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# Non-perturbative Physics in Precision Event Simulations



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# From High Energies to **Confinement**

#### Consider a "hard" process

"Hard" = large momentum transfers Example:  $gg \rightarrow t\bar{t}$ Here,  $Q^2 \sim m_t^2 \gg \Lambda_{\rm QCD}^2$ 

#### Accelerated charges (QED & QCD)

- → Bremsstrahlung (QED & QCD)
- Perturbative Methods
   Near-Future Goal: NNLO + NNLL
  - → Percent-level precision

#### At wavelengths ~ $r_{\rm proton}$ ~ $1/\Lambda_{\rm QCD}$

Some dynamical process must ensure quarks and gluons become confined inside hadrons: *Hadronization* 

How much do we know about that?



### Linear Confinement

# In lattice QCD, compute the potential energy of a colour-singlet $q\bar{q}$ state, as a function of the distance, r, between the q and $\bar{q}$



#### From **Partons** to **Strings**

#### Motivates a model:

Let colour field collapse into a narrow flux tube of uniform energy density

к ~ 1 GeV / fm

Limit  $\rightarrow$  Relativistic 1+1 dimensional worldsheet

#### g (<del>7</del>b) Map:

- Quarks → String Endpoints
- Gluons → Transverse Excitations (kinks)

#### Physics then in terms of string worldsheet evolving in spacetime

Nambu-Goto action  $\implies$  Area Law.





Gluon = kink on string, carrying energy and momentum

## String **Breaking**



Assume probability of string break constant per unit world-sheet area



## (Alternative: The Cluster Model — Used in Herwig and Sherpa)

#### In "unquenched" QCD

 $g \rightarrow q\bar{q} \implies$  The strings will "break" Non-perturbative so can't use  $P_{g \rightarrow q\bar{q}}(z)$ Altemative: force  $g \rightarrow q\bar{q}$  at end of shower





## Returning to Strings: the String Fragmentation Function

Schwinger  $\implies$  Gaussian  $p_{\perp}$  spectrum (transverse to string axis) & Prob(d:u:s)  $\approx$  1:1:0.2 The meson M takes a fraction z of the quark momentum, Probability distribution in  $z \in [0,1]$  parametrised by **Fragmentation Function**,  $f(z, Q_{HAD}^2)$ 



#### **Observation:** All string breaks are **causally disconnected**

- Lorentz invariance  $\implies$  string breaks can be considered in any order. Imposes "left-right symmetry" on the FF
- $\implies$  **FF** constrained to a form with **two free parameters**, *a* & *b*: constrained by fits to measured hadron spectra

$$x \frac{1}{z} (1-z)^{a} \exp\left(-\frac{b(m_{h}^{2}+p_{\perp h}^{2})}{t}\right)$$

Supresses high-z hadrons

Supresses low-z hadrons

## (Note on the Length of Strings)

#### In Spacetime:

String tension  $\approx$  1 GeV/fm  $\rightarrow$  a 50-GeV quark can travel 50 fm before all its kinetic energy is transformed to potential energy in the string. Then it must start moving the other way.

 $(\rightarrow$  "yo-yo" model of mesons. Note: string breaks  $\rightarrow$  several mesons)

# The MC implementation is formulated in momentum space Lightcone momenta $p_{\pm} = E \pm p_z$ along string axis $\rightarrow$ Rapidity (along string axis) and $p_{\perp}$ transverse to it $y = \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) = \frac{1}{2} \ln \left( \frac{(E + p_z)^2}{E^2 - p_z^2} \right) \qquad \Longrightarrow \qquad y_{\text{max}} \sim \ln \left( \frac{2E_q}{m_-} \right)$

#### **Particle Production:**

Scaling in  $z \implies$  flat in rapidity (long. boost invariance) "Lightcone scaling"



 $\langle n_{\rm ch} \rangle \approx c_0 + c_1 \ln E_{\rm cm}$ , ~ Poissonian multiplicity distribution

