

Recent results from GlueX

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for the GlueX Collaboration

Exotic Hadron Spectroscopy 2024

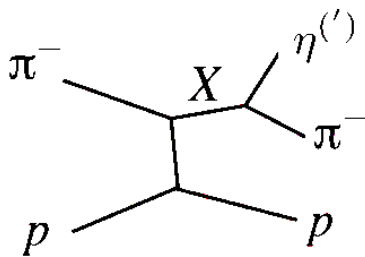
Swansea University, UK

July 2-4, 2024

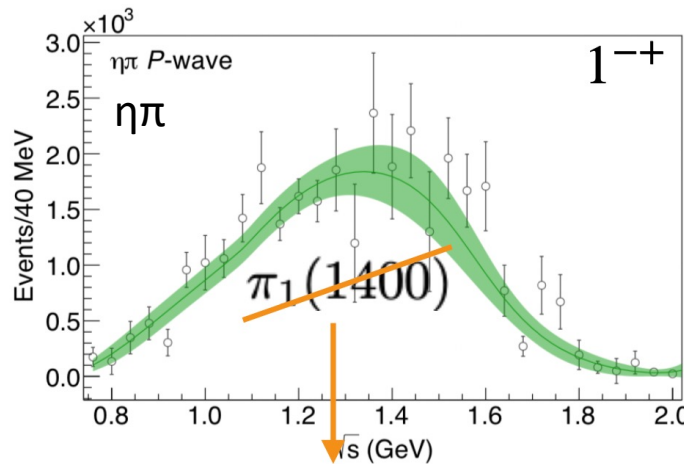
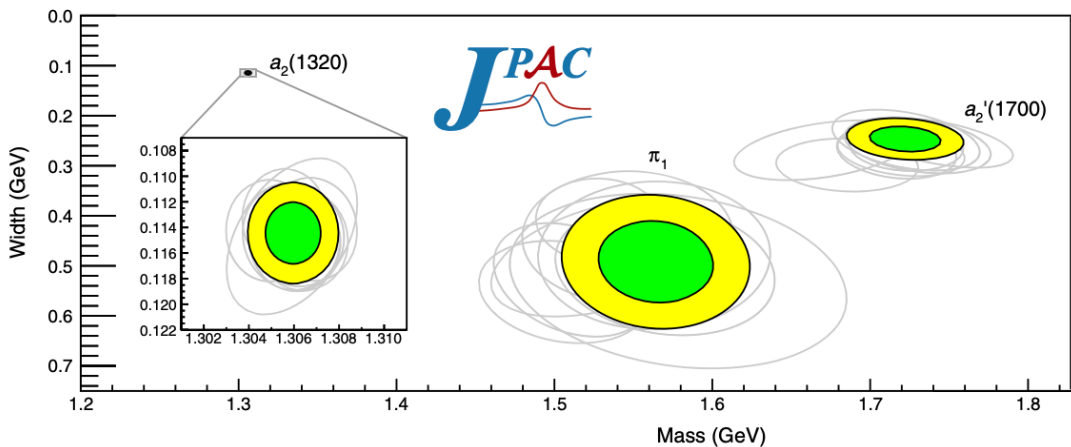


Evidence for exotic hybrid $\pi_1(1600)$

- Evidence for $\pi_1(1600)$ in data from COMPASS, 2015

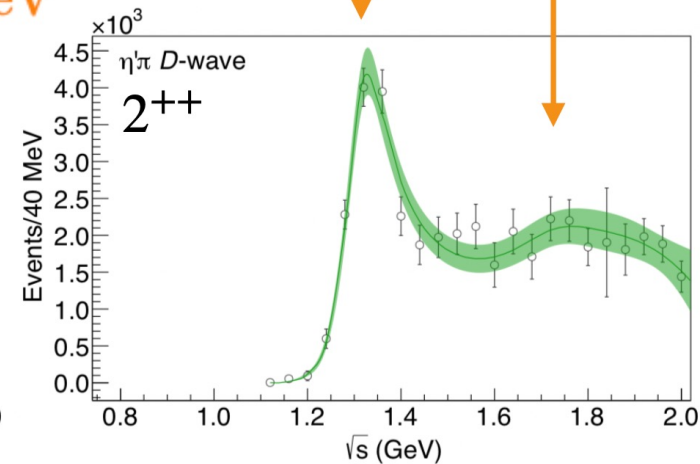
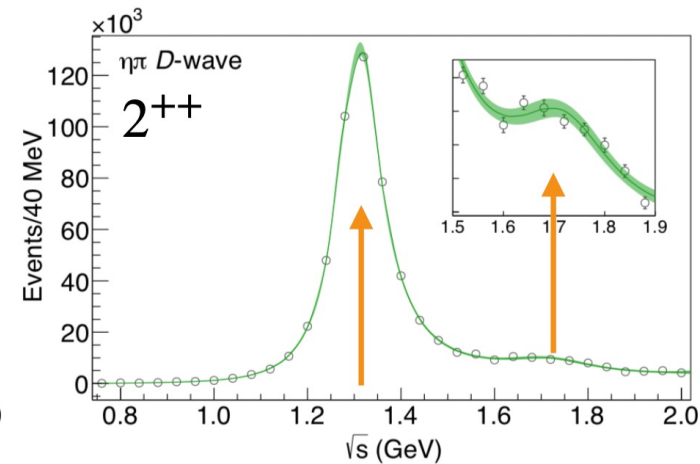
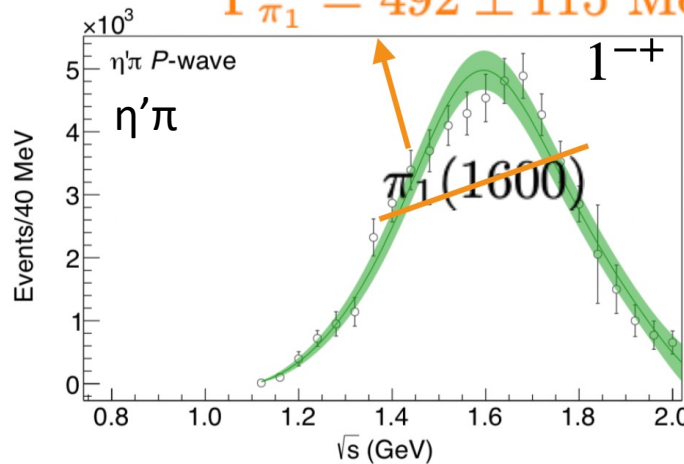


- JPAC re-analyzed published PW expansions
- Coupled channel fit to $\eta\pi$ and $\eta'\pi$ partial waves
- Determined pole positions for $a_2(1320)$, $a_2'(1700)$ and single exotic π_1 pole at 1564 MeV



$$M_{\pi_1} = 1564 \pm 89 \text{ MeV}$$

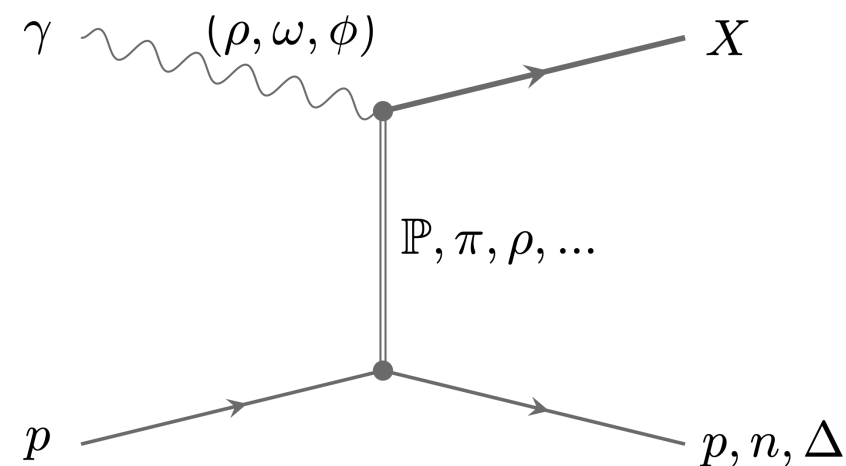
$$\Gamma_{\pi_1} = 492 \pm 115 \text{ MeV}$$



COMPASS: [PLB 740 \(2015\) 303](#) JPAC Rodas et al: [PRL 122 \(2019\) 042002](#)

Motivation for studying meson photo-production with polarized beam

- Wide range of states is accessible, including all lightest hybrids
 - Photons oscillate to vector mesons (vector meson dominance)
 - Virtual particle exchanged with the target proton
 - Exchanged particle could be Pomeron, π , ρ , ω , ...
- Polarization provides information on reaction mechanism
 - Extra constraint for amplitude analysis
- Little existing high-energy photoproduction data



Exchange		Exotic Final States	
\mathbb{P}	0^{++}	b, h, h'	$2^{+-}, 0^{+-}$
π^0	0^{-+}	b_2, h_2, h'_2	2^{+-}
π^\pm	0^{-+}	π_1^\pm	1^{-+}
ω	1^{--}	π_1, η_1, η'_1	1^{-+}

GlueX at Jefferson Lab, Newport News, VA, USA

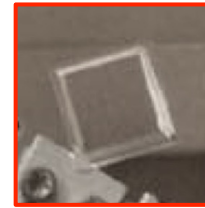
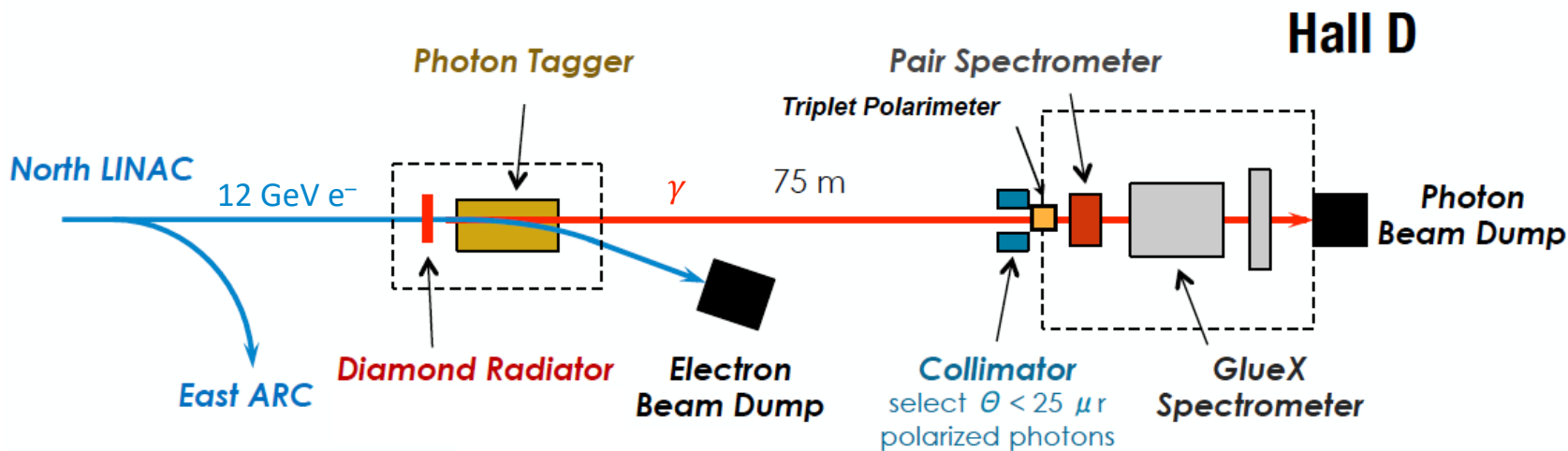


