

T_{cc}^+ via plane wave approach and including diquark-antidiquark operators

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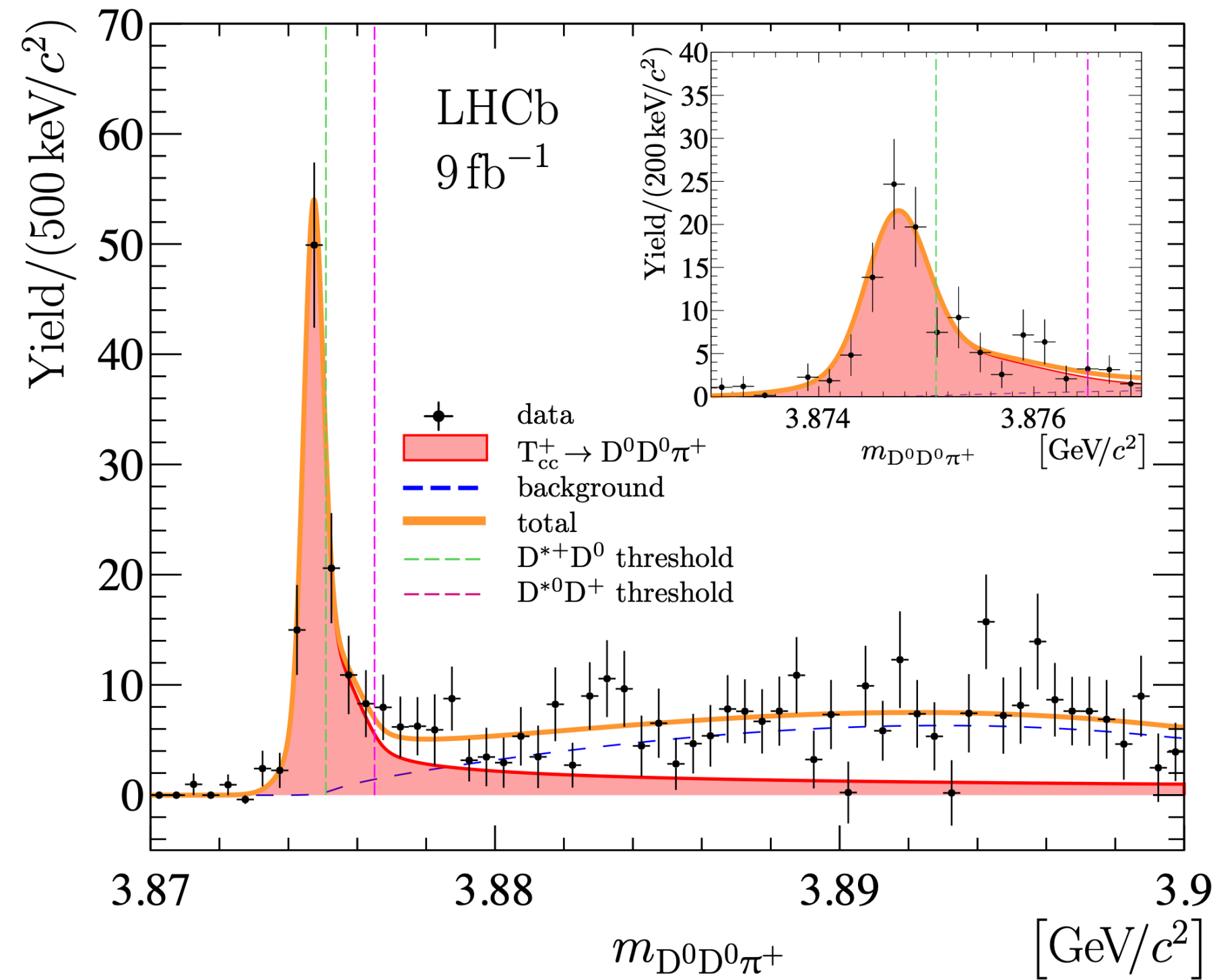
with S. Prelovsek, E. O. Pacheco, L. Leskovec, M. Padmanath and S. Collins.

A short intro

$$\delta m_{\text{pole}} = m_{T_{cc}^+} - (m_{D^{*+}} + m_{D^0}),$$

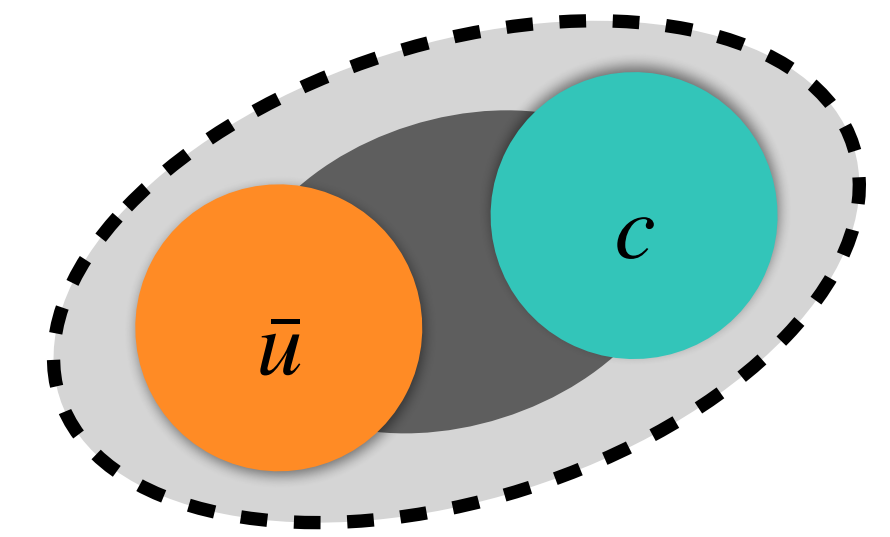
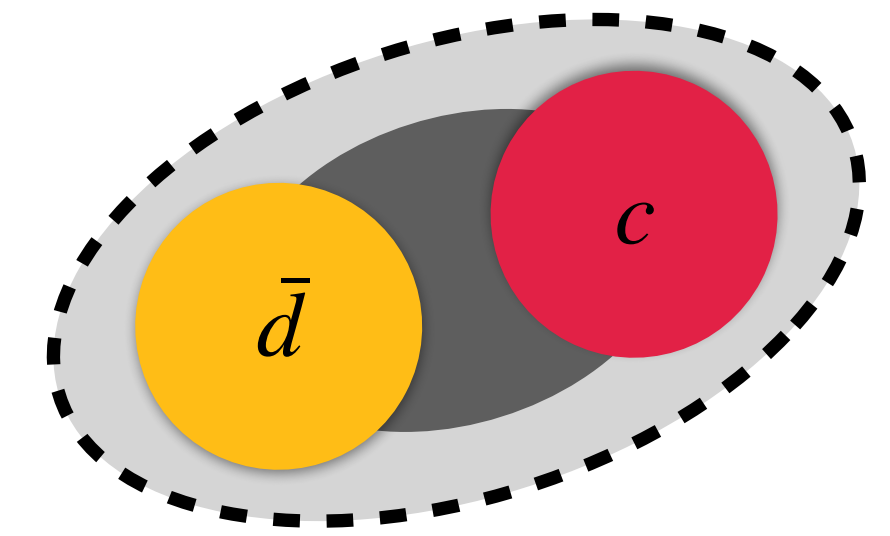
$$\delta m_{\text{pole}} = -360 \pm 40_{-0}^{+4} \text{ keV}/c^2,$$

