Electron-ion collisions in Pythia 8

MC4EIC 2024

Ilkka Helenius

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Outline

Pythia 8: A general purpose event generator

- Latest release 8.312 (May 2024)
- A new physics manual for 8.3

[SciPost Phys. Codebases 8-r8.3 (2022)]

Outline

- 1. Pythia 8 basics
- 2. Deep inelastic scattering (DIS)
- 3. Photoproduction in e+p
- 4. Ultraperipheral heavy-ion collision collisions (UPCs)
- 5. Summary & Outlook



[figure by P. Skands]

Pythia Collaboration

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[Pythia meeting in Monash 2019] https://pythia.org authors@pythia.org

Classify event generation in terms of "hardness"

1. Hard Process (here $t\bar{t}$)



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- 2. Resonance decays (t, Z, \ldots)



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- 3. Matching, Merging and matrix-element corrections



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- 5. Parton showers: ISR, FSR, QED, Weak



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- 6. Hadronization, Beam remnants



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- 6. Hadronization, Beam remnants
- 7. Decays, Rescattering



Multiparton interactions (MPIs)

• MPIs from 2 \rightarrow 2 QCD cross sections

$$\frac{\mathrm{d}\mathcal{P}_{\mathrm{MPI}}}{\mathrm{d}p_{\mathrm{T}}^{2}} = \frac{1}{\sigma_{\mathrm{nd}}(\sqrt{s})} \frac{\mathrm{d}\sigma^{2\rightarrow2}}{\mathrm{d}p_{\mathrm{T}}^{2}}$$

 $\sigma_{\rm nd}(\sqrt{\rm s})$ is the non-diffractive cross section

Partonic cross section diverges at p_T → 0
 ⇒ Introduce a screening parameter p_{T0}

$$\frac{\mathrm{d}\sigma^{2\to2}}{\mathrm{d}p_{\mathrm{T}}^2}\propto\frac{\alpha_{\mathrm{s}}(p_{\mathrm{T}}^2)}{p_{\mathrm{T}}^4}\rightarrow\frac{\alpha_{\mathrm{s}}(p_{\mathrm{T0}}^2+p_{\mathrm{T}}^2)}{(p_{\mathrm{T0}}^2+p_{\mathrm{T}}^2)^2}$$

- Energy-dependent parametrization: $p_{TO}(\sqrt{s}) = p_{TO}^{ref}(\sqrt{s}/\sqrt{s_{ref}})^{\alpha}$
- Number of interactions: $\langle n \rangle = \sigma_{\rm int}(p_{\rm T0})/\sigma_{\rm nd}$



σ_{int}(p_{T,min}) exceeds σ_{tot}
 ⇒ Several interactions

Parton-level evolution

Common evolution scale (p_T) for FSR, ISR and MPIs

• Probability for something to happen at given p_T

$$\begin{split} \frac{\mathrm{d}\mathcal{P}}{\mathrm{d}p_{\mathsf{T}}} &= \left(\frac{\mathrm{d}\mathcal{P}_{\mathsf{MPI}}}{\mathrm{d}p_{\mathsf{T}}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathsf{ISR}}}{\mathrm{d}p_{\mathsf{T}}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathsf{FSR}}}{\mathrm{d}p_{\mathsf{T}}}\right) \\ &\times \exp\left[-\int_{\rho_{\mathsf{T}}}^{\rho_{\mathsf{T}}^{\mathsf{max}}} \mathrm{d}p_{\mathsf{T}}' \left(\frac{\mathrm{d}\mathcal{P}_{\mathsf{MPI}}}{\mathrm{d}p_{\mathsf{T}}'} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathsf{ISR}}}{\mathrm{d}p_{\mathsf{T}}'} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathsf{FSR}}}{\mathrm{d}p_{\mathsf{T}}'}\right)\right] \end{split}$$

where exp[...] is a Sudakov factor (probability that nothing else has happened before p_T)

Simultaneous partonic evolution

- 1. Start the evolution from the hard-process scale
- 2. Sample p_T for each \mathcal{P}_i , pick one with highest p_T
- 3. Continue until $p_{\text{Tmin}} \sim \Lambda_{\text{QCD}}$ reached



