

# Bridging gaps in the GW spectrum: Ideas to detect $\mu\text{Hz}$ and high $f$ GWs

Diego Blas (ICREA/IFAE)

based on 2107.04063/2107.04601 (PRL/PRD22), 2112.11465 (PRD22) + 2303.01518 (PRD23)

(w. Alex Jenkins // A. Berlin, DB, R. T. D'Agnolo, S. Ellis, R. Harnik, Y. Kahn, J. Schütte-Engel)



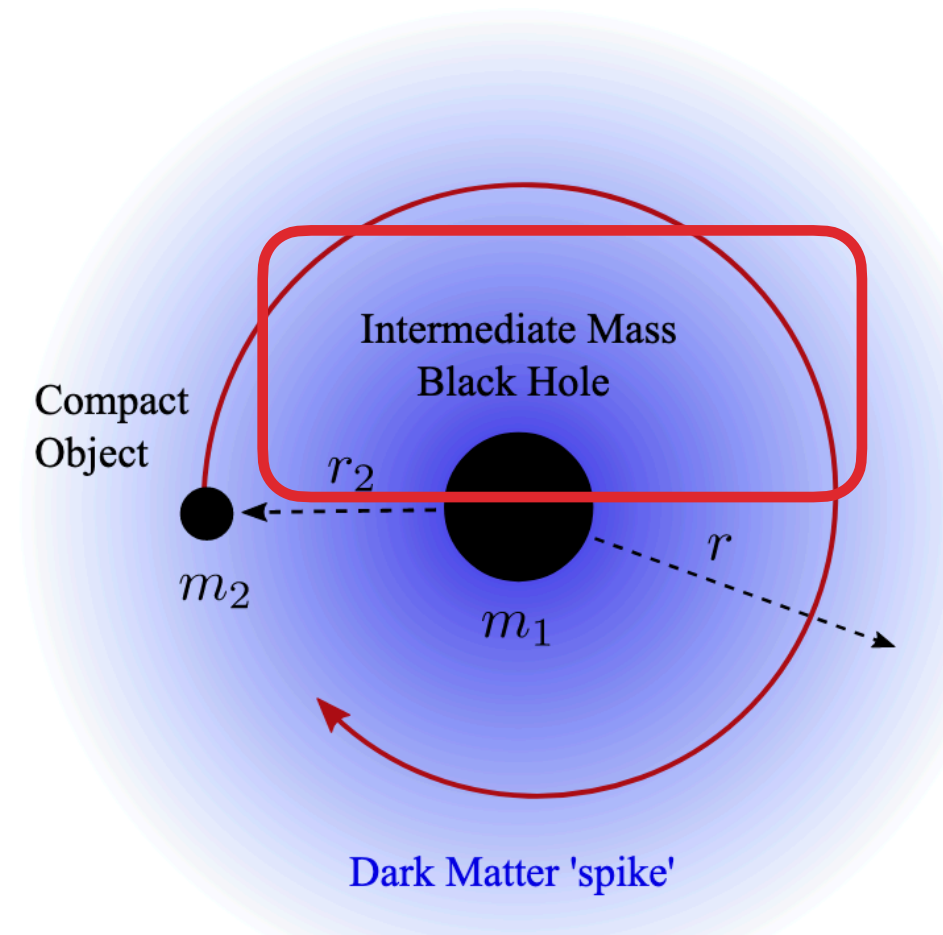
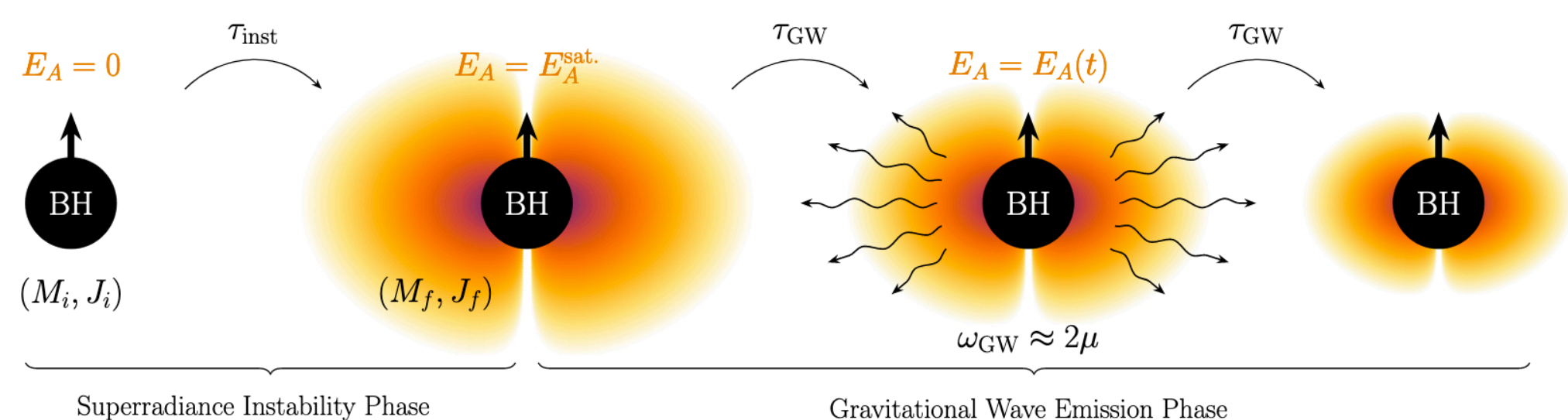


# Why this talk?

**Dark matter models** (beyond the weak scale) can be tested through **GWs of different frequencies**, e.g.

## Superradiance for ultralight?

Tsukada et al (2021)

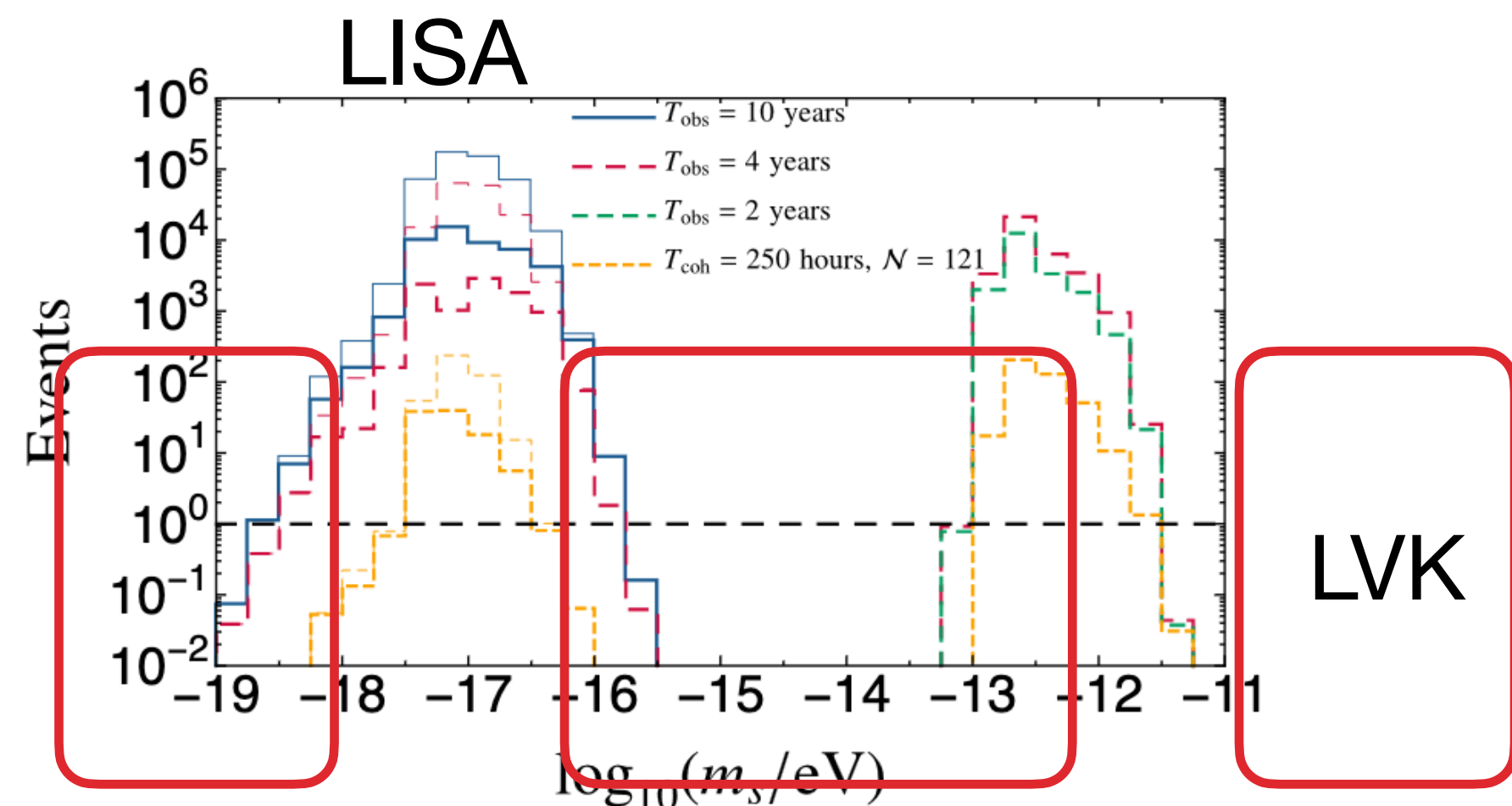


## Spikes?

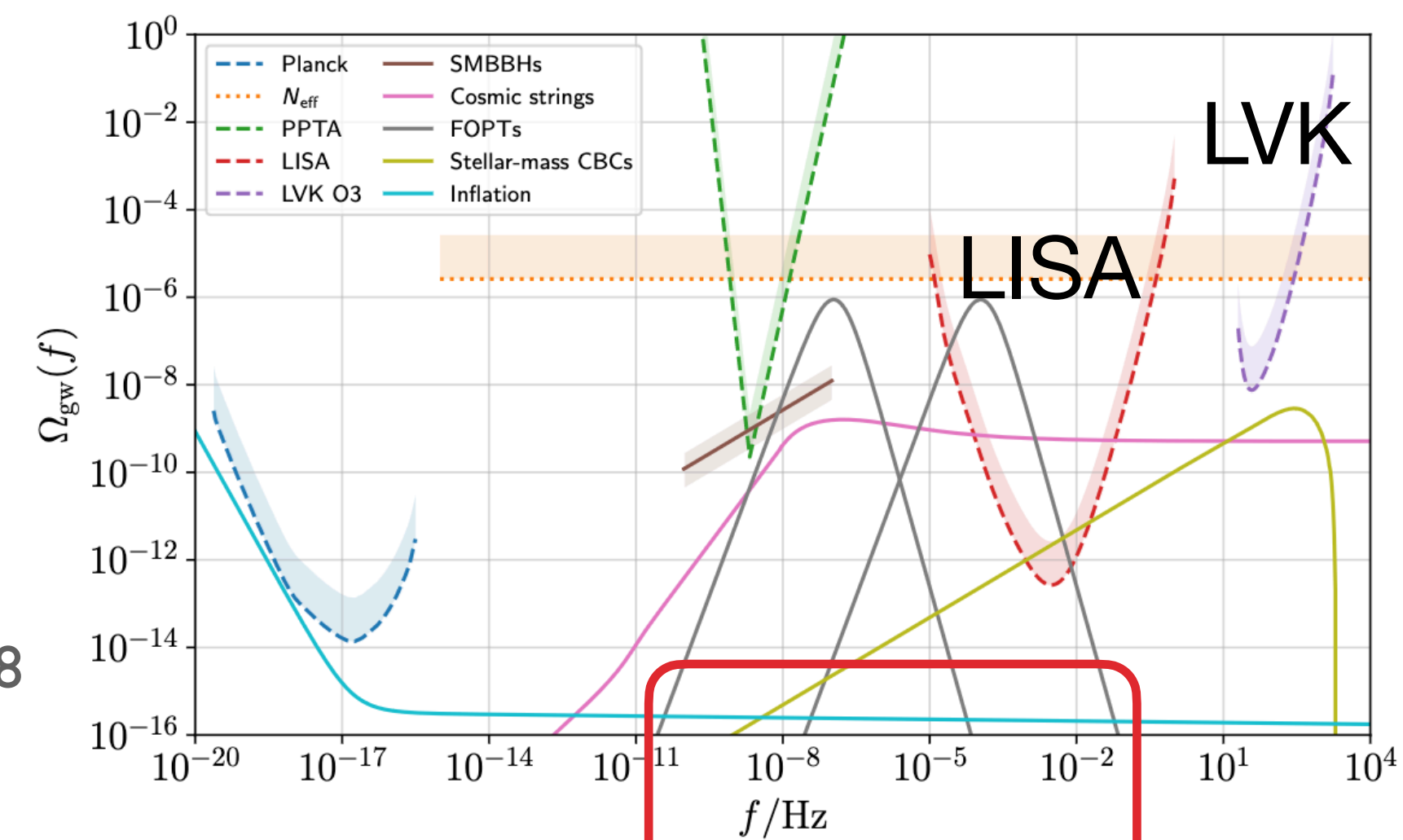
Cardoso & Maselli 1909.05870

Coogan et al. 2108.04154 [gr-qc]

## FOPT?



Renzini et al 2202.00178  
(based on 1512.06239)



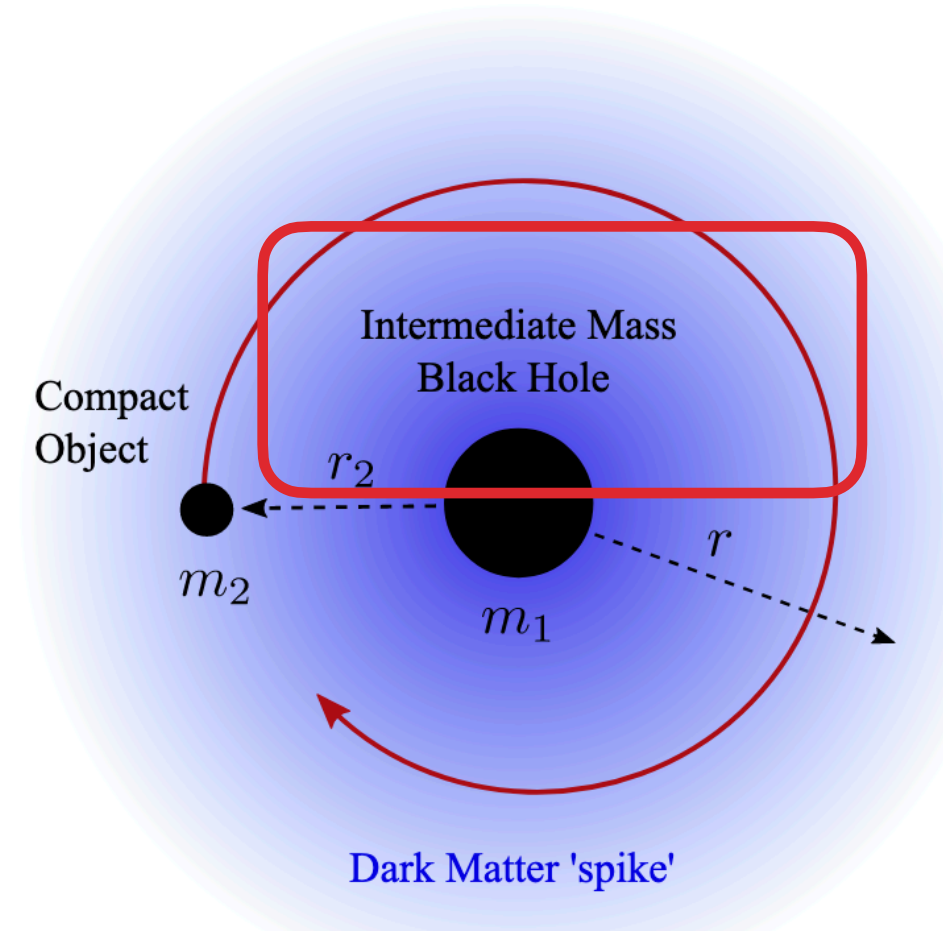
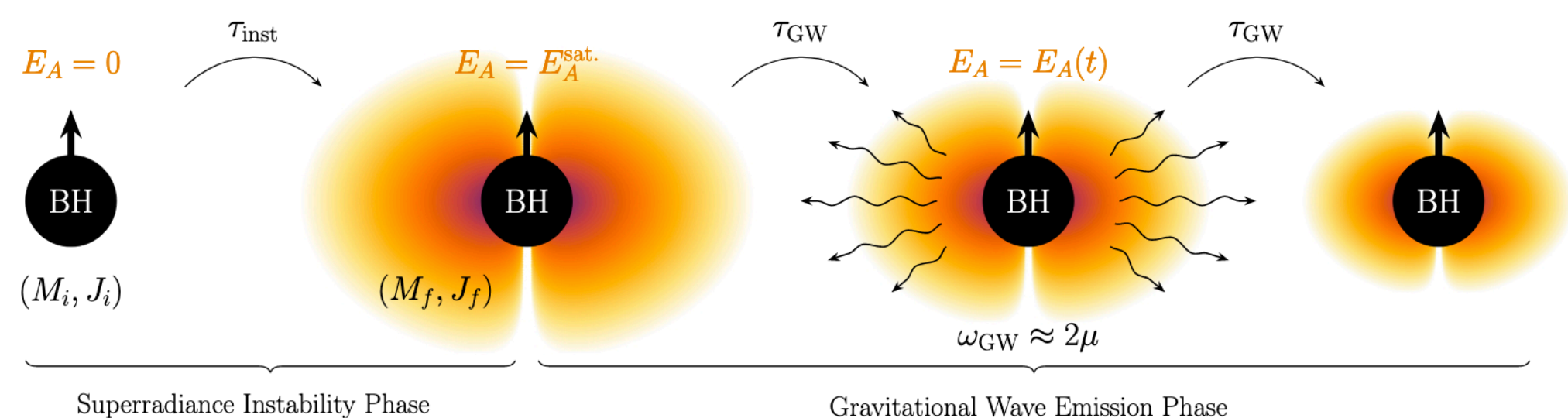


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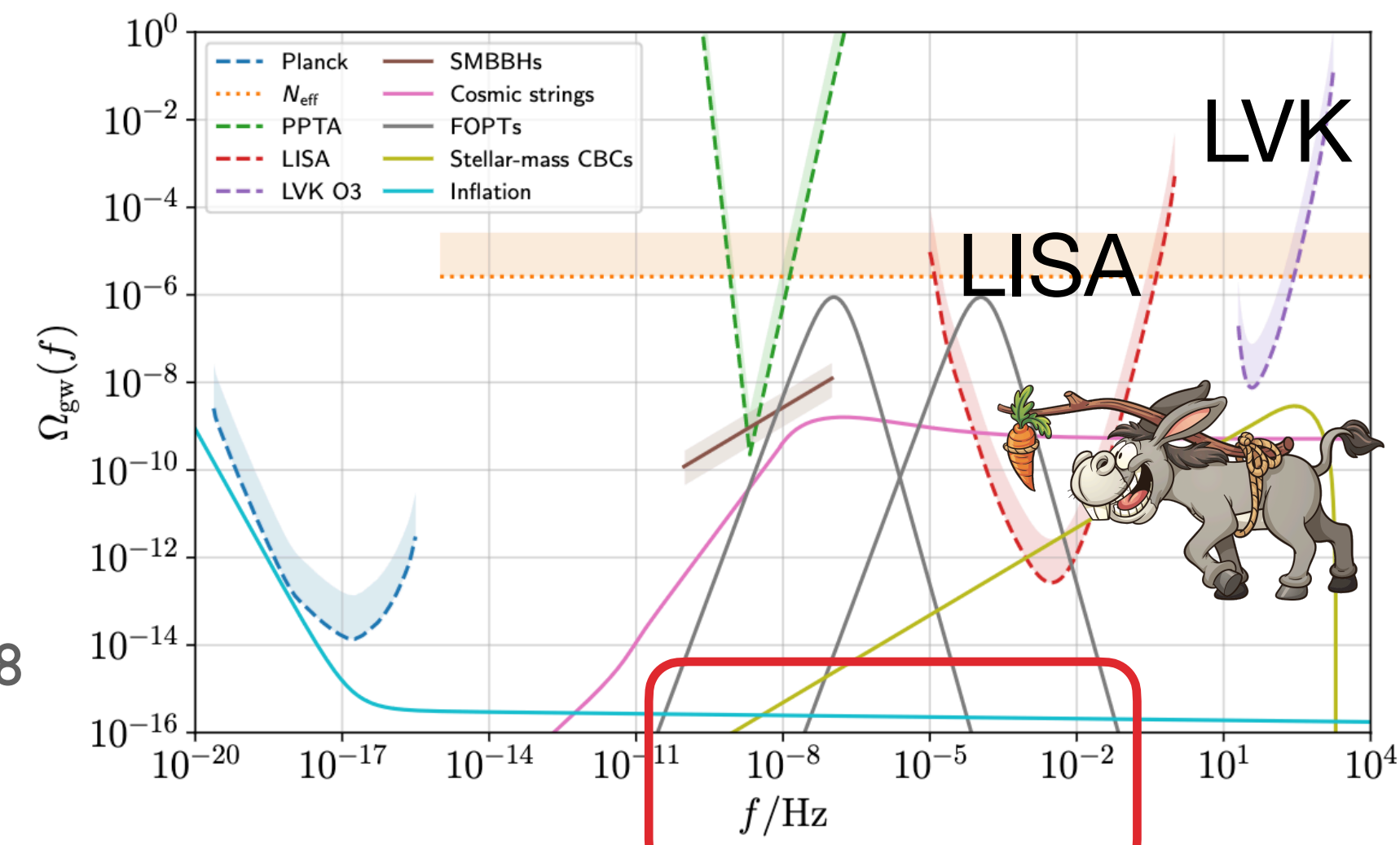
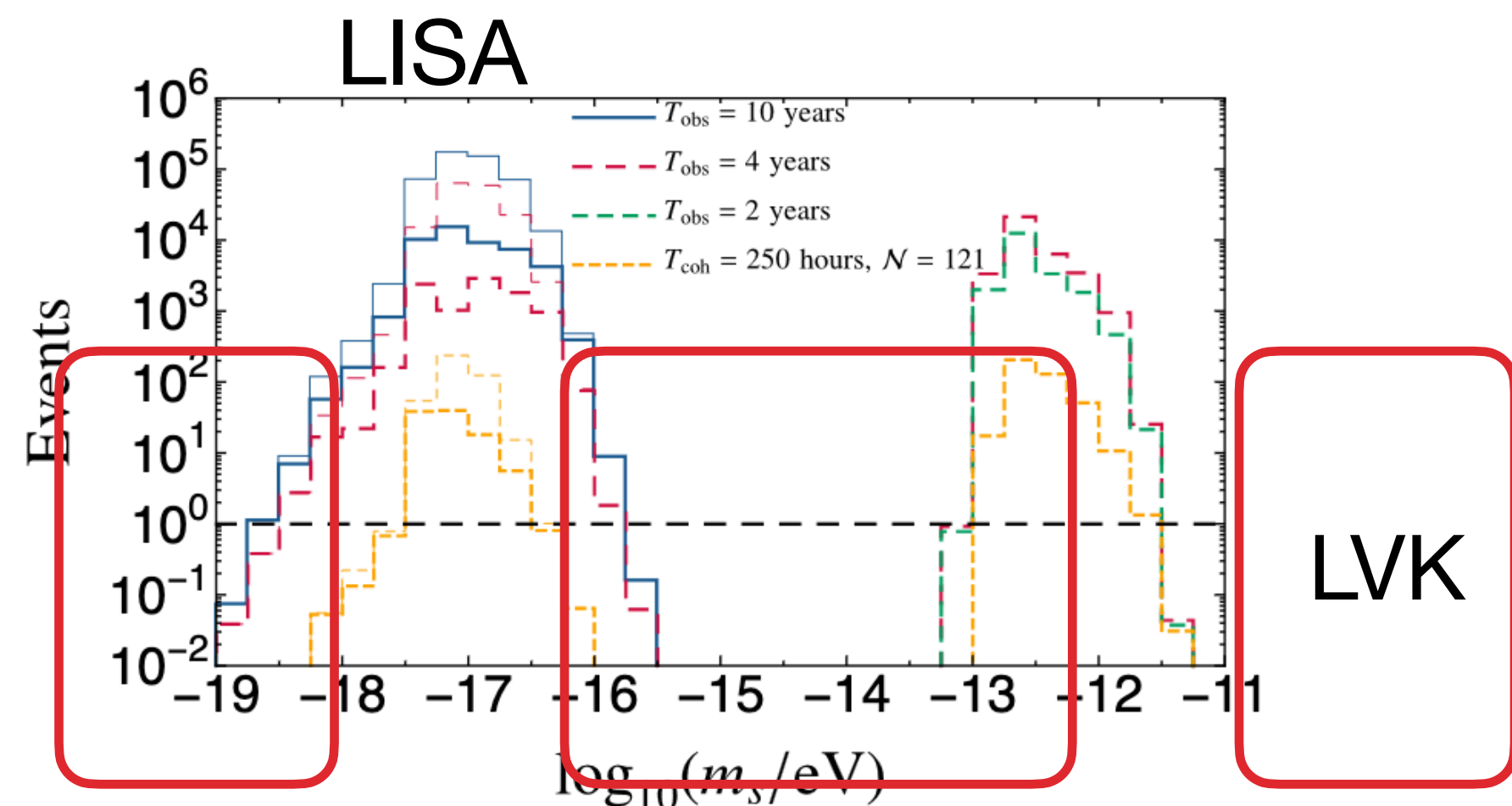


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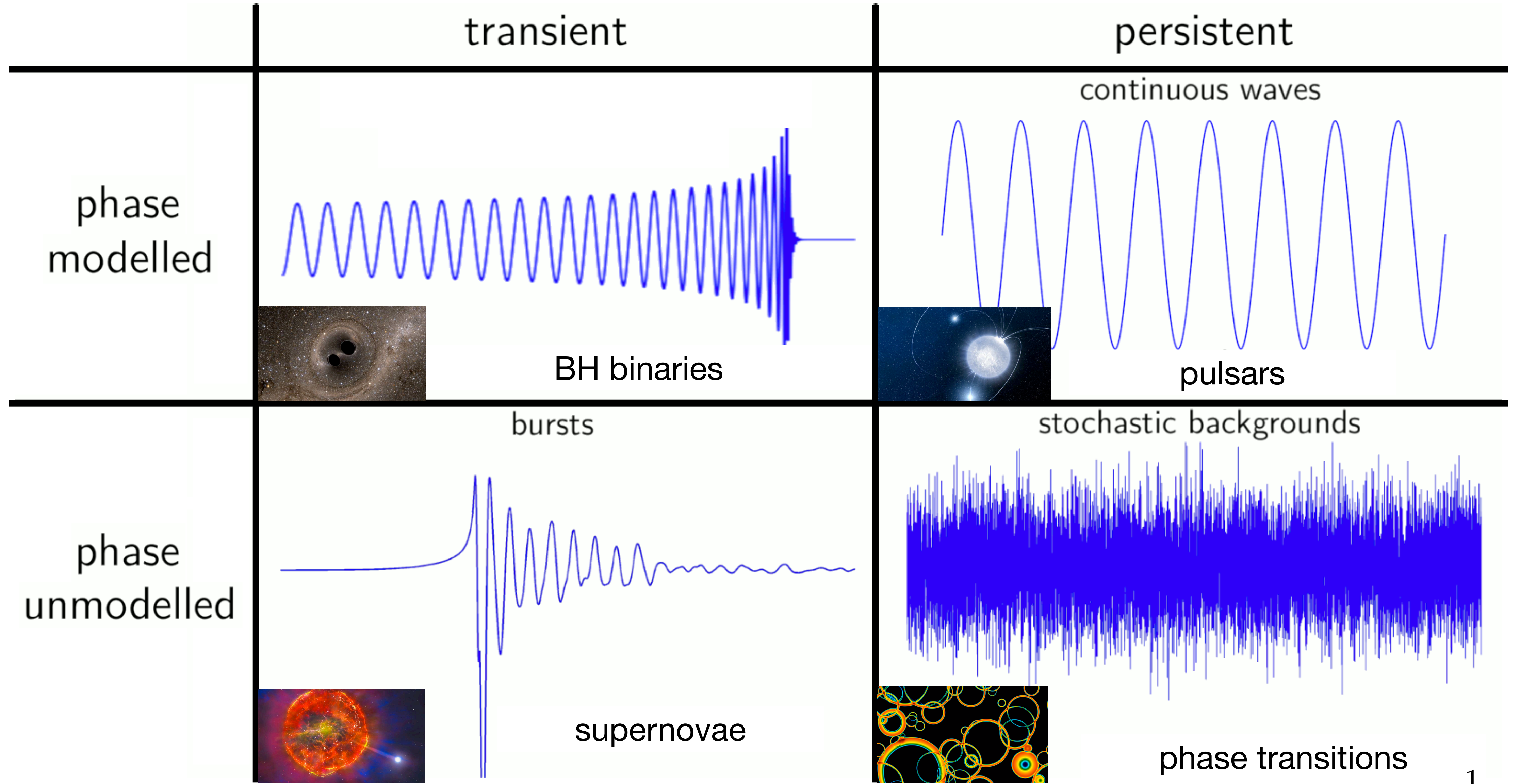


Renzini et al 2202.00178 (based on 1512.06239)



# Taxonomy of GWs

$h(t)$

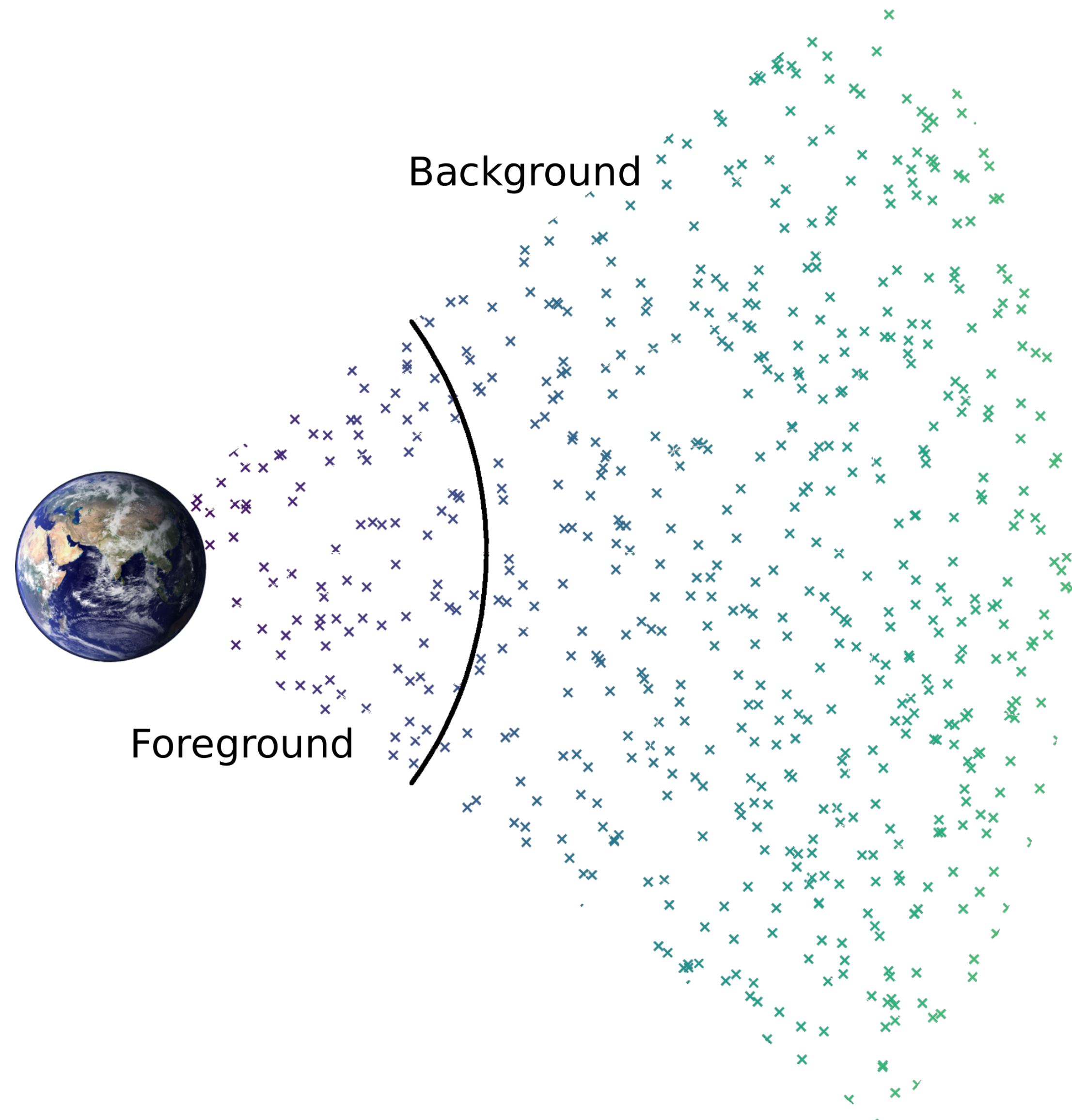


$$\rho_{\text{GW}} \sim M_{\text{P}}^2 \omega^2 h_{\text{GW}}^2$$

$$\rho_{\text{c}} \sim \text{keV}/\text{cm}^3 \quad \Omega_{\text{GW}}(f) = \frac{1}{\rho_{\text{crit}}} \frac{d\rho_{\text{GW}}}{d(\ln f)}$$



# Stochastic gravitational-wave background (SGWB)



- incoherent, persistent GW signal
- faint/numerous sources
- astrophysical and cosmological
- GW density parameter:

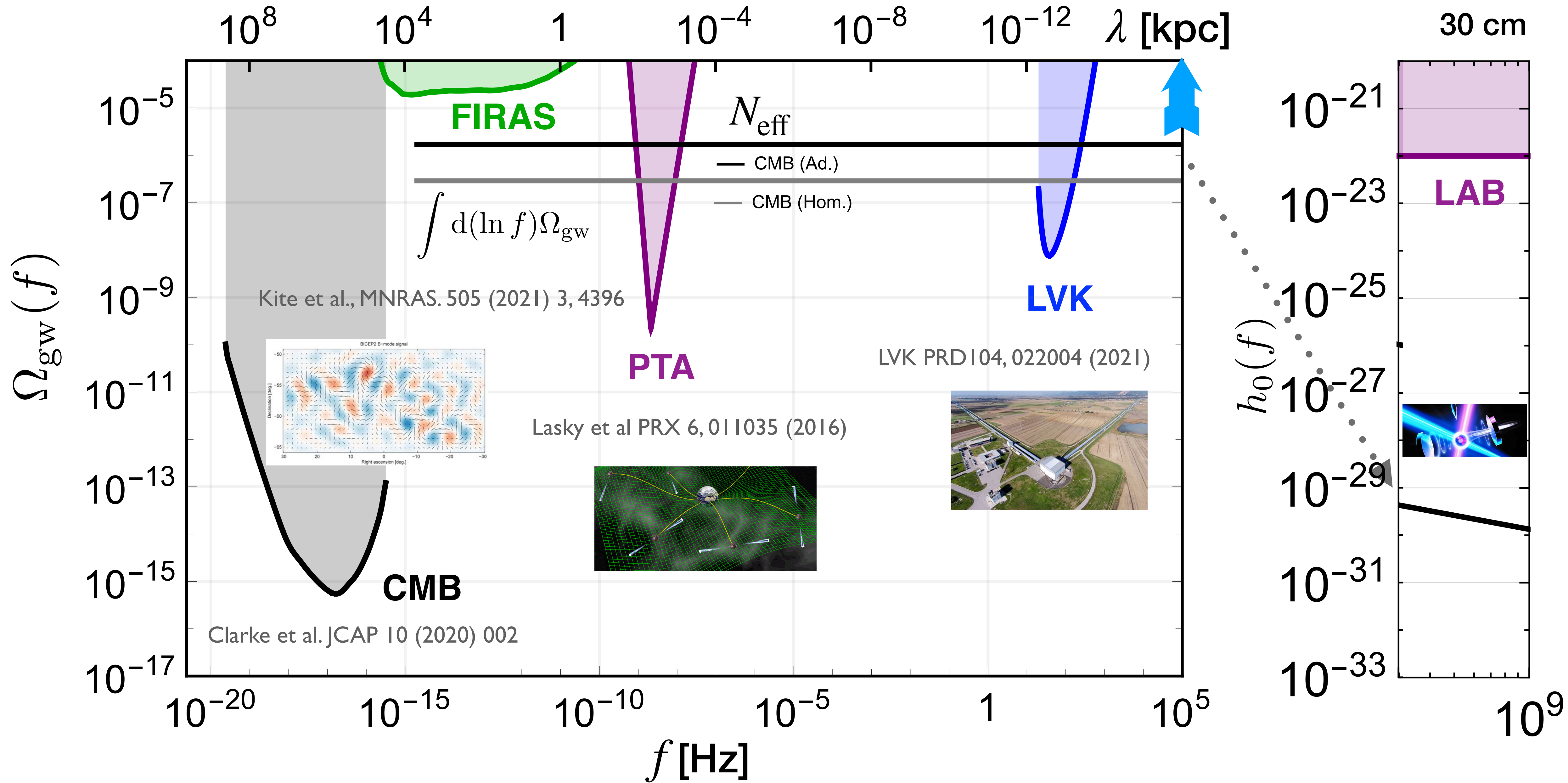
$$\Omega_{\text{GW}}(f) = \frac{1}{\rho_{\text{crit}}} \frac{d\rho_{\text{GW}}}{d(\ln f)}$$

$$\rho_{\text{GW}} \sim M_P^2 \omega^2 h_{\text{GW}}^2$$

$$\rho_c = 1.2 \times 10^{11} M_{\odot} \text{Mpc}^{-3} \\ \sim \text{keV}/\text{cm}^3$$

