

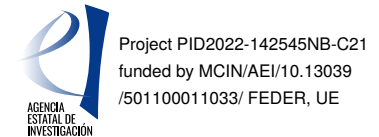
Beyond the Standard Model Physics with Neutrinos

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Neutrino oscillations: where we are

- Global 6-parameter fit (including δ_{CP}):
 - **Solar**: Cl + Ga + SK(1–4) + SNO-full (I+II+III) + BX(1–3);
 - **Atmospheric**: SK(1–4) + DeepCore;
 - **Reactor**: KamLAND + Dbl-Chooz + Daya-Bay + Reno;
 - **Accelerator**: Minos + T2K + NOvA;

- best-fit point and 1σ (3σ) ranges:

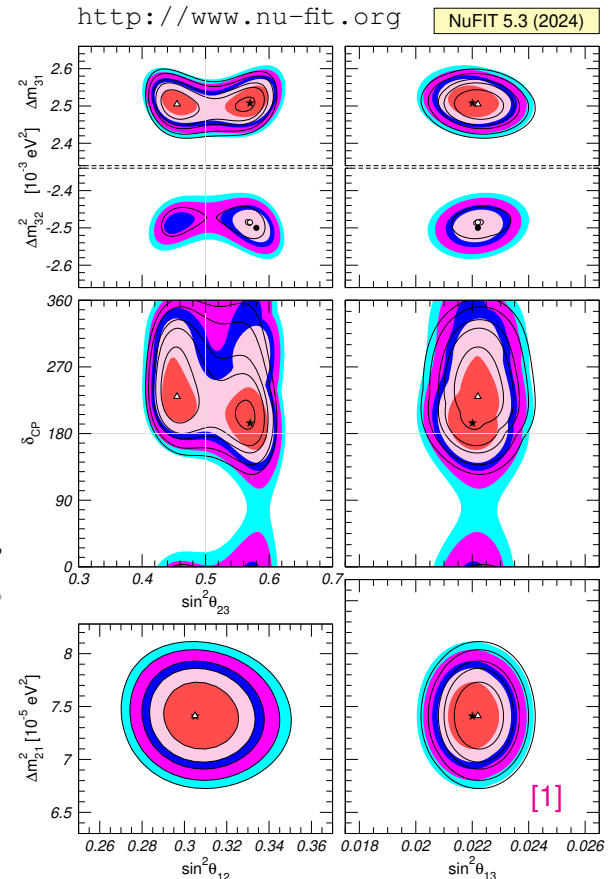
$$\theta_{12} = 33.66^{+0.73}_{-0.70} \left(\begin{smallmatrix} +2.28 \\ -2.06 \end{smallmatrix} \right), \quad \Delta m_{21}^2 = 7.41^{+0.21}_{-0.20} \left(\begin{smallmatrix} +0.62 \\ -0.60 \end{smallmatrix} \right) \times 10^{-5} \text{ eV}^2,$$

$$\theta_{23} = \begin{cases} 49.1^{+1.0}_{-1.3} \left(\begin{smallmatrix} +2.8 \\ -9.5 \end{smallmatrix} \right), \\ 49.5^{+0.9}_{-1.2} \left(\begin{smallmatrix} +2.6 \\ -9.5 \end{smallmatrix} \right), \end{cases} \quad \Delta m_{31}^2 = \begin{cases} +2.511^{+0.027}_{-0.027} \left(\begin{smallmatrix} +0.085 \\ -0.084 \end{smallmatrix} \right) \times 10^{-3} \text{ eV}^2, \\ -2.498^{+0.032}_{-0.024} \left(\begin{smallmatrix} +0.090 \\ -0.083 \end{smallmatrix} \right) \times 10^{-3} \text{ eV}^2, \end{cases}$$

$$\theta_{13} = 8.54^{+0.11}_{-0.11} \left(\begin{smallmatrix} +0.36 \\ -0.35 \end{smallmatrix} \right), \quad \delta_{\text{CP}} = 197^{+41}_{-25} \left(\begin{smallmatrix} +207 \\ -89 \end{smallmatrix} \right);$$

- neutrino mixing matrix:

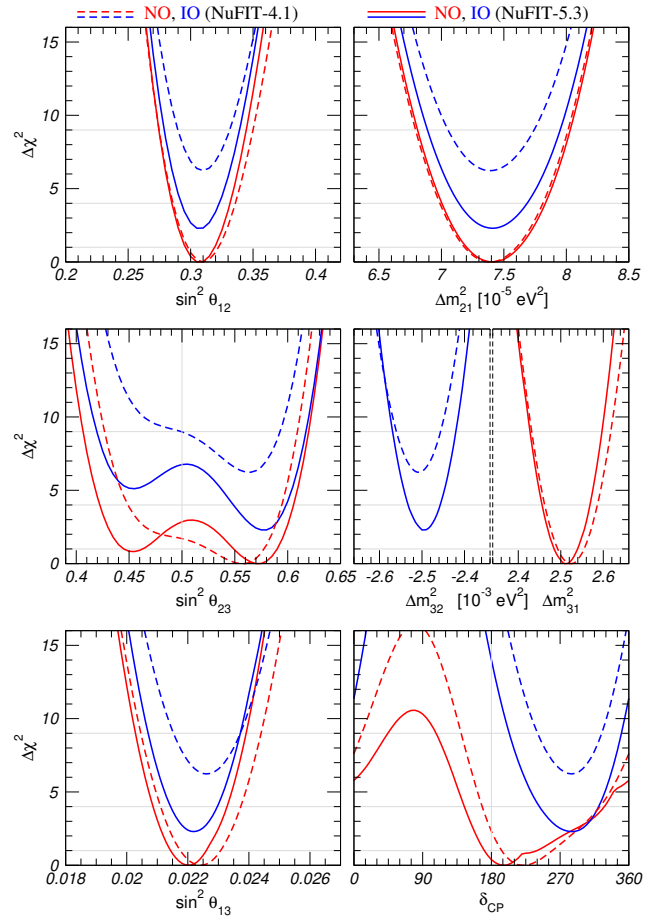
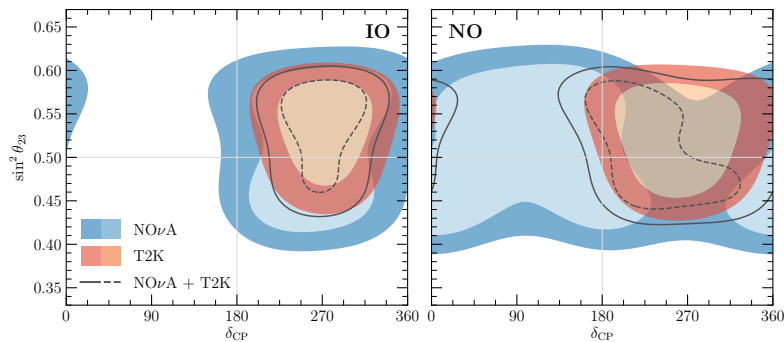
$$|U|_{3\sigma} = \begin{pmatrix} 0.801 \rightarrow 0.842 & 0.518 \rightarrow 0.580 & 0.143 \rightarrow 0.155 \\ 0.244 \rightarrow 0.500 & 0.498 \rightarrow 0.690 & 0.634 \rightarrow 0.770 \\ 0.276 \rightarrow 0.521 & 0.473 \rightarrow 0.672 & 0.621 \rightarrow 0.759 \end{pmatrix}.$$



[1] I. Esteban *et al.*, JHEP **09** (2020) 178 [arXiv:2007.14792] & NuFIT 5.3 [http://www.nu-fit.org].

Open issues in 3ν oscillations

- **CP violation**: tension on δ_{CP} between T2K and NOvA for the case of normal ordering (NO);
 - **Mass ordering**: due to such tension, long-standing hints in favor of NO is now reduced;
 - **θ_{23} octant**: still no clue on deviation of θ_{23} from maximal, and (if so) in which direction;
 - future experiments expected to shed light;
- ❓ can New Physics play a role in their task?



Non-standard neutrino interactions: formalism

- Effective low-energy Lagrangian for **standard** neutrino interactions with matter:

$$\mathcal{L}_{\text{SM}}^{\text{eff}} = -2\sqrt{2}G_F \sum_{f,\beta} ([\bar{\nu}_\beta \gamma_\mu P_L \ell_\beta][\bar{f} \gamma^\mu P_L f'] + \text{h.c.}) - 2\sqrt{2}G_F \sum_{f,P,\beta} g_P^f [\bar{\nu}_\beta \gamma_\mu P_L \nu_\beta][\bar{f} \gamma^\mu P f]$$

where $P \in \{P_L, P_R\}$, (f, f') form an SU(2) doublet, and g_P^f is the Z coupling to fermion f :

$$\begin{aligned} g_L^v &= \frac{1}{2}, & g_L^\ell &= \sin^2 \theta_W - \frac{1}{2}, & g_L^u &= -\frac{2}{3} \sin^2 \theta_W + \frac{1}{2}, & g_L^d &= \frac{1}{3} \sin^2 \theta_W - \frac{1}{2}, \\ g_R^v &= 0, & g_R^\ell &= \sin^2 \theta_W, & g_R^u &= -\frac{2}{3} \sin^2 \theta_W, & g_R^d &= \frac{1}{3} \sin^2 \theta_W; \end{aligned}$$

- here we consider **NC-like non-standard** neutrino-matter described by:

$$\mathcal{L}_{\text{NSI}}^{\text{eff}} = -2\sqrt{2}G_F \sum_{f,P,\alpha,\beta} \epsilon_{\alpha\beta}^{fP} [\bar{\nu}_\alpha \gamma_\mu P_L \nu_\beta][\bar{f} \gamma^\mu P f];$$

- ordinary matter composed by $\{e, u, d\} \Rightarrow \nu$ propagation sensitive to NSI with them;
- some experiments sensitive to $\nu - e$ elastic scattering \Rightarrow **NC-like** NSI with e affect both propagation and interactions \Rightarrow require dedicated treatment \Rightarrow ignored for now;
- conversely, **NC-like** NSI's with quarks do **not** affect processes such as **lepton appearance**, which involve quarks through **CC** interactions \Rightarrow only ν propagation affected.

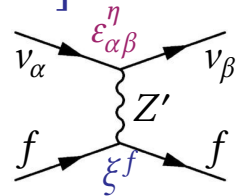
Non-standard neutrino interactions: formalism

- Conventionally, only NSI with either u or d quarks have been considered;
- still, both cases can appear simultaneously, and produce consequences (e.g., cancellations) which invalidate the u -only or d -only bounds;
- however, most general parameter space too large to handle \Rightarrow simplifications needed;
- here we assume that the ν flavor structure is **independent** of the charged fermion type:

$$\varepsilon_{\alpha\beta}^{fP} \equiv \varepsilon_{\alpha\beta}^{\eta} \xi^{fP} \Rightarrow \mathcal{L}_{\text{NSI}}^{\text{eff}} = -2\sqrt{2}G_F \left[\sum_{\alpha,\beta} \varepsilon_{\alpha\beta}^{\eta} (\bar{\nu}_{\alpha} \gamma^{\mu} P_L \nu_{\beta}) \right] \left[\sum_{fP} \xi^{fP} (\bar{f} \gamma_{\mu} P f) \right];$$

- since neutrino **propagation** is only sensitive to the vector couplings:

$$\varepsilon_{\alpha\beta}^f \equiv \varepsilon_{\alpha\beta}^{fL} + \varepsilon_{\alpha\beta}^{fR} = \varepsilon_{\alpha\beta}^{\eta} \xi^f \quad \text{with} \quad \xi^f = \xi^{fL} + \xi^{fR};$$



- only the direction in the (ξ^u, ξ^d) plane is non-trivial for ν oscillations \Rightarrow define an angle η :

$$\xi^u = \frac{\sqrt{5}}{3}(2 \cos \eta - \sin \eta), \quad \xi^d = \frac{\sqrt{5}}{3}(2 \sin \eta - \cos \eta);$$

- special cases: $\eta = \pm 90^\circ$ (n), $\eta = 0$ (p), $\eta \approx 26.6^\circ$ (u), $\eta \approx 63.4^\circ$ (d).

Non-standard interactions and 3ν oscillations

- Equation of motion: **6** (vac) + **8** (NSI- ν) + **1** (NSI- q) = **15** parameters [2]:

$$i\frac{d\vec{v}}{dt} = H\vec{v}; \quad H = U_{\text{vac}} \cdot D_{\text{vac}} \cdot U_{\text{vac}}^\dagger \pm V_{\text{mat}}; \quad D_{\text{vac}} = \frac{1}{2E_\nu} \mathbf{diag} (0, \Delta m_{21}^2, \Delta m_{31}^2);$$

$$U_{\text{vac}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} e^{i\delta_{\text{CP}}} & 0 \\ -s_{12} e^{-i\delta_{\text{CP}}} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \vec{v} = \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix},$$

$$\mathcal{E}_{\alpha\beta}(x) \equiv \sum_f \frac{N_f(x)}{N_e(x)} \varepsilon_{\alpha\beta}^f = \sqrt{5} \varepsilon_{\alpha\beta}^\eta [\cos \eta + Y_n(x) \sin \eta], \quad Y_n(x) \equiv \frac{N_n(x)}{N_e(x)},$$

$$V_{\text{mat}} \equiv V_{\text{SM}} + V_{\text{NSI}} = \sqrt{2} G_F N_e(x) \begin{pmatrix} 1 + \mathcal{E}_{ee}(x) & \mathcal{E}_{e\mu}(x) & \mathcal{E}_{e\tau}(x) \\ \mathcal{E}_{e\mu}^*(x) & \mathcal{E}_{\mu\mu}(x) & \mathcal{E}_{\mu\tau}(x) \\ \mathcal{E}_{e\tau}^*(x) & \mathcal{E}_{\mu\tau}^*(x) & \mathcal{E}_{\tau\tau}(x) \end{pmatrix};$$

- notice that our definition of U_{vac} differ by the “usual” one by an overall rephasing, $U_{\text{vac}} = \Phi \cdot U \cdot \Phi^*$ with $\Phi \equiv \mathbf{diag} (e^{i\delta_{\text{CP}}}, 1, 1)$, which is irrelevant in the standard case of no-NSI.

[2] I. Esteban *et al.*, JHEP **08** (2018) 180 [arXiv:1805.04530].

The generalized mass ordering degeneracy

- General symmetry: $H \rightarrow -H^*$ does not affect the neutrino probabilities;
- we have $H = H_{\text{vac}} \pm V_{\text{mat}}$. For vacuum, $H_{\text{vac}} \rightarrow -H_{\text{vac}}^*$ occurs if:

$$\begin{cases} \Delta m_{31}^2 \rightarrow -\Delta m_{32}^2, \\ \theta_{12} \rightarrow \pi/2 - \theta_{12}, \\ \delta_{\text{CP}} \rightarrow \pi - \delta_{\text{CP}}, \end{cases}$$
- notice how this transformation links together **mass ordering** and **solar octant** [3, 4, 5];
- for matter, $V_{\text{mat}} \rightarrow -V_{\text{mat}}^*$ requires:

$$\begin{cases} [\mathcal{E}_{ee}(x) - \mathcal{E}_{\mu\mu}(x)] \rightarrow -[\mathcal{E}_{ee}(x) - \mathcal{E}_{\mu\mu}(x)] - 2, \\ [\mathcal{E}_{\tau\tau}(x) - \mathcal{E}_{\mu\mu}(x)] \rightarrow -[\mathcal{E}_{\tau\tau}(x) - \mathcal{E}_{\mu\mu}(x)], \\ \mathcal{E}_{\alpha\beta}(x) \rightarrow -\mathcal{E}_{\alpha\beta}^*(x) \quad (\alpha \neq \beta), \end{cases}$$
- since $V_{\text{mat}} = V_{\text{SM}} + V_{\text{NSI}}$ and V_{SM} is fixed, this symmetry requires NSI;
- in general, $\mathcal{E}_{\alpha\beta}(x)$ varies along trajectory \Rightarrow symmetry only approximate, **unless**:
 - NSI proportional to electric charge ($\eta = 0$), so same matter profile for SM and NSI;
 - neutron/proton ratio $Y_n(x)$ is constant, and same for all the neutrino trajectories.

[3] M.C. Gonzalez-Garcia, M. Maltoni, JHEP **09** (2013) 152 [arXiv:1307.3092]

[4] P. Bakhti, Y. Farzan, JHEP **07** (2014) 064 [arXiv:1403.0744].

[5] P. Coloma, T. Schwetz, Phys. Rev. D **94** (2016) 055005 [arXiv:1604.05772].