Available beam configurations in Pythia 8

Hadronic collisions

- p-p: hard, soft and low-energy processes
- *h*-p, where $h=\pi^{\pm,0},$ K^{$\pm,0$}, ϕ^0,\ldots

Collisions with leptons

- e^+e^- , including $\gamma\gamma$ (also in p-p)
- e-p: (neutrino) DIS, photoproduction with soft and hard QCD processes

Heavy-ion collisions with Angantyr

- A-A, p-A and h-A
- UPCs with proton target, also VMD-A
- Some cosmic-ray related processes



[C. Bierlich, G. Gustafson, L. Lönnblad, H. Shah: JHEP10(2018)134]

Electron-proton collisions

Classified in terms photon virtuality Q^2

Deep inelastic scattering (DIS)

- High virtuality, $Q^2 > {\sf a}\, few\, GeV^2$
- Lepton scatters off from a parton by exchanging a highly virtual photon

Photoproduction

- Low virtuality, $Q^2 \rightarrow 0 \, GeV^2$
 - \Rightarrow Direct and resolved contributions
- Factorize γ flux, evolve γ p system
- Hard scale provided by the final state
- Also soft QCD processes, diffraction



Deep inelastic scattering

Event generation in DIS with Pythia 8

Hard scattering

• Convolution between PDFs and matrix element (ME) for partonic scattering

Parton shower

- Final state radiation (FSR)
- Initial state radiation (ISR) for hadron
- QED emissions from leptons (omitted) Hadronization
- String hadronization with colour reconnections
- Decays to stable hadrons



Parton shower options for DIS in Pythia I

The default shower with dipoleRecoil option [B. Cabouat, T. Sjöstrand, EPJC 78 (2018 no.3, 226)]

- No PS recoil for the scattered lepton
- Emissions from initial-final dipole
- No shower-specific tuning done
- Event shapes
 - Reasonable description of single-particle properties, such as transverse energy flow
 - Differences for energy-energy correlators
- Jet production
 - First emission match with matrix element
 - Can use "power shower" to fill the phase space
 - Good description of high-Q² dijets [See Joni's talk]



Parton shower options for DIS in Pythia II

Vincia antenna shower PartonShowers:model = 2 [H. Brooks, C. T. Preuss, P. Skands, JHEP 07 (2020) 032]

- QCD, QED, EW, interleaved with MPIs
- Efficient multi-jet merging with sectors

Dire in Pythia PartonShowers:model = 3 [S. Höche, S. Prestel, EPJC 75 (2015) no.9, 461]

- Correct soft-gluon interference at lowest order
- Inclusive NLO corrections to collinear splittings

H1 measurement 1-jettiness

$$\tau_1^b = \frac{2}{Q^2} \sum_{i \in HFS} \min[xP \cdot p_i, (q + xP) \cdot p_i]$$

• Sensitive to parton shower details



Photoproduction in e+p

Photoproduction in electron-proton collisions

Direct processes

• Convolute photon flux f_{γ} with proton PDFs f_i^p and $d\hat{\sigma}$

 $\mathrm{d}\sigma^{\mathrm{ep}\to kl+X} = f^{\mathrm{e}}_{\gamma}(\mathbf{x}, \mathsf{Q}^2) \, \otimes \, f^{\mathrm{p}}_{j}(\mathbf{x}_{\mathrm{p}}, \mu^2) \, \otimes \, \mathrm{d}\hat{\sigma}^{\gamma j \to kl}$

• Generate FSR and ISR for proton side

Resolved processes

• Convolute also with photon PDFs

 $\mathrm{d}\sigma^{\mathrm{ep}\to kl+X} = f_{\gamma}^{\mathrm{e}}(\mathbf{x}, \mathbf{Q}^2) \otimes f_{i}^{\gamma}(\mathbf{x}_{\gamma}, \mu^2) \otimes f_{j}^{\mathrm{p}}(\mathbf{x}_{\mathrm{p}}, \mu^2) \otimes \mathrm{d}\sigma^{ij \to kl}$

- Sample x and Q^2 , setup γp sub-system with $W_{\gamma p}$
- Evolve γp as any hadronic collision (including MPIs)

