

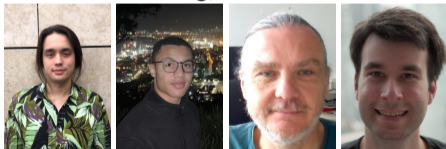


# Accelerating Metadynamics

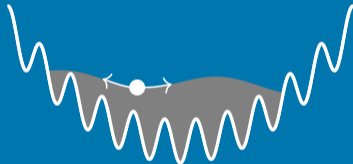
...with an eye on full QCD

[PhysRevD.109.114504]/[2307.04742]

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## Extending Metadynamics to QCD

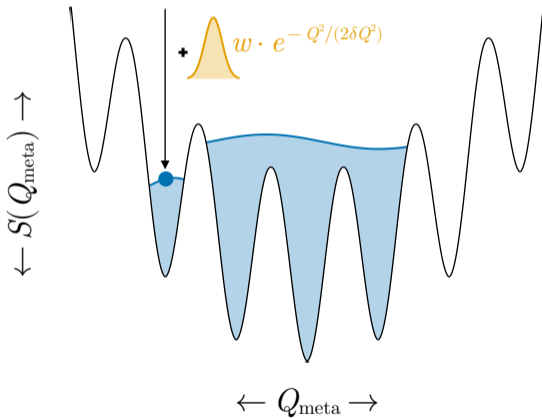
Reminder from previous talk...

- No conceptual difficulties
- HMC already required for dynamical fermions
- Stout smearing often used for fermions
- Compared to fermionic force calculation (especially at physical quark/pion masses), overhead is negligible
- **Buildup of potential may take too long**
  - ⇒ Have to accelerate buildup as much as possible

# Building a Metadynamics Bias Potential

Buildup speed determined by three parameters:

- Bin width  $\delta Q$  more or less bounded from above by the standard deviation of the collective variable in unbiased simulations (within a sector)
- Gaussian weight  $w$  has to be chosen while weighing speed against smoothness
- CV-space interval  $[Q_{\min}, Q_{\max}]$  does not have to be large (keyword: *bias modification*)





# Speeding up the Bias Thermalization

## 1. Make use of known charge parity symmetry $Q \leftrightarrow -Q$

- In practice: Whenever we update the bias potential at some  $Q_{\text{meta}}$  we also update it at  $-Q_{\text{meta}}$   
⇒ approx. 2x speed-up



# Speeding up the Bias Thermalization

## 2. Well-tempered Metadynamics [Barducci' 08]

- Standard Metadynamics

$$V_{t+1}(Q) = V_t(Q) + w \exp\left(-\frac{(Q_t - Q)^2}{2\sigma^2}\right)$$

- Well-tempered Metadynamics

$$V_{t+1}(Q) = V_t(Q) + \exp\left(-\frac{V_t(Q)}{\Delta T}\right) w \exp\left(-\frac{(Q_t - Q)^2}{2\sigma^2}\right)$$

Tunable parameter  $\Delta T$ :

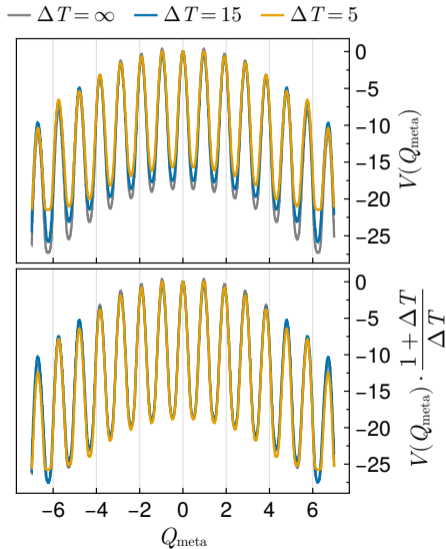
- $\Delta T \rightarrow 0$ : No Metadynamics
- $\Delta T \rightarrow \infty$ : Standard Metadynamics



# Speeding up the Bias Thermalization

## 2. Well-tempered Metadynamics [Barducci' 08]

- Able to choose larger  $w$  while maintaining smoothness in the end
- Quirk: Bias does not converge to  $-S(Q)$  but  $-\frac{\Delta T}{1+\Delta T}S(Q)$   
 $\hookrightarrow$  One has to be careful so as not to decrease the barrier height too much