Matter potential for solar and KamLAND neutrinos

- One mass dominance ($\Delta m_{31}^2 \rightarrow \infty$) $\Rightarrow P_{ee} = c_{13}^4 P_{\text{eff}} + s_{13}^4$ with the probability P_{eff} determined by an effective 2ν model (as in the SM):

$$i \frac{d\vec{v}}{dt} = [\mathbf{H}_{\text{vac}}^{\text{eff}} + \mathbf{H}_{\text{mat}}^{\text{eff}}] \vec{v}, \quad \vec{v} = \begin{pmatrix} v_e \\ v_a \end{pmatrix}, \quad \mathbf{H}_{\text{vac}}^{\text{eff}} \equiv \frac{\Delta m_{21}^2}{4E_\nu} \begin{pmatrix} -\cos 2\theta_{12} & \sin 2\theta_{12} e^{i\delta_{\text{CP}}} \\ \sin 2\theta_{12} e^{-i\delta_{\text{CP}}} & \cos 2\theta_{12} \end{pmatrix},$$

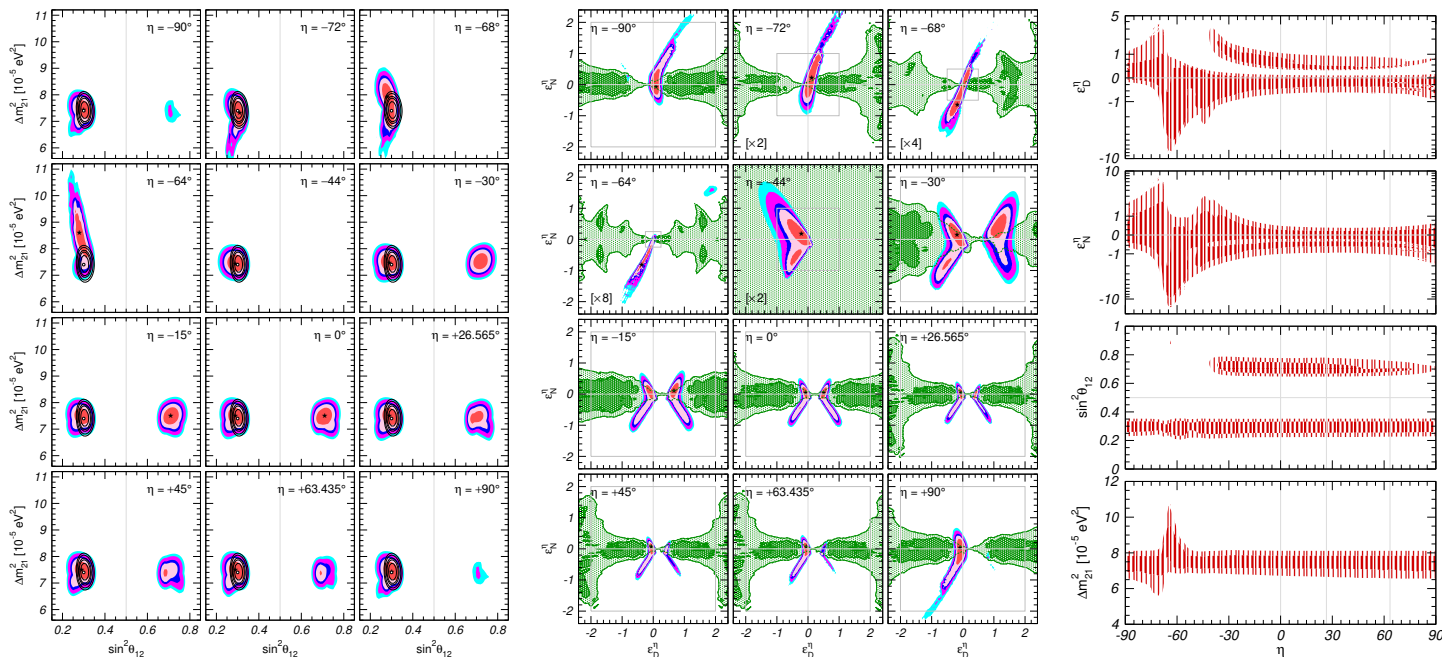
$$\mathbf{H}_{\text{mat}}^{\text{eff}} \equiv \sqrt{2} G_F N_e(r) \left[\begin{pmatrix} c_{13}^2 & 0 \\ 0 & 0 \end{pmatrix} + \sqrt{5} [\cos \eta + Y_n(x) \sin \eta] \begin{pmatrix} -\varepsilon_D^\eta & \varepsilon_N^\eta \\ \varepsilon_N^{\eta*} & \varepsilon_D^\eta \end{pmatrix} \right],$$

$$\begin{cases} \varepsilon_D^\eta = c_{13} s_{13} \text{Re}(s_{23} \varepsilon_{e\mu}^\eta + c_{23} \varepsilon_{e\tau}^\eta) - (1 + s_{13}^2) c_{23} s_{23} \text{Re}(\varepsilon_{\mu\tau}^\eta) \\ \quad - c_{13}^2 (\varepsilon_{ee}^\eta - \varepsilon_{\mu\mu}^\eta) / 2 + (s_{23}^2 - s_{13}^2 c_{23}^2) (\varepsilon_{\tau\tau}^\eta - \varepsilon_{\mu\mu}^\eta) / 2, \\ \varepsilon_N^\eta = c_{13} (c_{23} \varepsilon_{e\mu}^\eta - s_{23} \varepsilon_{e\tau}^\eta) + s_{13} [s_{23}^2 \varepsilon_{\mu\tau}^\eta - c_{23}^2 \varepsilon_{\mu\tau}^{\eta*} + c_{23} s_{23} (\varepsilon_{\tau\tau}^\eta - \varepsilon_{\mu\mu}^\eta)]; \end{cases}$$

- solar data can be perfectly fitted by **NSI only** \Rightarrow solar LMA solution **is unstable** with respect to the introduction of NSI;
- KamLAND **requires** Δm_{21}^2 but only weakly sensitive to NSI \Rightarrow it **determines** Δm_{21}^2 ;
- in the solar core $Y_n(x) \in [1/6, 1/2]$ \Rightarrow approximate cancellation of NSI for $\eta \in [-80^\circ, -63^\circ]$.

Oscillation results for solar and KamLAND neutrinos

- Generalized mass-ordering degeneracy \Rightarrow new LMA-D solution with $\theta_{12} > 45^\circ$ [6];
- $\eta = 0 \Rightarrow$ NSI terms proportional to $N_p(x) \equiv N_e(x) \Rightarrow$ the degeneracy becomes exact.



[6] O.G. Miranda, M.A. Tortola, J.W.F. Valle, JHEP 10 (2006) 008 [hep-ph/0406280].

Matter potential for atmospheric and long-baseline neutrinos

- In Earth matter: $Y_n(x) \rightarrow Y_n^\oplus \approx 1.051 \Rightarrow \mathcal{E}_{\alpha\beta}(x) \rightarrow \varepsilon_{\alpha\beta}^\oplus$ becomes an effective parameter:

$$\varepsilon_{\alpha\beta}^\oplus \equiv \sqrt{5} [\cos \eta + Y_n^\oplus \sin \eta] \varepsilon_{\alpha\beta}^\eta,$$

- the bounds on $\varepsilon_{\alpha\beta}^\oplus$ are independent of the quark couplings (*i.e.*, of η);
- for $\eta = \arctan(-1/Y_n^\oplus) \approx -43.6^\circ$ ATM+LBL data imply **no** bound on $\varepsilon_{\alpha\beta}^\eta$;
- the NSI parameter space is too big to be properly studied \Rightarrow simplification needed;
- bounds on $\varepsilon_{\alpha\beta}^\oplus$ are weakest when $V_{\text{mat}} \propto \delta_{e\alpha}\delta_{e\beta} + \varepsilon_{\alpha\beta}^\oplus$ has two degenerate eigenvalues [7] \Rightarrow focus on such case \Rightarrow introduce parameters $(\varepsilon_\oplus, \varphi_{12}, \varphi_{13}, \alpha_1, \alpha_2)$ and define:

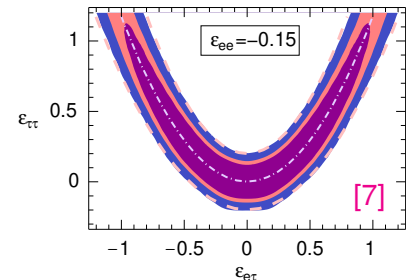
$$\varepsilon_{ee}^\oplus - \varepsilon_{\mu\mu}^\oplus = \varepsilon_\oplus (\cos^2 \varphi_{12} - \sin^2 \varphi_{12}) \cos^2 \varphi_{13} - 1,$$

$$\varepsilon_{\tau\tau}^\oplus - \varepsilon_{\mu\mu}^\oplus = \varepsilon_\oplus (\sin^2 \varphi_{13} - \sin^2 \varphi_{12} \cos^2 \varphi_{13}),$$

$$\varepsilon_{e\mu}^\oplus = -\varepsilon_\oplus \cos \varphi_{12} \sin \varphi_{12} \cos^2 \varphi_{13} e^{i(\alpha_1 - \alpha_2)},$$

$$\varepsilon_{e\tau}^\oplus = -\varepsilon_\oplus \cos \varphi_{12} \cos \varphi_{13} \sin \varphi_{13} e^{i(2\alpha_1 + \alpha_2)},$$

$$\varepsilon_{\mu\tau}^\oplus = \varepsilon_\oplus \sin \varphi_{12} \cos \varphi_{13} \sin \varphi_{13} e^{i(\alpha_1 + 2\alpha_2)}.$$

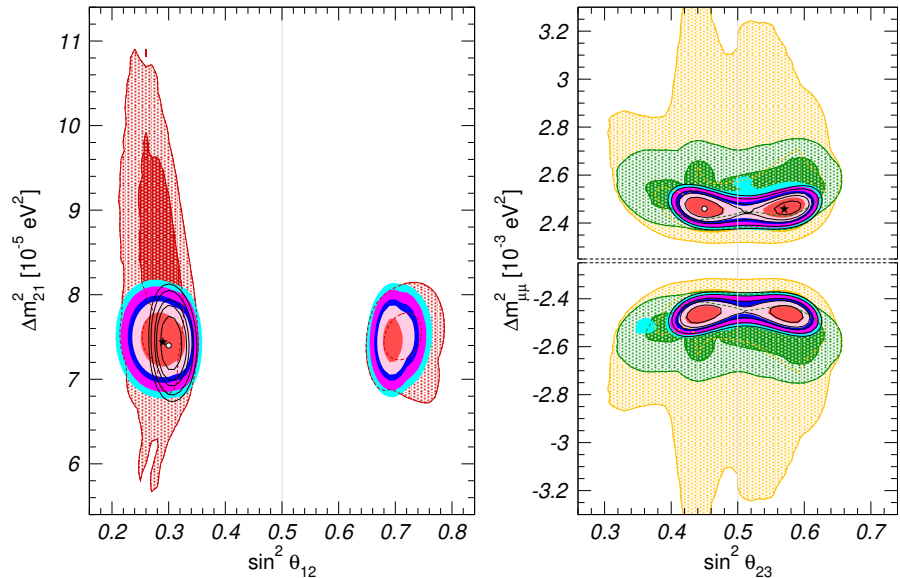


- for definiteness we also assume on CP conservation and set $\delta_{\text{CP}} = \alpha_1 = \alpha_2 = 0$.

[7] A. Friedland, C. Lunardini, M. Maltoni, Phys. Rev. D **70** (2004) 111301 [hep-ph/0408264].

Impact of NSI on the oscillation parameters

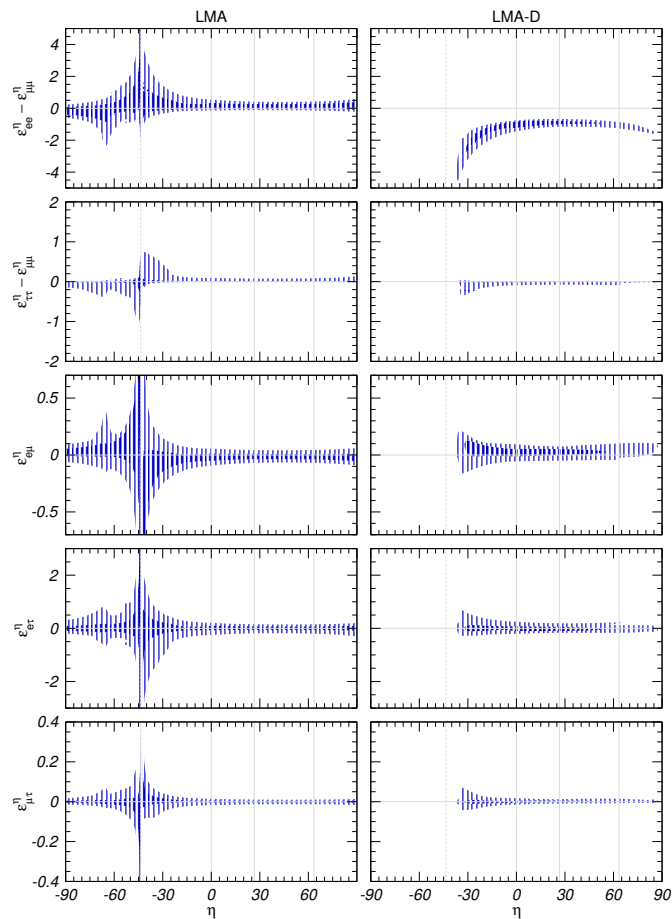
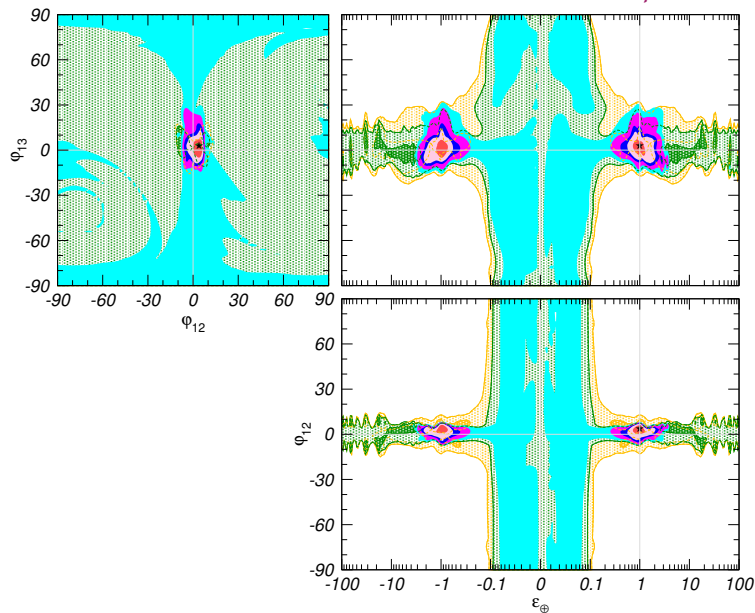
- Once marginalized over η , analysis of **solar + KamLAND** data shows strong deterioration of the precision on Δm_{21}^2 and θ_{12} , as well as the appearance of the LMA-D solution [6];
- a similar worsening appears in **ATM + LBL-dis + LBL-app + IceCUBE + MBL-rea** analysis;
- synergies between **solar** and **atmospheric** sectors allow to recover the SM accuracy on most parameters (except θ_{12});
- notice that the LMA-D solution persists also in the global fit;
- high-energy atmos. **IceCUBE** data have no sensitivity to oscillations ($P_{\mu\mu} \propto 1/E^2$), hence they contribute little.



[6] O.G. Miranda, M.A. Tortola, J.W.F. Valle, JHEP **10** (2006) 008 [hep-ph/0406280].

Determination of NSI parameters

- Reduced (ϵ_{\oplus} , φ_{12} , φ_{13}) parameter space can be constrained by joint solar+KamLAND and ATM+LBL analysis;
- bounds can then be recast in term of $\epsilon_{\alpha\beta}^{\eta}$.



The COHERENT experiment

- Observation of coherent neutrino-nucleus scattering [8] allows to put bounds on NSI through the effective charges ($Y_n^{\text{coh}} \approx 1.407$):

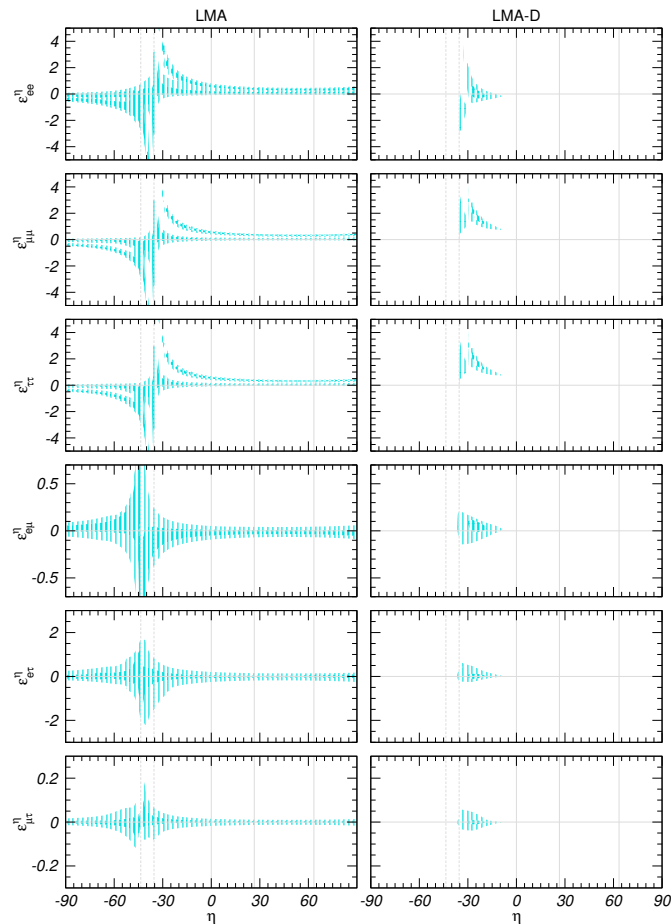
$$Q_\alpha^2 \propto \left[(g_p^V + Y_n^{\text{coh}} g_n^V) + \epsilon_{\alpha\alpha}^{\text{coh}} \right]^2 + \sum_{\beta \neq \alpha} (\epsilon_{\alpha\beta}^{\text{coh}})^2$$

$$\text{with } \epsilon_{\alpha\beta}^{\text{coh}} = \sqrt{5} \left[\cos \eta + Y_n^{\text{coh}} \sin \eta \right] \epsilon_{\alpha\beta}^\eta;$$

- for $\eta = \arctan(-1/Y_n^{\text{coh}}) \approx -35.4^\circ$ no bound on $\epsilon_{\alpha\beta}^\eta$ is implied;
- separate bounds on diagonal $\epsilon_{\alpha\alpha}^\eta$ couplings can be placed.

