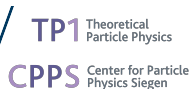


Investigating $SU(3)$ with $N_f = 8$ fundamental fermions at strong renormalized coupling

Oliver Witzel

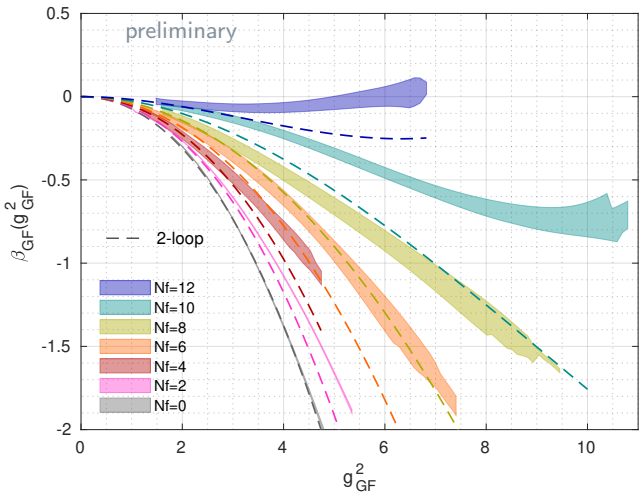
Anna Hasenfratz, Ethan Neil
(for the LSD collaboration)



41st Lattice Conference
Liverpool, United Kingdom · August 02, 2024

Landscape of SU(3)

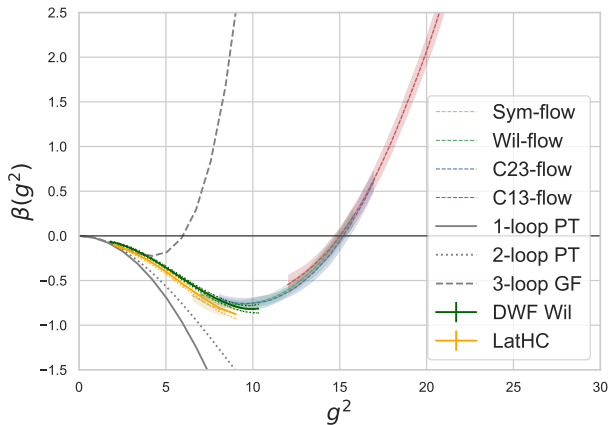
► Plot: Lattice 2023



- Simulations with stout-smear Möbius DWF and Symanzik gauge action
- Systematic effects for $N_f = 10$ likely underestimated
- Reach in g^2 limited by 1st order bulk phase transition (lattice artifact)
 - $N_f = 12$ Sign of IRFP
 - $N_f = 10$ likely turning around
- Qualitative behavior captured by 2-loop PT prediction
- 3-loop GF prediction tracks nonperturbative result longer, but then turns away showing different qualitative behavior
 [Harlander, Neumann JHEP06(2016)161]

$N_f = 10$ at strong coupling

[Hasenfratz, Neil, Shamir, Svetitsky, OW PRD 108 (2023) L071503]



▶ Simulating $N_f = 10$ with Wilson fermions and additional Pauli-Villars fields allows simulations at much stronger coupling

▶ Clear IRFP

→ $N_f = 10$ is conformal

→ Confirms $N_f = 12$ is conformal

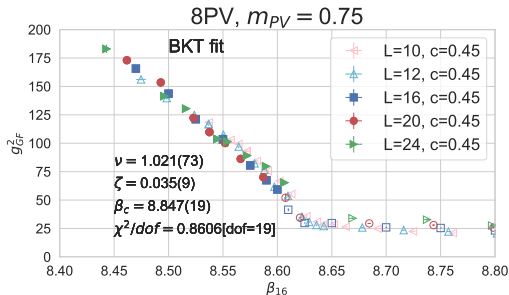
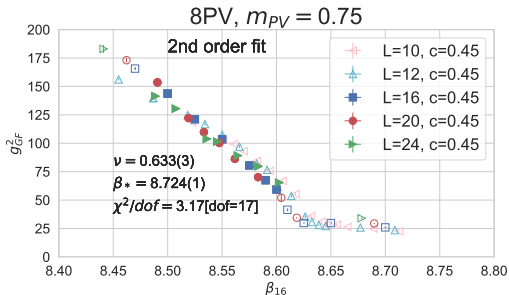
▶ What is the nature of $N_f = 8$?

▶ Where is the sill of the conformal window?