- 12 GeV electron beam from CEBAF Continuous Electron Beam Accelerator Facility
- Polarized photon beam created in Tagger Hall
- GlueX spectrometer located in Hall D
- 5th pass beam



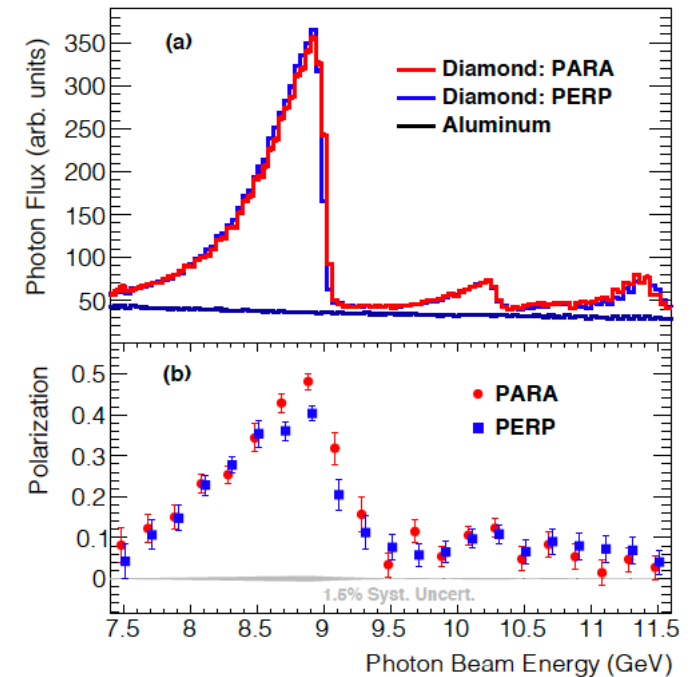
GlueX polarized photon beam

- 12 GeV e^- beam on thin diamond crystal
- 9 GeV linearly polarized photons via coherent Bremsstrahlung
- Intensity 5×10^7 γ/s in coherent peak
- Scintillator arrays measure energy of each scattered e^- , 'tag' its photon E_γ
tagging precision $\sim 0.1\%$ (resolution 5 MeV in coherent peak)
- $\sim 40\%$ linear polarization in coherent peak, measured in triplet polarimeter



Diamond
1cm x 1cm
x 20-70 μ m

Photon flux and polarization



[The GlueX Beamline and Detector
NIM A 987 \(2021\) 164807](#)

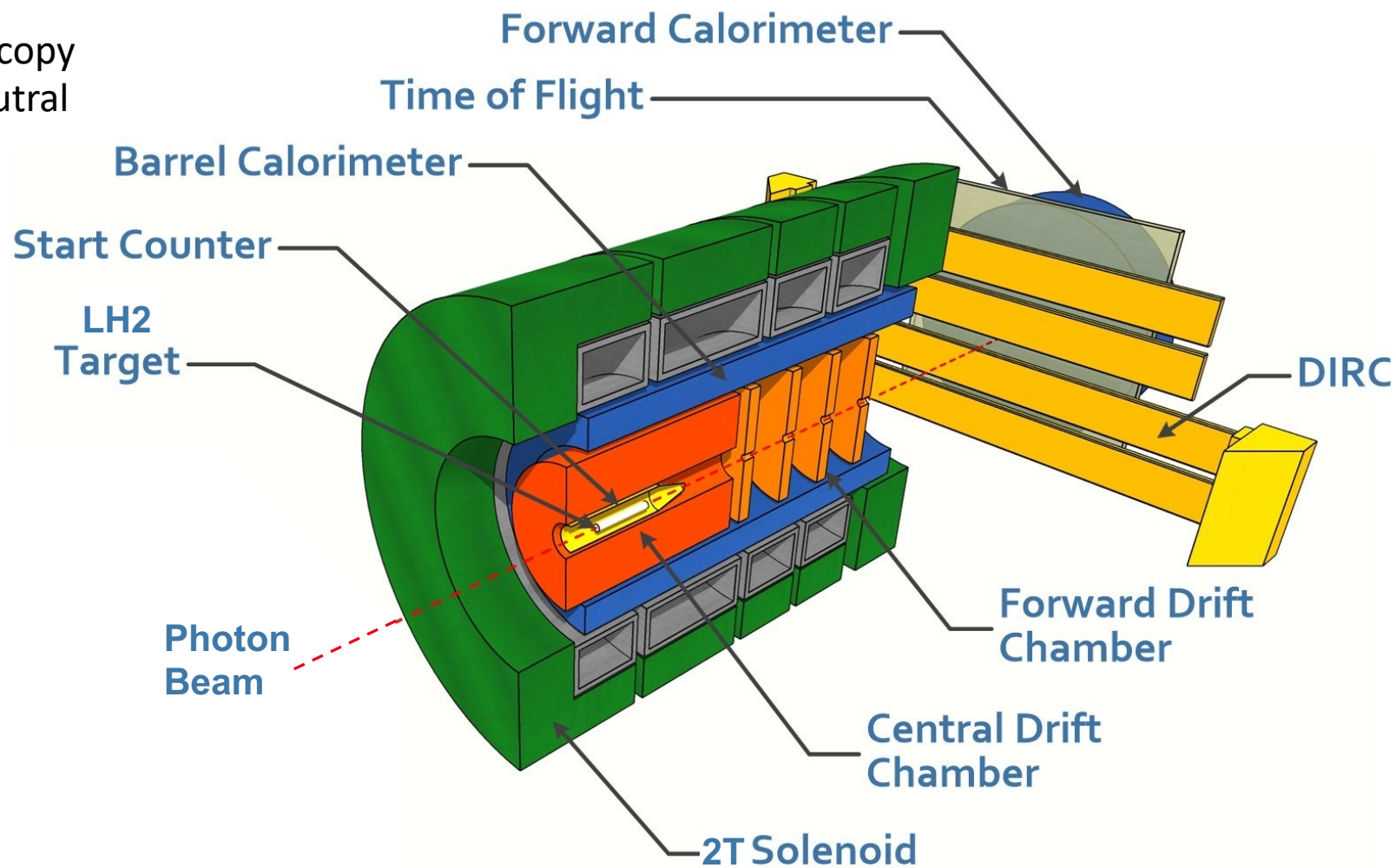
GlueX spectrometer

- Optimized for light meson spectroscopy
- Large acceptance for charged & neutral

- Acceptance $\theta = 1\text{--}120^\circ$
- Charged $\sigma_p/p \sim 1\text{--}5\%$
- Neutral $\sigma_E/E = 6\% / \sqrt{E} \oplus 2\%$

- GlueX-I 2017 – 2018
125 pb⁻¹ 8.2-8.8 GeV
- 2019 Added DIRC
- GlueX-II 2020 – 2025/6?
Expect 3-4 x GlueX-I

- Publications listed on gluex.org



[The GlueX Beamline and Detector](#)
[NIM A 987 \(2021\) 164807](#)

GlueX spectrometer



GlueX physics pathway – from familiar to exotic

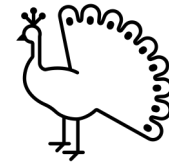
- Goal: explore spectrum of light hybrid mesons

- Strategy:

- study known mesons first
 - develop and refine software
 - improve knowledge of acceptance
 - learn about production mechanisms
 - talk to theorists



- look for exotics
 - keep talking to theorists



- Importance of Spin Density Matrix Elements (SDMEs):

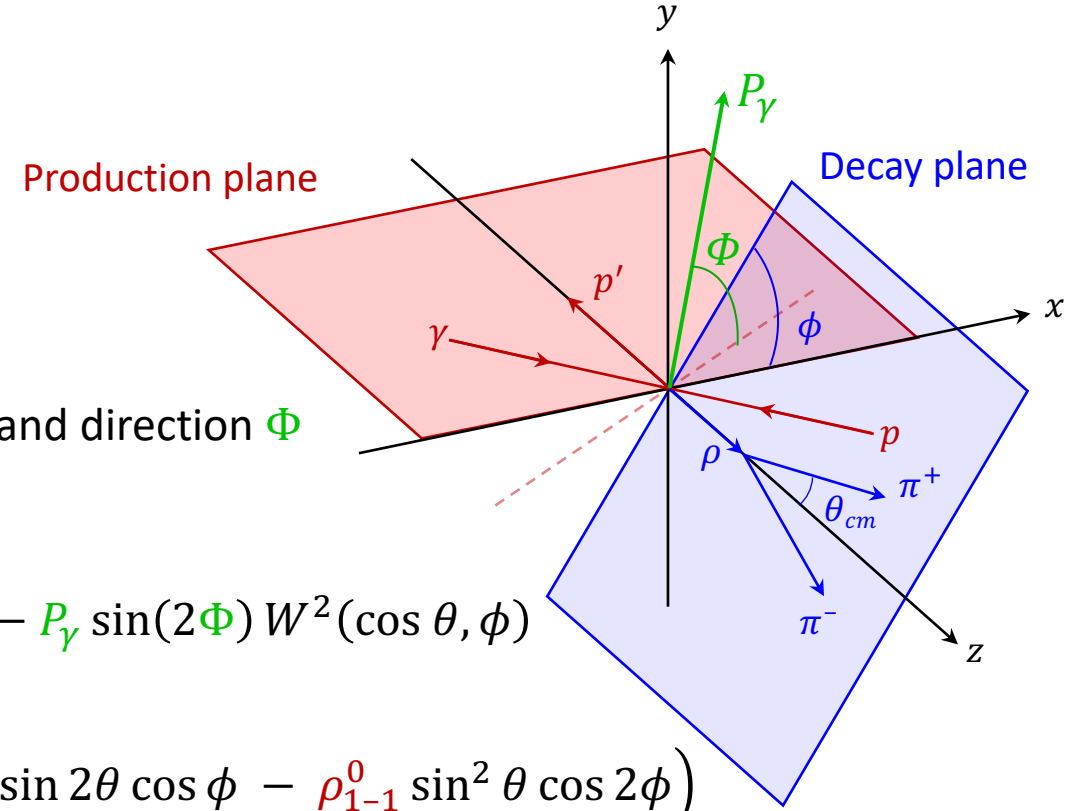
- useful observable
- production mechanism info
- input for theory and useful for modelling background processes
- very sensitive to acceptance
- amplitude analysis uses similar formalism and [AmpTools](#) software for multi-dimensional fits

- Published SDMEs: $\Lambda(1520)$ [Phys.Rev. C105 \(2022\) 035201](#)
 $\rho(770)$ [Phys.Rev. C108 \(2023\) 055204](#)

Upcoming: $\Delta^{++}(1232)$ <https://arxiv.org/abs/2406.12829>
Also working on $\phi(1020)$, $\omega(782)$