## Gluon Kinks: The Signature Feature of the Lund Model

#### Gluons are connected to two string pieces



Flow

Thaler et al., Les Houches, arXiv:1605.04692

## Other String Topologies



#### **Closed Strings**



 $q\bar{q}$  strings (with gluon kinks) E.g.,  $Z \rightarrow q\bar{q}$  + shower  $H \rightarrow b\bar{b} + \text{shower}$ 

Gluon rings E.g.,  $H \rightarrow gg$  + shower Open strings with  $N_C = 3$  endpoints  $\Upsilon \rightarrow ggg + shower$ E.g., Baryon-Number violating neutralino decay  $\tilde{\chi}^0 \rightarrow qqq$  + shower



# pp Collisions



# → Additional colour exchanges

## **A Brief History of MPI** (in PYTHIA)

**1987** [Sjöstrand & van Zijl, Phys.Rev.D 36 (1987) 2019]



## **Interleaved** Evolution in PYTHIA

2005 [Sjöstrand & PS, Eur.Phys.J.C 39 (2005) 129] **Interleave MPI & ISR** evolutions in one common sequence of pt → ISR & MPI "compete" for the available x in the proton remnant. 2011 [Corke & Sjöstrand, JHEP 03 (2011) 032] Also include **FSR** in interleaving [Brooks, **PS**, Verheyen, <u>SciPost Phys. 12 (2022) 3</u>] Also include **Resonance Decays** in interleaving (VINCIA)



Non-perturbative Physics in Precision Event Simulations

### Confinement

#### High-energy pp collisions with MPI + QCD bremsstrahlung

Final states with **very many** coloured partons With significant overlaps in phase space Who gets confined with whom?

### Each has a colour ambiguity $\sim 1/N_C^2 \sim 10\%$

E.g.: random triplet charge has 1/9 chance to be in singlet state with random antitriplet:  $3 \otimes \overline{3} = 8 \oplus 1$ , etc.

Many charges → Colour Reconnections\* (CR) more likely than not



\*): in this context, QCD CR simply refers to an ambiguity beyond Leading  $N_c$ , known to exist. Note the term "CR" can also be used more broadly to incorporate further physics concepts.



#### "Parton Level" (Event structure before confinement)

### Colour (Re)connections

#### **Colour Flow in MC Event Generators**

- Based on "Leading Colour":  $8 \sim 3 \otimes \overline{3}$ 
  - Gluons ~ Direct product of 3 and  $\overline{3}$
- Formally corresponds to a limit  $N_C \rightarrow \infty$
- Unique colour flow; no interferences
- 2015 [Christiansen & **PS** JHEP 08 (2015) 003] Stochastic sampling of beyond-LC correlations in colour space (incl MPI, etc) Weighted by SU(3) group weights:  $3 \otimes \overline{3} = 8 \oplus 1$  $3 \otimes 3 = 6 \oplus \overline{3}$  $3 \otimes 8 = 15 \oplus 6 \oplus 3$   $8 \otimes 8 = 27 \oplus 10 \oplus \overline{10} \oplus 8_S \oplus 8_A \oplus 1$ Interpret Confinement  $\leftrightarrow$  **any** connection that can screen QCD charge + Use string area law to split degeneracies: minimise string "length"



# QCRCGO THE REGODDRECTIONS

Stochastically restores colour-space ambiguities according to SU(3) algebra

> Allows for reconnections to minimise string lengths



#### What about the red-green-blue colour singlet state?





**Junctions!** 

## Fragmentation of String Junctions

#### Assume Junction Strings have same properties as ordinary ones (u:d:s, Schwinger p<sub>T</sub>, etc)

> No new string-fragmentation parameters



The Junction Baryon is the most "subleading" hadron in all three "jets".

Generic prediction: low p<sub>T</sub>

A Smoking Gun for String Junctions: Baryon enhancements at low pT



## Confront with Measurements

LHC experiments report very large (factor-10) enhancements in heavy-flavour baryon-to-meson ratios at low  $p_T$ !