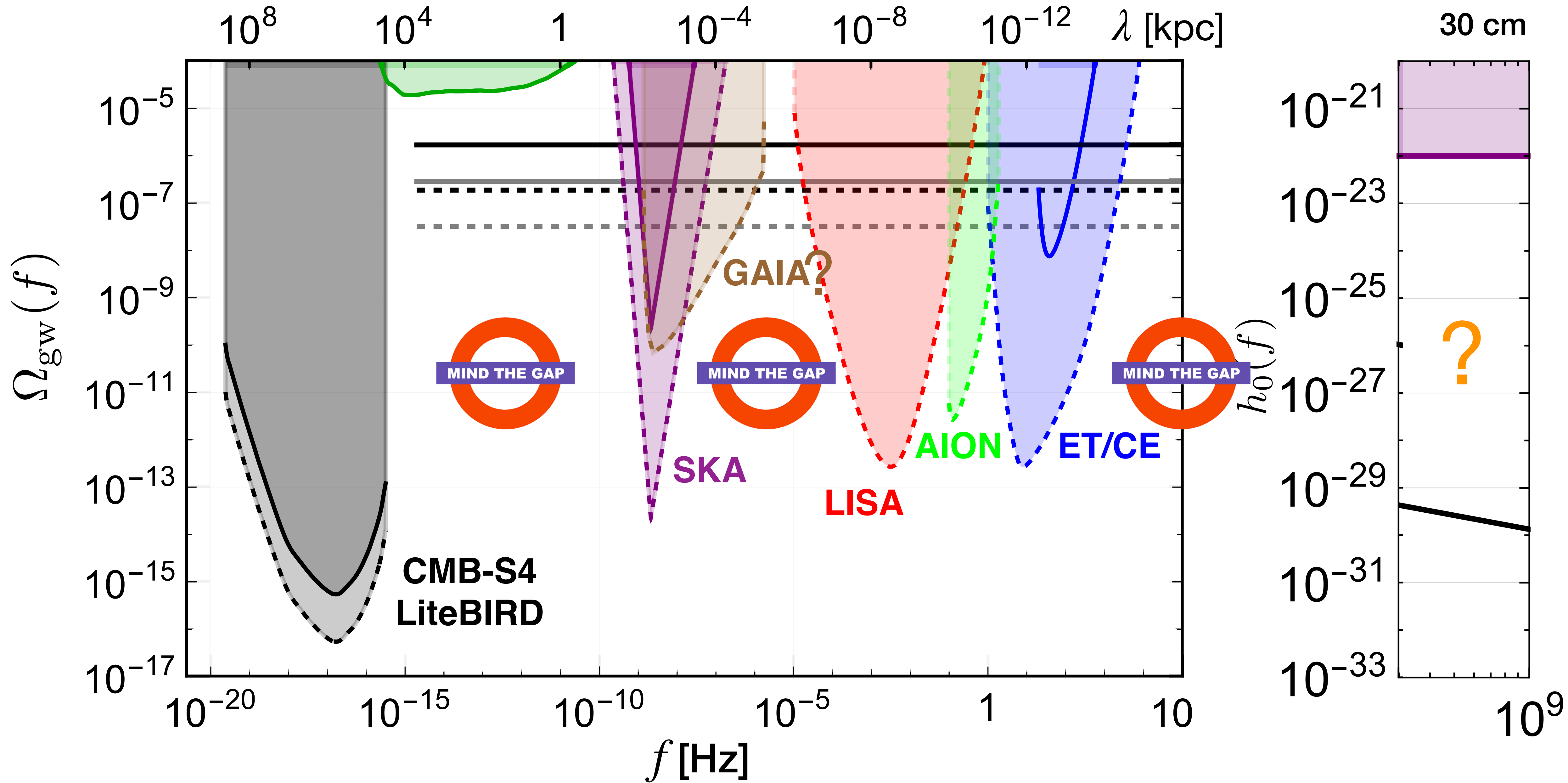


# GWs soundscape today





# GWs soundscape ca. 2040

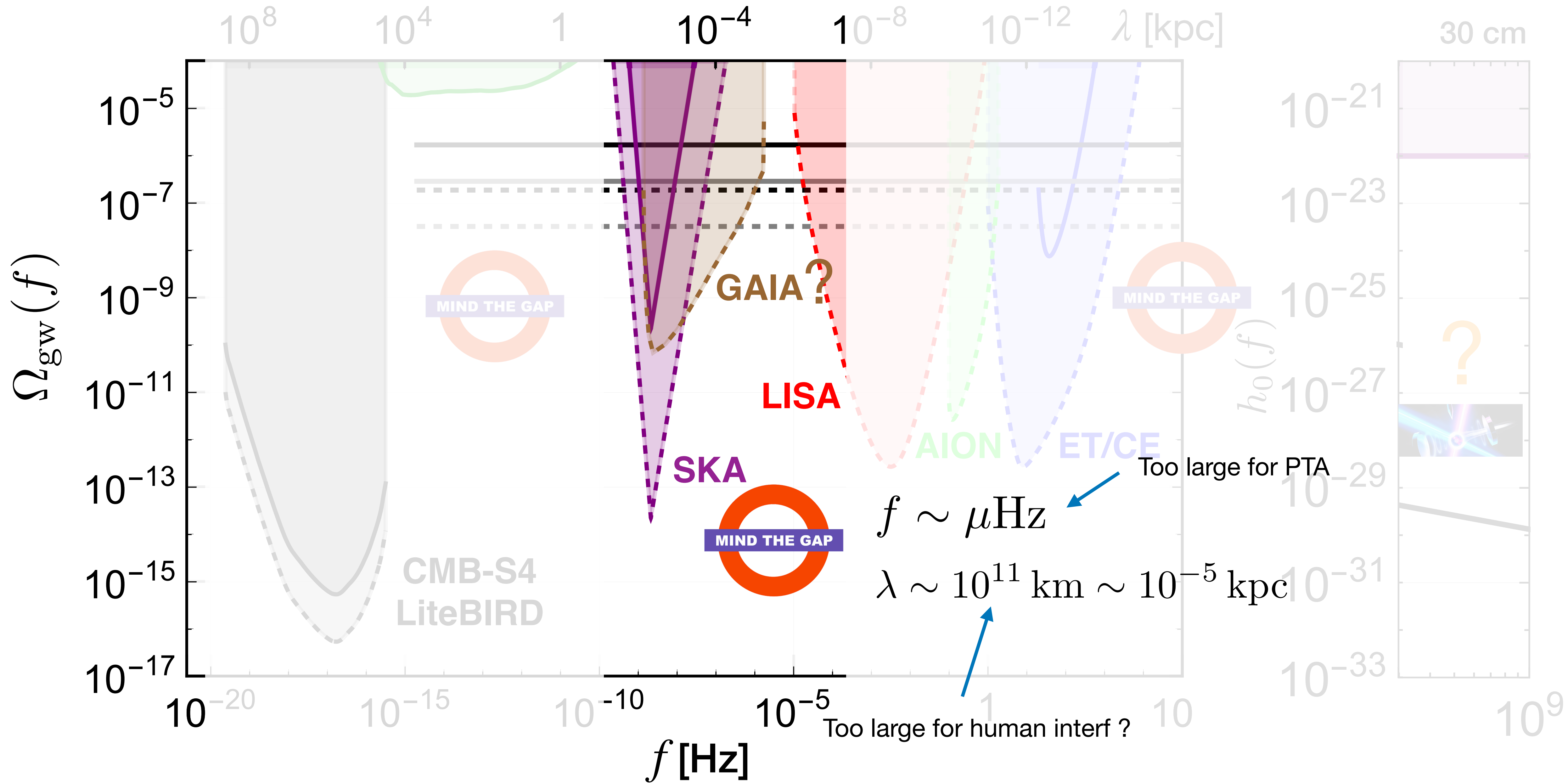




Possible **backgrounds** & ideas at  $\mu\text{Hz}$ : a rich band

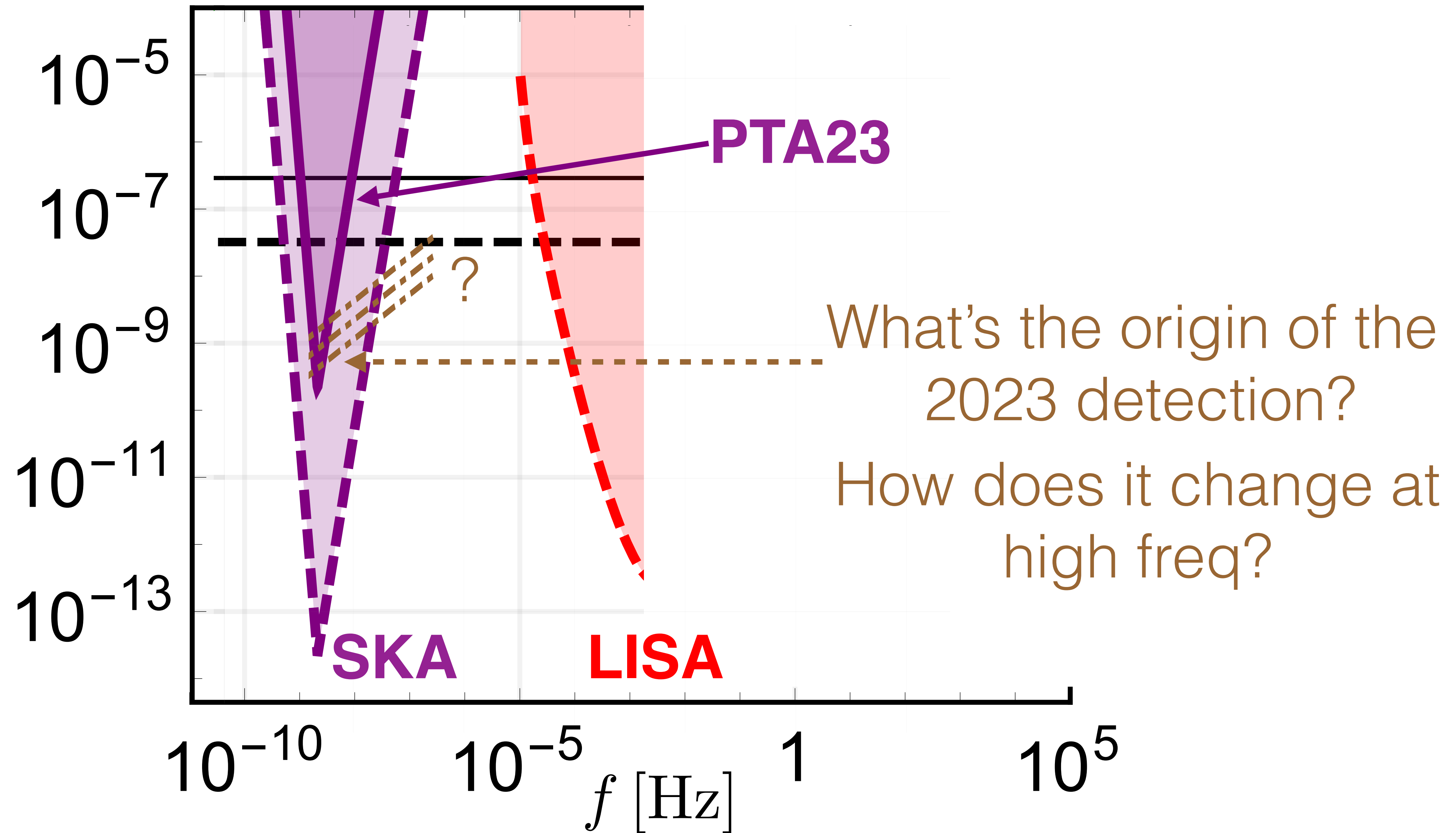


# Future soundscape (maybe 2040)?





# Possible backgrounds & ideas at $\mu\text{Hz}$ : a rich band

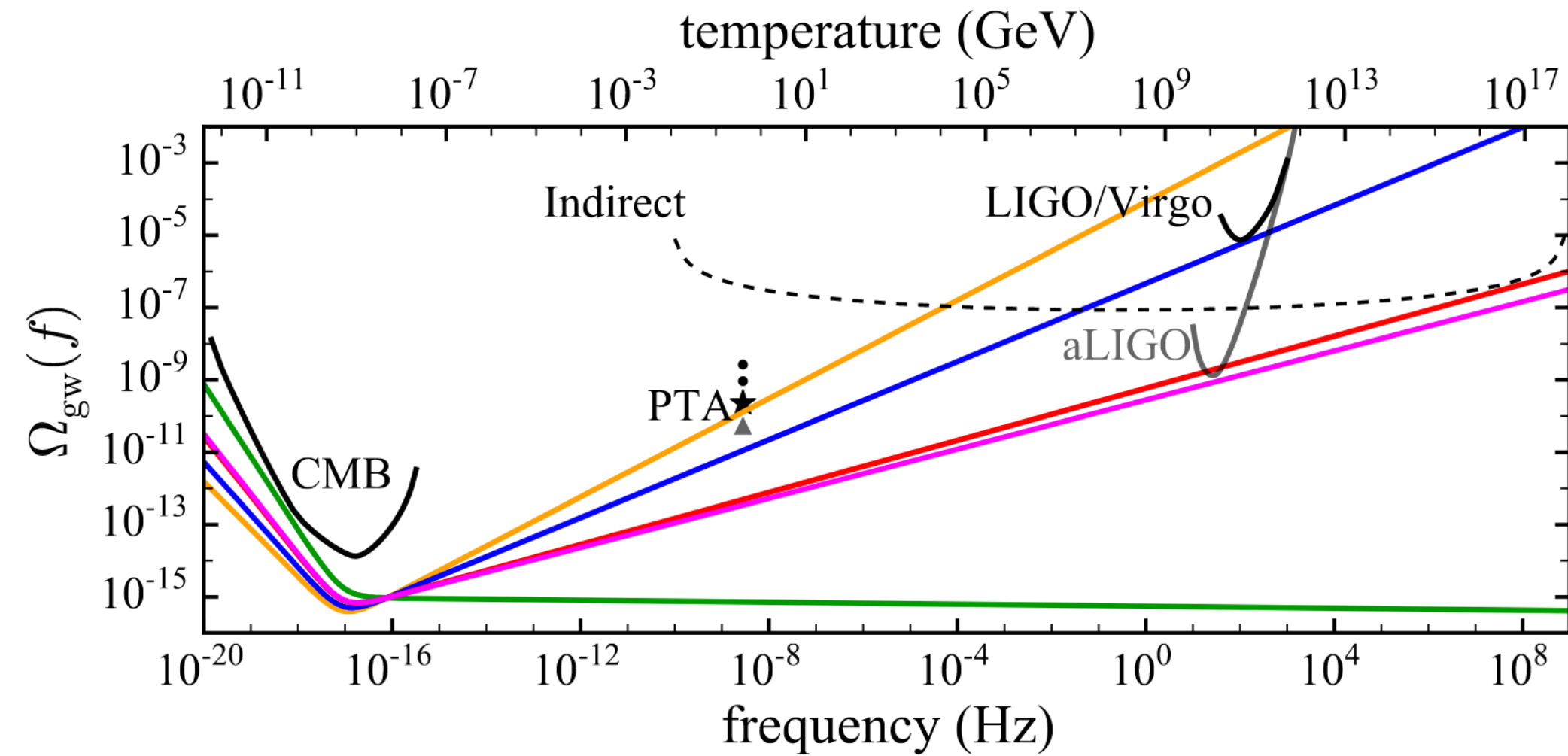




# Backgrounds from fundamental physics

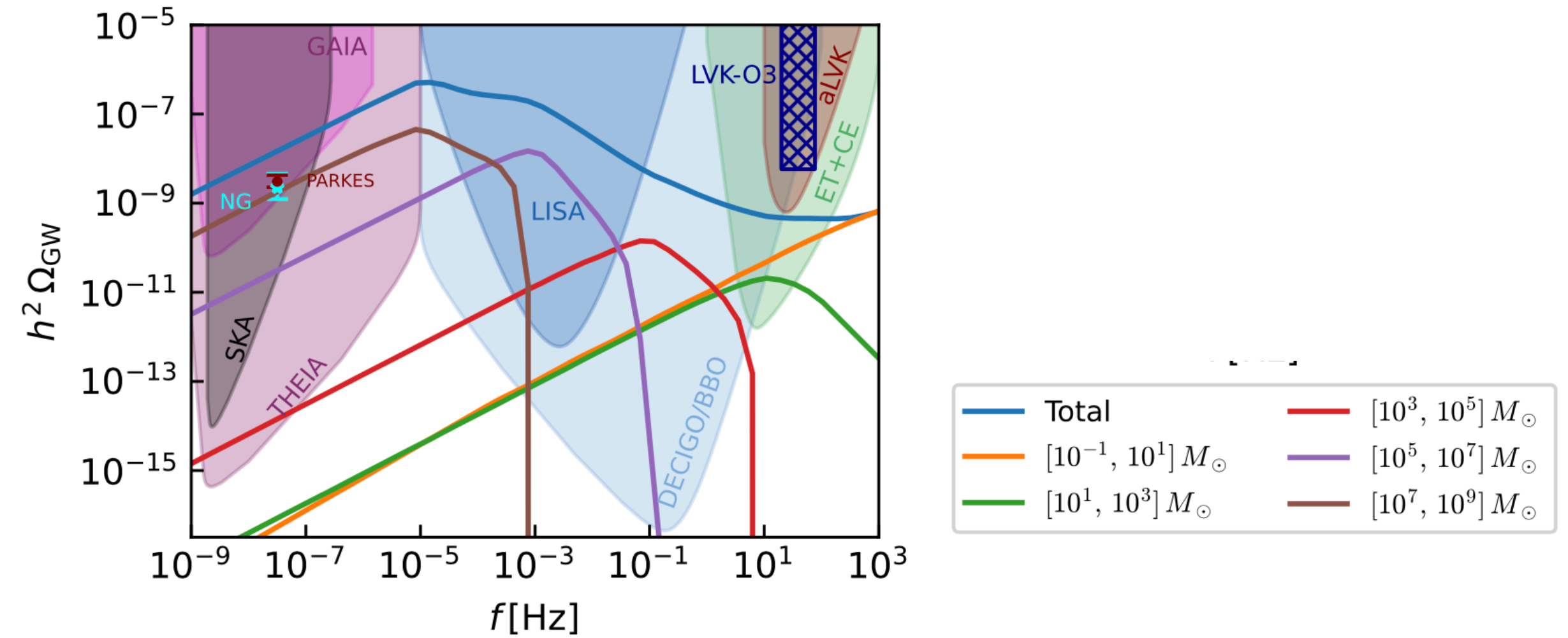
## Inflation

Lasky et al PRX 6, 011035 (2016)



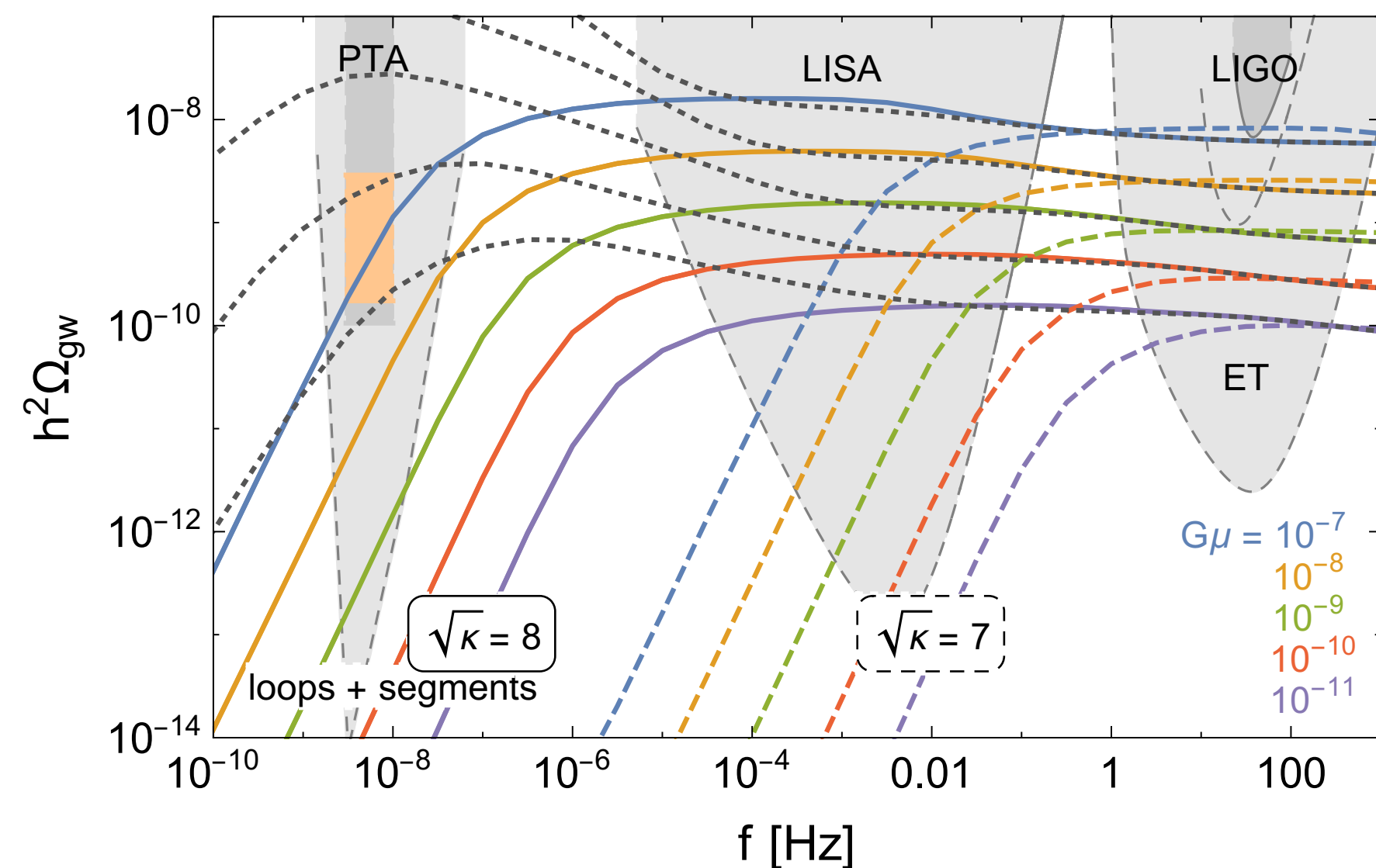
## PBH

Braglia et al. JCAP 12 (2021) 12



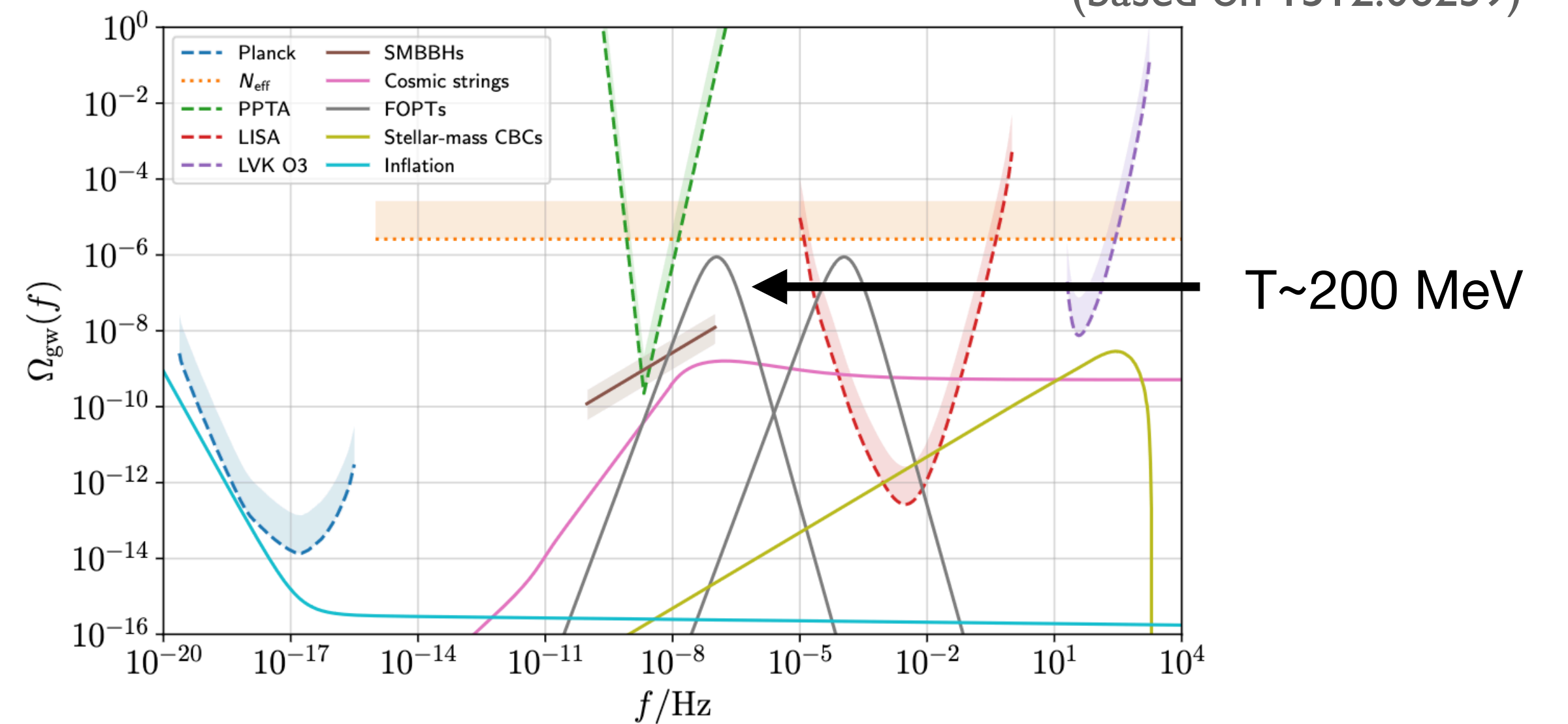
## Cosmic Strings

Buchmuller et al. 2107.04578



## FOPT

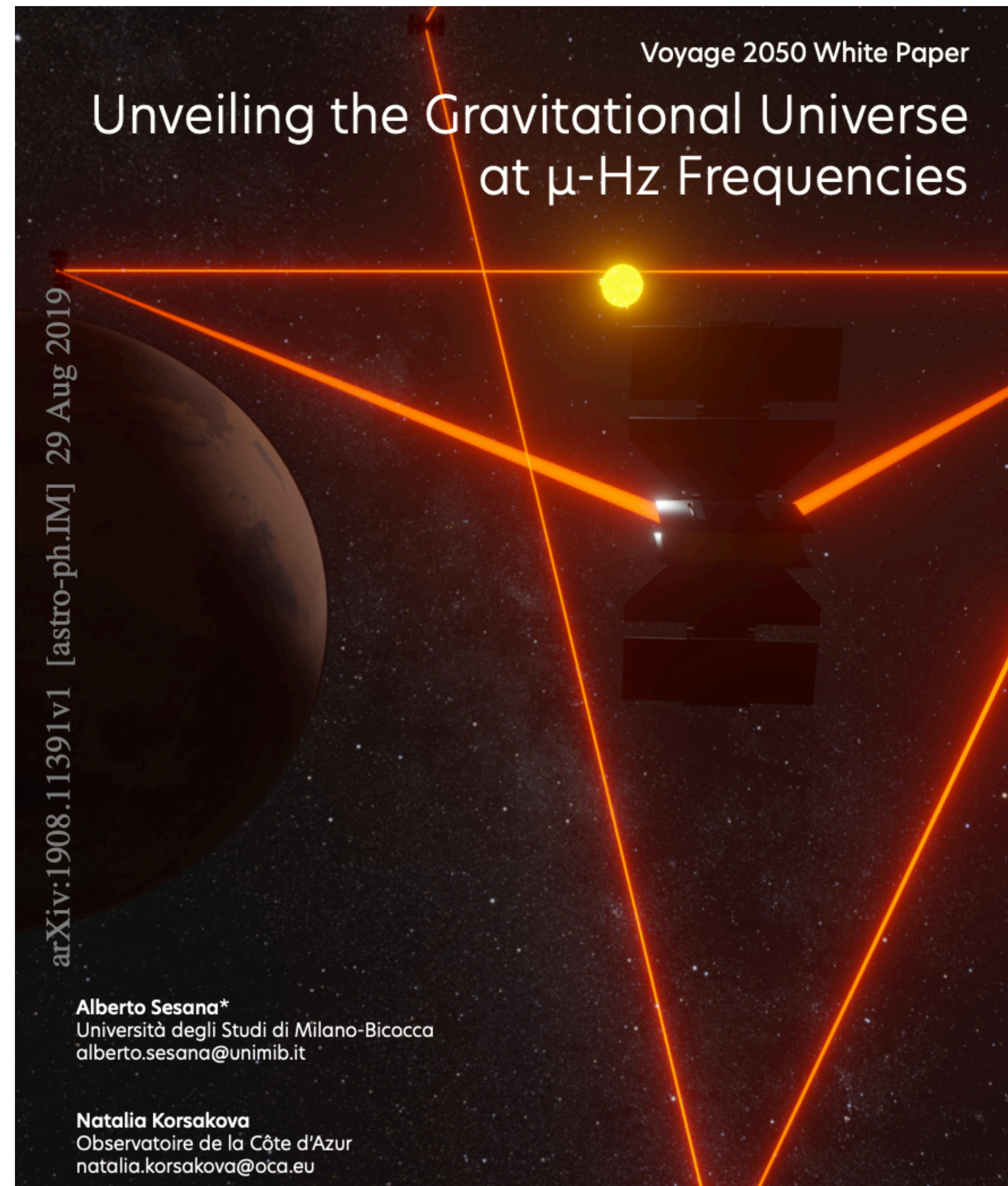
Renzini et al 2202.00178 (based on 1512.06239)



Possible backgrounds & **ideas** at  $\mu\text{Hz}$ : a rich band

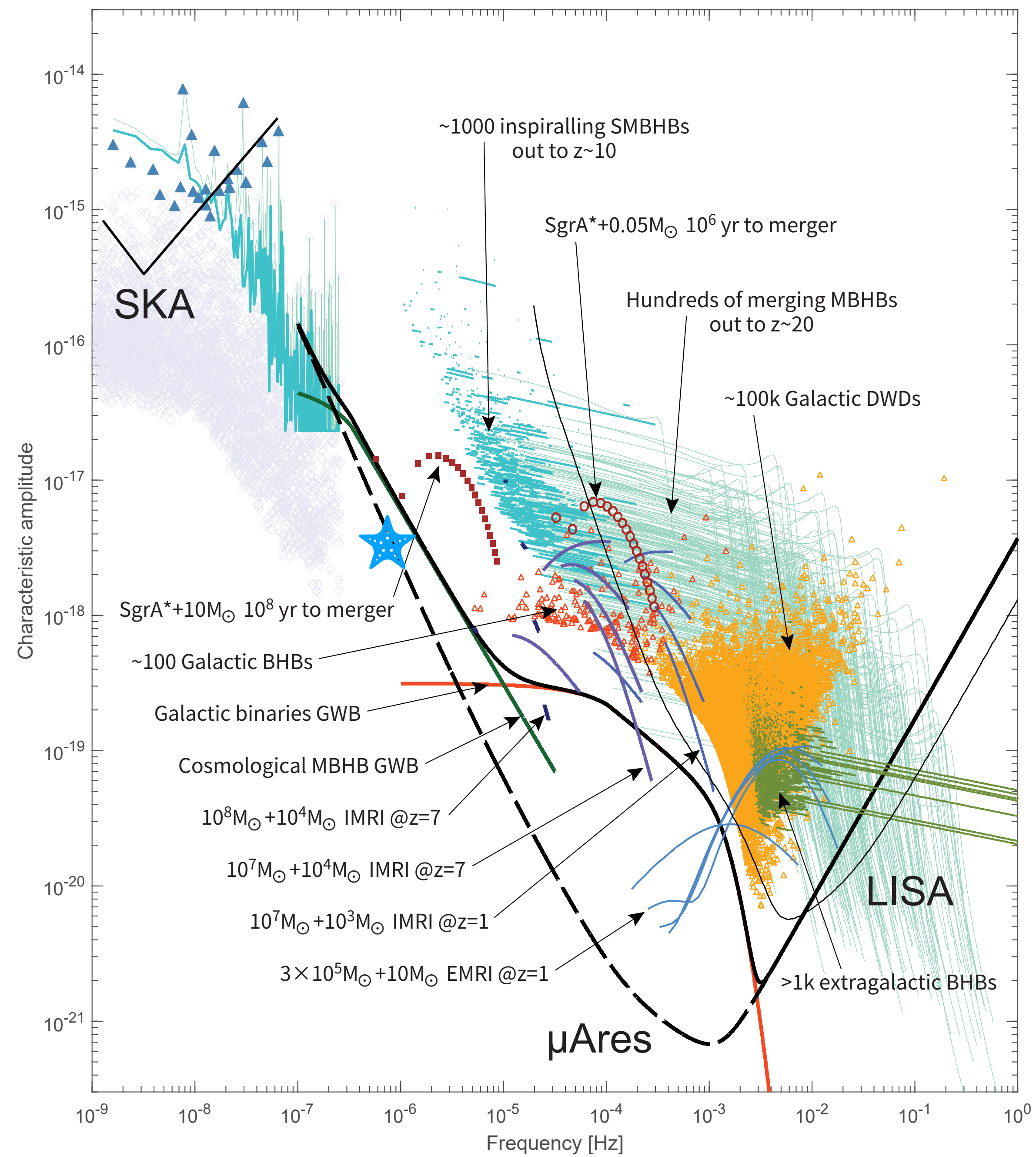
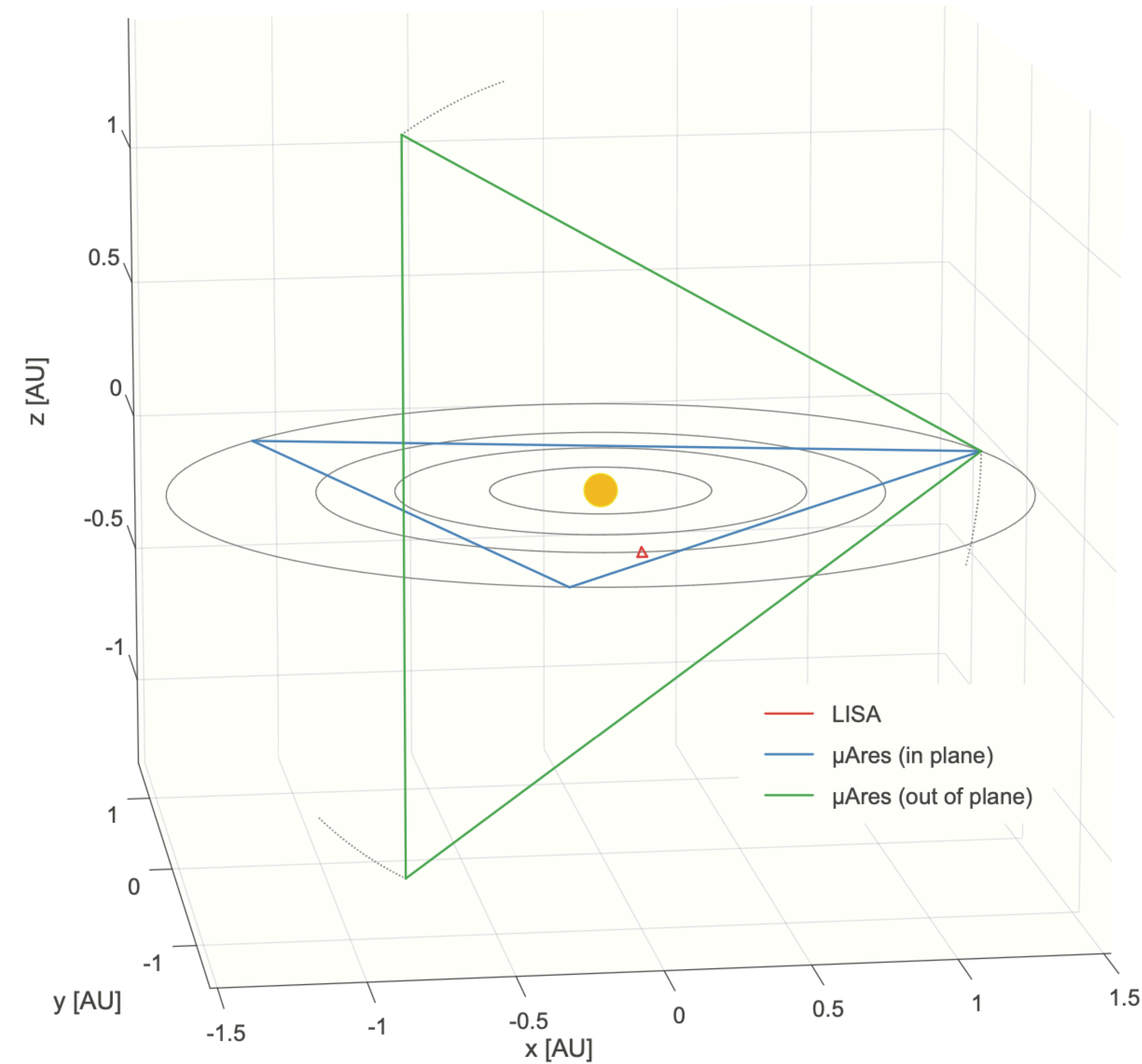