Vector Meson Spin Density Matrix Elements

- Detailed theory predictions, but previous measurements limited
- SDMEs ρ_{ij}^k measured by angular distribution of decay products
- Linear beam polarization gives access to 9 SDMEs
- Intensity expanded in $\cos \theta, \phi$ in helicity frame, beam polarization P_γ and direction Φ



$$W(\cos \theta, \phi, \Phi) = W^0(\cos \theta, \phi) - P_\gamma \cos(2\Phi) W^1(\cos \theta, \phi) - P_\gamma \sin(2\Phi) W^2(\cos \theta, \phi)$$

$$W^0(\cos \theta, \phi) = \frac{3}{4\pi} \left(\frac{1}{2}(1 - \rho_{00}^0) + \frac{1}{2}(3\rho_{00}^0 - 1) \cos^2 \theta - \sqrt{2} \operatorname{Re} \rho_{10}^0 \sin 2\theta \cos \phi - \rho_{1-1}^0 \sin^2 \theta \cos 2\phi \right)$$

$$W^1(\cos \theta, \phi) = \frac{3}{4\pi} \left(\rho_{11}^1 \sin^2 \theta + \rho_{00}^1 \cos^2 \theta - \sqrt{2} \operatorname{Re} \rho_{10}^1 \sin 2\theta \cos \phi - \rho_{1-1}^1 \sin^2 \theta \cos 2\phi \right)$$

$$W^2(\cos \theta, \phi) = \frac{3}{4\pi} \left(\sqrt{2} \operatorname{Im} \rho_{10}^2 \sin 2\theta \sin \phi + \operatorname{Im} \rho_{1-1}^2 \sin^2 \theta \sin 2\phi \right)$$

Schilling et al [NPB15\(1970\)397](#)

$\rho(770)$ Spin Density Matrix Elements

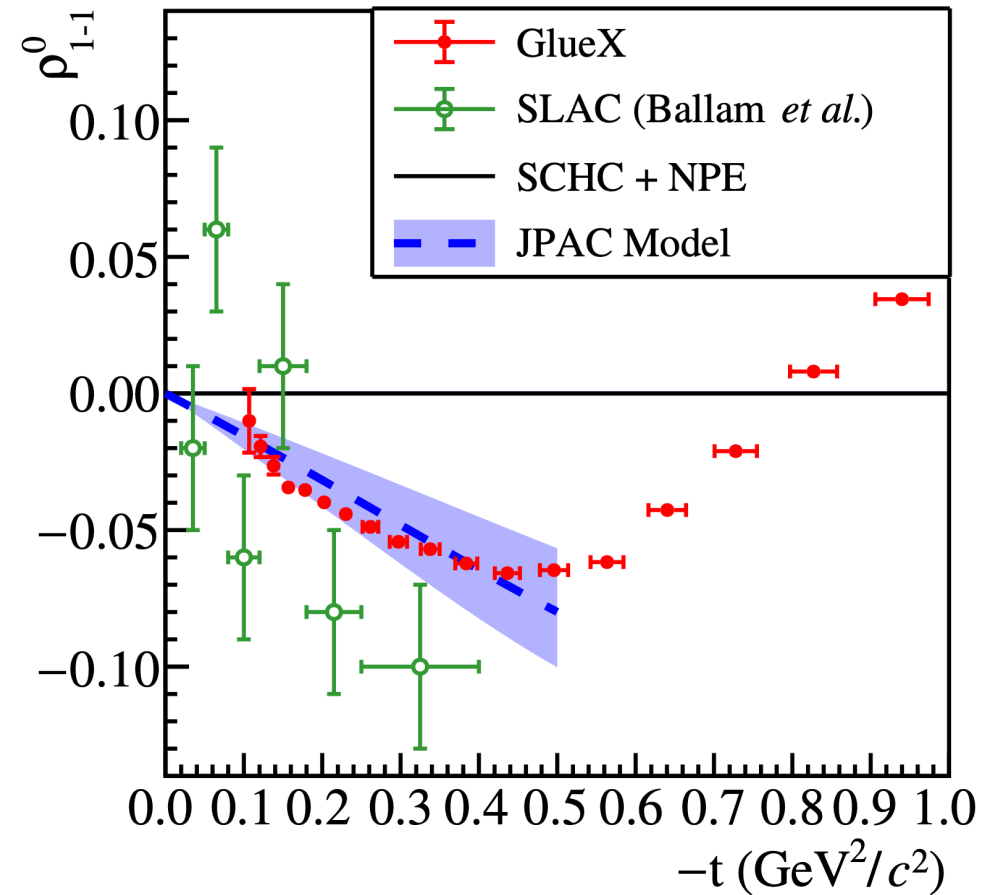
- 2017 data \sim 10% of eventual dataset
- Combined fit of 4 polarization orientations
- Consistent with previous measurements
- Consistent with JPAC Regge exchange model

GlueX data: [Phys.Rev. C108 \(2023\) 055204](#)

SLAC data: Ballam et al [Phys. Rev. D7 \(1973\) 3150](#)

JPAC model: Mathieu et al [Phys. Rev. D97 \(2018\) 094003](#)

ρ_{1-1}^0 (helicity frame) from $\gamma p \rightarrow \rho(770) p \rightarrow \pi^+\pi^- p$



$\rho(770)$ Spin Density Matrix Elements

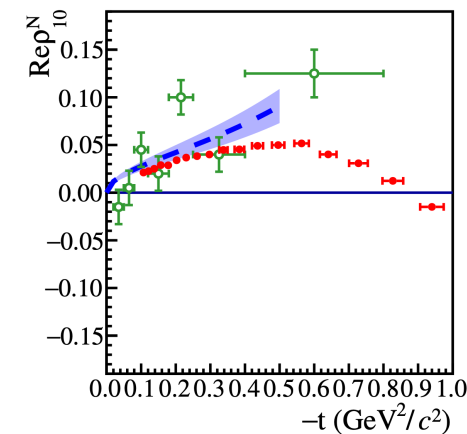
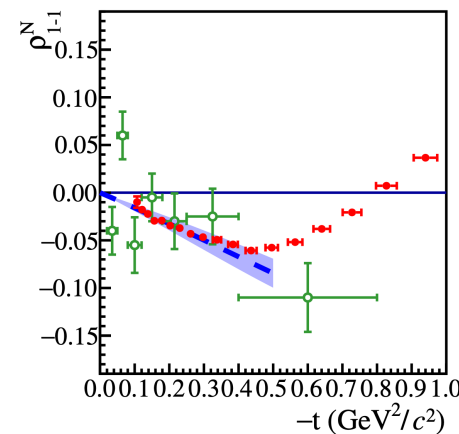
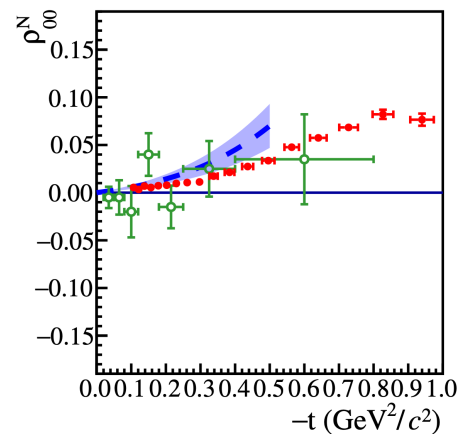
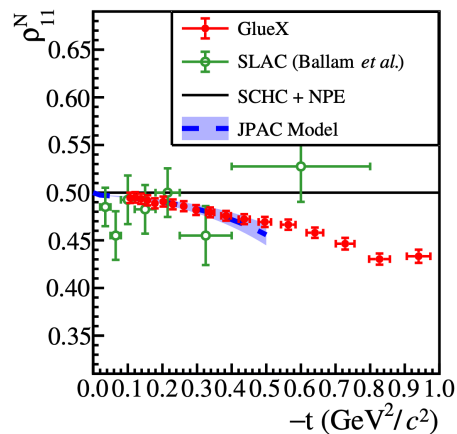
- SDMEs describe combinations of natural and unnatural parity exchange
- Unnatural parity components \ll natural parity components $\rho_{11}^N \sim 0.5$

GlueX [PRC 108 \(2023\) 055204](#)

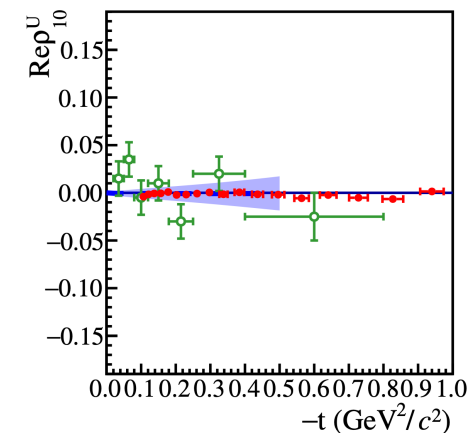
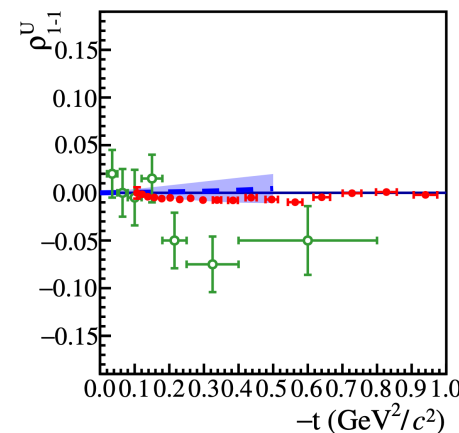
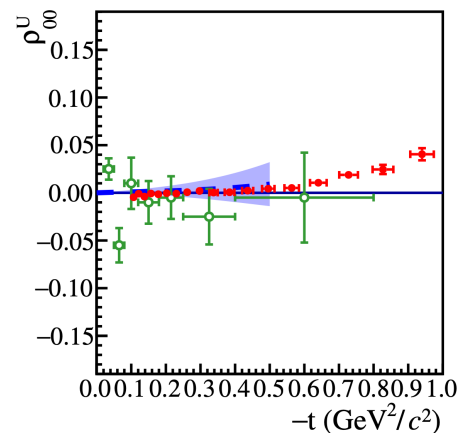
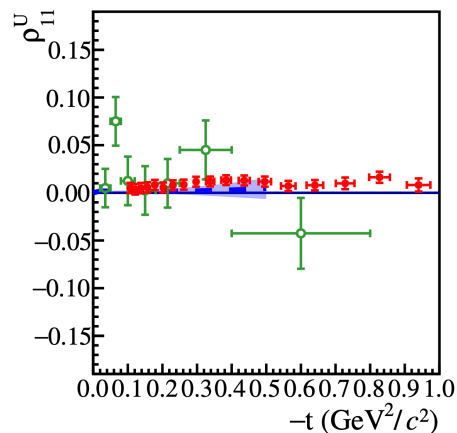
SLAC [PRD 7 \(1973\) 3150](#)

JPAC [PRD 97 \(2018\) 094003](#)