[8] D. Akimov *et al.* [COHERENT], *Science* **357** (2017) 1123 [arXiv:1708.01294]

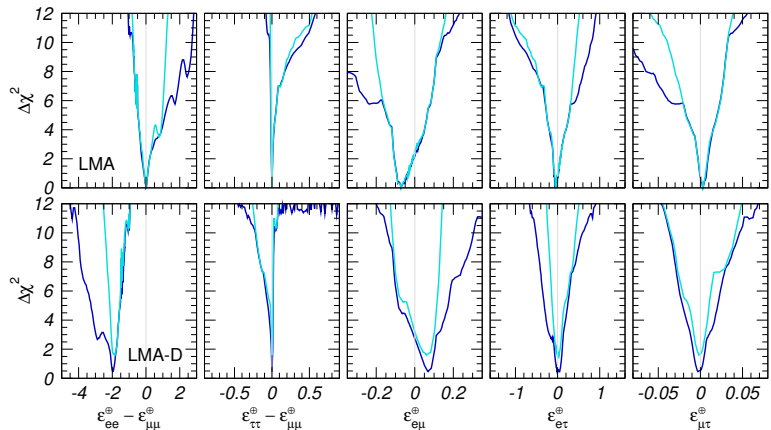
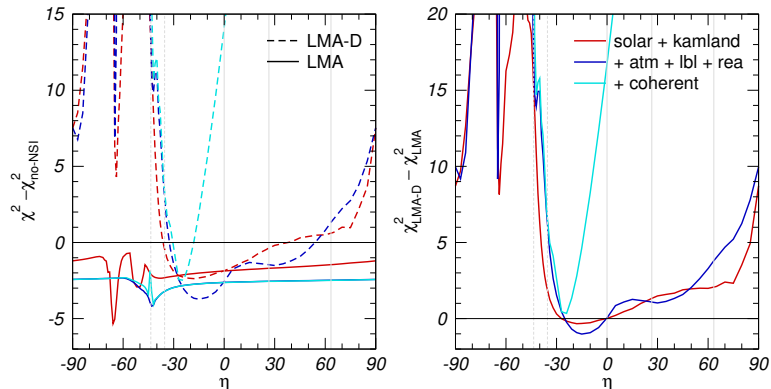
[9] P. Coloma, I. Esteban *et al.*, *JHEP* **02** (2020) 023 [arXiv:1911.09109].



General NSI bounds

- Inclusion of COHERENT data rules out LMA-D for NSI with u , d , or p , but **not** in the general case;
- our general 2σ bounds [9]:

OSCILLATIONS			+ COHERENT (t+E Duke)	
	LMA	LMA \oplus LMA-D	LMA = LMA \oplus LMA-D	
$\epsilon_{ee}^u - \epsilon_{\mu\mu}^u$	[-0.072, +0.321]	\oplus [-1.042, -0.743]	ϵ_{ee}^u	[-0.031, +0.476]
$\epsilon_{\tau\tau}^u - \epsilon_{\mu\mu}^u$	[-0.001, +0.018]	[-0.016, +0.018]	$\epsilon_{\mu\mu}^u$	[-0.029, +0.068] \oplus [+0.309, +0.415]
$\epsilon_{e\mu}^u$	[-0.050, +0.020]	[-0.050, +0.059]	$\epsilon_{\tau\tau}^u$	[-0.029, +0.068] \oplus [+0.309, +0.414]
$\epsilon_{e\tau}^u$	[-0.077, +0.098]	[-0.111, +0.098]	$\epsilon_{e\mu}^u$	[-0.048, +0.020]
$\epsilon_{\mu\tau}^u$	[-0.006, +0.007]	[-0.006, +0.007]	$\epsilon_{e\tau}^u$	[-0.077, +0.095]
			$\epsilon_{\mu\tau}^u$	[-0.006, +0.007]
$\epsilon_{ee}^d - \epsilon_{\mu\mu}^d$	[-0.084, +0.326]	\oplus [-1.081, -1.026]	ϵ_{ee}^d	[-0.034, +0.426]
$\epsilon_{\tau\tau}^d - \epsilon_{\mu\mu}^d$	[-0.001, +0.018]	[-0.001, +0.018]	$\epsilon_{\mu\mu}^d$	[-0.027, +0.063] \oplus [+0.275, +0.371]
$\epsilon_{e\mu}^d$	[-0.051, +0.020]	[-0.051, +0.038]	$\epsilon_{\tau\tau}^d$	[-0.027, +0.067] \oplus [+0.274, +0.372]
$\epsilon_{e\tau}^d$	[-0.077, +0.098]	[-0.077, -0.098]	$\epsilon_{e\mu}^d$	[-0.050, +0.020]
$\epsilon_{\mu\tau}^d$	[-0.006, +0.007]	[-0.006, +0.007]	$\epsilon_{e\tau}^d$	[-0.076, +0.097]
			$\epsilon_{\mu\tau}^d$	[-0.006, +0.007]
$\epsilon_{ee}^p - \epsilon_{\mu\mu}^p$	[-0.190, +0.927]	\oplus [-2.927, -1.814]	ϵ_{ee}^p	[-0.086, +0.884] \oplus [+1.083, +1.605]
$\epsilon_{\tau\tau}^p - \epsilon_{\mu\mu}^p$	[-0.001, +0.053]	[-0.052, +0.053]	$\epsilon_{\mu\mu}^p$	[-0.097, +0.220] \oplus [+1.063, +1.410]
$\epsilon_{e\mu}^p$	[-0.145, +0.058]	[-0.145, +0.145]	$\epsilon_{\tau\tau}^p$	[-0.098, +0.221] \oplus [+1.063, +1.408]
$\epsilon_{e\tau}^p$	[-0.238, +0.292]	[-0.292, +0.292]	$\epsilon_{e\mu}^p$	[-0.124, +0.058]
$\epsilon_{\mu\tau}^p$	[-0.019, +0.021]	[-0.021, +0.021]	$\epsilon_{e\tau}^p$	[-0.239, +0.244]
			$\epsilon_{\mu\tau}^p$	[-0.013, +0.021]

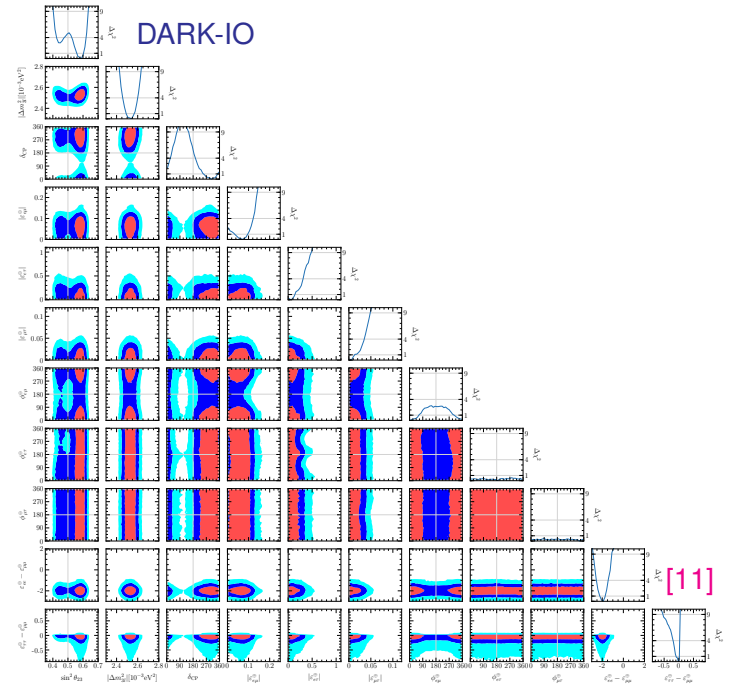
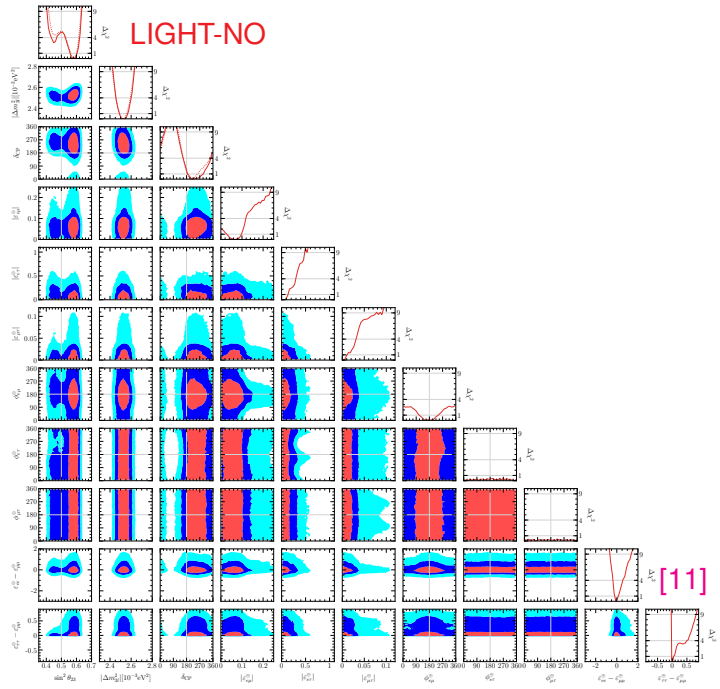


- Argon data add further $\Delta\chi^2 \sim 4$ [10].

[9] P. Coloma, I. Esteban, M.C. Gonzalez-Garcia, M. Maltoni, JHEP **02** (2020) 023 [arXiv:1911.09109].
 [10] M. Chaves and T. Schwetz, JHEP **05** (2021), 042 [arXiv:2102.11981].

CP violation in the presence of NSI

- NSI introduce three additional phases $\phi_{\alpha\beta}^\oplus$, associated to the non-diagonal elements $\varepsilon_{\alpha\beta}^\oplus$.



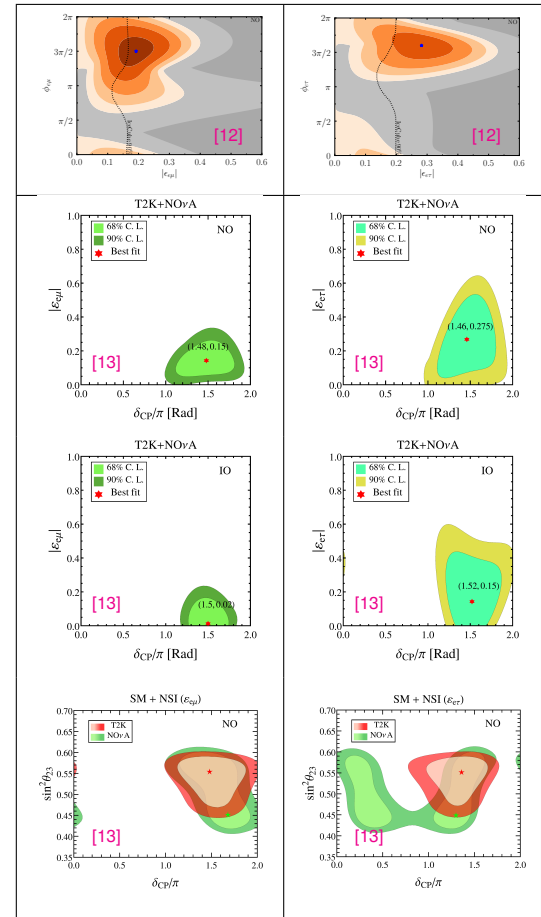
[11] I. Esteban *et al.*, JHEP 06 (2019) 055 [arXiv:1905.05203].

Impact of NSI on T2K and NOvA

- It has been noted [12, 13] that tension between T2K and NOvA in the determination of δ_{CP} for Normal Ordering can be alleviated by NSI;
- both papers suggest two alternative mechanisms: $|\epsilon_{e\mu}^\oplus| \sim 0.15$ and $|\epsilon_{e\tau}^\oplus| \sim 0.3$, yielding similar improvements ($\Delta\chi_{e\mu}^2 \sim 4.5$ and $\Delta\chi_{e\tau}^2 \sim 3.7$) w.r.t. SM for NO;
- no significant NSI contribution is found for IO;
- both mechanisms favor maximal CP violation ($\delta_{CP} \sim 270^\circ$) in the presence of NSI;
- by alleviating the T2K–NOvA tension, the worsening of NO w.r.t. IO does **not** take place.

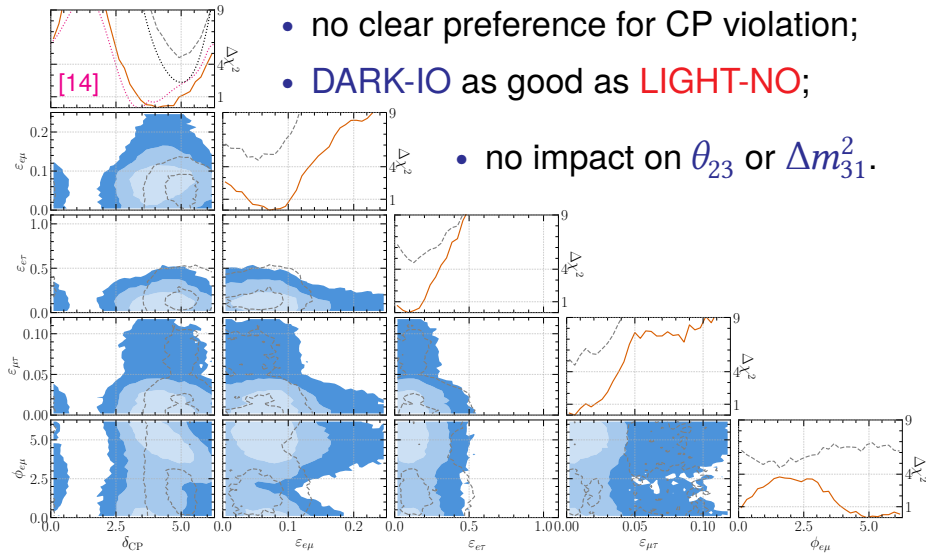
[12] P.B. Denton, J. Gehrlein, R. Pestes, Phys. Rev. Lett. **126** (2021) 051801 [arXiv:2008.01110].

[13] S.S. Chatterjee, A. Palazzo, Phys. Rev. Lett. **126** (2021) 051802 [arXiv:2008.04161].

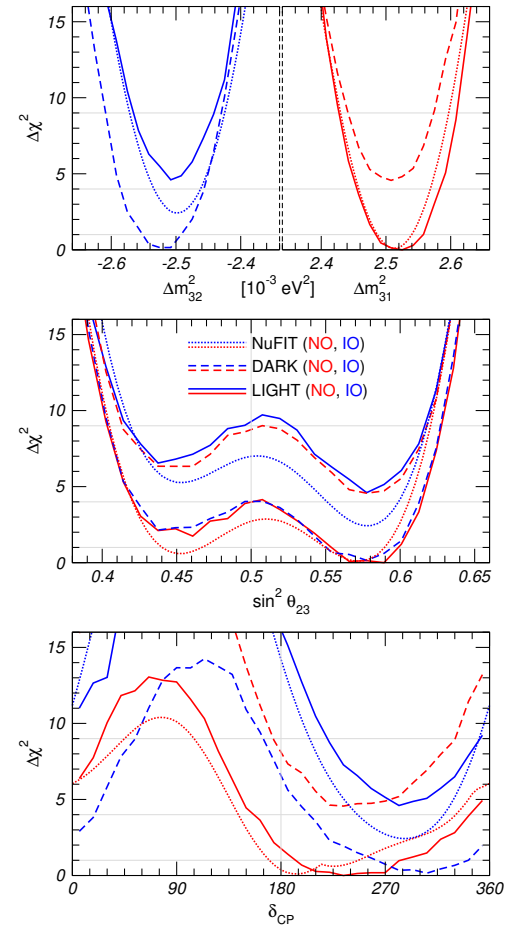


Impact of NSI on oscillation parameters

- Global fits of **all** neutrino data indicate that:
 - $\epsilon_{e\mu}^\oplus$ mechanism OK, but with smaller $|\epsilon_{e\mu}^\oplus| \simeq 0.08$;
 - $\epsilon_{e\tau}^\oplus$ mechanism severely constrained;
- preference of **NO** over **IO** increases by $\Delta\chi^2 \sim 2.3$;



- no clear preference for CP violation;
- **DARK-IO** as good as **LIGHT-NO**;
- no impact on θ_{23} or Δm_{31}^2 .



[14] I. Esteban, private communication & arXiv:2004.04745.

Non-standard interactions with electrons: formalism

- Let's focus here on solar neutrinos. In the presence of NC-like NSI with e , elastic scattering is modified \Rightarrow detection process (e.g., in SK, SNO, Borexino) is affected;

- in the SM, ν interactions (both CC and NC) are diagonal in the flavor basis. Hence:

$$N_{\text{ev}} \propto \sum_{\beta} P_{e\beta} \sigma_{\beta}^{\text{SM}} \quad \text{with} \quad P_{e\beta} \equiv |S_{\beta e}|^2 \quad (\nu_e \rightarrow \nu_{\beta} \text{ transition probabilities})$$

- this expression is only valid in the flavor basis. Unitary rotation $U \Rightarrow$ arbitrary basis:

$$S_{\beta e} = \sum_i U_{\beta i} S_{ie} \Rightarrow P_{e\beta} = \sum_{ij} U_{\beta i} \rho_{ij}^{(e)} U_{j\beta}^{\dagger} \quad \text{with} \quad \rho_{ij}^{(e)} \equiv S_{ie} S_{ej}^{\dagger} = \left[S \Pi^{(e)} S^{\dagger} \right]_{ij}$$

- where $\rho^{(e)}$ is the ν density matrix at the detector (for a ν_e at the source). Substituting:

$$N_{\text{ev}} \propto \sum_{ij} \rho_{ij}^{(e)} \sum_{\beta} U_{j\beta}^{\dagger} \sigma_{\beta}^{\text{SM}} U_{\beta i} = \boxed{\text{Tr} \left[\rho^{(e)} \sigma^{\text{SM}} \right]} \quad \text{with} \quad \sigma_{ji}^{\text{SM}} \equiv \left[U^{\dagger} \mathbf{diag} \{ \sigma_{\beta}^{\text{SM}} \} U \right]_{ji};$$

- here σ^{SM} is a matrix in flavor space, containing enough information to describe the ES interaction of *any* neutrino state without the need to explicitly project it onto the interaction eigenstates: such projection is now implicitly encoded into σ^{SM} .