# i) $\mu$ Ares: LISA-like concept





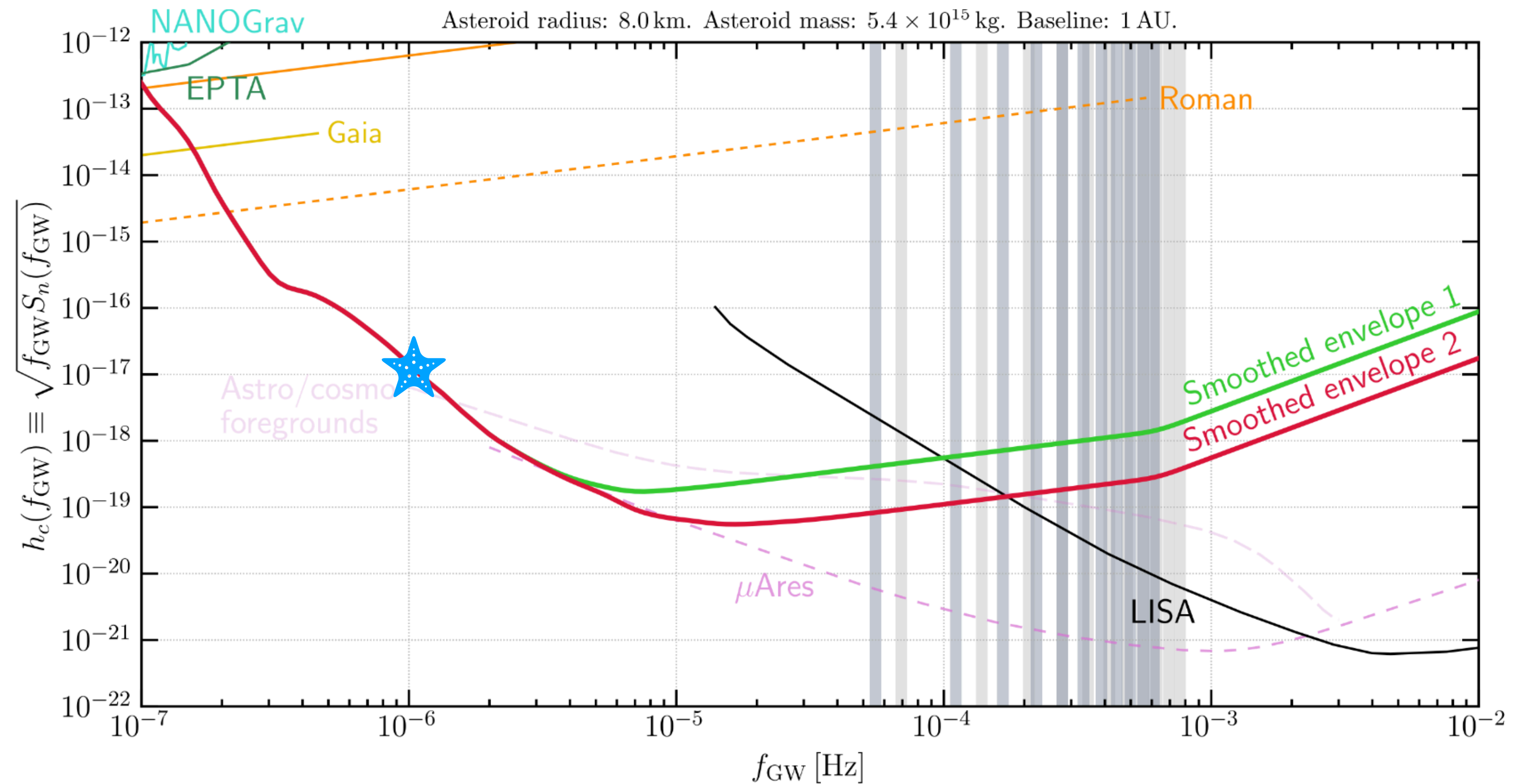
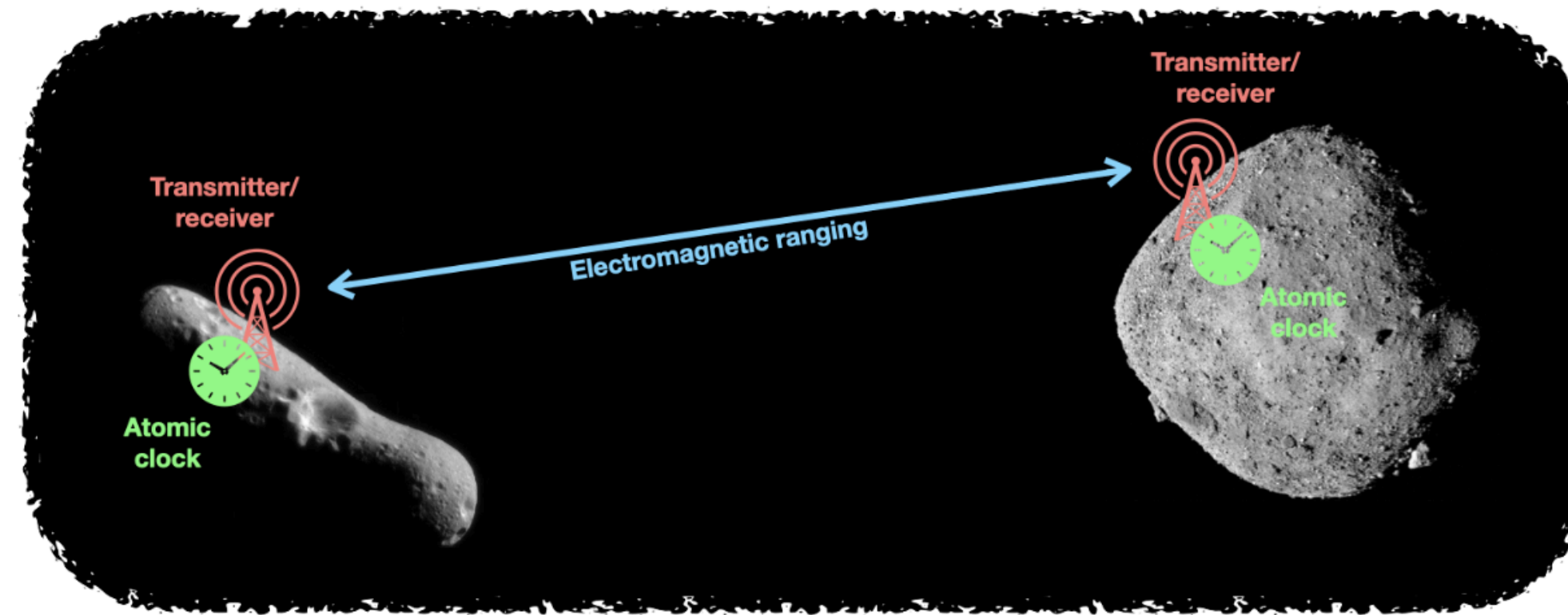
# The $\mu$ Ares detection landscape





# ii) Ranging of asteroids?

Fedderke et al 2112.11431





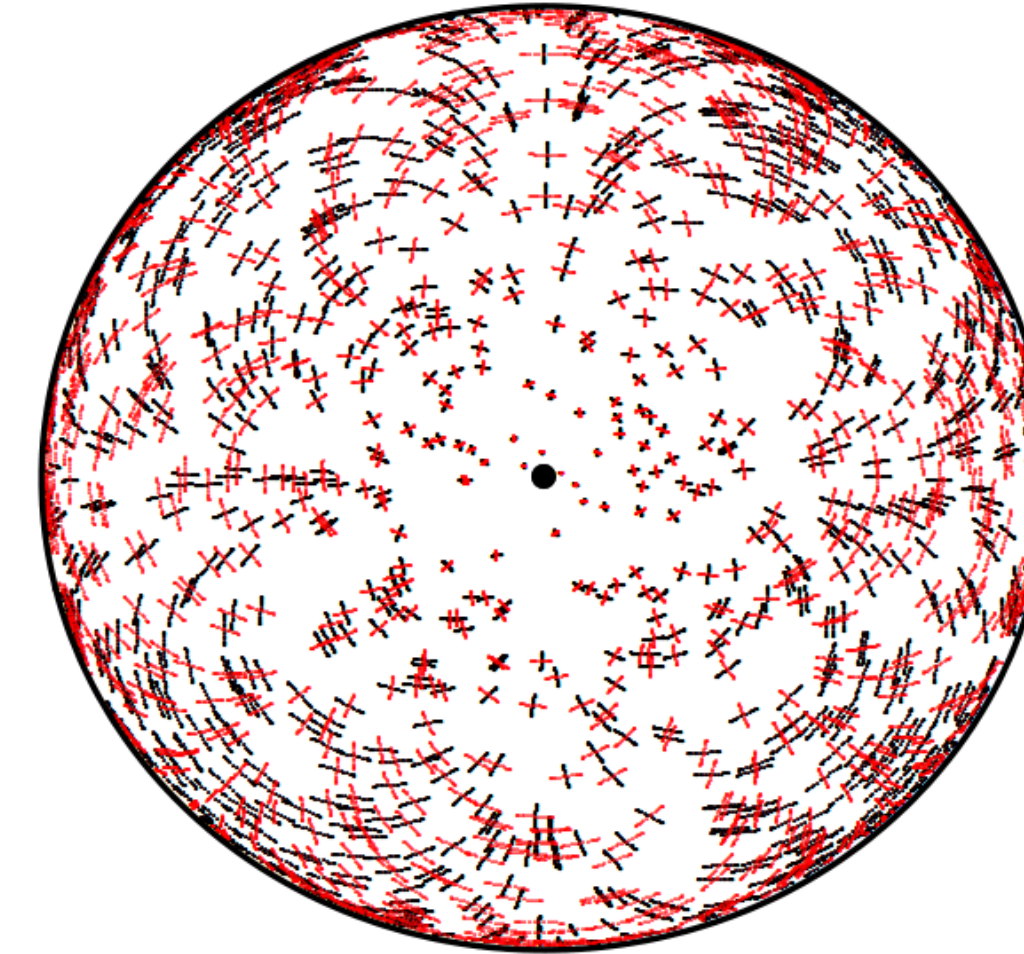
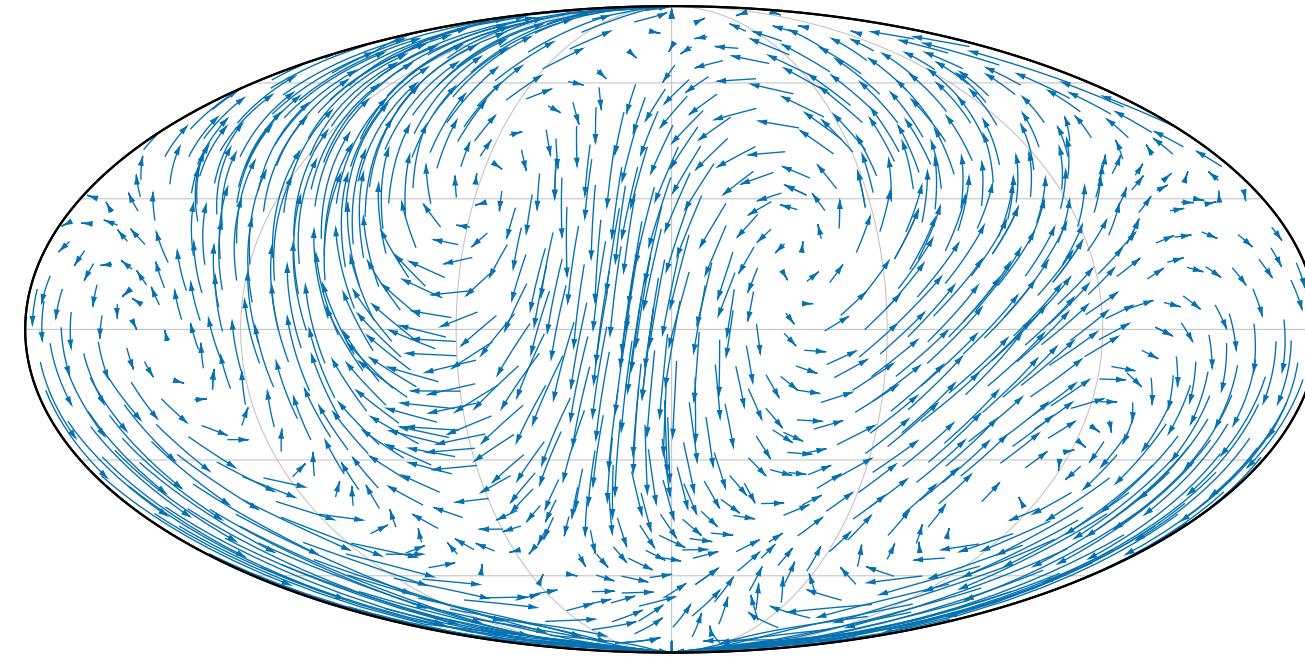
# iii) Future astrometry?

e.g. Moore et al 1707.06239  
Mihaylov et al. 1804.00660

Klioner 1710.11474

Garcia-Bellido et al. 2104.04778

## Monitoring many stars (GAIA or better)



Fedderke et al 2204.07677

## Stellar interferometry

We evaluate the potential for gravitational-wave (GW) detection in the frequency band from 10 nHz to 1  $\mu$ Hz using extremely high-precision astrometry of a small number of stars

at characteristic strains around  $h_c \sim 10^{-17} \times (\mu\text{Hz}/f_{\text{GW}})$ . The astrometric angular precision required to see these sources is  $\Delta\theta \sim h_c$  after integrating for a time  $T \sim 1/f_{\text{GW}}$ . We show that jitter in the photometric center of WD of this type due to starspots is bounded to be small enough to permit this high-precision, small- $N$  approach. We discuss possible noise arising from stellar reflex motion induced by orbiting objects and show how it can be mitigated. The only plausible technology able to achieve the requisite astrometric precision is a space-based stellar interferometer. Such a future mission with few-meter-scale collecting dishes and baselines of  $\mathcal{O}(100 \text{ km})$  is sufficient to achieve the target precision. This collector size is broadly in line with the collectors proposed for

Çalışkan et al 2312.03069



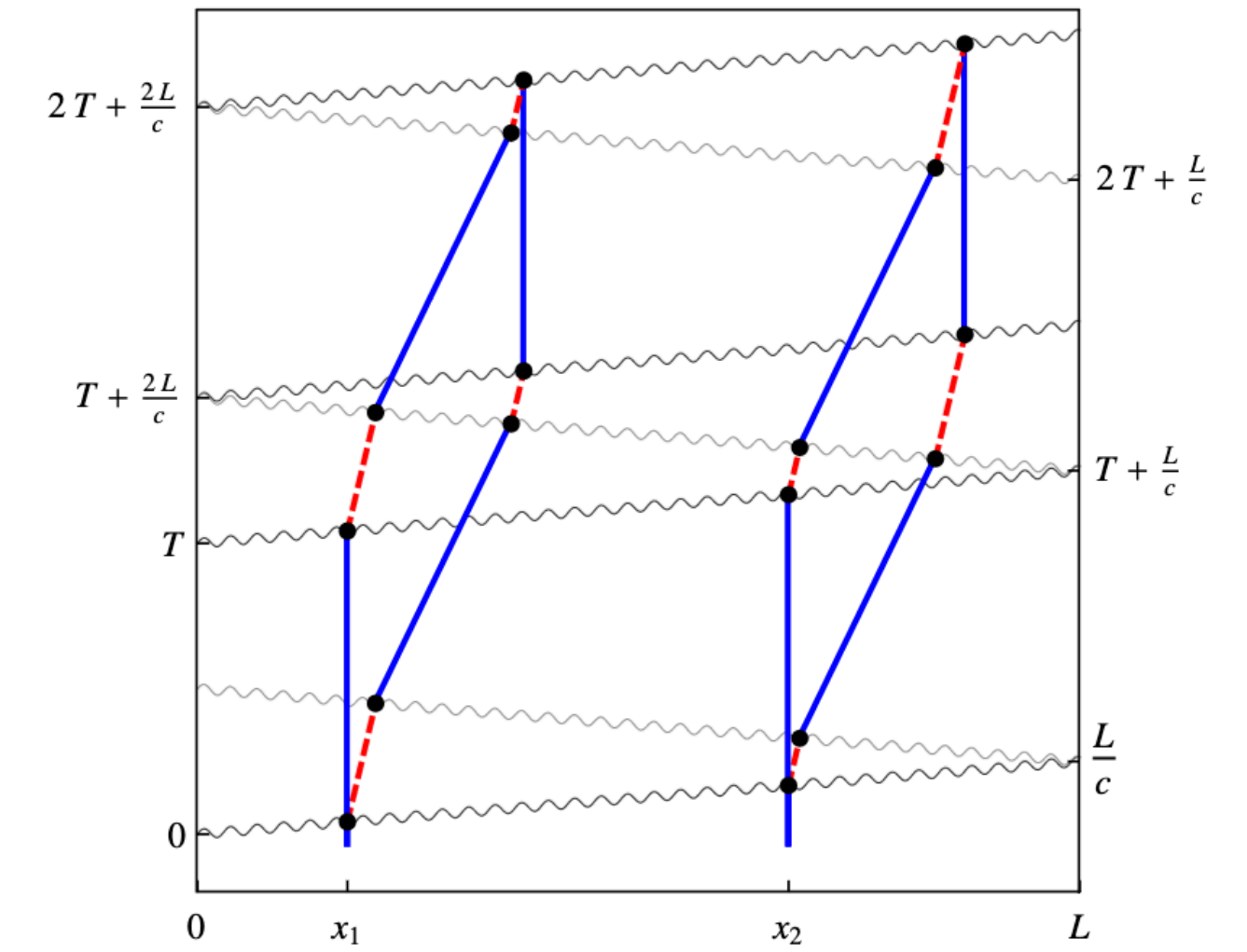
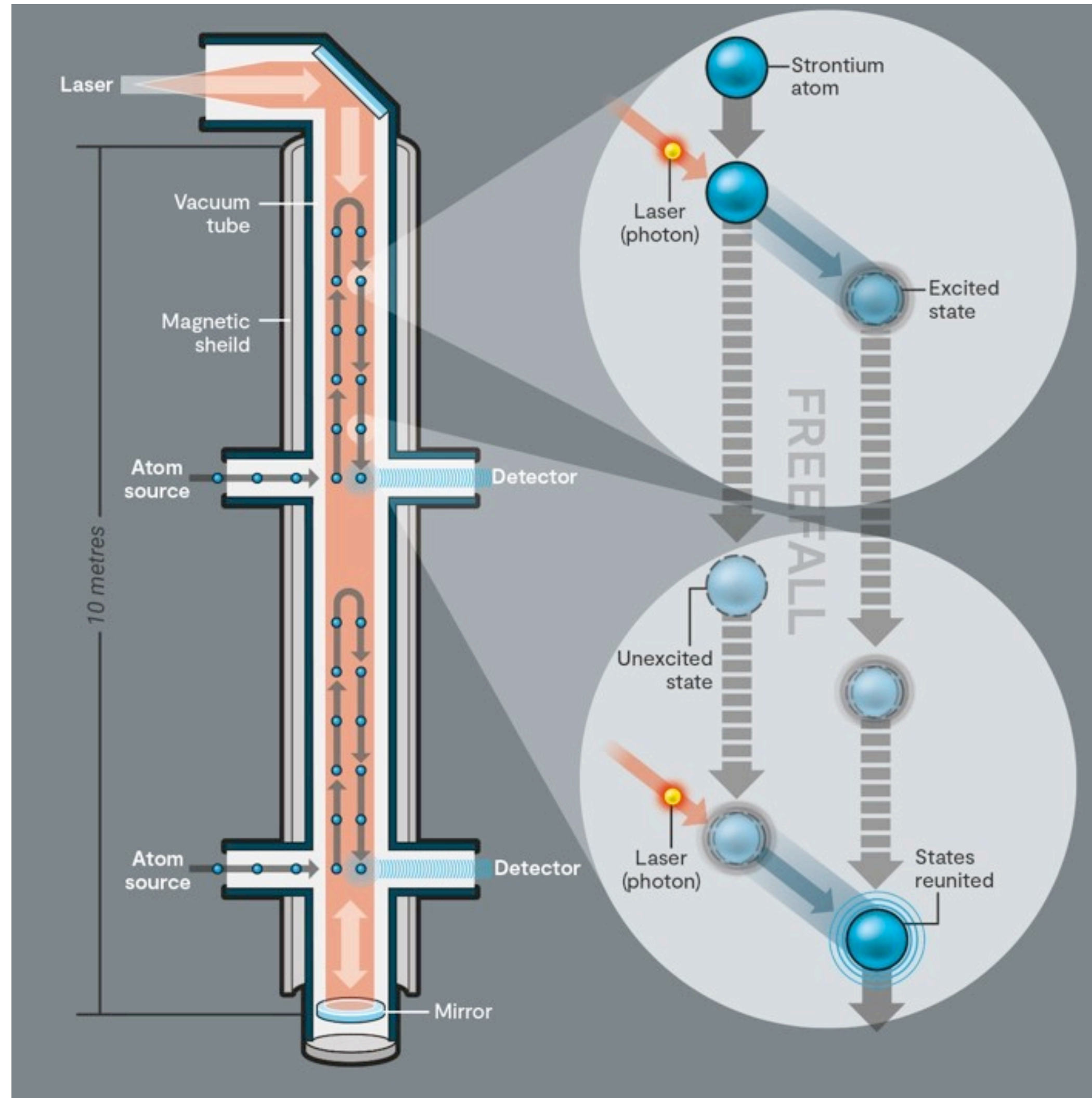
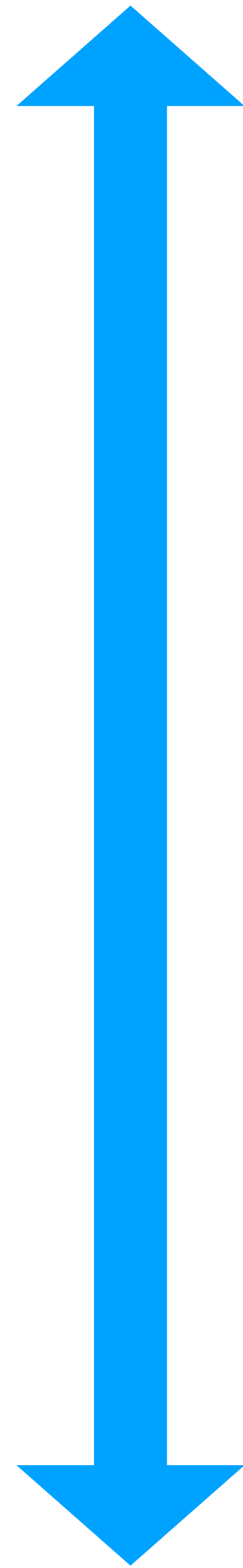
# iv) Atomic interferometry in space: AEDGE

Abou El-Neaj et al 1908.00802

Graham et al 1206.0818 (MAGIS)

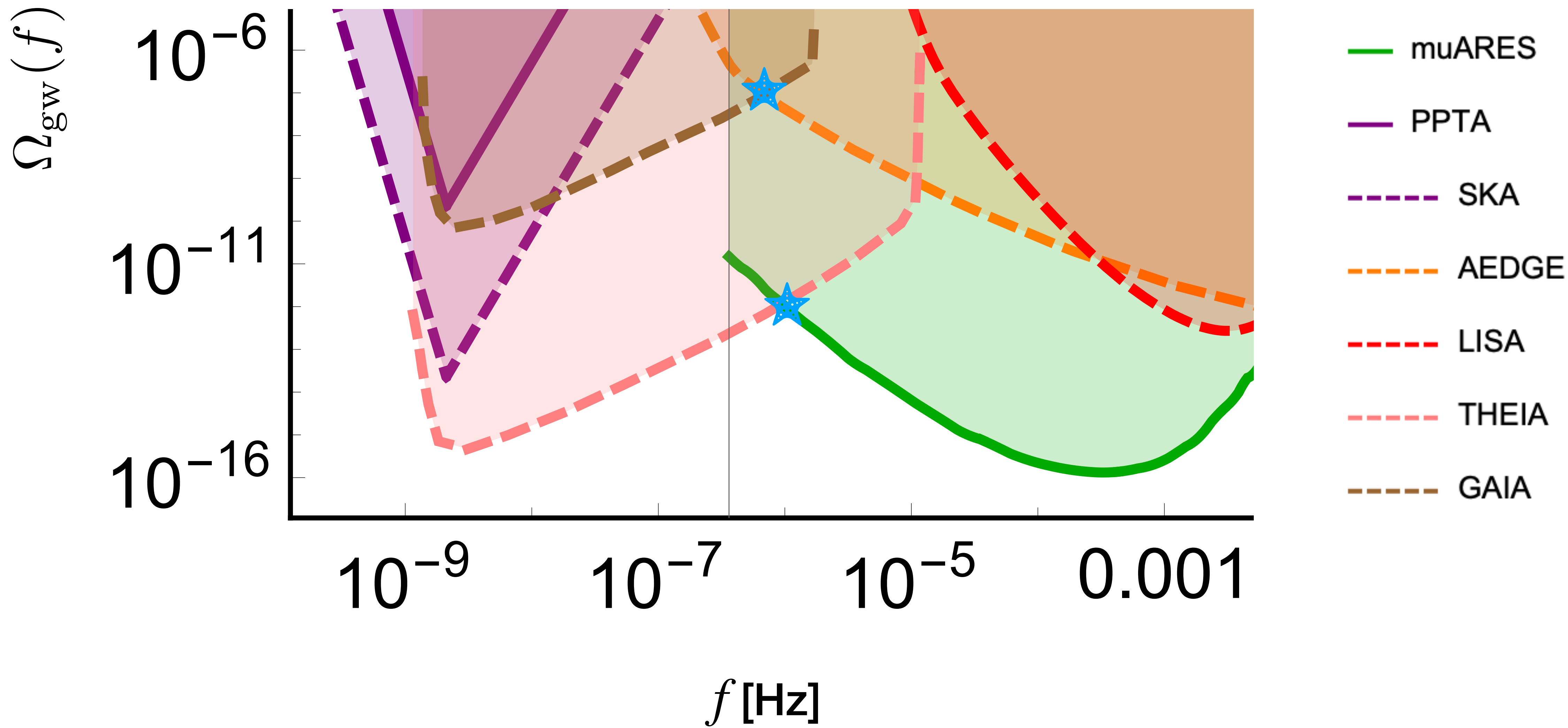
Badurina et al 2108.02468 (AION)

40000 km



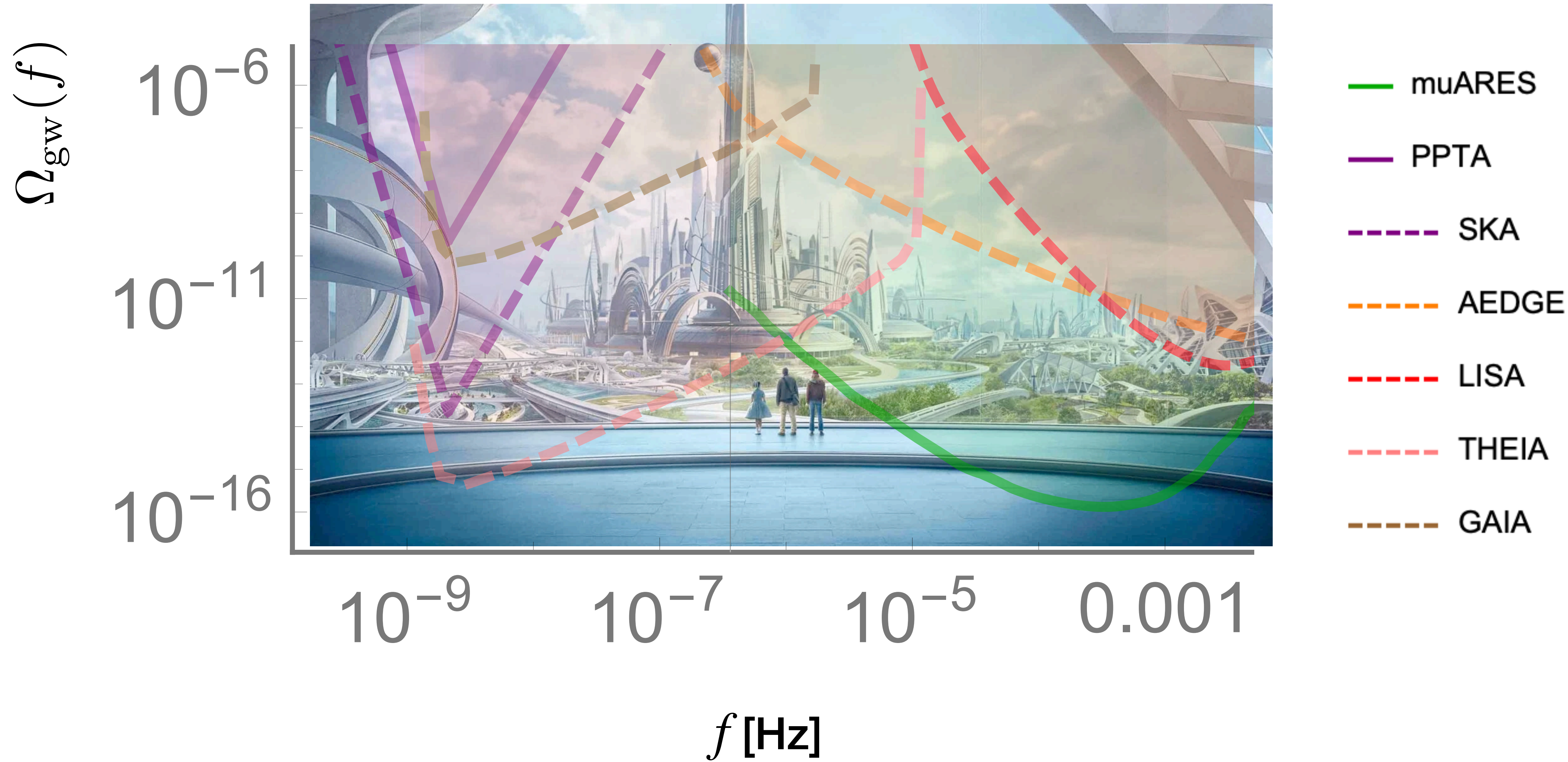
$$\Delta\phi \sim \omega Lh$$

# The most optimistic future...



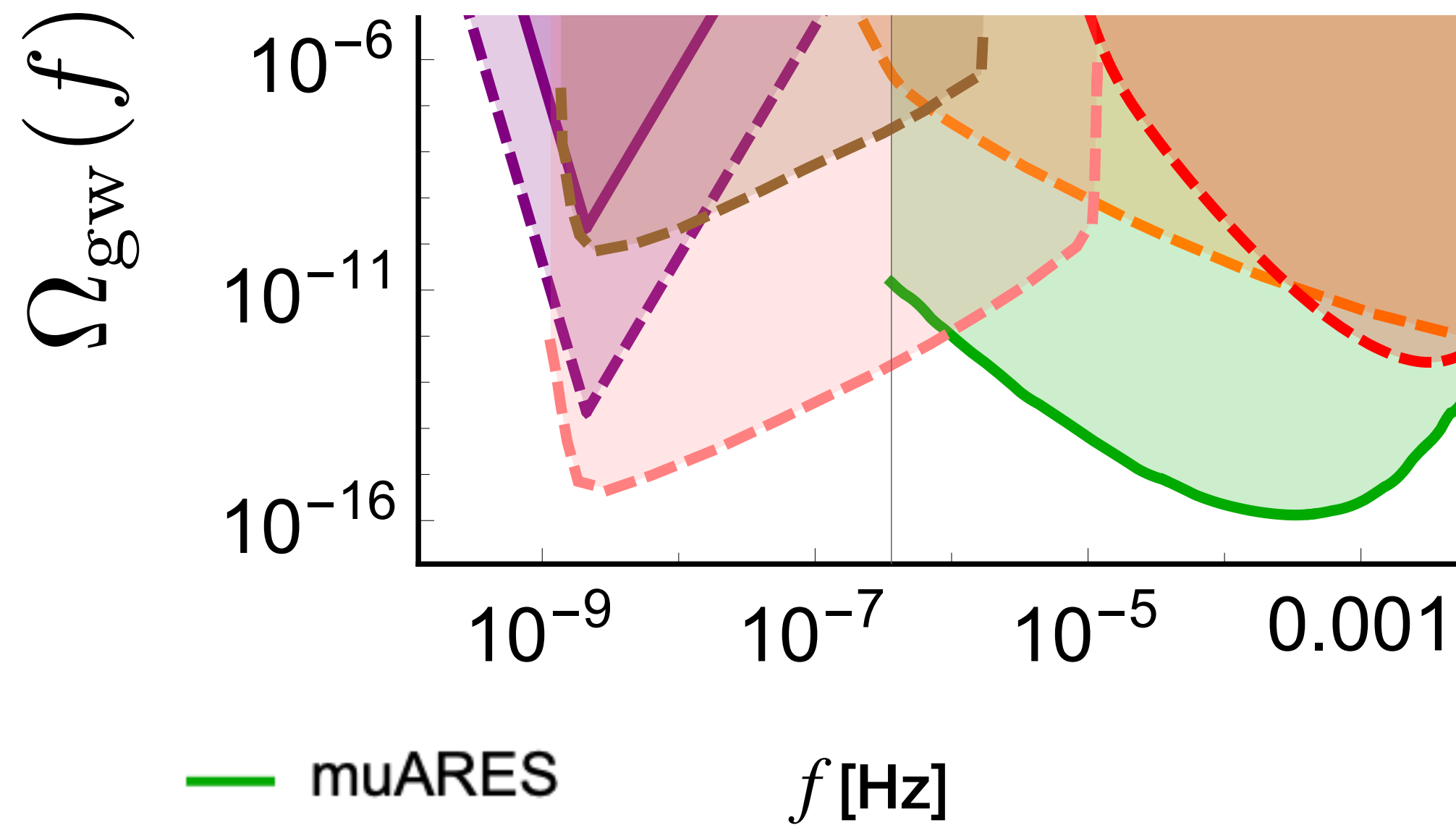


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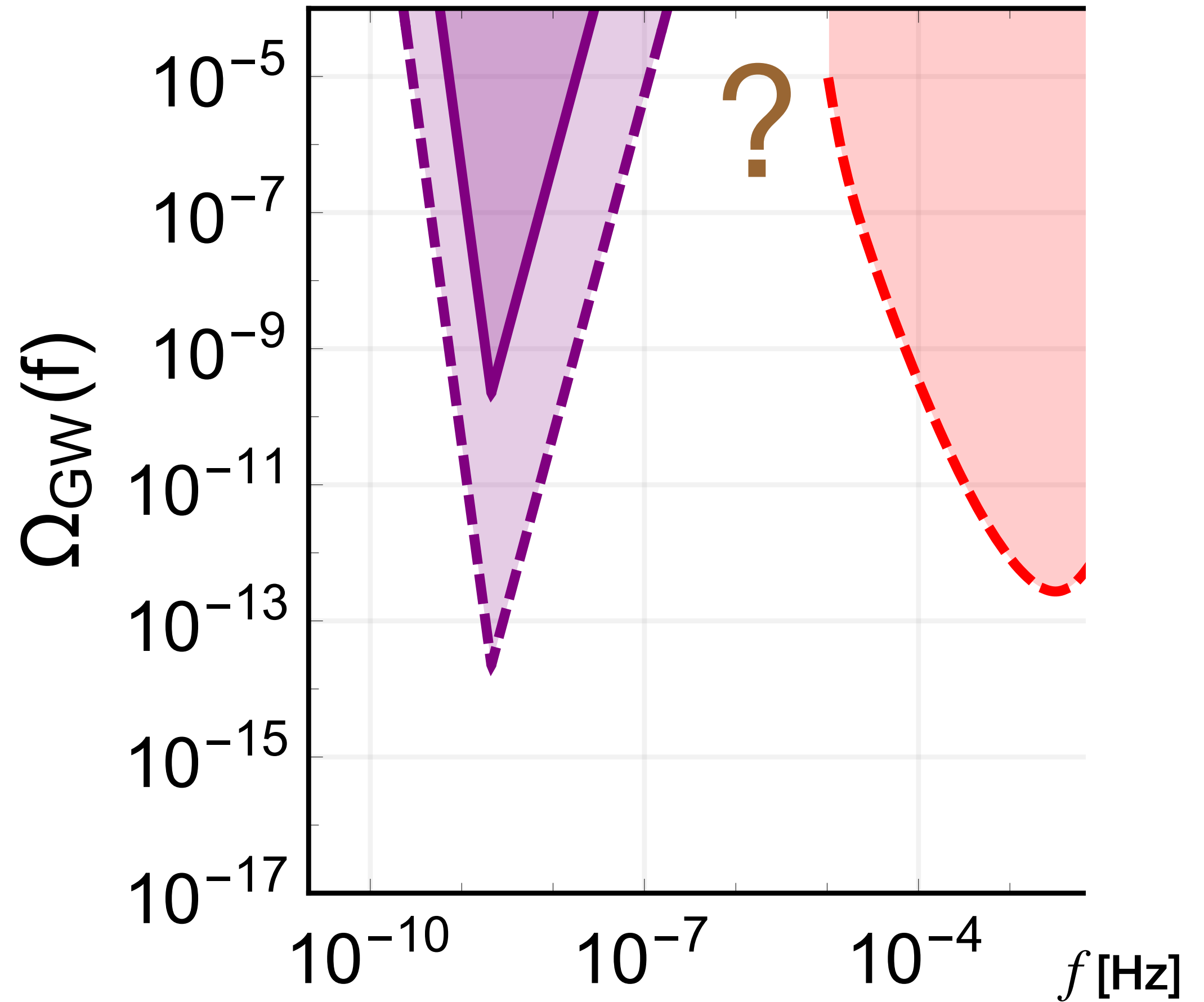




# The most optimistic future... vs 2038



- muARES
- PPTA
- - - SKA
- - - AEDGE
- - - LISA
- - - THEIA
- - - GAIA



GAIA DR3

Jaraba et al 2304.06350

$$h_{70}^2 \Omega_{\text{GW}} \lesssim 0.087 \text{ for } 4.2 \times 10^{-18} \text{ Hz} \lesssim f \lesssim 1.1 \times 10^{-8} \text{ Hz}$$

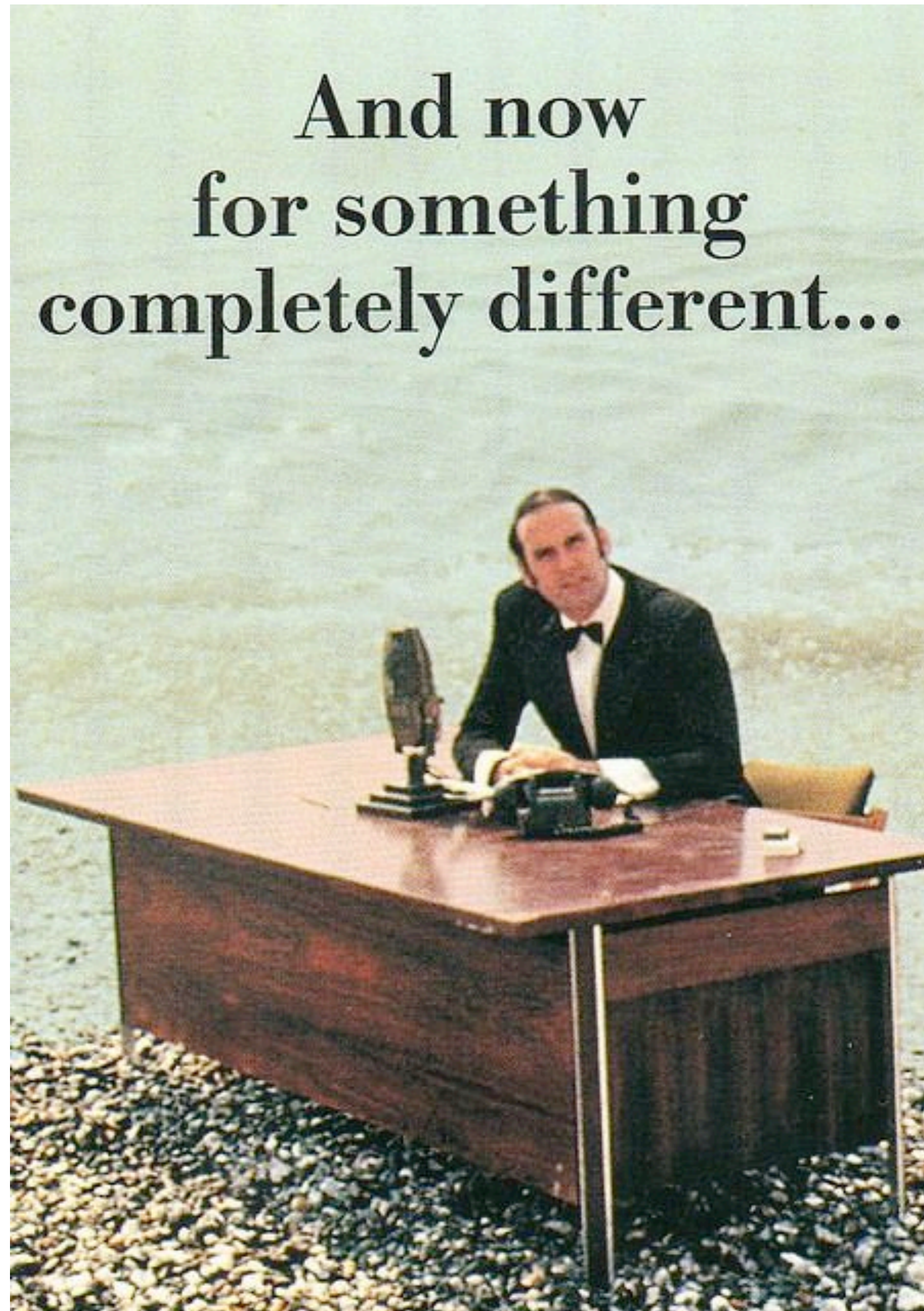
ROMAN?