Natural Parity Exchange
e.g. $0^+ \mathbb{P}, 1^- \rho$



Unnatural Parity Exchange
e.g. $0^- \pi$



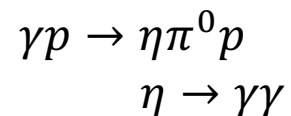
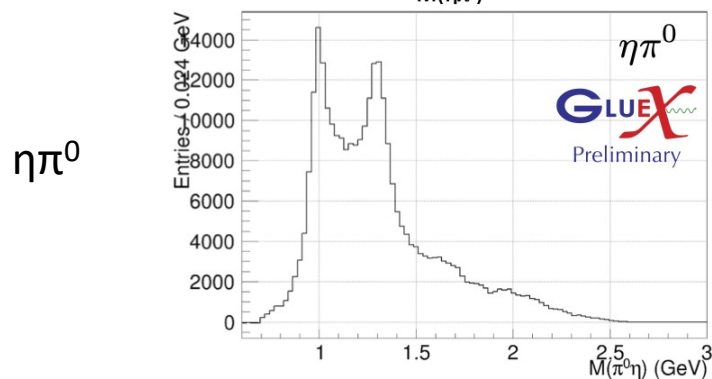
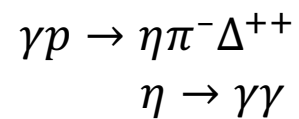
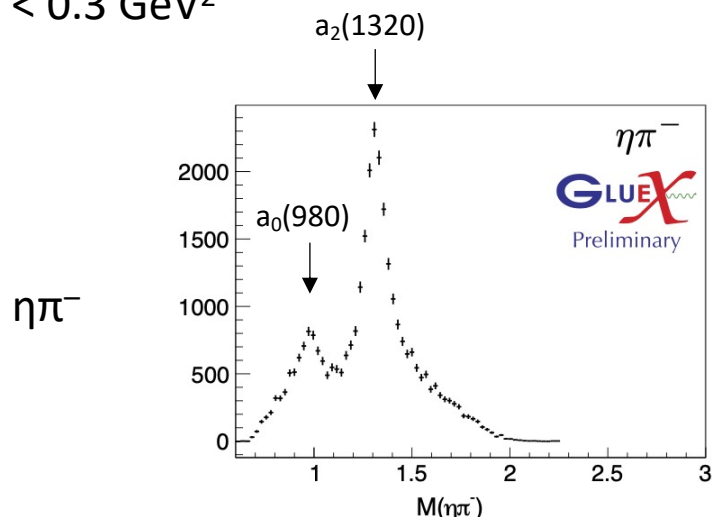
Using $a_2(1320)$ as a stepping-stone to spin-exotics

- Next progression in complexity is amplitude analysis of another non-exotic meson
- $a_2(1320)$ is well-known, not exotic, produced abundantly and decays via $\eta\pi$
- 2 decay modes - comparison helps to improve acceptance and background removal techniques
- Plan to use $a_2(1320)$ as a standard reference to compare with smaller exotic contributions to $\eta'\pi$
- Understanding the $a_2(1320)$ in $\eta\pi$ is a key step towards $\eta'\pi$ and exotics

$a_2(1320)$ in $\eta\pi$

- Clear signals at $a_0(980)$ and $a_2(1320)$ masses (not acceptance-corrected)

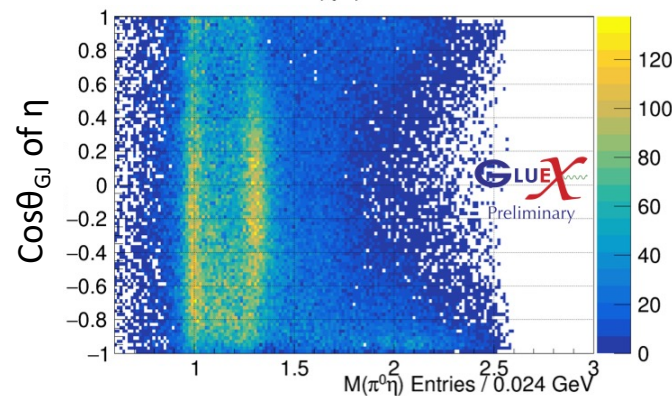
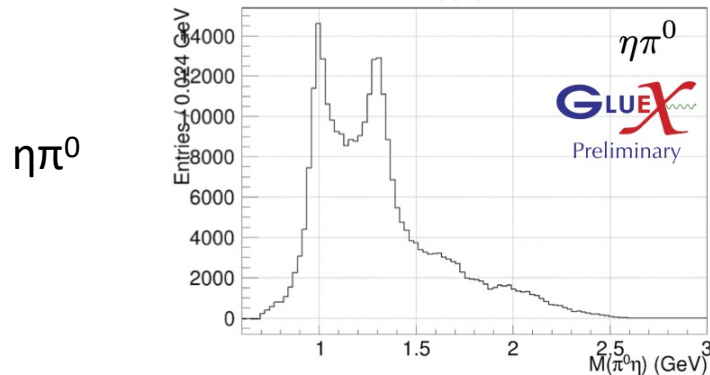
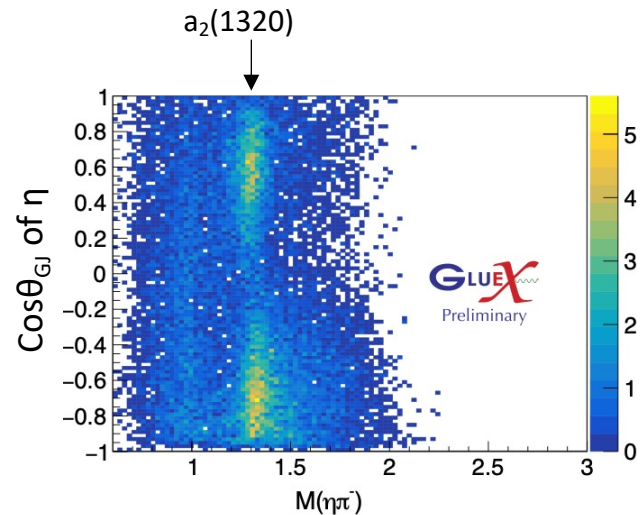
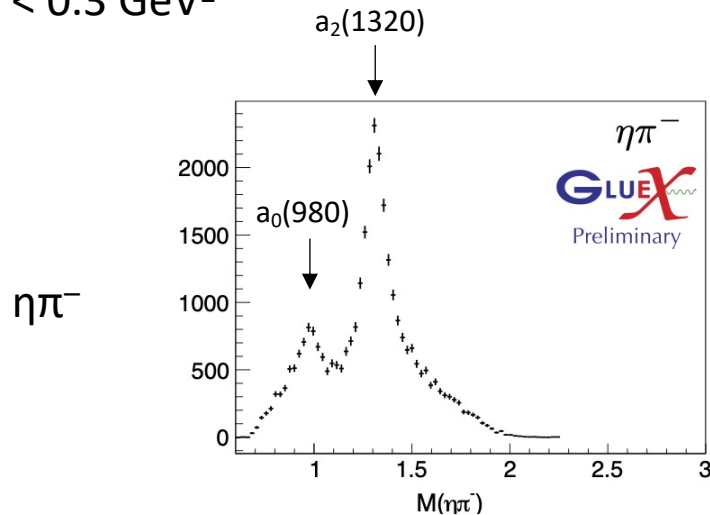
$0.1 < -t < 0.3 \text{ GeV}^2$



$a_2(1320)$ in $\eta\pi$

- Clear signals at $a_0(980)$ and $a_2(1320)$ masses
- $a_2(1320)$ angular distribution very different between charged and neutral decay modes

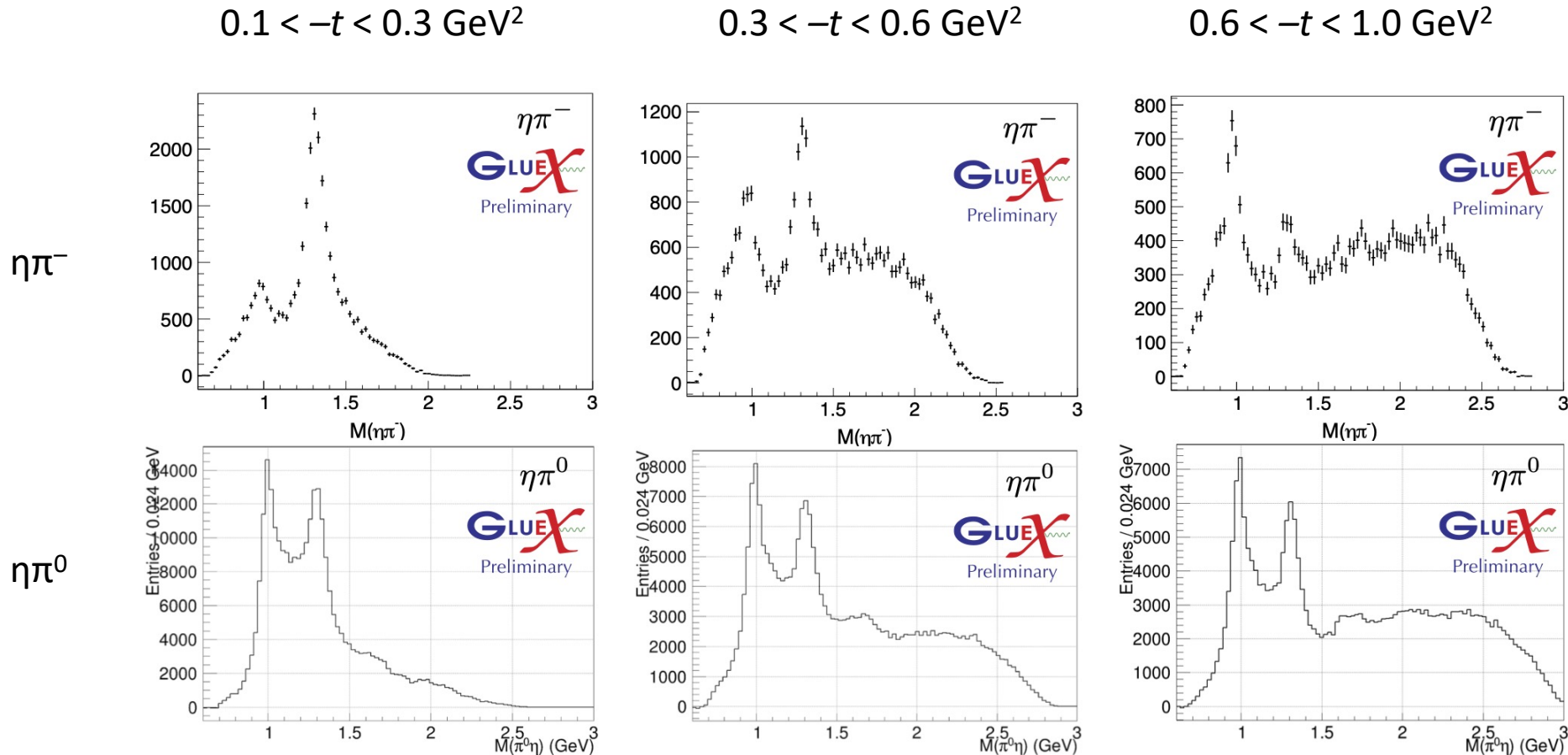
$0.1 < -t < 0.3 \text{ GeV}^2$



Different spin-projection states populated

$a_2(1320)$ in $\eta\pi$

- Clear signals at $a_0(980)$ and $a_2(1320)$ masses
- $a_2(1320)$ angular distribution very different between charged and neutral decay modes
- Relative population changes with t



$a_2(1320)$ in $\gamma p \rightarrow \eta \pi^0 p$ Semi-mass-independent amplitude analysis

- Amplitude formalism $Z_l^m(\Omega, \Phi) = Y_l^m(\Omega) e^{-i\Phi}$

JPAC: Mathieu et al [PRD 100 \(2019\) 054017](#)

Intensity(Ω, Φ) =

$$2\kappa \left\{ \begin{aligned} & (1 - P_\gamma) \left| \sum_{l,m} [l]_m^{(-)} \operatorname{Re}[Z_l^m(\Omega, \Phi)] \right|^2 + (1 - P_\gamma) \left| \sum_{l,m} [l]_m^{(+)} \operatorname{Im}[Z_l^m(\Omega, \Phi)] \right|^2 \\ & + (1 + P_\gamma) \left| \sum_{l,m} [l]_m^{(+)} \operatorname{Re}[Z_l^m(\Omega, \Phi)] \right|^2 + (1 + P_\gamma) \left| \sum_{l,m} [l]_m^{(-)} \operatorname{Im}[Z_l^m(\Omega, \Phi)] \right|^2 \end{aligned} \right\}$$

