Primordial black hole probes of heavy neutral leptons

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Based on arXiv:2405.00124,

in collaboration with Yuber F. Perez-Gonzalez and Valentina De Romeri

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In arXiv:2405.00124, we estimated the **sensitivity of IceCube** to **Heavy Neutral Leptons** (HNLs) decays from a 100s **Primordial Black Hole** (PBH) **burst**

Theoretical framework

$$\left. \frac{dN^{i}}{dEdt} \right|_{\text{prim}} = \frac{g_{i} \Gamma \left(M_{\text{PBH}}, E_{i} \right)}{2\pi \left(\exp \left\{ \frac{E_{i}}{T_{\text{PBH}}} \right\} - (-1)^{2s_{i}} \right)}$$



Figure 1: Primary spectrum of γ and ν from a 10⁸ g PBH ($T_{\rm PBH} \sim 10^5$ GeV) with BlackHawk v2.3 (Arbey&al.2019)

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ight|_{
m prim} = rac{g_i \Gamma\left(M_{
m PBH}, E_i
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 - → also BSM particles, as Heavy Neutral Leptons (HNLs)!

Hawking, Nature 248 (1974) 30-31 Carr et al., Ann. Rev. Nucl. Part. Sci. 70 (2020) Carr et al. Rept.Prog.Phys. 84 (2021) 11, 116902 Arbey et al., Eur. Phys. J. C 79 no. 8, (2019) 693

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- \Box Very massive particles *i* can be emitted, up to $m_i \sim T_{PBH}$
 - → also BSM particles, as Heavy Neutral Leptons (HNLs)!
- \Box 1 PBH with $M_{\rm PBH}^{in} \sim 10^{15} {\rm g},$ exploding now in a 100s burst $(M_{\rm PBH}^{now} \sim 6.2 \times 10^9 {\rm g})$

Hawking, Nature 248 (1974) 30-31 Carr et al., Ann. Rev. Nucl. Part. Sci. 70 (2020) Carr et al. Rept.Prog.Phys. 84 (2021) 11, 116902 Arbey et al., Eur. Phys. J. C 79 no. 8, (2019) 693

Abdullahi et al., J. Phys. G 50 no. 2, (2023) 020501

 $\hfill\square$ Phenomenological study: 1 HNL

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□ Lepton mixing matrix:

$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \end{pmatrix}$$

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 \Box 1 $|U_{\alpha4}|^2 \neq 0$ at time: 1:0:0, 0:1:0, 0:0:1

Abdullahi et al., J. Phys. G 50 no. 2, (2023) 020501

Looking for HNLs signatures at IceCube

□ Photons are a smoking gun of PBH burst

H.E.S.S. Collaboration, ICRC2013, p. 0930. 7 (2013) Milagro et al., Astropart. Phys. 64 (2015) 4-12 HAWC Collaboration, JCAP, 04 (2020) 026 Fermi-LAT Collaboration, Astrophys. J., 857, no. 1, (2018) 49 VERITAS Collaboration, PAS ICRC2017, (2018) 691 Carr et al., Rep., Prog. Phys. 84, 116902 (2021) Perez-Gonzalez, PRD 108 no. 8, (2023) 083014 H.E.S.S. Collaboration, JCAP 04 (2023) 040 IceCube Collaboration, PRL, 124 no. 5, (2020) 051103 □ Photons are a smoking gun of PBH burst

→ 1 PBH at d_{PBH} ≤ 1 pc compatible with constraints from gamma-ray bursts searches (H.E.S.S., Milagro, VERITAS...) and overdensities (Carr&al.2021 and Perez-Gonzalez2023)

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Looking for HNLs signatures at IceCube



Figure 2: IceCube Neutrino Observatory. Credits: the IceCube collaboration

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□ HNLs decay into muonic neutrino might produce a visible excess at IceCube

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Analysis and Results

$$\left. \frac{dN_{\nu_{\mu}}}{dE} \right|_{\rm SM} = \left. \frac{dN_{\nu_{\mu}}}{dE} \right|_{\rm prim} + \left. \frac{dN_{\nu_{\mu}}}{dE} \right|_{\rm sec}$$

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$$\frac{dN_{\nu\mu}}{dE}\Big|_{\text{HNL}} = \begin{cases} \left. \frac{dN_{\nu\mu}}{dE} \right|_{\nu_4 \to \nu\nu\nu} + \left. \frac{dN_{\nu\mu}}{dE} \right|_{\nu_4 \to \nu\pi}, & \text{if } m_4 \in [0.1, 1] \text{ GeV} \\ \\ \left. \frac{dN_{\nu\mu}}{dE} \right|_{\nu_4 \to H/Z\nu} + \left. \frac{dN_{\nu\mu}}{dE} \right|_{\nu_4 \to W\mu}, & \text{if } m_4 \in [0.5, 2] \text{ TeV} \end{cases}$$