$$\Gamma_{\text{pole}} = 48 \pm 2_{-14}^{+0} \text{ keV}$$



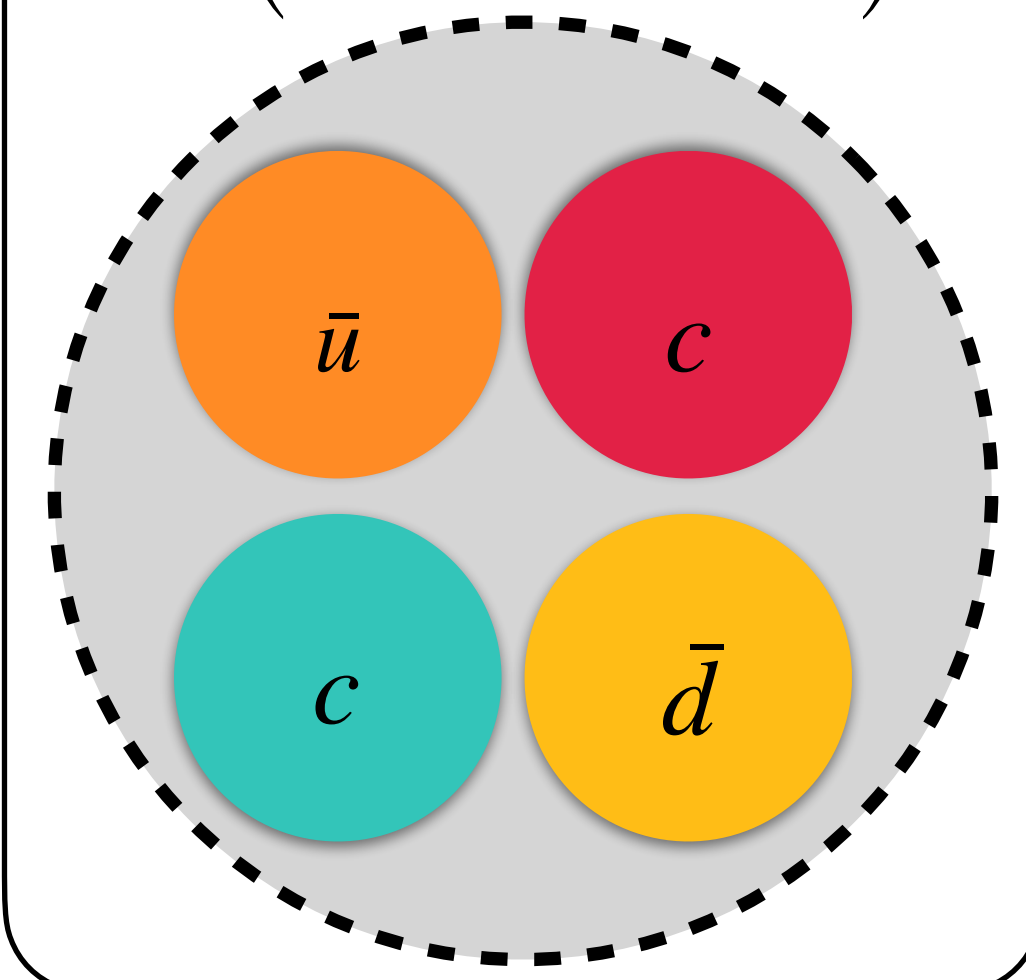
- ♦ doubly charmed tetraquark ($cc\bar{u}\bar{d}$)
- ♦ recently observed by LHCb
- ♦ most frequent approach in LQCD:

1. simulate DD^* scattering correlators
2. extract finite-volume energies
3. apply Lüscher's QC to get the amplitude



D/D^* ($J^P = 0^-, 1^-$)

T_{cc}^+ ($I(J^P) = 0(1^+)$)



Addition of diquark-antidiquark operators

❖ basic building block for the scattering operators:

$$\mathcal{O}_{I=0}^{DD^*}(\vec{p}_1, \vec{p}_2) = \sum_{\vec{x}_1, \vec{x}_2} e^{i\vec{p}_1 \cdot \vec{x}_1} e^{i\vec{p}_2 \cdot \vec{x}_2} \cdot [\bar{u}(x_1) \Gamma_V c(x_1)] [\bar{d}(x_2) \Gamma_P c(x_2)] - \{\bar{u} \leftrightarrow \bar{d}\}$$

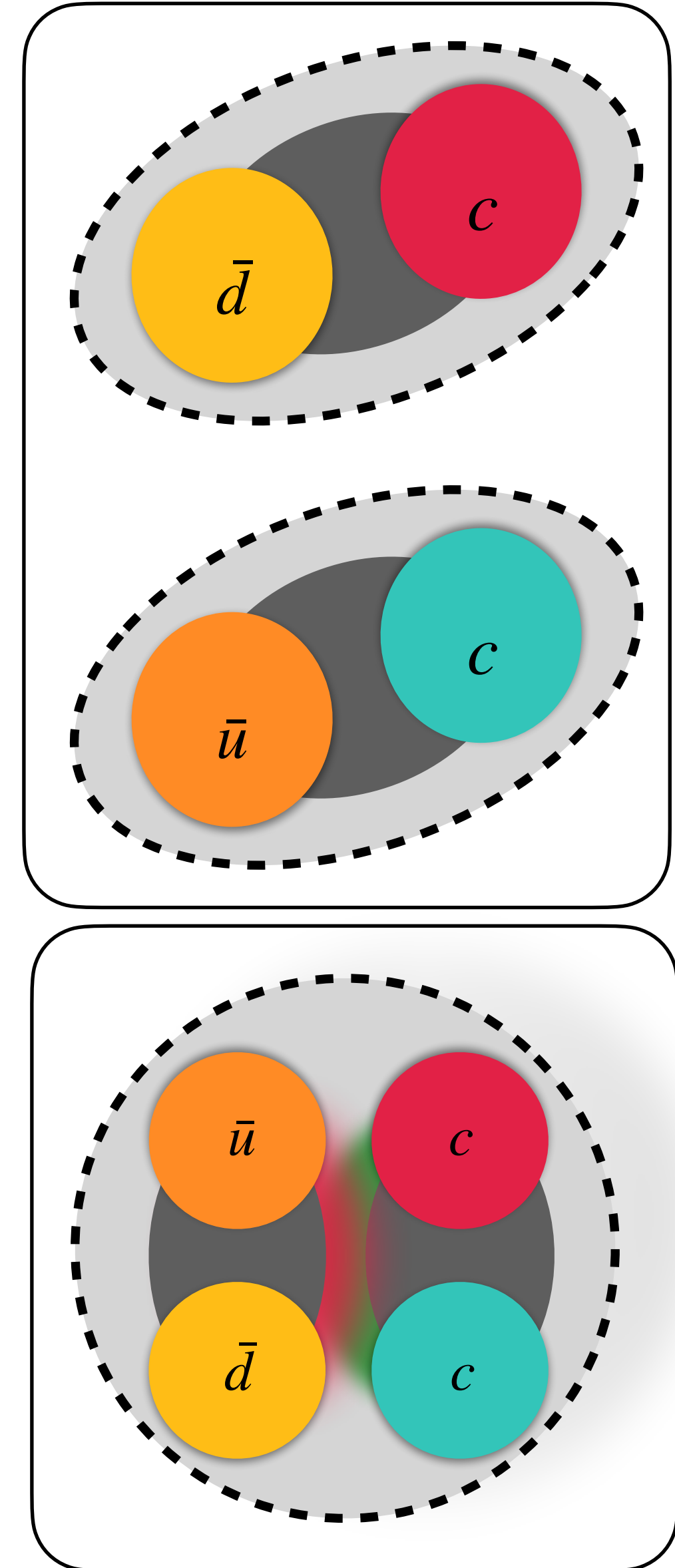
❖ inclusion of $[cc] [\bar{u}\bar{d}]_{I=0}$ operators in analysis:

