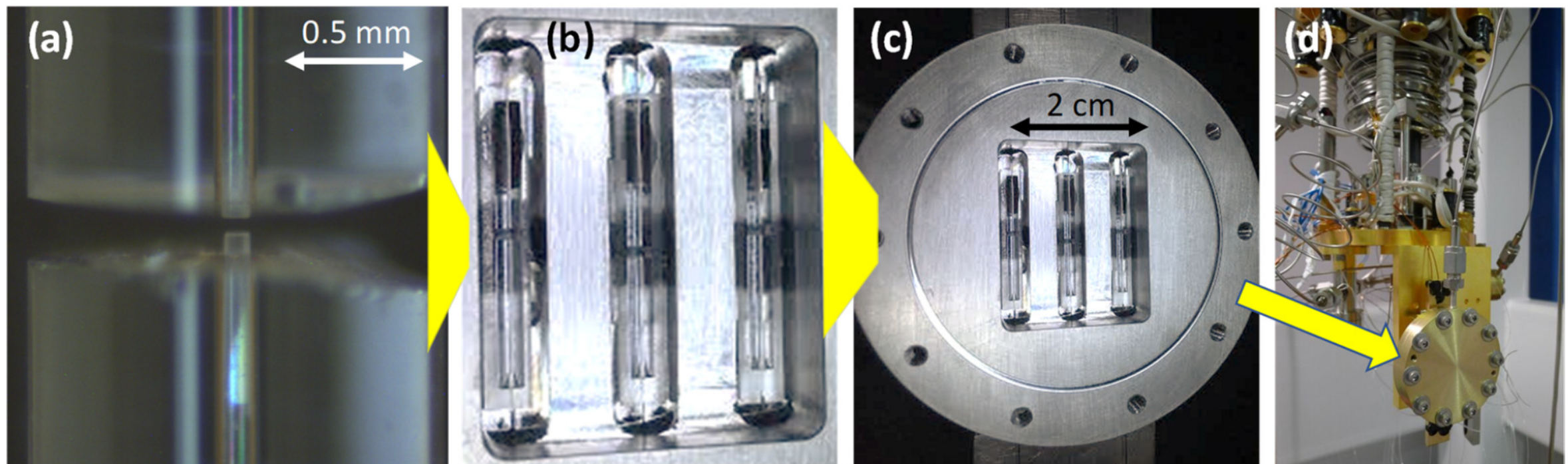
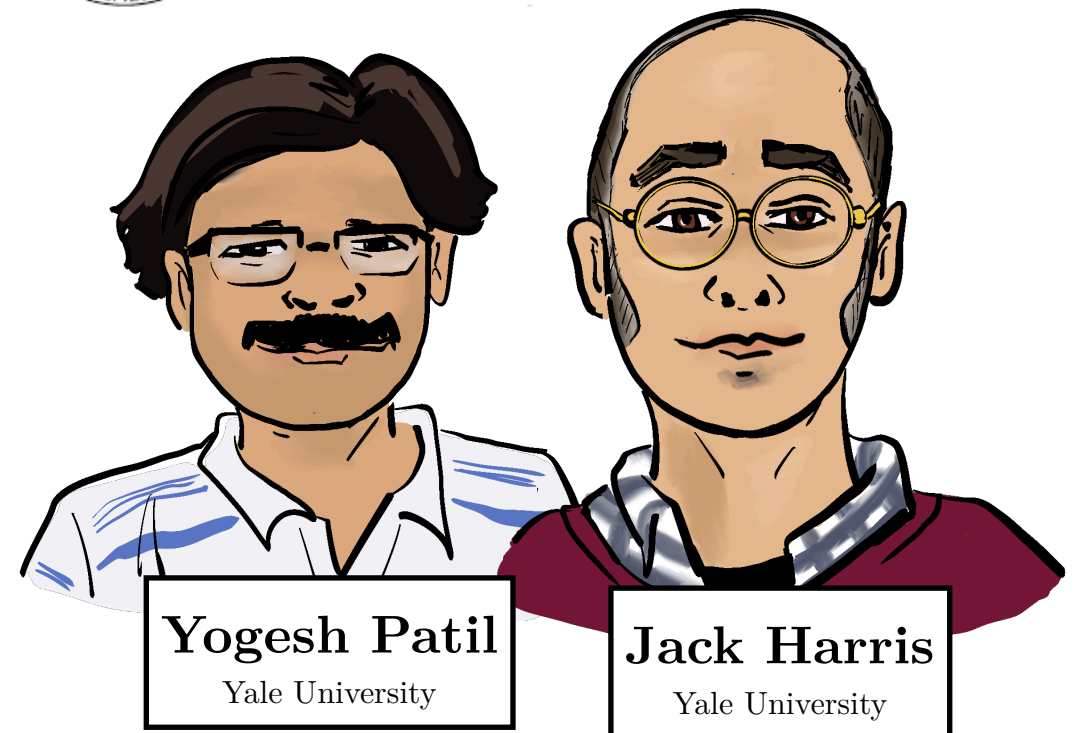
$$\Rightarrow N_{\phi} \simeq 10^5$$

$$L \sim 100 \mu\text{m}$$

$$\mathcal{F}_{\text{opt}}/\pi \sim 10^5$$



Yale University Jack Harris Lab



Axioptomechanics: Numbers

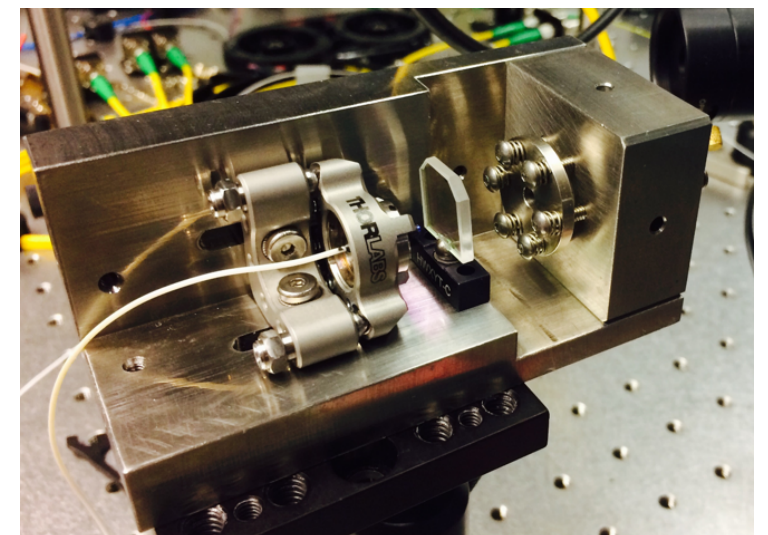
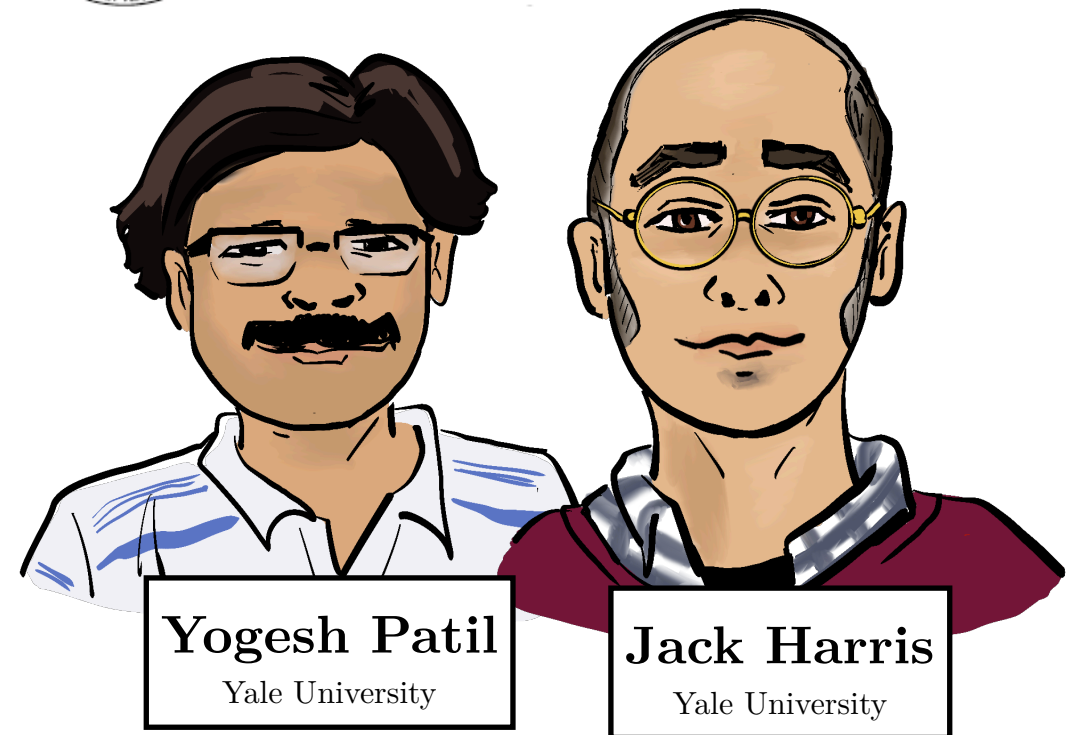
[A.D. Kashkanova, A.B. Shkarin, C.D. Brown, et al. , 2017]

He What could be feasible to achieve:

$$\begin{aligned} \Rightarrow N_{\text{pump}} &\simeq 10^{17} & P_{\text{pump}} &\sim 1 \text{ W} \\ \Rightarrow N_{\phi} &\simeq 10^{14} & L &\sim 1 \text{ m} \\ & & \mathcal{F}_{\text{opt}}/\pi &\sim 10^6 \end{aligned}$$



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RadioOptomechanics: Numbers

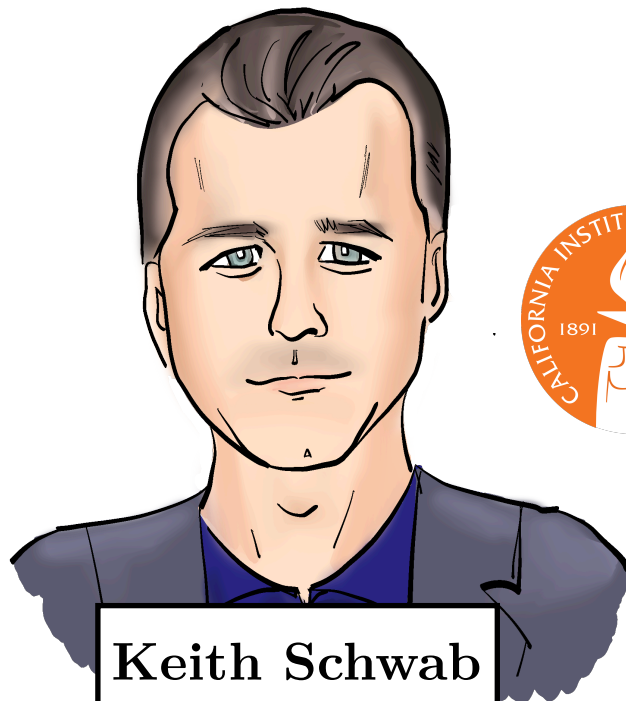
[A.D. Kashkanova, A.B. Shkarin, C.D. Brown, et al. , 2017]



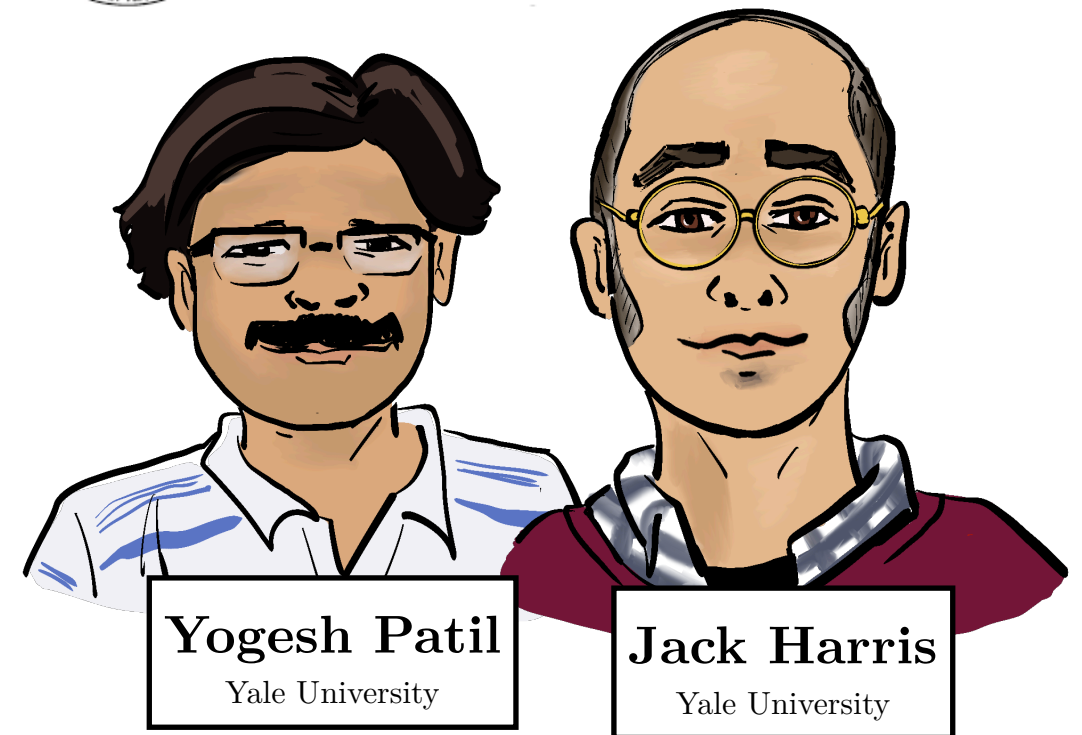
Yale University Jack Harris Lab

He What could be feasible to achieve:

$$\begin{aligned} \Rightarrow N_{\text{pump}} &\simeq 10^{17} & P_{\text{pump}} &\sim 1 \text{ W} \\ \Rightarrow N_{\phi} &\simeq 10^{14} & L &\sim 1 \text{ m} \\ & & \mathcal{F}_{\text{opt}}/\pi &\sim 10^6 \end{aligned}$$



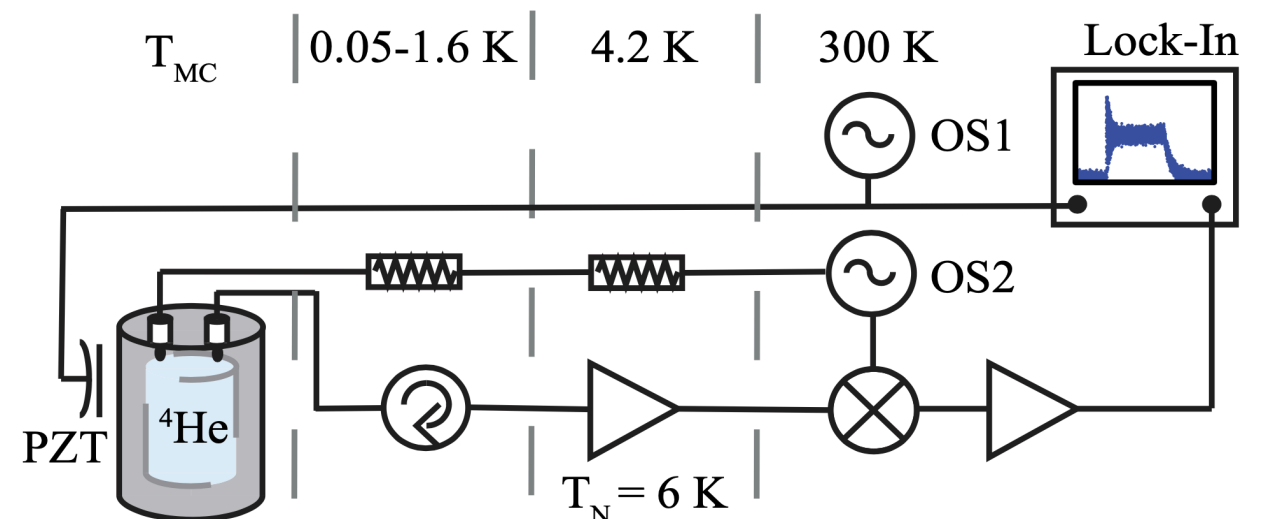
Keith Schwab
Caltech



Yogesh Patil
Yale University

Jack Harris
Yale University

[A. L. De Lorenzo, K. C. Schwab, 2017]



He

$$\begin{aligned} \Rightarrow N_{\text{pump}} &\simeq 10^{12} & P_{\text{pump}} &\sim 1 \mu\text{W} \\ \Rightarrow N_{\phi} &\simeq 10^{15} & L &\sim 4 \text{ cm} \\ & & \mathcal{F}_{\text{opt}}/\pi &\sim 10^8 \end{aligned}$$

Axioptomechanics: Numbers

Si What could be feasible to achieve:

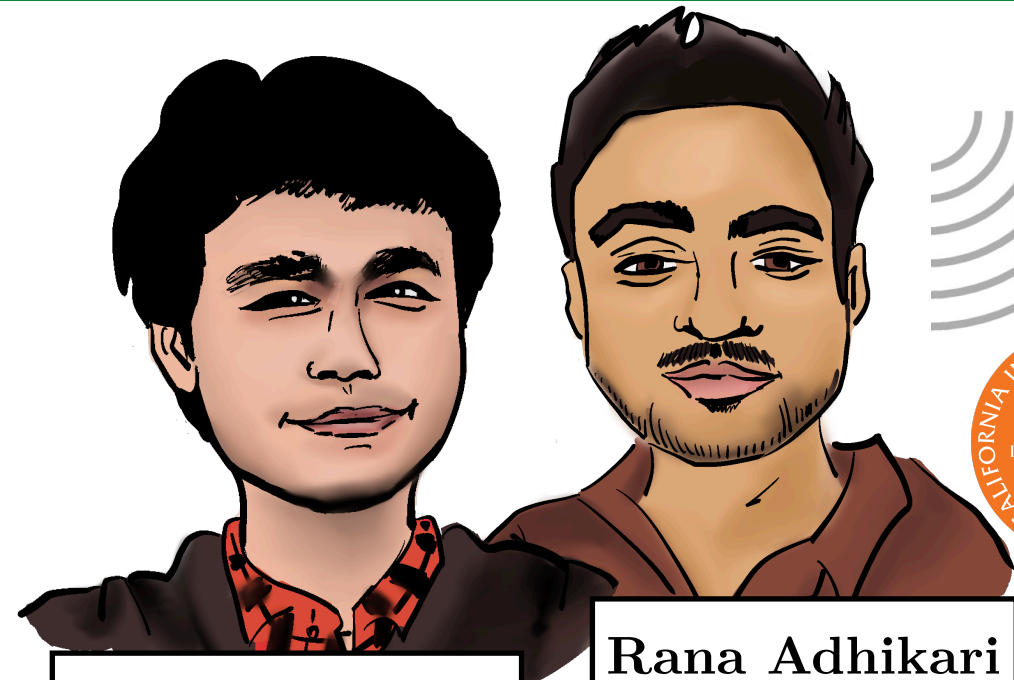
$$\Rightarrow N_{\text{pump}} \simeq 10^{16}$$

$$\Rightarrow N_{\phi} \simeq 10^{19}$$

$$P_{\text{pump}} \sim 1 \text{ W}$$

$$L \sim 10 \text{ cm}$$

$$\mathcal{F}_{\text{opt}}/\pi \sim 10^6$$



Yuta Michimura

Caltech, U. Tokyo

Rana Adhikari

Caltech



Axiotomechanics: Numbers

Si What could be feasible to achieve:

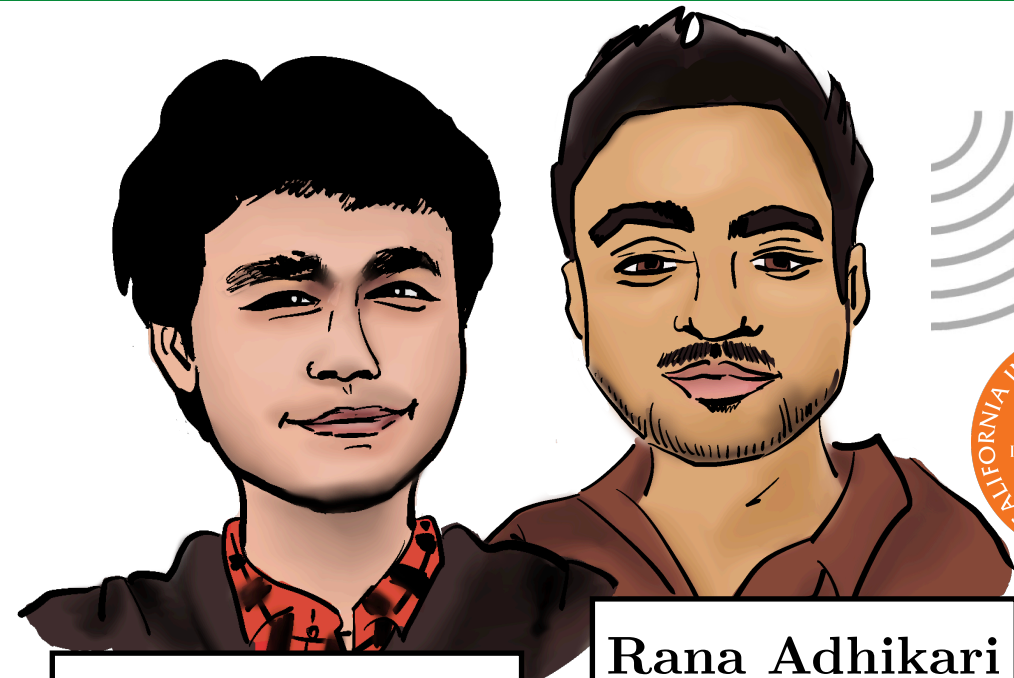
$$\Rightarrow N_{\text{pump}} \simeq 10^{16}$$

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$$P_{\text{pump}} \sim 1 \text{ W}$$

$$L \sim 10 \text{ cm}$$

$$\mathcal{F}_{\text{opt}}/\pi \sim 10^6$$

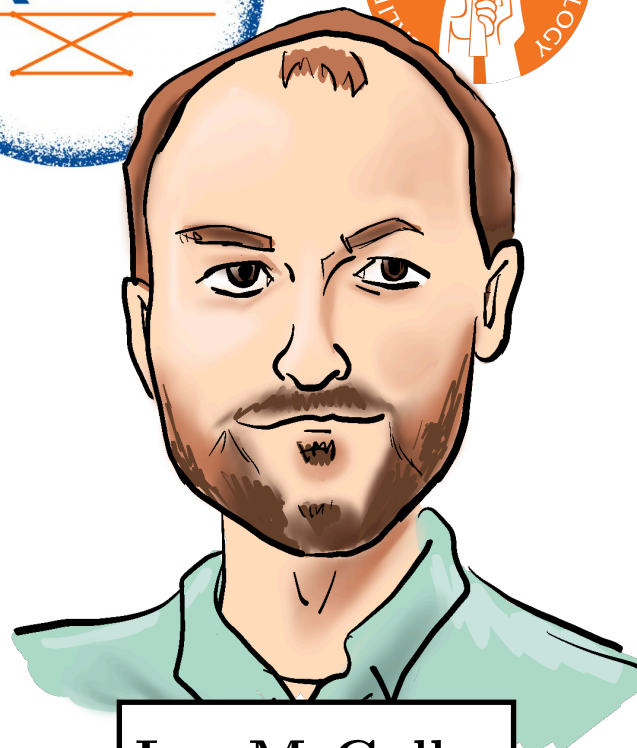


Yuta Michimura

Caltech, U. Tokyo

Rana Adhikari

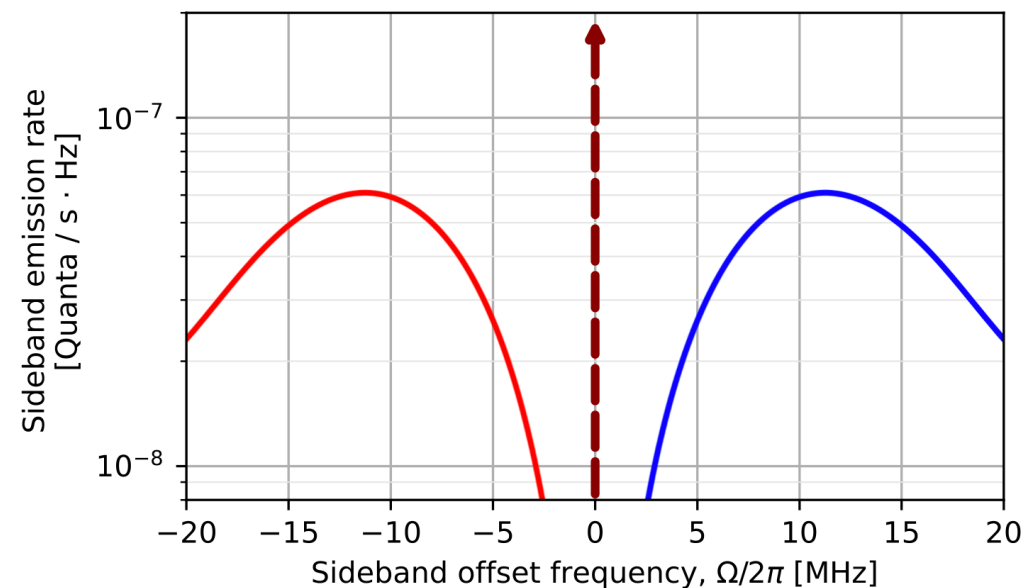
Caltech



Lee McCuller

Caltech,

[L. McCuller, 2022]



$$\Rightarrow N_{\text{pump}} \simeq 10^{22}$$

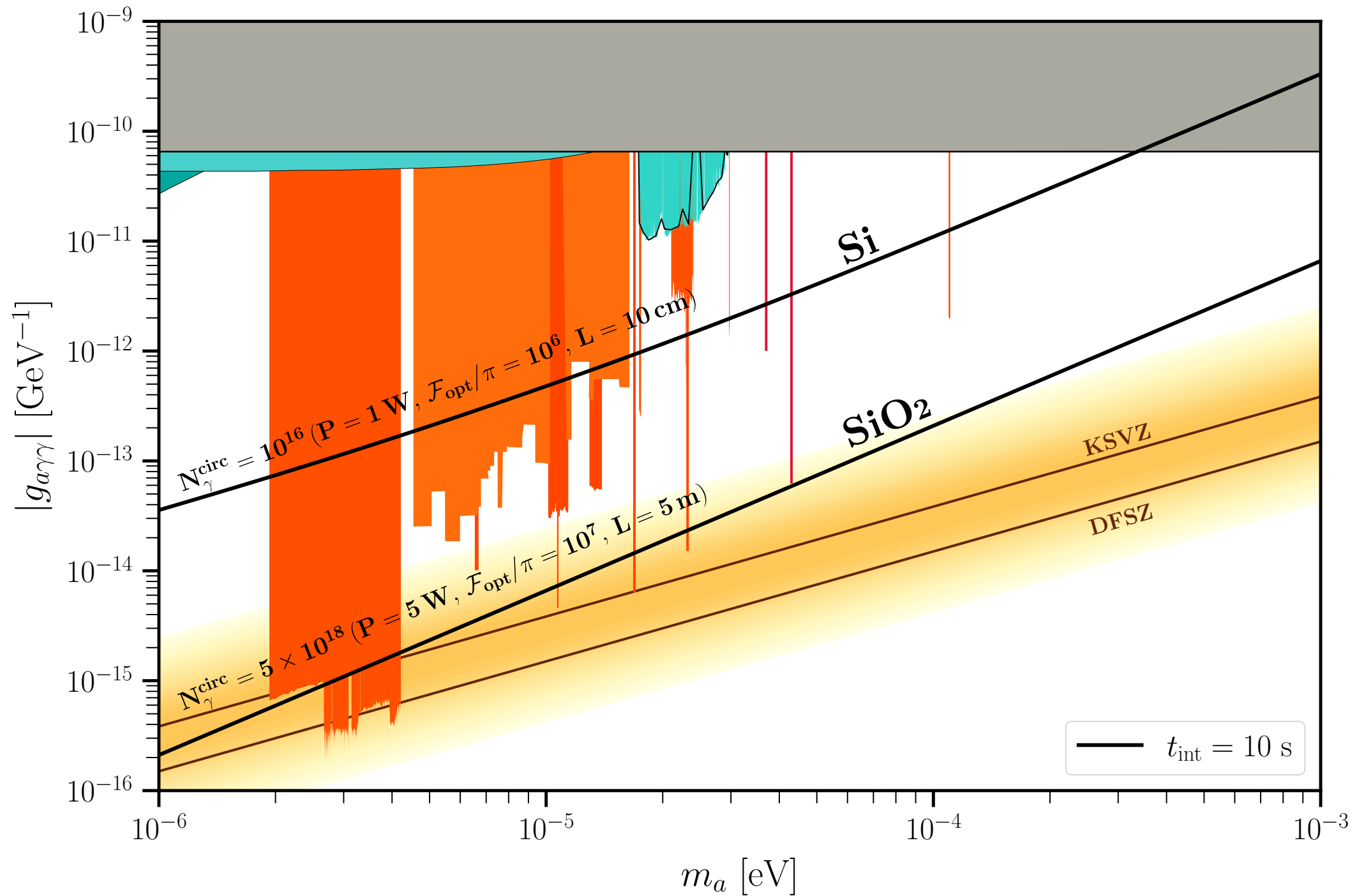
$$P_{\text{pump}} \sim 10 \text{ kW}$$

$$L \sim 5 \text{ m}$$

$$\mathcal{F}_{\text{opt}}/\pi \sim 10^6$$

Sensitivity: heavy axion regime

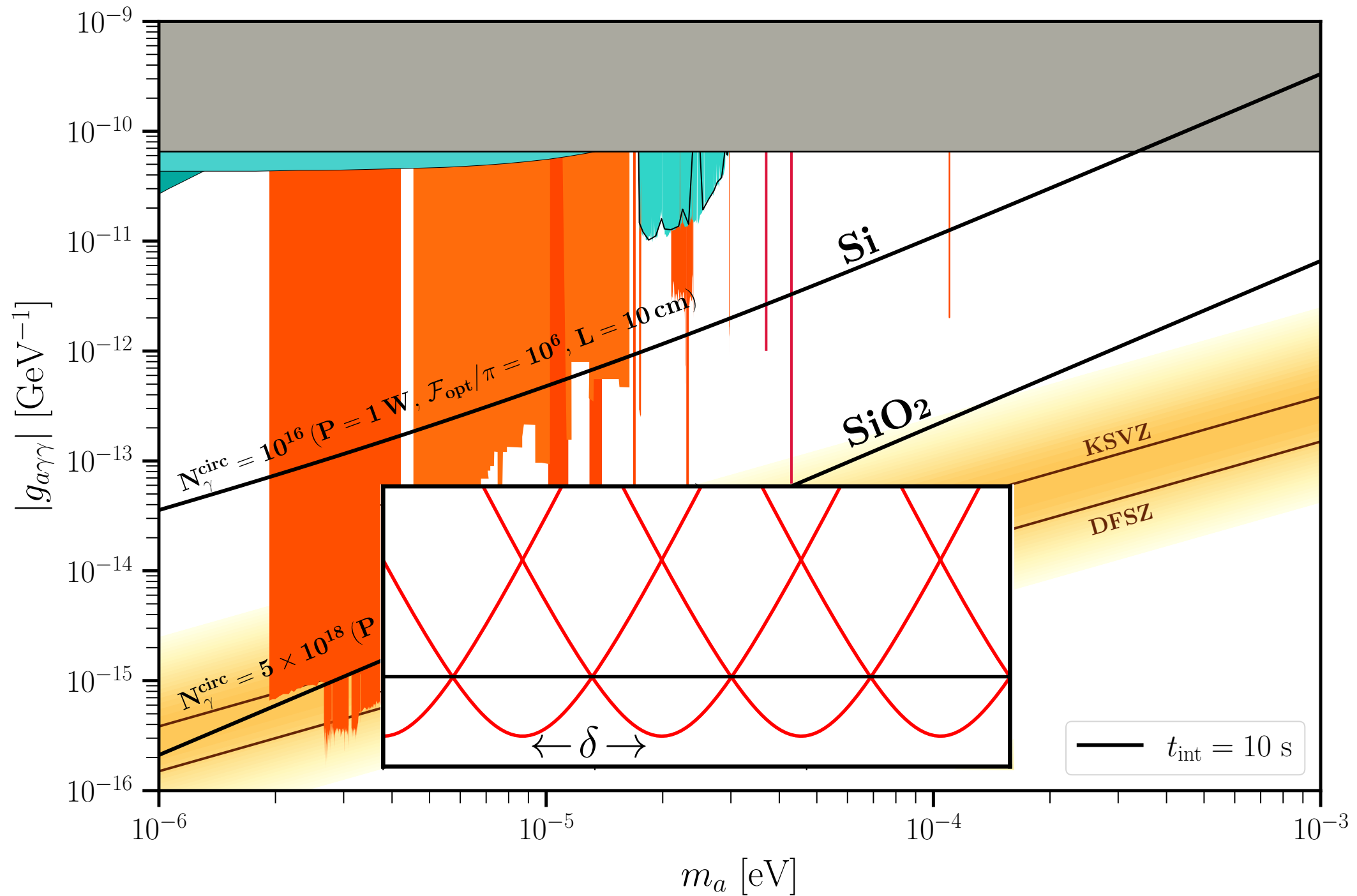
[CM, Y. Wang, K. M. Zurek. 2022]



$$g_{a\gamma\gamma}^{\phi\text{-pop}} \propto \frac{\epsilon_r + 2}{\epsilon_r - 1} \epsilon_r^{1/2} \frac{1}{\mathcal{F}_{\text{opt}}^{1/2}} \frac{1}{L^{1/2}} \frac{1}{\omega_{\text{opt}}^{1/2}} \frac{1}{P_{\text{pump}}^{1/2}} \frac{m_a^{3/2}}{\rho_a^{1/2}} \Gamma_{\text{DCR}}^{1/2}$$

Sensitivity: heavy axion regime

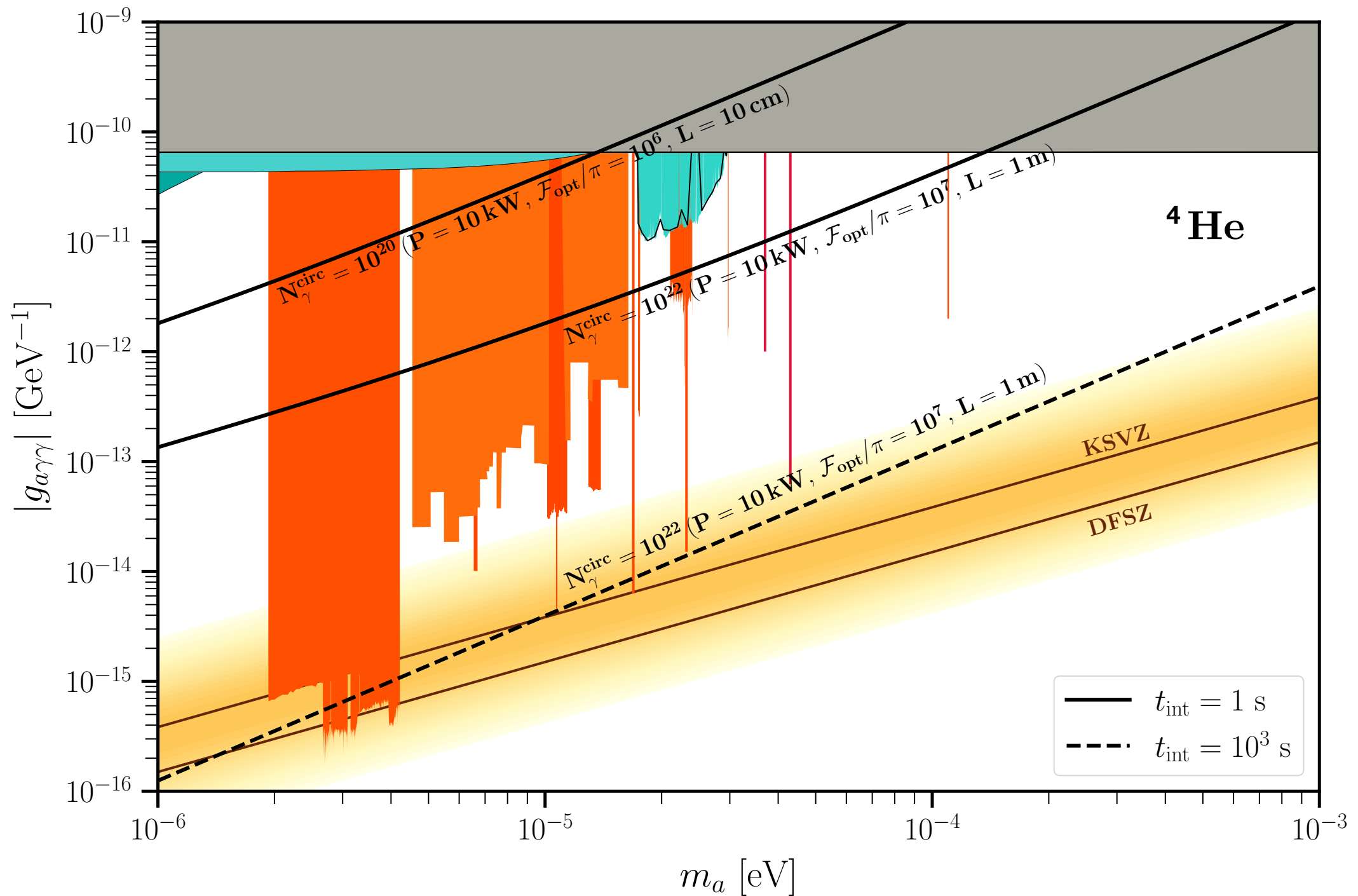
[CM, Y. Wang, K. M. Zurek. 2022]



$$g_{a\gamma\gamma}^{\phi\text{-pop}} \propto \frac{\epsilon_r + 2}{\epsilon_r - 1} \epsilon_r^{1/2} \frac{1}{\mathcal{F}_{\text{opt}}^{1/2}} \frac{1}{L^{1/2}} \frac{1}{\omega_{\text{opt}}^{1/2}} \frac{1}{P_{\text{pump}}^{1/2}} \frac{m_a^{3/2}}{\rho_a^{1/2}} \Gamma_{\text{DCR}}^{1/2}$$

Sensitivity: heavy axion regime

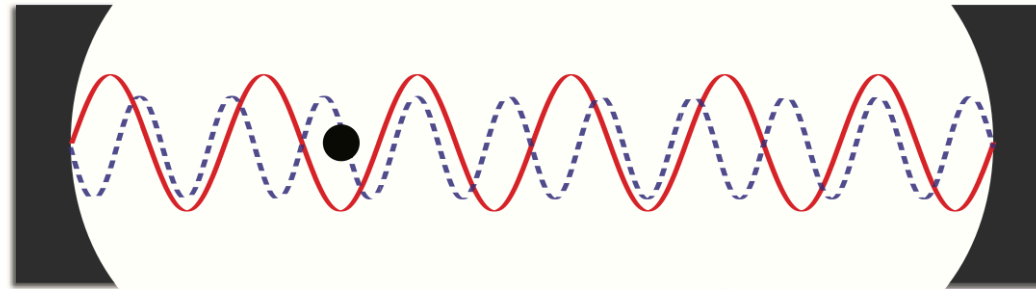
[CM, Y. Wang, K. M. Zurek. 2022]



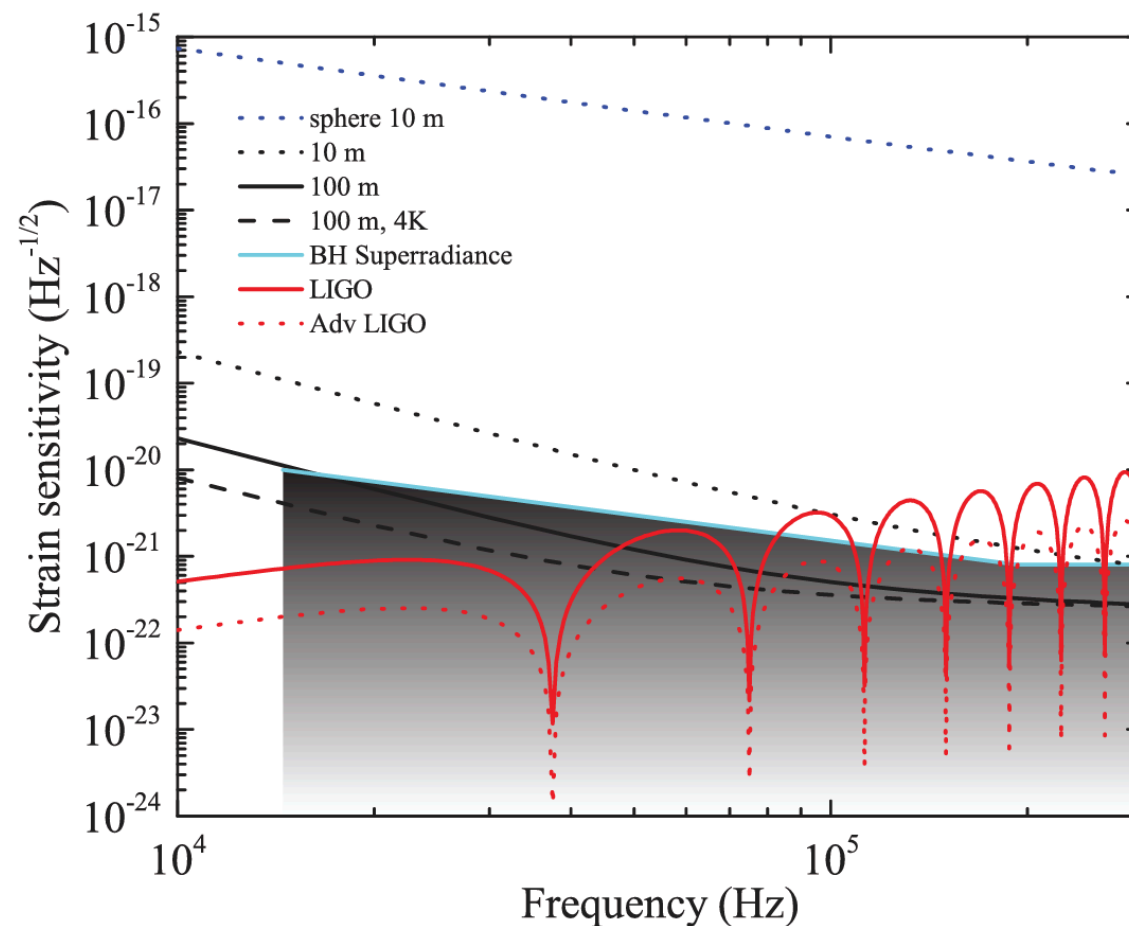
$$g_{a\gamma\gamma}^{\phi\text{-pop}} \propto \frac{\epsilon_r + 2}{\epsilon_r - 1} \epsilon_r^{1/2} \frac{1}{\mathcal{F}_{\text{opt}}^{1/2}} \frac{1}{L^{1/2}} \frac{1}{\omega_{\text{opt}}^{1/2}} \frac{1}{P_{\text{pump}}^{1/2}} \frac{m_a^{3/2}}{\rho_a^{1/2}} \Gamma_{\text{DCR}}^{1/2}$$

Optomechanics

High-Frequency Gravitational Waves with Optically Levitated Sensors
[Arvanitaki, Geraci, 2013]



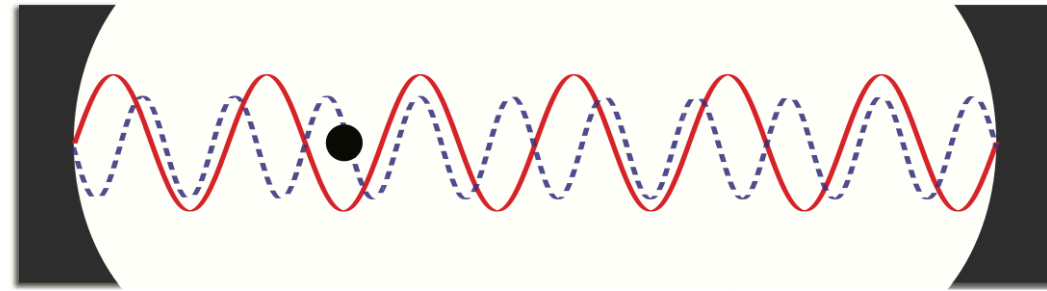
$$F_{gw} = -\frac{m\omega_{gw}^2}{2}(x_s - \ell_m)h_o \cos(\omega_{gw}t + \Delta\phi)$$



Optomechanics

High-Frequency Gravitational Waves with Optically Levitated Sensors

[Arvanitaki, Geraci, 2013]



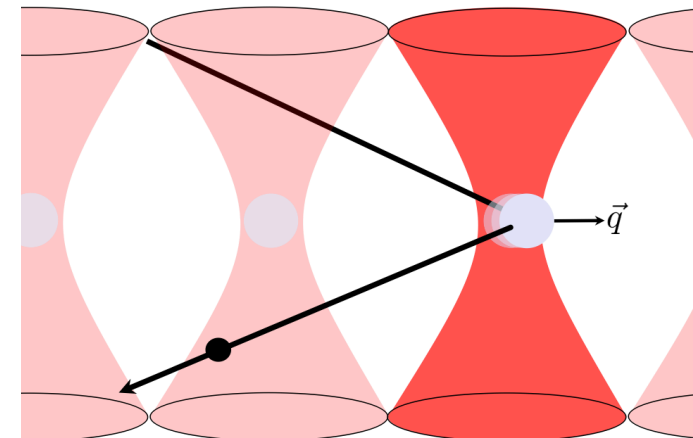
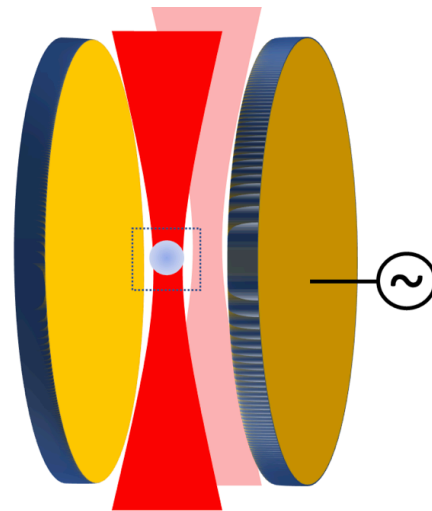
Dark Matter searches with optically levitated sensors

[Monteiro et al., 2020]

[Afek, et. al., 2021]

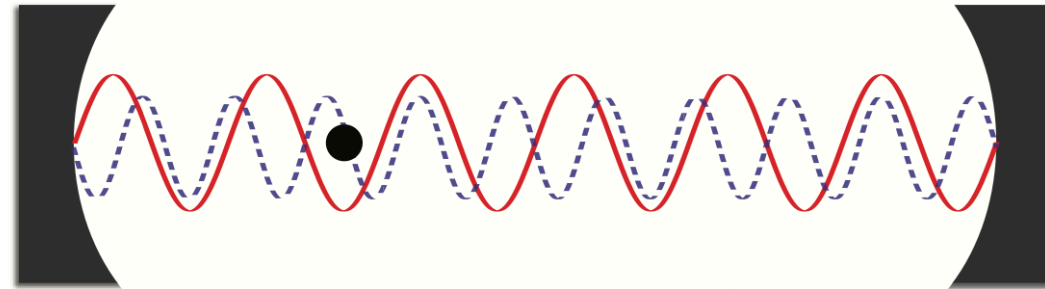
[Carney, et al., 2021]

[Afek, Carney, Moore, 2022]



Optomechanics

High-Frequency Gravitational Waves with Optically Levitated Sensors
[Arvanitaki, Geraci, 2013]



