



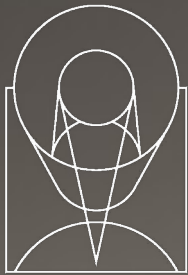
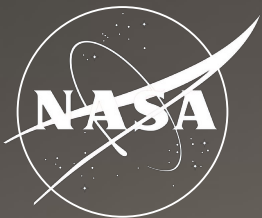
Stockholm  
University



PRINCETON  
UNIVERSITY

# Scintillating Methods to Detect Dark Matter from Nano to Astro Scales

CARLOS BLANCO



SPACE  
TELESCOPE  
SCIENCE  
INSTITUTE

# MW Dark Matter Halo

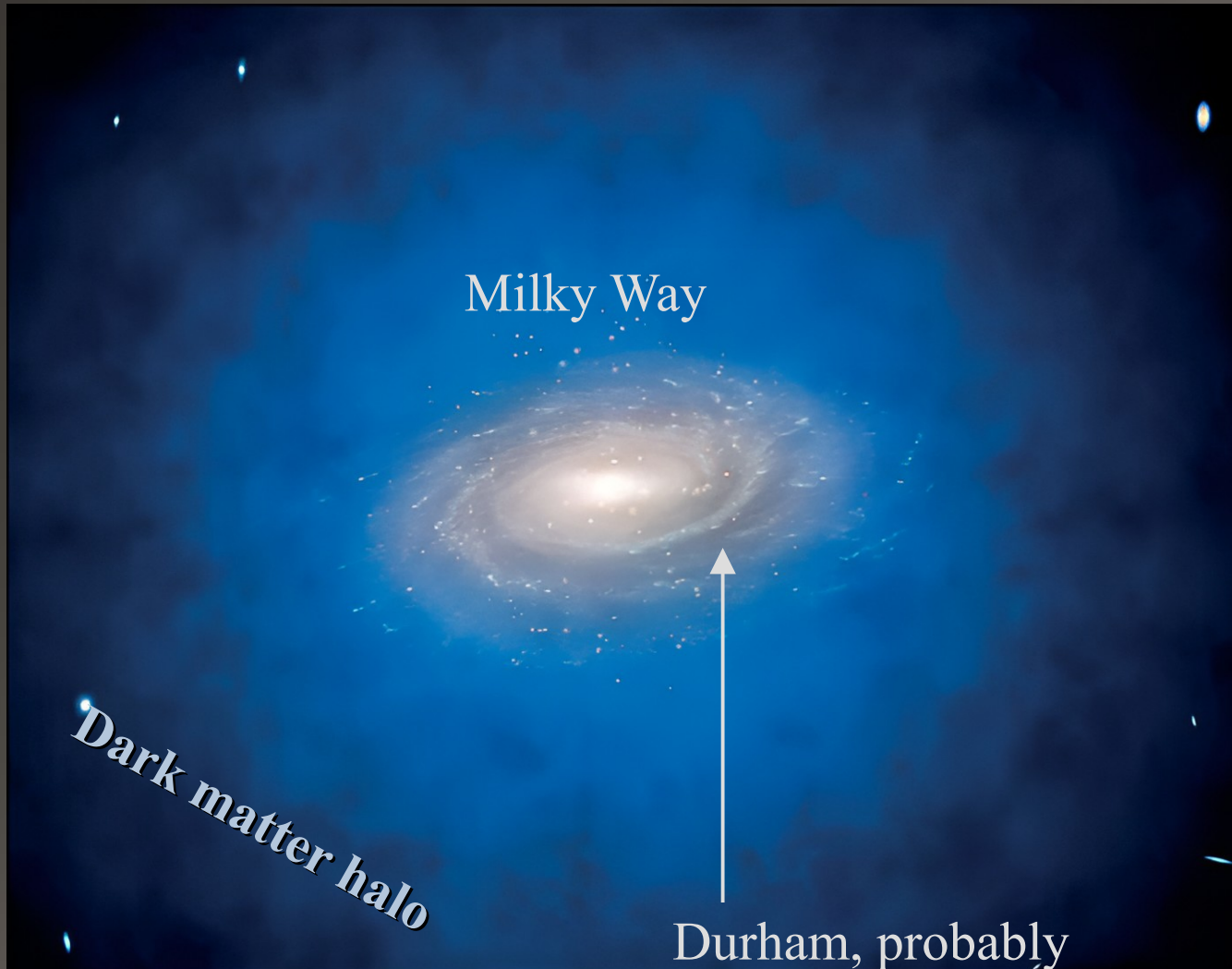


Image credit: ESO/L Calçada

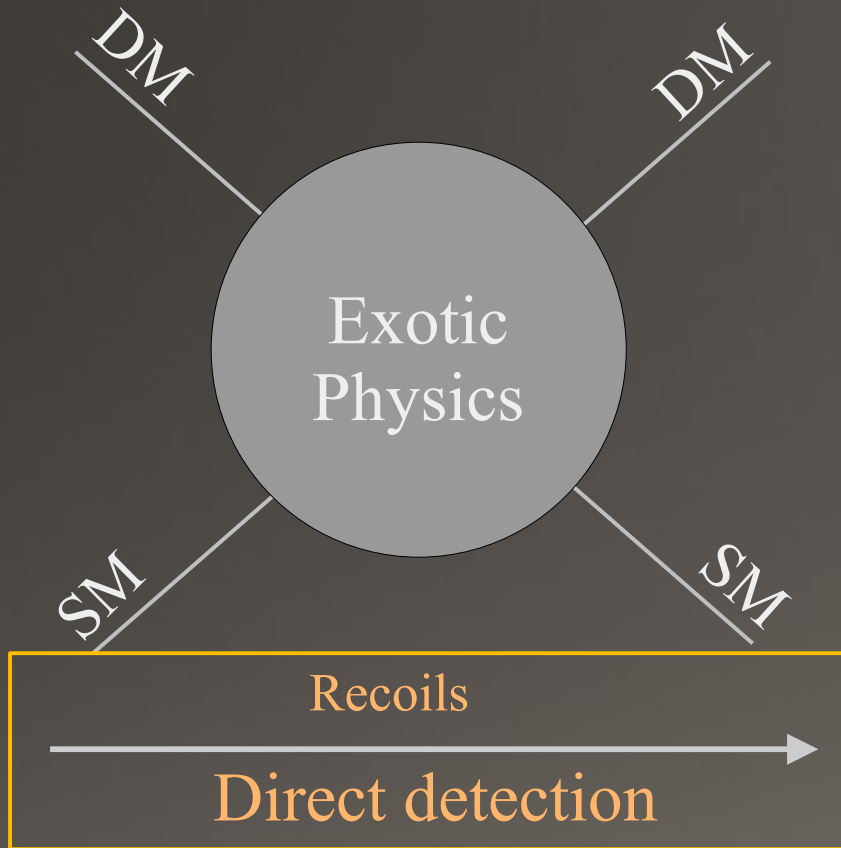
Local dark matter density  
 $\rho_{\text{DM}} = 0.4 \text{ GeV}/\text{cm}^3$

Local dark matter velocity  
 $\langle v_{\text{DM}} \rangle \approx 300 \text{ km/s}$

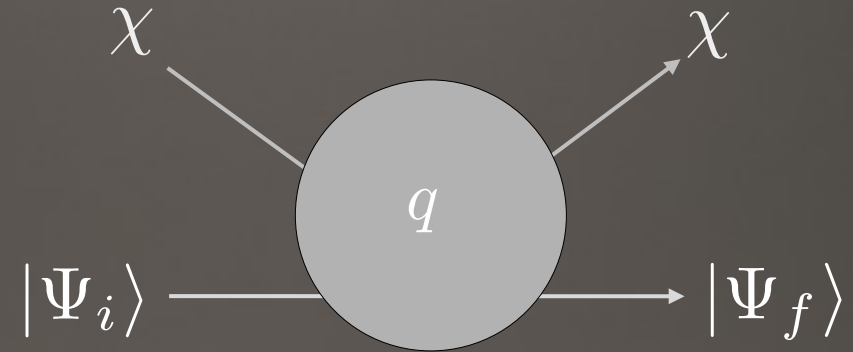
Lighter mass  $\rightarrow$  more particles  
 $n_{\text{DM}} = \rho_{\text{DM}}/m_{\text{DM}}$

More particles  $\rightarrow$  larger fluxes  
 $\phi_{\text{DM}} \sim v_{\text{DM}} n_{\text{DM}}$

# Dark Matter in The Lab



Direct WIMP-like *interaction*



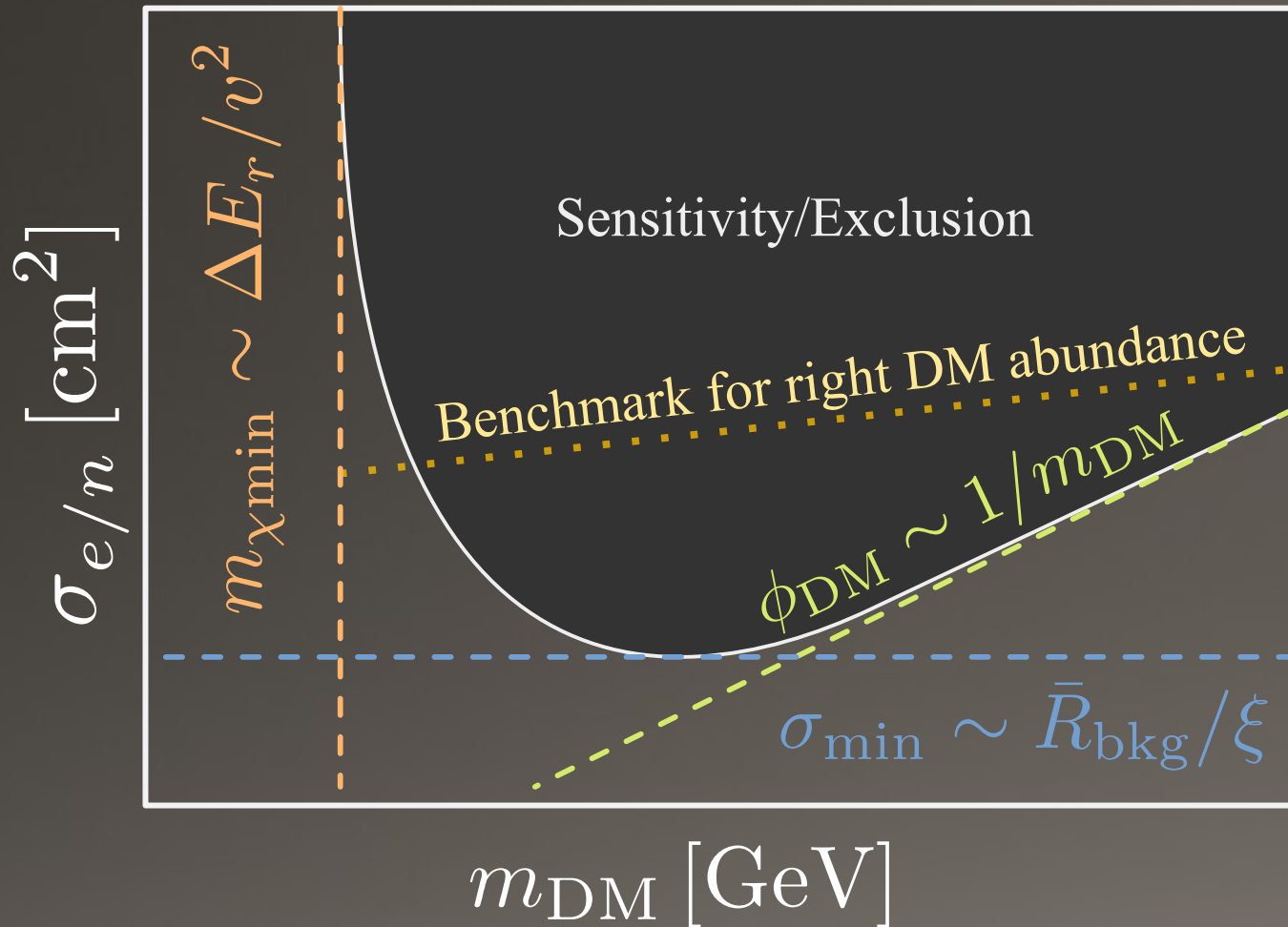
Energy Budget

$$E \sim v^2 m_\chi \approx \mathcal{O}(\text{keV}) \left( \frac{m_\chi}{1 \text{ GeV}} \right)$$

Momentum Budget

$$q \sim v m_\chi \approx \mathcal{O}(\text{MeV}) \left( \frac{m_\chi}{1 \text{ GeV}} \right)$$

# Direct Detection



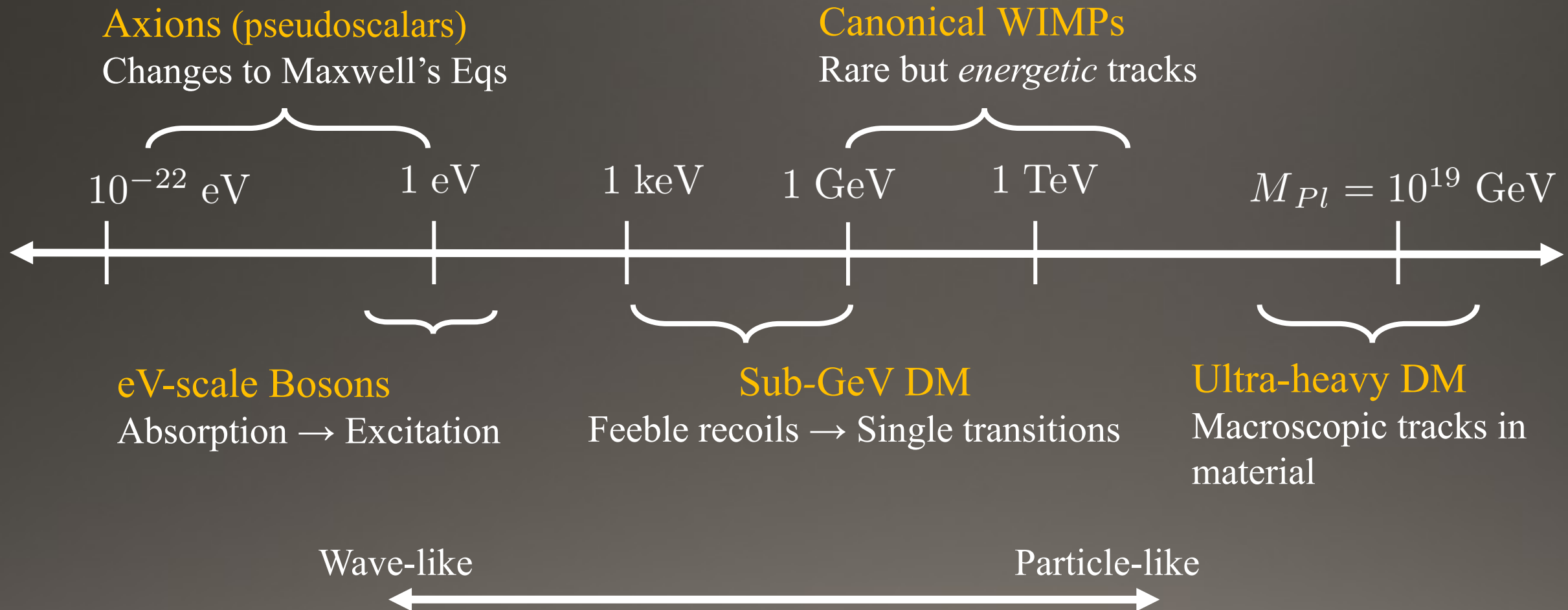
Need to *delve deep and search wide*

Minimize threshold energies  $\Delta E_r$

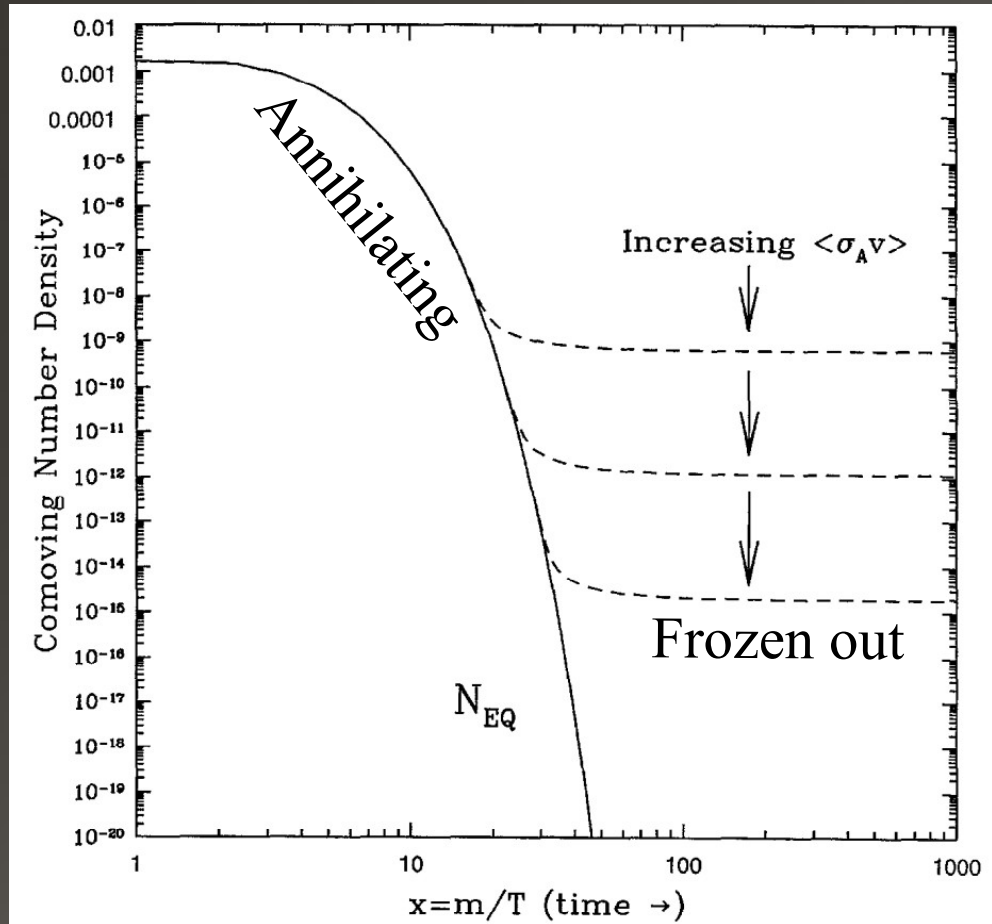
Maximize signal efficiencies  $\xi$

Minimize backgrounds  $R_{\text{bkg}}$

# Mass Range & Detection Methods



# WIMPs: The Miracle



Griest et. al: Phys Rep. 1996

Present-day abundance set by *freeze-out*

$$\Omega_c h^2 \sim \frac{1}{\langle\sigma v\rangle}$$

The appeal

Weak-scale masses and cross sections

$$\langle\sigma v\rangle_{\text{FO}} = 3 \times 10^{-26} \text{ cm}^3 / \text{s}$$

$$\approx \frac{\alpha_W^2}{(100 \text{ GeV})^2}$$









# Interaction Rate

Rate *spectrum* (events in detector)

$$\Gamma \sim \int \frac{d^3 \vec{q}}{q} \eta(v) |F_{\text{DM}}(q)|^2 |f_{i \rightarrow f}(q)|^2$$

Mean inverse velocity (Astrophysics)

$$\eta(v)$$

Transition form factor (Condensed matter / Chemistry)

$$f_{i \rightarrow f}(q) = \langle \tilde{\Psi}_f(k + q) | \tilde{\Psi}_i(k) \rangle$$

Dark matter form factor (Particle physics)

$$F_{\text{DM}}(q) \propto \begin{cases} 1 & , \text{Contact interaction} \\ \left(\frac{1}{q}\right)^2 & , \text{Long-range interaction} \end{cases}$$

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Rate *spectrum* (events in detector)

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Mean inverse velocity (Astrophysics)

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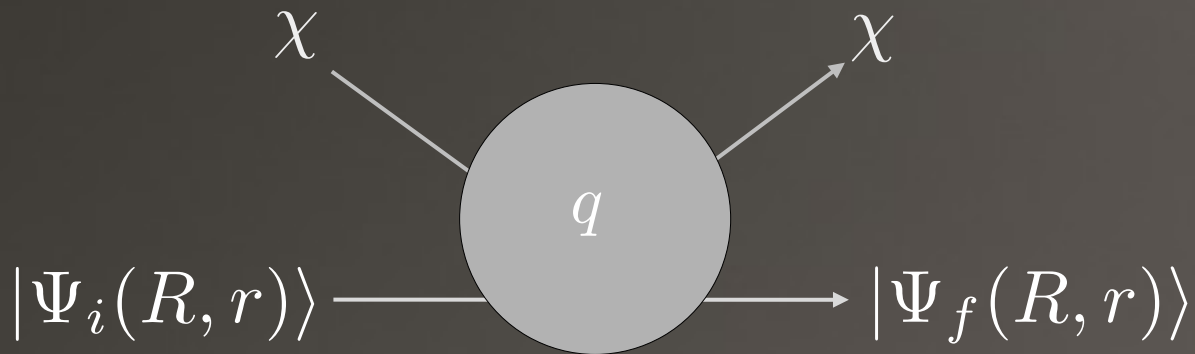
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# Sub-GeV Direct Detection



$R$  : Nuclei

$r$  : Electrons

$\chi$  : Dark matter

Imparted momentum in *scattering*

$$q \approx \mathcal{O}(\text{keV}) \left( \frac{m_\chi}{1 \text{ MeV}} \right)$$

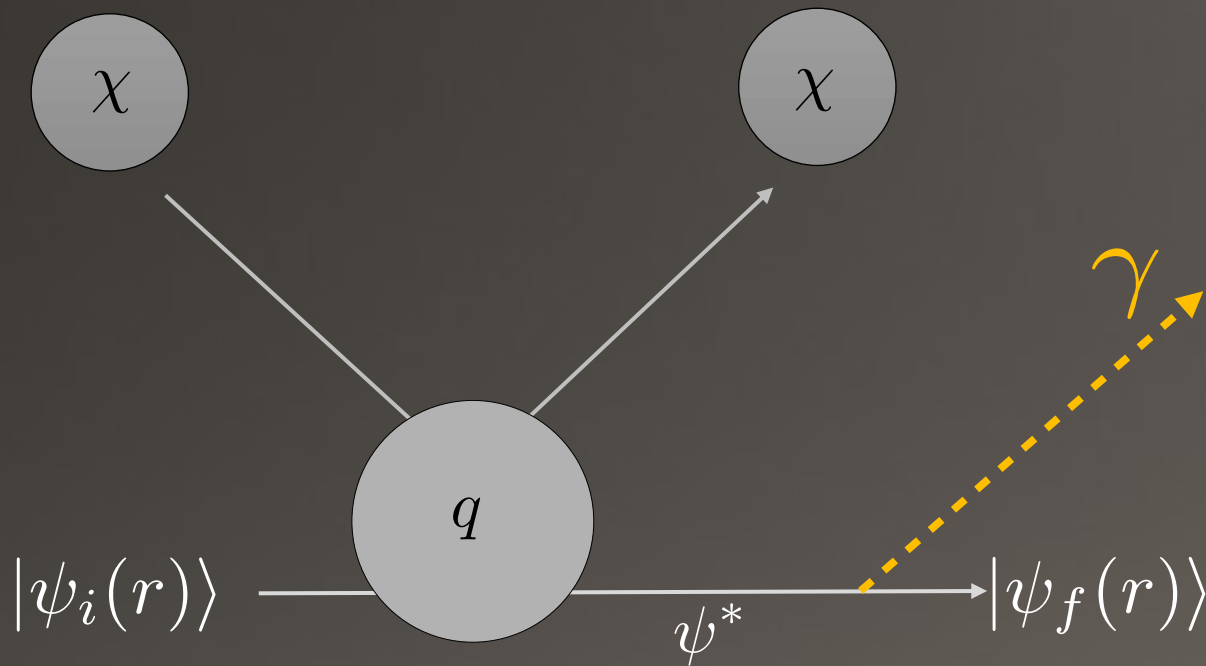
Energy Budget

$$\Delta E \approx \mathcal{O}(\text{eV}) \left( \frac{m_\chi}{1 \text{ MeV}} \right)$$

Energy equals momentum in *absorption*

$$\Delta E = q = \left( \frac{m_\chi}{1 \text{ eV}} \right)$$

# Electron Recoil → Photon Signal



## Molecules and Atoms (Quantized)

$$|\psi_i\rangle \sim \psi_{\text{lcao}}(r) \quad |\psi\rangle^* \sim \psi_{\text{lcao}}^*(r)$$

HOMO → LUMO

## Crystals (Continuous)

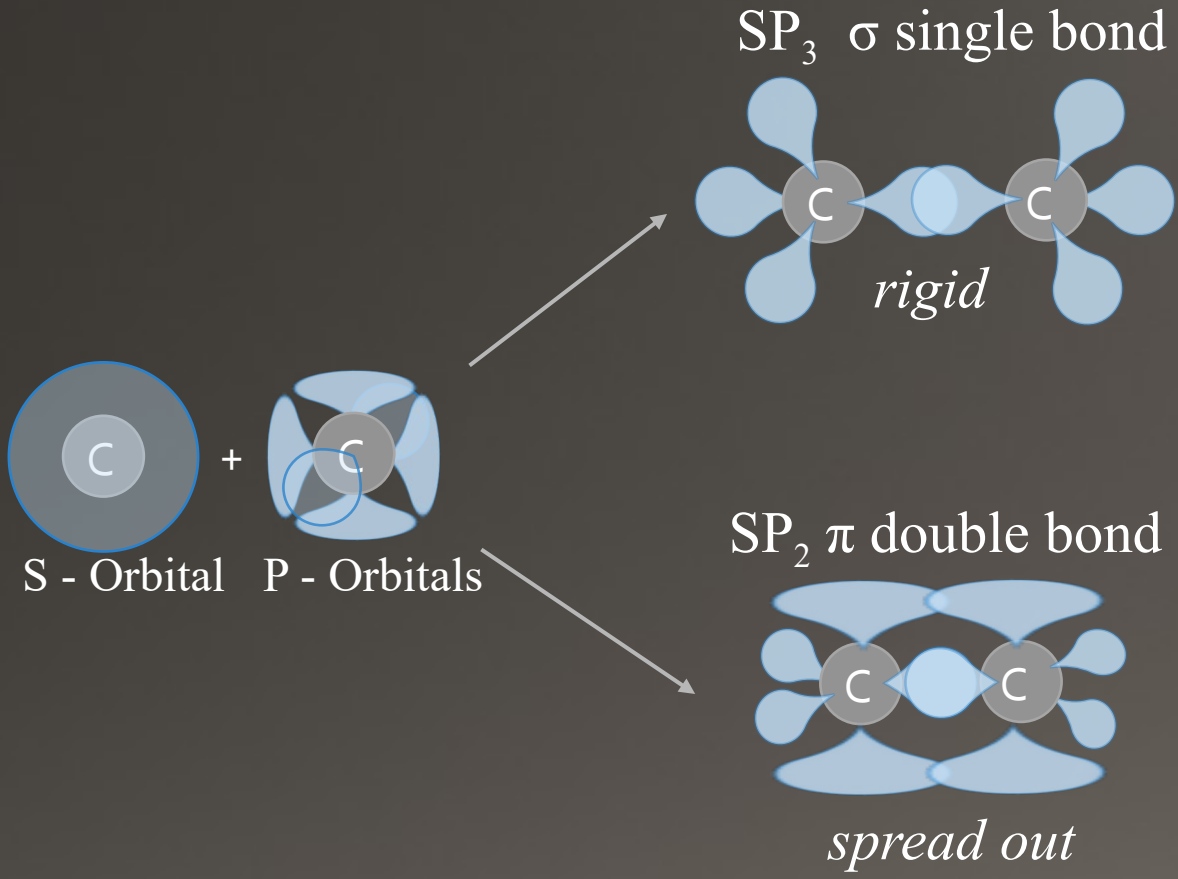
$$|\psi_i\rangle \sim u_v(r)e^{ik \cdot r} \quad |\psi\rangle^* \sim u_c(r)e^{ik \cdot r}$$

Valence → Conduction

## Chromophores

Electronic excitation → Unstable state → Photon emission.

