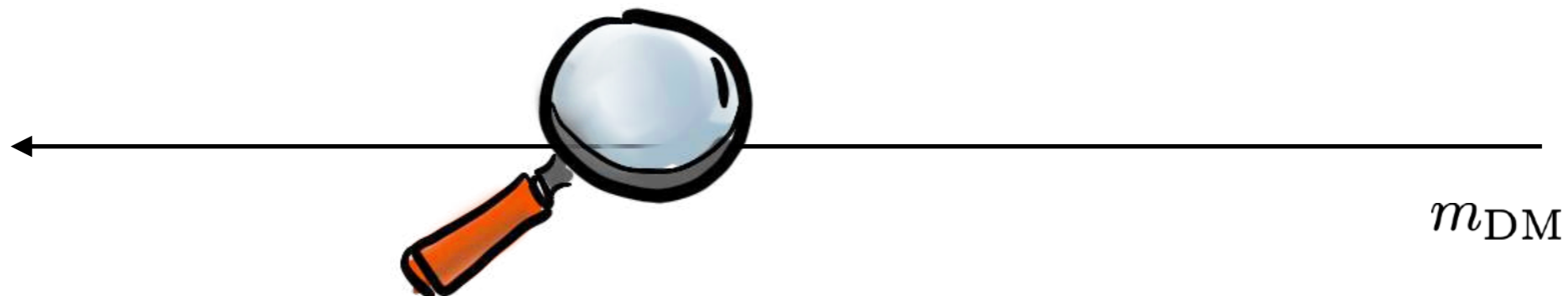


Targeting soft imprints of dark matter

Clara Murgui (UAB/IFAE/CERN)

L. Badurina, Y. Du, K. Pardo, R. Plestid, Y. Wang, and K. M. Zurek [all @ Caltech]

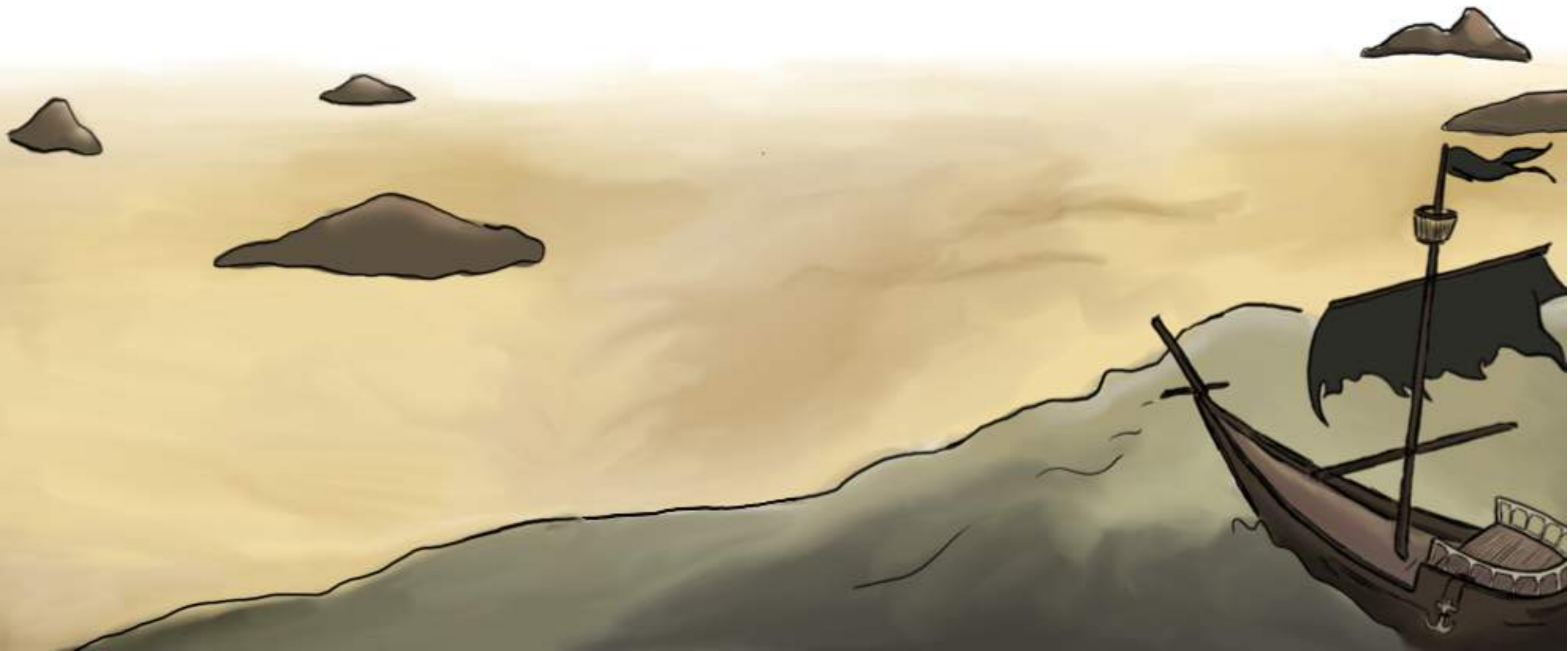
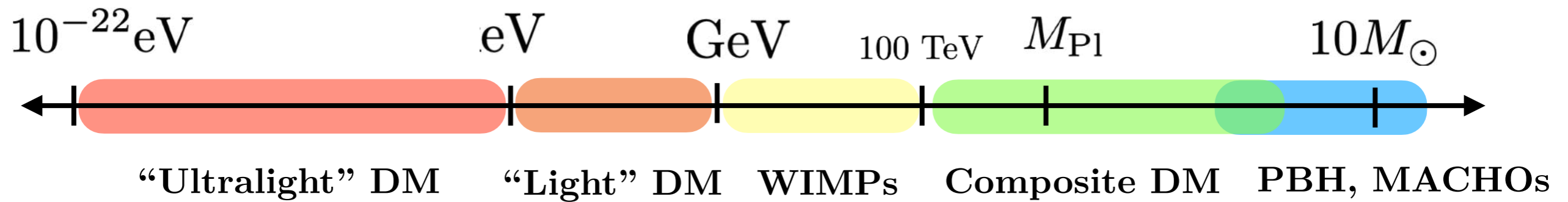


R. Adhikari [Caltech], S. Chiow [JPL], L. P. McCuller [Caltech], Y. Michimura [Caltech], K. Schwab [Caltech], Y. Patil [Yale U.], J. Harris [Yale U.]

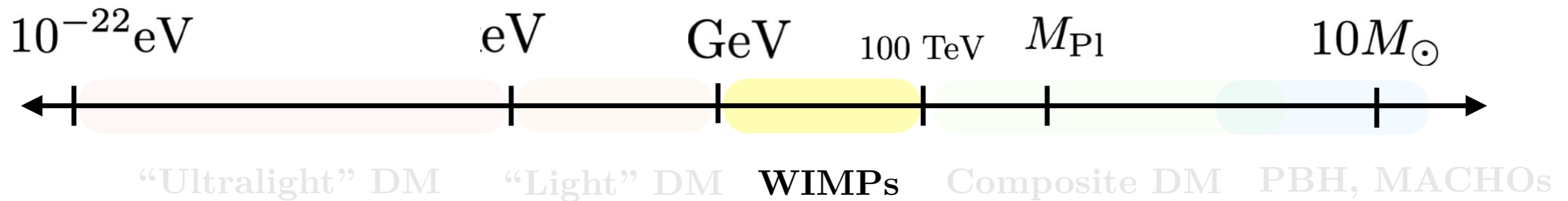
Dark Matter Beyond the Weak Scale II

26th March 2024

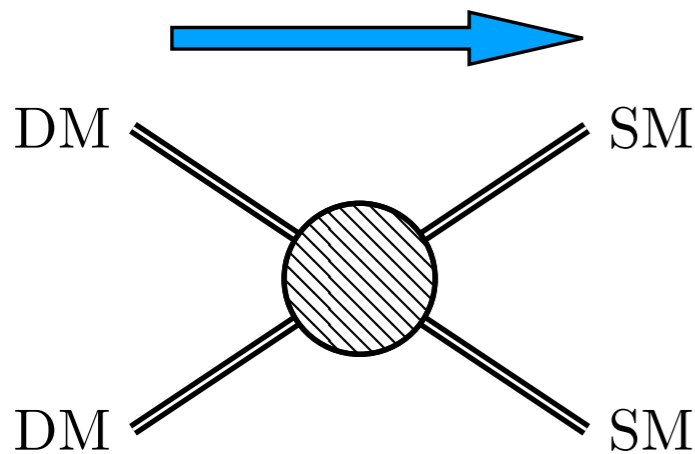
Dark Matter: where to look?



Dark Matter: where to look?




The WIMP miracle



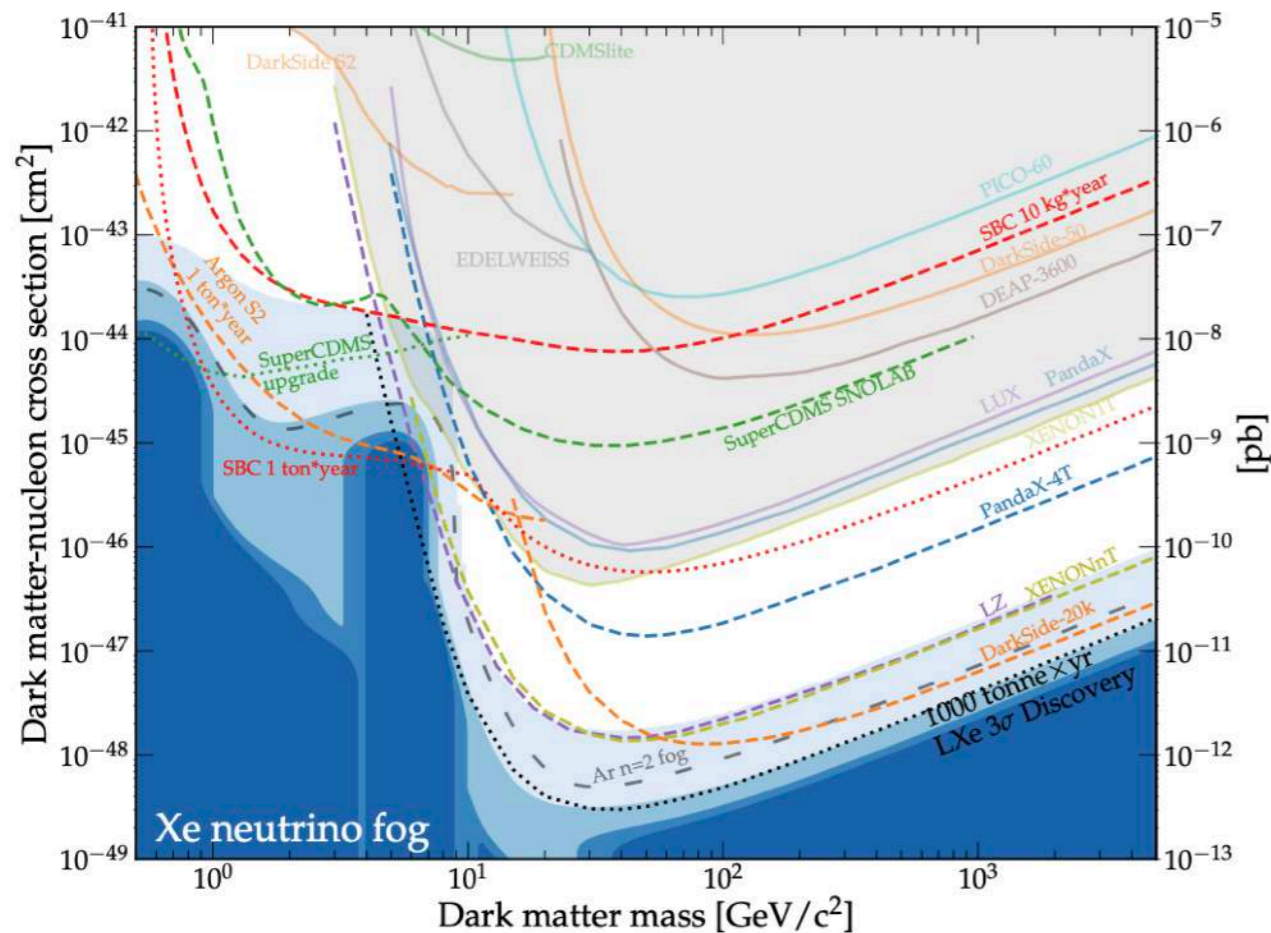
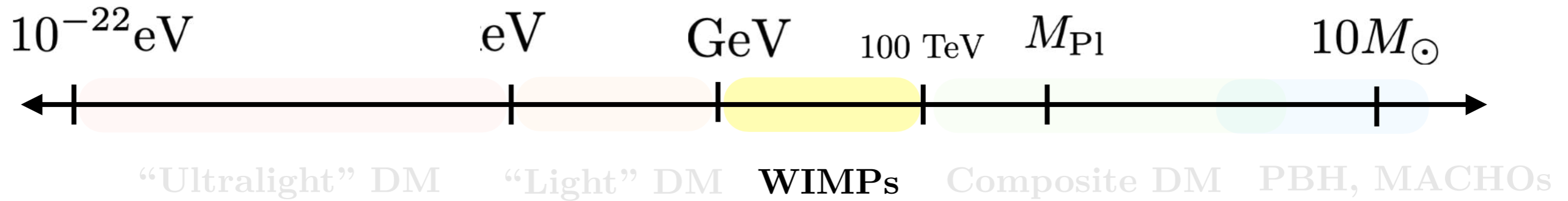
$\Rightarrow \langle \sigma v \rangle \sim \frac{G_F^2}{8\pi} m_{\chi}^2 \frac{c}{3} \sim 10^{-24} \text{ cm}^3/\text{s} \left(\frac{m_{\chi}}{100 \text{ GeV}} \right)^2$

weak coupling

$\Omega_{\text{DM}} \sim 0.1 \times \left(\frac{3 \times 10^{-26} \text{ cm}^3/\text{s}}{\langle \sigma v \rangle} \right)$



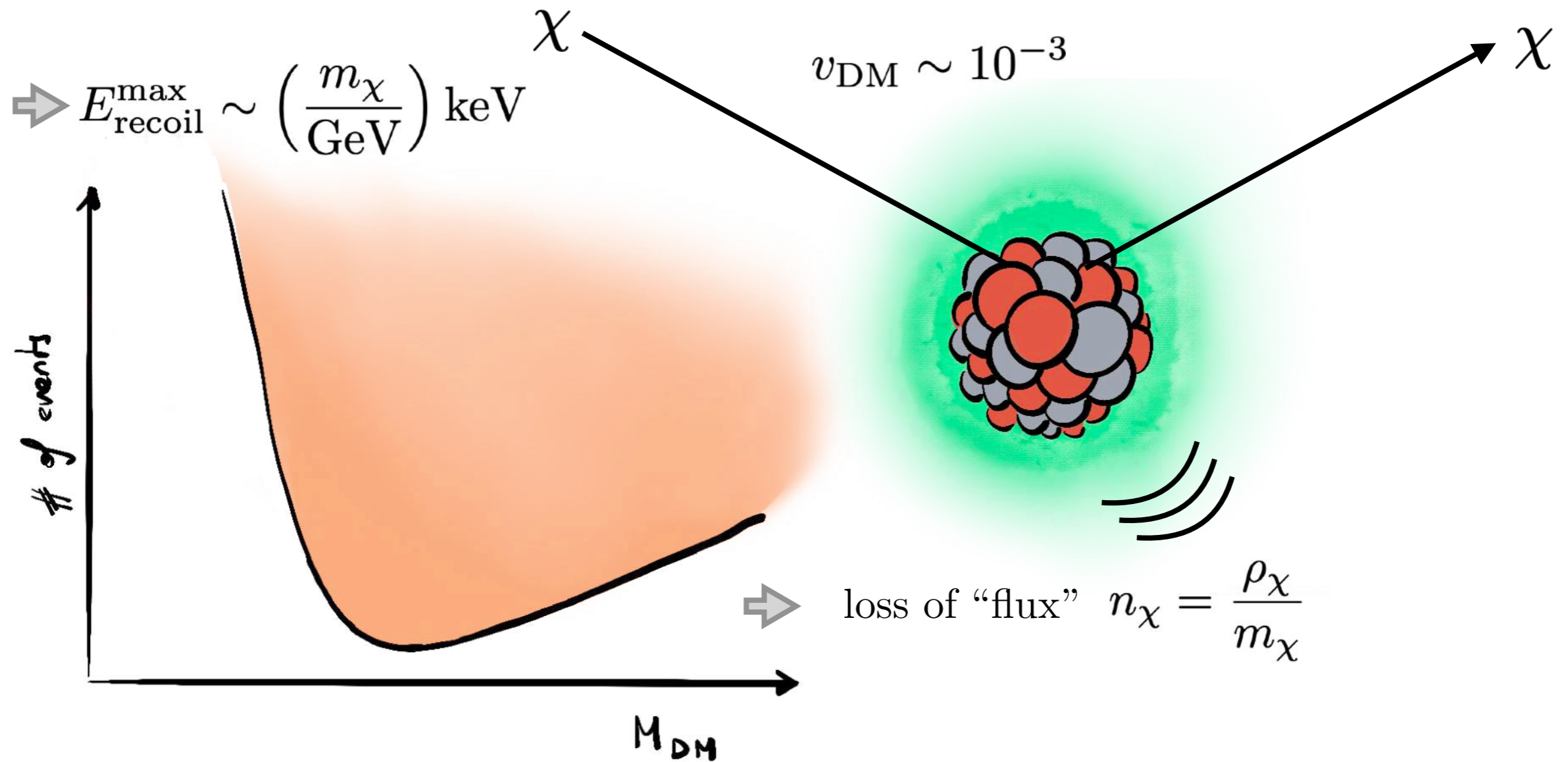
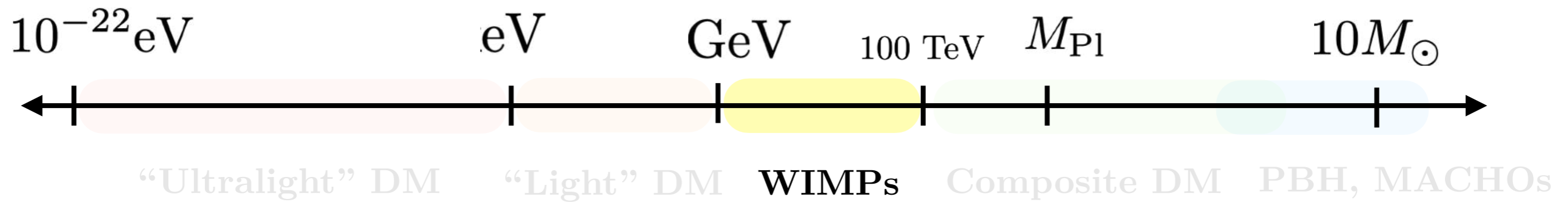
Dark Matter: where to look?



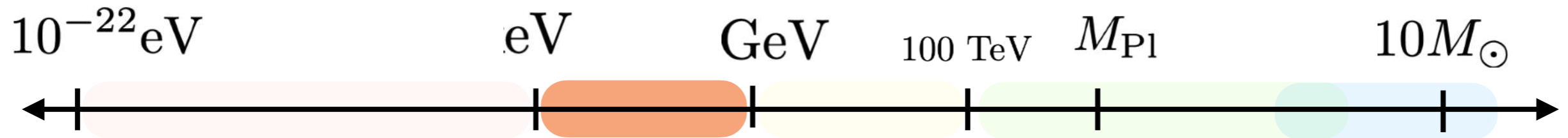
$$\sigma \sim 10^{-34} \text{ cm}^2 \left(\frac{m_{\chi}}{100 \text{ GeV}} \right)^2$$

[Akerib, D. S., et al., Snowmass2021, 2203.08084]

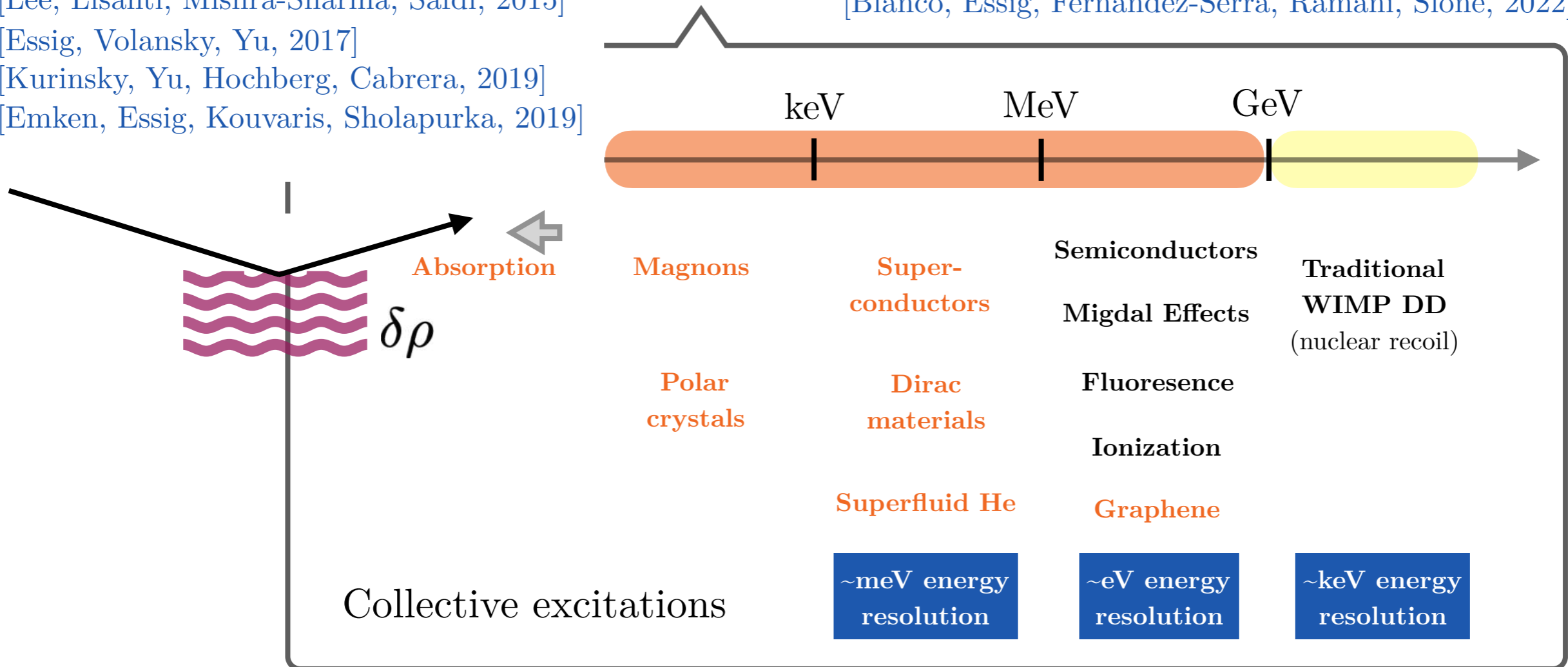
Dark Matter: where to look?



Dark Matter: where to look?



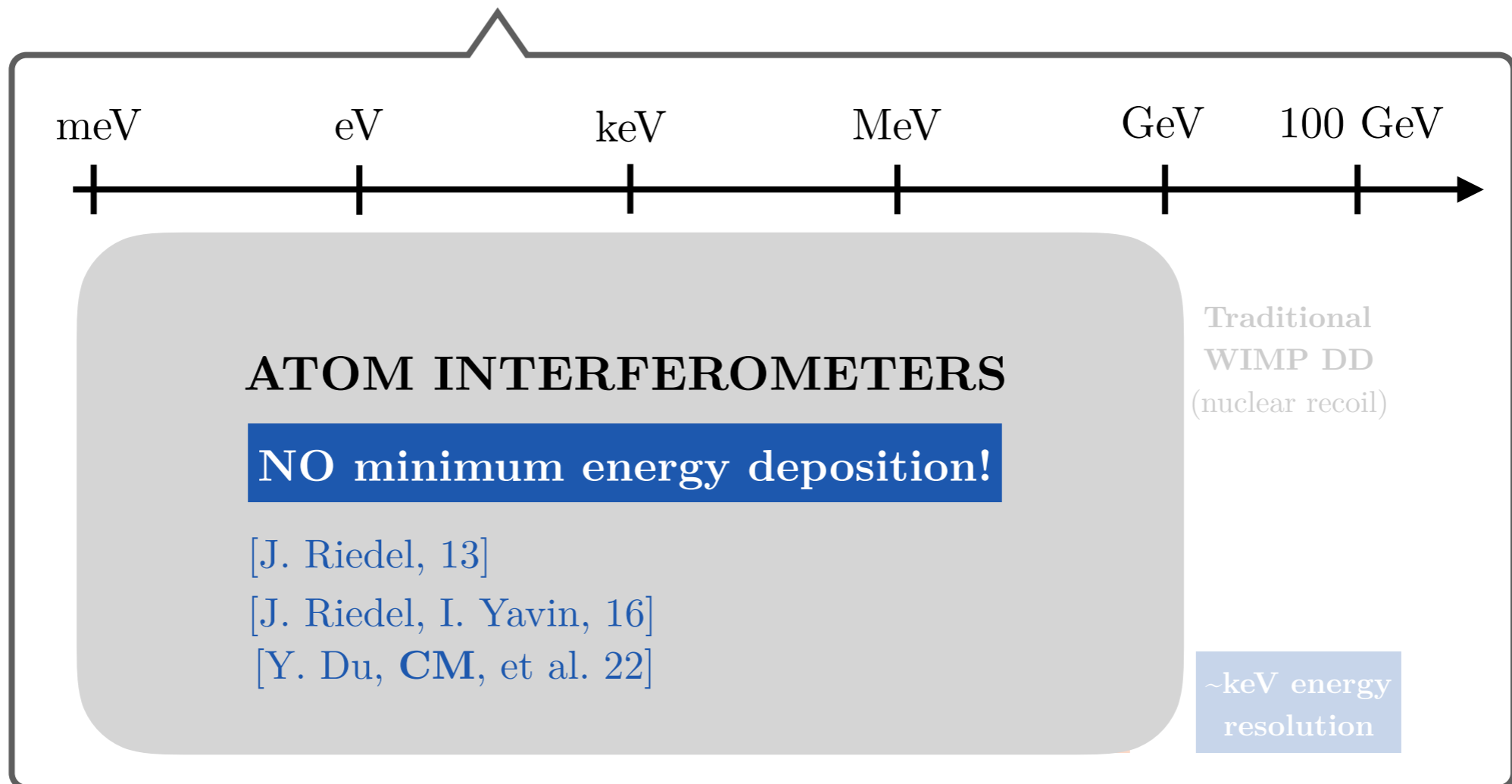
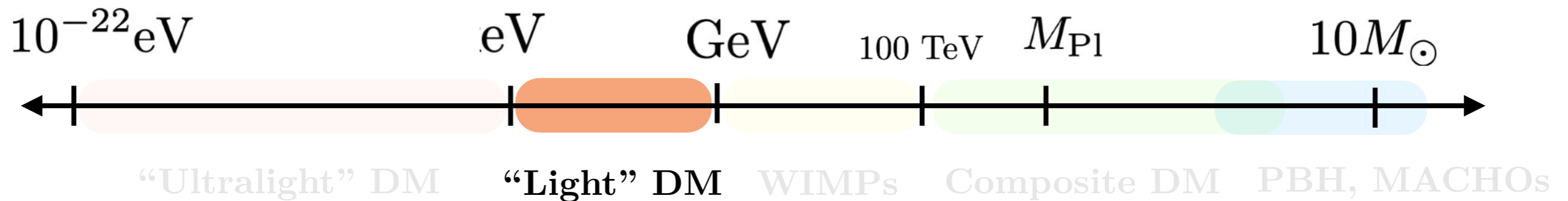
[\[Essig, Mardon, Volansky, 2011\]](#) “Ultra-light” DM
[\[Graham, Kaplan, Rajendran, Walters, 2012\]](#) “Light” DM
[\[Lee, Lisanti, Mishra-Sharma, Safdi, 2015\]](#) WIMPs
[\[Essig, Volansky, Yu, 2017\]](#) Composite DM
[\[Kurinsky, Yu, Hochberg, Cabrera, 2019\]](#) PBH, MACHOs
[\[Emken, Essig, Kouvaris, Sholapurka, 2019\]](#)



[\[Essig, Fernandez-Serra, Mardon, Soto, Volansky, Yu, 2015\]](#)
[\[Derenzo, Essig, Massari, Soto, Yu, 2016\]](#)
[\[Hochberg, Lin, Zurek, 2016\]](#)
[\[Bloch, Essig, Tobioka, Volansky, Yu, 2016\]](#)

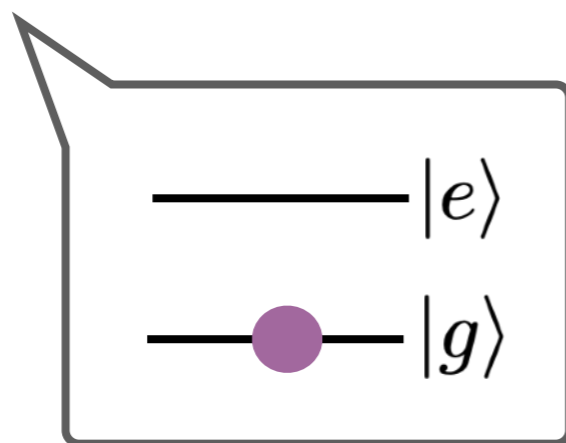
[\[Griffin, Inzani, Trickle, Zhang, Zurek, 2019\]](#)
[\[Coskuner, Mitridate, Olivares, Zurek, 2020\]](#)
[\[Mitridate, Trickle, Zhang, Zurek, 2021\]](#)
[\[Chen, Mitridate, Trickle, et al, 2022\]](#)

Dark Matter: where to look?



AIs: the Principle

Review: arXiv:2003.12516

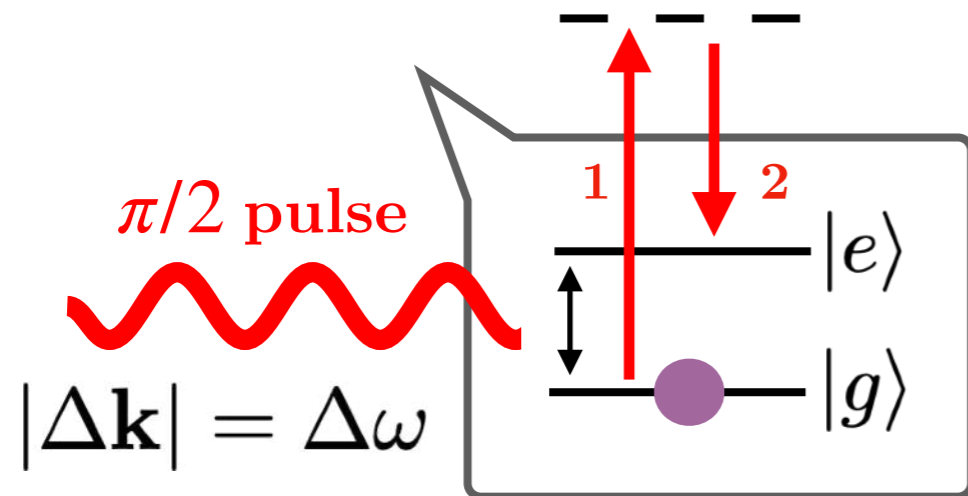
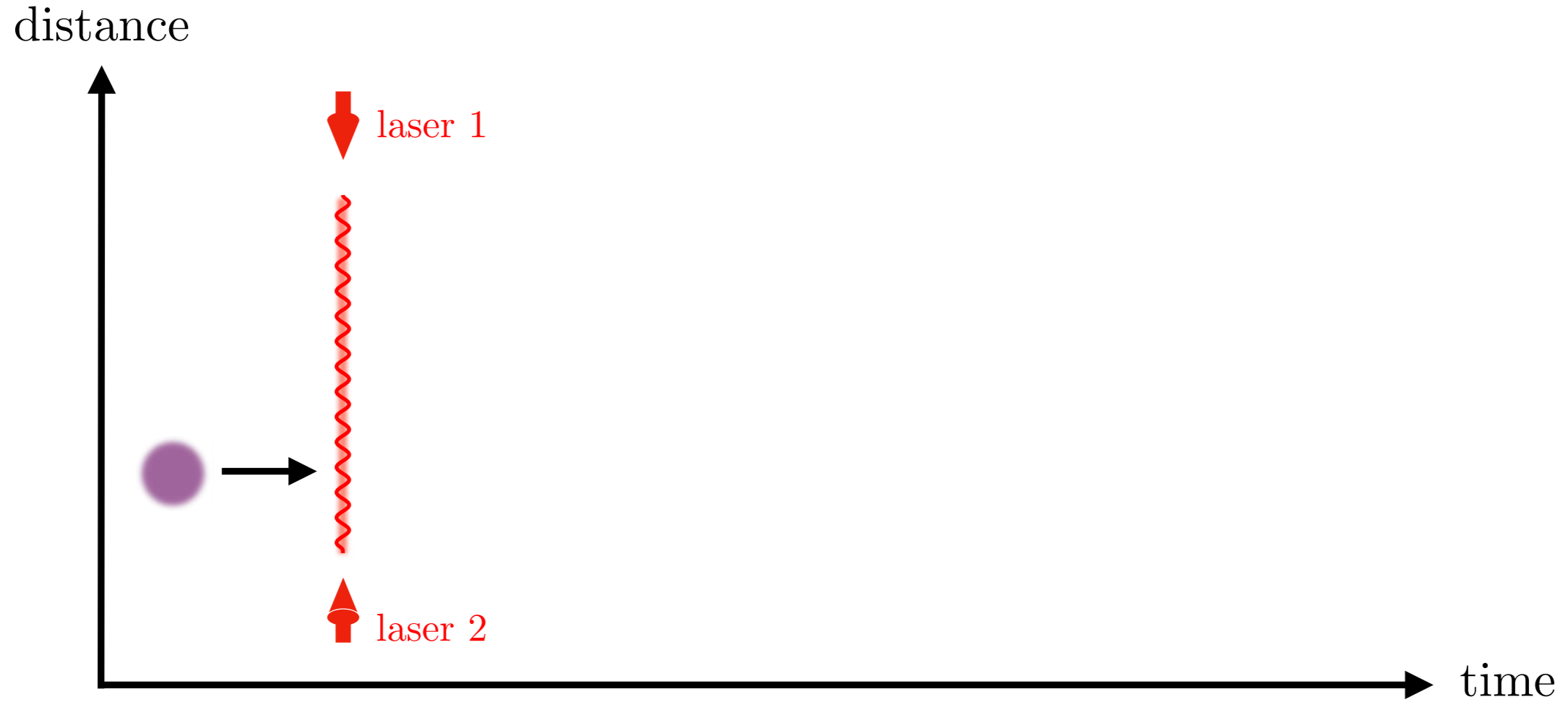


$$\Rightarrow |\Psi\rangle_0 = |g\rangle$$



AIs: the Principle

Review: arXiv:2003.12516

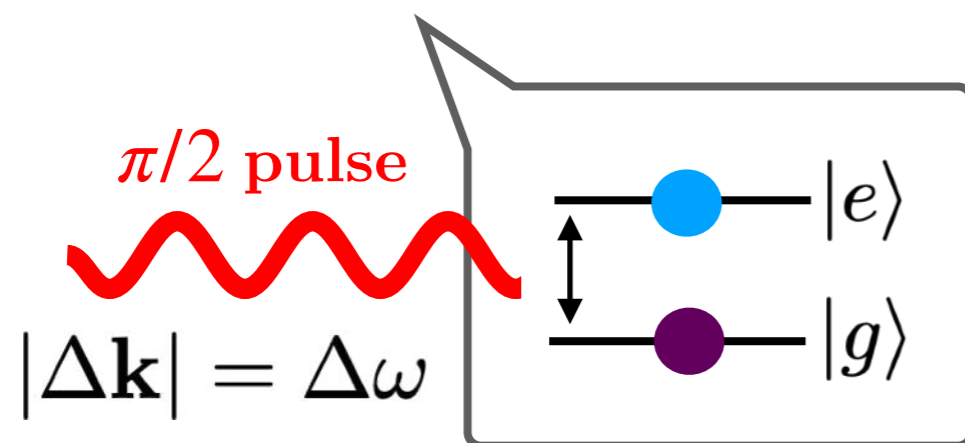
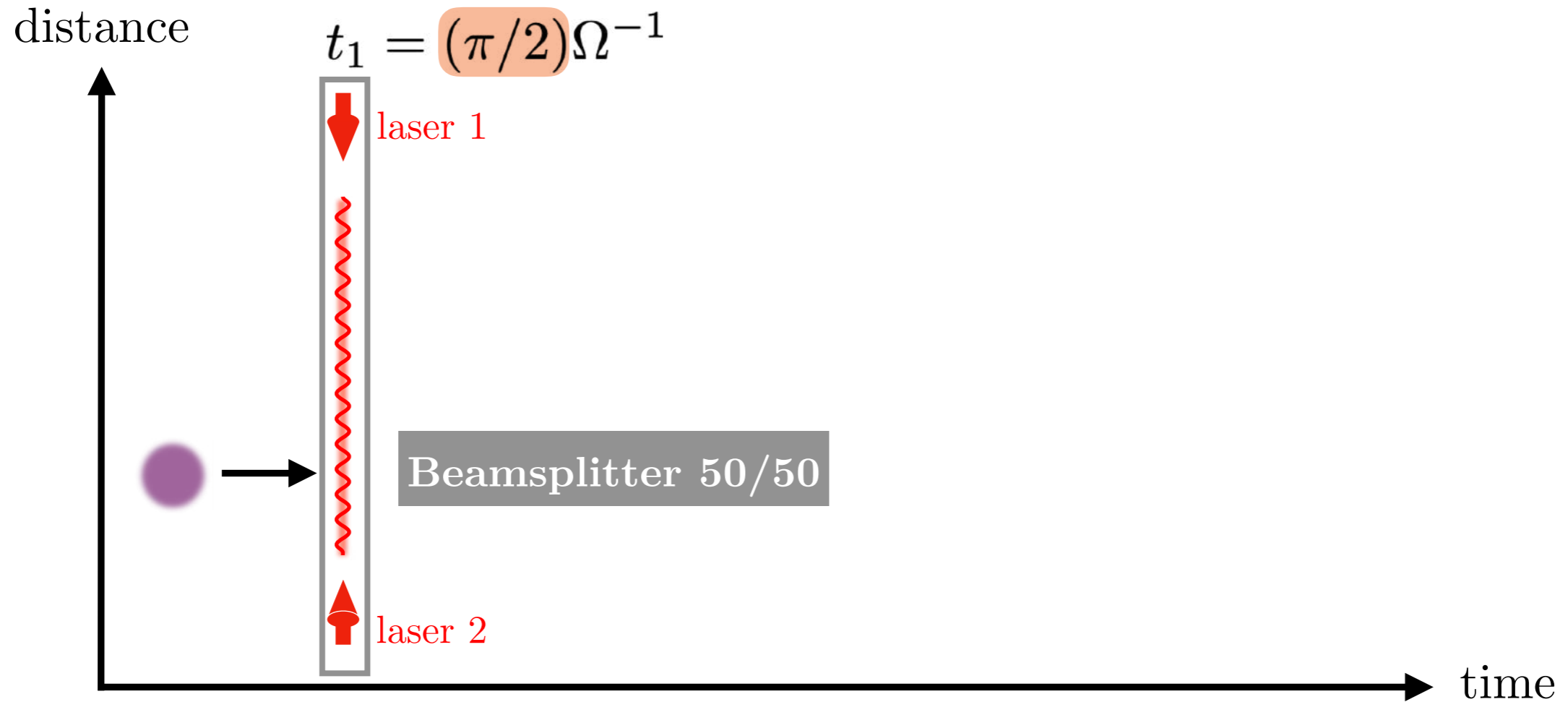


$$\Rightarrow |\Psi\rangle_t = \cos(\Omega t/2)|g\rangle + i \sin(\Omega t/2)|e\rangle$$

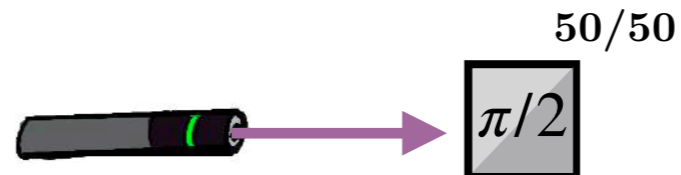


AIs: the Principle

Review: arXiv:2003.12516

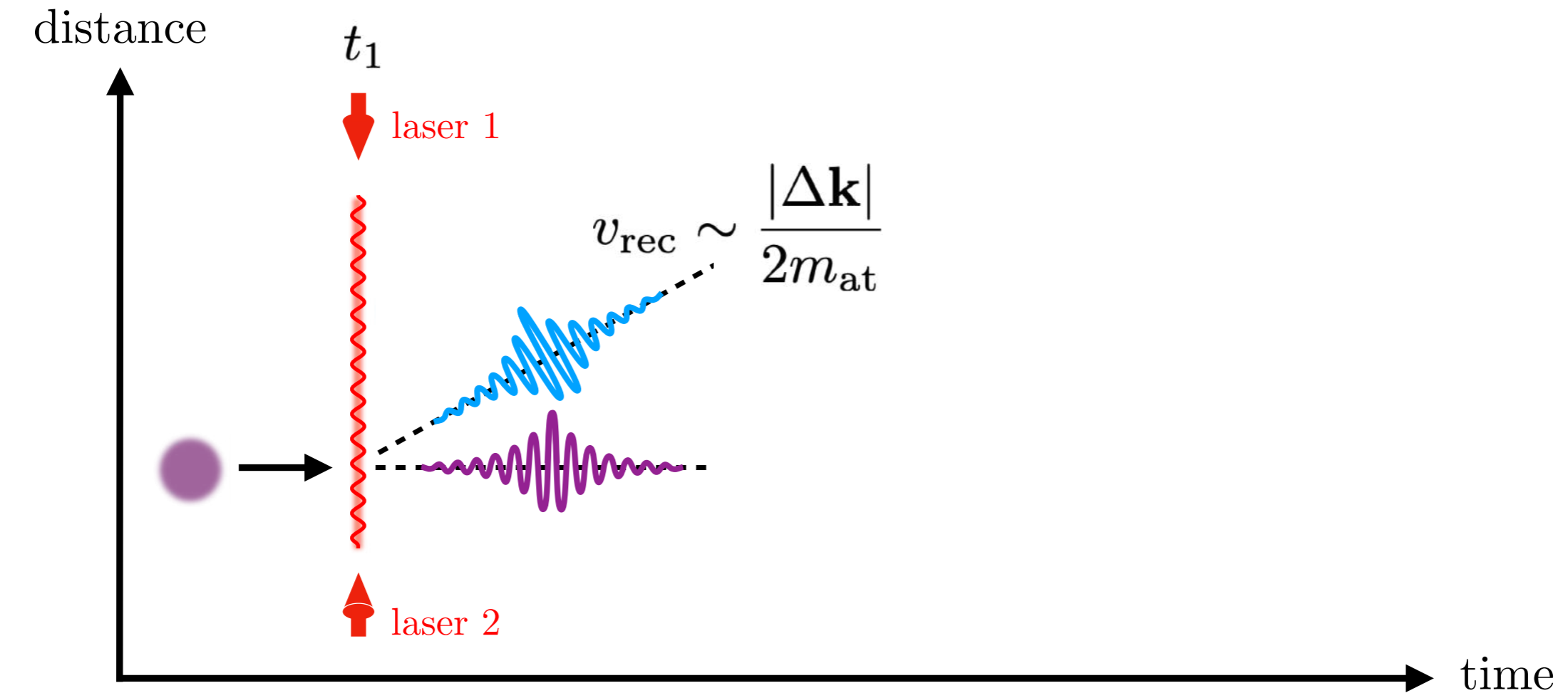


$$\Rightarrow |\Psi\rangle_t = \cos(\pi/4)|g\rangle + i\sin(\pi/4)|e\rangle$$



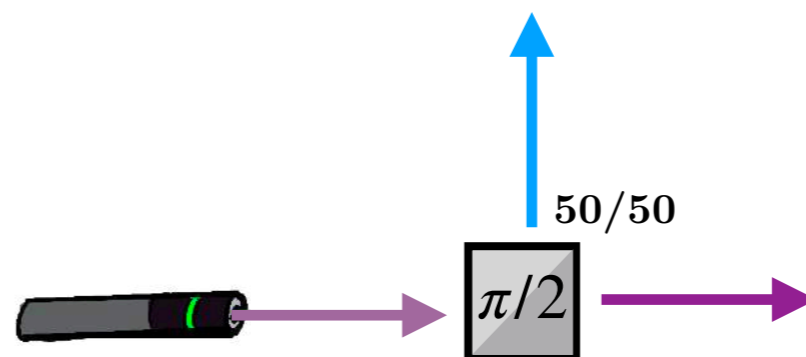
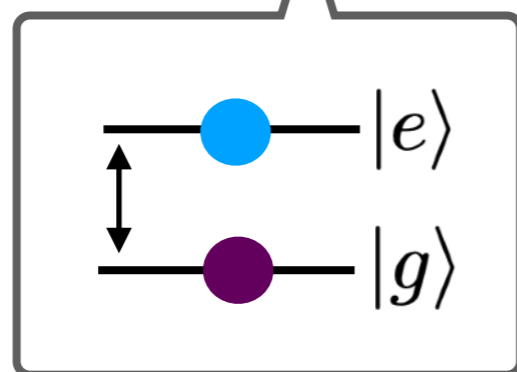
AIs: the Principle