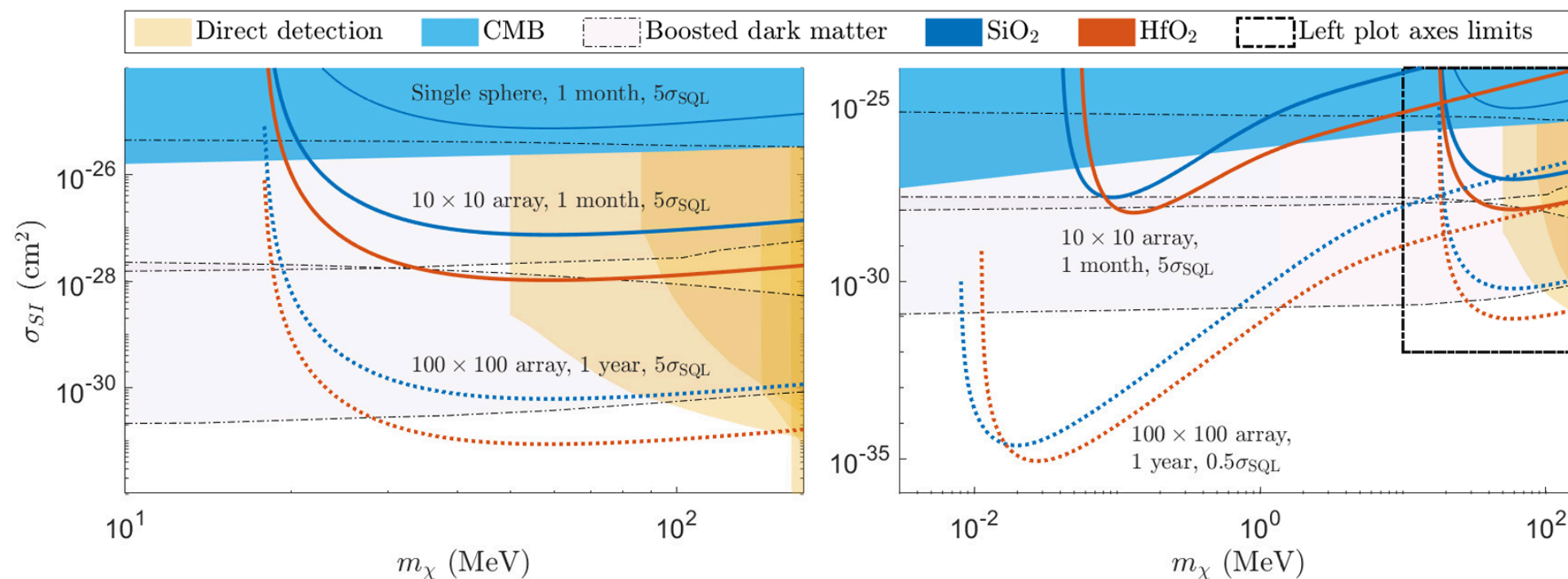
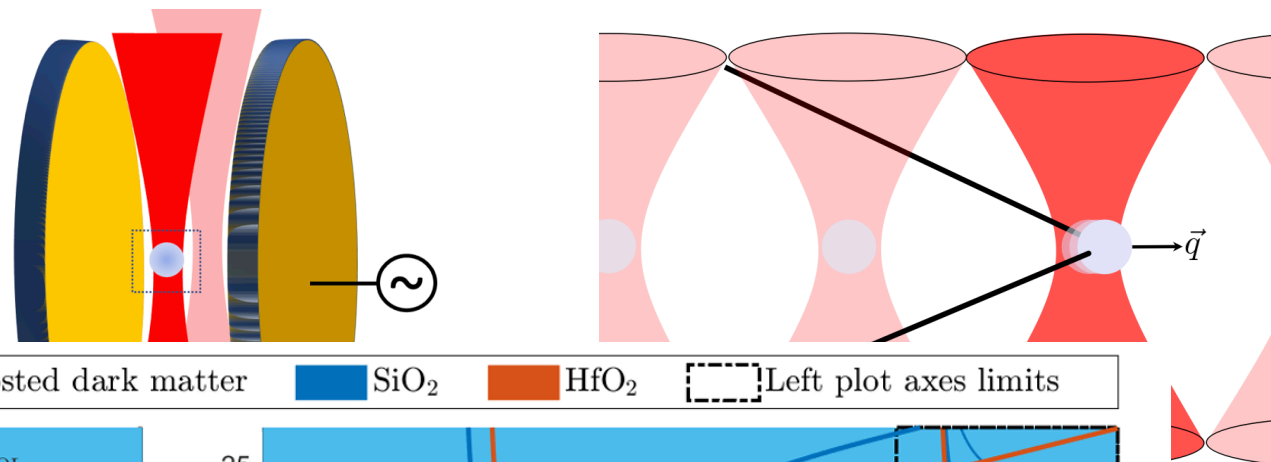
Dark Matter searches with optically levitated sensors

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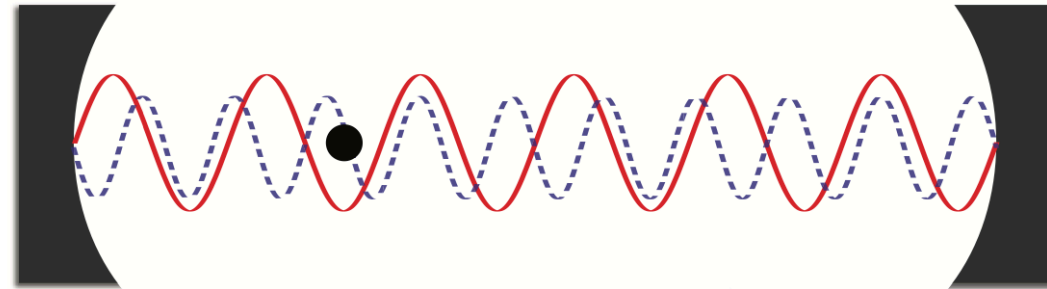
[Carney, et al., 2021]

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Optomechanics

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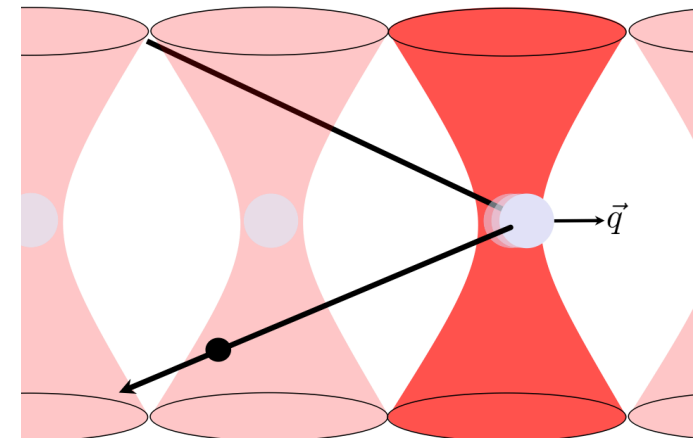
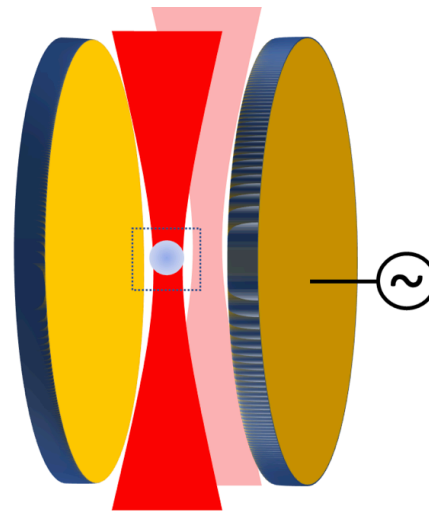
Dark Matter searches with optically levitated sensors

[Monteiro et al., 2020]

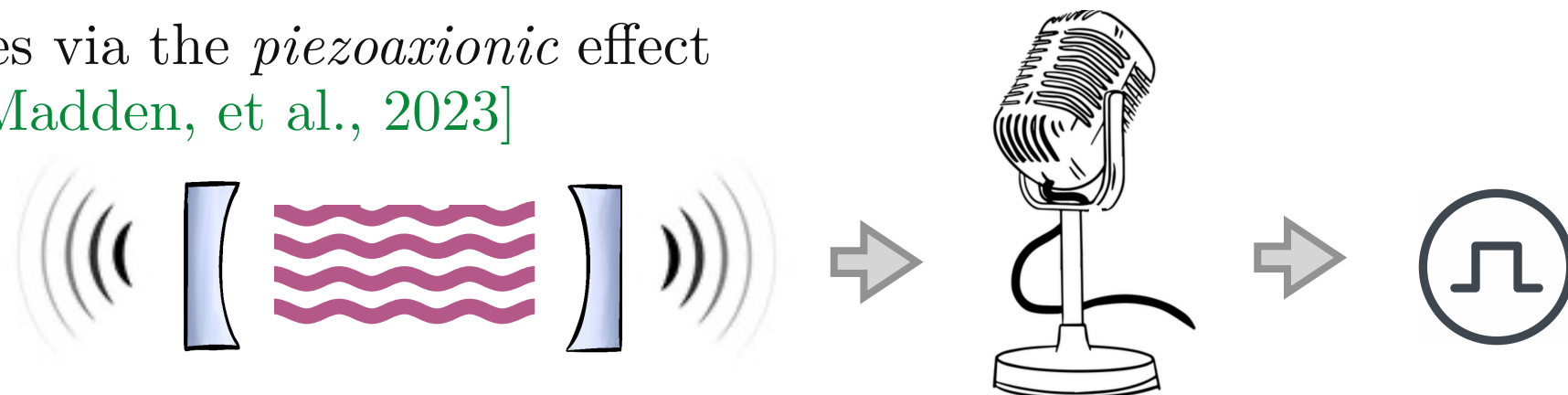
[Afek, et. al., 2021]

[Carney, et al., 2021]

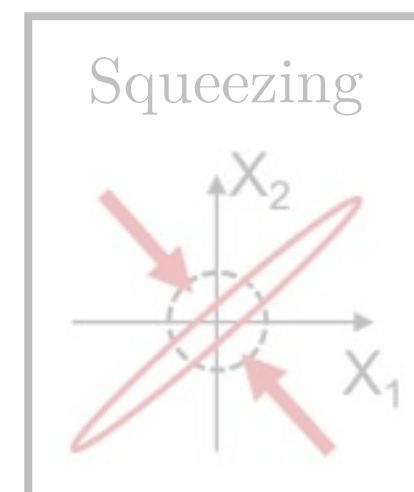
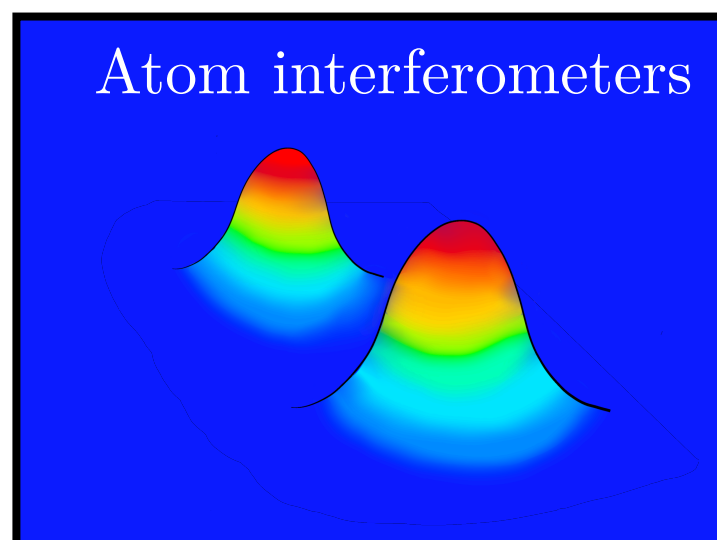
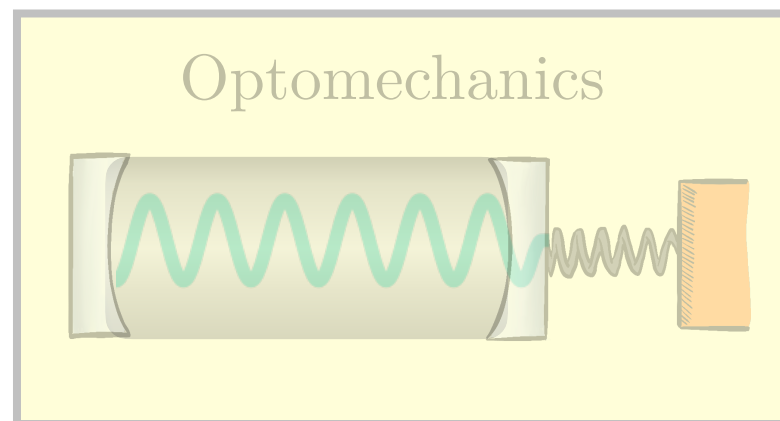
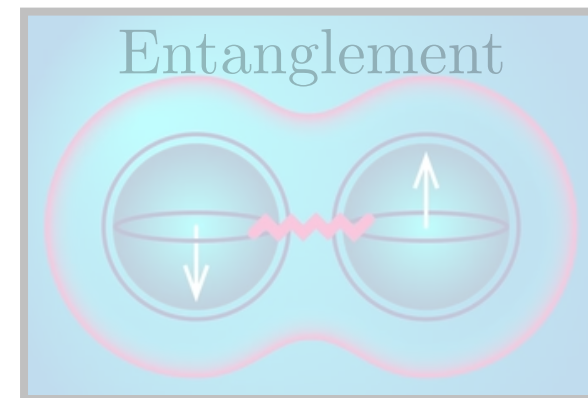
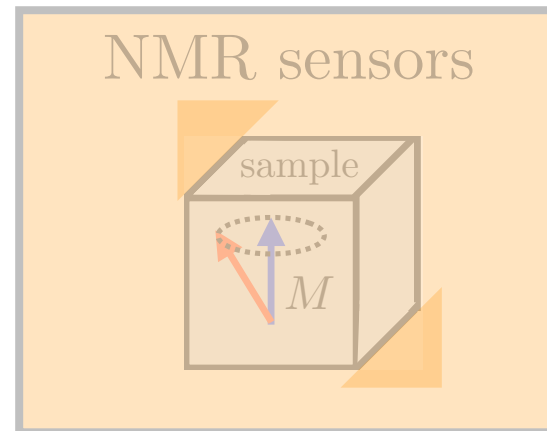
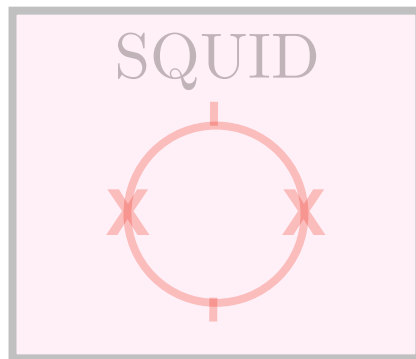
[Afek, Carney, Moore, 2022]



Axion searches via the *piezoaxionic* effect
[Arvanitaki, Madden, et al., 2023]

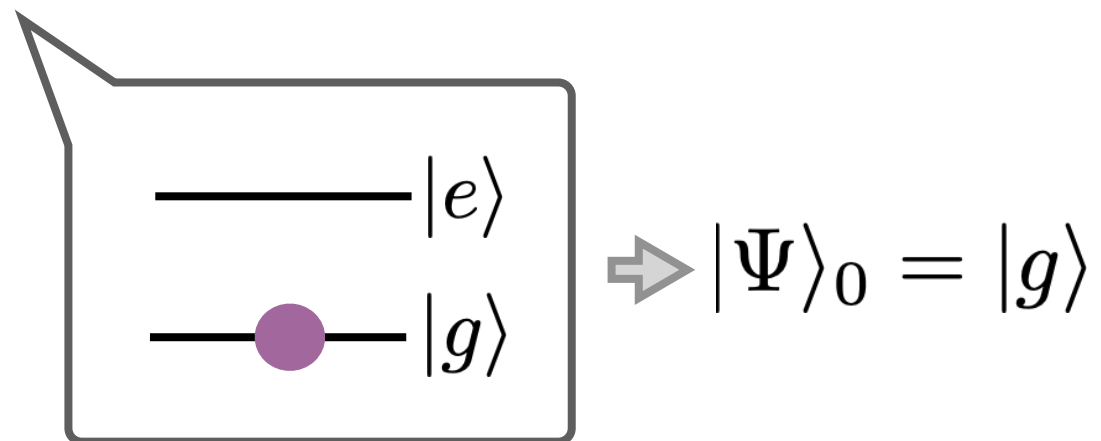


Quantum Sensing: examples



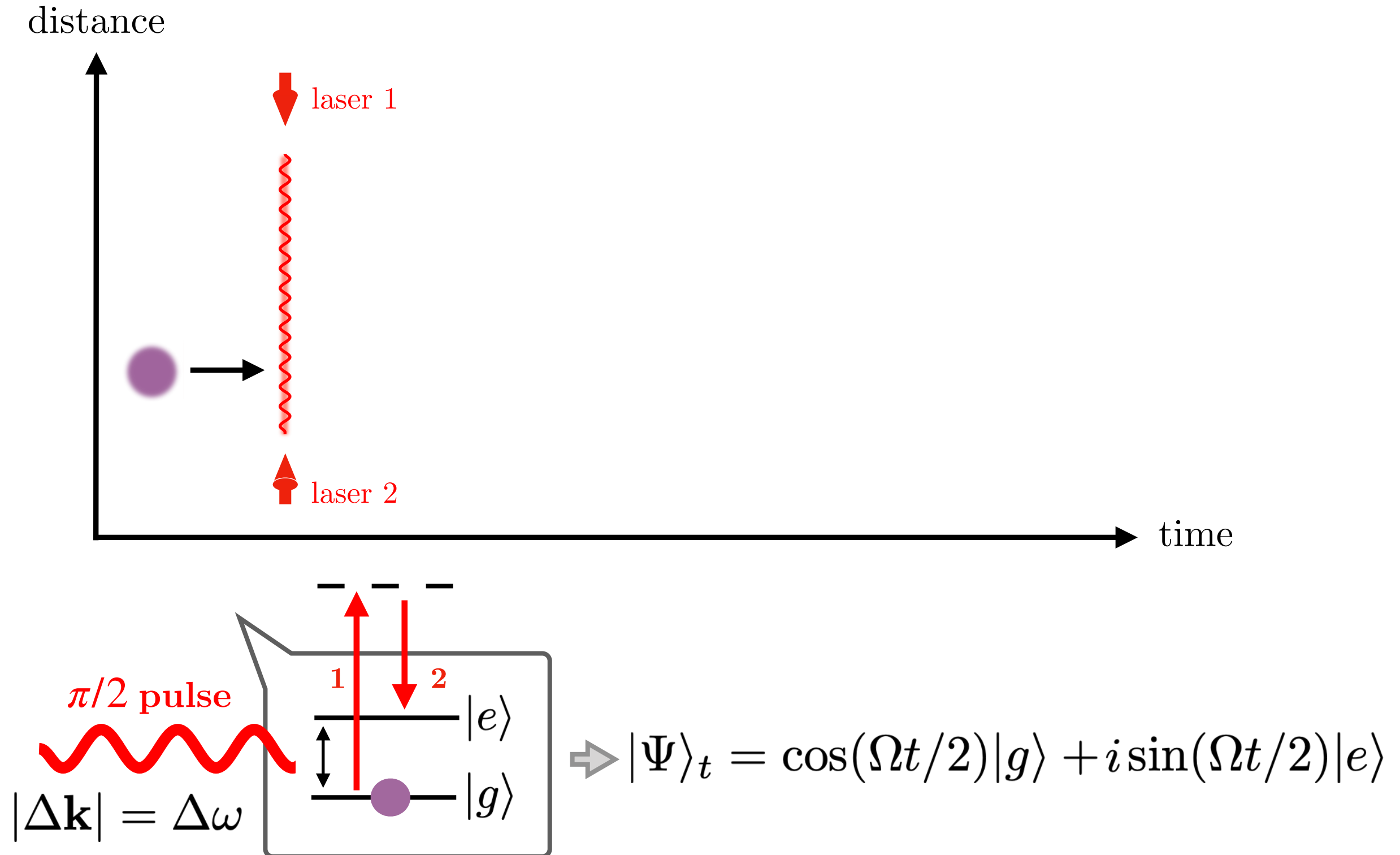
AIs: the Principle

Review: arXiv:2003.12516



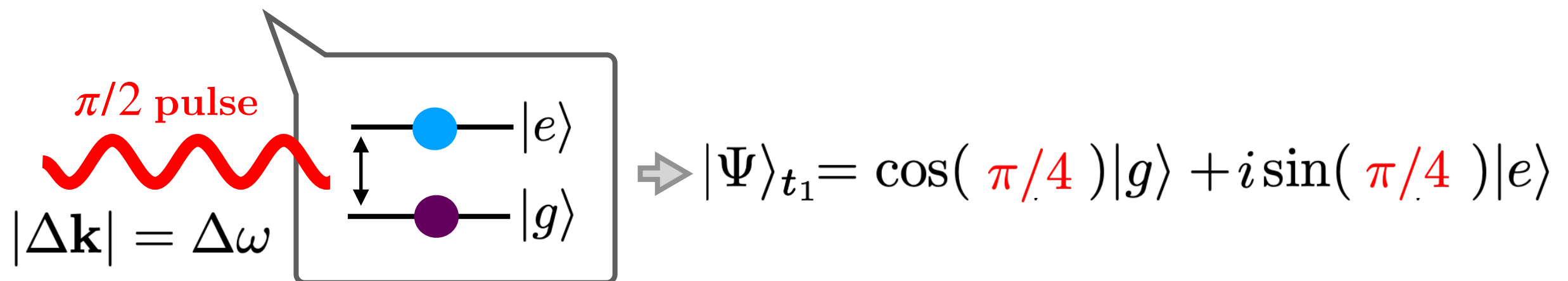
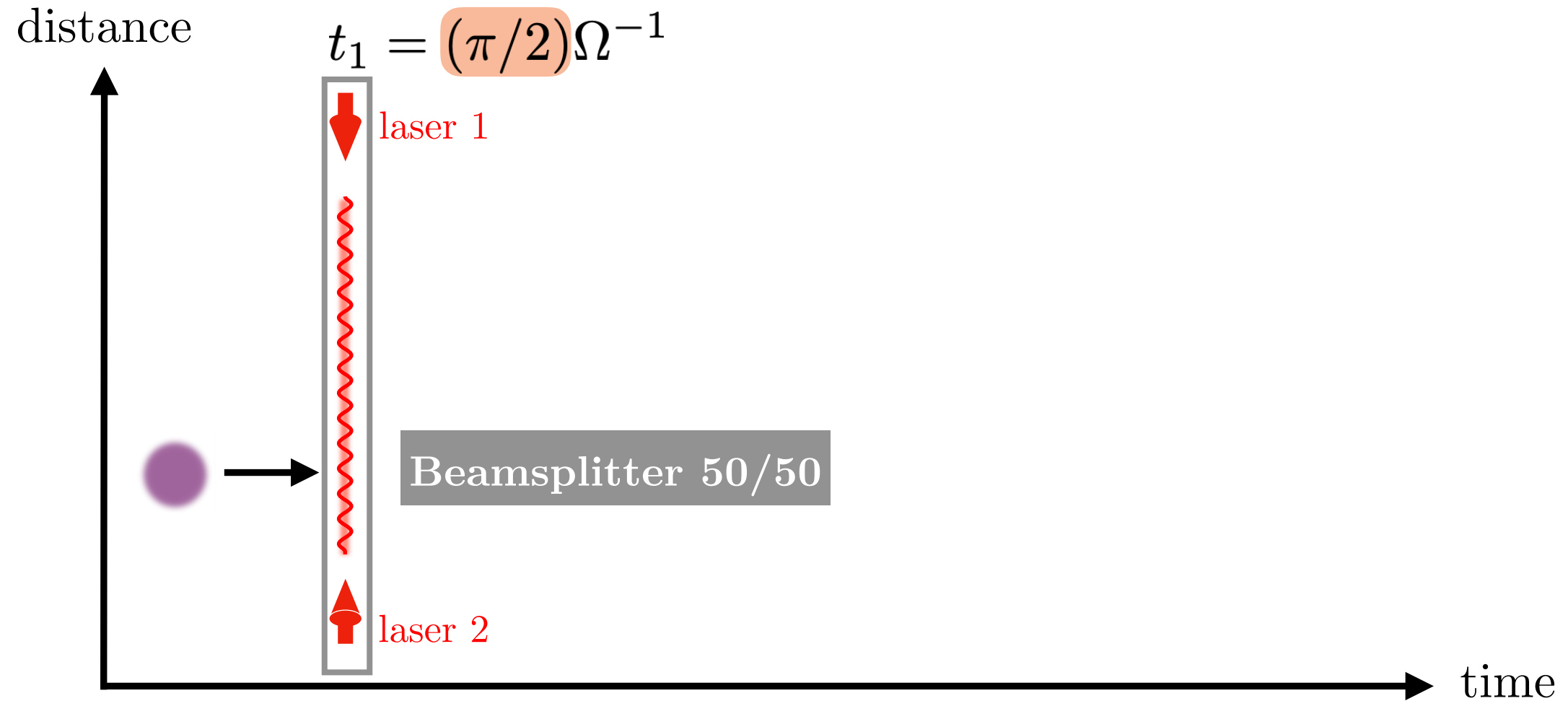
AIs: the Principle

Review: arXiv:2003.12516



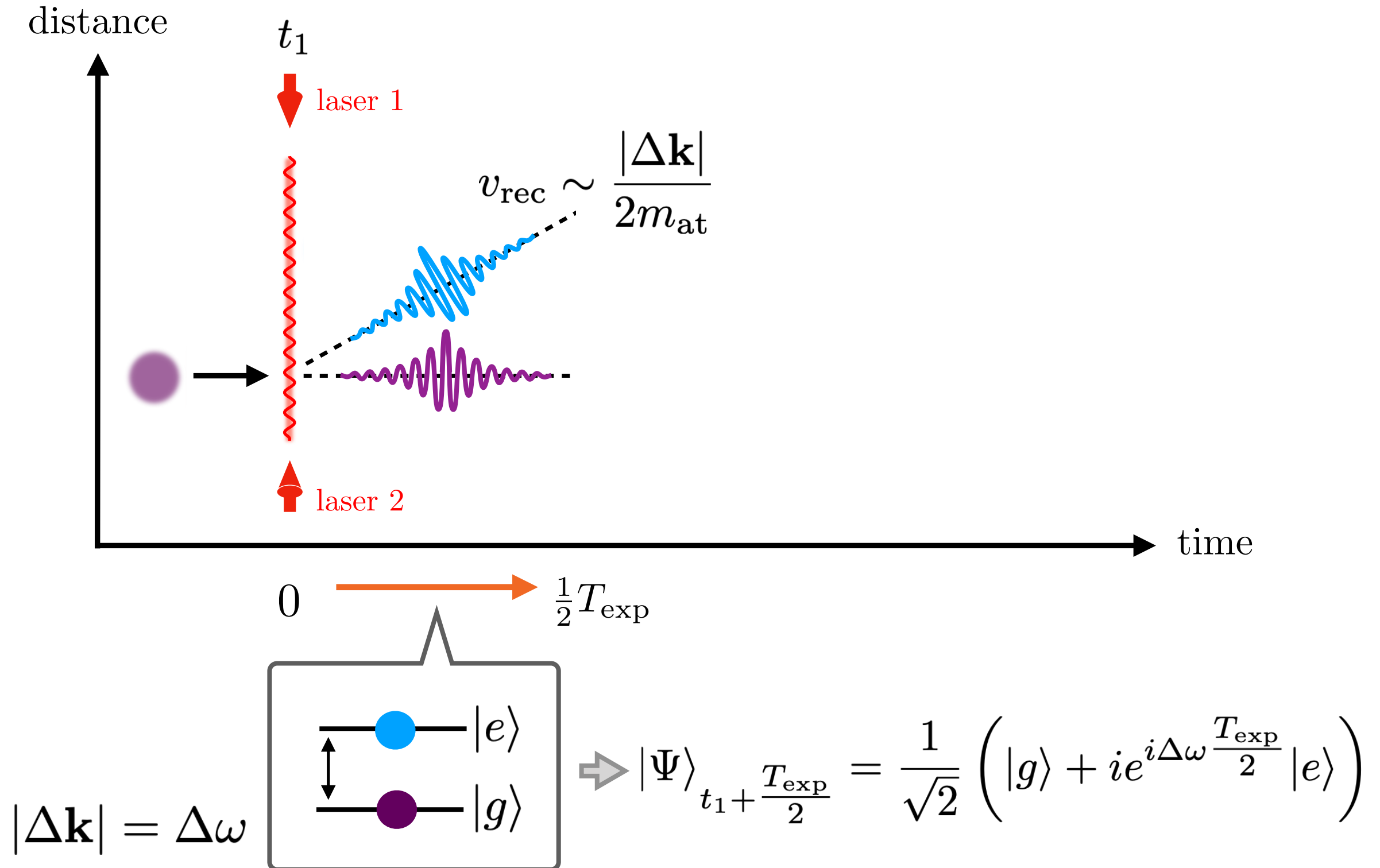
AIs: the Principle

Review: arXiv:2003.12516



AIs: the Principle

Review: arXiv:2003.12516



AIs: the Principle

Review: arXiv:2003.12516

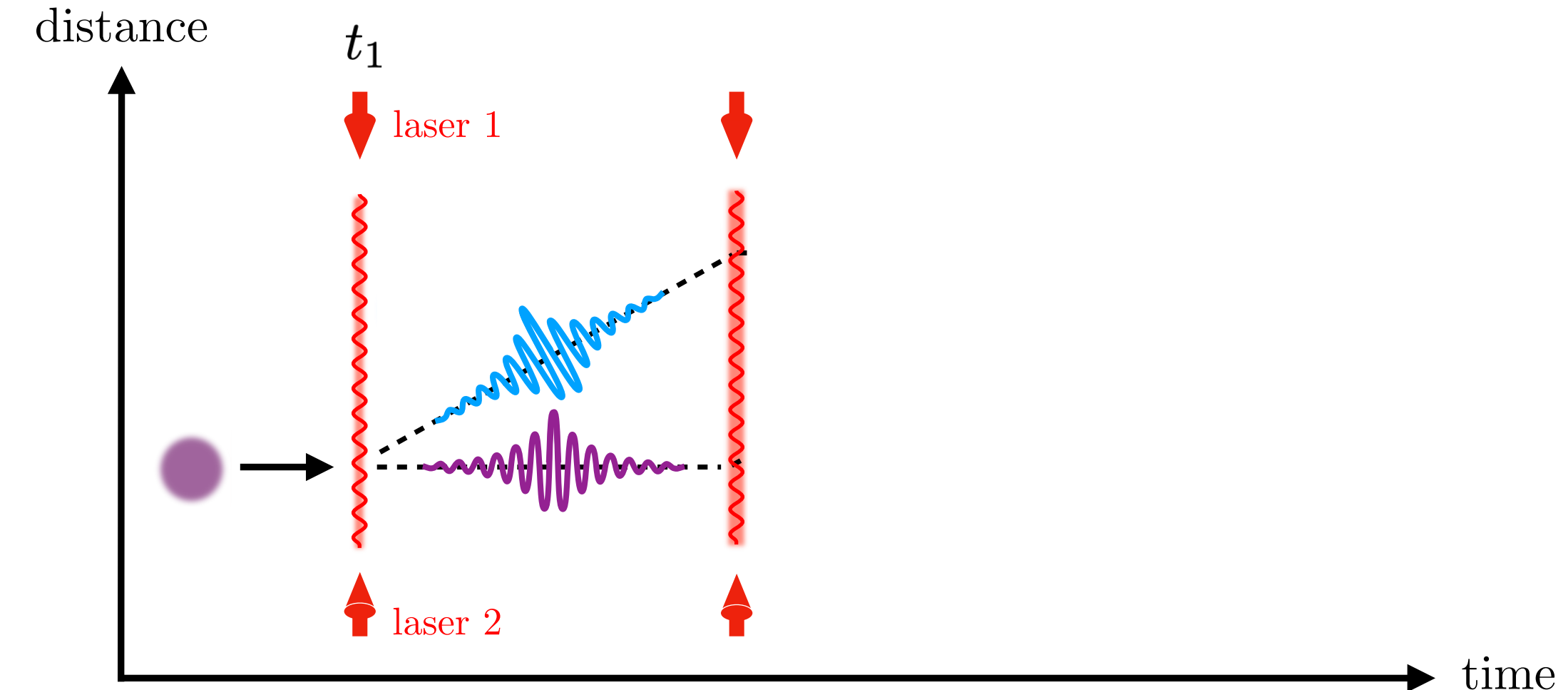


Diagram illustrating the quantum state evolution and the resulting wave function:

A π pulse (red wavy line) is applied, with the condition $|\Delta \mathbf{k}| = \Delta \omega$. The system is shown in a two-level state with ground state $|g\rangle$ (blue dot) and excited state $|e\rangle$ (purple dot).

The resulting wave function at time $t_1 + \frac{T_{\text{ext}}}{2} + t_2$ is given by:

$$|\Psi\rangle_{t_1 + \frac{T_{\text{ext}}}{2} + t_2} = \frac{1}{\sqrt{2}} \left(-e^{i\Delta\omega \frac{T_{\text{exp}}}{2}} |g\rangle + i|e\rangle \right)$$

AIs: the Principle

Review: arXiv:2003.12516

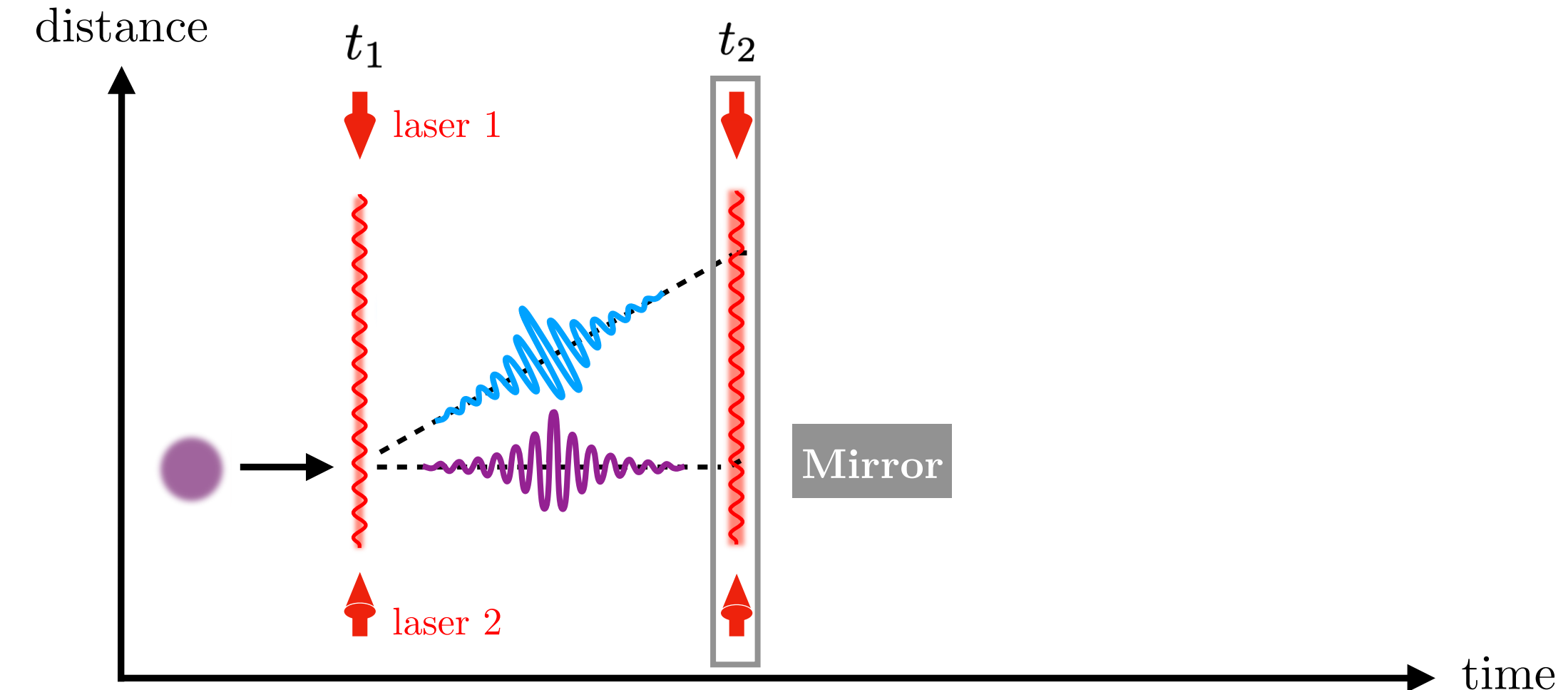


Diagram illustrating the atomic energy levels and the resulting wave function:

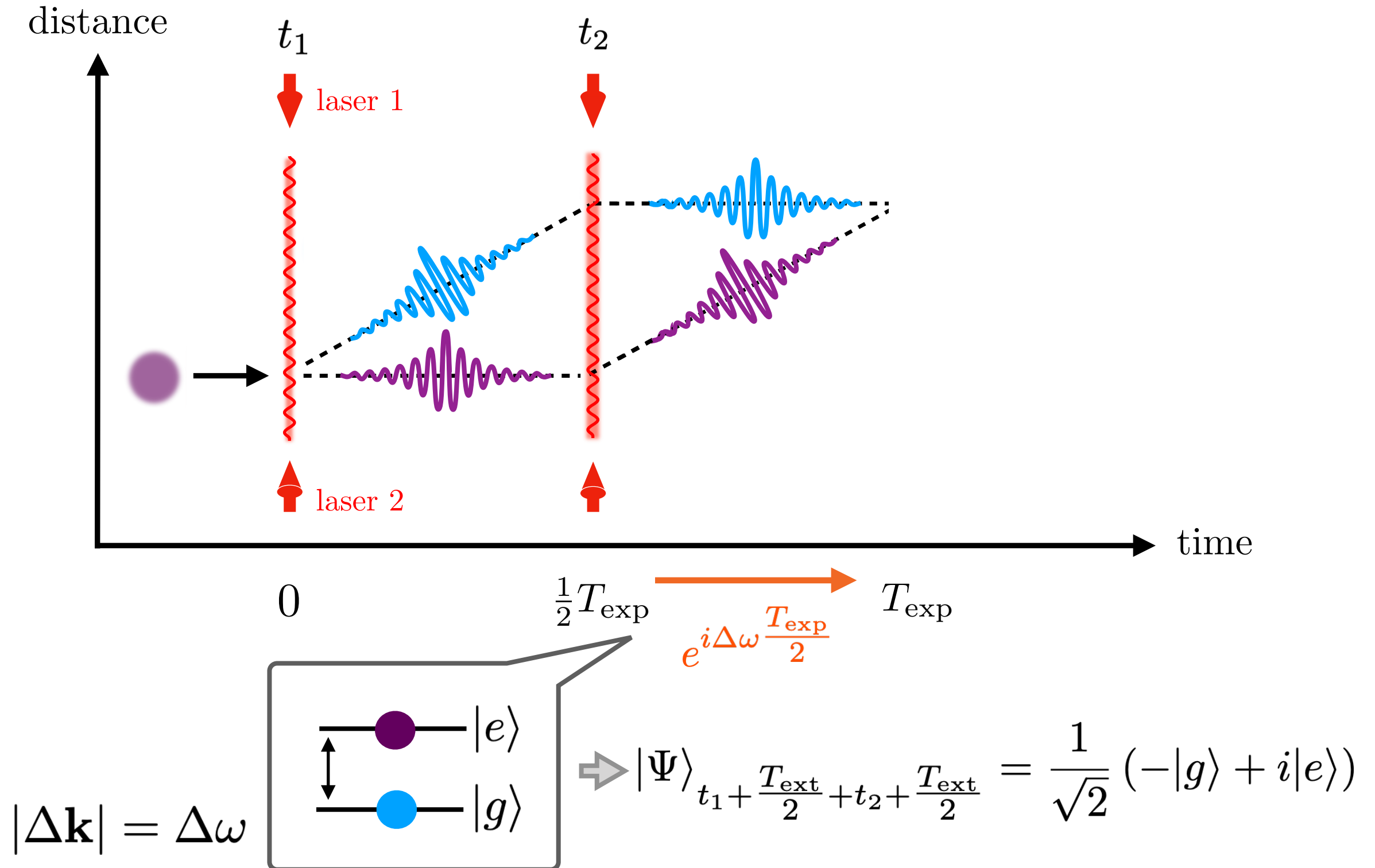
A π pulse is applied, with the condition $|\Delta \mathbf{k}| = \Delta \omega$. The energy levels are shown as $|e\rangle$ (excited state, purple dot) and $|g\rangle$ (ground state, blue dot).

The resulting wave function at time $t_1 + \frac{T_{\text{ext}}}{2} + t_2$ is given by:

$$|\Psi\rangle_{t_1 + \frac{T_{\text{ext}}}{2} + t_2} = \frac{1}{\sqrt{2}} \left(-e^{i\Delta\omega \frac{T_{\text{exp}}}{2}} |g\rangle + i|e\rangle \right)$$

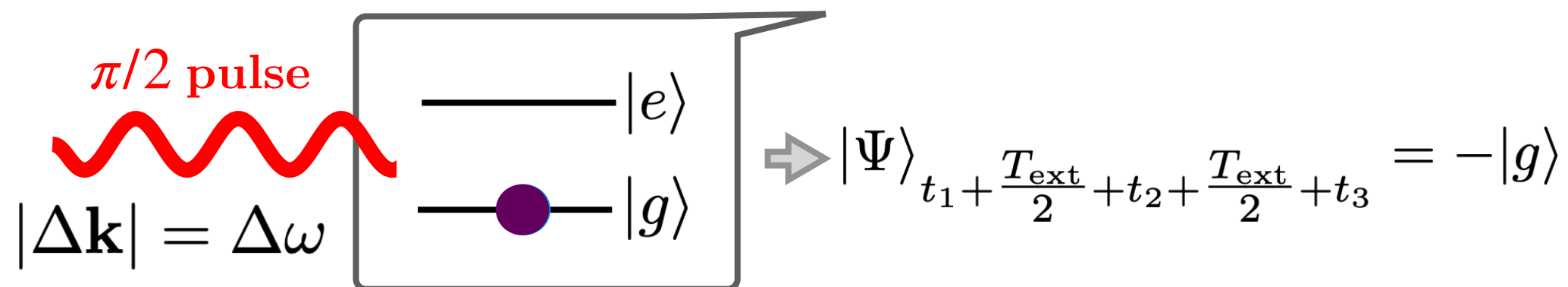
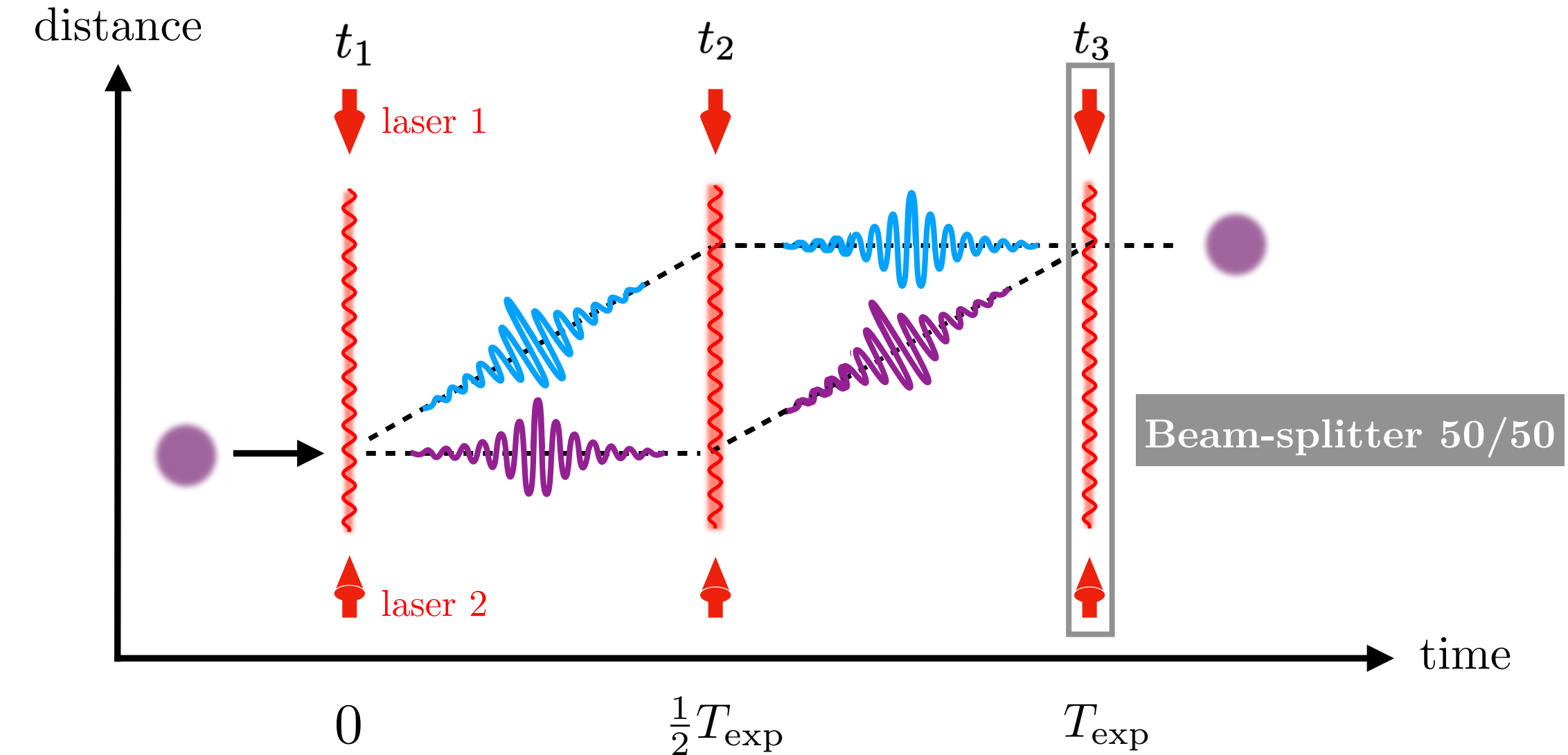
AIs: the Principle

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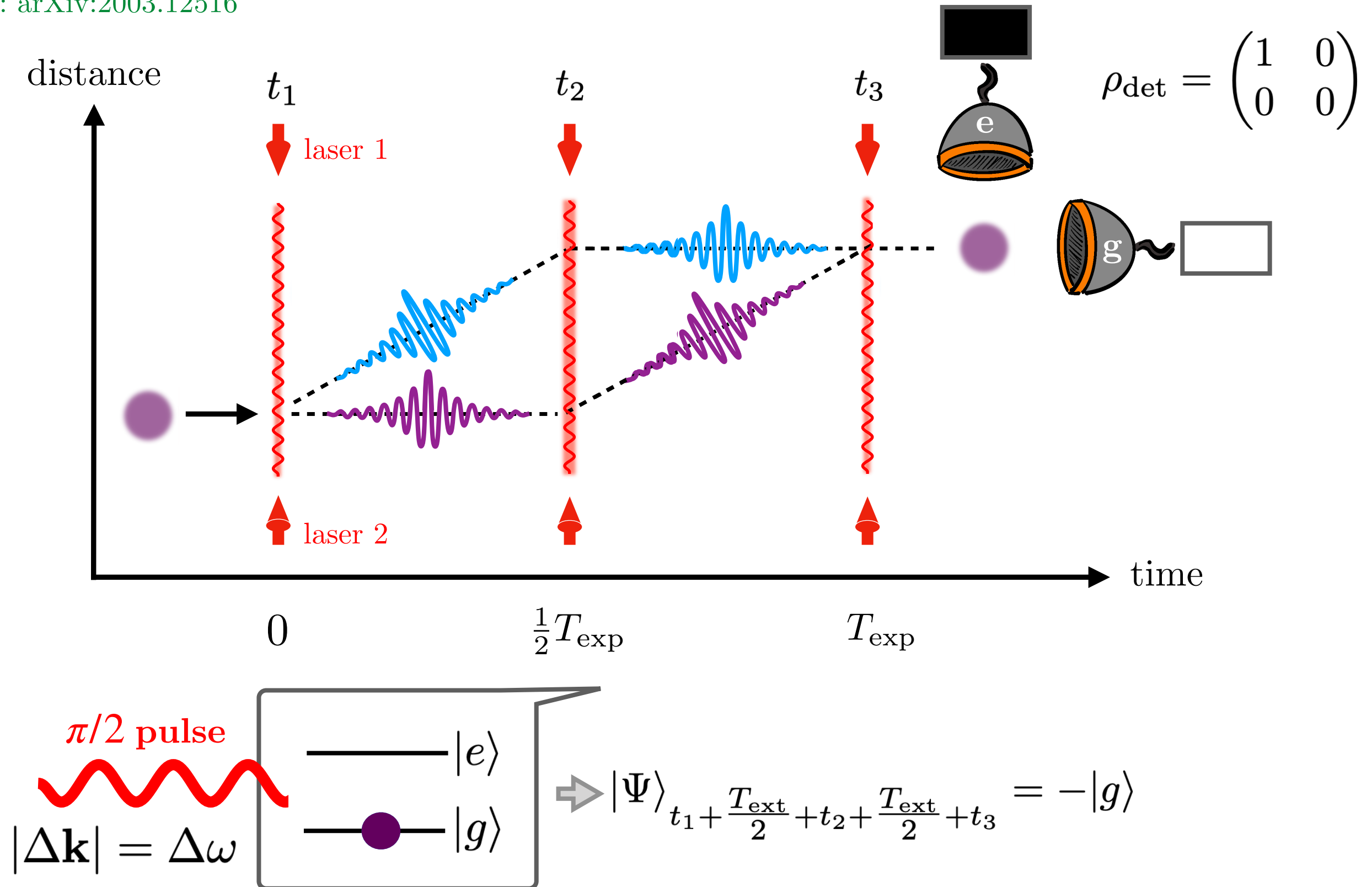
AIs: the Principle