# Carbon: a Natural Candidate



## Organic Chromophores

σ electrons form *rigid* network



π electrons *delocalized* on ring

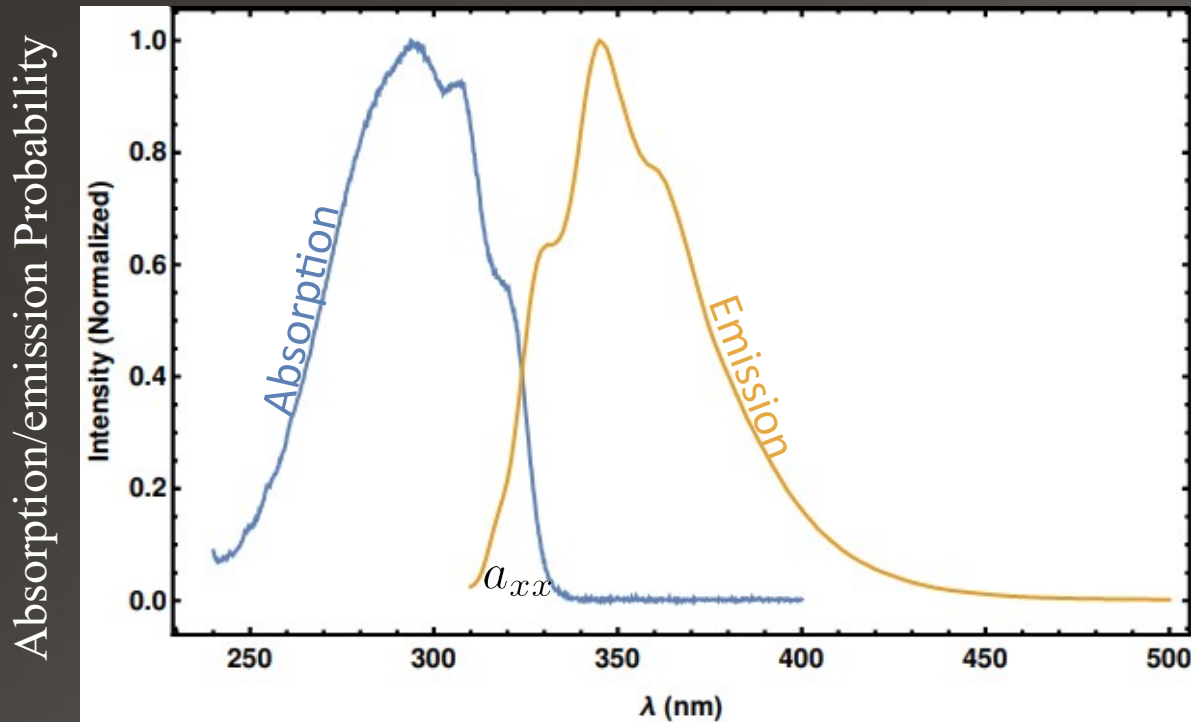
excite to produce photoemission

Delocalized π networks in molecules are natural DM detector candidates due to kinematic matching

$$q_e \approx 1/a_0 \sim \mathcal{O}(\text{keV}) \quad q \sim m_\chi v_\chi \approx \mathcal{O}(\text{keV}) \left( \frac{m_\chi}{1 \text{ MeV}} \right)$$

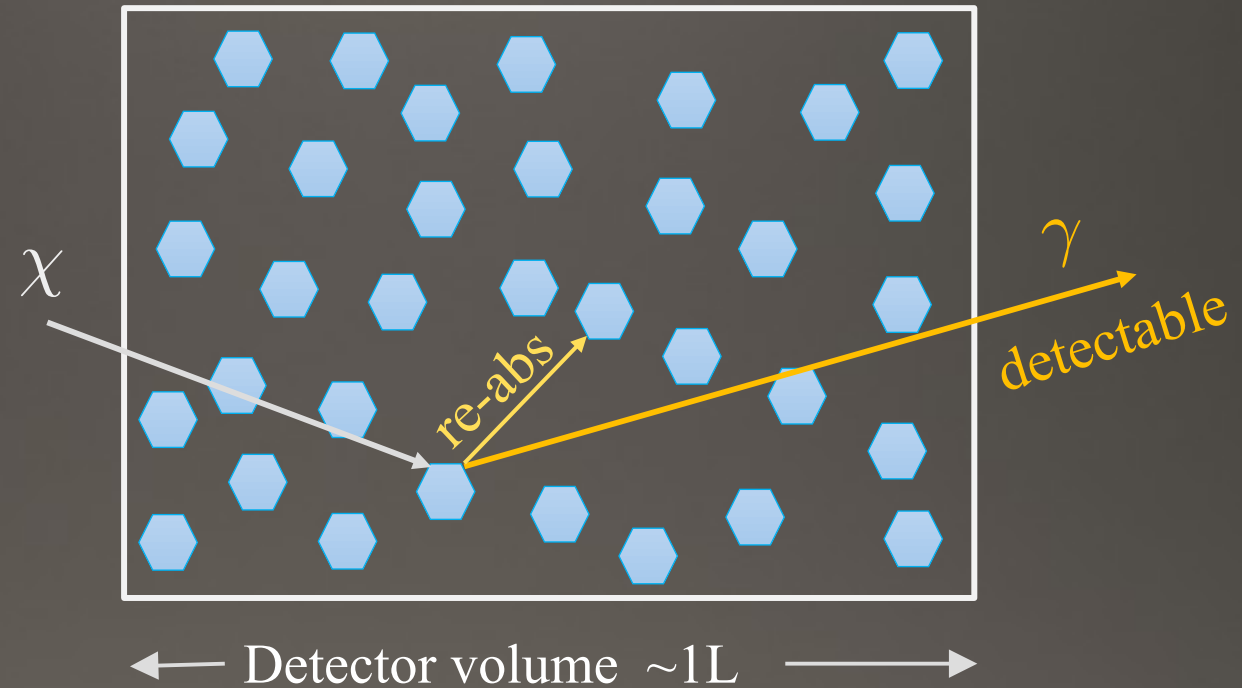
# Fluorescence with DM

fluorescence spectra



Decreasing energy (E)  $\rightarrow$

⬡: Chromophore:



Probability for the photon to free stream

$$\Phi_{FB} \sim (1 - a_{xx}) \quad \text{e.g. molecular crystals: } \Phi_{FB} \approx 65\%$$

# Pilot Experiment

## Problem

Describe the interaction between DM (BSM) with molecules (chemistry)

Many-body ground state is easy.

$$\Psi_G = |\psi_2 \overline{\psi_2} \psi_1 \overline{\psi_1} \psi_{1'} \overline{\psi_{1'}}|$$

How to compute the excited states?

The standards in the field:

FCI Hartree-Fock or *Density Functional Theory*

## Molecular scintillators



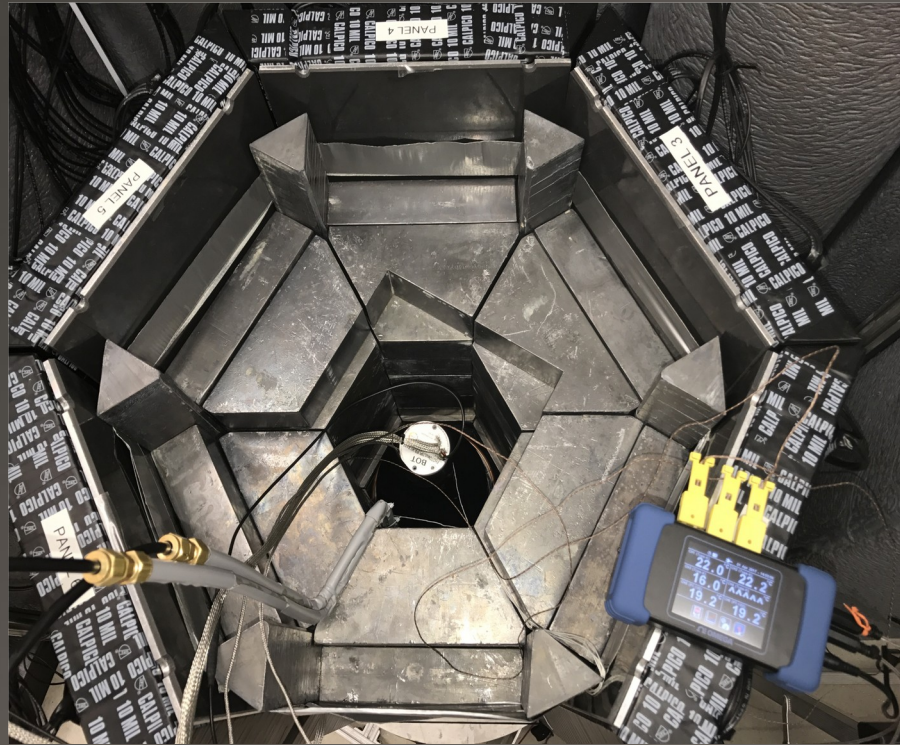
Para-xylene (EJ-301)



# First Experimental Setup



1L of EJ-301



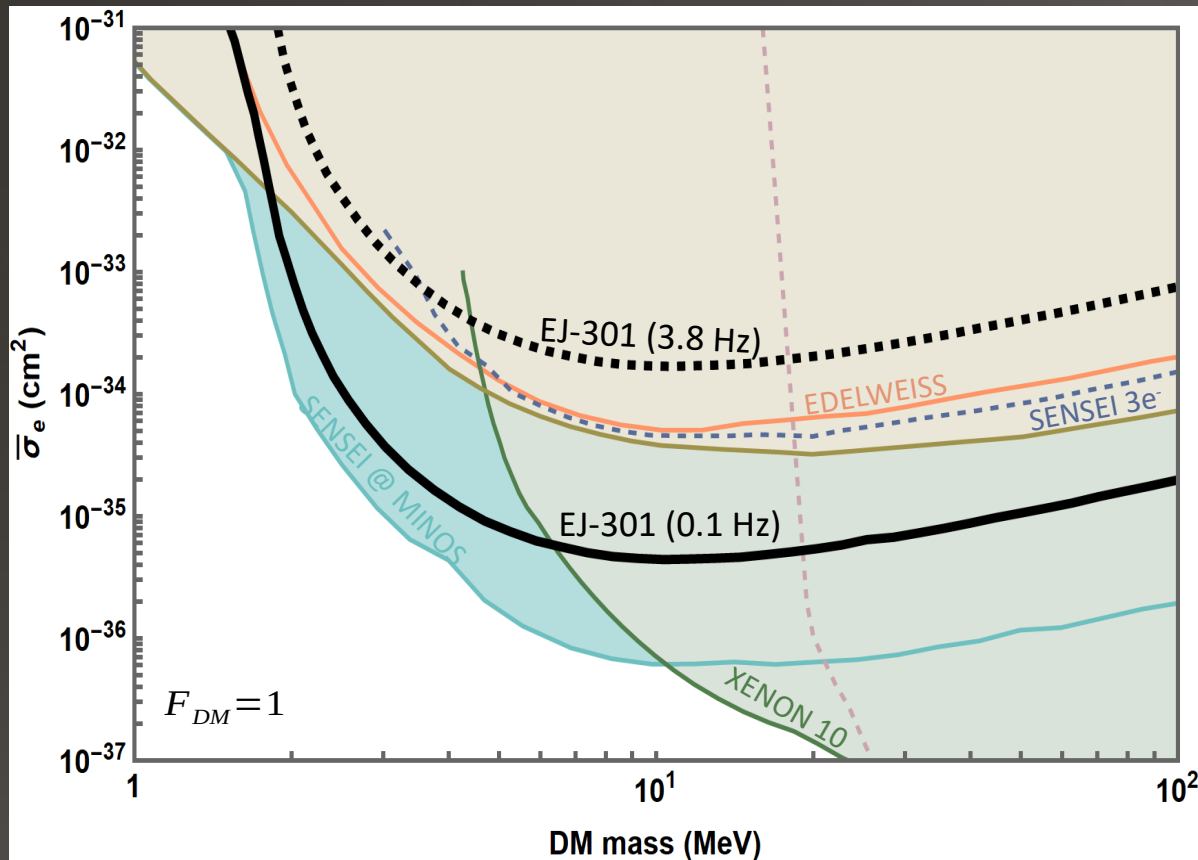
Ancient lead & Vetos



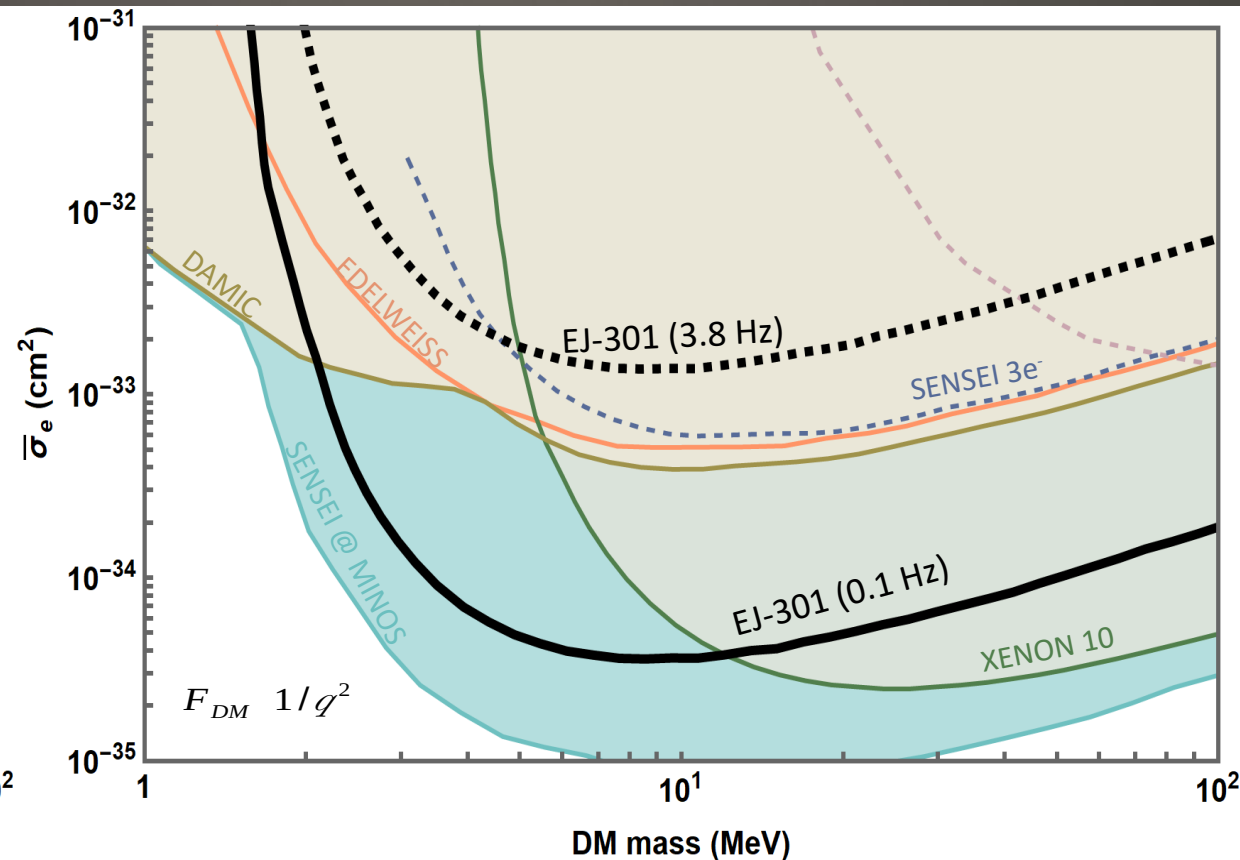
Surface run at UChicago

# Results: EJ-301

(Contact interaction)



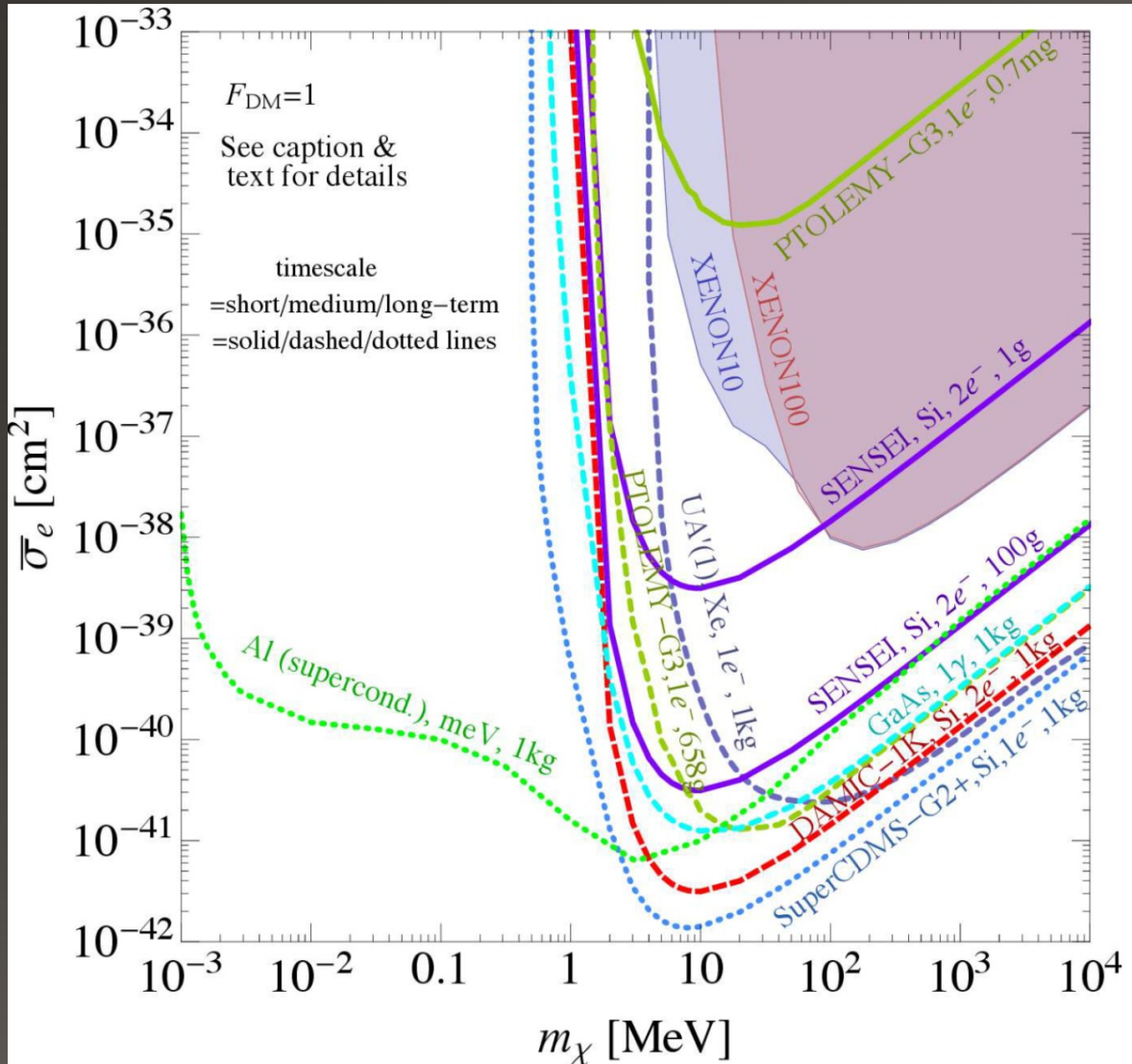
(Long-range interaction)



[CB, Collar, Kahn, Lillard: 1912.02822]

Theory → Experiment → Results in about 6 months

# The Field in Context



Many materials are proposed to probe the sub-GeV Space

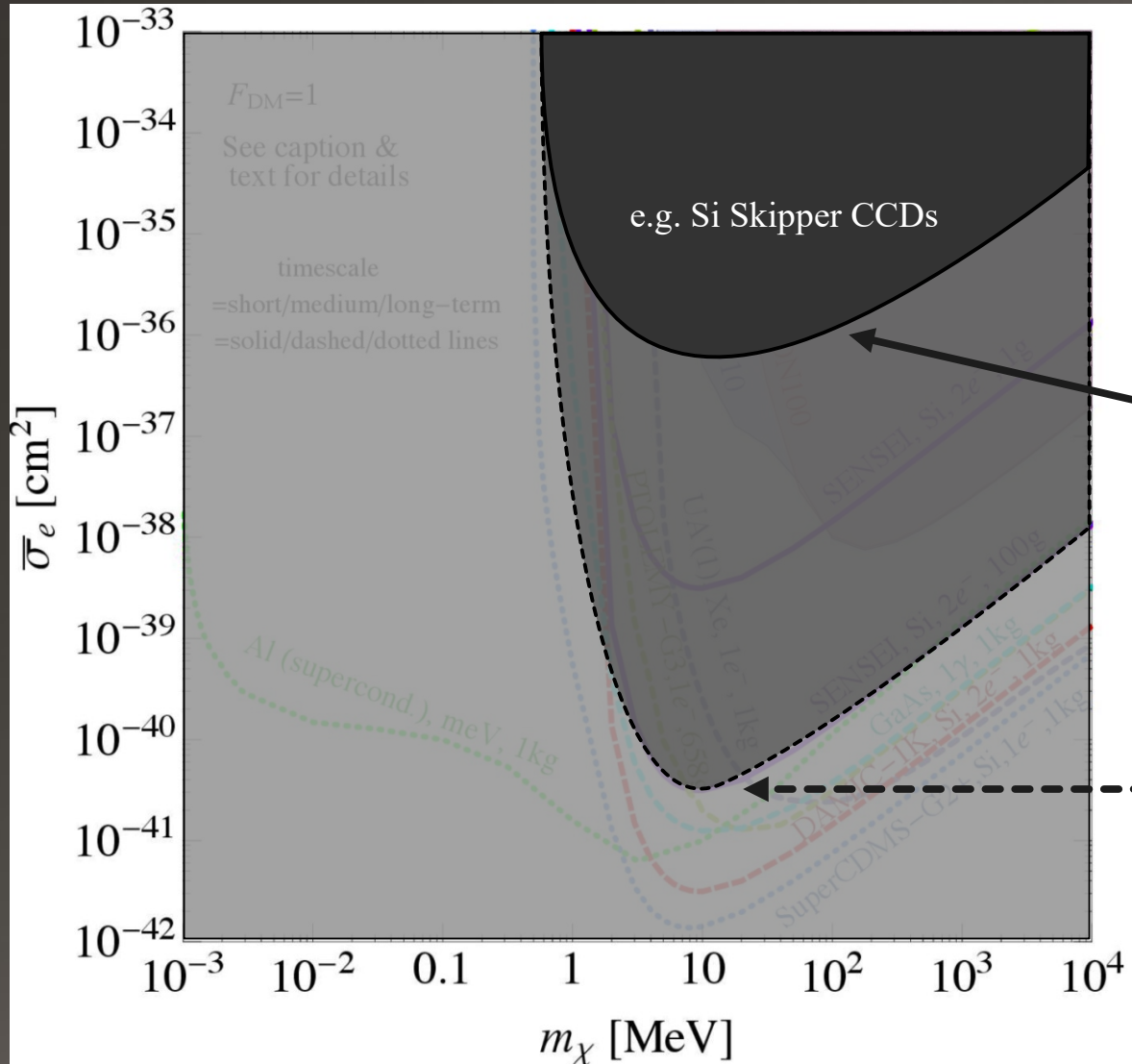
In 2017:

← Short term (2 years)

← Medium term (2-5 years)

← Long term

# Outlook and Potential Reach

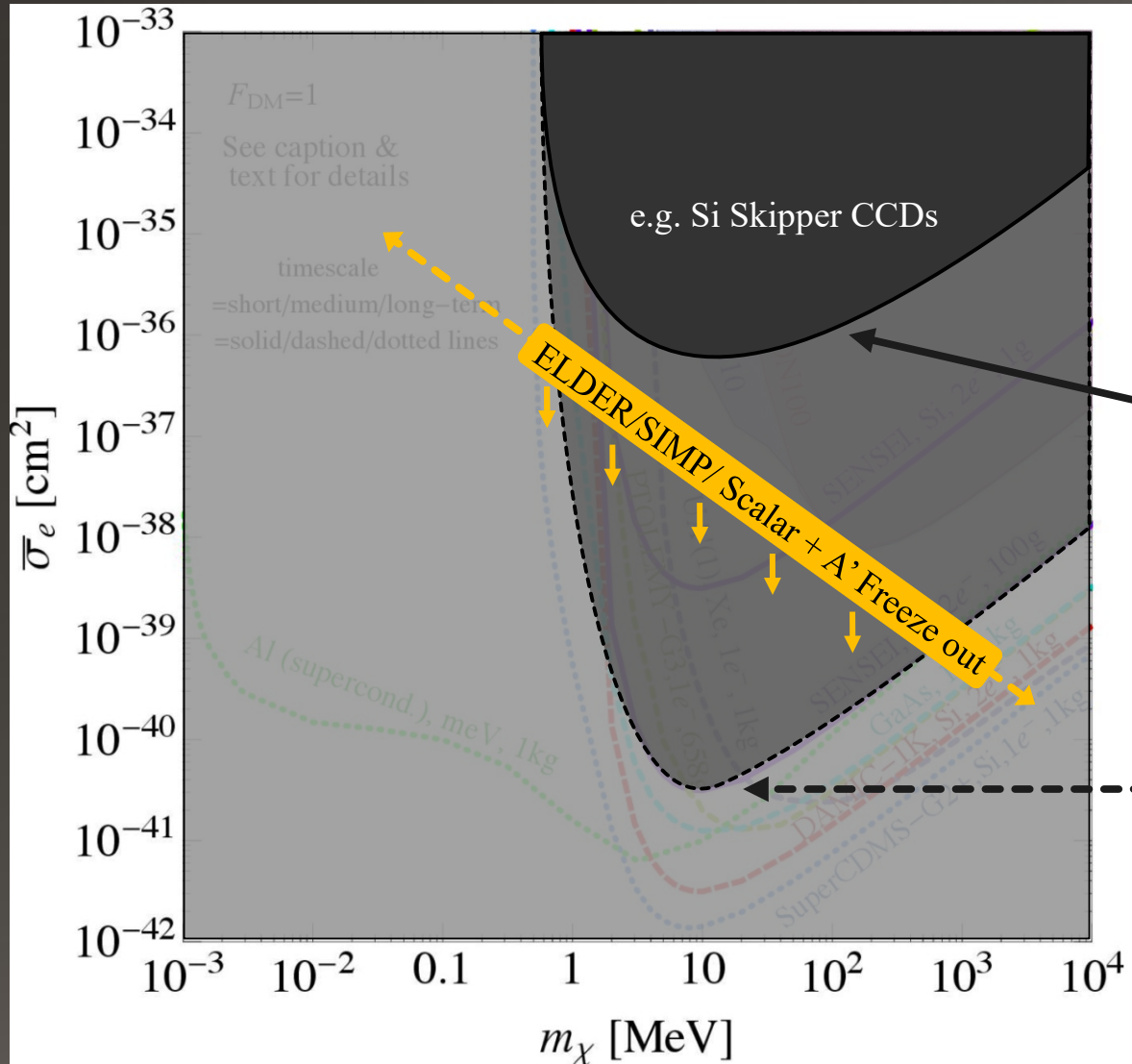


Present day:

Experimental results

Zero-background projection

# Outlook and Potential Reach



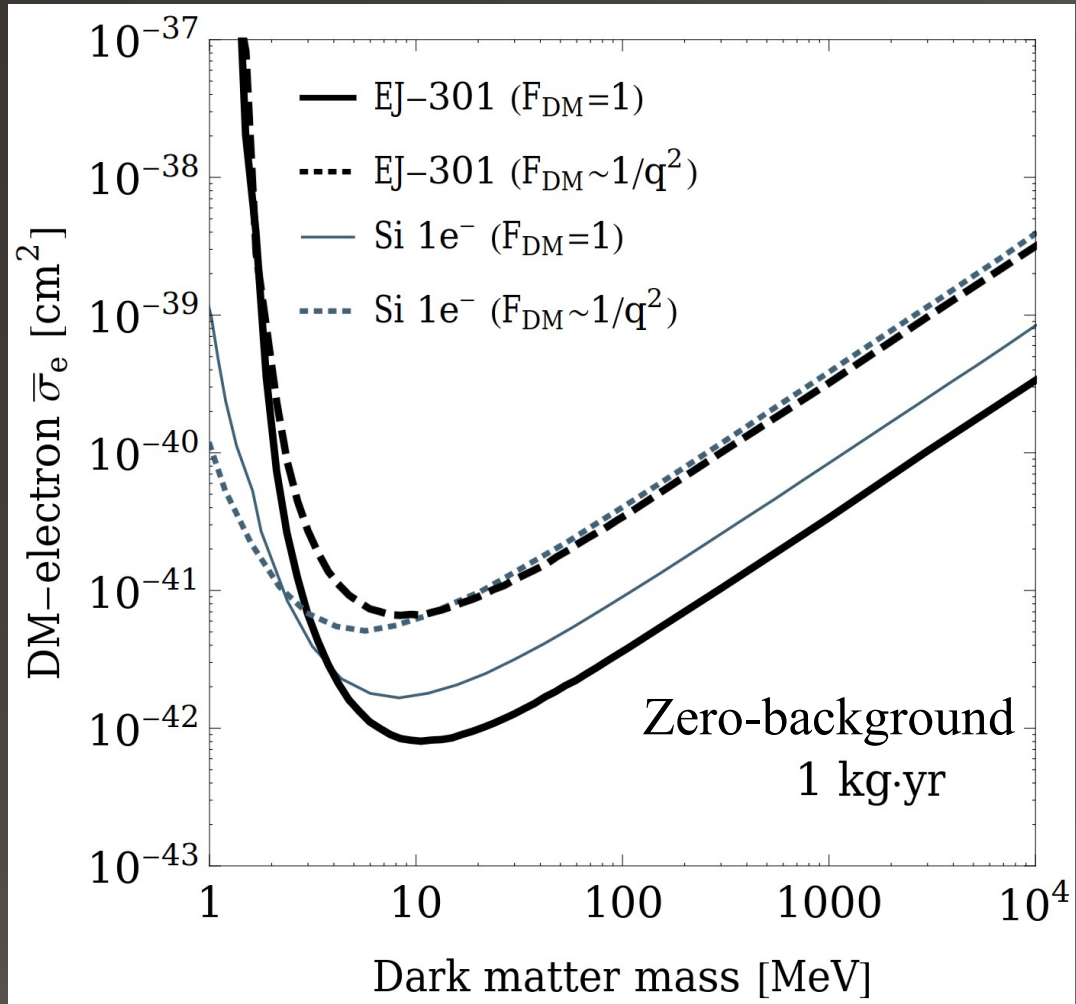
Present day:

Experimental results

Zero-background projection

# Outlook and Potential Reach

[CB, Collar, Kahn, Lillard: 1912.02822]



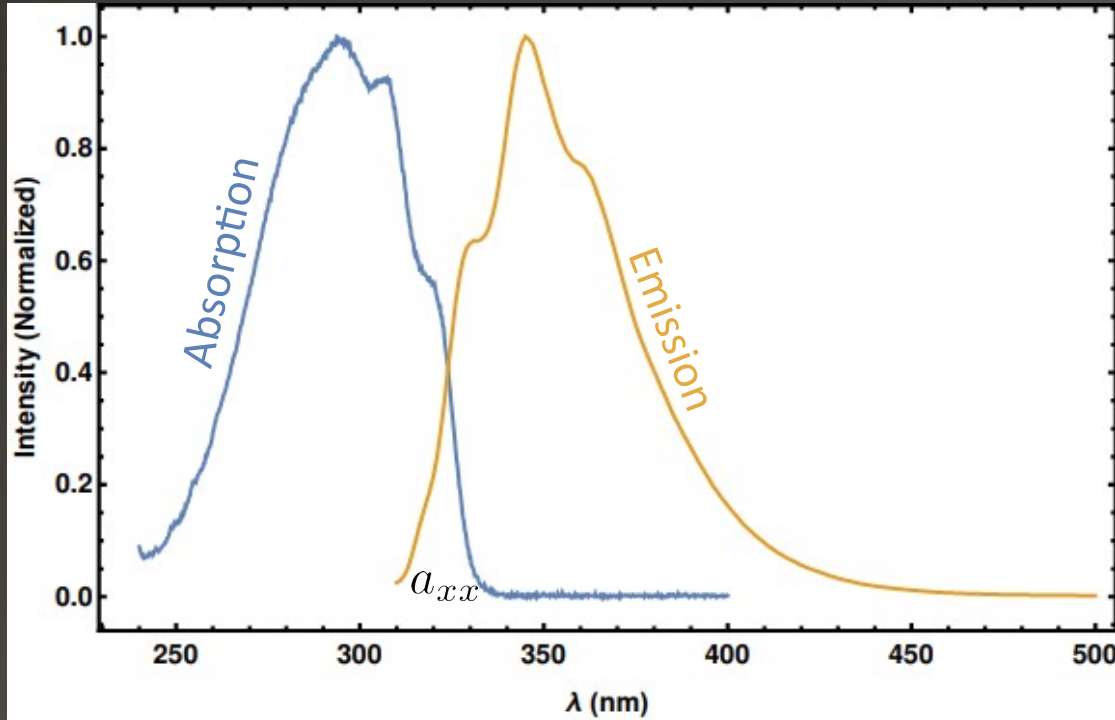
The obstacle

# Backgrounds

6 orders of magnitude of potential reach awaiting

Pound (kg) for Pound (kg) molecules produce about as much signal as e.g. Si.

# Fluorescence with DM Works



**Next Step**  
Minimize background

## Option 1

Reduce background in the excitation.