Continuous β function for $N_f = 8$ at strong coupling

- ▶ Work in progress by Hasenfratz, Peterson
- ▶ nHYP-smearred staggered fermions with additional Pauli-Villars fields
fundamental gauge action with adjoint term
- ▶ Reaching $g^2 \sim 24$
 - β function may be turning, but no sign of a fixed point
 - Simulations troubled by large topological artifacts in the gradient flow
 - Close to a phase transition?

Signs that $N_f = 8$ is special [Hasenfratz PRD 106 (2022) 014513]



► Finite size scaling

2nd order: $g^2(\beta; L; c) = f_{2nd}^{(c)} ((\beta/\beta_* - 1) L^{1/\nu})$

► BKT fit preferred for these (small volume) data

BKT: $g^2(\beta; L; c) = f_{BKT}^{(c)} (L \exp(-\zeta|\beta/\beta_* - 1|^{-\nu}))$

Simulations

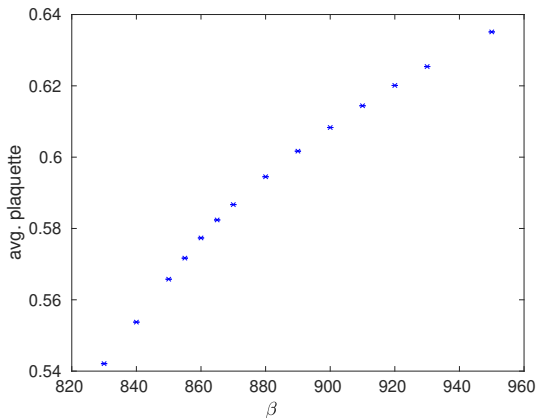
- ▶ nHYP-smearred staggered fermions
- ▶ Additional Pauli-Villars fields
- ▶ Plaquette gauge action with adjoint term

- ▶ Volume $16^3 \times 32$, $24^3 \times 64$, $32^3 \times 64$, $48^3 \times 96$
- ▶ $\beta_b = 8.10, 8.20, 8.30, 8.40, 8.50, 8.60, 8.70, 8.80, 8.90, 9.10, 9.20, 9.30, 9.50$
 - Simulations cross from weak coupling to symmetric mass generation (SMG) phase
[Hasenfratz PRD 106 (2022) 014513]

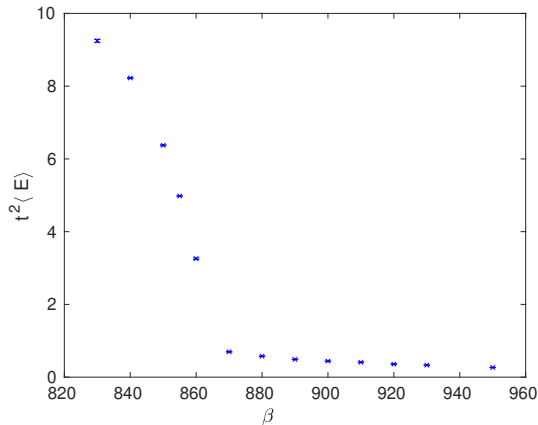
- ▶ HMC: QEX (Osborn, Jin, Peterson)
- ▶ Spectrum: MILC (DeTar et al., . . . , Schaich, Hasenfratz)
- ▶ Gauge flow: QLUA (Pochinsky et al.)

$24^3 \times 64$ ensembles

► Average plaquette



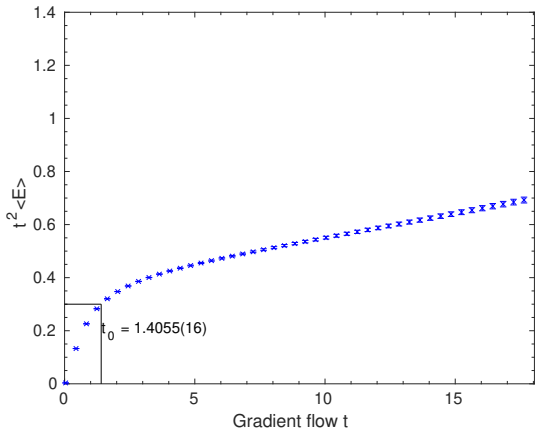
► $t^2 \langle E(t) \rangle$ at $t = L^2/32 = 18$