Review: arXiv:2003.12516



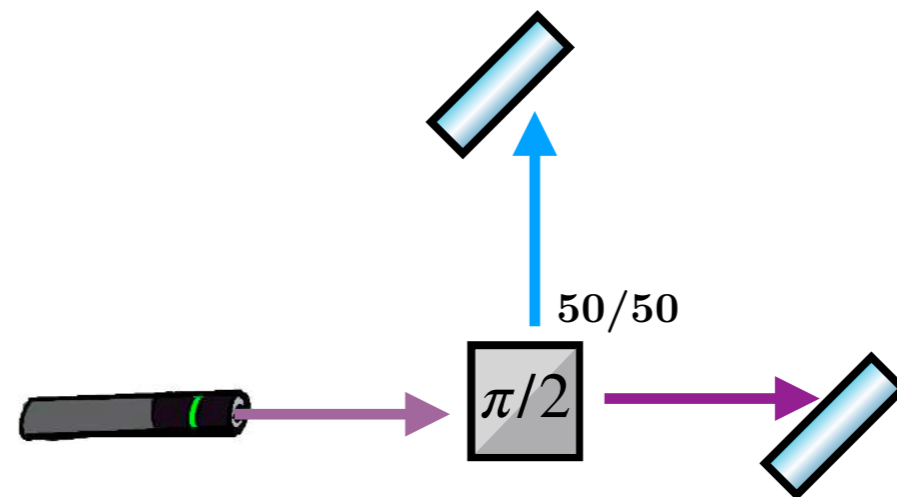
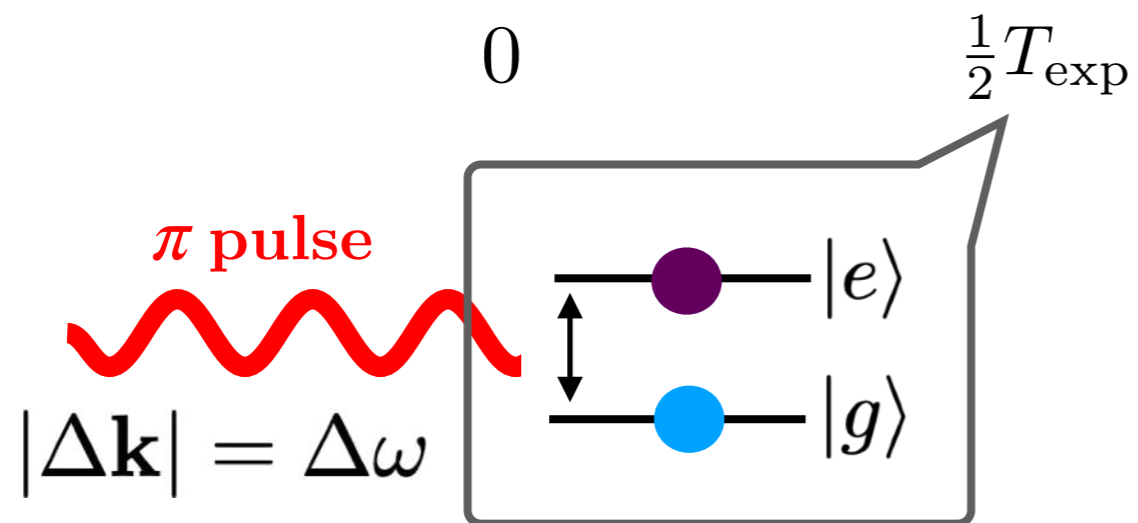
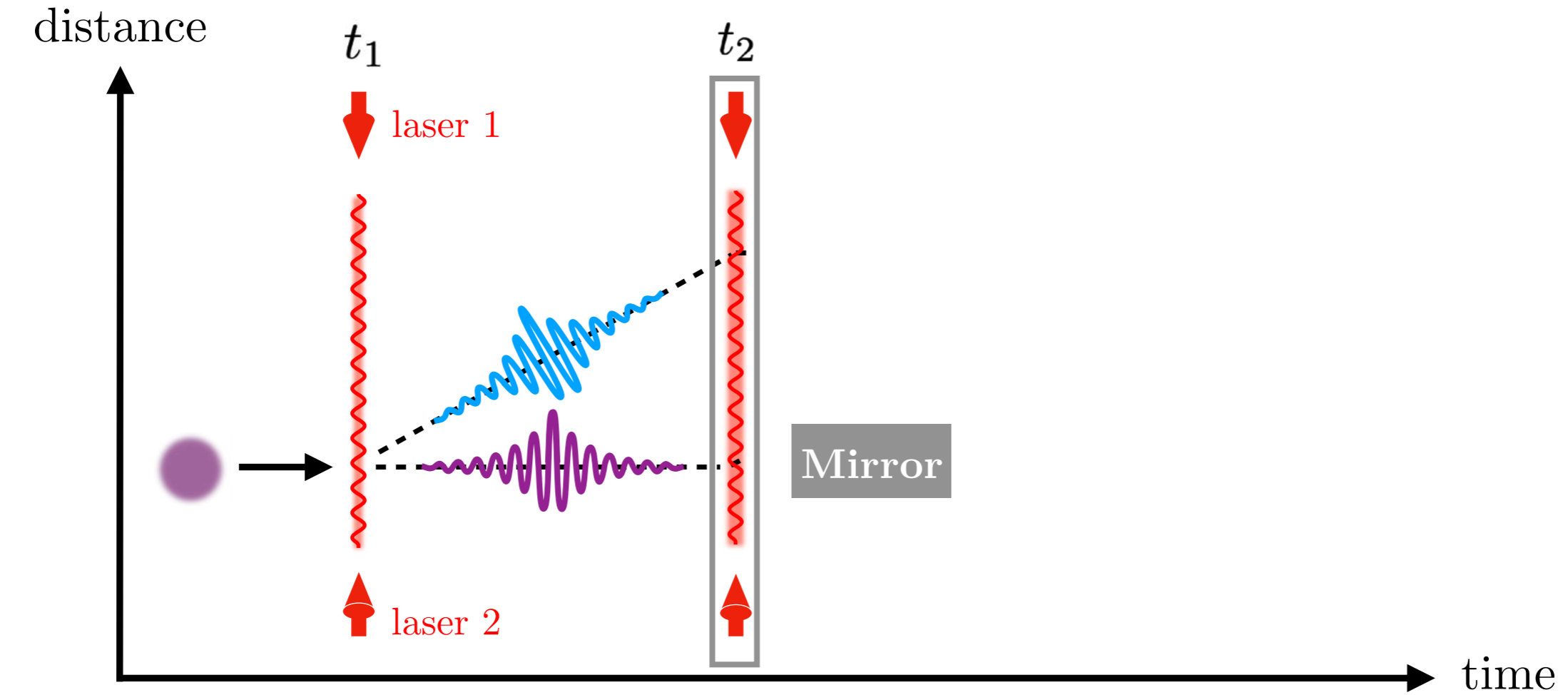
0 $\xrightarrow{\text{orange arrow}}$ $\frac{1}{2}T_{\text{exp}}$

$$|\Delta \mathbf{k}| = \Delta \omega$$



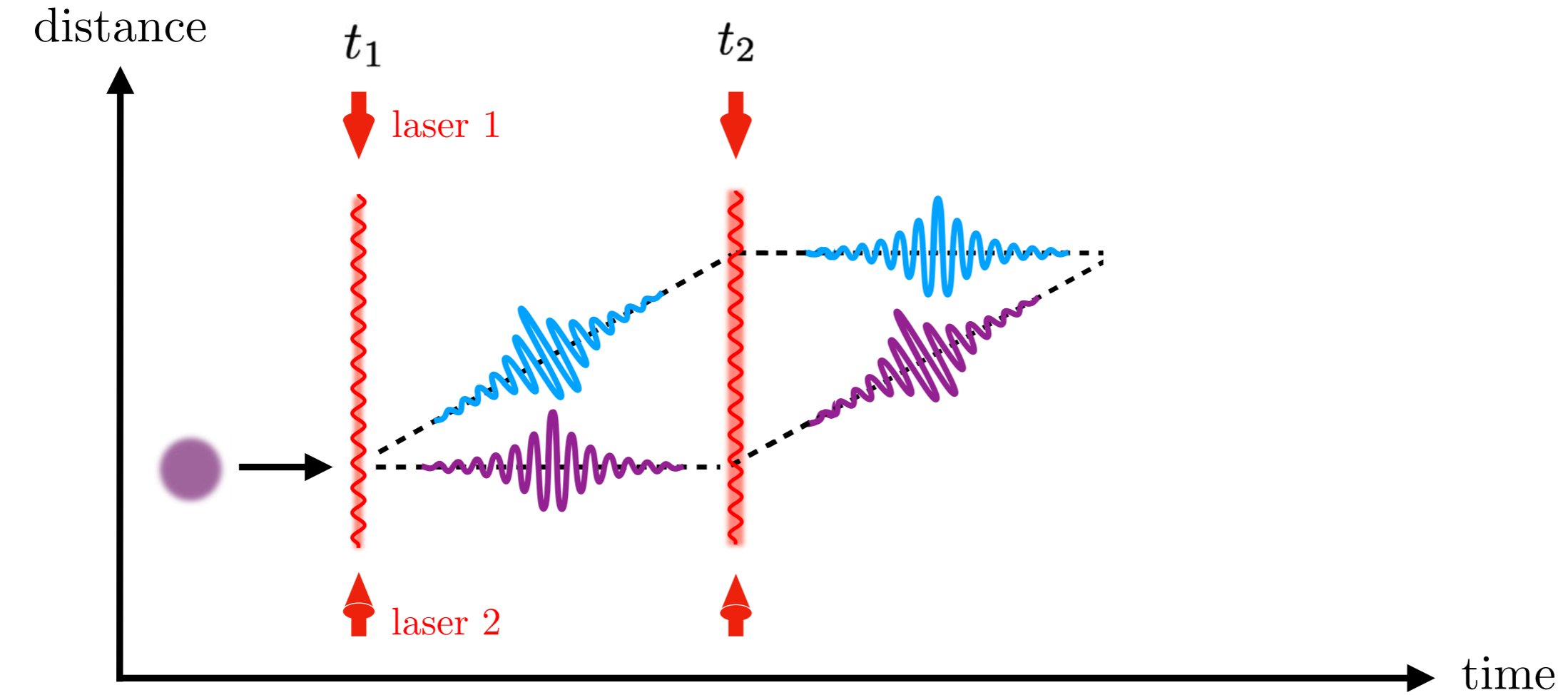
AIs: the Principle

Review: arXiv:2003.12516



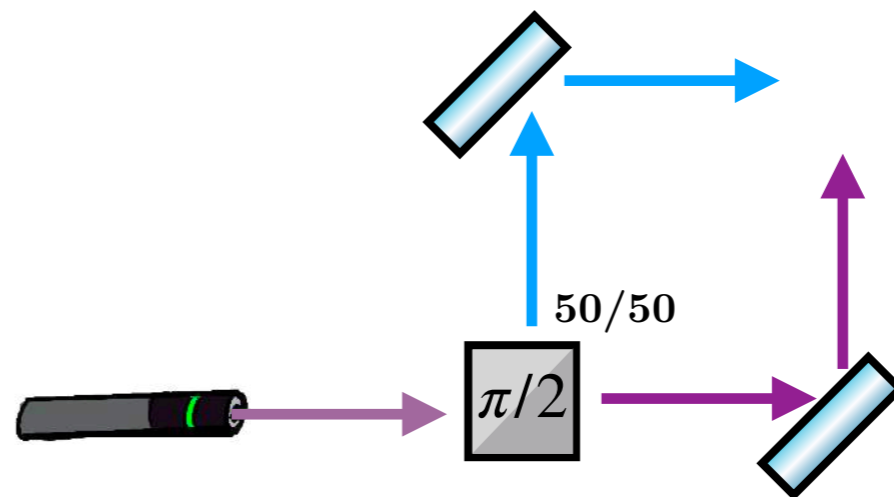
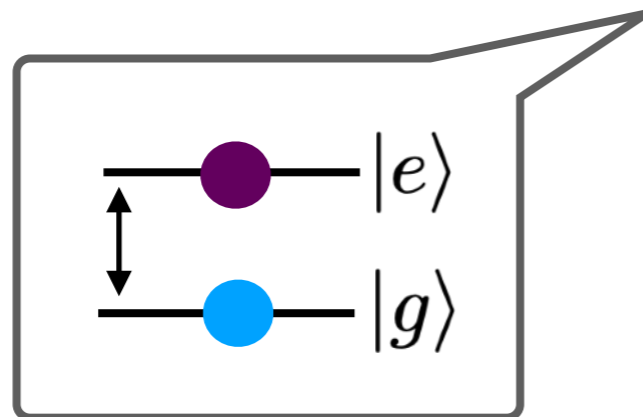
AIs: the Principle

Review: arXiv:2003.12516



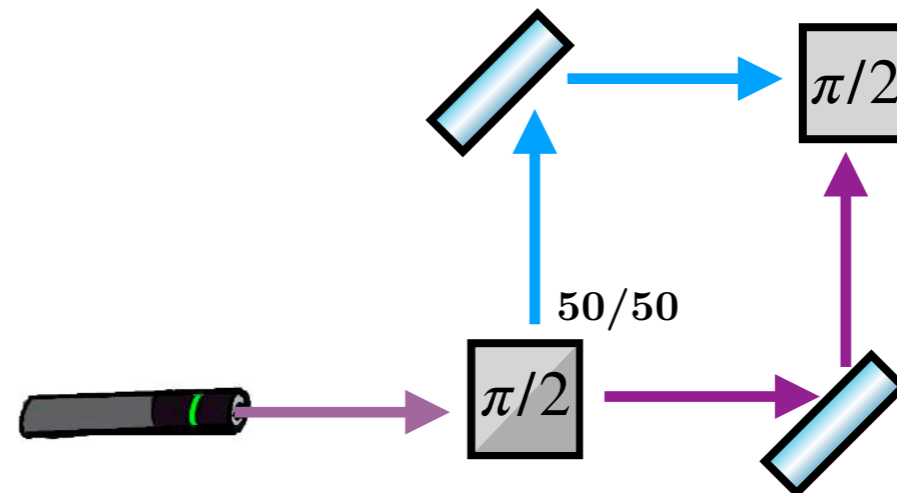
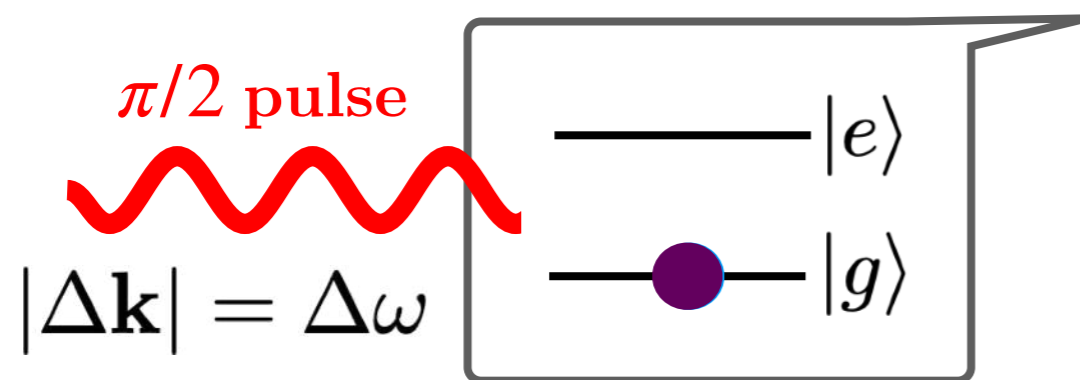
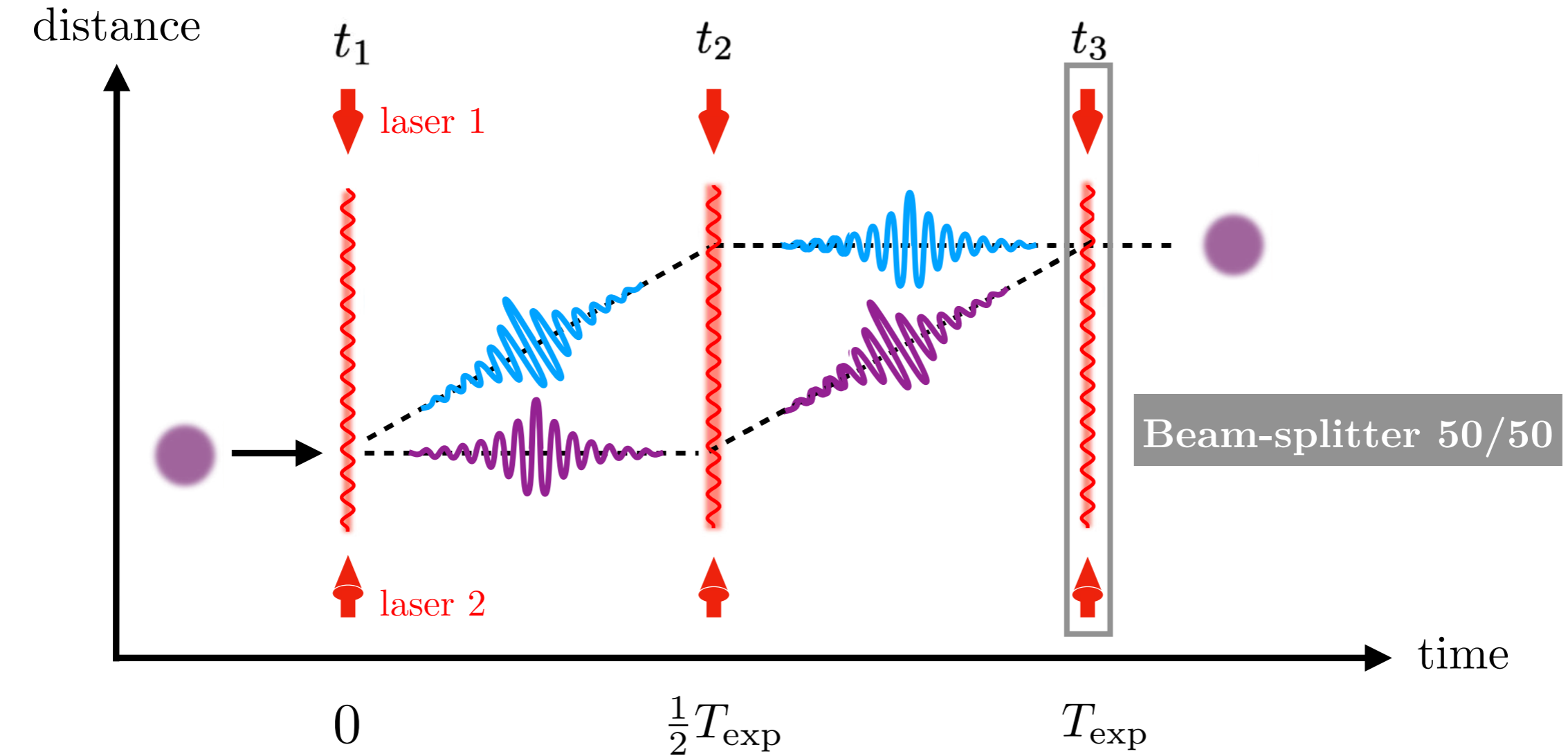
0 $\frac{1}{2}T_{\text{exp}}$ T_{exp}

$$|\Delta \mathbf{k}| = \Delta \omega$$



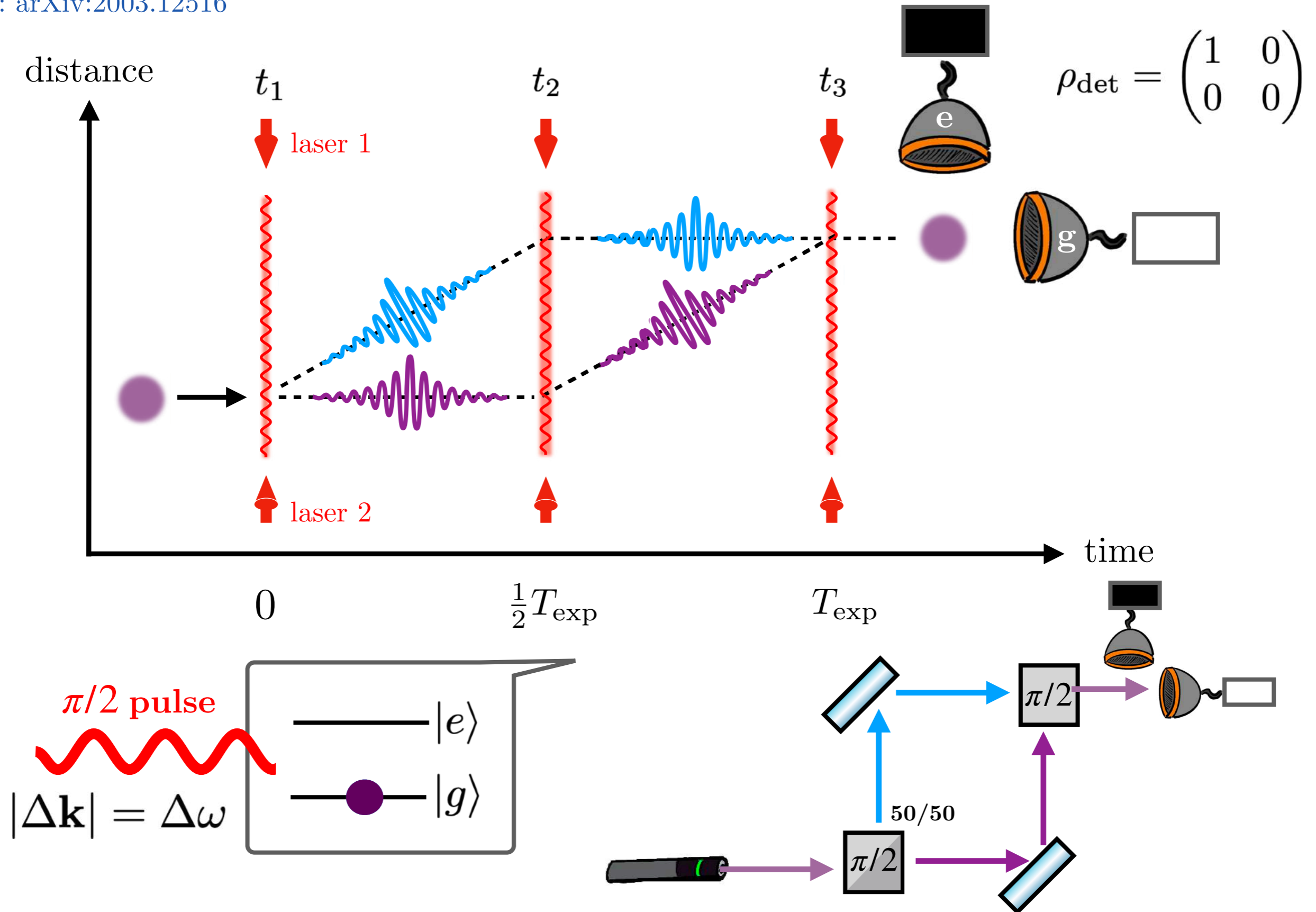
AIs: the Principle

Review: arXiv:2003.12516



AIs: the Principle

Review: arXiv:2003.12516



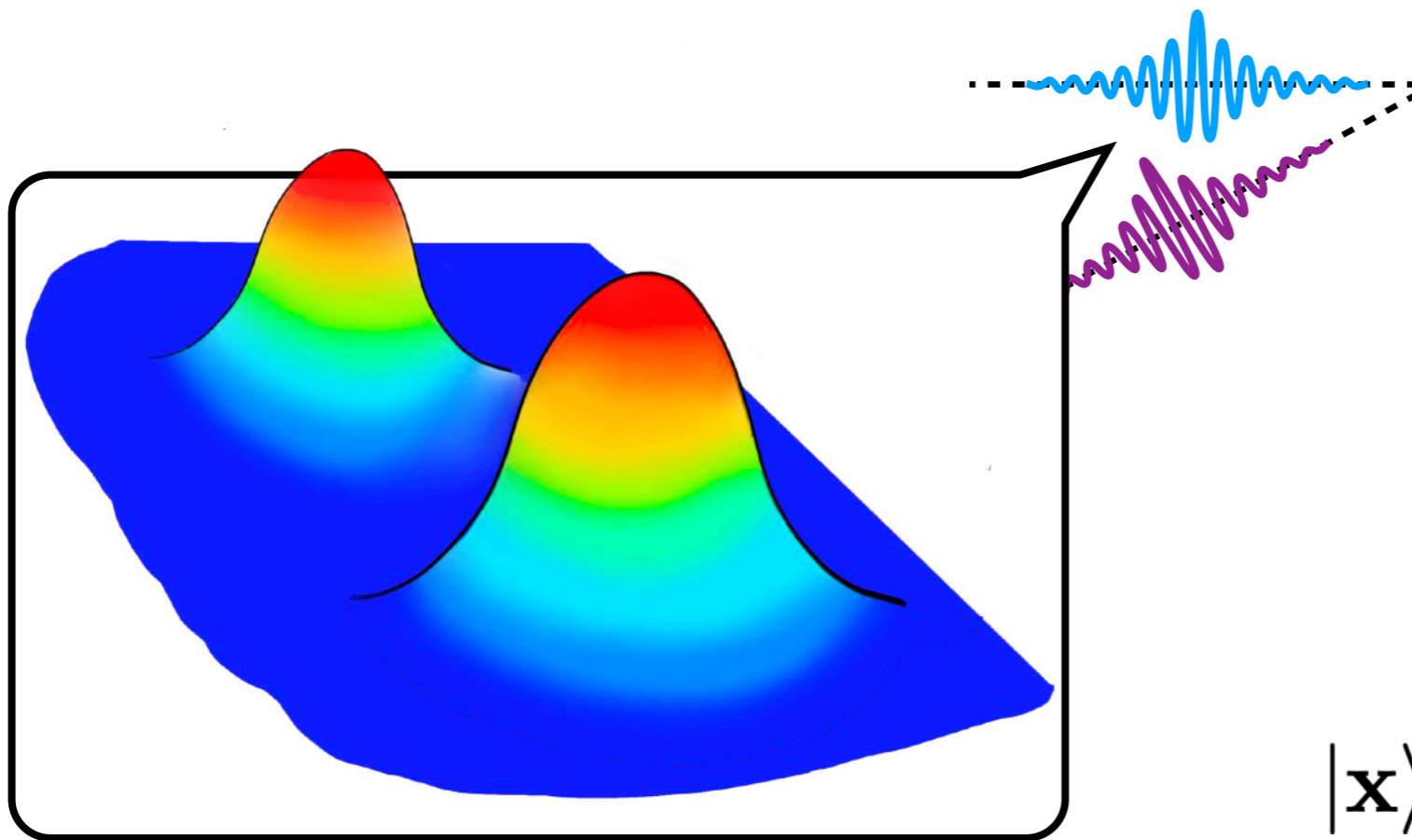
AIs: Collisional Decoherence

A **single** atom

[Joss, Zeh, 1985]

[Hornberger, Sipe, 2003]

$$\rho = \frac{1}{2} \begin{pmatrix} 1 & e^{i\phi} \\ e^{-i\phi} & 1 \end{pmatrix}$$

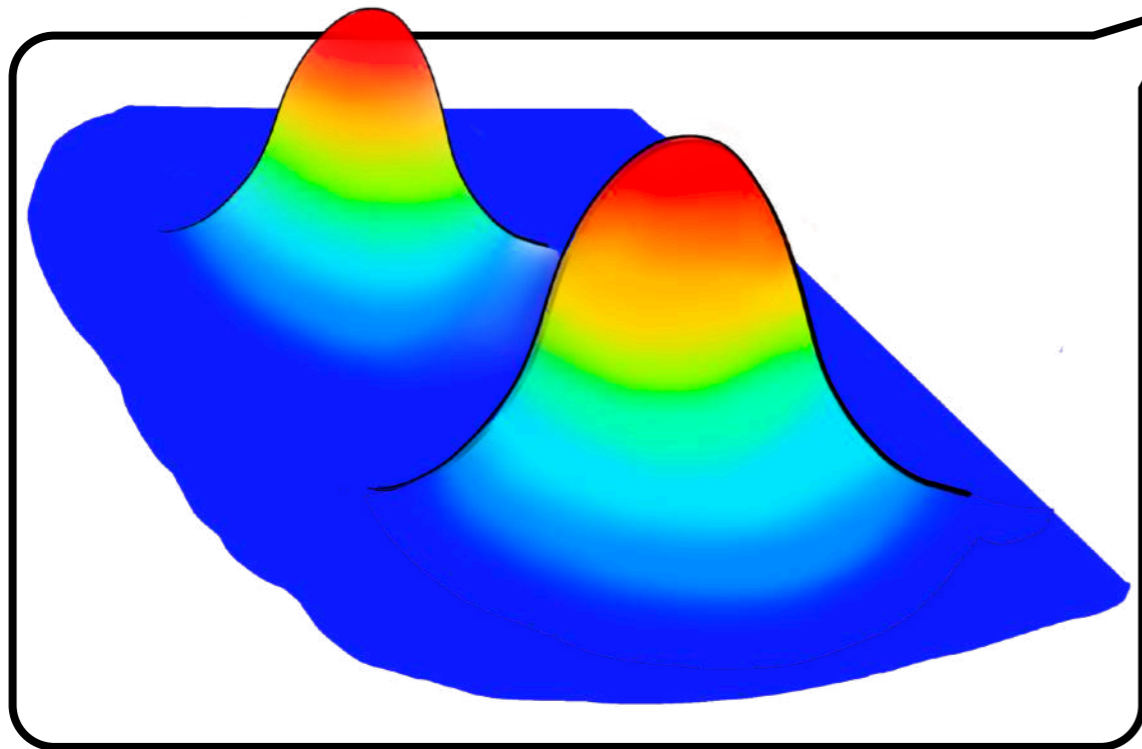


AIs: Collisional Decoherence

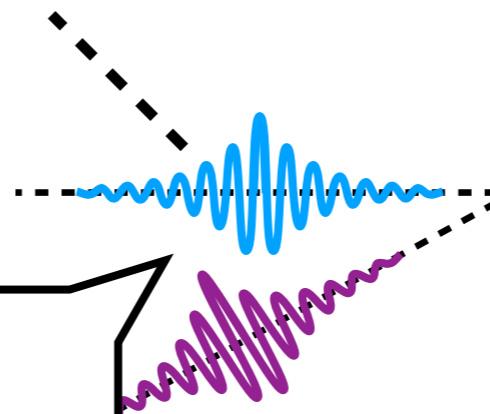
A **single** atom

[Joss, Zeh, 1985]

[Hornberger, Sipe, 2003]



$\chi(\mathbf{k})$



$$\rho = \frac{1}{2} \begin{pmatrix} 1 & e^{i\phi} \\ e^{-i\phi} & 1 \end{pmatrix}$$

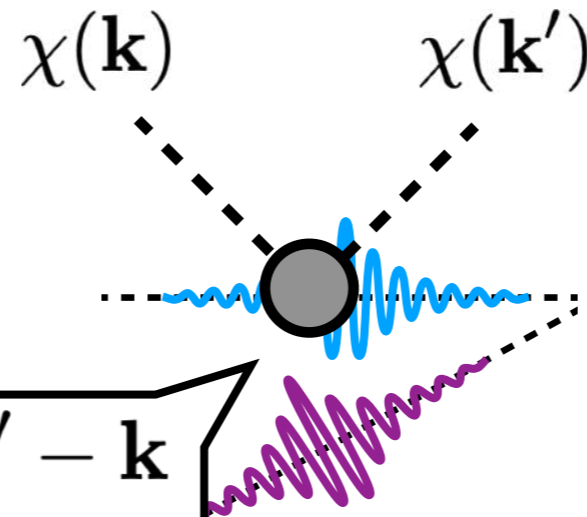
$$|\mathbf{x}\rangle \otimes |\mathbf{k}\rangle$$

AIs: Collisional Decoherence

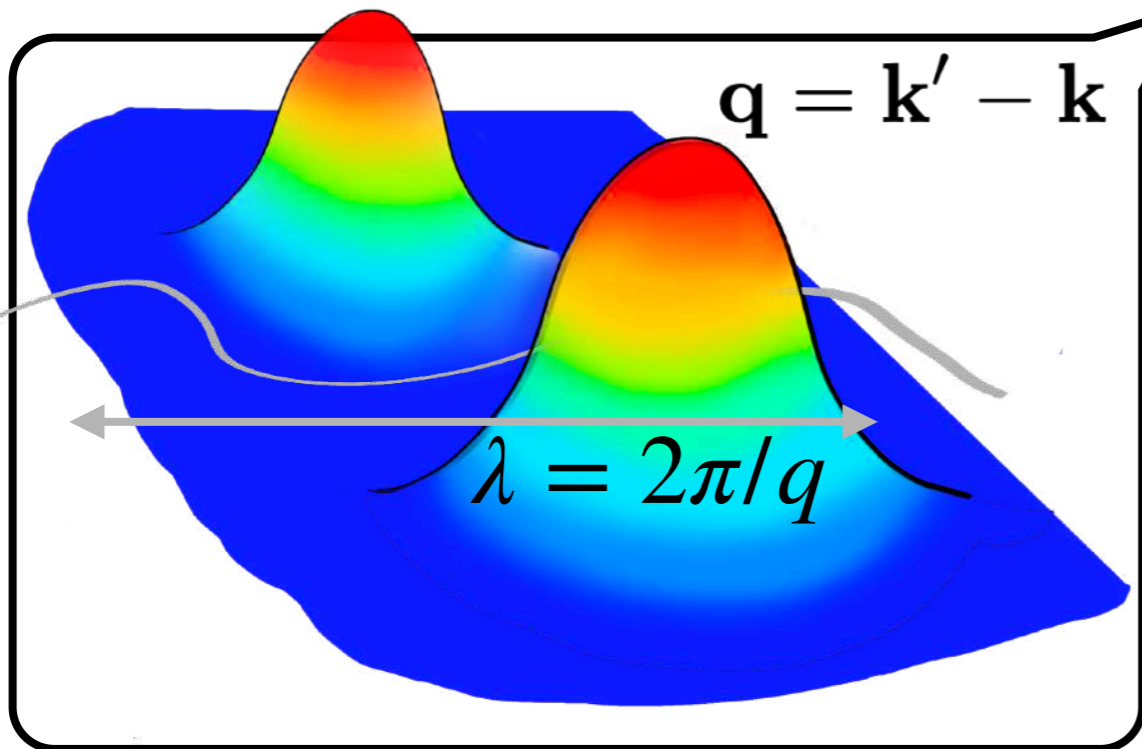
A single atom

[Joss, Zeh, 1985]

[Hornberger, Sipe, 2003]



$$\rho = \frac{1}{2} \begin{pmatrix} 1 & e^{i\phi} \\ e^{-i\phi} & 1 \end{pmatrix}$$



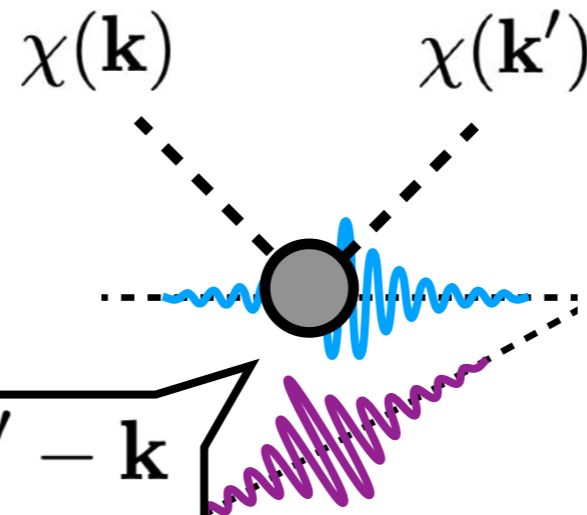
$$S(|\mathbf{x}\rangle \otimes |\mathbf{k}\rangle) = |\mathbf{x}\rangle \otimes S_{\{\mathbf{x}\}}|\mathbf{k}\rangle$$

AIs: Collisional Decoherence

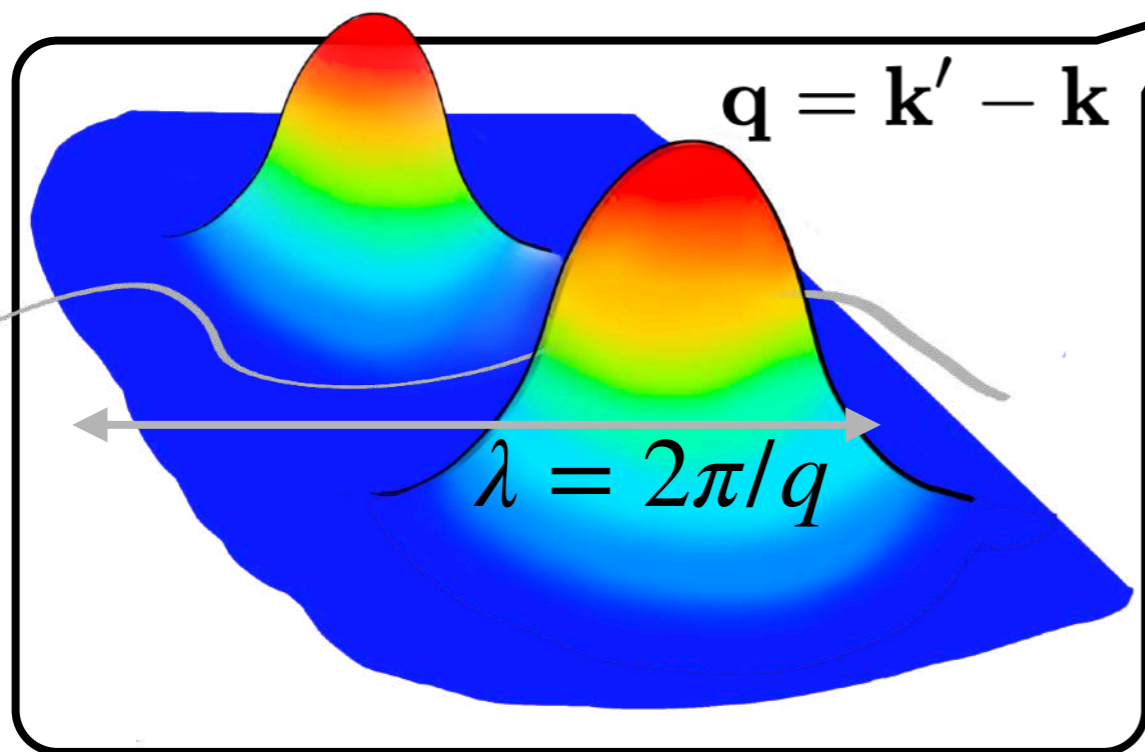
A single atom

[Joss, Zeh, 1985]

[Hornberger, Sipe, 2003]



$$\rho = \frac{1}{2} \begin{pmatrix} 1 & e^{i\phi} \\ e^{-i\phi} & 1 \end{pmatrix}$$



$$S(|\mathbf{x}\rangle \otimes |\mathbf{k}\rangle) = |\mathbf{x}\rangle \otimes S_{\{\mathbf{x}\}}|\mathbf{k}\rangle$$

$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

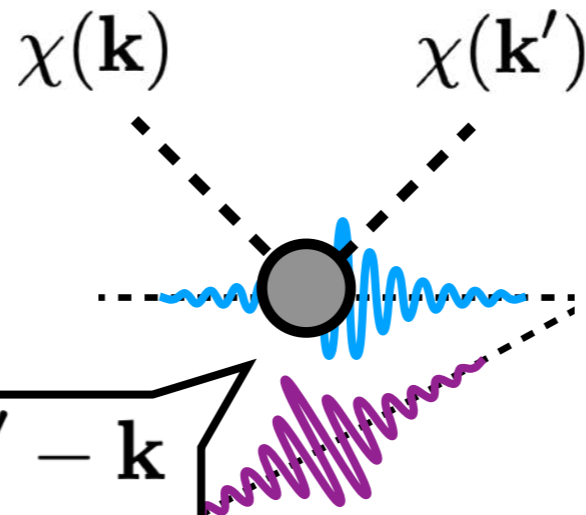
$$\Rightarrow \Delta\rho = \frac{i}{2}[T + T^\dagger, \rho] - \frac{1}{2}\{T^\dagger T, \rho\} + T\rho T^\dagger$$