*Molecular crystals*

Anisotropic excitation → Time-varying DM signal

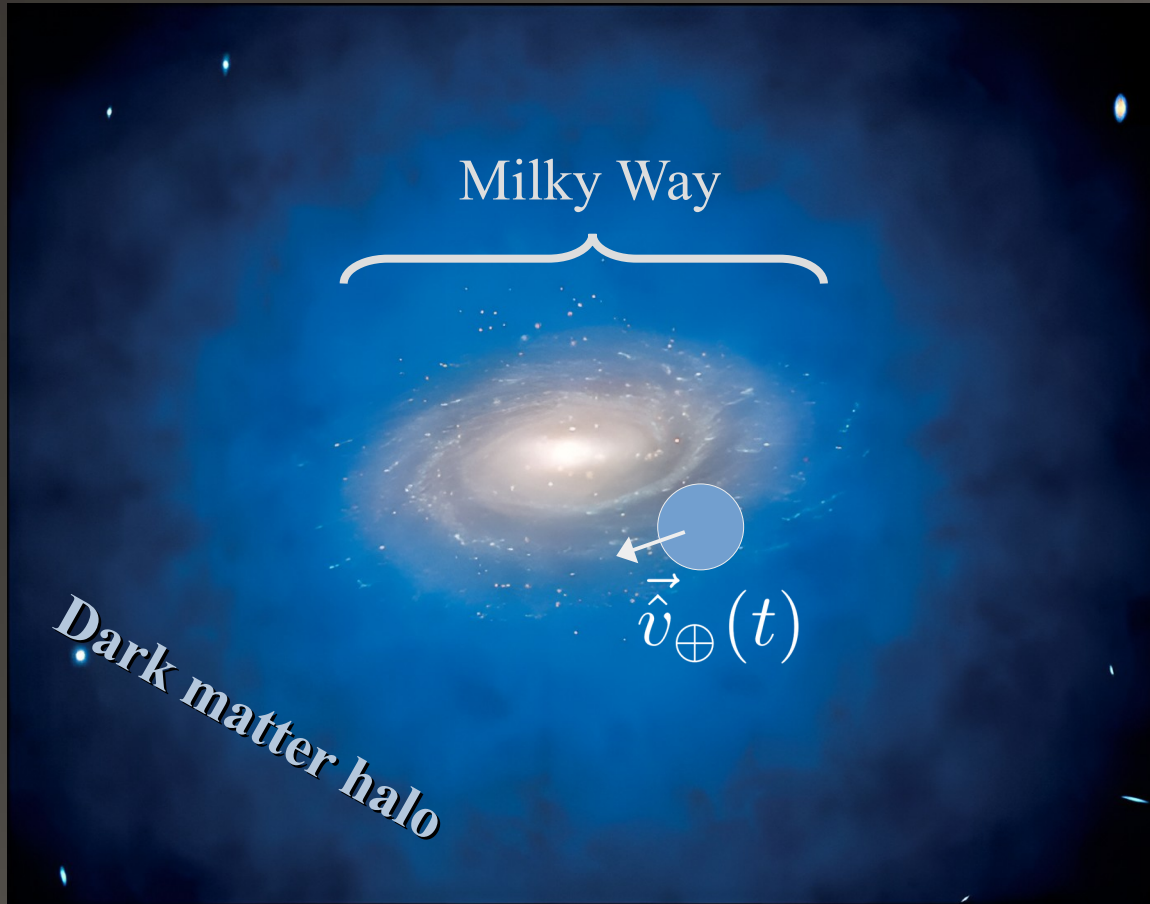
## Option 2

Reduce background in the emission.

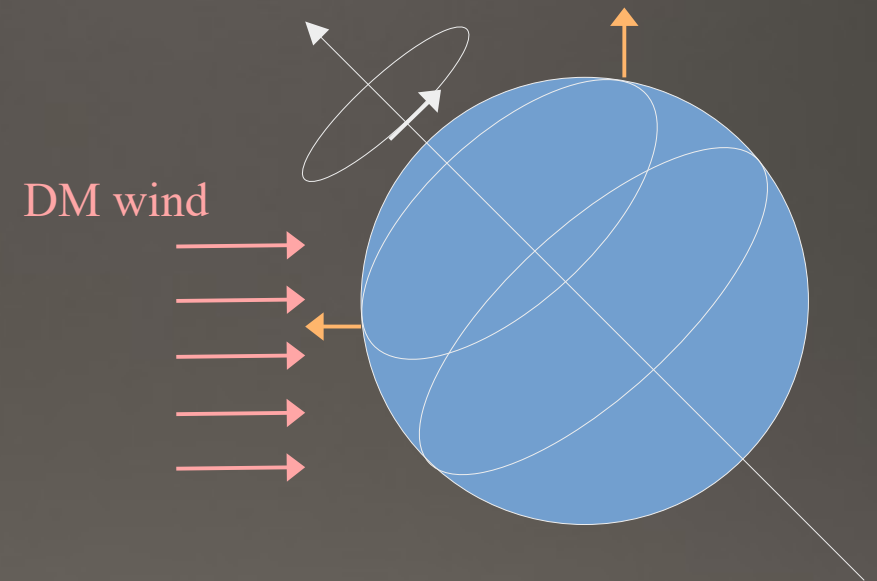
*Quantum dots*

Multiple excitons → Time-coincident DM signal

# Directional Detection



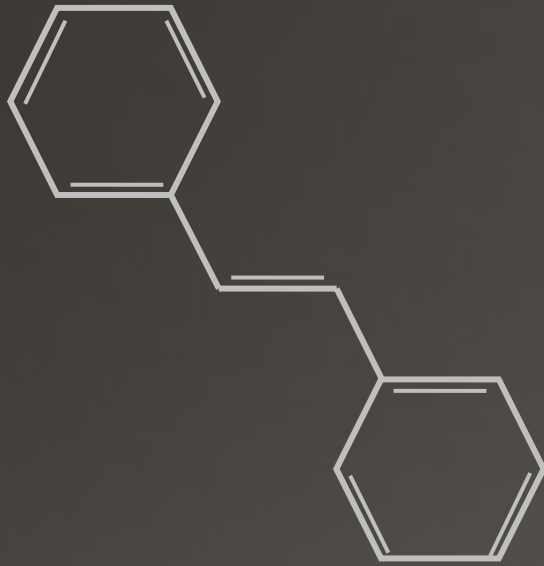
Effective dark matter “wind” from  $\vec{v}_{\oplus}(t)$



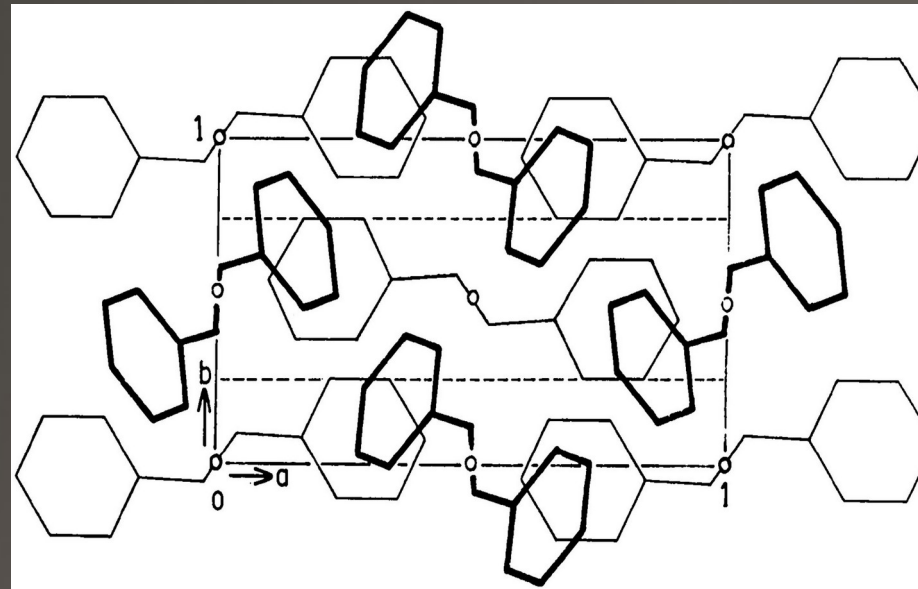
Change in relative orientation between detector and dark matter wind leads to *daily* modulation



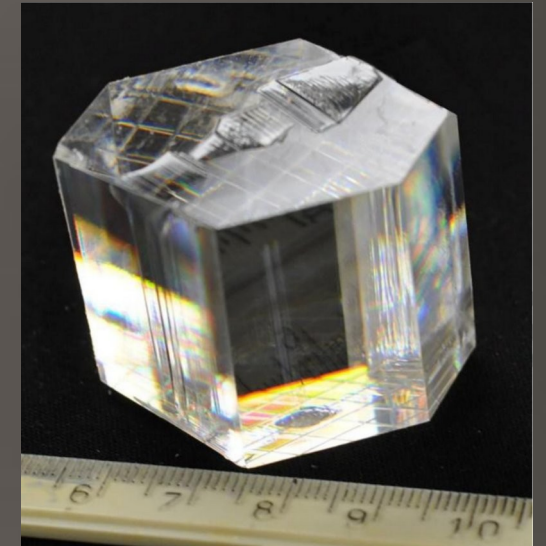
# Trans-Stilbene



Delocalized and planar network  
of double bonds



Molecular planes oriented in  
crystal lattice

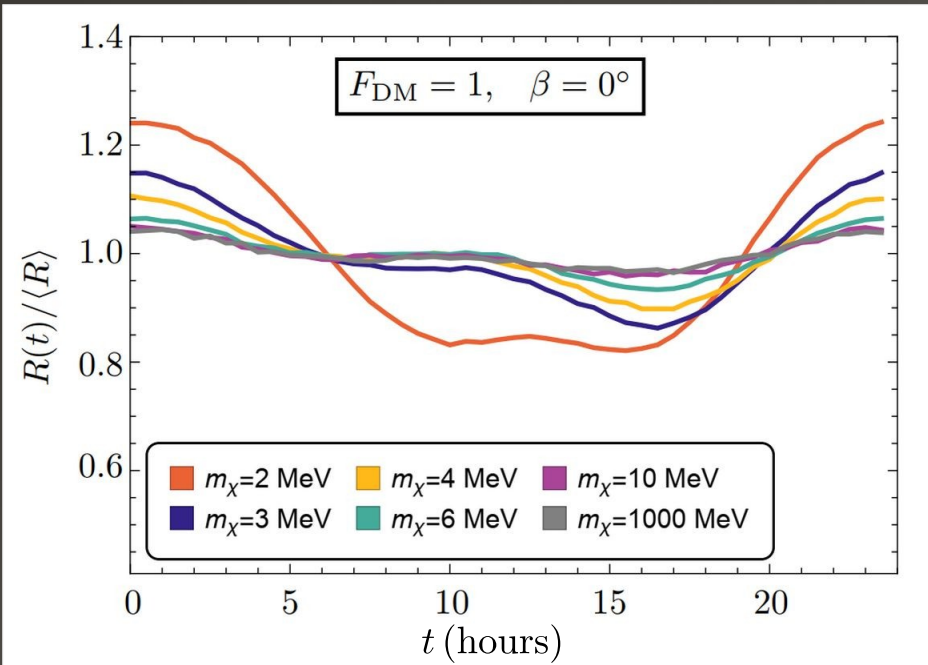


Carman, et.al. '18 (J. of Crystal Growth)

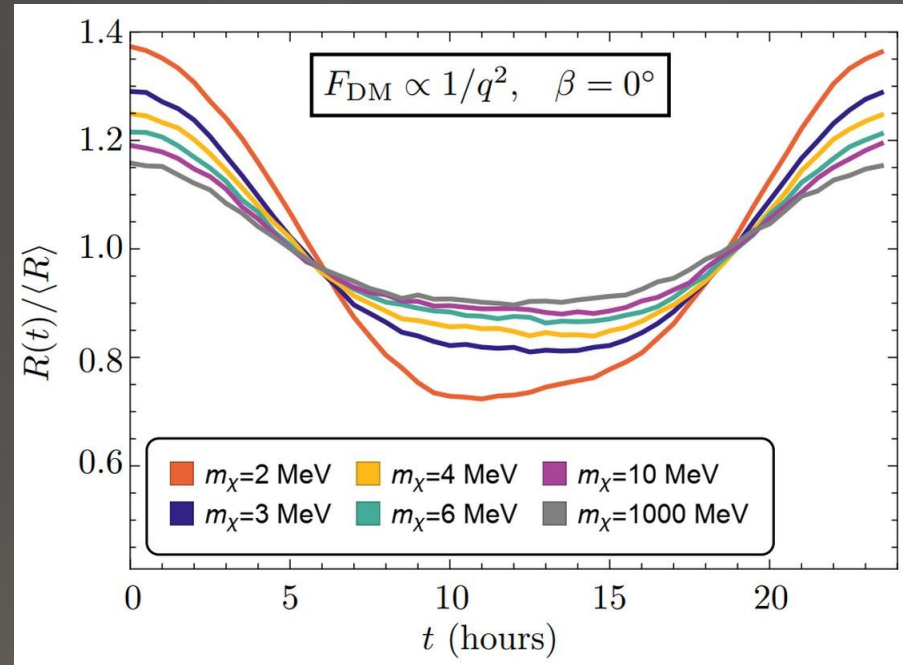
Large optical-quality crystals

# Daily Modulation

(Contact interaction)



(Long-range interaction)



Varies up to 70%  
Verifiable signal!

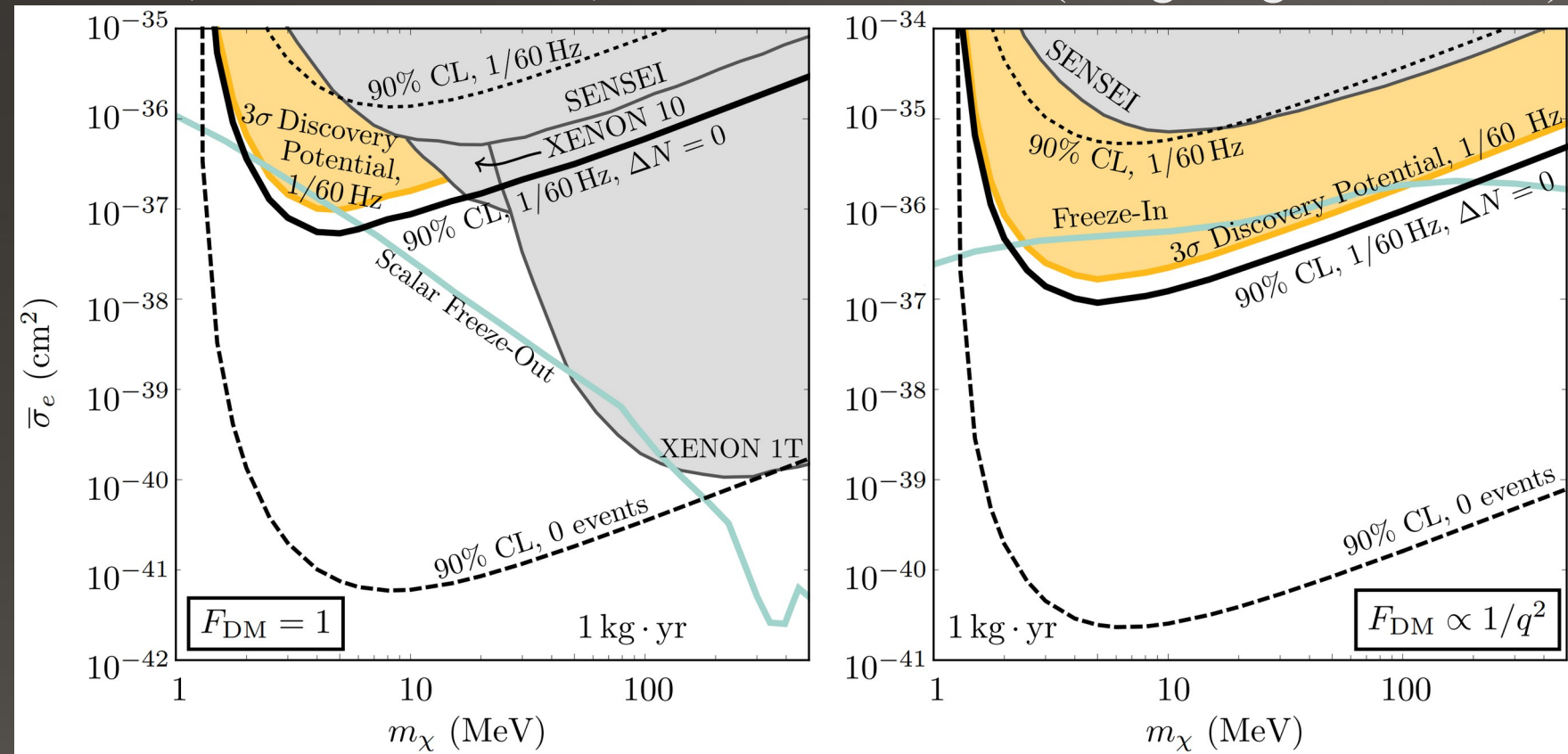
[CB, Kahn, Lillard, McDermott: 2103.08601]

Modulation amplitude remains as high as 10% even at the highest masses due to the fundamental anisotropy of the molecular form factor.

# Improved Sensitivity & Reach

(Contact interaction)

(Long-range interaction)



Sensitivity w/o modulation

Modulation discovery

Exclusion w/ modulation

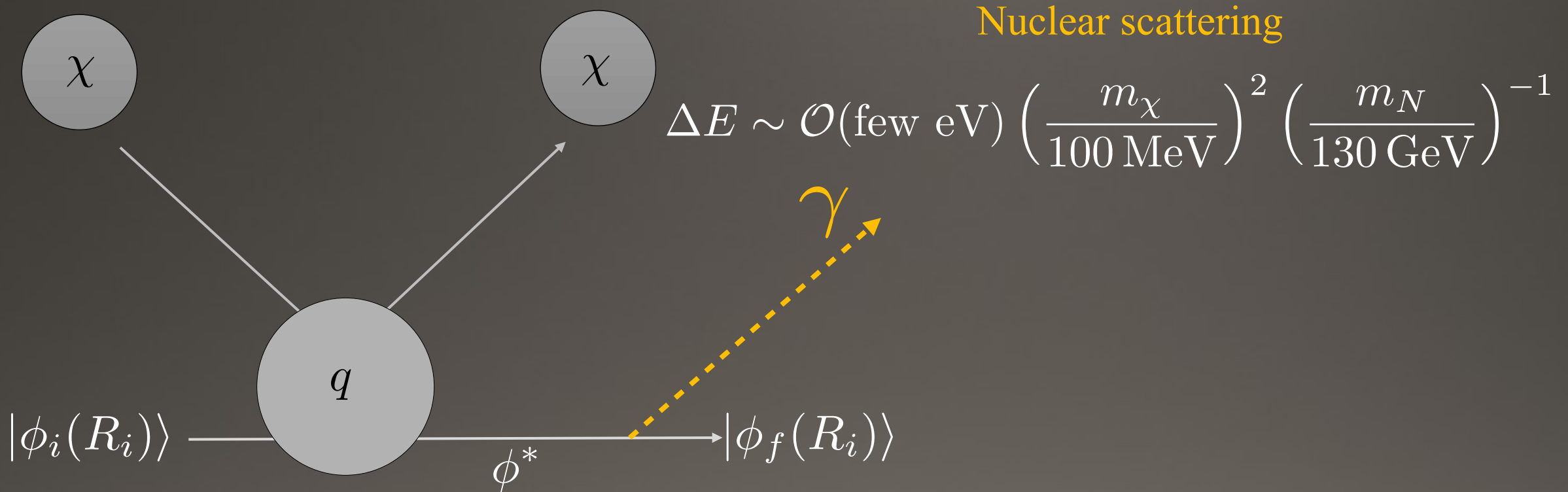
*With dark rate  
(1/min)*

\*1kg of t-stilbene can probably be found within a few blocks of this room

[CB, Kahn, Lillard, McDermott: 2103.08601]

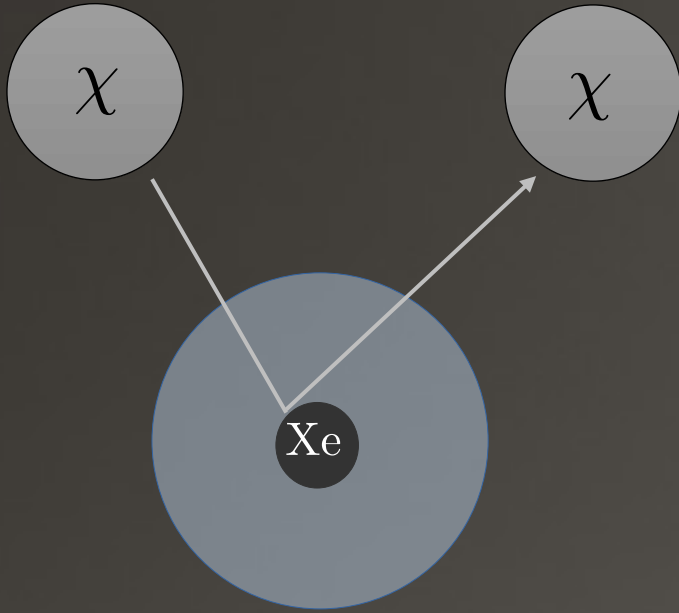
Improvement of *two orders of magnitude* & potential for discovery

# Nuclear Recoil $\rightarrow$ Photon Signal



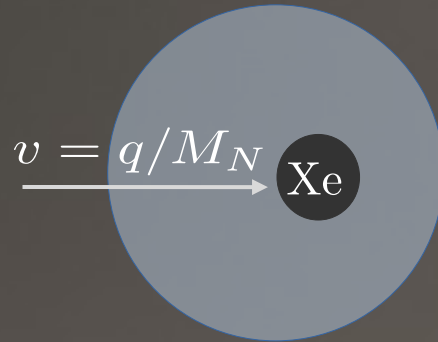
Next step in *complexity*: Nuclear recoil  $\rightarrow$  ???  $\rightarrow$  Radiative emission

# Ionizing Atoms Through Nuclear Recoil:

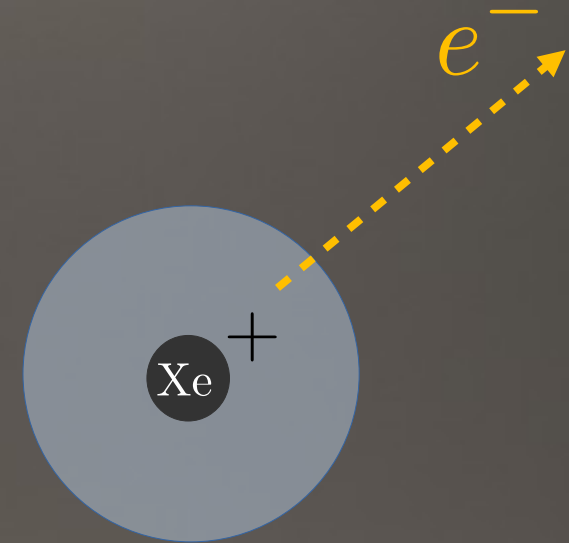


Initial nuclear recoil

$$|\psi_i\rangle \sim e^{i \frac{m_e}{M_N} \vec{q} \cdot \vec{r}} \psi_{\text{AO}}(r_\beta)$$



Nucleus moves faster than electrons



Electronic transition to ionized state

## The Migdal effect

Extend the sensitivity of detectors to lower masses.  
e.g. Xenon

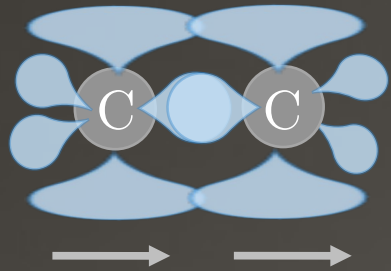
$$f_{i \rightarrow f} \approx \frac{m_e}{M_N} \vec{q} \cdot \langle \vec{r} \rangle_{i \rightarrow f}$$

Kinematic *penalty*

# The Molecular Migdal Effect(s)

Center of mass recoil (CMR)

Cause by center of mass motion



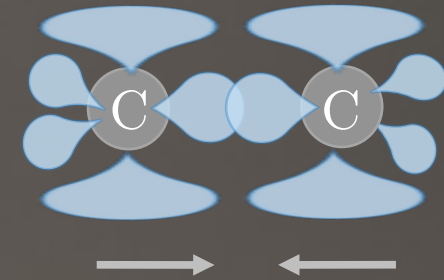
Analogous to atomic Migdal effect

$$P_{CMR} \sim \frac{m_e}{M_{mol}}$$

Moving whole molecule  $\rightarrow$  BIG penalty

Non-adiabatic coupling (NAC)

Caused by relative motion



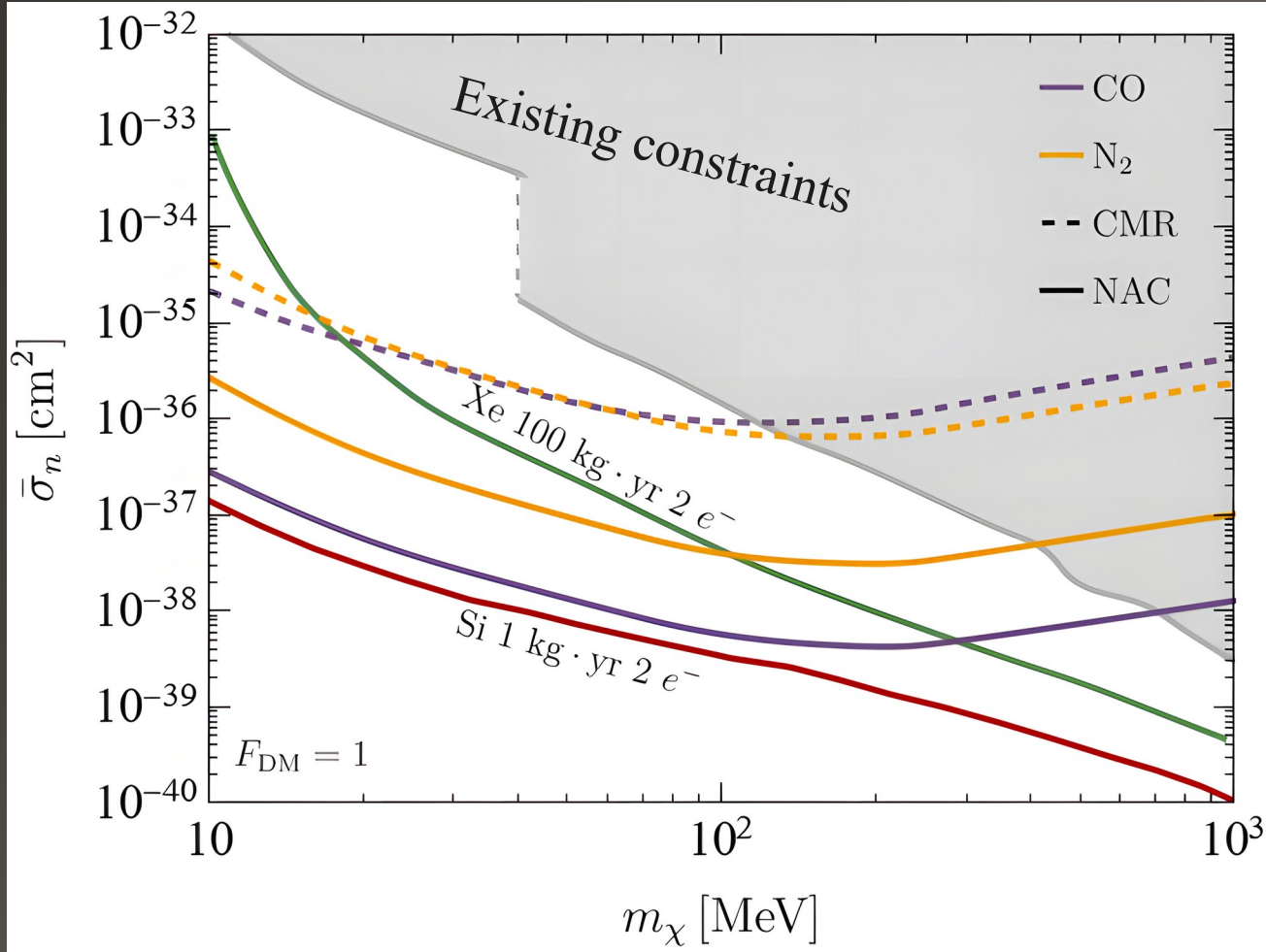
Effect beyond Born-Oppenheimer

$$P_{NAC} \sim \frac{m_e}{M_N}$$

Crumpling molecule  $\rightarrow$  small Penalty

# The Molecular Migdal Effect(s)

(Contact interaction)



Si rate is calculated using the *CMR*-equivalent Migdal effect. Is there an *NAC*-equivalent in Si?

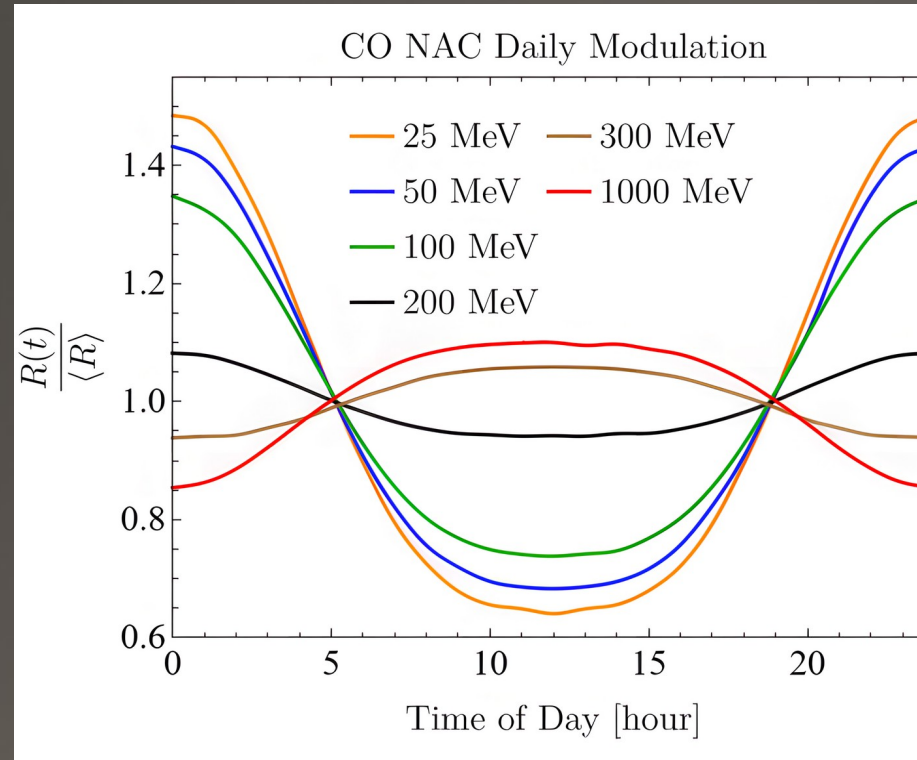
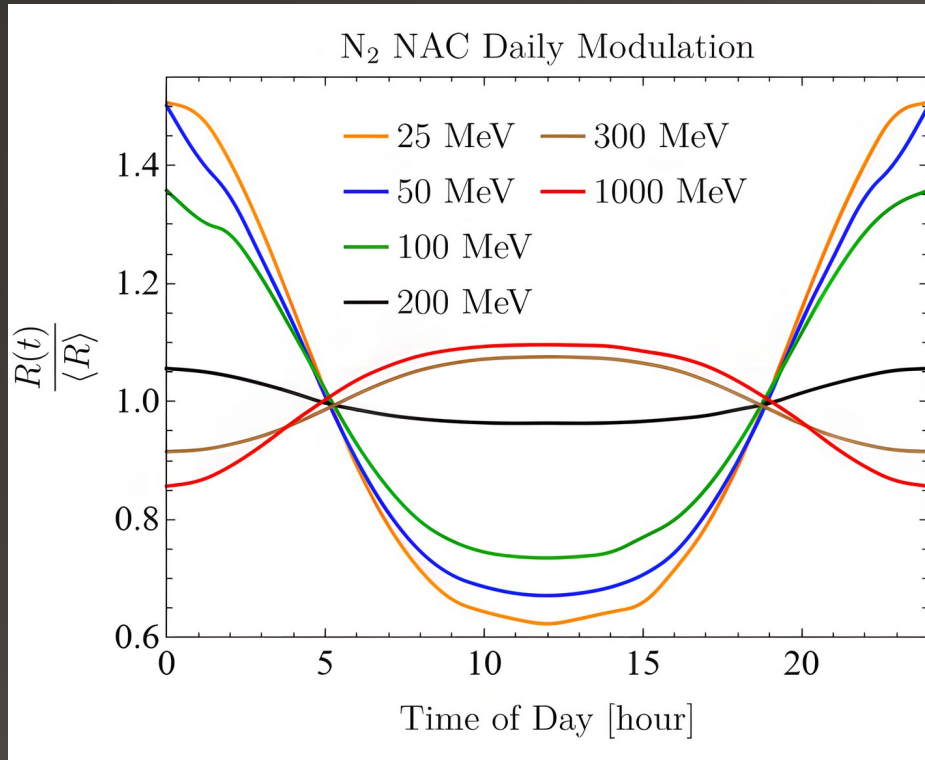
← *Center of mass recoil*  
Subdominant at all masses.