Wang et al 2205.07962

AION 10m/MAGIS 100m in 2025? (small interferometers)



Is this all we can do in this band?



$$f \sim \mu\text{Hz}$$

few days



# Absorption of GWs by binaries

$$f \sim \mu\text{Hz}$$

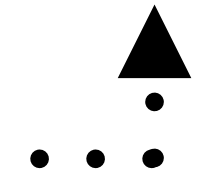
few days

## Intuitive idea (from '60s)

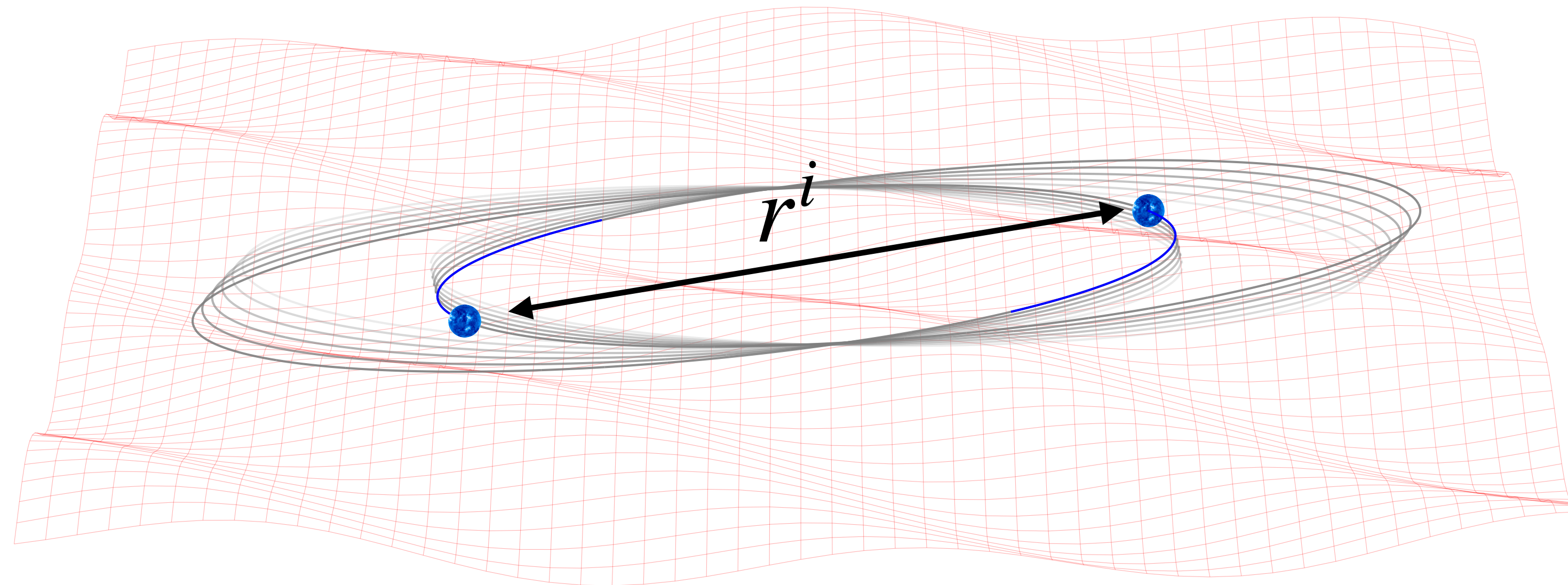
Influence of a GW on a binary system (e.g. non-relativistic)

$$\ddot{r}^i + \frac{GM}{r^3} r^i = \delta^{ik} \frac{1}{2} \ddot{h}_{kj} r^j$$

Newtonian potential



GW



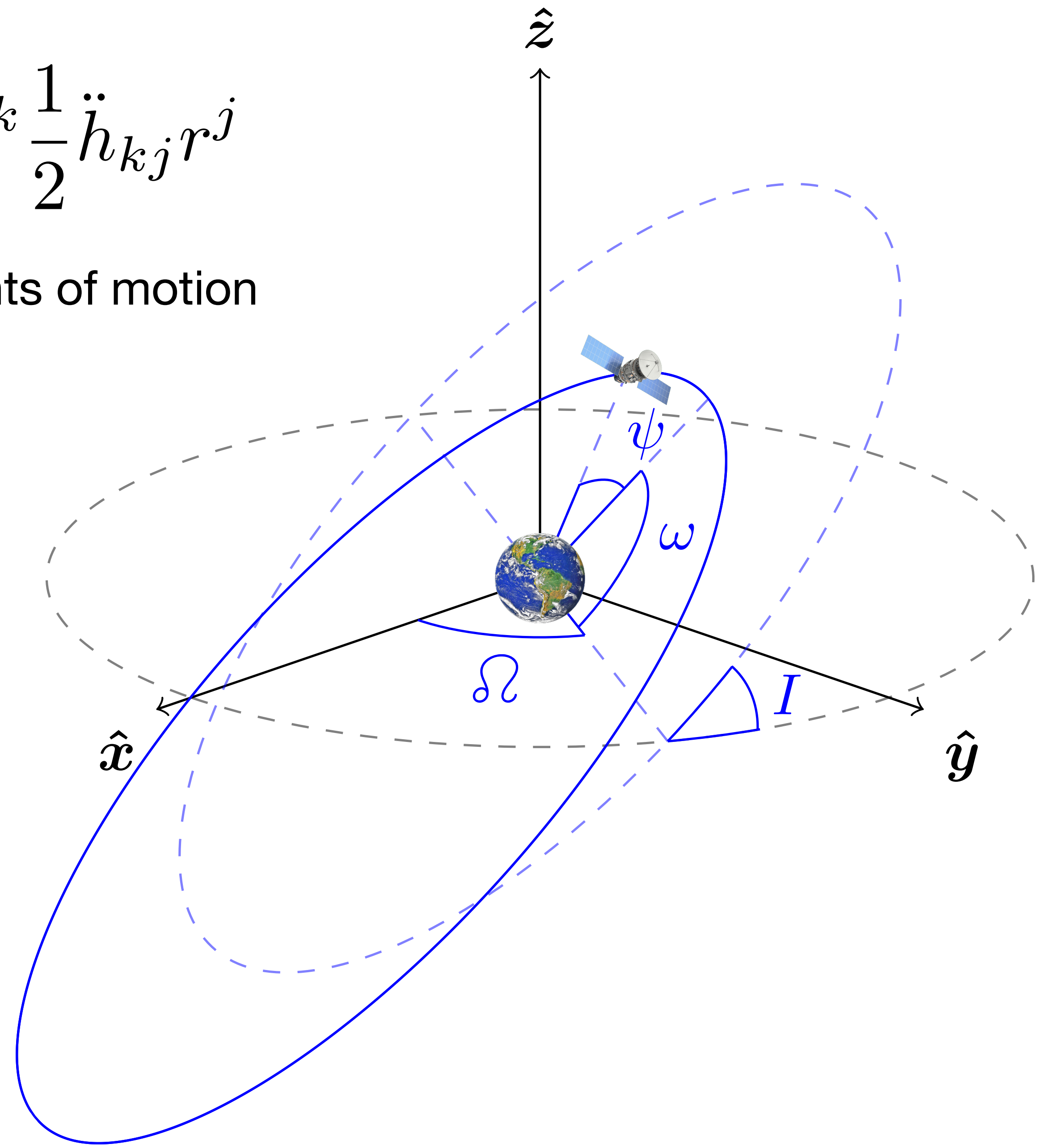


# Absorption of GWs by binaries

$$\ddot{r}^i + \frac{GM}{r^3} r^i = \delta^{ik} \frac{1}{2} \ddot{h}_{kj} r^j$$

Better characterised for its 6 Newtonian constants of motion


- **period  $P$ , eccentricity  $e$ :**  
*size and shape of orbit*
- **inclination  $I$ , ascending node  $\Omega$ :**  
*orientation in space*
- **pericentre  $\omega$ ,  
mean anomaly at epoch  $\varepsilon$ :**  
*radial and angular phases*



# Absorption of GWs by binaries

$$\ddot{\mathbf{r}} + \frac{GM}{r^2} \hat{\mathbf{r}} = \delta\ddot{\mathbf{r}}.$$

■ for generic perturbation:

$$\delta\ddot{\mathbf{r}} = r(\mathcal{F}_r \hat{\mathbf{r}} + \mathcal{F}_\theta \hat{\boldsymbol{\theta}} + \mathcal{F}_\ell \hat{\boldsymbol{\ell}}),$$


$$\dot{P} = \frac{3P^2\gamma}{2\pi} \left[ \frac{e \sin \psi \mathcal{F}_r}{1 + e \cos \psi} + \mathcal{F}_\theta \right],$$

$$\dot{e} = \frac{\dot{P}\gamma^2}{3Pe} - \frac{P\gamma^5 \mathcal{F}_\theta}{2\pi e(1 + e \cos \psi)^2},$$

$$\dot{I} = \frac{P\gamma^3 \cos \theta \mathcal{F}_\ell}{2\pi(1 + e \cos \psi)^2},$$

$$\dot{\Omega} = \frac{\tan \theta}{\sin I} \dot{I},$$

$$\dot{\omega} = \frac{P\gamma^3}{2\pi e} \left[ \frac{(2 + e \cos \psi) \sin \psi \mathcal{F}_\theta}{(1 + e \cos \psi)^2} - \frac{\cos \psi \mathcal{F}_r}{1 + e \cos \psi} \right] - \cos I \dot{\Omega},$$

$$\dot{\epsilon} = -\frac{P\gamma^4 \mathcal{F}_r}{\pi(1 + e \cos \psi)^2} - \gamma(\cos I \dot{\Omega} + \dot{\omega}),$$



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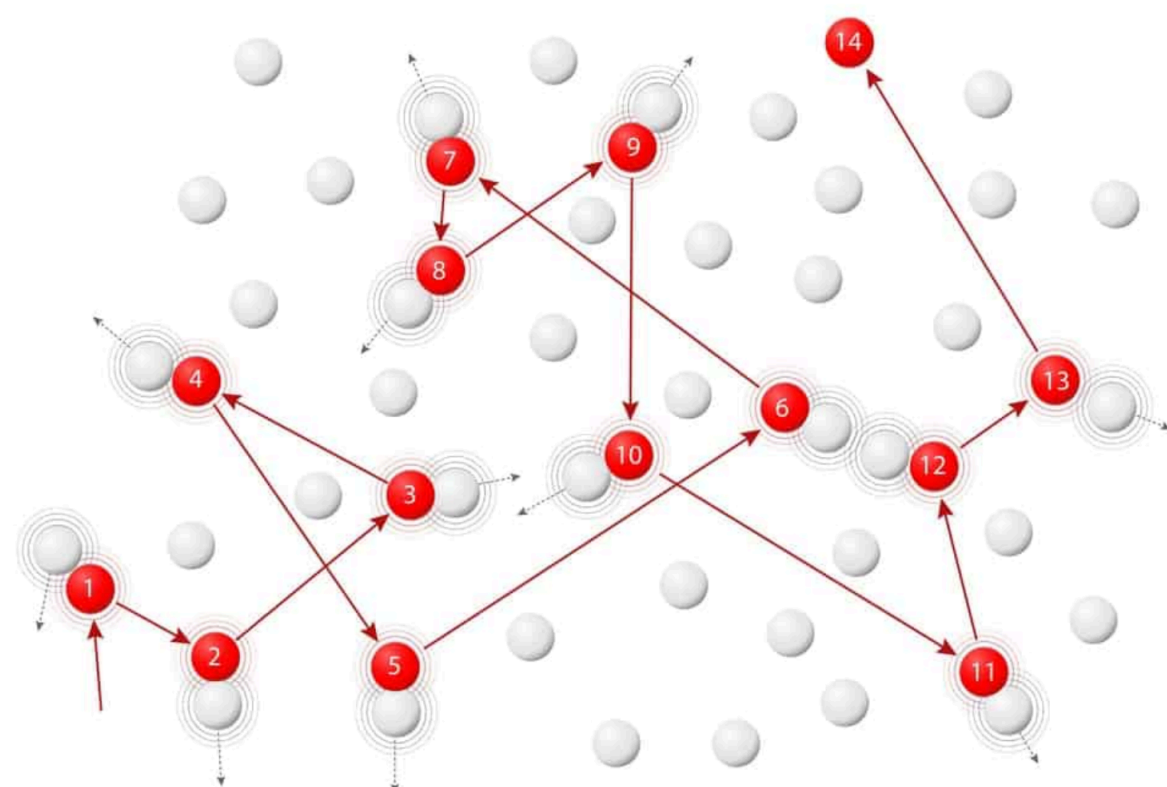
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# For the SGWB... Fokker-Planck approach

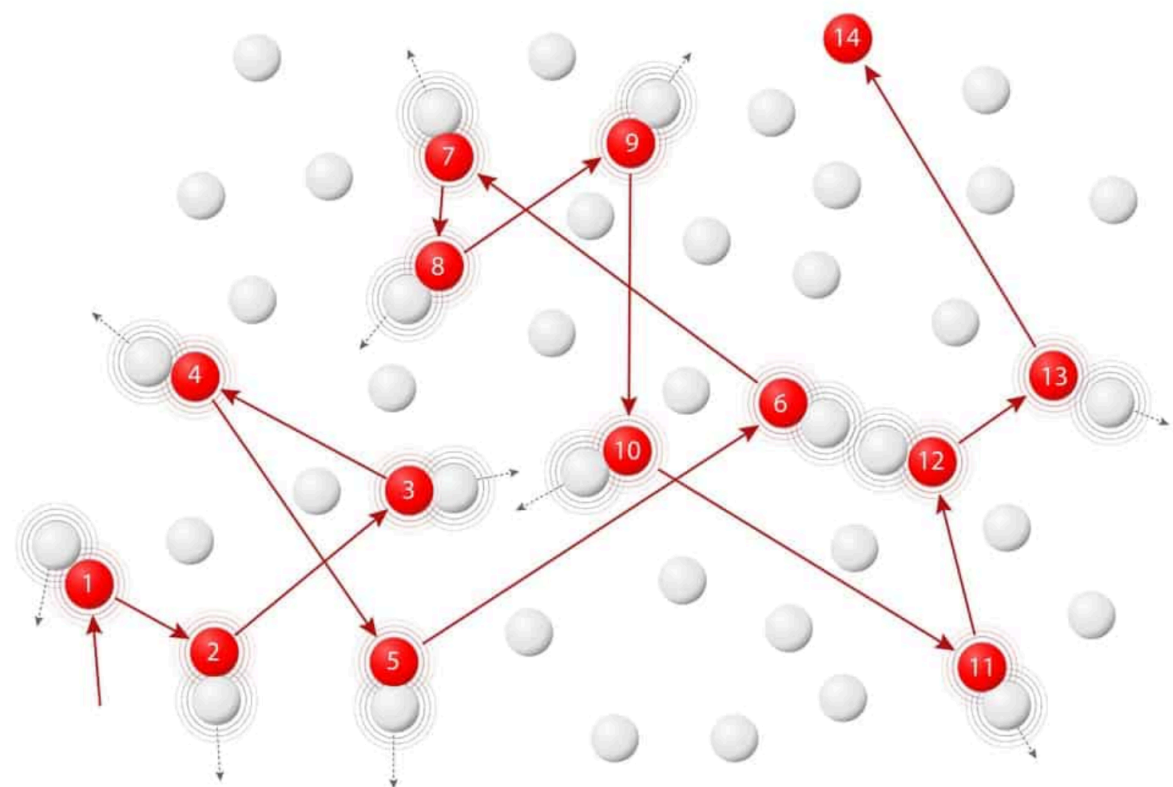
$$\ddot{r}^i + \frac{GM}{r^3} r^i = \delta^{ik} \frac{1}{2} \ddot{h}_{kj} r^j$$

deterministic

$$\dot{X}_i(\mathbf{X}, t) = V_i(\mathbf{X}) + \Gamma_i(\mathbf{X}, t)$$

stochastic

we move from dynamics of the variable to dynamics of the **distribution  $W(\mathbf{X})$**



$$\frac{\partial W}{\partial t} = -\partial_i \left( D_i^{(1)} W \right) + \partial_i \partial_j \left( D_{ij}^{(2)} W \right)$$

with  $\partial_i \equiv \partial / \partial X_i$

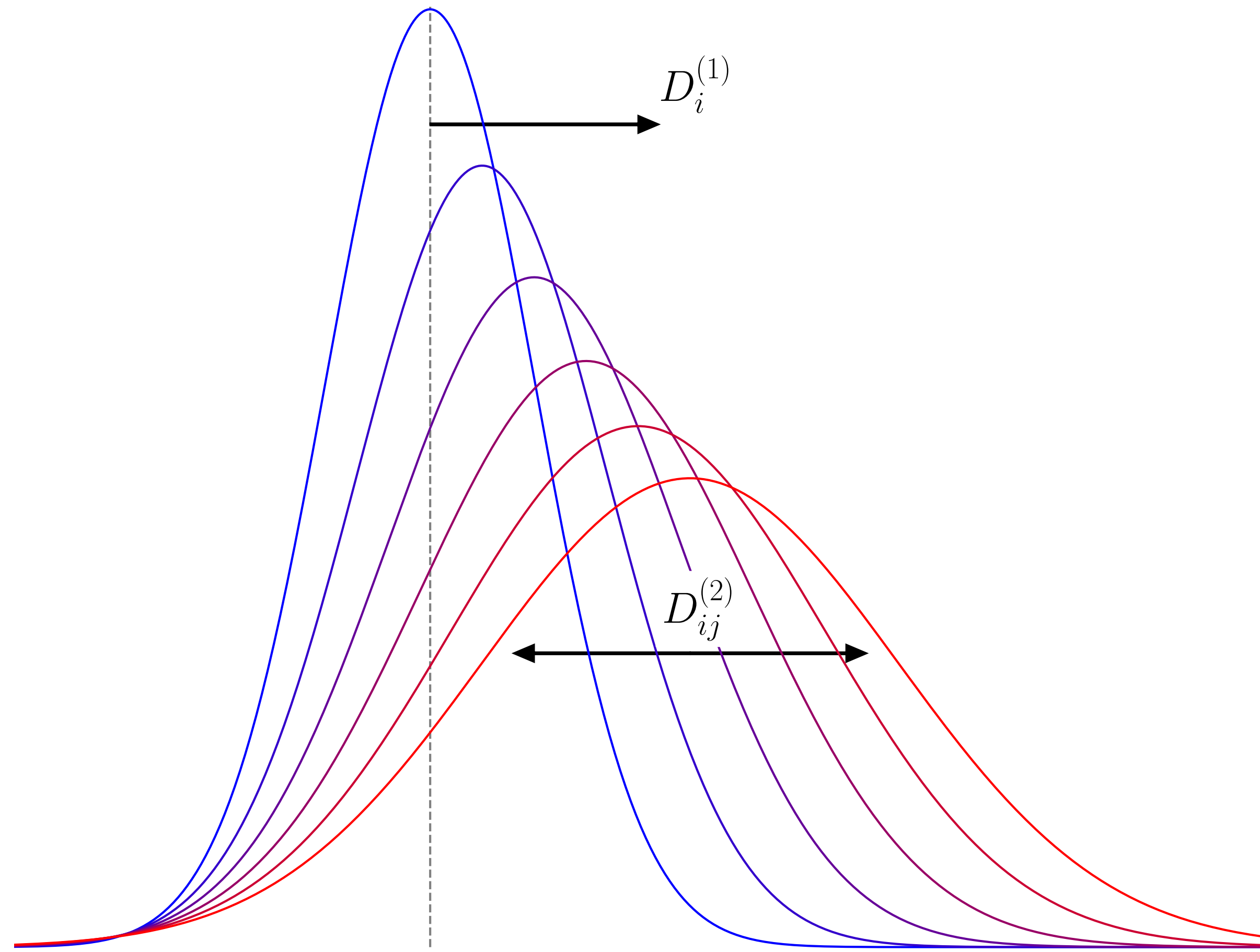
$$D_i^{(1)} = V_i + \lim_{\tau \rightarrow 0} \frac{1}{\tau} \int_t^{t+\tau} dt' \int_t^{t'} dt'' \langle \Gamma_j(\mathbf{x}, t'') \partial_j \Gamma_i(\mathbf{x}, t') \rangle .$$

$$D_{ij}^{(2)} = \lim_{\tau \rightarrow 0} \frac{1}{2\tau} \int_t^{t+\tau} dt' \int_t^{t'+\tau} dt'' \langle \Gamma_i(\mathbf{x}, t') \Gamma_j(\mathbf{x}, t'') \rangle .$$



# Our approach to the problem

Blas&Jenkins Phys.Rev.Lett. 128 (2022) 10, 101103



- track distribution function  $W(\mathbf{X}, t)$  of orbital elements  $\mathbf{X} = (P, e, I, \delta\Omega, \omega, \varepsilon)$
- evolves through *Fokker-Planck eqn.*

$$\frac{\partial W}{\partial t} = -\frac{\partial}{\partial X_i} \left( D_i^{(1)} W \right) + \frac{\partial}{\partial X_i} \frac{\partial}{\partial X_j} \left( D_{ij}^{(2)} W \right)$$

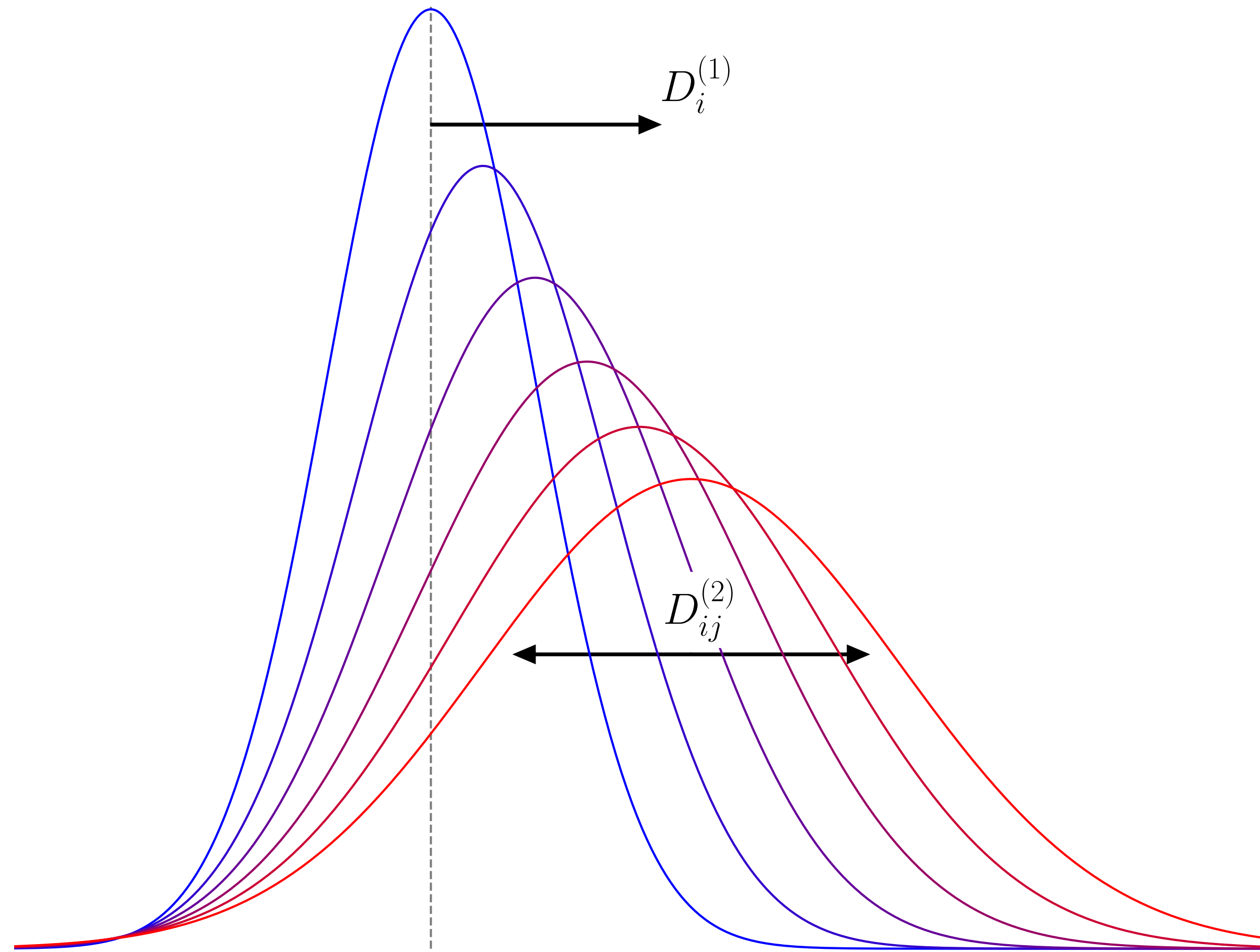
- *drift and diffusion coefficients*  
(averaged over orbits)

$$D_i^{(1)}(\mathbf{X}) = V_i(\mathbf{X}) + \sum_{n=1}^{\infty} \mathcal{A}_{n,i}(\mathbf{X}) \Omega_{\text{gw}}(n/P)$$

$$D_{ij}^{(2)}(\mathbf{X}) = \sum_{n=1}^{\infty} \mathcal{B}_{n,ij}(\mathbf{X}) \Omega_{\text{gw}}(n/P)$$

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Blas&Jenkins Phys.Rev.Lett. 128 (2022) 10, 101103



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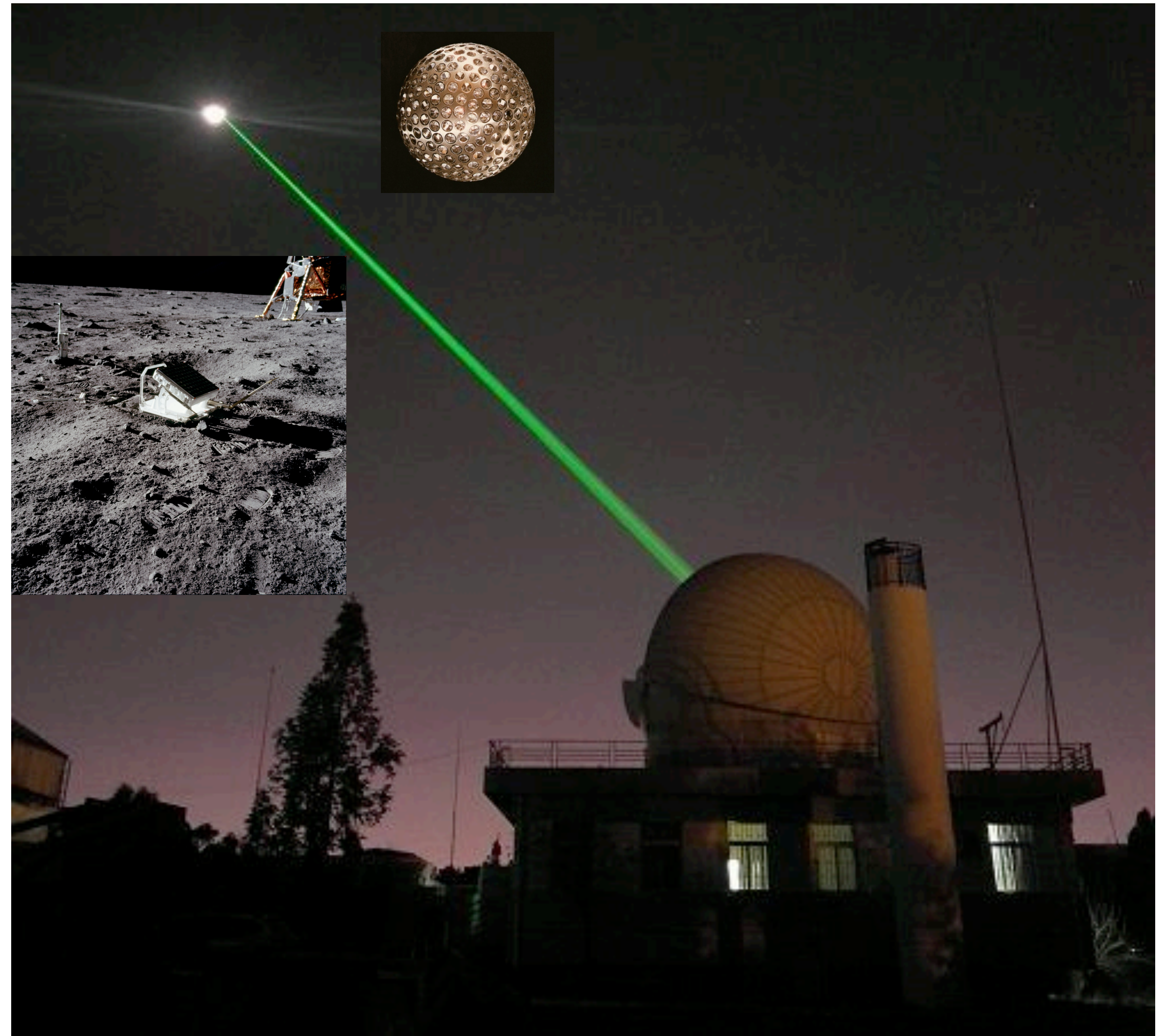
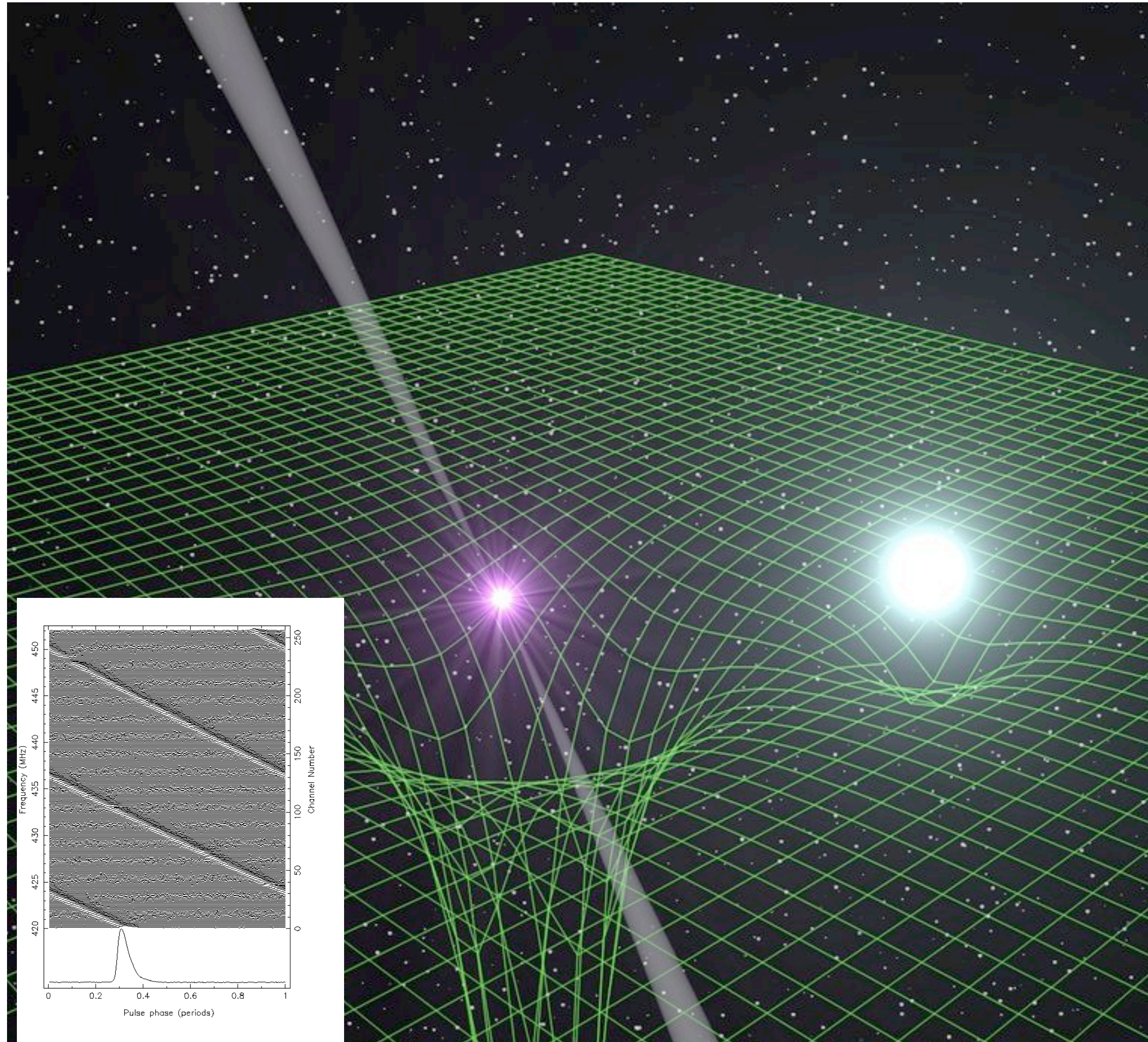
$$D_{ij}^{(2)}(\mathbf{X}) = \sum_{n=1}^{\infty} \mathcal{B}_{n,ij}(\mathbf{X}) \Omega_{\text{gw}}(n/P)$$