AIs: Collisional Decoherence

A single atom

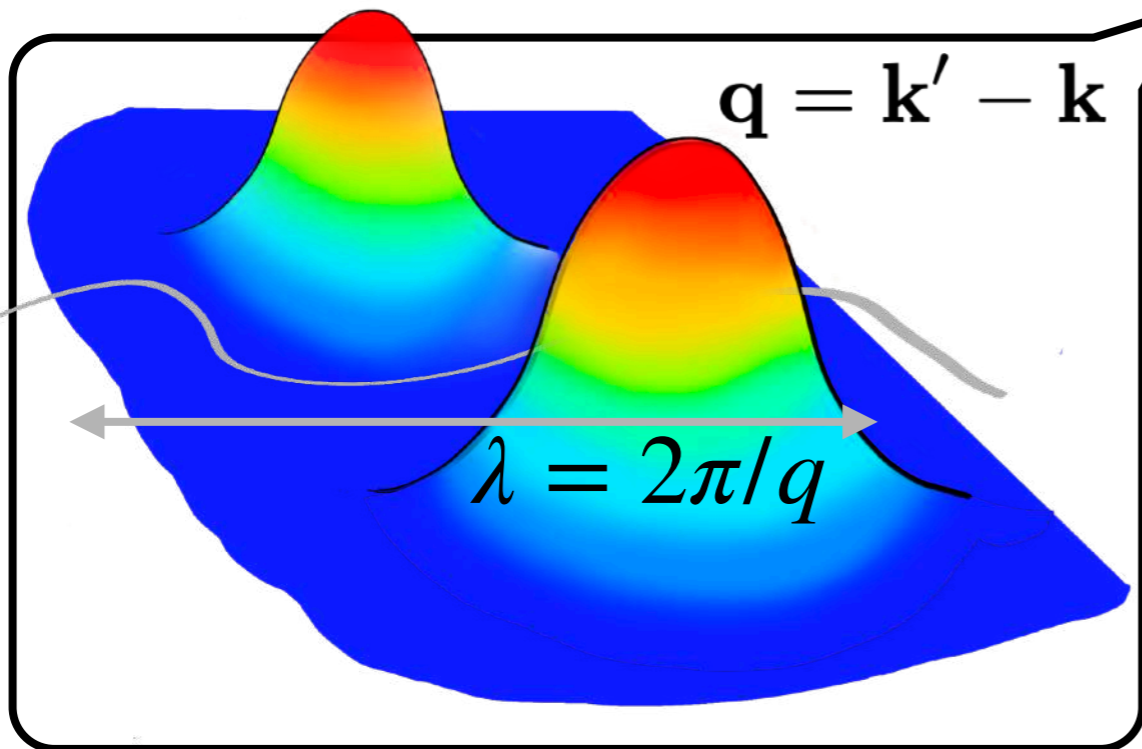
[Joss, Zeh, 1985]

[Hornberger, Sipe, 2003]



$$\rho = \frac{1}{2} \begin{pmatrix} 1 & \gamma e^{i\phi} \\ \gamma^* e^{-i\phi} & 1 \end{pmatrix}$$

$$\ln \gamma = - \int_{q,t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$



Decoherence Kernel

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta \mathbf{x})$$

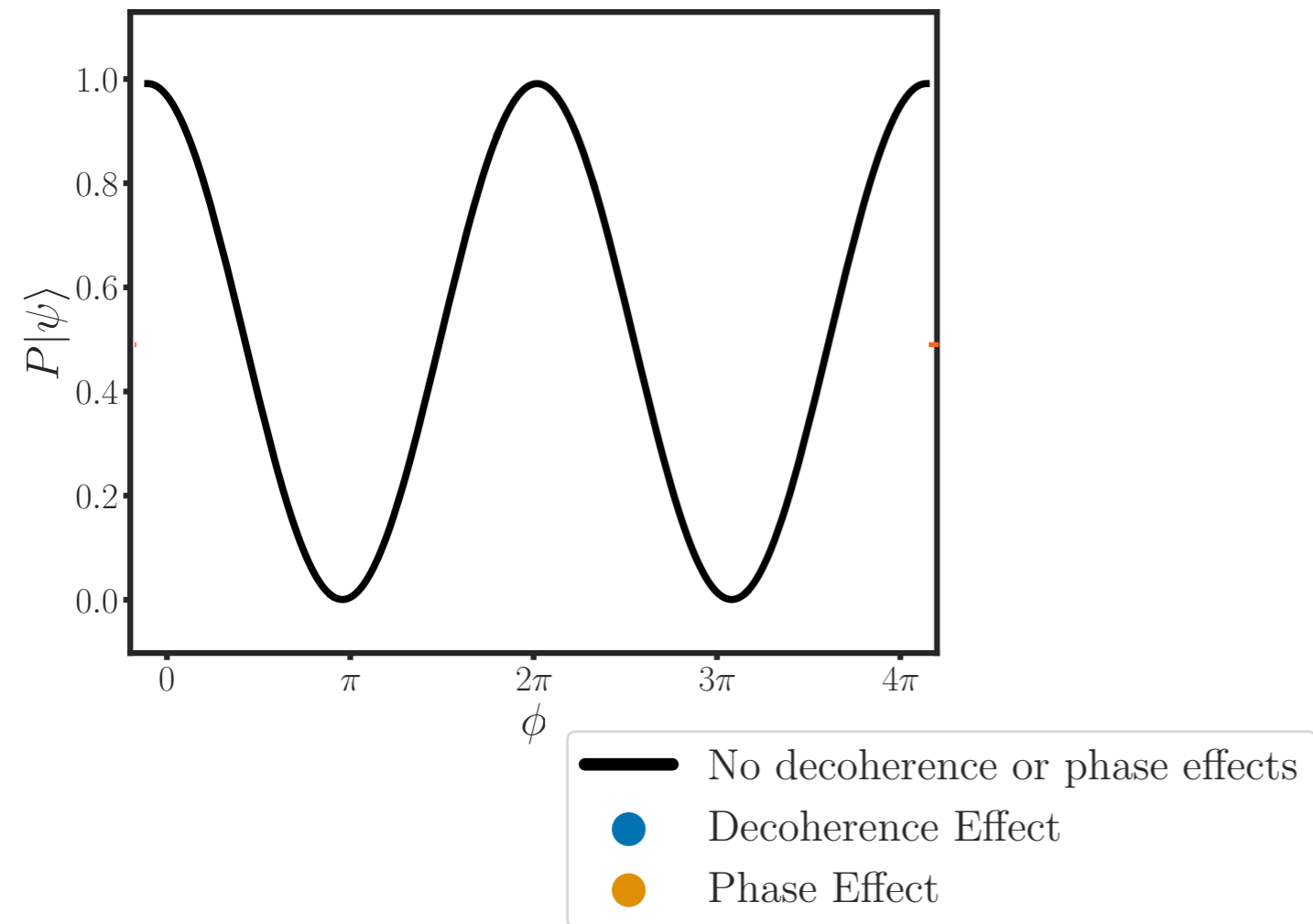
$$S(|\mathbf{x}\rangle \otimes |\mathbf{k}\rangle) = |\mathbf{x}\rangle \otimes S_{\{\mathbf{x}\}}|\mathbf{k}\rangle$$

$$\rho'_A = \text{Tr}_{\mathbf{k}} \rho'$$

$$\rho' = S \rho S^\dagger = (\mathbb{I} + T) \rho (\mathbb{I} + T)^\dagger$$

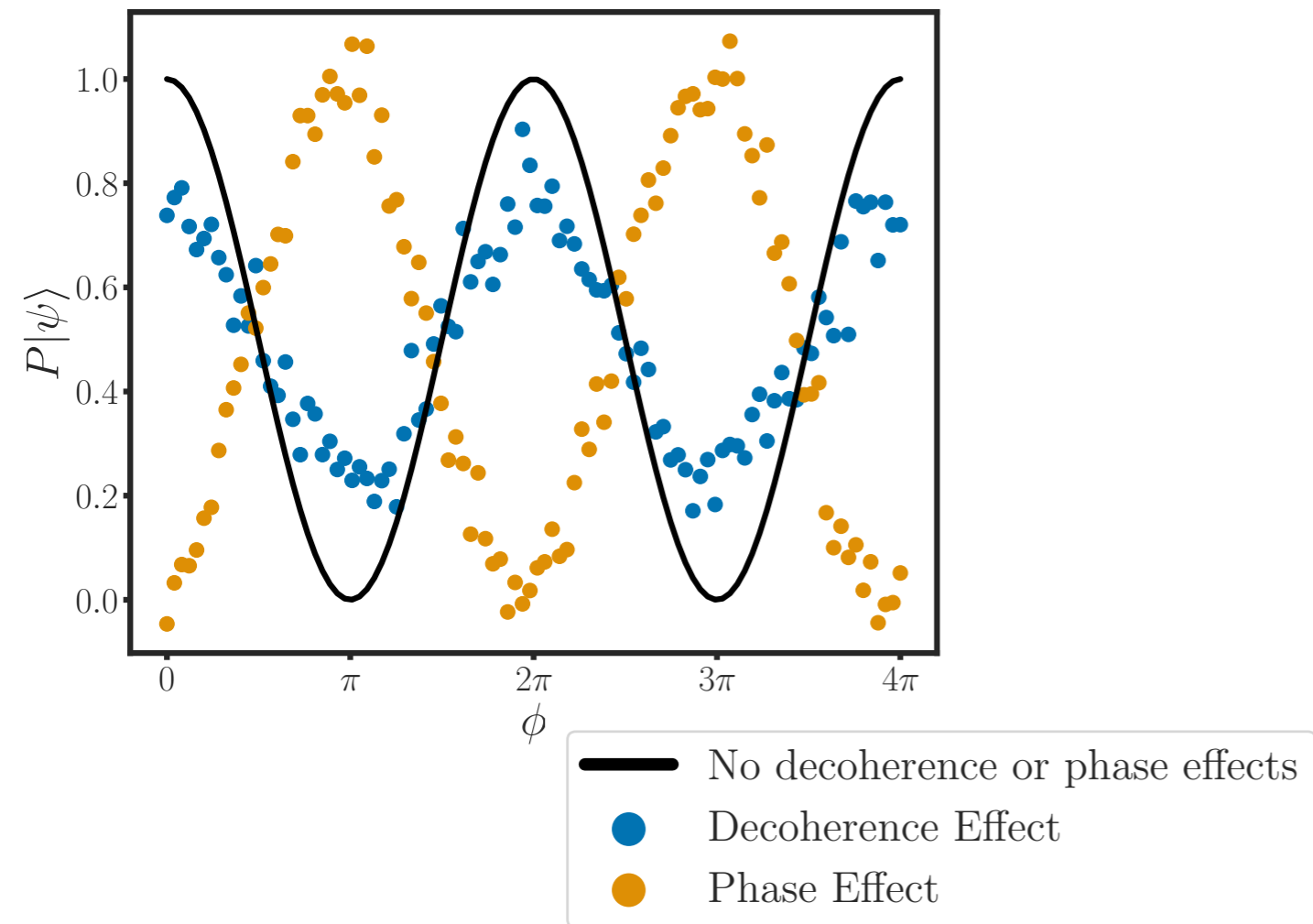
$$\Rightarrow \Delta \rho = \frac{i}{2} [T + T^\dagger, \rho] - \frac{1}{2} \{T^\dagger T, \rho\} + T \rho T^\dagger$$

AIs: Collisional Decoherence



$$\frac{N_I}{N_I + N_{II}} \Big|_{\text{exp}} = \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

AIs: Collisional Decoherence



$$\rho = \frac{1}{2} \begin{pmatrix} 1 & \gamma e^{i\phi} \\ \gamma^* e^{-i\phi} & 1 \end{pmatrix}$$

$$\ln \gamma = - \int_{\mathbf{q}, t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

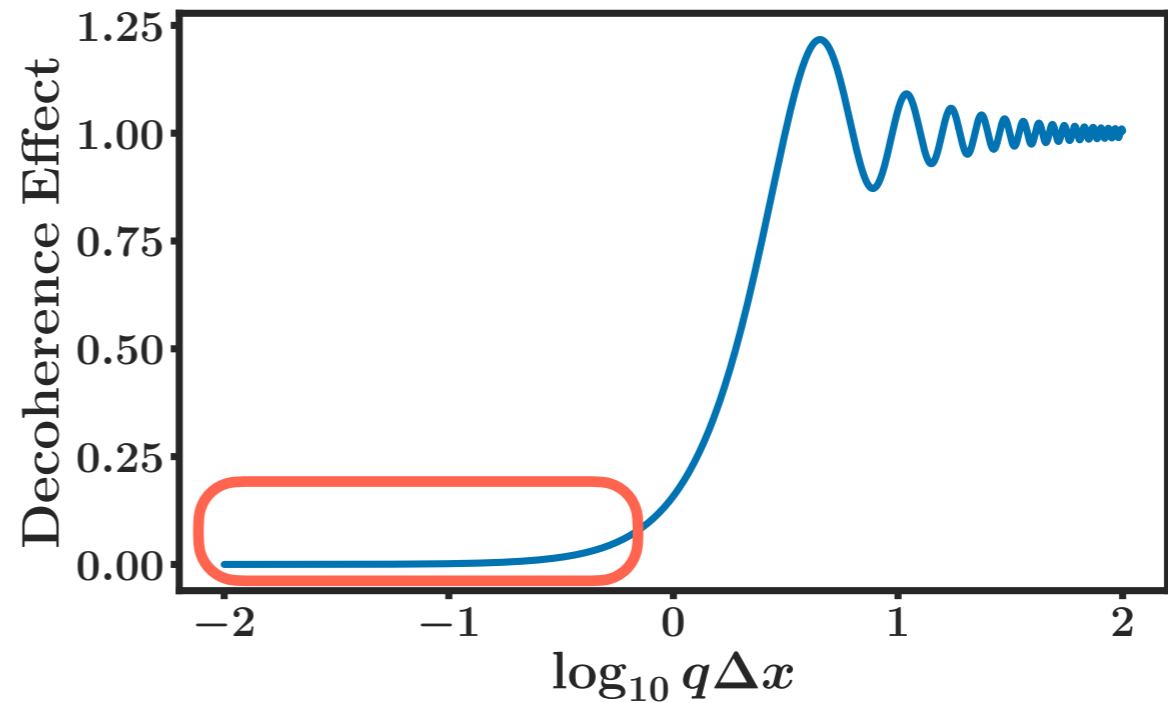
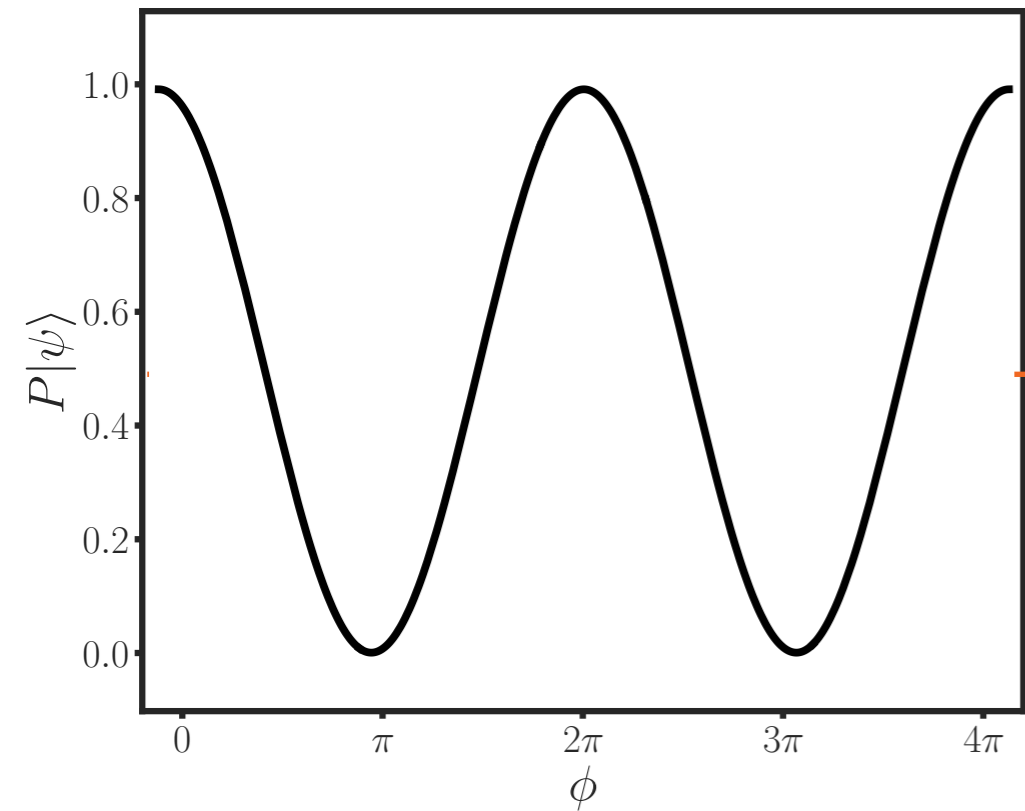
Decoherence Kernel

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$

$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

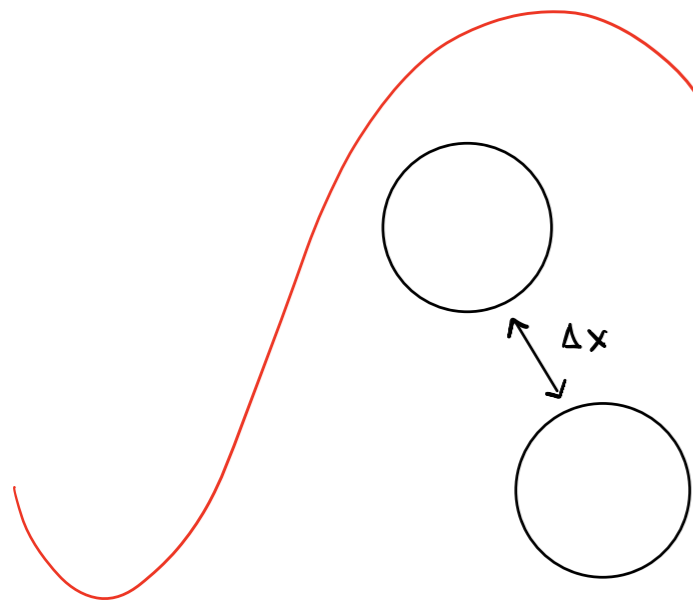
$$\text{Tr}\{\rho \mathcal{O}_1\} = \frac{1}{2} \left[1 + e^{-\int_{\mathbf{q}, t} R(\mathbf{q})(1 - \cos(\mathbf{q} \cdot \Delta\mathbf{x}))} \cos\left(\phi + \int_{\mathbf{q}, t} R(\mathbf{q}) \sin(\mathbf{q} \cdot \Delta\mathbf{x})\right) \right]$$

AIs: Collisional Decoherence



Decoherence Kernel

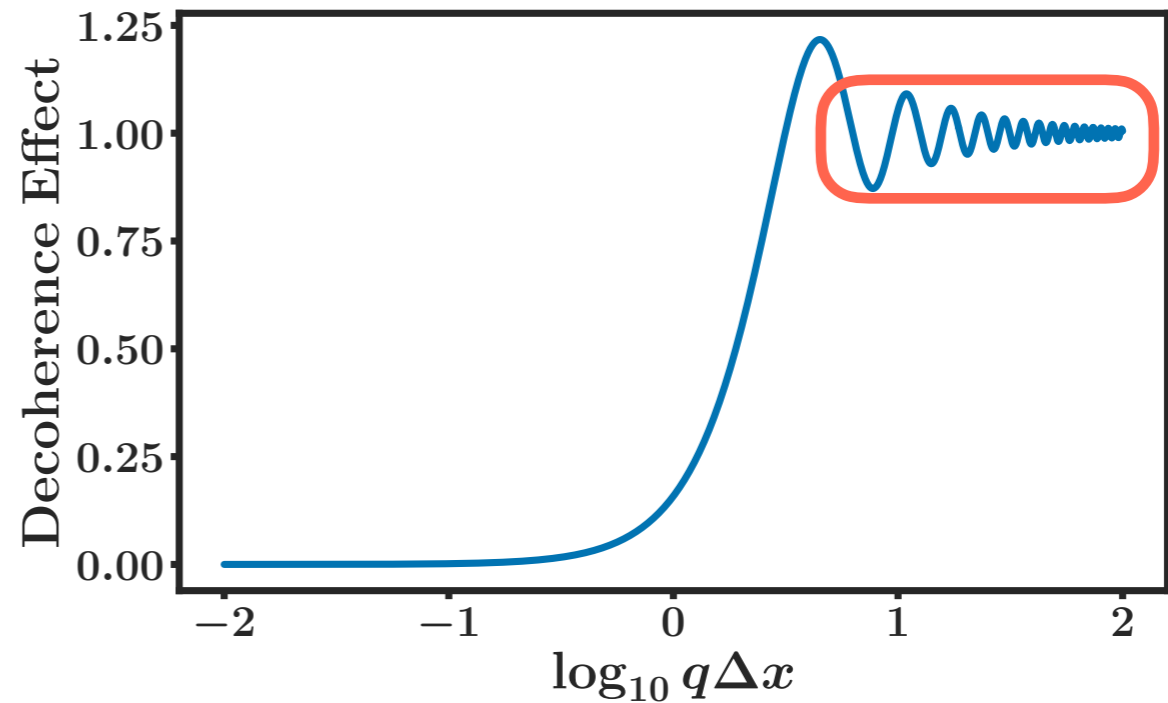
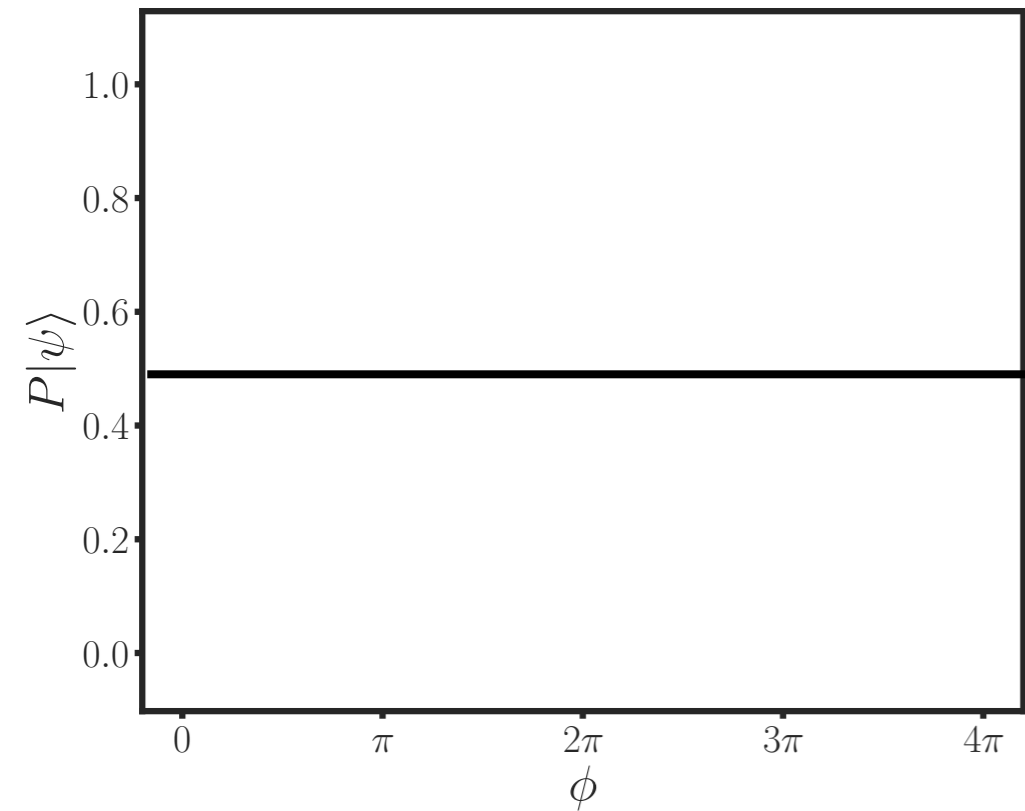
$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$



$$\frac{N_I}{N_I + N_{II}} \Big|_{\text{exp}} = \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

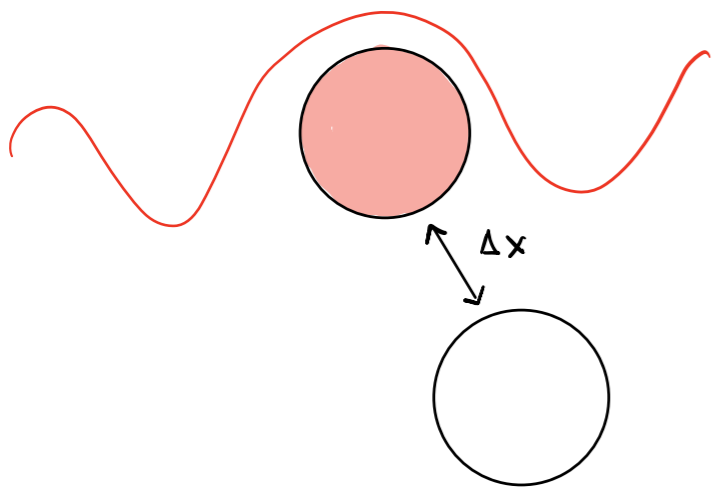
$$\text{Tr}\{\rho \mathcal{O}_1\} = \frac{1}{2} \left[1 + e^{-\int_{\mathbf{q},t} R(\mathbf{q})(1 - \cos(\mathbf{q} \cdot \Delta\mathbf{x}))} \cos\left(\phi + \int_{\mathbf{q},t} R(\mathbf{q}) \sin(\mathbf{q} \cdot \Delta\mathbf{x})\right) \right]$$

AIs: Collisional Decoherence



Decoherence Kernel

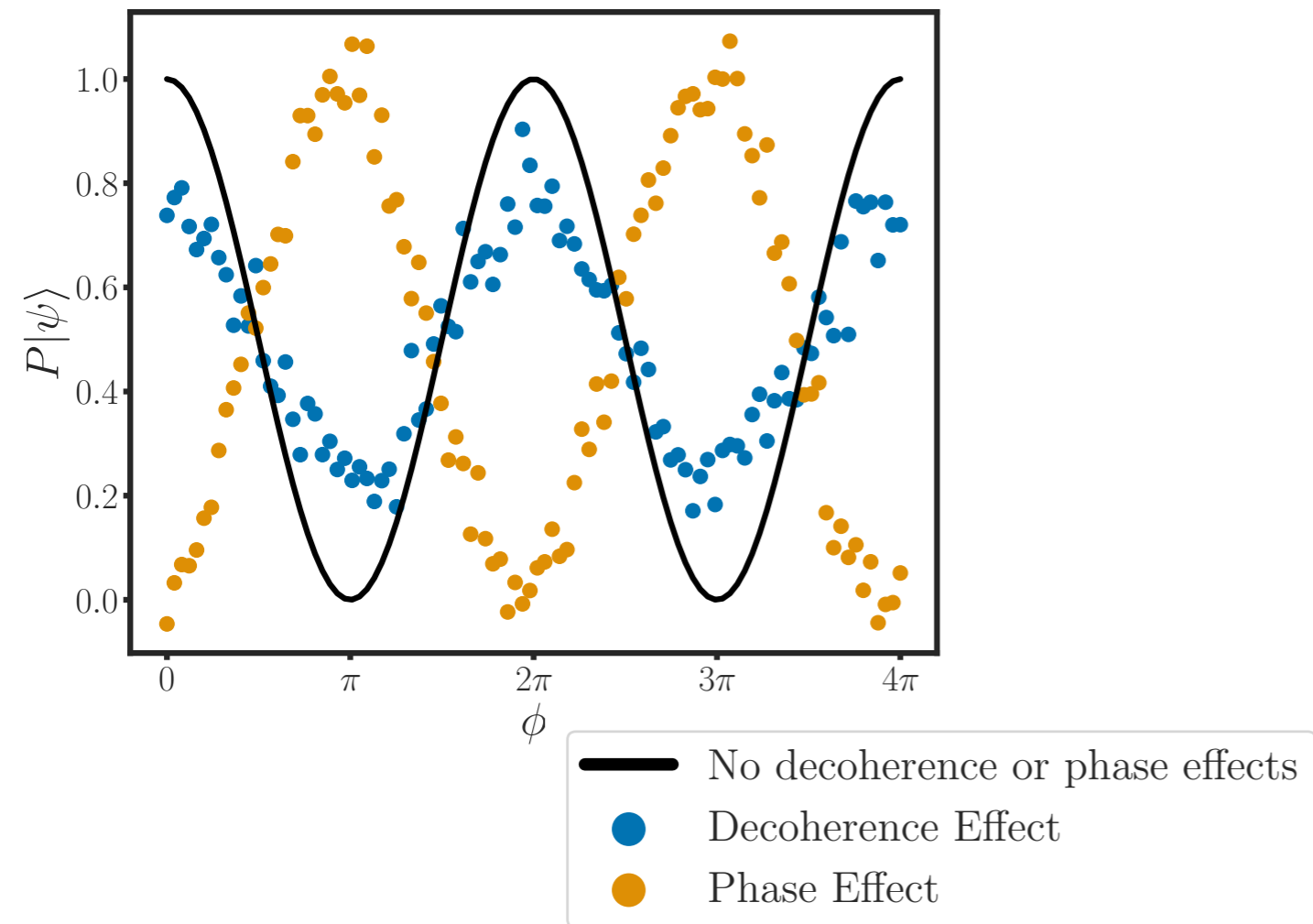
$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta\mathbf{x})$$



$$\frac{N_I}{N_I + N_{II}} \Big|_{\text{exp}} = \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

$$\text{Tr}\{\rho \mathcal{O}_1\} = \frac{1}{2} \left[1 + e^{-\int_{\mathbf{q},t} R(\mathbf{q})(1 - \cos(\mathbf{q} \cdot \Delta\mathbf{x}))} \cos\left(\phi + \int_{\mathbf{q},t} R(\mathbf{q}) \sin(\mathbf{q} \cdot \Delta\mathbf{x})\right) \right]$$

AIs: Collisional Decoherence



$$\rho = \frac{1}{2} \begin{pmatrix} 1 & \gamma e^{i\phi} \\ \gamma^* e^{-i\phi} & 1 \end{pmatrix}$$

$$\ln \gamma = - \int_{\mathbf{q}, t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

Decoherence Kernel

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta \mathbf{x})$$

$$\left. \frac{N_I}{N_I + N_{II}} \right|_{\text{exp}} = \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

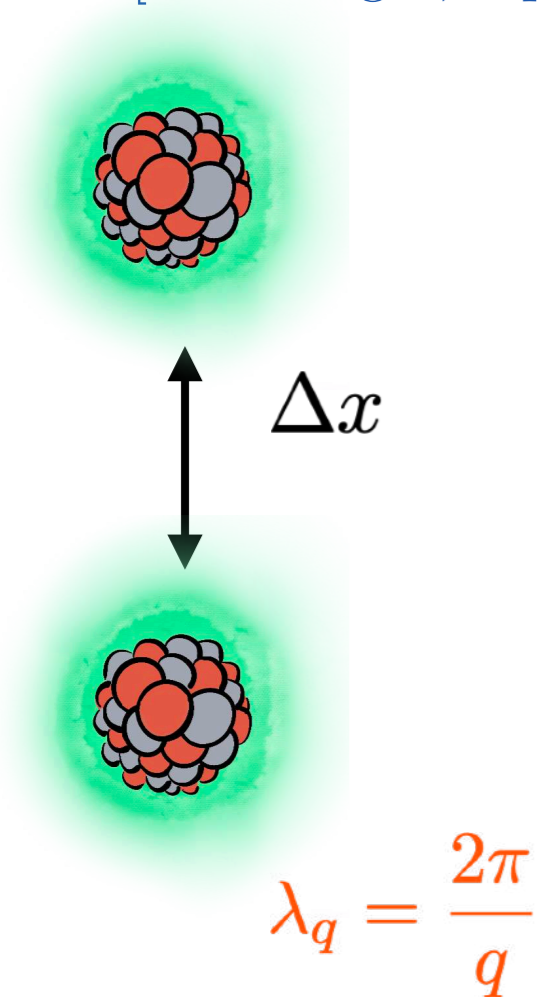
$$\text{Tr}\{\rho \mathcal{O}_1\} = \frac{1}{2} \left[1 + e^{-\int_{\mathbf{q}, t} R(\mathbf{q})(1 - \cos(\mathbf{q} \cdot \Delta \mathbf{x}))} \cos\left(\phi + \int_{\mathbf{q}, t} R(\mathbf{q}) \sin(\mathbf{q} \cdot \Delta \mathbf{x})\right) \right]$$

AIs: Collisional Decoherence

Single-atom system

[Joss, Zeh, 1985]

[Hornberger, Sipe, 2003]



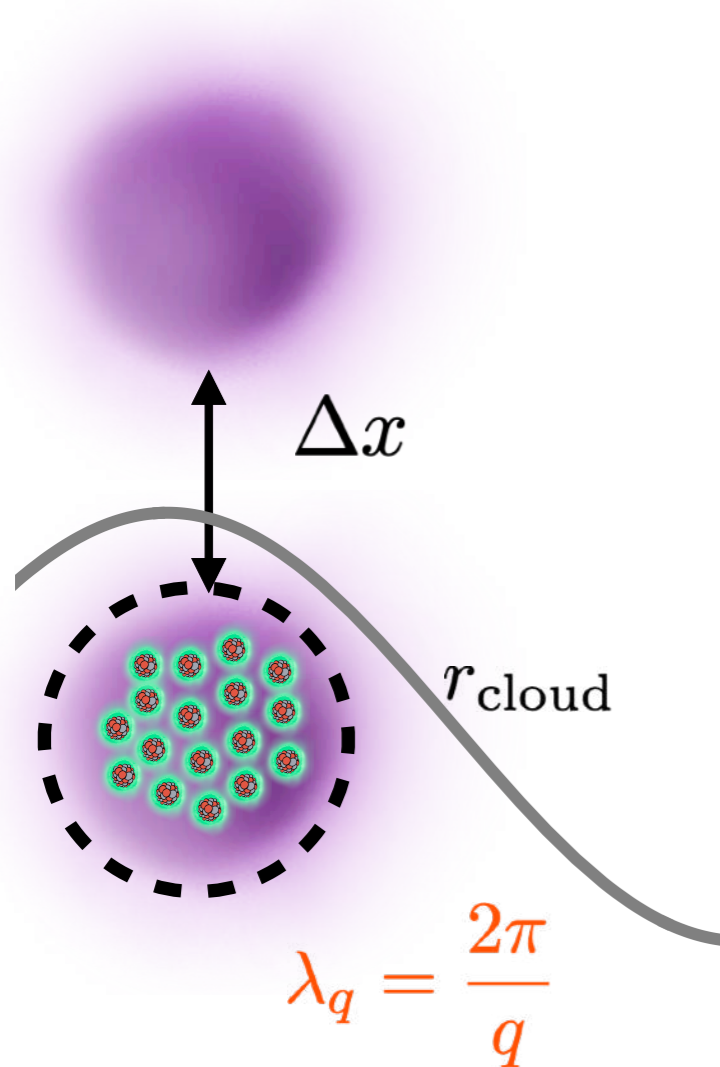
$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

$$\Rightarrow \Delta\rho = \frac{i}{2}[T + T^\dagger, \rho] - \frac{1}{2}\{T^\dagger T, \rho\} + T\rho T^\dagger$$

AIs: Collisional Decoherence

Multi-atom system (distinguishable)

[Badurina, CM, Plestid, 2024]



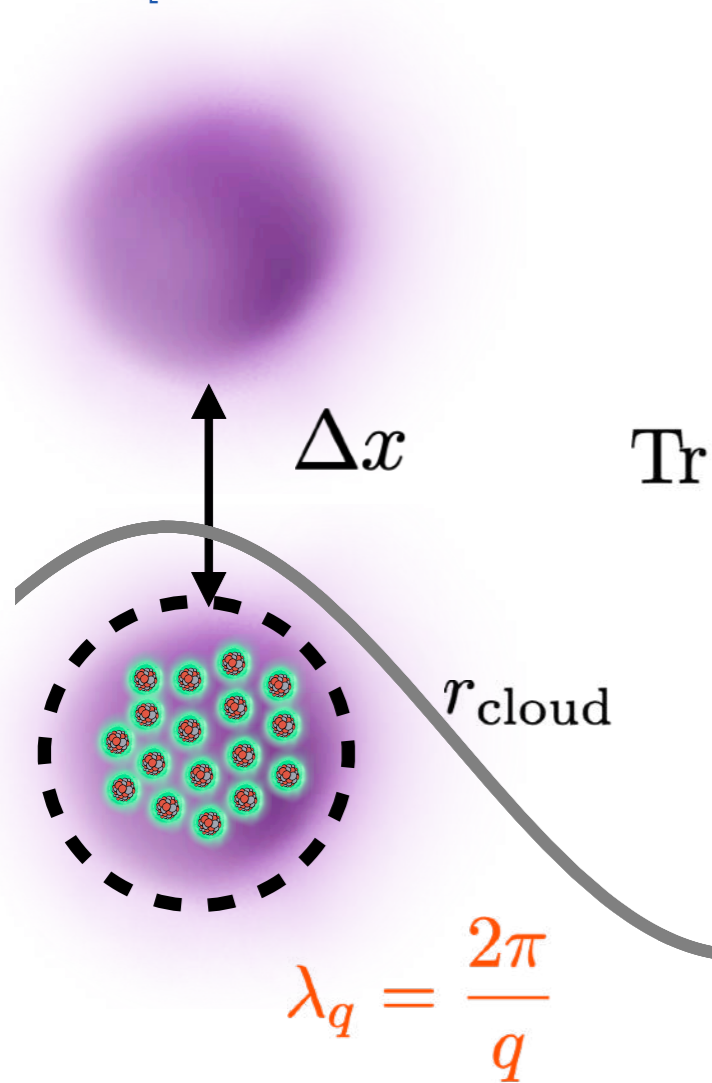
$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

$$\Rightarrow \Delta\rho = \frac{i}{2}[T + T^\dagger, \rho] - \frac{1}{2}\{T^\dagger T, \rho\} + T\rho T^\dagger$$

AIs: Collisional Decoherence

Multi-atom system (distinguishable)

[Badurina, CM, Plestid, 2024]



$$\text{Tr}\{\rho_N \sum_i^N \mathcal{O}_i\}$$

$$\rho_{(N=2)} = \begin{pmatrix} \circ & \blacksquare & \blacksquare & \star \\ \blacksquare & \circ & \circ & \blacksquare \\ \blacksquare & \circ & \circ & \blacksquare \\ \star & \blacksquare & \blacksquare & \circ \end{pmatrix}$$

$$\stackrel{!}{=} N \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

$$\Rightarrow \Delta\rho = \frac{i}{2} [T + T^\dagger, \rho] - \frac{1}{2} \{T^\dagger T, \rho\} + T\rho T^\dagger$$

AIs: Collisional Decoherence

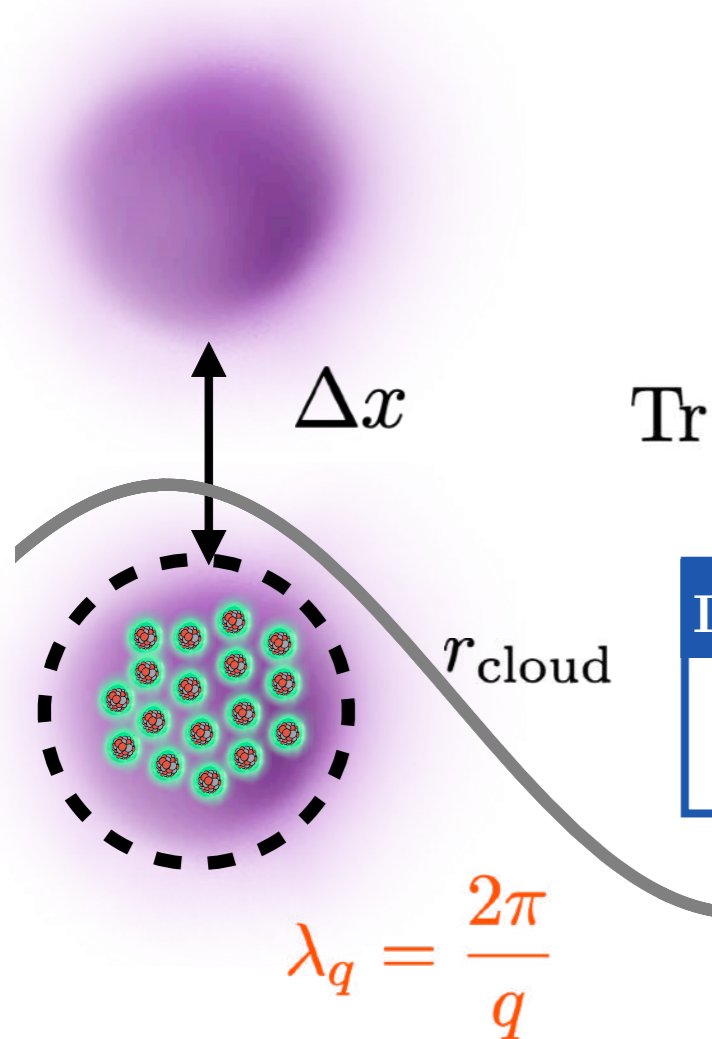
Multi-atom system (distinguishable)

[Badurina, CM, Plestid, 2024]

$$\rho_1 = \frac{1}{2} \begin{pmatrix} 1 & \gamma e^{i\phi} \\ \gamma^* e^{-i\phi} & 1 \end{pmatrix}$$

$$\ln \gamma = - \int_{q,t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

$$\text{Tr}\{\rho_N \sum_i \mathcal{O}_i\} = N \text{Tr}\{\rho_1 \mathcal{O}_i\} \stackrel{!}{=} N \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$



Decoherence Kernel 1-body measurement

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = (1 - \cos(\mathbf{q} \cdot \Delta \mathbf{x})) - iN \sin(\mathbf{q} \cdot \Delta \mathbf{x})$$

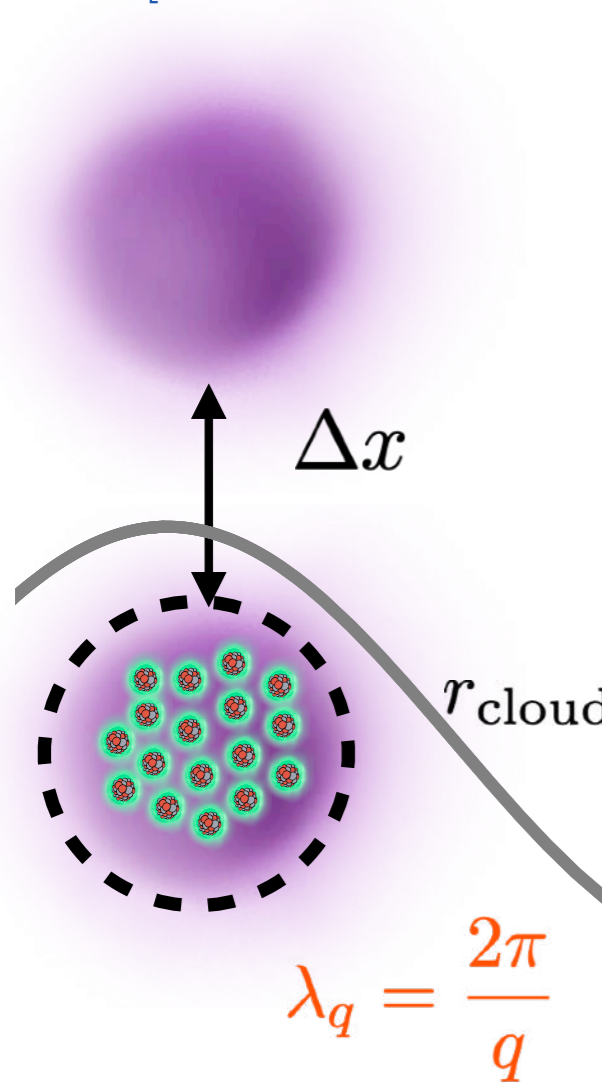
$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

$$\Rightarrow \Delta\rho = \frac{i}{2} [T + T^\dagger, \rho] - \frac{1}{2} \{T^\dagger T, \rho\} + T\rho T^\dagger$$