# Speeding up the Bias Thermalization

## 3. Multiple walkers [Raiteri' 06]

- Run  $N_{\text{walkers}}$  simulation streams in parallel, all working on the same potential
- Minimal communication between processes required (e.g., a single `MPI.Allgather` call per iteration)  
↳ speed-up of factor  $\sim N_{\text{walkers}}$
- **Possible Enhancement:** Start each walker in a different topological sector to eliminate time before falling into unexplored sector



## Speeding up the thermalization

Some strategies not mentioned in this talk and/or not explored so far:

- On-the-fly parametric optimization (**complicated**)
- Alternative biased sampling methods, e.g., OPES [**Parrinello' 20**] (**so far only slightly ahead of MetaD in some cases, but might become very useful**)
- Using information from previous simulations on coarser lattices (**unexplored**)





## Question to be Answered

Do these improvements enable us to use PT-MetaD in full QCD?



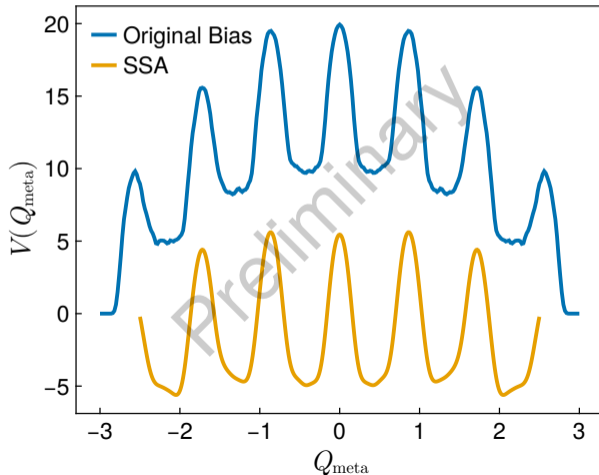
## First Unquenched Case Study

- Fermion Action:  $4 \times 0.125$  Stout-smearred Staggered,  $N_f = 2$  @  $am = 0.02$
- Gauge Action: DBW2 @  $\beta = 1.05$   
 $\hookrightarrow a^{-1} \approx 3.5\text{-}4$  GeV
- Lattice Volume:  $(16a)^4 \approx (0.8 \text{ fm})^4$
- Collective Variable: Clover-Charge with  $6 \times 0.12$  Stout smearing
- Bias parameters:  $\delta Q = w = 0.02$ ,  $\gamma = \infty$ ,  $[Q_{\min}, Q_{\max}] = [-3, 3]$  and 6 walkers



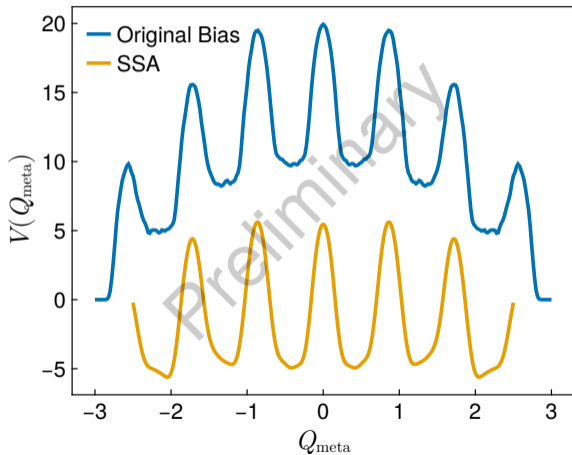
## First Unquenched Case Study — Bias Potential

Bias potential after 5000 HMC trajectories per walker:





## First Unquenched Case Study — Bias Potential

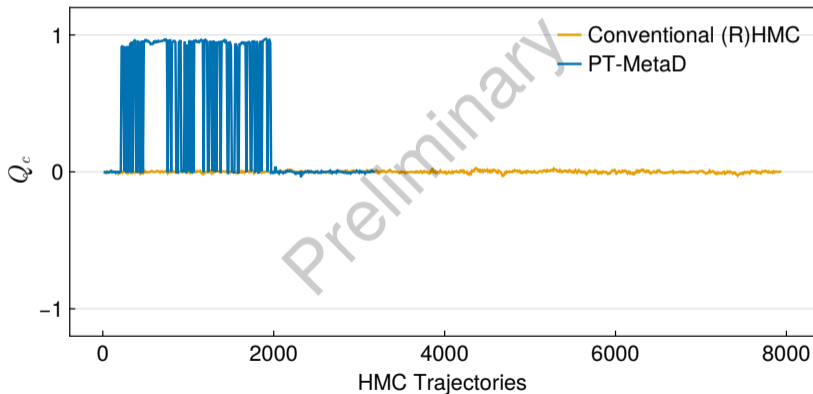


- Very similar shape to pure gauge bias potentials
- Broader valleys most likely caused by longer, possibly excessive, smearing ( $4 \times 0.12 \rightarrow 6 \times 0.12$ )
- *Maybe possible to guesstimate unquenched potentials from quenched ones?*



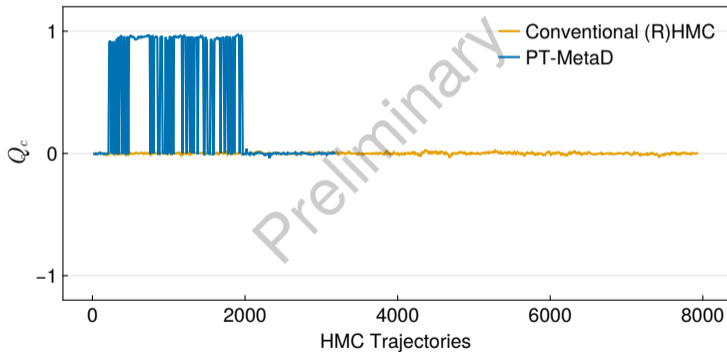
## First Unquenched Case Study — PT-MetaD

PT-MetaD successfully unfreezes the system:





## First Unquenched Case Study — PT-MetaD



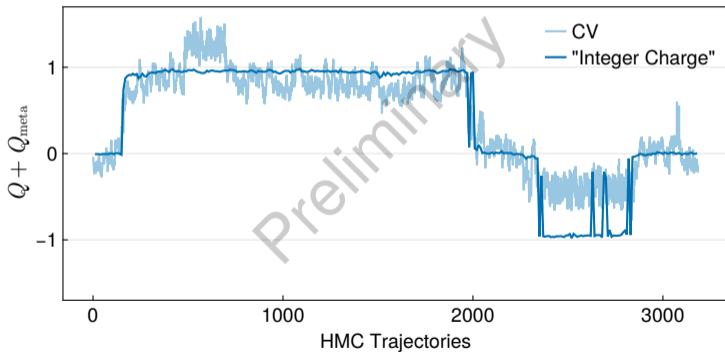
### Important to stress:

- All streams use the exact same gauge and fermion actions
  - ↔ swap probability only depends on the difference in the bias potential
- Only **2** streams required to facilitate tunneling



## First Unquenched Case Study — PT-MetaD

Summed timeseries of measurement stream and biased stream:



- More effective tunneling events than we see in the measurement stream
- Biased stream steps into transition regions, but jumps back instead of tunneling through  
⇒ more tuning of the bias potential required  
(*Better CV and/or higher resolution*)



## Summary

- Bias thermalization time can be significantly reduced by combining multiple strategies
- Time scales make it reasonable to use Metadynamics in full QCD  
(*Further improvements certainly desired and possible*)
- Preliminary case study shows **successful unfreezing in full QCD** using Staggered Fermions

### Outlook

- Scaling of autocorrelation times
- Usage in  $SU(N)$  theories and/or with chiral fermions, where topological freezing is even more problematic





## Quick Aside...

In case you missed it, check out [\[part 1 of this talk\]](#) by Timo Eichhorn (Thu 9:20)

### How was this data generated?

- In-house written Lattice QCD code written in Julia, mainly for prototyping, inspired by [\[LatticeQCD.jl\]](#) by Akio Tomiya et al.:



[\[MetaQCD.jl\]](#) "dirac" branch (still being developed)



# Backup