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Quick example of expected signal $\frac{dN_{\nu\mu}}{dE}\Big|_{\text{SM+HNL}}$



Figure 2: Total time-integrated spectrum (HNL + SM) of ν_μ at the Earth for $\tau=$ 100s for two test-masses and 0:1:0; arXiv:2405.00124





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 \Box We evaluated the ${\bf expected}\ {\bf number}\ {\bf of}\ \nu_{\mu}$ at IceCube emitted in a 100s PBH burst from HNL + SM

IceCube Collaboration, PRL, 124 no. 5, (2020) 051103

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IceCube Collaboration, PRL, 124 no. 5, (2020) 051103

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- \Box We estimated the IceCube sensitivities to HNL decays from a 100s PBH burst with a simple χ^2 analysis

IceCube Collaboration, PRL, 124 no. 5, (2020) 051103



Figure 3: IceCube sensitivity to HNLs from a PBH burst lasting 100s; arXiv:2405.00124



Figure 4: Expected IceCube sensitivity at 90% CL for a 100s PBH burst; arXiv:2405.00124

Conclusions

- \Box We evaluated the ν_{μ} signal at IceCube from the decay of HNLs emitted in a 100s PBH burst
 - → Two HNL mass ranges: [0.1-1] GeV and [0.5-2] TeV
 - → Three mixing scenarios: ν_e , ν_μ or ν_τ mixing with ν_4 , i.e. 1:0:0, 0:1:0, 0:0:1

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- \Box In the [0.5-2] TeV range, 0:1:0 even at 2.5 $\times\,10^{-4}$ pc
- \Box IceCube would be able to set stringent constraints on m_4 and $|U_{\alpha 4}|^2$

Thanks for your attention!



Questions?

Backup slides

Bounds on exploding PBHs - I

- Photons are a smoking gun of exploding PBHs
 - → constraints on searches for gamma-ray bursts from H.E.S.S., Milagro, VERITAS, Fermi-LAT, HAWK

□ Strongest constraint on the PBH burst rate from H.E.S.S. collaboration

 $\dot{n}_{\rm PBH} \sim 2000 {\rm pc}^{-3} {\rm yr}^{-1}$ \Box Bounds on **overdensities** (Carr&al.2021 + Perez-Gonzalez2023): $\begin{pmatrix} -\beta' \\ -\gamma \end{pmatrix} \begin{pmatrix} 10^{15} {\rm gr} \end{pmatrix}$

$$n_{\mathrm{PBH}} \lesssim 0.35 \left(rac{eta'}{10^{-29}}
ight) \left(rac{10^{15} \mathrm{ g}}{M_{\mathrm{PBH}}^{\mathrm{in}}}
ight) \mathrm{pc}^{-3},$$

In 1pc^3 for $\beta' \leq 10^{-29}$ we expect \sim 1.5 exploding PBH

 \Box Hence, expecting 1 PBH at $d_{\mathrm{PBH}} \leq 1$ pc from Earth is compatible with bounds

H.E.S.S. Collaboration, ICRC2013, p. 0930. 7 (2013)

Milagro et al., Astropart. Phys. 64 (2015) 4-12

HAWC Collaboration, JCAP, 04 (2020) 026

Fermi-LAT Collaboration, Astrophys. J., 857, no. 1, (2018) 49

VERITAS Collaboration, PoS ICRC2017, (2018) 691

Carr et al., Rep., Prog. Phys. 84, 116902 (2021)

Perez-Gonzalez, PRD 108 no. 8, (2023) 083014

H.E.S.S. Collaboration, JCAP 04 (2023) 040

Bounds on exploding PBHs - II

$$eta' \sim 10^{-9} rac{\Omega_{
m PBH}}{\Omega_{
m DM}} \left(rac{M_{
m PBH}^{
m in}}{M_{\odot}}
ight)^{1/2}$$



Figure 5: Bounds on β' and $\frac{\Omega_{\text{PBH}}}{\Omega_{\text{DM}}}$. Left: from H.E.S.S. 2023, right from Carr 2021.