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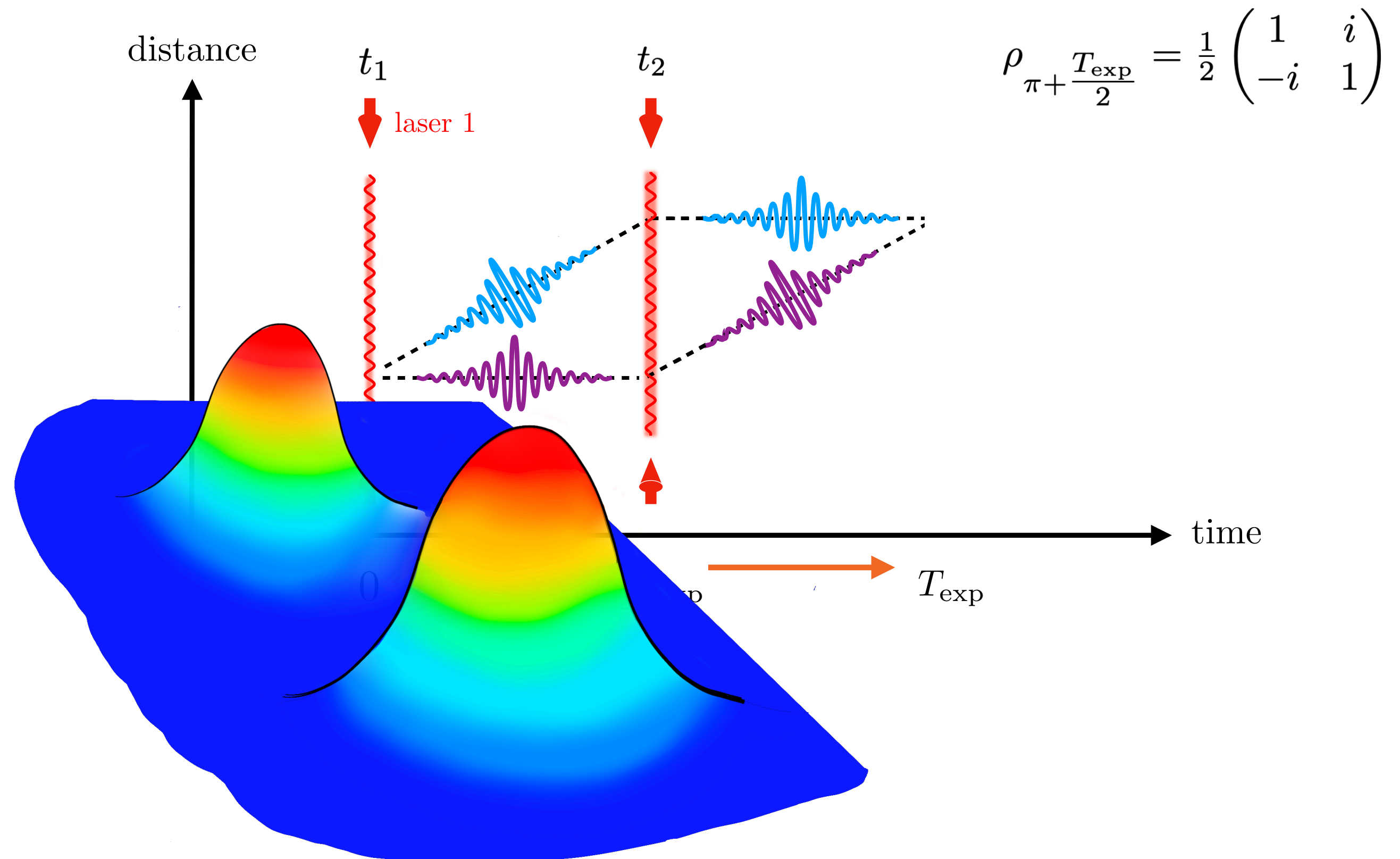


AIs: the Principle

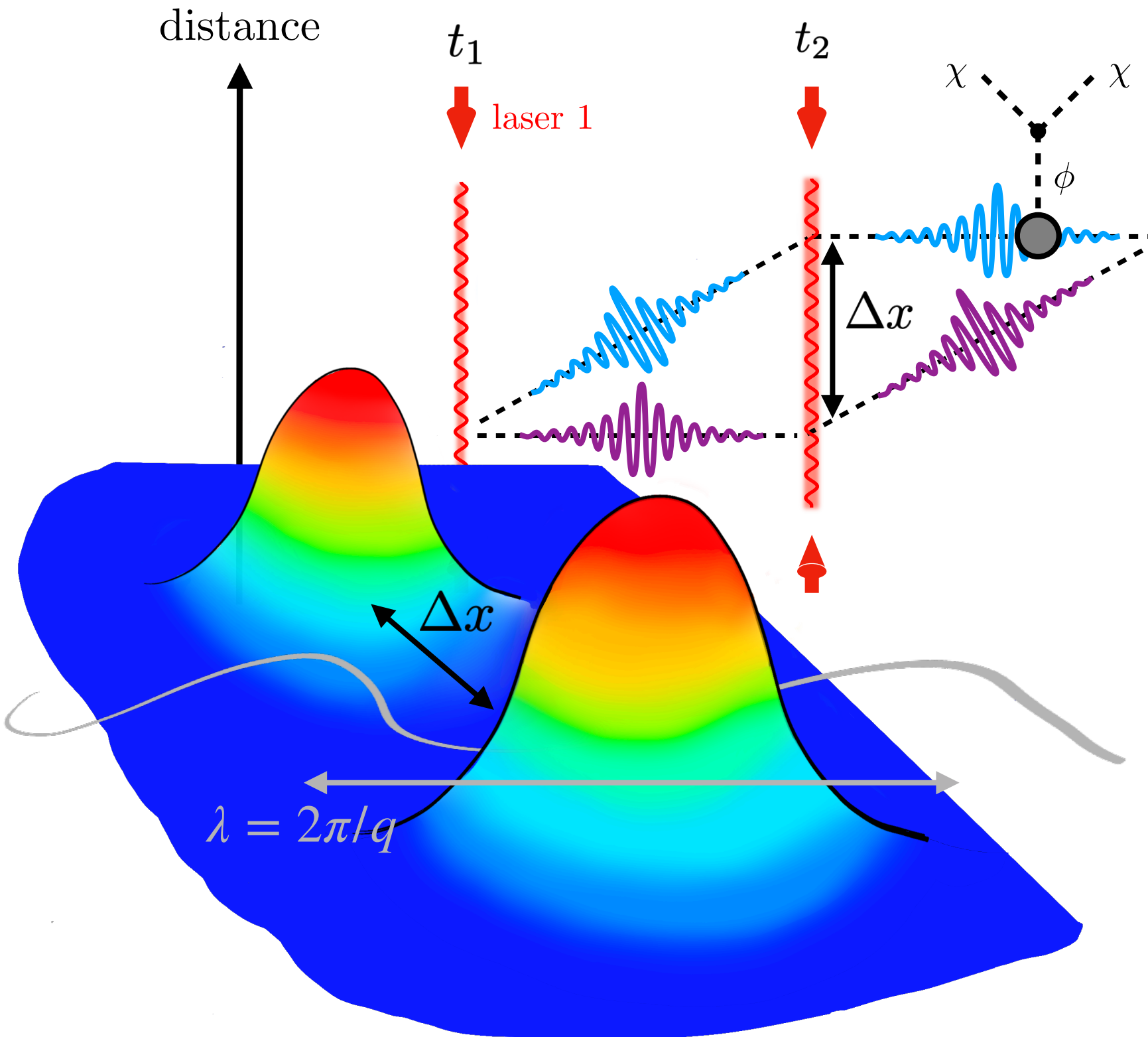
Review: arXiv:2003.12516



AIs: Decoherence



AIs: Decoherence



open system

$$\rho_{\pi + \frac{T_{\text{exp}}}{2}} = \frac{1}{2} \begin{pmatrix} 1 & i\gamma \\ -i\gamma & 1 \end{pmatrix}$$

$$= e^{-t_{\text{exp}} \Gamma_{\text{cloud}}} \mathcal{F}_{\text{dec}} / N_{\text{ind}}$$

$$= e^{-t_{\text{exp}} / \tau_{\text{dec}}}$$

$$\gamma = e^{-s+i\phi} = e^{-s} e^{i\phi}$$

AIs: Decoherence

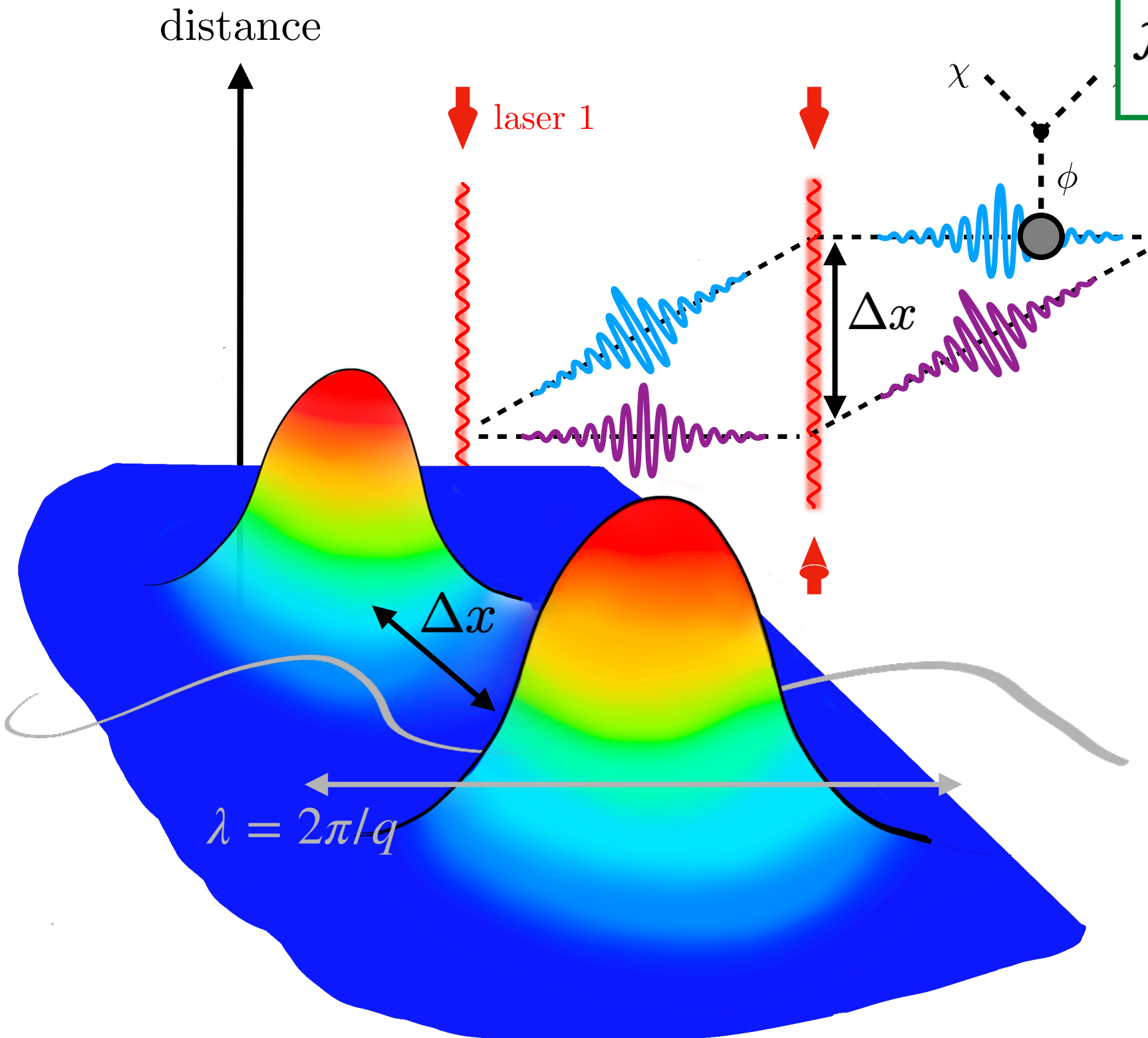
Form Factor

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$

[Joss, Zeh, 1985]

[Gallis, Fleming, 1990]

[Hornberger, Sipe, 2003]

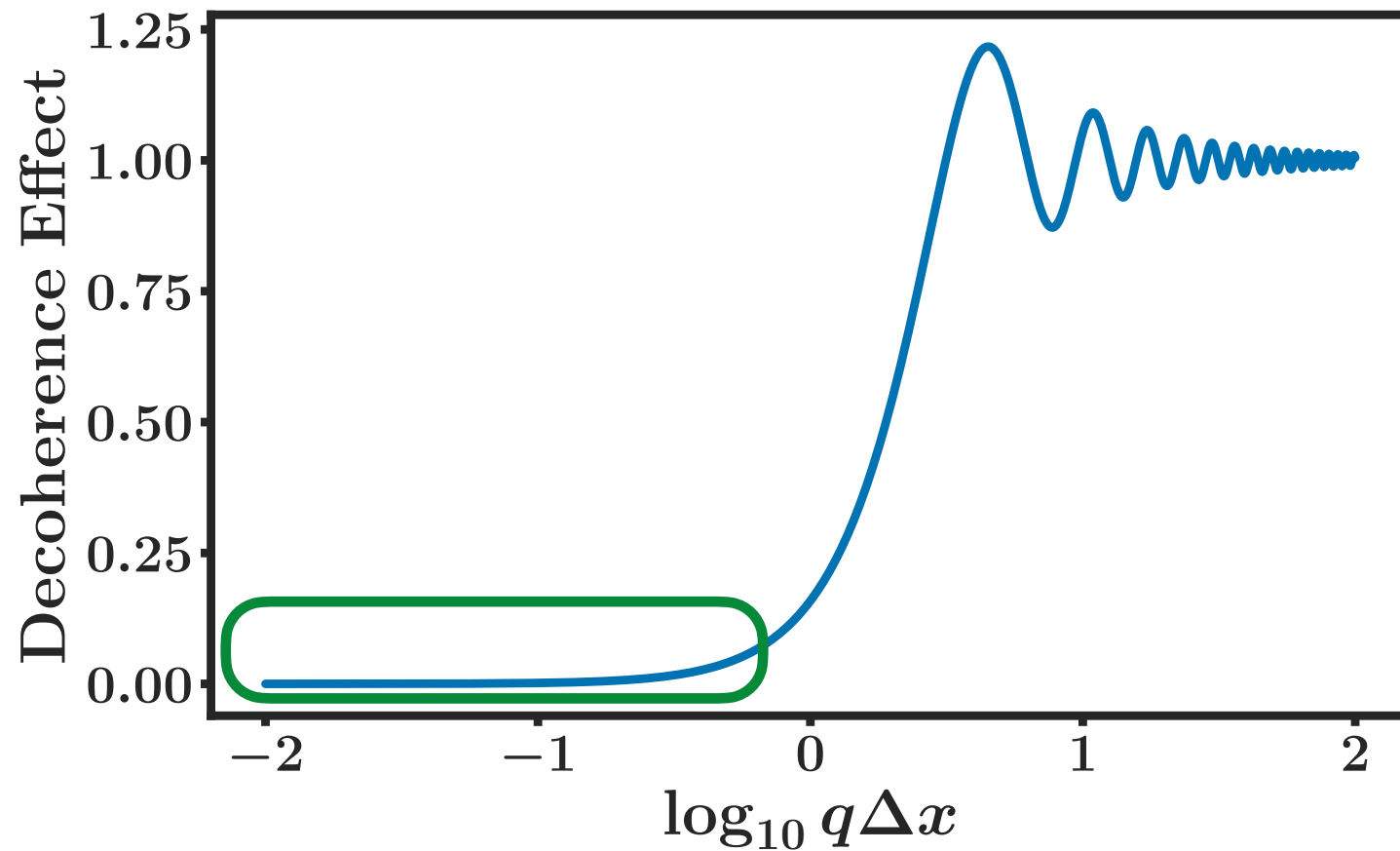


$$= e^{-t_{\text{exp}} \Gamma_{\text{cloud}} \mathcal{F}_{\text{dec}} / N_{\text{ind}}}$$

$$= e^{-t_{\text{exp}} / \tau_{\text{dec}}}$$

$$\gamma = e^{-s+i\phi} = e^{-s} e^{i\phi}$$

AIs: Decoherence



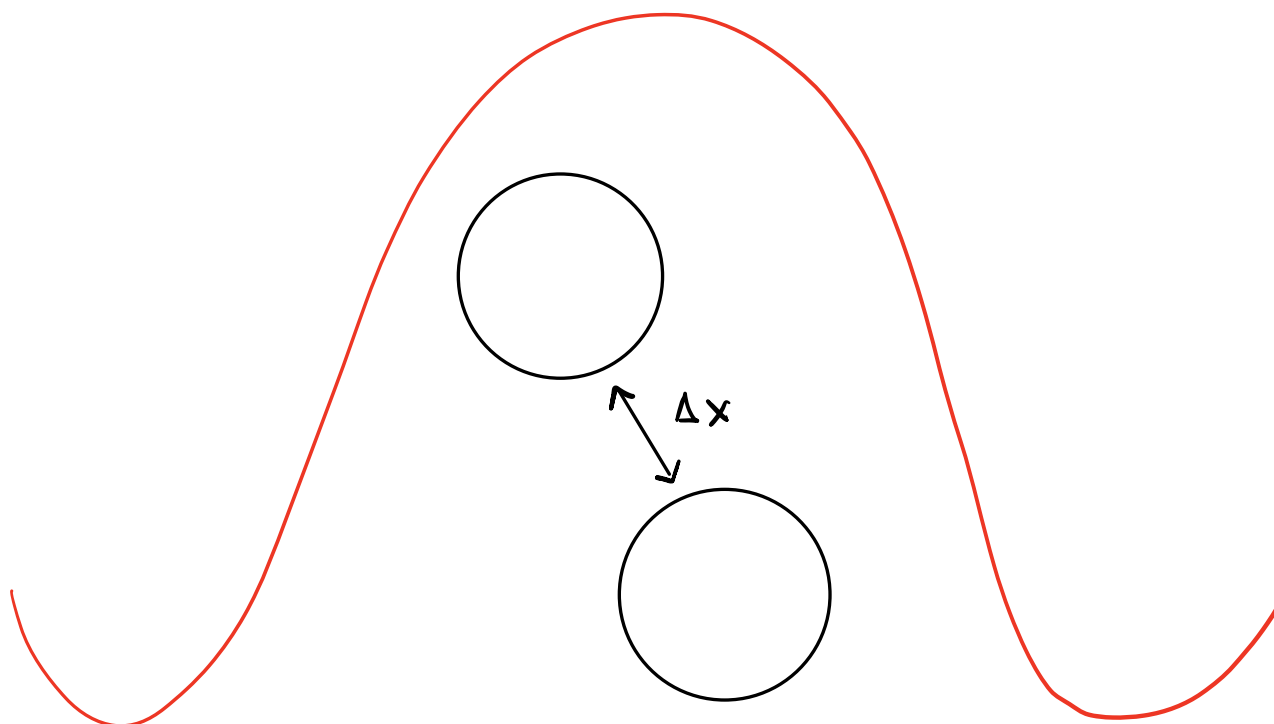
Form Factor

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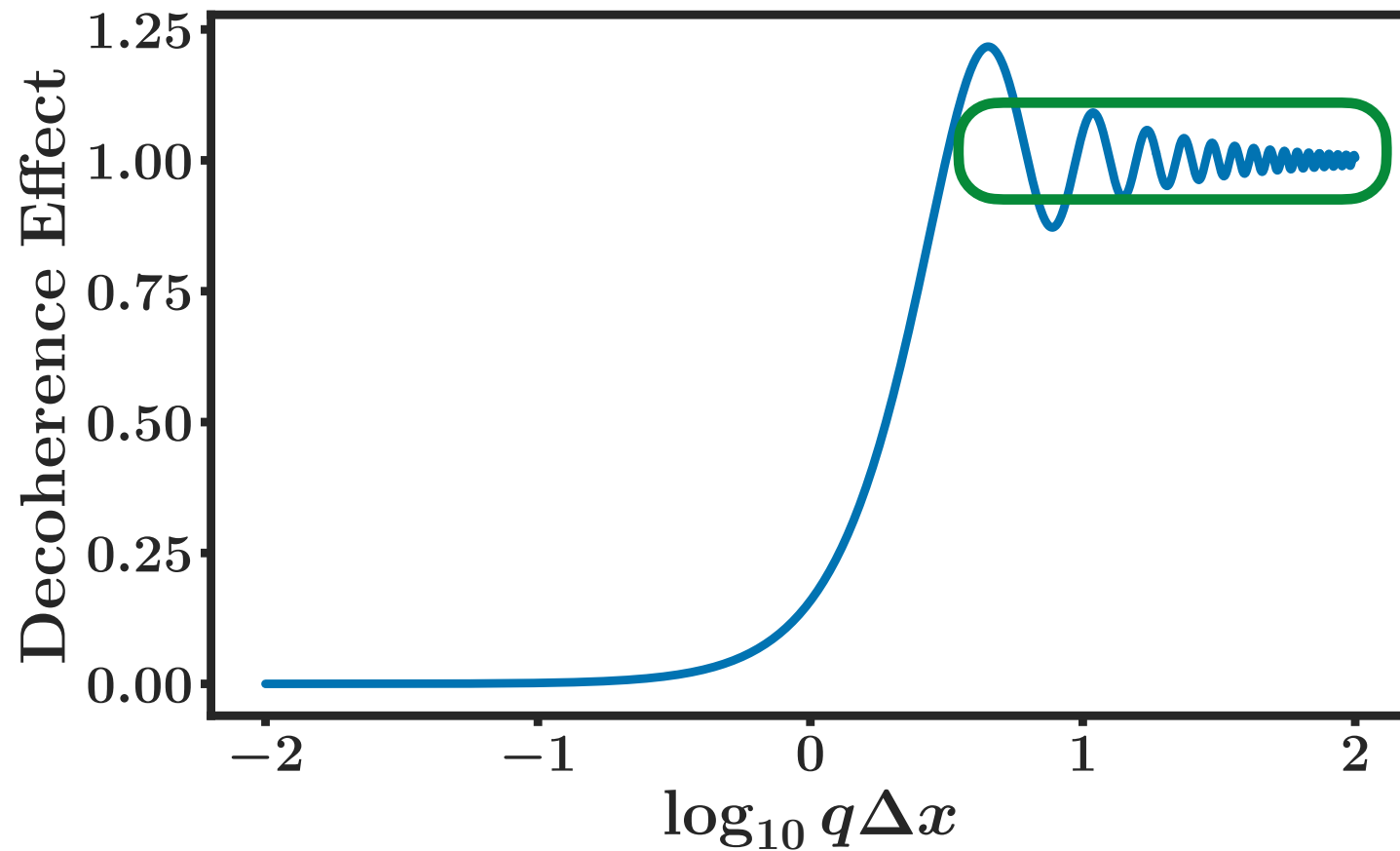


$$= e^{-t_{\text{exp}} \Gamma_{\text{cloud}} \mathcal{F}_{\text{dec}} / N_{\text{ind}}}$$

$$= e^{-t_{\text{exp}} / \tau_{\text{dec}}}$$

$$\gamma = e^{-s+i\phi} = e^{-s} e^{i\phi}$$

AIs: Decoherence



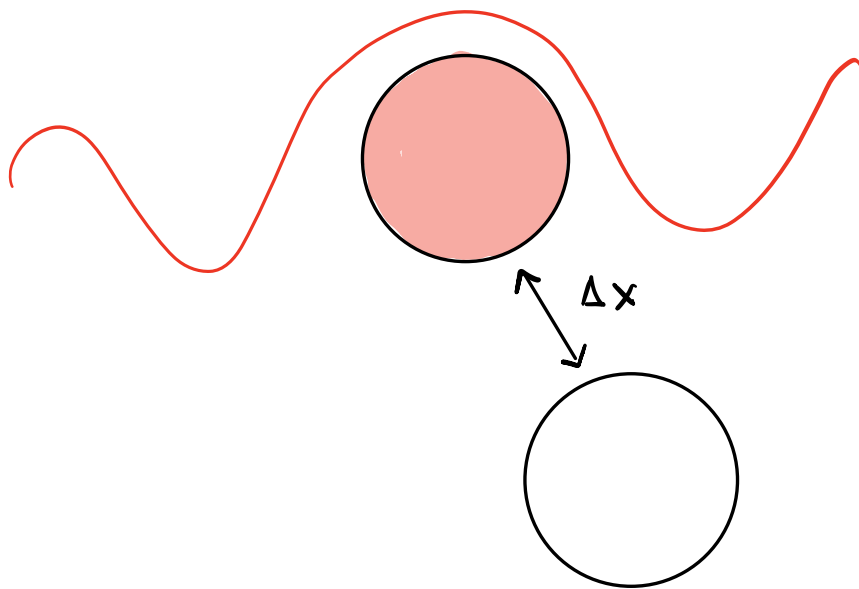
Form Factor

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$

[Joss, Zeh, 1985]

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[Hornberger, Sipe, 2003]

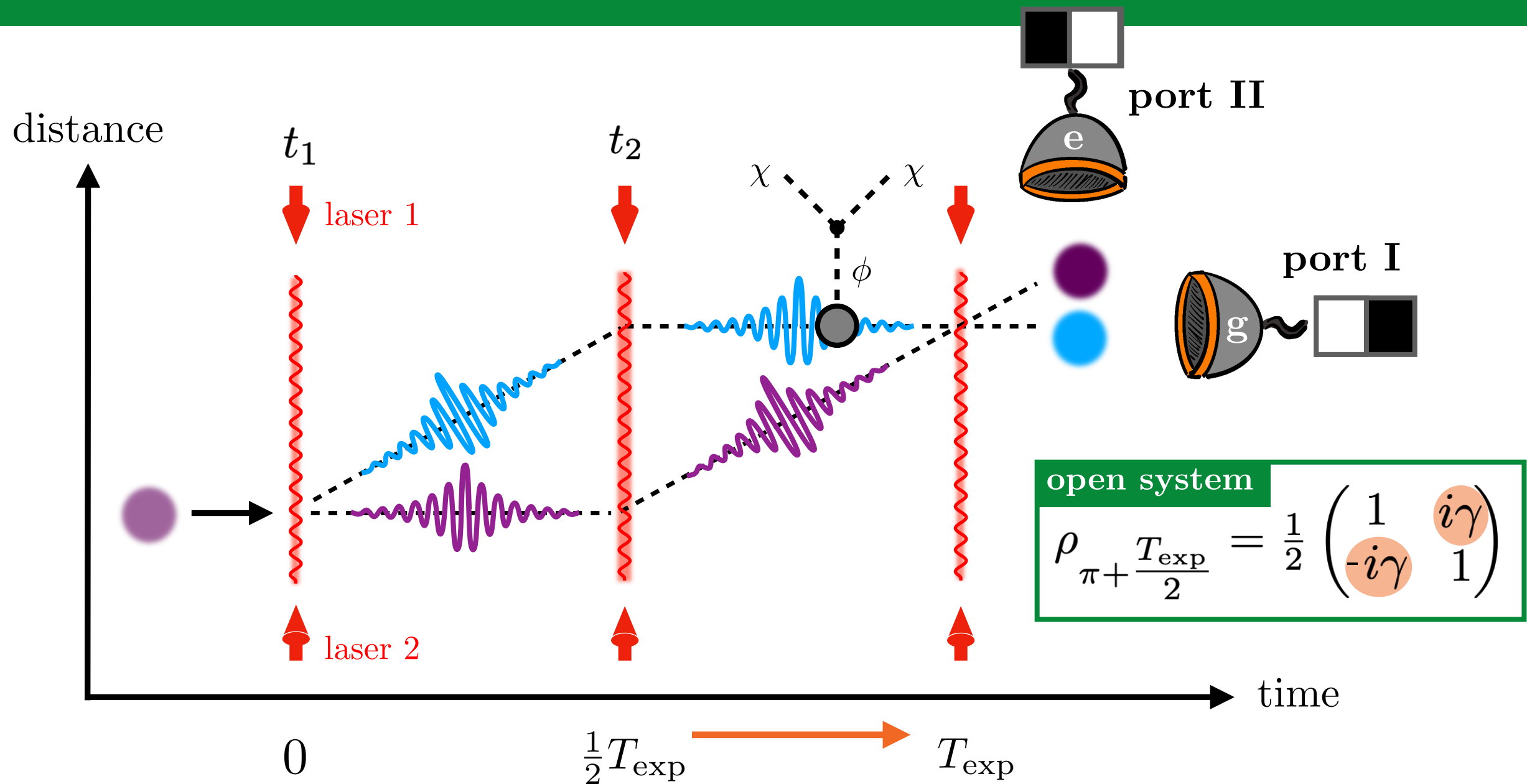


$$= e^{-t_{\text{exp}} \Gamma_{\text{cloud}} \mathcal{F}_{\text{dec}} / N_{\text{ind}}}$$

$$= e^{-t_{\text{exp}} / \tau_{\text{dec}}}$$

$$\gamma = e^{-s+i\phi} = e^{-s} e^{i\phi}$$

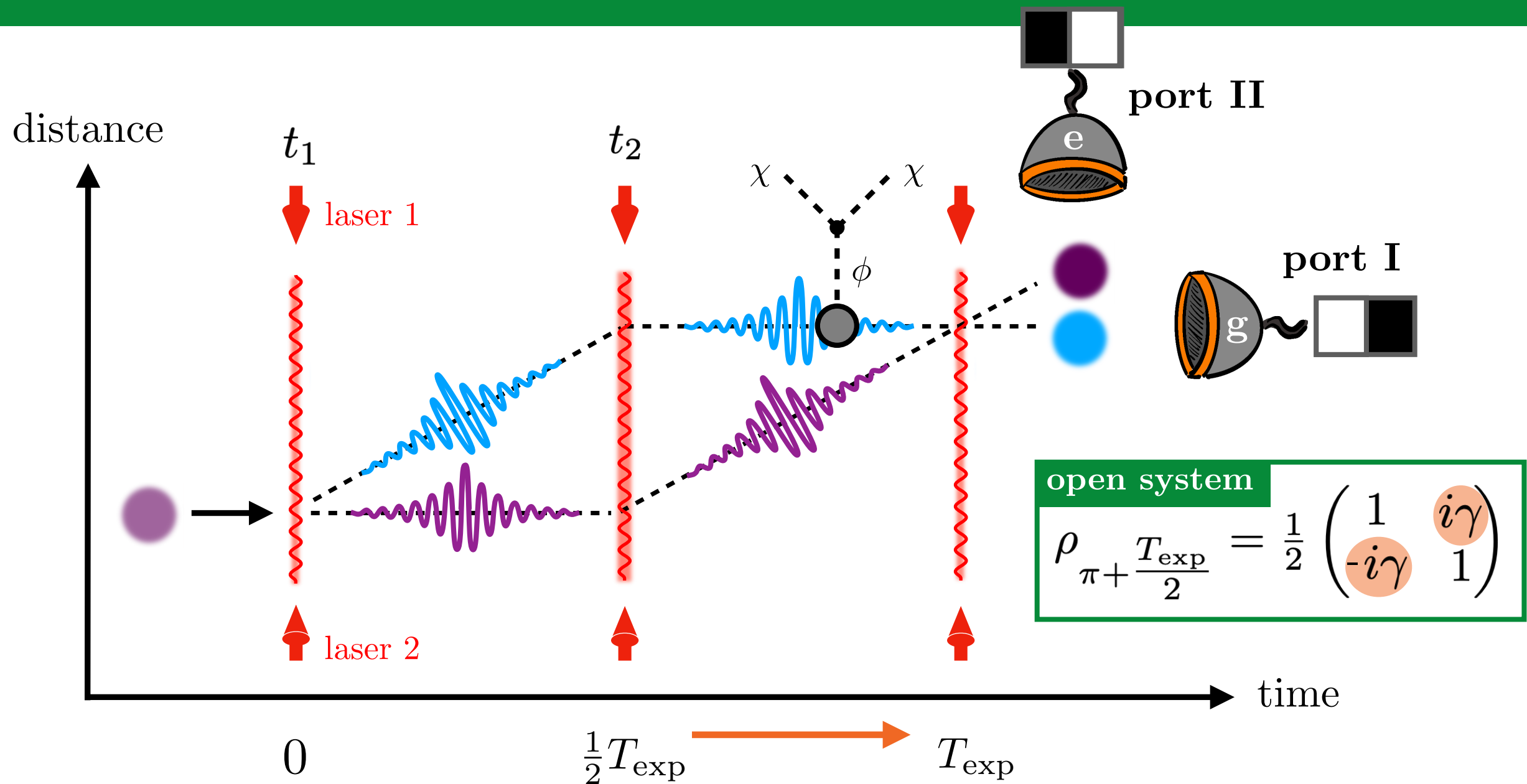
AIs: single measurement



$$\begin{aligned}
 p(|\Psi\rangle)_I &= \text{Tr}\{\rho|g\rangle\langle g|\} \\
 &= \frac{1}{2} (1 + \text{Re}\{\gamma\}) \\
 &= \frac{1}{2} (1 + e^{-s} \cos \phi)
 \end{aligned}$$

$$\gamma = e^{-s+i\phi} = e^{-s} e^{i\phi}$$

AIs: single measurement



$$\begin{aligned} p(|\Psi\rangle)_I &= \text{Tr}\{\rho|g\rangle\langle g|\} \\ &= \frac{1}{2} (1 + \text{Re}\{\gamma\}) \\ &= \frac{1}{2} (1 + e^{-s} \cos \phi) \end{aligned}$$

(assume fully decohered)

$$\gamma = e^{-s+i\phi} = e^{-s} e^{i\phi}$$

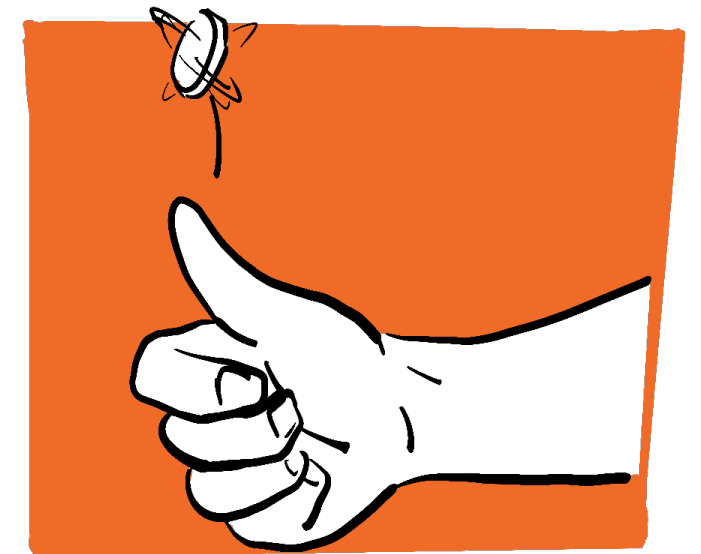
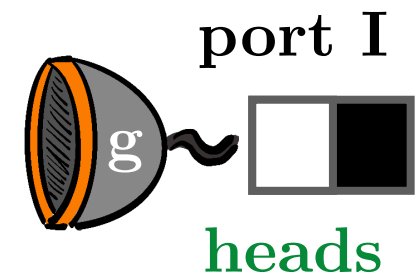
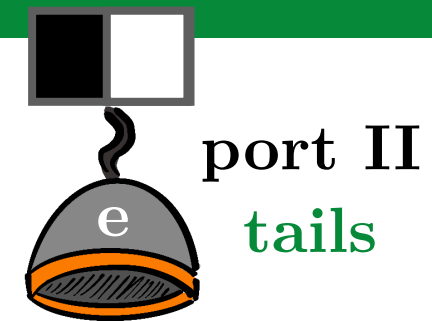
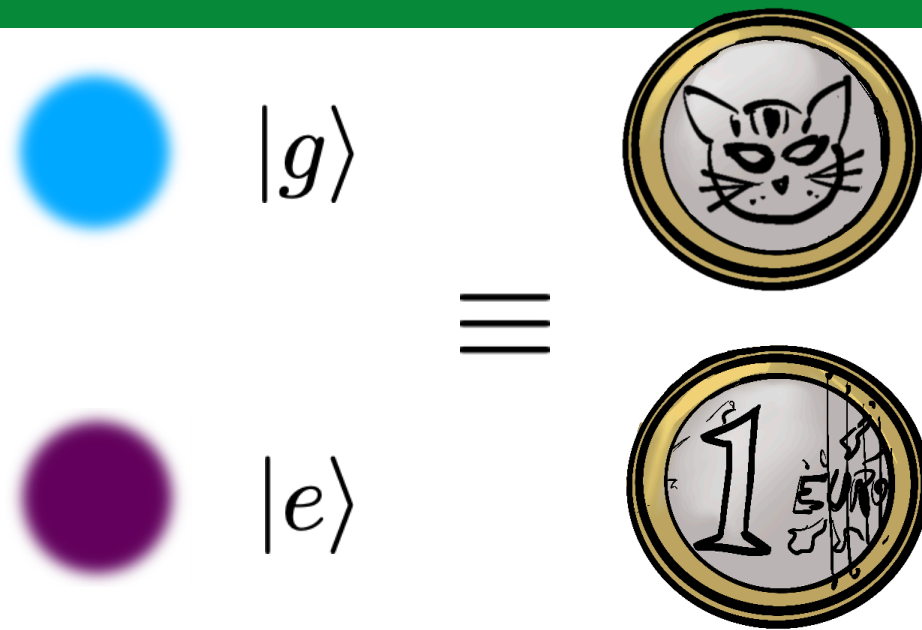
AIs: single measurement



$$p_I = \frac{1}{2}$$

(assume fully decohered)

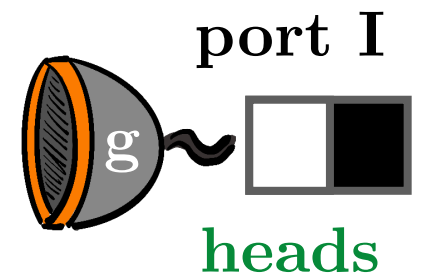
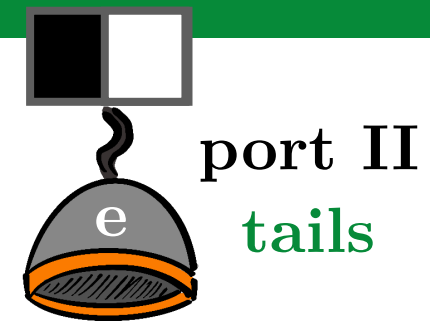
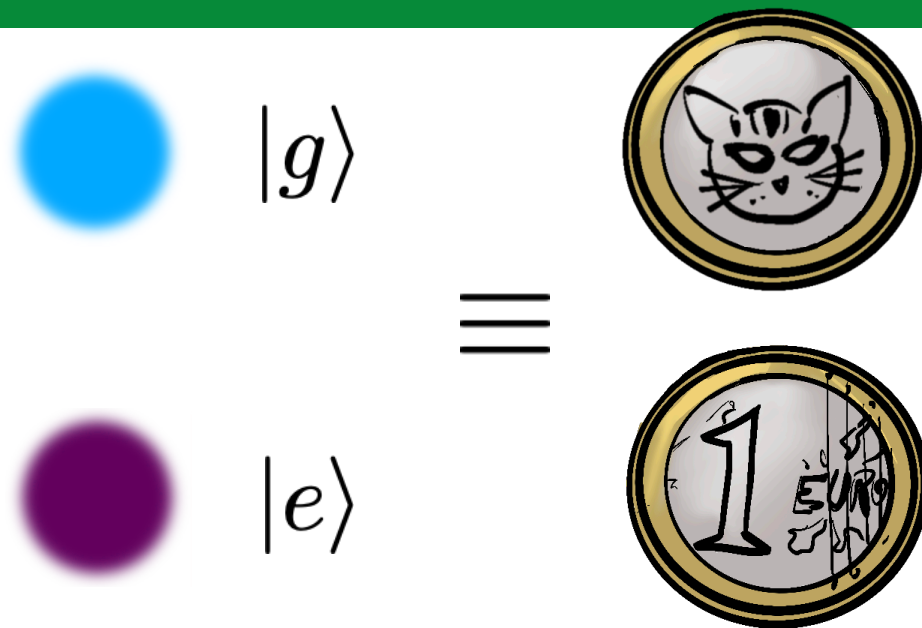
AIs: single measurement



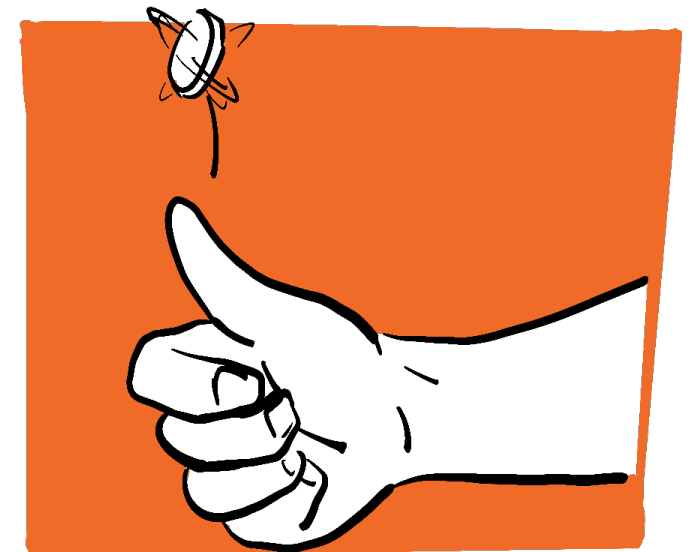
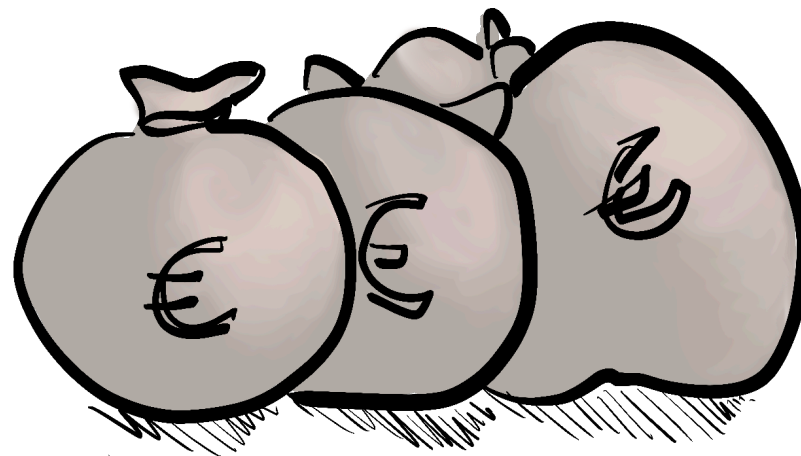
$$p_I = \frac{1}{2}$$

(assume fully decohered)

AIs: N_{ind} measurements



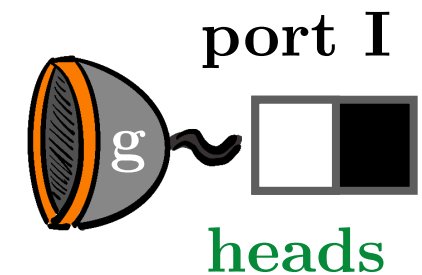
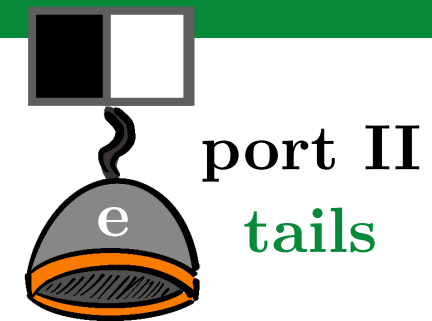
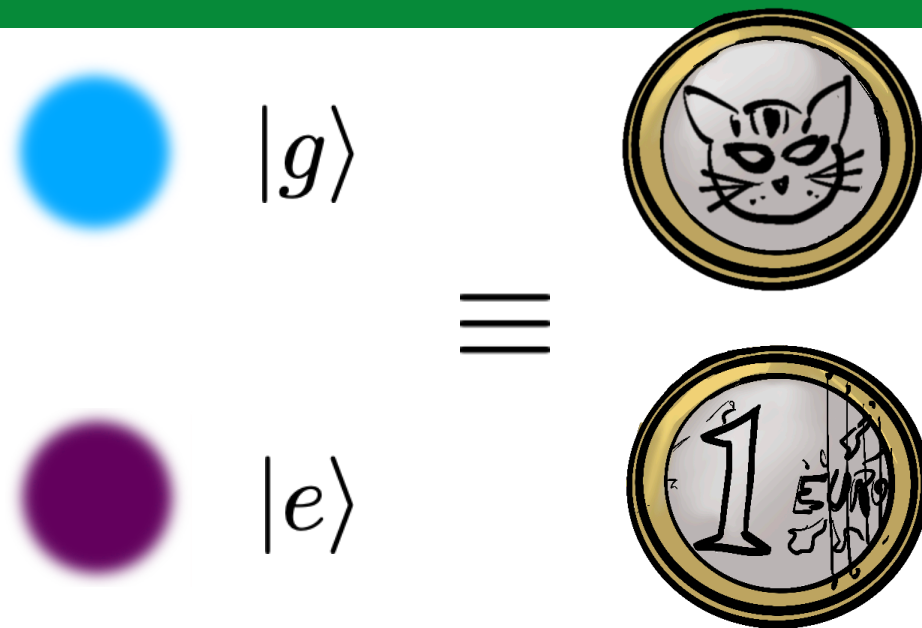
$N_{\text{ind}} =$



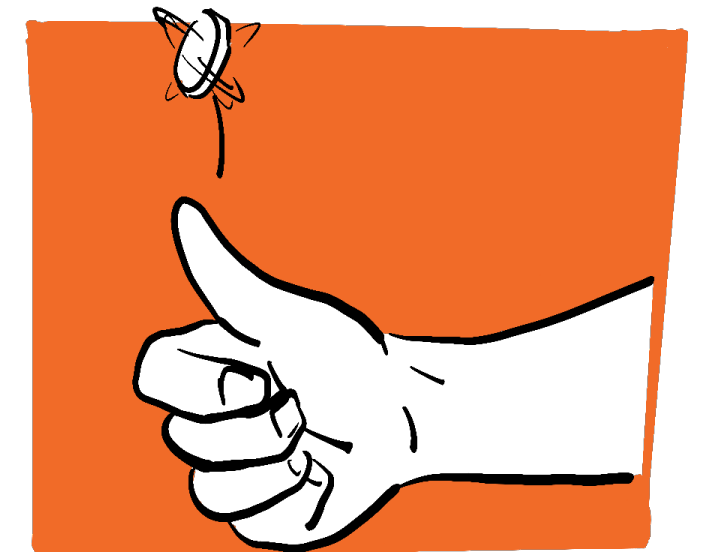
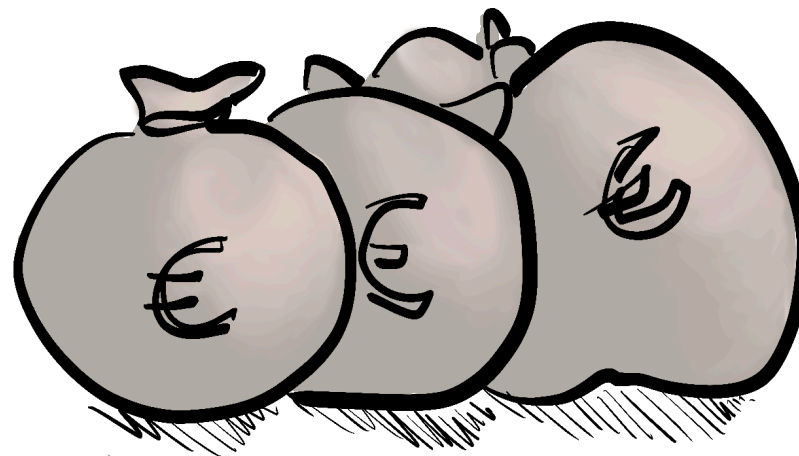
$$p_I = \frac{1}{2}$$

(assume fully decohered)