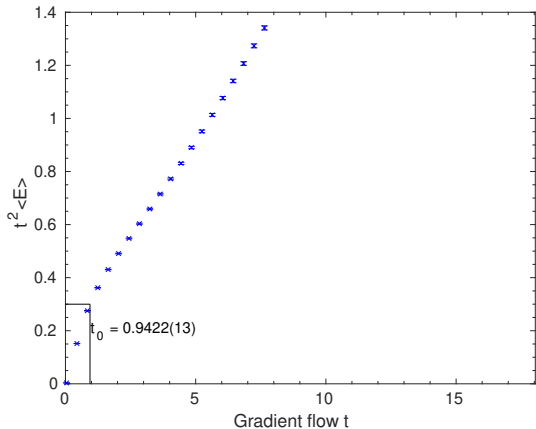
► Something interesting is happening

$t^2 \langle E(t) \rangle$ vs. t

► $\beta_b = 8.70$

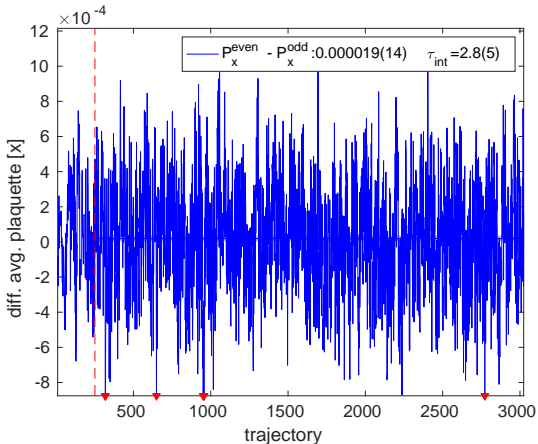


► $\beta_b = 8.60$

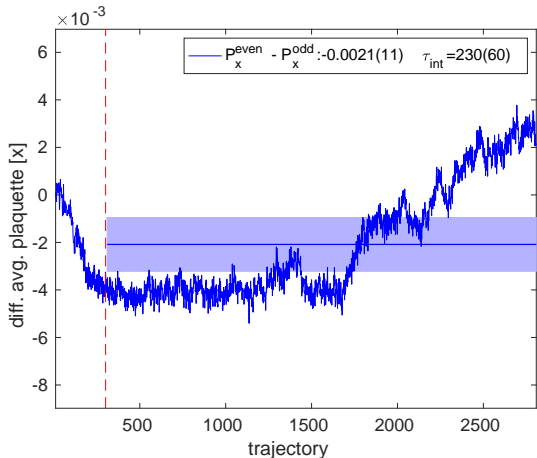


Broken symmetry between even and odd sites

► $\beta_b = 8.70$

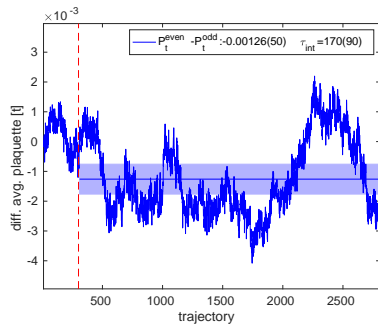
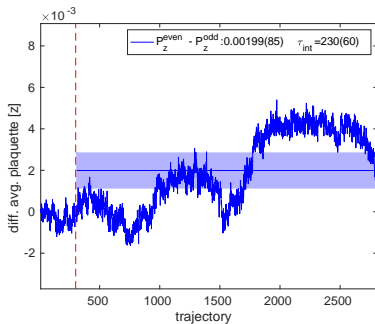
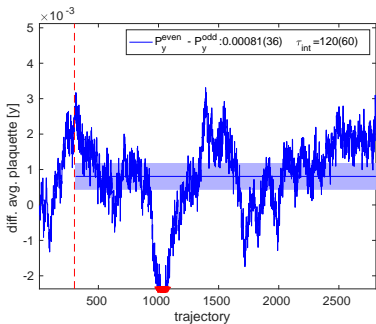


► $\beta_b = 8.60$



Broken symmetry between even and odd sites

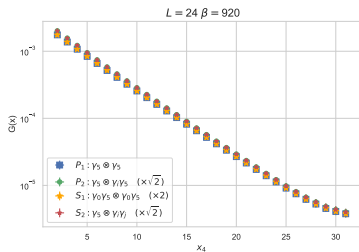
► $\beta_b = 8.60$



Pseudoscalar correlator

► Weak coupling

$\beta_b = 9.20$ (conformal)

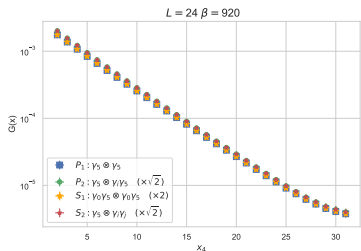


► Degenerate pseudoscalar and scalar (parity doubling)