Neutrino-electron cross-section in the presence of NSI

- In the presence of flavor-changing NSI, the SM flavor basis no longer coincides with the interaction eigenstates. Hence, the general formula $N_{\text{ev}} \propto \text{Tr} [\rho^{(e)} \sigma^{\text{NSI}}]$ must be used;

- the cross-section matrix σ^{NSI} is the integral over T_e of the following expression:

$$\frac{d\sigma^{\text{NSI}}}{dT_e}(E_\nu, T_e) = \frac{2G_F^2 m_e}{\pi} \left\{ \mathbf{C}_L^2 \left[1 + \frac{\alpha}{\pi} f_-(y) \right] + \mathbf{C}_R^2 (1-y)^2 \left[1 + \frac{\alpha}{\pi} f_+(y) \right] - \{ \mathbf{C}_L, \mathbf{C}_R \} \frac{m_e y}{2E_\nu} \left[1 + \frac{\alpha}{\pi} f_\pm(y) \right] \right\}$$

- where f_+ , f_- , f_\pm are loop functions, $y \equiv T_e/E_\nu$, and \mathbf{C}_L , \mathbf{C}_R are 3×3 hermitian matrices:

$$\begin{cases} \mathbf{C}_{\alpha\beta}^L \equiv \mathbf{c}_{L\beta} \delta_{\alpha\beta} + \varepsilon_{\alpha\beta}^{Le} \\ \mathbf{C}_{\alpha\beta}^R \equiv \mathbf{c}_{R\beta} \delta_{\alpha\beta} + \varepsilon_{\alpha\beta}^{Re} \end{cases} \quad \text{with} \quad \begin{cases} \mathbf{c}_{L\tau} = \mathbf{c}_{L\mu} = g_L^l \quad \text{and} \quad \mathbf{c}_{Le} = g_L^l + 1, \\ \mathbf{c}_{R\tau} = \mathbf{c}_{R\mu} = \mathbf{c}_{Re} = g_R^l \quad (\text{at tree level}); \end{cases}$$

- when the NSI terms $\varepsilon_{\alpha\beta}^{Le}$ and $\varepsilon_{\alpha\beta}^{Re}$ are set to zero, the matrix $d\sigma^{\text{NSI}}/dT_e$ becomes diagonal and the SM expressions are recovered;
- the cross section for antineutrinos can be obtained by interchanging $\mathbf{C}_L \leftrightarrow \mathbf{C}_R^*$;
- NSI effects on neutrino [propagation](#) are the same as in the previous section (for $\eta = 0$) and are accounted by the density matrix $\rho^{(e)}$.

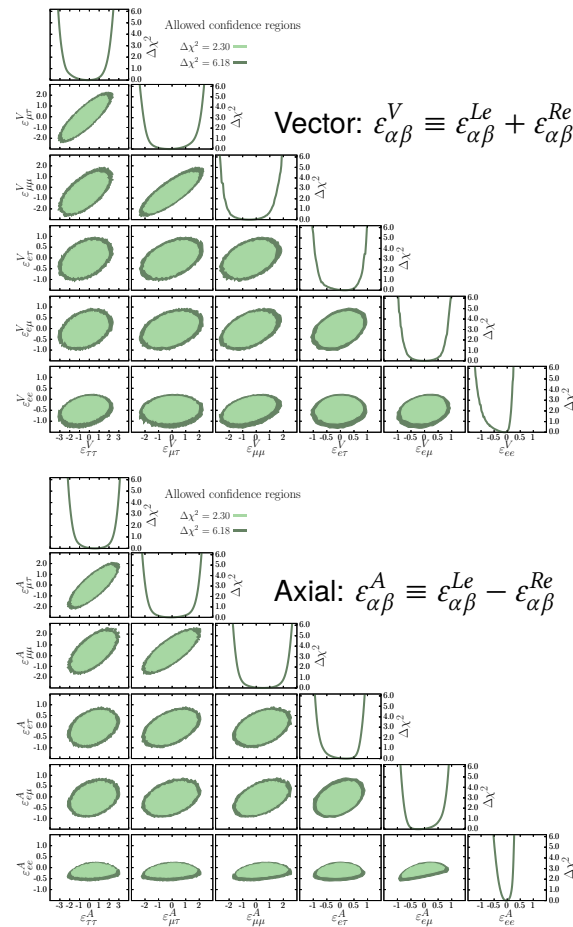
Bounds on NSI- e from Borexino II

- Ref. [15]: analysis of NSI- e with Borexino. Caveats:
 - only diagonal NSI considered;
 - only 1 or 2 NSI parameters varied at-a-time;
- in [16] we studied the general case. We found:
 - degeneracies strongly weakens the bounds;
 - yet a definite $\mathcal{O}(1)$ bound is always found.

	Allowed regions at 90% CL ($\Delta\chi^2 = 2.71$)			
	Vector		Axial Vector	
	1 Parameter	Marginalized	1 Parameter	Marginalized
ε_{ee}	$[-0.09, +0.14]$	$[-1.05, +0.17]$	$[-0.05, +0.10]$	$[-0.38, +0.24]$
$\varepsilon_{\mu\mu}$	$[-0.51, +0.35]$	$[-2.38, +1.54]$	$[-0.29, +0.19] \oplus [+0.68, +1.45]$	$[-1.47, +2.37]$
$\varepsilon_{\tau\tau}$	$[-0.66, +0.52]$	$[-2.85, +2.04]$	$[-0.40, +0.36] \oplus [+0.69, +1.44]$	$[-1.82, +2.81]$
$\varepsilon_{e\mu}$	$[-0.34, +0.61]$	$[-0.83, +0.84]$	$[-0.30, +0.43]$	$[-0.79, +0.76]$
$\varepsilon_{e\tau}$	$[-0.48, +0.47]$	$[-0.90, +0.85]$	$[-0.40, +0.38]$	$[-0.81, +0.78]$
$\varepsilon_{\mu\tau}$	$[-0.25, +0.36]$	$[-2.07, +2.06]$	$[-1.10, -0.75] \oplus [-0.13, +0.22]$	$[-1.95, +1.91]$

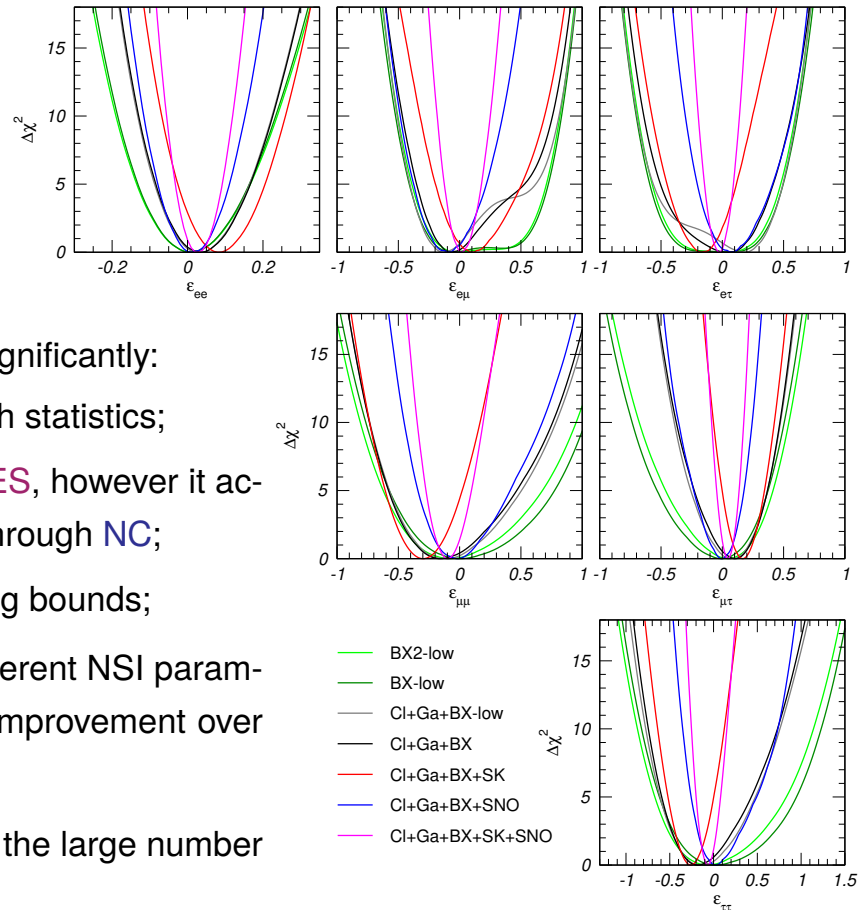
[15] Borexino coll., JHEP 02 (2020) 038 [arXiv:1905.03512]

[16] Coloma *et al.*, JHEP 07 (2022) 138 [arXiv:2204.03011]



NSI- e from all solar data

- Caveat: in this slide we vary only 1 NSI parameter at-a-time;
- other low-E data such as **BX1** and **Cl+Ga** have little impact;
- however, **SK** and **SNO** contribute significantly:
 - **SK** measures **ES** events with high statistics;
 - **SNO** is only weakly sensitive to **ES**, however it accurately determines the ^8B flux through **NC**;
 - **SK+SNO** combination yield strong bounds;
- of course, degeneracies among different NSI parameters will weaken the bounds, but improvement over **BX2**-only data still expected;
- global analysis is tough because of the large number of parameters, but not impossible...

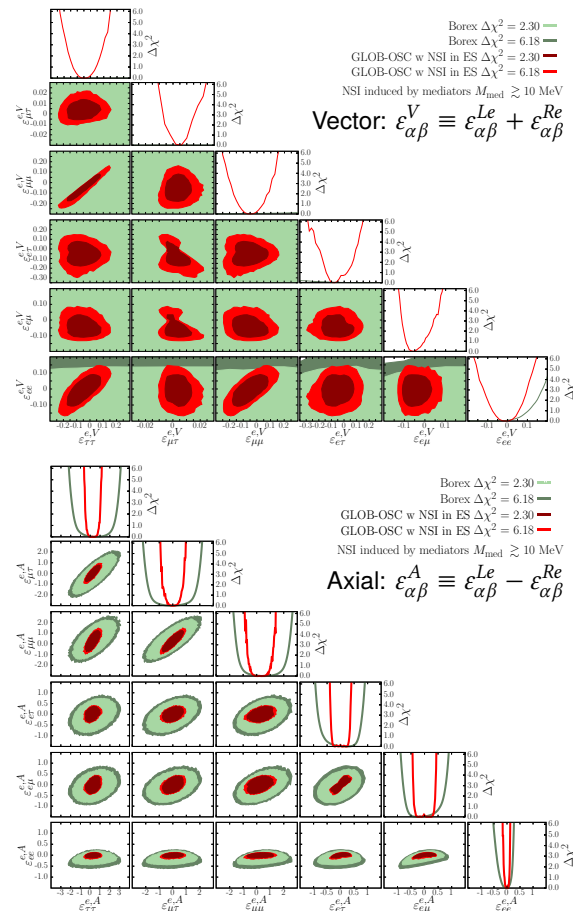


Bounds on NSI- e from global data

- In [17] we performed a global analysis of all solar data, varying all parameters simultaneously;
- indeed, the bounds from Borexino alone are greatly enhanced, both for vector and axial couplings;
- the limits are dominated by NSI contributions to the ES cross-section, which allow to derive separate bounds on diagonal $\epsilon_{\alpha\alpha}^{e,V}$ and $\epsilon_{\alpha\alpha}^{e,A}$ couplings.

	Allowed ranges at 90% CL (marginalized)			
	Vector ($X = V$)		Axial-vector ($X = A$)	
	Borexino	GLOB-OSC w NSI in ES	Borexino	GLOB-OSC w NSI in ES
$\epsilon_{ee}^{e,X}$	$[-1.1, +0.17]$	$[-0.13, +0.10]$	$[-0.38, +0.24]$	$[-0.13, +0.11]$
$\epsilon_{\mu\mu}^{e,X}$	$[-2.4, +1.5]$	$[-0.20, +0.10]$	$[-1.5, +2.4]$	$[-0.70, +1.2]$
$\epsilon_{\tau\tau}^{e,X}$	$[-2.8, +2.1]$	$[-0.17, +0.093]$	$[-1.8, +2.8]$	$[-0.53, +1.0]$
$\epsilon_{e\mu}^{e,X}$	$[-0.83, +0.84]$	$[-0.097, +0.011]$	$[-0.79, +0.76]$	$[-0.41, +0.40]$
$\epsilon_{e\tau}^{e,X}$	$[-0.90, +0.85]$	$[-0.18, +0.080]$	$[-0.81, +0.78]$	$[-0.36, +0.36]$
$\epsilon_{\mu\tau}^{e,X}$	$[-2.1, +2.1]$	$[-0.0063, +0.016]$	$[-1.9, +1.9]$	$[-0.79, +0.81]$

[17] Coloma *et al.*, JHEP 08 (2023) 032 [arXiv:2305.07698]



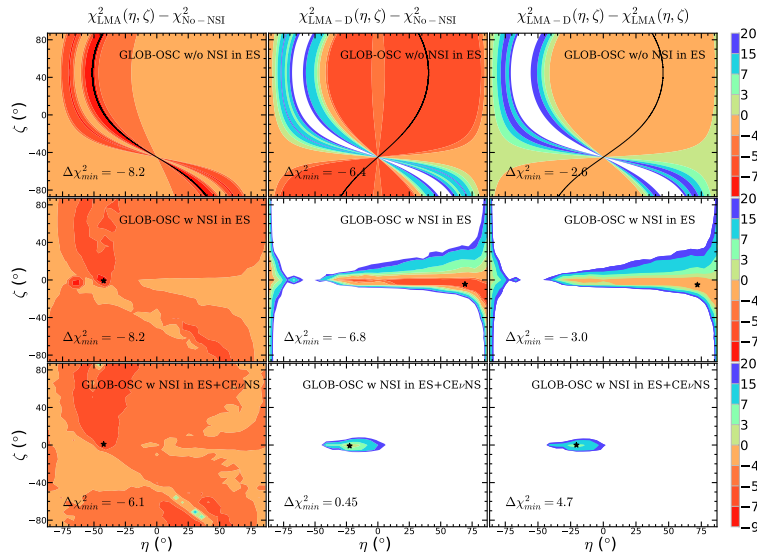
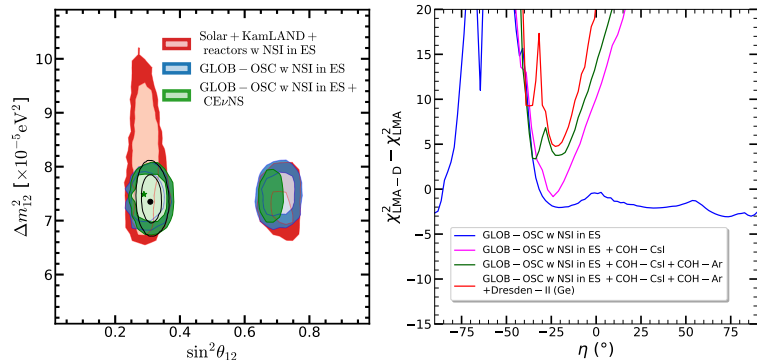
Bounds on generic NSI

- Choose *two* angles (η, ζ) and define:

$$\varepsilon_{\alpha\beta}^{fP} \equiv \varepsilon_{\alpha\beta}^{\eta} \xi^f \chi^P, \quad \begin{cases} \xi^e = \sqrt{5} \cos \eta \sin \zeta, \\ \xi^p = \sqrt{5} \cos \eta \cos \zeta, \\ \xi^n = \sqrt{5} \sin \eta; \end{cases}$$

- direction of $(\xi^e, \xi^u, \xi^d) \leftrightarrow$ half-sphere.