**HARDICK** 



### Confront with Measurements: Strangeness



P. Skands

19

## What a strange world we live in, said Alice

# We know ratios of strange hadrons to pions strongly increase with event activity

Landmark measurement by ALICE (2017)

![](_page_19_Picture_3.jpeg)

TOPOLOGICAL PHOTONICS Optical Weyl points and Fermi arcs

![](_page_19_Figure_7.jpeg)

# → Non-Linear String Dynamics?

#### $\mathsf{MPI} \Longrightarrow \mathsf{lots}$ of coloured partons scattered into the final states

Count # of flux lines crossing y = 0 in pp collisions (according to PYTHIA):

![](_page_20_Figure_3.jpeg)

1,-1

# Work in Progress: Strangeness Enhancement from Close-Packing - <u>nhononno</u>

Idea: each string exists in an effective background produced by the others

![](_page_21_Figure_2.jpeg)

![](_page_21_Figure_5.jpeg)

## Implications for Precision Event Generators

![](_page_22_Picture_1.jpeg)

#### ATLAS PUB Note

ATL-PHYS-PUB-2022-021

29th April 2022

![](_page_22_Picture_5.jpeg)

#### Dependence of the Jet Energy Scale on the Particle Content of Hadronic Jets in the ATLAS Detector Simulation

The dependence of the ATLAS jet energy measurement on the modelling in Monte Carlo simulations of the particle types and spectra within jets is investigated. It is found that the hadronic jet response, i.e. the ratio of the reconstructed jet energy to the true jet energy, varies by  $\sim 1-2\%$ depending on the hadronisation model used in the simulation. This effect is mainly due to differences in the average energy carried by kaons and baryons in the jet. Model differences observed for jets initiated by *quarks* or *gluons* produced in the hard scattering process are dominated by the differences in these hadron energy fractions indicating that measurements of the hadron content of jets and improved tuning of hadronization models can result in an improvement in the precision of the knowledge of the ATLAS jet energy scale.

#### Variation largest for gluon jets For $E_T = [30, 100, 200]$ GeV Max JES variation = [3%, 2%, 1.2%]

# Fraction of jet $E_T$ carried by baryons (and kaons) varies significantly

- Reweighting to force similar baryon and kaon fractions
- Max variation → [1.2%, 0.8%, 0.5%]
- Significant potential for improved Jet Energy Scale uncertainties!

#### Motivates Careful Models & Careful Constraints

Interplay with advanced UE models In-situ constraints from LHC data Revisit comparisons to LEP data

### Summary

#### MC generators connect theory with experiment

![](_page_23_Picture_2.jpeg)

Much new work on non-perturbative physics

Driven by **new measurements** at LHC

# + expect NNLO+NNLL perturbative predictions in MCs ~ soon

→ era of percent-level perturbative accuracy

![](_page_23_Figure_9.jpeg)

# Extra Slides

#### From **Partons** to **Pions**

#### Consider a parton emerging from a hard scattering (or decay) process

Hard: Large momentum transfer  $Q_{\rm Hard} \gg 1 \,{\rm GeV}$ 

It showers

![](_page_25_Picture_4.jpeg)