Reflectivity + natural parity exchange

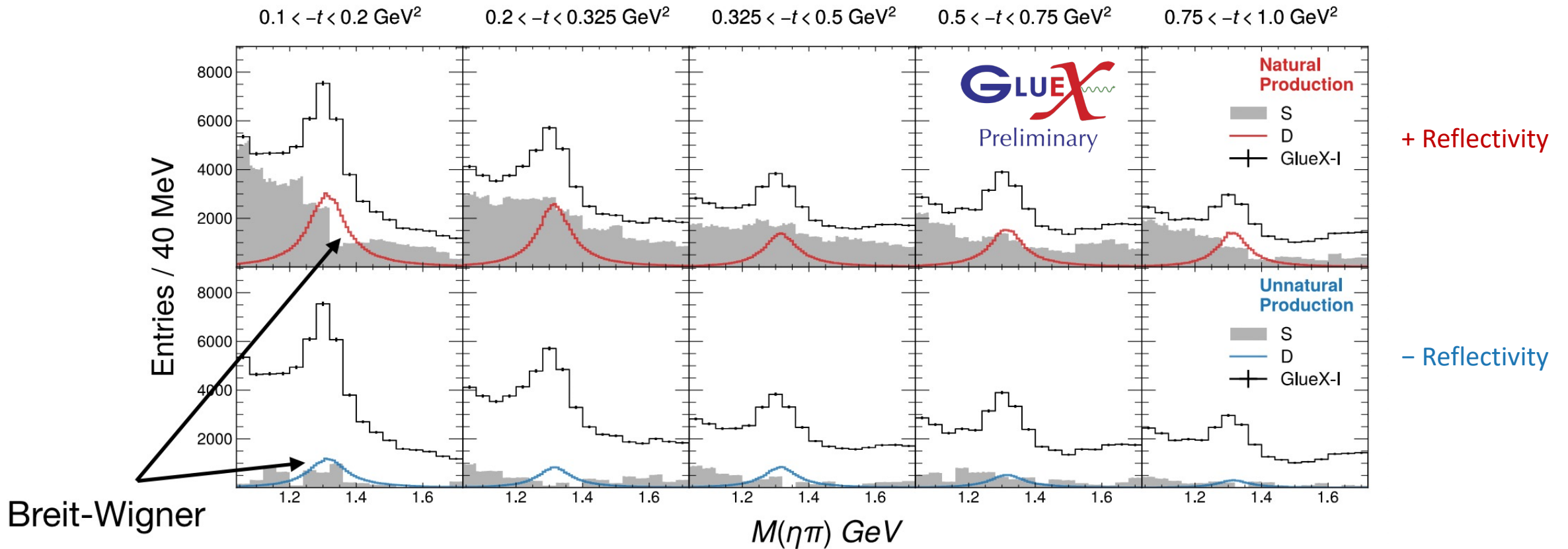
Reflectivity - unnatural parity exchange

Naturality $N = P(-1)^J$ $N=+1$ 'natural' for $0+$ etc

Reflectivity = $N(\text{exchanged particle}) \times N(\text{resonance})$

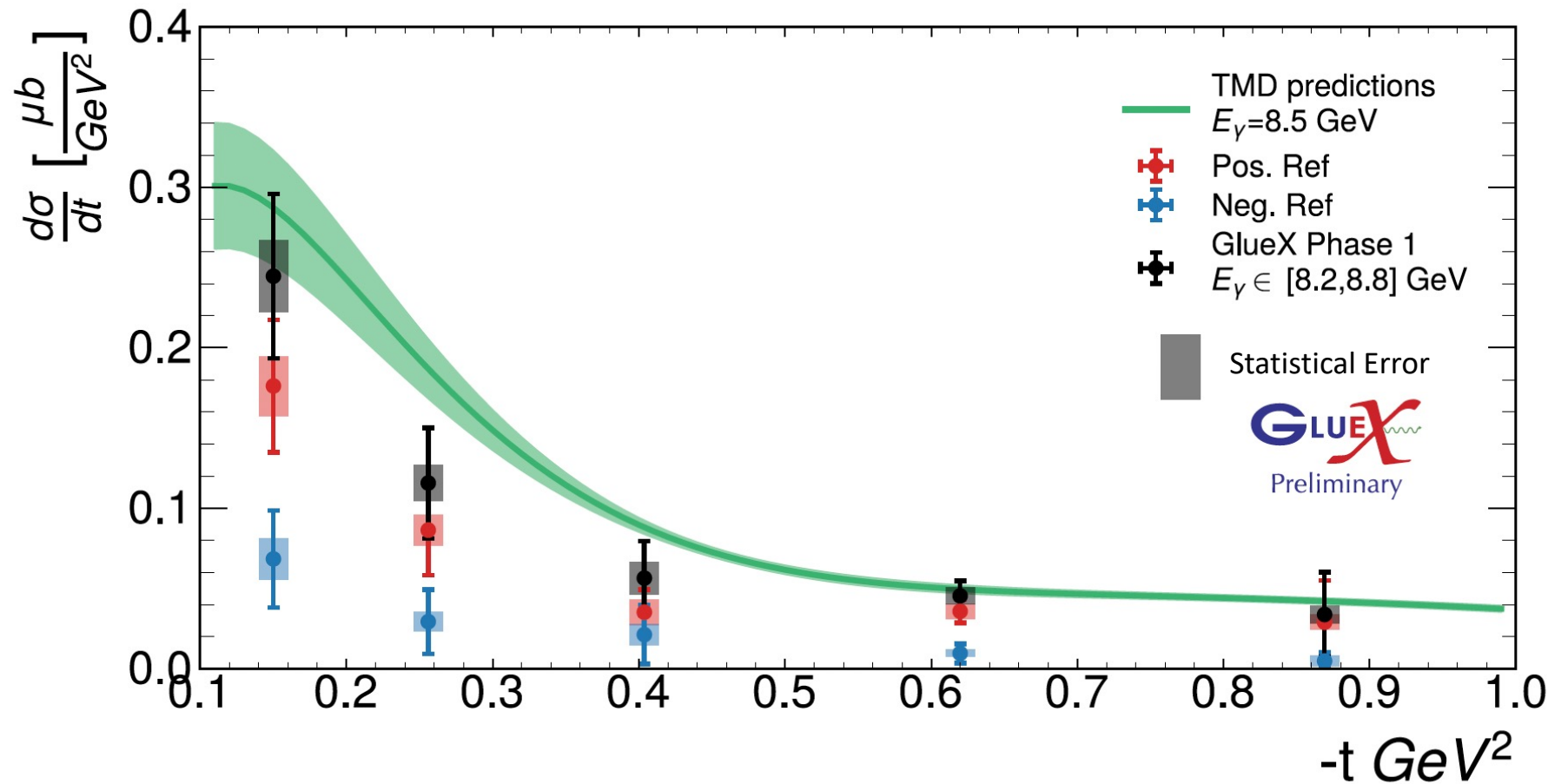
$a_2(1320)^0$ in $\gamma p \rightarrow \eta\pi^0 p$ Semi-mass-independent amplitude analysis

- Mass binned approach for the S-wave (complicated, includes double Regge + non-resonant processes)
- Model $a_2(1320)$ using a Breit-Wigner, as it is reasonably well isolated



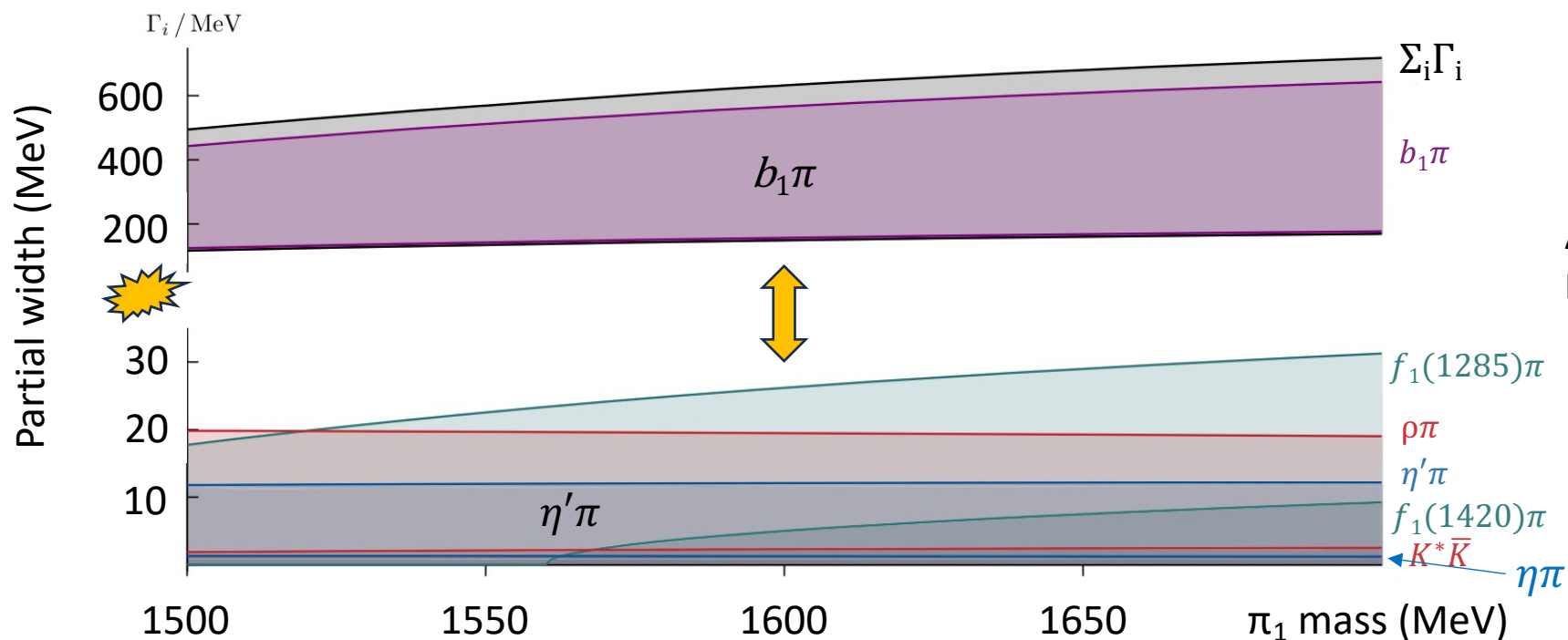
$a_2(1320)^0$ differential cross-section from $\gamma p \rightarrow \eta\pi^0 p$

- Good agreement with TMD theory from JPAC Mathieu et al [PRD 102 \(2020\) 014003](#)
- Predominantly + reflectivity, ie natural parity exchange, eg ρ , ω
- Publication in preparation



$\pi_1(1600)$ partial decay width predictions

- HadSpec, Woss et al [PRD 103 \(2021\) 054502](#)
- Lattice QCD predictions of partial decay widths of $\pi_1(1600)$ as a function of its mass
- $\pi_1(1600)$ decay channels are dominated by $b_1\pi$ ($\sim 95\%$); decays to $\omega\pi$, final state 5π
- Experimentally, decay to $\eta\pi$ and $\eta'\pi$ might be easier to identify, although much less populated.



