

Non-relativistic QCD Study of Bottomonia at Finite **Temperatures on a Finer Lattice**



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Quarkonia as a probe

Quarkonium suppression via color screening in Quark-Gluon Plasma

T. Matsui, H. Satz, PLB178 (1986) 416



In-medium quarkonium properties are encoded in spectral function, which is related to Euclidean correlator calculable on the lattice:

 $C(\tau, T) =$

 $-\infty$

Sequential in-medium modifications at finite temperatures in experiments

$$d\omega \rho(\omega, T) K(\tau, \omega, T)$$



Motivation: why Lattice NRQCD + extended sources

Relativistic QCD

Limited sensitivity in $C(\tau, T)$: $\tau_{max} = 1/(2T)$

A. Mocsy, P. Petreczky, PRD 77, 014501(2008)

P. Petreczky, EPJC 62, 85 (2009)



Large discretization effects $\sim aM_h$

Non-relativistic QCD



Pair creation is not allowed $\Rightarrow \tau_{max} = 1/T$

N. Brambilla, J. Ghiglieri, et.al., PRD 78, 014017(2008)



Heavy quark mass scale is integrated out

More sensitive to thermal effects



- Solution Able to study sequential in-medium modifications in excited states





Correlators with extended sources

Gaussian-smeared source

R. Larsen, et.al., PRD 100, 074506 (2019)



Gaussian-shaped factor



X

Correlator: $C(\tau) = \sum \langle O(\mathbf{x}, \tau) O^{\dagger}(\mathbf{0}, 0) \rangle$

Wave-function optimized source

R. Larsen, et.al., PLB 800, 135119 (2020)

$$O_{\alpha}(\mathbf{x},\tau) = \sum_{\mathbf{r}} \Psi_{\alpha}(\mathbf{r}) \bar{q}(\mathbf{x}+\mathbf{r},\tau) \Gamma q(\mathbf{x},\tau)$$

From the discretized 3-d Schrodinger equation:

$$\begin{bmatrix} -\frac{\Delta}{m_b} + V(\mathbf{r}) \end{bmatrix} \Psi(\mathbf{r}) = E\Psi(\mathbf{r})$$

 $O(a^4)$ -improved discretized Laplacian

Cornell potential

S. Meinel, PRD 82, 114502 (2010)





Simulation Details

- Bottom quark on the lattice:
- Tree-level tadpole-improved NRQCD action, with $\mathcal{O}(v^6)$ corrections R. Larsen, et.al., PRD 100, 074506 (2019) ____ R. Larsen, et.al., PLB 800, 135119 (2020)

- Background gauge fields with (2+1)-flavor dynamical sea quarks:
- HISQ/tree action
- Quark mass: $m_s^{\text{phy}}/m_l = 20 \ (m_\pi \approx 160 \text{ MeV})$
- Fixed finer lattice spacing: a = 0.0493 fm

- Temperature is increased by reducing the temporal extent: $N_{\tau} \in [16, 30], T \in (133, 250)$ MeV

S. Meinel, PRD 82, 114502 (2010)

- Bare bottom mass tuning: matching kinetic mass M_{kin,n_b} to its PDG value, leading to $aM_b = 0.955(17)$



Results in Vacuum: effective mass

 $M_{\rm eff}(\tau) = -\frac{1}{\omega}$

All vertical scales are calibrated with the spin-averaged mass of 1S bottomonium hereafter



Mild effects from different extended sources for ground states

 $\overset{\star}{=}$ Plateau region from $au \sim$ 0.25 fm, shorter for excited states with worse SNR

$$\frac{1}{a} \log \left[\frac{C(\tau, T)}{C(\tau + a, T)} \right]$$



Results in Vacuum: mass spectra







Results at finite temperatures: effective mass

Measured with Gaussian-smeared sources



- Ş Overlaps within small τ : mild temperature dependence
- Solution As T increases: plateau ends at shorter τ , followed by a faster drop at the tail
- Earlier onset of fall-off and steeper slope: P-wave channels are more sensitive to thermal effects ĕ







Results at finite temperatures: effective mass

Measured with wave-function optimized sources



High excited states are more sensitive to thermal modifications





Continuum-subtracted correlator

$$C(\tau, T) = \int_{-\infty}^{+\infty}$$

$$\rho(\omega, T) = \rho_{\rm med}$$

Extended sources lead to selective overlap with particular states:

In vacuum $\rho_{\text{med}}(\omega, T = 0) = A\delta(\omega - M)$

Mass of a state targeted for projection

Define continuum-subtracted correlator: $C_{sub}(\tau, T) = C(\tau, T) - C_{cont}(\tau)$



Extract continuum part at zero temperature: $C_{\text{cont}}(\tau) = C(\tau, T = 0) - Ae^{-M\tau}$



Continuum-subtracted effective mass





$${}_{\rm d}(T) \exp\left(-\frac{\left[\omega - M_{\rm med}(T)\right]^2}{2\Gamma_{\rm med}^2(T)}\right) + A_{\rm cut}(T)\delta\left(\omega - \omega_{\rm cut}(T)\right)$$

Linear behavior of $M_{
m eff}^{
m sub}$ in middle au

Tail of $M_{
m eff}^{
m sub}$



In-medium parameters: mass shift

 $\Delta M = M_{\rm med}(T) - M(T=0)$



Solution \cong Overlaps between green and black points: in-medium quantities independent of extended sources $\triangleq \Delta M$ consistent with zero: almost no change in the in-medium masses





11

In-medium parameters: thermal width



Significant increasement with rising temperatures

Sequential hierarchy appeared in the magnitudes of the thermal widths





12

Summary

 \mathbf{M} From Lattice NRQCD calculations with two types of smeared sources within $T \in (133, 250)$ MeV, temperature dependences in correlators are presented



Mo significant changes in in-medium masses



In-medium modification is not affected by the choices of extended sources

Sequential thermal broadening





Backup

Ground state extraction



2. Excited-state contribution to the effective mass is under statistical uncertainty:

 $\frac{\log[f_1(\tau)/f_1(\tau+a)] - \log[f_0(\tau)/f_0(\tau+a)]}{E_0} < 25\% \times \frac{\delta_{M_{\text{eff}}}(\tau)}{M_{\text{eff}}(\tau)}$

Ground states are extracted by 1-state fits on correlators within $[\tau_{min}, \tau_{max}]$

P. Fritzsch, et.al., NPB 865, 397(2012)





Bottomonium system from PDG





Continuum-subtracted effective mass

Measured with wave-function optimized sources



Larger slopes for higher excited states: High excited states are more sensitive to thermal modifications