## Local Parton Hadron Duality - Independent Fragmentation

#### Late 70<sup>s</sup> MC models: Independent Fragmentation

E.g., PYTHIA (then called JETSET) anno 1978

![](_page_26_Picture_4.jpeg)

```
SUBROUTINE JETGEN(N)
      COMMON /JET/ K(100,2), P(100,5)
      COMMON /PAR/ PUD, PS1, SIGMA, CX2, EBEG, WFIN, IFLBEG
      COMMON /DATA1/ MESO(9,2), CMIX(6,2), PMAS(19)
      IFLSGN=(10-IFLBEG)/5
      W=2.*E8EG
      I=0
      IPD=0
C 1 FLAVOUR AND PT FOR FIRST QUARK
      IFL1=IABS(IFLBEG)
      PT1=SIGMA*SQRT(-ALOG(RANF(D)))
      PHI1=6.2832*RANF(0)
      PX1=PT1*COS(PHI1)
      PY1=PT1*SIN(PHI1)
  100 I=I+1
C 2 FLAVOUR AND PT FOR NEXT ANTIQUARK
       IFL2=1+INT(RANF(0)/PUD)
      PT2=SIGMA*SQRT(-ALOG(RANF(0)))
      PH12=6.2832*RANF(0)
       PX2=PT2*COS(PHI2)
       PY2=PT2*SIN(PHI2)
C 3 MESON FORMED, SPIN ADDED AND FLAVOUR MIXED
      K(I,1)=MESO(3*(IFL1-1)+IFL2,IFLS6N)
       ISPIN=INT(PS1+RANF(0))
       K(I:2)=1+9*ISPIN+K(I:1)
       IF(K(I,1).LE.6) GOTO 110
       TMIX=RANF(0)
       KM=K(I,1)-6+3*ISPIN
       K(I,2)=8+9*ISPIN+INT(TMIX+CMIX(KM,1))+INT(TMIX+CMIX(KM,2))
C 4 MESON MASS FROM TABLE, PT FROM CONSTITUENTS
   110 P(1,5)=PMAS(K(1,2))
       P(I,1) = PX1 + PX2
       P(1,2) = PY1 + PY2
       PMTS=P(1,1)**2+P(1,2)**2+P(1,5)**2
 C 5 RANDOM CHOICE OF X=(E+PZ)MESON/(E+PZ)AVAILABLE GIVES E AND PZ
       x = RANF(0)
       IF(RANF(D).LT.CX2) X=1.-X**(1./3.)
       P(I,3) = (X*W-PMTS/(X*W))/2.
       P(1,4)=(X*W+PMTS/(X*W))/2.
 C & IF UNSTABLE, DECAY CHAIN INTO STABLE PARTICLES
   120 IPD=IPD+1
       IF(K(IPD:2).GE.8) CALL DECAY(IPD:1)
       IF(IPD.LT.I.AND.I.LE.96) GOTO 120
 C 7 FLAVOUR AND PT OF QUARK FORMED IN PAIR WITH ANTIQUARK ABOVE
       IFL1=IFL2
       PX1 = -PX2
       PY1 = -PY2
 C 8 IF ENOUGH E+PZ LEFT, GO TO 2
        W = (1, -X) * W
       IF(W.GT.WFIN.AND.I.LE.95) GOTO 100
       M = I
        RETURN
        END
                                                                   27
```

### **Colour Neutralisation**

#### A physical hadronization model

Should involve at least two partons, with opposite colour charges

A strong **confining field** emerges between the two when their separation ≥ 1fm

![](_page_27_Figure_4.jpeg)

### **Iterative String Breaks**

#### Causality → May iterate from outside-in

Note: using light-cone coordinates:  $p_+ = E + p_z$ 

![](_page_28_Figure_3.jpeg)

On average, expect energy of n<sup>th</sup> "rank" hadron ~  $E_n \sim \langle z \rangle^n E_0$ 

# Fragmentation of String Junction Systems

![](_page_29_Picture_1.jpeg)

sume vortex-line string picture still OK hich topology? Y,  $\Delta$ , V, T, ...? aryon wave functions & minimal string length  $\Rightarrow$  Picture of Y-shaped topology with "string junction"

**String-Junction Fragmentation Model** Sjöstrand & PS, Nucl.Phys.B 659 (2003) 243 ocused on hard BNV processes:  $\tilde{\chi} \rightarrow q_i q_j q_k$ ,  $\tilde{t}_i^* \rightarrow q_j q_{k'} \dots$ In (but a bit of a long shot ...)

#### (Junction strings can also have kinks):

![](_page_29_Figure_5.jpeg)

![](_page_29_Figure_8.jpeg)

![](_page_29_Figure_9.jpeg)

Would love to tell you **this** has been seen at LHC But then you probably wouldn't be hearing about it from me However, **string junctions** may have been seen!