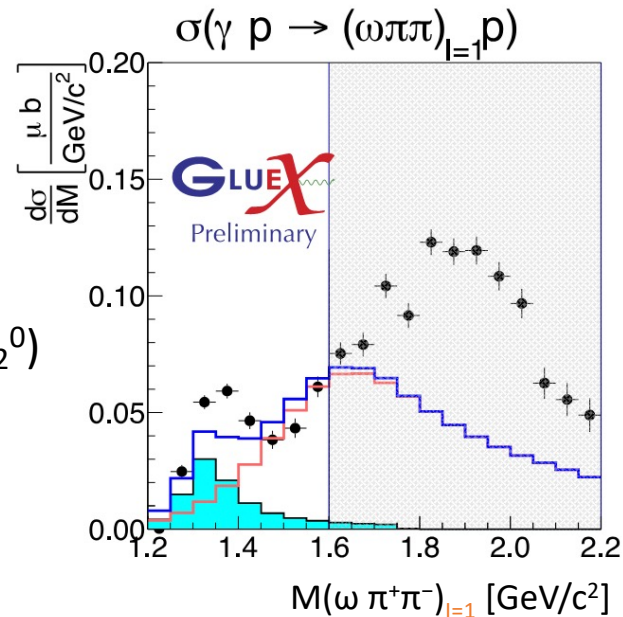
All modes except $K^*\bar{K}$ observed
 Meyer and Swanson [PPNP 82 \(2015\) 21](#)

$\pi_1(1600)$ cross-section upper limit

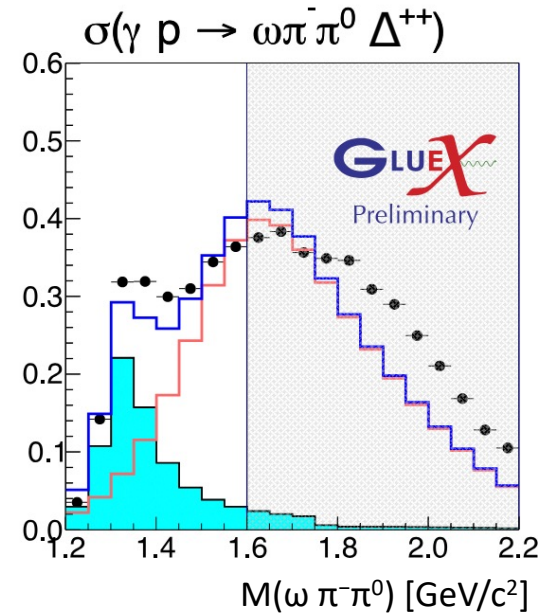
- π_1 has **isospin 1**, predicted to decay predominantly to $b_1(1235)\pi$, then to $\omega\pi\pi$
- Measured cross-sections for

$\gamma p \rightarrow \omega \pi^+ \pi^- p$	$\omega\pi\pi$ isospin 0 and 1
$\gamma p \rightarrow \omega \pi^0 \pi^0 p$	$\omega\pi\pi$ isospin 0
- Used Clebsch-Gordan coefficients to obtain $\sigma(\omega\pi\pi)_{I=1} = \sigma(\omega\pi^+\pi^-) - 2\sigma(\omega\pi^0\pi^0)$
- Also measured cross-section for $\gamma p \rightarrow \omega \pi^- \pi^0 \Delta^{++}$ $\omega\pi\pi$ **isospin 1**
- Fit the **I=1** cross-section **up to 1600 MeV** as $a_2(1320) + \pi_1(1600)$ using Breit-Wigners (widths from PDG & JPAC)

Neutral mode
 $\sigma(\pi_1^0) < 2.09 \sigma(a_2^0)$

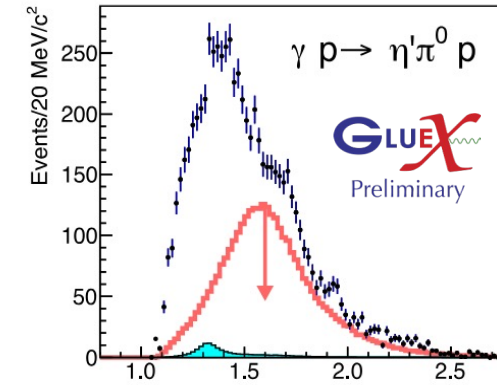
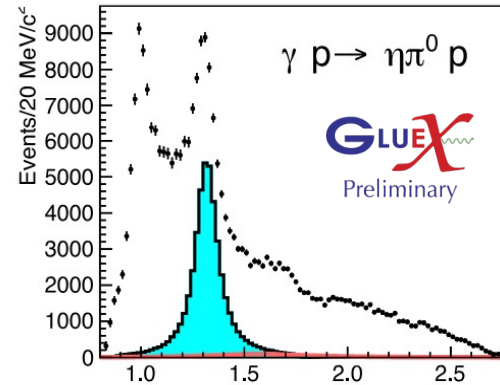


Charged mode
 $\sigma(\pi_1^-) < 1.40 \sigma(a_2^-)$

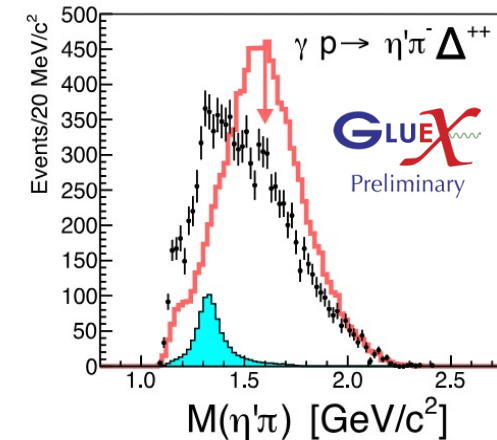
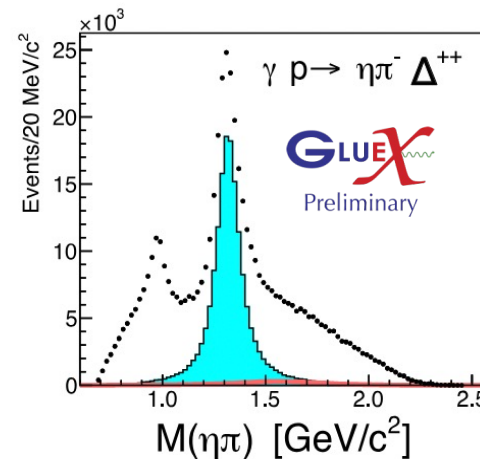


$\pi_1(1600)$ cross-section upper limit, projected into $\eta\pi$ and $\eta'\pi$

- Used decay widths from HadSpec [PRD 103 \(2021\) 054502](#) to estimate upper limits for π_1 decaying to $\eta\pi$ and $\eta'\pi$
- Combined estimated maximum cross sections with GlueX luminosity and acceptance using Monte Carlo
- $\pi_1(1600)$ contribution appears to be small in $\eta\pi$, **could be large in $\eta'\pi$**
- Publication in preparation

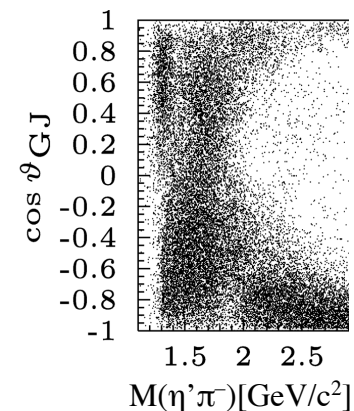


- —●— GlueX-I Data
- a_2 MC Projection
- π_1 MC Upper Limit

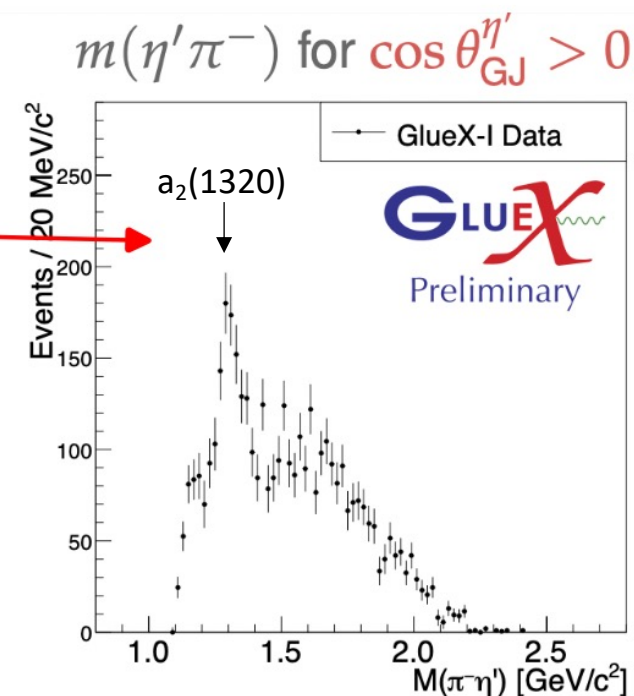
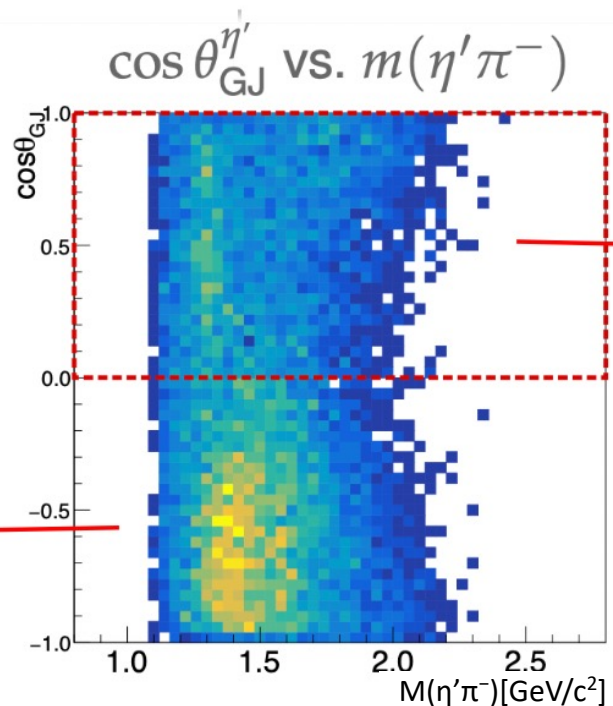
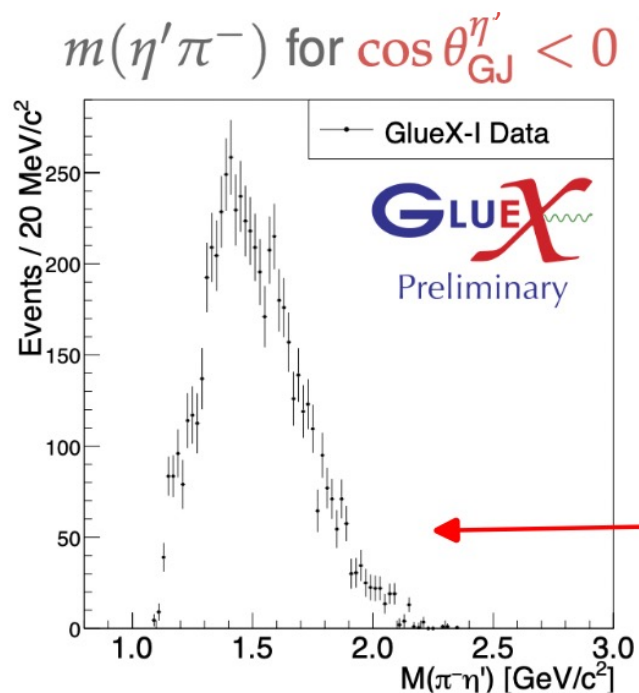