Carr et al., Rep. Prog. Phys. 84 (2021) 116902 H.E.S.S. Collaboration, JCAP 04 (2023) 040

Other results - I



Figure 6: Total time-integrated spectrum of muon neutrinos expected at the Earth from the evaporation of a PBH multiplied by squared-energy, for an observation time of $\tau = 100$ s. In each panel, we show the SM-only contribution (black, dashed) and the SM + HNL spectrum for different HNL benchmark masses (solid, color) and mixings.



Figure 7: Expected number of muon-neutrino events at lceCube as a function of the HNL mass, from the last stages (100 s) of an evaporating PBH located at a distance $d_{\rm PBH} = 10^{-4}$ pc from Earth and at a declination angle [30° < δ < 90°]. The black dashed curve corresponds to the SM-only case.

List of bounds of Fig.4:

- □ 1:0:0: NA62, T2K, PiENU, BEBC and PS191
- □ 0:1:0: T2K, MicroBooNE, NuTeV, E949
- 0:0:1: T2K, CHARM and constraints from IceCube looking for low-energy "double-bang" events
- + SN 1987A detection bounds, not shown for space limits, up to O(100MeV)

NA62 Collaboration, Phys. Lett. B 807 (2020) 135599 T2K Collaboration, Phys. Rev. D 100 no. 5, (2019) 052006 PIENU Collaboration, Phys. Rev. D 97 no. 7, (2018) 072012 Barouki et al., SciPost Phys. 13 (2022) 118, arXiv:2208.00416 Bernardi et al. Phys. Lett. B 203 (1988) 332-334 MicroBooNE Collaboration, Phys. Rev. D 101 no. 5, (2020) 052001 NuTeV, E815 Collaboration, Phys. Rev. Lett. 83 (1999) 4943-4946 E949 Collaboration, Phys. Rev. D 91 no. 5, (2015) 052001 CHARM II Collaboration, Phys. Lett. B 343 (1995) 453-458 Coloma et al., Phys. Rev. D 109 no. 6, (2021) 201804 Carenza et al., Phys. Rev. D 109 no. 6, (2024) 063010 $\hfill\square$ The most general mass term for neutrinos can be written as

$$\begin{split} \mathscr{L}_{\mathsf{RHN}}^{m} &= -Y_{\alpha i}\overline{L}_{\alpha}\widetilde{H}N_{i} - \frac{1}{2}M_{R}^{ij}\overline{N_{i}^{c}}N_{j} + \mathsf{h.c.} \\ &= \frac{1}{2}\overline{\mathcal{N}_{L}^{c}}M_{\nu}\mathcal{N}_{L} + \mathsf{h.c.} \end{split}$$

 $\hfill\square$ After EW symmetry breaking $\mathscr{L}^m_{\mathsf{RHN}}$ becomes

$$\mathscr{L}_{\mathsf{RHN}}^{m} = -\frac{1}{2} \overline{\mathcal{N}_{L}^{c}} M_{\nu} \mathcal{N}_{L} + \mathsf{h.c.},$$

with

$$\mathcal{N}_{L} = \begin{pmatrix} \nu_{L} \\ (N_{R})^{c} \end{pmatrix}, \quad M_{\nu} = \begin{pmatrix} \mathbf{0}_{3 \times 3} & Y\nu/\sqrt{2} \\ Y^{T}\nu/\sqrt{2} & M_{R} \end{pmatrix}$$

R. N. Mohapatra et al., Phys. Rev. D 34 (1986) 1642

□ By diagonalizing the mass matrix $M_{\nu} = U_{\nu} M_{\nu}^{\text{diag}} U_{\nu}^{T}$ ($U_{\nu}^{T} U_{\nu} = 1$), $\mathscr{L}_{\text{RHN}}^{m}$ is written in terms of the neutrino mass states:

$$\mathcal{N}_L^m = \mathcal{U}_\nu^T \mathcal{N}_L$$

where \mathcal{U}_{ν} is the unitary $(3 + n) \times (3 + n)$ diagonalizing mass matrix

 \Box The CC lepton mixing matrix is the top $(3 + n) \times 3$ submatrix of U_{ν} $(U_{l} \sim \mathbb{K}_{3 \times 3})$:

$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} & \dots & U_{en} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} & \dots & U_{\mu n} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} & \dots & U_{\tau n} \end{pmatrix}$$