AIs: N_{ind} measurements



$N_{\text{ind}} =$

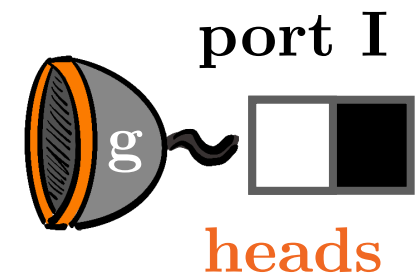
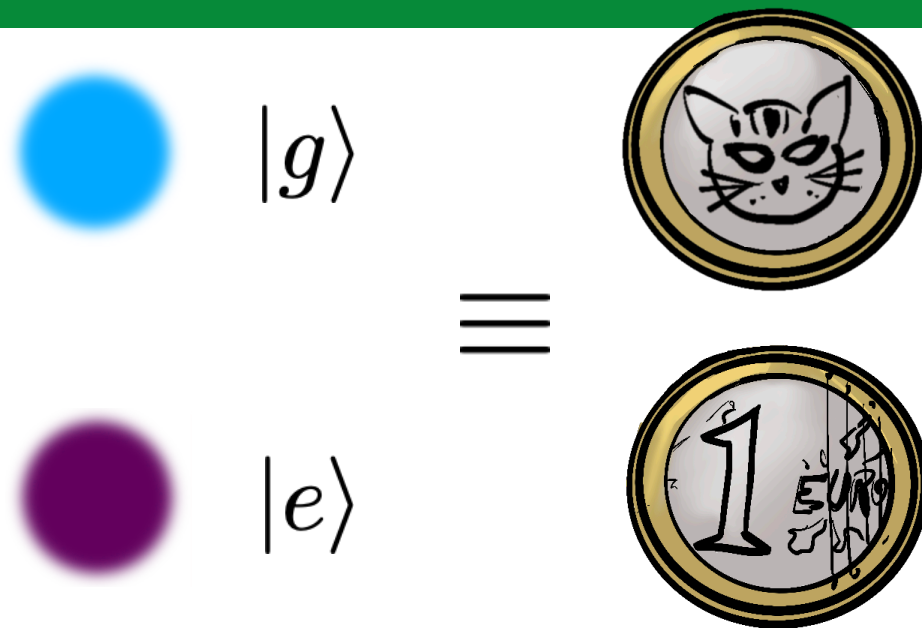


$$P_I = \binom{N_{\text{ind}}}{N_I} p_I^{N_I} (1 - p_I)^{N_{II}}$$

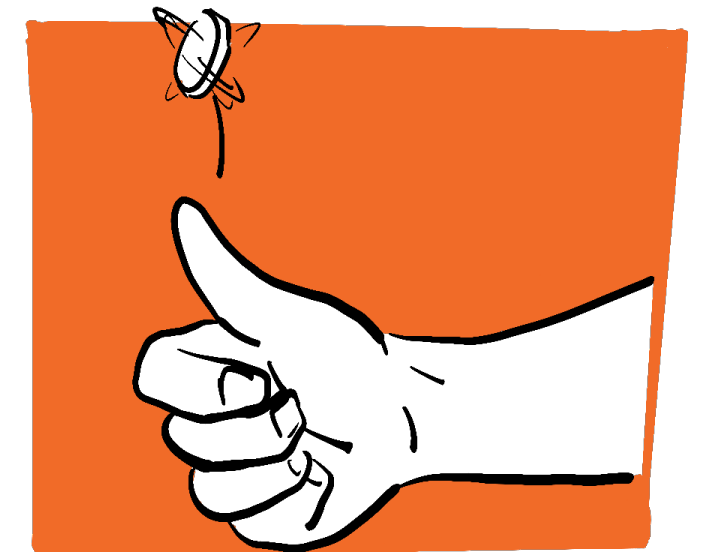
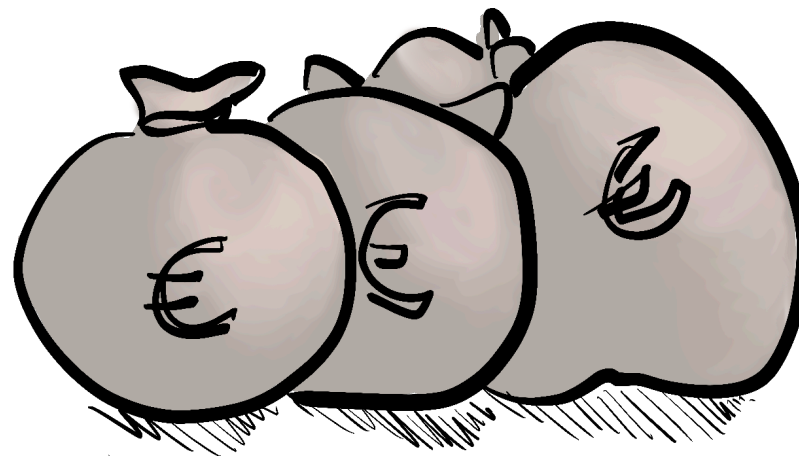
$$p_I = \frac{1}{2}$$

(assume fully decohered)

AIs: N_{ind} measurements



$N_{\text{ind}} =$



$$P_I = \binom{N_{\text{ind}}}{N_I} p_I^{N_I} (1 - p_I)^{N_{II}}$$

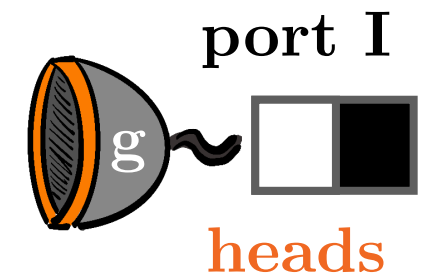
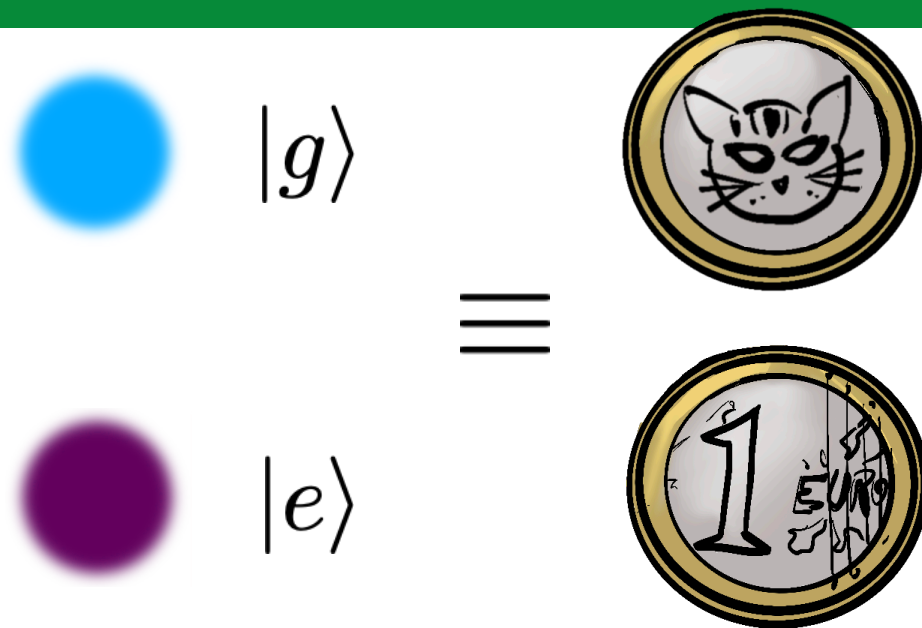
$$p_I = \frac{1}{2}$$

(assume fully decohered)

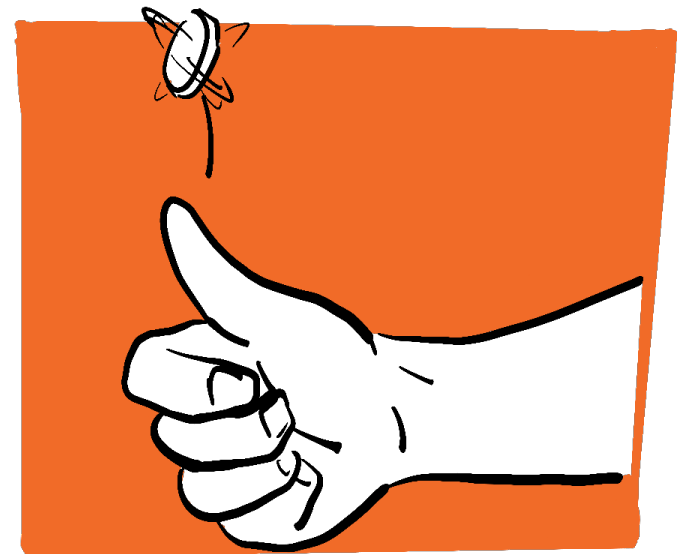
$$\Rightarrow \langle P_I \rangle = (N_I + N_{II}) p_I = N_{\text{ind}} p_I$$

$$\Rightarrow \sigma^2 = N_{\text{ind}} p_I (1 - p_I)$$

AIs: N_{ind} measurements



$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2}(1 + V \cos \Delta\phi)$$



$$P_I = \binom{N_{\text{ind}}}{N_I} p_I^{N_I} (1 - p_I)^{N_{II}}$$

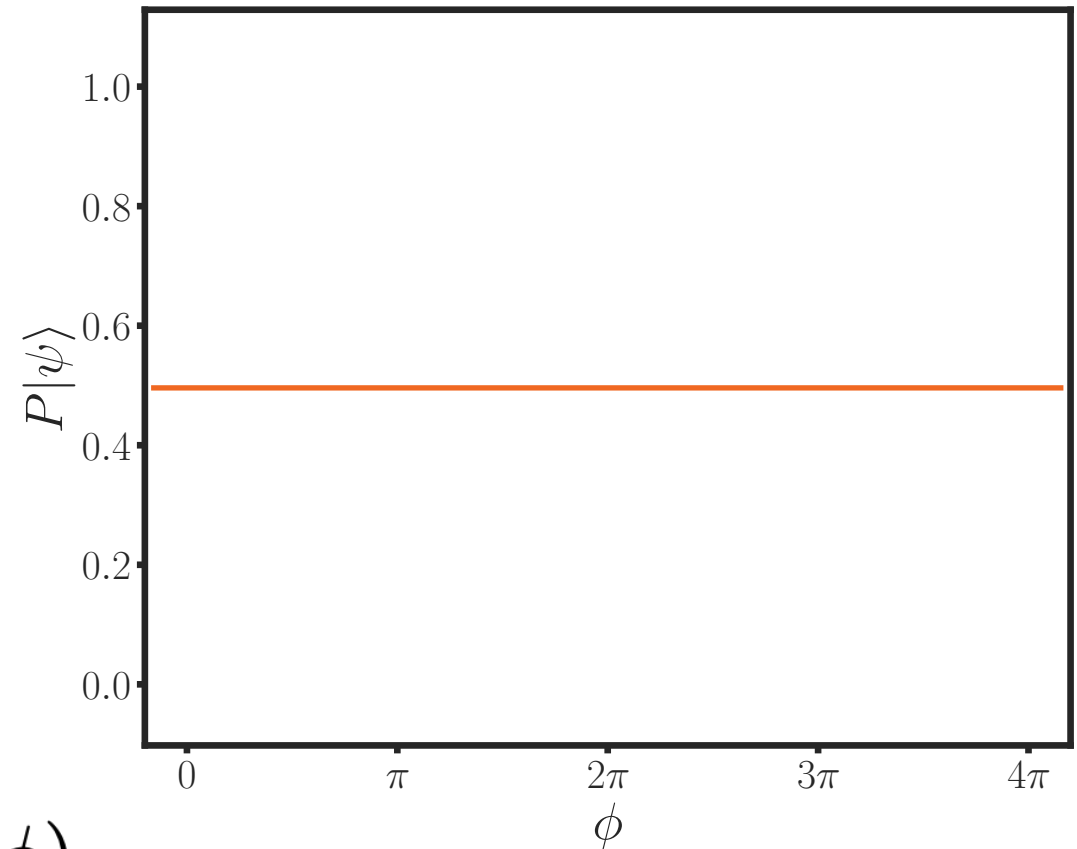
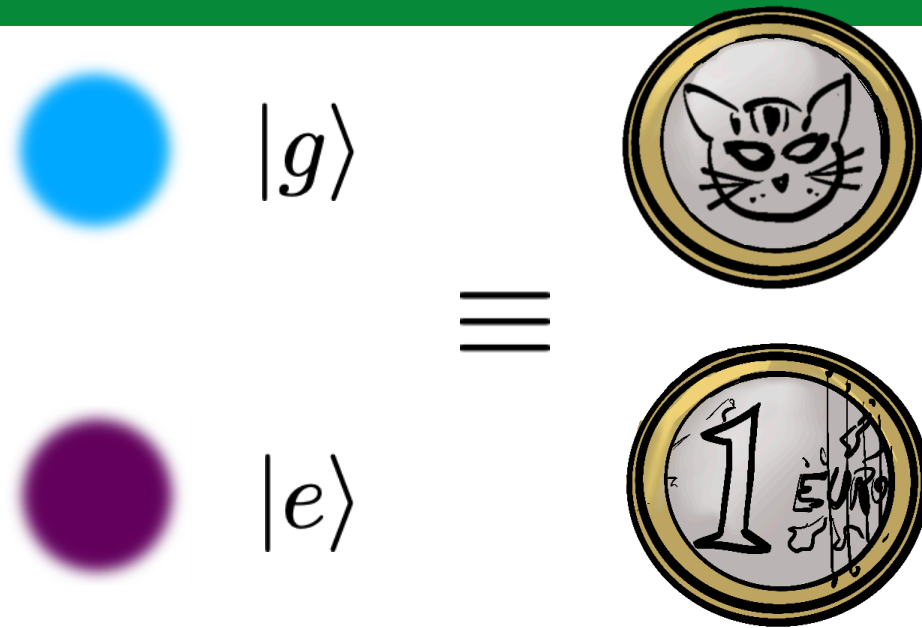
$$p_I = \frac{1}{2}$$

(assume fully decohered)

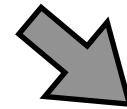
$$\Rightarrow \langle P_I \rangle = (N_I + N_{II}) p_I = N_{\text{ind}} p_I$$

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AIs: N_{ind} measurements



$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2}(1 + V \cos \Delta\phi)$$



$$V = 0$$



$$P_I = \binom{N_{\text{ind}}}{N_I} p_I^{N_I} (1 - p_I)^{N_{II}}$$

$$p_I = \frac{1}{2}$$

(assume fully decohered)

$$\Rightarrow \langle P_I \rangle = (N_I + N_{II})p_I = N_{\text{ind}} p_I$$

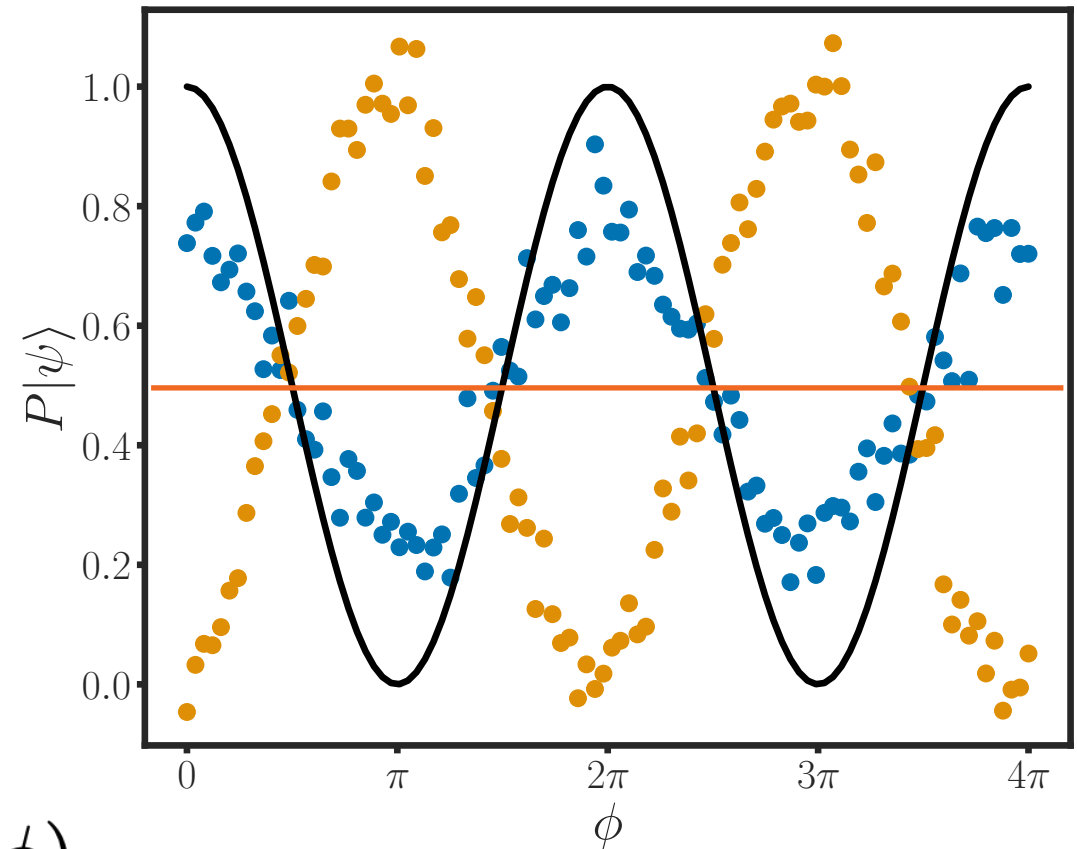
$$\Rightarrow \sigma^2 = N_{\text{ind}} p_I (1 - p_I)$$

AIs: N_{ind} measurements

- No decoherence or phase effects
- Decoherence Effect
- Phase Effect

Visibility

$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos \Delta\phi)$$

$$V = e^{-s}$$

$$\sigma^{\text{QNL}} = \frac{\sqrt{N_{\text{ind}}}}{2}$$

$$\Rightarrow \langle P_I \rangle = (N_I + N_{II})p_I = N_{\text{ind}} p_I$$

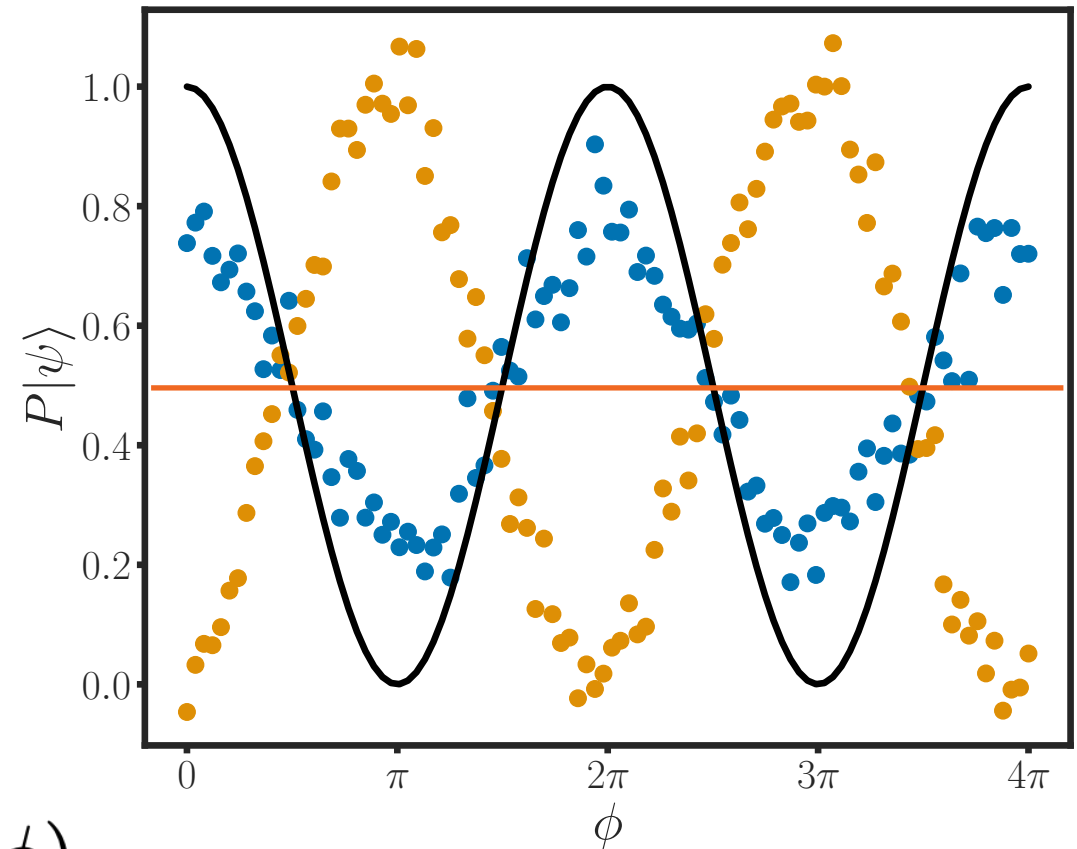
$$\Rightarrow \sigma^2 = N_{\text{ind}} p_I (1 - p_I)$$

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$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos \Delta\phi)$$

$$V = e^{-s}$$

$$\sigma^{\text{QNL}} = \frac{\sqrt{N_{\text{ind}}}}{2}$$

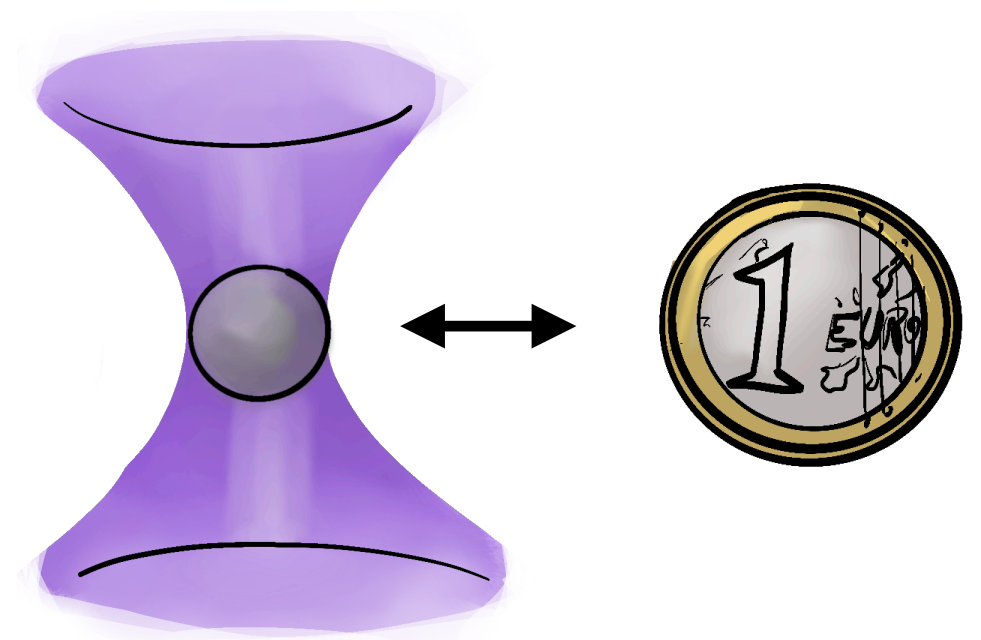
$$\Rightarrow \langle P_I \rangle = (N_I + N_{II})p_I = N_{\text{ind}} p_I$$

$$\Rightarrow \sigma^2 = N_{\text{ind}} p_I (1 - p_I)$$

Beating the classical sensitivity

Visibility

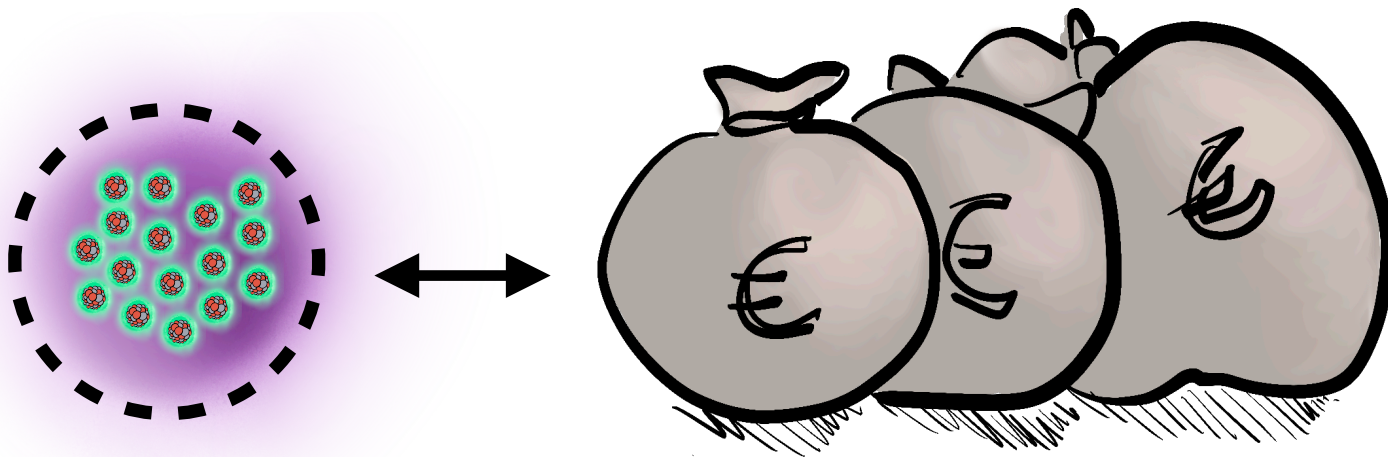
$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



Matter Interferometers

VS

Atom Interferometers



$$\sigma^{\text{QNL}} = \frac{\sqrt{N_{\text{ind}}}}{2}$$

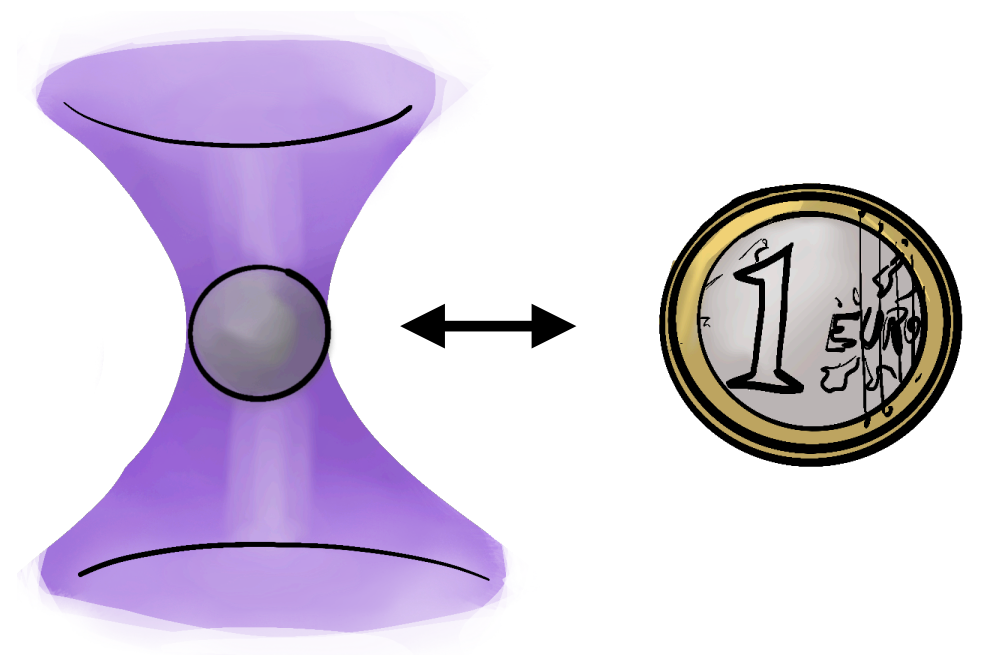
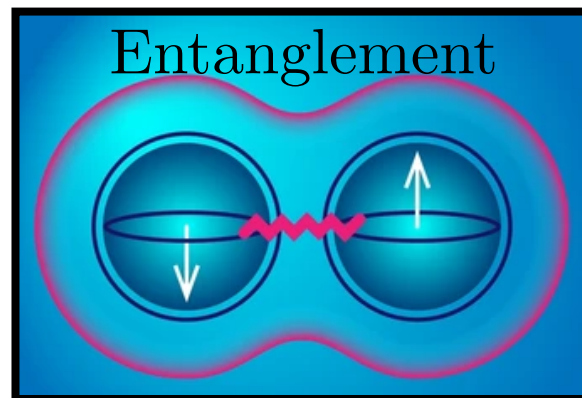
$$\begin{aligned} \Rightarrow \langle P_I \rangle &= (N_I + N_{II})p_I = N_{\text{ind}} p_I \\ \Rightarrow \sigma^2 &= N_{\text{ind}} p_I (1 - p_I) \end{aligned}$$

Beating the classical sensitivity

$$|\text{GHZ}\rangle = \frac{|000\rangle + |111\rangle}{\sqrt{2}}$$

N00N states

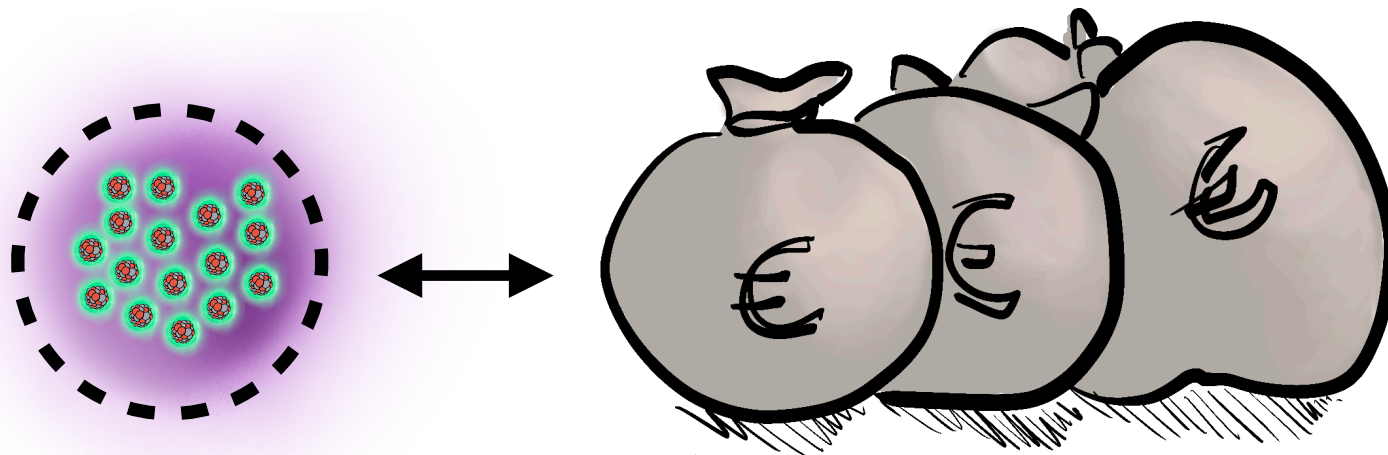
Cat states



Matter Interferometers

VS

Atom Interferometers

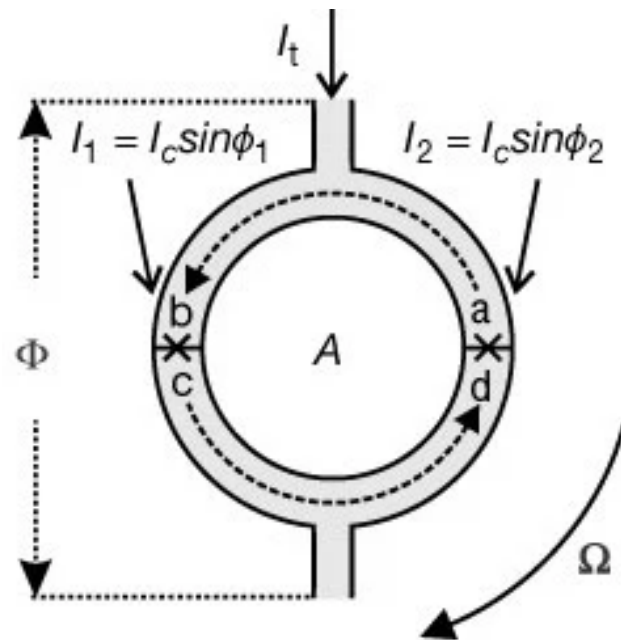


$$\sigma^{\text{QNL}} = \frac{\sqrt{N_{\text{ind}}}}{2}$$

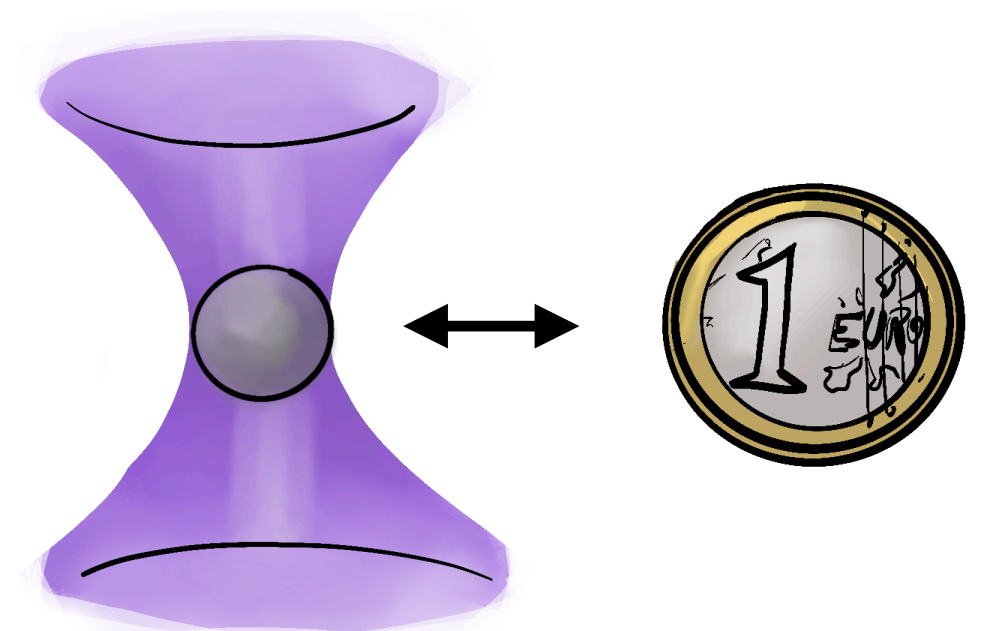
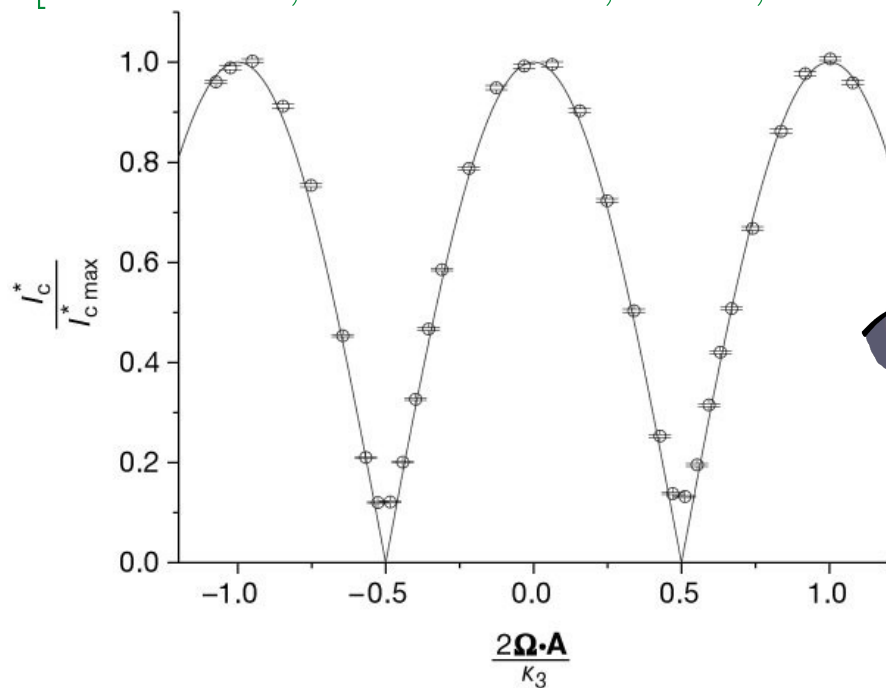
$$\Rightarrow \langle P_I \rangle = (N_I + N_{II})p_I = N_{\text{ind}} p_I$$

$$\Rightarrow \sigma^2 = N_{\text{ind}} p_I (1 - p_I)$$

Beating the classical sensitivity



[Simmonds, Marchenkov, et al., 2001]



Matter Interferometers

VS

Atom Interferometers

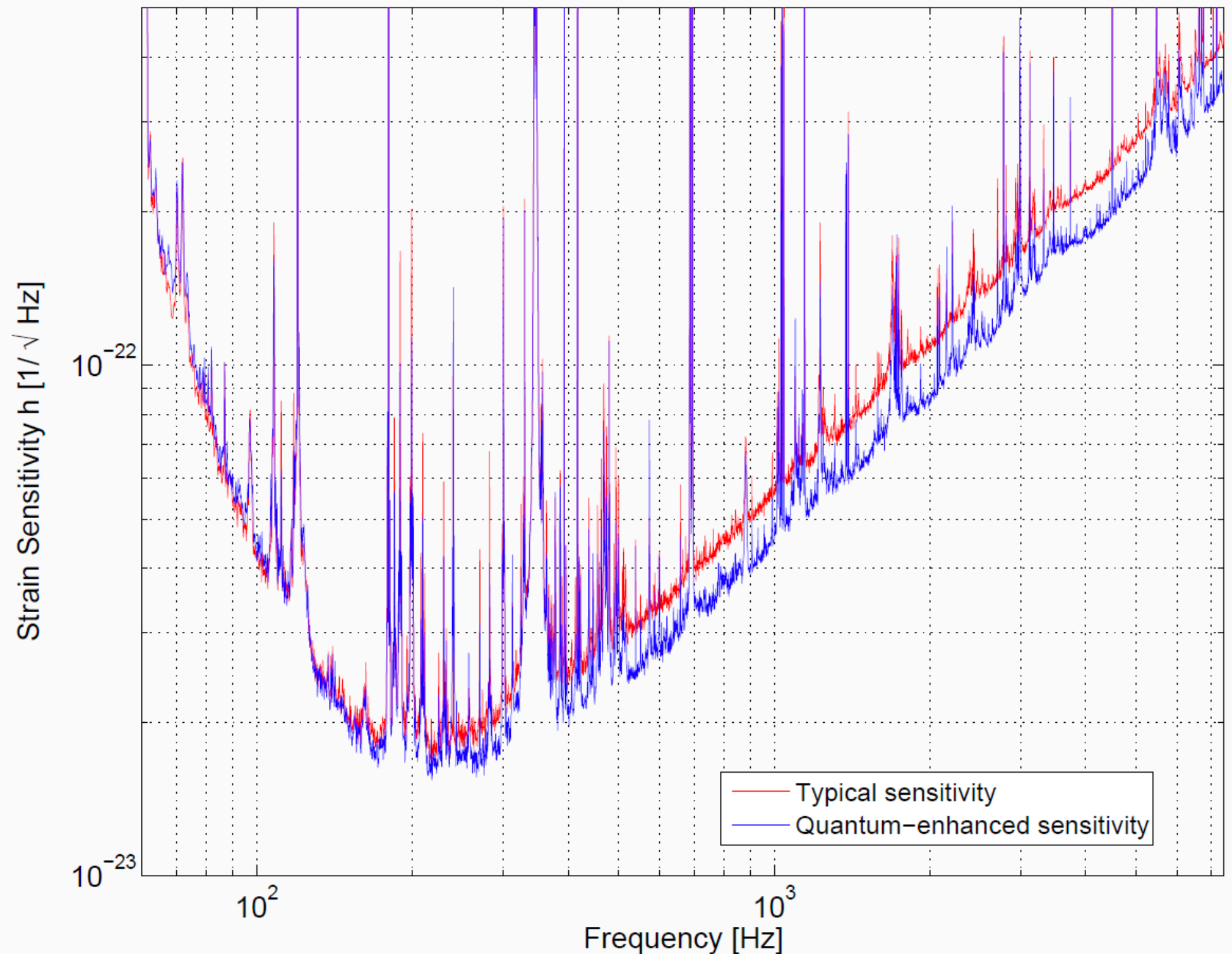
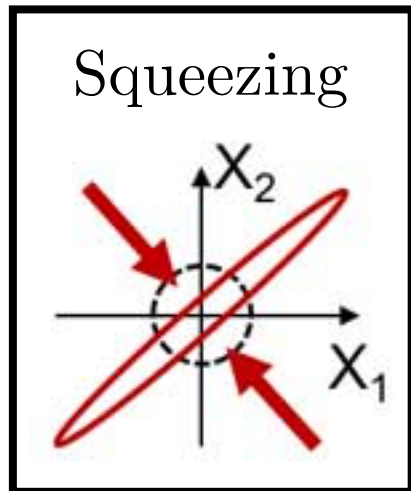
$$\sigma^{\text{QNL}} = \frac{\sqrt{N_{\text{ind}}}}{2}$$

$$\Rightarrow \langle P_I \rangle = (N_I + N_{II})p_I = N_{\text{ind}} p_I$$

$$\Rightarrow \sigma^2 = N_{\text{ind}} p_I (1 - p_I)$$

Beating the classical sensitivity

<https://www.ligo.org/science/Publication-SqueezedVacuum/>

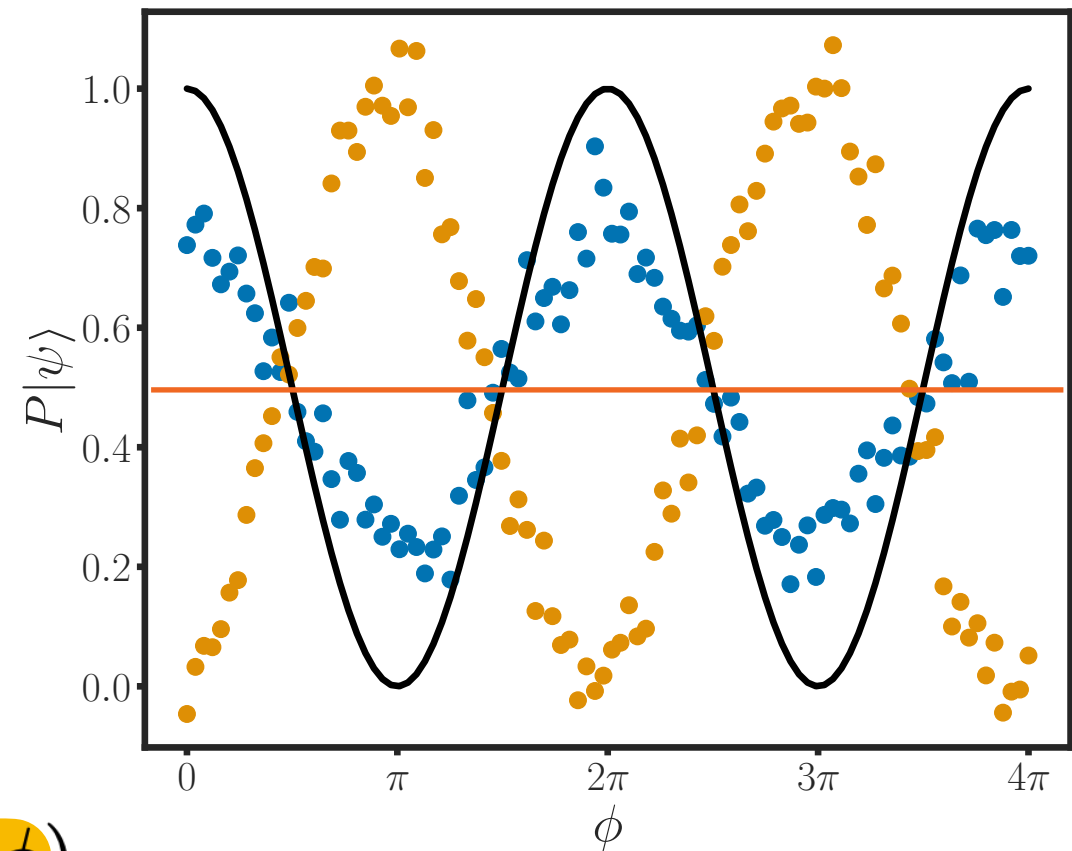


AIs: N_{ind} measurements

- No decoherence or phase effects
- Decoherence Effect
- Phase Effect

Visibility

$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos \Delta\phi)$$

$$V = e^{-s}$$

$$\sigma_V^{\text{QNL}} = \frac{2}{\sqrt{N_{\text{ind}}}}$$

$\Rightarrow \langle P_I \rangle = (N_I + N_{II})p_I = N_{\text{ind}} p_I$
 $\Rightarrow \sigma^2 = N_{\text{ind}} p_I (1 - p_I)$

Phase Shifts in Atom Interferometers

[Dimopoulos, Graham, et al. 2008] [Hogan, Johnson, et al. 2011], [Yu, Tinto, 2011] [Graham, Hogan, 2013], [Canuel, Bertoldi, et al. 2018] [Canuel, Abend, et al. 2020] [Kolkowitz, Pikovski, et al., 2016] [Zhan, Wang, et al. 2020] [El-Neaj, Alpigiani, et al. 2020] [Badurina, Bentine, et al. 2020] [Graham, Hogan, et al. 2016] [Graham, Hogan, et al. 2017], [Ballmer, Adhikari, et al. 2022]

GWs

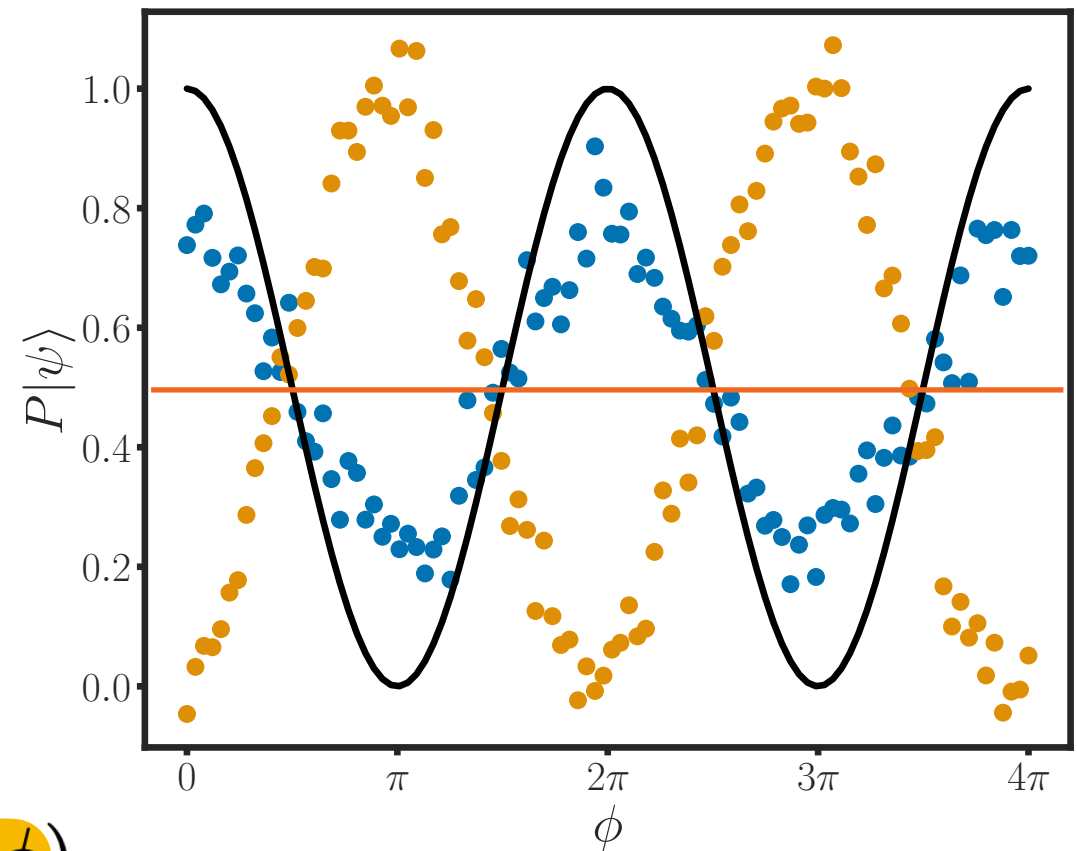
$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos \Delta\phi)$$

ULDM

[Graham, Kaplan, et al. 2016]
[Arvanitaki, Graham, et al. 2018]
[Kolb, Weers, et al. 2018]
[Antypas, Banerjee, 2022]
[Badurnina, Gipson, et al. 2022]
[Badurnina, Beniwal, et al. 2023]
...