$$\mathcal{O}_{I=0}^{[cc][\bar{u}\bar{d}]}(\vec{p}) = \sum_{\vec{x}} e^{i\vec{p} \cdot \vec{x}} \cdot \epsilon_{abc} \left[c_b^\alpha(x) (C\gamma_i)^{\alpha\beta} c_c^\beta(x) \right] \epsilon_{ade} \left[\bar{u}_d^\gamma(x) (C\gamma_5)^{\gamma\delta} \bar{d}_e^\delta(x) \right]$$

❖ its effects are generally dependent on the heavy-quark mass

❖ ensembles used: U101, H105 (CLS) $\left\{ \begin{array}{l} N_L = 24, 32 \\ N_f = 2 + 1 \\ m_\pi = 280(3) \text{ MeV} \\ a = 0.08636(98)(40) \text{ fm} \end{array} \right.$

- distillation $\rightarrow N_V = 60, 90$



Finite-volume energy shifts

$$m_c^{lat} \sim m_c^{phys}$$

T_1^+ operator basis

$$\mathcal{O}_1, \mathcal{O}_2 \sim D(0)D^*(0)$$

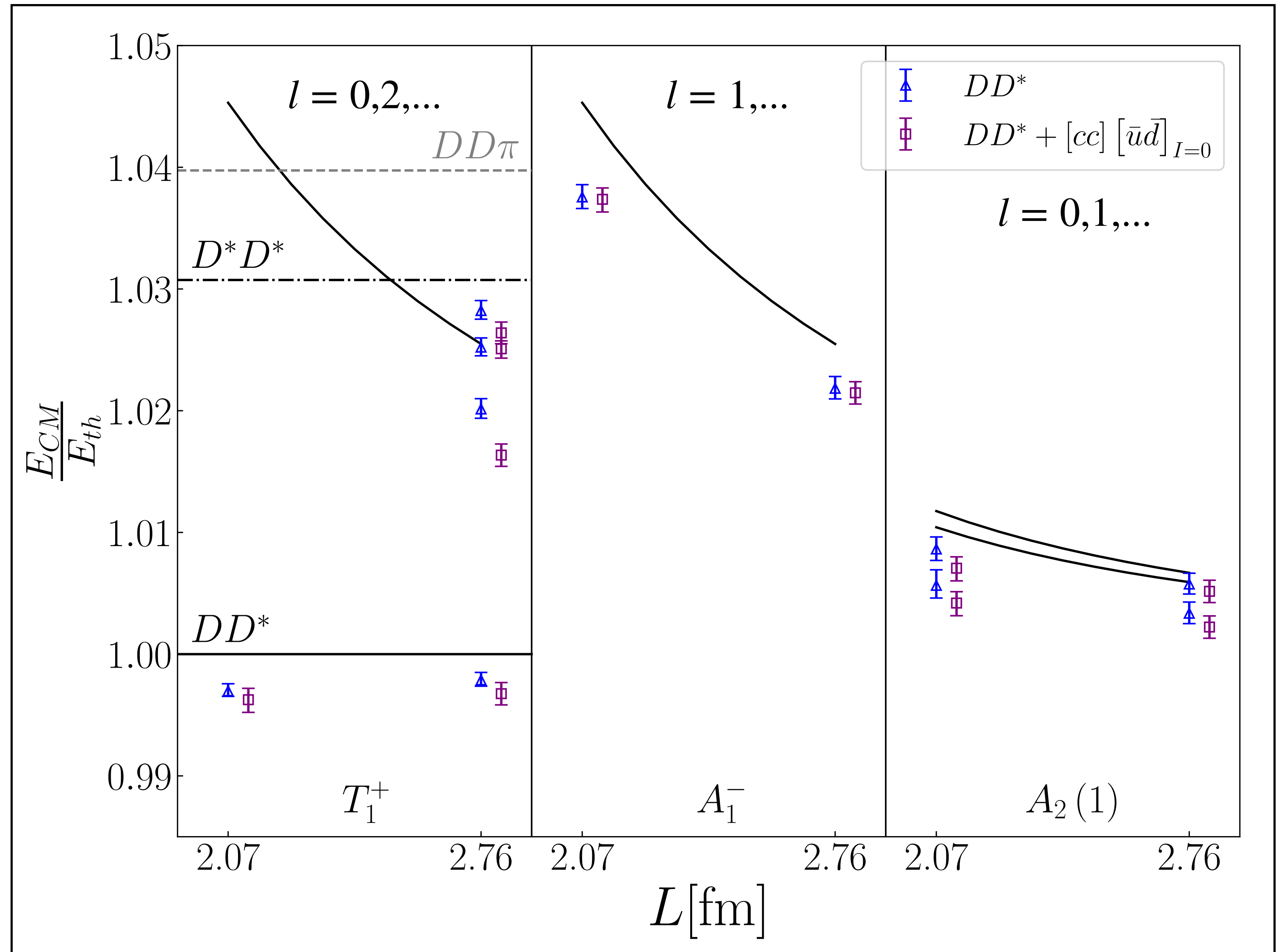
$$\mathcal{O}_3 = [D(1)D^*(-1)]_{l=0}$$