AIs: Collisional Decoherence

Multi-atom system (distinguishable)

[Badurina, CM, Plestid, 2024]



$$\rho_{(N=2)} = \begin{pmatrix} \circ & \blacksquare & \blacksquare & \star \\ \blacksquare & \circ & \circ & \blacksquare \\ \blacksquare & \circ & \circ & \blacksquare \\ \star & \blacksquare & \blacksquare & \circ \end{pmatrix}$$

$$\text{Tr}\{\rho_N \sum_i \mathcal{O}_i\} = N \text{Tr}\{\rho_1 \mathcal{O}_i\} \stackrel{!}{=} N \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

Decoherence Kernel n-body measurement

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = n^2 (1 - \cos(\mathbf{q} \cdot \Delta \mathbf{x})) - iNn \sin(\mathbf{q} \cdot \Delta \mathbf{x})$$

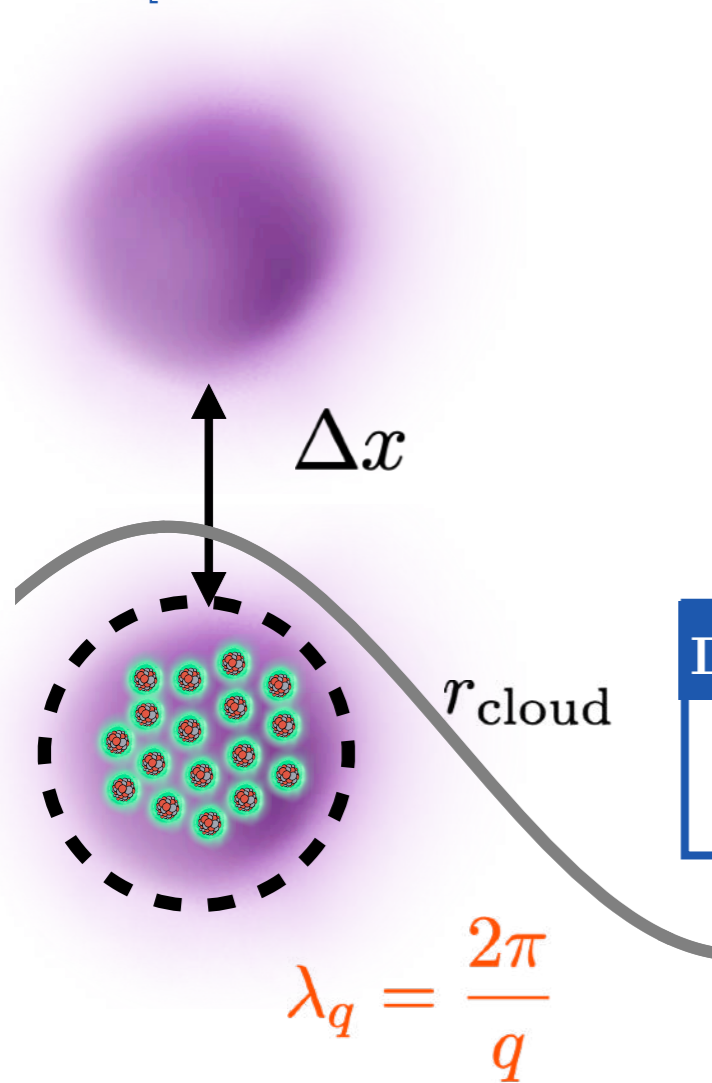
$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

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$$\text{Tr}\{\rho_N \mathcal{O}_\star\} \stackrel{!}{=} \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

Decoherence Kernel n-body measurement

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = N^2 (1 - \cos(\mathbf{q} \cdot \Delta\mathbf{x})) - i N^2 \sin(\mathbf{q} \cdot \Delta\mathbf{x})$$

$$\rho' = S \rho S^\dagger = (\mathbb{I} + T) \rho (\mathbb{I} + T)^\dagger$$

$$\Rightarrow \Delta\rho = \frac{i}{2} [T + T^\dagger, \rho] - \frac{1}{2} \{T^\dagger T, \rho\} + T \rho T^\dagger$$

AIs: Collisional Decoherence

Particle scattering

[Riedel, 2013]

[Riedel, Yavin, 2017]

[Du, CM, Pardo, Wang, Zurek, 2022]

[Du, CM, Pardo, Wang, Zurek, 2023]

$$\rho_1 = \frac{1}{2} \begin{pmatrix} 1 & \gamma e^{i\phi} \\ \gamma^* e^{-i\phi} & 1 \end{pmatrix}$$

$$\ln \gamma = - \int_{q,t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

$$R(\mathbf{q}) = n_\chi \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}, \mathbf{q})$$

AIs: Collisional Decoherence

Particle scattering

[Riedel, 2013]

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[Du, CM, Pardo, Wang, Zurek, 2022]

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$$\ln \gamma = - \int_{q,t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

$$f(\mathbf{v}) = \frac{1}{N_0} \exp\left(-\frac{(\mathbf{v} + \mathbf{v}_e)^2}{v_0^2}\right) \Theta(v_{\text{esc}} - \|\mathbf{v} + \mathbf{v}_e\|)$$

$$R(\mathbf{q}) = n_\chi \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}, \mathbf{q})$$

$$\frac{\rho_\chi}{\rho_T} \frac{m_T}{m_\chi}$$

$$\Gamma(\mathbf{v}, \mathbf{q}) = V \sum_f |\langle f | H_{\text{int}} | i \rangle|^2 (2\pi) \delta(E_f - E_i - \omega_{\mathbf{q}})$$

AIs: Collisional Decoherence

Particle scattering

[Riedel, 2013]

[Riedel, Yavin, 2017]

[Du, CM, Pardo, Wang, Zurek, 2022]

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$$\ln \gamma = - \int_{q,t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

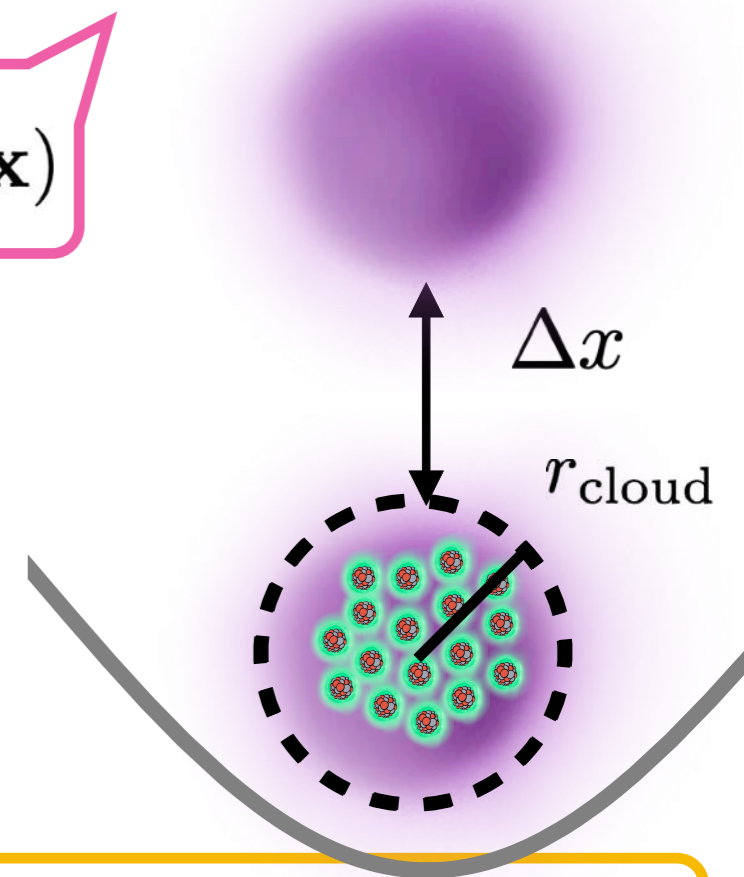
$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = n^2 (1 - \cos(\mathbf{q} \cdot \Delta \mathbf{x})) - i N n \sin(\mathbf{q} \cdot \Delta \mathbf{x})$$

$$f(\mathbf{v}) = \frac{1}{N_0} \exp\left(-\frac{(\mathbf{v} + \mathbf{v}_e)^2}{v_0^2}\right) \Theta(v_{\text{esc}} - \|\mathbf{v} + \mathbf{v}_e\|)$$

$$R(\mathbf{q}) = n_\chi \int d^3 \mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}, \mathbf{q})$$

$$\frac{\rho_\chi}{\rho_T} \frac{m_T}{m_\chi}$$

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AIs: Collisional Decoherence

Particle scattering

[Riedel, 2013]

[Riedel, Yavin, 2017]

[Du, CM, Pardo, Wang, Zurek, 2022]

[Du, CM, Pardo, Wang, Zurek, 2023]

[Joss, Zeh, 1985]

[Hornberger, Sipe, 2003]

$$\rho_1 = \frac{1}{2} \begin{pmatrix} 1 & \gamma e^{i\phi} \\ \gamma^* e^{-i\phi} & 1 \end{pmatrix}$$

$$\ln \gamma = - \int_{q,t} R(\mathbf{q}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

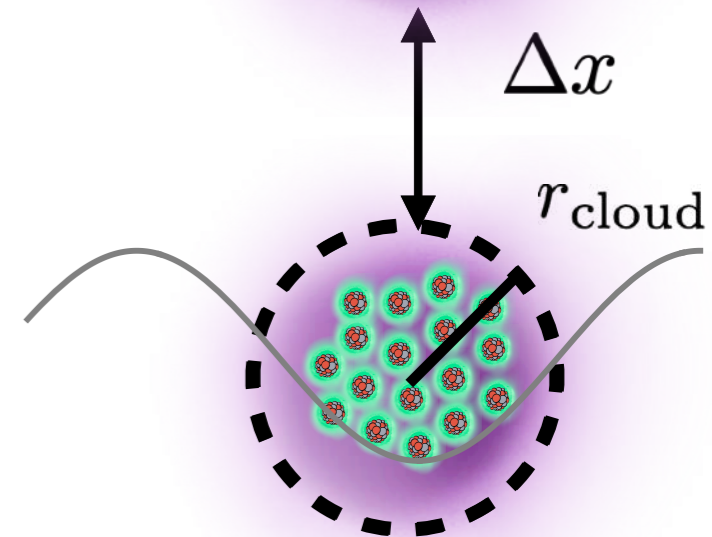
$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = 1 - \exp(i\mathbf{q} \cdot \Delta \mathbf{x})$$

$$f(\mathbf{v}) = \frac{1}{N_0} \exp\left(-\frac{(\mathbf{v} + \mathbf{v}_e)^2}{v_0^2}\right) \Theta(v_{\text{esc}} - \|\mathbf{v} + \mathbf{v}_e\|)$$

$$R(\mathbf{q}) = n_\chi \int d^3 \mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}, \mathbf{q})$$

$$\frac{\rho_\chi}{\rho_T} \frac{m_T}{m_\chi}$$

$$\Gamma(\mathbf{v}) = V \int \frac{d^3 \mathbf{q}}{(2\pi)^3} \sum_f |\langle f | H_{\text{int}} | i \rangle|^2 (2\pi) \delta(E_f - E_i - \omega_{\mathbf{q}})$$



AIs: Collisional Decoherence

Particle scattering

[Riedel, 2013]

[Riedel, Yavin, 2017]

[Du, CM, Pardo, Wang, Zurek, 2022]

[Du, CM, Pardo, Wang, Zurek, 2023]

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T_{exp}

$$\ln \gamma = - \int R(\mathbf{q}) \mathcal{F}(\mathbf{q})$$

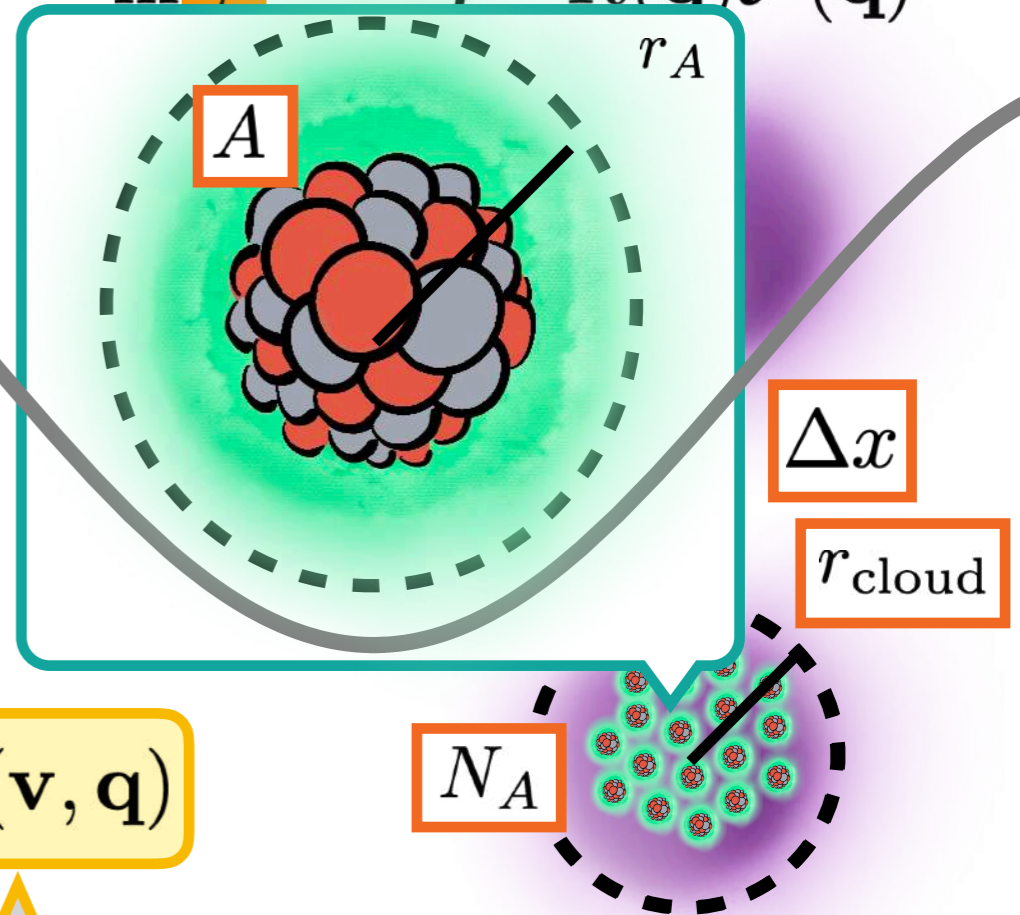
$$f(\mathbf{v}) = \frac{1}{N_0} \exp \left(- \frac{(\mathbf{v} + \mathbf{v}_e)^2}{v_0^2} \right) \Theta(v_{\text{esc}} - \|\mathbf{v} + \mathbf{v}_e\|)$$

$$R(\mathbf{q}) = n_\chi \int d^3 \mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}, \mathbf{q})$$

$$\frac{\rho_\chi m_T}{\rho_T m_\chi}$$

$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_T^2(\mathbf{q})$$

$$\mathcal{F}_T(\mathbf{q}) = A \mathcal{F}_A^2(q r_A)$$



Δx

r_{cloud}

N_A

r_A

A

AIs: Collisional Decoherence

Particle scattering

[Riedel, 2013]

[Riedel, Yavin, 2017]

[Du, CM, Pardo, Wang, Zurek, 2022]

[Du, CM, Pardo, Wang, Zurek, 2023]

$$\rho_1 = \frac{1}{2} \begin{pmatrix} 1 & \gamma e^{i\phi} \\ \gamma^* e^{-i\phi} & 1 \end{pmatrix}$$

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$$\ln \gamma = - \int_{t, \mathbf{q}} R(\mathbf{q}) \mathcal{F}(\mathbf{q})$$

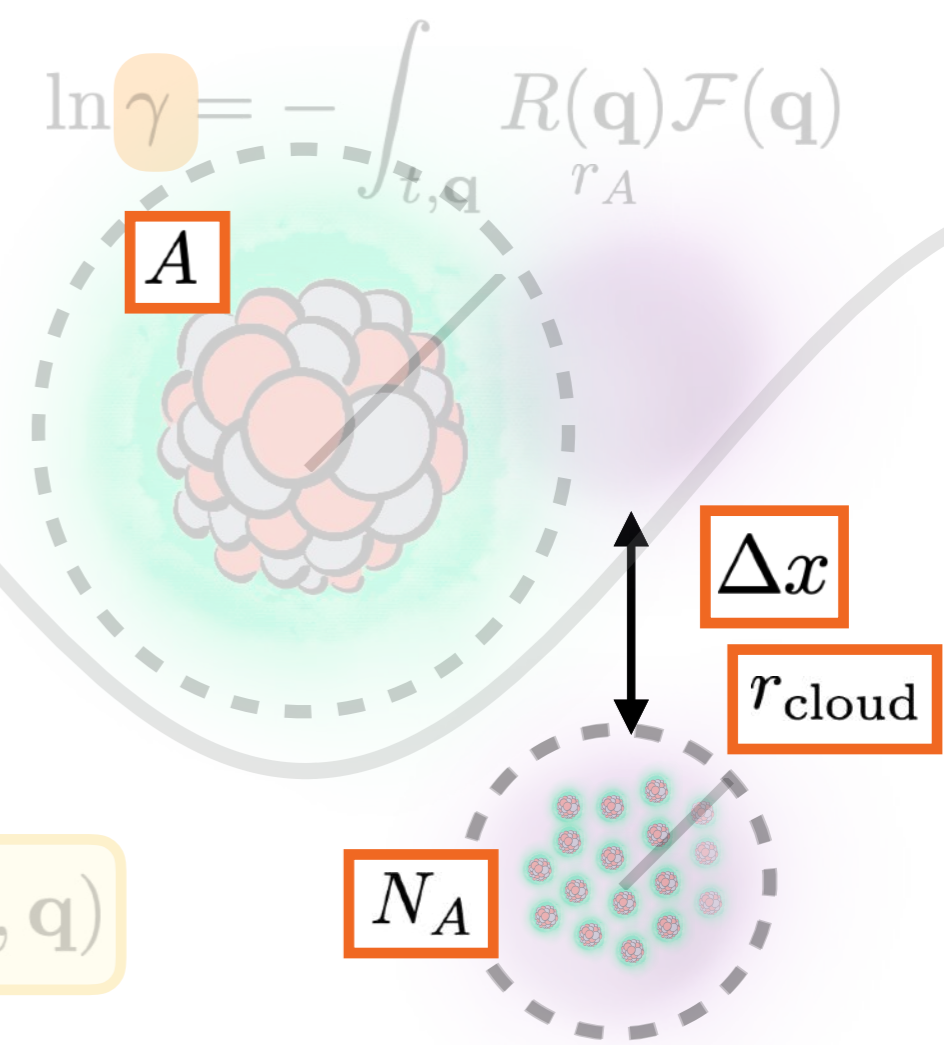
$$f(\mathbf{v}) = \frac{1}{N_0} \exp \left(- \frac{(\mathbf{v} + \mathbf{v}_e)^2}{v_0^2} \right) \Theta(v_{\text{esc}} - \|\mathbf{v} + \mathbf{v}_e\|)$$

$$R(\mathbf{q}) = n_\chi \int d^3 \mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}, \mathbf{q})$$

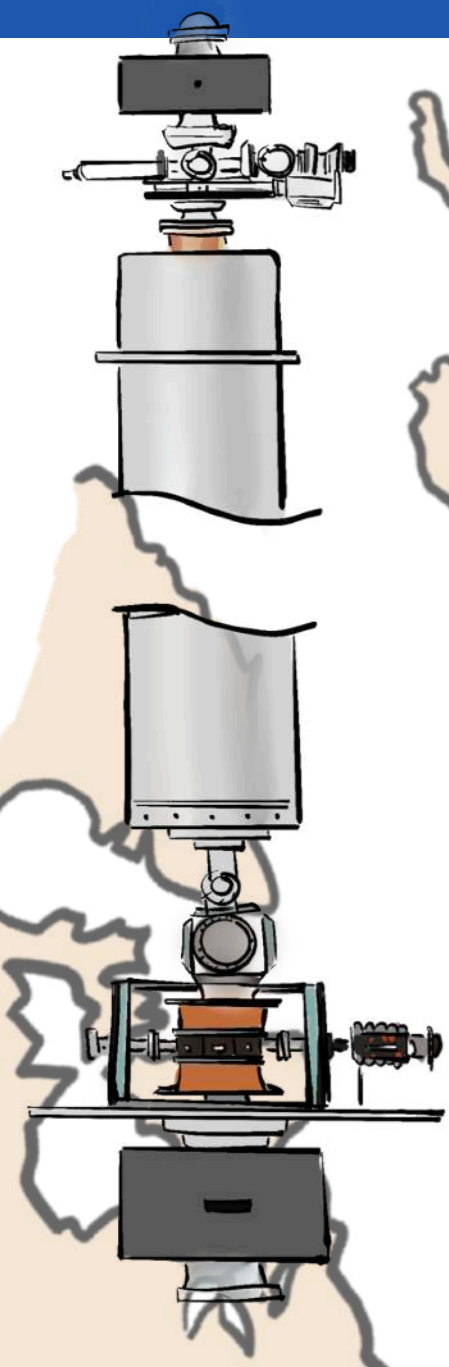
$$\frac{\rho_\chi m_T}{\rho_T m_\chi}$$

$$\frac{1}{V^2} \frac{\pi \bar{\sigma}}{\mu^2} \mathcal{F}_{\text{med}}^2(\mathbf{q}) \mathcal{F}_T^2(\mathbf{q})$$

$$\mathcal{F}_T(\mathbf{q}) = A \mathcal{F}_A^2(q r_A)$$



AIs: Examples



STANFORD ^{87}Rb

10-m atomic fountain

$$r_{\text{cloud}} \sim 0.2\text{mm}, N \sim 10^8$$

$$\Delta x = 0.1\text{m}, t_{\text{exp}} = 2\text{s}$$

ELGAR ⁸⁷Rb

European Laboratory for Gravitation
and Atom-interferometric Research

MIGA ⁸⁷Rb

Matter wave-laser based
Interferometer Gravitation Antenna

AION

Atom Interferometer
Observatory and Network

MAGIS-100

Matter-wave Atomic Gradiometer
Interferometric Sensor

★ STANFORD ⁸⁷Rb

10-m atomic fountain

$$r_{\text{cloud}} \sim 0.2\text{mm}, N \sim 10^8$$

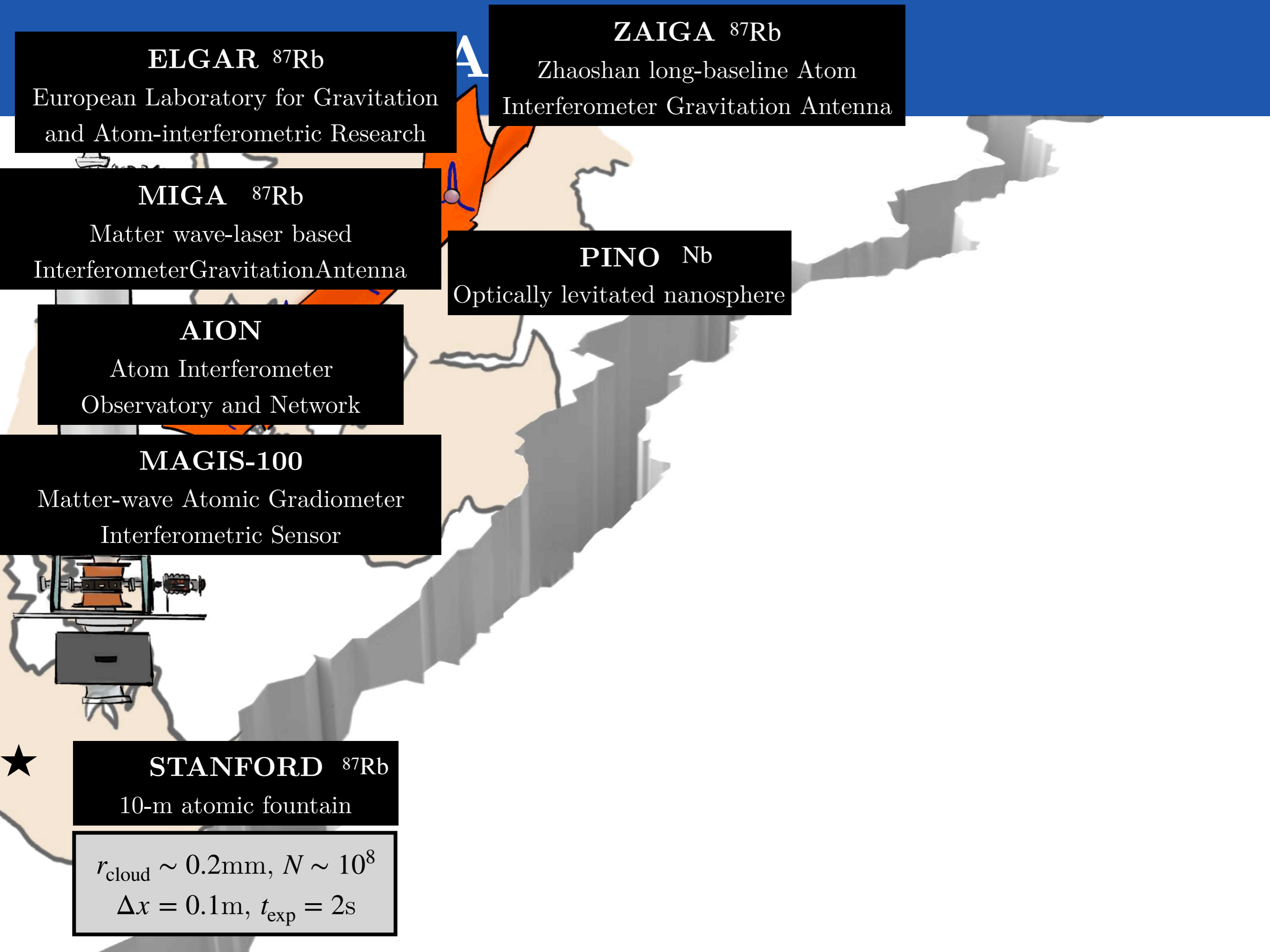
$$\Delta x = 0.1\text{m}, t_{\text{exp}} = 2\text{s}$$

ZAIGA ⁸⁷Rb

Zhaoshan long-baseline Atom
Interferometer Gravitation Antenna

PINO Nb

Optically levitated nanosphere



ELGAR ⁸⁷Rb

European Laboratory for Gravitation and Atom-interferometric Research

MIGA ⁸⁷Rb

Matter wave-laser based Interferometer Gravitation Antenna

AION

Atom Interferometer Observatory and Network

MAGIS-100

Matter-wave Atomic Gradiometer Interferometric Sensor

★ STANFORD ⁸⁷Rb

10-m atomic fountain

$r_{\text{cloud}} \sim 0.2\text{mm}, N \sim 10^8$
 $\Delta x = 0.1\text{m}, t_{\text{exp}} = 2\text{s}$

ZAIGA ⁸⁷Rb

Zhaoshan long-baseline Atom Interferometer Gravitation Antenna

PINO Nb

Optically levitated nanosphere

BECCAL

Bose-Einstein Condensate ⁸⁷Rb Cold Atom Laboratory

MAQRO SiO₂

Macroscopic Quantum Resonators

$r_{\text{cloud}} \sim 0.1\mu\text{m}, N \sim 10^{10}$
 $\Delta x = 0.1\mu\text{m}, t_{\text{exp}} = 100\text{s}$



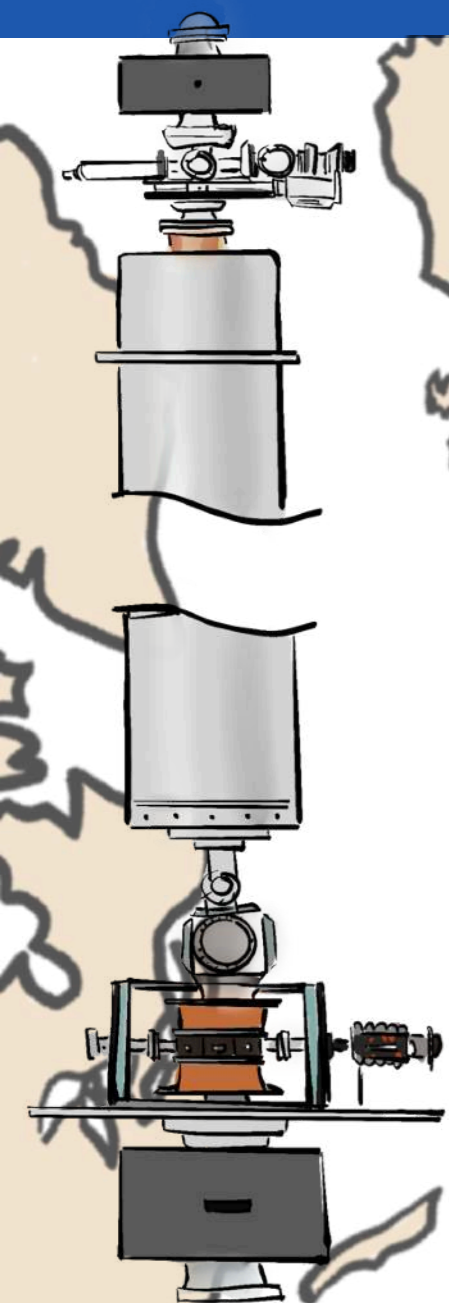
GDM ⁸⁷Rb

Gravity Dark energy Mission

AEDGE

Atomic Experiment for Dark Matter and Gravity Exploration in Space

AIs: Examples



MAQRO SiO₂
Macroscopic Quantum Resonators

$$r_{\text{cloud}} \sim 0.1 \mu\text{m}, N \sim 10^{10}$$
$$\Delta x = 0.1 \mu\text{m}, t_{\text{exp}} = 100\text{s}$$



⁸⁷Rb

⁸⁷Rb



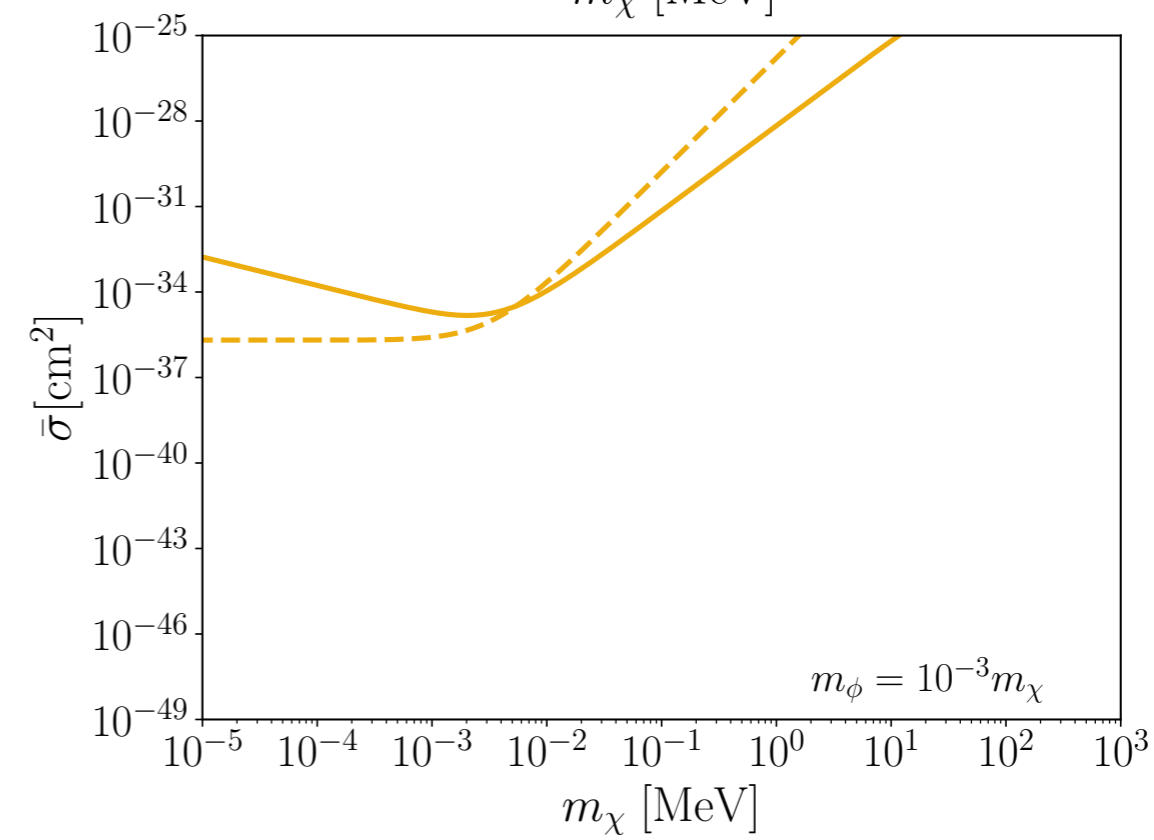
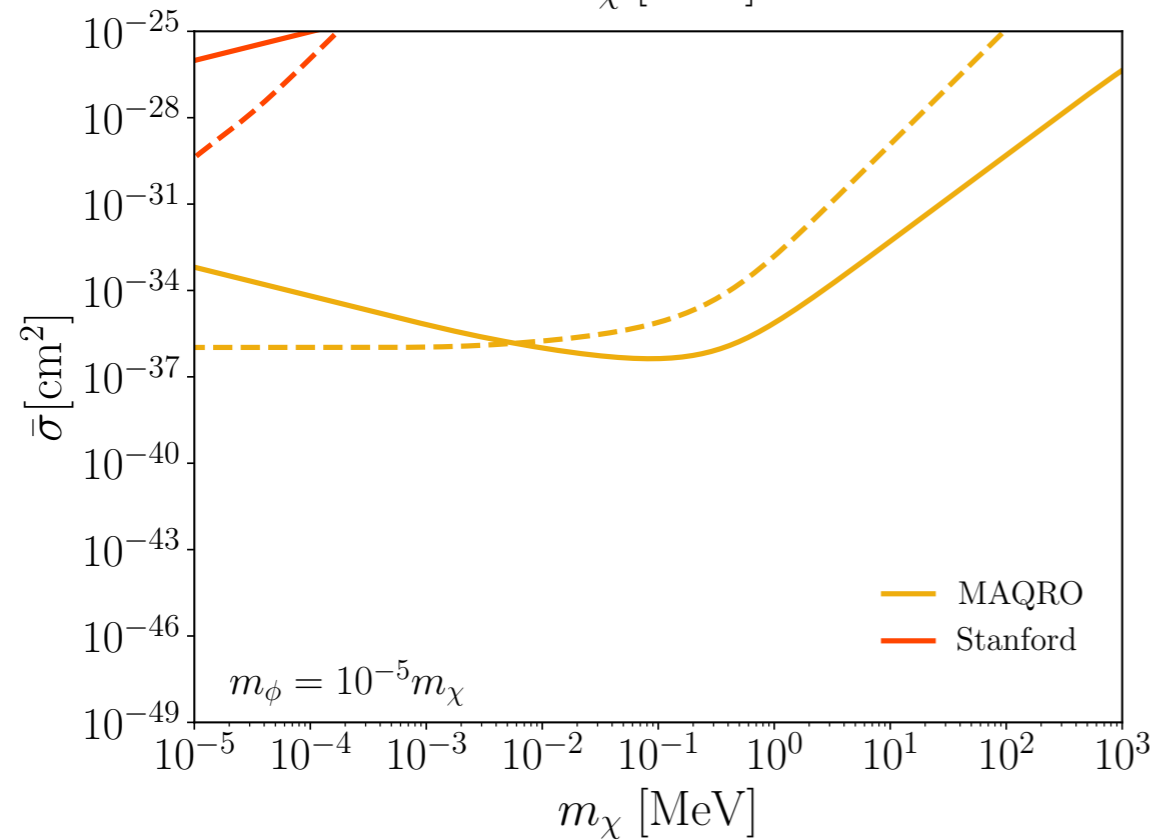
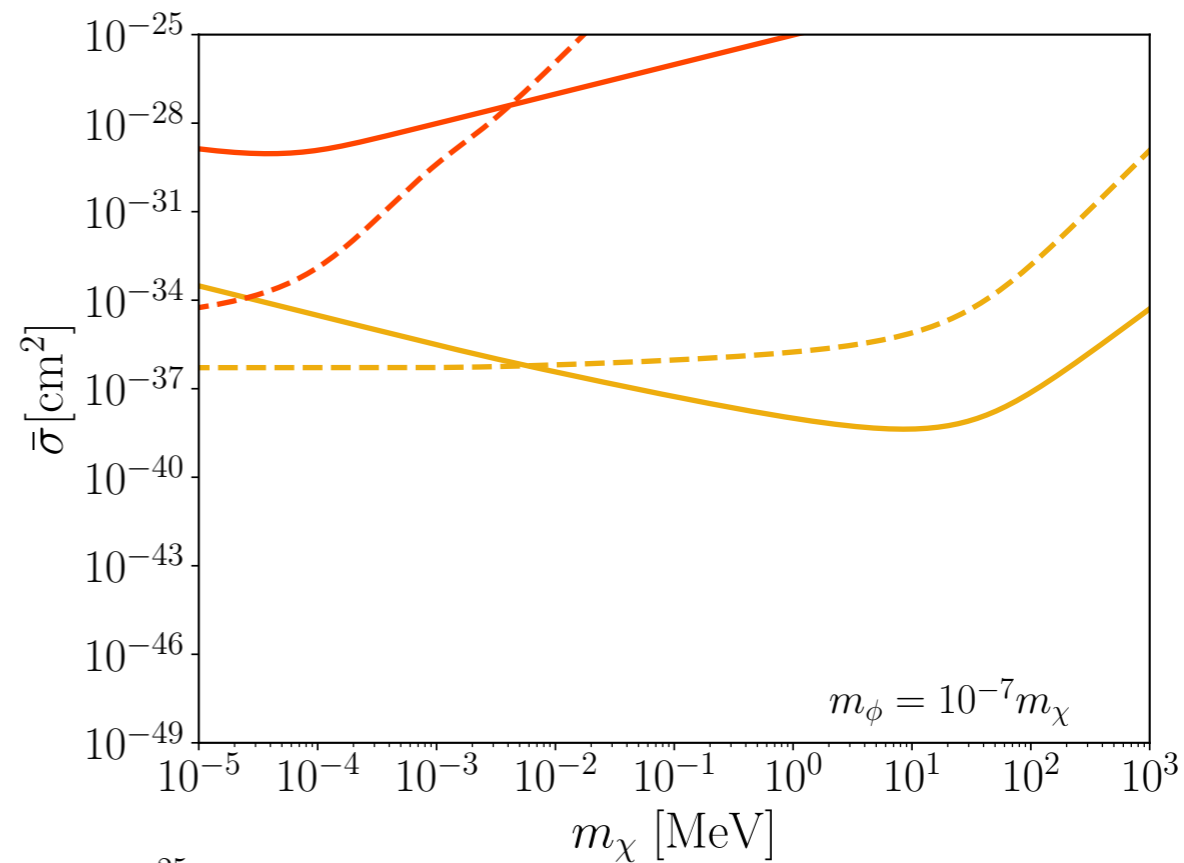
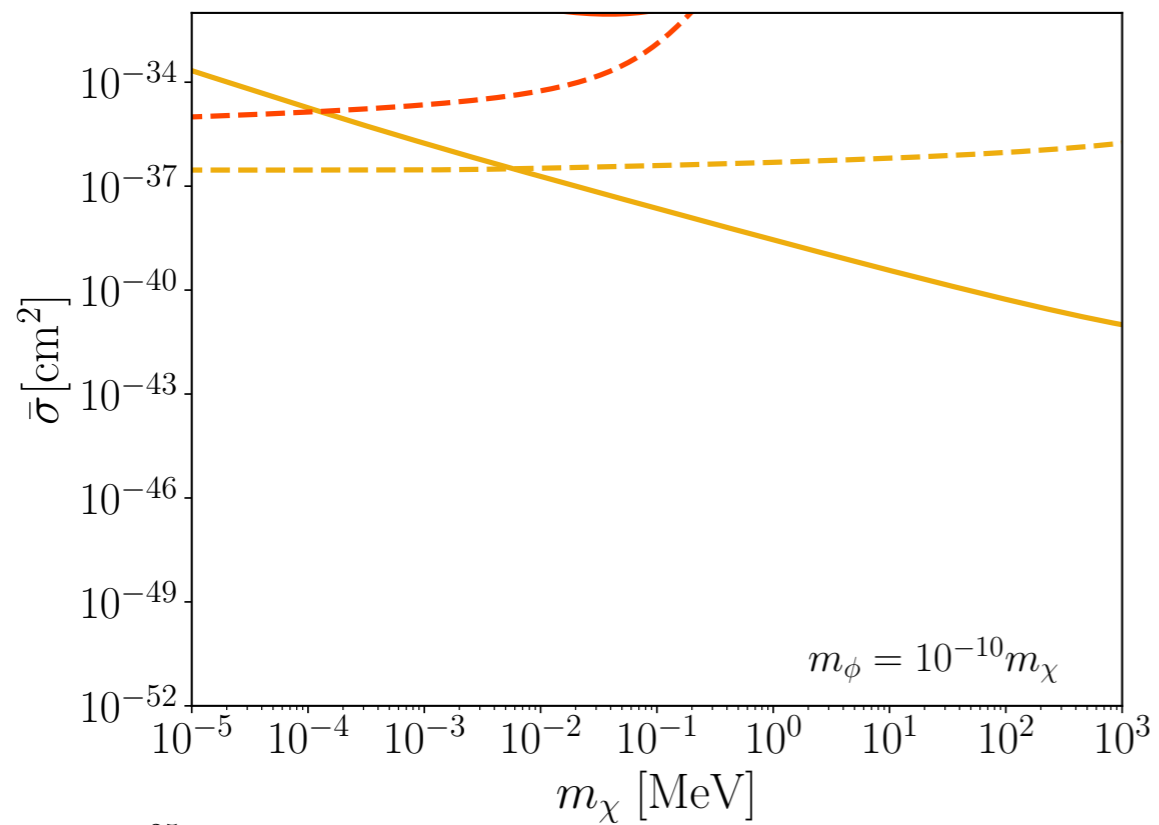
★ STANFORD ⁸⁷Rb