Photon flux from EPA

$$f_{\gamma}^{e}(x,Q^{2}) = \frac{\alpha_{em}}{2\pi} \frac{1}{Q^{2}} \frac{(1+(1-x)^{2})^{2}}{x}$$



Comparison to HERA dijet photoproduction data

ZEUS dijet measurement

- $Q^2 < 1.0 \, {\rm GeV}^2$
- $134 < W_{\gamma p} < 277 \, \text{GeV}$
- $E_T^{jet1} > 14 \, GeV$, $E_T^{jet2} > 11 \, GeV$
- $-1 < \eta^{jet1,2} < 2.4$

Two contributions

- Momentum fraction of partons in photon $x_{\gamma}^{obs} = \frac{E_{T}^{jet1}e^{\eta^{jet1}} + E_{T}^{jet2}e^{\eta^{jet2}}}{2yE_{e}} \approx x_{\gamma}$
- Sensitivity to process type
- At high- $x_{\gamma}^{\rm obs}$ direct processes dominate



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Pseudorapidity

- Data well reproduced
- Not sensitive to MPI modelling $(p_{T,0})$



[ZEUS: JHEP 12 (2021) 102]

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Multiplicity

- Sensitivity to MPI parameters, clear support for MPIs
- Data within $p_{T,0}$ variations



[ZEUS: JHEP 12 (2021) 102]

Pseudorapidity

- Data well reproduced
- Not sensitive to MPI modelling $(p_{T,0})$

Multiplicity

- Sensitivity to MPI parameters, clear support for MPIs
- Data within $p_{T,0}$ variations
- Direct contribution negligible in high-multiplicity events (N_{ch} > 20)



[ZEUS: JHEP 12 (2021) 102]

Alternative VMD-based approach

- Resolved contribution dominates total cross section
- ⇒ Set up an explicit VMD model with linear combination of vector-meson states (ρ, ω, ϕ and J/ψ)
 - Use VM PDFs from SU21

[Sjöstrand, Utheim; EPJC 82 (2022) 1, 21]

• Cross sections from SaS

[Schuler, Sjöstrand; PRD 49 (1994) 2257-2267]

- Sample collision energy from flux
- \Rightarrow Vector meson-proton scatterings



[with Marius Utheim]

00

000

1/wp

Charged multiplicity (non-diffractive events)

2.00

1.75

1.50

1.25

▲ 1.00

0.50

0.25

50

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• Cross sections from SaS

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- Sample collision energy from flux
- \Rightarrow Vector meson-proton scatterings
 - In line with the full photoproduction



[ZEUS: JHEP 12 (2021) 102]

[with Marius Utheim]

Intermediate Q² region

Solid theory for $Q^2 = 0$ and at high Q^2

 \Rightarrow What happens in between?

Pythia 6 (inspired) model (\neq Pythia 8)

• Select suitable scales and suppress contributions by hand

$$\sigma_{\text{tot}}^{\gamma^* p} = \tilde{\sigma}_{\text{DIS}}^{\gamma^* p} \exp\left[-\frac{\tilde{\sigma}_{\text{Dir}}^{\gamma^* p}}{\tilde{\sigma}_{\text{DIS}}^{\gamma^* p}}\right] + \tilde{\sigma}_{\text{Dir}}^{\gamma^* p} + \tilde{\sigma}_{\text{Res}}^{\gamma^* p}$$
where

•
$$\tilde{\sigma}_{\text{DIS}}^{\gamma^* p} = \left[\frac{Q^2}{Q^2 + m_{\rho}^2}\right]^2 \sigma_{\text{DIS}}^{\gamma^* p}$$

• $\tilde{\sigma}_{\text{Res}}^{\gamma^* p} = \sigma_{\text{Res}}^{\gamma^* p} \left[\frac{m_{\rho}^2}{m_{\rho}^2 + Q^2}\right]^2 \left[\frac{W^2}{W^2 + Q^2}\right]^n$
• $\tilde{\sigma}_{\text{Dir}}^{\gamma^* p} = \sigma_{\text{Dir}}^{\gamma^* p}(\hat{p}_{\text{T,min}} = max(Q, p_{\text{T,min}})))$
 $p_{\text{T,min}} = 1.3 \,\text{GeV}, \, n = 3, \, m_{\rho} = 0.7755 \,\text{GeV}$