← *Non-adiabatic coupling*  
Favorable kinematic factor.

Simplest molecular models already competitive. Is there an optimal molecular target?

[CB, Harris\*, Kahn, Lillard, Perez-Rios: 2208.09002]

# Directional Molecular Migdal Effect



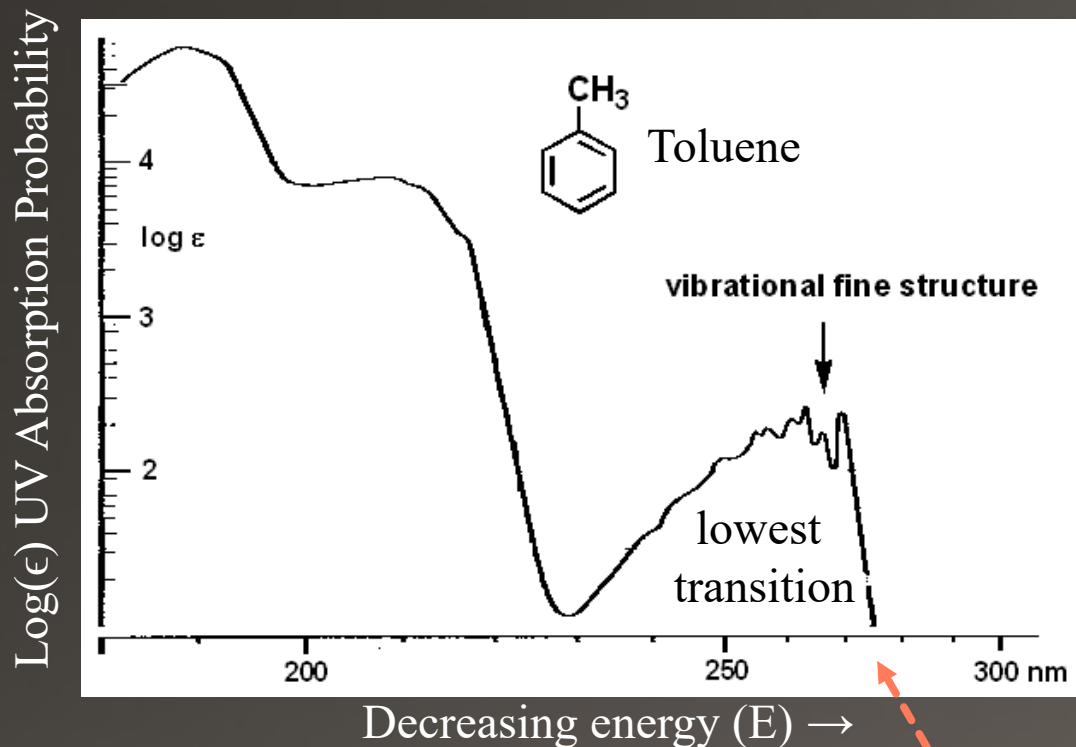
Varies up to 80%  
*Mass dependent phase*

[CB, Harris\*, Kahn, Lillard, Perez-Rios: 2208.09002]

Molecular alignment → Directional electronic excitation → Directional molecular Migdal effect(s)



# Experimental Evidence for NAC



## Claim

NAC is visible in existing data

Photon absorption probability

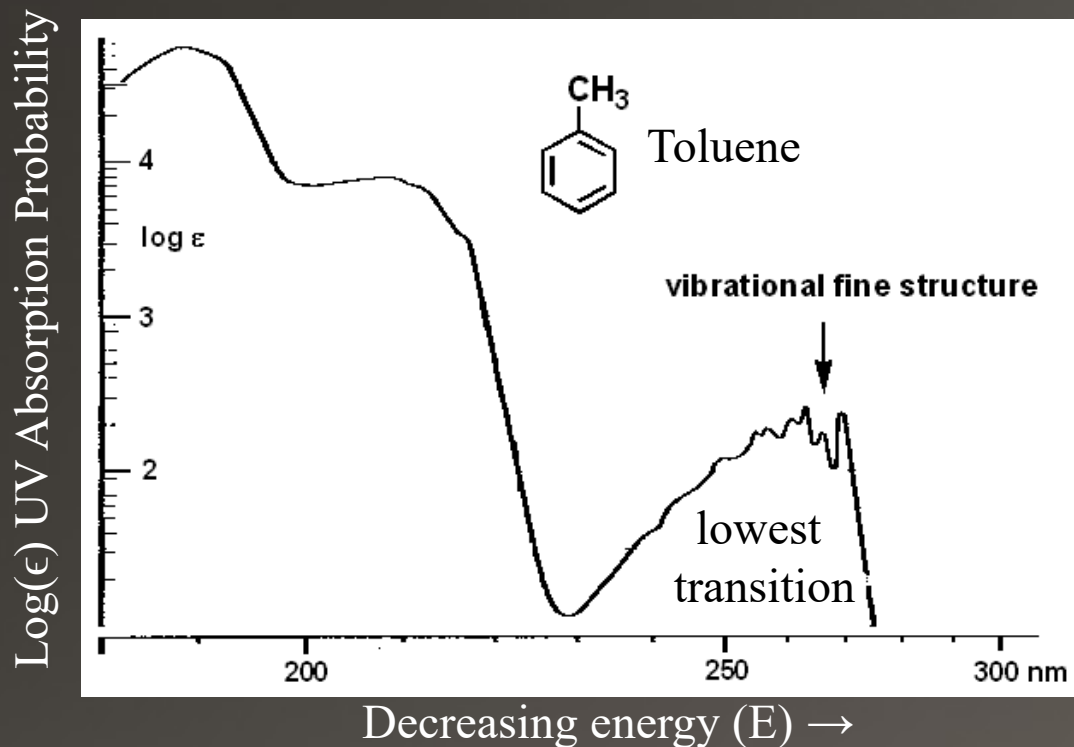
$$\langle \Psi_f | \vec{r} | \Psi_i \rangle = 0 \quad \text{e.g. toluene}$$

dipole transition

Classically forbidden by symmetry

No dipole moment  $\rightarrow$  Classically forbidden UV absorption

# Experimental Evidence for NAC



## NAC form factor

How electrons respond to nuclear deformation.

$$f_{e,NAC} \sim \langle \psi_f | \nabla_R | \psi_i(r) \rangle$$

Photon absorption probability

$$\epsilon \sim \langle \Psi_f | \vec{r} | \Psi_i \rangle = 0 \quad \text{e.g. toluene}$$

dipole transition

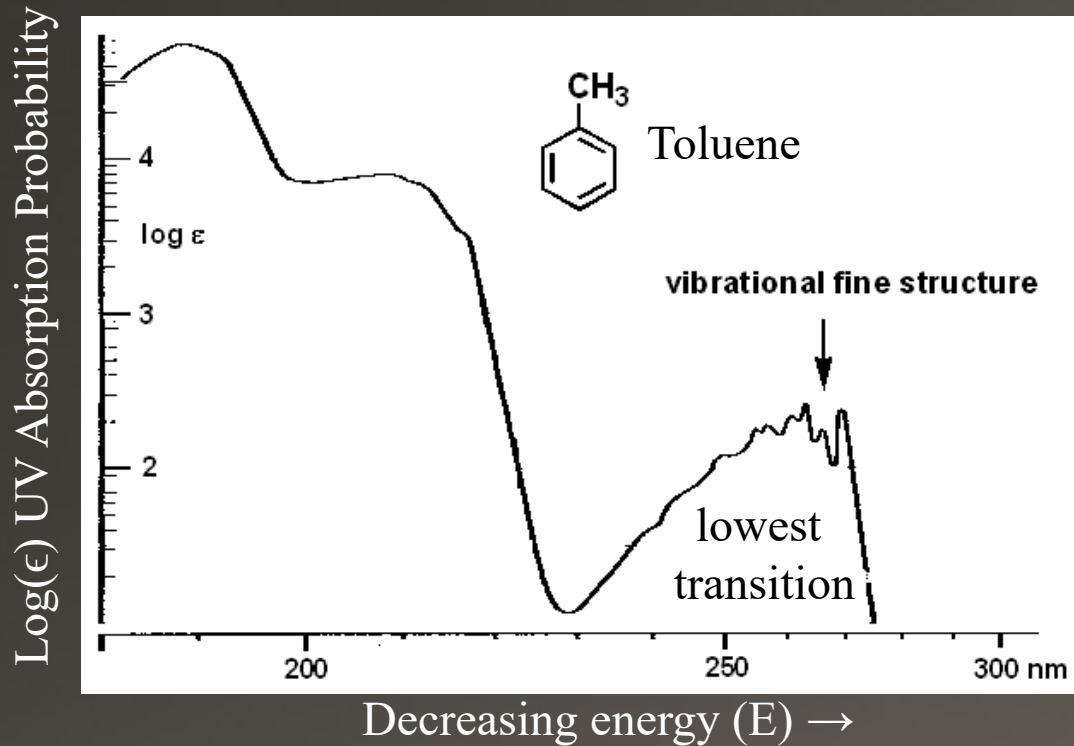
## NAC-induced UV absorption

$$\epsilon \sim \langle \psi_f(r; R) | \vec{r} | \psi_i(r; R) \rangle |_{R \neq R_0} \neq 0$$

*However*

Nuclear deformation  $\rightarrow$  Non-adiabatic dipole

# Finding Optimal Targets



Find molecules with max NAC

Large NAC → Large DM interactions

Molecular symmetries → Forbidden transitions

Measured with vibrational substructure  
→ Evidence of NAC

# Finding Optimal Targets

**Problem:** Chemical space is unreasonably large

How many molecules possible with  
C, O, N, F, H?

< 9 atoms: 100s of Thousands (DFT Computable)

< 30 atoms: 100s of Billions (Intractable)

...toluene has 15, xylene has 18, t-stilbene has 26

## Method

1. Look for known favorable properties - *cheminformatics*
2. Extra(intra)polate onto new molecules – *machine learning*

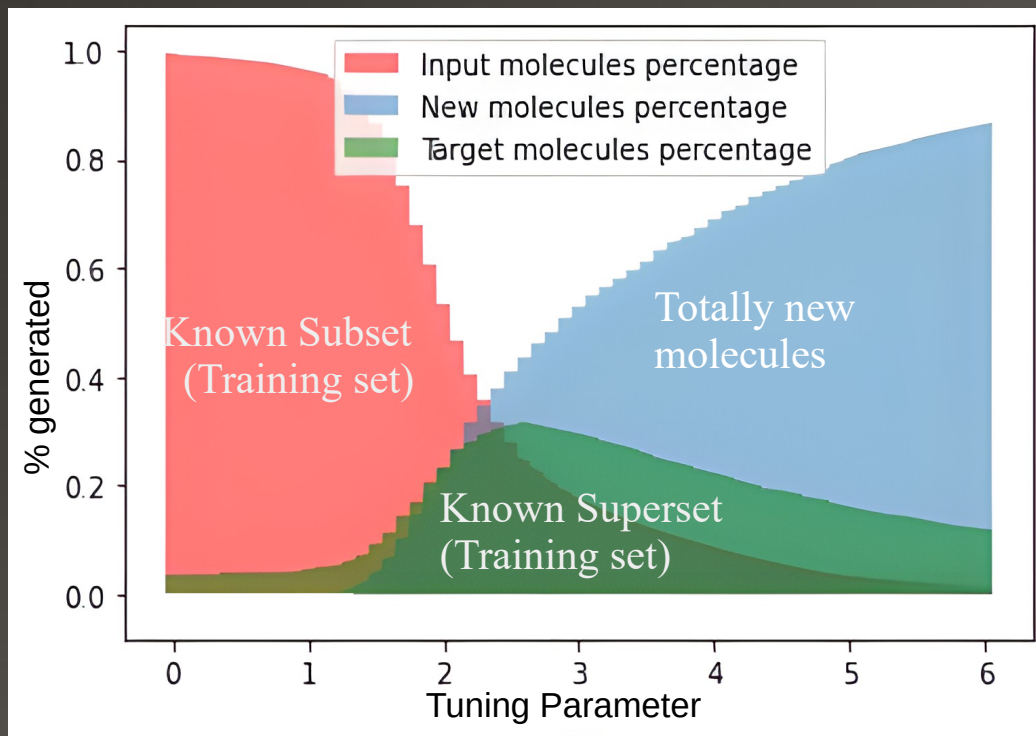
# ML for DM Direct Detection

Property prediction

Energies & Matrix elements

Molecular Generation

Sample latent space  $\rightarrow$  new molecules



Using exhaustive database (< 9 atoms)

Characterize neural nets

$\rightarrow$  Possible to learn from small subsample

Next: Large but sparse dataset up to 10s of atoms

Scale architecture

$\rightarrow$  Generate candidate molecule *shortlist*

[CB, Cook\*, Smirnov: 2404.xxxxx]

# Future Experiment

## Experimental Deployment

The DIANA experiment

Daily modulation from an Intrinsically Anisotropic Array

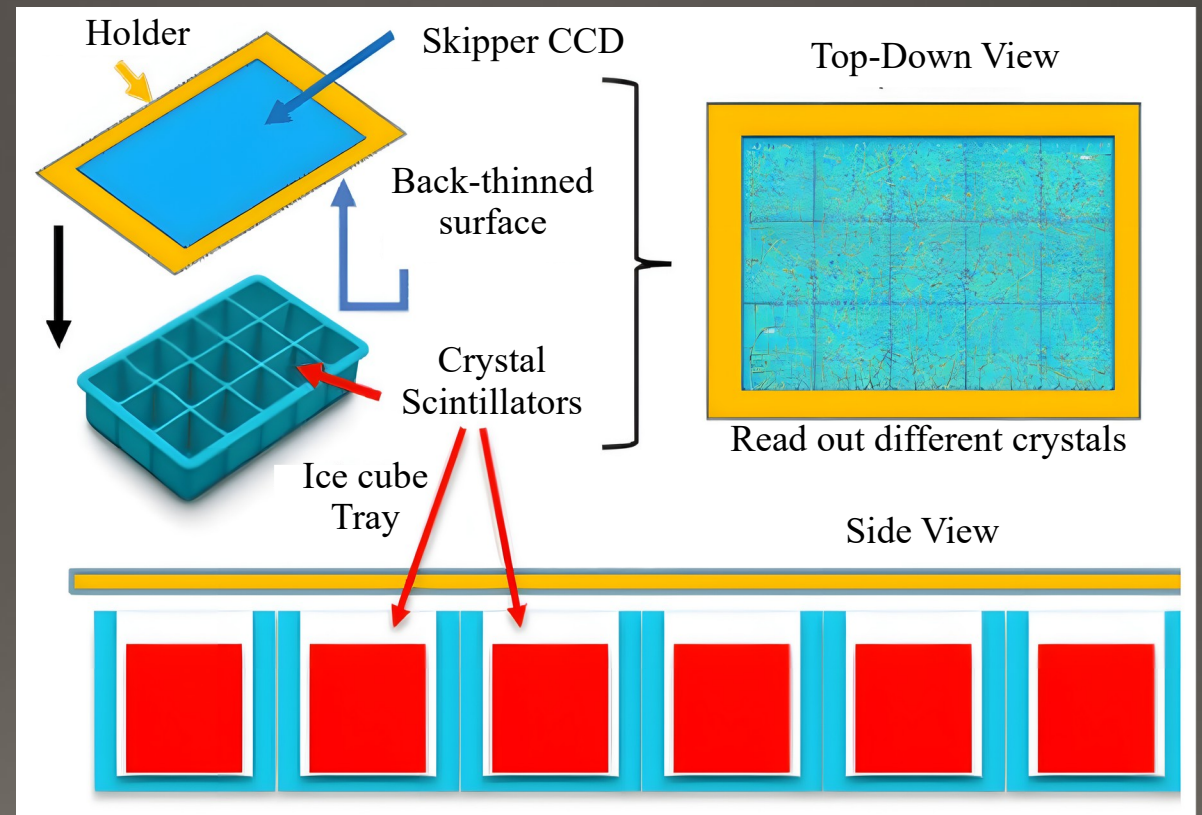
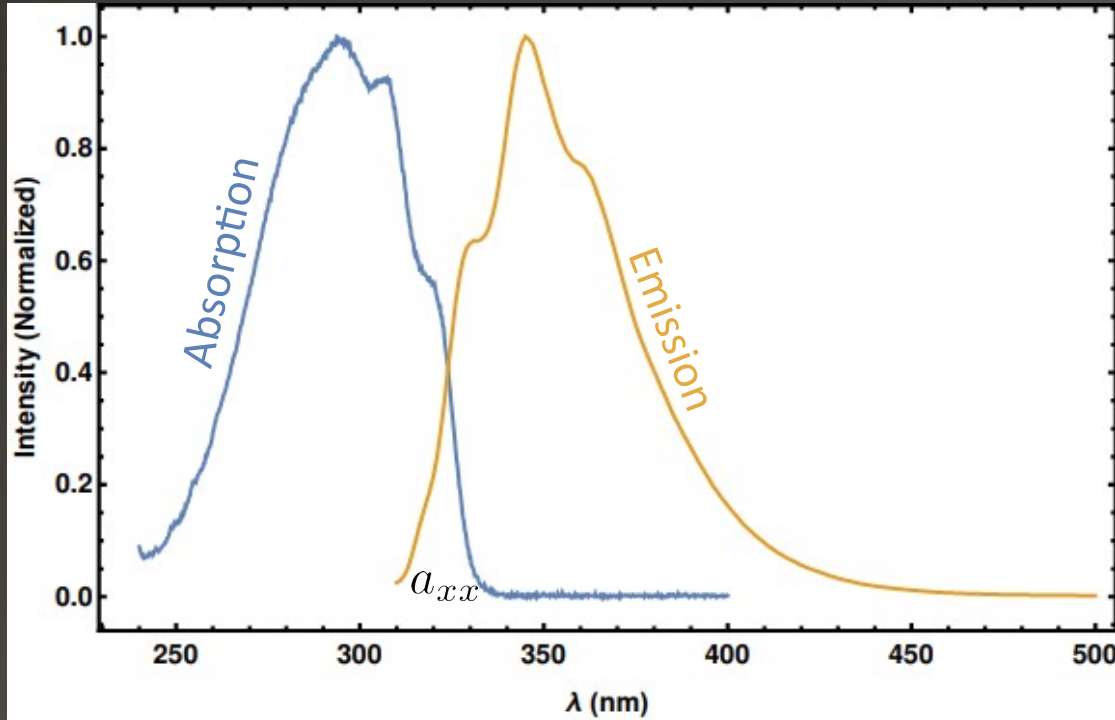


Fig: Dan Baxter

Collab: Uchicago, FermiLab, Northwestern, MIT, and UIUC

# Fluorescence with DM Works



**Focus**  
Minimize background

## Option 1

Reduce background in the excitation.

*Molecular crystals*

Anisotropic excitation → Time-varying DM signal

## Option 2

Reduce background in the emission.

*Quantum dots*

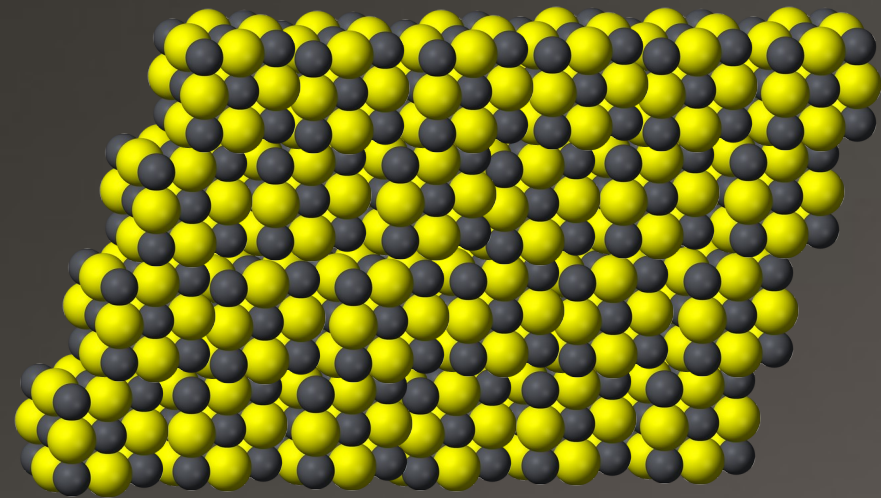
Multiple excitons → Time-coincident DM signal

# Nanocrystals: Quantum Dots

Quantum confinement affects long-wavelength physics

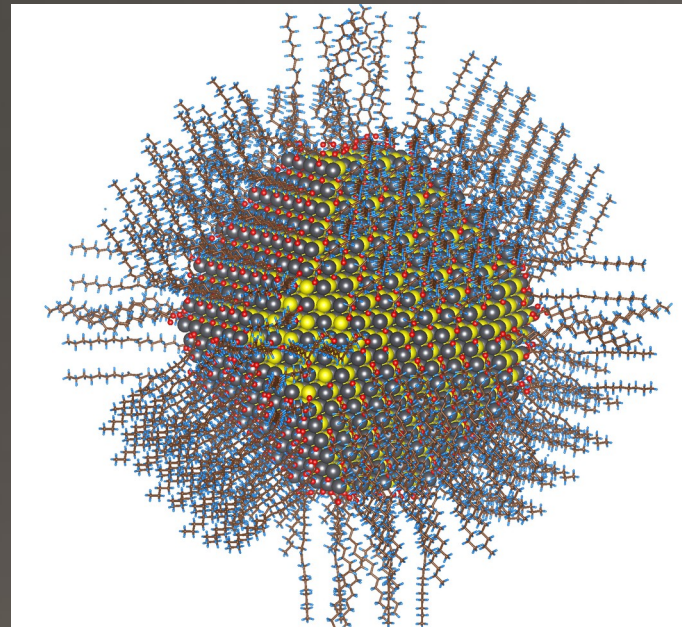
Quantum confinement

Example: PbS



$R \rightarrow \infty \text{ nm}$

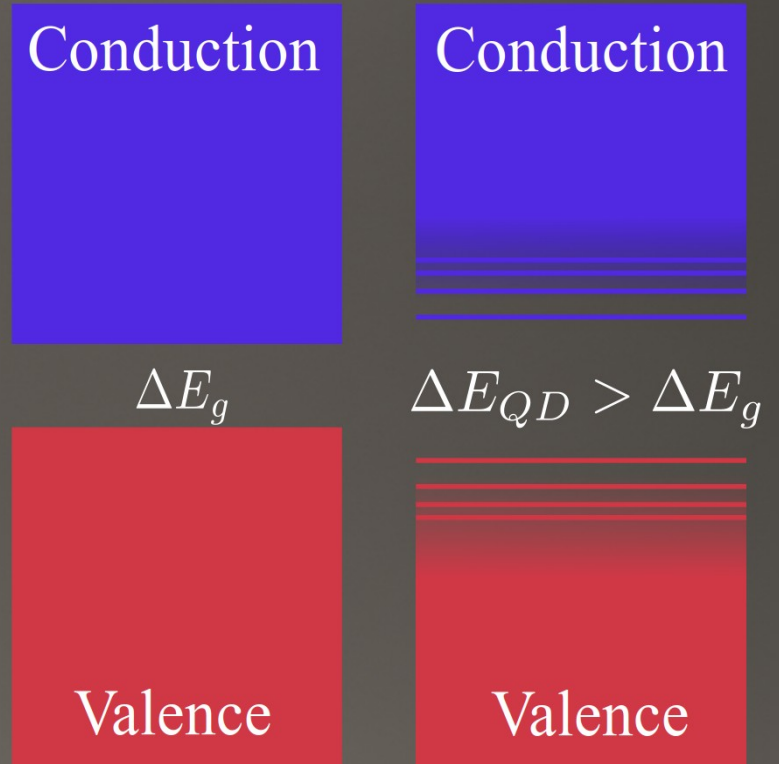
$$|\psi_i\rangle \sim u_{\text{Bloch}}(r) e^{ik \cdot r}$$



Zherebetskyy et al., Science 344, 1380 (2014)

$R \sim \mathcal{O}(\text{few nm})$

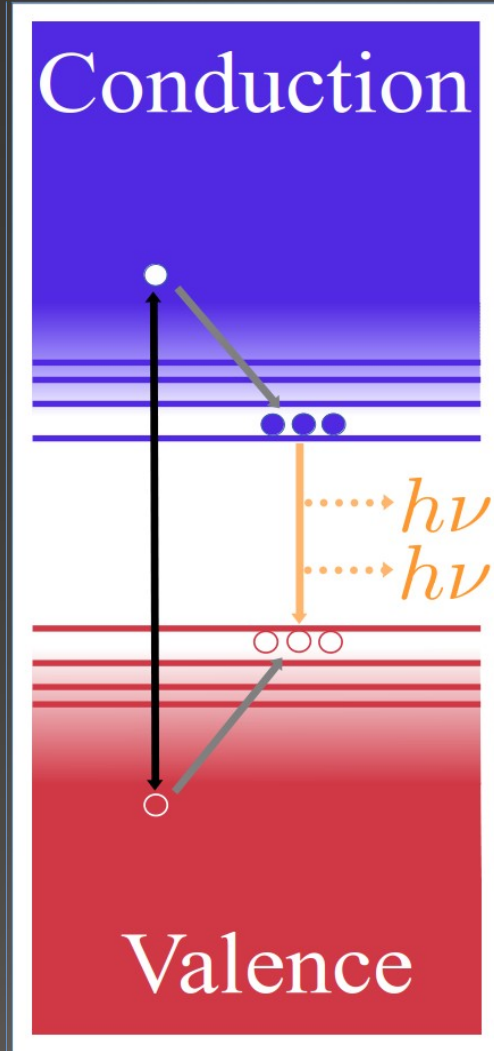
$$|\psi_i\rangle \sim u_{\text{Bloch}}(r) \psi_{\text{bound}}(r)$$



$E(k)$



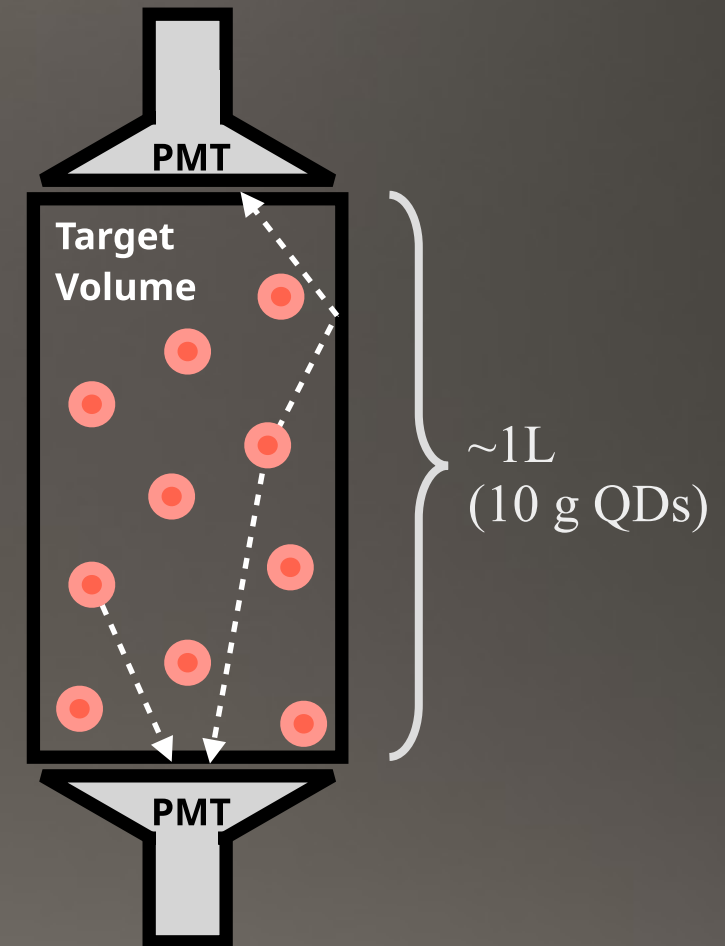
# Quantum Dots: Coincident Signal



Absorption  $\rightarrow$  *Very energetic exciton*

Multi-exciton generation  $\rightarrow$  several excitons  
If energy is greater than twice the bandgap

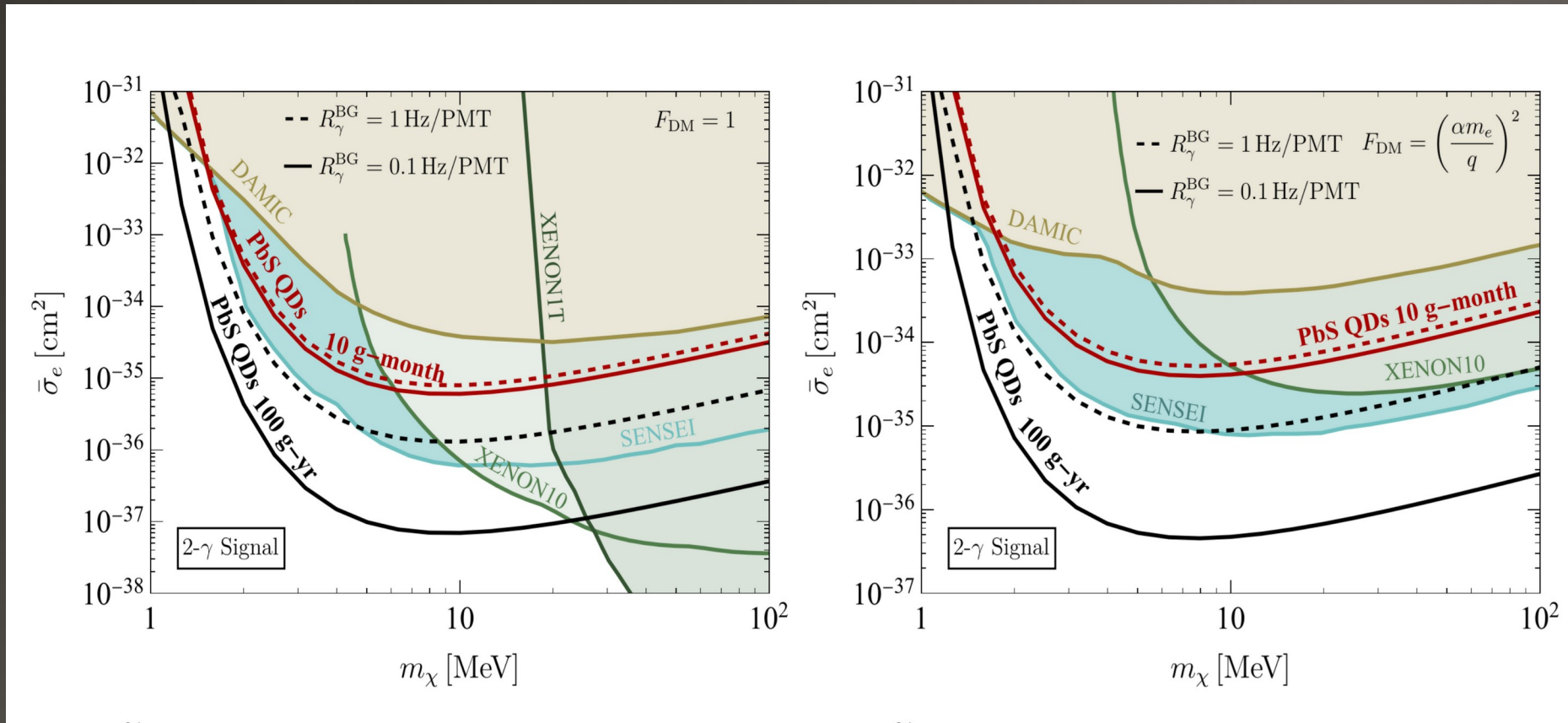
Radiative recombination  $\rightarrow$  coincident photons  
Band-edge excitons produce light



# PbS Quantum Dots

(Contact interaction)

(Long-range interaction)



[CB, Essig, Fernandez-Serra, Ramani, Slone: 2208.05967]

With realistic dark rate for photodetectors.