► No taste splitting

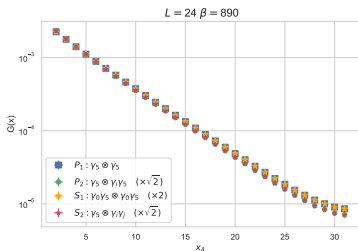
Pseudoscalar correlator

- ▶ Weak coupling
 $\beta_b = 9.20$ (conformal)



- ▶ Degenerate pseudoscalar and scalar (parity doubling)
- ▶ No taste splitting

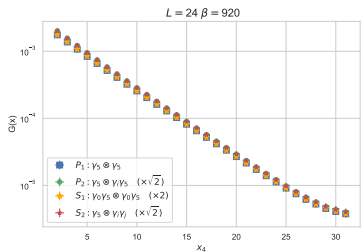
- ▶ $\beta_b = 8.90$



- ▶ Degenerate pseudoscalar and scalar (parity doubling)

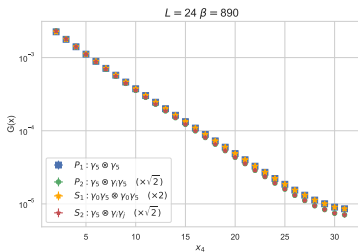
Pseudoscalar correlator

- ▶ Weak coupling
 $\beta_b = 9.20$ (conformal)



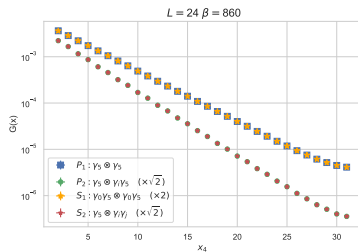
- ▶ Degenerate pseudoscalar and scalar (parity doubling)
- ▶ No taste splitting

- ▶ $\beta_b = 8.90$



- ▶ Degenerate pseudoscalar and scalar (parity doubling)

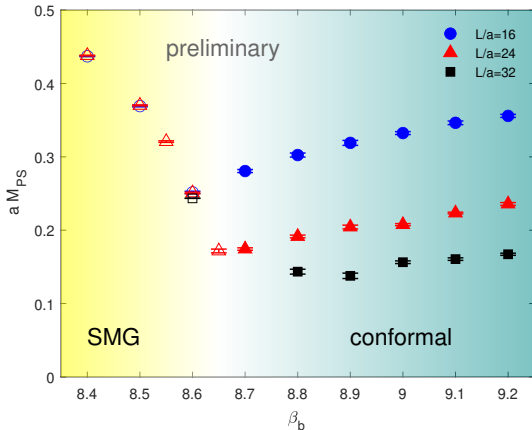
- ▶ Strong coupling
 $\beta_b = 8.60$ (SMG)



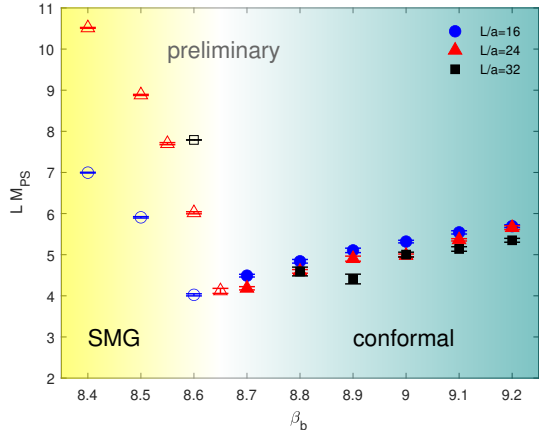
- ▶ Degenerate pseudoscalar and scalar (parity doubling)
- ▶ No chiral symmetry breaking

Pseudoscalar correlator

► aM_{PS}



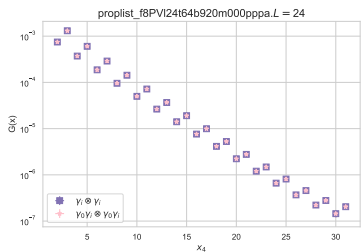
► LM_{PS}



► Conformal scaling for $\beta_b > 8.6$

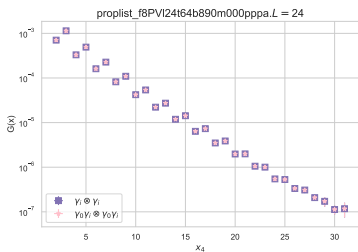
Vector correlator

- ▶ Weak coupling
 $\beta_b = 9.20$ (conformal)