$$\mathcal{O}_4 = [D(1)D^*(-1)]_{l=2}$$

$$\mathcal{O}_5 = D^{*0}(0)D^{*+}(0)$$

$$\mathcal{O}_6 = [cc] [\bar{u}d]_{I=0}$$

Preliminary results



Overlap factors

$$Z_n^j = \langle n | \mathcal{O}_j | 0 \rangle$$

$$\mathcal{O}_1, \mathcal{O}_2 \sim D(0)D^*(0)$$

$$\mathcal{O}_3 = [D(1)D^*(-1)]_{l=0}$$

$$\mathcal{O}_4 = [D(1)D^*(-1)]_{l=2}$$

$$\mathcal{O}_5 = D^{*0}(0)D^{*+}(0)$$

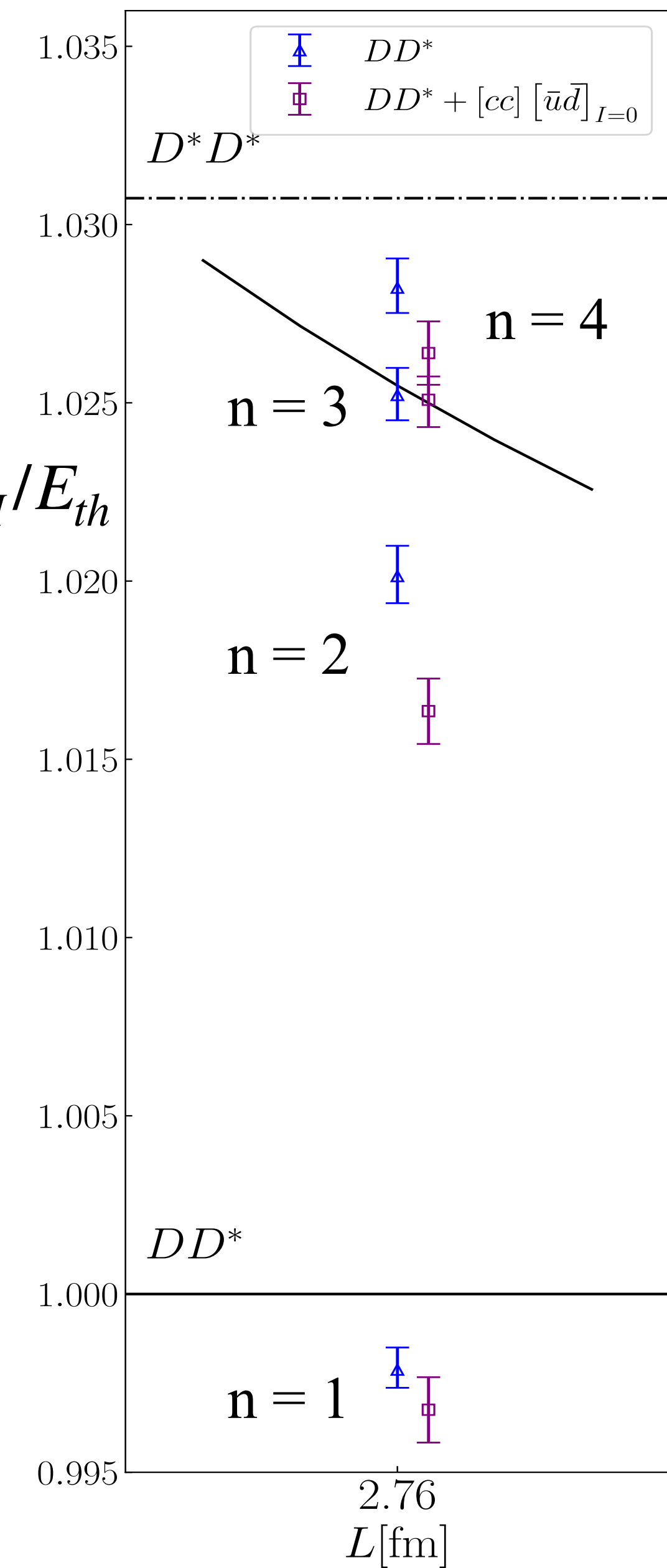
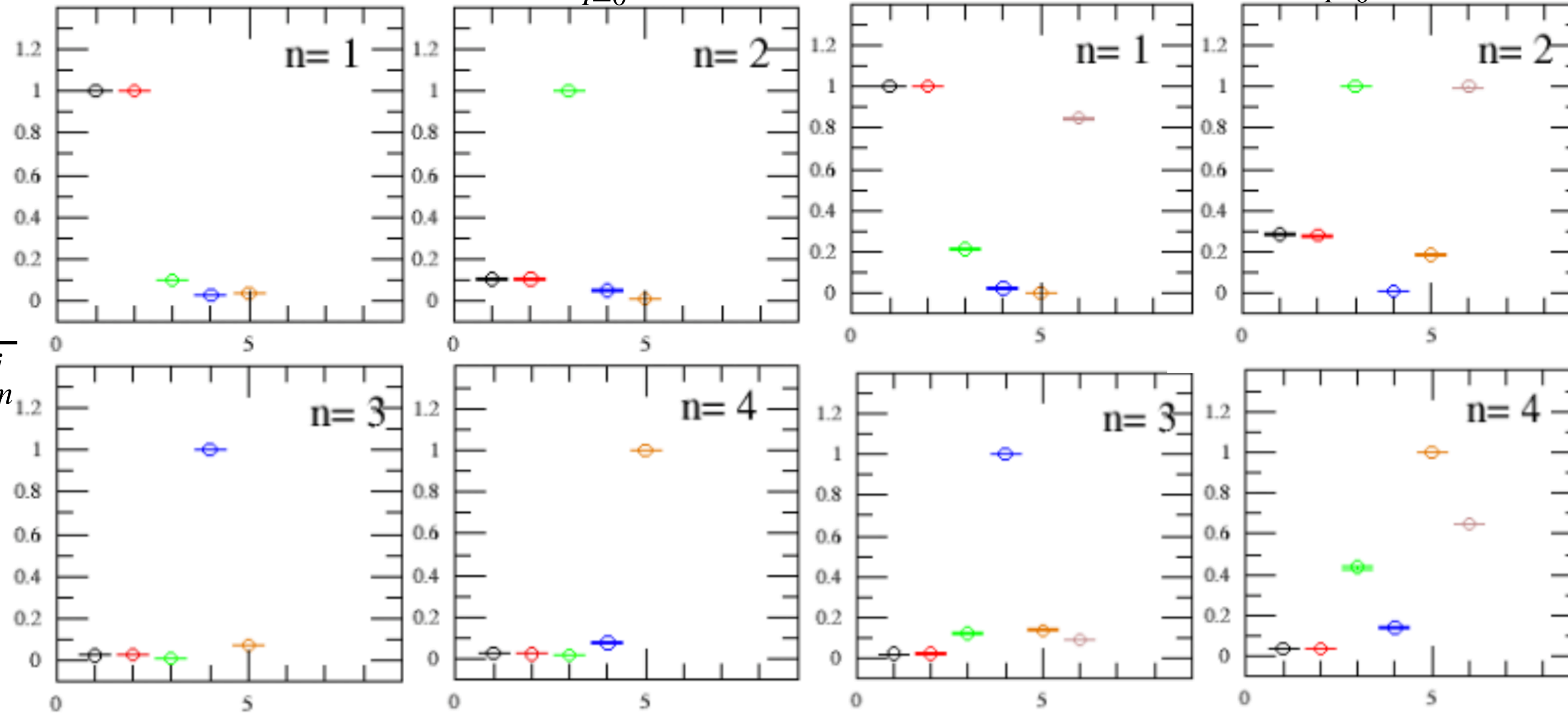
$$\mathcal{O}_6 = [cc] [\bar{u}\bar{d}]_{I=0}$$

without $[cc] [\bar{u}\bar{d}]_{I=0}$

with $[cc] [\bar{u}\bar{d}]_{I=0}$

E_{CM}/E_{th}

Z_n^i
 $\max_{j,m} Z_m^j$



❖ analysis of the results with $m_b^{lat} \sim m_b^{phys}$: $[bb] [\bar{u}\bar{d}]_{I=0}$ introduces significant mixing between BB^* and B^*B^* channels