# Future Experiment

## Experimental Deployment

DarkDot & The QUADRA experiment

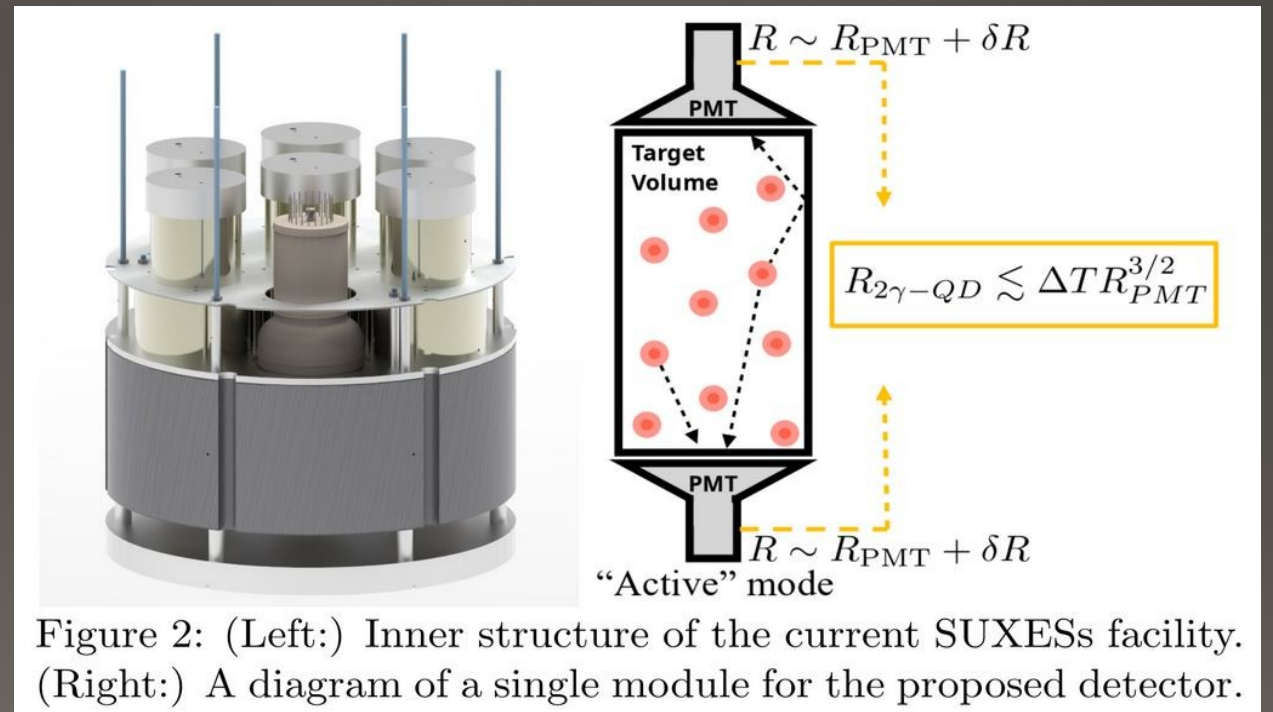
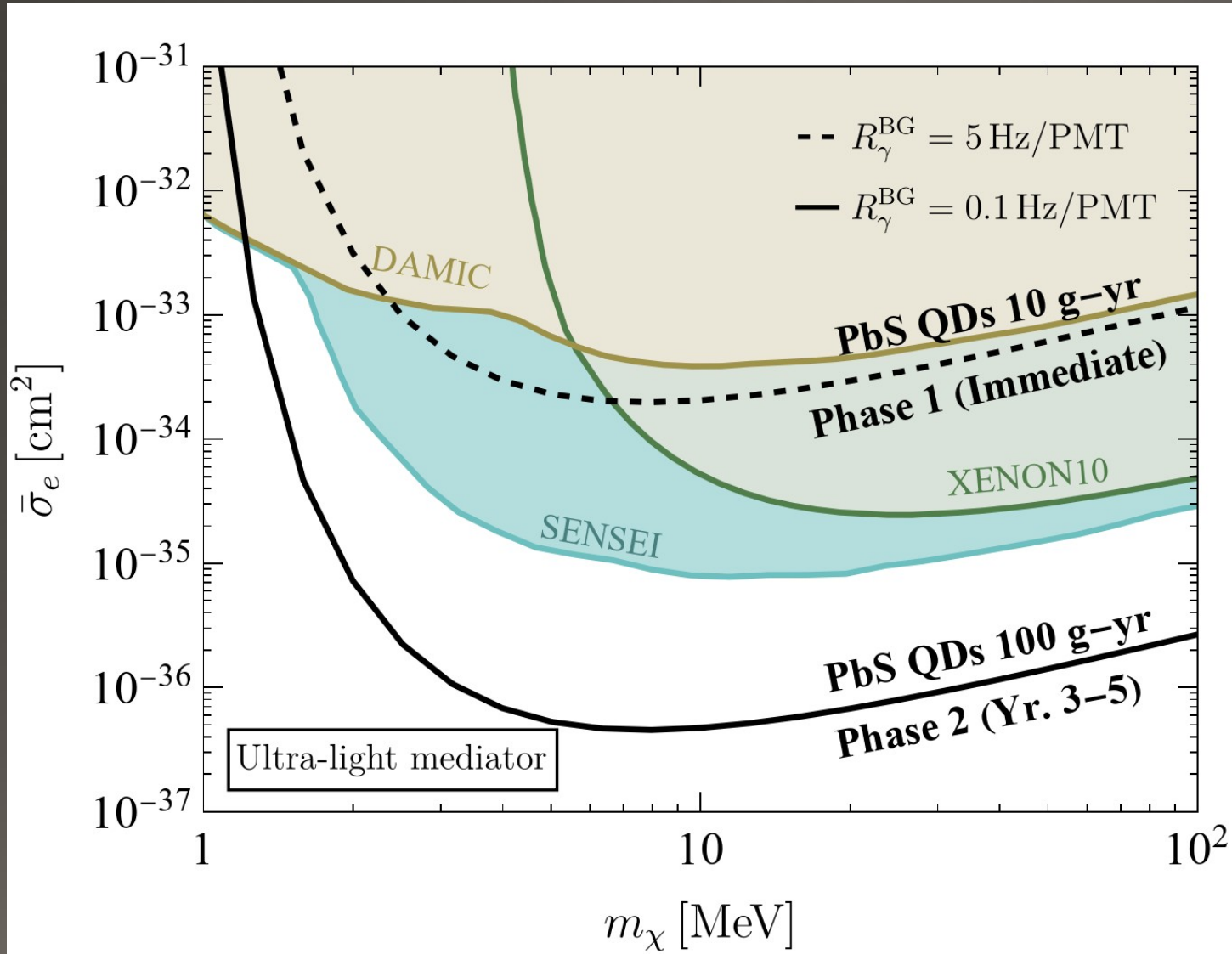


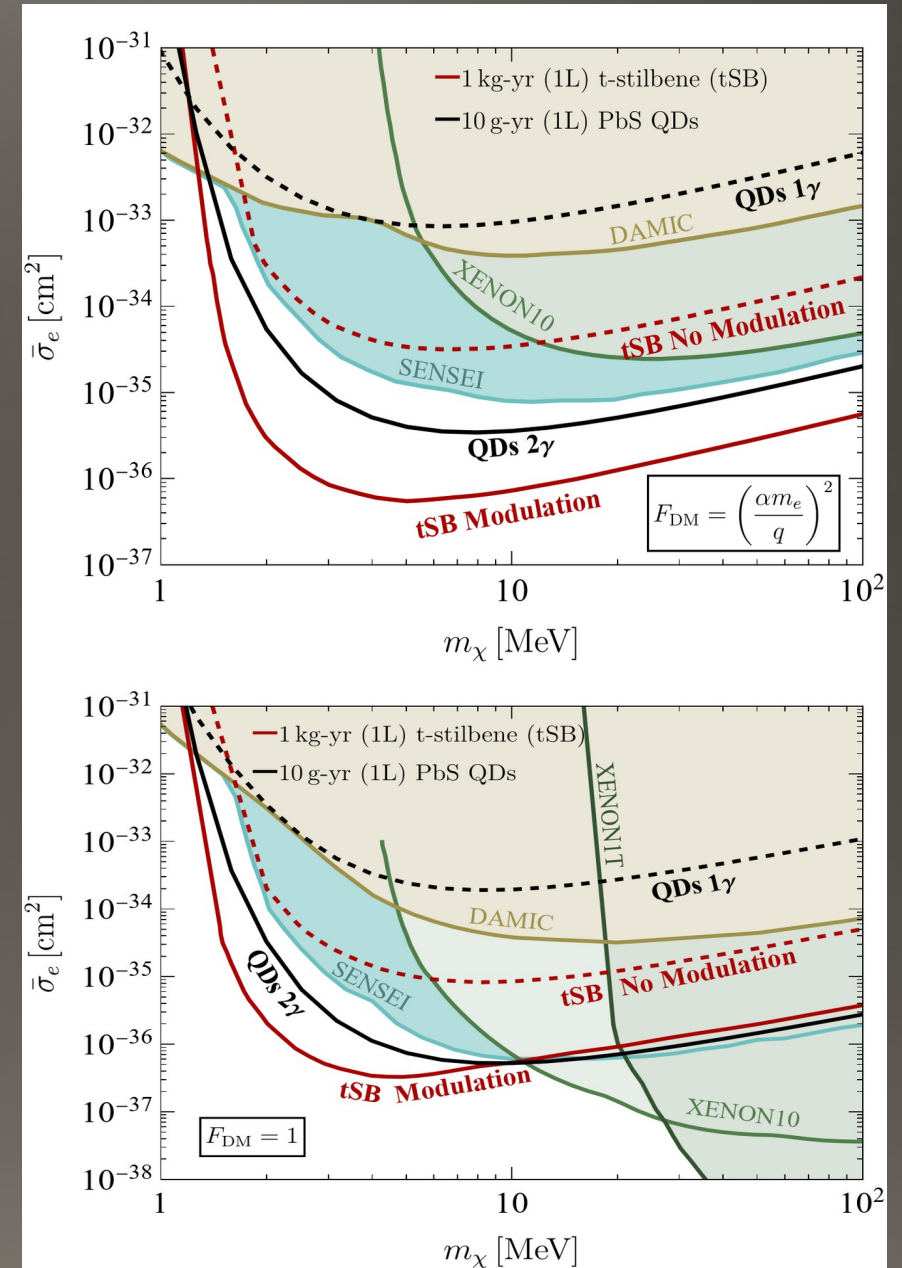
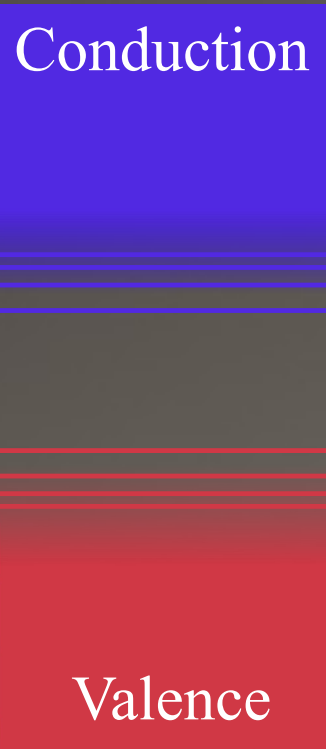
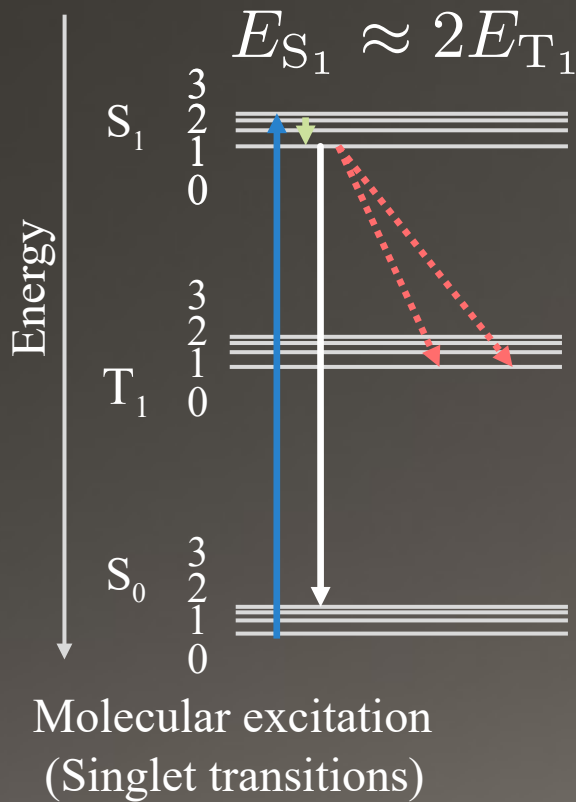
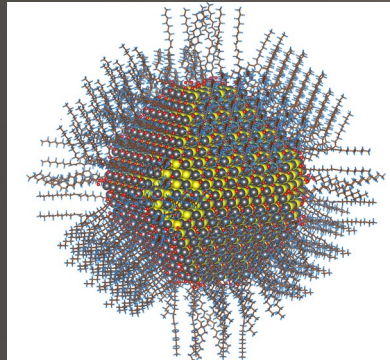
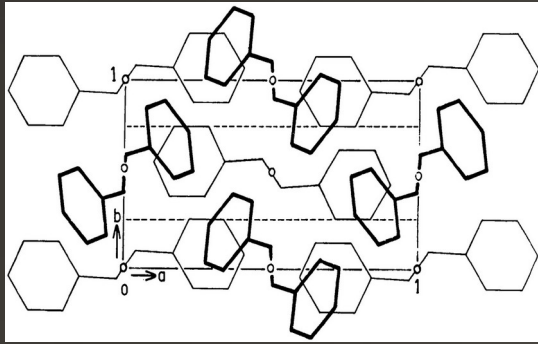
Figure 2: (Left:) Inner structure of the current SUXESs facility. (Right:) A diagram of a single module for the proposed detector.

Fig: Joern Mahlstedt Collab: Stockholm U, MIT, & Stony Brook

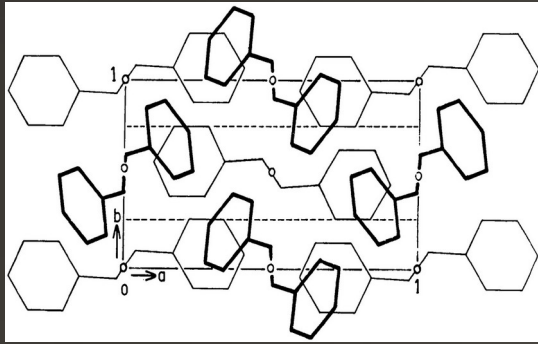
# Deployment



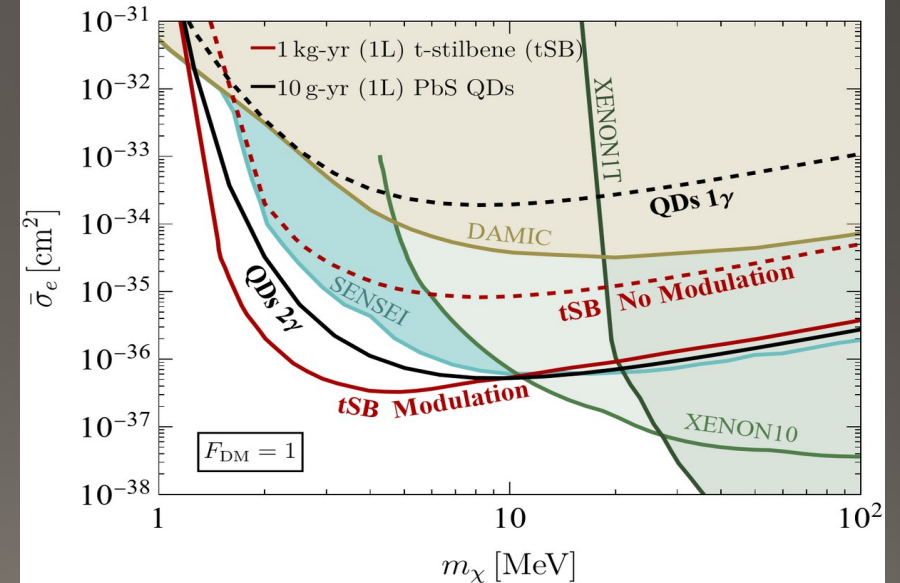
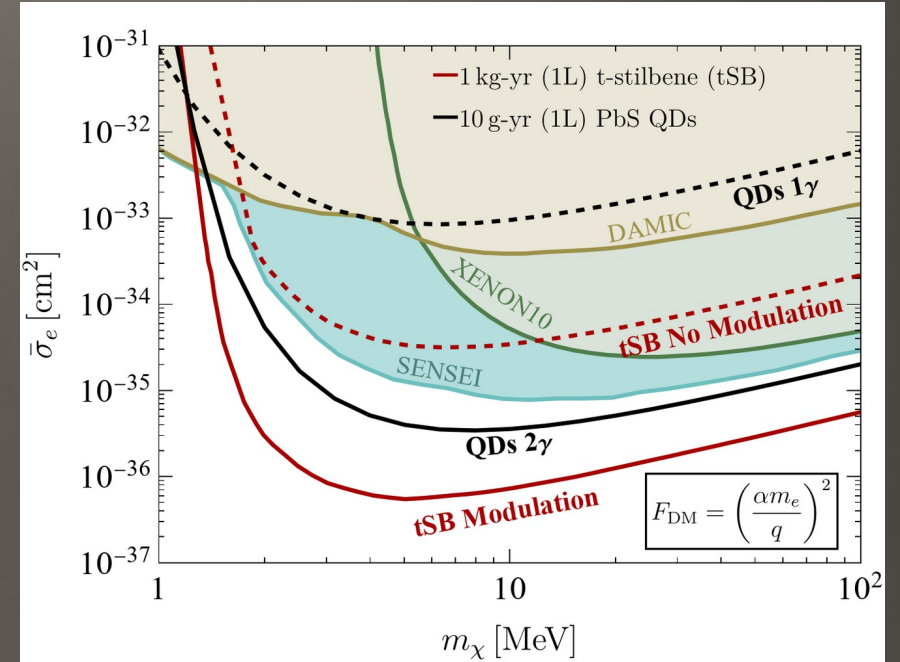
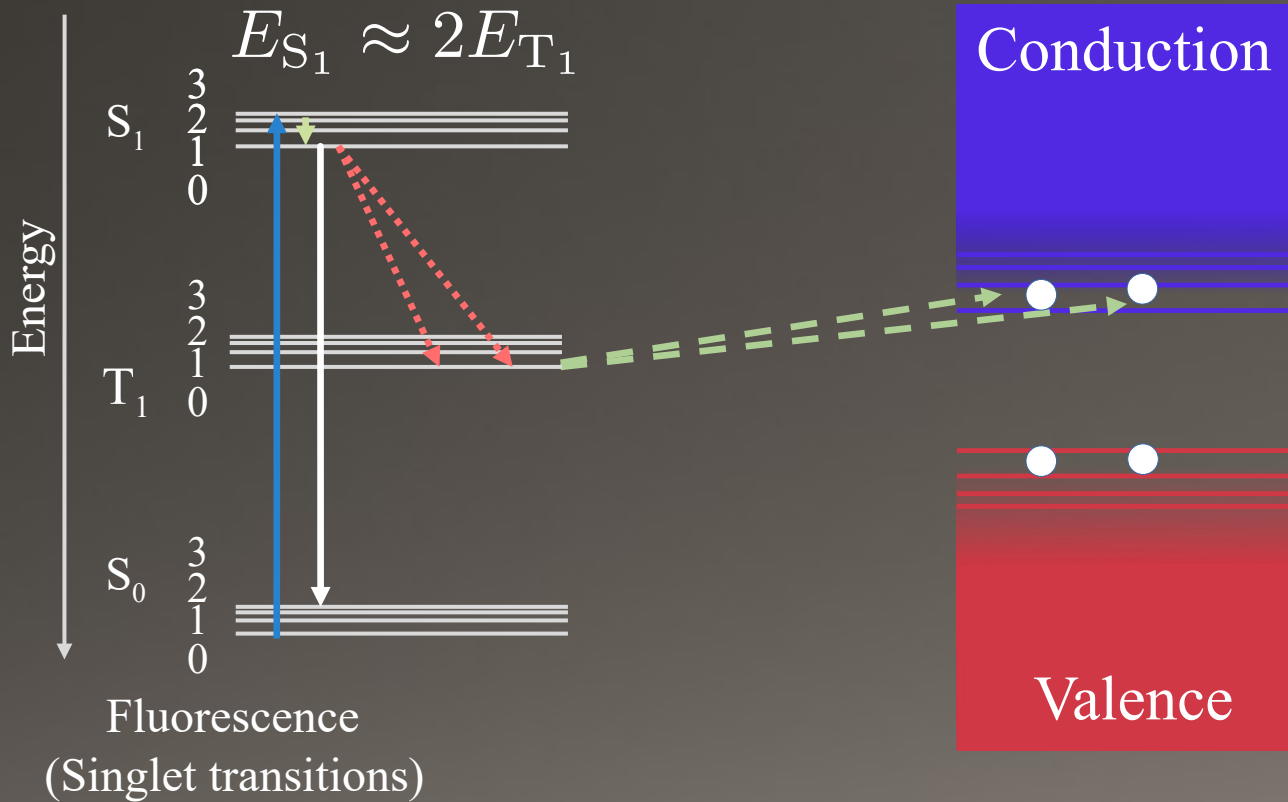
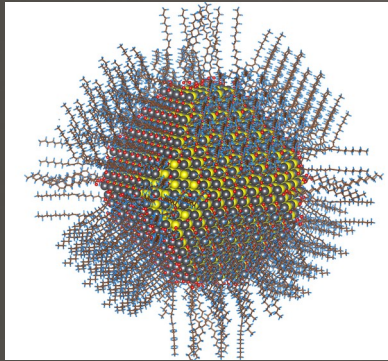
# Hybrid Detectors



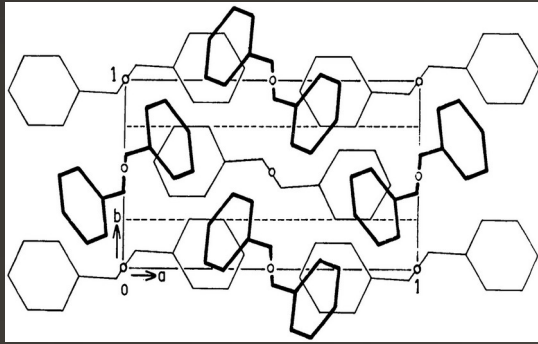
# Hybrid Detectors



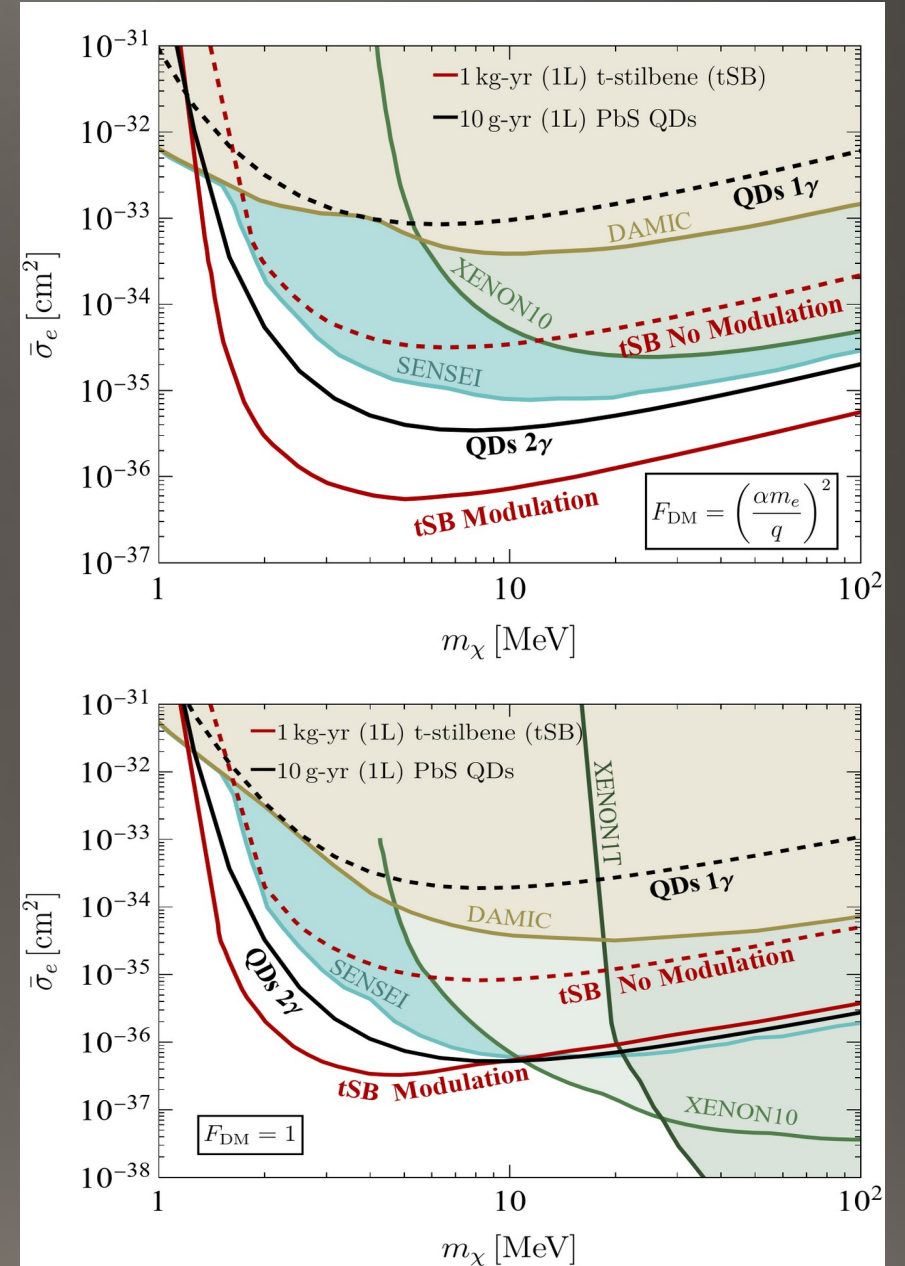
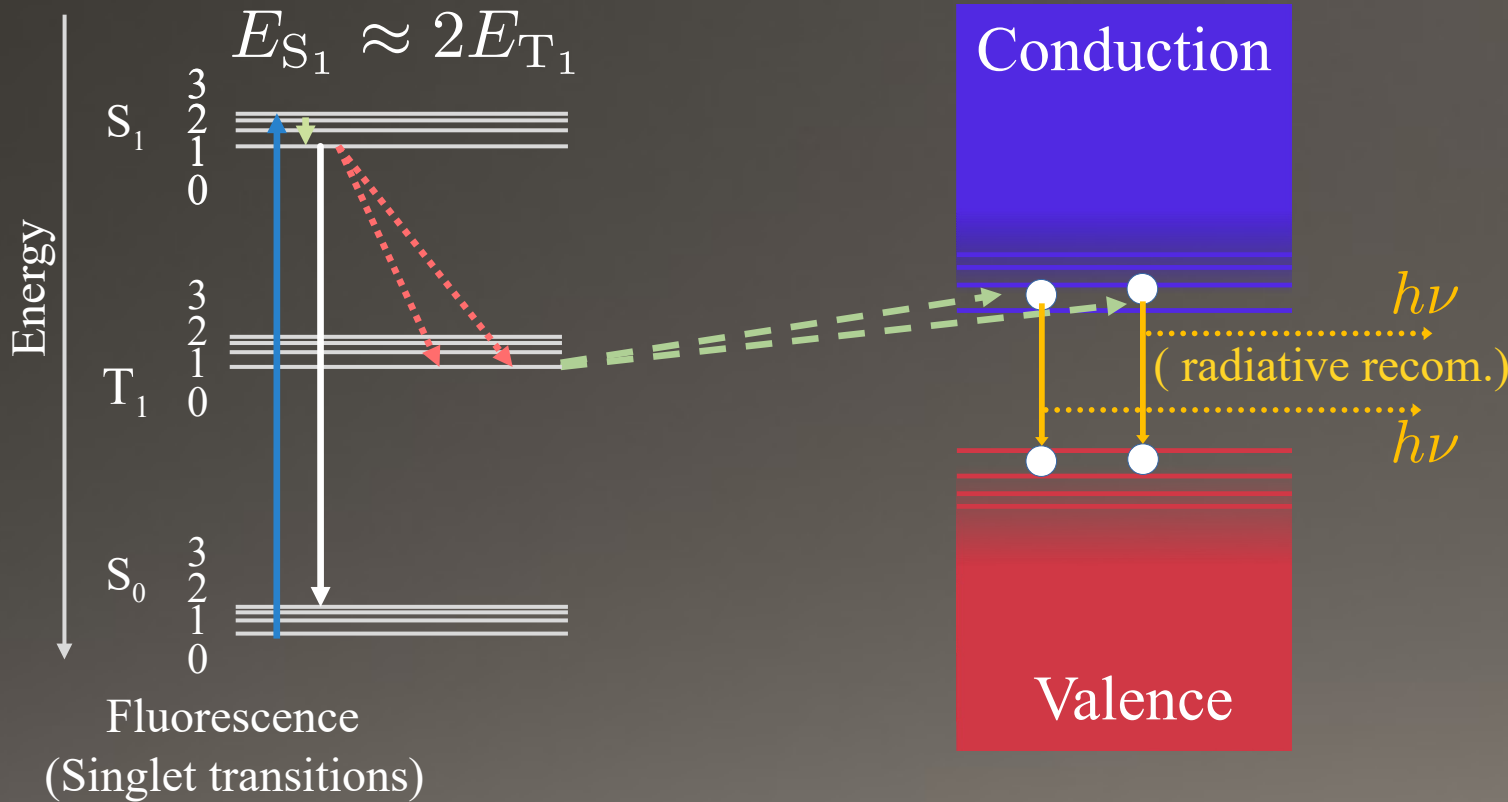
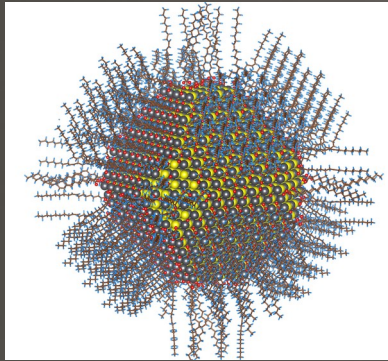
(Charge Transfer)