# Two probes

timing of binary pulsars

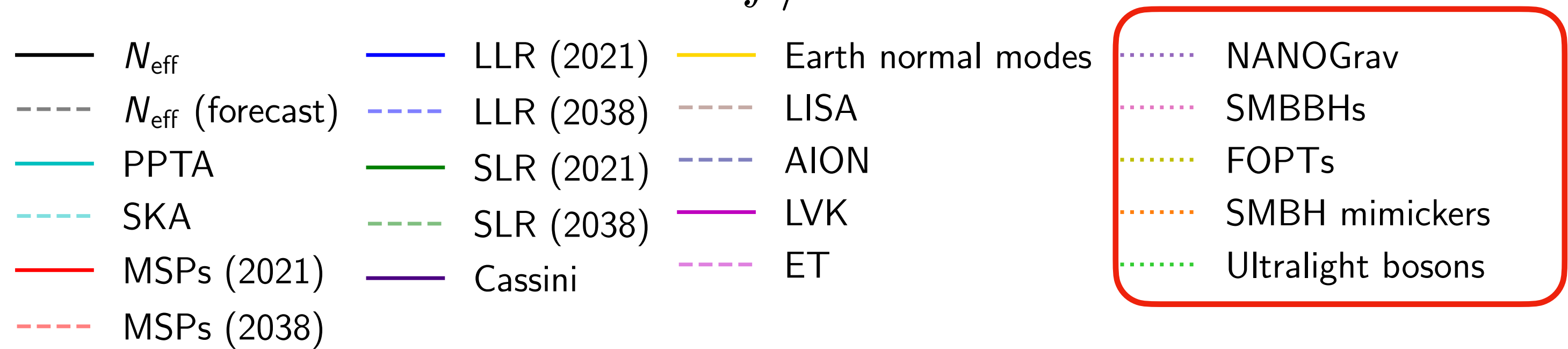
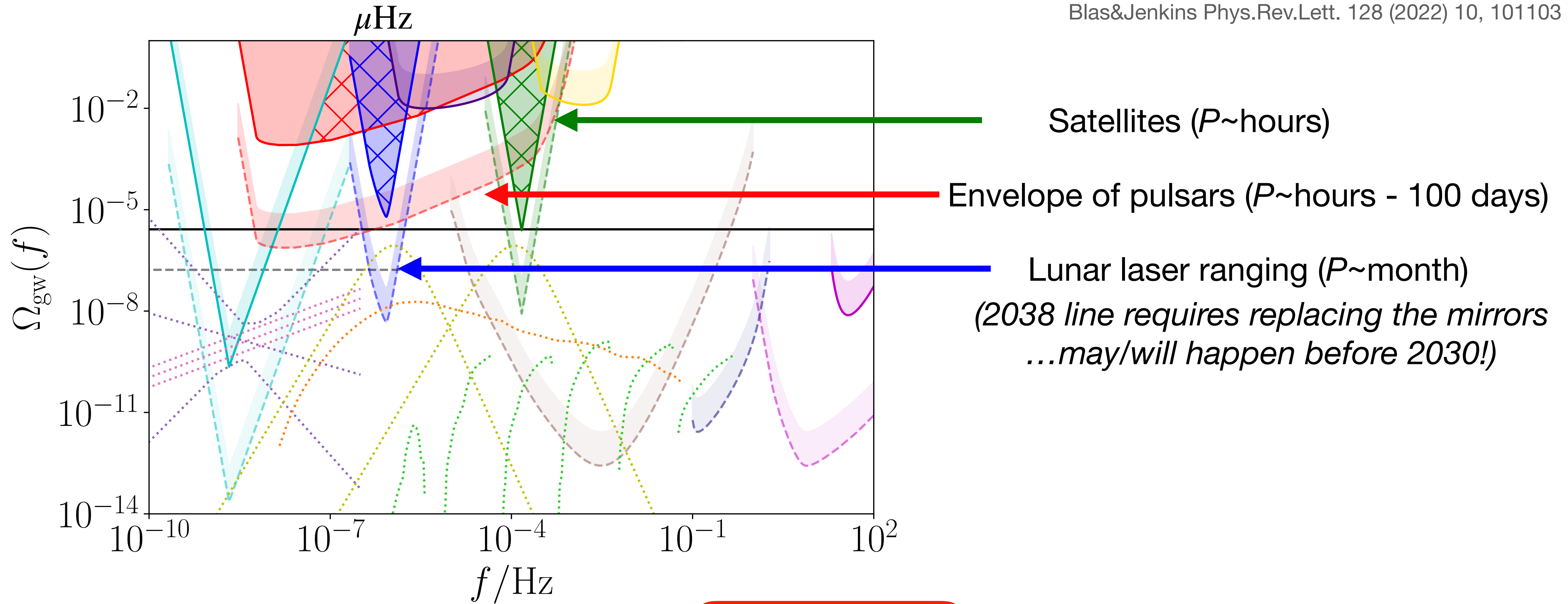
lunar and satellite laser ranging





# Our estimates (solid: today; dashed 2038)

Blas&Jenkins Phys.Rev.Lett. 128 (2022) 10, 101103

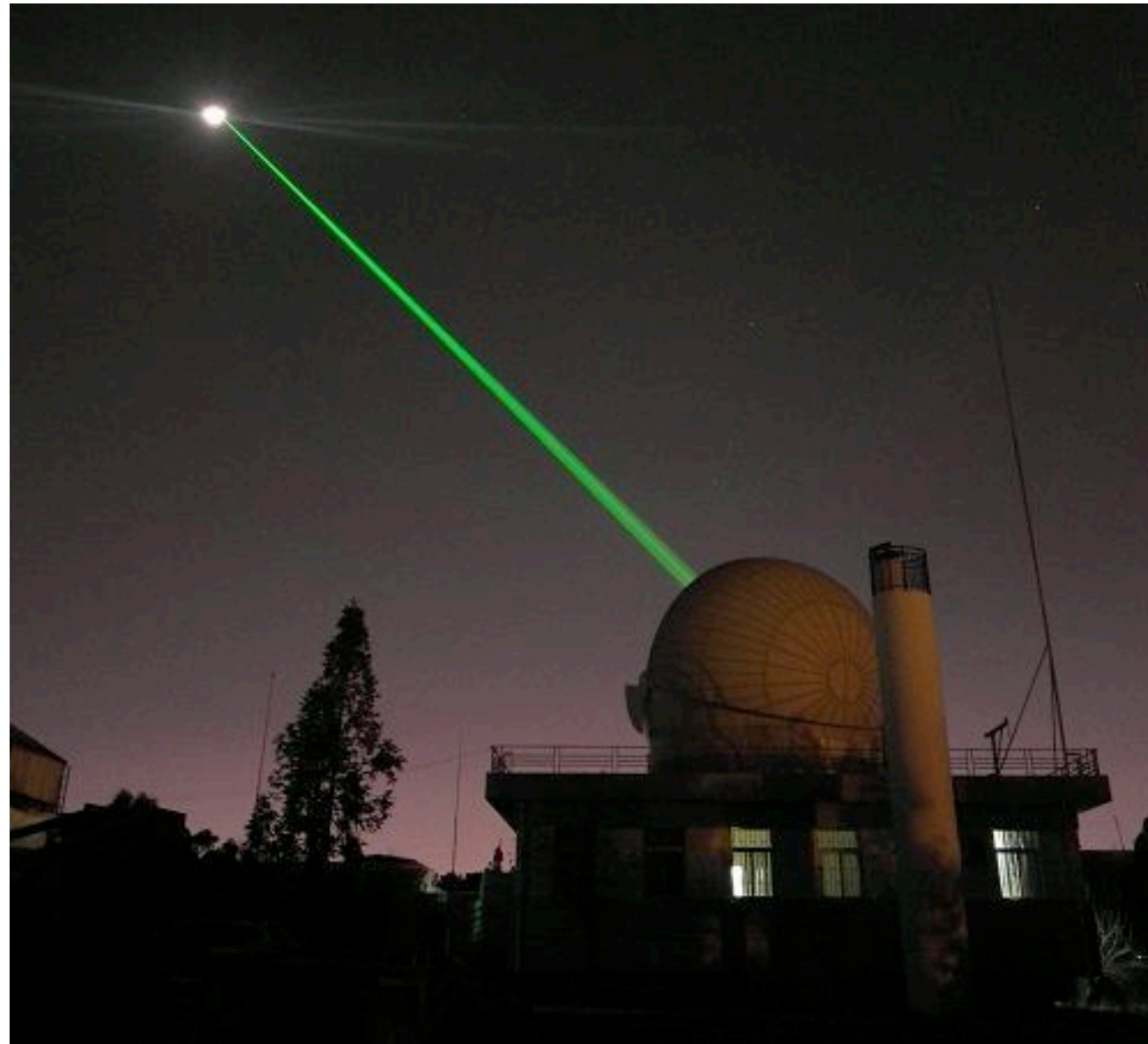
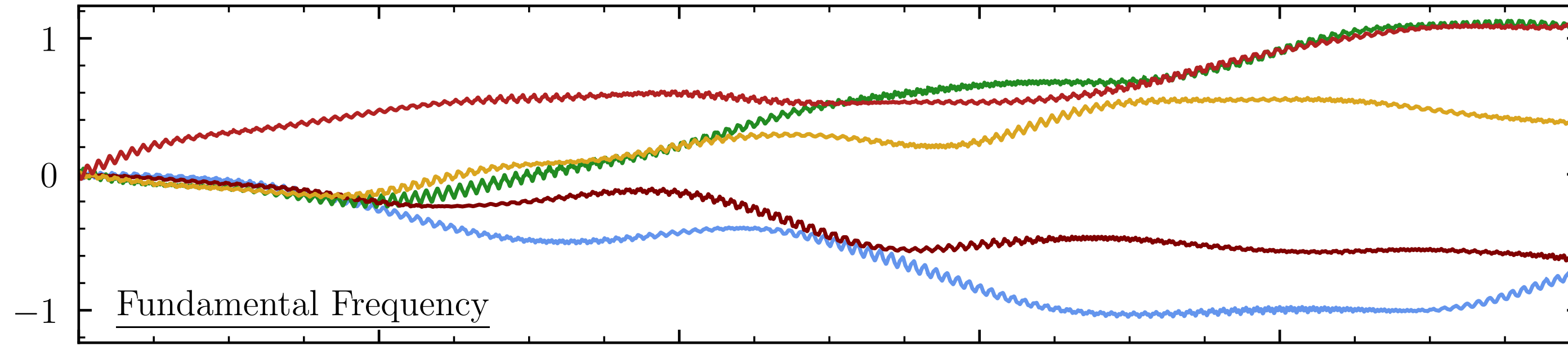


**Possible backgrounds**



# Confirming with simulations

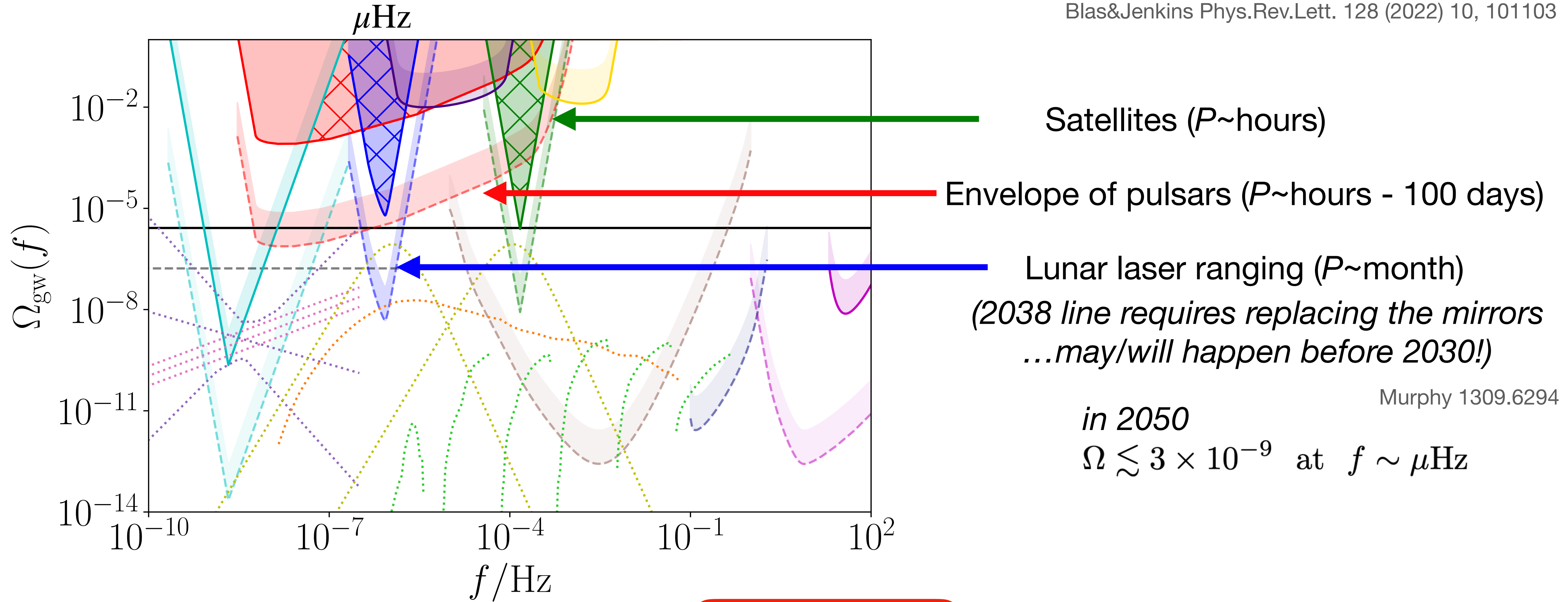
Semi-latus Rectum Perturbation [cm]



Credit: J. Foster  
(work in progress, Blas, Bourguin, Foster, Hees, Herrero, Jenkins)

# Our estimates (solid: today; dashed 2038)

Blas&Jenkins Phys.Rev.Lett. 128 (2022) 10, 101103



Murphy 1309.6294

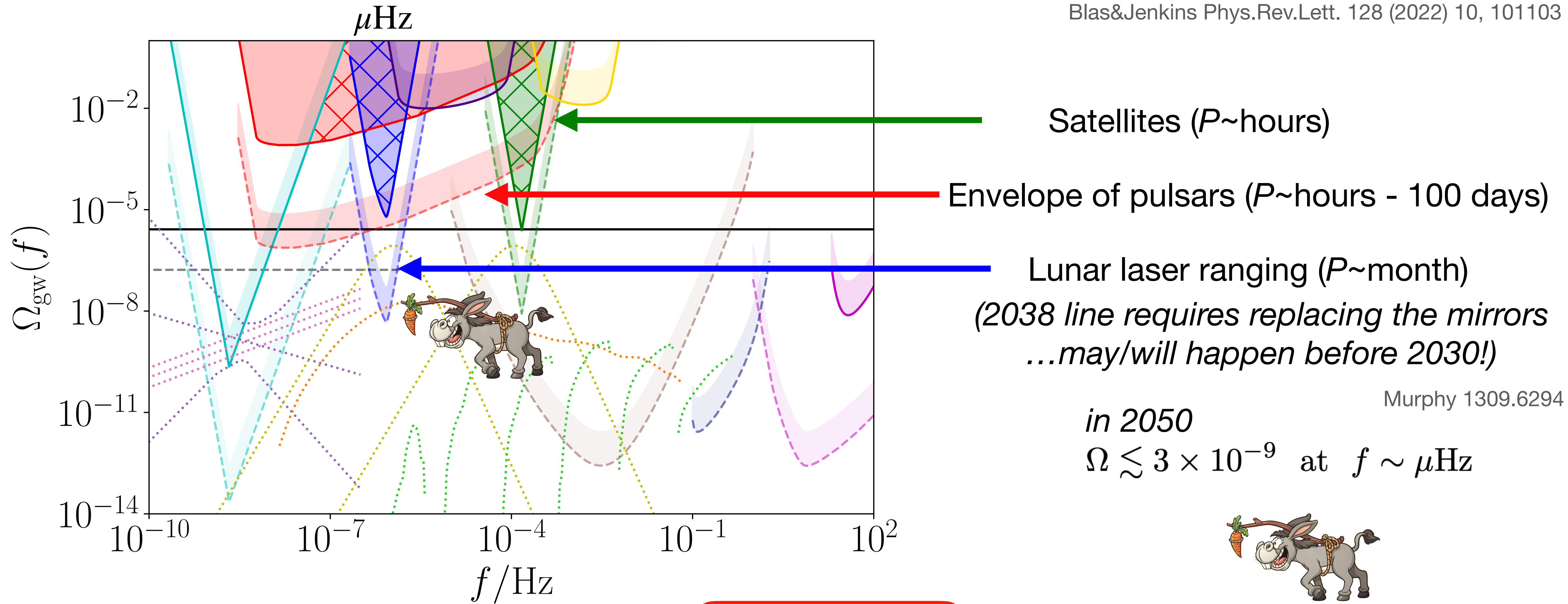
- |                                   |                  |                      |                     |
|-----------------------------------|------------------|----------------------|---------------------|
| — $N_{\text{eff}}$                | — LLR (2021)     | — Earth normal modes | ⋯ NANOGrav          |
| - - - $N_{\text{eff}}$ (forecast) | - - - LLR (2038) | - - - LISA           | ⋯ SMBBHs            |
| — PPTA                            | — SLR (2021)     | - - - AION           | ⋯ FOPTs             |
| - - - SKA                         | - - - SLR (2038) | — LVK                | ⋯ SMBH mimickers    |
| — MSPs (2021)                     | — Cassini        | - - - ET             | ⋯ Ultralight bosons |
| - - - MSPs (2038)                 |                  |                      |                     |

**Possible backgrounds**

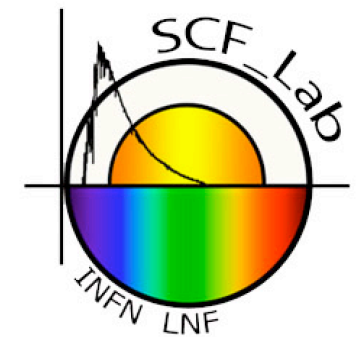
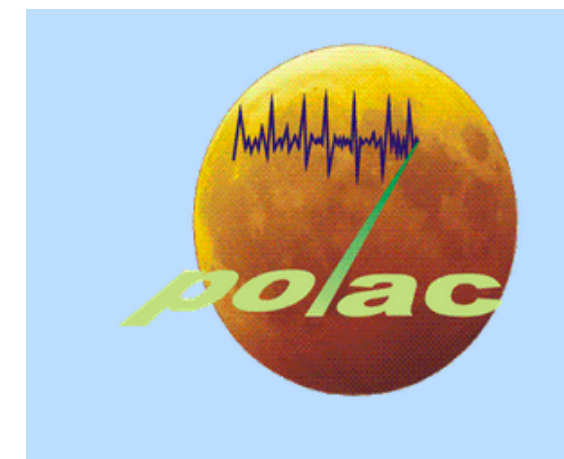


# Our estimates (solid: today; dashed 2038)

Blas&Jenkins Phys.Rev.Lett. 128 (2022) 10, 101103



- |       |                             |       |            |       |                    |   |                   |
|-------|-----------------------------|-------|------------|-------|--------------------|---|-------------------|
| —     | $N_{\text{eff}}$            | —     | LLR (2021) | —     | Earth normal modes | ⋯ | NANOGrav          |
| - - - | $N_{\text{eff}}$ (forecast) | - - - | LLR (2038) | - - - | LISA               | ⋯ | SMBBHs            |
| —     | PPTA                        | —     | SLR (2021) | - - - | AION               | ⋯ | FOPTs             |
| - - - | SKA                         | —     | SLR (2038) | —     | LVK                | ⋯ | SMBH mimickers    |
| —     | MSPs (2021)                 | —     | Cassini    | - - - | ET                 | ⋯ | Ultralight bosons |
| - - - | MSPs (2038)                 |       |            |       |                    |   |                   |





# $\mu\text{Hz}$ GWs

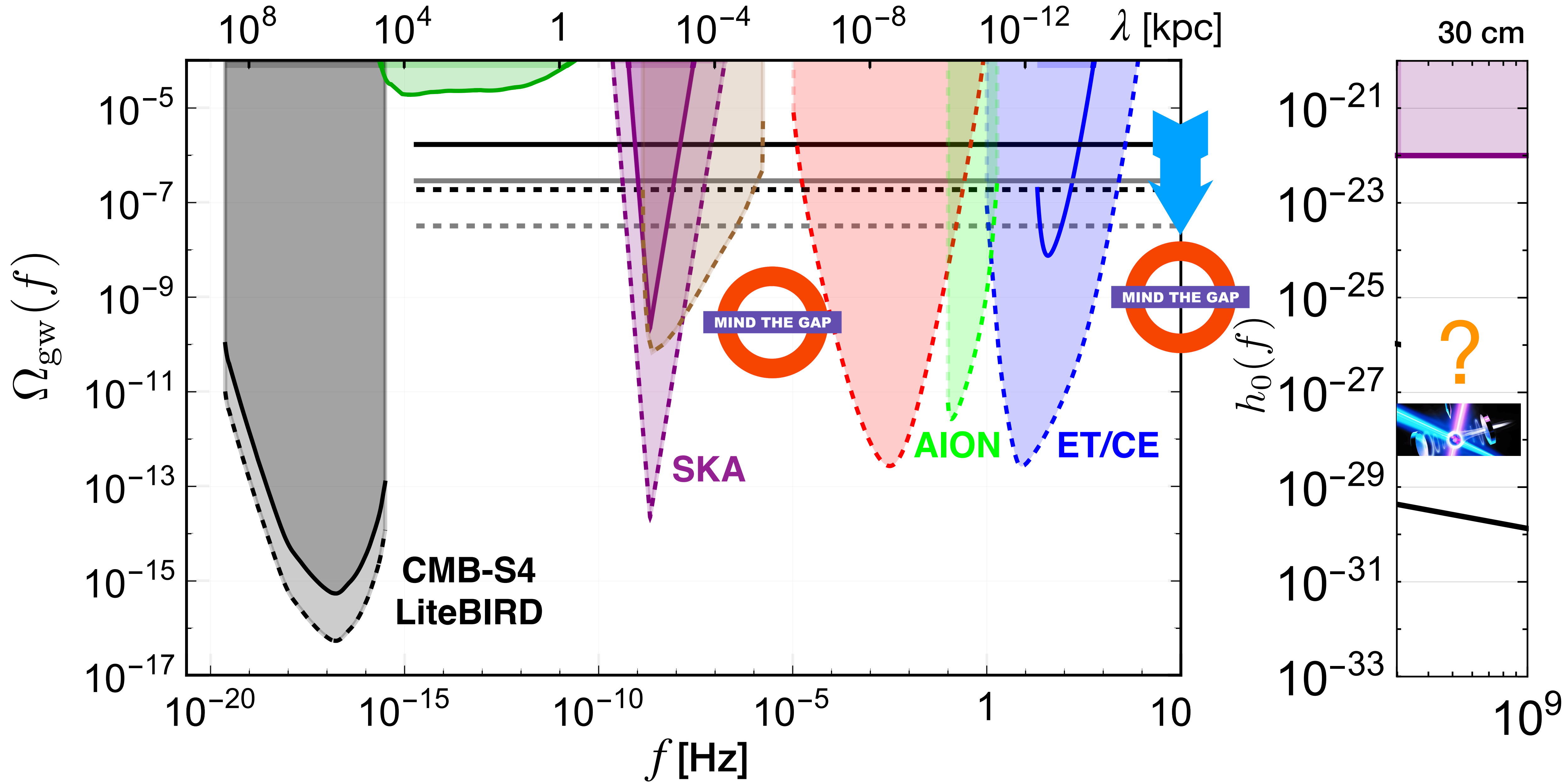
- The  $\mu\text{Hz}$  band is very rich for **astrophysical** and **cosmological** sources
- There are **ideas** of how to access it, though **most** of them are **futuristic**
- The resonant **absorption of GWs by binaries** (LLR/SLR/pulsars) may give a handle at level (in 2038)

$$\Omega_{\text{gw}} \geq 4.8 \times 10^{-9} \quad f = 0.85 \mu\text{Hz} \qquad \Omega_{\text{gw}} \geq 8.3 \times 10^{-9} \quad f = 0.15 \text{ mHz}$$

- **Future plans:** use LLR, SLR, pulsar **data** (w/ SYRTE, SCF\_Lab, MPIfRA, Nanograv people...): we need/welcome new hands.  
Find **other resonant effects**  
(e.g. in rotation, w. M de Amicis, wide binaries....which frequencies?)



# UHFGWs



*UHFPGWs -> Laboratory searches*

GWs interact with **every** source of energy-momentum!

*in the laboratory*

*Interaction GWs with **light***

*Interaction GWs with **matter external dofs***

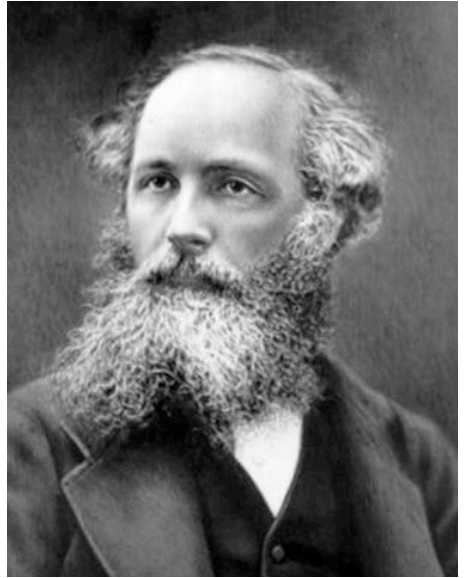
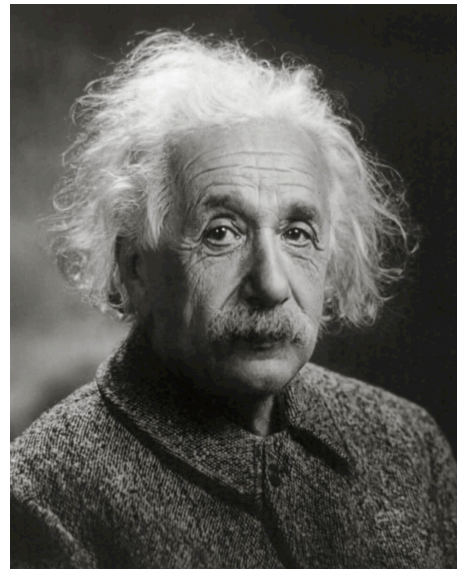
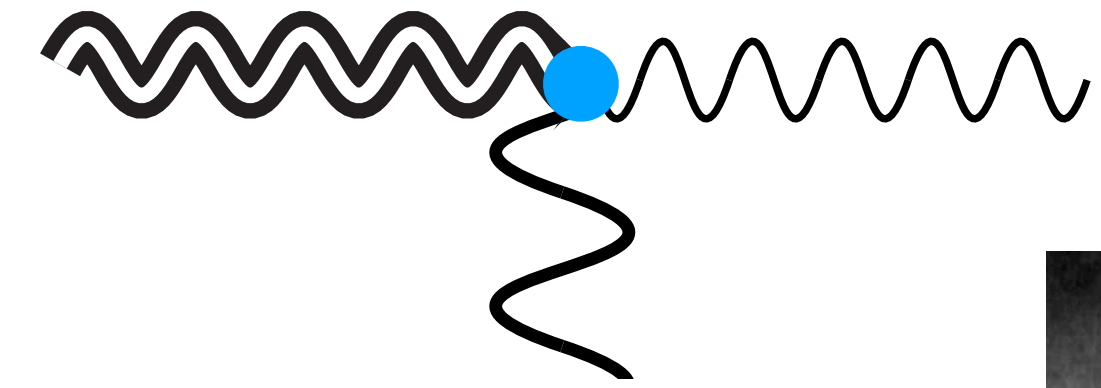
*Interaction GWs with **spin or other internal dofs***

**we have a lot to learn from DM searches!**



# GWs and EM fields

GWs + EM field  $\rightarrow$  EM field



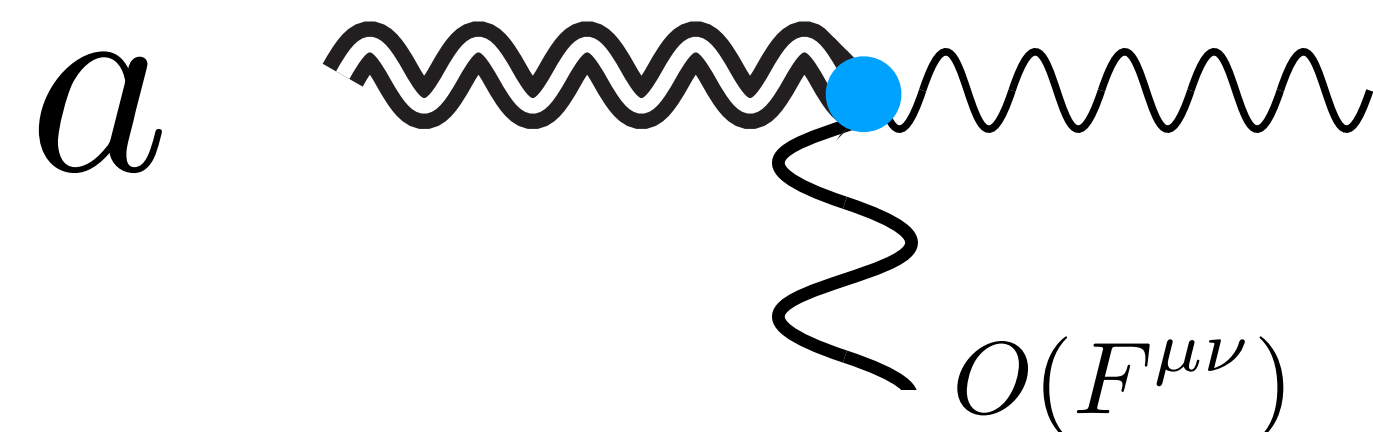
$$\mathcal{L} = \sqrt{-g} (R + F_{\mu\nu} F^{\mu\nu}) \supset \frac{1}{2} A_\mu j_{\text{eff}}^\mu(h) + \eta^{\mu\alpha} \eta^{\nu\beta} F_{\mu\nu} F_{\alpha\beta} + O(h^2)$$



$$j_{\text{eff}}^\mu = -\partial_\beta \left( \frac{1}{2} h F^{\mu\beta} + h_\alpha^\beta F^{\alpha\mu} - h_\alpha^\mu F^{\alpha\beta} \right)$$

analogy with **axions** + EM field  $\rightarrow$  EM field

$$a \tilde{F} F$$



# Connection to axions



This already sets the scale of the GW we want to measure:

for resonant production (for constant  $\vec{B}$ )  $\lambda_{gw} \approx L$

waves of (a priori) laboratory size

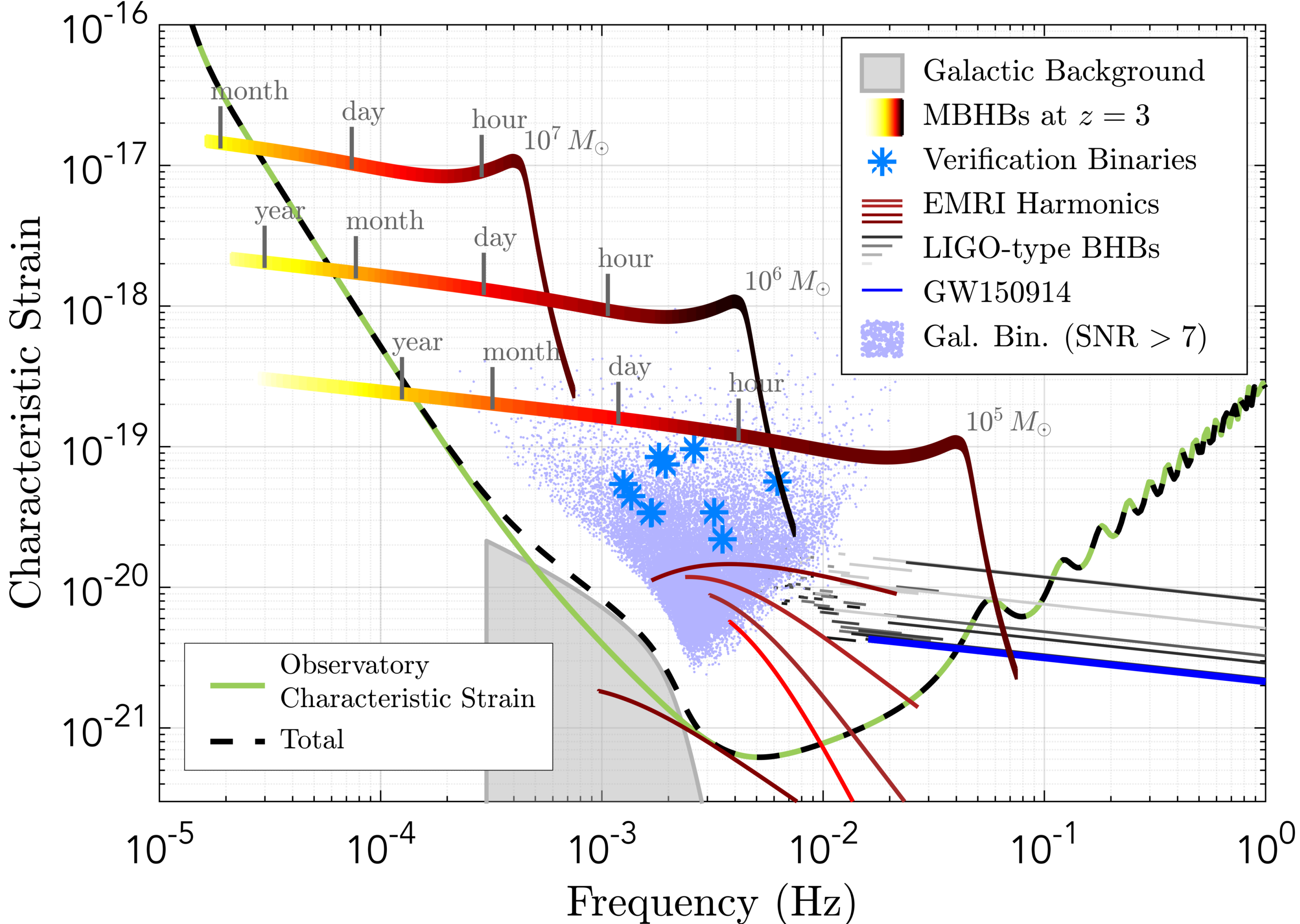






# LISA Sources

Amaro-Seoane et al. 1702.00786

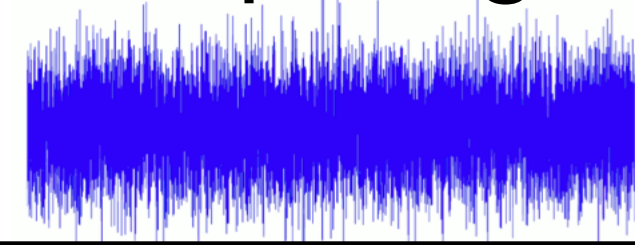




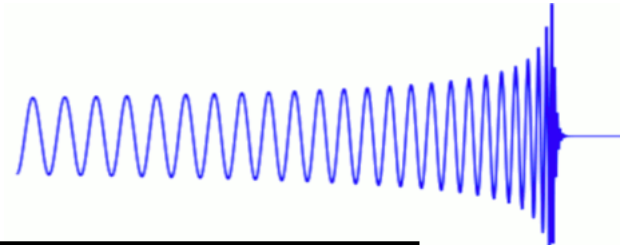
# Sources of UHFGW ( $> 10$ kHz)