EFT: DD^* elastic scattering

$$\mu^2 = m_\pi^2 - (m_{D^*} - m_D)^2$$

$$\vec{k} = \vec{p} + \vec{p}'$$

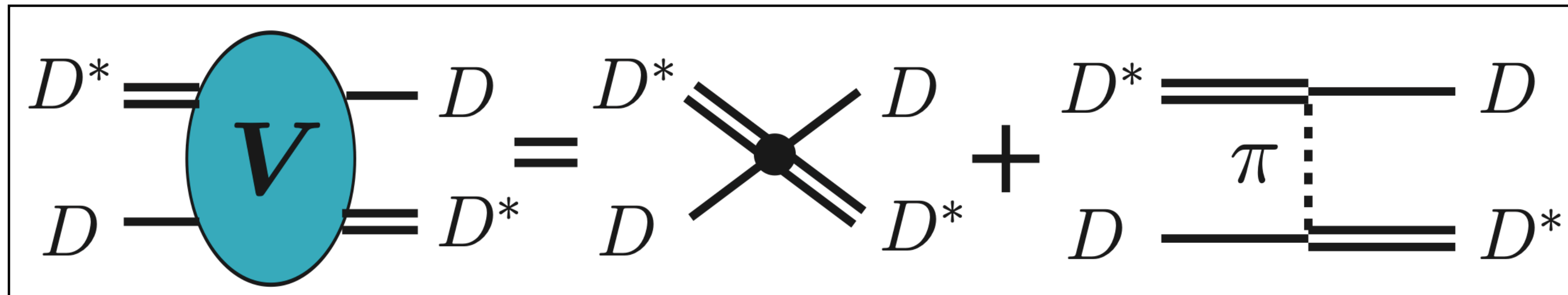
◆ effective potential V derived from chiral EFT, up to $\mathcal{O}(Q^2)$:

$$V(\vec{p}, \vec{p}') = \left(2c_{S0} + 2(\vec{p}^2 + \vec{p}'^2) c_{S2} \right) (\vec{\epsilon} \cdot \vec{\epsilon}'^*) + 2(\vec{p}' \cdot \vec{\epsilon}'^*) (\vec{p} \cdot \vec{\epsilon}) c_{P2} - \frac{3g^2 (\vec{k} \cdot \vec{\epsilon})(\vec{k} \cdot \vec{\epsilon}'^*)}{4f_\pi^2 (\vec{k}^2 + \mu^2)}$$

One pion exchange

◆ low energy constants (LECs) c_{S0} , c_{S2} , c_{P2} are treated as fit parameters

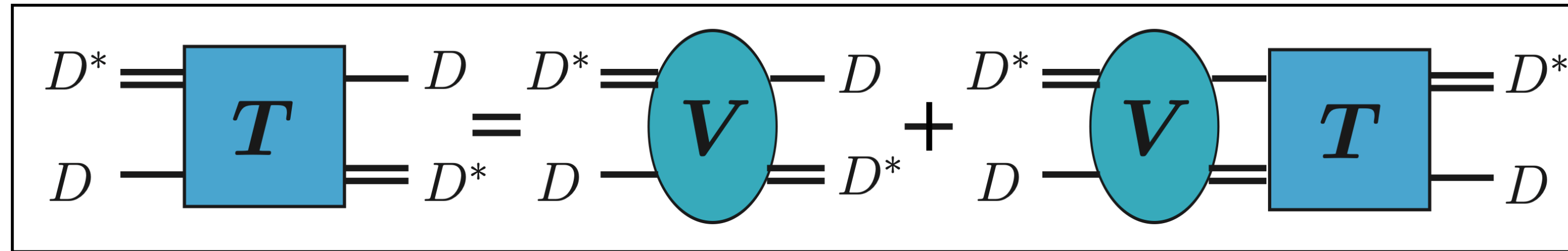
◆ we employ cutoff to each term in the potential: $F(p, p'; \Lambda, n) = \exp\left(-\frac{p^n + p'^n}{\Lambda^n}\right)$



Lippmann-Schwinger equation

$$\hat{T} = \hat{V} + \hat{V}\hat{G}\hat{T}$$

\hat{T} - scattering matrix
 \hat{V} - EFT potential
 \hat{G} - propagator



in nonrelativistic regime:

projected to various lattice irreps Λ :

poles: $\det(\hat{G}^{-1} - \hat{V}) = 0 \longrightarrow \det(\hat{H} - E\hat{I}) = 0 \longrightarrow \det(\hat{H}_\Lambda - E_\Lambda\hat{I}) = 0$

L. Meng, E. Eppelbaum, [2108.02709](#)

Plane wave basis

$$\hat{H} = \frac{\hat{p}^2}{2m_r} + \hat{V} \rightarrow \text{well defined in plane wave basis}$$