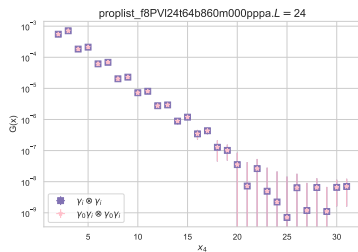
- ▶ Degenerate vector and axial (parity doubling)

- ▶ $\beta_b = 8.90$



- ▶ Degenerate vector and axial (parity doubling)

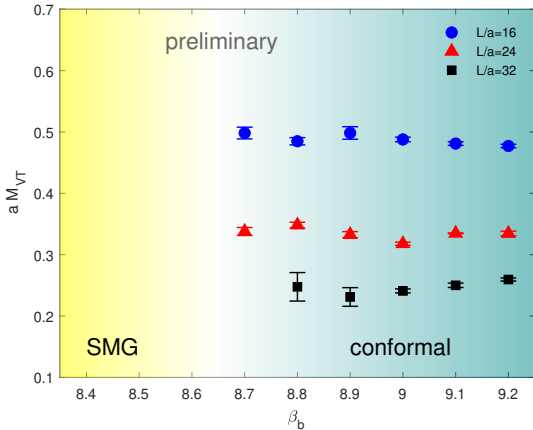
- ▶ Strong coupling
 $\beta_b = 8.60$ (SMG)



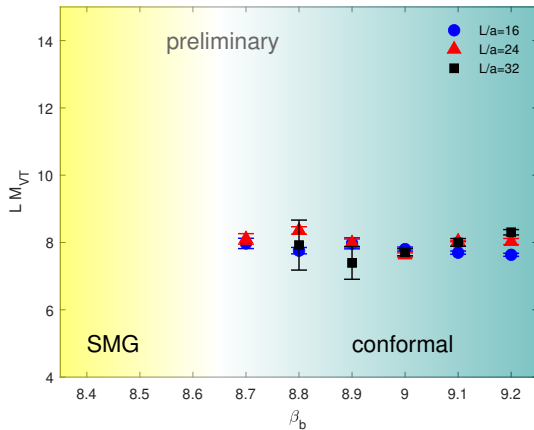
- ▶ Degenerate vector and axial (parity doubling)
- ▶ No chiral symmetry breaking

Vector correlator

► aM_{VT}

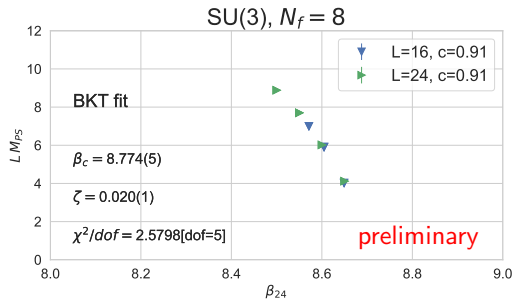
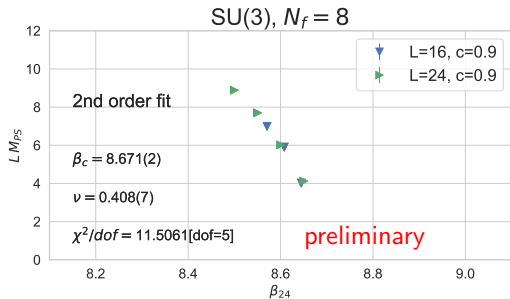


► LM_{VT}



► Conformal scaling for $\beta_b > 8.6$

Outlook: finite size scaling



► Finite size scaling

2nd order: $L \cdot m(\beta; L) = f_{2nd}^{(c)} ((\beta/\beta_c - 1) L^{1/\nu})$

BKT: $L \cdot m(\beta; L) = f_{BKT}^{(c)} (L \exp(-\zeta|\beta/\beta_c - 1|^{-\nu}))$

Summary

- ▶ Large scale simulations to test SU(3) with $N_f = 8$ fundamental flavors at strong coupling using additional Pauli-Villars fields
- ▶ Preliminary findings support picture of a conformal and an SMG phase
→ No chiral symmetry breaking
- ▶ Further simulations on larger volumes needed/planned

Acknowledgment

- ▶ Special thanks to Amitoj Singh and his team at Jefferson Lab for granting us access and early science time on the new 24s cluster