Below 1 GeV, the following two channels dominate

$$\begin{array}{ll} \nu_4 & \rightarrow & \nu_\alpha \pi^0 \,, \\ \\ \nu_4 & \rightarrow & \nu_\alpha \nu_\ell \bar{\nu}_\ell \ \ \left(\ell = e, \mu, \tau\right), \end{array}$$

where α indicates the neutrino flavor that mixes with ν_4

The partial decay widths are

$$\Gamma_{lpha}\left(
u_{4}
ightarrow
u_{lpha} \pi^{0}
ight) = 2rac{G_{F}^{2}m_{4}^{3}}{32\pi}f_{\pi}^{2}|U_{lpha 4}|^{2}\left[1-\left(rac{m_{\pi_{0}}}{m_{4}}
ight)^{2}
ight]^{2}\,,$$

$$\Gamma_{\alpha}\left(\nu_{4} \rightarrow \nu_{\alpha}\sum_{\ell}\nu_{\ell}\bar{\nu}_{\ell}\right) = \sum_{\ell}\left[\Gamma\left(\nu_{4} \rightarrow \nu_{\alpha}\nu_{\ell}\bar{\nu}_{\ell}\right) + \left(\nu_{4} \rightarrow \bar{\nu}_{\alpha}\nu_{\ell}\bar{\nu}_{\ell}\right)\right] = 2\frac{G_{F}^{2}m_{4}^{5}}{64\pi^{3}}|U_{\alpha4}|^{2}.$$

where u_{α} is the neutrino flavour that mixes with u_4

A. Atre et al., JHEP 05 (2009) 030

The neutrino spectrum from HNL decay can be computed as

$$\frac{dN_{\alpha}}{dE} = \mathcal{B}_{a} \int d\cos\theta \int_{E_{s,\min}}^{E_{s,\max}} dE_{s} \frac{1}{\gamma_{s} \left(1 + \beta_{s}\cos\theta\right)} \frac{dN_{s}}{dE_{s}} \mathcal{F}_{\alpha} \left[\frac{E}{\gamma_{s} \left(1 + \beta_{s}\cos\theta\right)}, \cos\theta\right]$$

- \Box *E*, *E*_s are the energies of ν_{α} and the HNL in the laboratory frame;
- \Box θ is the angle formed between ν_{α} in the HNL rest frame and its velocity in the laboratory frame;
- \square $\mathcal{B}_{\alpha} = \Gamma_{\alpha}/\Gamma_{tot}$ indicates the branching ratio of the decay process;
- $\Box \frac{dN_s}{dE_c}$ is the total primary spectrum of HNLs;
- \Box \mathcal{F}_a is the angular and energetic distribution of the resulting ν_a in the HNL frame

The primary HNL spectra have been evaluated with BlackHawk, as the SM neutrino spectra

Mastrototaro et al., Phys. Rev. D 104 no. 1, (2021) 016026 Arbey et al., Eur. Phys. J. C 81 (2021) 910

Details of the spectrum computation - III

Light-mass regime [0.1-1] GeV

2-body

$$\left.\frac{dN_\alpha}{dE}\right|^{2\mathrm{b}} = \frac{\mathcal{B}_\alpha m_4^2}{m_4^2 - m_{\pi^0}^2} \int_{E_{s,\mathrm{min}}}^{E_{s,\mathrm{max}}} dE_s \frac{1}{p_s} \frac{dN_s}{dE_s} \,.$$

as \mathcal{F}_{a} is a Dirac delta

3-body

$$\begin{split} \mathcal{F}_{\mathrm{I},\alpha}^{\mathrm{3b}}\left(E'\right) &= \left.\frac{dN_{\alpha}}{dE'd\cos\theta}\right|_{\mathrm{I}}^{\mathrm{3b}} = \frac{1}{2}16\frac{E'^2}{m_4^3}\left(3-4\frac{E'}{m_4}\right)\,,\\ \mathcal{F}_{\mathrm{II},\alpha}^{\mathrm{3b}}\left(E'\right) &= \left.\frac{dN_{\alpha}}{dE'd\cos\theta}\right|_{\mathrm{II}}^{\mathrm{3b}} = \frac{1}{2}96\frac{E'^2}{m_4^3}\left(1-2\frac{E'}{m_4}\right)\,. \end{split}$$

If the neutrino mixes with ν_4

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$$\mathcal{F}_{\alpha}^{3\mathrm{b}}\left(\mathcal{E}'\right) = rac{1}{4} \left(3\mathcal{F}_{\mathrm{I}}^{3\mathrm{b}} + \mathcal{F}_{\mathrm{II}}^{3\mathrm{b}}\right) \,.$$

$$\frac{dN_{\alpha(\ell)}}{dE}\Big|^{^{3\mathrm{b}}} = \mathcal{B}_{\alpha}m_{4}\int_{E_{s},\mathrm{min}}^{E_{s},\mathrm{max}} dE_{s}\frac{1}{p_{s}}\frac{dN_{s}}{dE_{s}}\int_{E_{\mathrm{min}}'}^{E_{\mathrm{max}}'} dE'\frac{1}{E'}\mathcal{F}_{\alpha(\ell)}^{^{3\mathrm{b}}}\left(E'\right) ,$$