Allowed ranges at 90% CL		99% CL marginalized	
GLOB-OSC w/o NSI in ES		GLOB-OSC w NSI in ES + CE ν NS	
$\varepsilon_{ee}^{\oplus} - \varepsilon_{\mu\mu}^{\oplus}$	$[-3.1, -2.8] \oplus [-2.1, -1.88] \oplus [-0.15, +0.17]$ $[-4.8, -1.6] \oplus [-0.40, +2.6]$	$\varepsilon_{ee}^{\oplus}$	$[-0.19, +0.20] \oplus [+0.95, +1.3]$ $[-0.23, +0.25] \oplus [+0.81, +1.3]$
$\varepsilon_{\tau\tau}^{\oplus} - \varepsilon_{\mu\mu}^{\oplus}$	$[-0.0215, +0.0122]$ $[-0.075, +0.080]$	$\varepsilon_{\mu\mu}^{\oplus}$	$[-0.43, +0.14] \oplus [+0.91, +1.3]$ $[-0.29, +0.20] \oplus [+0.83, +1.4]$
$\varepsilon_{\mu\mu}^{\oplus}$	$[-0.11, -0.021] \oplus [+0.045, +0.135]$ $[-0.32, +0.40]$	$\varepsilon_{\mu\mu}^{\oplus}$	$[-0.12, +0.011]$ $[-0.18, +0.08]$
$\varepsilon_{\mu\tau}^{\oplus}$	$[-0.22, +0.088]$ $[-0.49, +0.45]$	$\varepsilon_{\mu\tau}^{\oplus}$	$[-0.16, +0.083]$ $[-0.25, +0.33]$
$\varepsilon_{\mu\tau}^{\oplus}$	$[-0.0063, +0.013]$ $[-0.043, +0.039]$	$\varepsilon_{\mu\tau}^{\oplus}$	$[-0.0047, +0.012]$ $[-0.020, +0.021]$



[17] Coloma *et al.*, JHEP [arXiv:2305.07698]

Neutrino oscillations in the presence of extra mass states

- Equation of motion: same as usual, but only in the mass basis (identified by suffix “mb”):

$$i \frac{d\vec{v}_{\text{mb}}}{dt} = \mathbf{H}_{\text{mb}} \vec{v}_{\text{mb}}; \quad \mathbf{H}_{\text{mb}} = \mathbf{D}_{\text{vac}} \pm \mathbf{U}_{\text{vac}}^\dagger \cdot \mathbf{V}_{\text{mat}} \cdot \mathbf{U}_{\text{vac}};$$

$$\mathbf{U}_{\text{vac}} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} & \dots \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} & \dots \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} & \dots \end{pmatrix}, \quad \vec{v}_{\text{mb}} = (v_1, v_2, v_3, v_4, \dots)^T;$$

$$\mathbf{D}_{\text{vac}} = \frac{1}{2E_\nu} \mathbf{diag}(0, \Delta m_{21}^2, \Delta m_{31}^2, \Delta m_{41}^2, \dots), \quad \mathbf{V}_{\text{mat}} = \sqrt{2} G_F \left[N_e \mathbf{diag}(1, 0, 0) - \frac{N_n}{2} \mathbf{I}_3 \right];$$

- notice that \mathbf{U}_{vac} is a rectangular $3 \times N$ matrix, fulfilling unitarity relation $\mathbf{U}_{\text{vac}} \cdot \mathbf{U}_{\text{vac}}^\dagger = \mathbf{I}_3$;
- formally, we can extend \mathbf{U}_{vac} to a full $N \times N$ unitary matrix \mathbf{U} by considering $N - 3$ “flavor” states $\{v_{s_1}, \dots, v_{s_{N-3}}\}$. In this case \mathbf{V}_{mat} is extended with null diagonal entries, and:

$$\mathbf{U} = \begin{pmatrix} & & \mathbf{U}_{\text{vac}} & & \\ U_{s_11} & U_{s_12} & U_{s_13} & U_{s_14} & \dots \\ \dots & \dots & \dots & \dots & \dots \end{pmatrix}, \quad \vec{v} = (v_e, v_\mu, v_\tau, v_{s_1}, \dots)^T;$$

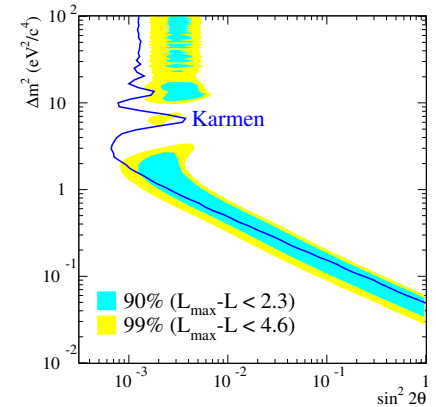
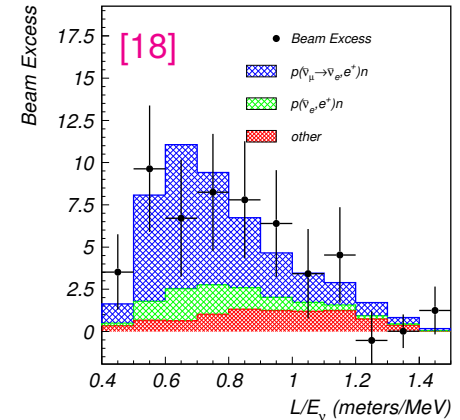
- but notice that v_{s_i} states are defined arbitrarily, hence mixing among them is unphysical.

A long time ago... the LSND anomaly

- Back in the 90's, the **LSND** experiment observed an excess of $\bar{\nu}_e$ events in a $\bar{\nu}_\mu$ beam ($E_\nu \sim 30$ MeV, $L \simeq 35$ m) [18];
- the **Karmen** collaboration did not confirm the claim, but couldn't fully exclude it either [19];
- the signal is compatible with $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillations provided that $\Delta m^2 \gtrsim 0.1$ eV²;
- on the other hand, global neutrino data give (at 3σ):

$$\Delta m_{\text{SOL}}^2 \simeq [6.8 \rightarrow 8.0] \times 10^{-5} \text{ eV}^2,$$

$$|\Delta m_{\text{ATM}}^2| \simeq [2.4 \rightarrow 2.6] \times 10^{-3} \text{ eV}^2;$$
- hence, to explain LSND with mass-induced ν oscillations one needs **new** neutrino mass eigenstates;
- **MiniBooNE**: much larger E_ν and L but similar L/E_ν .

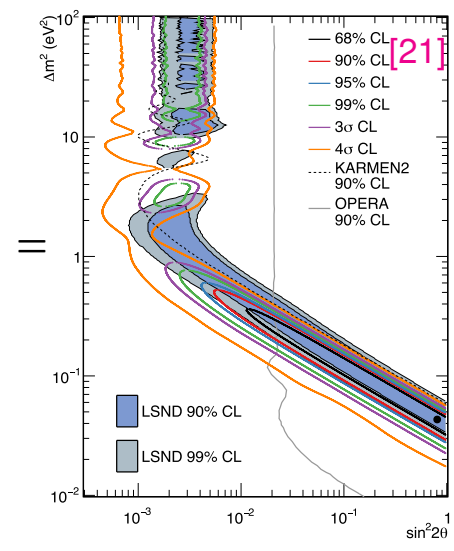
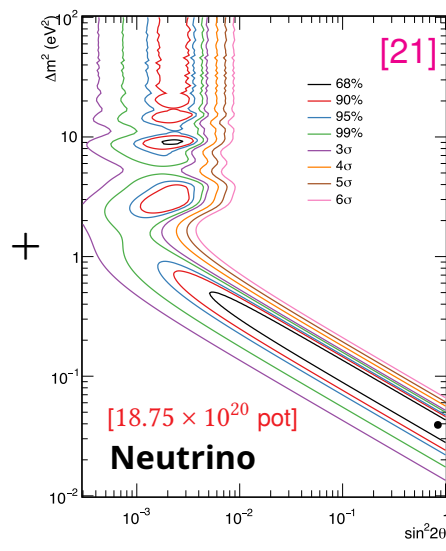
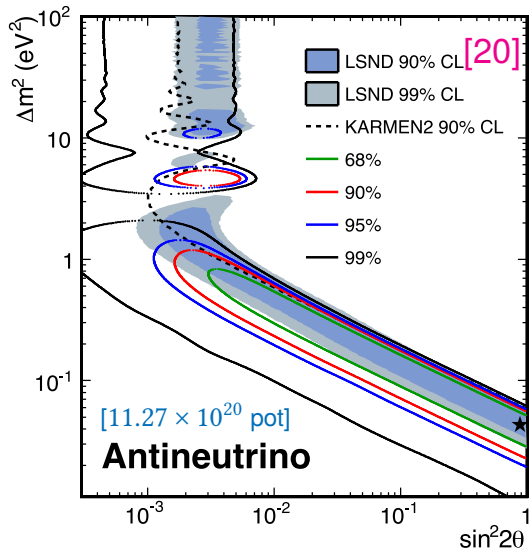


[18] A. Aguilar-Arevalo *et al.* [LSND collab], Phys. Rev. D **64** (2001) 112007 [hep-ex/0104049]

[19] B. Armbruster *et al.* [KARMEN collab], Phys. Rev. D **65** (2002) 112001 [hep-ex/0203021]

The MiniBooNE experiment

- MiniBooNE searched for $\bar{\nu}_e \rightarrow \bar{\nu}_\mu$ conversion ($E = 200 \rightarrow 1250$ MeV, $L \simeq 541$ m);
- excess in both $\bar{\nu}$ and $\nu \Rightarrow$ oscillations compatible with LSND ($ev = 4.8\sigma$, $gof = 12.3\%$);
- however, the low energy part of the excess **cannot** be accounted just by oscillations...

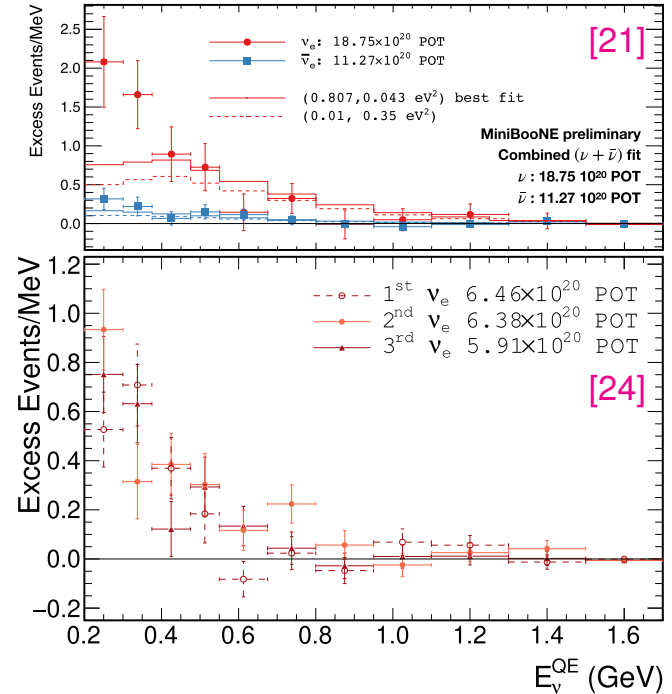


[20] A.A. Aguilar-Arevalo *et al.* [MiniBooNE collab], PRL **110** (2013) 161801 [[arXiv:1303.2588](https://arxiv.org/abs/1303.2588)]

[21] A. Hourlier, talk at Neutrino 2020, Fermilab (online), USA, 22/6-2/7/2020

MiniBooNE low-energy excess

- Excess present from the very beginning;
- 2007 (ν): **low-E** excess too steep for oscillation fit ($P_{\text{osc}} \approx 1\%$) \Rightarrow set $E \geq 475$ MeV \Rightarrow no signal left \Rightarrow **reject** LSND [22];
- 2013 ($\bar{\nu}$): **low-E** not so steep + **mid-E** excess observed \Rightarrow good oscillation fit ($P_{\text{osc}} \approx 66\%$) \Rightarrow **confirm** LSND [20];
- 2018 (ν): **low-E** softened + **mid-E** excess seen also in $\nu \Rightarrow$ mild oscillation fit ($P_{\text{osc}} \approx 15\%$) [23];
- 2020 (ν): more data released [24], oscillations confirmed but **low-E** excess definitely there.



[21] A. Hourlier, talk at Neutrino 2020, Fermilab (online), USA, 22/6-2/7/2020

[22] A.A. Aguilar-Arevalo *et al.* [MiniBooNE], Phys. Rev. Lett. **98** (2007) 231801 [arXiv:0704.1500]

[20] A.A. Aguilar-Arevalo *et al.* [MiniBooNE], Phys. Rev. Lett. **110** (2013) 161801 [arXiv:1303.2588]

[23] A.A. Aguilar-Arevalo *et al.* [MiniBooNE], Phys. Rev. Lett. **121** (2018) 221801 [arXiv:1805.12028]

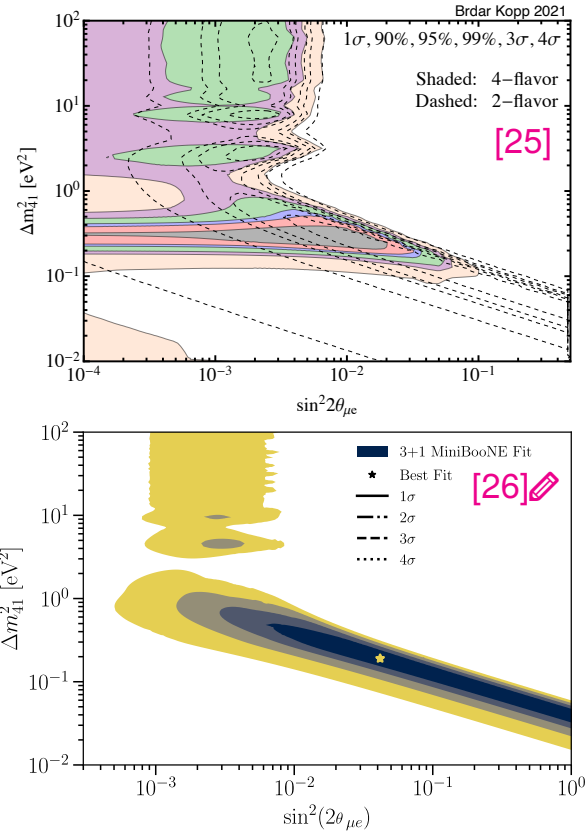
[24] A.A. Aguilar-Arevalo *et al.* [MiniBooNE], Phys. Rev. D **103** (2021) 052002 [arXiv:2006.16883]

Present status of MiniBooNE

- Possible systematics related to the low-E excess:
 - misreconstruction of neutrino energy;
 - π^0 from NC reconstructed as ν_e ;
 - single photon from NC misidentified as ν_e ;
 - extensive studies performed by the collaboration;
 - present status: no combination of known systematics could account for the whole excess [25];
- ⇒ independent experimental confirmation is required.

2ν versus 4ν oscillations

- Former MB studies overlooked oscillations of $\bar{\nu}_e$ beam contamination and $\bar{\nu}_\mu$ calibration sample [25];
- such effects can be very important. Omission corrected in recent reanalysis [26].

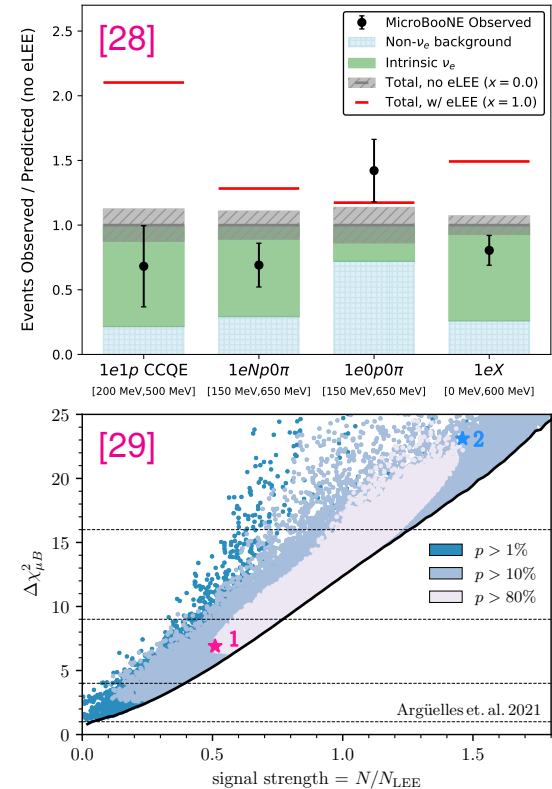


[25] V. Brdar and J. Kopp, Phys. Rev. D **105** (2022) 115024 [arXiv:2109.08157]

[26] A.A. Aguilar-Arevalo *et al.* [MiniBooNE], Phys. Rev. Lett. **129** (2022) 201801 [arXiv:2201.01724]

The MicroBooNE experiment

- Baseline = 468.5 m (72.5 m upstream of MiniBooNE);
- LArTPC \Rightarrow imaging with mm-scale spatial resolution;
- \Rightarrow perfectly suited to cross-check MiniBooNE excess;
- first results presented in fall 2021:
 - no evidence of enhanced π^0 or γ production [27];
 - no evidence of ν_e excess over SM prediction [28];
- however, rejection of MB signal in [28] based on the assumption that the entire ν_e excess matches the difference between data and best-fit MB background;
- but in [29] it was noticed that various signal/background compositions can fit MB equally well, but lead to different μB sensitivity \Rightarrow rejection **not** model-independent...