Analysis of $\gamma p \rightarrow \eta' \pi^- \Delta^{++}$

- Invariant mass of $\eta' \pi^-$ vs $\cos \theta_{GJ}^{\eta'}$
- Striking forward/backward asymmetry, reminiscent of [COMPASS data](#)
- Amplitude analysis is ongoing



[Phys Lett B](#)
[740 \(2015\)](#)
[303-311](#)

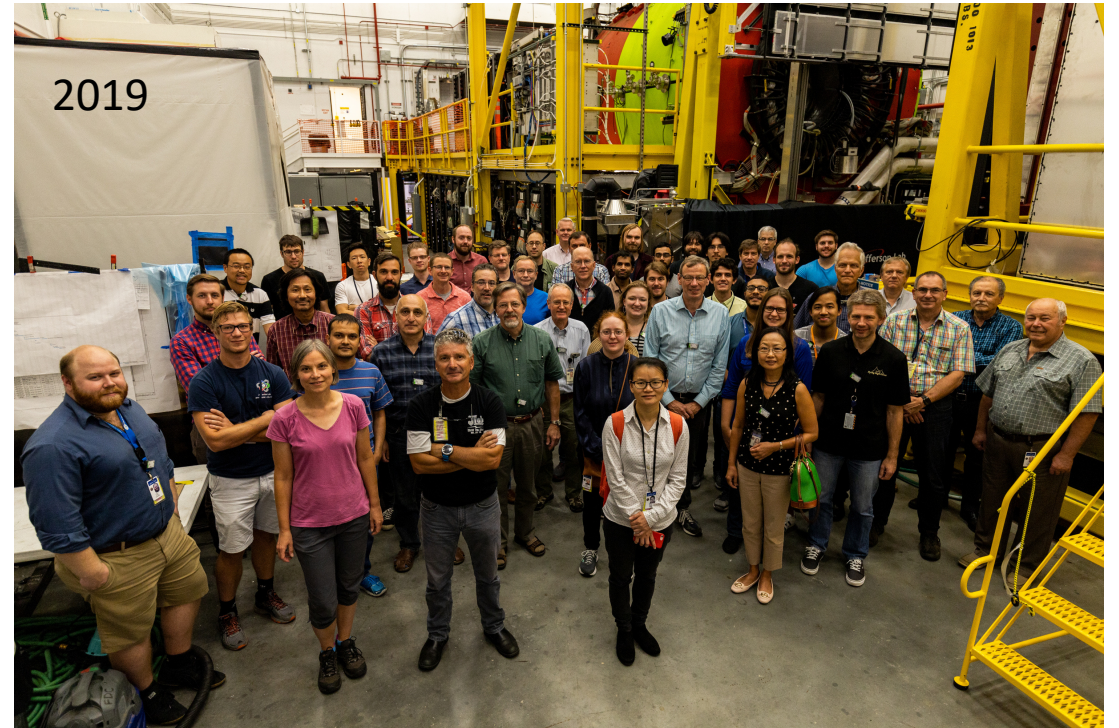


Conclusion and acknowledgements

Many GlueX analyses are in progress.

More publications are on the way.

Thank you for listening!



GlueX acknowledges the support of several funding agencies and computing facilities: www.gluex.org/thanks

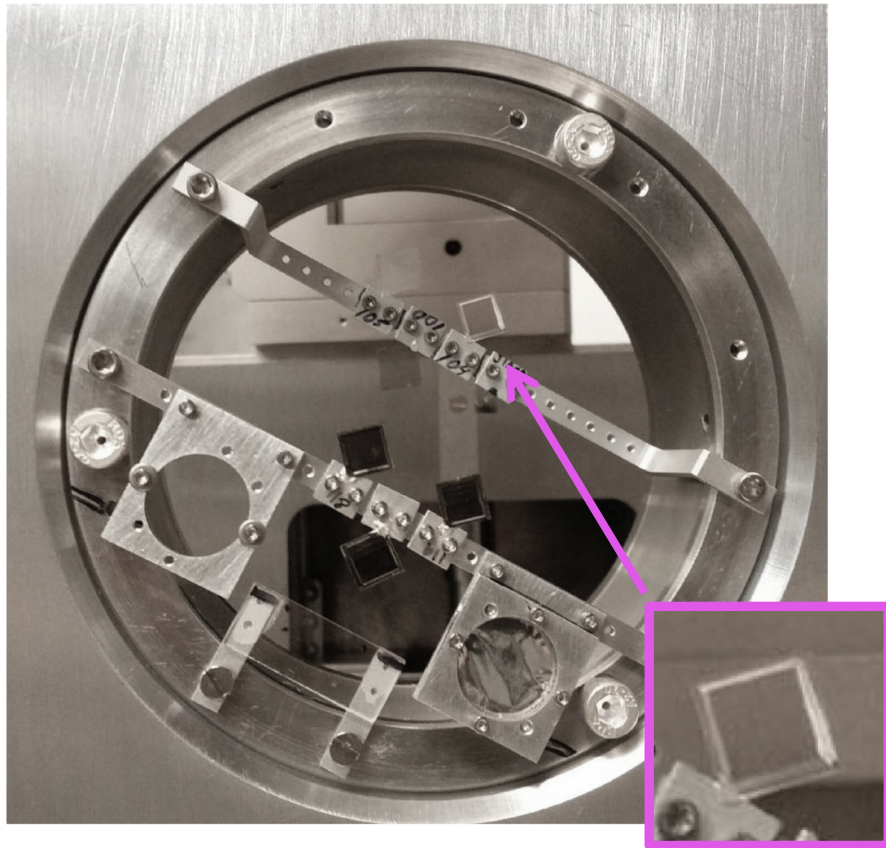
The Carnegie Mellon Group is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics, DOE Grant No. DE-FG02-87ER40315.

Extra slides



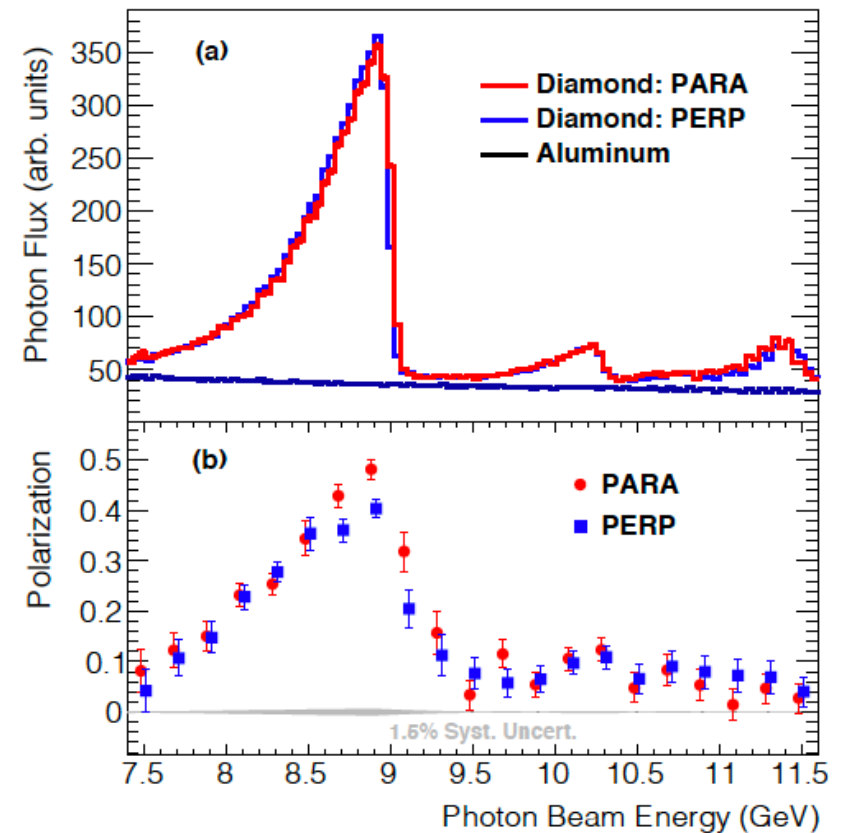
GlueX polarized photon beam

Radiators on goniometer



Diamond wafer size 1cm x 1cm x 20-70 μ m

Photon flux and polarization



[The GlueX Beamline and Detector](#)
[NIM A 987 \(2021\) 164807](#)

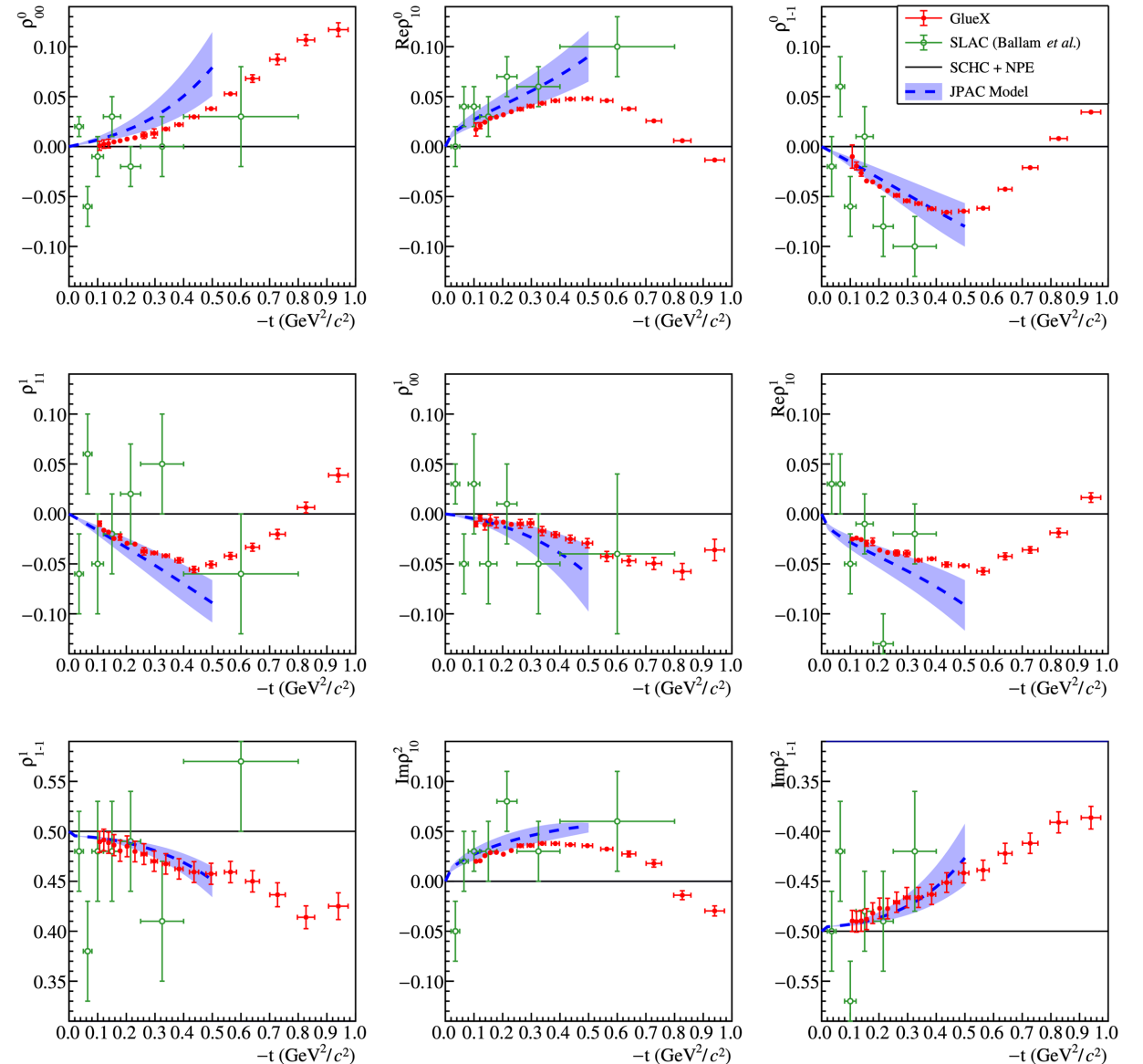
$\rho(770)$ Spin Density Matrix Elements

- 2017 data $\sim 10\%$ of eventual dataset
- Combined fit of 4 orientations of polarization
- Good agreement with previous measurements and model
- Natural parity exchange dominates, exchanged virtual particle could be (eg) \mathbb{P} , ρ , ω ...