# **Predicting** the Junction Baryon Spectrum

#### The Junction Baryon = smoking gun of String Junctions Predicting the movement of the string junction is crucial!

- To make solid predic<sup>®</sup> The movement of the string junction is crucial, it is the smoke of the BNV gun! we use a trick: Sjöstrand & PS, Nucl.Phys.B 659 (2003) 243 Find the Lorentz fram • A junction is a topological feature of the string confinement field:  $V(r) = \kappa r$ . Each string piece **Inverse boost** (+  $\mathcal{O}(r)$  acts on the other two with a constant force,  $\kappa \vec{e_r}$ .
- Junction = Topologi  $\Rightarrow \Rightarrow$  in junction rest frame (JRF) the angle is 120° between the string pieces.  $V(r) = \kappa r$
- $\implies$  each "leg" (strin <sup>o</sup> Or better, 'pull vectors' lie at 120°:
- $\overrightarrow{F} = \kappa \overrightarrow{e}_r.$
- $p_{\text{pull}}^{\mu} = \sum p_i^{\mu} e^{-\sum_{j=1}^{i-1} \frac{E_j}{\kappa}}$ i=1.N

 $\implies$  In "Mercedes Fr

Massless legs: exact s

(since soft gluons 'eaten' by string)

Massive legs (eg heavy flavours or ones with lots of kinks!) => Iterative algorithm. But org algorithm often broke down (failed to converge) for "soft legs"

![](_page_30_Picture_17.jpeg)

# Does a Boost to the Mercedes Frame Always Exist?

#### Consider the following kinematic case

In the **rest frame of one of the partons**, and the angle between the other two is **greater than 120 degrees** (not considered in org algorithmic implementation)

![](_page_31_Figure_3.jpeg)

3

I.e., can only happen for massive partons

 $q_3$ 

Org algorithm failed to converge

 $q_3$ 

Slide adapted from J. Altmann

#### The case of a heavy slow endpoints: Pearl on a String atrino

String Motion: Soft Massless Case

![](_page_32_Figure_2.jpeg)

With thanks to G. Gustafson. Slide adapted from J. Altmann

# String Motion: Slow Massive Case

## New: the case of a heavy slow endpoint: Pearl on a String

The junction gets "stuck" to the soft quark, which we call a pearl-on-a-Example of pearl-on-a-string viewed in the Ariadne frame string of the green quark

More likely to occur for junctions with heavy flavour endpoints

For a string junction to make a **heavy baryon**, the junction leg with the heavy quark can't "break" (i.e. a "soft" junction leg) = pearl-on-a-string!

![](_page_33_Figure_4.jpeg)

# String Motion: Slow Massive Case

![](_page_33_Figure_8.jpeg)

#### How many MPI are there?

### Example for pp collisions at 13 TeV — PYTHIA's default MPI model

Averaged over all pp impact parameters (Really: averaged over all pp overlap

enhancement factors)

![](_page_34_Figure_4.jpeg)

# 13000 GeV ---- ND --**→**-- UE (p̂<sub>\_</sub>=20) --0--Z CIAROO 20 n<sub>MPI</sub>

\*note: can be arbitrarily soft

## Collective Flow in PYTHIA: String Shoving

Bierlich, Chakraborty, Gustafson, Lönnblad, arXiv:1710.09725, 2010.07595

## Strings should push each other transversely Colour-electric fields -> Classical force

#### Model string radial shape & shoving physics

$$\implies \text{force} \quad f(d_{\perp}) = \frac{g\kappa d_{\perp}}{R^2} \exp\left(-\frac{d_{\perp}^2}{4R^2}\right)$$

g: fraction of energy in chromoelectric field (as opposed to in condensate or magnetic flux)

 $d_1$ : transverse distance (in string-string "shoving frame")

R: string radius----

 $\kappa$ : string tension ~ 1 GeV/fm

![](_page_35_Figure_9.jpeg)