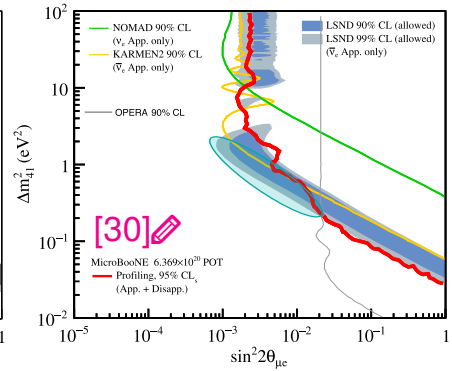
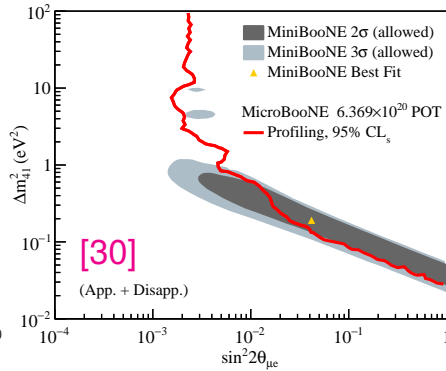
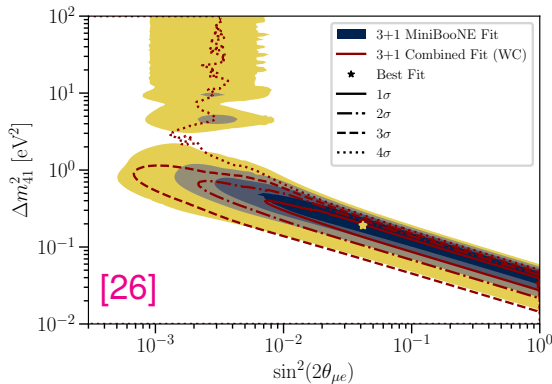
[27] P. Abratenko *et al.* [MicroBooNE], Phys. Rev. Lett. **128** (2022) 111801 [arXiv:2110.00409]

[28] P. Abratenko *et al.* [MicroBooNE], Phys. Rev. Lett. **128** (2022) 241801 [arXiv:2110.14054]

[29] C.A. Argüelles *et al.*, Phys. Rev. Lett. **128** (2022) 241802 [arXiv:2111.10359]

Comparison of MicroBooNE and MicroBooNE results

- MiniBooNE: updated analysis including μ B bounds [26] $\Rightarrow 3\sigma$ region at $\Delta m_{41}^2 \lesssim 1$ eV;
- MicroBooNE: global 4ν analysis [30] disfavors MB/LSND but does not rule it out completely;
- other experiments exclude large Δm^2 (NOMAD) and large $\theta_{\mu e}$ (ICARUS, OPERA);
- remaining allowed region at $0.1 \lesssim \Delta m_{41}^2 / \text{eV}^2 \lesssim 1$ and $10^{-3} \lesssim \sin^2 \theta_{\mu e} \lesssim \text{few} \times 10^{-2}$;
- Short Baseline Neutrino Program @ Fermilab: see next talks;
- Japan: JSNS² will provide an independent check of LSND/MiniBooNE excess.

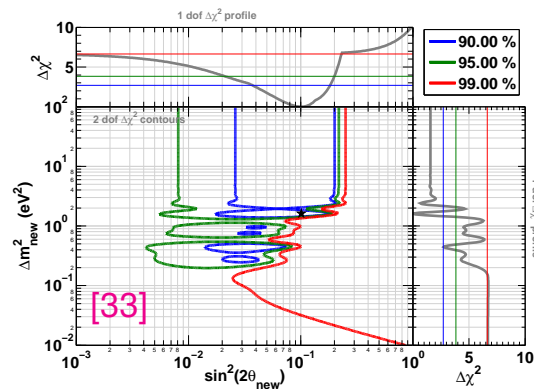
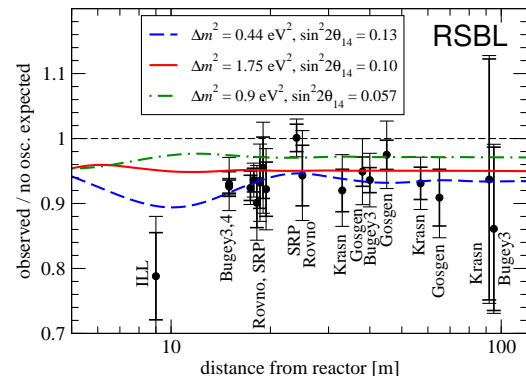


[26] A.A. Aguilar-Arevalo *et al.* [MiniBooNE], Phys. Rev. Lett. **129** (2022) 201801 [arXiv:2201.01724]

[30] P. Abratenko *et al.* [MicroBooNE], Phys. Rev. Lett. **130** (2023) 011801 [arXiv:2210.10216]

$\bar{\nu}_e$ disappearance: the reactor anomaly

- In [31, 32] the reactor $\bar{\nu}$ fluxes was reevaluated;
 - the new calculations result in a small increase of the flux by about **3.5%**;
 - hence, **all** reactor short-baseline (RSBL) finding **no evidence** are actually **observing a deficit**;
 - this deficit **could** be interpreted as being due to SBL neutrino oscillations;
 - no visible dependence on $L \Rightarrow \Delta m^2 \gtrsim 1 \text{ eV}^2$;
 - global data (3σ):
$$\begin{cases} \Delta m_{\text{SOL}}^2 \simeq [6.8 \rightarrow 8.0] \times 10^{-5} \text{ eV}^2, \\ |\Delta m_{\text{ATM}}^2| \simeq [2.4 \rightarrow 2.6] \times 10^{-3} \text{ eV}^2; \end{cases}$$
- \Rightarrow solutions: **add new neutrinos** or **revise fluxes**.



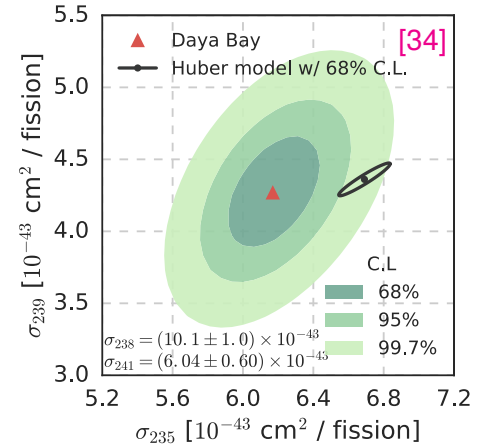
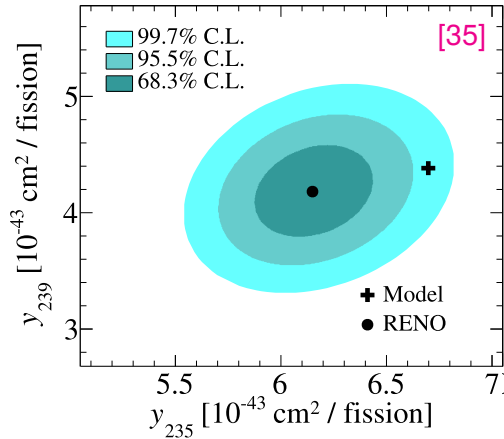
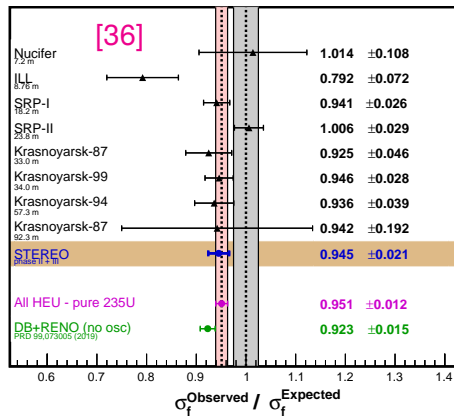
[31] T.A. Mueller *et al.*, Phys. Rev. **C83** (2011) 054615 [arXiv:1101.2663]

[32] P. Huber, Phys. Rev. C **84** (2011) 024617 [arXiv:1106.0687]

[33] G. Mention *et al.*, Phys. Rev. **D83** (2011) 073006 [arXiv:1101.2755]

Reactor anomaly: sterile ν or wrong fluxes?

- DB [34] and RENO [35]: fuel burnup cycle \Rightarrow reconstruct contribution of main isotopes;
- Results: ^{239}Pu mostly agrees with Huber-Mueller model, while ^{235}U substantially below;
- STEREO data [36] (pure ^{235}U reactor) indicate a deficit similar to DB and RENO ones;
- sterile ν : deficit should be the same for all isotopes \Rightarrow disagrees with observations.



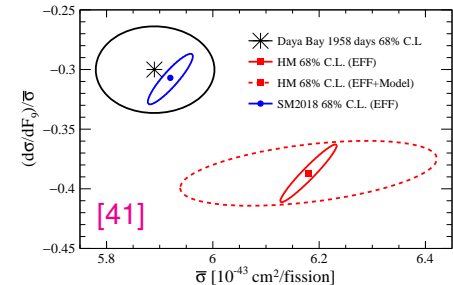
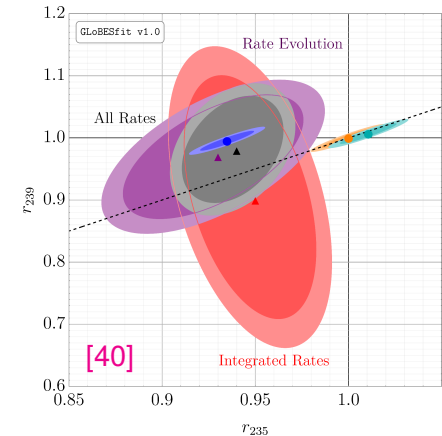
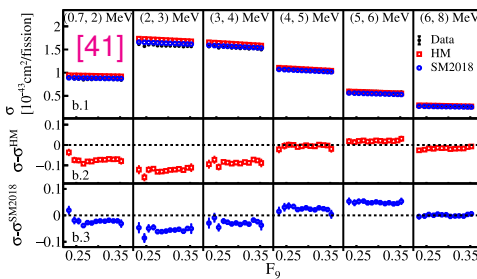
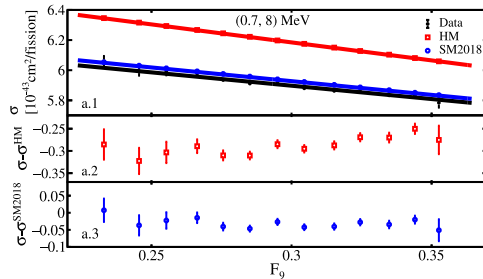
[34] F.P. An *et al.* [Daya-Bay], Phys. Rev. Lett. **118** (2017) 251801 [arXiv:1704.01082]

[35] G. Bak *et al.* [RENO], Phys. Rev. Lett. **122** (2019) 232501 [arXiv:1806.00574]

[36] H. Almazán *et al.* [STEREO], Nature **613** (2023) 257-261 [arXiv:2210.07664]

Recent improvements in reactor flux models

- New reactor flux calculations: EF [37], HKSS [38], KI [39];
- EF model (summation) in good agreement with total rates, although the spectral shape is still not optimal;
- KI model (conversion) yields very similar results to EF;
- conversely, HKSS (conversion) gives rates similar to HM.



[37] M. Estienne *et al.* [EF model], Phys. Rev. Lett. **123** (2019) 022502 [arXiv:1904.09358]

[38] L. Hayen *et al.* [HKSS model], Phys. Rev. C **100** (2019) 054323 [arXiv:1908.08302]

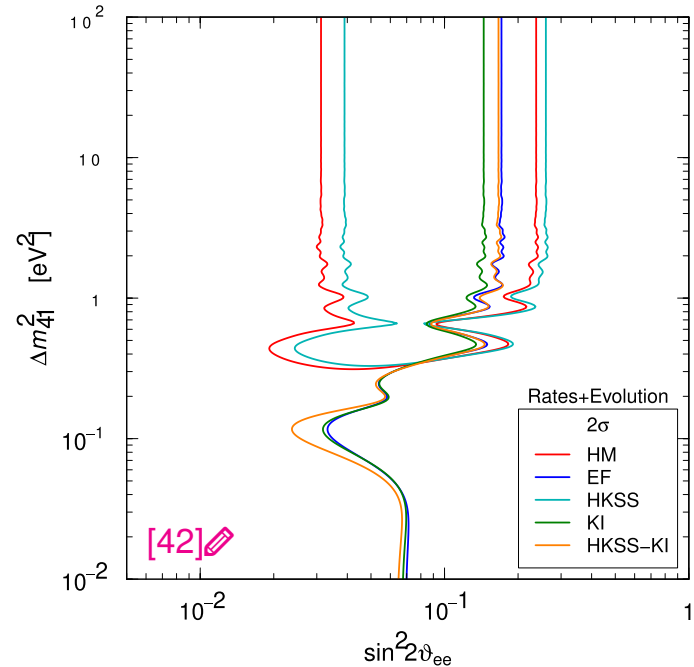
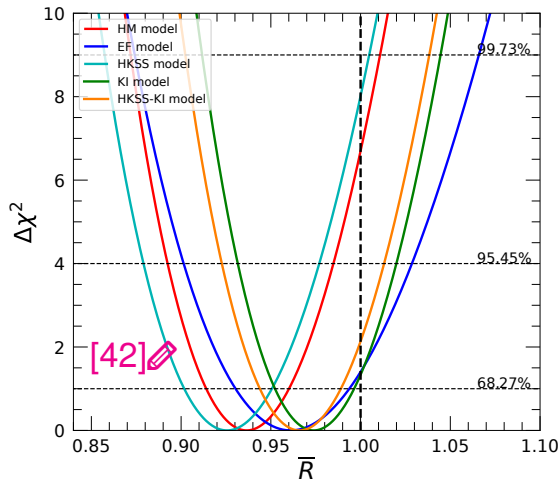
[39] V. Kopeikin *et al.* [KI model], Phys. Rev. D **104** (2021) L071301 [2103.01684]

[40] J.M. Berryman and P. Huber, JHEP **01** (2021) 167 [arXiv:2005.01756]

[41] F.P. An *et al.* [Daya-Bay], Phys. Rev. Lett. **130** (2023) 211801 [arXiv:2210.01068]

Global fit of reactor $\bar{\nu}_e$ disappearance (total rates)

- From Ref. [42]: hint of sterile ν strongly reduced for **EF** (0.8σ) and **KI** (1.4σ);
- hint sizable for **HM** (2.8σ) and **HKSS** (3.0σ).



[37] M. Estienne *et al.* [EF model], Phys. Rev. Lett. **123** (2019) 022502 [arXiv:1904.09358]

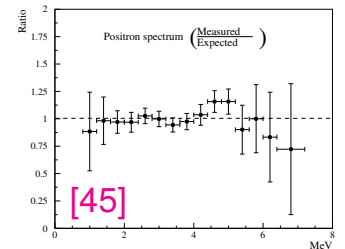
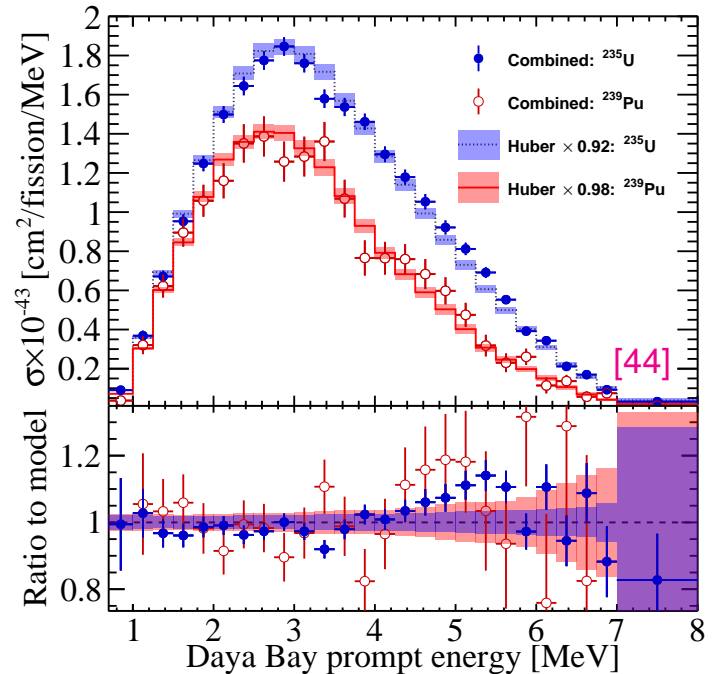
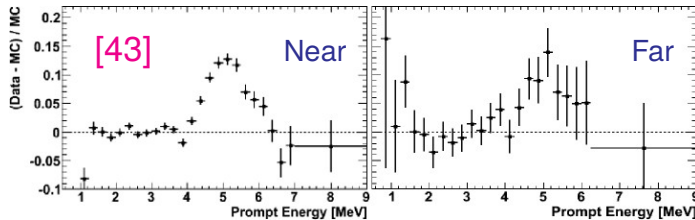
[38] L. Hayen *et al.* [HKSS model], Phys. Rev. C **100** (2019) 054323 [arXiv:1908.08302]

[39] V. Kopeikin *et al.* [KI model], Phys. Rev. D **104** (2021) L071301 [2103.01684]

[42] C. Giunti *et al.*, Phys. Lett. B **829** (2022) 137054 [arXiv:2110.06820]

$\bar{\nu}_e$ disapp: 5 MeV excess

- Neutrino 2014: RENO [43] reported an excess of events around 5 MeV;
- seen by most reactors (also old Chooz [45]);
- DB+Prospect [44]: affect both ^{235}U & ^{239}Pu ;
- excess (not deficit) & independent of $L \Rightarrow$ **flux feature**, not **sterile oscillations**;
- accounted by **HKSS**, but not by **EF** and **KI** \Rightarrow reactor fluxes require further scrutiny.