GlueX data: [Phys.Rev. C108 \(2023\) 055204](#)

SLAC data: Ballam et al [PRD 7 \(1973\) 3150](#)

JPAC model: Mathieu et al [PRD 97 \(2018\) 094003](#)



Parity asymmetry for $\rho(770)$ photoproduction

- SDMEs describe combinations of natural & unnatural parity exchanges

Naturality of exchanged J^P $N = P(-1)^J$

$N = +1$ 'natural', eg $0^+ \mathbb{P}$, $1^- \rho$

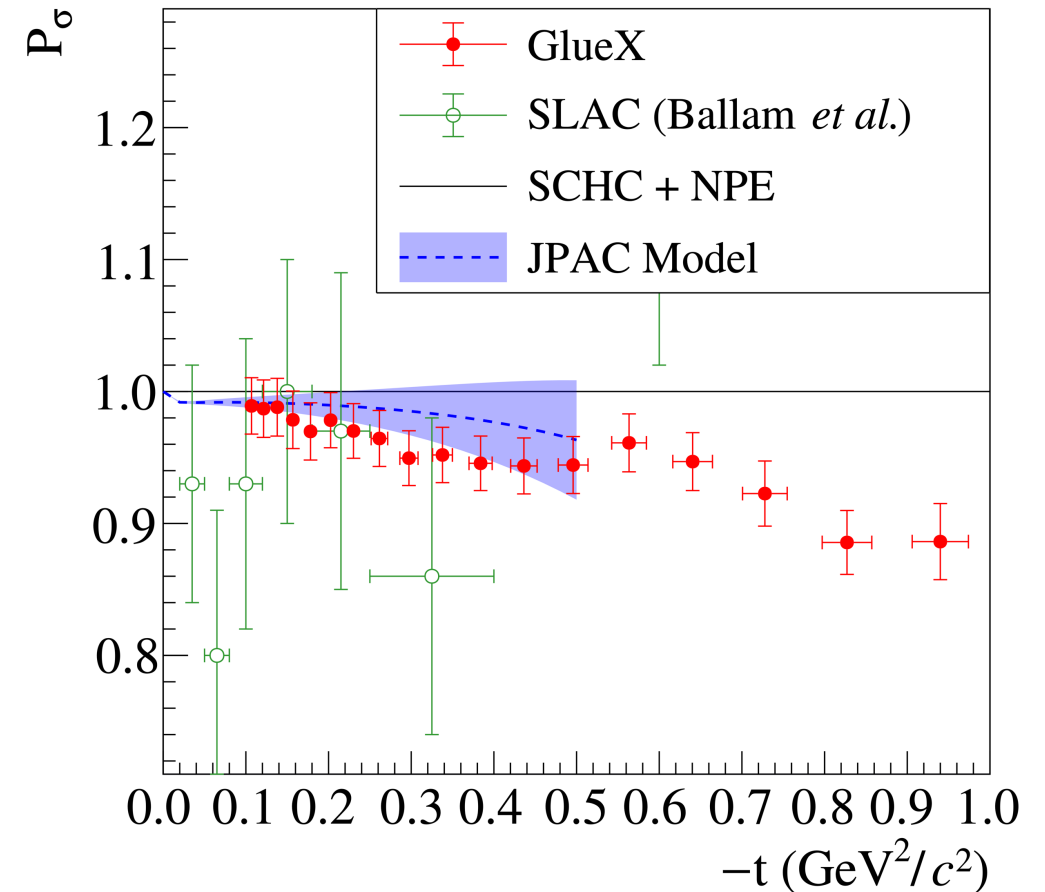
$N = -1$ 'unnatural', eg $0^- \pi$

- Separate N and U from SDMEs to find parity asymmetry


$$P_\sigma = \frac{\sigma^N - \sigma^U}{\sigma^N + \sigma^U} = 2\rho_{1-1}^1 - \rho_{00}^1$$

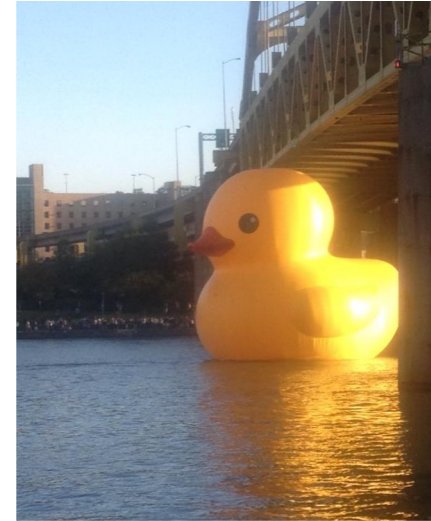
- Natural parity exchange dominates

P_σ for $\rho(770)$ photoproduction



GlueX physics pathway – from familiar to exotic

- Goal: explore spectrum of light hybrid mesons
- Strategy:
 - study known mesons first 
 - develop and refine software
 - improve knowledge of acceptance
 - learn about production mechanisms
 - talk to theorists
 - look for exotics
 - keep talking to theorists
- Importance of Spin Density Matrix Elements (SDMEs):
 - useful observable
 - production mechanism info
 - input for theory and useful for modelling background processes
 - very sensitive to acceptance
 - amplitude analysis uses similar formalism and [AmpTools](#) software for multi-dimensional fits
- Published SDMEs: $\Lambda(1520)$ [Phys.Rev. C105 \(2022\) 035201](#)
 $\rho(770)$ [Phys.Rev. C108 \(2023\) 055204](#)
- Upcoming: $\Delta^{++}(1232)$ <https://arxiv.org/abs/2406.12829>
Also working on $\phi(1020)$, $\omega(782)$



Search for exotic mesons via PWA of $\eta^{(\prime)}\pi$ system using new model of intensity

Model predicted number of events per unit phase space

Partial wave amplitudes (production of the wave)

Decay into two pseudo-scalars (parity constraints, L cons.)

$$I(\Omega, \Phi) = 2\kappa \sum_k \left\{ (1 - P_\gamma) \left| \sum_{l,m} [l]_{m;k}^{(-)} \operatorname{Re}[Z_l^m(\Omega, \Phi)] \right|^2 + (1 - P_\gamma) \left| \sum_{l,m} [l]_{m;k}^{(+)} \operatorname{Im}[Z_l^m(\Omega, \Phi)] \right|^2 \right. \\ \left. + (1 + P_\gamma) \left| \sum_{l,m} [l]_{m;k}^{(+)} \operatorname{Re}[Z_l^m(\Omega, \Phi)] \right|^2 + (1 + P_\gamma) \left| \sum_{l,m} [l]_{m;k}^{(-)} \operatorname{Im}[Z_l^m(\Omega, \Phi)] \right|^2 \right\}$$

P_γ - degree of polarization

$Z_l^m(\Omega, \Phi) \equiv Y_l^m(\Omega) e^{-i\Phi}$

$\Omega = (\theta, \varphi)$

l, m - spin, its projection

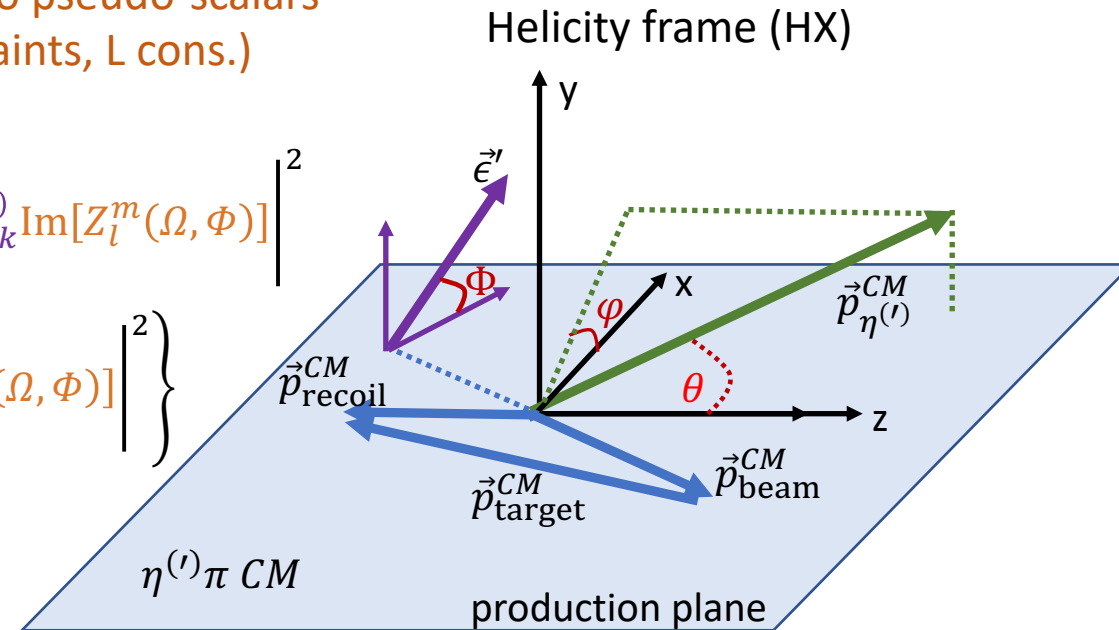
$\vec{\epsilon}'$ - γ polarization vector

κ - kinematical factors

Nucleon spin flip $k=1$, non-flip $k=0$

Reflectivity $\varepsilon = \pm 1$ corresponds to naturality of exchanged particle $\eta = P(-1)^J$

- natural parity $J^P = 0^+, 1^-, 2^+, \dots$
- unnatural parity $J^P = 0^-, 1^+, 2^-, \dots$



V. Mathieu et al. Phys. Rev. D 100, 054017 (2019)

Determine $[l]_{m;k}^{(-)}$, $[l]_{m;k}^{(+)}$ by fitting I_{EXP} using extended unbinned (in (θ, φ)) maximum likelihood method

(AmpTools package <https://github.com/mashephe/AmpTools>)