10-m atomic fountain

$$r_{\text{cloud}} \sim 0.2\text{mm}, N \sim 10^8$$

$$\Delta x = 0.1\text{m}, t_{\text{exp}} = 2\text{s}$$

AIs: Limits



AIs: Constraints

[Knapen, Lin, Zurek, 2017]

$$R = \frac{n_\chi}{m_T} \int d^3\mathbf{v} f(\mathbf{v}) \Gamma(\mathbf{v}) \mathcal{F}_{\text{decoh}}(\mathbf{q})$$

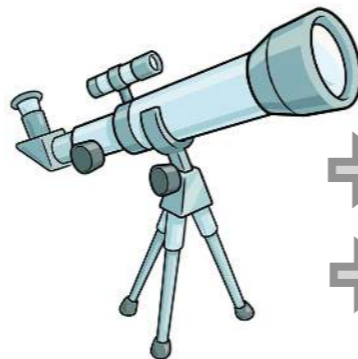
$\bar{\sigma} = \frac{y_\chi^2 y_n^2}{4\pi} \frac{\mu^2}{(m_\chi^2 v_0^2 + m_\phi^2)^2}$

Terrestrial



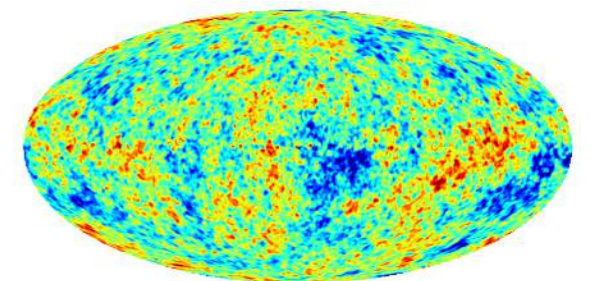
- ⇒ Collider
- ⇒ 5th force

Astrophysical

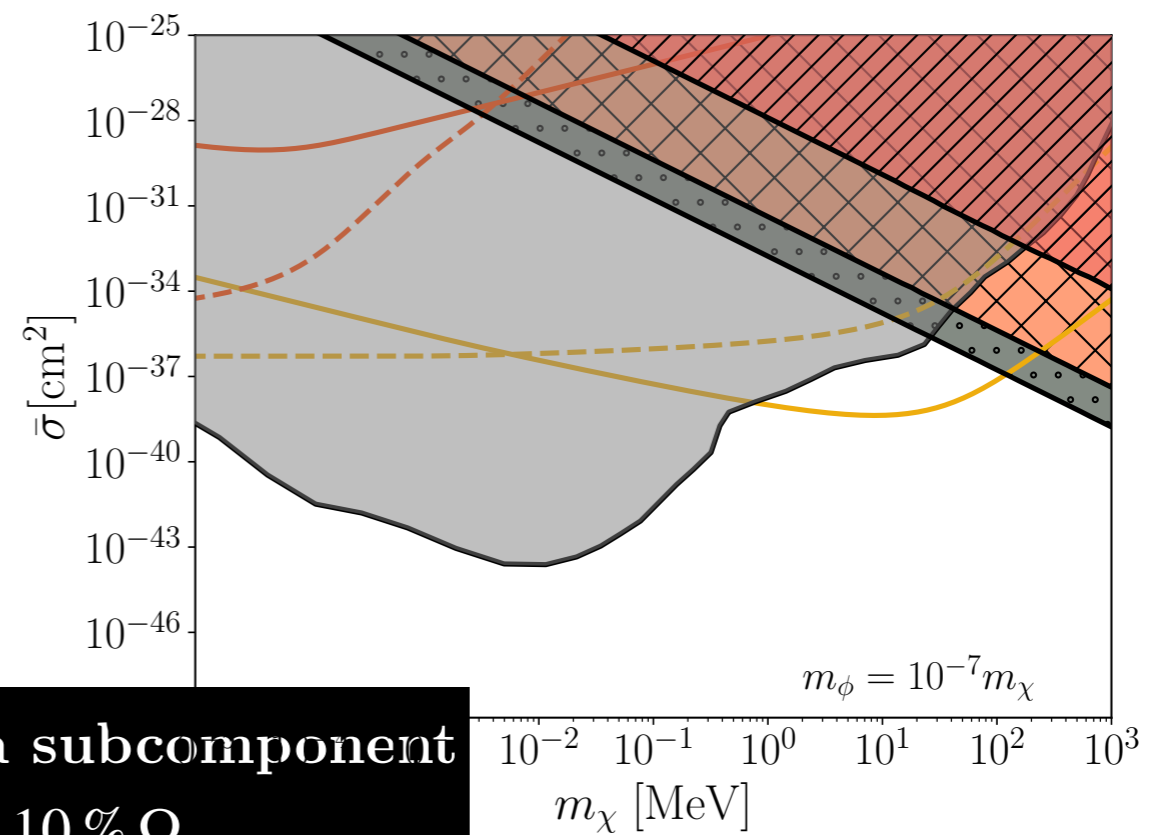
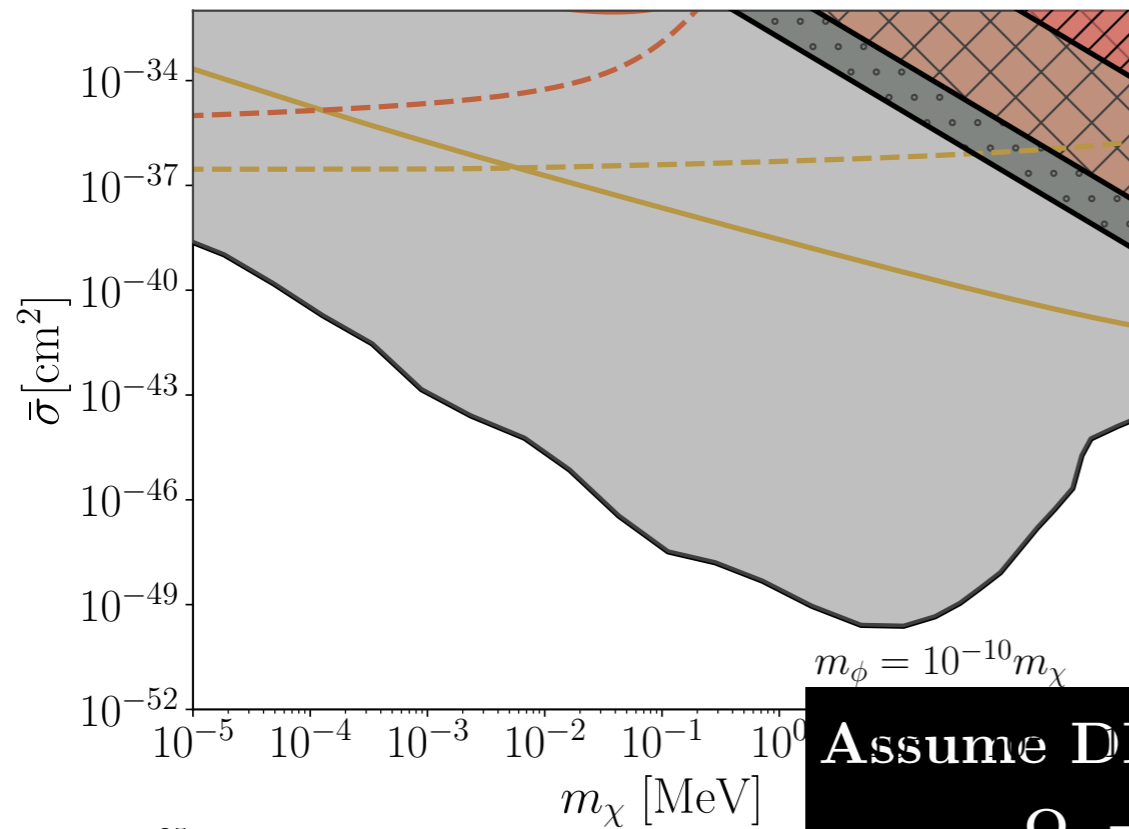


- ⇒ Stellar emission
- ⇒ DMSI

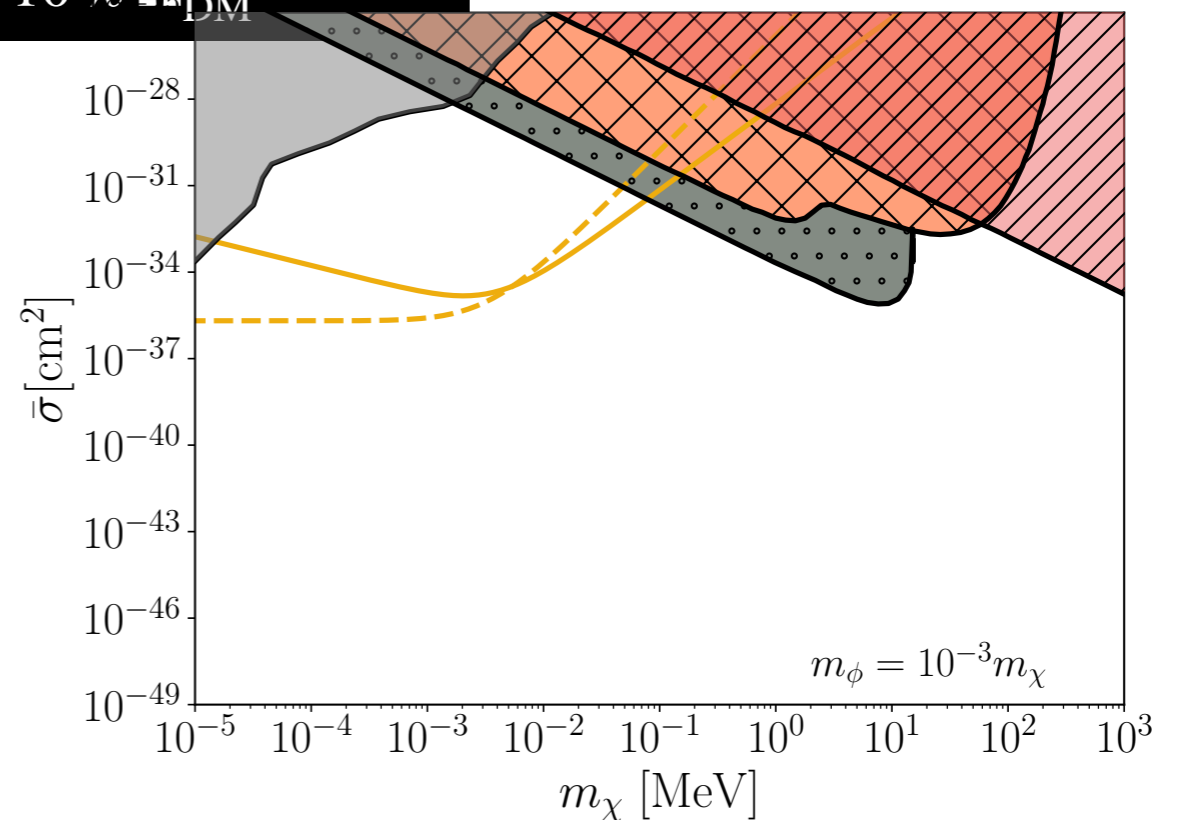
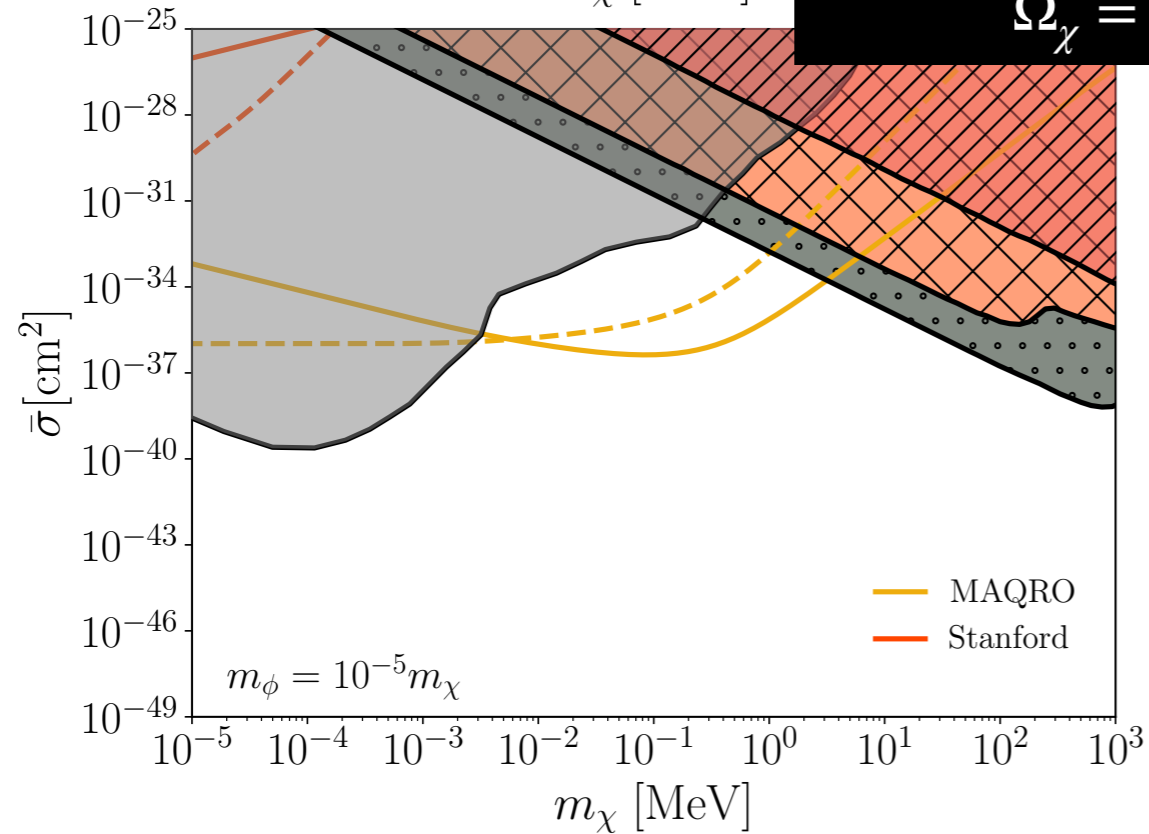
Cosmological



AIs: Constraints



Assume DM is a subcomponent
 $\Omega_\chi = 5\% - 10\% \Omega_{\text{DM}}$



AIs: Applications

[Dimopoulos, Graham, et al. 2008] [Hogan, Johnson, et al. 2011], [Yu, Tinto, 2011] [Graham, Hogan, 2013], [Canuel, Bertoldi, et al. 2018] [Canuel, Abend, et al. 2020] [Kolkowitz, Pikovski, et al., 2016] [Zhan, Wang, et al. 2020] [El-Neaj, Alpigiani, et al. 2020] [Badurina, Bentine, et al. 2020], [Graham, Hogan, et al. 2016] [Graham, Hogan, et al. 2017], [Ballmer, Adhikari, et al. 2022]

GWs

EDMs

[Wicht et al, 2002] [Bennet et al. 2006] [Cadoret et al. 2008] [Terranova, Tino, 2014]...

$$N_I \stackrel{!}{=} \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

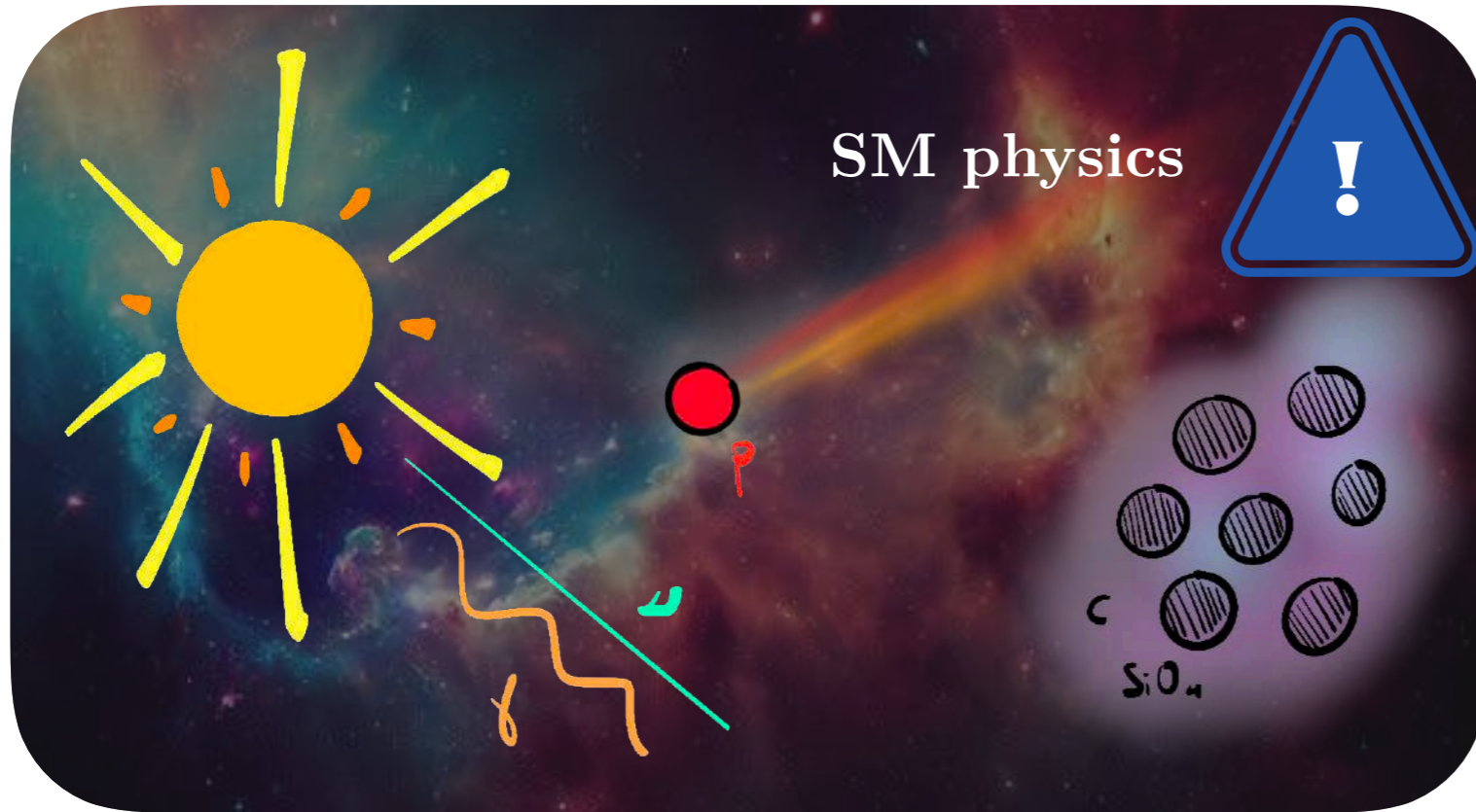
5th forces

[Wacker, 2010], [Rosi, Sorrentino, et al. 2014] [Biedermann, Wu, et al. 2015] [Rosi, D'Amico, et al. 2017] [Fray, Diez, et al. 2004] [Schlippert, Hartwig, et al. 2014] [Zhou, Long, et al. 2015] [Barrett, Antoni-Micollier, et al. 2016] [Kuhn, McDonald, et al. 2014] [Barrett, Antoni-Micollier, et al. 2015] [Fiorillo, Mazzoni, et al. 2014] [Bonnin, Zahzam et al. 2013] [Harmon, Abend, et al. 2015] [Asenbaum, Overstreet, et al. 2020] [Williams, Chiow, et al. 2016] [Battelier, Berge, et al., 2019] ...

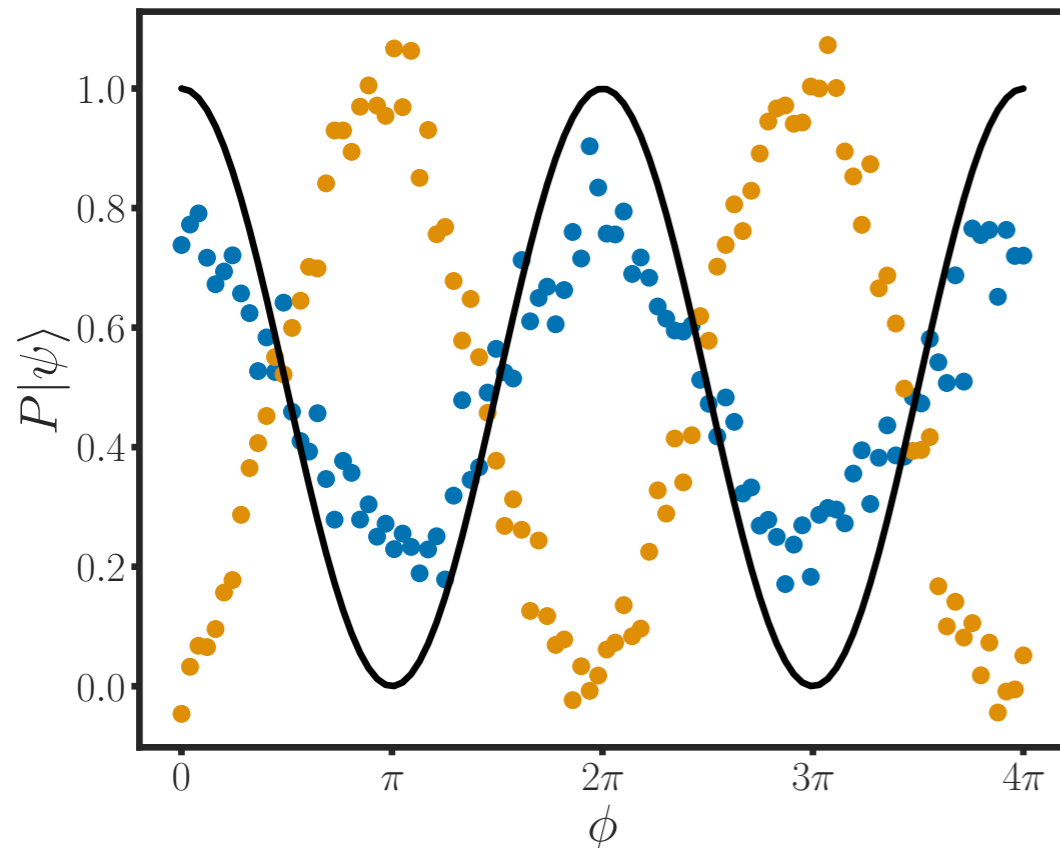
ULDM

[Graham, Kaplan, et al. 2016] [Arvanitaki, Graham, et al. 2018] [Kolb, Weers, et al. 2018] [Badurina, Blas, McCabe, 2021] [Antypas, Banerjee, 2022] [Badurnina, Gipson, et al. 2022] [Badurnina, Beniwal, et al. 2023]

AIs: Measurement



$$\frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

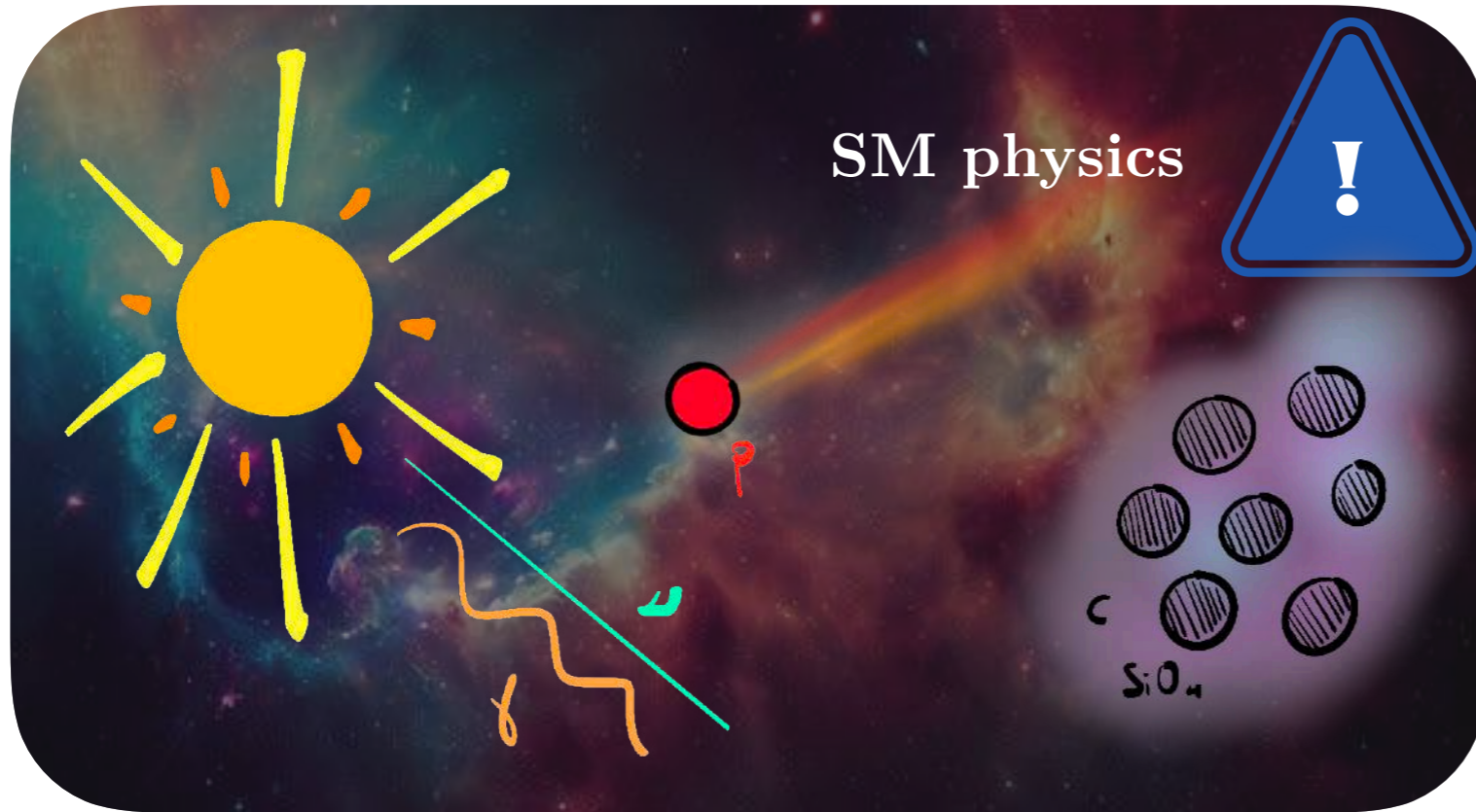


Visibility

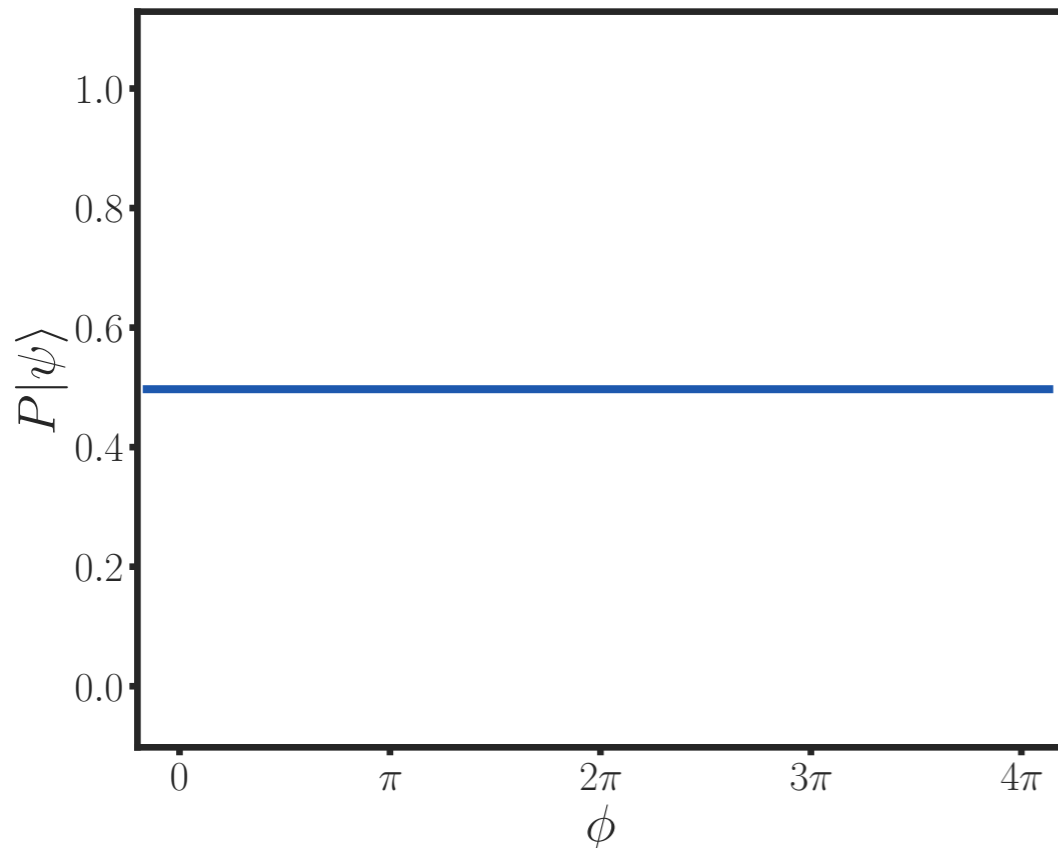
$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$

- No decoherence or phase effects
- Decoherence Effect
- Phase Effect

AIs: Measurement



$$\frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$



Visibility

$$\text{SNR}|_{\text{shot}} \equiv \frac{|\Delta V|}{\sigma_V}$$

- No decoherence or phase effects
- Decoherence Effect
- Phase Effect

AIs: Destructive Decoherence

Multi-atom system (distinguishable)

[Badurina, CM, Plestid, 2024]

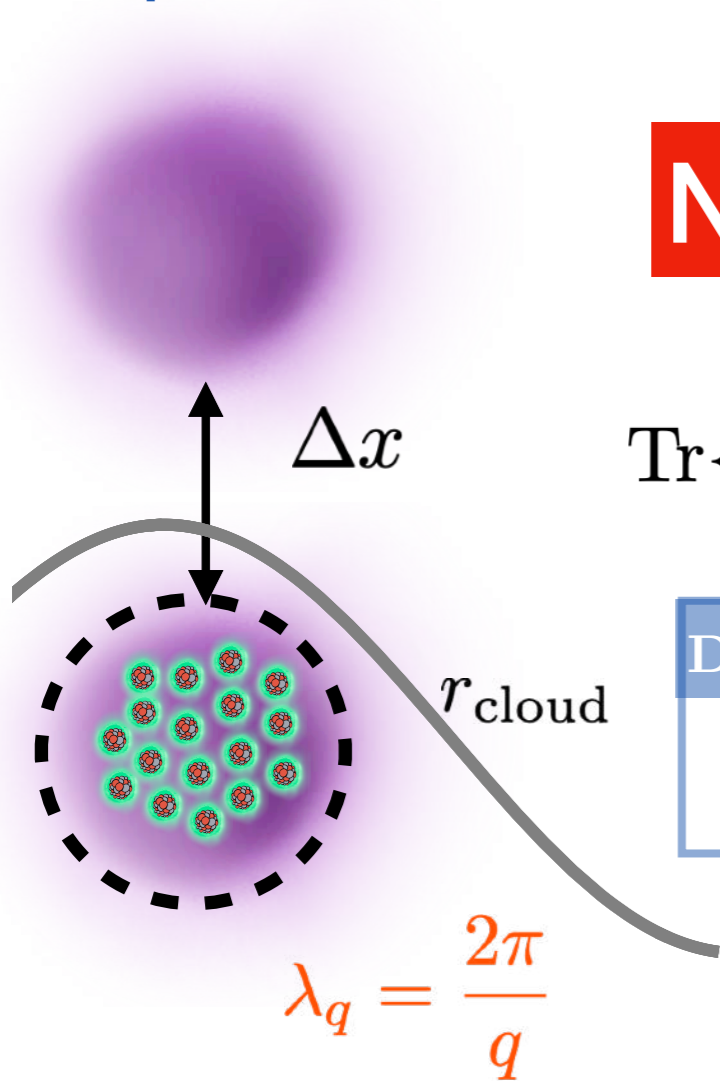
NEW!

$$\rho_{(N=2)} = \begin{pmatrix} \circ & \blacksquare & \blacksquare & \star \\ \blacksquare & \circ & \circ & \blacksquare \\ \blacksquare & \circ & \circ & \blacksquare \\ \star & \blacksquare & \blacksquare & \circ \end{pmatrix}$$

$$\text{Tr}\{\rho_N \sum_i^N \mathcal{O}_i\} = N \text{Tr}\{\rho_1 \mathcal{O}_i\} \stackrel{!}{=} N \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

Decoherence Kernel n-body measurement

$$\mathcal{F}_{\text{decoh}}(\mathbf{q}) = n^2 (1 - \cos(\mathbf{q} \cdot \Delta\mathbf{x})) - iNn \sin(\mathbf{q} \cdot \Delta\mathbf{x})$$



$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

$$\Rightarrow \Delta\rho = \frac{i}{2} [T + T^\dagger, \rho] - \frac{1}{2} \{T^\dagger T, \rho\} + T\rho T^\dagger$$

AIs: Destructive Decoherence

Multi-atom system (distinguishable)

[Badurina, CM, Plestid, 2024]

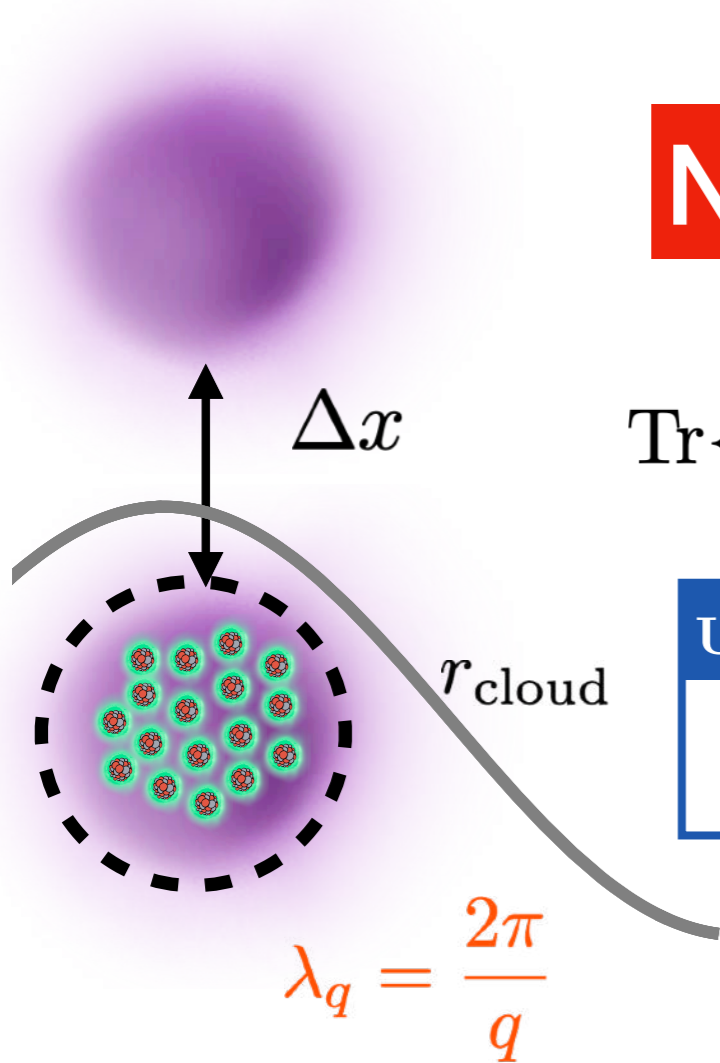
NEW!

$$\rho_{(N=2)} = \begin{pmatrix} \circ & \blacksquare & \blacksquare & \star \\ \blacksquare & \circ & \circ & \blacksquare \\ \blacksquare & \circ & \circ & \blacksquare \\ \star & \blacksquare & \blacksquare & \circ \end{pmatrix}$$

$$\text{Tr}\{\rho_N \sum_i^N \mathcal{O}_i\} = N \text{Tr}\{\rho_1 \mathcal{O}_i\} \stackrel{!}{=} N \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

Unitary Kernel n-body measurement

$$\mathcal{F}_{\text{unitary}}(\mathbf{q}') = in(n + N - 2N_g)[1 - \cos(\mathbf{q}' \cdot \Delta\mathbf{x})]$$



$$\rho' = S\rho S^\dagger = (\mathbb{I} + T)\rho(\mathbb{I} + T)^\dagger$$

$$\Rightarrow \Delta\rho = \frac{i}{2}[T + T^\dagger, \rho] - \frac{1}{2}\{T^\dagger T, \rho\} + T\rho T^\dagger$$

AIs: Destructive Decoherence

Multi-atom system (distinguishable)

[Badurina, CM, Plestid, 2024]

NEW!

$$\rho_{(N=2)} = \begin{pmatrix} \circ & \blacksquare & \blacksquare & \star \\ \blacksquare & \circ & \circ & \blacksquare \\ \blacksquare & \circ & \circ & \blacksquare \\ \star & \blacksquare & \blacksquare & \circ \end{pmatrix}$$

$$\text{Tr}\{\rho_N \sum_i \mathcal{O}_i\} = N \text{Tr}\{\rho_1 \mathcal{O}_i\} \stackrel{!}{=} N \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

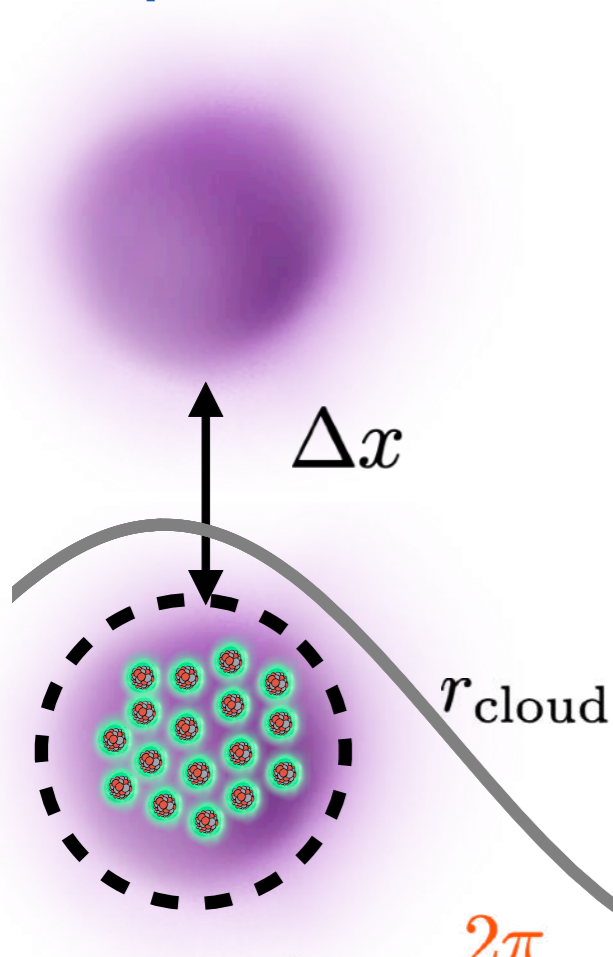
Unitary Kernel n-body measurement

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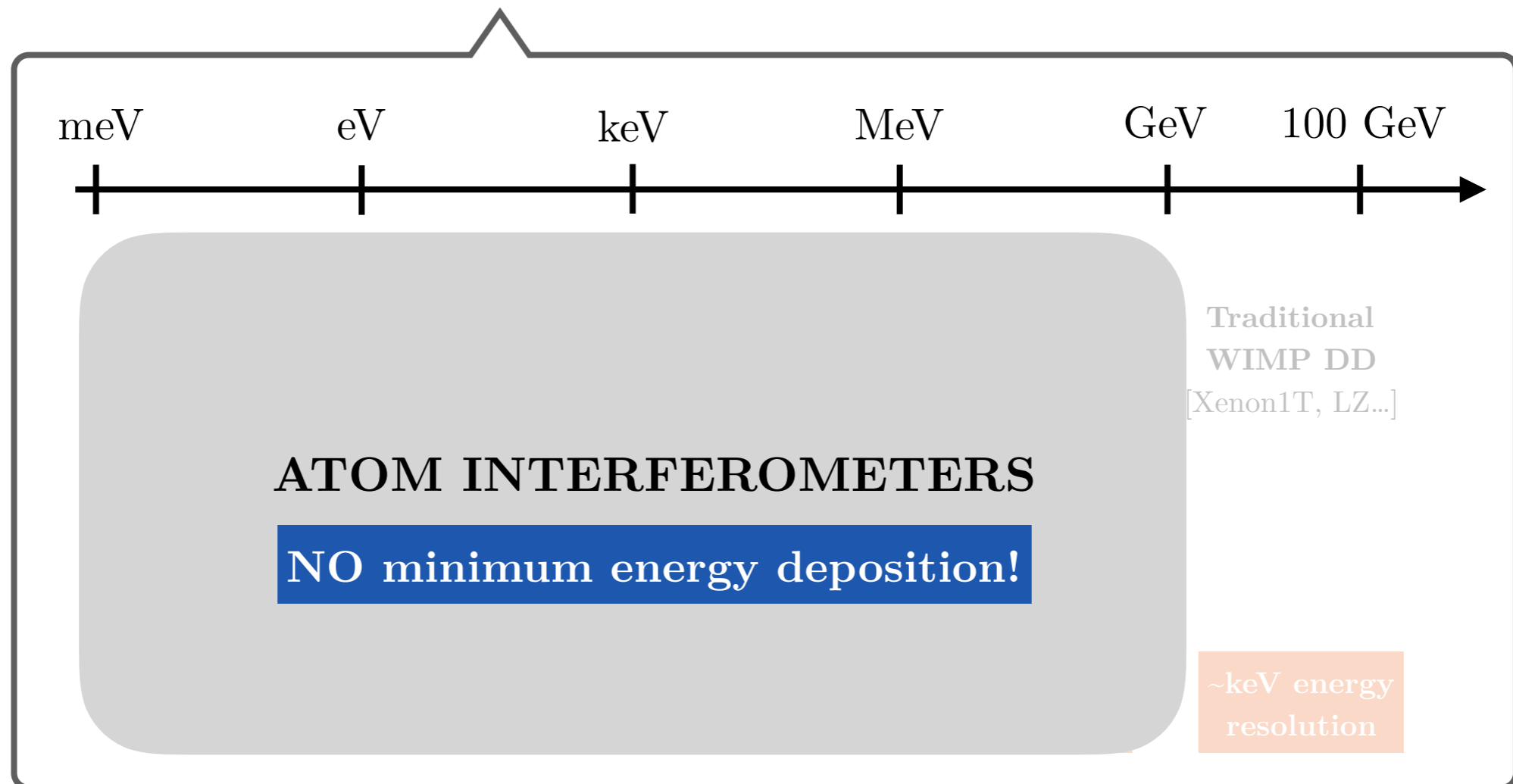
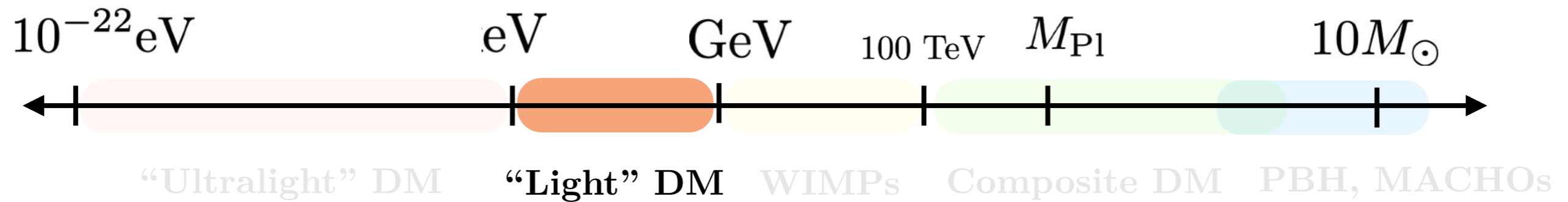
$$\lambda_q = \frac{2\pi}{q}$$

$$\frac{N_I}{N_I + N_{II}} \Big|_{\text{exp}} = \frac{1}{2} (1 + V \cos(\phi + \Delta\phi))$$

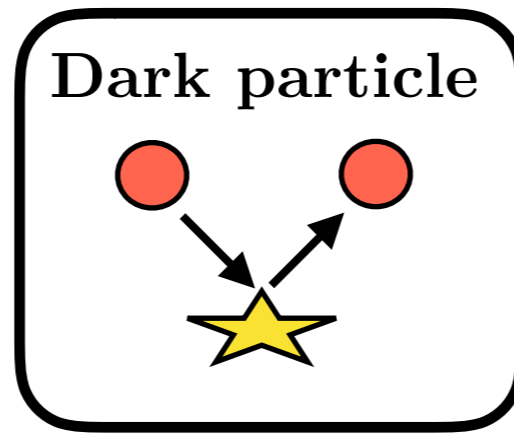
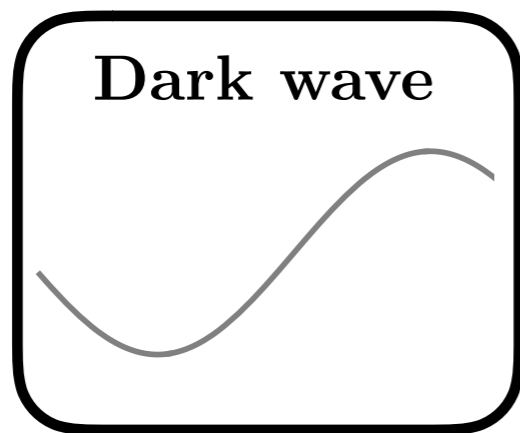
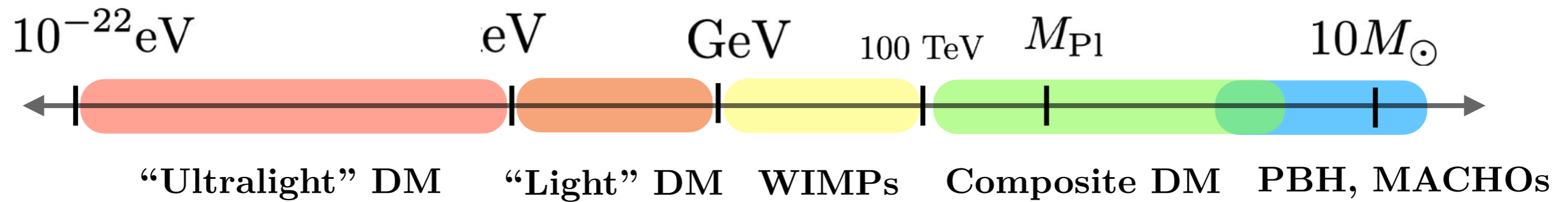
$$\text{Tr}\{\rho \mathcal{O}_1\} = \frac{1}{2} \left[1 + e^{-\int_{\mathbf{q},t} R(\mathbf{q})(1 - \cos(\mathbf{q} \cdot \Delta\mathbf{x}))} \cos^{N-1} \left(\int_{\mathbf{q}',t} \omega(\mathbf{q}') (1 - \cos(\mathbf{q}' \cdot \Delta\mathbf{x})) \right) \times \cos \left(\phi + \int_{\mathbf{q},t} R(\mathbf{q}) \sin(\mathbf{q} \cdot \Delta\mathbf{x}) \right) \right]$$



Dark Matter: where to look?