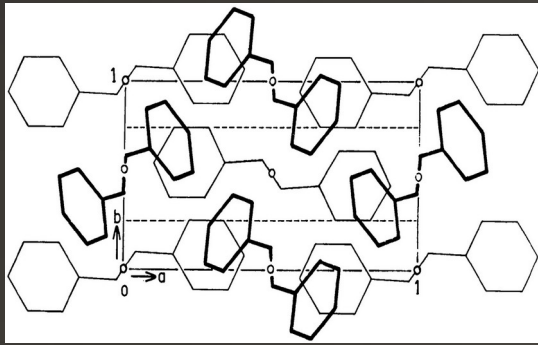
# Hybrid Detectors



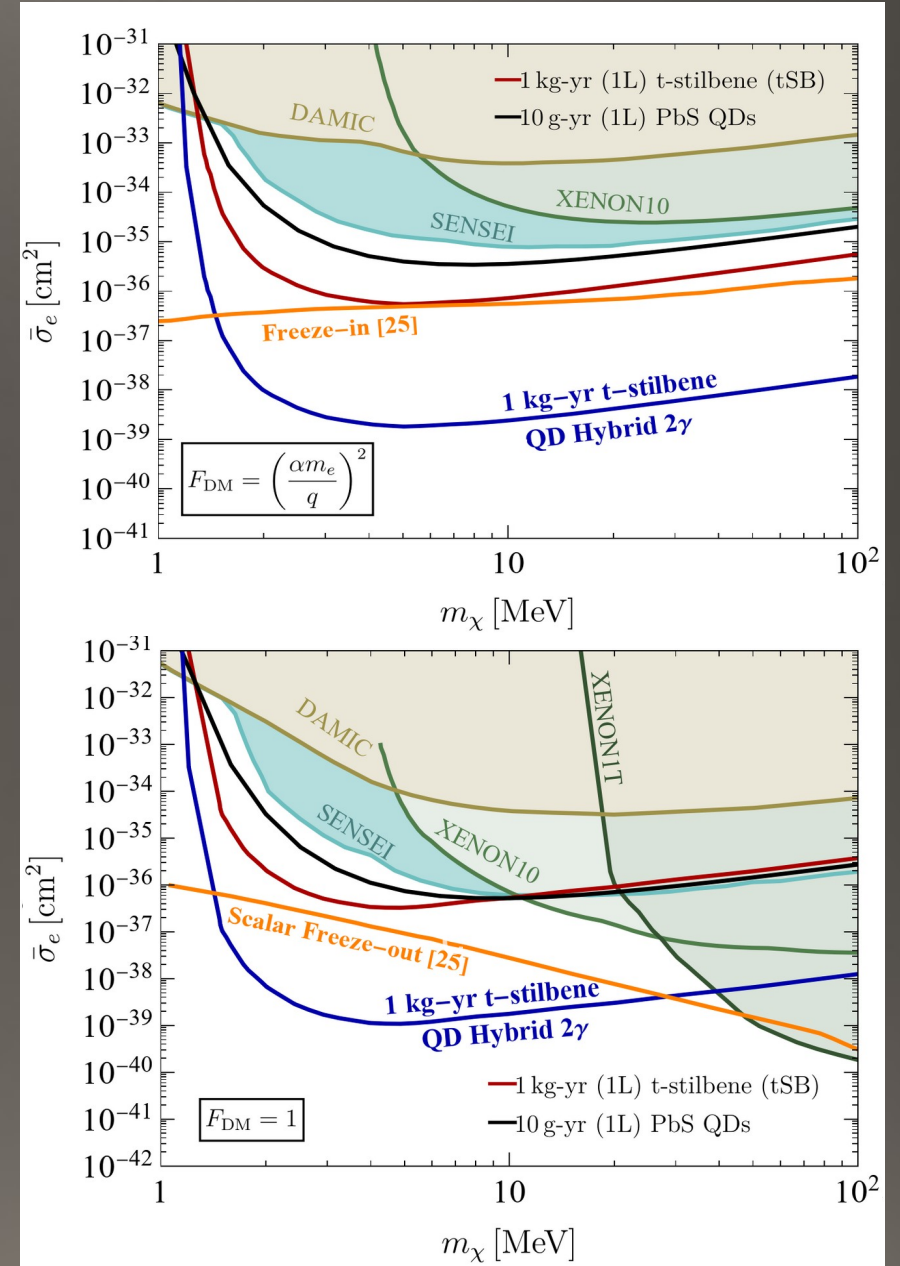
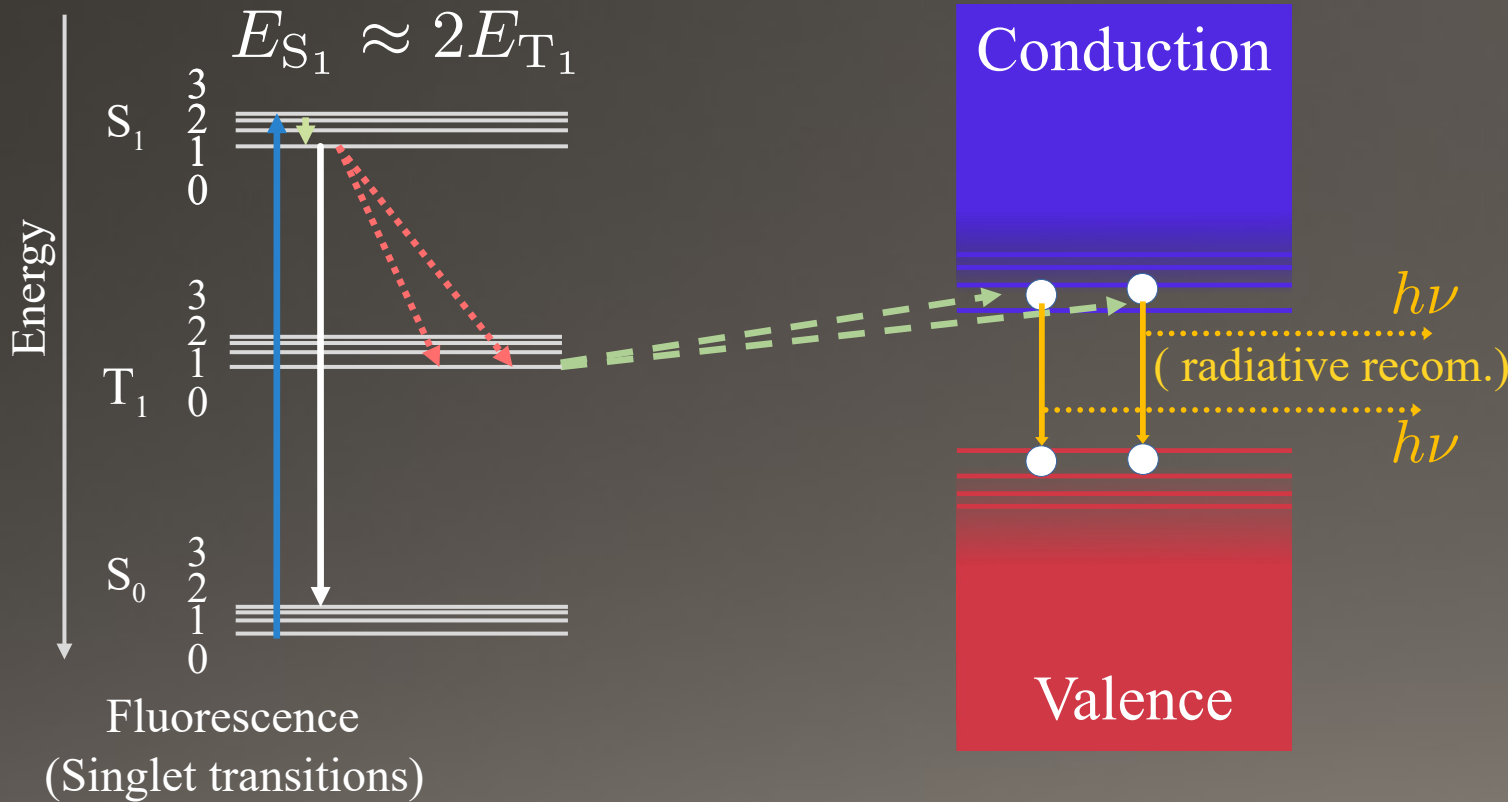
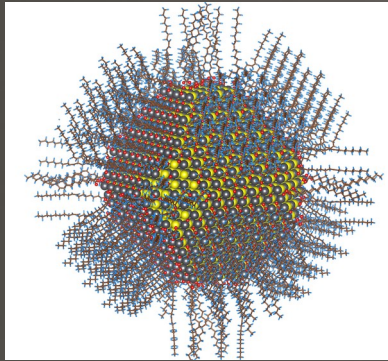
(Charge Transfer)



# Hybrid Detectors

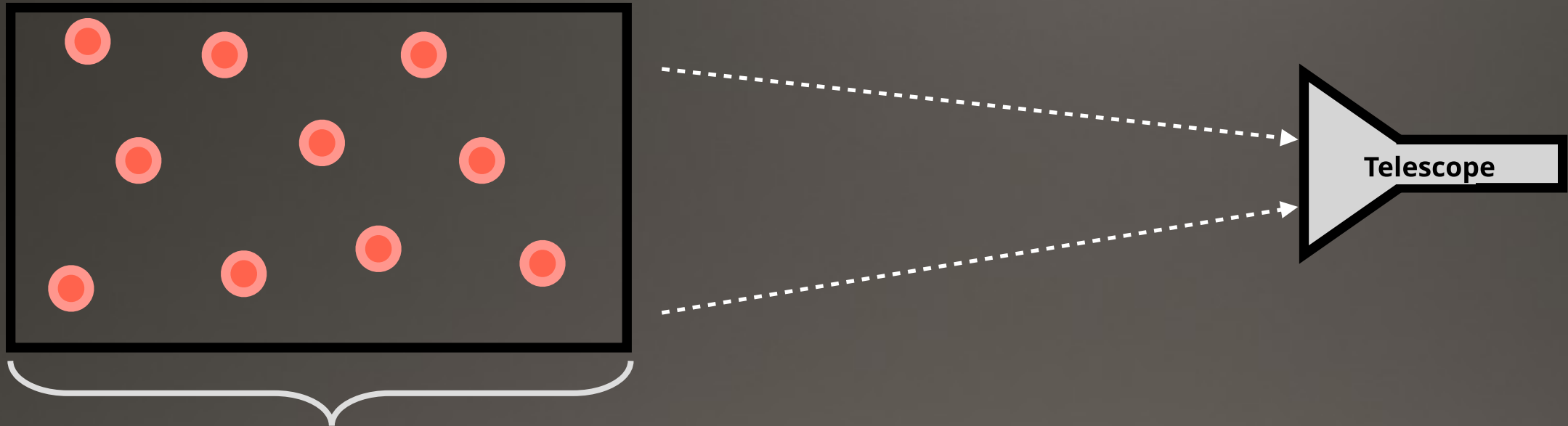


(Charge Transfer)





# Beyond direct detection



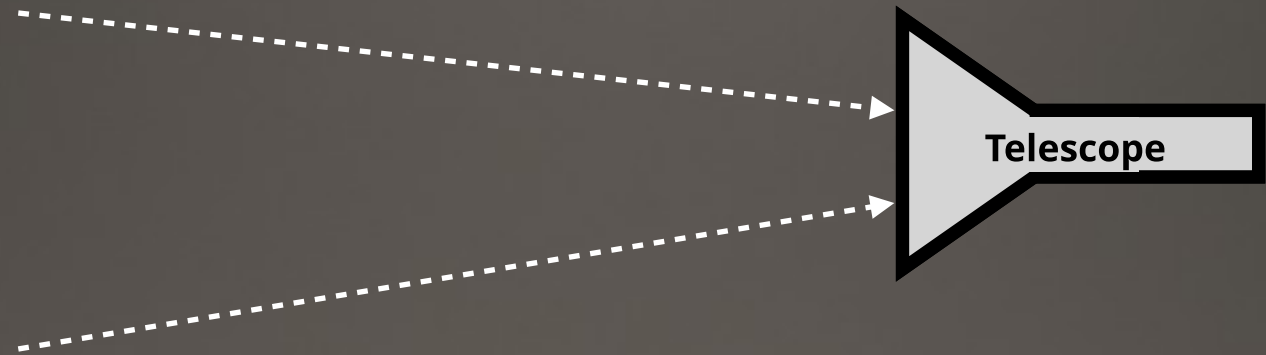
Astrophysical volume of molecules

Same theoretical techniques → Predict rates in *astrophysical* objects

# Beyond direct detection



Cold molecular cloud



Same theoretical techniques  $\rightarrow$  Predict rates in *astrophysical* objects

# Dark matter in Molecular Clouds



→  
~ 0.5 ly

Dense cold molecular clouds are almost entirely opaque.

$$n_{\text{H}_2} \sim O(10^2)\text{cm}^{-3}$$

Ionization from CR produces ionization fraction:  $\zeta^{\text{H}_2}$



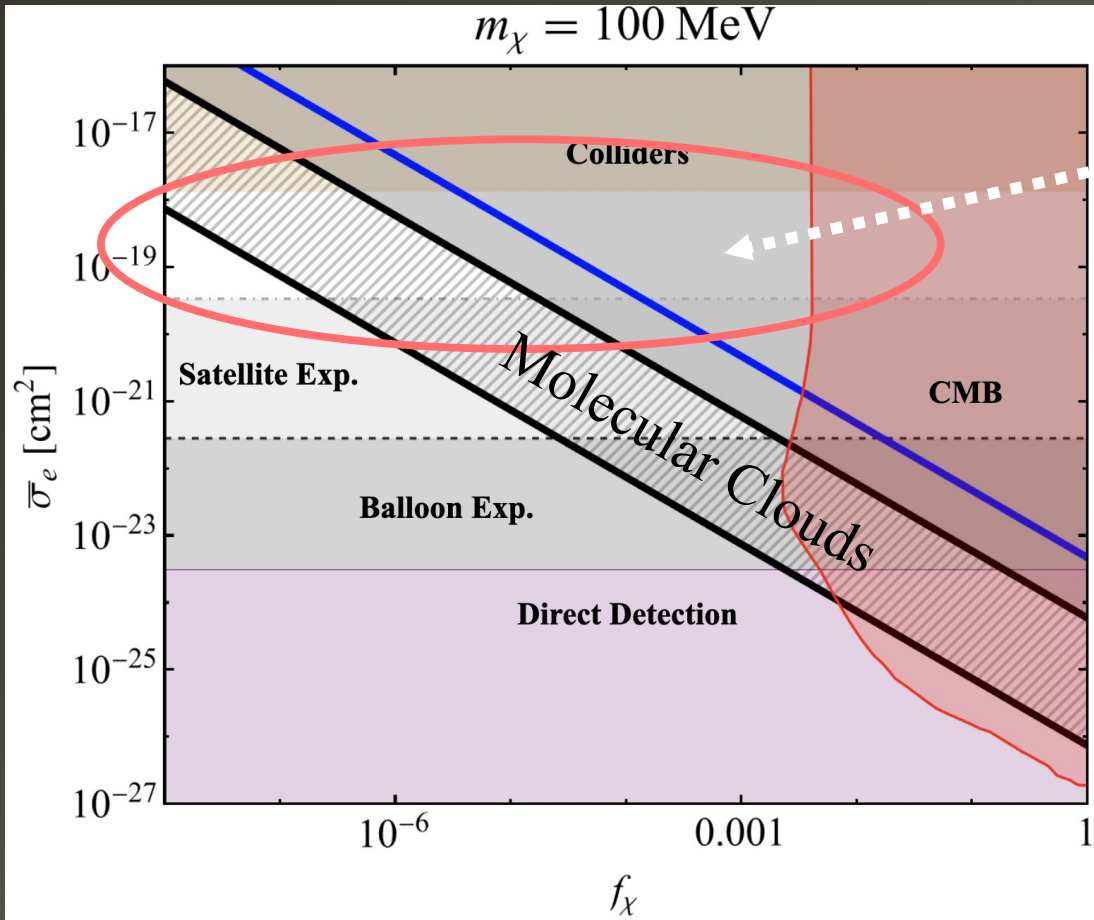
Well measured through astro-spectroscopy of tracer molecules  
(line intensity measurements)

**DM scattering → Add ionized SM particles**

$$\zeta_i^{\text{H}_2} = 2\pi \int \frac{dN_i}{dE}(E)\sigma_i(E)dE$$

# Dark matter in Molecular Clouds

## Constraints on DM w/ ultra-light mediator



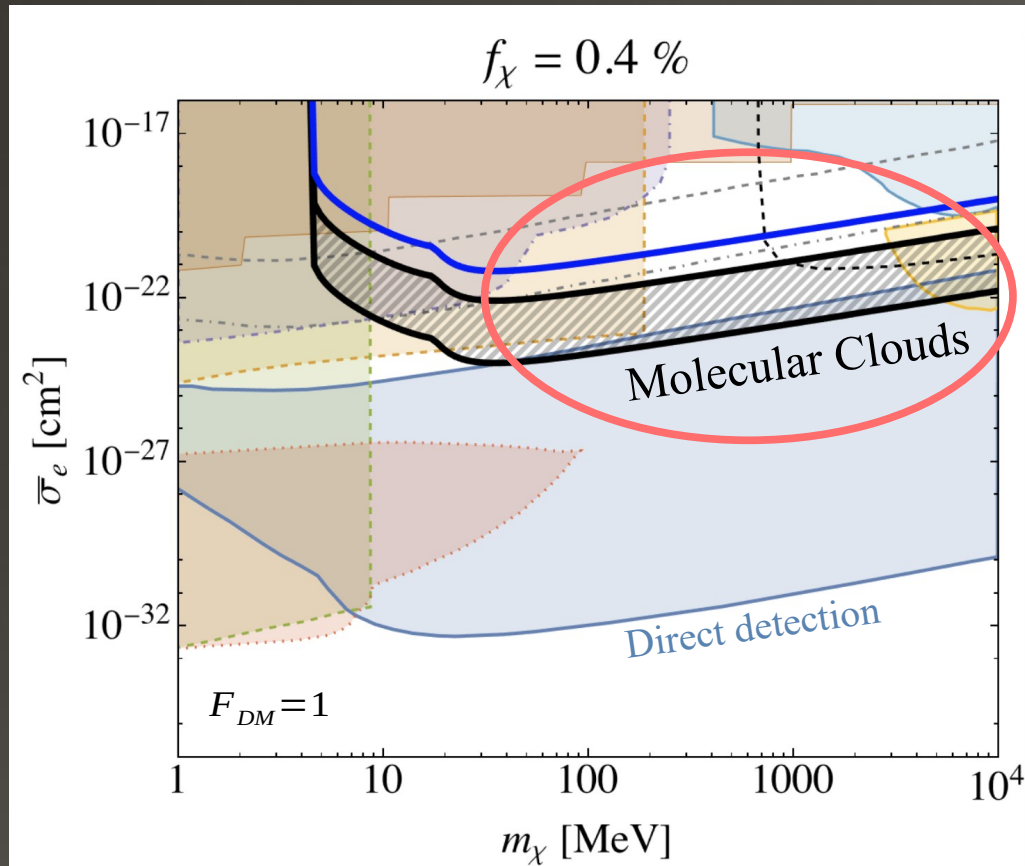
Otherwise open parameter space

Strongly-coupled dark matter is stopped before reaching experiments.

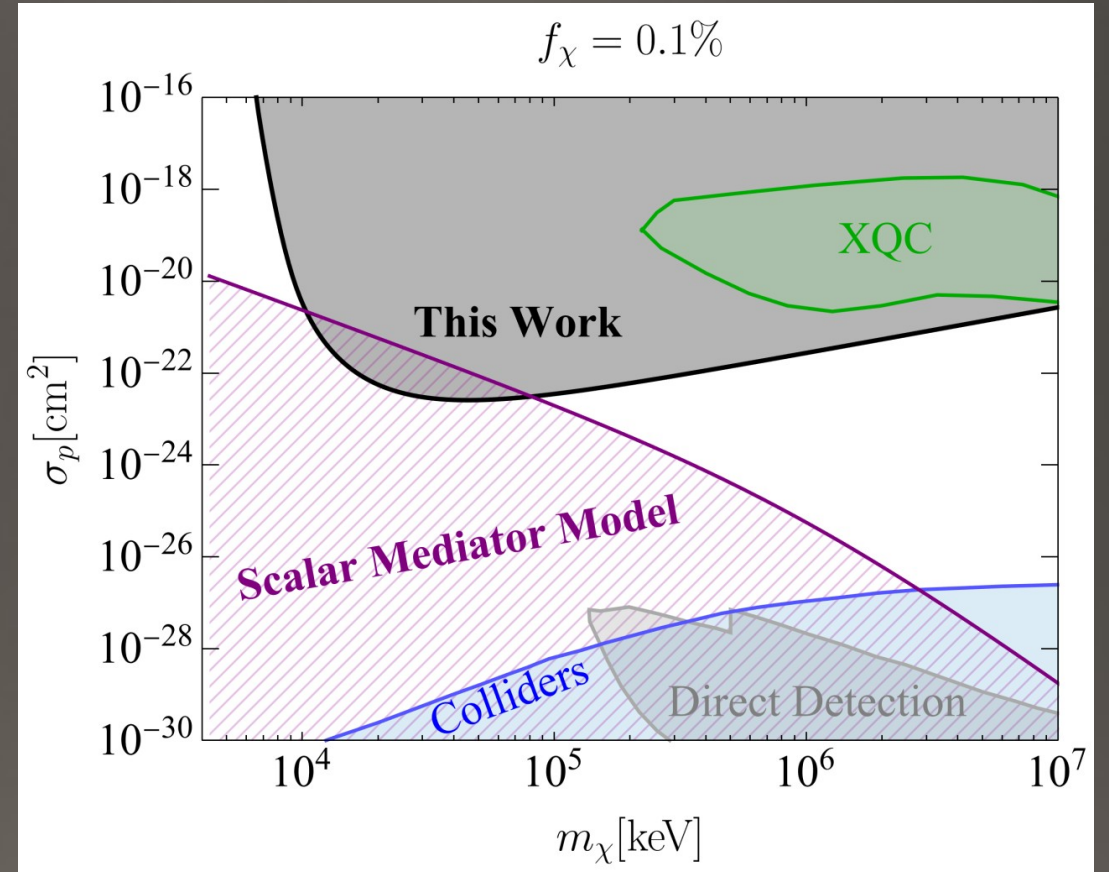
\*Uncertainty from inferred CR ionization rate due to gas depletion onto grain surfaces.

[Prabhu,CB: 2211.05787]

# Dark matter in Molecular Clouds



[Prabhu,CB : 2211.05787]



[CB, Harris, Kahn, Prabhu: 2310.00740]

The Molecular Migdal effect(s) *in space*

# Conclusions

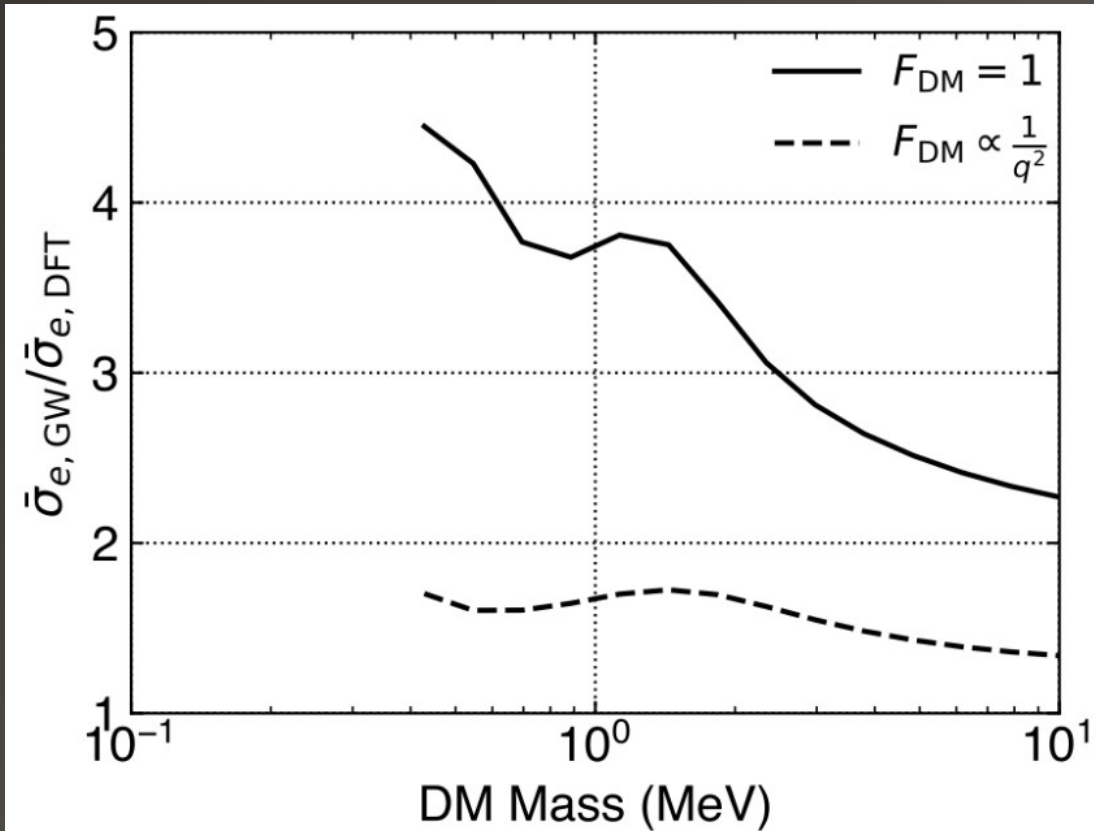
- Successful campaign for WIMPs → Now we must look beyond.
- By developing the formalism that describes the interaction between dark matter and molecules or nano-materials, we can propose detection strategies capable of *delving deep* and *searching wide* across the dark matter parameter space.
- This remains one of the few ways to probe *high-energy* physics at the *bench-top* scale.
- Stay tuned for hybrid methods giving multiplicative improvements to sensitivity.

# Acknowledgements

- **Grad Students:** Ian Harris (UIUC), Sandip Roy (Princeton), & Cameron Cook (Edinburgh --- soon Liverpool)
- **Collaborators & colleagues:** Ani Prabhu, Yoni Kahn, Ben Lillard, Juan Collar, Jesus Perez-Rios, Rouven Essig, Hari Ramani, Oren Slone, Dan Baxter, Marivi Fernandez-Serra, Sam McDermott, Ian Harris, Juri Smirnov (In no particular order)
- The work of C.B. was supported in part by NASA through the NASA Hubble Fellowship Program grant HST-HF2-51451.001-A awarded by the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., for NASA, under contract NAS5-26555 as well as by the European Research Council under grant 742104.



# The DFT Problem



[Peterson, Watkins, Lane, Zhu '23: 2310.00147]

DFT is a *ground-state* theory

The systematic uncertainty from *out-of-the-box* DFT can be very large.

## The Alternative

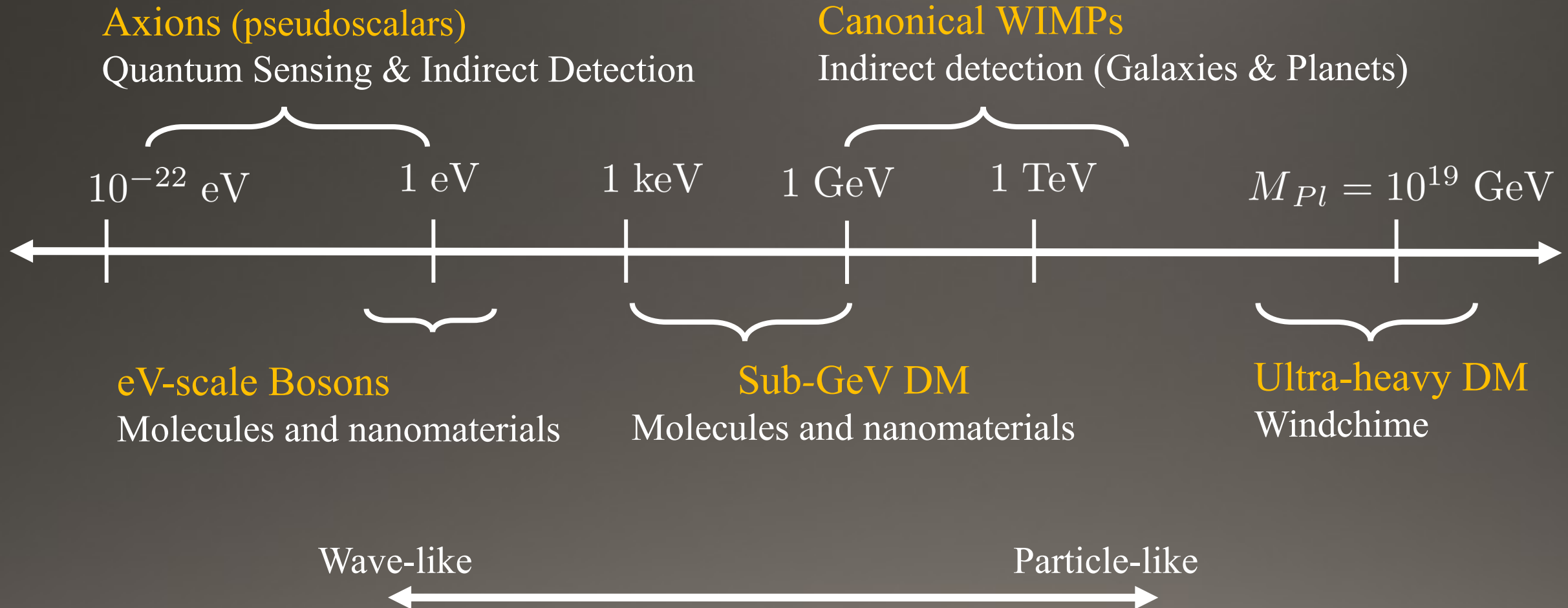
Self-consistent molecular orbital theory

Excited states

$$\Psi_i^j = \frac{1}{\sqrt{2}} (|\psi_1 \bar{\psi}_1 \dots \psi_i \bar{\psi}_j \dots \psi_N \bar{\psi}_N| - |\psi_1 \bar{\psi}_1 \dots \psi_j \bar{\psi}_i \dots \psi_N \bar{\psi}_N|)$$

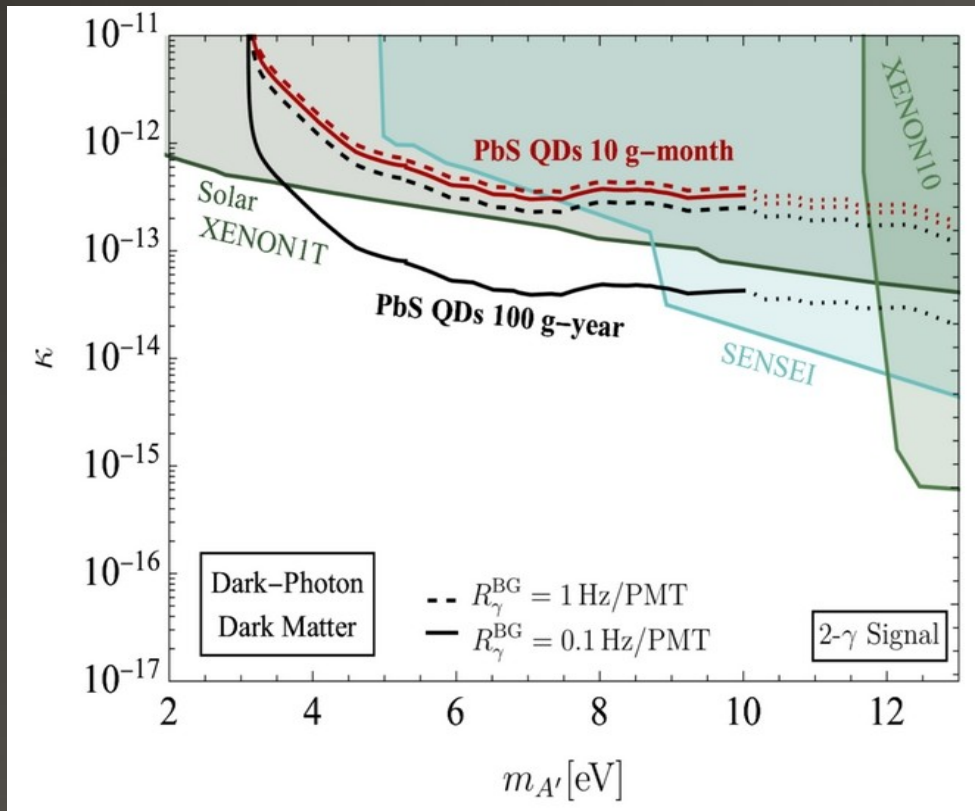


# Many Methods in One Program



# PbS QDs

Dark photon kinetic coupling



[CB, Essig, Fernandez-Serra, Ramani, Slone: 2208.05967]

In the case of eV-scale dark photon absorption, we can use existing *data* to predict the sensitivity of QD-based detectors.