Intermediate: $0.5 \lesssim Q^2 \lesssim 5.0 \, \text{GeV}^2$

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 $p_{\text{T,min}} = 1.3 \text{ GeV}, n = 3, m_\rho = 0.7755 \text{ GeV}$



Intermediate: $0.3 \lesssim Q^2 \lesssim 3.0 \, \text{GeV}^2$

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• $\tilde{\sigma}_{\text{Dir}}^{\gamma^* p} = \sigma_{\text{Dir}}^{\gamma^* p}(\hat{p}_{\text{T,min}} = max(Q, p_{\text{T,min}}))$
 $p_{\text{T,min}} = 1.3 \text{ GeV}, n = 3, m_\rho = 0.7755 \text{ GeV}$



Intermediate: $0.2 \lesssim Q^2 \lesssim 2.0 \, \text{GeV}^2$

Ultraperipheral collisions (UPCs)

Ultraperipheral heavy-ion collisions

- Large impact parameter (b ≥ 2R_A) ⇒ No strong interactions
- At LHC relevant for p+p, p+Pb, Pb+Pb
- Large flux due to large EM charge of nuclei
- $\Rightarrow \gamma\gamma$ and γ A collisions

Photon flux from equivalent photon approximation

- Define flux in impact-parameter space \Rightarrow Reject hadronic interactions with b_{\min}
- Integrating the point-like approximation we get

$$f_{\gamma}^{A}(x) = \frac{2\alpha_{\rm EM}Z^{2}}{x \pi} \left[\xi \, K_{1}(\xi) K_{0}(\xi) - \frac{\xi^{2}}{2} \left(K_{1}^{2}(\xi) - K_{0}^{2}(\xi) \right) \right]$$

where $\xi = b_{\min} x m$ where $b_{\min} \approx 2R_A$ and m per nucleon mass

• Nuclear form factor heavily suppresses Q^2 of the photon \Rightarrow Photoproduction!



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Dijets in ultra-peripheral heavy-ion collisions in Xn0n

- Good agreement out of the box when accounting both direct and resolved
- EM nuclear break-up significant
- Pythia setup with nucleon target only
 ⇒ Is such a setup enough for γ+A?



See also [Eskola, Guzey, IH, Paakkinen, Paukkunen; arXiv:2404.09731]



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Multiplicity distributions in UPCs



 Multiplicity distribution well reproduced in γ+p interactions



High multiplicities missed with γ+p
 ⇒ Multi-nucleon interactions

Modelling $\gamma\text{+}A$ with Pythia

[with Marius Utheim]

Angantyr model for heavy ions in Pythia

[Bierlich, Gustafson, Lönnblad, Shah; JHEP 10 (2018) 134]

- Monte Carlo Glauber to sample nucleon configurations
- Cross section fluctuations, fitted to partial nucleon-nucleon cross sections
- Secondary (wounded) collisions as diffractive excitations
- Can now handle generic hadron-ion and varying energy [I.H., Utheim; in progress]
- \Rightarrow VMD-nucleus scatterings



Comparison with data for γ +A



- ATLAS data not corrected for efficiency, estimated with $N_{
 m ch}^{
 m rec} pprox 0.8 \cdot N_{
 m ch}$
- Relative increase in multiplicity well in line with the VMD-Pb setup

Comparison with data for γ +A



- Multiplicity cut adjusted according to the limited efficiency
- Good description of the measured rapidity distribution with the VMD-Pb setup

Summary & Outlook

Deep inelastic scattering

- Several parton showers available
- \Rightarrow No specific tuning, sparse validation

Photoproduction

- Soft and hard QCD processes included
- Validated against some HERA data
- \Rightarrow More global MPI tuning
- \Rightarrow Model transition from photoproduction to DIS

Nuclear target

- First steps with VMD+A in 8.311, applied to UPCs at the LHC
- In line with single-particle observables analyzed by ATLAS
- \Rightarrow Further modelling to include complete structure of real photons