$$\vec{p} = \frac{2\pi}{L}\vec{n}, \vec{n} \in \mathbb{Z}^3$$

$$i = x, y, z$$

$$|\vec{p}_1\rangle \otimes |\vec{p}_2, i\rangle$$

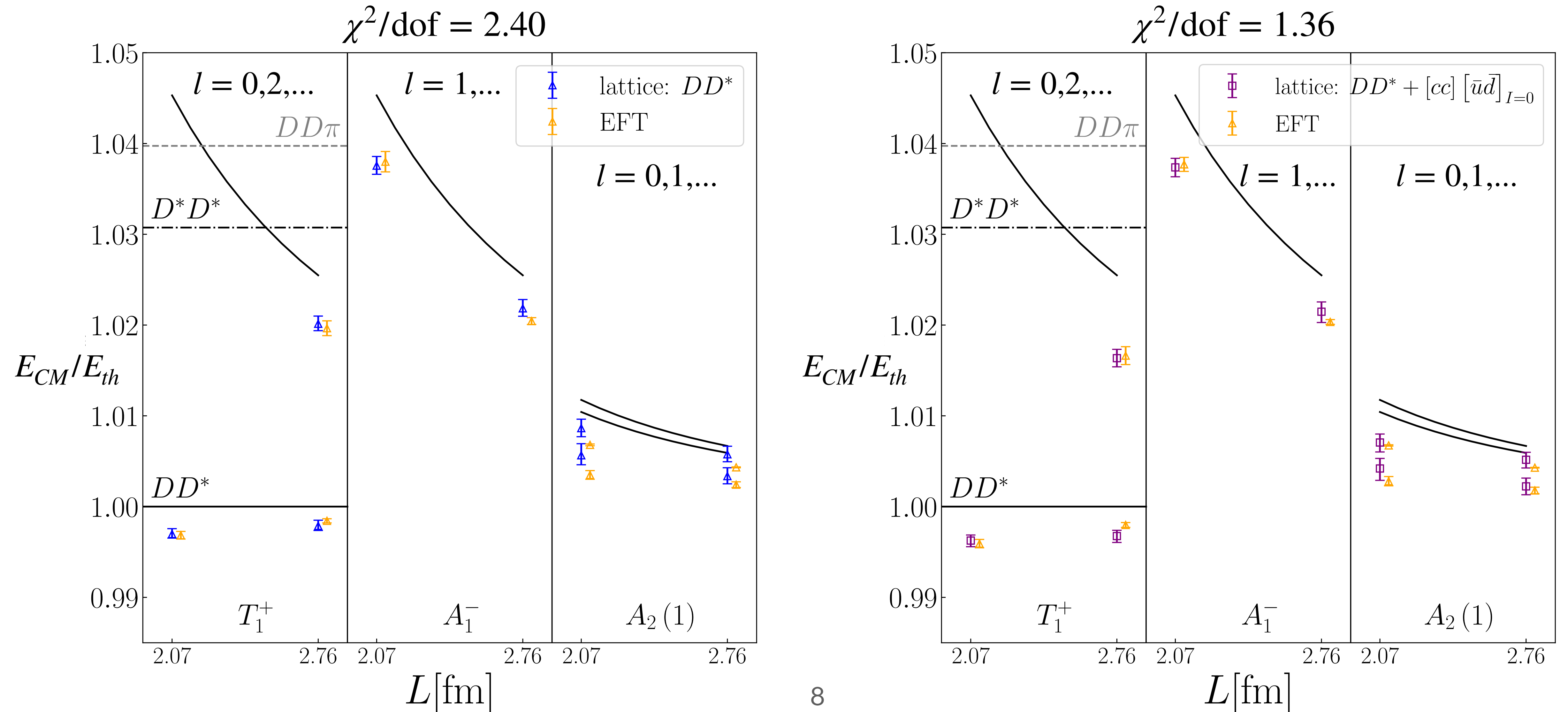
additional constraints: T_1^+, A_1^-

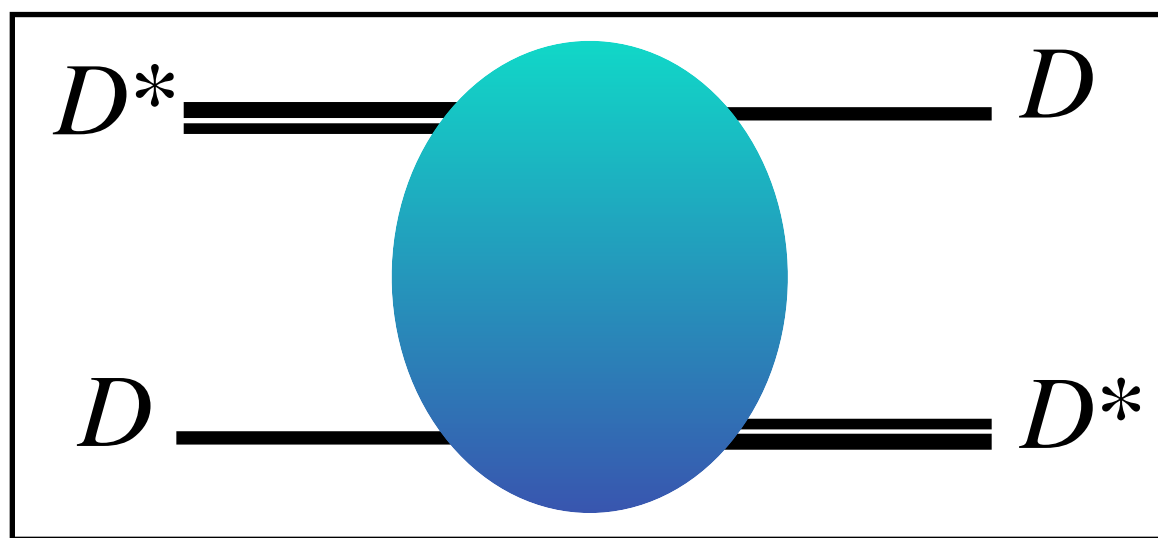
$$\vec{p}_1 + \vec{p}_2 = \vec{0}, \frac{2\pi}{L}(0,0,1) A_2(1)$$