Mastrototaro et al., Phys. Rev. D 104 no. 1, (2021) 016026

Details of the spectrum computation - IV

If only ν_{μ} mixes with $\nu_{\rm 4},$ three HNL decay channels are relevant in the [0.5-2] TeV mass range

$$\begin{array}{rcl} \nu_4 & \rightarrow & W^{\pm} \mu^{\mp} \; , \\ \nu_4 & \rightarrow & Z^0 \nu_{\mu} \; , \\ \nu_4 & \rightarrow & H^0 \nu_{\mu} \; . \end{array}$$

with partial decay widths

$$\begin{split} & \Gamma\left(\nu_{4} \to \mu W_{L}\right) = 2 \frac{g^{2}}{64\pi M_{W}^{2}} |U_{\mu4}|^{2} m_{4}^{3} \left[1 - \left(\frac{M_{W}}{m_{4}}\right)^{2}\right]^{2}, \\ & \Gamma\left(\nu_{4} \to \mu W_{T}\right) = 2 \frac{g^{2}}{32\pi} |U_{\mu4}|^{2} m_{4} \left[1 - \left(\frac{M_{W}}{m_{4}}\right)^{2}\right]^{2}, \\ & \Gamma\left(\nu_{4} \to \nu_{\mu} Z_{L}^{0}\right) = \frac{g^{2}}{64\pi M_{Z}^{2}} |U_{\mu4}|^{2} m_{4}^{3} \left[1 - \left(\frac{M_{Z}}{m_{4}}\right)^{2}\right]^{2}, \\ & \Gamma\left(\nu_{4} \to \nu_{\mu} Z_{T}^{0}\right) = \frac{g^{2}}{32\pi \cos^{2} \theta_{W}} |U_{\mu4}|^{2} m_{4} \left[1 - \left(\frac{M_{Z}}{m_{4}}\right)^{2}\right]^{2}, \\ & \Gamma\left(\nu_{4} \to \nu_{\mu} H^{0}\right) = \frac{g^{2}}{64\pi M_{H}^{2}} |U_{\mu4}|^{2} m_{4}^{3} \left[1 - \left(\frac{M_{H}}{m_{4}}\right)^{2}\right]^{2} \end{split}$$

The resulting spectrum will be

$$\frac{dN_{\nu_{\mu}}}{dE} = \sum_{i.s.} \mathcal{B}(\nu_4 \rightarrow i.s.) \ m_4 \int_{E_s,\min}^{E_s,\max} dE_s \frac{1}{p_s} \frac{dN_s}{dE_s} \int_{E'_{\min}}^{E'_{\max}} dE' \frac{1}{E'} \frac{dN}{dE'} \left(\nu_4 \rightarrow i.s. \rightarrow \nu_{\mu}\right) \,,$$

where PPPC4DM has been employed to evaluate $\frac{dN}{dE'}$

Mastrototaro et al., Phys. Rev. D 104 no. 1, (2021) 016026 A. Atre et al., JHEP 05 (2009) 030 Cirelli et al., JCAP 03 (2011) 051

Details of the χ^2 analysis

 \Box The expected $N_{\nu\mu}$ at lceCube depends on the declination angle δ and the effective area \mathcal{A}_{eff} :

$$N_{\nu_{\mu}}\left(\delta\right) = \frac{1}{4\pi d_{\rm PBH}^2} \int dE \left. \frac{dN_{\nu_{\mu}}}{dE} \right|_{\rm HNL+SM} \mathcal{A}_{\rm eff}(E,\delta)$$

- \Box Little atmospheric background for ν_{μ} from the northern hemisphere (if $\tau_{\rm obs} \sim$ 100s)
 - → set $\delta \in [30 \deg, 90 \deg]$

 $\hfill\square$ Sensitivity at IceCube estimated with χ^2 test statistics :

$$\chi^2 = \frac{\left(N_{\nu_{\mu}}^{\rm HNL+SM} - N_{\nu_{\mu}}^{\rm SM}\right)^2}{N_{\nu_{\mu}}^{\rm SM}}$$

(negligible background and d_{PBH} nuisance)

IceCube Collaboration, PRL, 124 no. 5, (2020) 051103