[figure by P. Skands]

Backup slides

Vector meson dominance (VMD)





Linear combination of three components

$$|\gamma
angle = c_{
m dir}|\gamma_{
m dir}
angle + \sum_{q} c_{q}|q\overline{q}
angle + \sum_{V} c_{V}|V
angle$$

where the last term includes a linear combination of vector meson states up to J/Ψ

$$c_{\rm V} = \frac{4\pi\alpha_{\rm EM}}{f_{\rm V}^2}$$

 V
 $f_V^2/(4\pi)$
 ρ^0 2.20

 ω 23.6

 ϕ 18.4

 J/Ψ 11.5

Photon fluxes from Equivalent Photon Approximation (EPA)

• In case of a point-like lepton we have (neglecting electron mass)

$$f_{\gamma}^{I}(x,Q^{2}) = rac{lpha_{
m em}}{2\pi} rac{1}{Q^{2}} rac{(1+(1-x)^{2})}{x}$$

For protons need to include form factors, using dipole form factor

$$f_{\gamma}^{p}(x,Q^{2}) = \frac{\alpha_{\text{em}}}{2\pi} \frac{x}{Q^{2}} \frac{1}{(1+Q^{2}/Q_{0}^{2})^{4}} \left[\frac{2(1+\mu_{p}\tau)}{1+\tau} \left(\frac{1-x}{x^{2}} - \frac{M_{p}^{2}}{Q^{2}} \right) + \mu_{p}^{2} \right]$$

where $\tau = Q^2/4M_p^2$, $\mu_p = 2.79$, $Q_0^2 = 0.71 \,\text{GeV}^2$

• Drees-Zeppenfeld approximation ($M_p = 0, \mu_p = 1$)

$$f_{\gamma}^{p}(x,Q^{2}) = rac{lpha_{em}}{2\pi} rac{1}{Q^{2}} rac{1}{(1+Q^{2}/Q_{0}^{2})^{4}} rac{(1+(1-x)^{2})}{x}$$

- \Rightarrow Large Q² suppressed wrt. leptons \Rightarrow photoproduction
- In ME generators (such as MG5) integrated over Q² and assumed collinear

Equivalent photon approximation

Compare to full calculation

- Example process $pp \rightarrow \gamma \gamma \rightarrow \mu^+ \mu^-$
- Different approximations (e.g.) by Drees and Zeppenfeld \sim 20% difference to full calculation
- Keeping finite mass and correct magnetic moment provides ~ few percent accuracy
- Not checked for other observables, such as acoplanarity



Define your own photon flux for Pythia 8

• Derive a new object from PDF class

class Proton2gammaEPA : public PDF {

public:

```
// Constructor.
ProtonZgammaEPA(int idBeamIn) : PDF(idBeamIn) {}
// Update the photon flux.
void xfUpdate(int , double x, double Q2) {
    double m2proton = pow2(0.938);
    double m2proton = pow2(2.79);
    double Q20 = 0.71;
    double Coupling = 0.5 * 0.007297353080 / N_PI * FQ4;
    double tou = Q2 / (4. * m2proton);
    xgamma = coupling * ( pow2(x) / Q2 ) * ( 2. * (1. + mup2*tau ) / (1. + tau)
        * ( (1 - x)/pow2(x) - m2proton / Q2 ) + mup2);
}
```

• Pass as a pointer to Pythia

pythia.readString("PDF:becm&2gamma = on"); pythia.readString("PDF:becm&2gamma5et = 0"); pythia.readString("PDF:proton2gamma5et = 0"); PDFPtr photonFluxA = make_shared<Proton2gammaEPA>(2212); PDFPtr photonFluxB = make_shared<Proton2gammaEPA>(2212); pythia.setPhotonFluxBtr(photonFluxA, photonFluxB);

Example in p-p: $\gamma\gamma \rightarrow \mu^+\mu^-$



• No finite-size effects accounted

• Enable γ +p in e+p

pythia.readString("Beams:idA = -11");
pythia.readString("Beams:idB = 2212");
pythia.readString("PDF:beamA2gamma = on");



• Enable γ +p in e+p

pythia.readString("Beams:idA = -11");
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pythia.readString("PDF:beamA2gamma = on");