Very different picture comparing to EM spectrum

Stochastic



Coherent



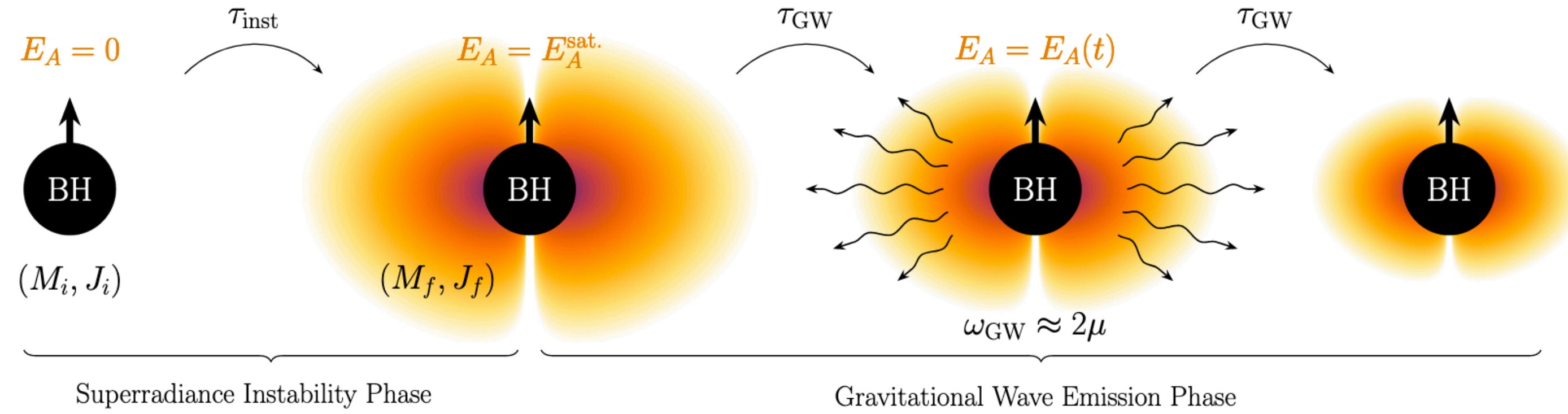
	Stochastic	Coherent
standard physics	<p>Primordial plasma thermal fluctuations</p> <p>Ghiglieri et al JHEP 07 (2020) 092 Ringwald et al JCAP 03 (2021) 054</p> 	<p>?</p> 
new physics	<p>Inflation</p>	
	<p>Phase transitions, Cosmic strings Close encounters of BHs</p> 	<p>Light PBHB Ultra-light DM Exotic objects</p> 



# Two words on sources

- SR

from Tsukada et al, '20



$$h \sim 10^{-23} \left( \frac{\Delta a_*}{0.1} \right) \left( \frac{1 \text{ kpc}}{D} \right) \left( \frac{M_b}{1 M_\odot} \right) \left( \frac{\alpha}{0.2} \right)^7$$

$$(M_b/M_\odot) \sim (10^3 \text{ Hz}/\omega_{\text{gw}})$$

$$t \sim 10^5 \text{ yrs} \times (\text{MHz}/\omega_g)^2$$

- BBH merger

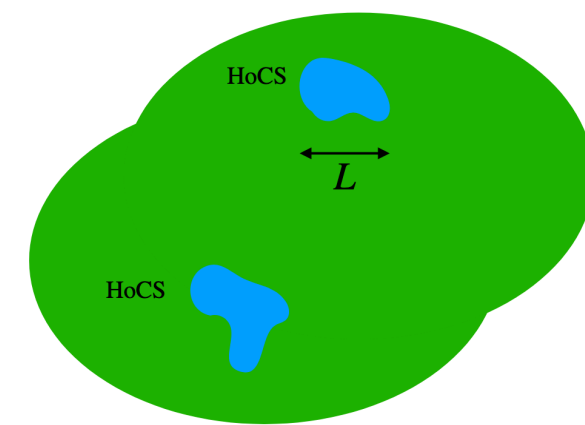
Franciolini et al 2205.02153

$$h_0 \sim 10^{-29} \times \left( \frac{1 \text{ pc}}{D} \right) \left( \frac{M_b}{10^{-11} M_\odot} \right)^{5/3} \left( \frac{\omega_g}{1 \text{ GHz}} \right)^{2/3}$$

$$\tau_b \sim 10^{-3} \text{ s} \left( \frac{10^5}{Q} \right) \left( \frac{10^{-11} M_\odot}{M_b} \right)^{5/3} \left( \frac{1 \text{ GHz}}{\omega_g} \right)^{8/3}$$

- NS/NS mergers

Casalderrey et al. 2210.03171



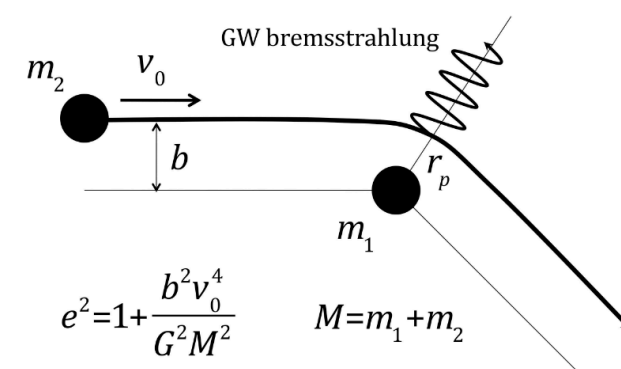
MHz

$$h_c^{\text{obs}} \simeq 2.1 \times 10^{-24} v_f^2 \left( \frac{100 \text{ Mpc}}{d} \right)$$

$$\Delta t \simeq L \simeq 1.7 \times 10^{-2} \text{ ms}$$

- Hyperbolic encounters of PBH

Garcia Bellido & S. Nesseris 1706.02111



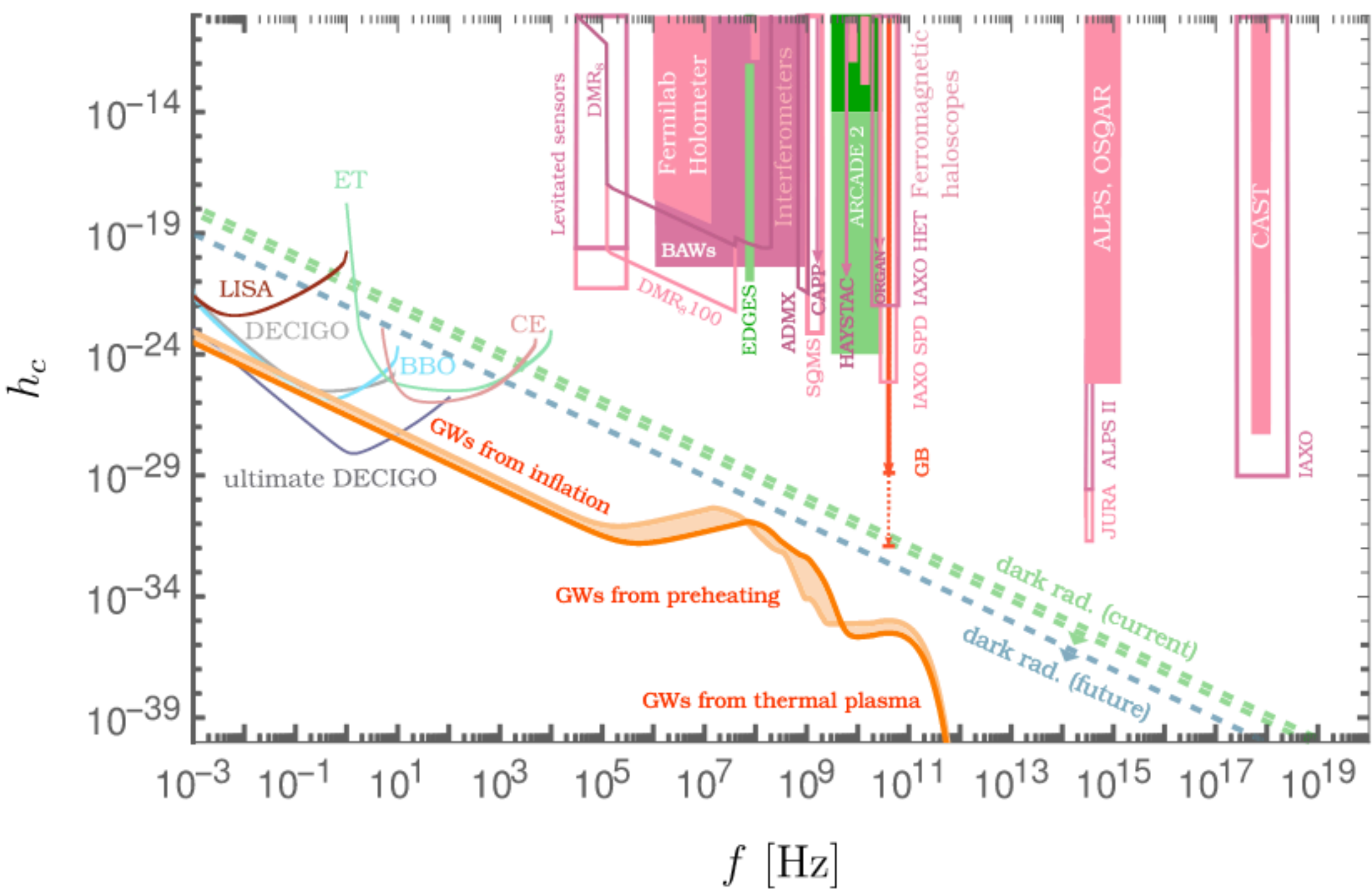
$$t_{1/2} \simeq 1 \text{ ms} \left( \frac{b}{10^{-8} \text{ AU}} \right) \left( \frac{0.01}{\beta} \right) (e - 1) \sqrt{\frac{3 \ln 2}{e + 35(1 + e)e}}$$



# Sources of UHFGW: spoiler!

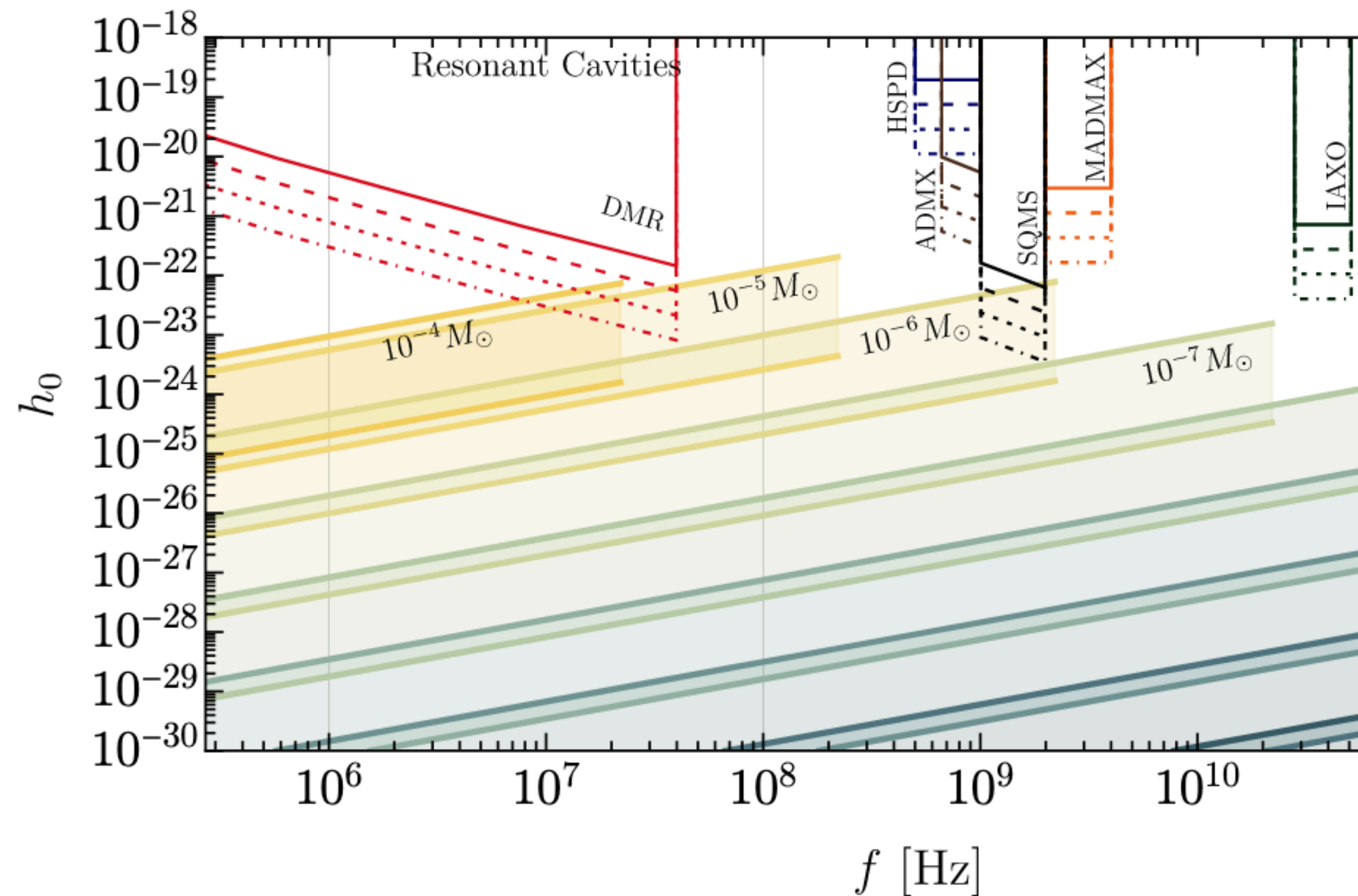
## SMASH model full spectrum

Ringwald Tamarit 22



## GWs from PBHs (rates 1/year)

Franciolini et al 2205.02153

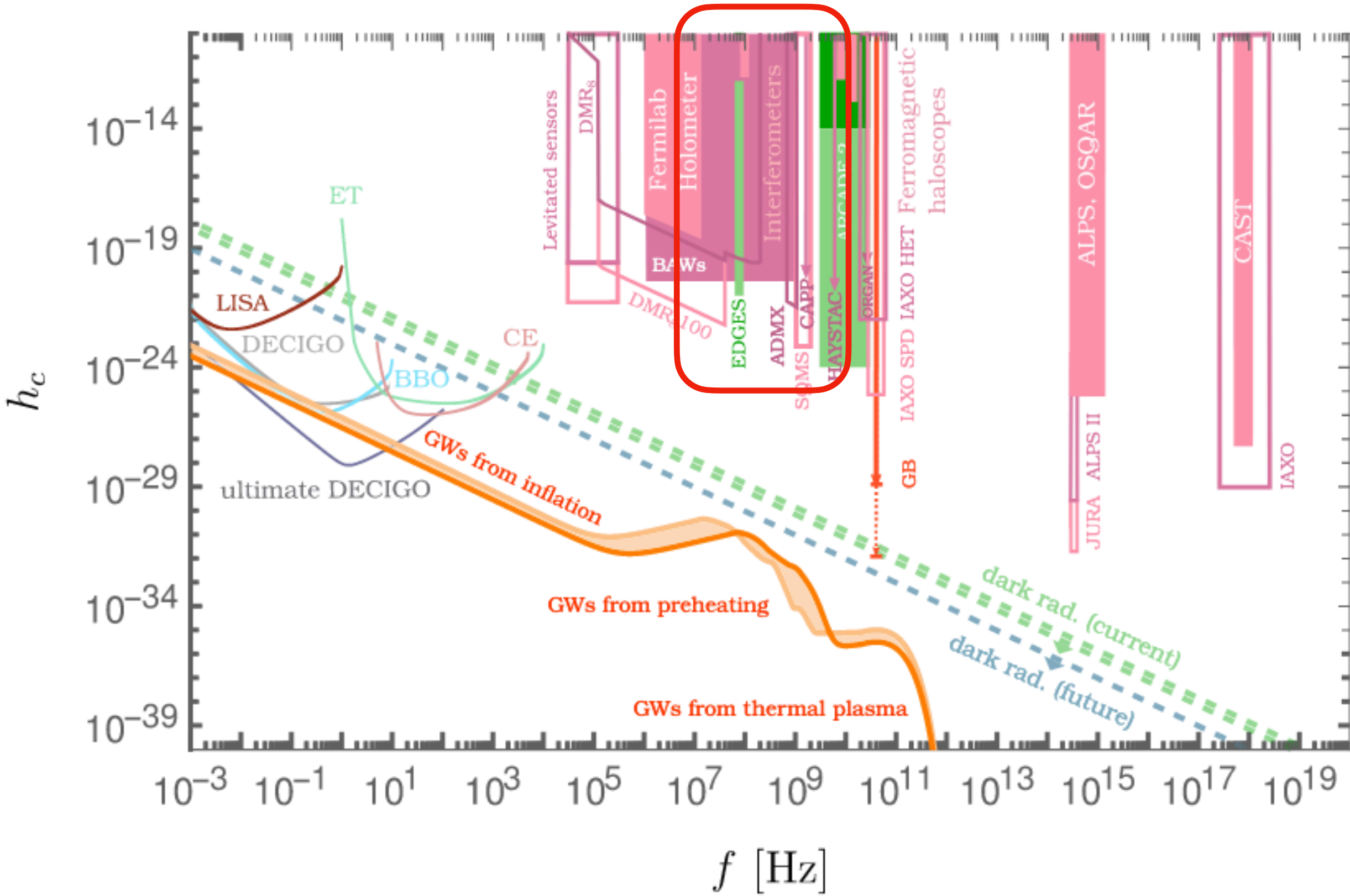




# Sources of UHFGW: spoiler!

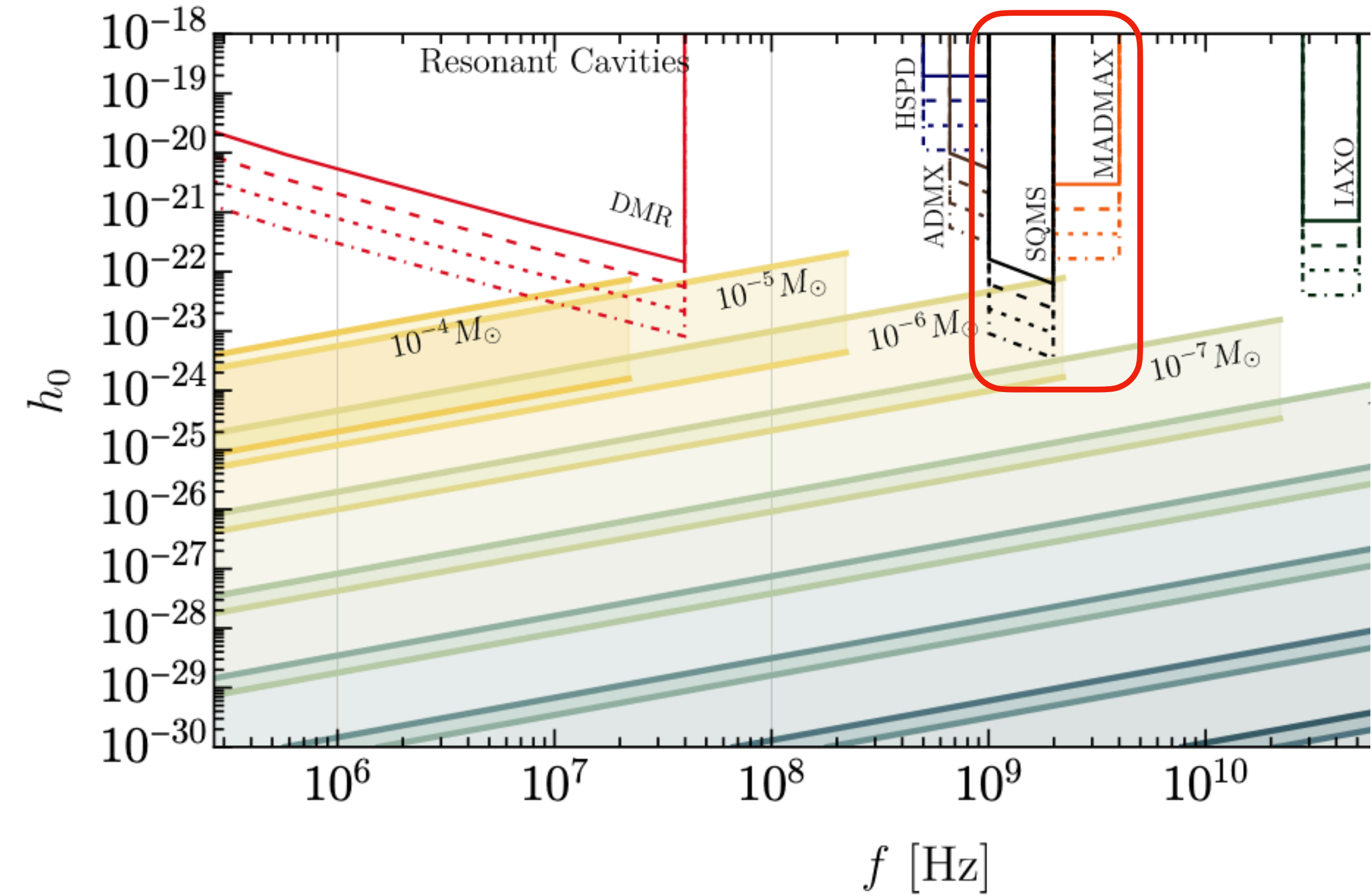
## SMASH model full spectrum

Ringwald Tamarit 22

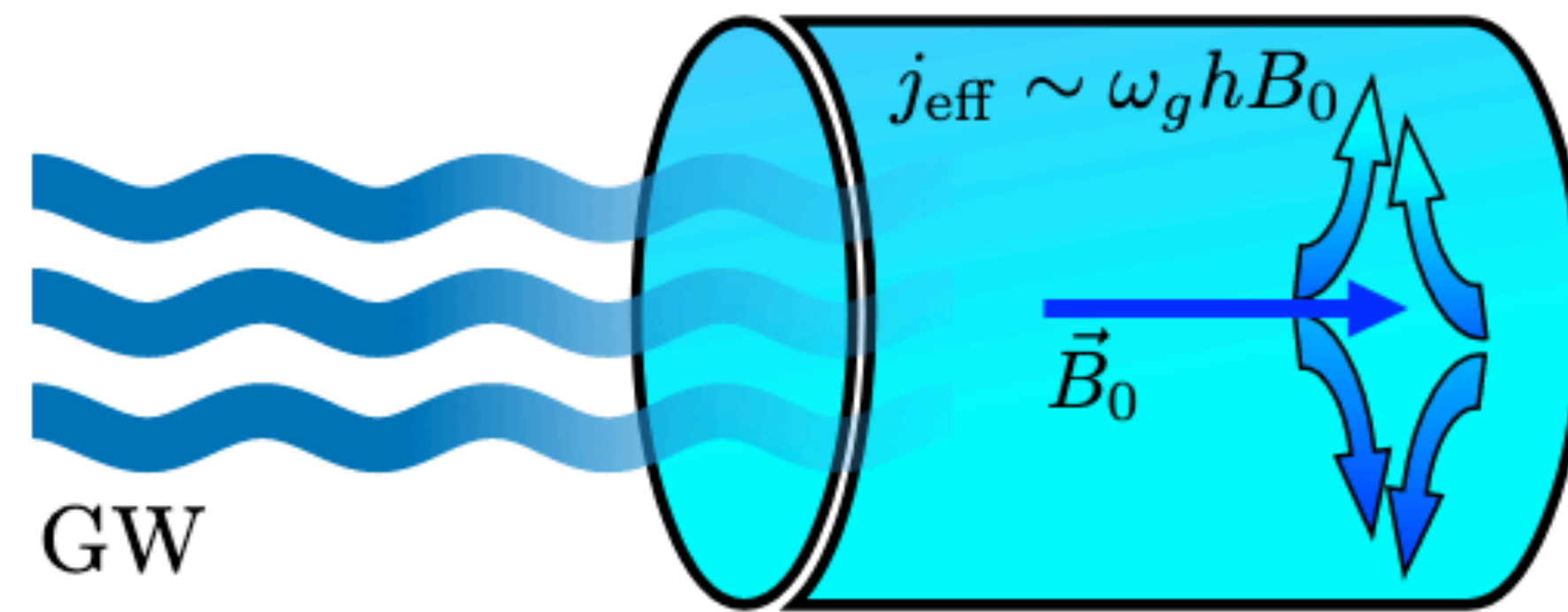


## GWs from PBHs (rates 1/year)

Franciolini et al 2205.02153



# Searching for GWs with light

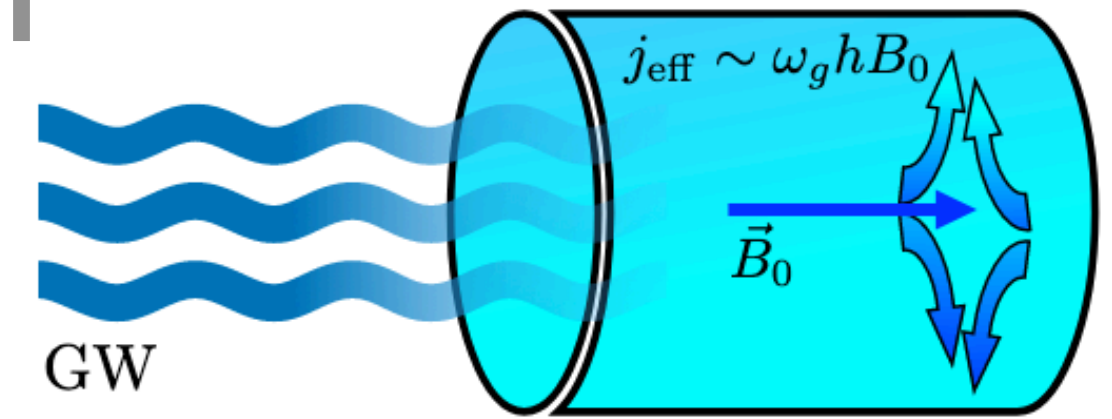


$$\mathcal{L} = \sqrt{-g} (R + F_{\mu\nu} F^{\mu\nu}) \supset \frac{1}{2} A_\mu j_{\text{eff}}^\mu (h) + \eta^{\mu\alpha} \eta^{\nu\beta} F_{\mu\nu} F_{\alpha\beta} + O(h^2)$$

$$j_{\text{eff}}^\mu = -\partial_\beta \left( \frac{1}{2} h F^{\mu\beta} + h_\alpha^\beta F^{\alpha\mu} - h_\alpha^\mu F^{\alpha\beta} \right)$$



# Cavity modes excitation



$$j_{\text{eff}}^{\mu} = -\partial_{\beta} \left( \frac{1}{2} h F^{\mu\beta} + h_{\alpha}^{\beta} F^{\alpha\mu} - h_{\alpha}^{\mu} F^{\alpha\beta} \right)$$

$$\mathbf{E}(\mathbf{x}, t) = \sum \mathbf{E}_{sn}(\mathbf{x}, t) + \mathbf{E}_{in}(\mathbf{x}, t)$$

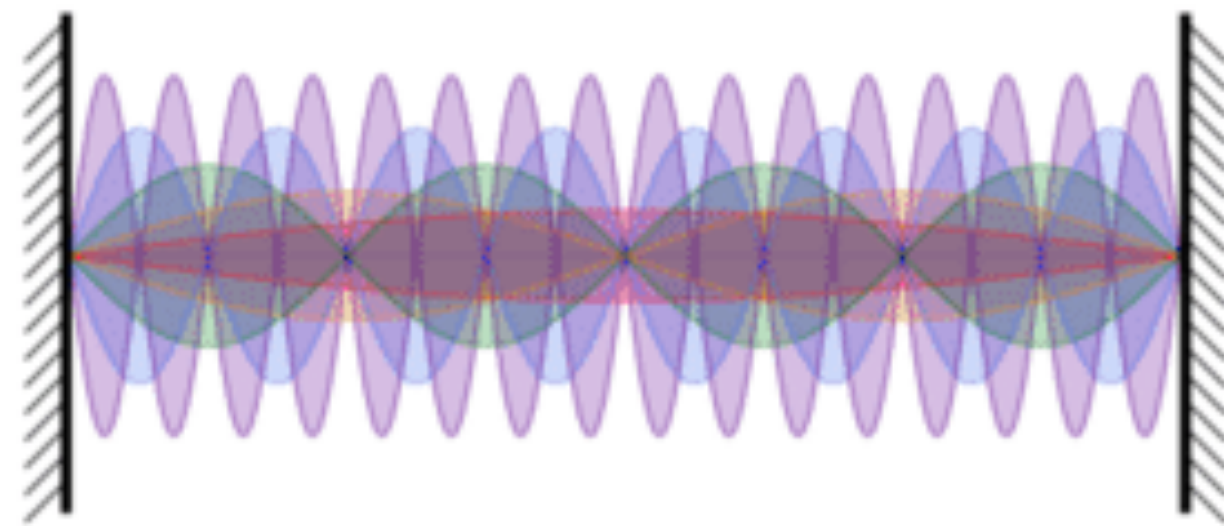


solenoidal

irrotational

$$\mathbf{E}_{sn}(\mathbf{x}, t) = e_{sn}(t) \mathbf{E}_{sn}(\mathbf{x})$$

$$\mathbf{E}_{in}(\mathbf{x}, t) = e_{in}(t) \mathbf{E}_{in}(\mathbf{x})$$



$$(\omega_{sm}^2 + \partial_t^2 + \sigma_{sm} \partial_t) e_{sm}(t) = e^{-i\omega_G t} \eta_{sm}$$

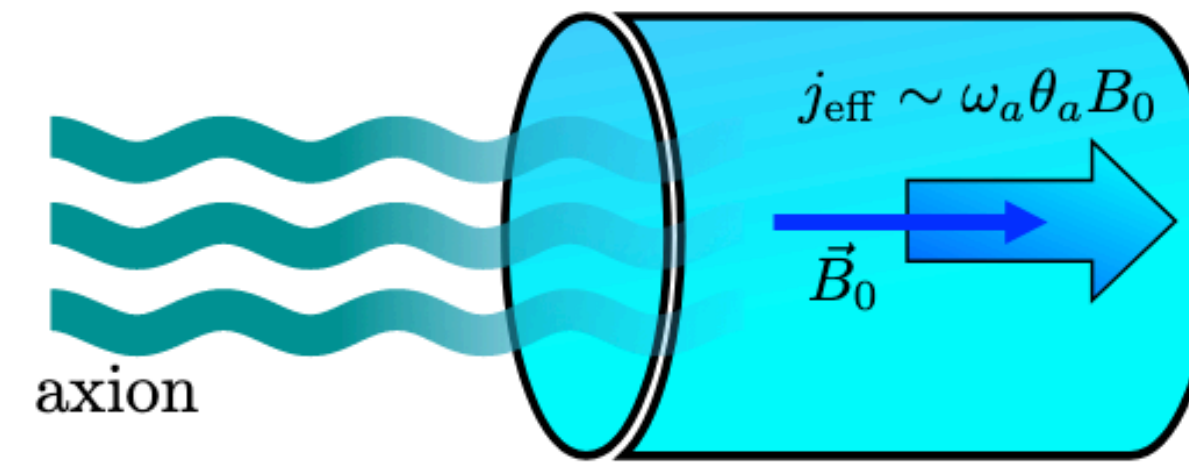
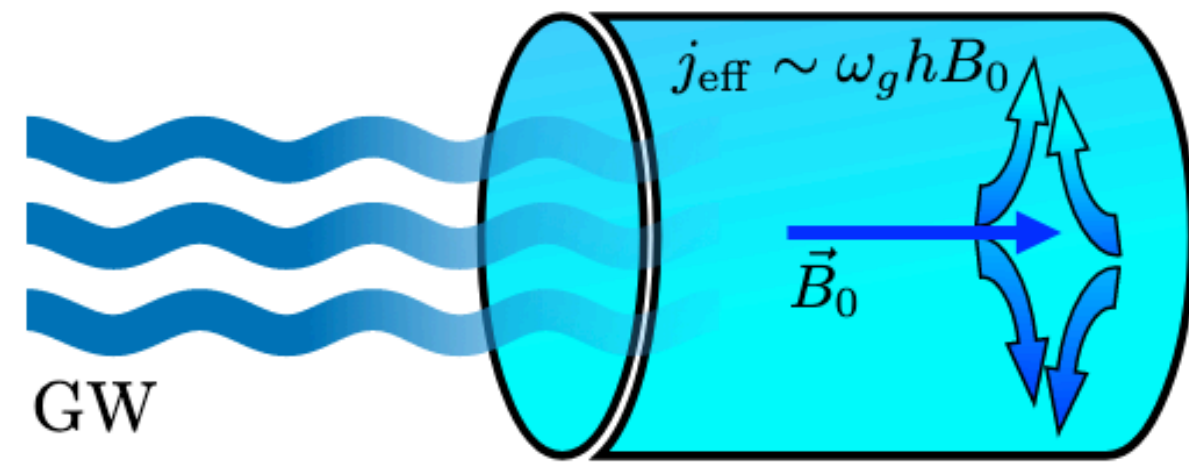
$$(\partial_t^2 + \sigma_{im} \partial_t) e_{im}(t) = e^{-i\omega_G t} \eta_{im}$$



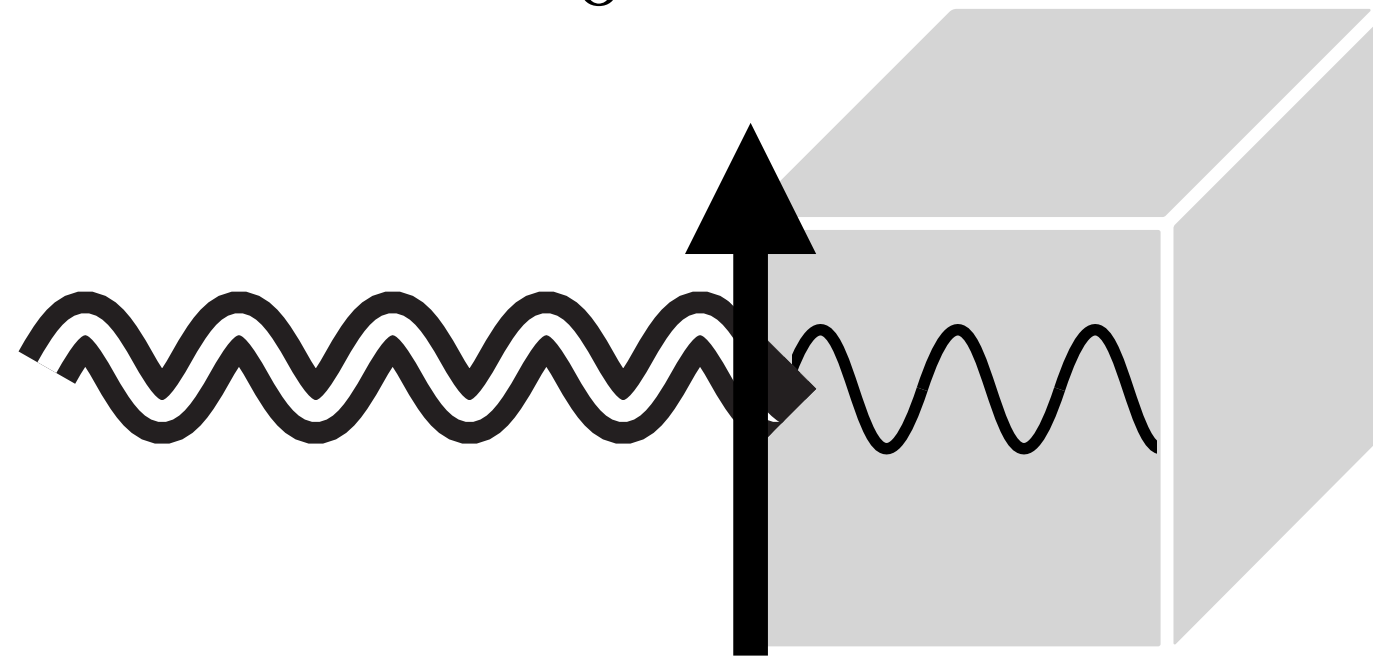
$$\eta \sim \int_V d^3x E J_{eff}$$

'source' (here we want to maximise. It is also directional)

# From axions to GWs



$$P_h \sim h_0^2$$



Du et al 2018

indeed: ADMX sensitivity

$$P_{\text{axion}} = 1.9 \times 10^{-22} \text{ W} \left( \frac{V}{136l} \right) \left( \frac{B}{6.8 \text{ T}} \right)^2 \left( \frac{C}{0.4} \right) \left( \frac{g_\gamma}{0.97} \right)^2 \left( \frac{\rho_a}{0.45 \text{ GeV cm}^{-3}} \right) \left( \frac{f}{650 \text{ MHz}} \right) \left( \frac{Q}{50,000} \right)$$