5th forces

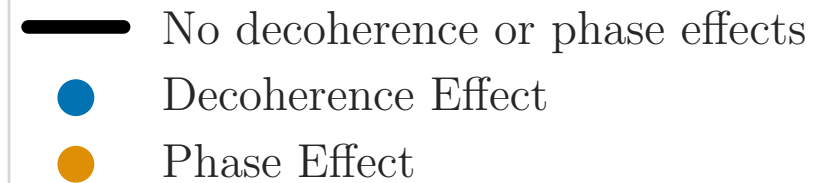
[Wacker, 2010], [Rosi, Sorrentino, et al. 2014] [Biedermann, Wu, et al. 2015] [Rosi, D'Amico, et al. 2017] [Fray, Diez, et al. 2004] [Schlippert, Hartwig, et al. 2014] [Zhou, Long, et al. 2015] [Barrett, Antoni-Micollier, et al. 2016] [Kuhn, McDonald, et al. 2014] [Barrett, Antoni-Micollier, et al. 2015] [Tarallo, Mazzoni, et al. 2014] [Bonnin, Zahzam et al. 2013] [Hartwig, Abend, et al. 2015] [Asenbaum, Overstreet, et al. 2020] [Williams, Chiow, et al. 2016] [Battelier, Berge, et al., 2019]



EDMs

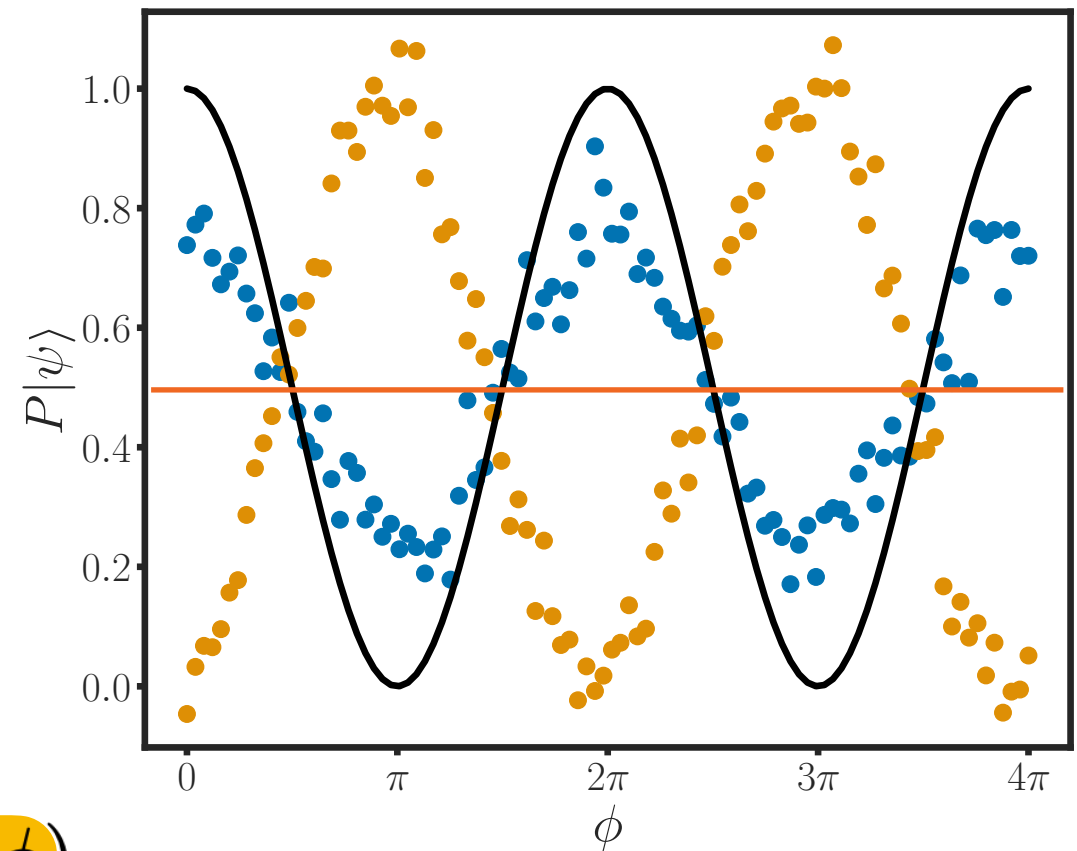
[Wicht et al, 2002] [Bennet et al. 2006] [Cadoret et al. 2008] [Terranova, Tino, 2014]...

Decoherence in Atom Interferometers



Visibility

$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos \Delta\phi)$$

$$V = e^{-s}$$

Particle scattering

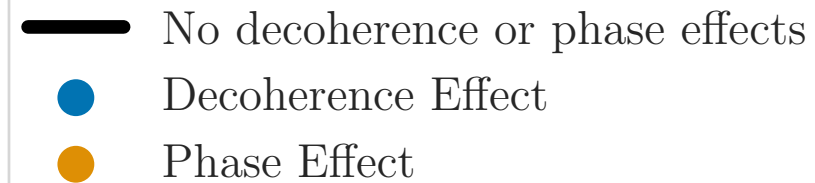
[Riedel, 2013]

[Riedel, Yavin, 2017]

[Du, CM, Pardo, Wang, Zurek, 2022]

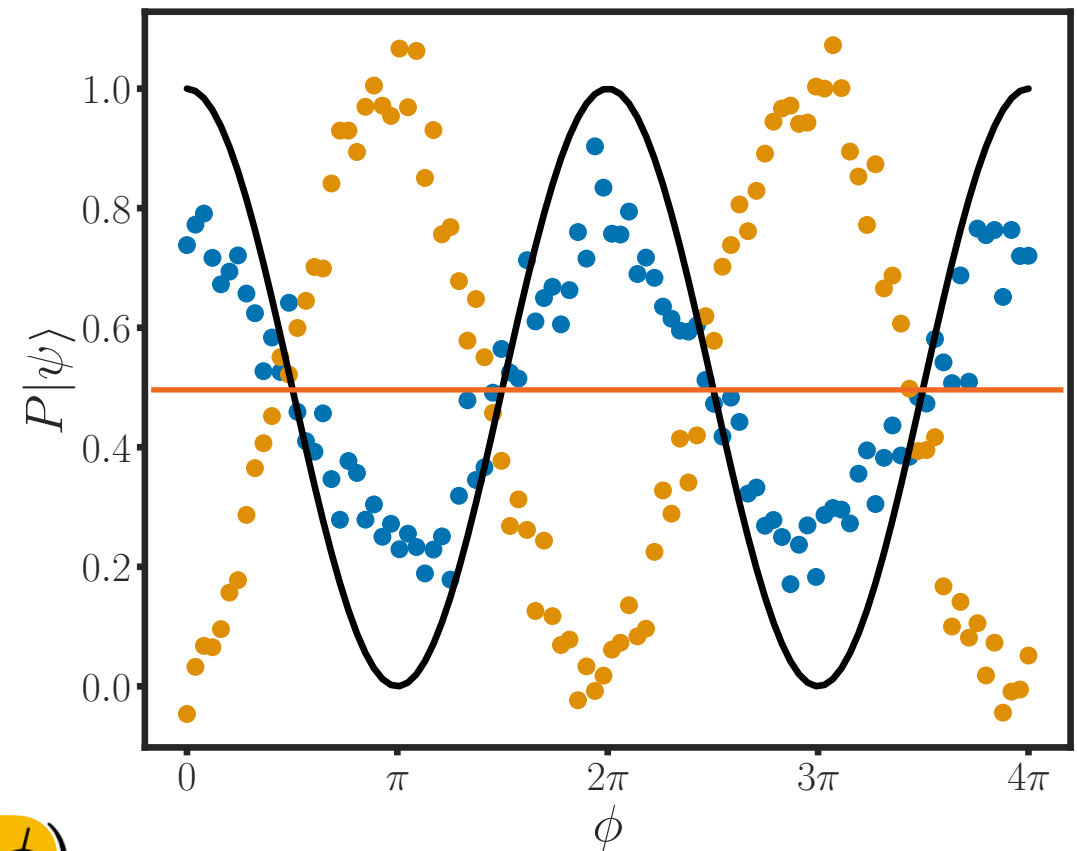
[Du, CM, Pardo, Wang, Zurek, 2023]

Decoherence in Atom Interferometers



Visibility

$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos \Delta\phi)$$

$$V = e^{-s} = e^{\left[-m_{\text{cloud}} \int_0^{t_{\text{exp}}} R dt \right]} = e^{t/\tau}$$

Particle scattering

[Riedel, 2013]

[Riedel, Yavin, 2017]

[Du, CM, Pardo, Wang, Zurek, 2022]

[Du, CM, Pardo, Wang, Zurek, 2023]

AIs: the Rate

[Y. Du, CM, et al. 2022]

Number of events / (target mass · time)

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

Accumulated decoherence: **Rate**

$$= e^{\left[-m_{\text{cloud}} \int_0^{t_{\text{exp}}} R dt \right]}$$

$$= e^{t/\tau}$$

$$\gamma = e^{-s+i\phi} = \underbrace{e^{-s}}_V e^{i\phi}$$

AIs: the Rate

$$f(\mathbf{v}) = \frac{1}{N_0} \exp \left(-\frac{(\mathbf{v} + \mathbf{v}_e)^2}{v_0^2} \right) \Theta(v_{\text{esc}} - \|\mathbf{v} + \mathbf{v}_e\|)$$

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

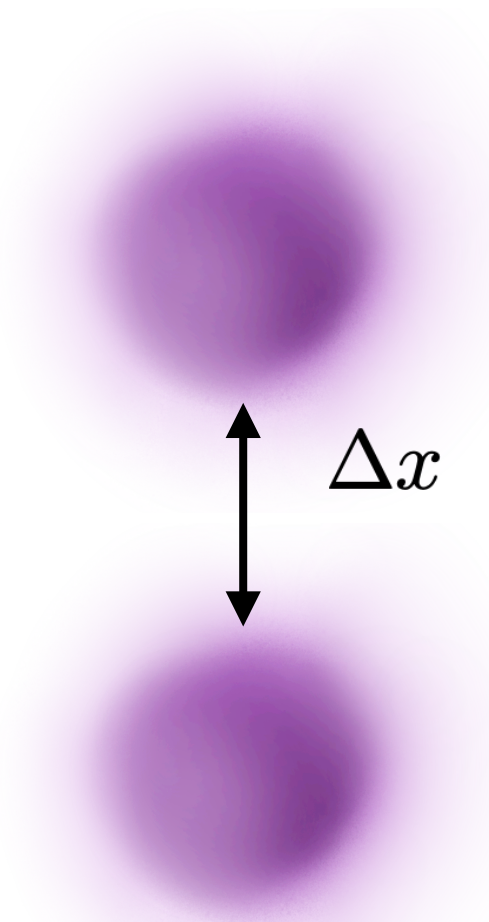
$$\frac{1}{\rho_T} \frac{\rho_\chi}{m_\chi}$$

$$\Gamma(\mathbf{v}) = V \int \frac{d^3\mathbf{q}}{(2\pi)^3} \sum_f |\langle f | H_{\text{int}} | i \rangle|^2 (2\pi) \delta(E_f - E_i - \omega_{\mathbf{q}})$$

AIs: the Rate

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

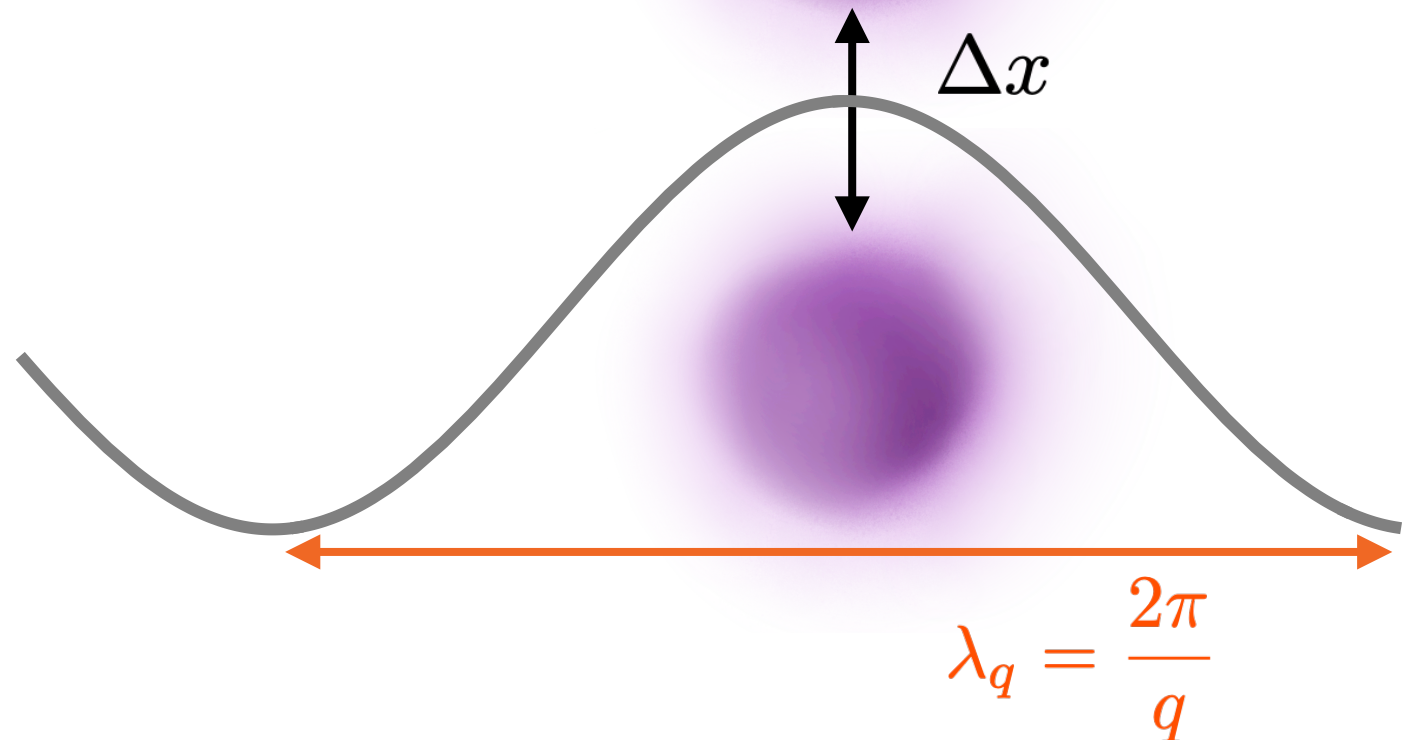
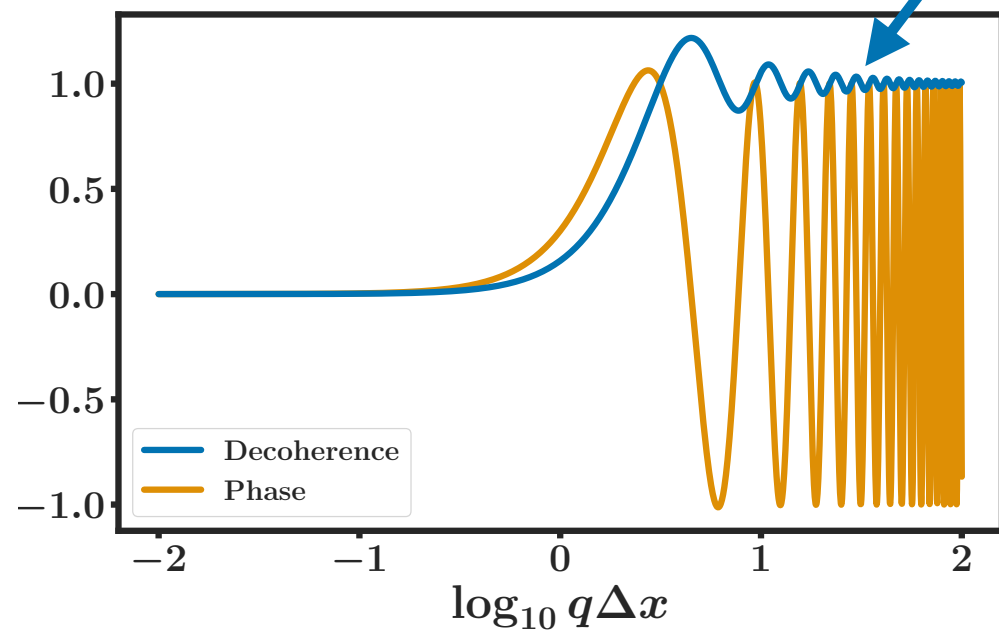


AIs: the Rate

$$\frac{1}{2} \int_{-1}^1 \text{Re}\{\mathcal{F}_{\text{decoh}}(\mathbf{q})\} d \cos \theta_{\mathbf{q}\Delta\mathbf{x}} = 1 - \frac{\sin(q\Delta x)}{q\Delta x}$$

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$

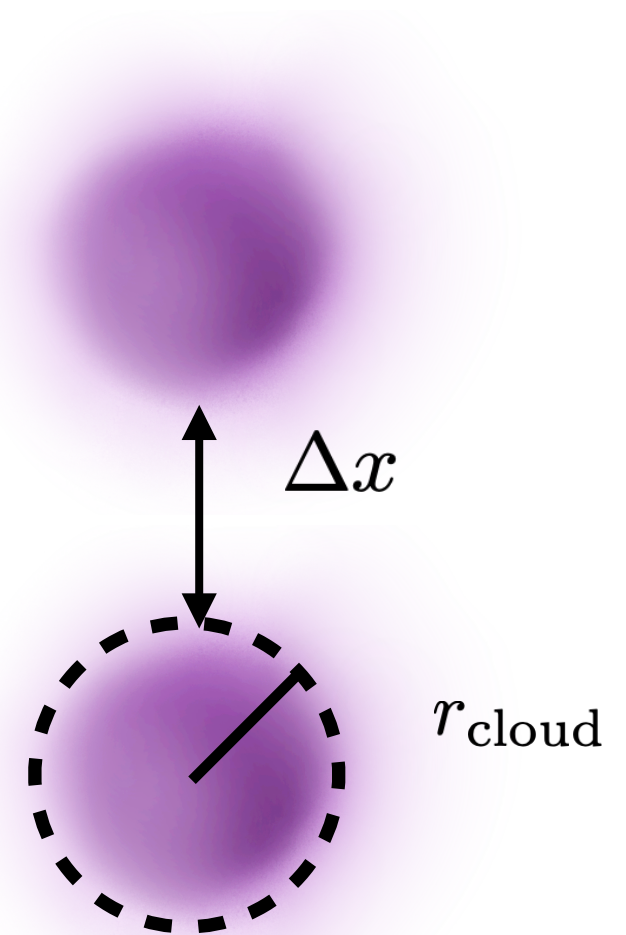
$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$



AIs: the Rate

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

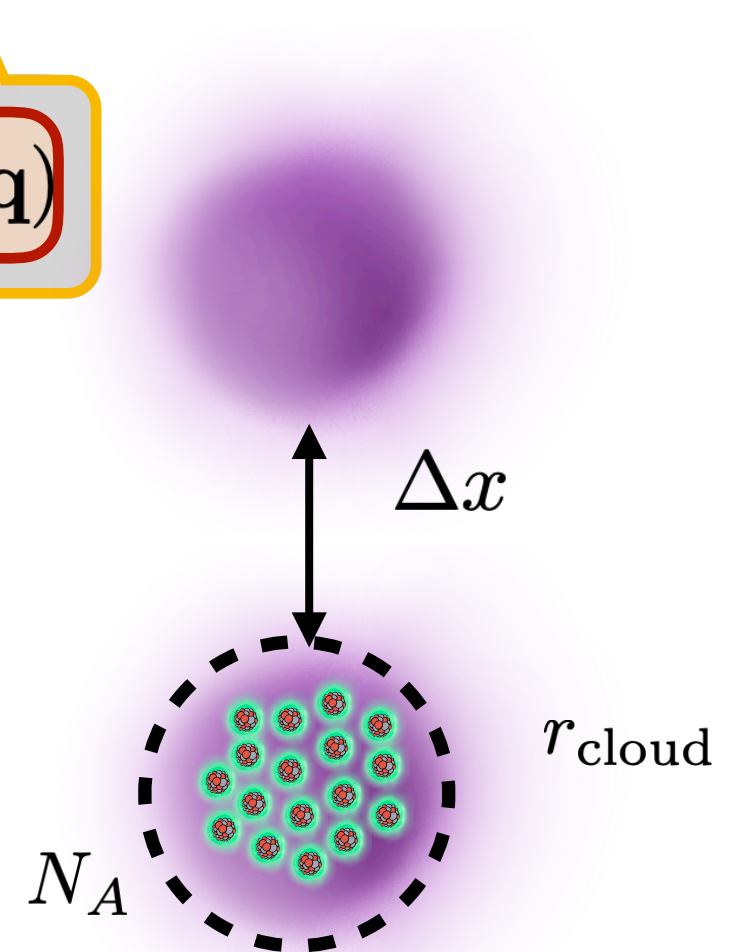
$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_{\text{T}}^2(\mathbf{q})$$



AIs: the Rate

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_{\text{T}}^2(\mathbf{q})$$



AIs: the Rate

[Y. Du, CM, et al. 2022]

Number of events / (target mass · time)

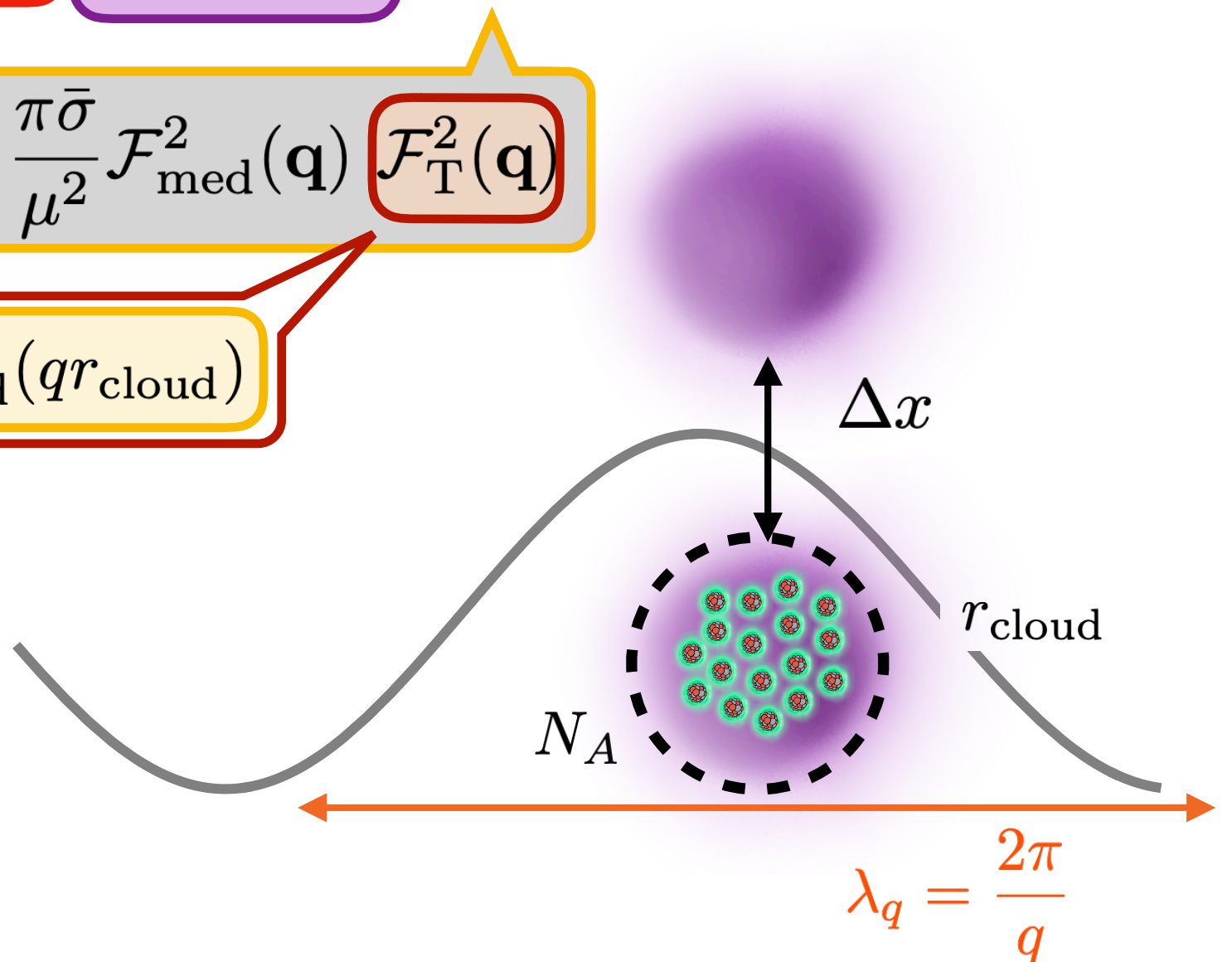
$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

Born (coherent) enhancement!

$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_T^2(\mathbf{q})$$

$$\mathcal{F}_T(\mathbf{q}) = N[1 + A(N_A - 1) \mathcal{F}_{\text{cloud}}^2(qr_{\text{cloud}})]$$

$$\mathcal{F}_{\text{cloud}}(qr_{\text{cloud}}) \begin{cases} \frac{3j_1(qr_{\text{cloud}})}{qr_{\text{cloud}}} \\ \exp\left(-\frac{q^2}{(2r_{\text{BEC}})^2}\right) \end{cases}$$



[V. Bednyakov and D. V. Naumov, 2018]

AIs: the Rate

[Y. Du, CM, et al. 2022]

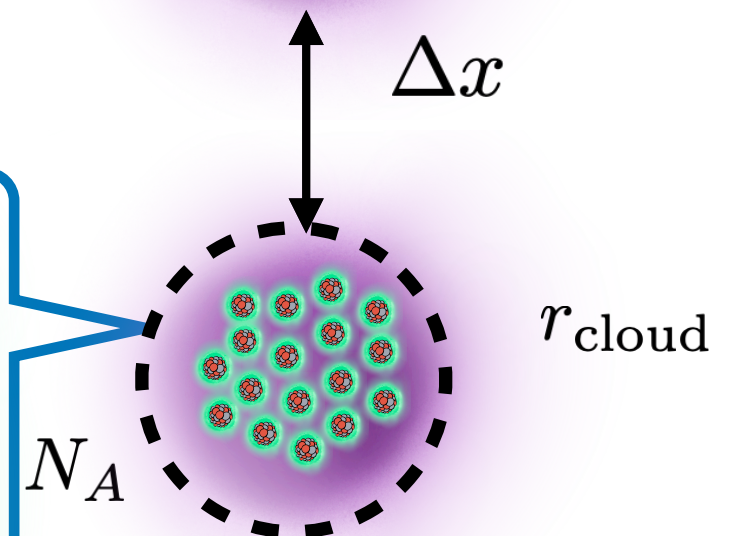
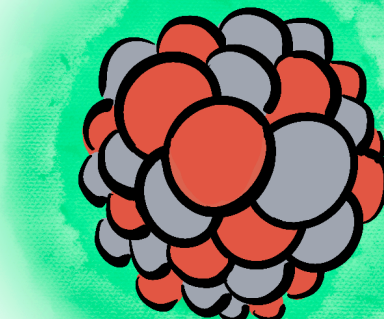
Number of events / (target mass · time)

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

Born (coherent) enhancement!

$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_T^2(\mathbf{q})$$

$$\mathcal{F}_T(\mathbf{q}) = N[1 + A(N_A - 1) \mathcal{F}_{\text{cloud}}^2(qr_{\text{cloud}})]$$



AIs: the Rate

[Y. Du, CM, et al. 2022]

Number of events / (target mass · time)

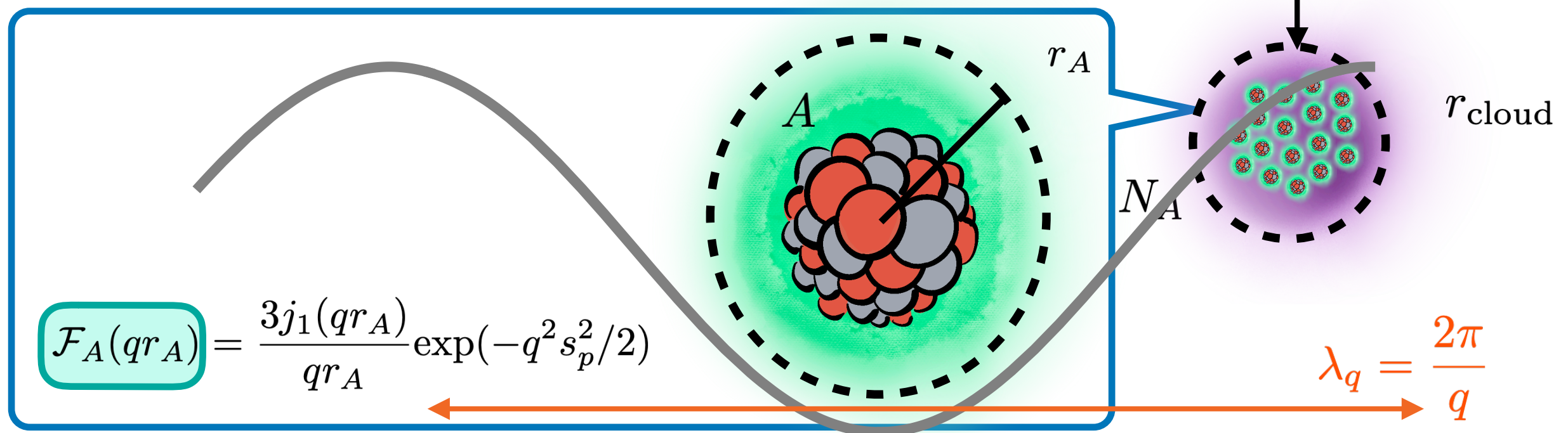
$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

Born (coherent) enhancement!
(x2)

$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_T^2(\mathbf{q})$$

$$\mathcal{F}_T(\mathbf{q}) = N[1 + A(N_A - 1) \mathcal{F}_{\text{cloud}}^2(qr_{\text{cloud}}) + A \mathcal{F}_A^2(qr_A)]$$

$$\mathcal{F}_A(qr_A) = \frac{3j_1(qr_A)}{qr_A} \exp(-q^2 s_p^2/2)$$



AIs: the Rate

[Y. Du, CM, et al. 2022]

Number of events / (target mass · time)

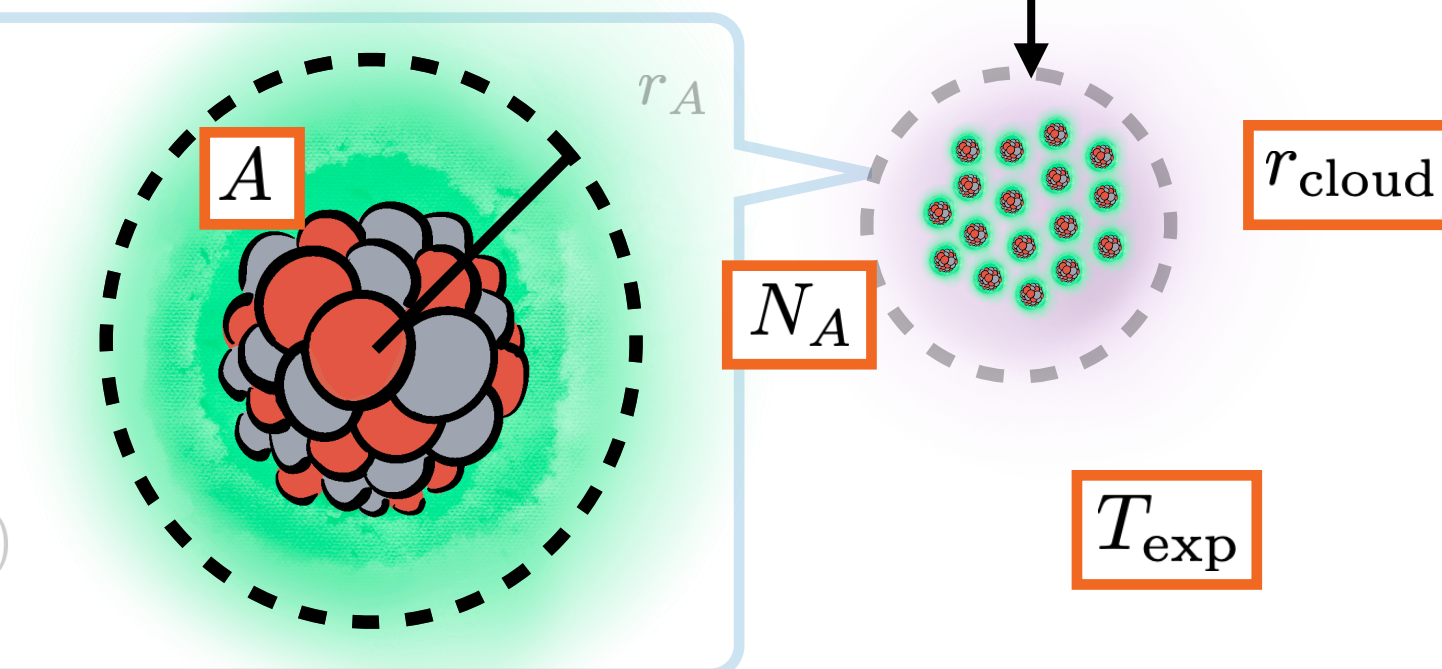
$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

Born (coherent) enhancement!
(x2)

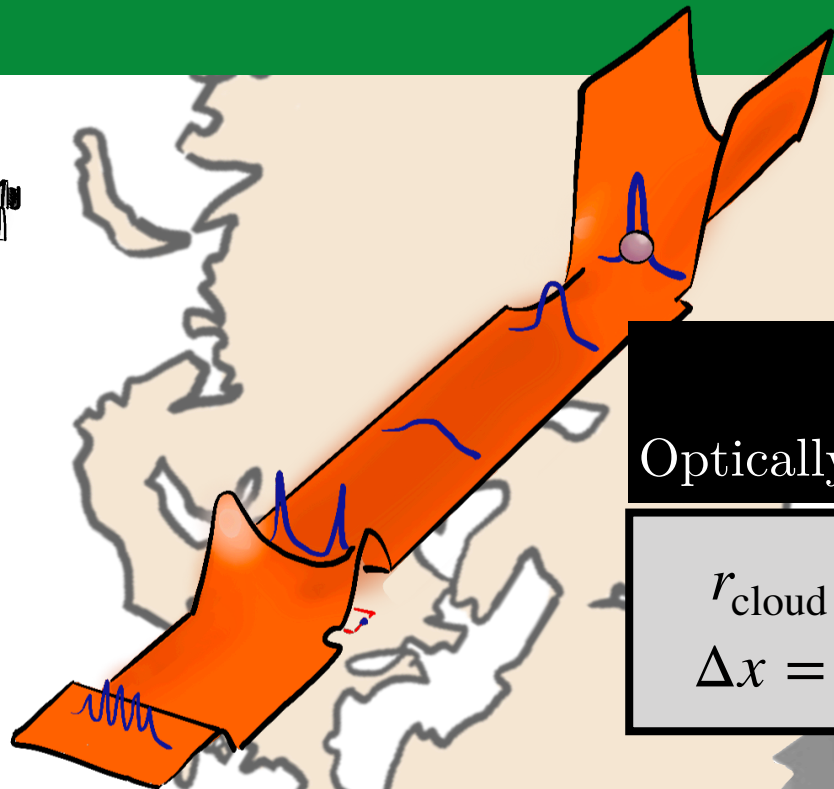
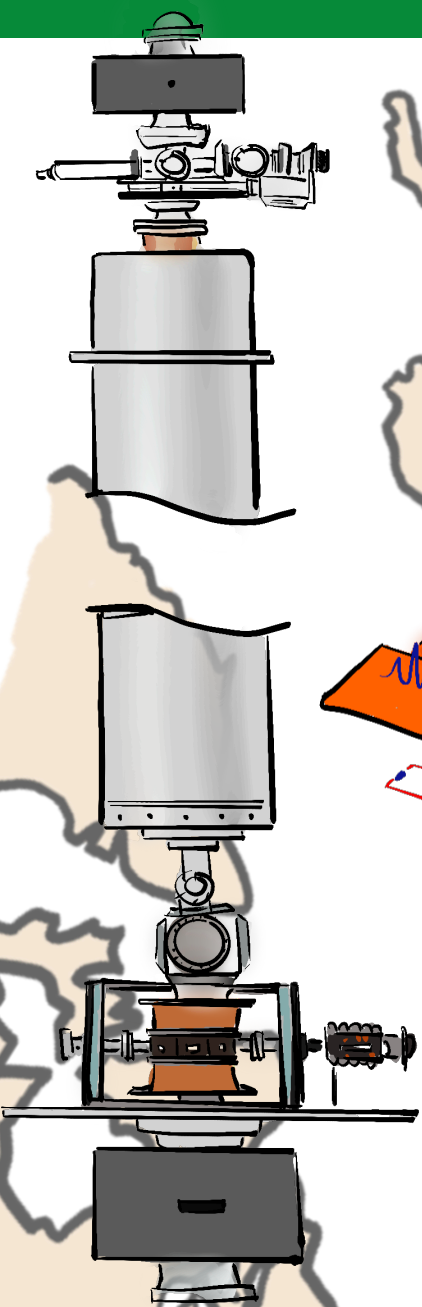
$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_T^2(\mathbf{q})$$

$$\mathcal{F}_T(\mathbf{q}) = N[1 + A(N_A - 1) \mathcal{F}_{\text{cloud}}^2(qr_{\text{cloud}}) + A \mathcal{F}_A^2(qr_A)]$$

$$\mathcal{F}_A(qr_A) = \frac{3j_1(qr_A)}{qr_A} \exp(-q^2 s_p^2/2)$$



AIs: Examples



PINO Nb
Optically levitated nanosphere

$$r_{\text{cloud}} \sim 1\mu\text{m}, N \sim 10^{13}$$
$$\Delta x = 0.1\mu\text{m}, t_{\text{exp}} = 0.5\text{s}$$



STANFORD ⁸⁷Rb
10-m atomic fountain

$$r_{\text{cloud}} \sim 0.2\text{mm}, N \sim 10^8$$
$$\Delta x = 0.1\text{m}, t_{\text{exp}} = 2\text{s}$$

ELGAR ^{87}Rb

European Laboratory for Gravitation
and Atom-interferometric Research

MIGA ^{87}Rb

Matter wave-laser based
Interferometer Gravitation Antenna

AION

Atom Interferometer
Observatory and Network

ZAIGA ^{87}Rb

Zhaoshan long-baseline Atom
Interferometer Gravitation Antenna

PINO Nb

Optically levitated nanosphere

$$r_{\text{cloud}} \sim 1\mu\text{m}, N \sim 10^{13}$$

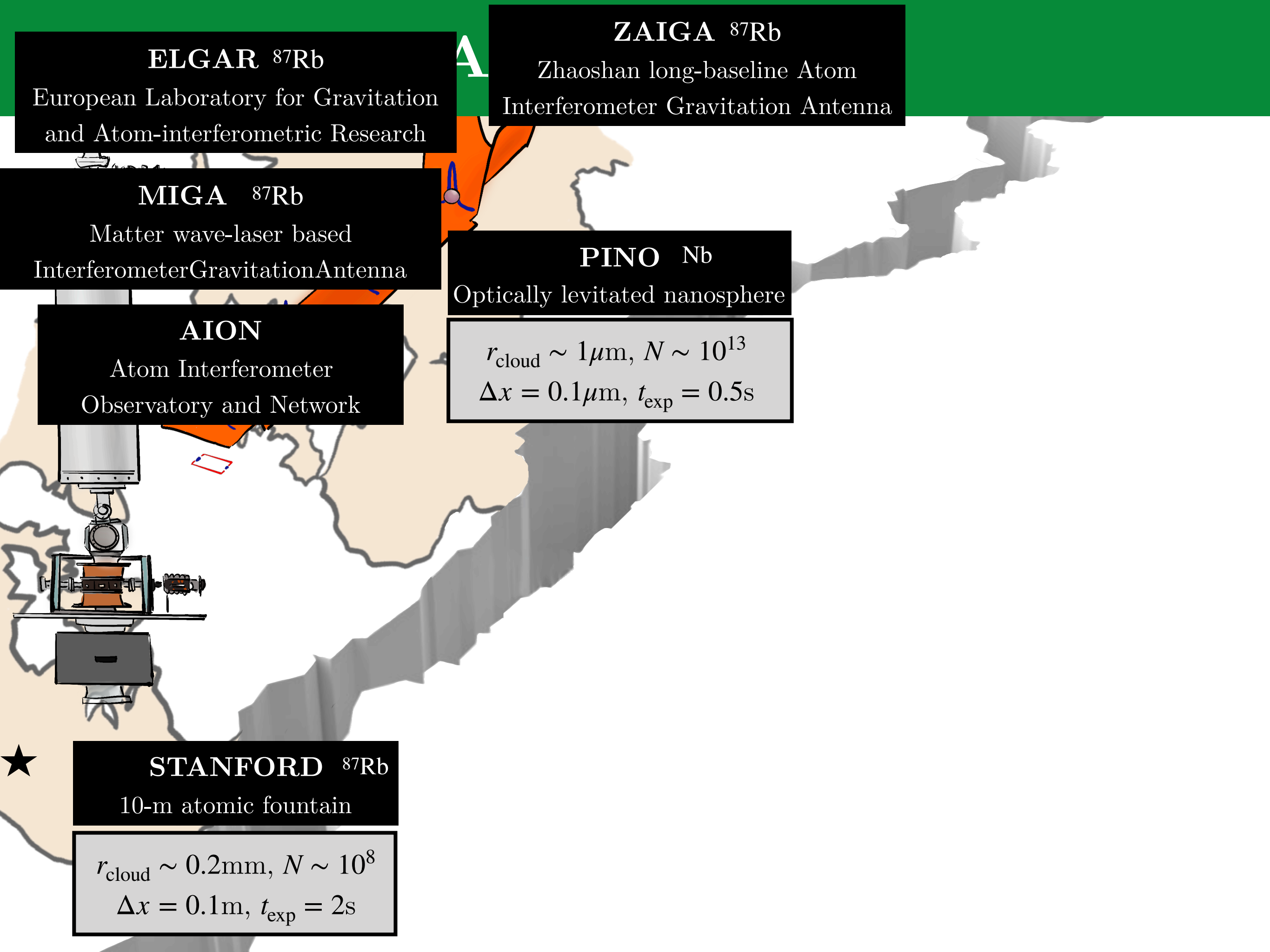
$$\Delta x = 0.1\mu\text{m}, t_{\text{exp}} = 0.5\text{s}$$

★ STANFORD ^{87}Rb

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★ STANFORD

10-m atomic fountain

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$$\Delta x = 0.1\text{m}, t_{\text{exp}} = 2\text{s}$$

^{87}Rb

^{87}Rb

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Interferometer Gravitation Antenna

PINO Nb

Optically levitated nanosphere

$$r_{\text{cloud}} \sim 1\mu\text{m}, N \sim 10^{13}$$
$$\Delta x = 0.1\mu\text{m}, t_{\text{exp}} = 0.5\text{s}$$

MAQRO SiO_2

Macroscopic Quantum Resonators

$$r_{\text{cloud}} \sim 0.1\mu\text{m}, N \sim 10^{10}$$
$$\Delta x = 0.1\mu\text{m}, t_{\text{exp}} = 100\text{s}$$



GDM ^{87}Rb

Gravity Dark energy Mission

$$r_{\text{cloud}} \sim 1\text{mm}, N \sim 10^{10}$$
$$\Delta x = 25\text{m}, t_{\text{exp}} = 20\text{s}$$

BECCAL ^{87}Rb

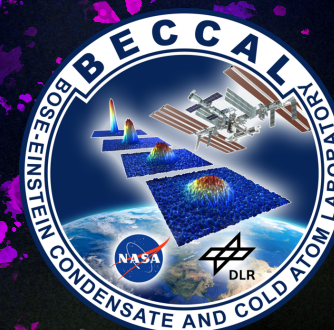
Bose-Einstein Condensate
Cold Atom Laboratory

$$r_{\text{cloud}} \sim 0.1\text{mm}, N \sim 10^8$$
$$\Delta x = 1\text{mm}, t_{\text{exp}} = 3\text{s}$$