## Key conclusions of QD analysis

- 1) The interaction rate in a semiconductor generated by DM is the same if the semiconductor is *monolithic* or *nanoscopically* disperse.
- 2) In a QD-based experiment, the readout is independent of the target.
- 3) The signal can be tuned through control of quantum confinement.

# QDs – Cheap, tunable and scalable

## QDot™ PbS Quantum Dots

\$399.00 - \$2,500.00

 Shipping worldwide

QDot™ PbS (Lead Sulfide) Quantum Dots, oleic acid capped, absorb the light from high energy photons up to near-infrared (NIR) range and re-emit in NIR range. The absorption/emission profiles can be tuned from 800 to 2200 nm, simply by changing nanoparticle sizes from 2 to 12 nm. This material has outstanding light absorption and photoelectrical properties, and is utilised for for near-infrared (NIR) or short-wave infrared (SWIR) image sensors. For specific application convenience, two lines of QDs are available:

- With specific absorption peak in 800 - 2200 nm range
- With specific emission peak in 900 - 1600 nm range [Read more](#)

Absorption/Emission

Emission

Wavelength

1600 nm

Quantity

1g

Form


Toluene 10 mg/mL

[Reset](#)

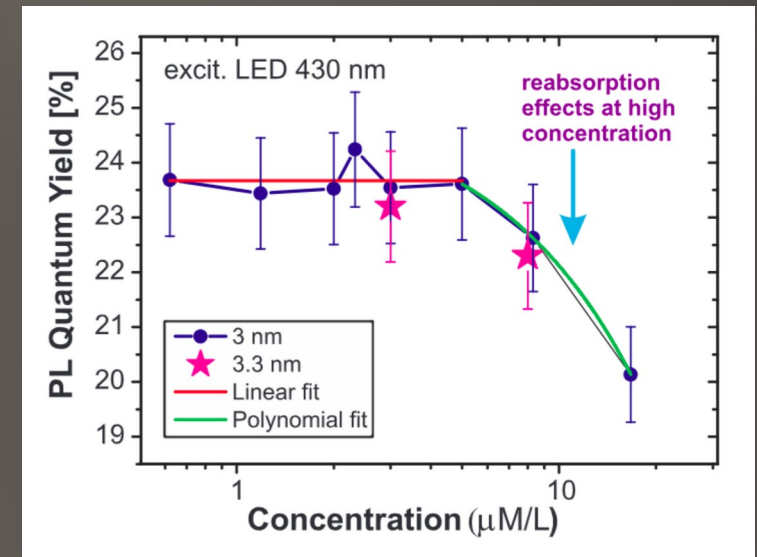
Price for chosen options

**\$1,700.00**

1

 Add to cart

[Contact with our expert](#)



$\Phi$  dependence on the solution concentration for 3nm and 3.3nm PbS QDs in toluene.

$$n_e \sim 10^{20} \text{ cm}^{-3} = 10^{23} \text{ L}^{-1}$$

# Strongly Confining Quantum Dots

Semiconducting nano-spheres



$\xrightarrow{a \ll a_0}$

$$E_{\text{confinement}} = \frac{\hbar^2 \pi^2}{2a^2} \left( \frac{1}{m_e} + \frac{1}{m_h} \right) = \frac{\hbar^2 \pi^2}{2\mu a^2}$$



$$E = E_{\text{bandgap}} + E_{\text{confinement}}$$

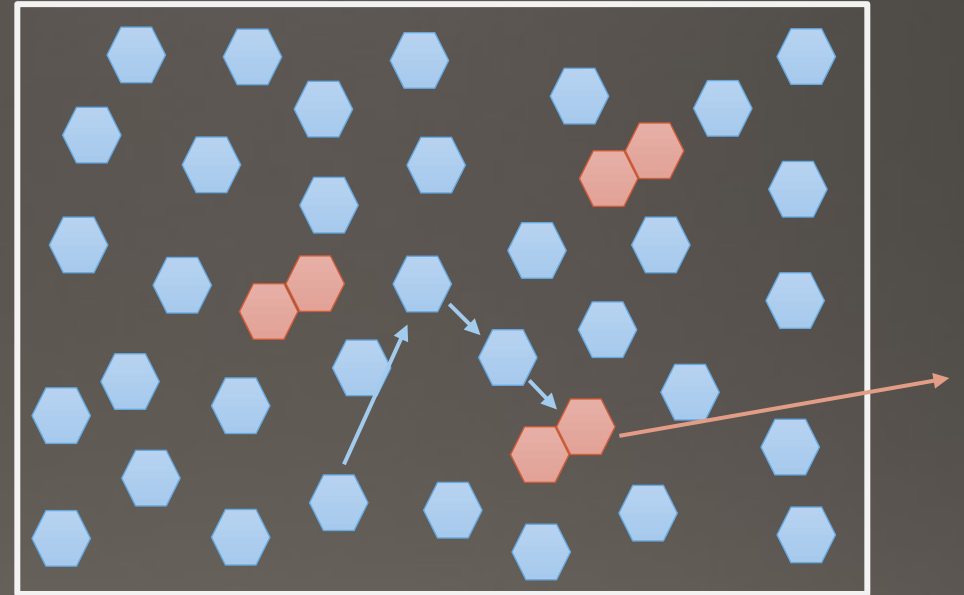
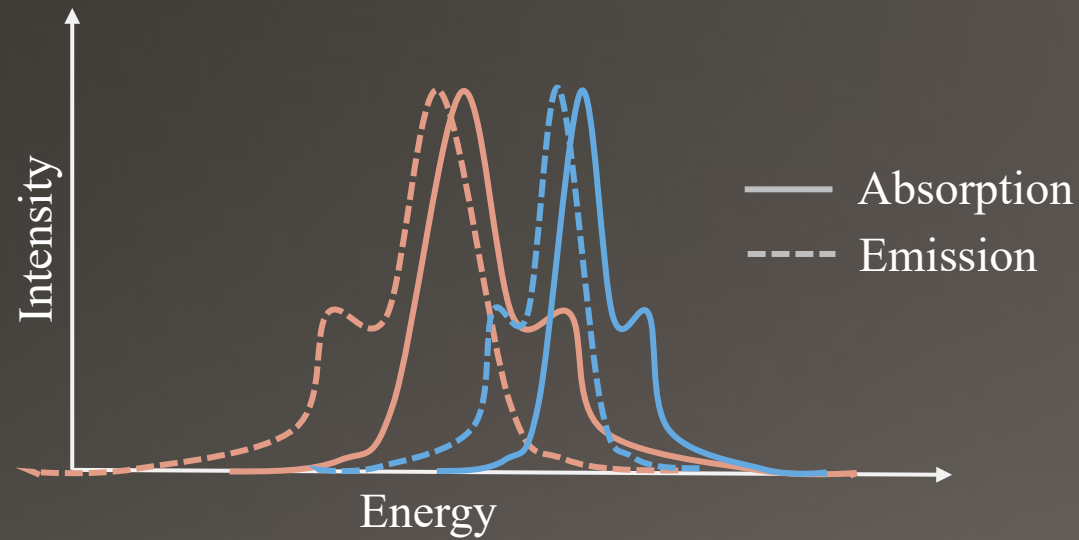
$$= E_{\text{bandgap}} + \frac{\hbar^2 \pi^2}{2\mu a^2}$$

$$E_{\text{kin}} \sim \frac{1}{r^2}$$

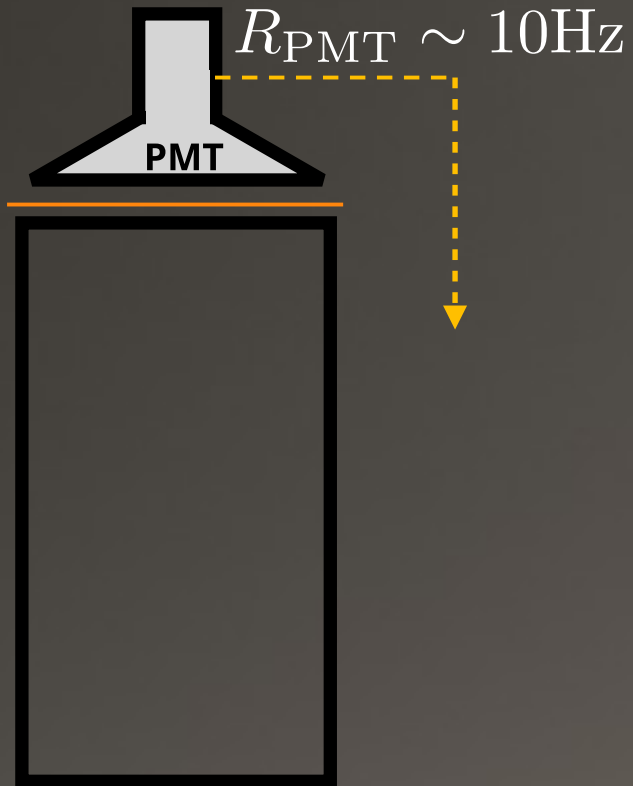
$$E_{\text{coulomb}} \sim \frac{1}{r}$$

# Fluorescence: Binary Scintillators

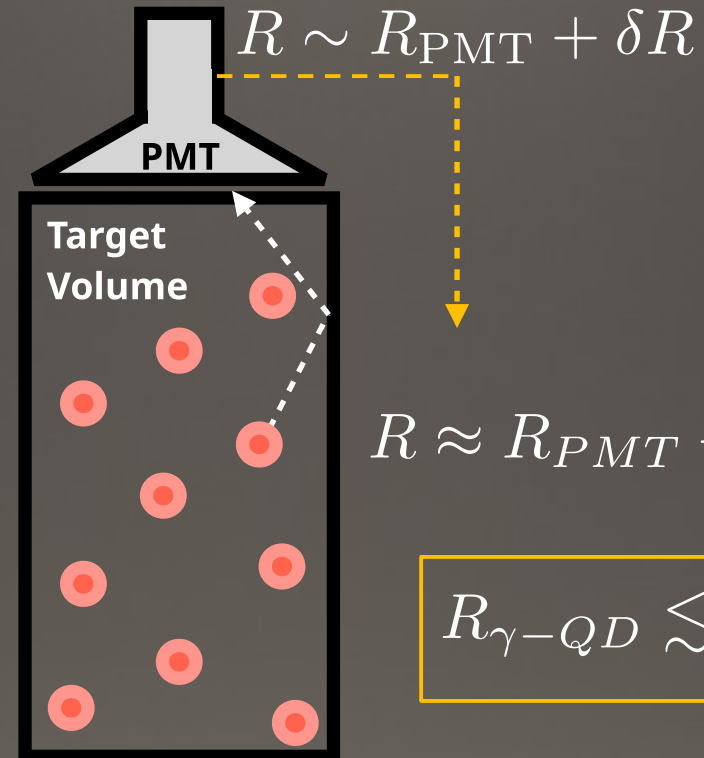
-  Solvent: Primary target starts the signal
-  Solute: Dilute fluor gets the signal out of the bulk



# PbS QDs: Improvements



“Blind” mode



$$R \approx R_{\text{PMT}} + \delta R + R_{\gamma\text{-QD}}$$

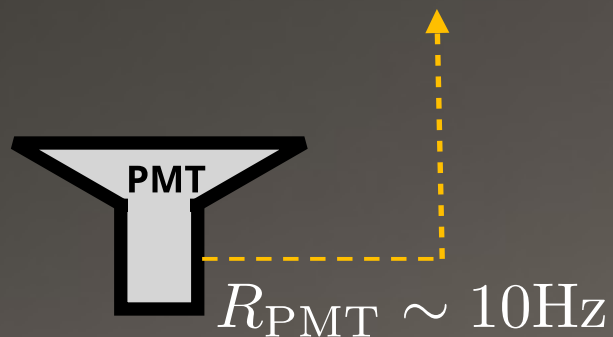
$$R_{\gamma\text{-QD}} \lesssim \sqrt{R_{\text{PMT}}}$$

“Active” mode

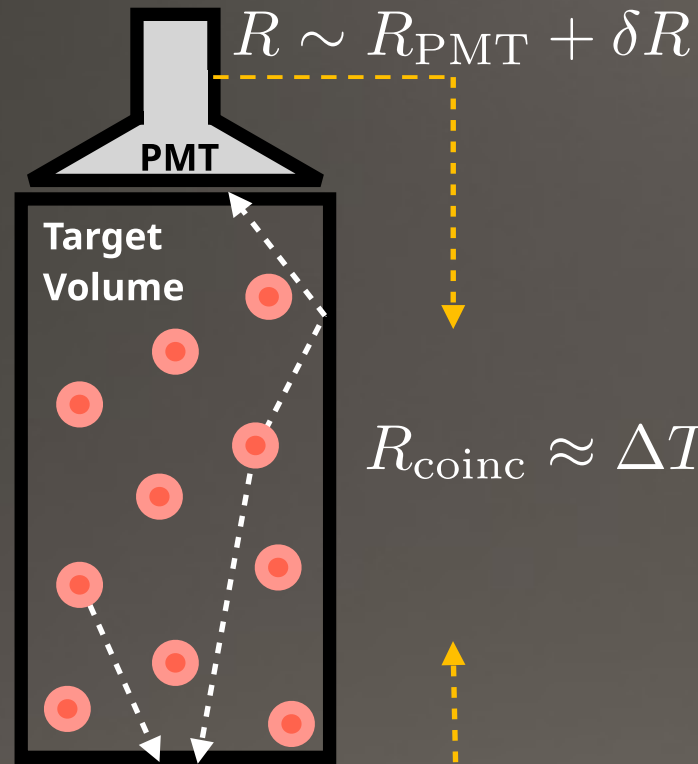
# PbS QDs: Improvements



$$R_{\text{coinc}}^0 \approx \Delta T R_{\text{PMT}}^2$$



“Blind” mode

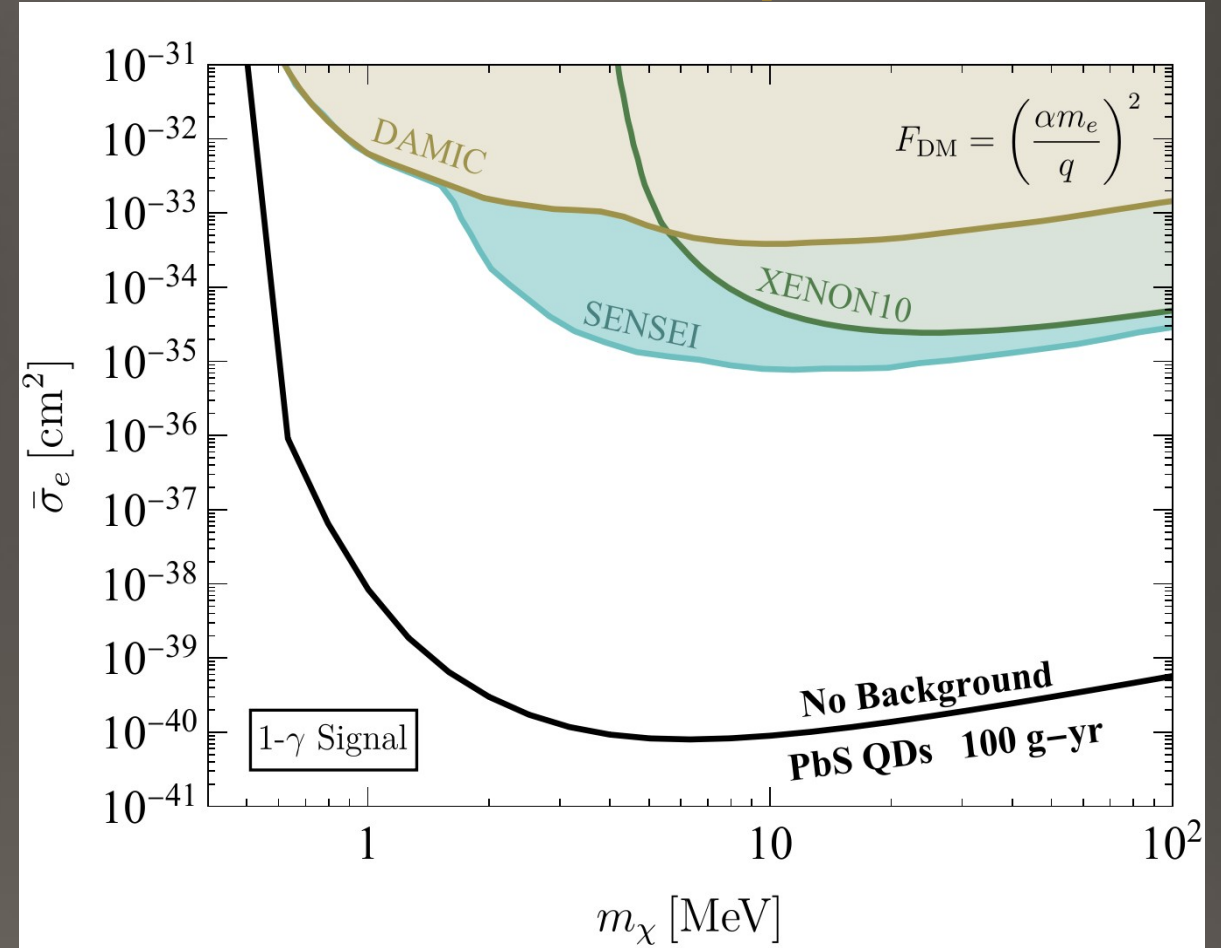
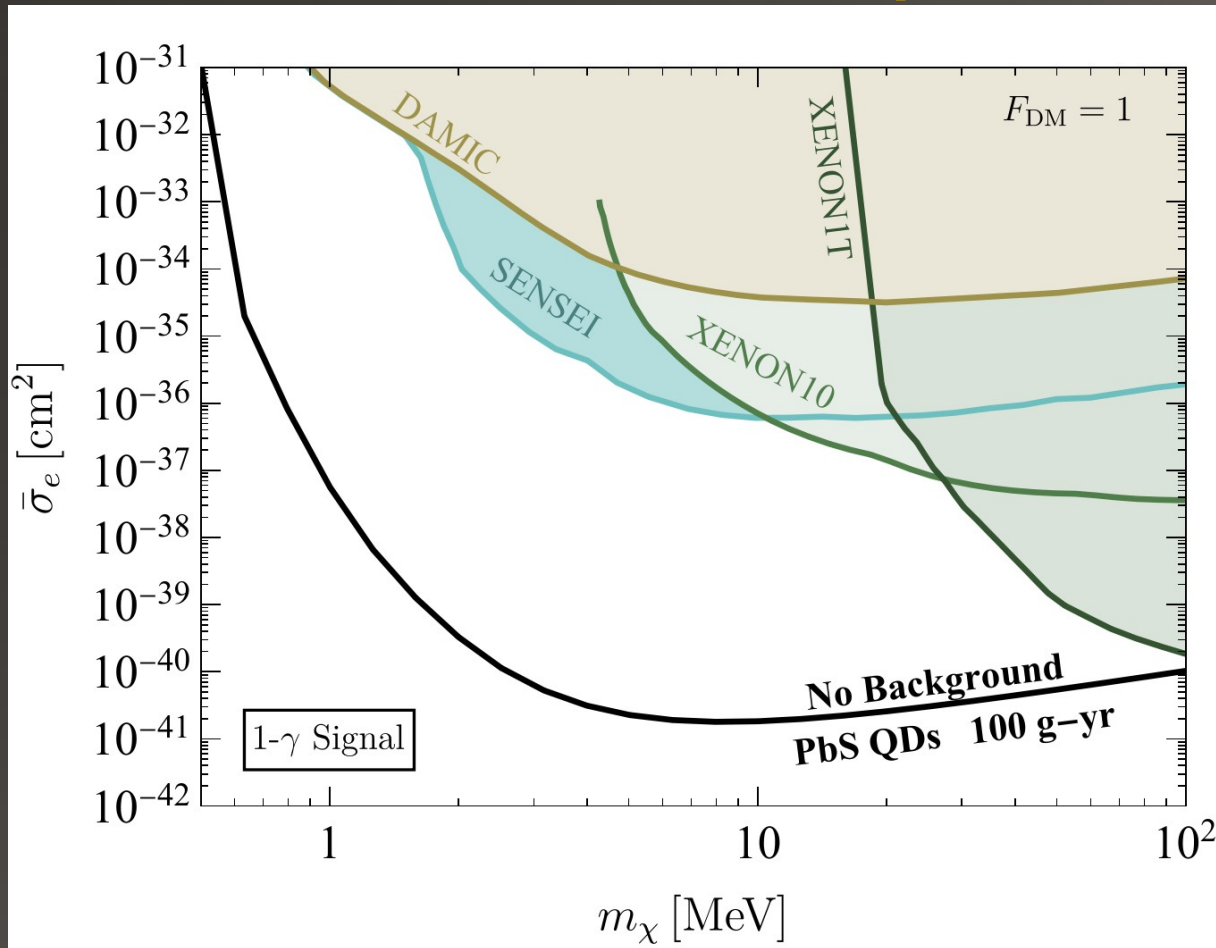


$$R_{\text{coinc}} \approx \Delta T R_{\text{PMT}}^2 + 2\Delta T R_{\text{PMT}} \delta R + R_{2\gamma-QD}$$

$$R_{2\gamma-QD} \lesssim \Delta T R_{\text{PMT}}^{3/2}$$

“Active” mode

# PbS QDs: Optimism for comparison

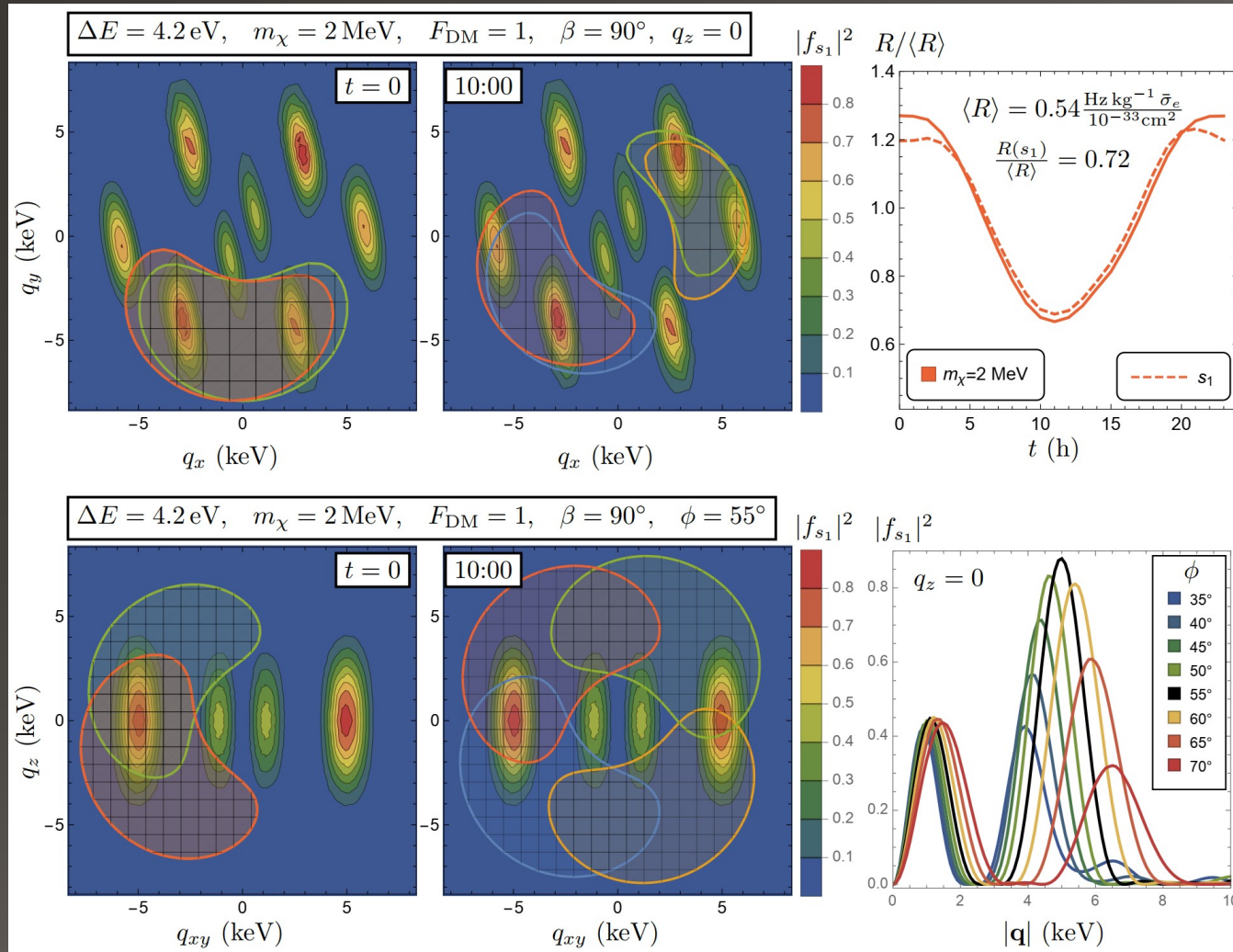


Blanco '22: 2208.05967

DM-Electron Scattering (no background 1-photon signal)

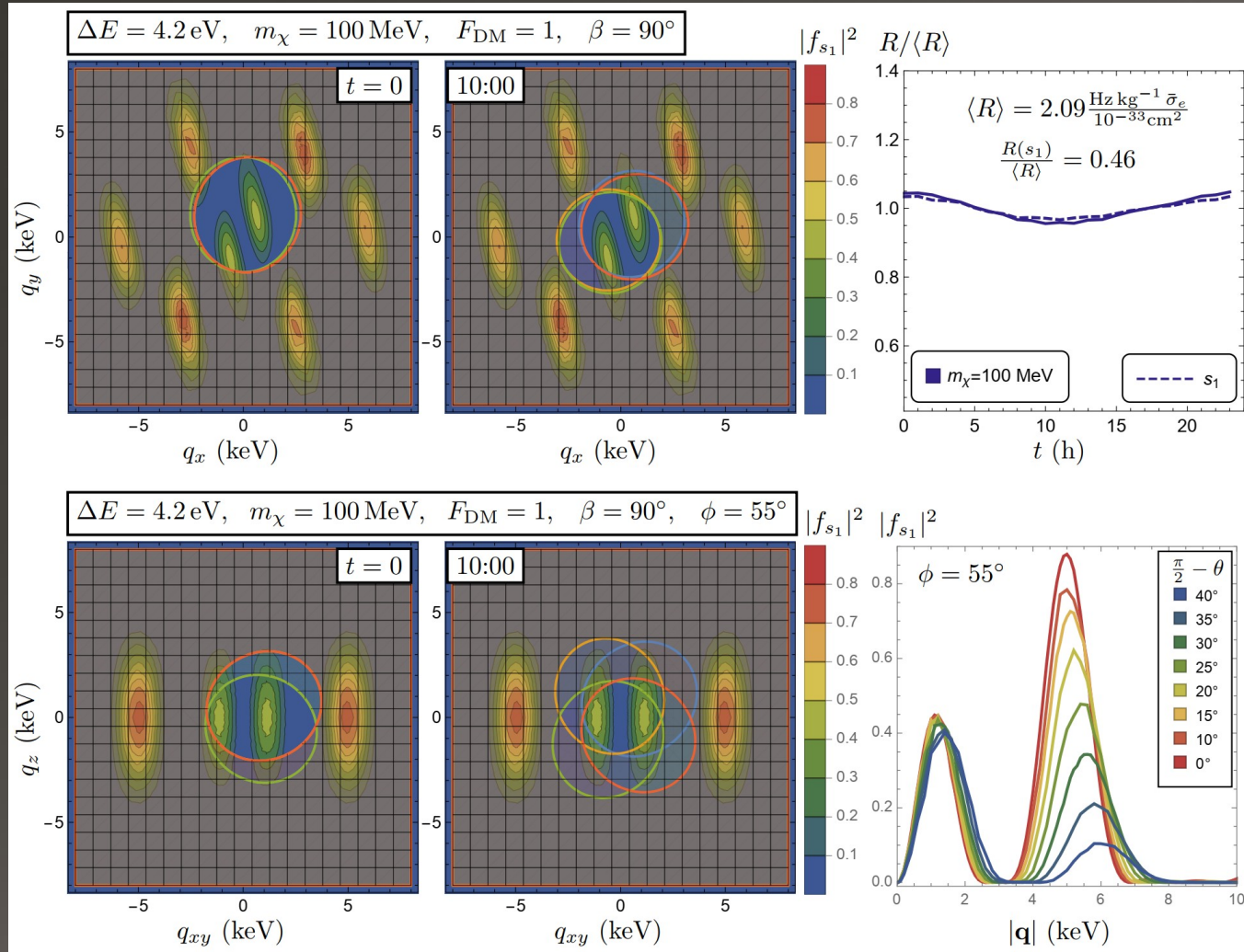


# Daily Modulation: Small Mass



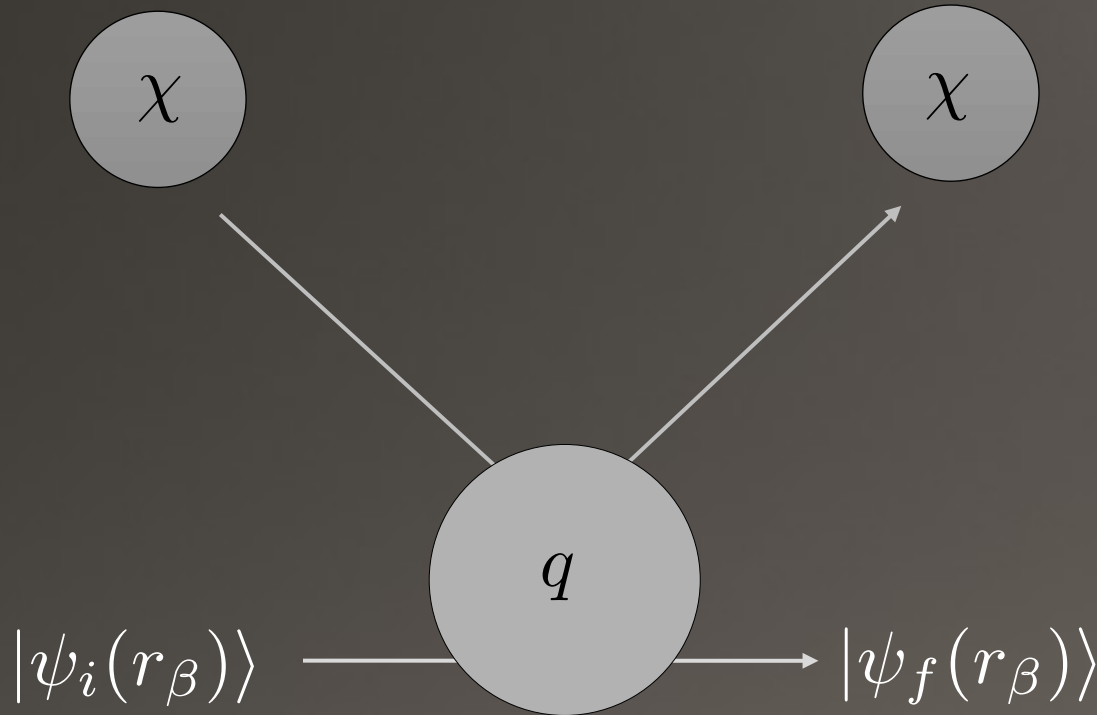
Molecular form factors and modulating rates for DM masses near threshold,  $m_\chi = 2 \text{ MeV}$ . In the contour plots, the gridded shaded regions indicate the kinematically accessible momentum transfers  $\vec{q}$  for the four molecules that comprise the unit cell of the crystal, shown at  $t = 0$  and  $t = 10 \text{ h}$ . Here,  $\vec{q}$  is given in the molecular basis,  $q_x = \vec{q} \cdot \hat{L}$ ,  $q_y = \vec{q} \cdot \hat{M}$ , and the kinematically accessible region is defined by  $v_-(\vec{q}) < v_{\text{esc}}$ .