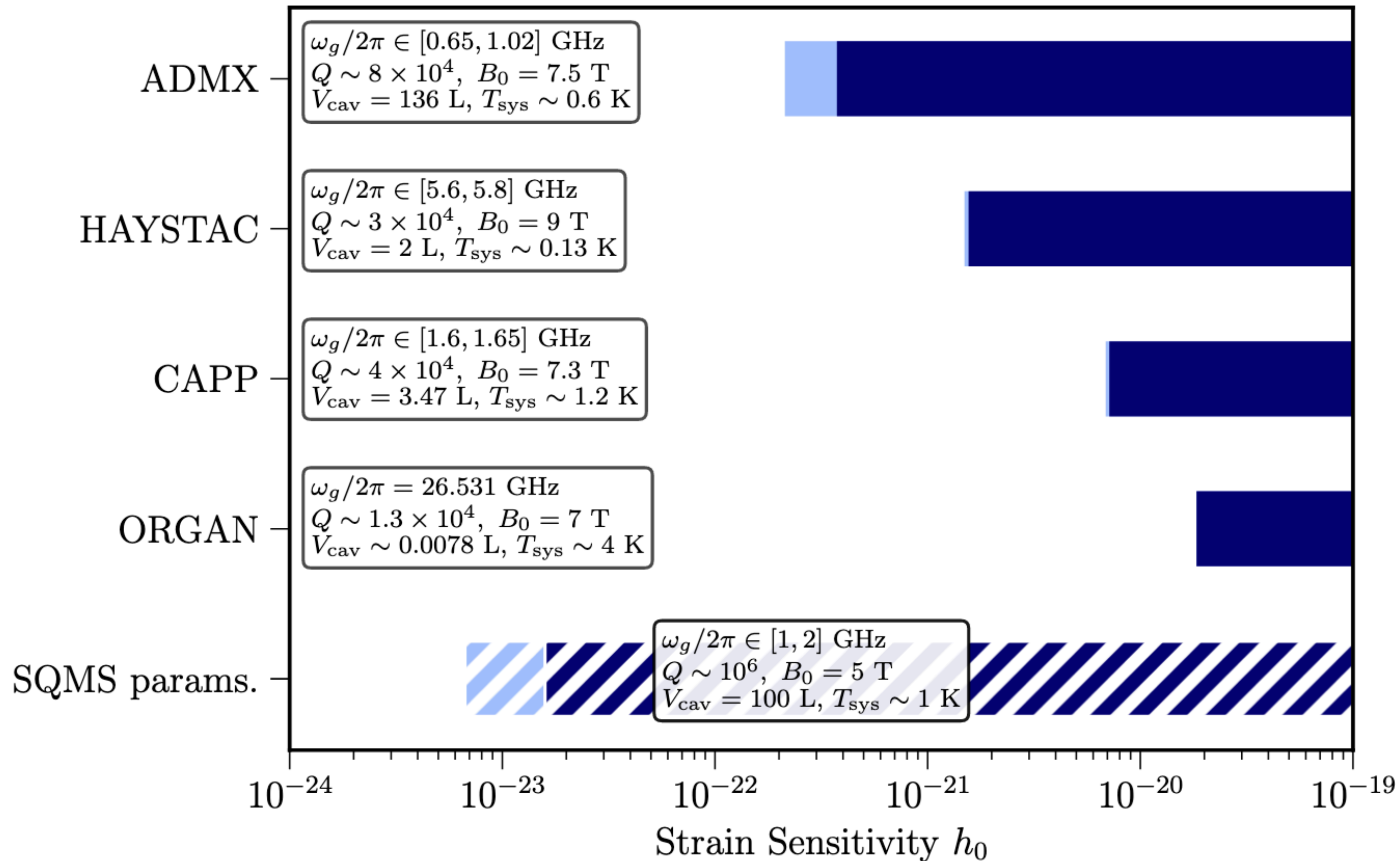
quadratic in axion field and in  $h$

$$P_h \sim h_0^2$$

$$h_0 \gtrsim 3 \times 10^{-22} \times \left( \frac{1 \text{ GHz}}{\omega_g/2\pi} \right)^{3/2} \left( \frac{0.1}{\eta_n} \right) \left( \frac{8 \text{ T}}{B_0} \right) \left( \frac{0.1 \text{ m}^3}{V_{\text{cav}}} \right)^{5/6} \left( \frac{10^5}{Q} \right)^{1/2} \left( \frac{T_{\text{sys}}}{1 \text{ K}} \right)^{1/2} \left( \frac{\Delta\nu}{10 \text{ kHz}} \right)^{1/4} \left( \frac{1 \text{ min}}{t_{\text{int}}} \right)^{1/4}$$



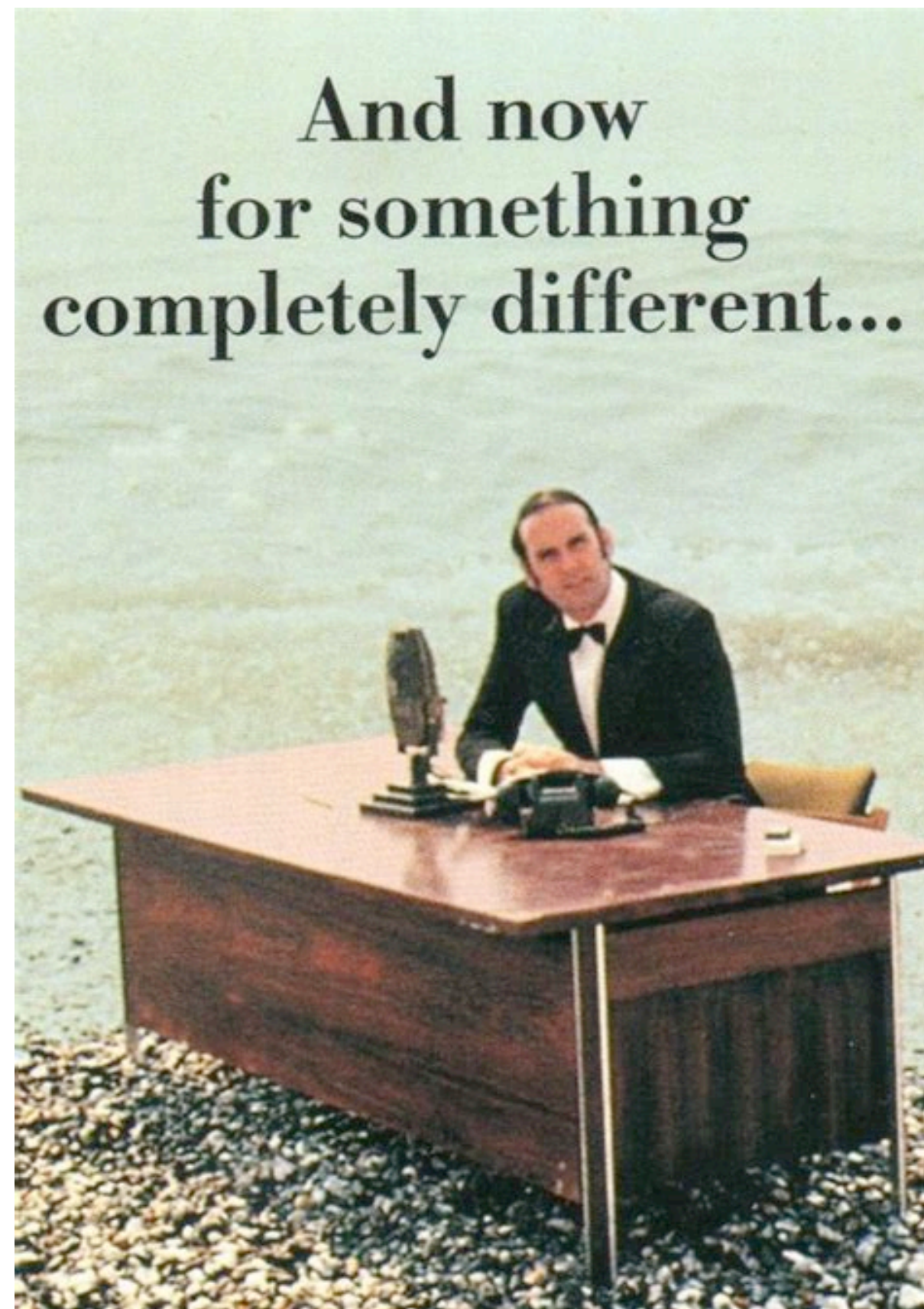
# Projected Sensitivities of Axion Experiments



A very exploratory field...

we still need to **deeply think what's better** for the future

do we move to something else ?





# LIGO lesson

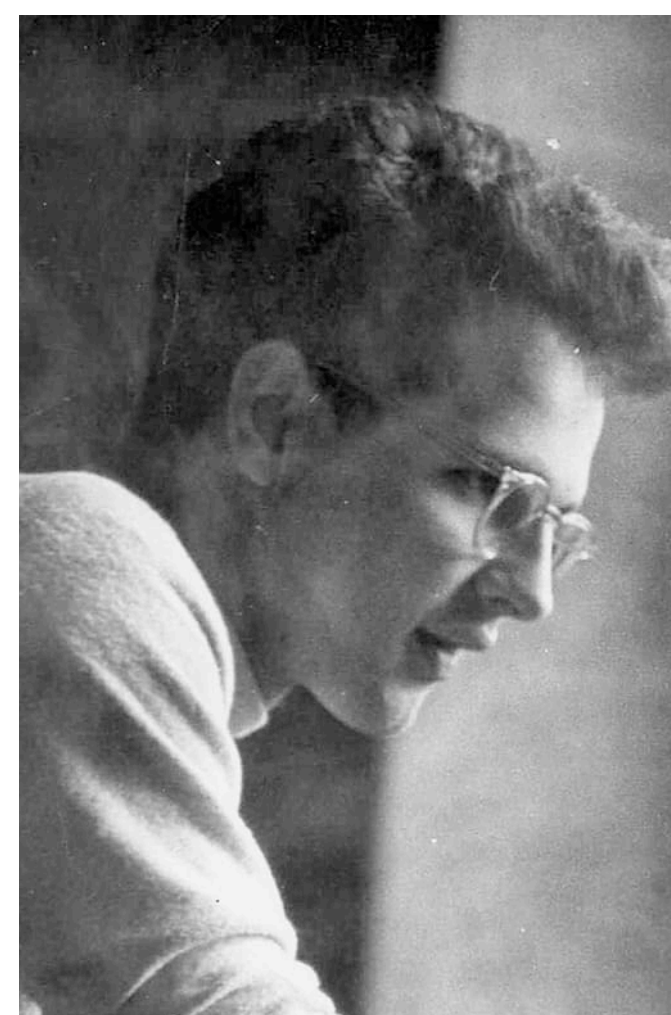
A very exploratory field...

we still need to **deeply think what's better** for the future

do we move to something else?



Rainer Weiss, ca. 1972



LIGO concept  
Weiss 1972

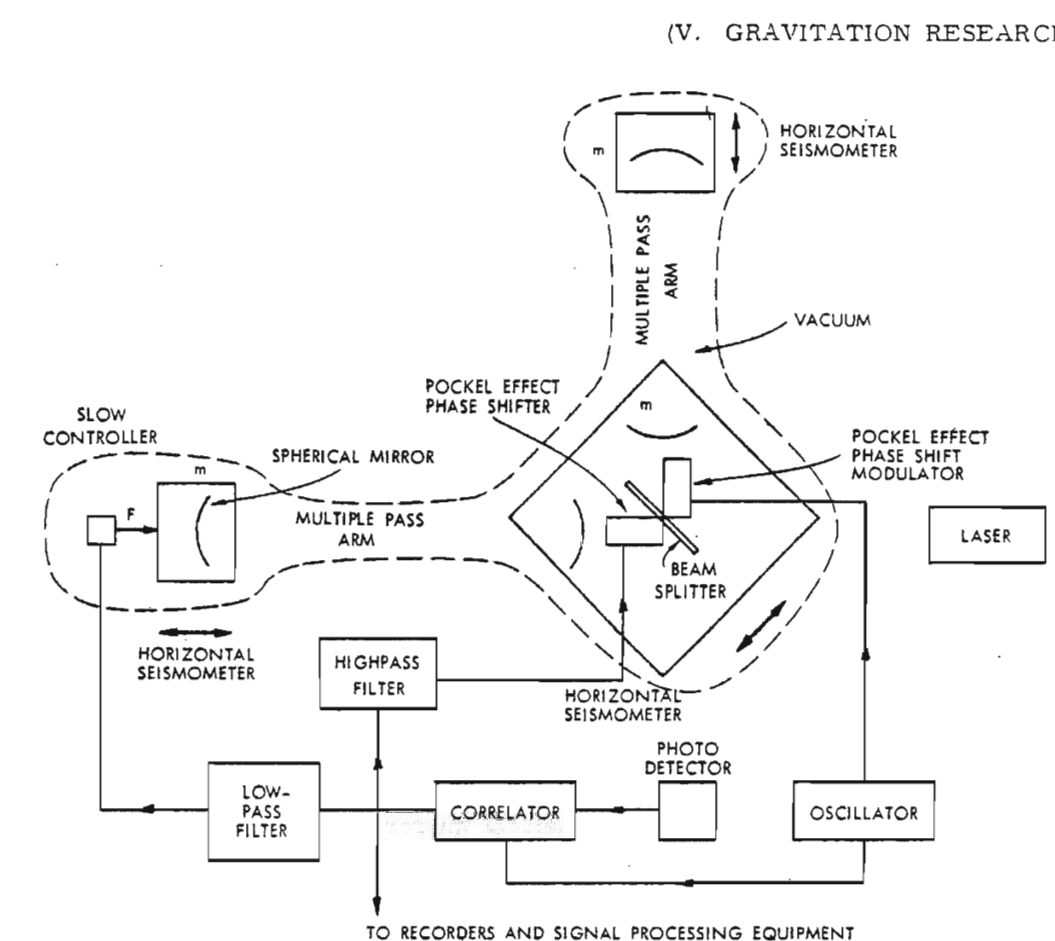


Fig. V-20. Proposed antenna.

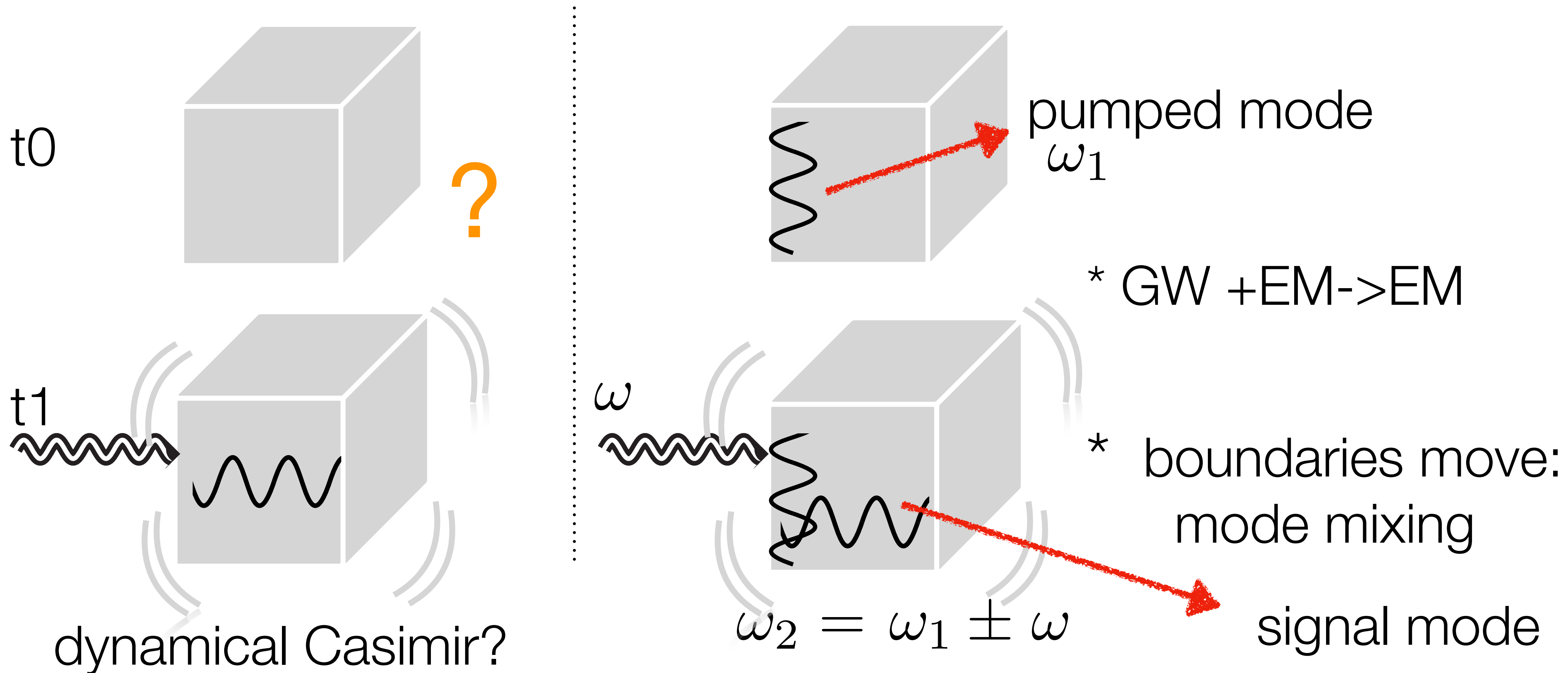
For continuous gravitational waves, the minimum detectable gravitational wave metric spectral density is then

$$h^2(f) > \frac{4}{f^2} \frac{\Delta x_n^2(f)}{\Delta f} \approx \frac{4 \times 10^{-33}}{f^2(\text{cm})} \text{ Hz}^{-1}.$$

# Recycling axion experiments II

Mechanical-coupling  
(shaking the walls)

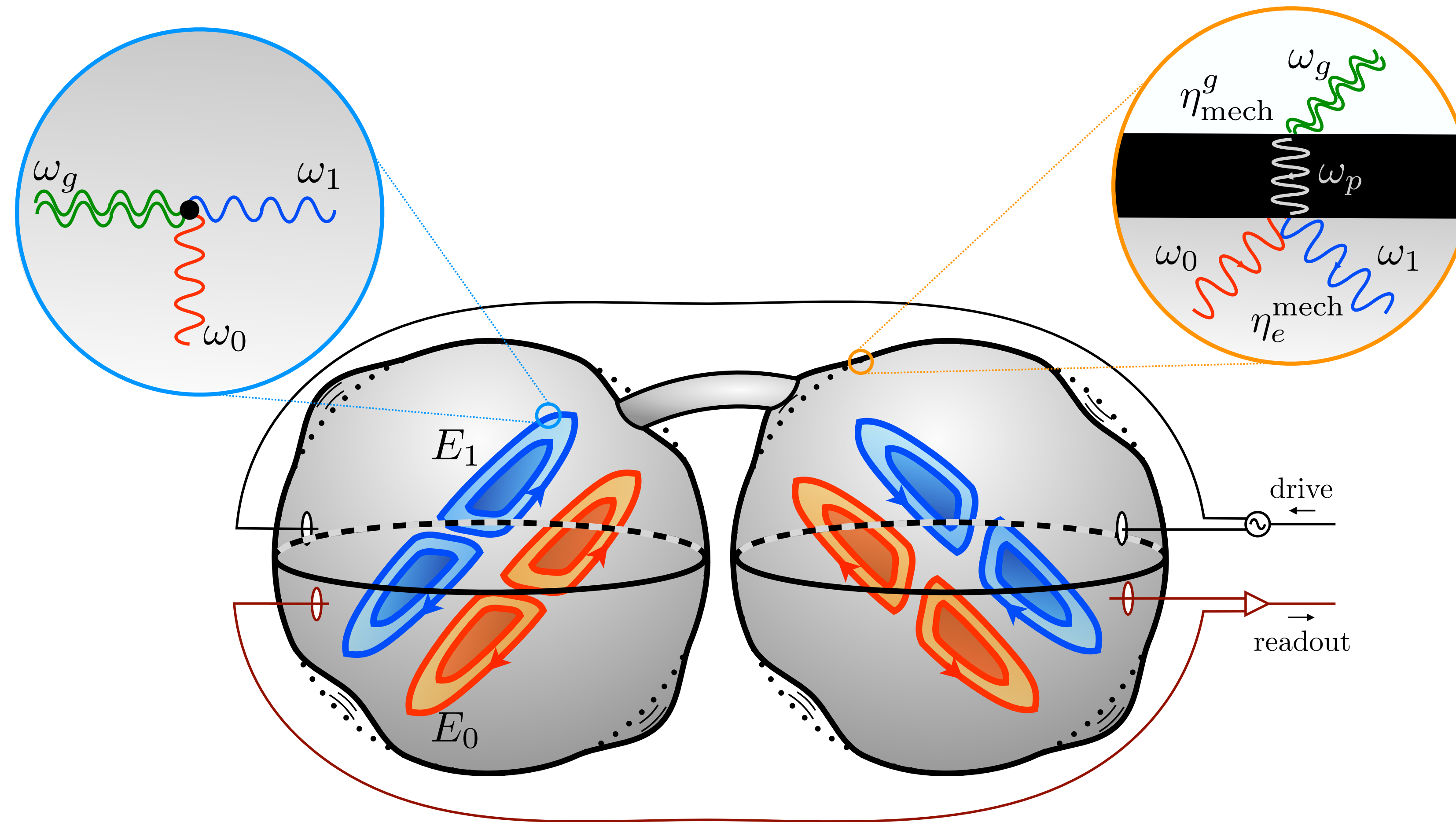
MAGO design from CERN (gr-qc/0502054)  
Berlin, DB et al 2303.01518





# MAGO set-up

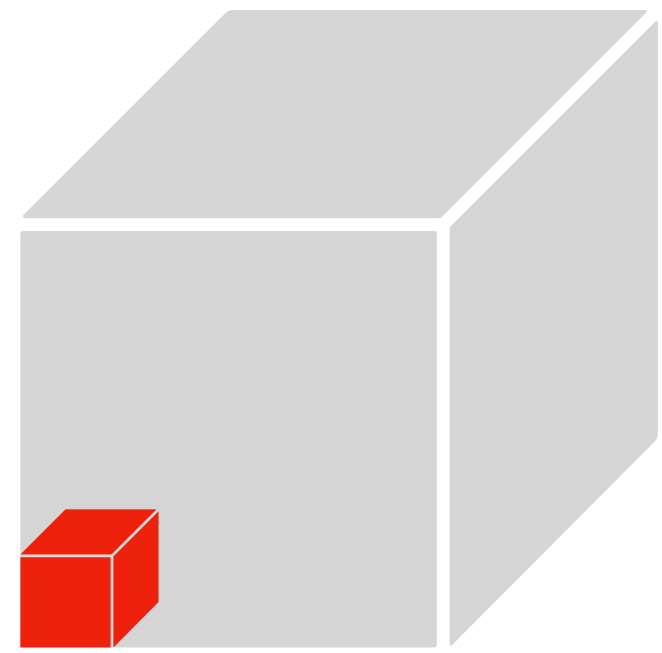
(Microwave Apparatus for Gravitational Waves Observation)



# GWs exciting solids

searched for many years (Weber bars)

a solid affected by an external source (e.g.  $x$  direction)



$dm(x + u(x, t))$

$$dm \left( \frac{\partial^2 u}{\partial t^2} - v_s^2 \frac{\partial^2 u}{\partial x^2} \right) = dF_x(t, x),$$
$$dF_i = \frac{1}{2} \ddot{h}_{ij}^{TT} x^j dm$$

In terms of eigenmodes:

$$\mathbf{u}(\mathbf{x}, t) = u_p(t) \mathbf{u}_p(\mathbf{x})$$



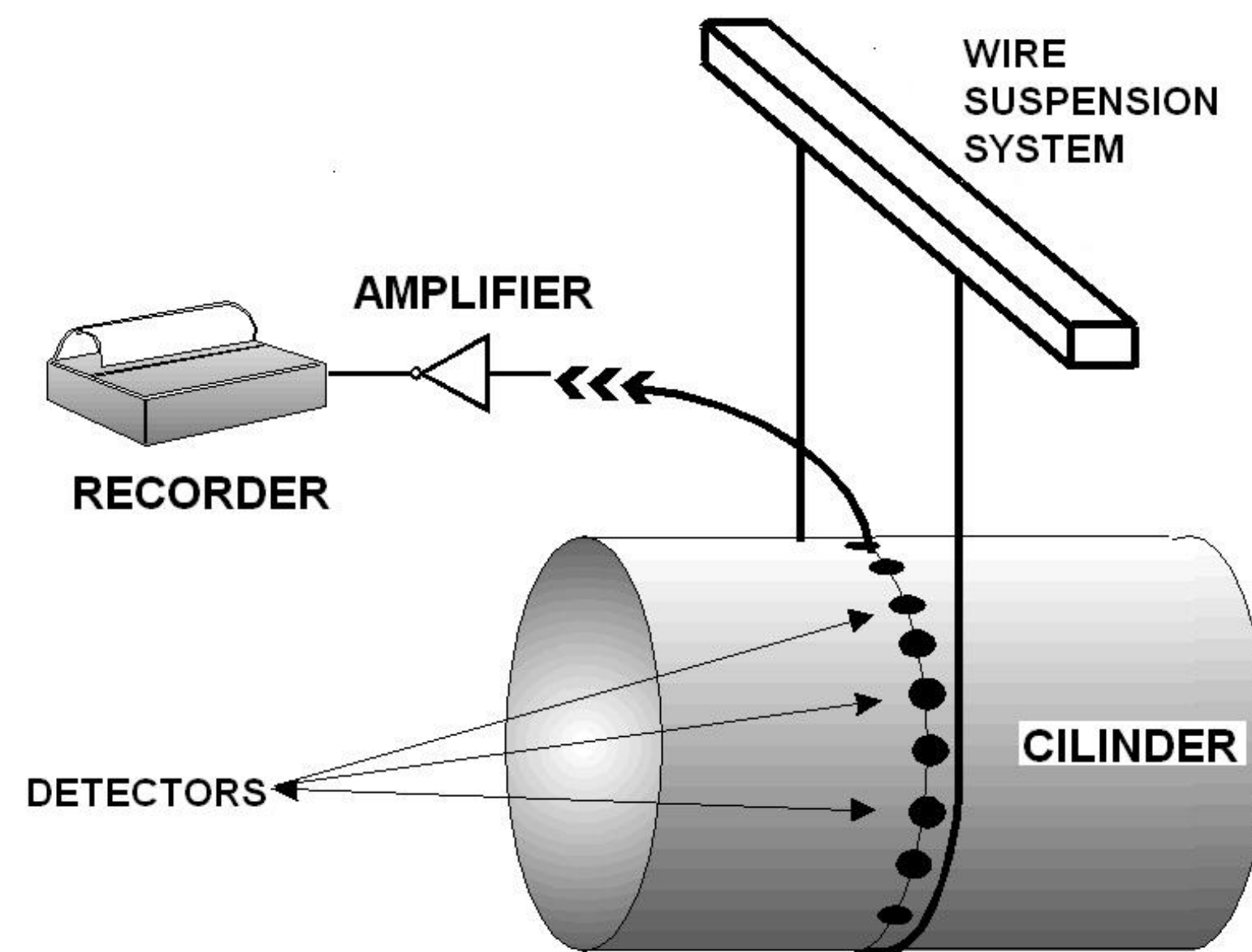
# GWs exciting solids

$$\mathbf{u}(\mathbf{x}, t) = u_p(t)\mathbf{u}_p(\mathbf{x})$$

$$\ddot{u}_p + \frac{\omega_p}{Q_p} \dot{u}_p + \omega_p^2 u_p \simeq -\frac{1}{2} \omega_g^2 V_{\text{cav}}^{1/3} \eta_{\text{mech}}^g h_0 e^{i\omega_g t}$$

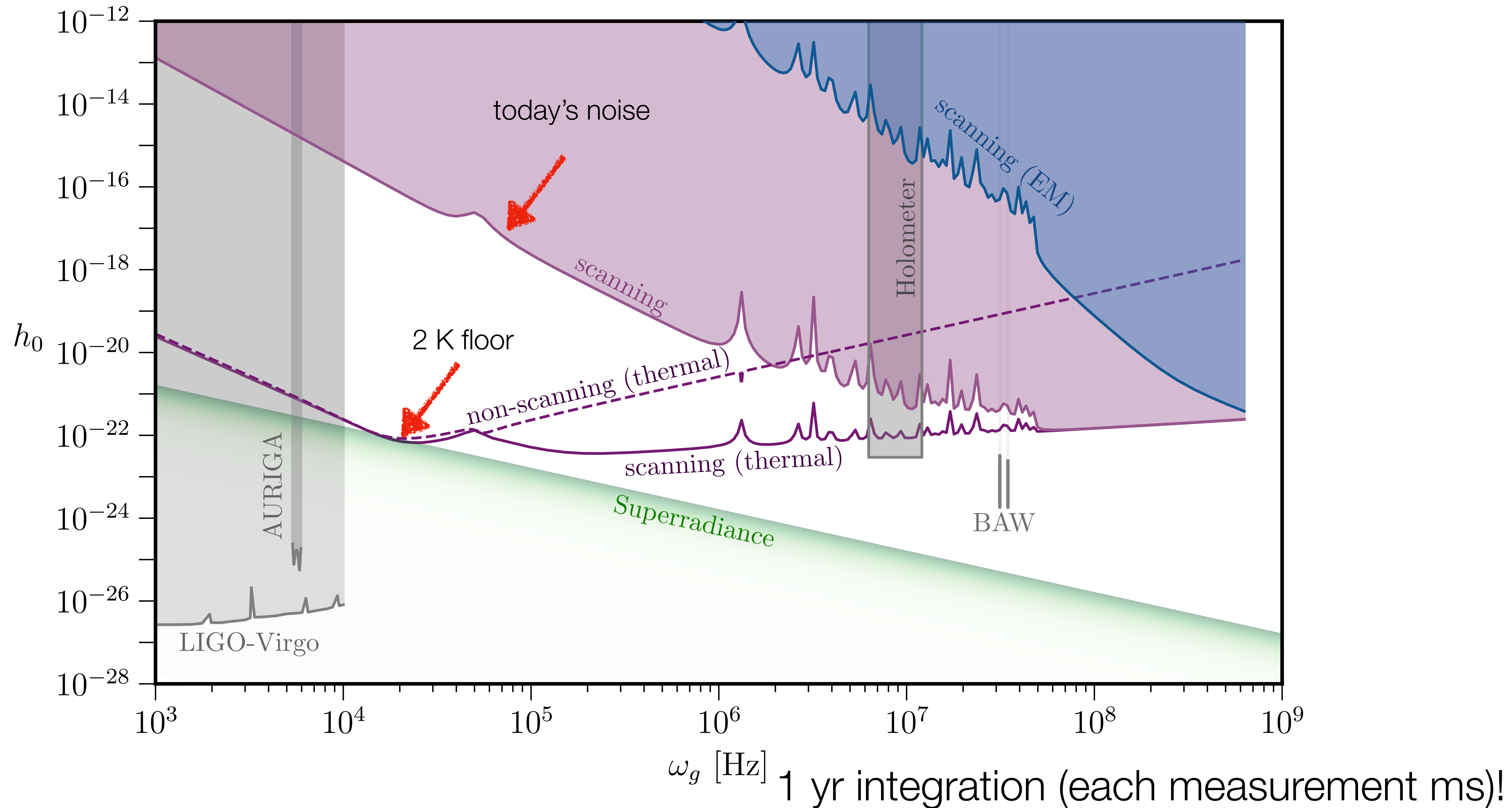
$$\eta_{\text{mech}}^g = \frac{\hat{h}_{ij}^{\text{TT}}}{V_{\text{cav}}^{1/3} V_{\text{shell}}} \int_{V_{\text{shell}}} d^3\mathbf{x} U_p^{*i} x^j$$

this rings the solid (Weber bars)



# Estimates

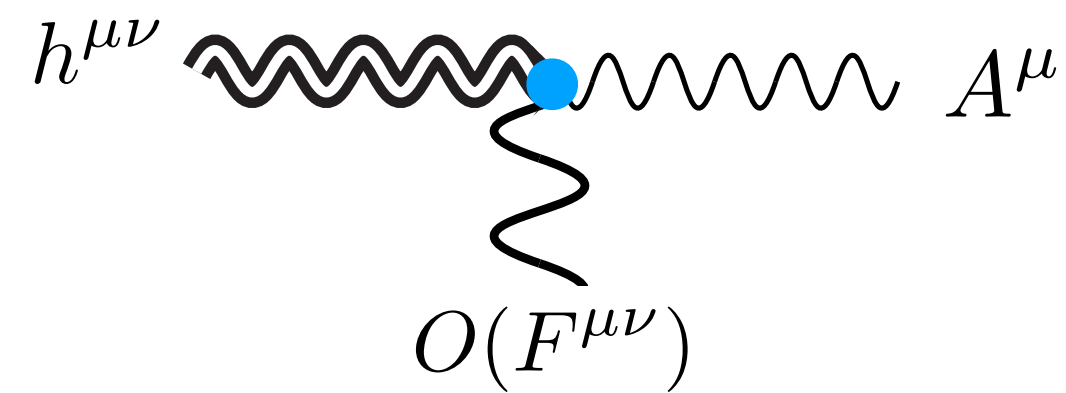
A. Berlin, DB, R.T. D'Agnolo, S. Ellis, R. Harnik,  
Y. Kahn, J. Schütte-Engel, M. Wentze 2303.01518





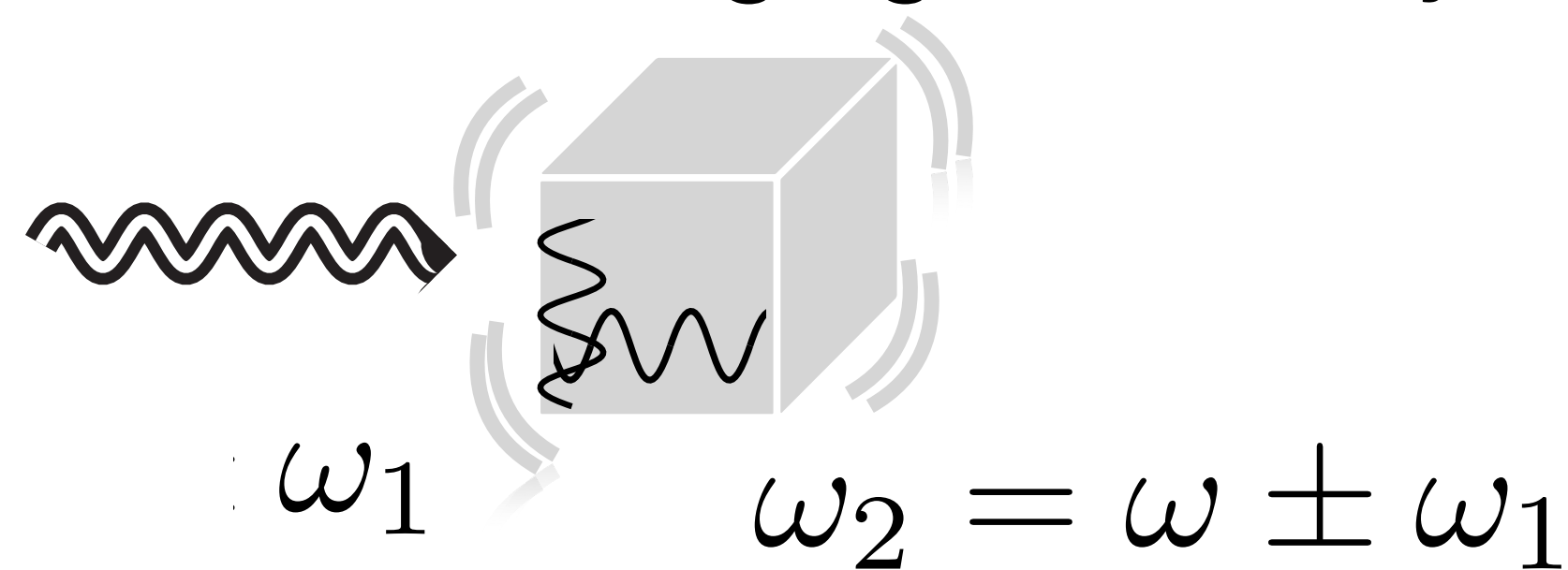
# Summary and outlook

- SRF cavities are a mature technology to look for GWs at GHz either
  - Coupling to photons in a cavity



- 'ADMX' like  $\omega = \omega_g$
- Heterodyne  $\omega_2 = \omega_g \pm \omega_1$

- Ringing the cavity and generating mode mixing



- Heterodyne
- Casimir?