STANFORD ^{87}Rb

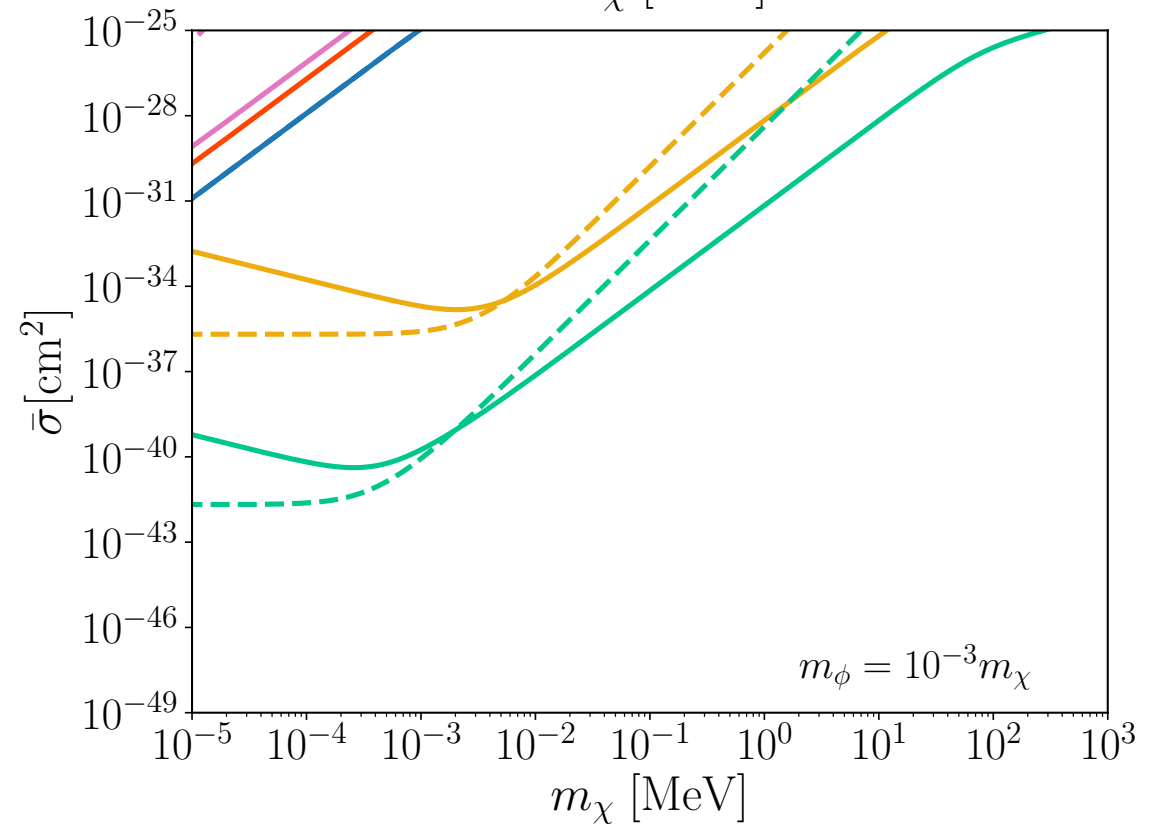
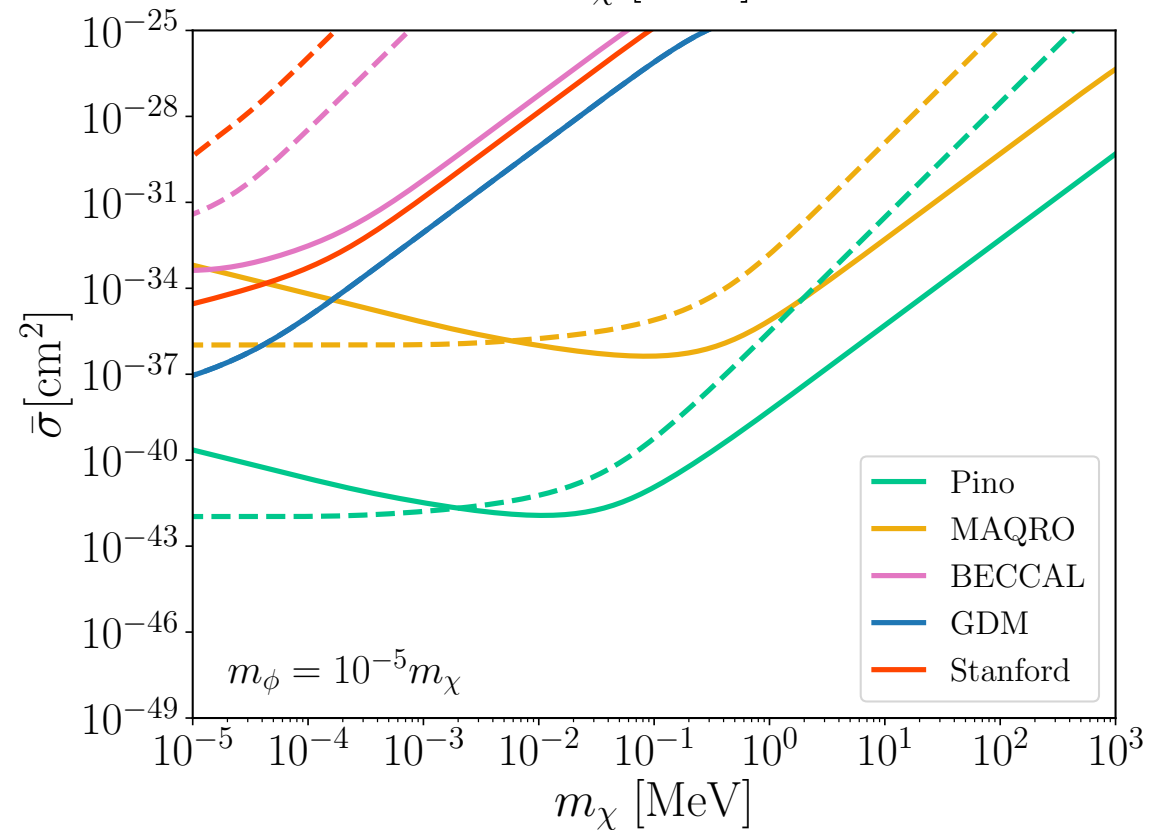
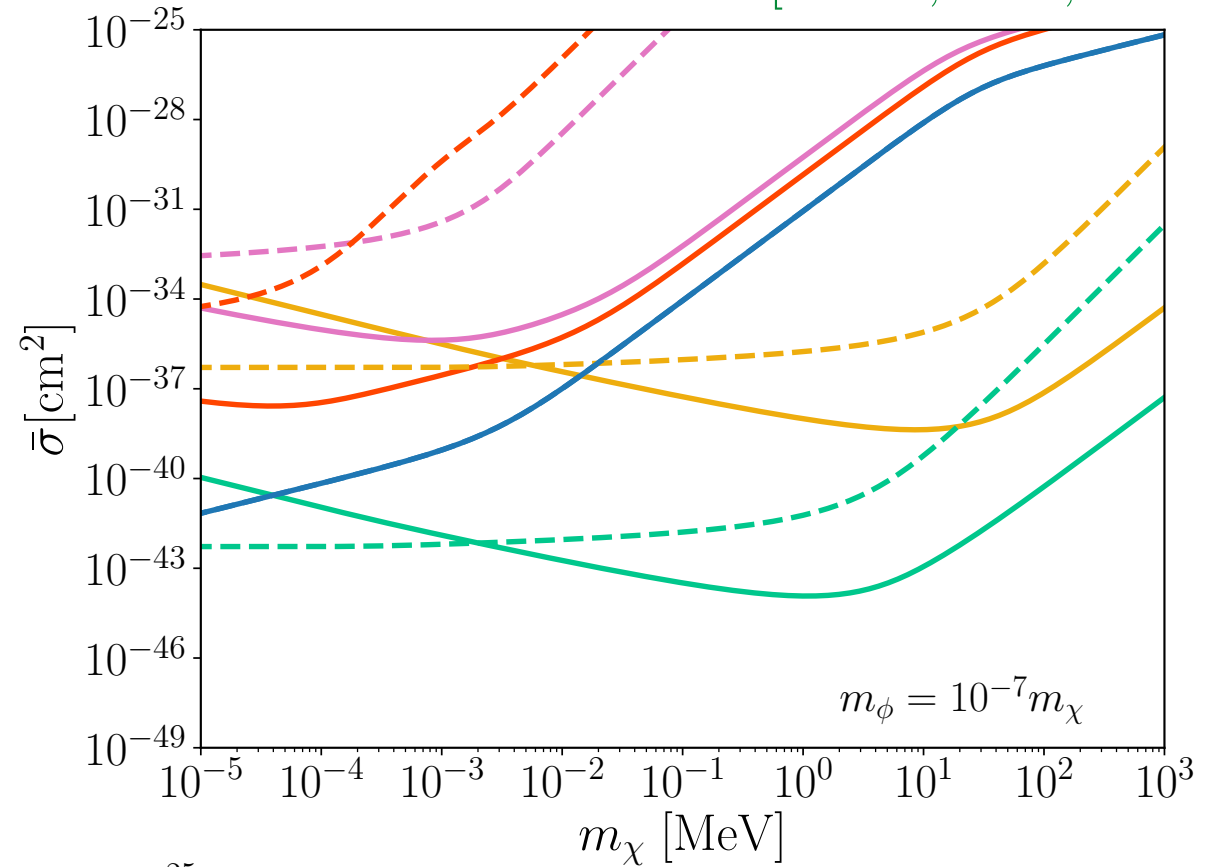
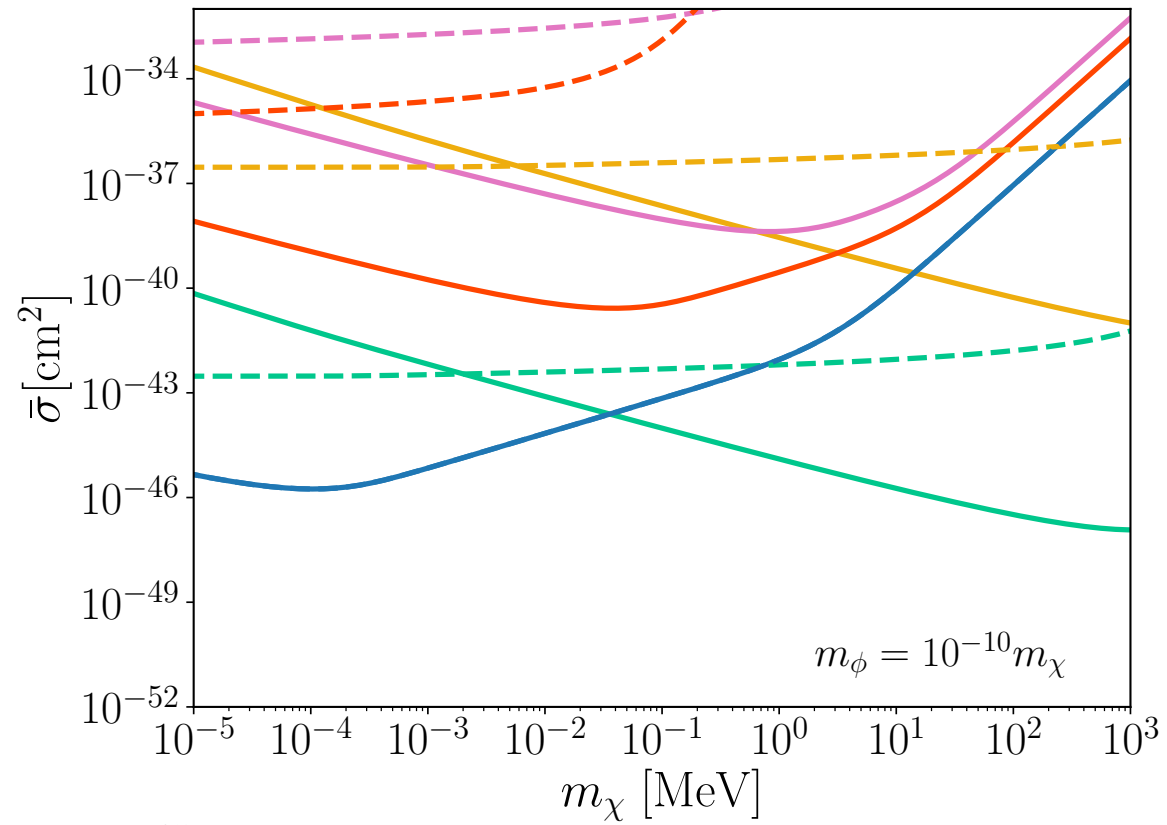
10-m atomic fountain

$$r_{\text{cloud}} \sim 0.2\text{mm}, N \sim 10^8$$
$$\Delta x = 0.1\text{m}, t_{\text{exp}} = 2\text{s}$$



AIs: Results

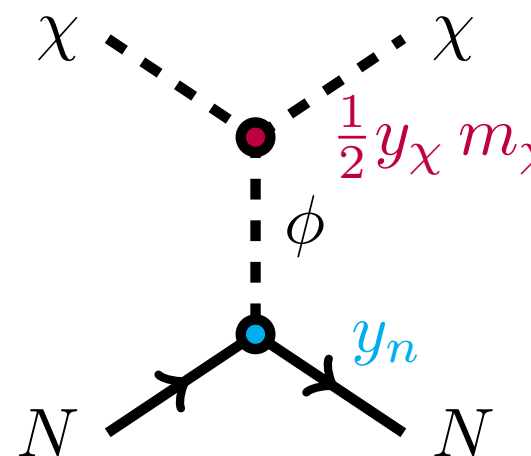
[Y. Du, CM, et al. 2022]



AIs: Constraints

[Knapen, Lin, Zurek, 2017]

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$



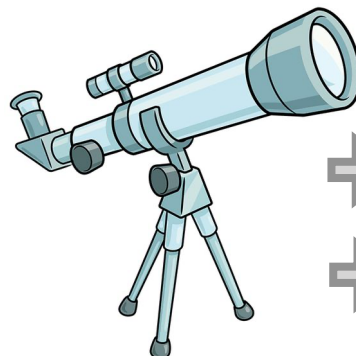
$$\bar{\sigma} = \frac{y_\chi^2 y_n^2}{4\pi} \frac{\mu^2}{(m_\chi^2 v_0^2 + m_\phi^2)^2}$$

Terrestrial



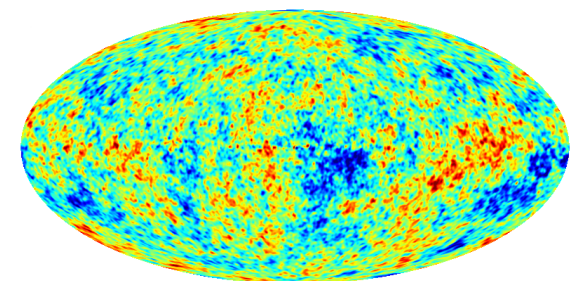
⇒ Collider
⇒ 5th force

Astrophysical



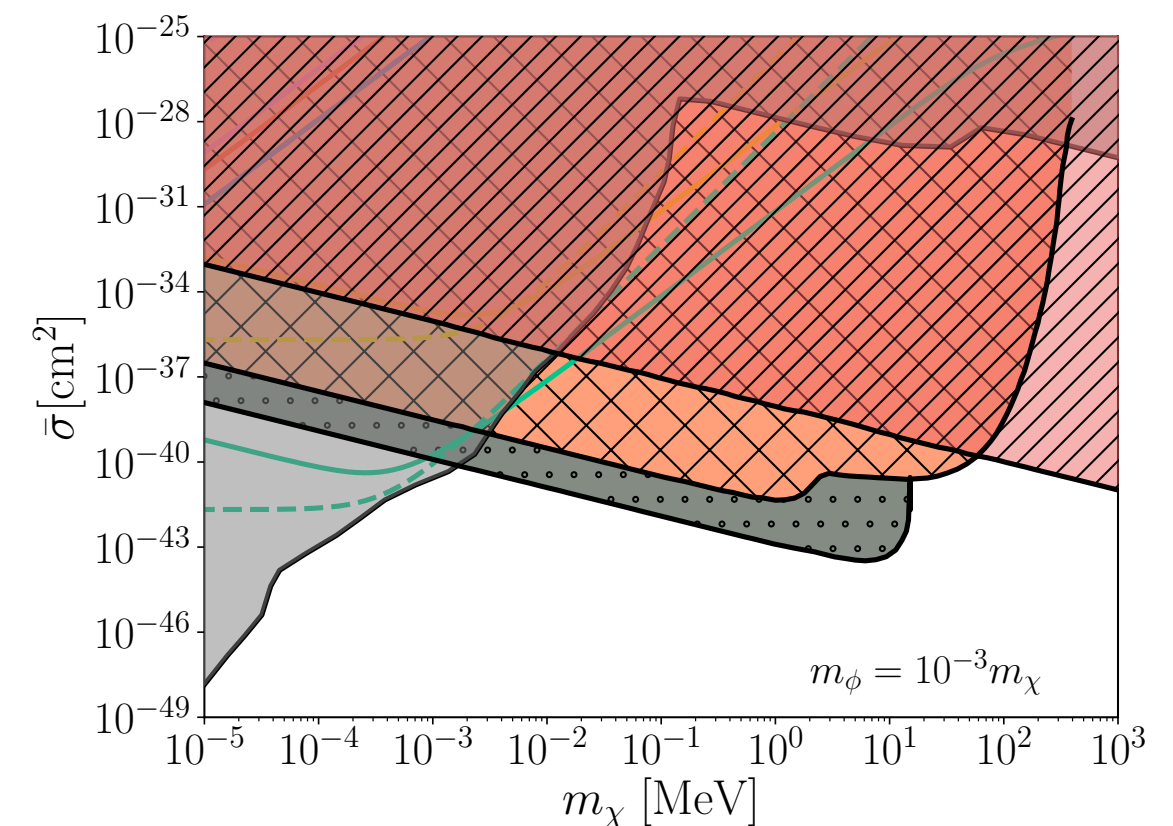
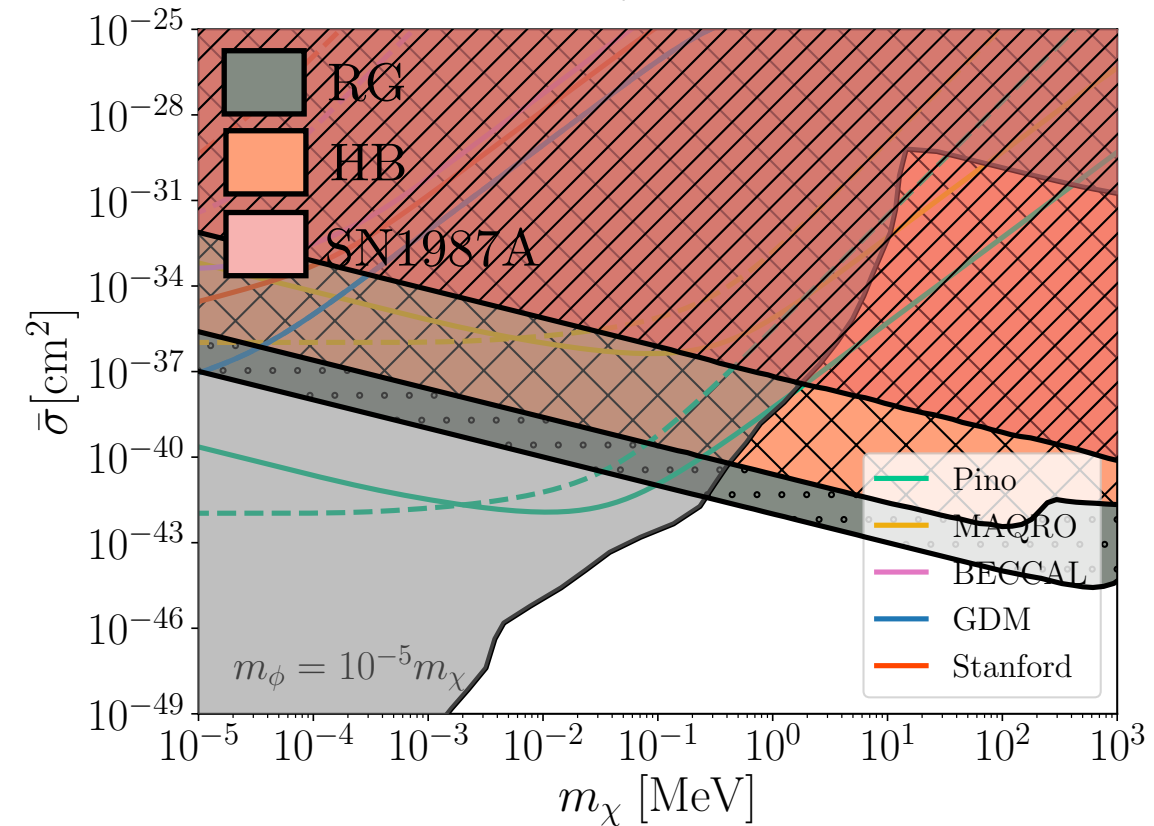
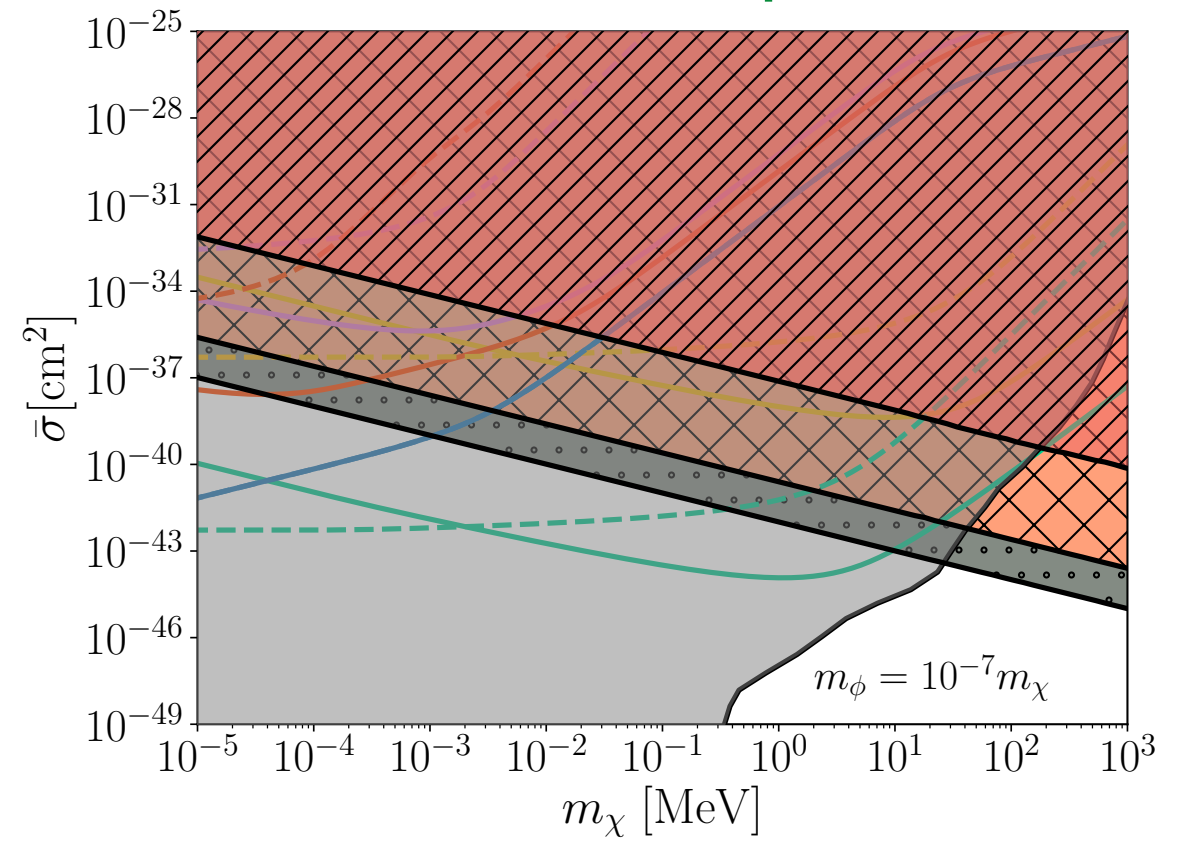
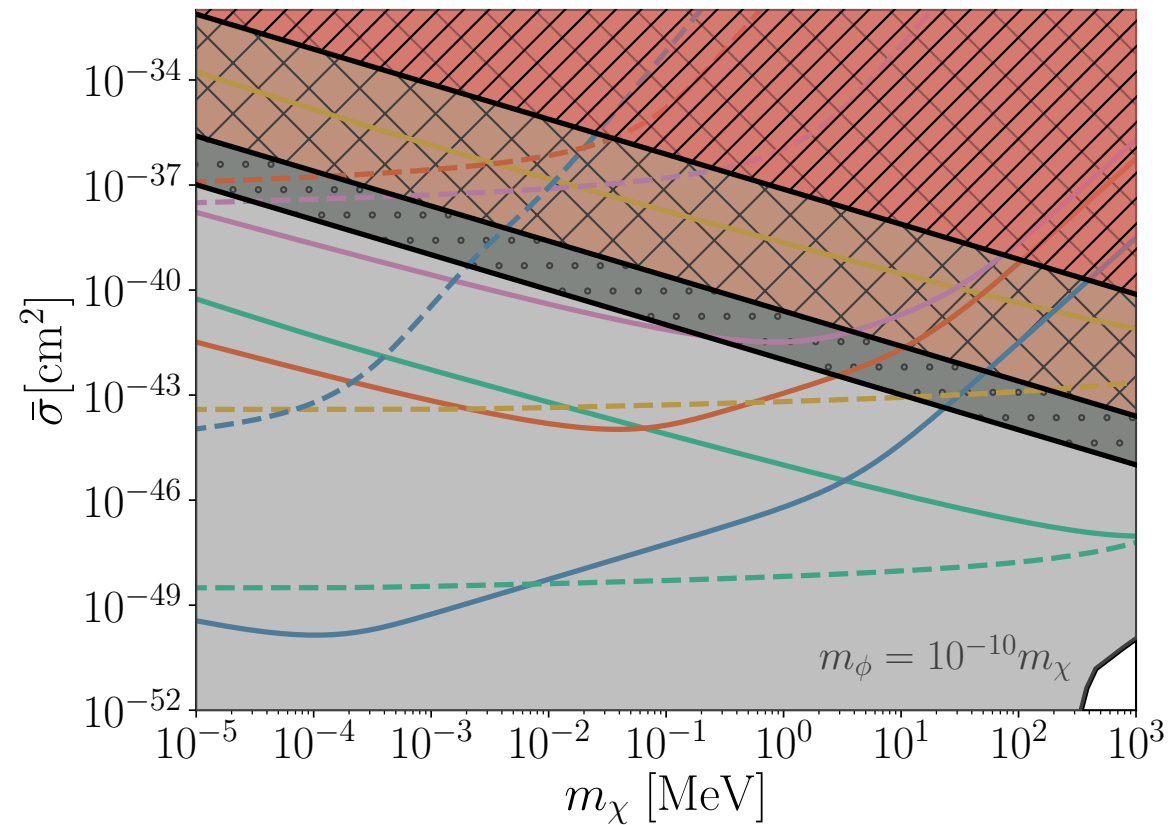
⇒ Stellar emission
⇒ DMSI

Cosmological



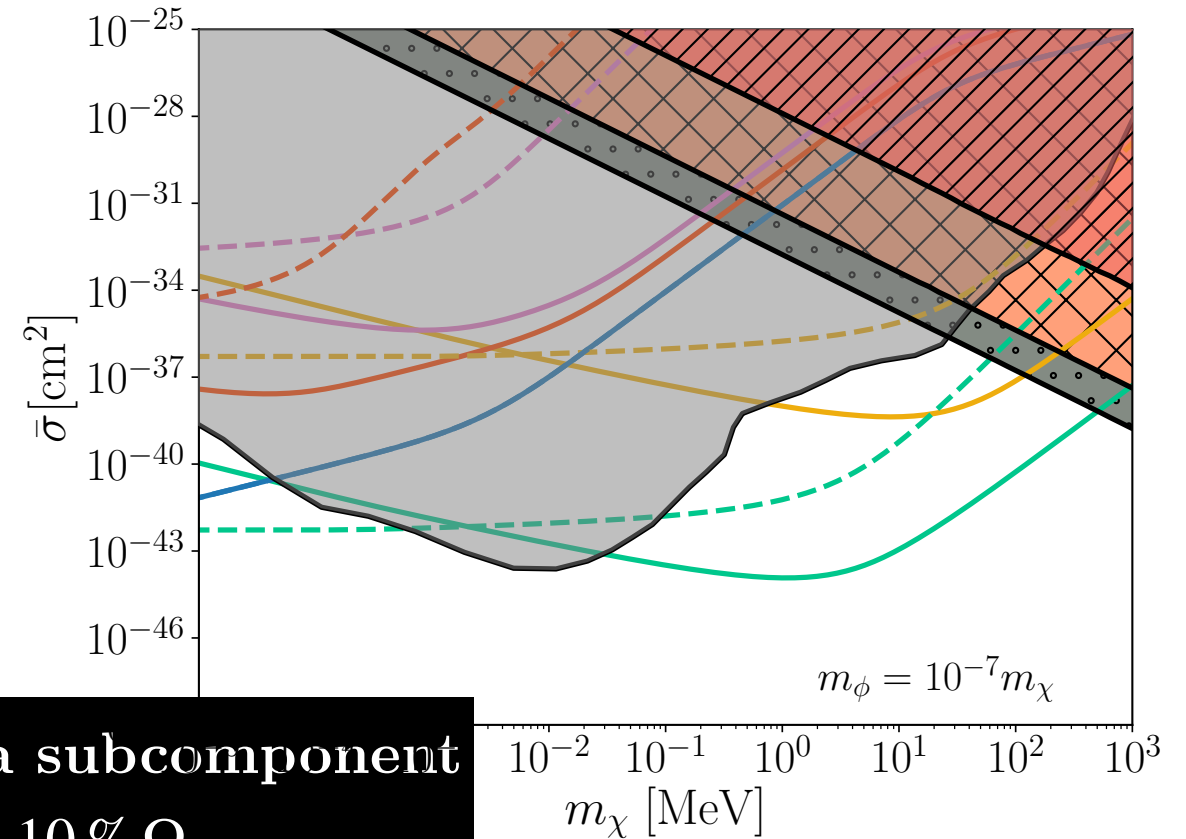
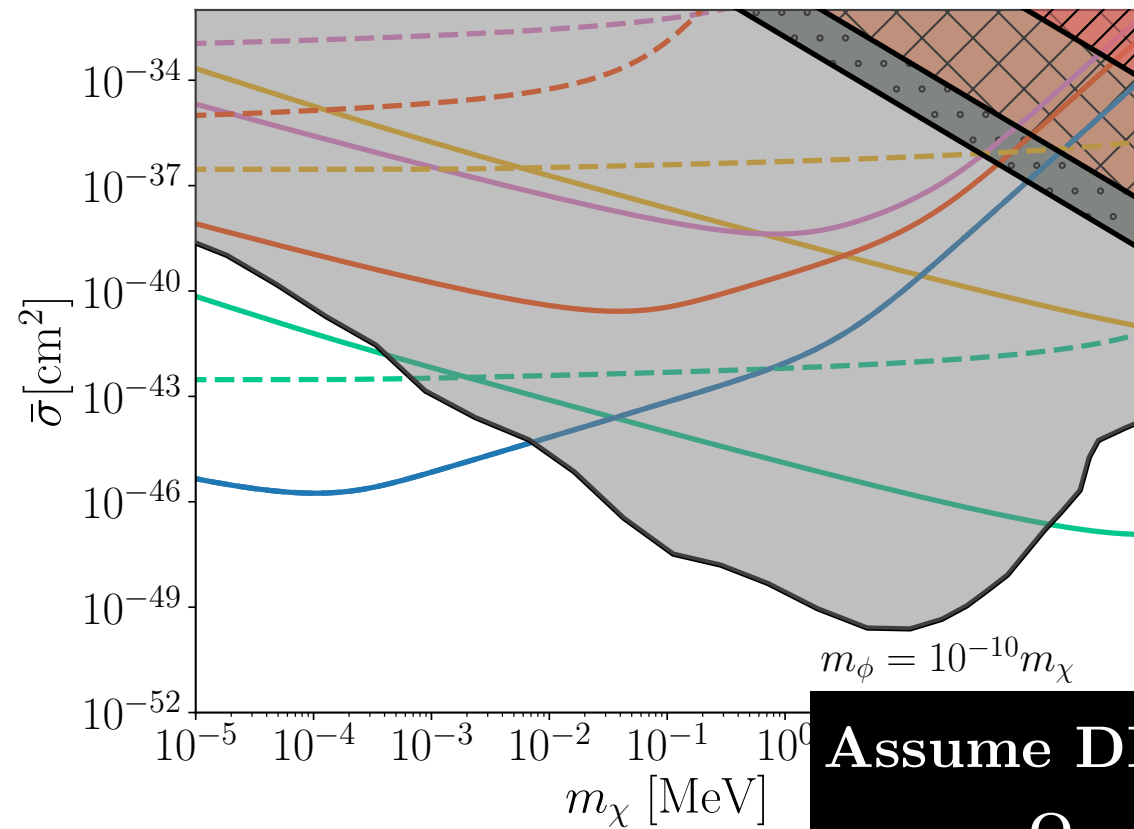
AIs: Constraints

[Y. Du, CM, et al. 2022]

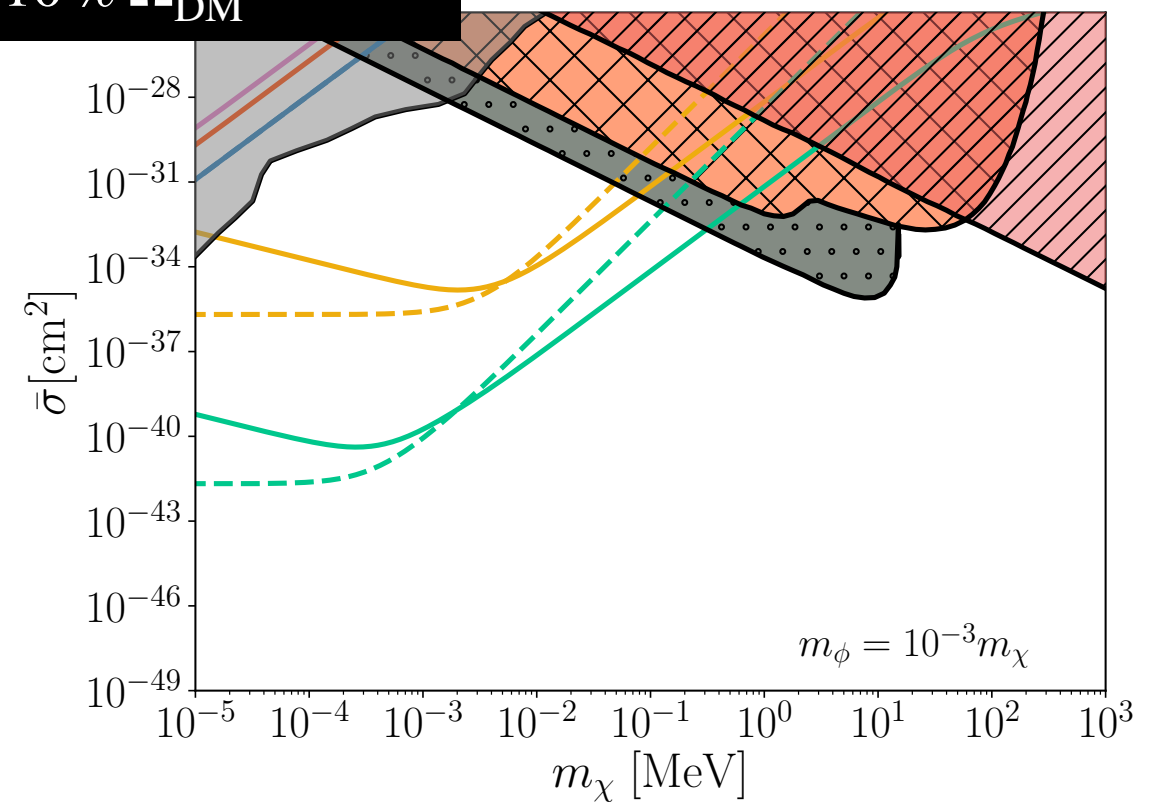
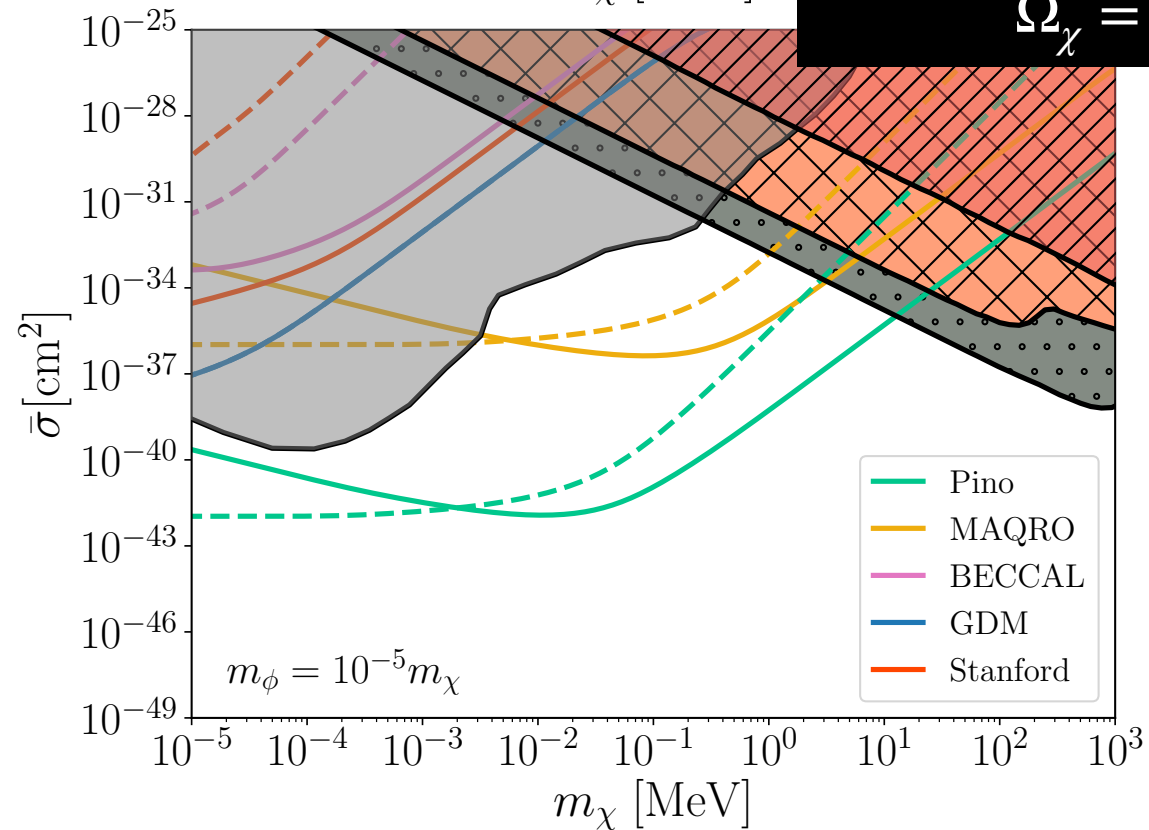


AIs: Constraints

[Y. Du, CM, et al. 2022]



Assume DM is a subcomponent
 $\Omega_\chi = 5\% - 10\% \Omega_{\text{DM}}$

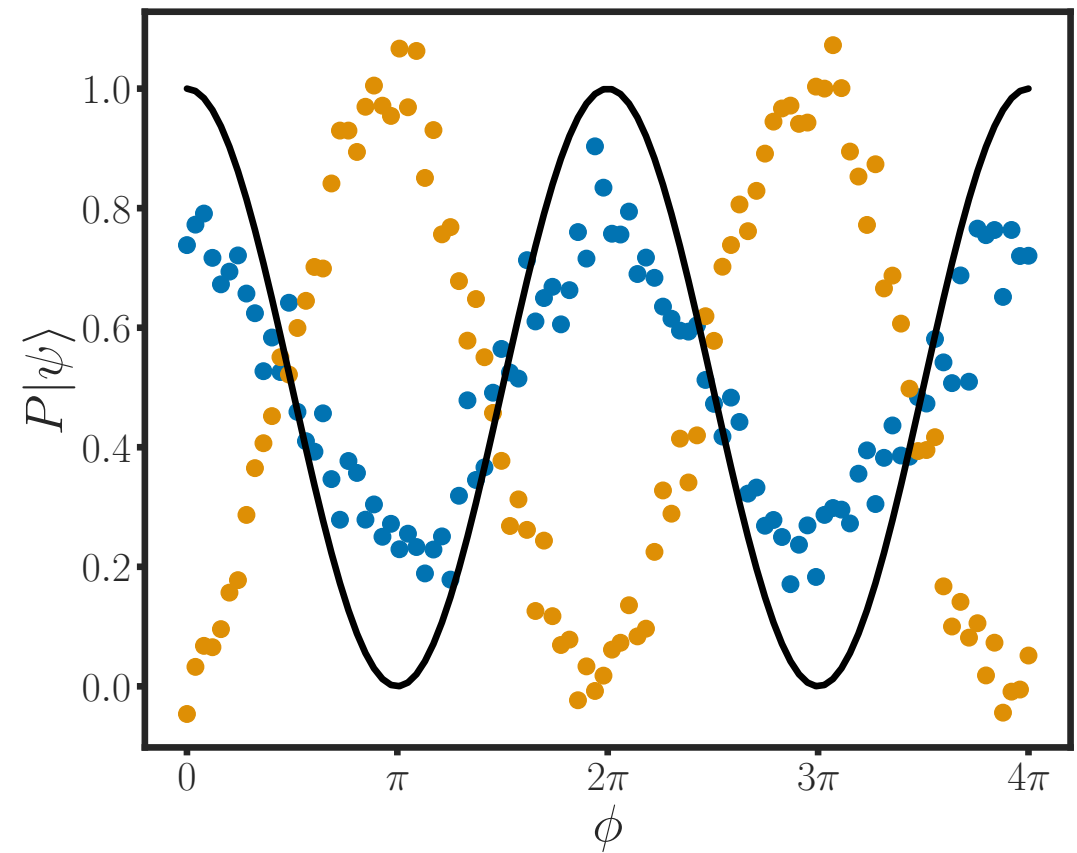


AIs: Measurement

- No decoherence or phase effects
- Decoherence Effect
- Phase Effect

Visibility

$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$

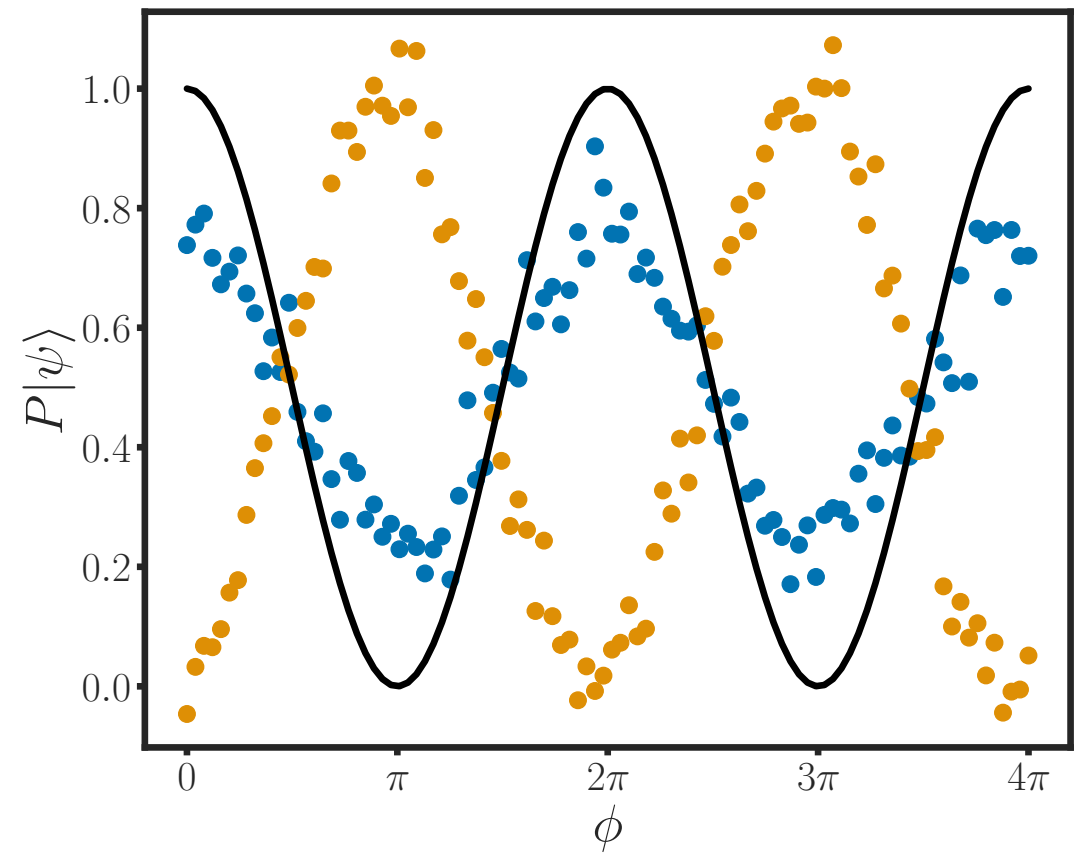


AIs: Measurement

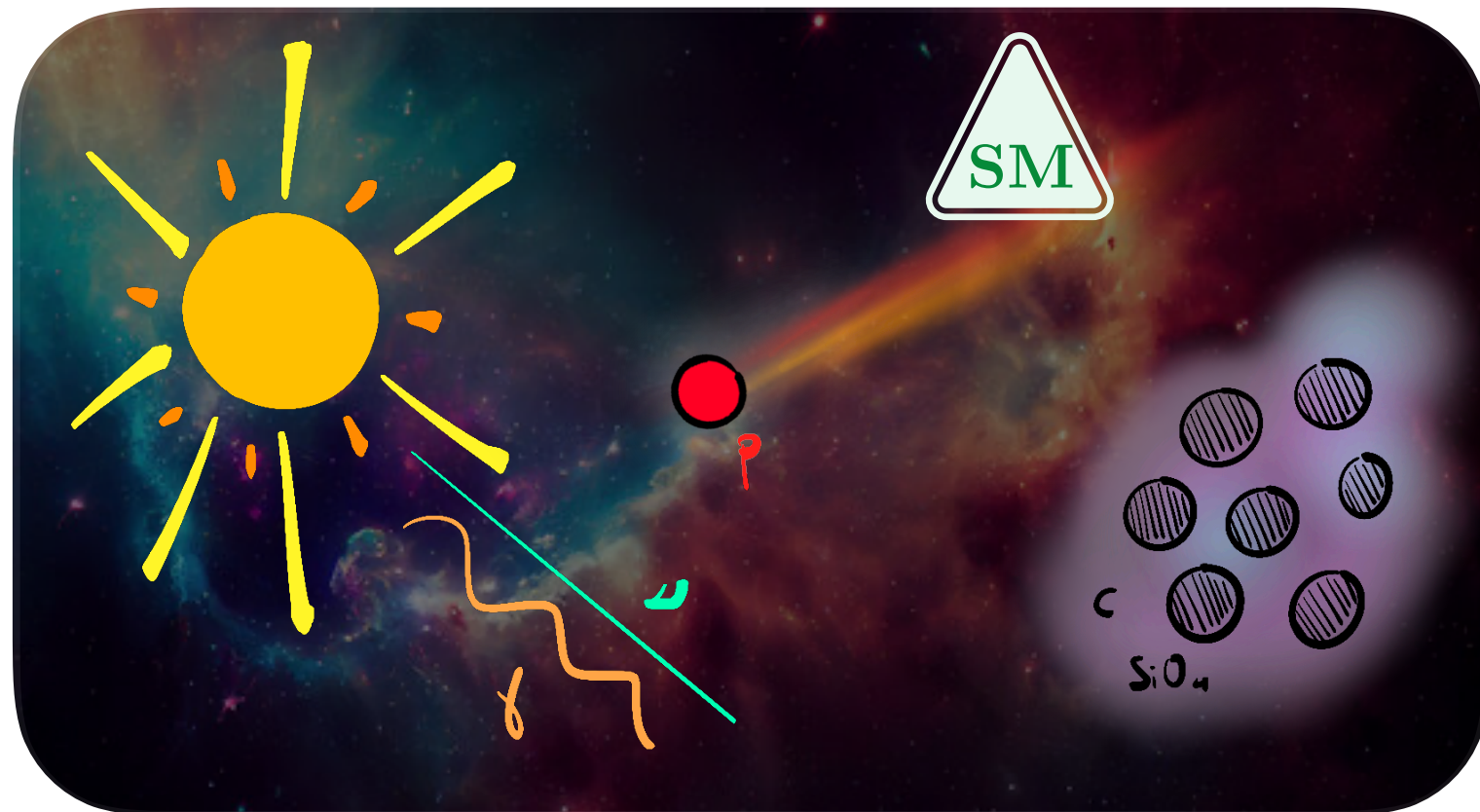
- No decoherence or phase effects
- Decoherence Effect
- Phase Effect

Visibility

$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



[Y. Du, CM, et al. 2022]

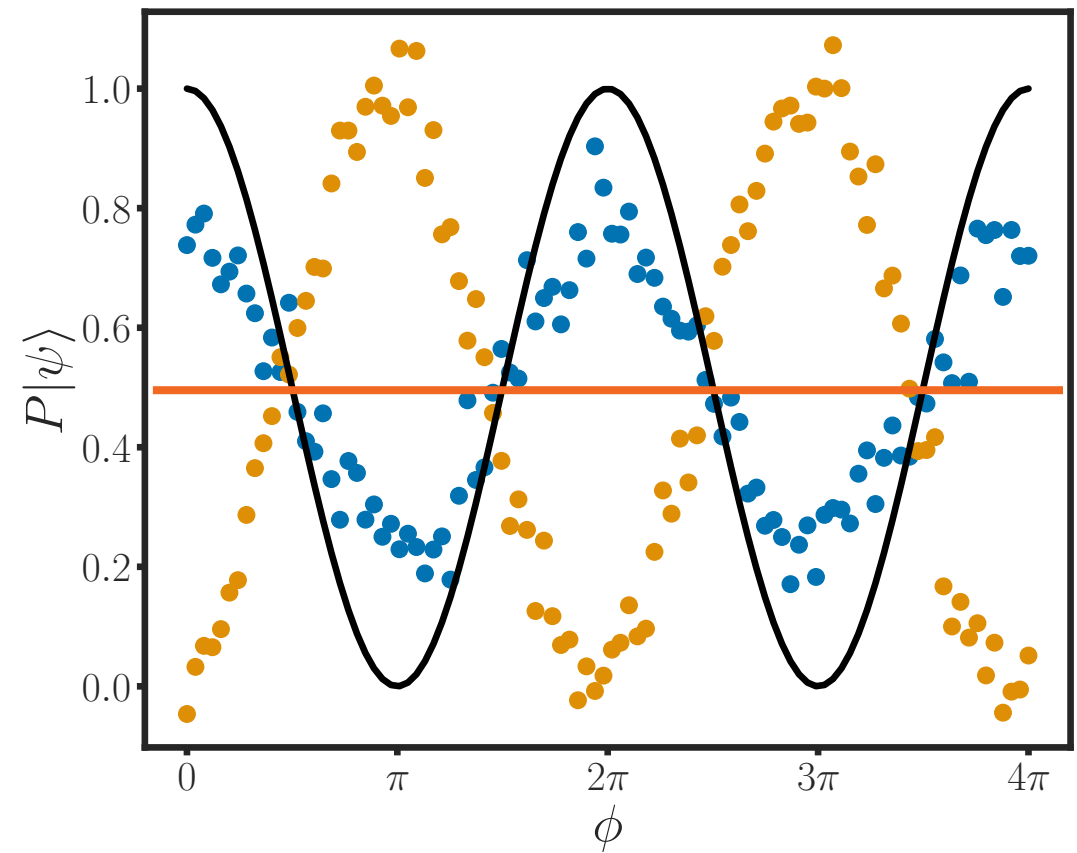


AIs: Measurement

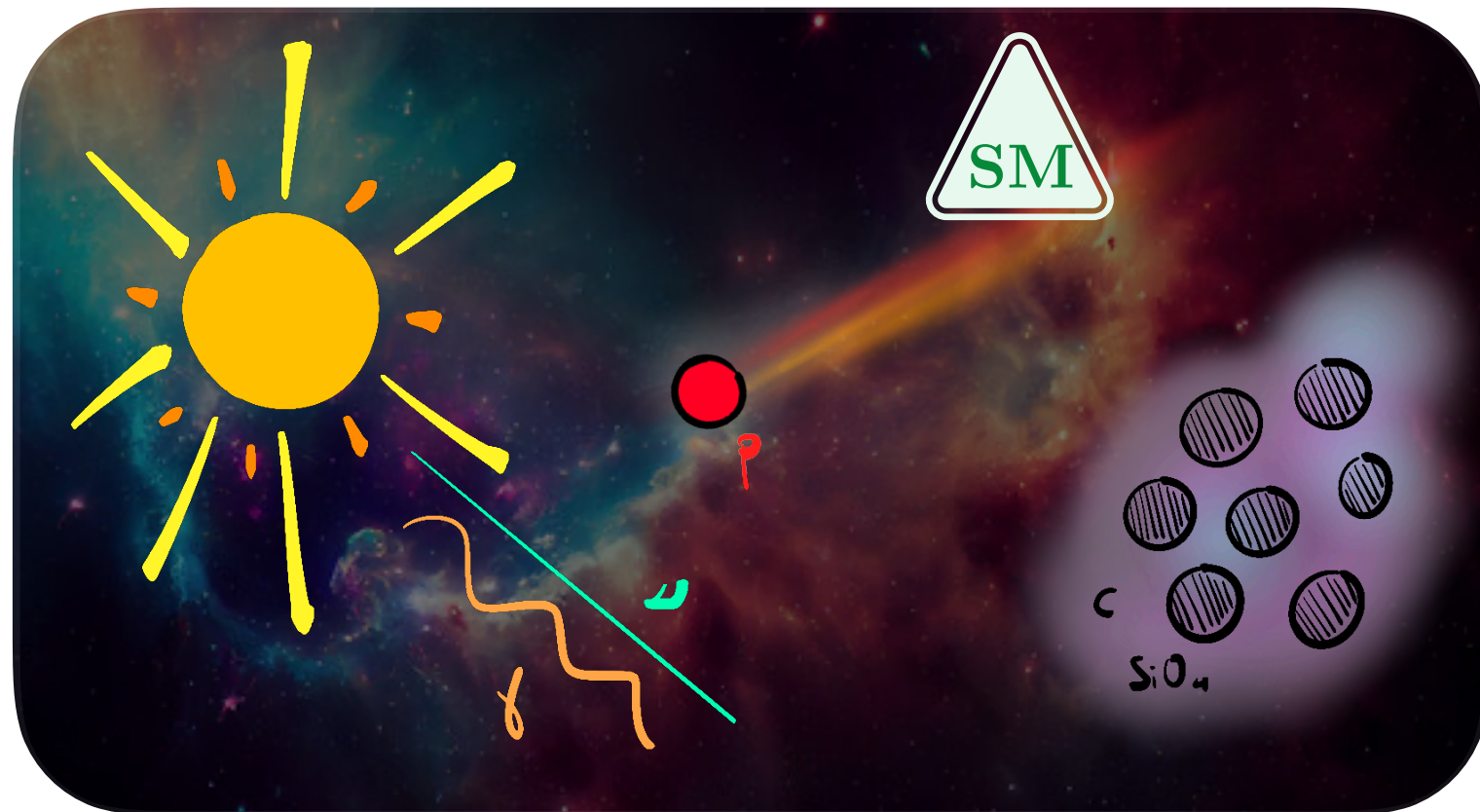
- No decoherence or phase effects
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- Phase Effect