Fitting low energy constants: C_{S0}, C_{S2}, C_{P2}

❖ sharp cutoff: $\Lambda = 0.65$ GeV, $n = 40$

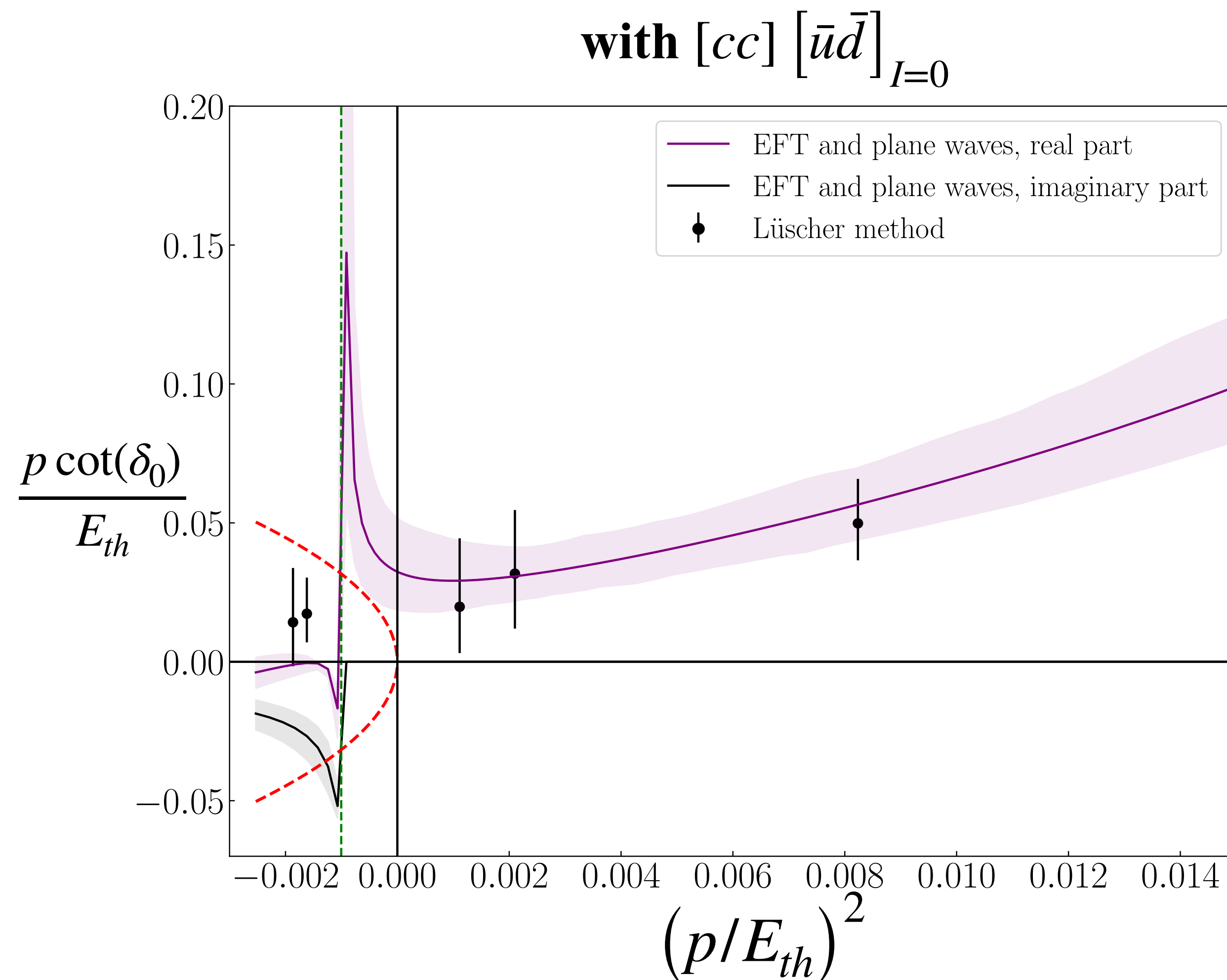
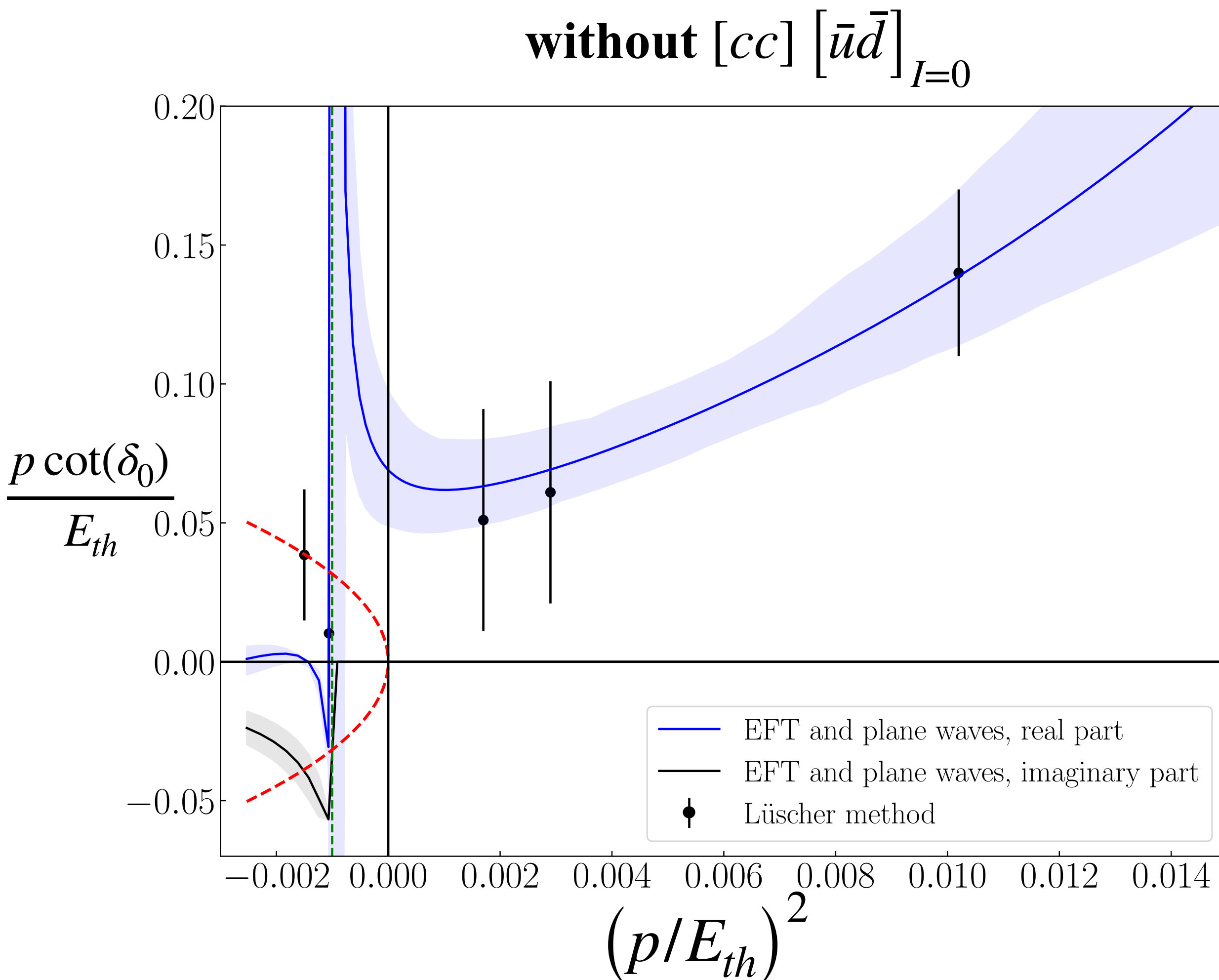
Preliminary results





Plane waves and Lüscher: a comparison

Preliminary results



T_{cc} pole

❖ subthreshold resonant state in both cases

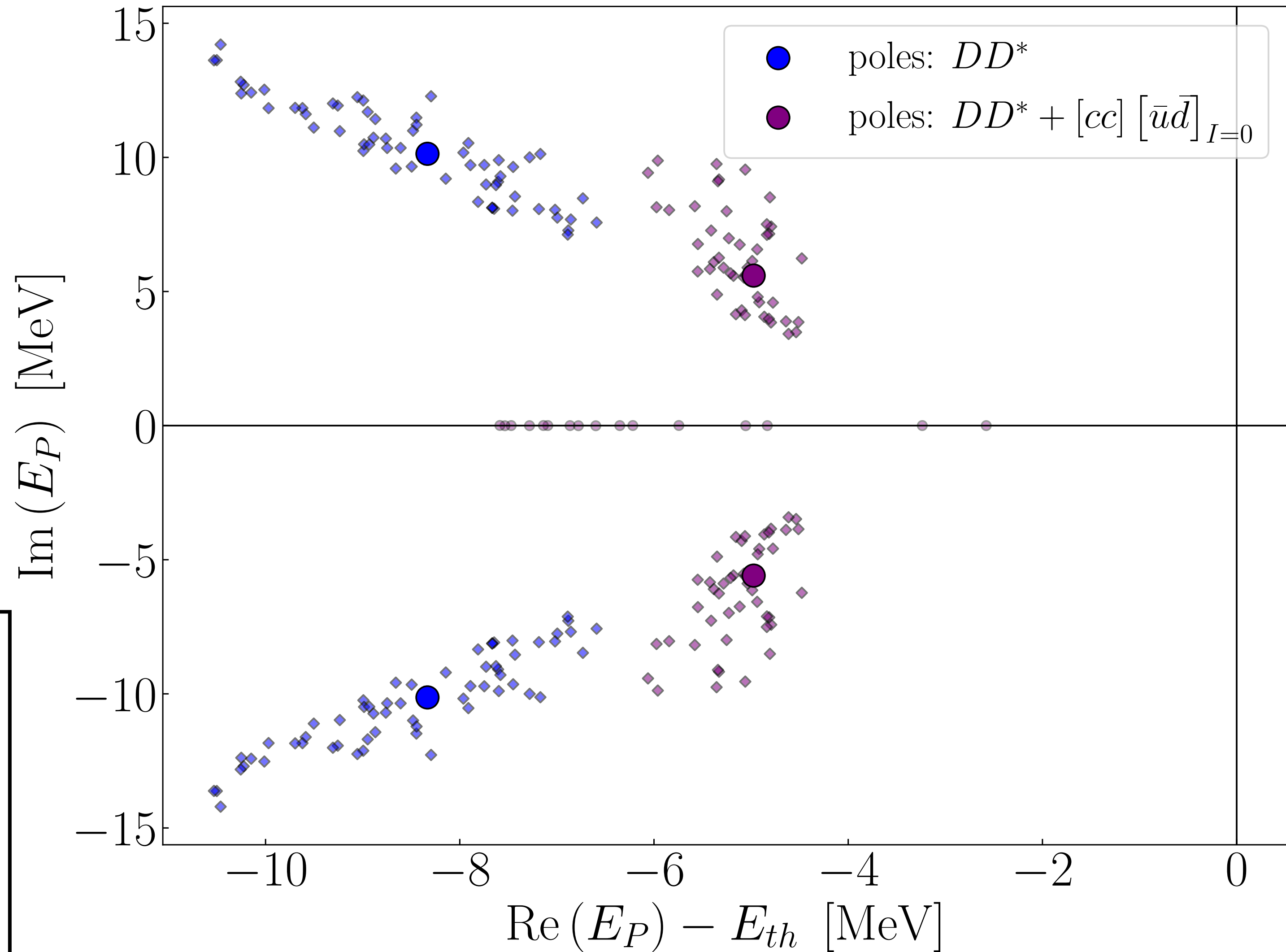
$$\text{Re}(E_P) - E_{th} = -8.33^{+1.79}_{-2.20} \text{ MeV}$$