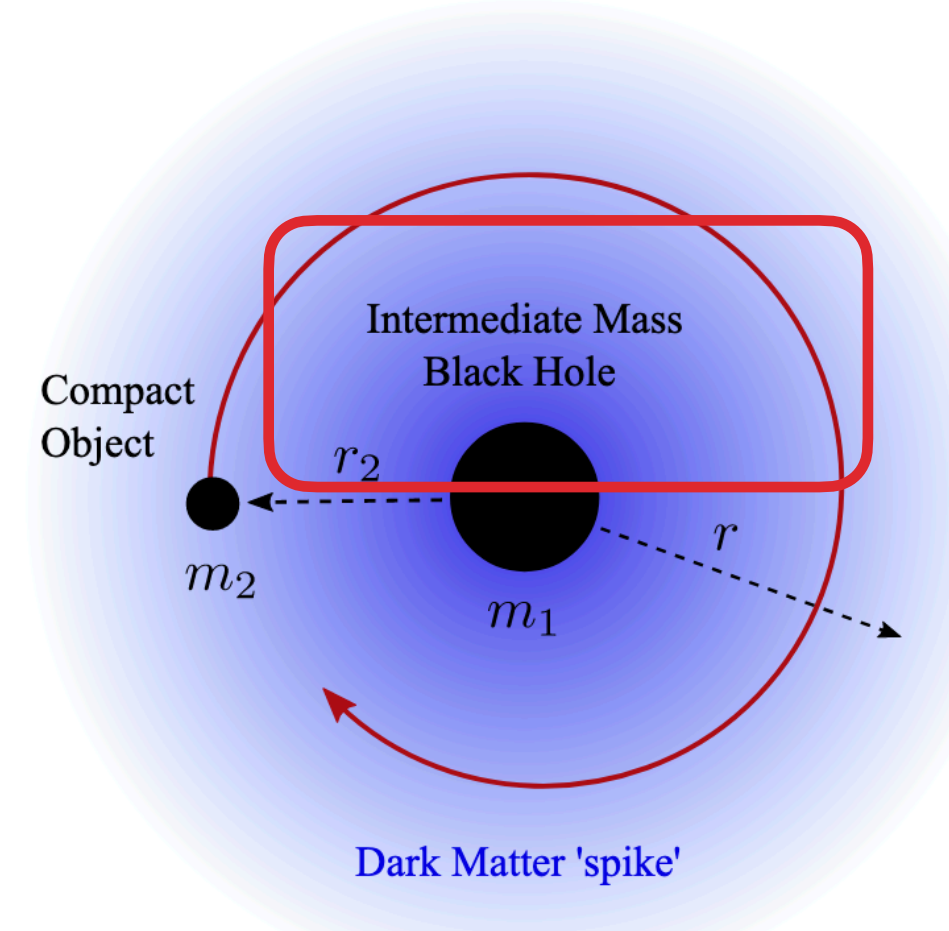
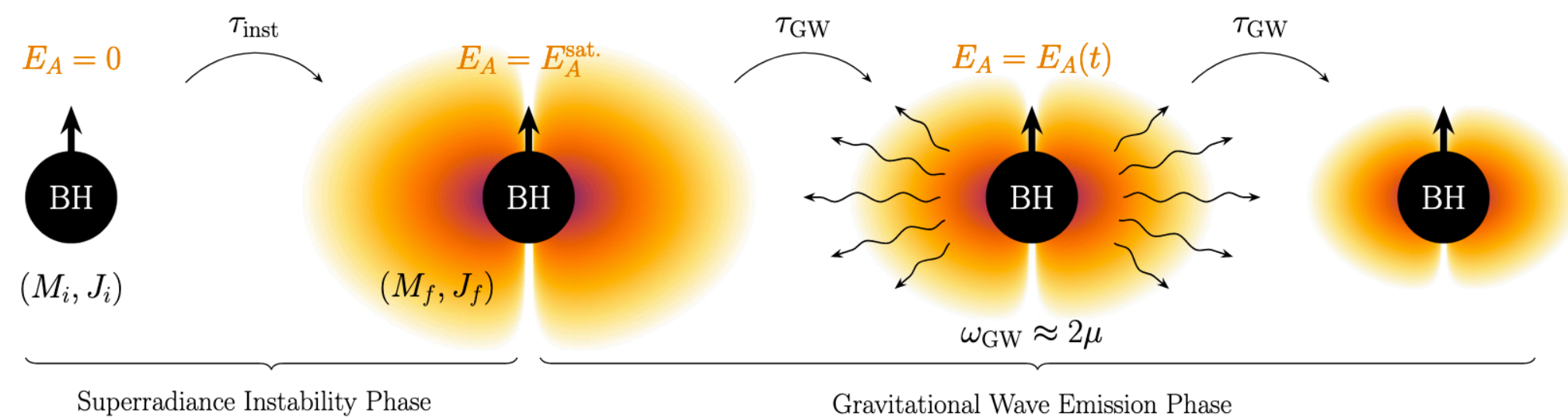
\* Reach of  $h_0 \sim 10^{-23}$  possible (100 kHz-GHz), though far from known signals

# Why this talk?

**Dark matter models** (beyond the weak scale) can be tested through **GWs of different frequencies**, e.g.

## Superradiance for ultralight?

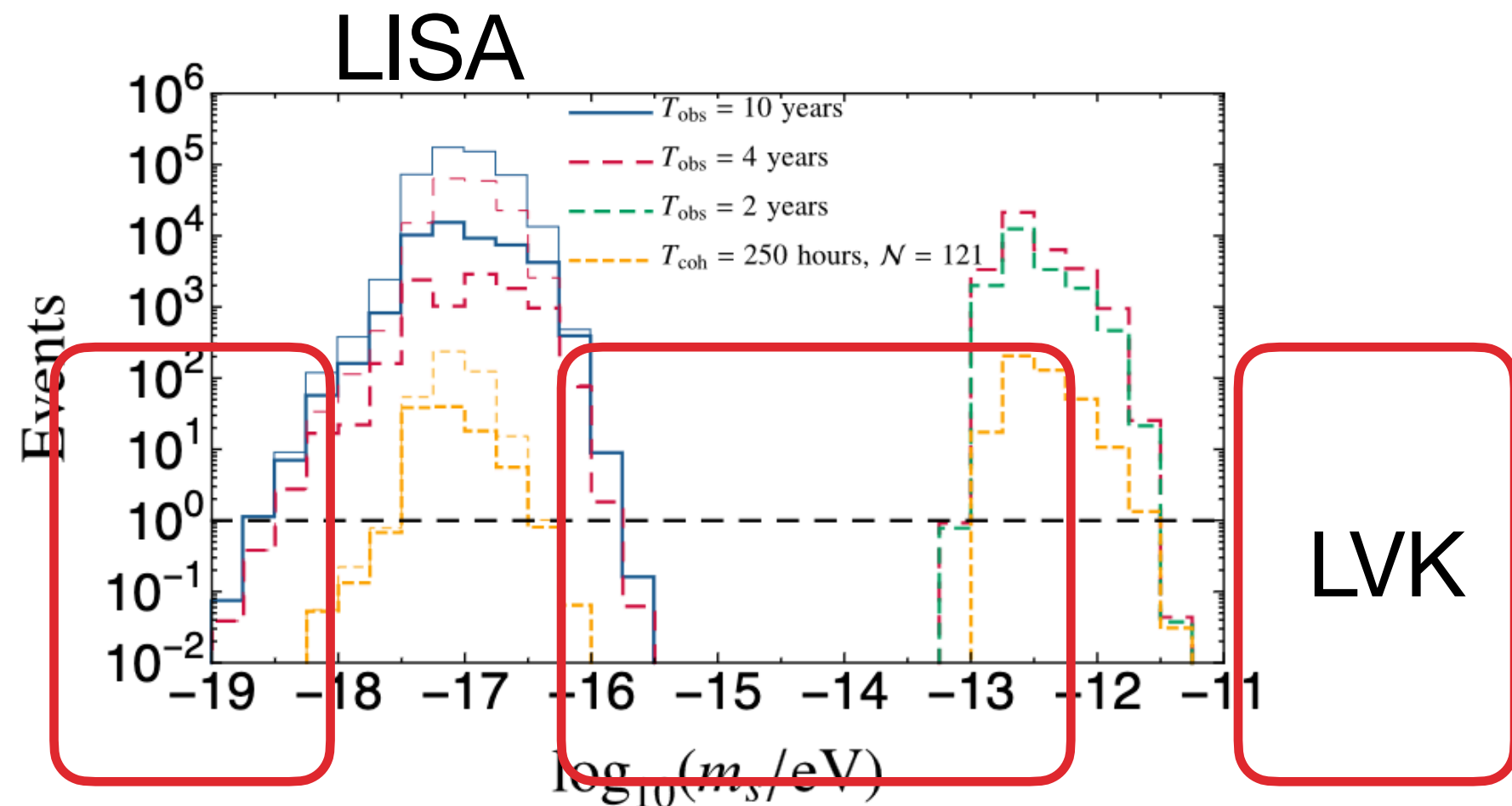
Tsukada et al (2021)



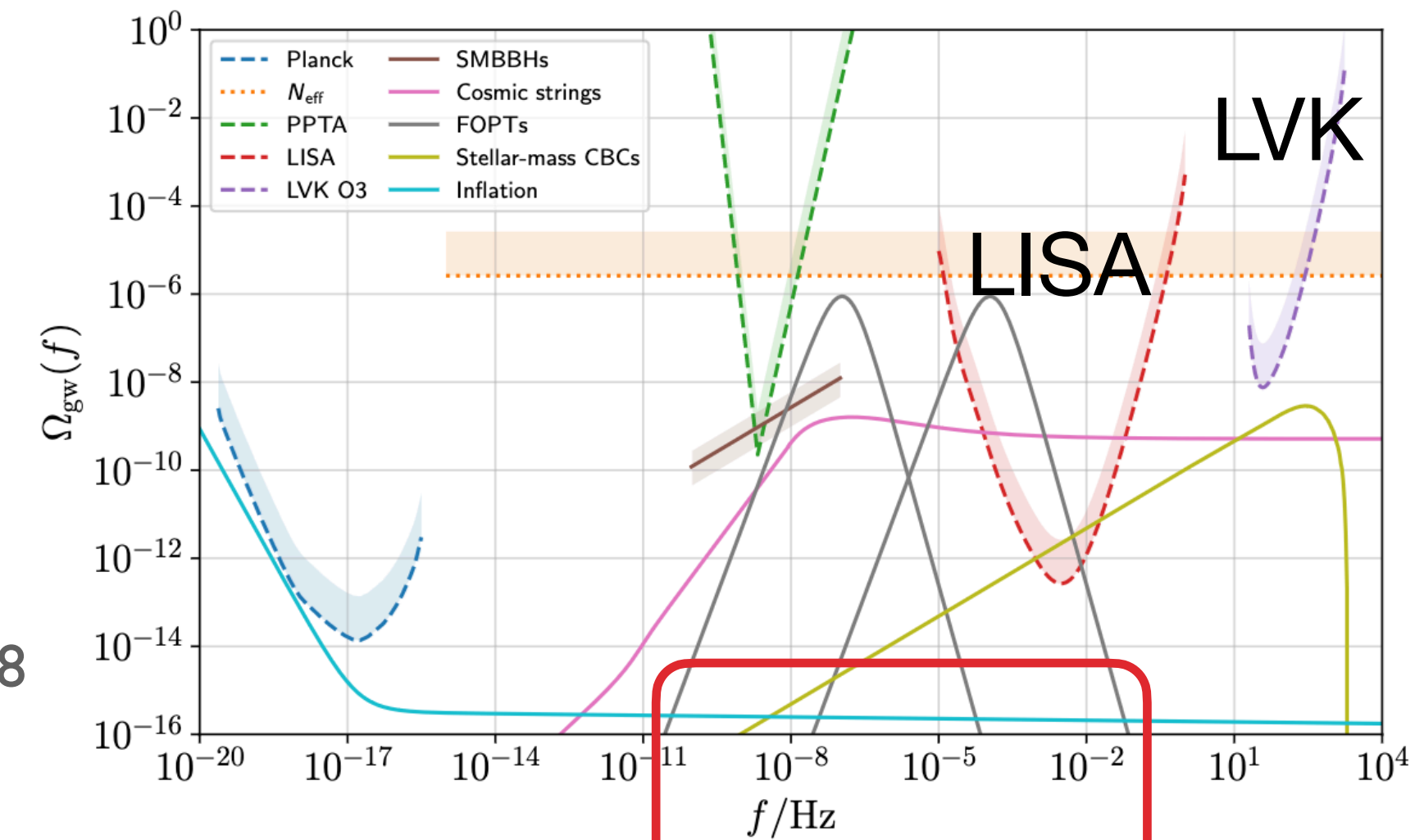
## Spikes?

Cardoso & Maselli 1909.05870  
Coogan et al. 2108.04154 [gr-qc]

## FOPT?



Renzini et al 2202.00178  
(based on 1512.06239)



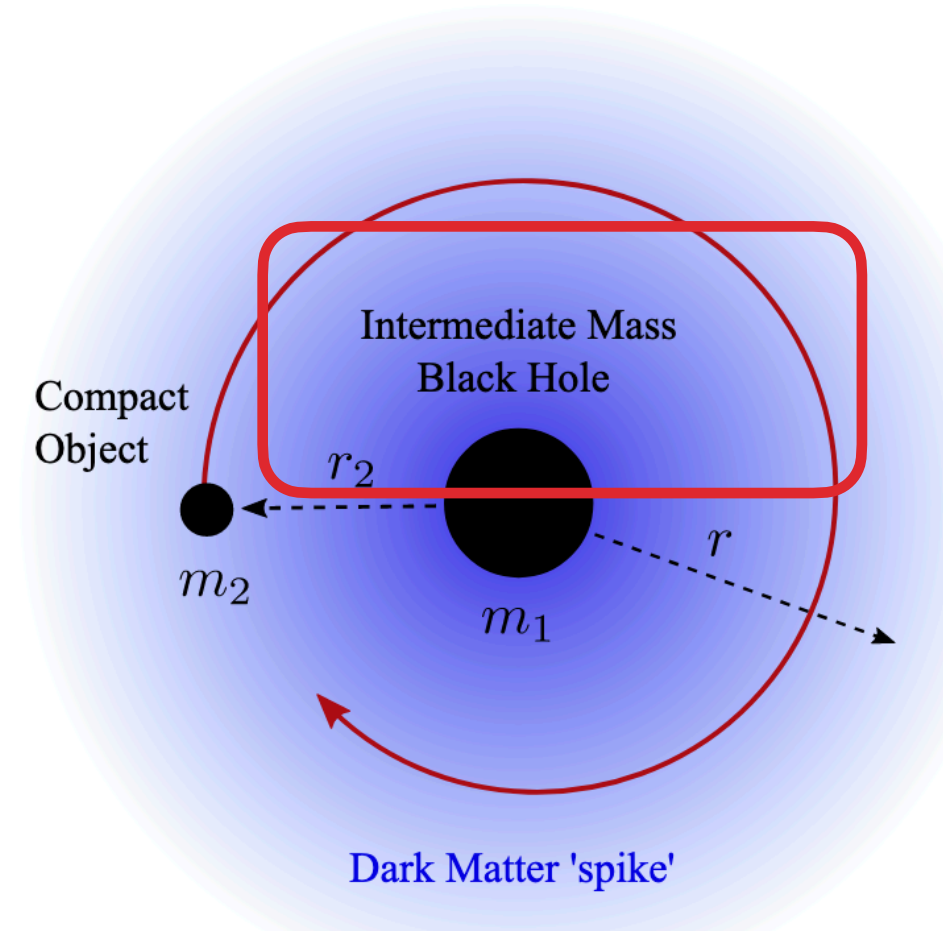
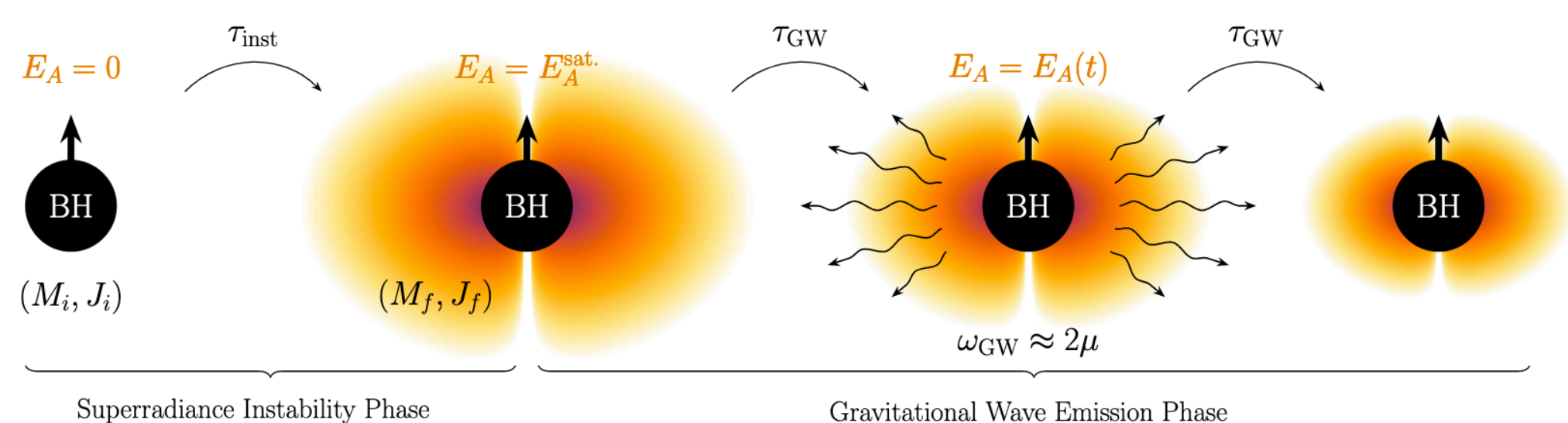


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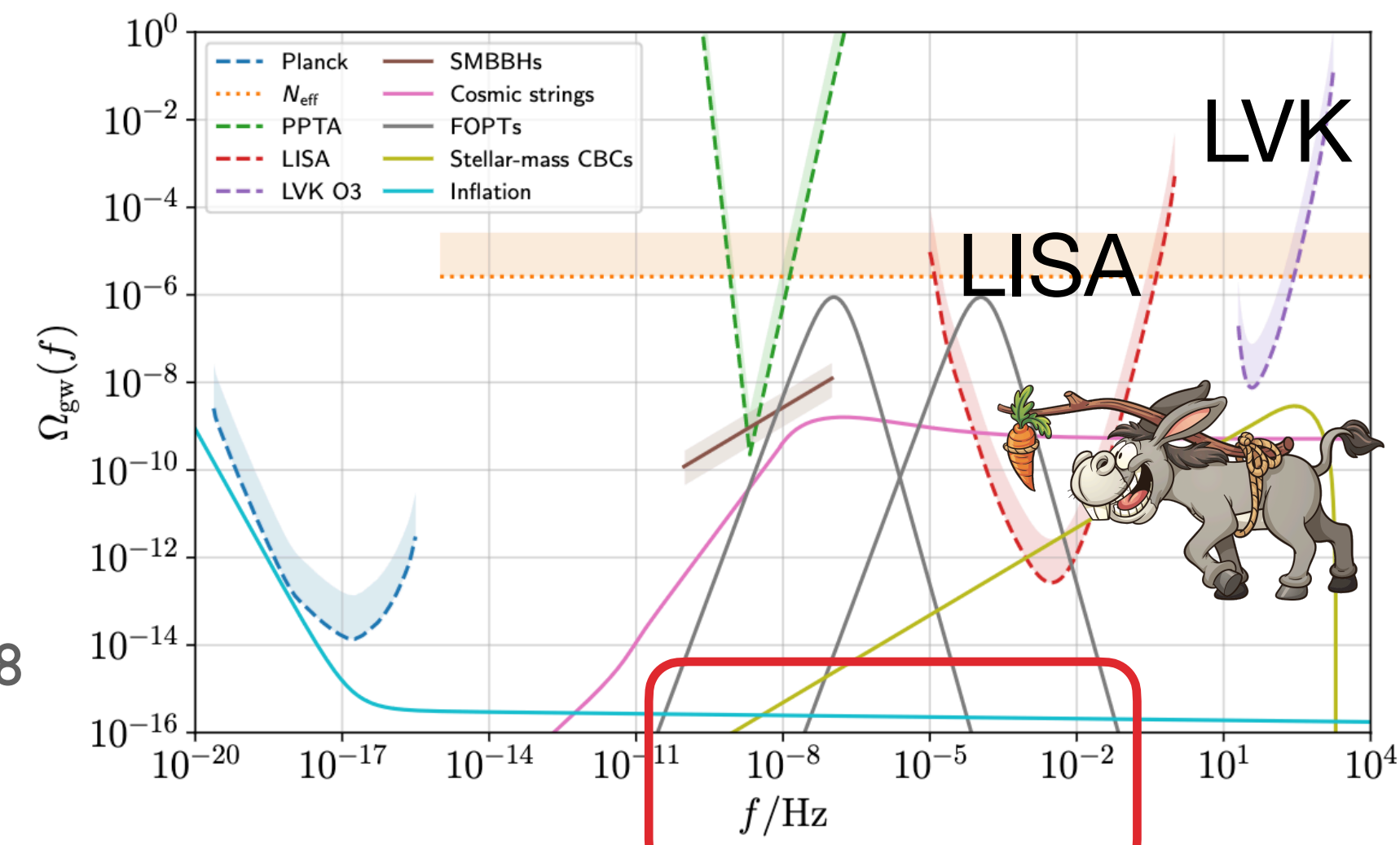
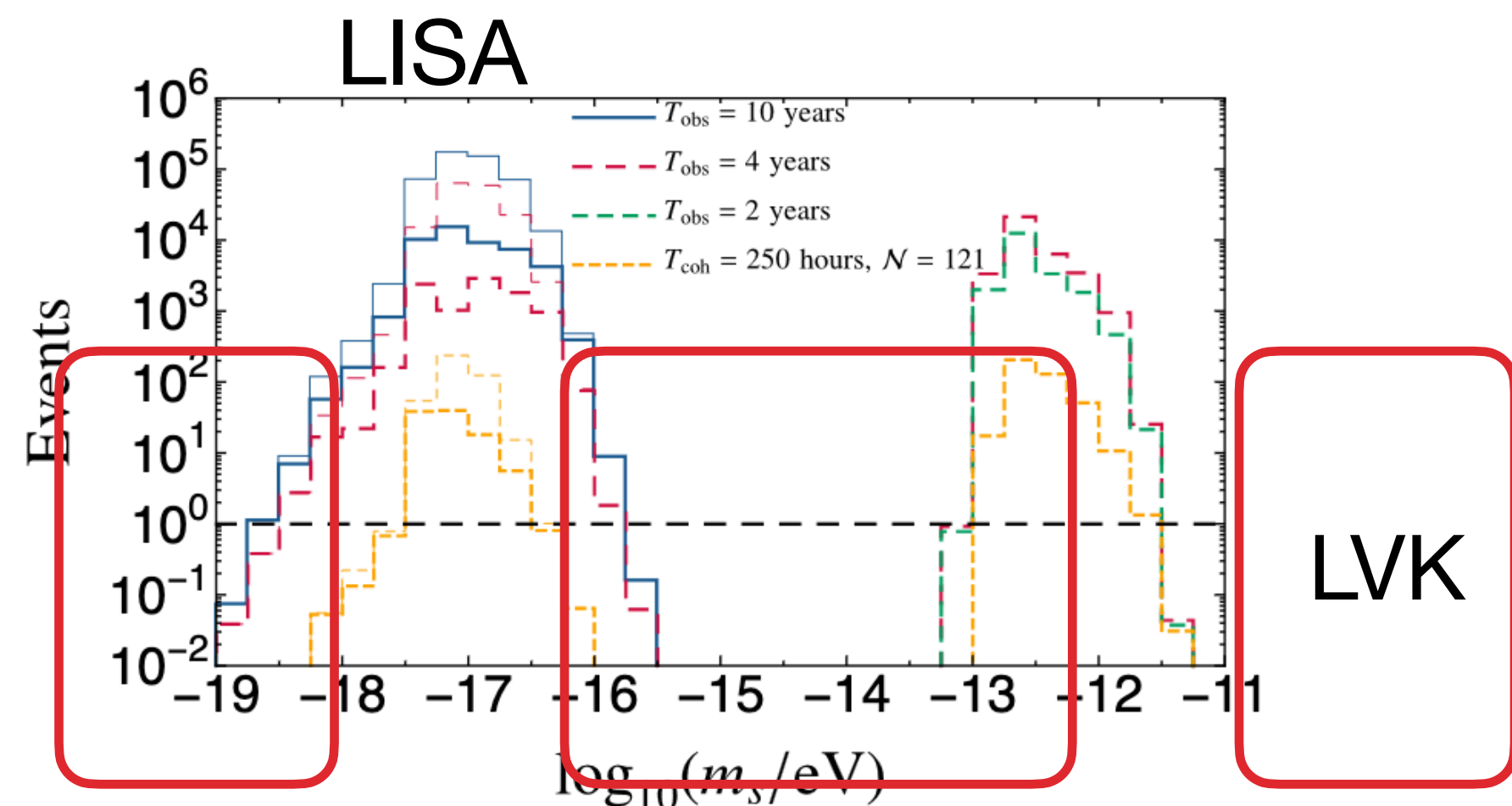


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Cardoso & Maselli 1909.05870

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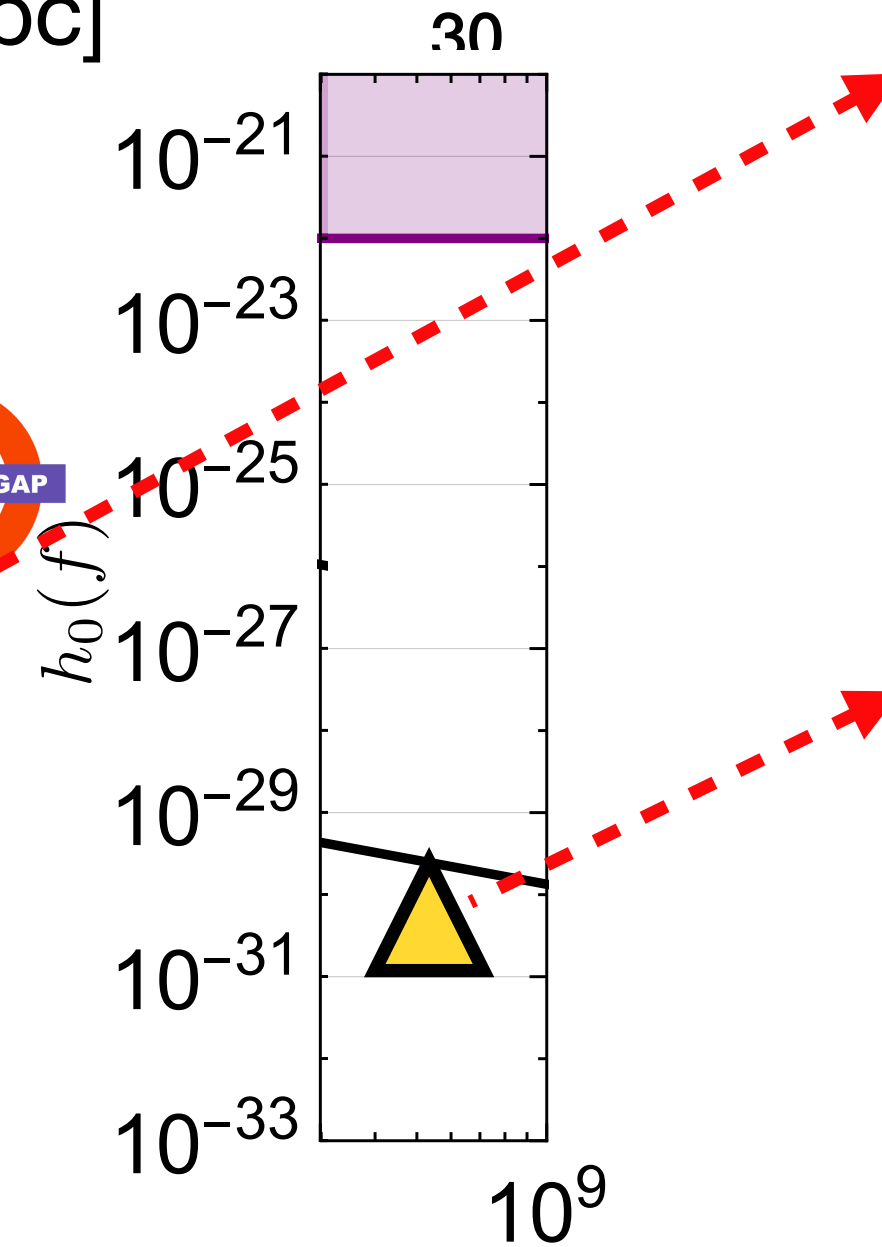
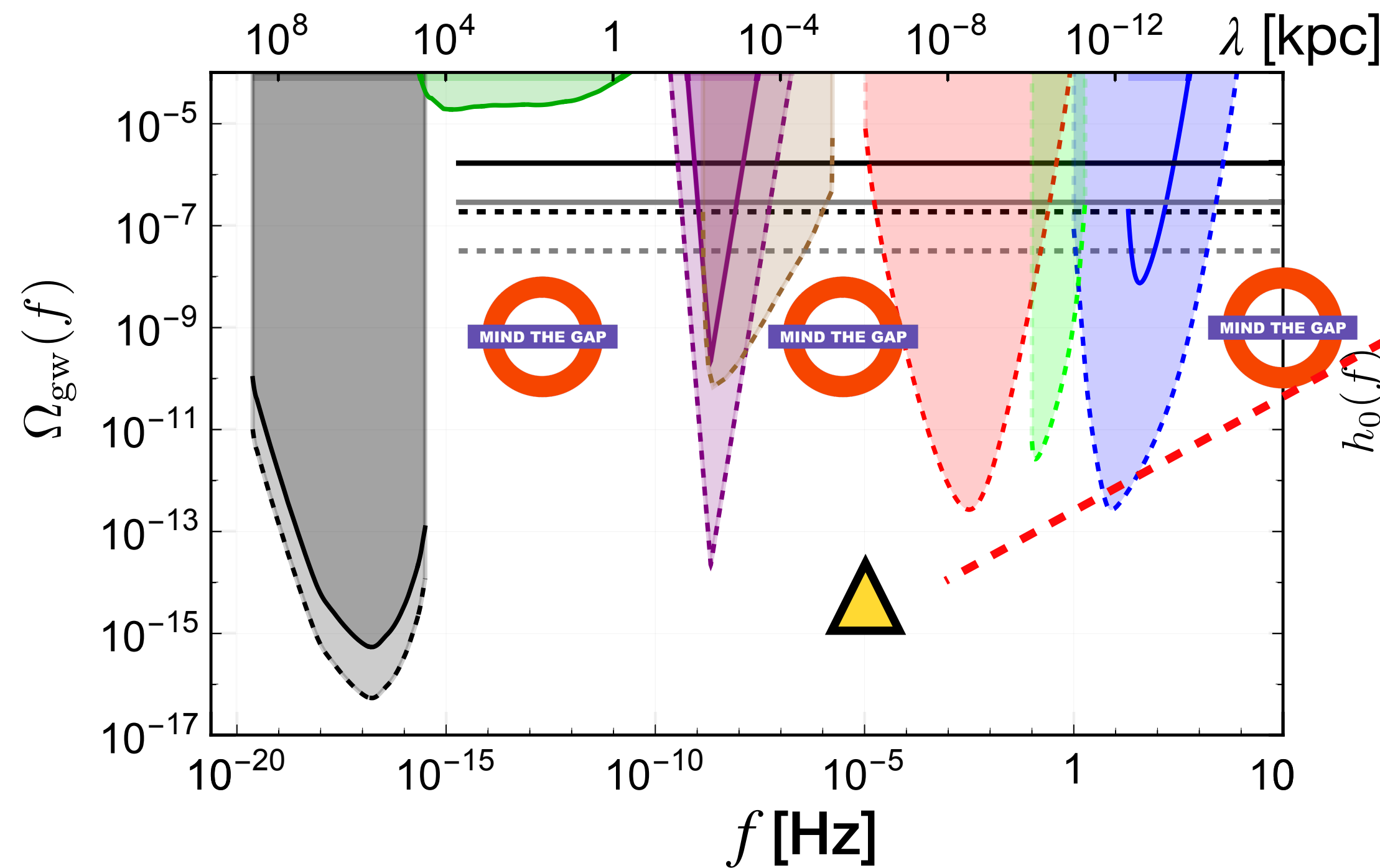
Renzini et al 2202.00178 (based on 1512.06239)

# Conclusions

**Multiband approach to GWs:** great potential to transform both astrophysics and BSM

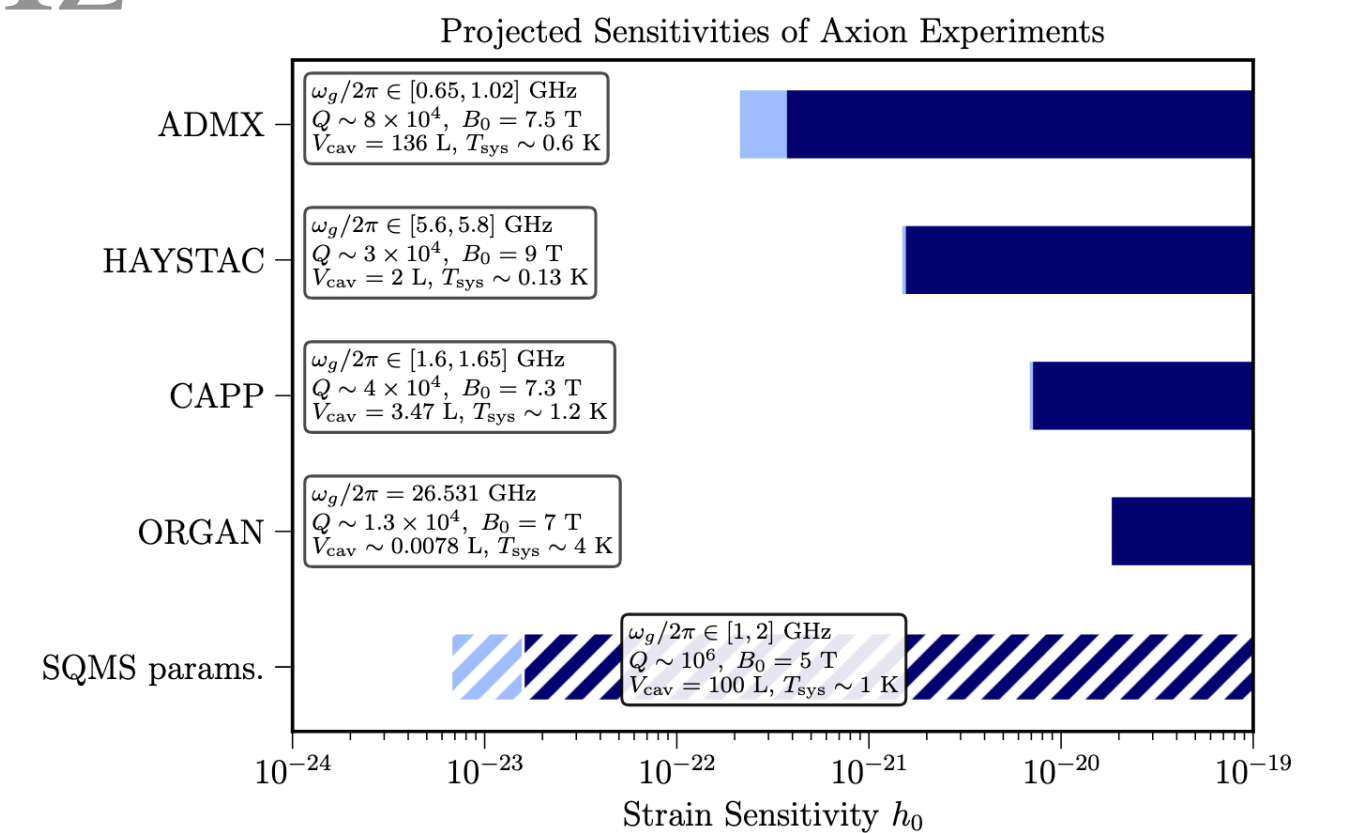
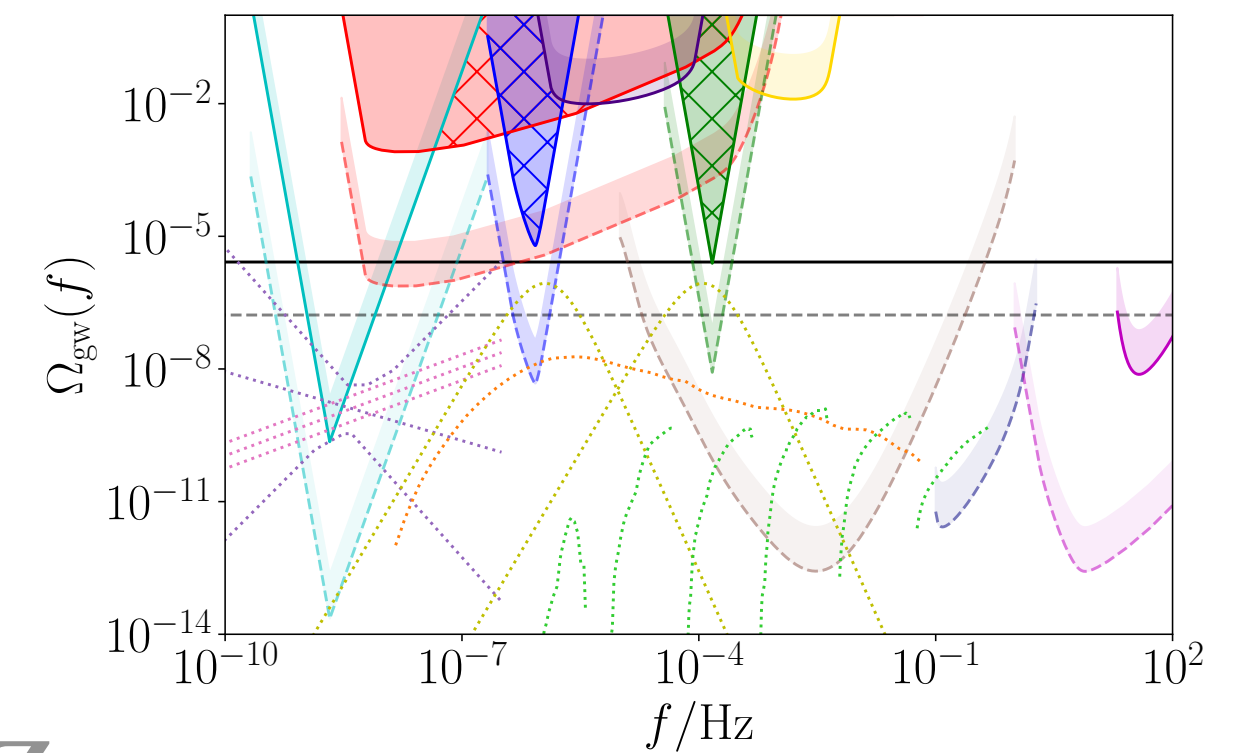
**For this:**

- i) there is vigours effort to in four regions (CMB/PTA/LISA/LVK)
- ii) new ideas are needed in other phenomenologically rich regions



$\mu\text{Hz}$

$\text{GHz}$





Multiband