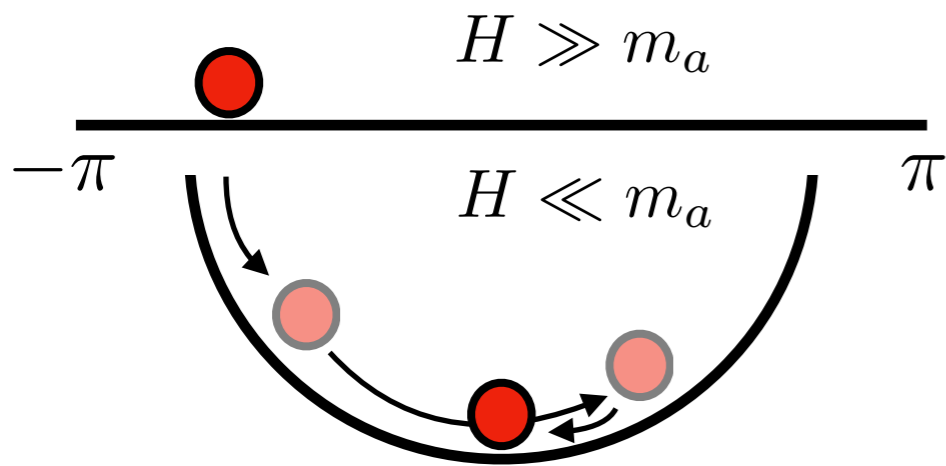
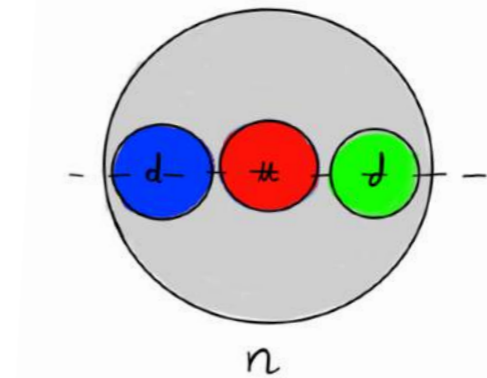
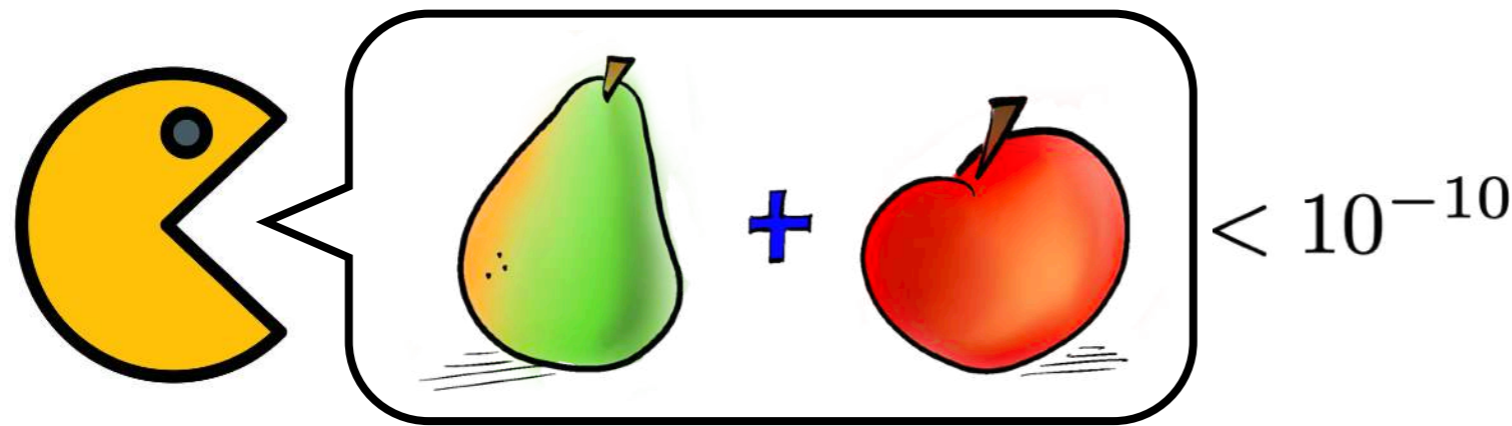
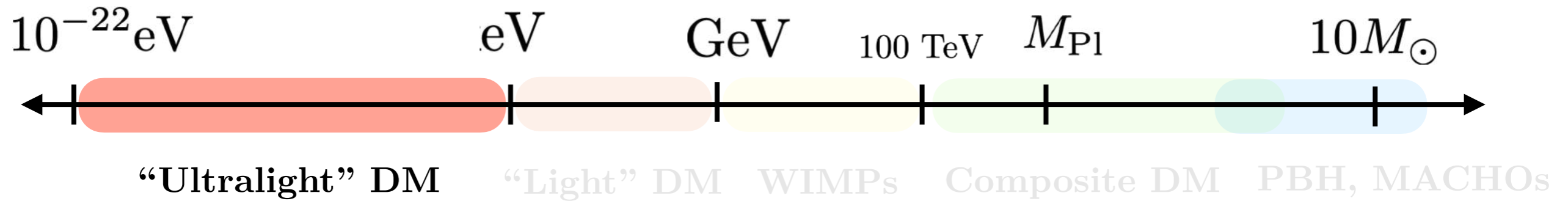


Dark Matter: where to look?



$$\left(\frac{\rho_{\text{DM}}}{m_{\text{DM}}}\right)^{-1/3} < \lambda_{dB} = \frac{1}{m_{\text{DM}}v_{\text{DM}}}$$

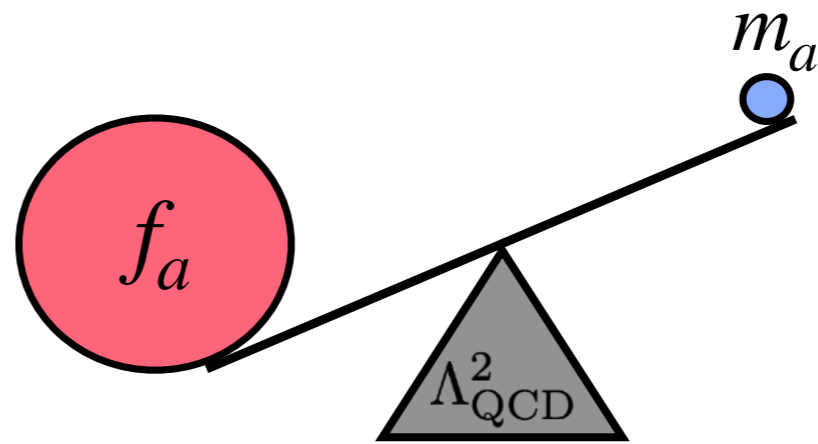
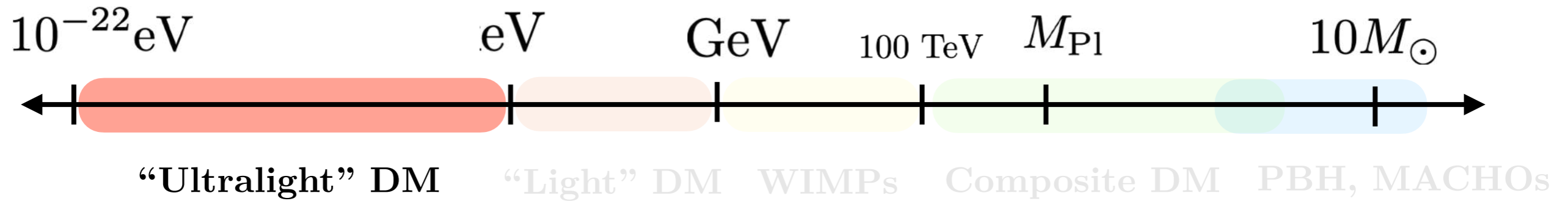
Axion Dark Matter



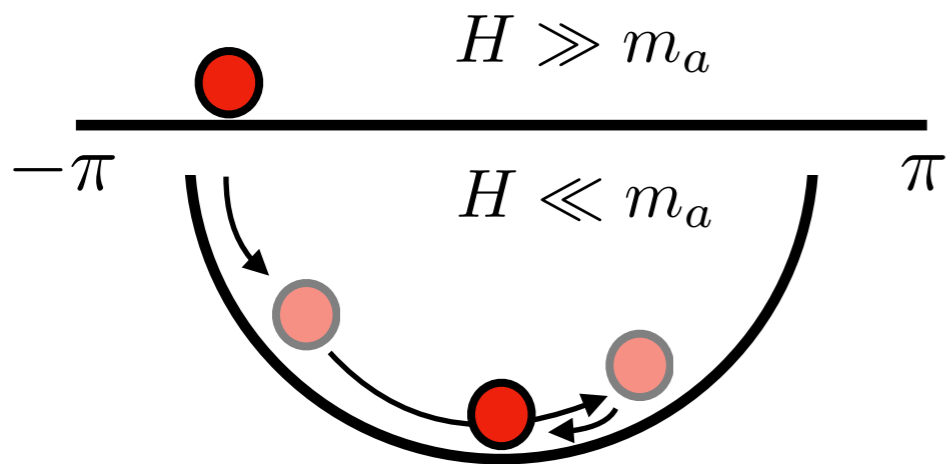
[Preskill, Wise, Wilczek, 1983]
 [Abbott, Sikivie, 1983]
 [Dine, Fischler, 1983]

[Peccei, Quinn, 1977] [Wilzeck, 1978] [Weinberg, 1978]
 [Dine, Fischler, Srednicki, 1981] [Zhitnitsky, 1980]
 [Kim, 1979] [Shifman, Vainshtein, Zakharov, 1980]

Axion Dark Matter



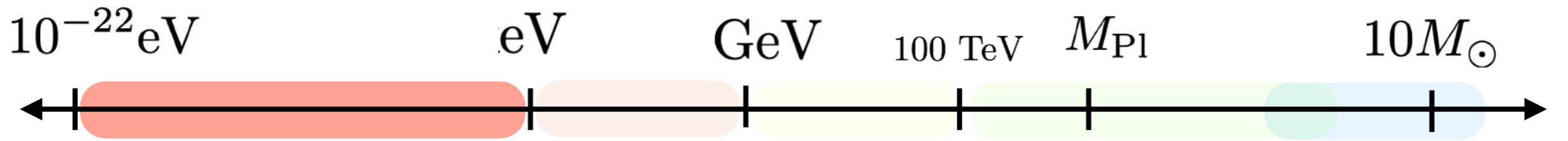
$$m_a \sim \frac{\Lambda_{\text{QCD}}^2}{f_a}$$



[Preskill, Wise, Wilczek, 1983]
 [Abbott, Sikivie, 1983]
 [Dine, Fischler, 1983]

[Peccei, Quinn, 1977] [Wilzeck, 1978] [Weinberg, 1978]
 [Dine, Fischler, Srednicki, 1981] [Zhitnitsky, 1980]
 [Kim, 1979] [Shifman, Vainshtein, Zakharov, 1980]

Axion Dark Matter



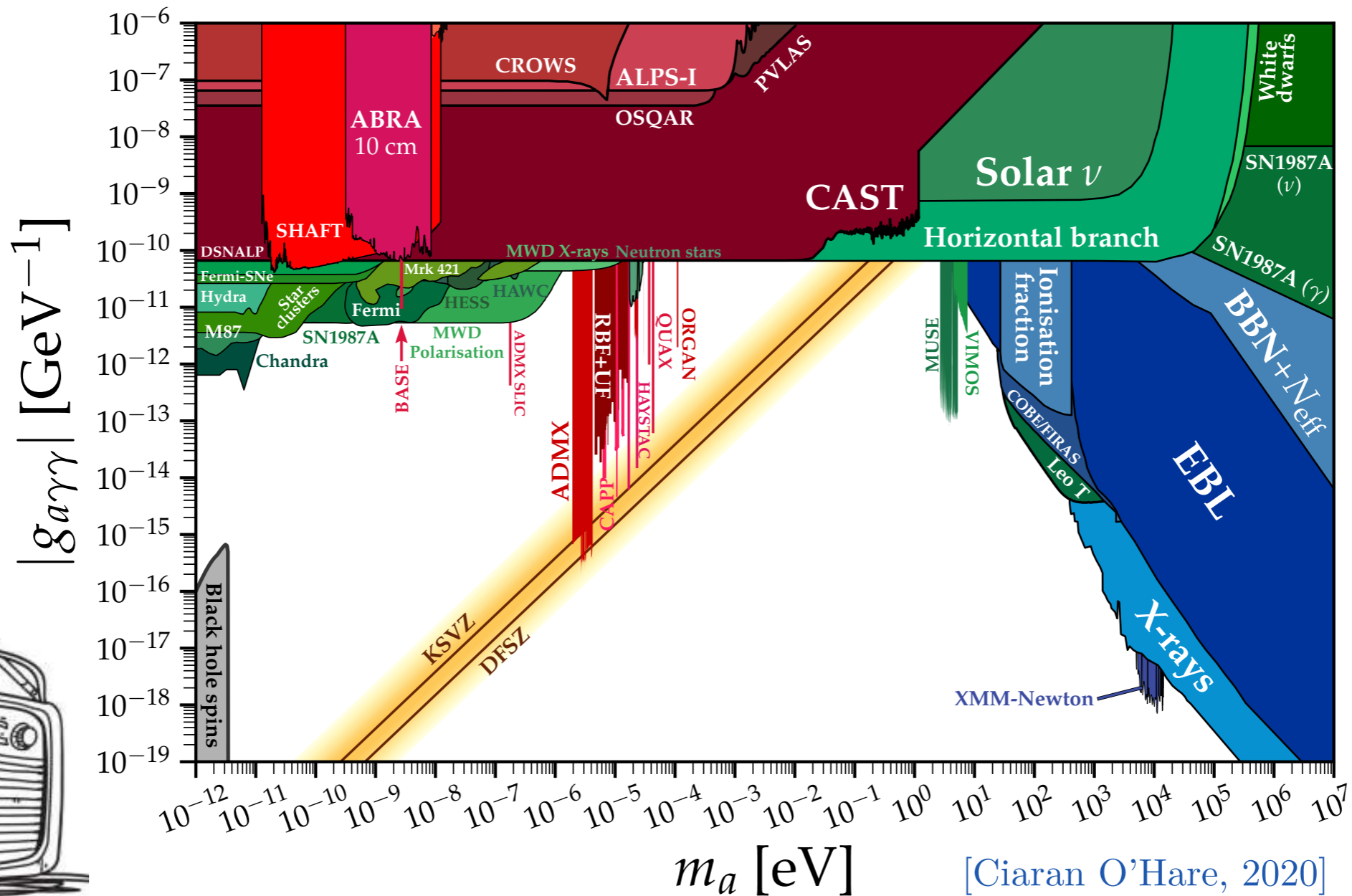
"Ultralight" DM

"Light" DM

WIMPs

Composite DM

PBH, MACHOs

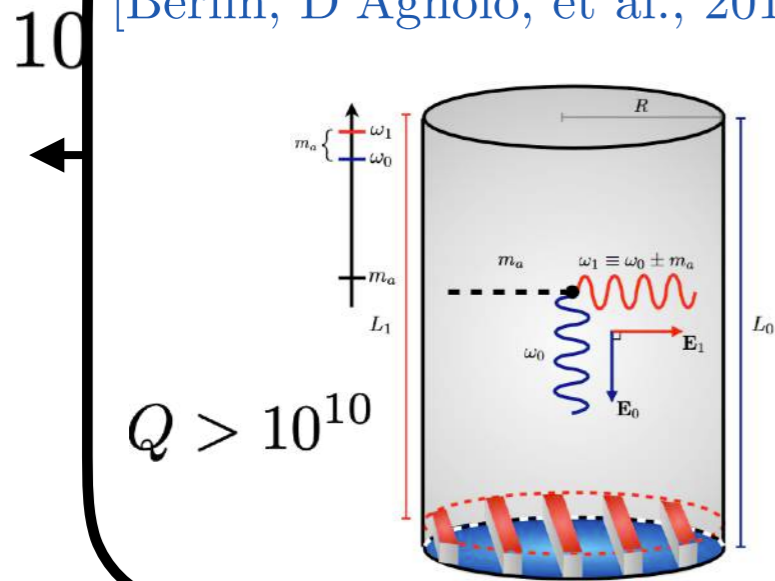


[Ciaran O'Hare, 2020]

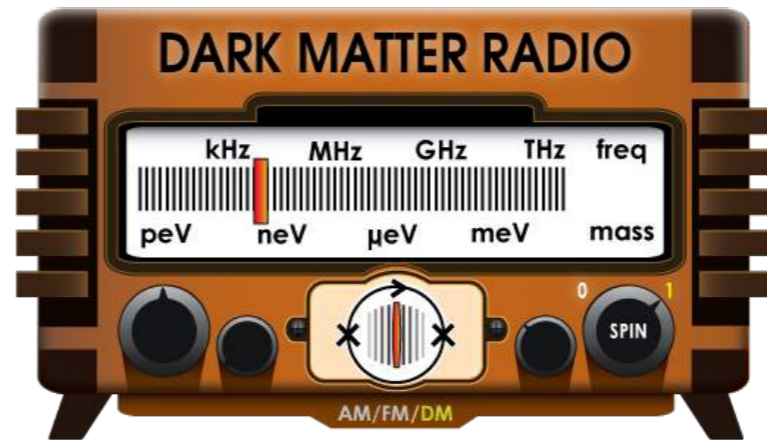
Axion Dark Matter

SRF cavities

[Berlin, D'Agnolo, et al., 2019]



DARK MATTER RADIO



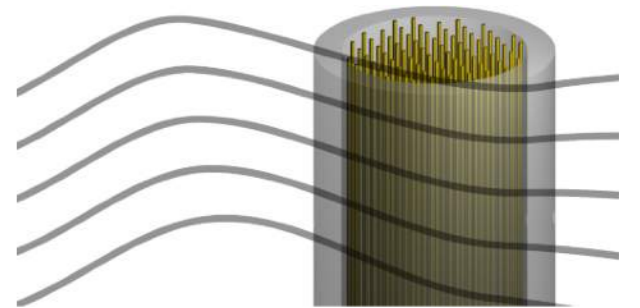
[Winslow et al., 2016]

$10M_{\odot}$

DM PBH, MACHOS

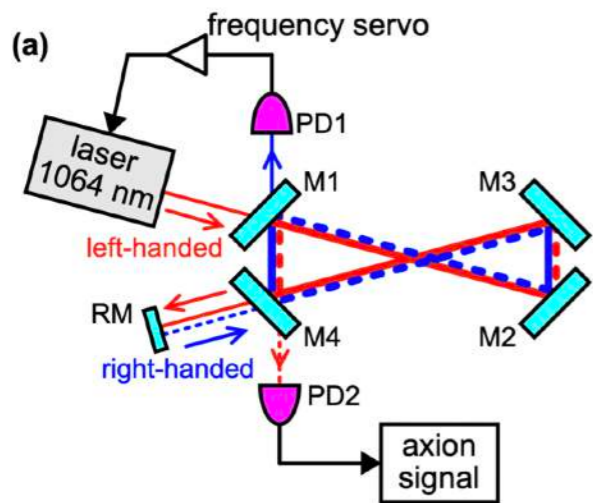
Tunable plasma

[Lawson, Millar, et al., 2019]



DANCE

[Obata, Fujita, Michimura, 2018]

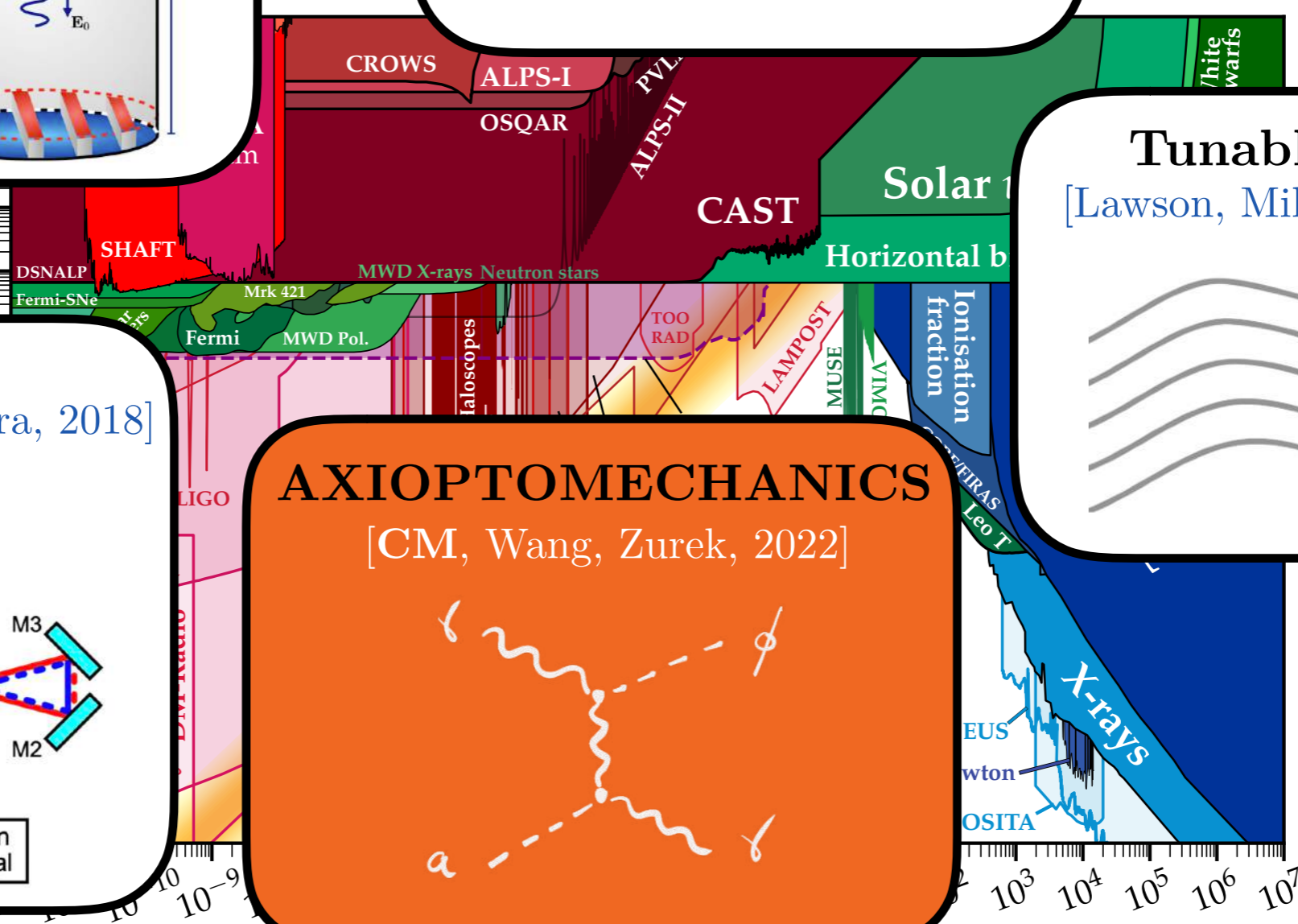


AXIOPTOMECHANICS

[CM, Wang, Zurek, 2022]

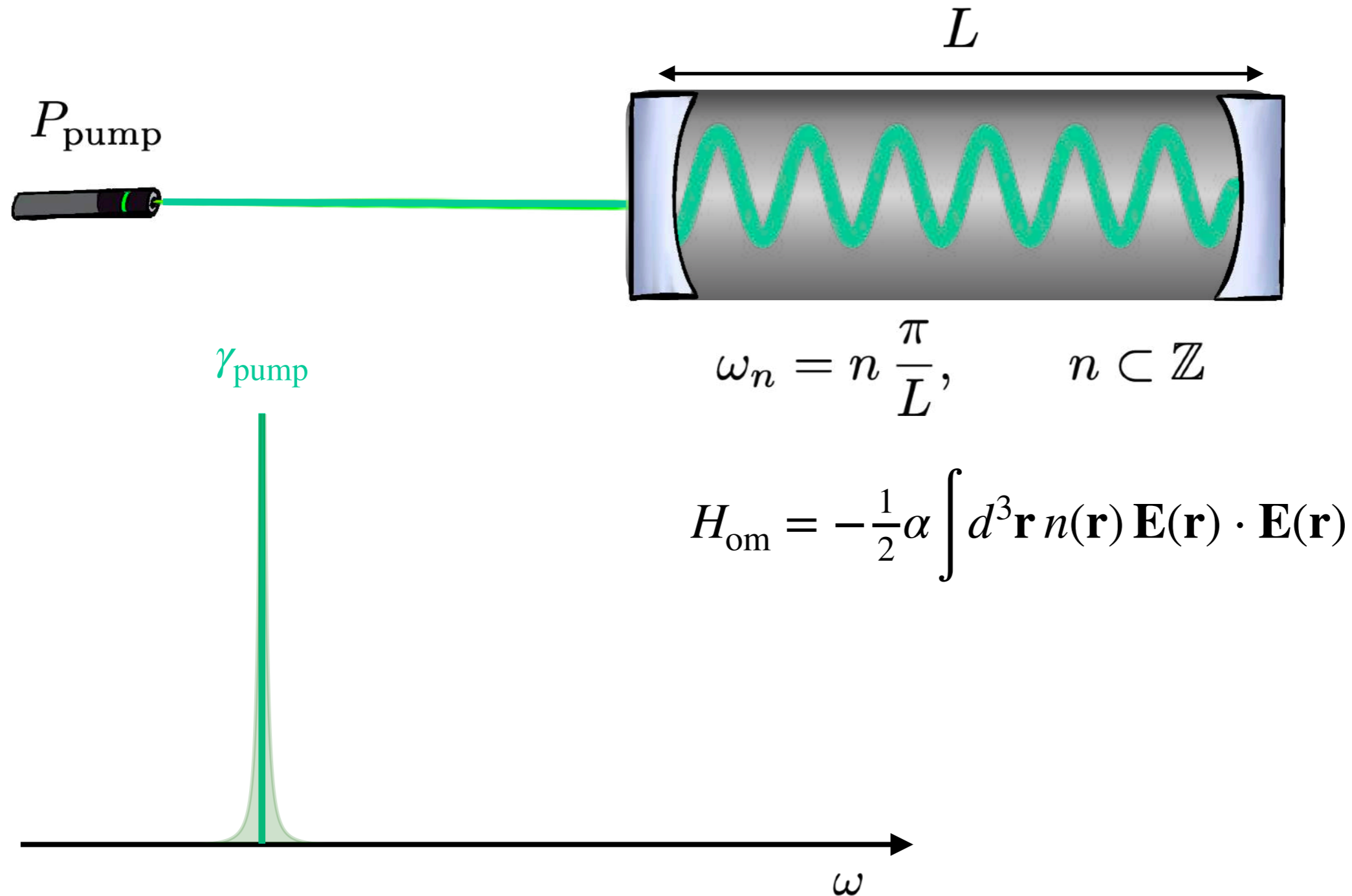


m_a [eV]



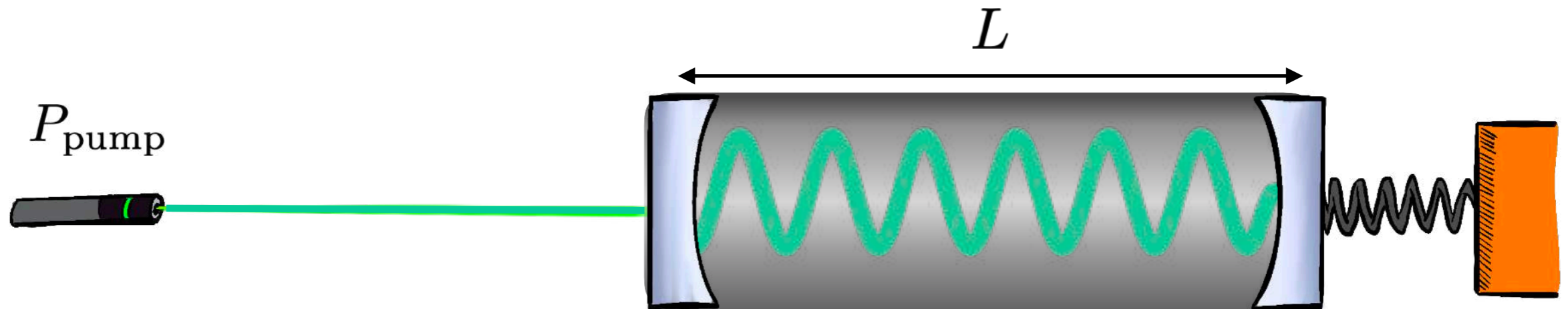
Standard Optomechanics

[Review: M. Aspelmeyer, T. J. Kippenberg, F. Marquardt, 2013. Thesis at J. Harris lab.]



Standard Optomechanics

[Review: M. Aspelmeyer, T. J. Kippenberg, F. Marquardt, 2013. Thesis at J. Harris lab.]



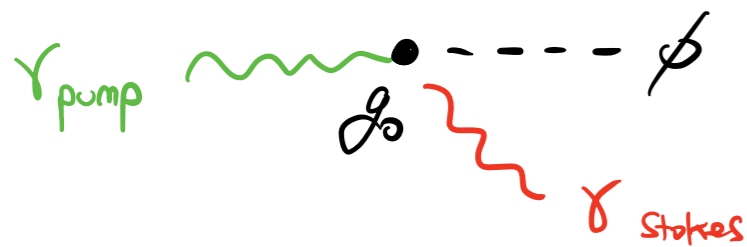
γ_{pump}

$$\omega_{\text{mec}} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger + \dots \right)$$

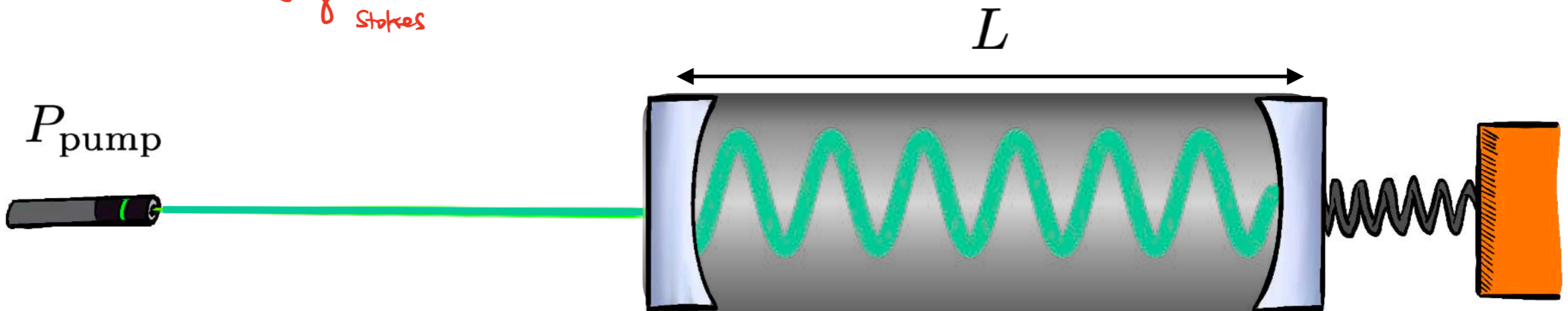
ω

Standard Optomechanics



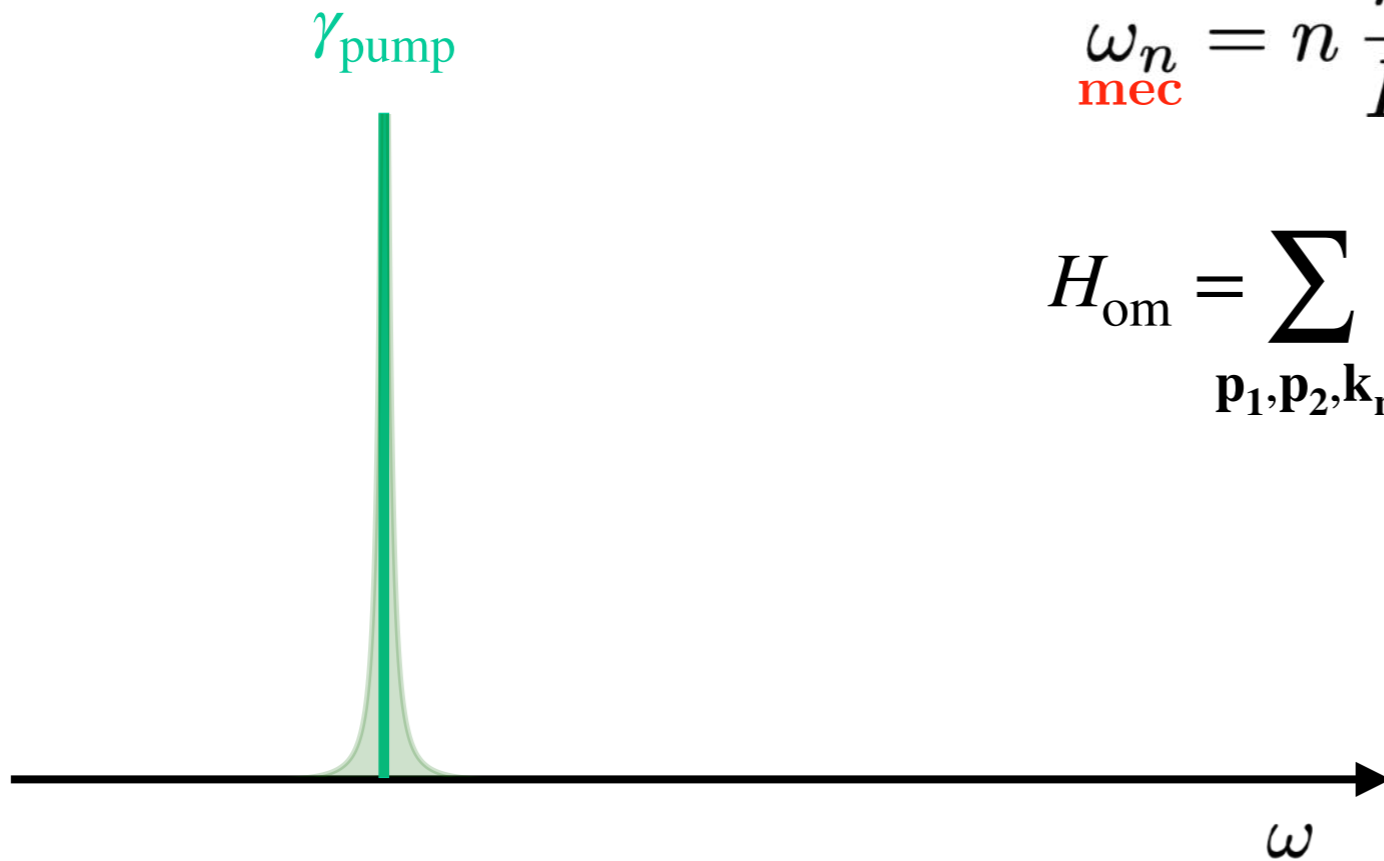
$$\vec{p}_{\gamma 1} = \vec{p}_{\phi} + \vec{p}_{\gamma 2}$$

$$\omega_{\gamma 1} = \omega_m + \omega_{\gamma 2}$$

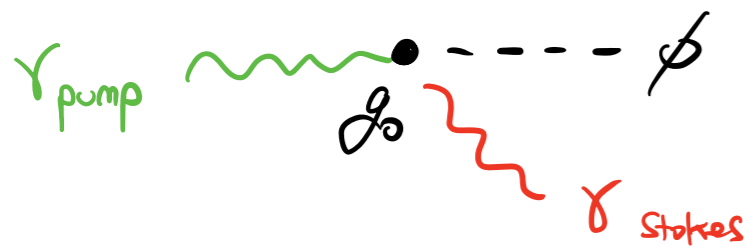


$$\omega_{\text{mec } n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger + \dots \right)$$