[43] S.H Seo [RENO], talk at Neutrino 2014, Boston, USA, June 2-7, 2014

[44] F.P. An *et al.* [DB+Prospect], PRL **128** (2022) 081801 [arXiv:2106.12251]

[45] M. Apollonio *et al.* [Chooz], PLB **466** (1999) 415 [hep-ex/9907037]

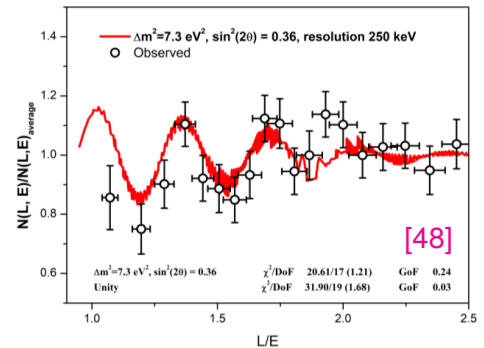
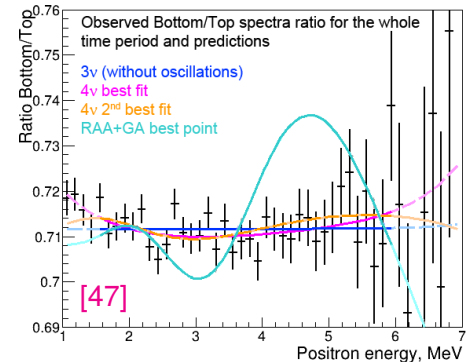
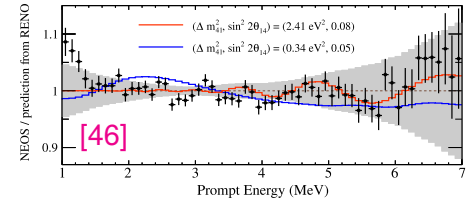
Sterile ν : spectra and baselines

- New detectors with spectral capability and baseline range:
 - NEOS (Korea), **commercial**, $L = 23.7$ m;
 - STEREO (France), **enriched**, $L = 9 \rightarrow 11$ m;
 - PROSPECT (USA), **enriched**, $L = 7 \rightarrow 12$ m;
 - DANSS (Russia) **commercial**, $L = 10.9 \rightarrow 12.9$ m;
 - SOLID (Belgium), **enriched**, $L = 5.5 \rightarrow 12$ m;
 - Neutrino4 (Russia), **enriched**, $L = 6 \rightarrow 12$ m;
- goals:
 - accurate study of reactor ν spectrum;
 - flux-independent osc. by near/far ratio;
- results: most experiments report no evidence, a few observe wiggles at low significance (**DANSS**, **NEOS**);
- exception: **Neutrino4** reports 3σ signal with $\Delta m^2 \sim 7 \text{ eV}^2$.

[46] Z. Atif *et al.* [NEOS & RENO], Phys. Rev. D **105** (2022) L111101 [arXiv:2011.00896]

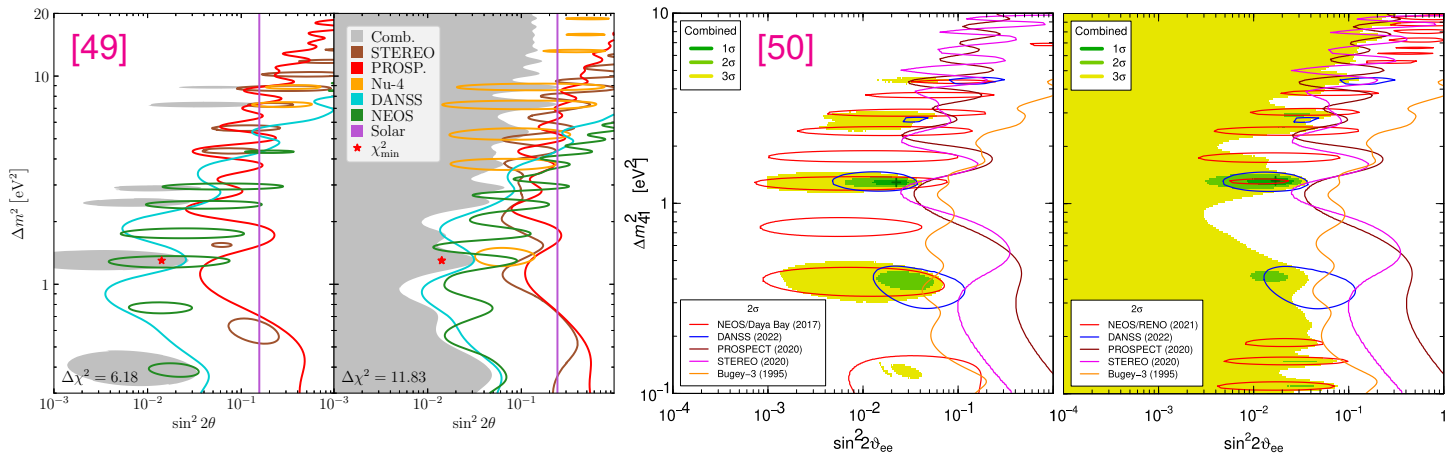
[47] E. Samigullin [DANSS], talk at NuFact 23, Seoul, Korea, 25/08/2023

[48] A.P. Serebrov *et al.* [NEUTRINO4], arXiv:2302.09958



Flux-independent fits of reactor $\bar{\nu}_e$ disappearance data

- Fits based on spectral ratios at various distances are independent of the reactor ν spectrum;
- NEOS + Daya-Bay exhibits stronger wiggles than NEOS + RENO [50];
- no consistent pattern from various “hints”. Combined fit weakly prefers $\Delta m^2 \sim 1.3 \text{ eV}^2$;
- SOLID’s first results presented at TAUP’23 [51] not included here.



[49] J.M. Berryman *et al.*, JHEP **02** (2022) 055 [arXiv:2111.12530]

[50] C. Giunti *et al.*, JHEP **10** (2022) 164 [arXiv:2209.00916]

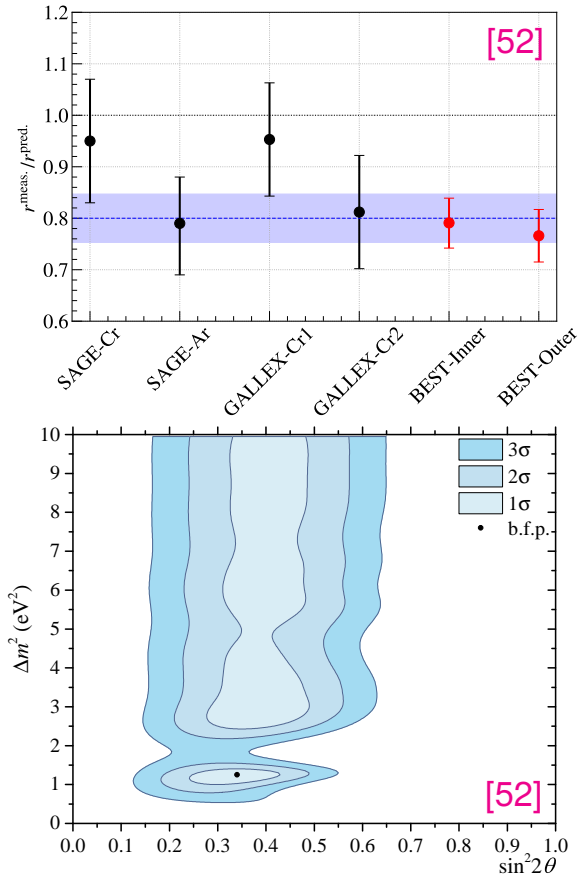
[51] D. Galbinski [SOLID], talk at TAUP 23, Vienna, Austria, 30/08/2023

ν_e disappearance: the gallium anomaly

- $^{71}\text{Ga} \rightarrow ^{71}\text{Ge}$ ν capture cross-section was calibrated with intense ^{51}Cr and ^{37}Ar sources by GALLEX & SAGE (20 years ago) as well as BEST (2022);
- these measurements show a significant deficit with respect to the predicted values [52]:

$$\left. \begin{array}{l}
 \text{GALLEX: } \left\{ \begin{array}{l} R_1(\text{Cr}) = 0.953 \pm 0.11 \\ R_2(\text{Cr}) = 0.812 \pm 0.11 \end{array} \right\} \\
 \text{SAGE: } \left\{ \begin{array}{l} R_3(\text{Cr}) = 0.95 \pm 0.12 \\ R_4(\text{Ar}) = 0.79 \pm 0.095 \end{array} \right\} \\
 \text{BEST: } \left\{ \begin{array}{l} R_5(\text{I}) = 0.791 \pm 0.05 \\ R_6(\text{O}) = 0.766 \pm 0.05 \end{array} \right\}
 \end{array} \right\} \Rightarrow \boxed{0.80 \pm 0.047}$$

- such deficit can be interpreted in terms of oscillations;
- data suggest $\Delta m^2 \gtrsim 1 \text{ eV}^2$ but require very large θ_{ee} .

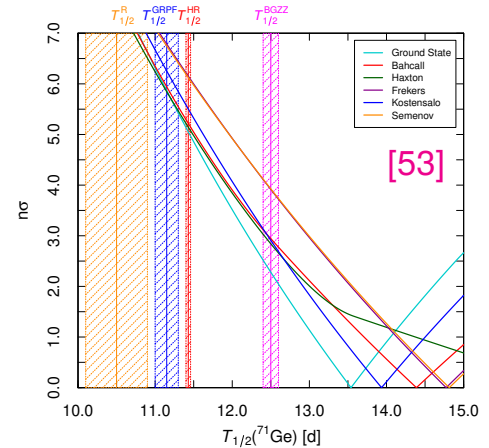
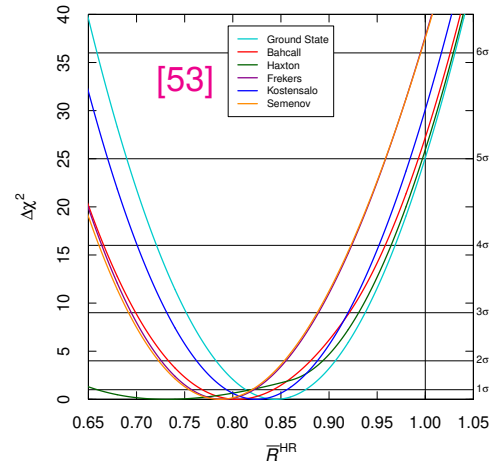
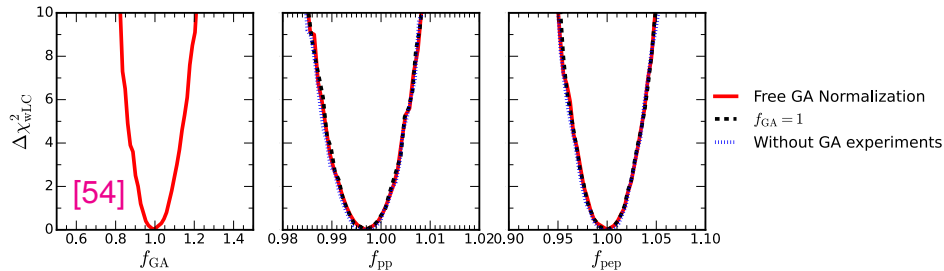


[52] V.V. Barinov *et al.* [BEST], Phys. Rev. C **105** (2022) no.6, 065502 [arXiv:2201.07364]

Origin of the gallium anomaly

- Large θ_{ee} required by Gallium ν_e oscill. clashes with:
 - reactor $\bar{\nu}_e$ data, as seen in previous slides;
 - solar ν_e data, which don't tolerate a large ν_s fraction;
- can the Gallium cross-section be overestimated?
 - well-known **ground-state** suffices for the tension;
 - ^{71}Ge half-life may be wrong, but needed “error” very large;
 - solar data show no tension with current cross-section;

⇒ no obvious solution to the Gallium puzzle.

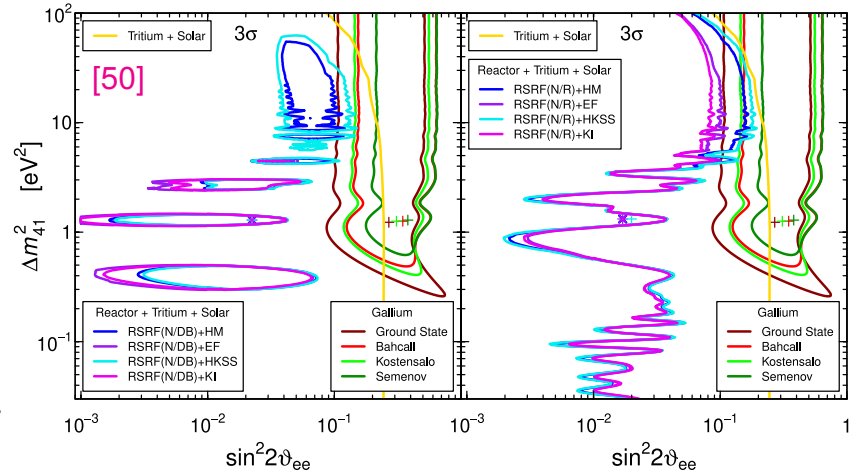
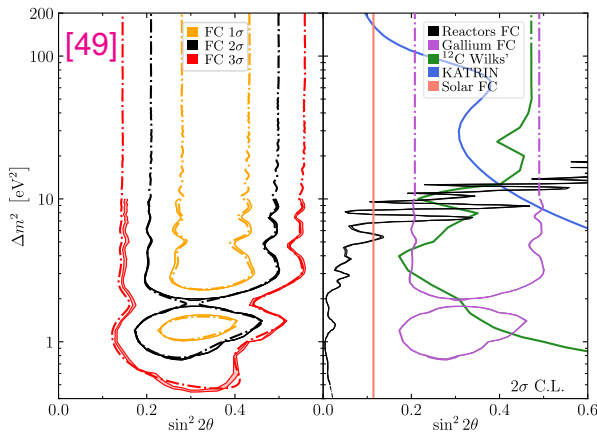


[53] C. Giunti *et al.*, *Phys. Lett. B* **842** (2023) 137983 [2212.09722]

[54] M.C. Gonzalez-Garcia *et al.*, *JHEP* **02** (2024) 064 [2311.16226]

Comparison of all ν_e and $\bar{\nu}_e$ disappearance data

- **Reactors**: proper FC statistics relaxes bounds by about 1σ w.r.t. Wilk's limits [49];
- **Gallium**: FC not so important [49], but it cannot be reconciled with other data [49, 50];
- “least tension” $\bar{\nu}_e \rightarrow \bar{\nu}_e$ at $\Delta m^2 \sim 10 \text{ eV}^2$, **in tension** with $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ value $\Delta m^2 \sim 1 \text{ eV}^2$;
- **solar** data also disfavor large mixing angle, and **tritium** does so at large Δm^2 .

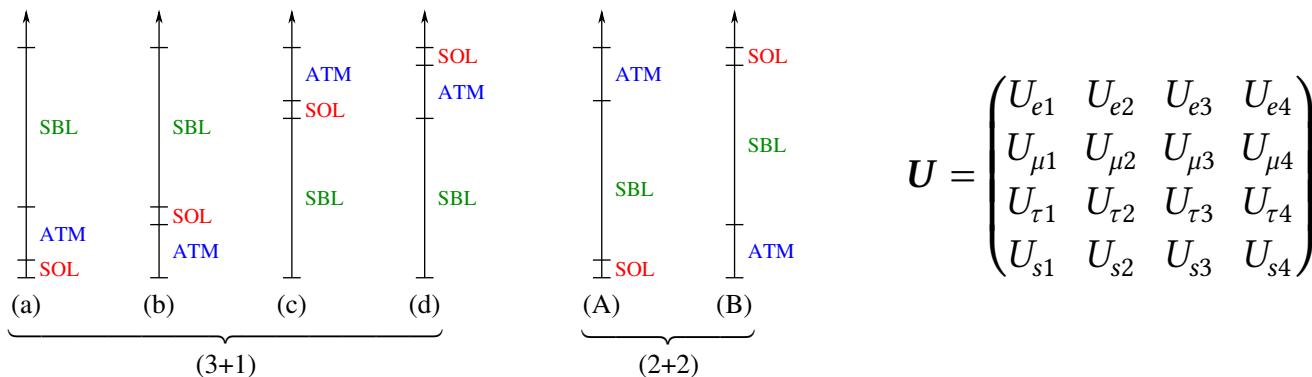


[49] J.M. Berryman *et al.*, JHEP **02** (2022) 055 [arXiv:2111.12530]

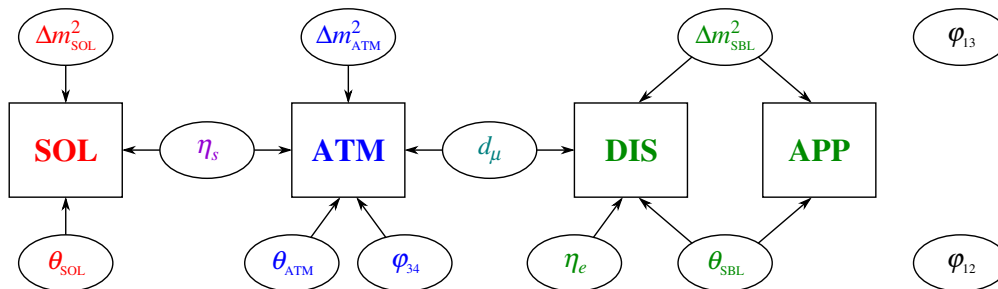
[50] C. Giunti *et al.*, JHEP **10** (2022) 164 [arXiv:2209.00916]

Four neutrino mass models

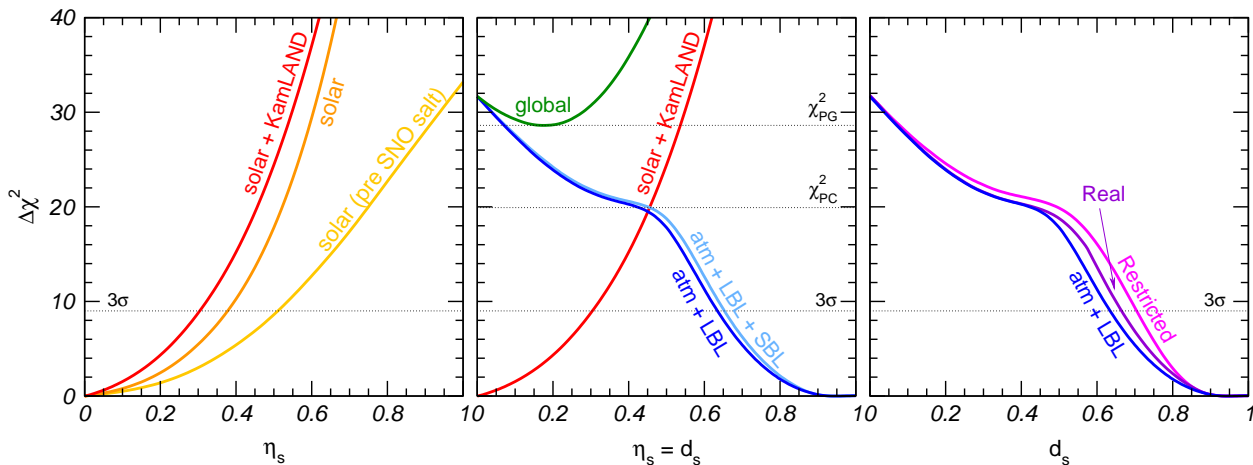
- Approximation: $\Delta m_{\text{SOL}}^2 \ll \Delta m_{\text{ATM}}^2 \ll \Delta m_{\text{SBL}}^2 \Rightarrow$ 6 different mass schemes:



- Total: 3 Δm^2 , 6 angles, 3 phases. Different set of experimental data *partially decouple*:



(2+2): ruled out by solar and atmospheric data



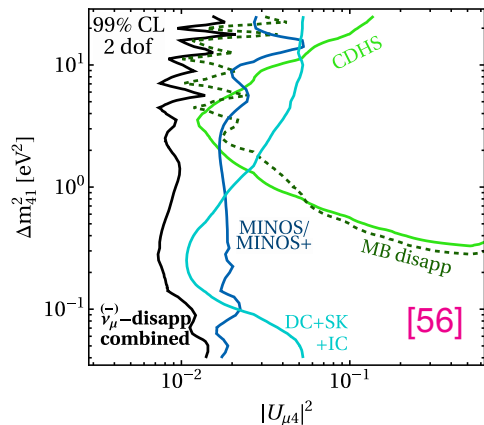
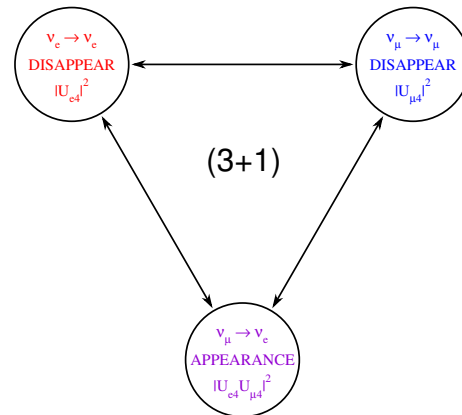
- in (2+2) models, fractions of ν_s in **solar** (η_s) and **atmos** ($1 - d_s$) add to one $\Rightarrow \boxed{\eta_s = d_s}$;
- 3σ allowed regions $\eta_s \leq 0.31$ (**solar**) and $d_s \geq 0.63$ (**atmos**) do not overlap; superposition occurs only above 4.5σ ($\chi_{PC}^2 = 19.9$);
- the χ^2 increase from the combination of **solar** and **atmos** data is $\chi_{PG}^2 = 28.6$ (1 dof), corresponding to a $PG = 9 \times 10^{-8}$ [55].

[55] M. Maltoni, T. Schwetz, M.A. Tortola, J.W.F. Valle, Nucl. Phys. **B643** (2002) 321 [hep-ph/0207157].

(3+1): appearance versus disappearance

- (3+1): $P_{\nu_\mu \rightarrow \nu_e} \propto |U_{e4} U_{\mu 4}|^2$ with $\begin{cases} |U_{e4}|^2 \propto P_{\nu_e \rightarrow \nu_e}, \\ |U_{\mu 4}|^2 \propto P_{\nu_\mu \rightarrow \nu_\mu}; \end{cases}$
- hence, $P_{\nu_\mu \rightarrow \nu_e} > 0$ requires $\begin{cases} P_{\nu_e \rightarrow \nu_e} > 0, \\ P_{\nu_\mu \rightarrow \nu_\mu} > 0; \end{cases}$

❓ are $\nu_\mu \rightarrow \nu_\mu$ searches compatible with this?



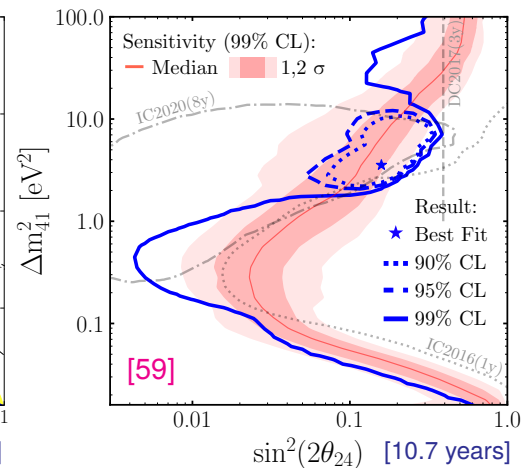
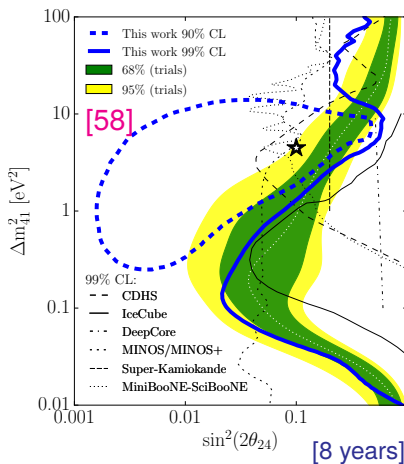
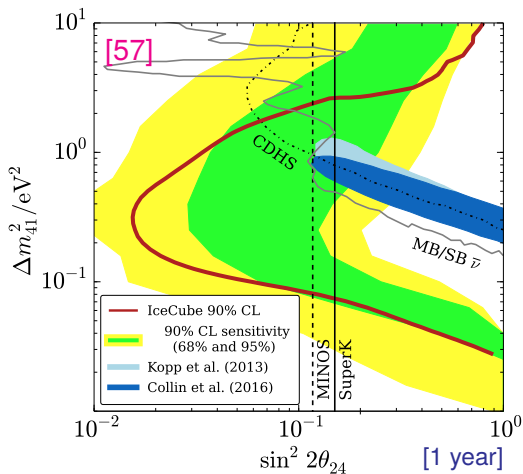
ν_μ disappearance: long-term situation

- Many experiments have been performed:
 - CDHS (ν)
 - MiniBooNE ($\nu, \bar{\nu}$)
 - SciBooNE ($\nu, \bar{\nu}$)
 - MINOS (ν)
 - NO ν A (ν)
 - SK atmos ($\nu, \bar{\nu}$)
- no hint of ν_μ disappearance has been observed;
- bound on $|U_{\mu 4}|^2$ may be in tension with other data...

[56] M. Dentler *et al.*, JHEP 08 (2018) 010 [arXiv:1803.10661]

Search for ν_μ disappearance at IceCube

- Since oscillations only depend on $\Delta m^2/E$, larger Δm^2 produce visible effects at larger E ;
- IceCube has been detecting high-energy (\sim TeV) atmos. neutrinos since its construction;
- a small “island” around $\Delta m^2 \sim \text{few eV}^2$ and $\sin^2 2\theta_{\mu\mu} \sim 0.1$ has been gaining prominence;
- p -value for no-oscillation: of 47% (1 year), 8% (8 years), 3.1% (10.7 years) \Rightarrow still OK.



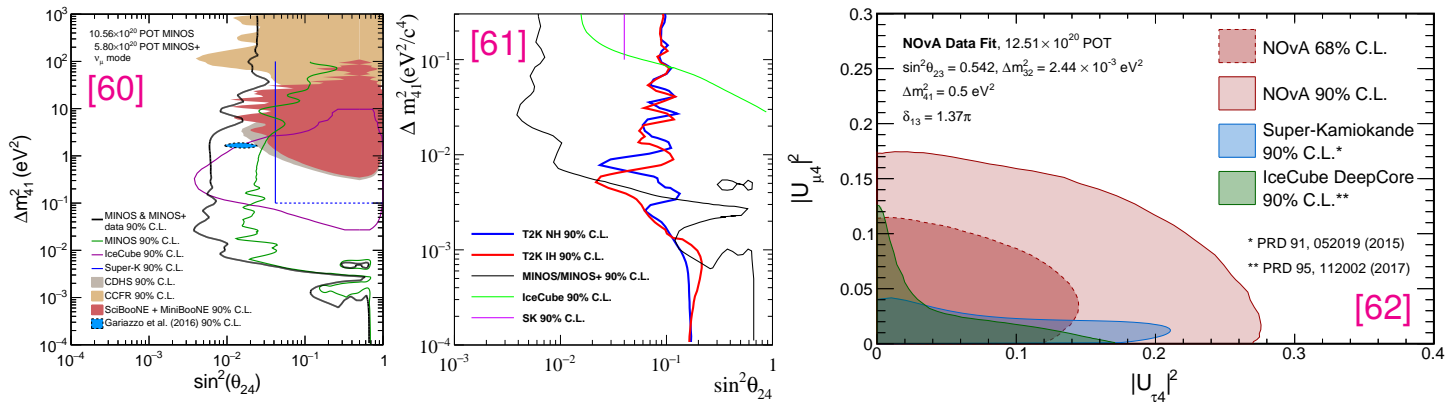
[57] M.G. Aartsen *et al.* [IceCube], Phys. Rev. Lett. **117** (2016) 071801 [arXiv:1605.01990]

[58] M.G. Aartsen *et al.* [IceCube], Phys. Rev. Lett. **125** (2020) 141801 [arXiv:2005.12942]

[59] R. Abbasi *et al.* [IceCube], arXiv:2405.08070

Search for ν_μ disappearance at LBL experiments

- Sterile ν can be searched at LBL experiments by “switching” the roles of **near** & **far** detectors:
 - **far** detector observes fully averaged oscillations \Rightarrow fixes the *energy shape* of the beam;
 - **near** detector looks for spectral distortions which would indicate SBL oscillations;
- results presented by MINOS/MINOS+ [60], T2K [61], and NOvA [62] collaborations;
- sterile oscillations can also be studied by looking for deficit in neutral-current data [62].



[60] P. Adamson *et al.* [MINOS+], Phys. Rev. Lett. **122** (2019) no.9, 091803 [arXiv:1710.06488]

[61] K. Abe *et al.* [T2K], Phys. Rev. D **99** (2019) no.7, 071103 [arXiv:1902.06529]

[62] M.A. Acero *et al.* [NOvA], Phys. Rev. Lett. **127** (2021) no.20, 201801 [arXiv:2106.04673]

(3+1): tension among data samples

- Inconsistency between **Reactors** and **Gallium** results **prevents** a combined fit of all $\nu_e \rightarrow \nu_e$ data;
- Limits on a subset of $\nu_e \rightarrow \nu_e$ and $\nu_\mu \rightarrow \nu_\mu$ disappearance [63] imply a bound on $\nu_\mu \rightarrow \nu_e$ **stronger** than what required to explain the **LSND** and **MiniBooNe** excesses;
- such tension between **APP** and **DIS** data was first pointed out in 1999 [64]. Full global fit in 2001 [65] cornered (3+1) models. No conceptual change since then...

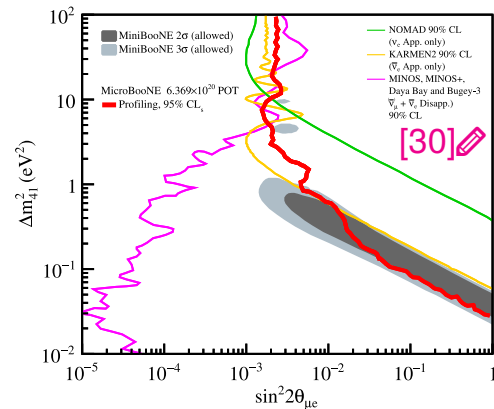
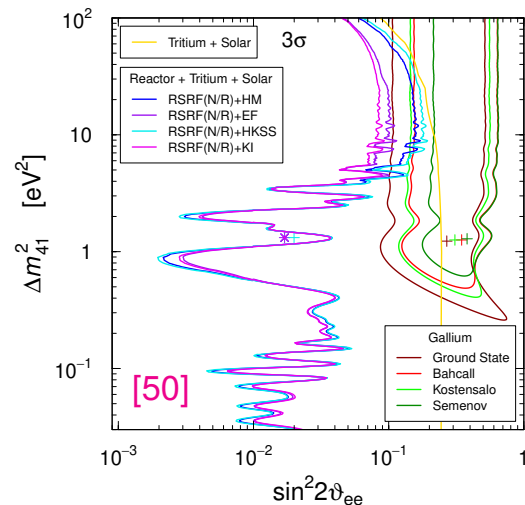
[30] P. Abratenko *et al.* [MicroBooNE], Phys. Rev. Lett. **130** (2023) 011801 [arXiv:2210.10216]

[50] C. Giunti *et al.*, JHEP **10** (2022) 164 [arXiv:2209.00916]

[63] P. Adamson *et al.* [MINOS+ and Daya-Bay], Phys. Rev. Lett. **125** (2020) 071801 [arXiv:2002.00301]

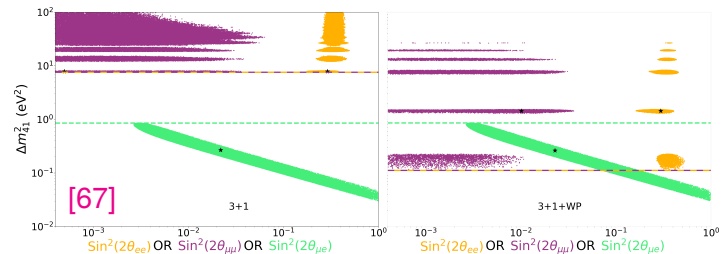
[64] S.M. Bilenky *et al.*, PRD **60** (1999) 073007 [hep-ph/9903454]

[65] MM, Schwetz, Valle, PLB **518** (2001) 252 [hep-ph/0107150]



Beyond (3+1) oscillations

- If (3+1) models do not work (and never did), why do we keep discussing them?
 - they are a natural extension of 3ν ;
 - they individually explain each anomaly;
 - hence, they make a great starting point;
 - can we do better than this?
 - more steriles (3+2, 3+3, ...) not enough;
 - recent trend towards “dumping” [67] (first noted in [66]), but tensions remain;
 - alternatives explain some (not all) data;
 - usually very “exotic” and “ad-hoc”;
- ⇒ “vanilla ν_s ” still best working tool.



Explanations beyond the Standard Model [Goal: account for the Gallium anomaly]

ν_s coupled to ultralight DM (MSW resonance, Sec. 5.1.1)	several exotic ingredients; somewhat tuned MSW resonance; new ν_4 decay channel required for cosmology. ★★★★★
ν_s coupled to dark energy (MSW resonance, Sec. 5.1.2)	several exotic ingredients; somewhat tuned MSW resonance; cosmology similar to the previous scenario. ★★★★★
ν_s coupled to ultralight DM (param. resonance, Sec. 5.1.3)	several exotic ingredients; somewhat tuned parametric resonance; cosmology requires post-BBN DM production via misalignment. ★★★★★
decaying ν_s (Section 5.2)	difficult to reconcile with reactor and solar data; regeneration of active neutrinos in ν_s decays alleviates tension, but does not resolve it. ★★★☆☆
vanilla eV-scale ν_s (Refs. [17, 18])	preferred parameter space is strongly disfavored by solar and reactor data. ★☆☆☆☆
ν_s with CPT violation (Refs. [130])	avoids constraints from reactor experiments, but those from solar neutrinos cannot be alleviated.
extra dimensions (Refs. [131–133])	neutrinos oscillate into sterile Kaluza–Klein modes that propagate in extra dimensions; in tension with reactor data.
stochastic neutrino mixing (Ref. [134])	based on a difference between sterile neutrino mixing angles at production and detection (see also [135, 136]); fit worse than for vanilla ν_s .
decoherence (Refs. [137, 138])	non-standard source of decoherence needed; known experimental energy resolutions constrain wave packet length, making an explanation by wave packet separation alone challenging.
ν_s coupled to ultralight scalar (Ref. [139])	ultralight scalar coupling to ν_s and to ordinary matter affects sterile neutrino parameters; can not avoid reactor constraints

[68]

[66] S. Palomares-Ruiz *et al.*, JHEP **09** (2005) 048 [hep-ph/0505216]

[67] J.M. Hardin *et al.*, JHEP **09** (2023) 058 [arXiv:2211.02610]

[68] V. Brdar *et al.*, JHEP **05** (2023) 143 [arXiv:2303.05528]

- Most of the present data from **solar**, **atmospheric**, **reactor** and **accelerator** experiments are well explained by the 3ν oscillation hypothesis. The 3ν scenario is well proven and **robust**;
- however, the possibility of physics beyond the 3ν paradigm remains open (and it is even supported by a few anomalies, albeit inconclusive). Here we have focused on two mechanisms:

NC-like non-standard neutrino-matter interactions

- we have considered NSI with arbitrary ratios of couplings to e , u , d (parametrized by angles η and ζ) and a common structure of the lepton-flavor vertex (parametrized by a matrix $\varepsilon_{\alpha\beta}^{\eta}$);
- we have found that NSI **cannot** spoil the precise determination of the oscillation parameters once all the data are combined together – except for θ_{12} where a new region (LMA-D) appears;
- a degeneracy between LMA-D and the ν mass ordering cannot be resolved by oscillation data alone. Combination with scattering experiments (e.g., COHERENT) is essential;

Sterile neutrinos with masses in the eV range

- $\nu_e \rightarrow \nu_e$ **disappearance** data exhibit a serious tension in solar/reactor vs gallium results, as well as some issue between different “spectral shape” reactor experiments;
- $\nu_{\mu} \rightarrow \nu_e$ **appearance** data show an excess in low-E neutrino data, which cannot be explained by oscillations alone and so far has eluded the searches for new systematics;
- each anomalous data set can be **individually** explained by sterile neutrinos, but no **global** explanation of all data (or even data sharing the same oscillation channel) is possible.