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• Enable γ +p in e+p

pythia.readString("Beams:idA = -11");
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pythia.readString("PDF:beamA2gamma = on");

• Enable γ +p in p+p

pythia.readString("Beams:idA = 2212");
pythia.readString("Beams:idB = 2212");
pythia.readString("PDF:beamA2gamma = on");

• Enable γ +p in Pb+p

pythia.readString("Beams:idA = 2212"); pythia.readString("PDF:beamA2gamma = on"); pythia.readString("PDF:beamA2gammaSet = 0"); pythia.readString("PDF:beam2gammaApprox = 2"); pythia.readString("Photon:sample02 = off"); PDFPtr photonFlux = make_shared<Nucleus2gamma>(2212); pythia.setPhotonFluxPtr(photonFlux, 0);



For more examples see main68.cc,main69.cc, main70.cc,main78.cc in examples directory



[from main70.cc]



An example process: $\gamma\gamma \rightarrow \mu^+\mu^-$

- Can take place in EE, SD and DD (also DY processes with resolved photons?)
- Implemented natively in Pythia, can also generate with an ME generator (MG5, SC)

EE contribution

- Clean process to study fluxes
- However, fluxes only does not account for finite-size effects



[ATLAS: PLB 777 (2018) 303-323]

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EE contribution

- Clean process to study fluxes
- However, fluxes only does not account for finite-size effects
- Not quite back-to-back due to
 - *p*_T generated by non-collinear photons
 - QED radiation in the final state
- Acoplanarity $|\pi \Delta \phi|$ quantify the effect



- Needed to tune Pythia primordial k_T parameters for external events
- Can use (user-defined) flux for Q² sampling

Heavy-ion collisions

• Angantyr in Pythia provides a full heavy-ion collisions framework

[Bierlich, Gustafson, Lönnblad & Shah: 1806.10820]

• Hadronic rescattering can be included as well, enhances collective effects

[CB, Ferreres-Solé, Sjöstrand & Utheim: 1808.04619, 2005.05658, 2103.09665]





p+A collisions

[Bierlich, Gustafson, Lönnblad & Shah: 1806.10820]

- Angantyr can be applied also to asymmetric p+A collisions
- The centrality measure well reproduced
- Similarly centraility-dependent multiplicities



Experimental heavy-ion UPC classification

- Event selection typically relies on Zero-degree calorimeters (X > 0)
- XnXn: At least one neutron on both sides
 - \Rightarrow A+A (hadronic interaction)
- XnOn: At least one neutron only on one side
 - $\Rightarrow \gamma$ +A
- OnOn: No neutrons on either side

 $\Rightarrow \gamma + \gamma$

Possible caveats

- Additional EM interactions may break up the nuclei in "near-encounter" events
- Also diffractive processes will keep nuclei intact
 - \Rightarrow XnOn condition will remove diffractive contribution to $\gamma \text{+} \text{A}$

See e.g. [Guzey, Klasen; PRD 104 (2021) 11 114013]



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Dijets in ultra-peripheral heavy-ion collisions in 0n0n



- Per-event yield underestimated by a factor of ten!
- Shape in a reasonable agreement
- $\gamma\gamma \rightarrow \mu^+\mu^-$ ok so likely a QCD effect \Rightarrow Contribution from diffractive events?

Collectivity in UPCs at the LHC



Finite v₂ for γ+p, in line with Pythia
 ⇒ Jet-like correlations?

γ+Pb [ATLAS: PRC 104, 014903 (2021)]



ATLAS data for v_n in γ +Pb



- Non-zero flow coefficients also for γ+Pb
- Expected baseline from MC simulations?



- Pythia8 γ +p in ATLAS result should correspond to gm-p on right
- Relative increase in multiplicity well in line with the VMD setup



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- $\Sigma_{\gamma} \Delta \eta$: Sum of rapidity gaps for which $\Delta \eta > 0.5$
- Similar for γ -p and γ -Pb

Role of cross section fluctuations



• High-multiplicity tail less pronounced with Angantyr:CollisionModel = 0 with fixed nucleon radius, ATLAS data seem to favour fluctuations