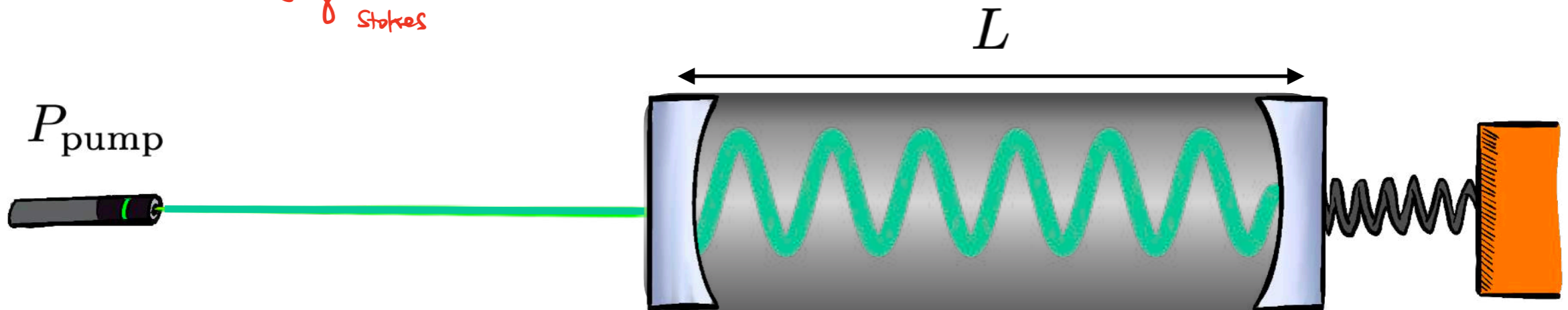


Standard Optomechanics



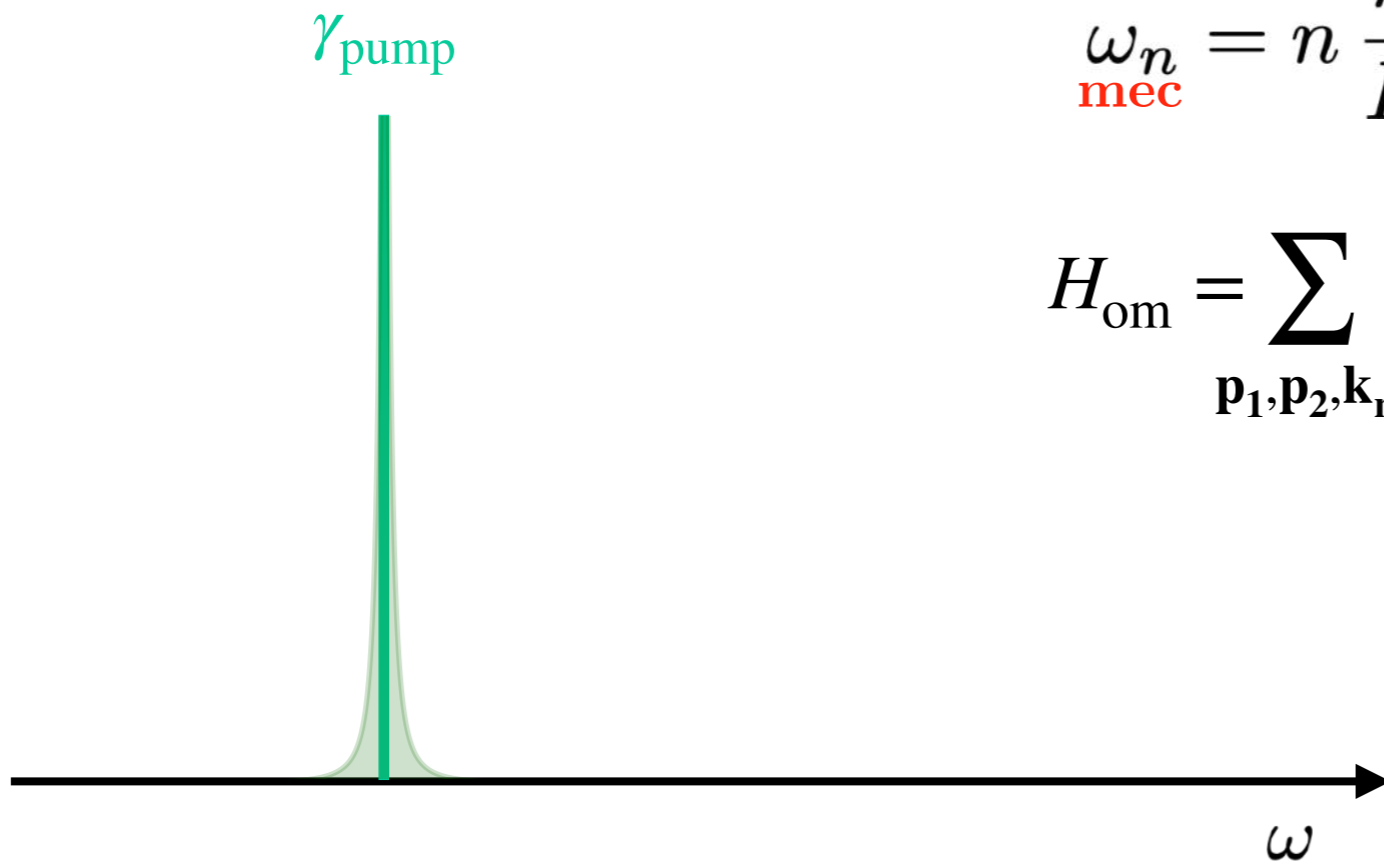
$$p_\phi = 2p_\gamma$$

$$\Omega_m = 2c_s \omega_{\text{opt}}$$

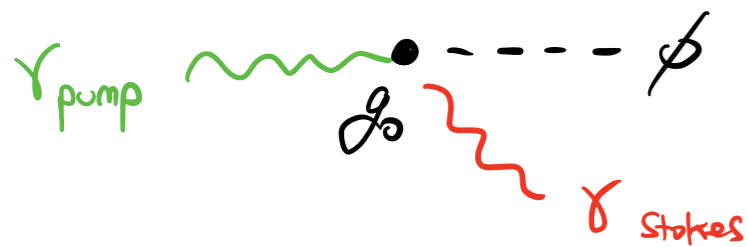


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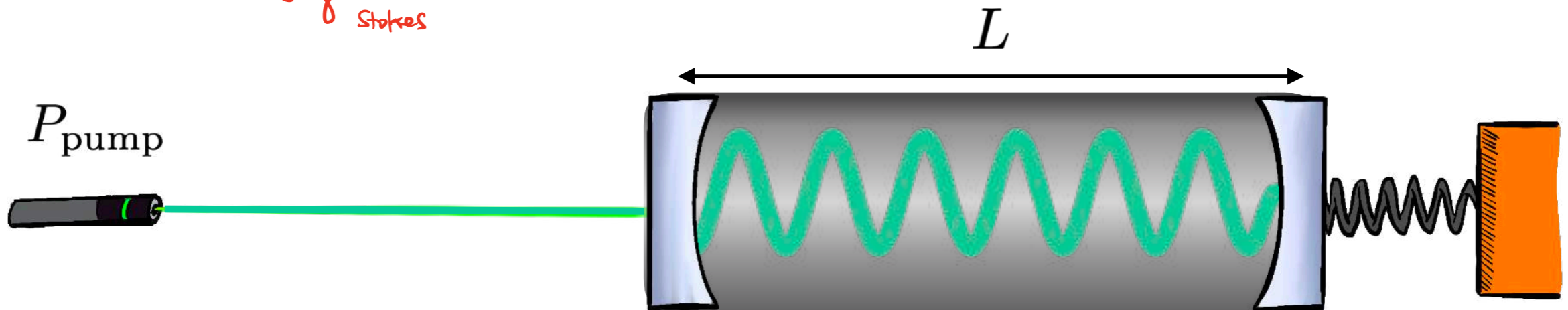


Standard Optomechanics



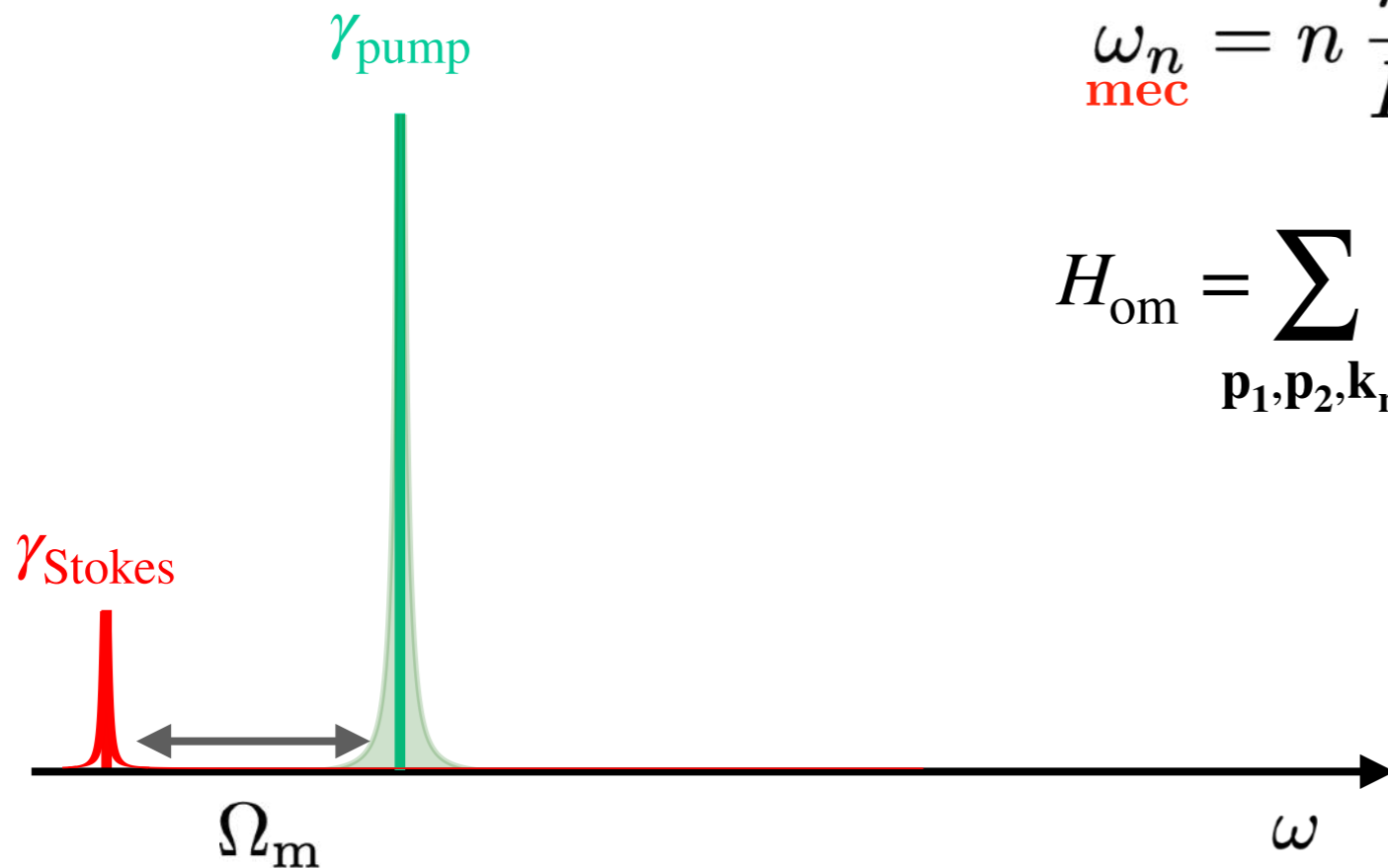
$$p_\phi = 2p_\gamma$$

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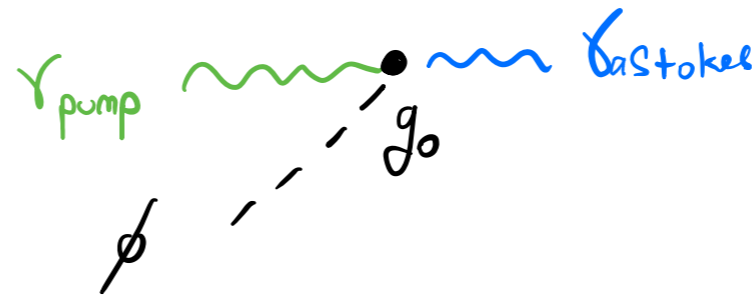
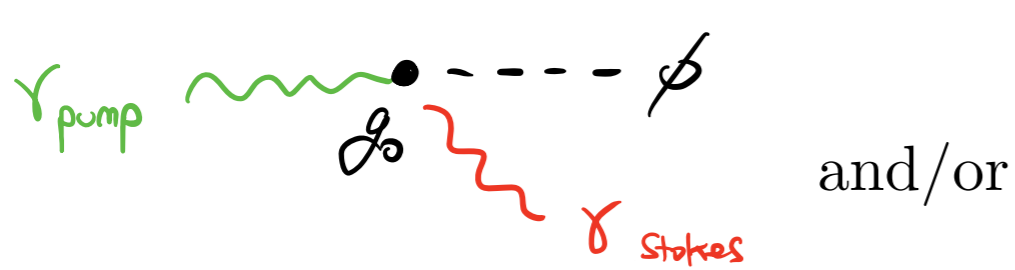


$$\omega_{\text{mec } n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger + \dots \right)$$

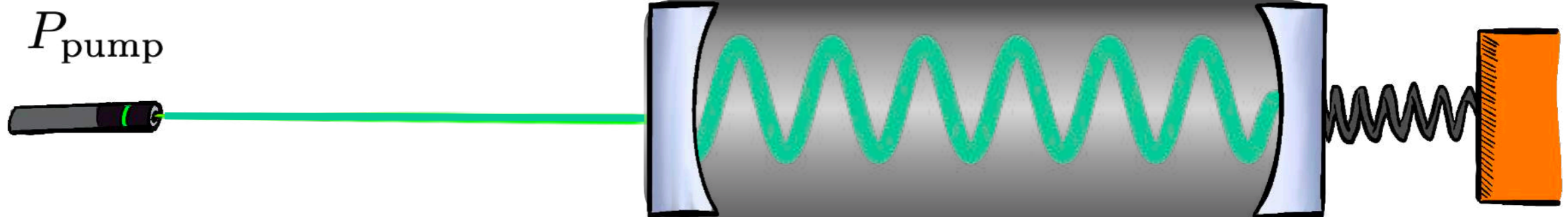


Standard Optomechanics



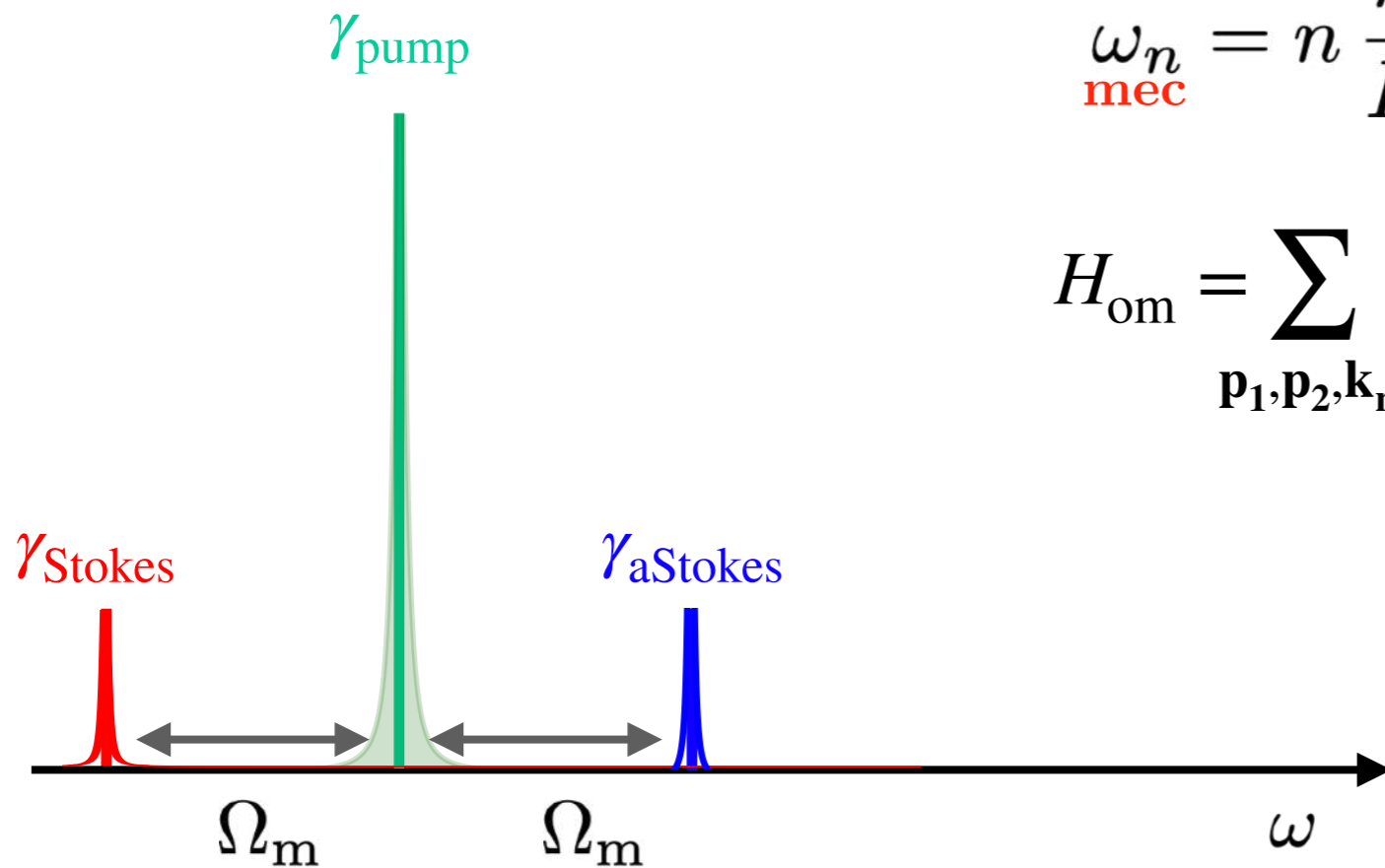
$$p_\phi = 2p_\gamma$$

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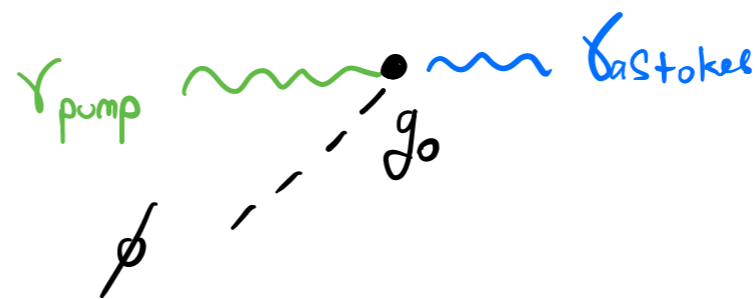
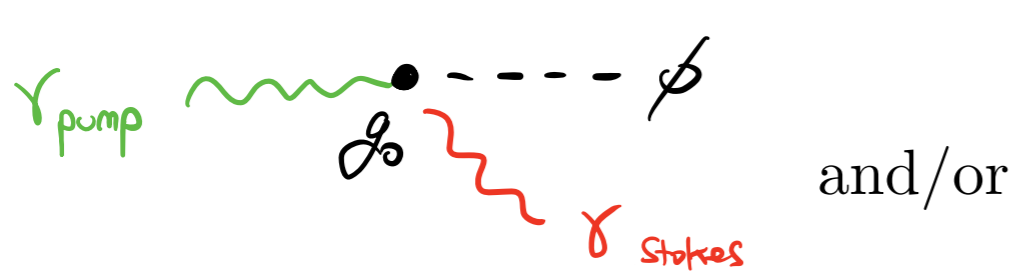


$$\omega_{\text{mec } n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger + a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m} \right)$$

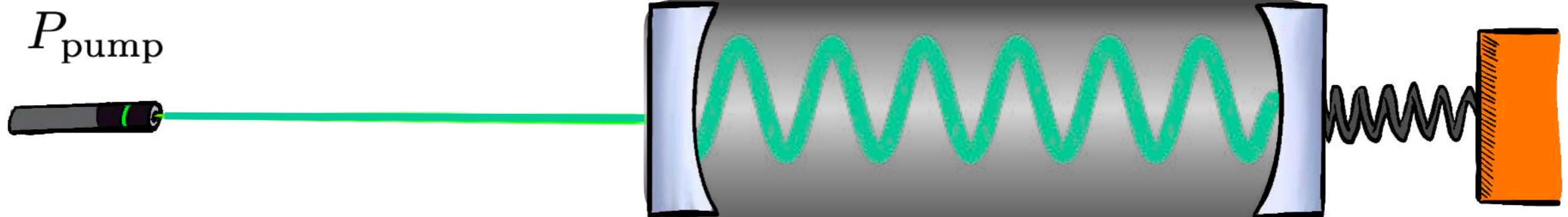


Standard Optomechanics



$$p_\phi = 2p_\gamma$$

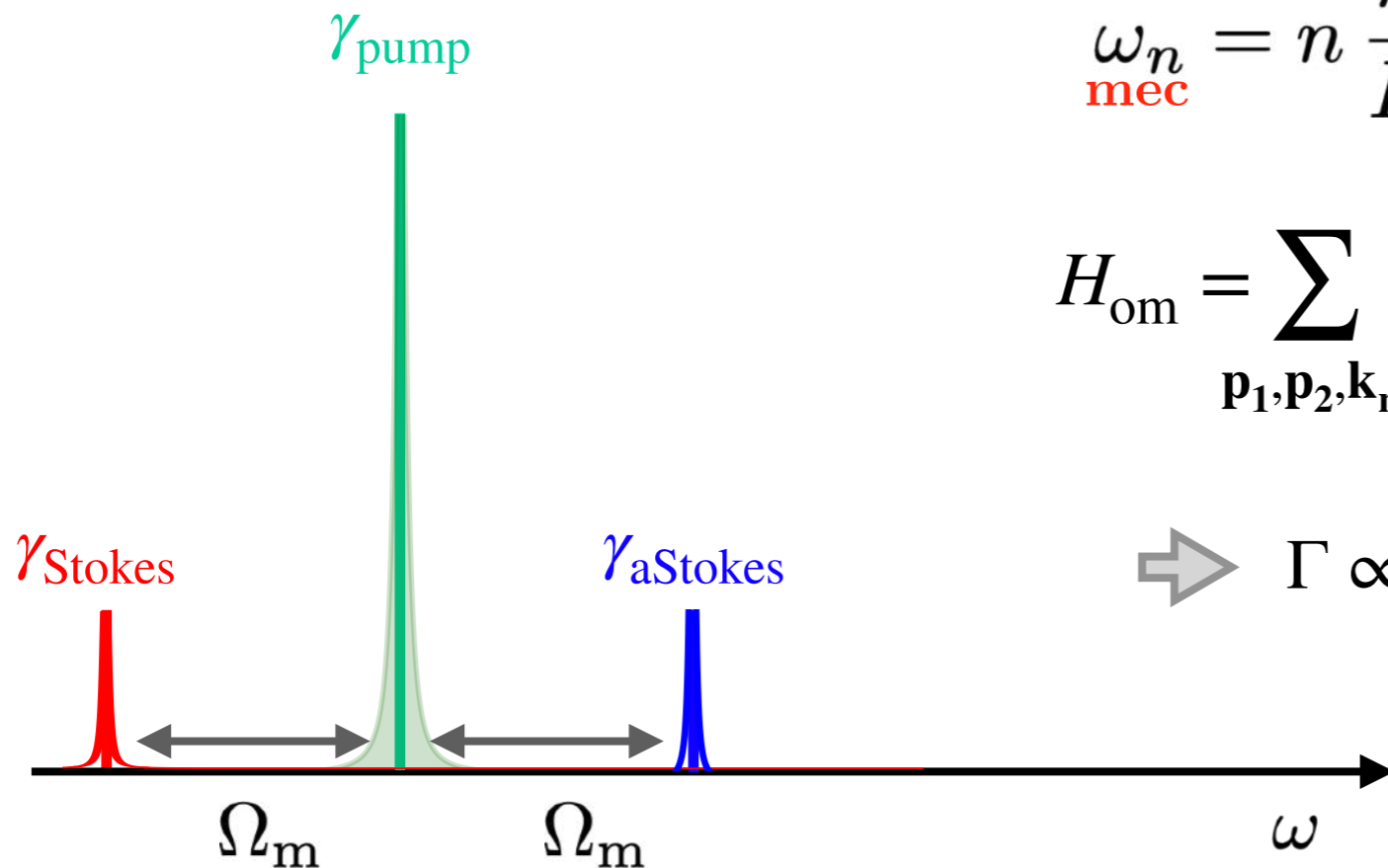
$$\Omega_m = 2c_s \omega_{\text{opt}}$$



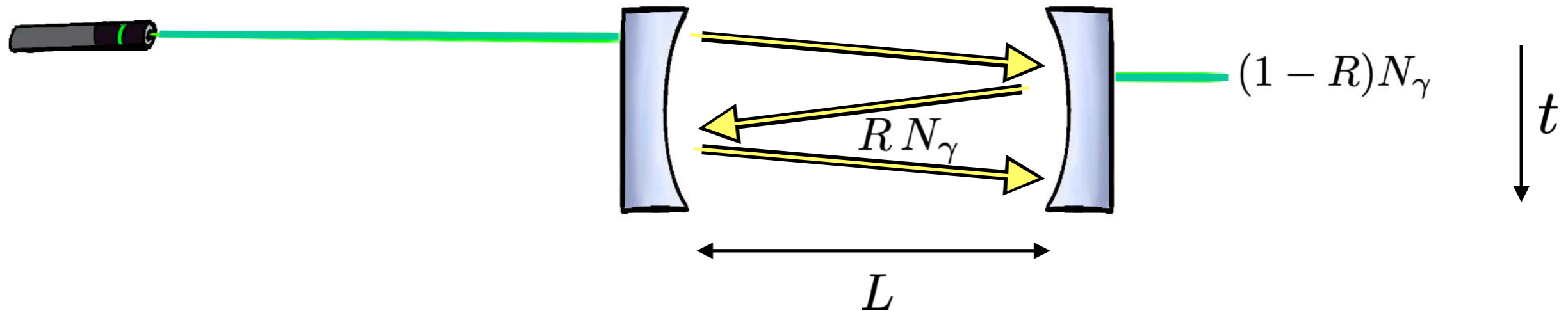
$$\omega_{\text{mec}, n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

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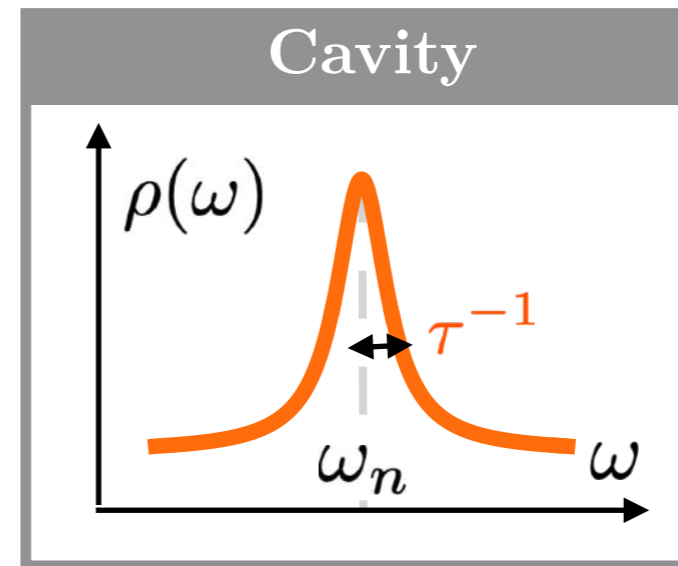
$$\Rightarrow \Gamma \propto |g_0|^2 N_{\gamma, \text{pump}}^{\text{circ}} [\Delta_{\text{pump}}]$$



Standard Optomechanics



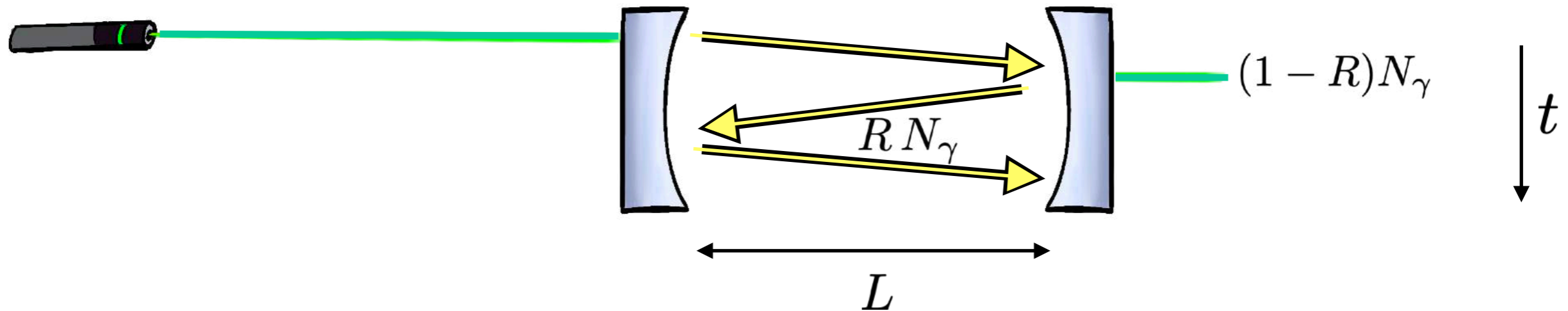
$$\frac{dN_\gamma}{dt} \simeq \frac{\Delta N_\gamma}{L/c} = \frac{c(1-R)}{L} N_\gamma \quad \Rightarrow \quad \tau_\gamma^{-1} \equiv \kappa \simeq \frac{c}{(1-R)^{-1}L}$$



\mathcal{F}_{opt}

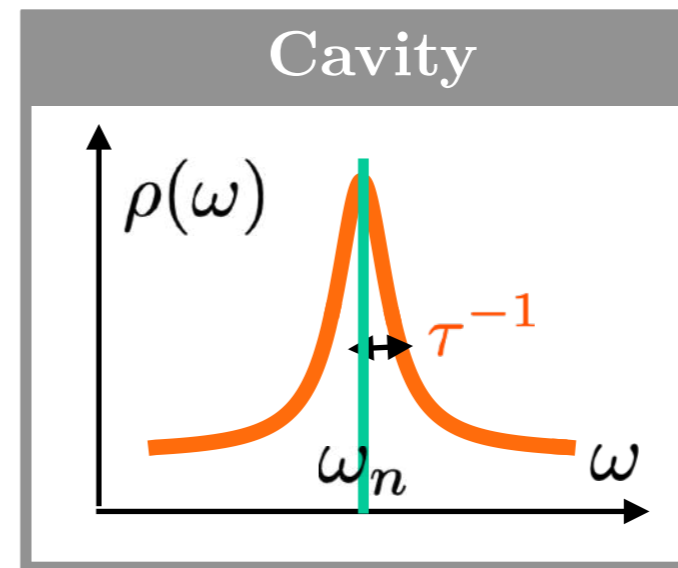
$$\rho(\omega) = \sum_i \delta(\omega - \omega_i) = \sum_n \frac{1}{2\pi} \int dt e^{i(\omega - \omega_n)t} e^{-t/(2\tau)} = \sum_n \frac{\tau^{-1}/2}{(\omega - \omega_n)^2 + (\tau^{-1}/2)^2}$$

Standard Optomechanics



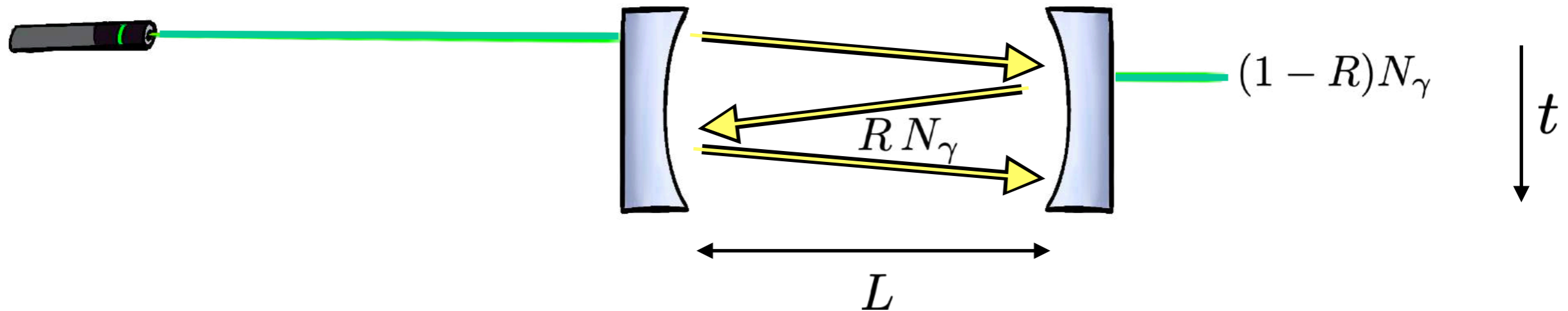
$$\frac{dN_\gamma}{dt} \simeq \frac{\Delta N_\gamma}{L/c} = \frac{c(1 - R)}{L} N_\gamma \quad \Rightarrow \quad \tau_\gamma^{-1} \equiv \kappa \simeq \frac{c}{(1 - R)^{-1} L}$$

$$N_{\gamma,L}^{\text{circ}} \sim \frac{4P_L \tau}{\omega_L}$$



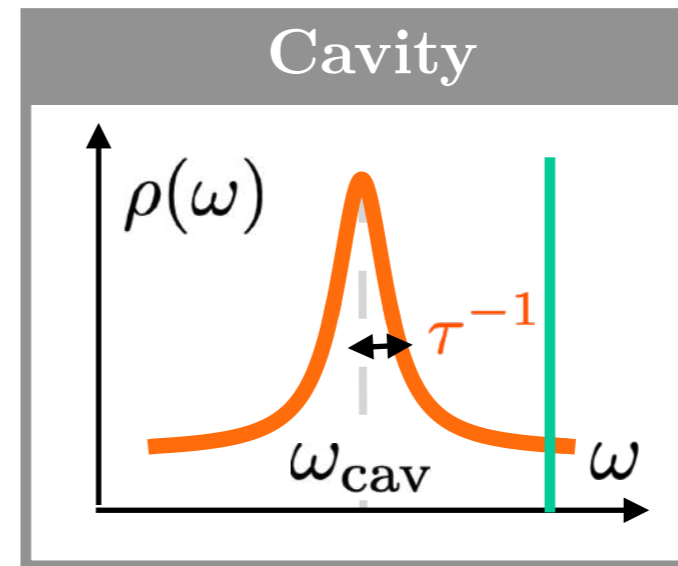
$$\rho(\omega) = \sum_i \delta(\omega - \omega_i) = \sum_n \frac{1}{2\pi} \int dt e^{i(\omega - \omega_n)t} e^{-t/(2\tau)} = \sum_n \frac{\tau^{-1}/2}{(\omega - \omega_n)^2 + (\tau^{-1}/2)^2}$$

Standard Optomechanics



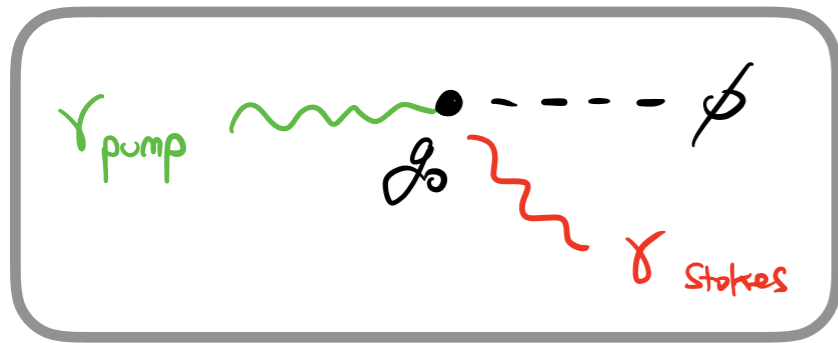
$$\frac{dN_\gamma}{dt} \simeq \frac{\Delta N_\gamma}{L/c} = \frac{c(1-R)}{L} N_\gamma \quad \Rightarrow \quad \tau_\gamma^{-1} \equiv \kappa \simeq \frac{c}{(1-R)^{-1}L}$$

$$N_{\gamma,L}^{\text{circ}} \sim \frac{4P_L \tau}{\omega_L} \frac{(\tau^{-1}/2)^2}{\Delta_L^2 + (\tau^{-1}/2)^2}$$



$$\rho(\omega) = \sum_i \delta(\omega - \omega_i) = \sum_n \frac{1}{2\pi} \int dt e^{i(\omega - \omega_n)t} e^{-t/(2\tau)} = \sum_n \frac{\tau^{-1}/2}{(\omega - \omega_n)^2 + (\tau^{-1}/2)^2}$$

Standard Optomechanics



$$p_\phi = 2p_\gamma$$

$$\Omega_m = 2c_s \omega_{\text{opt}}$$

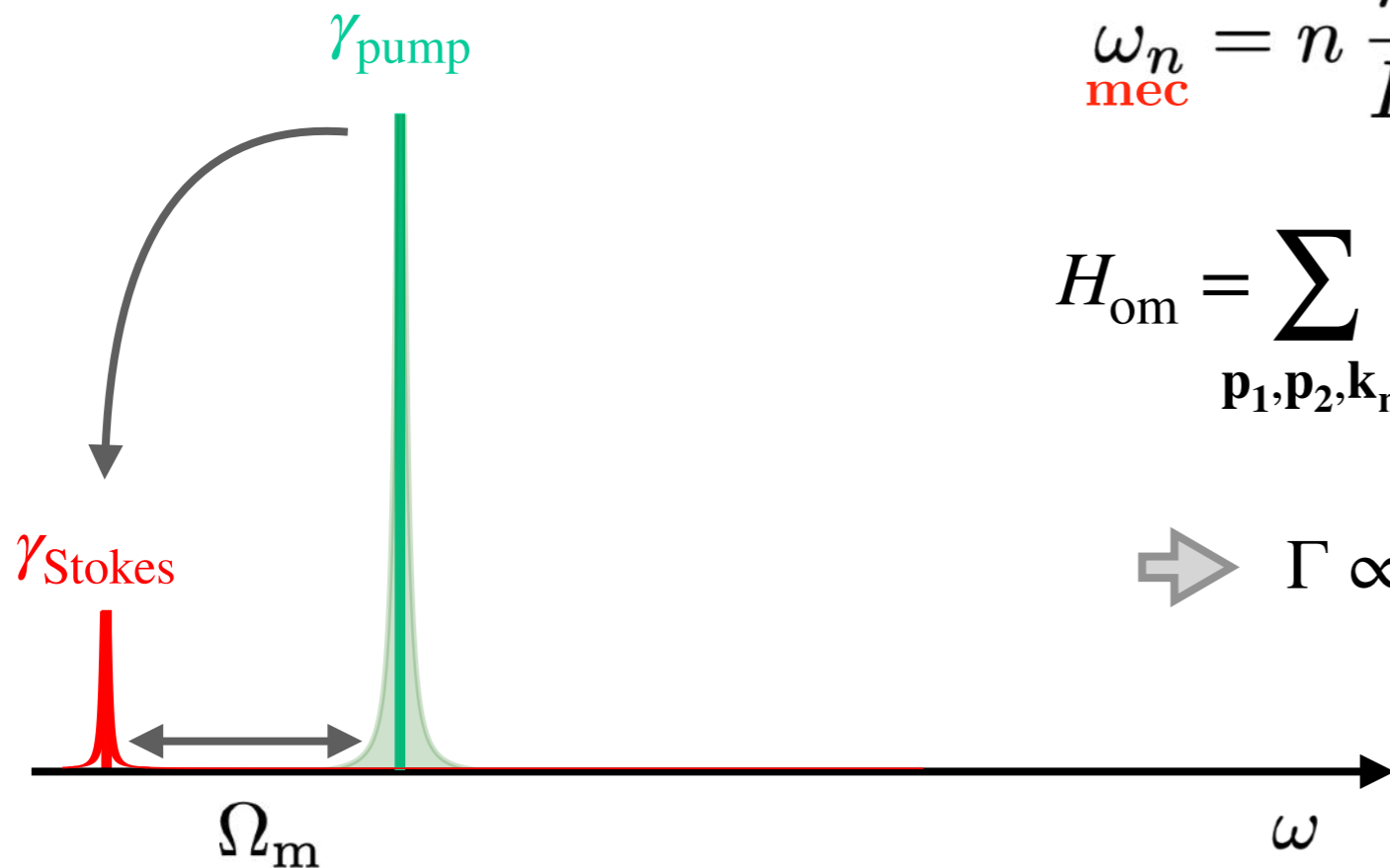
P_{pump}



$$\omega_{\text{mec},n} = n \frac{\pi}{L} c_s, \quad n \in \mathbb{Z}$$

$$H_{\text{om}} = \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0 \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger \right)$$

$$\Rightarrow \Gamma \propto |g_0|^2 N_{\gamma, \text{pump}}$$



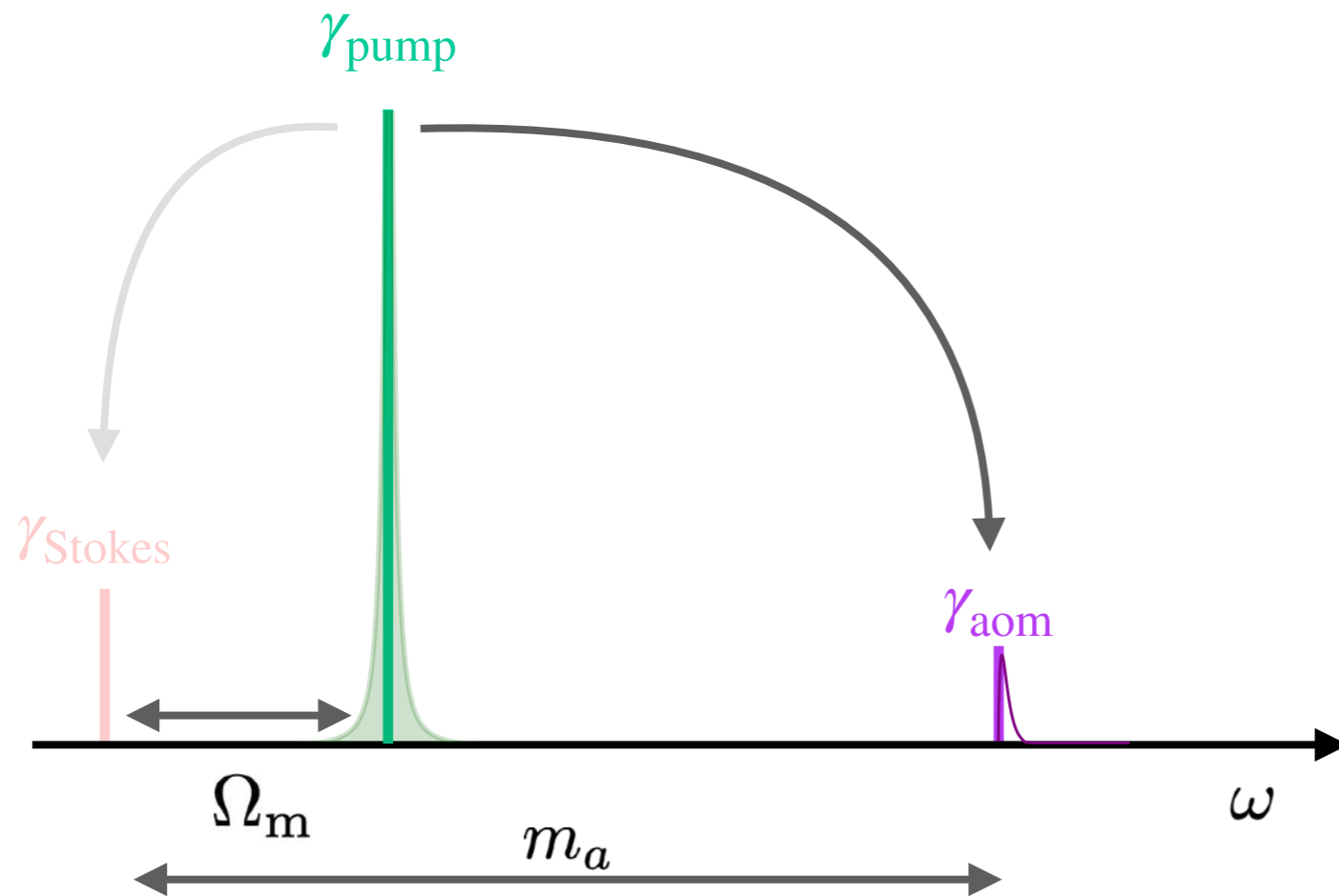
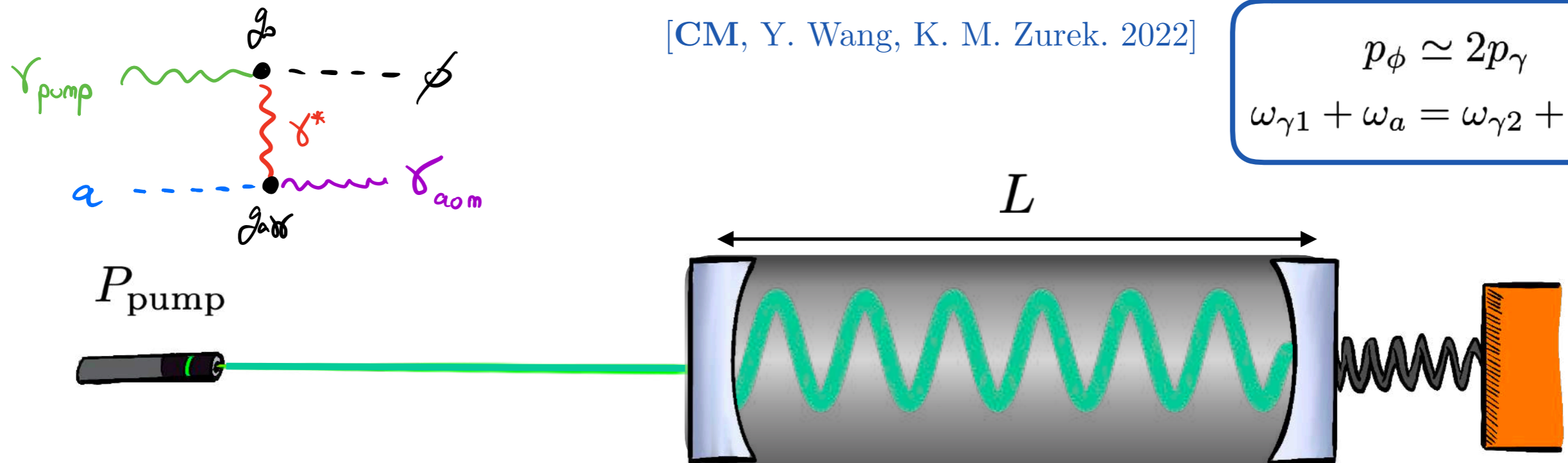
[Kashkanova et al., 2017]
[Reningner et al., 2017]