Visibility

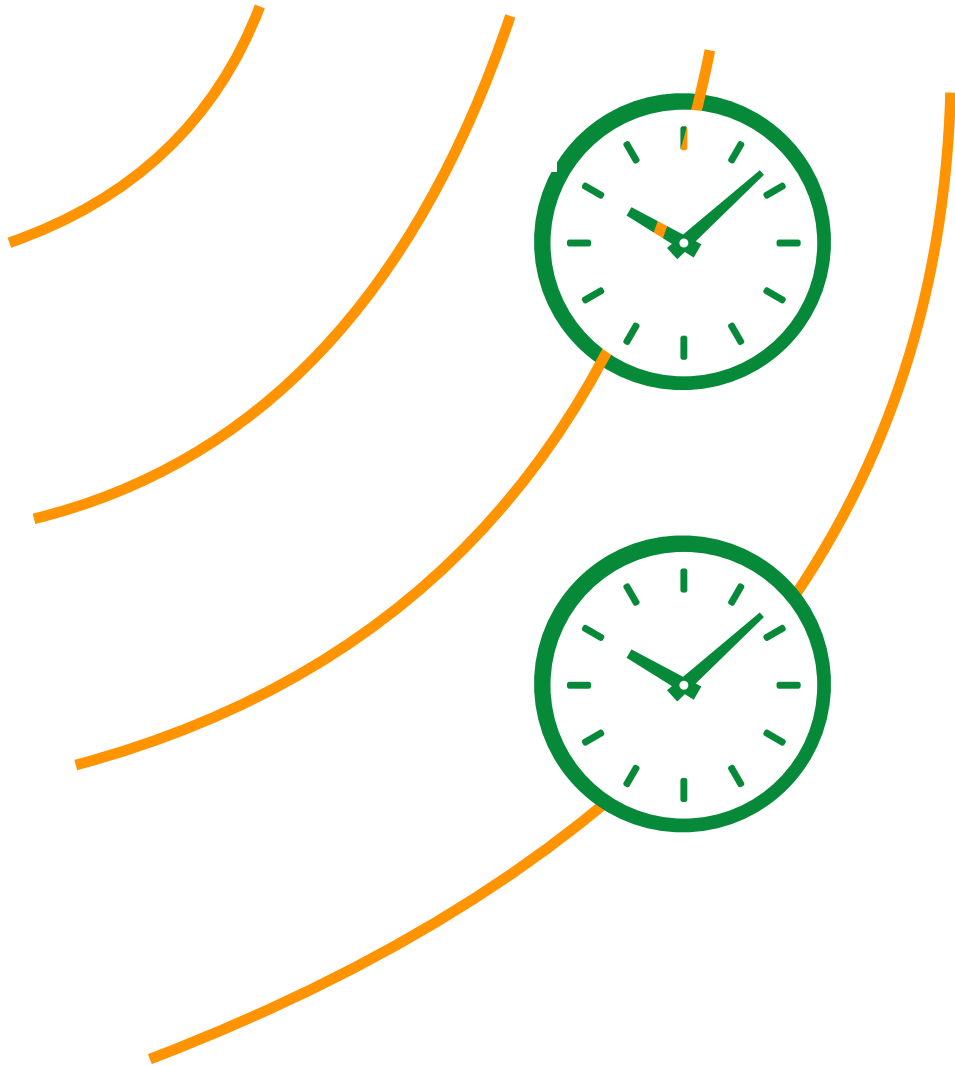
$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$



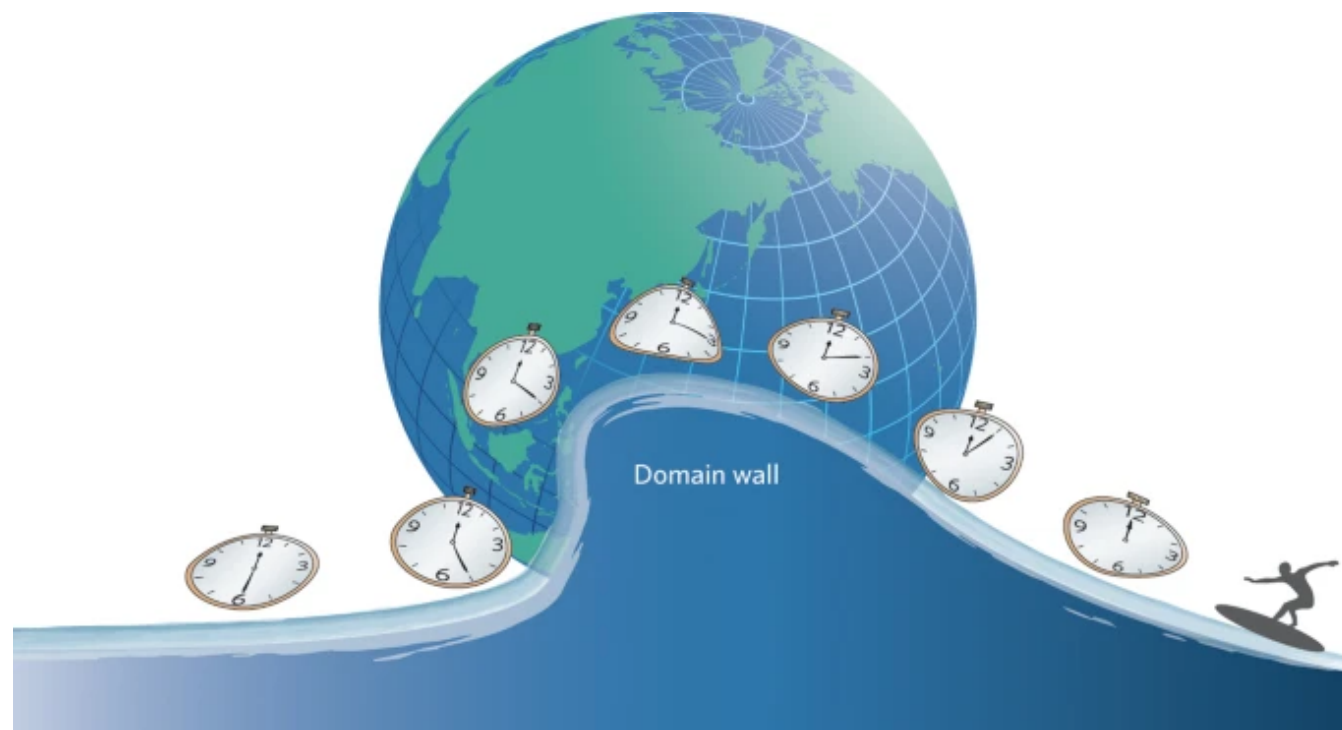
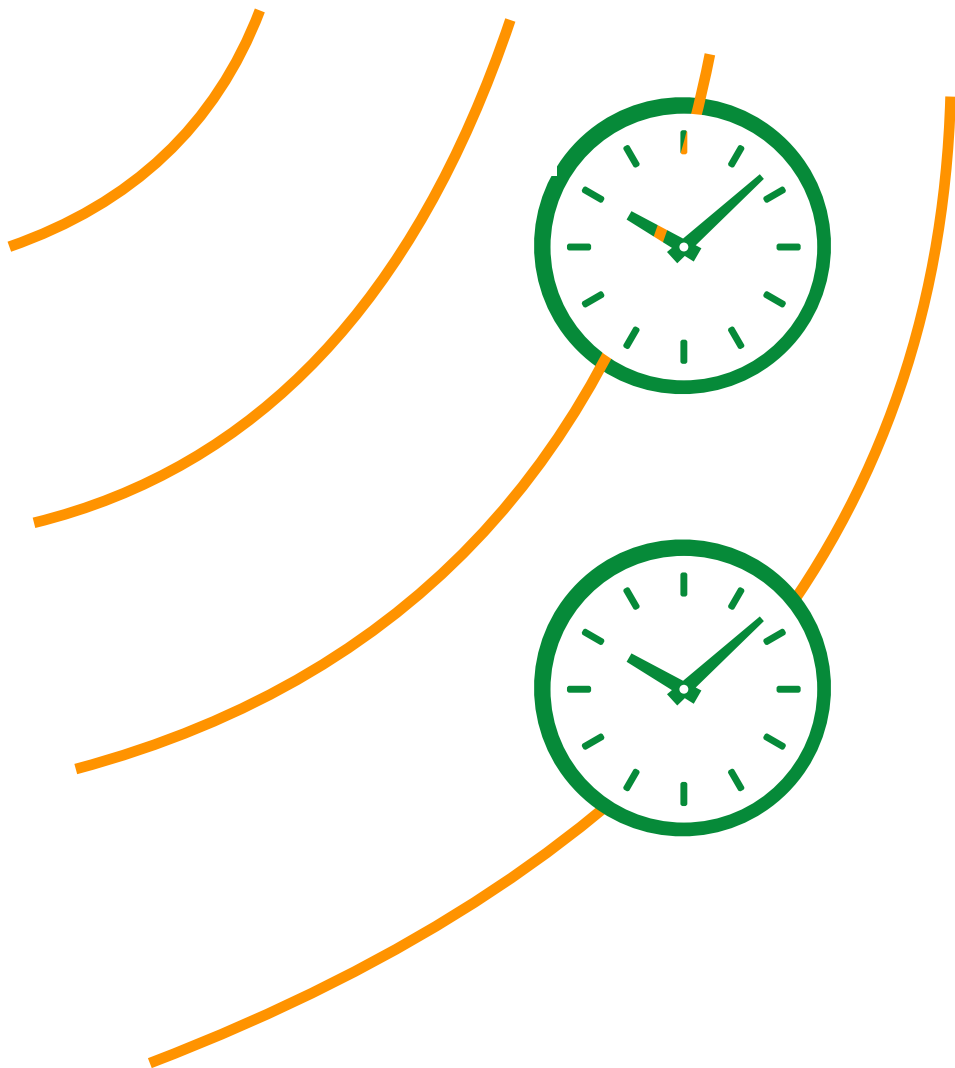
[Y. Du, CM, et al. 2022]



Atomic Clocks

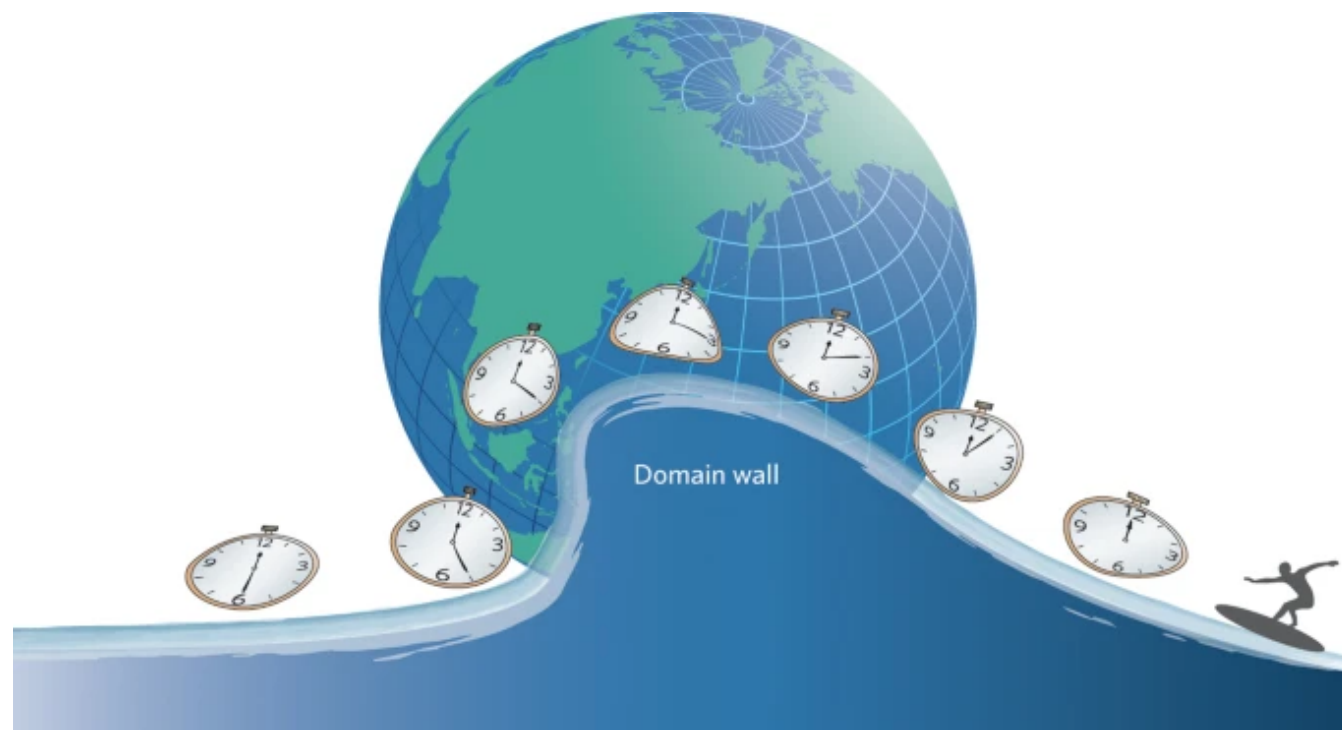
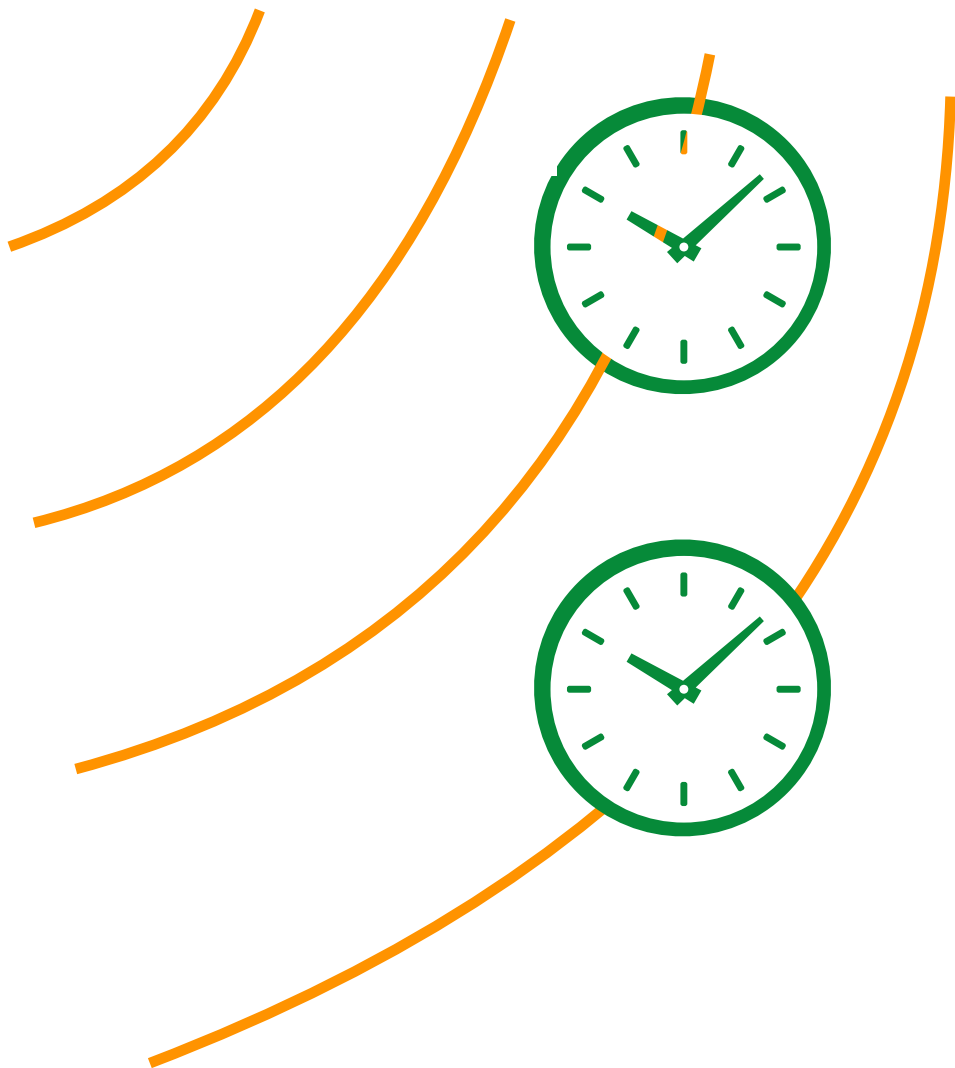


Atomic Clocks



[Adhikari, Hamilton, et. al, 2014]

Atomic Clocks

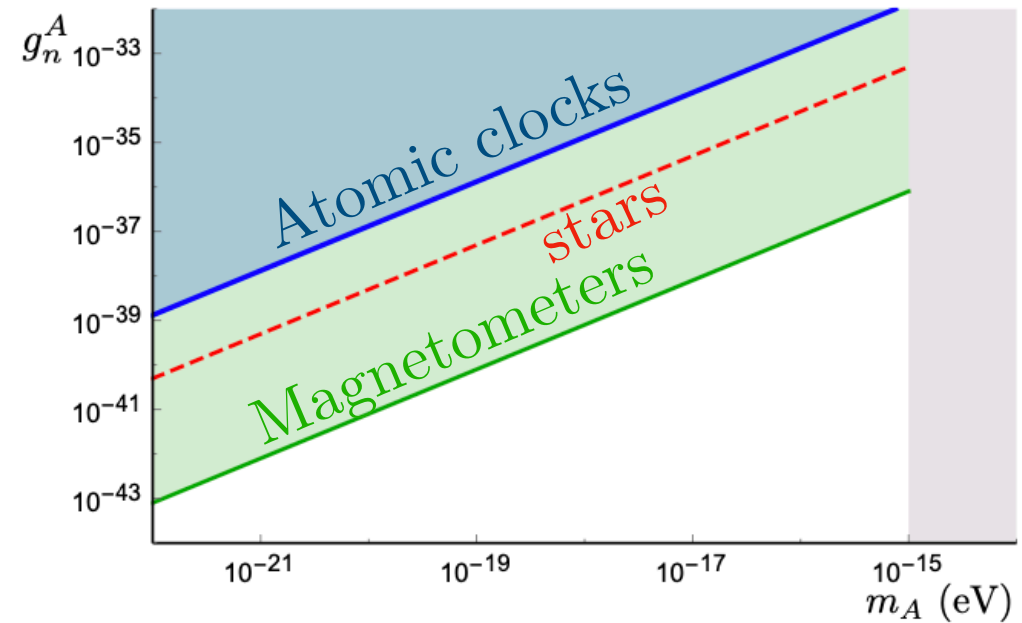
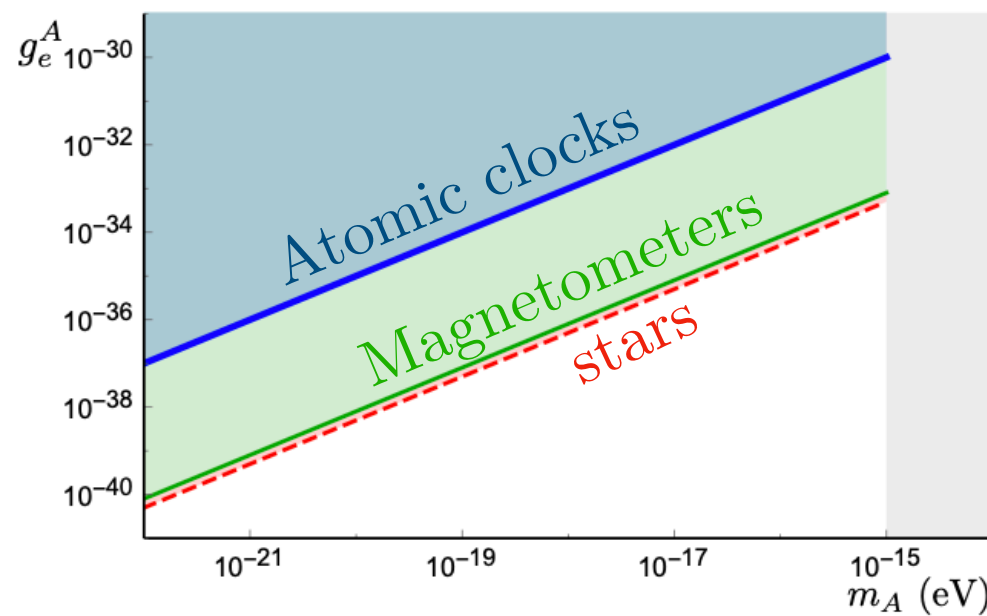


[Adhikari, Hamilton, et. al, 2014]

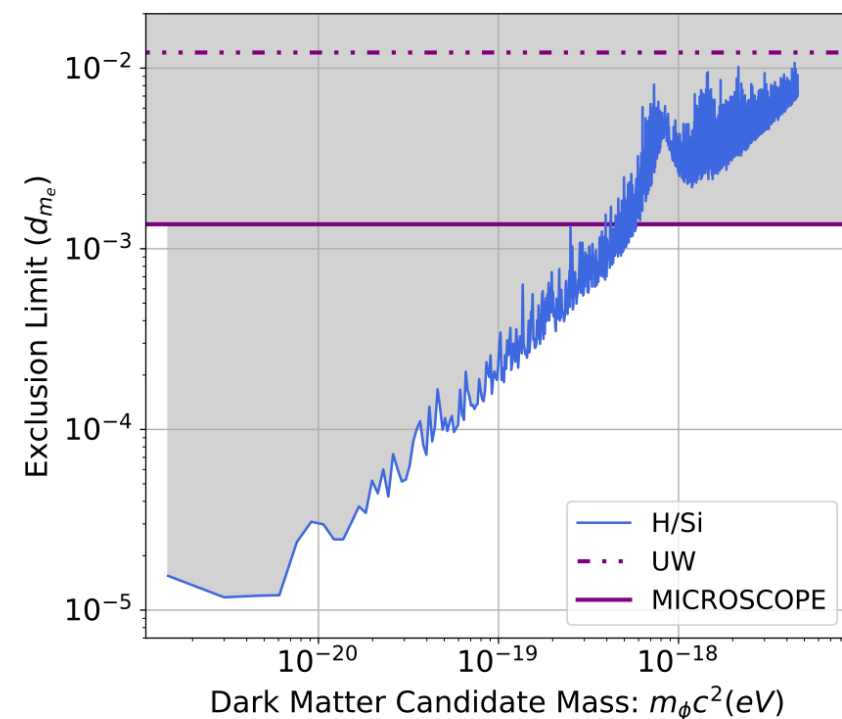
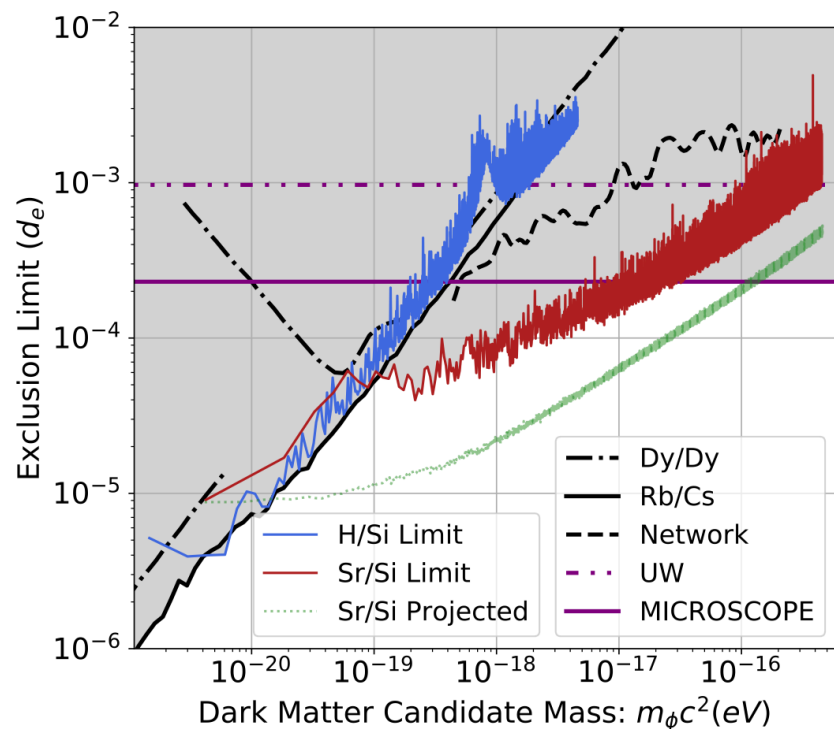
Topological DM	[Derevianko, Pospelov, 2014],[Derevianko, 2016 [Wcislo et al. 2018]
Wave DM	[Arvanitaki et al. 2015]
5th forces	[Brzeminski, Chacko, et al. 2022]
GWs	[Loeb, Maoz, 2015]
Particle DM	[Alonso, Blas, Wolf, 2018]

Atomic Clocks

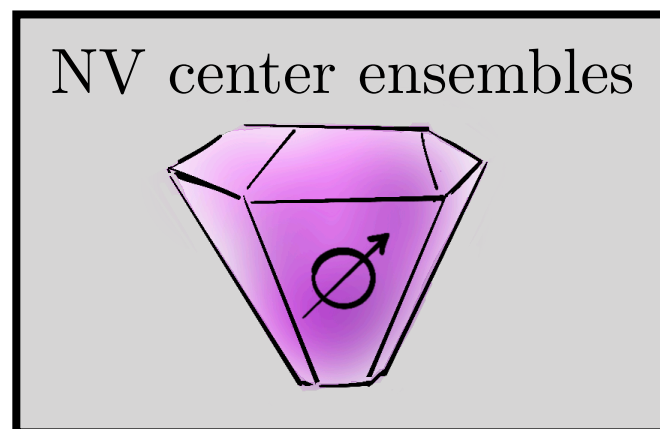
[Alonso, Blas, Wolf, 2019]



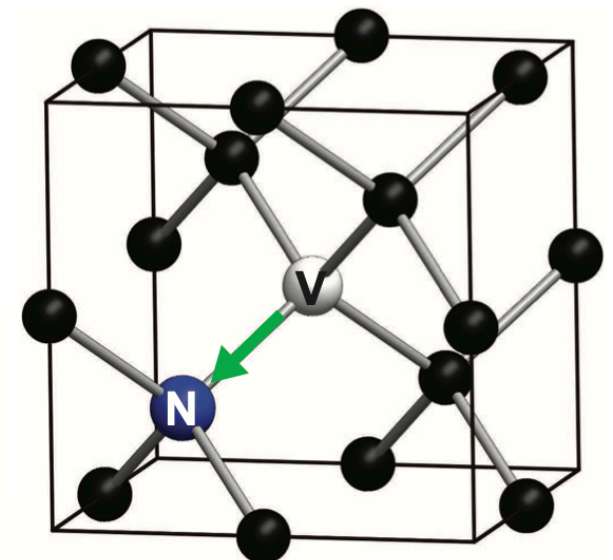
$$\mathcal{L}_\phi = \sqrt{4\pi G_N} \phi \left(\frac{d_e}{4} F_{\mu\nu} F^{\mu\nu} - d_{m_e} m_e \bar{\Psi}_e \Psi_e \right) \quad [\text{Kennedy, Oelker, et al. 2020}]$$



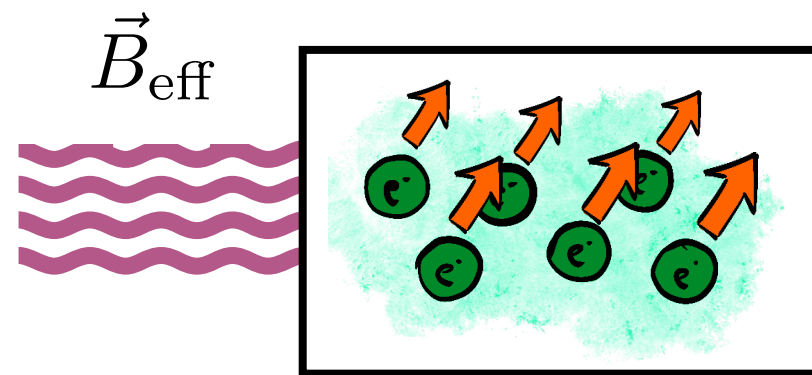
NV center ensembles



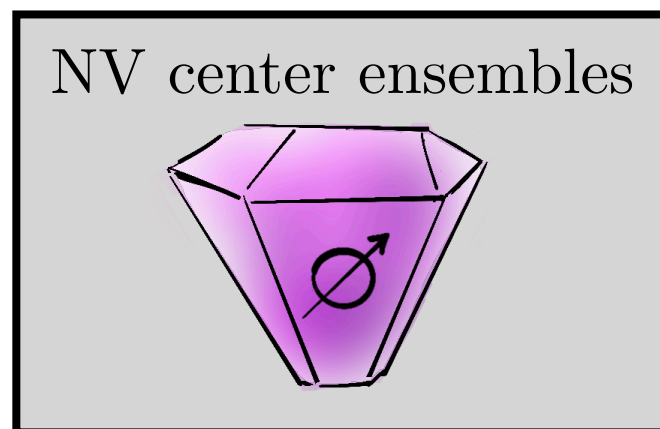
[Pham, 2013]
[Degen, Reinhard, et al, 2017]
[Schloss, et al, 2018]
[Barry, Schloss, et al, 2019]
[Chigusa, Hazumi, et al, 2023]



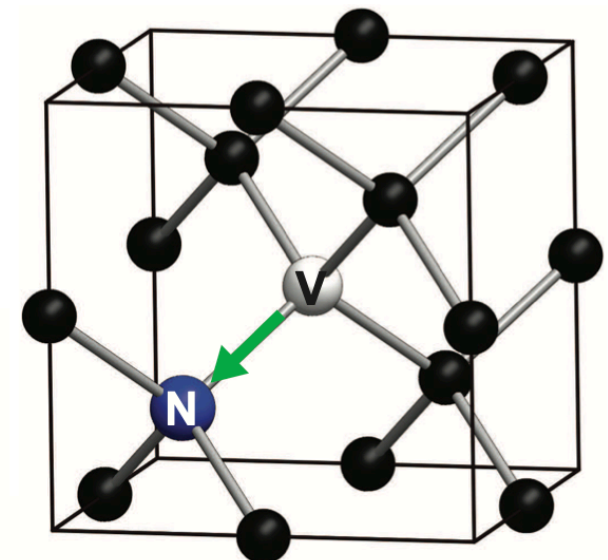
NV center ensembles



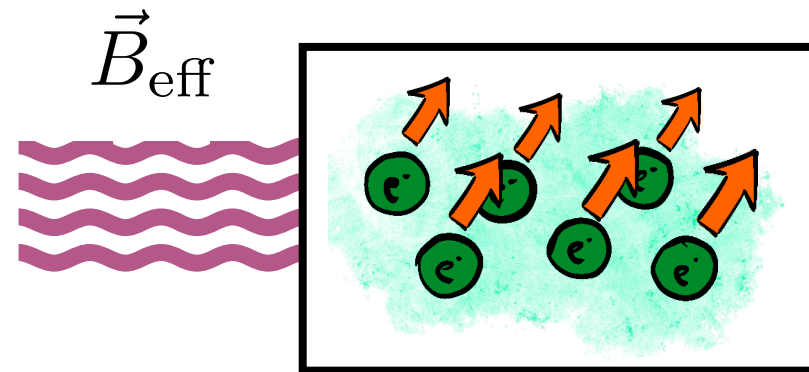
$$\mathcal{H} \supset -\vec{\mu} \cdot \vec{B}$$



[Pham, 2013]
[Degen, Reinhard, et al, 2017]
[Schloss, et al, 2018]
[Barry, Schloss, et al, 2019]
[Chigusa, Hazumi, et al, 2023]



NV center ensembles

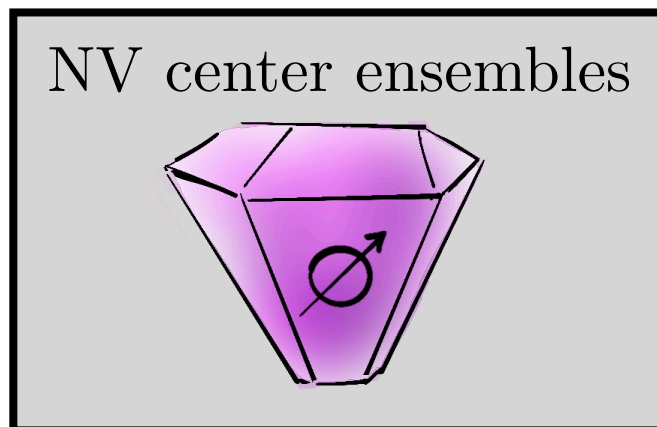
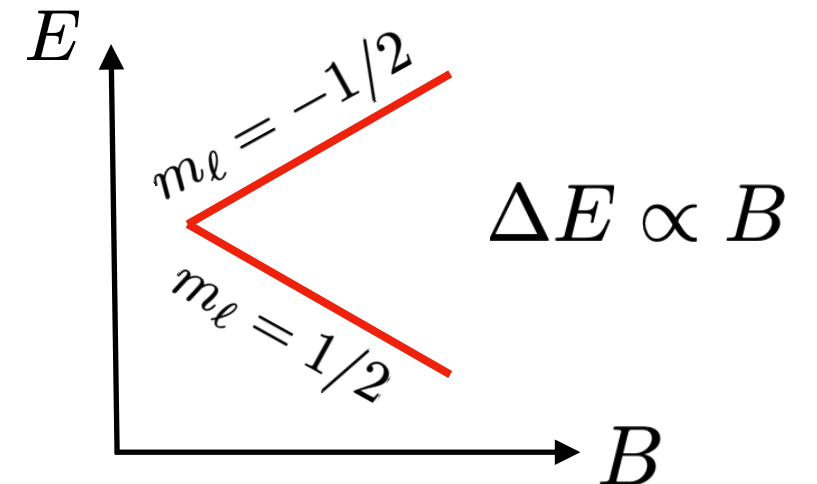


$$\mathcal{H} \supset -\vec{\mu} \cdot \vec{B}$$

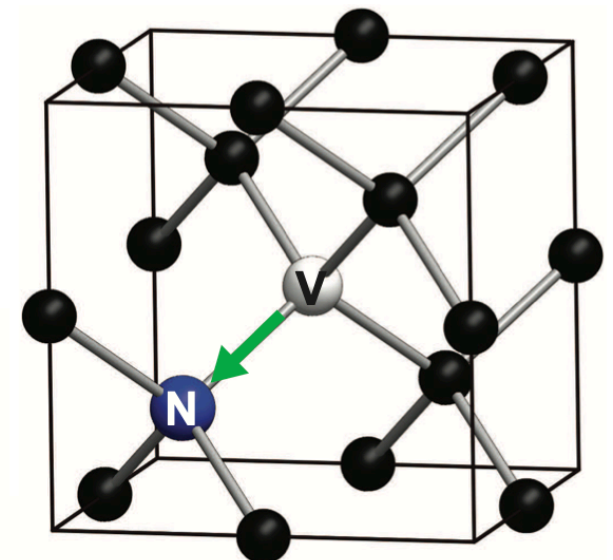
e.g.

$$g_{aee} \frac{\partial_\mu a}{2m_e} \bar{\Psi}_e \gamma_\mu \gamma_5 \Psi_e \Rightarrow \frac{g_{aee}}{m_e} \nabla a \cdot \vec{S}_e$$

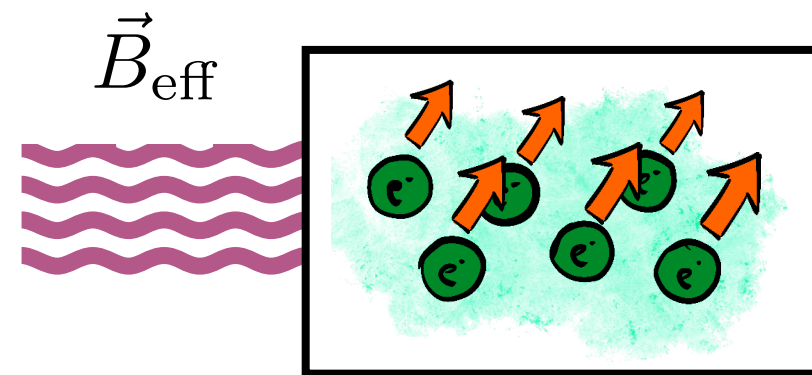
$$\frac{\epsilon}{2} F_{\mu\nu} F'^{\mu\nu} \Rightarrow \frac{\epsilon e}{m_e} (\nabla \times \vec{A}) \cdot \vec{S}_e$$



[Pham, 2013]
 [Degen, Reinhard, et al, 2017]
 [Schloss, et al, 2018]
 [Barry, Schloss, et al, 2019]
 [Chigusa, Hazumi, et al, 2023]

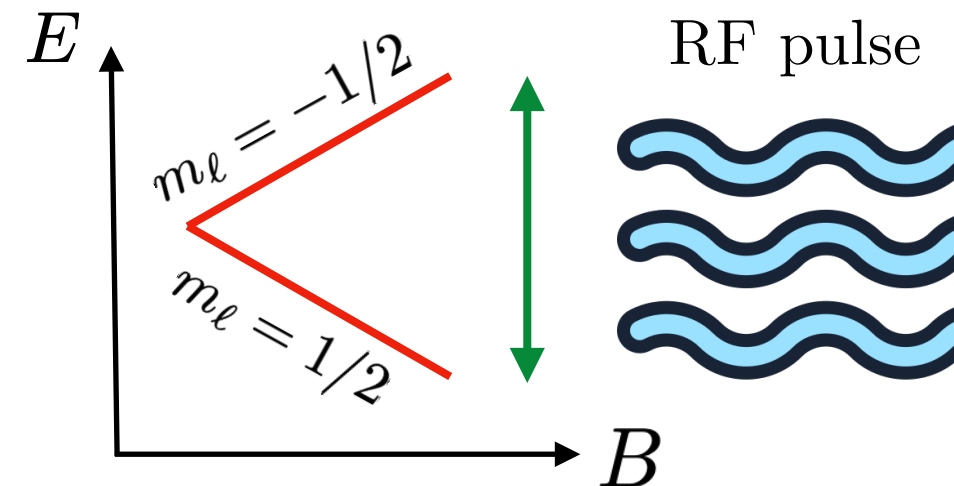
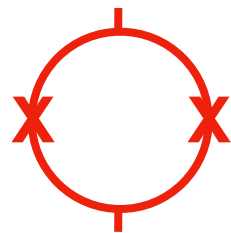


NV center ensembles

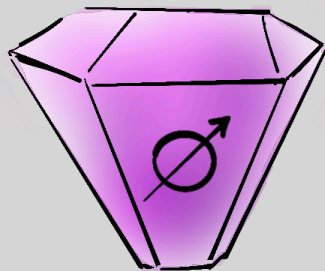


$$\mathcal{H} \supset -\vec{\mu} \cdot \vec{B}$$

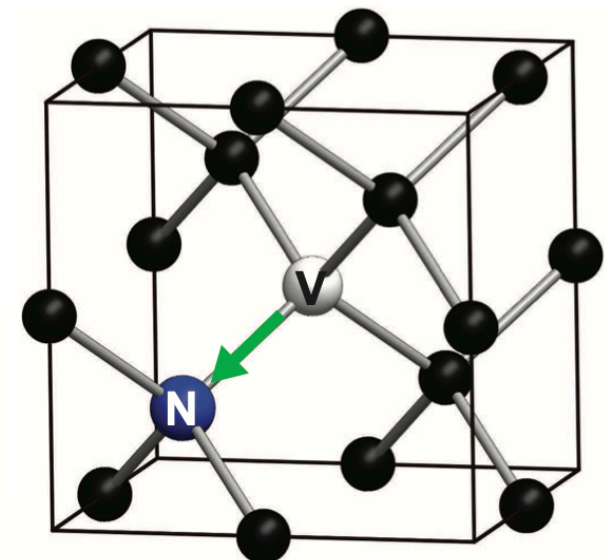
SQUID



NV center ensembles

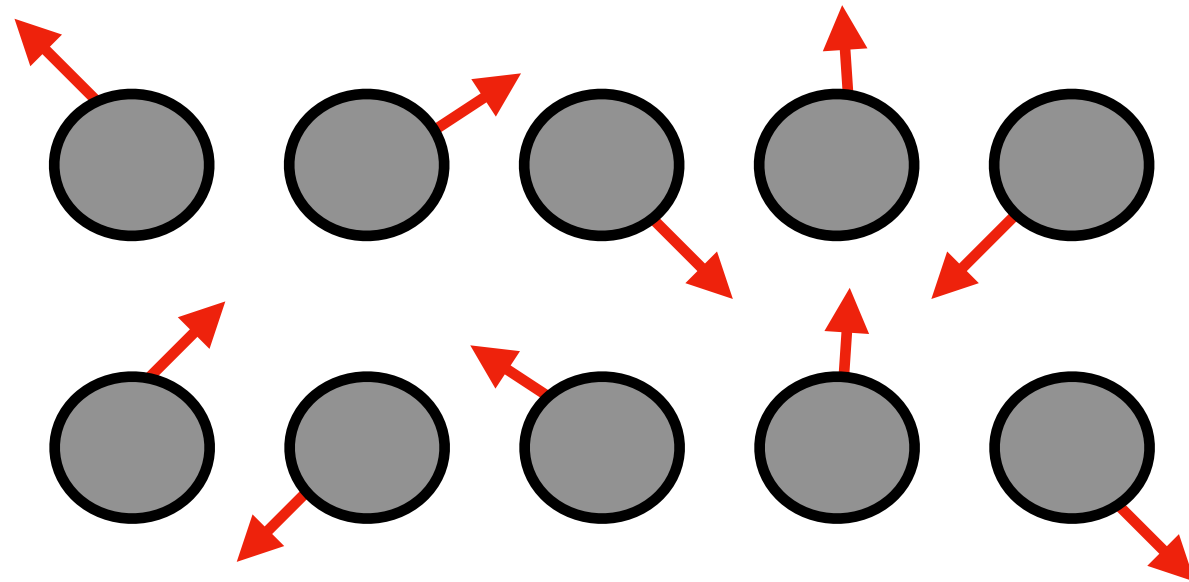


[Pham, 2013]
 [Degen, Reinhard, et al, 2017]
 [Schloss, et al, 2018]
 [Barry, Schloss, et al, 2019]
 [Chigusa, Hazumi, et al, 2023]



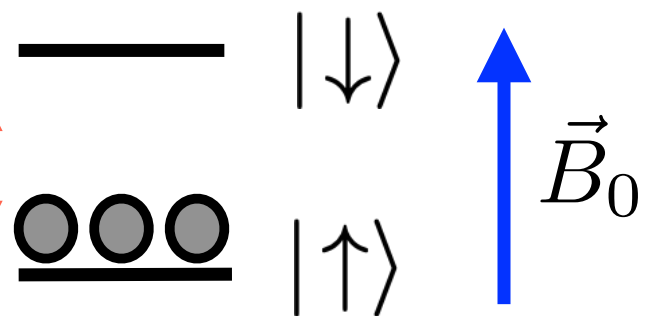
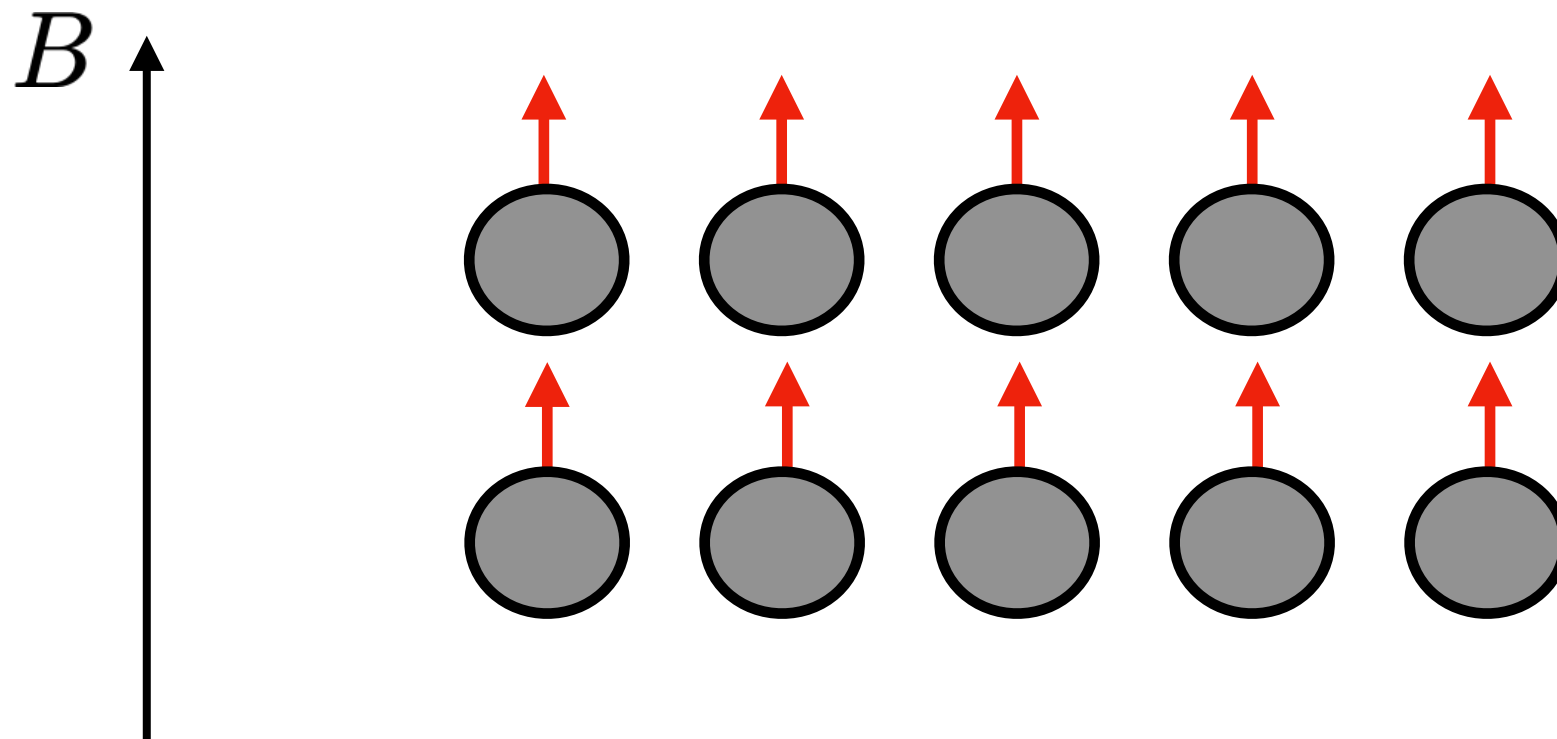
CASPER

[Budker, Graham, et al. 2014]
[Garcon, Blanchard, et al. 2019]



