



# Re-Evaluation of the HVP Contribution to the Anomalous Magnetic Moment of the Muon

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# The Anomalous Magnetic Moment & $g - 2$

- Dirac:  $g = 2$ , QFT:  $g = 2 + a_\mu$  (bottom)
- Largest theory uncertainty: hadronic contribution due to QCD non-perturbativity.
- Hadronic contribution can be calculated using lattice QCD or dispersive methods (this presentation).
- Dispersive result is in strong tension with recent results of the  $g - 2$  experiment.

$$g =$$

Dirac:  
2

$a_\mu^{QED, N^4LO}:$   
 $116\,584\,718.931(104) \times 10^{-11}$

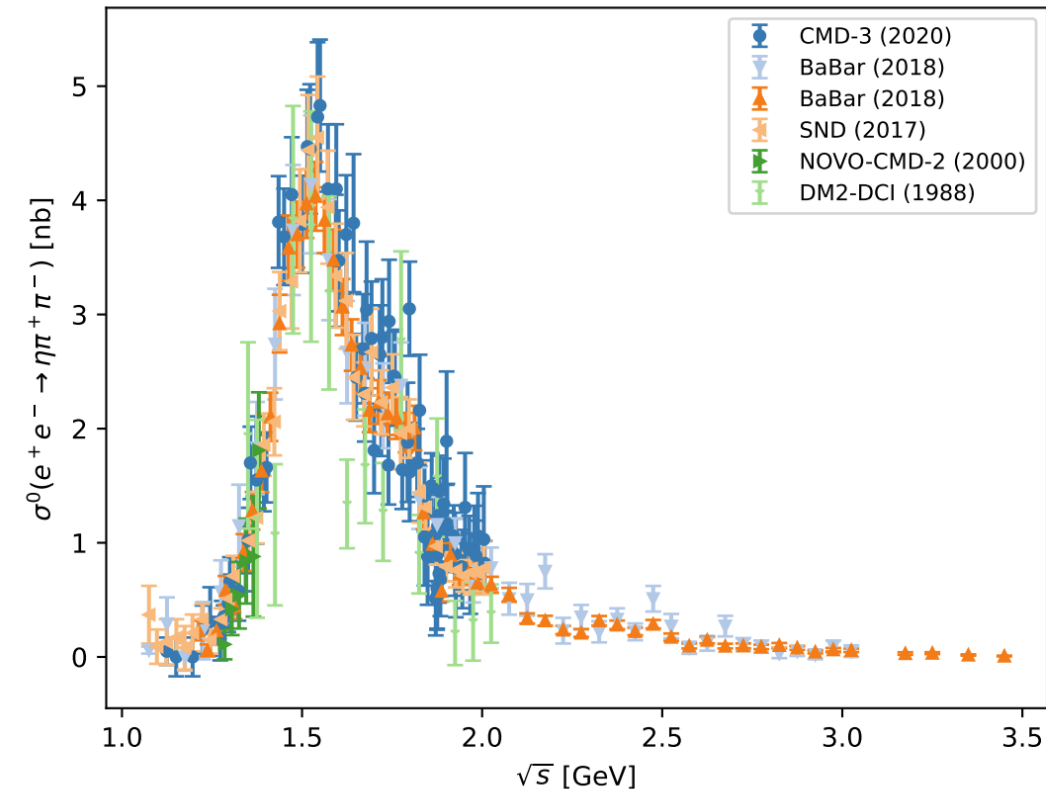
$a_\mu^{EW, NNLO}:$   
 $153.6(1.0) \times 10^{-11}$

$a_\mu^{HVP, NNLO, disp.}:$   
 $6845(40) \times 10^{-11}$

$a_\mu^{HLbL, NLO}:$   
 $92(18) \times 10^{-11}$

# Dispersive $a_{\mu}^{HVP}$

- Take experimental inputs of  $e^+e^- \rightarrow hadrons$  in non-perturbative region and integrate cross section  $\sigma$  with a known kernel  $K(s)$ .
- Complicated by:
  - Multiple hadronic final states
  - Tension between  $e^+e^-$  datasets (CMD-3  $\pi^+\pi^-$ )
  - Radiative corrections
  - Data combination
- (Right) Plot of  $\sigma$  vs.  $\sqrt{s}$  in the  $\eta\pi^+\pi^-$  channel.





# Database Introduction and Structure

- Previous FORTRAN code read in data from saved .txt files.
- New Python3 code uses a relational SQL database which is then used to construct objects.
- (Right) Structure of the database:  
Channels → Datasets → Data → Covariances
- Dataset object inherits channel attributes and contains its data.

channel_id	channel_name	num_sets	radcorr_1	radcorr_2	...
0	Inclusive data HIGH	19	-	Y	...
1	Inclusive data LOW	6	-	Y	...
2	#eta#pi^+#pi^-	7	-	Y	...
3	K^+K^-	17	N	Y	...
4	K^+K^-#pi^0	4	-	Y	...



dataset_id	channel_id	use	num_data_points	experiment	year	...
0	0	y	14	BES-III	2021.0	...
1	0	y	22	KEDR-VEPP4M	2019.0	...
2	0	y	122	BaBar	2009.0	...
3	0	y	3	BES-II	2009.0	...
5	0	y	7	CLEO	2007.0	...
...	...	..	...	...	...	...



data_id	channel_id	dataset_id	energy_min	energy_max	cross_section	...
0	0	0	2.2324	2.2324	2.286	...
1	0	0	2.4000	2.4000	2.260	...
2	0	0	2.8000	2.8000	2.233	...
3	0	0	3.0500	3.0500	2.252	...
4	0	0	3.0600	3.0600	2.255	...
...	...	...	...	...	...	...



data_id1	data_id2	stat0_or_syst1	value
14	14	0	0.019321
14	15	0	0.000000
14	16	0	0.000000
14	17	0	0.000000
14	18	0	0.000000
...	...	...	...



# Blinding

- Previous analysis was not blinded.
- New analysis should be.
- Blind using seeds  $\{s_1, s_2, s_3, s_4, s_5\}$ :
  - Channel number (s5:  $c \rightarrow c' = (c + s_5) \bmod 100$ )
  - Sign:  $a = \pm 1$
  - Scale:  $b$  in  $0.1 \rightarrow 0.9$  or  $1.1 \rightarrow 10$
  - Offset:  $s_0$  in  $-0.01 \text{ GeV}^2 \rightarrow 1.00 \text{ GeV}^2$
  - Power:  $p$  with  $0.01 \leq |p| \leq 0.05$
- Blinding variables  $\{a, b, s_0, p\}$  use concatenations of  $c'$  and  $\{s_1, s_2, s_3, s_4\}$ .  
e.g.:  $s_1 = 1, c' = 63 \Rightarrow \text{sign\_seed} = \text{python.random.seed}(163)$

$$B(s) = a \cdot b(s + s_0)^p$$