Standard Axioptomechanics

[CM, Y. Wang, K. M. Zurek. 2022]

$$p_\phi \simeq 2p_\gamma$$

$$\omega_{\gamma 1} + \omega_a = \omega_{\gamma 2} + \omega_\phi$$

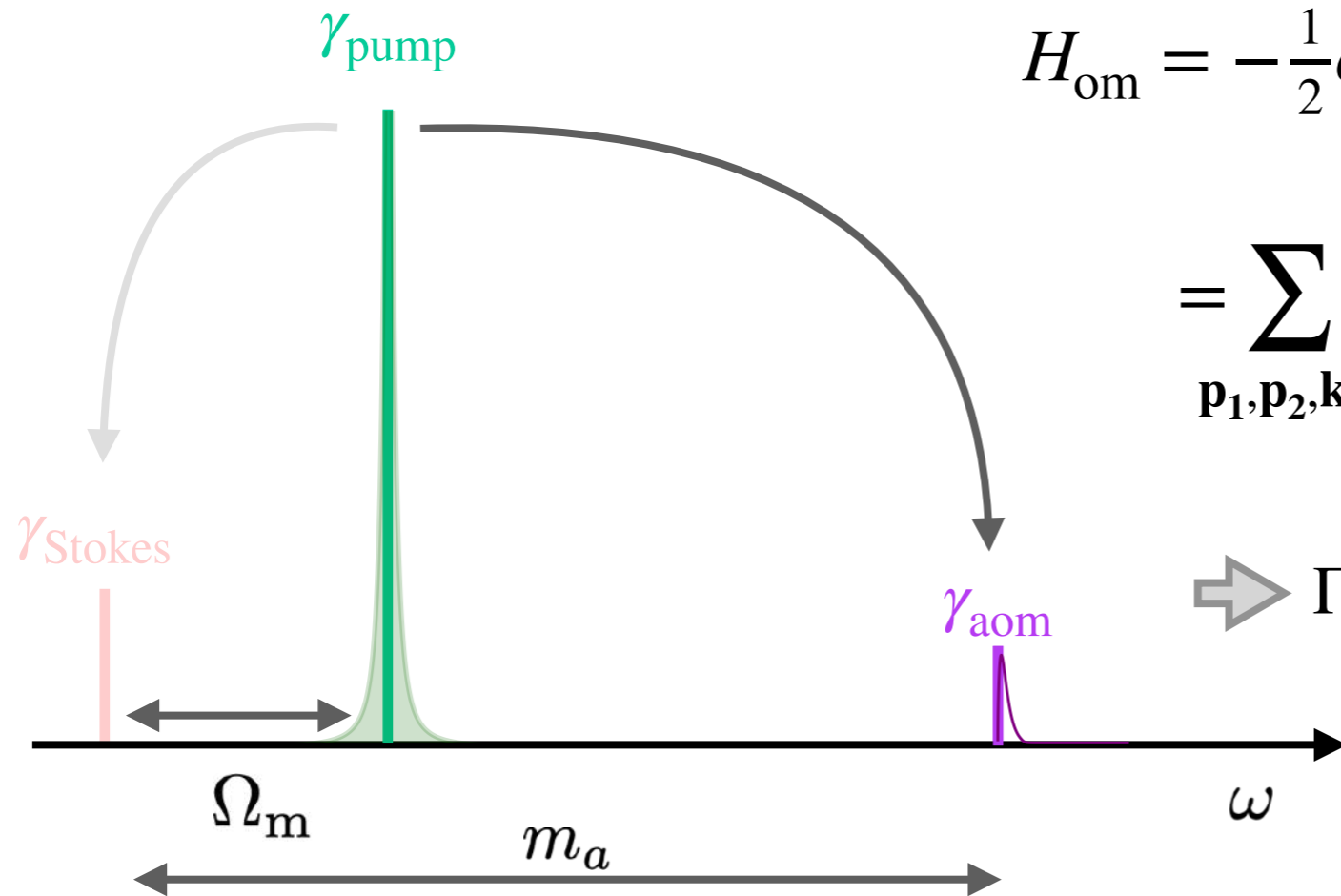
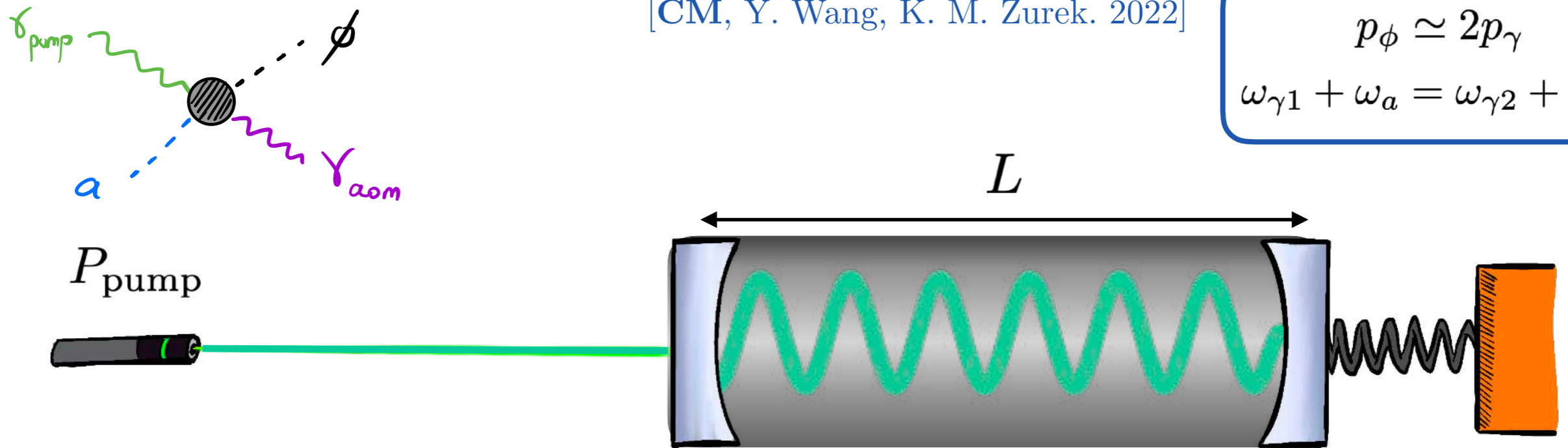


Standard Axioptomechanics

[CM, Y. Wang, K. M. Zurek. 2022]

$$p_\phi \simeq 2p_\gamma$$

$$\omega_{\gamma 1} + \omega_a = \omega_{\gamma 2} + \omega_\phi$$



$$H_{\text{om}} = -\frac{1}{2} \alpha g_{a\gamma\gamma} \int d^3\mathbf{r} a(\mathbf{r}) n(\mathbf{r}) \mathbf{E}(\mathbf{r}) \cdot \mathbf{B}(\mathbf{r})$$

$$= \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0^{(a)} \left(g_{a\gamma\gamma} \frac{\sqrt{2\rho_a}}{m_a} \right) \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger \right)$$

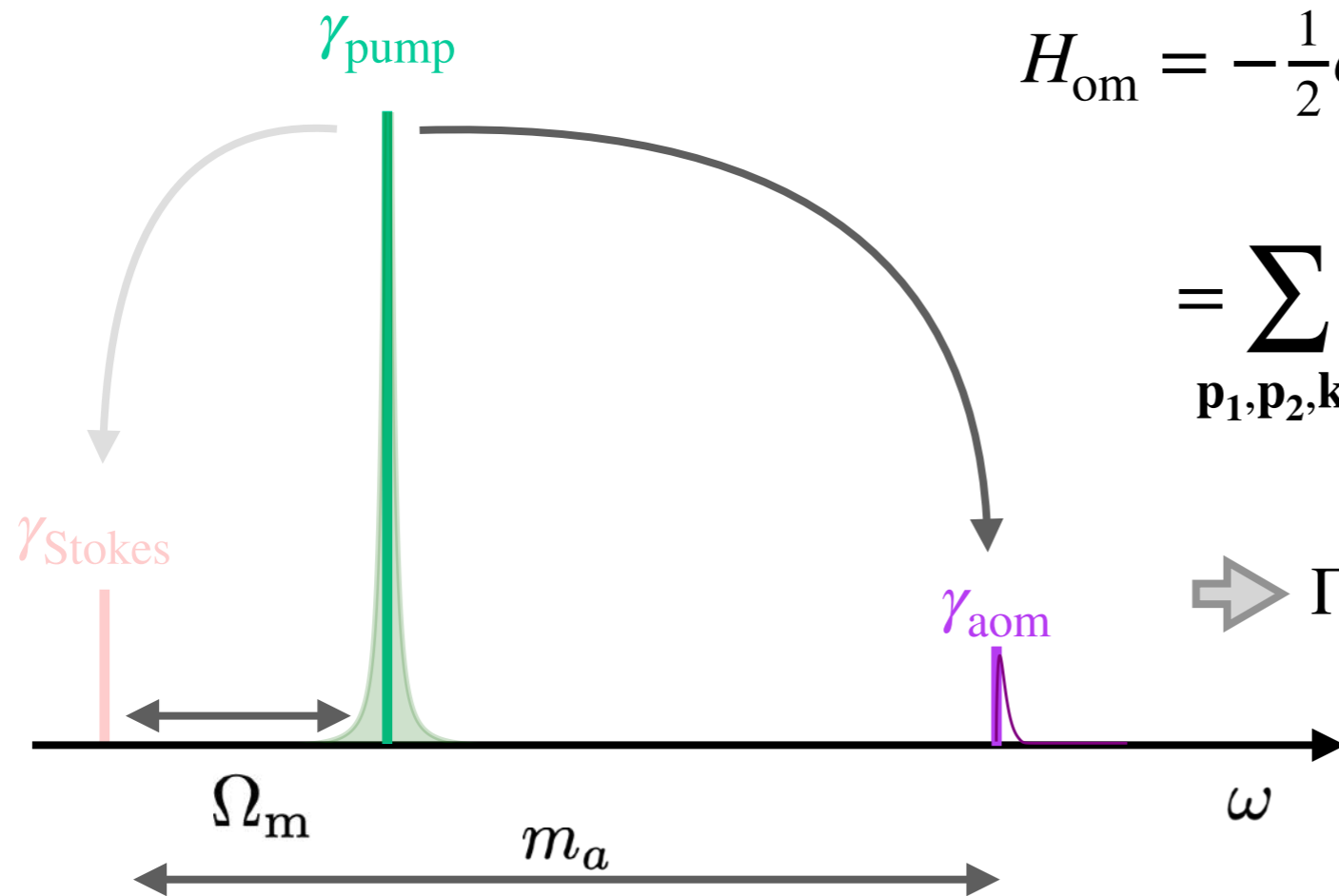
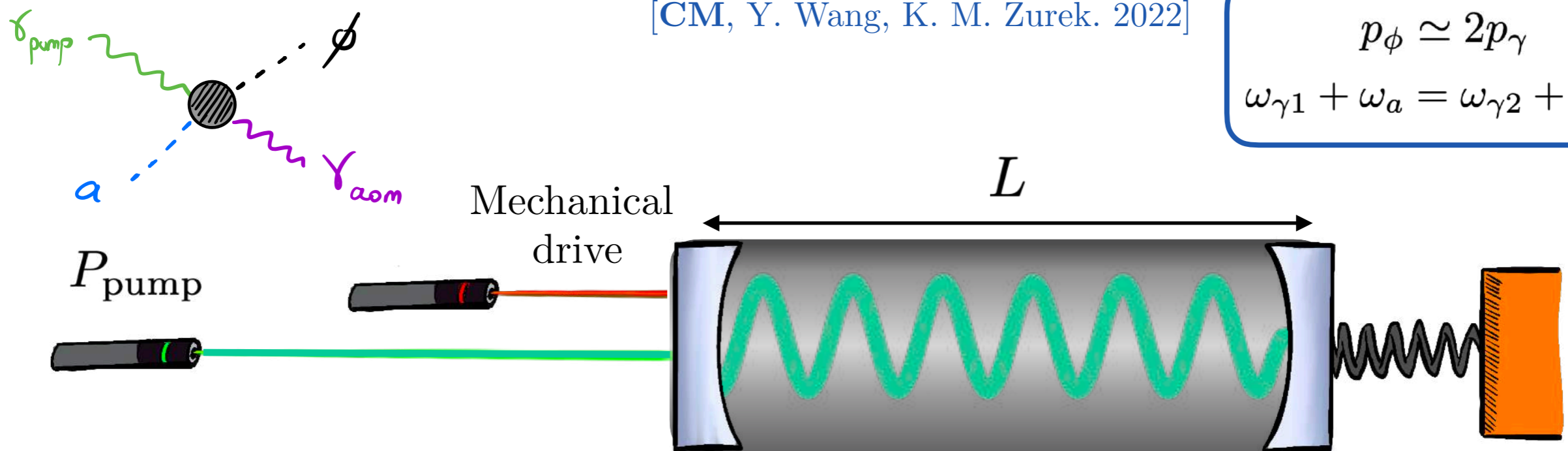
$$\Rightarrow \Gamma \propto |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \times N_{\gamma, \text{pump}} \sim 10^{-22} \text{ for QCD axion}$$

Coherent enhancement: Phonons

[CM, Y. Wang, K. M. Zurek. 2022]

$$p_\phi \simeq 2p_\gamma$$

$$\omega_{\gamma 1} + \omega_a = \omega_{\gamma 2} + \omega_\phi$$



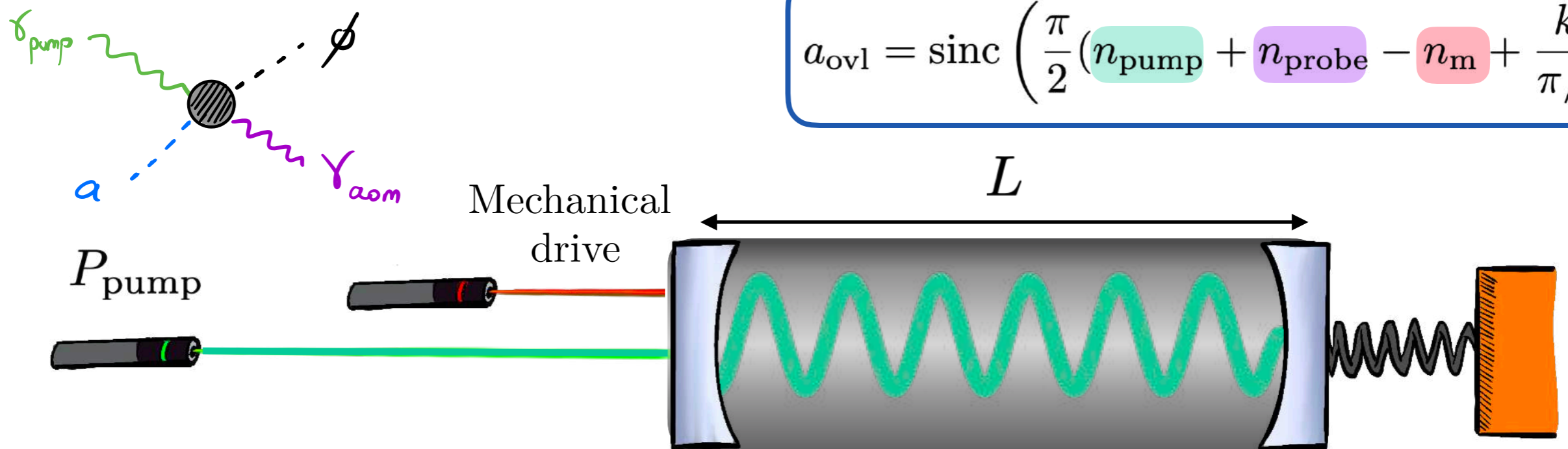
$$H_{\text{om}} = -\frac{1}{2}\alpha g_{a\gamma\gamma} \int d^3\mathbf{r} a(\mathbf{r}) n(\mathbf{r}) \mathbf{E}(\mathbf{r}) \cdot \mathbf{B}(\mathbf{r})$$

$$= \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0^{(a)} \left(g_{a\gamma\gamma} \frac{\sqrt{2\rho_a}}{m_a} \right) \left(a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger \right)$$

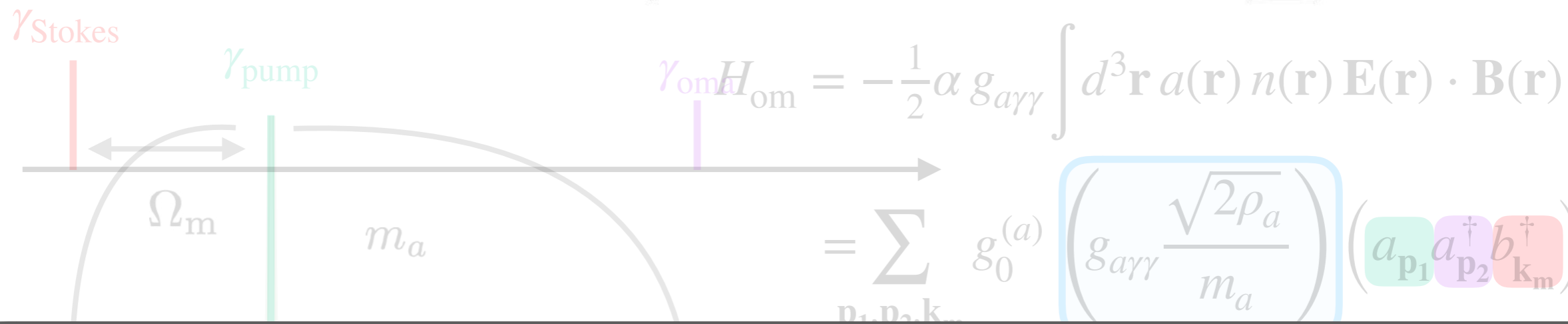
$$\Rightarrow \Gamma \propto |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \times N_{\gamma, \text{pump}} N_\phi^{\text{circ}} [\Delta_m]$$

$\sim 10^{-22}$ for QCD axion

Axioptomechanics: Rates



$$a_{\text{ovl}} = \text{sinc} \left(\frac{\pi}{2} (n_{\text{pump}} + n_{\text{probe}} - n_m + \frac{k_a}{\pi/L}) \right)$$



$$H_{\text{om}} = -\frac{1}{2} \alpha g_{a\gamma\gamma} \int d^3\mathbf{r} a(\mathbf{r}) n(\mathbf{r}) \mathbf{E}(\mathbf{r}) \cdot \mathbf{B}(\mathbf{r})$$

$$= \sum_{\mathbf{p}_1, \mathbf{p}_2, \mathbf{k}_m} g_0^{(a)} \left(g_{a\gamma\gamma} \frac{\sqrt{2\rho_a}}{m_a} \right) (a_{\mathbf{p}_1} a_{\mathbf{p}_2}^\dagger b_{\mathbf{k}_m}^\dagger)$$

Phonon populated

$$\Gamma = (2\pi) |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \int d\omega_{\gamma_{\text{aom}}} B_{m_a}(\omega_{\gamma_{\text{aom}}} + \Omega_m - \omega_{\text{pump}}) L(\omega_{\gamma_{\text{aom}}} - \omega_{\text{res}}, \kappa) \times N_{\gamma, \text{pump}} N_{\phi}^{\text{circ}} [\Delta_m]$$



[CM, Y. Wang, K. M. Zurek. 2022]

Axioptomechanics: Sensitivity

$$\text{SNR} = \frac{\Gamma_{\text{sig}} (t_{\text{int}}/\tau_a)}{\Gamma_{\text{back}}} > 3 \Rightarrow g_{a\gamma\gamma} > f(m_a, \text{cavity, lasers, material})$$

Phonon populated

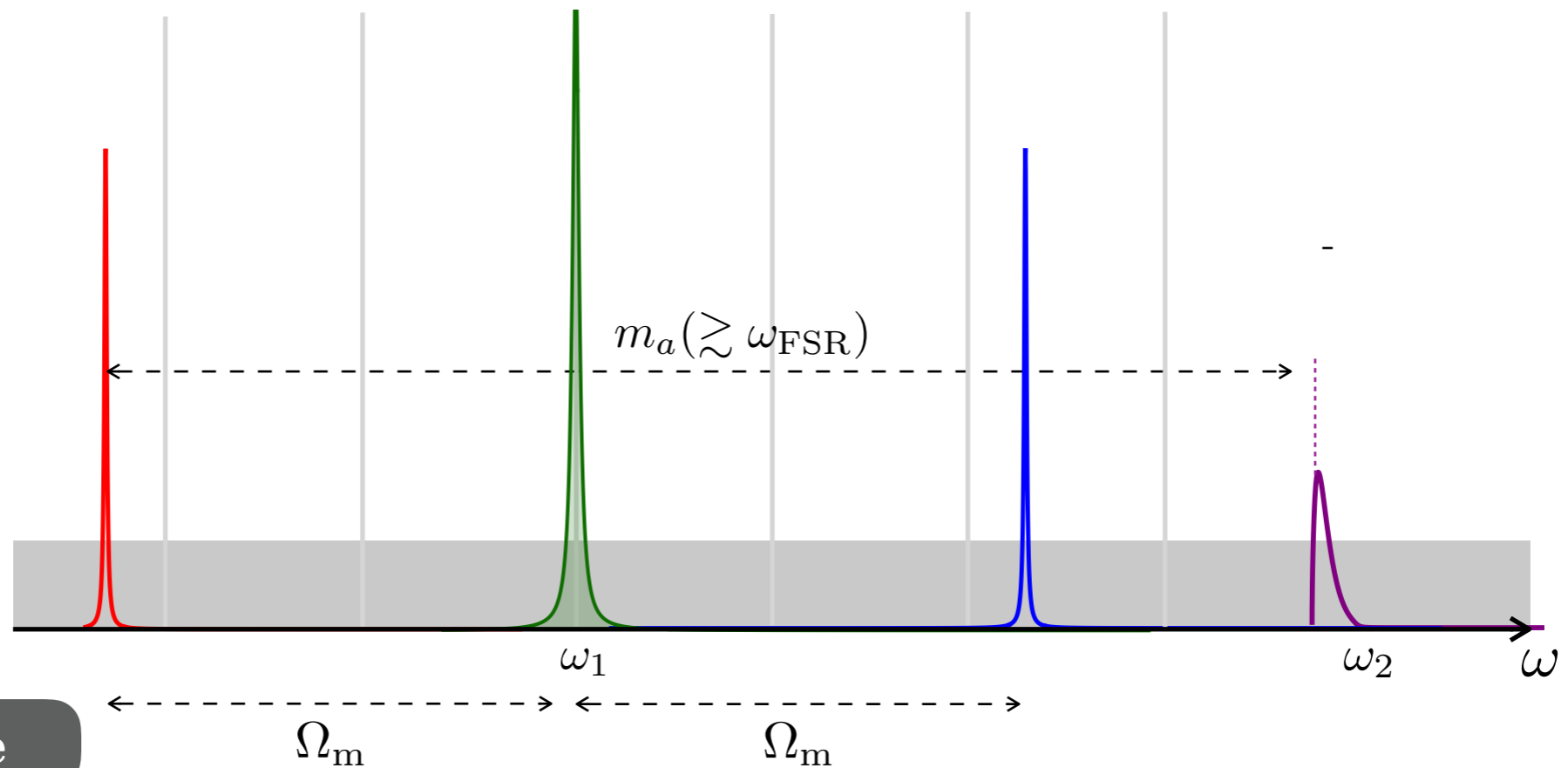
$$\Rightarrow \Gamma = (2\pi) |g_0^{(a)}|^2 \left(g_{a\gamma\gamma}^2 \frac{\rho_a}{m_a^2} \right) \int d\omega_{\gamma_{\text{aom}}} B_{m_a}(\omega_{\gamma_{\text{aom}}} + \Omega_m - \omega_{\text{pump}}) L(\omega_{\gamma_{\text{aom}}} - \omega_{\text{res}}, \kappa) \times N_{\gamma, \text{pump}} N_{\phi}^{\text{circ}} [\Delta_m]$$



[CM, Y. Wang, K. M. Zurek. 2022]

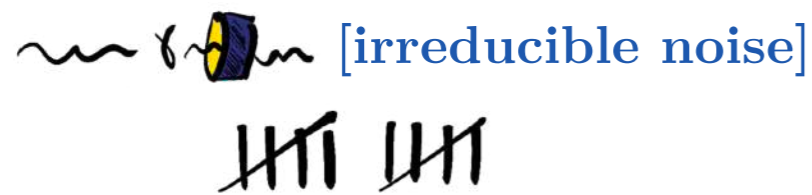
Axioptomechanics: Sensitivity

$$\text{SNR} = \frac{\Gamma_{\text{sig}} (t_{\text{int}}/\tau_a)}{\Gamma_{\text{back}}} > 3 \Rightarrow g_{a\gamma\gamma} > f(m_a, \text{cavity, lasers, material})$$



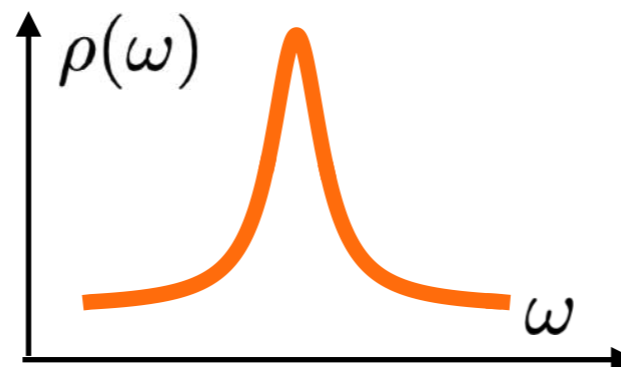
Sources of noise

Dark Count Rate

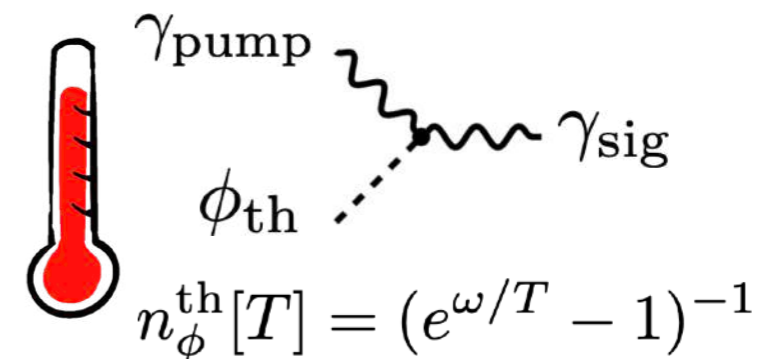


$$\text{SNR} = \frac{\Gamma_{\text{sig}}}{\Gamma_{\text{DCR}}} > 3$$

Laser frequency noise

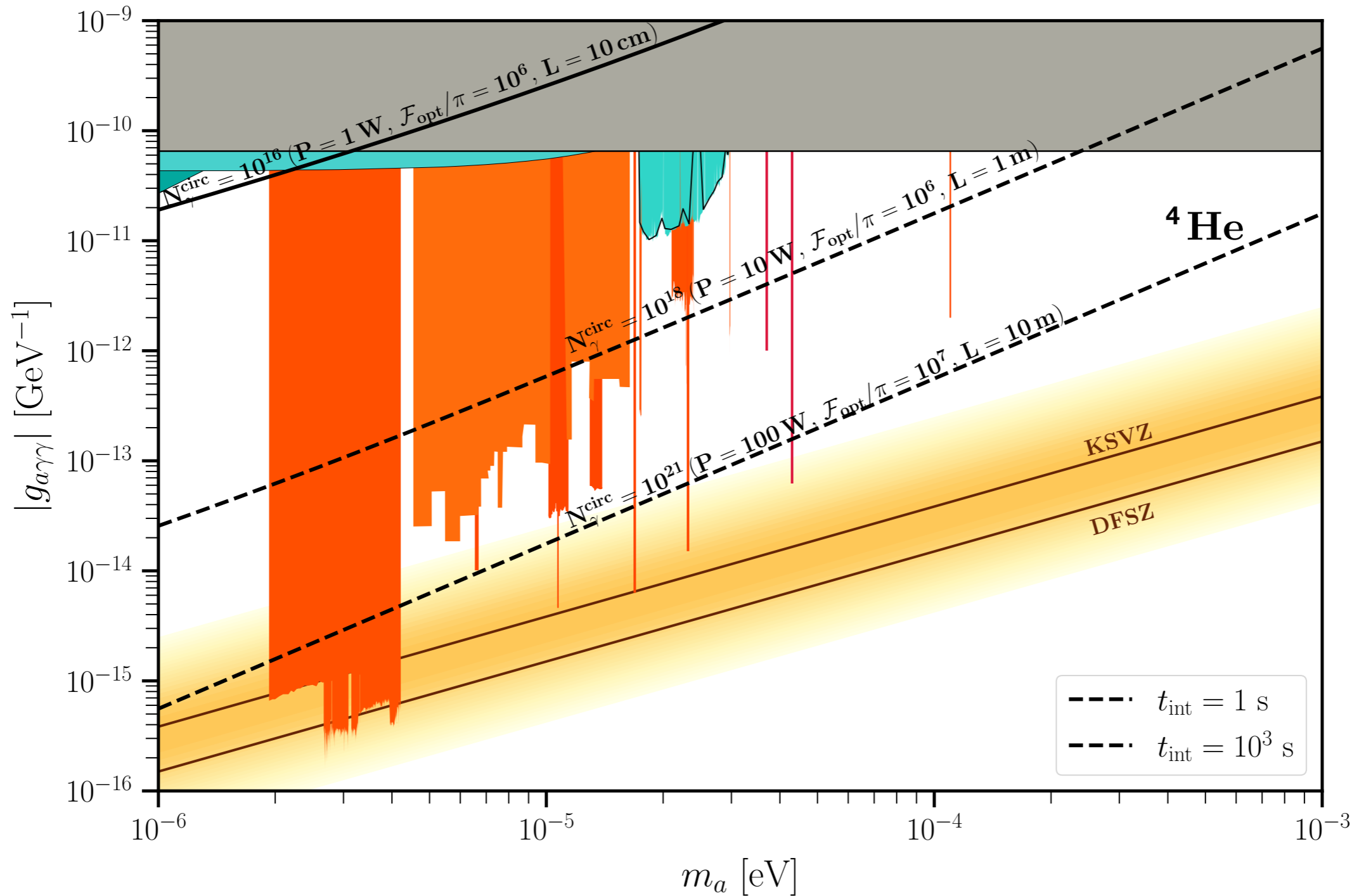


Thermal phonons



Curves: heavy axion regime

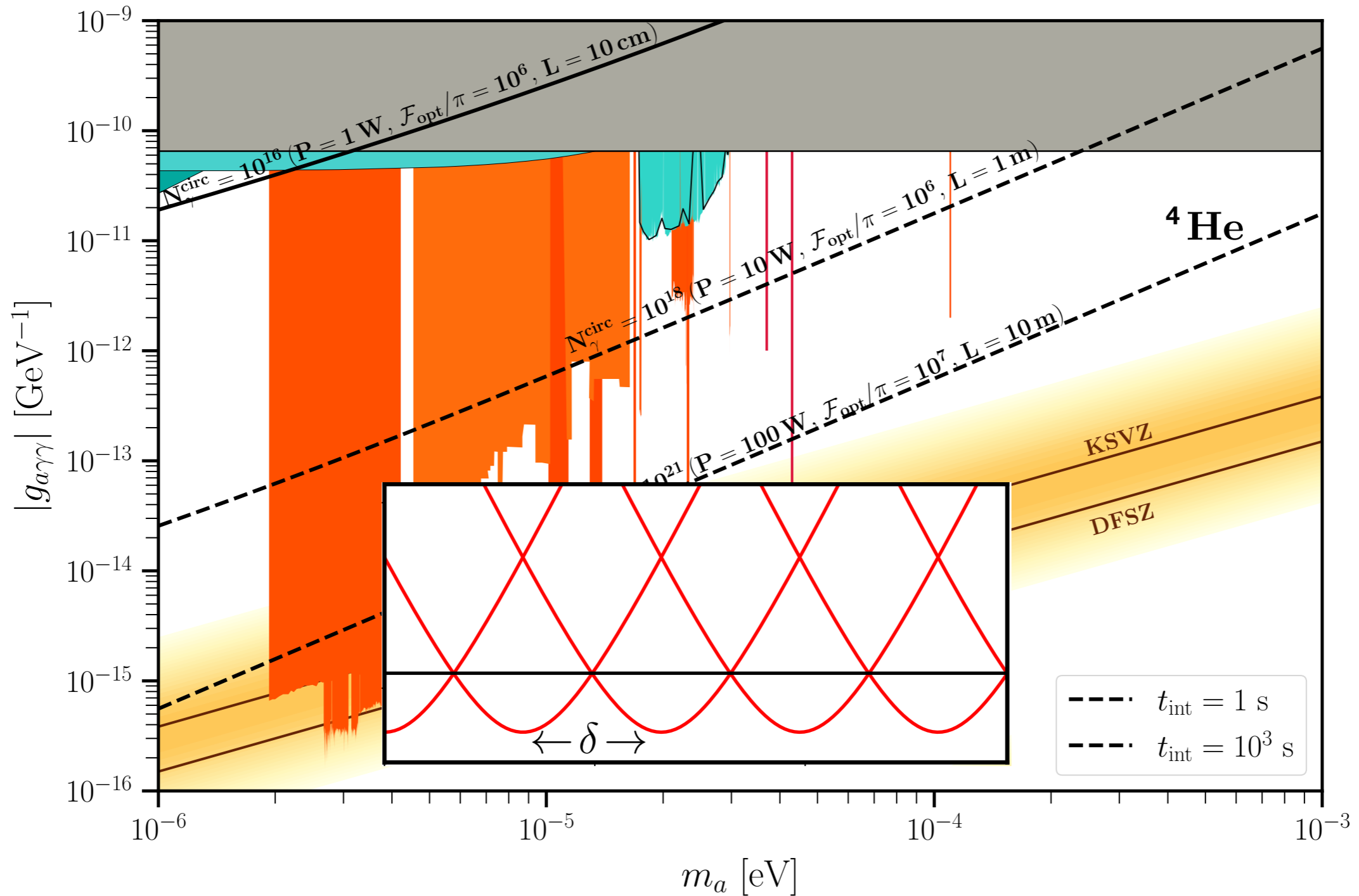
[CM, Y. Wang, K. M. Zurek. 2022]



$$g_{a\gamma\gamma}^{\phi\text{-pop}} \propto \frac{\epsilon_r + 2}{\epsilon_r - 1} \epsilon_r^{1/2} \frac{1}{\mathcal{F}_{\text{opt}}^{1/2}} \frac{1}{L^{1/2}} \frac{1}{\omega_{\text{opt}}^{1/2}} \frac{1}{P_{\text{pump}}^{1/2}} \frac{m_a^{3/2}}{\rho_a^{1/2}} \Gamma_{\text{DCR}}^{1/2}$$

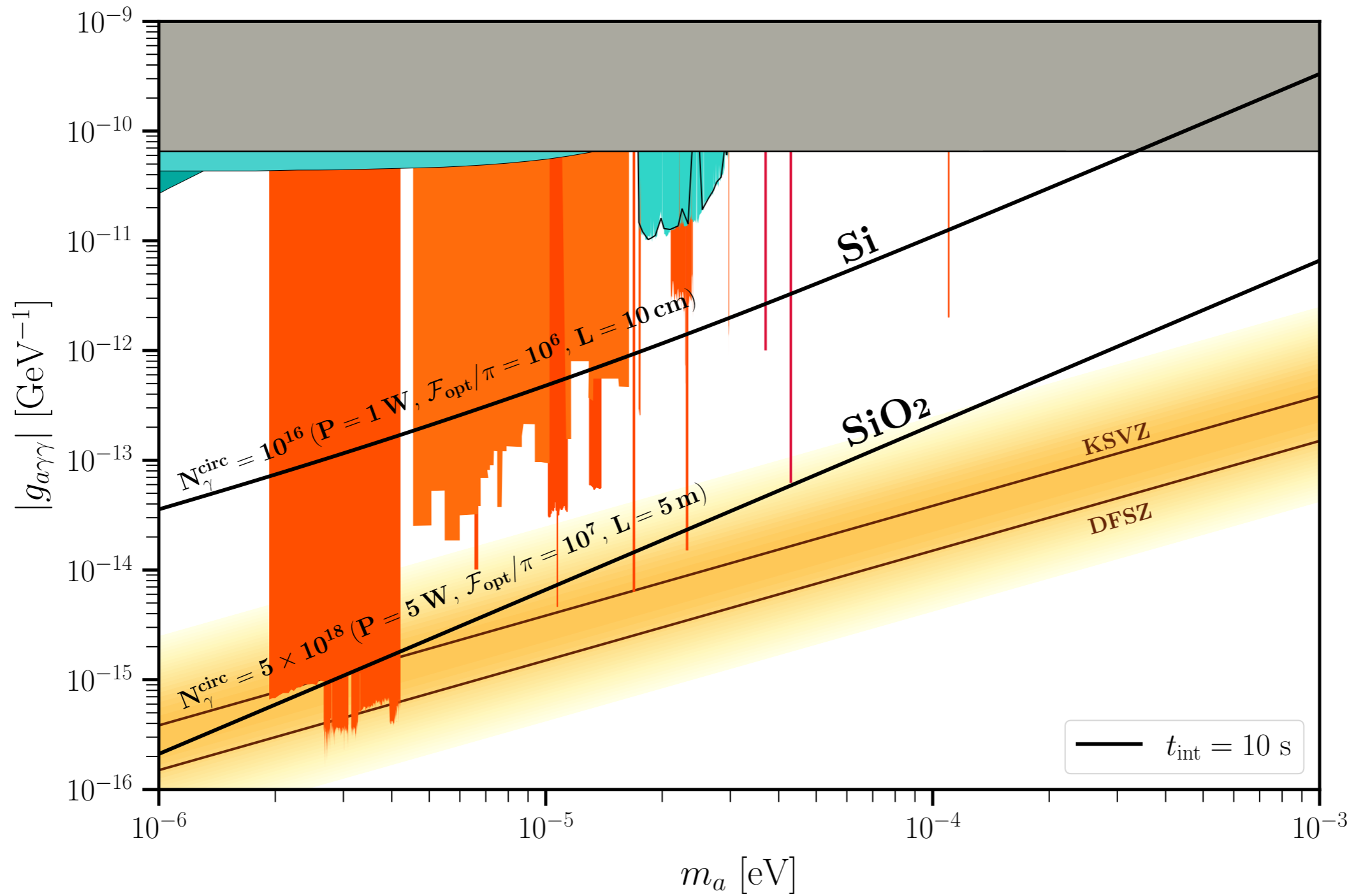
Curves: heavy axion regime

[CM, Y. Wang, K. M. Zurek. 2022]



$$g_{a\gamma\gamma}^{\phi\text{-pop}} \propto \frac{\epsilon_r + 2}{\epsilon_r - 1} \epsilon_r^{1/2} \frac{1}{\mathcal{F}_{\text{opt}}^{1/2}} \frac{1}{L^{1/2}} \frac{1}{\omega_{\text{opt}}^{1/2}} \frac{1}{P_{\text{pump}}^{1/2}} \frac{m_a^{3/2}}{\rho_a^{1/2}} \Gamma_{\text{DCR}}^{1/2}$$

Curves: heavy axion regime



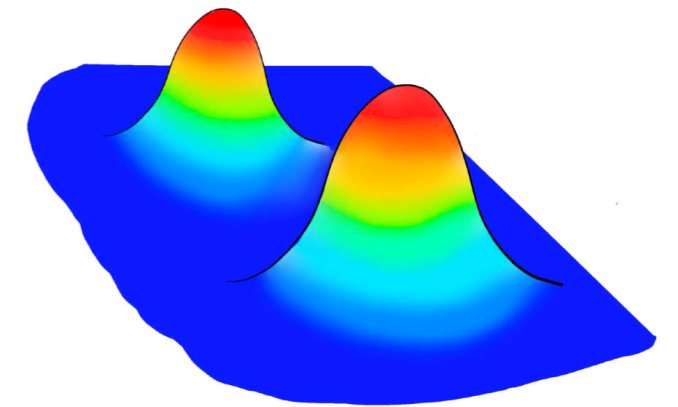
$$g_{a\gamma\gamma}^{\phi\text{-pop}} \propto \frac{\epsilon_r + 2}{\epsilon_r - 1} \epsilon_r^{1/2} \frac{1}{\mathcal{F}_{\text{opt}}^{1/2}} \frac{1}{L^{1/2}} \frac{1}{\omega_{\text{opt}}^{1/2}} \frac{1}{P_{\text{pump}}^{1/2}} \frac{m_a^{3/2}}{\rho_a^{1/2}} \Gamma_{\text{DCR}}^{1/2}$$

Conclusions

Importance of exploiting potential of existing /upcoming experiments to explore dark matter possibilities.

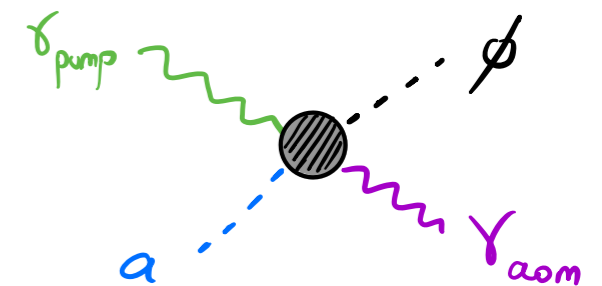
Atom Interferometers

- ⇒ Already (or will) exist!
- ⇒ No minimum energy deposition — decoherence
- ⇒ Coherent enhancement



Axioptomechanics

- ⇒ Decoupling length — axion mass: phonons!
- ⇒ ~ background-free experiment
- ⇒ Complementary to other axion searches



Thank you!