$$\text{Im}(E_P) = -10.13^{+3.03}_{-4.07} \text{ MeV}$$

$$\text{Re}(E_P) - E_{th} = -4.99^{+0.56}_{-0.95} \text{ MeV}$$

$$\text{Im}(E_P) = -5.60^{+1.97}_{-3.55} \text{ MeV}$$

+ complex conjugate poles

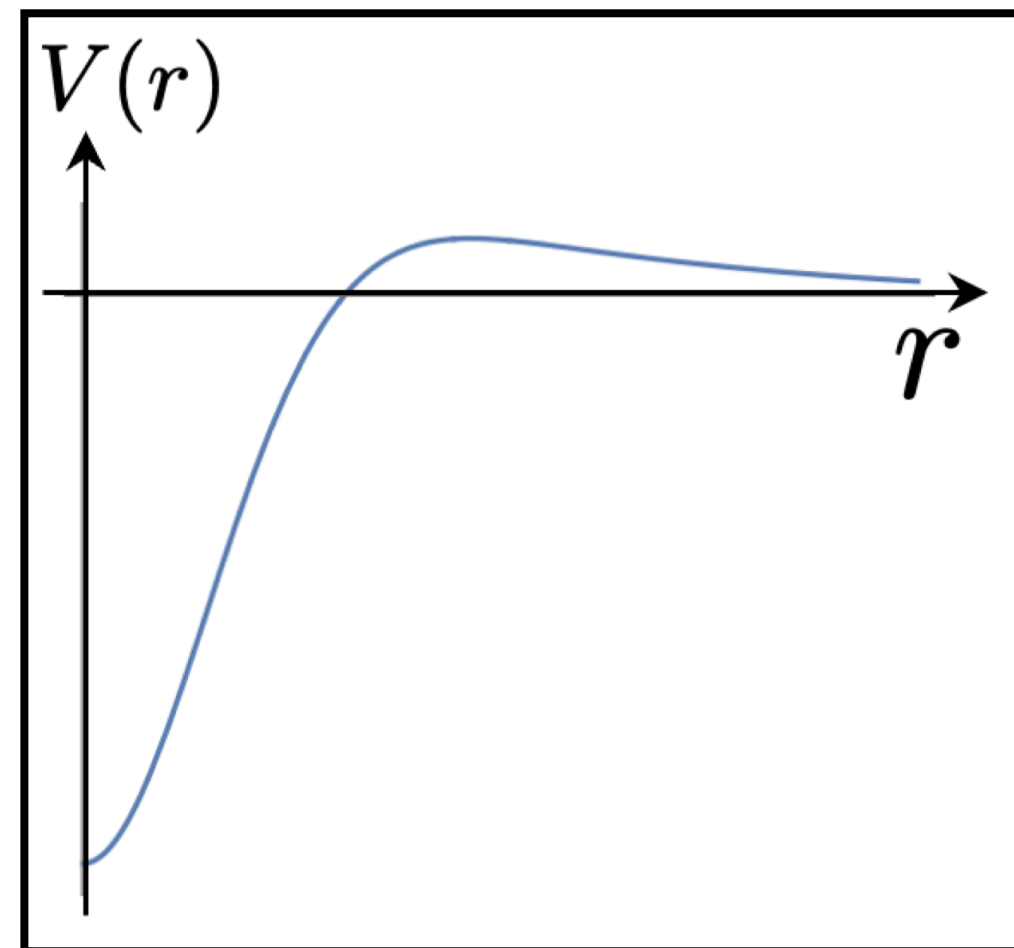


❖ Contact terms → short range attraction

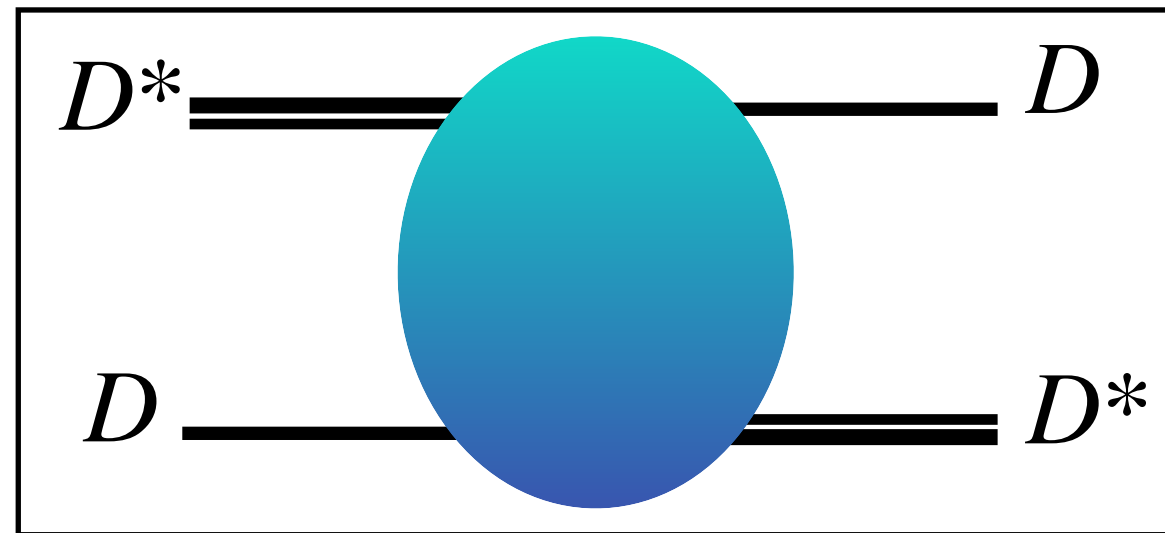
❖ One-pion exchange → long range repulsion

$$m_\pi = 280 \text{ MeV}$$

S. Collins, A. Nefediev, M. Padmanath,
S. Prelovsek; [2402.14715](#)



Summary



❖ study of the T_{cc} pole:

- addition of local diquark-antidiquark interpolators: **energy shifts, overlap factors**
- explicit accounting for the left-hand cut: **effective potential** featuring OPE
- in both cases: subthreshold resonance
 - ♦ shift towards the real line with the addition of $[cc] [\bar{u}\bar{d}]_{I=0}$