# Daily Modulation: Large Mass



Same as previous figure but for large DM masses,  $m_\chi = 100 \text{ MeV}$ . Only the nearly-spherical region near  $q \sim 0$  with inner boundary  $q_{\text{min}} \simeq 1.6 \text{ keV}$  is kinematically forbidden. As a result, the daily modulation amplitude is smaller, driven by the anisotropy of the inner secondary peaks and the tails of the primary peaks.

# Electron Recoil: Charge Signal



Electron scattering

$$\Delta E_r = (m_\chi^2 / m_T) \times 10^{-6}$$

$$\Delta E \sim \mathcal{O}(\text{few eV}) \left( \frac{m_\chi}{1 \text{ MeV}} \right)^2$$

What has such transition energies?

- Semiconductor band gaps
- Maybe atomic ionization

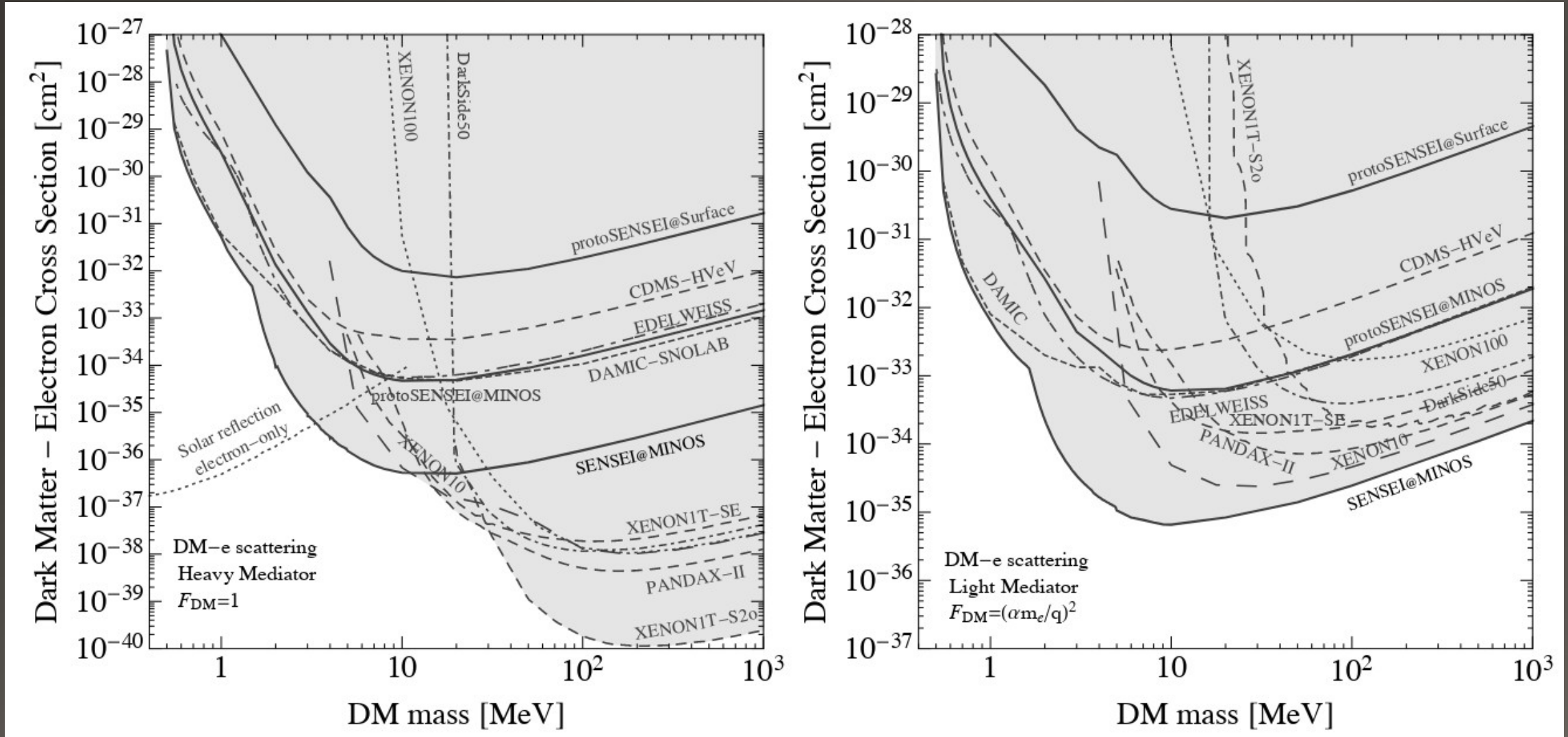
Electrons in crystals (exciton generation)

$$|\psi_i\rangle \sim u_v(r) e^{ik' \cdot r} \quad |\psi_f\rangle \sim u_c(r) e^{ik \cdot r}$$

Electrons in atoms (ionization)

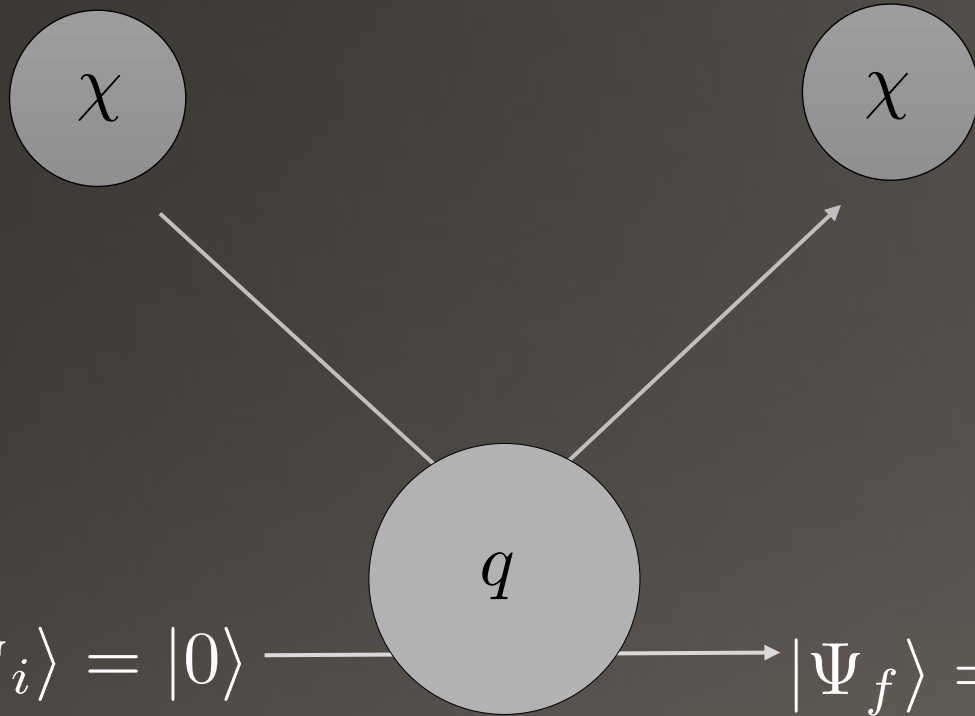
$$|\psi_i\rangle \sim \psi_{\text{STO}}(r_\beta) \quad |\psi_f\rangle \sim e^{ik \cdot r}, \quad r \gg a_0$$

# Semiconductor CCDs



Essig R., et al. "Snowmass2021 Cosmic Frontier The landscape of low-threshold dark matter direct detection in the next decade" arXiv:2203.08297 (2022).

# Nuclear Recoil: Phonon Signal



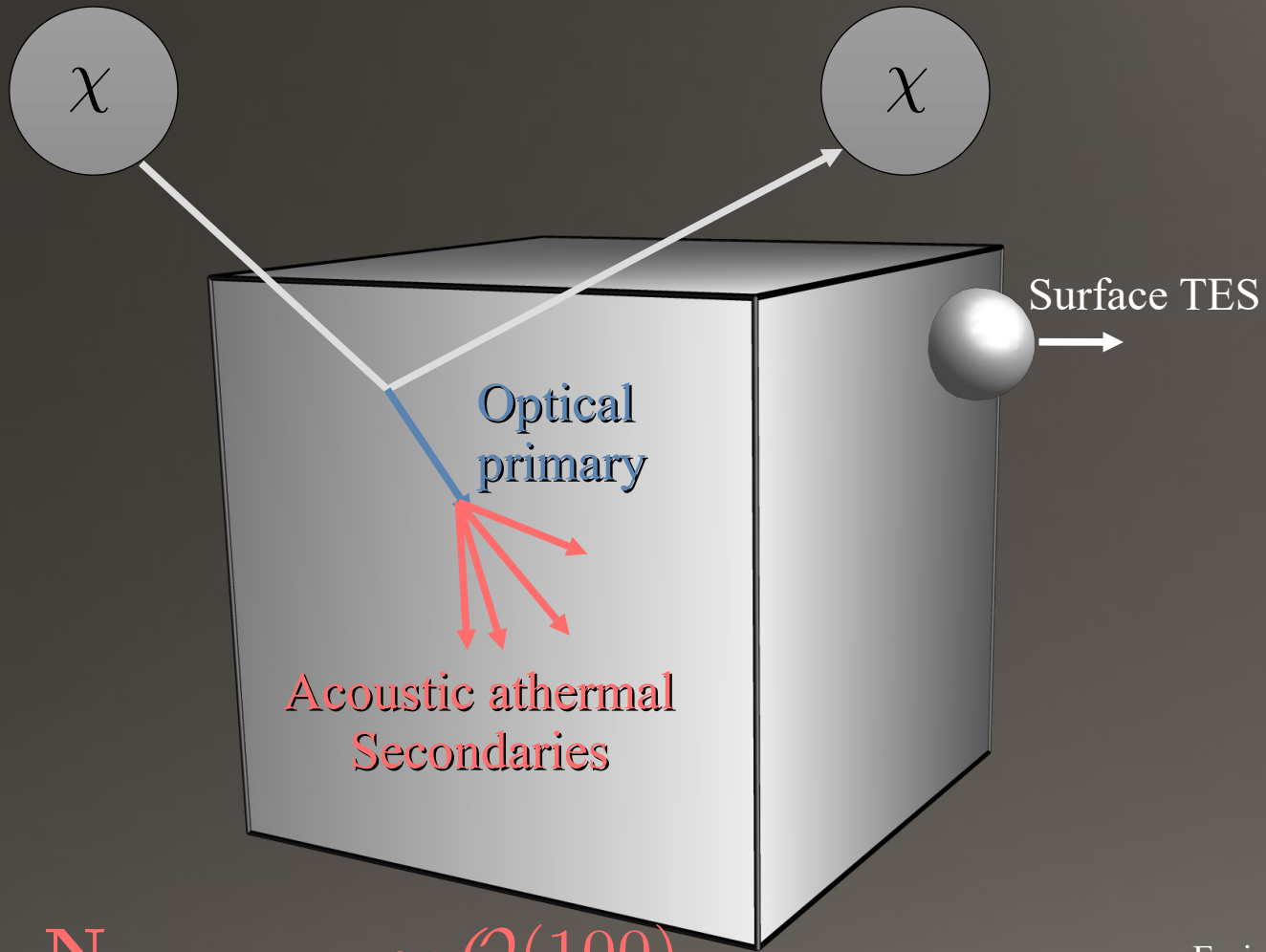
Nuclear scattering

$$\Delta E \sim \mathcal{O}(\text{few eV}) \left( \frac{m_\chi}{100 \text{ MeV}} \right)^2 \left( \frac{m_N}{130 \text{ GeV}} \right)^{-1}$$

$$\omega \sim \mathcal{O}(10\text{-}100 \text{ meV})$$

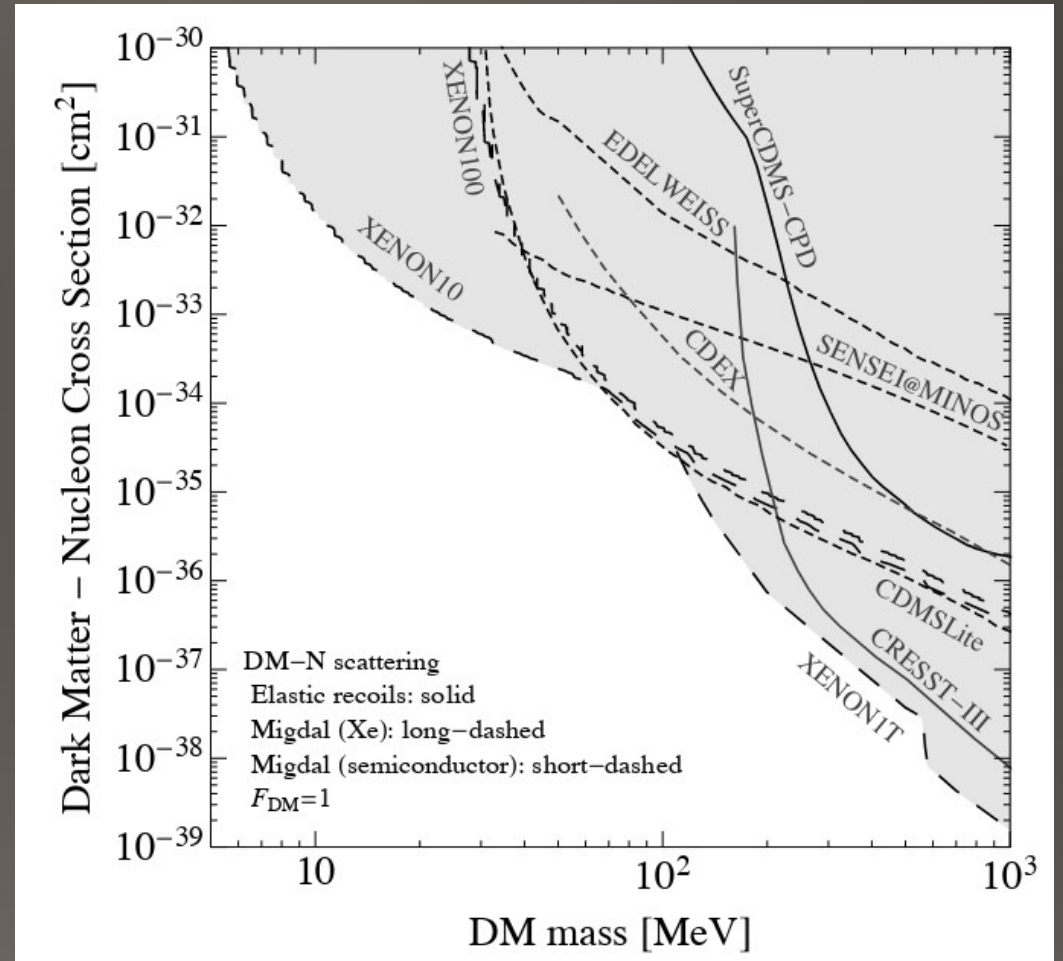
$$|\Psi_i\rangle = |0\rangle \longrightarrow |\Psi_f\rangle = a^\dagger(k) |0\rangle$$

# Calorimeters



$$N_{\text{acoustic}} \sim \mathcal{O}(100)$$

$$E_0 \sim 10 - 100 \text{ meV}$$



Essig R., et al. "Snowmass2021 Cosmic Frontier The landscape of low-threshold dark matter direct detection in the next decade" arXiv:2203.08297 (2022).

# Trans-Stilbene

$s$	Platt Symbol	Symmetry	$\Delta E$ [eV]	Configuration amplitudes			
$s_1$	${}^1B$	$B_u$	4.240	$d_{7,8} = 0.94,$	$d_{4,11} = -0.24$		
$s_2$	${}^1G^-$	$B_u$	4.788	$d_{7,10} = 0.53,$	$d_{5,8} = 0.53,$	$d_{6,11} = 0.37,$	$d_{4,9} = -0.37$
$s_3$	${}^1G^-$	$A_g$	4.800	$d_{7,9} = 0.53,$	$d_{6,8} = 0.53,$	$d_{5,11} = 0.37,$	$d_{4,10} = -0.37$
$s_4$	${}^1(C, H)^+$	$A_g$	5.137	$d_{7,11} = 0.41,$	$d_{5,9} = -0.41,$	$d_{6,10} = -0.41,$	$d_{4,8} = -0.59$
$s_5$	${}^1H^+$	$B_u$	5.791	$d_{5,10} = 0.54,$	$d_{6,9} = 0.54,$	$d_{7,12} = 0.33,$	$d_{3,8} = 0.33$
$s_6$	${}^1G^+$	$A_g$	6.264	$d_{7,9} = 0.68,$	$d_{6,8} = -0.68$		
$s_7$	${}^1C^-$	$A_g$	6.013	$d_{7,11} = 0.66,$	$d_{4,8} = 0.54,$		
$s_8$	${}^1G^+$	$B_u$	6.439	$d_{7,10} = 0.65,$	$d_{5,8} = -0.65$		

Table 1: The first eight excited states  $s_{n=1\dots 8}$ , with their energy eigenvalues  $\Delta E(s_n)$  with respect to the ground state and coefficients  $d_{ij}^{(n)}$  as calculated by Ting and McClure.

$$|s_n\rangle = \sum_{i,j>i} d_{ij}^{(n)} |\psi_i^j\rangle,$$

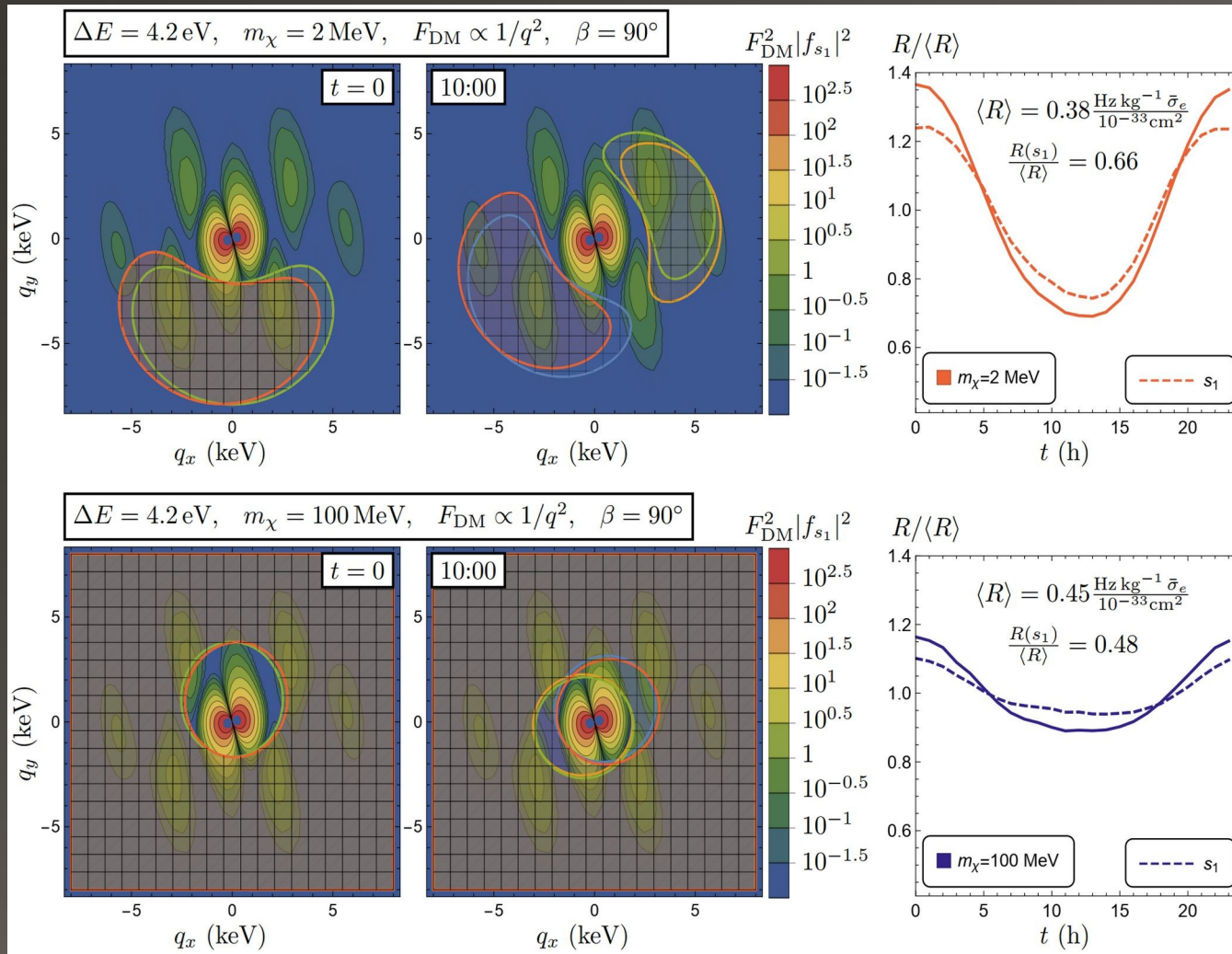
$$\sum_{ij} |d_{ij}^{(n)}|^2 = 1.$$

$$f_{g \rightarrow s_n}(\vec{q}) = \left\langle \psi_{s_n}(\vec{r}_1 \dots \vec{r}_{14}) \left| \sum_{m=1}^{14} e^{i\vec{q} \cdot \vec{r}_m} \right| \psi_G(\vec{r}_1 \dots \vec{r}_{14}) \right\rangle$$

$$= \sum_{ij} d_{ij}^{(n)} \langle \psi_i^j | e^{i\vec{q} \cdot \vec{r}} | \psi_G \rangle$$

$$= \sqrt{2} \sum_{ij} d_{ij}^{(n)} \langle \Psi_j(\vec{r}) | e^{i\vec{q} \cdot \vec{r}} | \Psi_i(\vec{r}) \rangle.$$

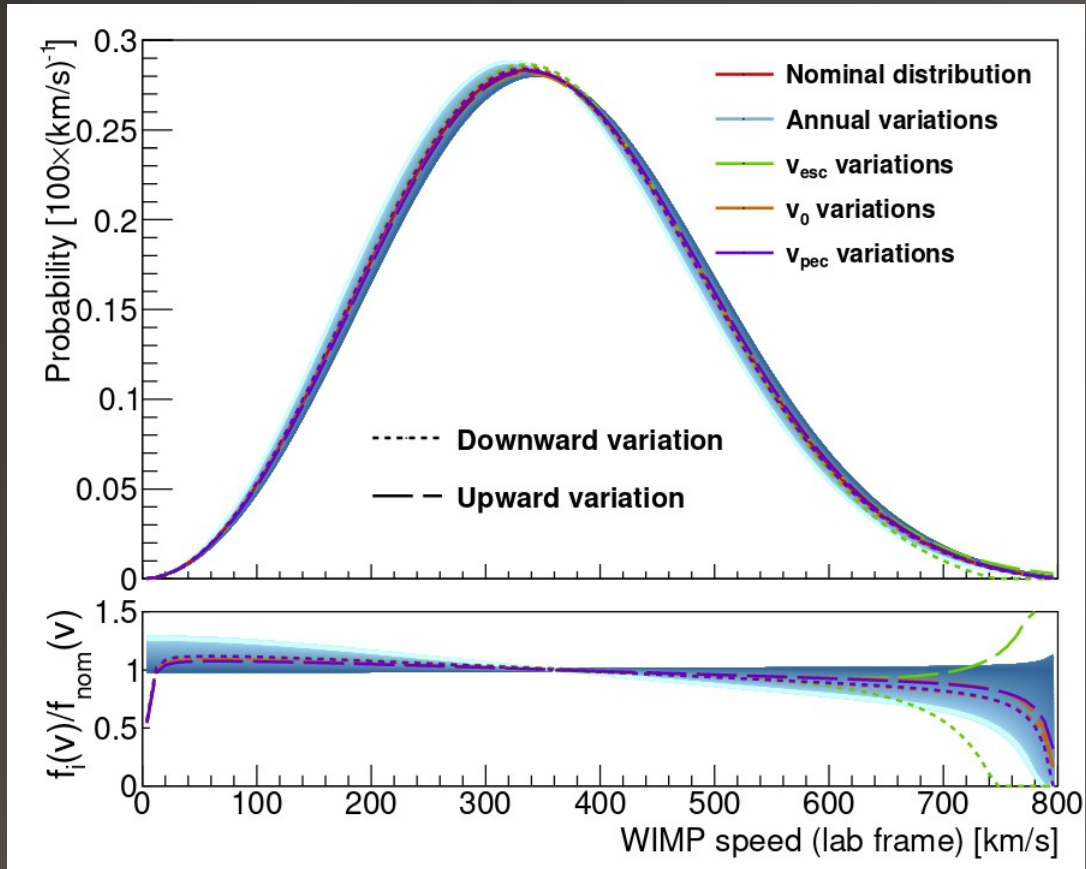
# Daily Modulation: Light Mediator



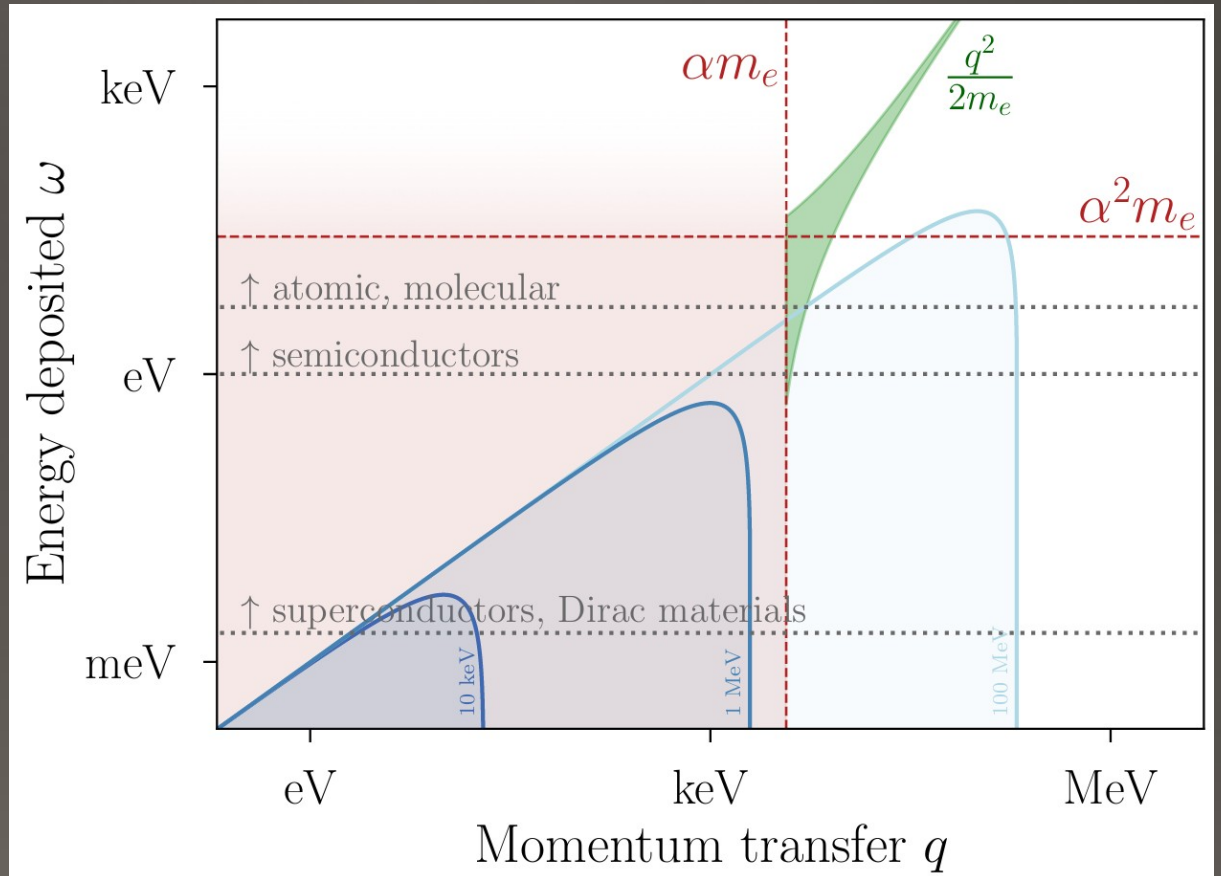
Same as previous figures (top) for a light mediator DM form factor  $F_{\text{DM}} = (\alpha m_e/q)^2$ . Here, the contour plots show  $F_{\text{DM}}^2 |f(s_1)|^2$  which appears in the rate integrand; the scattering is dominated by the smallest kinematically-allowed  $q$ . **Top:** Molecular form factors with  $q_z = 0$  and rate modulations for  $m_\chi = 2 \text{ MeV}$ . **Bottom:** Molecular form factors with  $q_z = 0$  and rate modulations for  $m_\chi = 100 \text{ MeV}$ .



# Local DM Phase Space



Baxter, D., et al. "Recommended conventions for reporting results from direct dark matter searches." The European Physical Journal C 81.10 (2021): 1-19.



Lin, Tongyan. "Sub-GeV dark matter models and direct detection." SciPost Physics Lecture Notes (2022): 043.