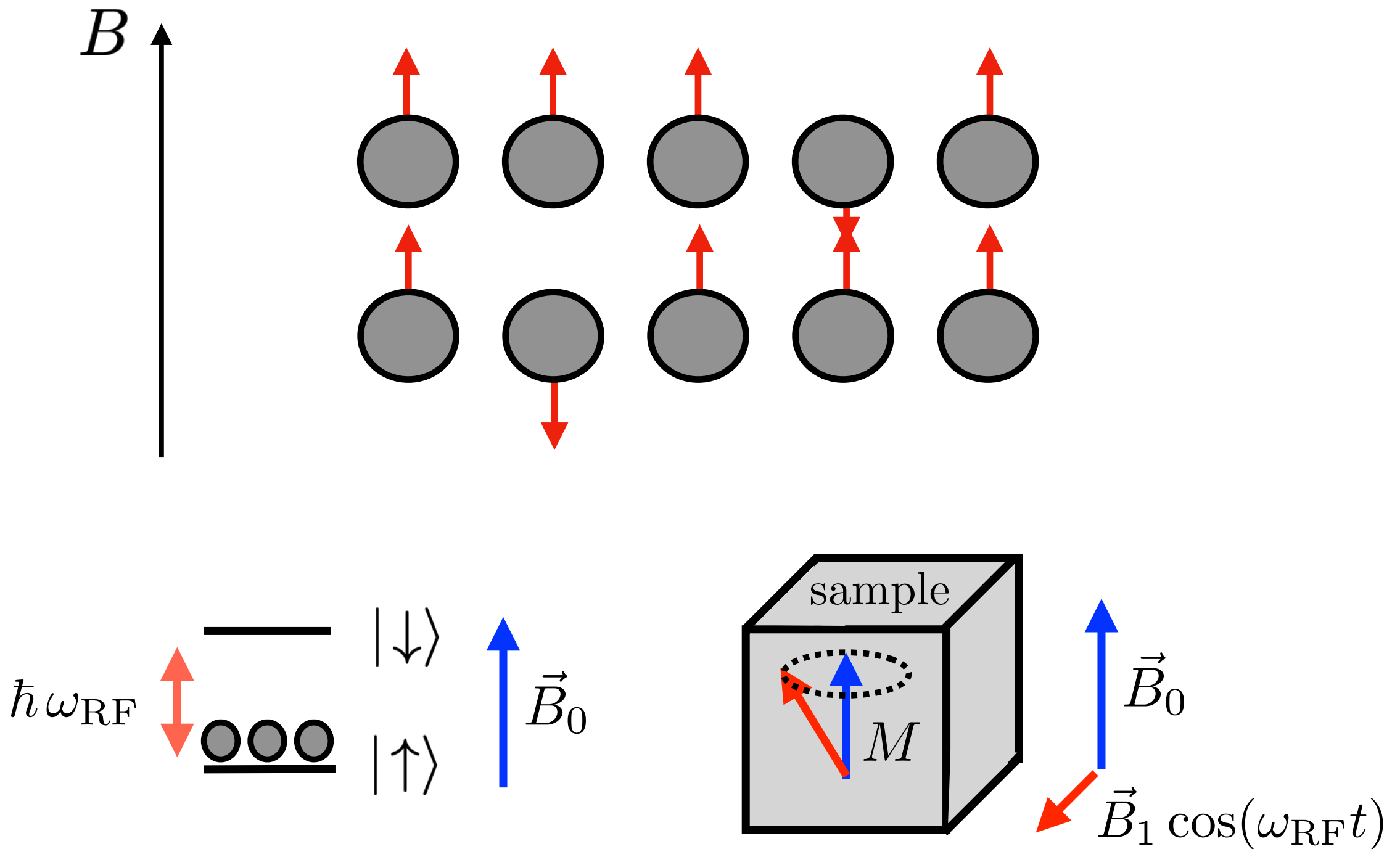
CASPER

[Budker, Graham, et al. 2014]
[Garcon, Blanchard, et al. 2019]



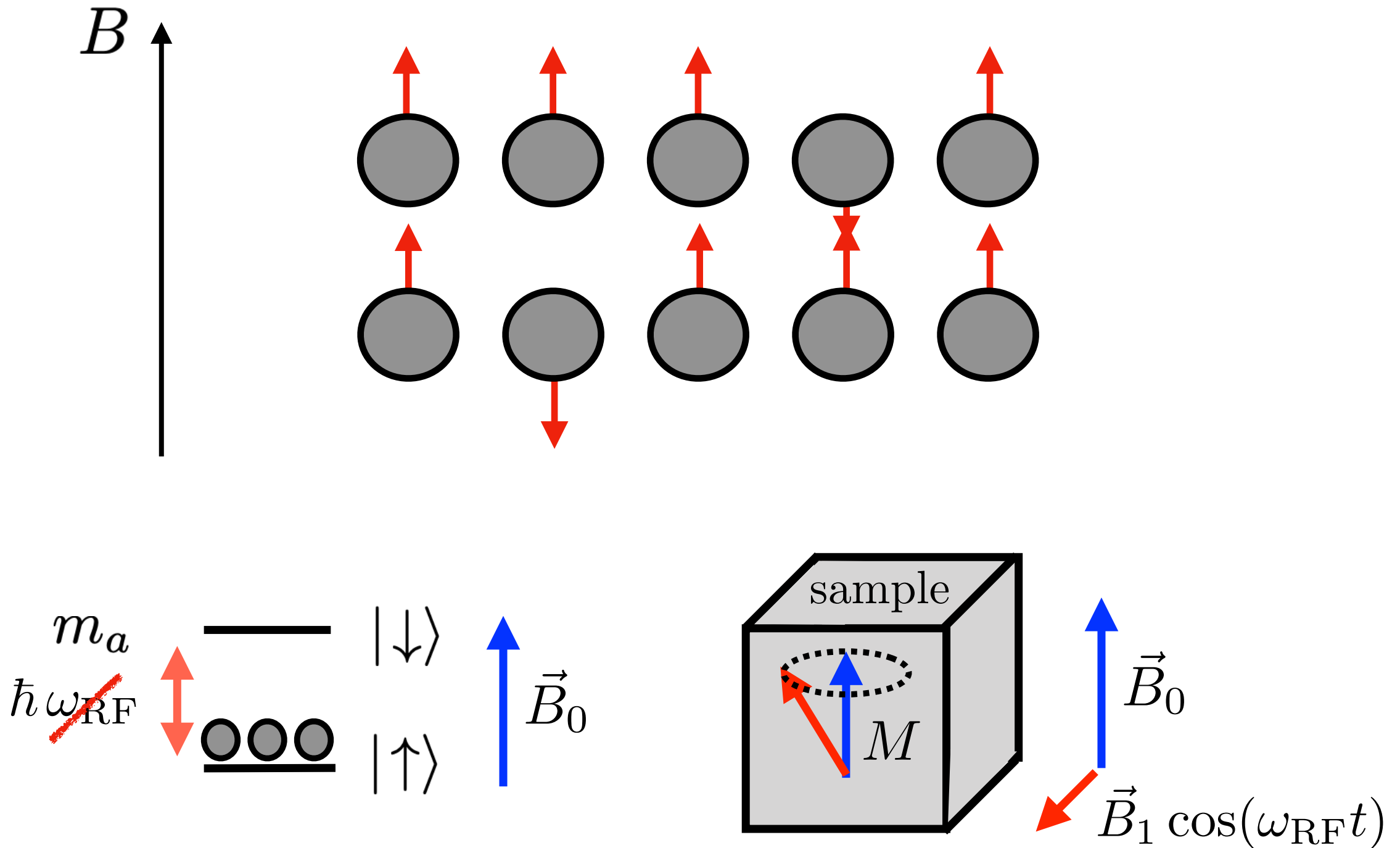
CASPER

[Budker, Graham, et al. 2014]
[Garcon, Blanchard, et al. 2019]



CASPER

[Budker, Graham, et al. 2014]
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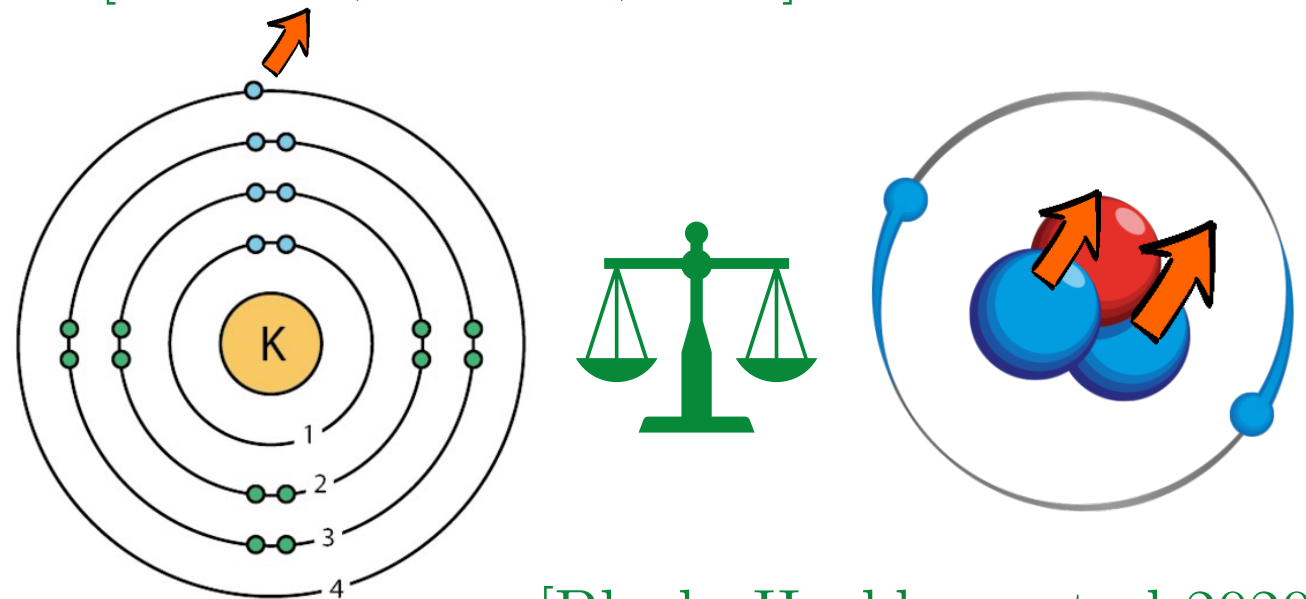
Co-Magnetometers

sensitive to the difference between the magnetic fields measured by
two strongly interacting magnetometers

$$\mathcal{H}_{\text{spin}} = \cancel{\mathcal{H}_{\text{mag}}} + \mathcal{H}_{\text{anomalous}}$$

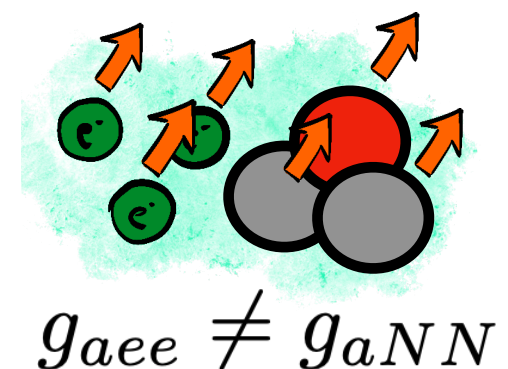
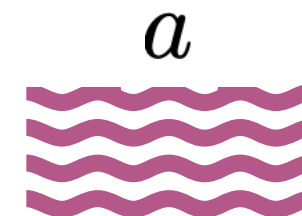
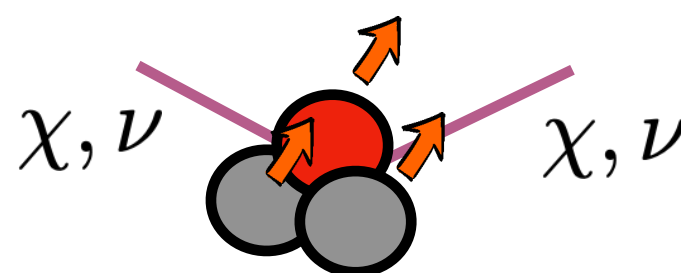
Noble-alkali comagnetometers

[Kornack, Romalis, 2002] e.g. K – ^3He



[Graham, Kaplan, et al. 2018] [Bloch, Hochberg et al 2020]
[Agrawal, Hutzler et al 2023]

[Alonso, Blas, Wolf, 2019]
[Terrano, Romalis, 2021]



Co-Magnetometers

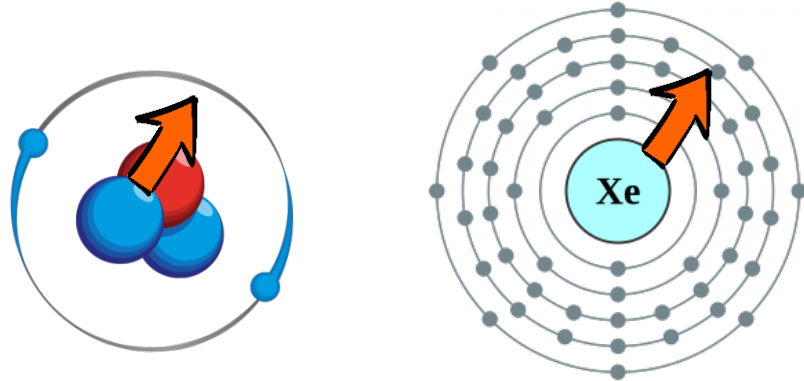
sensitive to the difference between the magnetic fields measured by
two strongly interacting magnetometers

$$\mathcal{H}_{\text{spin}} = \cancel{\mathcal{H}_{\text{mag}}} + \mathcal{H}_{\text{anomalous}}$$

Noble-Noble comagnetometers

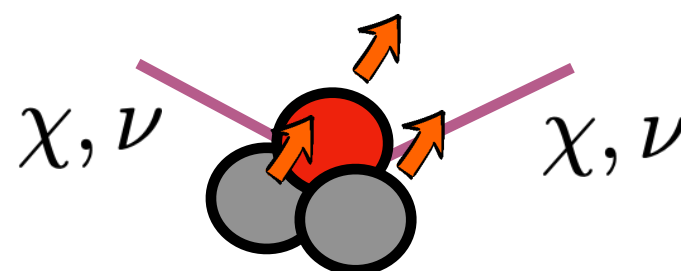
e.g. $^3\text{He} - ^{129}\text{Xe}$

[Allmendiger, Heil, et al. 2013]



$$\Delta\omega = \omega_{\text{He}} - \frac{\gamma_{\text{He}}}{\gamma_{\text{Xe}}} \omega_{\text{Xe}}$$

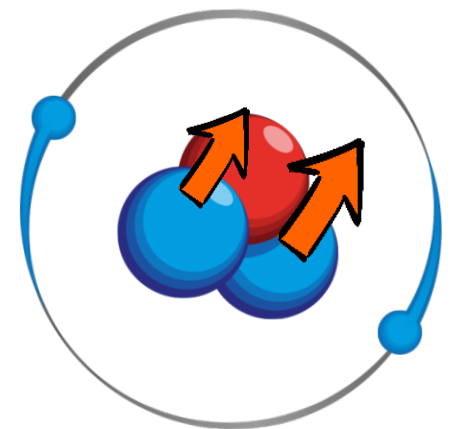
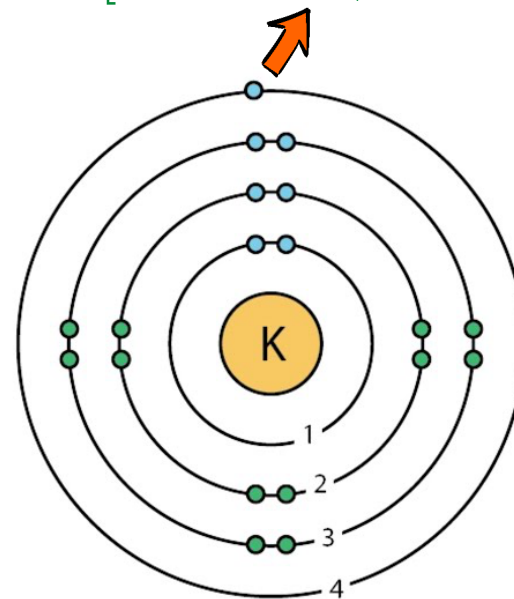
[Graham, Kaplan, et al. 2018]



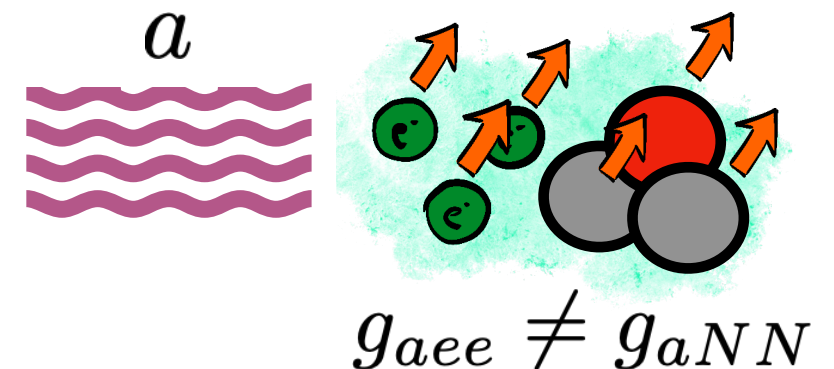
[Alonso, Blas, Wolf, 2019]
[Terrano, Romalis, 2021]

Noble-alkali comagnetometers

[Kornack, Romalis, 2002] e.g. $\text{K} - ^3\text{He}$



[Bloch, Hochberg et al 2020]
[Agrawal, Hutzler et al 2023]



Collective excitations

[Essig, Mardon, Volansky, 2011]

[Graham, Kaplan, Rajendran, Walters, 2012]

[Lee, Lisanti, Mishra-Sharma, Safdi, 2015]

[Essig, Fernandez-Serra, Mardon, Soto, Volansky, Yu, 2015]

[Derenzo, Essig, Massari, Soto, Yu, 2016]

[Hochberg, Lin, Zurek, 2016]

[Bloch, Essig, Tobioka, Volansky, Yu, 2016]

[Essig, Volansky, Yu, 2017]

[Kurinsky, Yu, Hochberg, Cabrera, 2019]

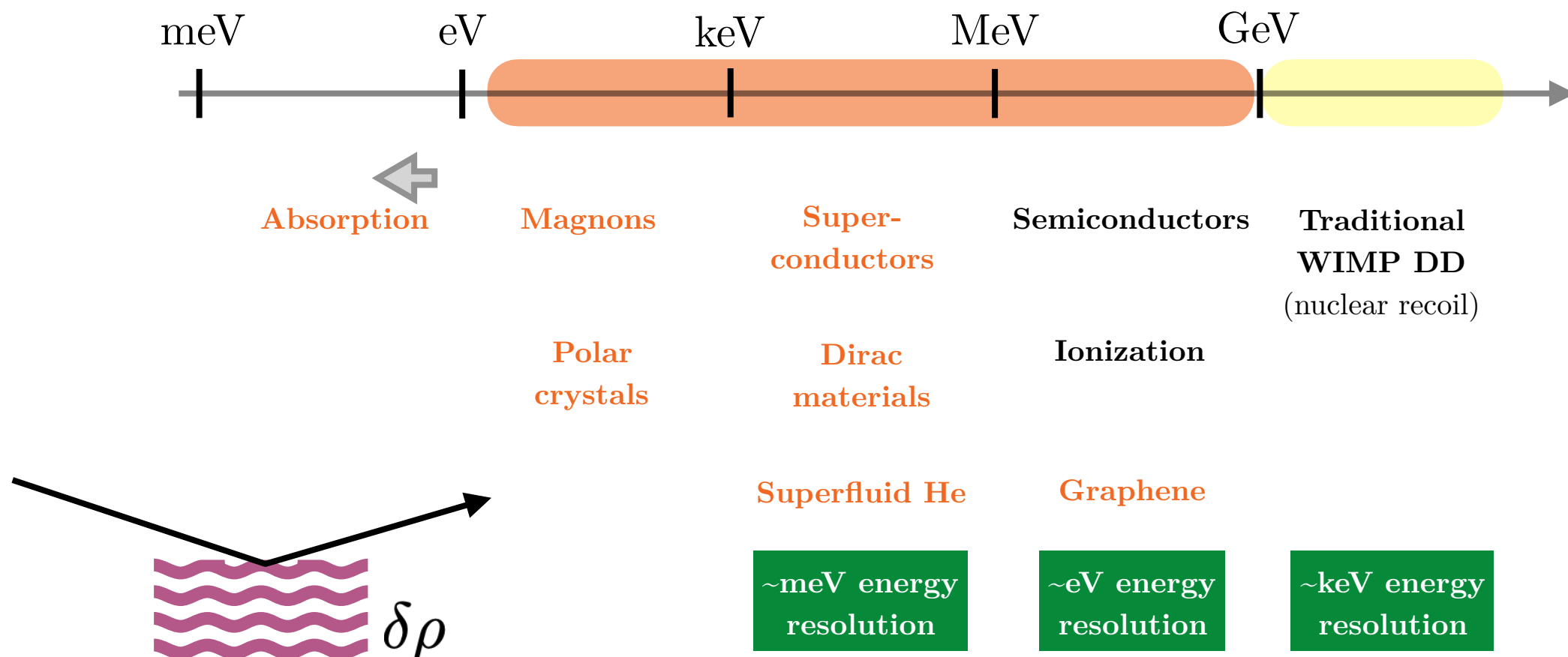
[Emken, Essig, Kouvaris, Sholapurka, 2019]

[Griffin, Inzani, Trickle, Zhang, Zurek, 2019]

[Coskuner, Mitridate, Olivares, Zurek, 2020]

[Mitridate, Trickle, Zhang, Zurek, 2021]

[Chen, Mitridate, Trickle, et al, 2022]



Etc etc etc

➡ Atom spectroscopy

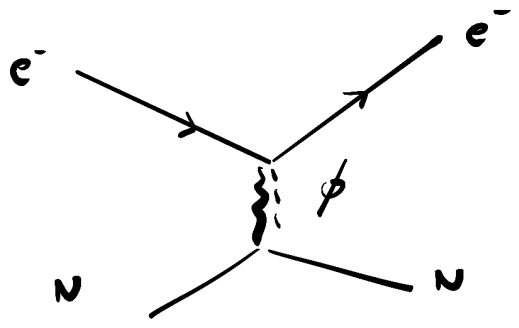
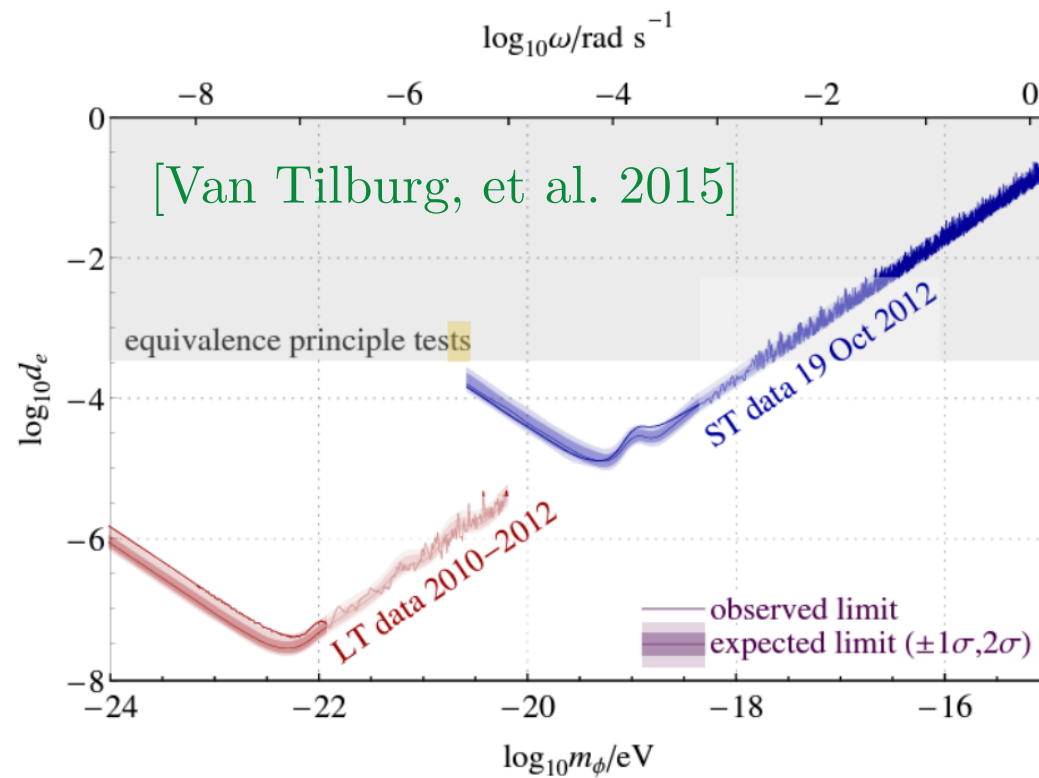
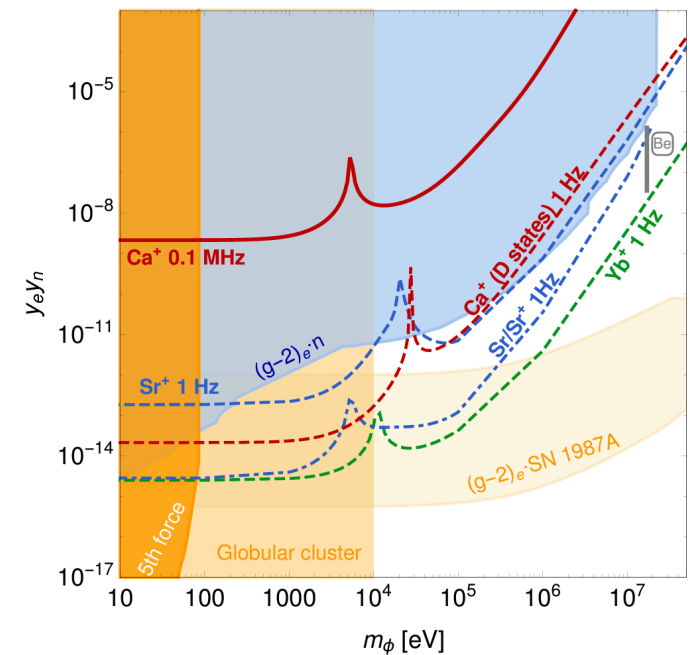


Diagram showing electron-electron scattering via a photon exchange. The Lagrangian is given by:

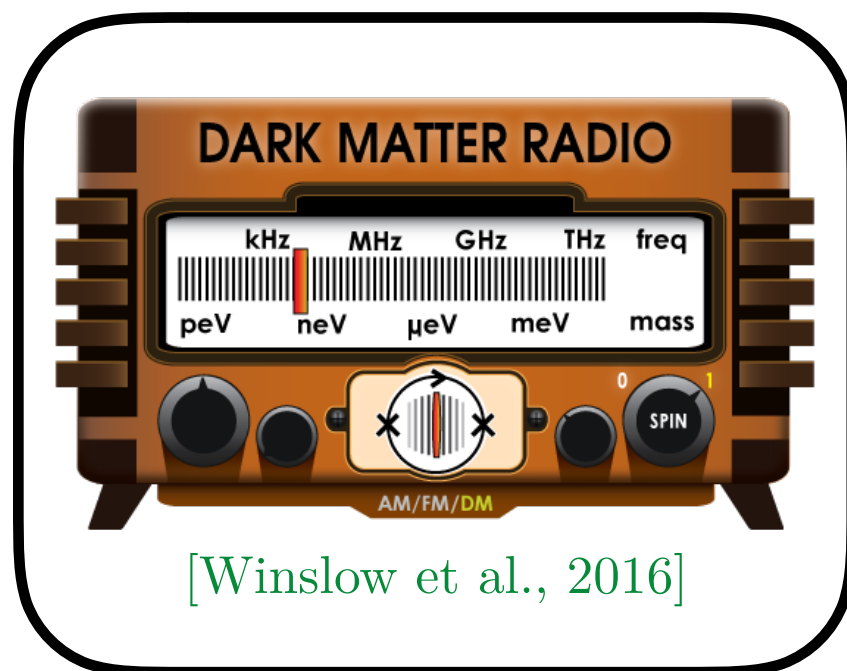
$$\mathcal{L} \supset \frac{-1 + d_e \kappa \phi}{4e^2} F_{\mu\nu} F^{\mu\nu}$$



[Berengut, et al. 2018]



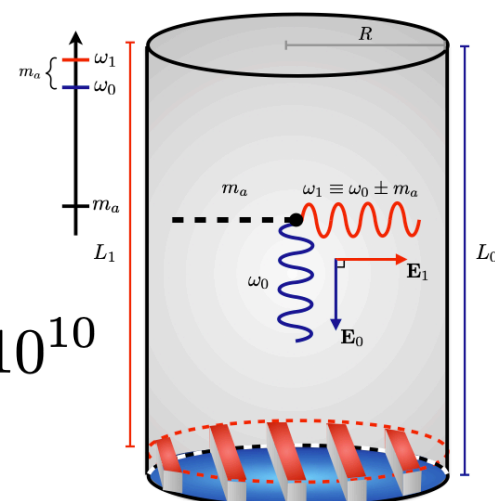
➡ Microwave / radiowave cavities



[Winslow et al., 2016]

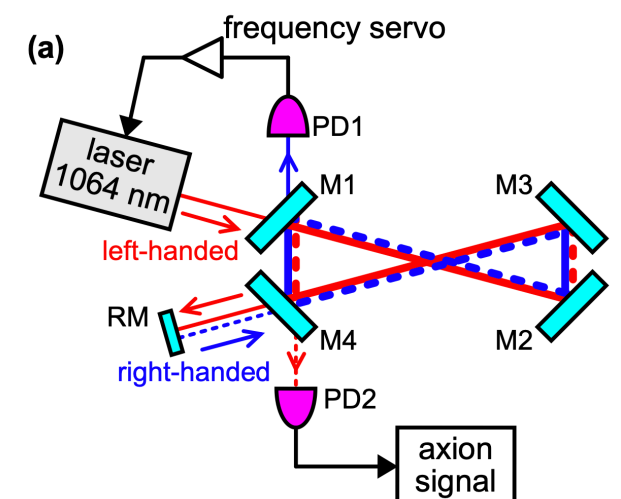
SRF cavities

[Berlin, D'Agnolo, et al., 2019]



DANCE

[Obata, Fujita, Michimura, 2018]

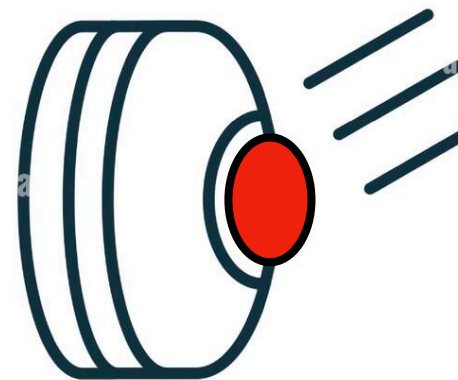
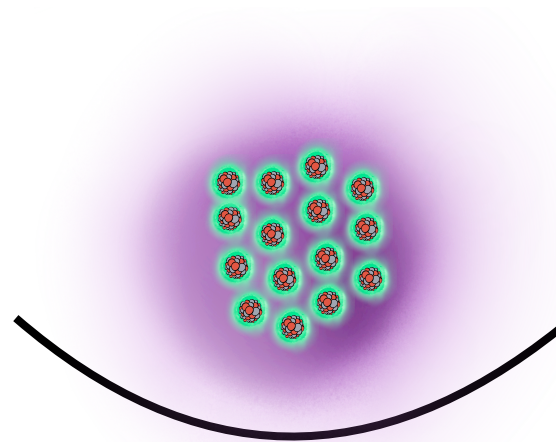
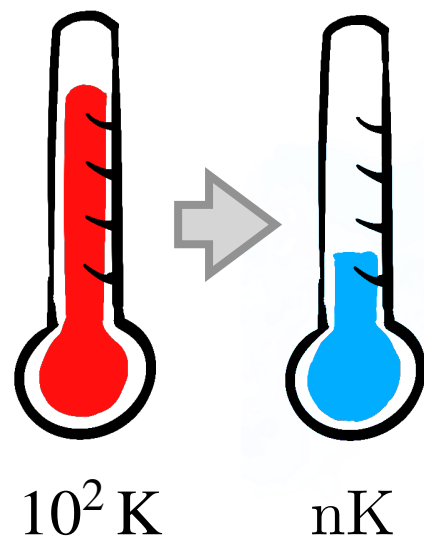


Quantum Sensing: impact

Emergent field

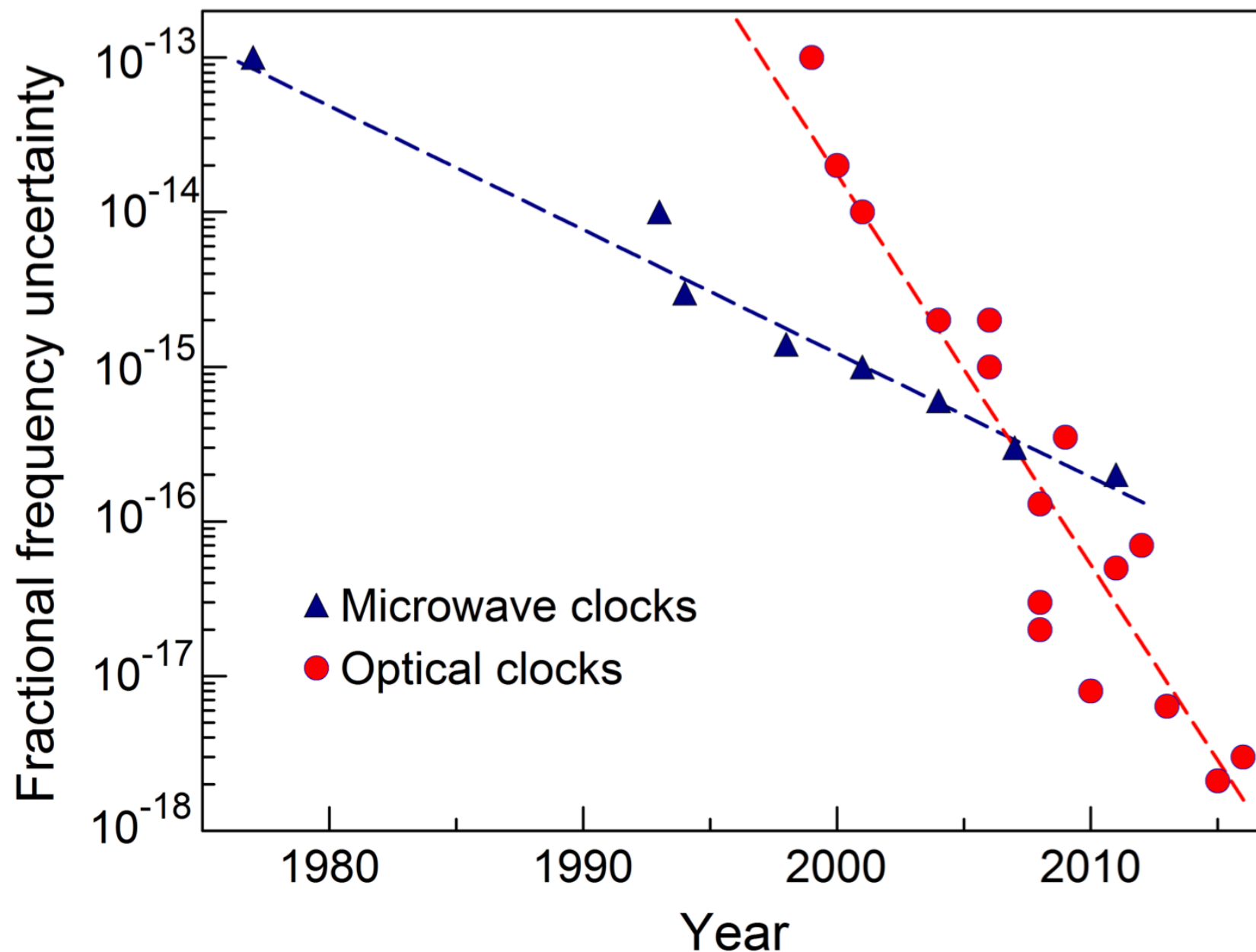
DYNAMICAL

Unknown boundaries



Quantum Sensing: impact

e.g. Atomic clocks

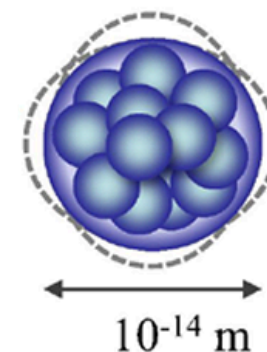
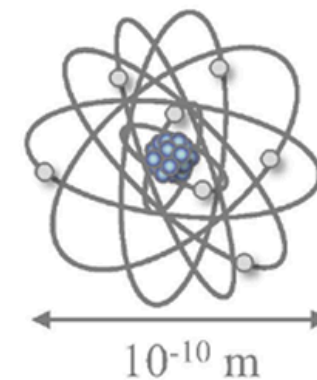


[Huntemann et al., 2016]

[Nicholson et al. 2015]

[Poli et al. 2013]

[Safranova et al. 2017]

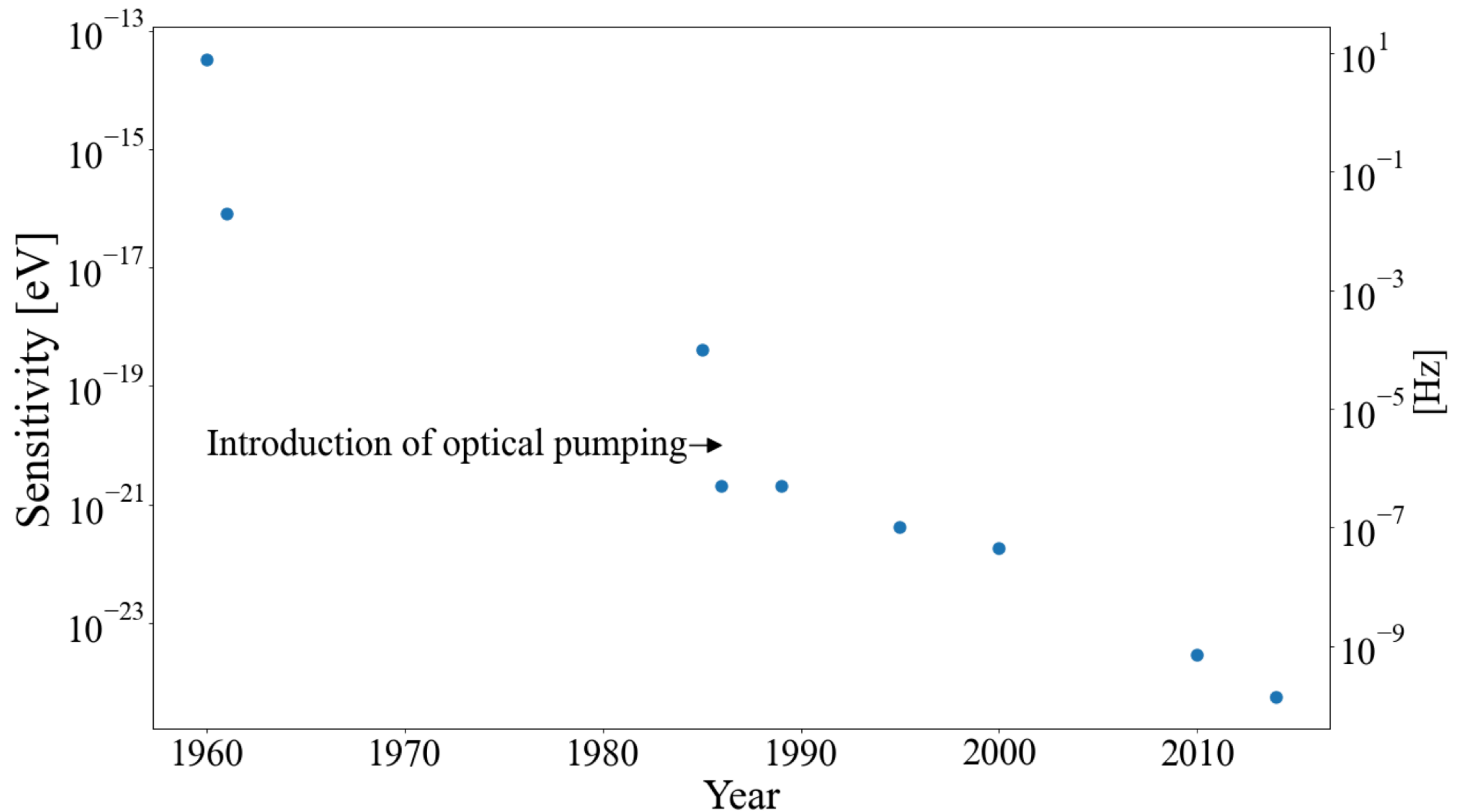


Nuclear clocks [Peik et al. 2021]

Quantum Sensing: impact

e.g. Magnetometers

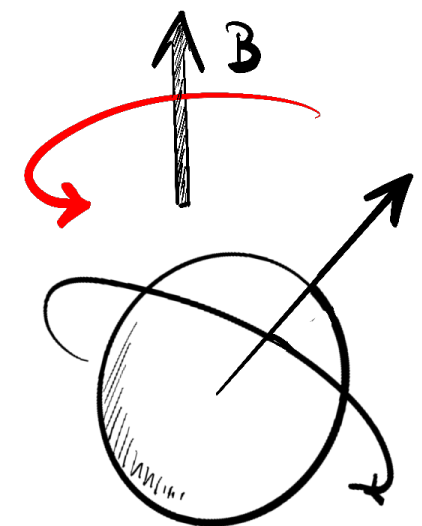
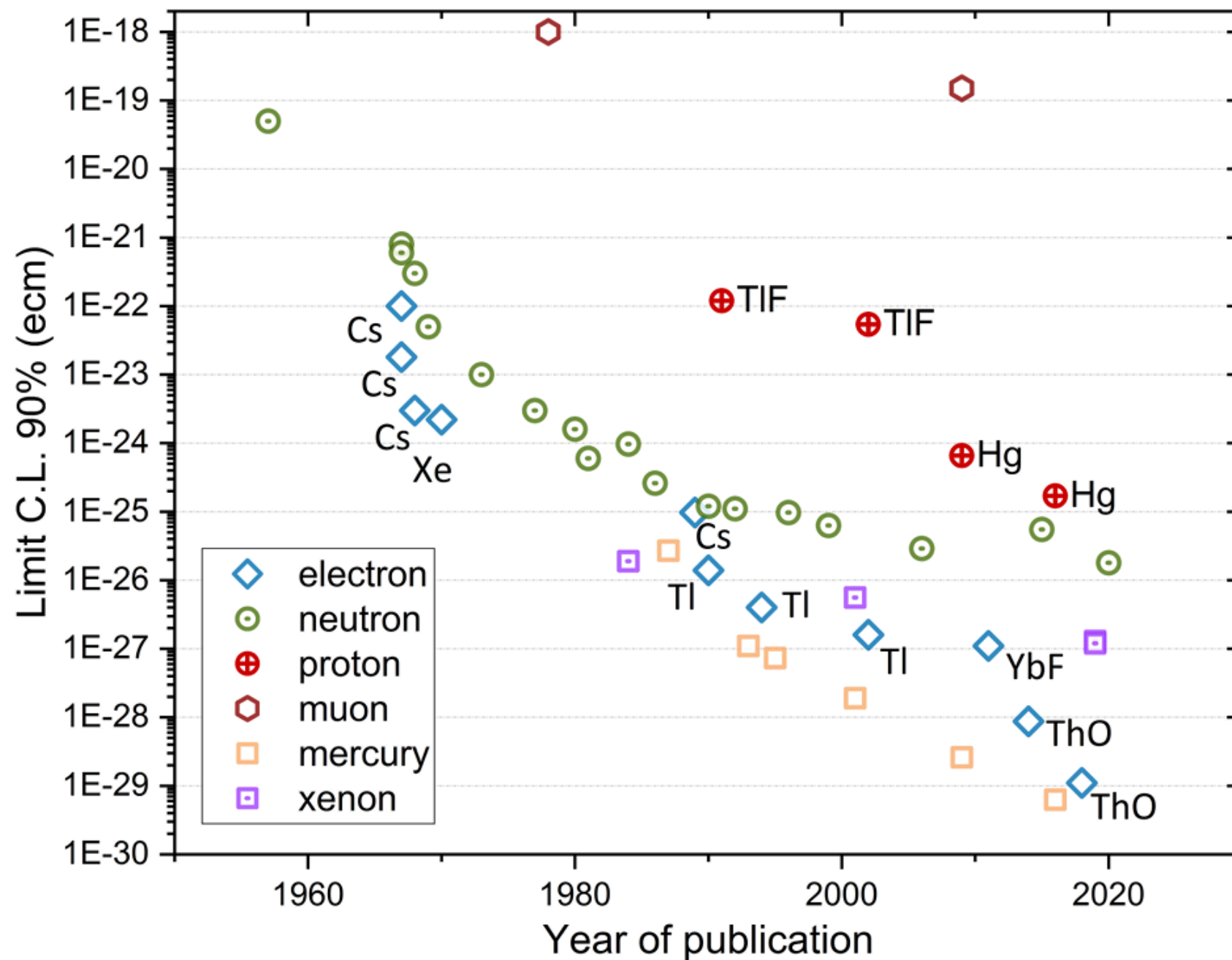
[Terrano and M. V. Romalis, 2021]



Quantum Sensing: impact

e.g. eEDM

[Adelman et al, 2021]



Conclusions

- ⇒ WE NEED quantum sensors to detect elusive phenomena / particles
 - 👁 Will allow us to access unexplored parameter space

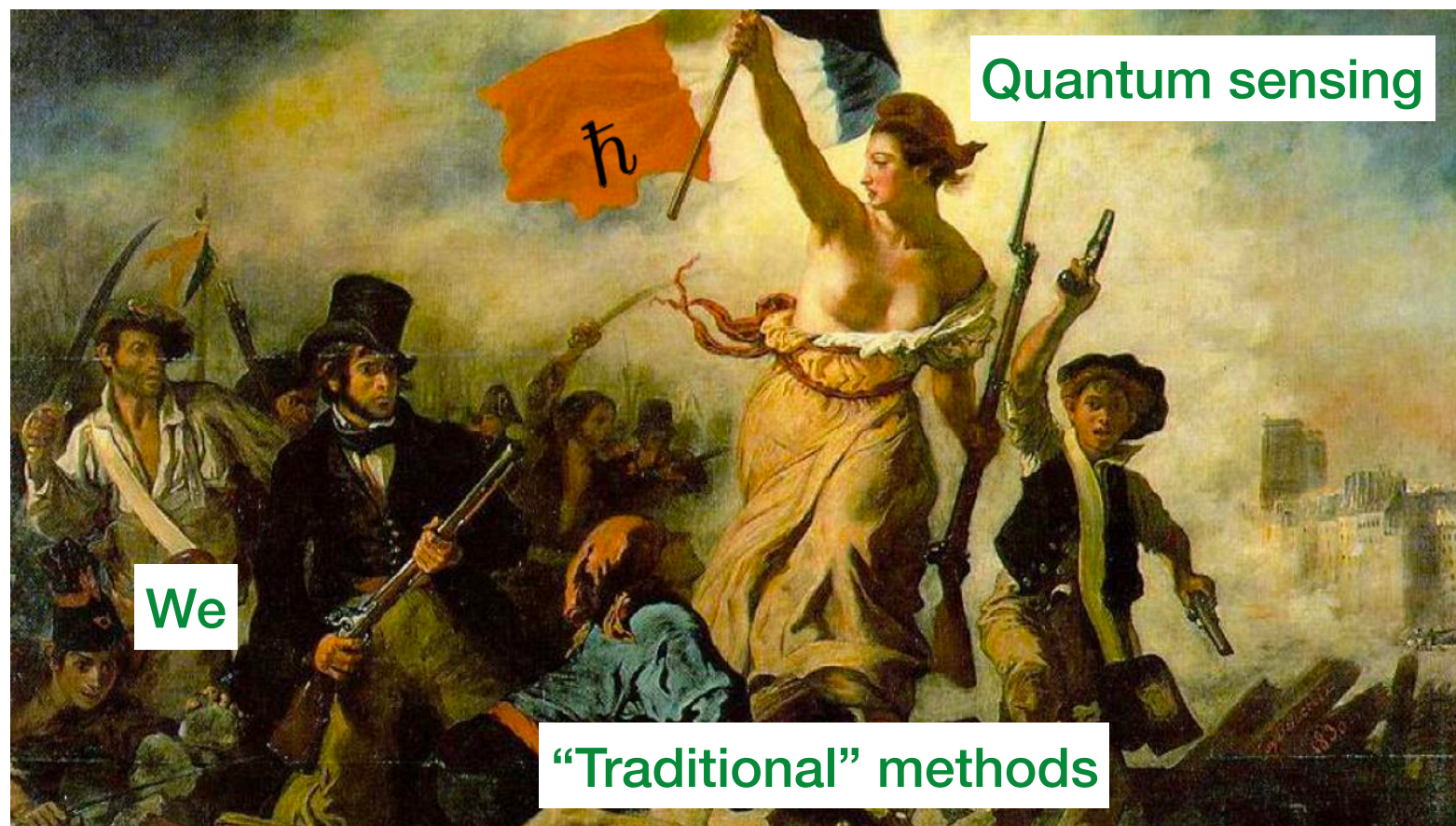
Conclusions

⇒ WE NEED quantum sensors to detect elusive phenomena / particles

👁 Will allow us to access unexplored parameter space

⇒ WE SHOULD BE EXCITED!

Quantum sensing is an emmergent field: lots of improvement expected



Quantum sensing

We

“Traditional” methods

[*La Liberté guidant le peuple*. Delacroix, 1839]

Thank you!