

## Hot Leptogenesis

*A naturalness-motivated solution to baryon asymmetry*

*HEP Forum 2024*

Ansh Bhatnagar (+ M. Baker, D. Croon and J. Turner)

IPPP, Durham University

✉ [ansh.bhatnagar@durham.ac.uk](mailto:ansh.bhatnagar@durham.ac.uk)

# Leptogenesis: the answer to the origin of the BAU?

Seesaw mechanism introduces heavy Majorana right-handed neutrinos (RHN) with Yukawa coupling  $Y_{\alpha i} \overline{L}_{\alpha} \widetilde{H} N_i$ .

$$m_{\nu}^{\text{tree}} \approx v^2 Y^T M_R^{-1} Y, \quad (1)$$

## Leptogenesis

Out-of-equilibrium **decays** of heavy RHN could seed a  $L$  asymmetry that is converted to a  $B$  asymmetry through  $B+L$  violating sphaleron interactions [Fukugita and Yanagida, 1986].

Requires a lightest RHN mass of  $m_N \gtrsim 10^8 \text{ GeV}^1$  to generate the **observed** baryon asymmetry<sup>2</sup> of  $\eta_B = (5.8 - 6.3) \times 10^{-10}$ .

Naturalness constraints **limit**  $m_N \lesssim 7.4 \times 10^7 \text{ GeV}^3$ .

---

<sup>1</sup>[Davidson and Ibarra, 2002]

<sup>2</sup>PDG 2023

<sup>3</sup>[Vissani, 1998]

# Hot Leptogenesis

## ***Increase the RHN temperature!***

A thermally disconnected hot RHN sector, with a thermal number density could allow for the observed  $\eta_B$  to be produced with a lower RHN mass spectrum.

First proposed in [Bernal and Fong, 2017], we present a comprehensive model and numerical analysis of this scenario.

## ***Kinetic equilibrium***

Requires fast (vs Hubble) elastic scattering processes.

$$\frac{n}{n_{\text{eq}}} = \frac{f}{f_{\text{FD}}} \quad (2)$$

## ***Kinetic + chemical equilibrium***

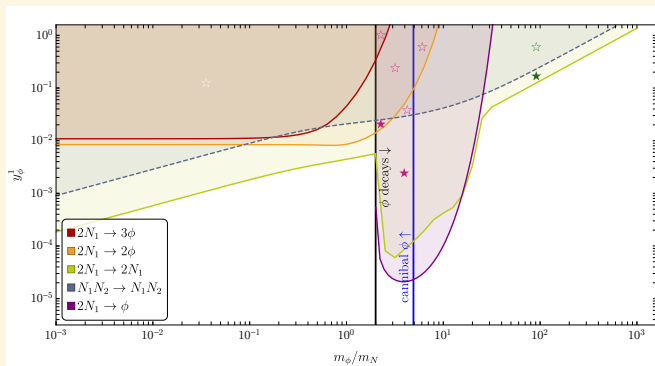
Kinetic + chemical equilibrium requires fast number changing processes as well.

$$n = n_{\text{eq}} \quad (3)$$

# Coupling constraints

Introduce a scalar  $\phi$  with coupling  $y_\phi \phi \bar{N}_i N_i$  and  $\frac{\lambda}{4!} \phi^4$ .

Compute thermally averaged number-changing interaction rates  $\Gamma_{2N_1 \rightarrow 3\phi}$ ,  $\Gamma_{2N_1 \rightarrow 2\phi}$ ,  $\Gamma_{2N_1 \rightarrow \phi}$ , and the elastic scattering rates  $\Gamma_{2N_i \rightarrow 2N_i}$ , and compare to Hubble at  $T_H = m_{N_1}$ .



# Boltzmann equations

$$aH \frac{dN_{N_1}}{da} = -\Gamma_{D_1}(z_{N_1}) N_{N_1} + \Gamma_{D_1}(z_{SM}) N_{N_1}^{\text{eq}}, \quad (4)$$

$$aH \frac{dN_{N_2}}{da} = -\Gamma_{D_2}(z_{N_2}) (N_{N_2} - N_{N_2}^{\text{eq}}), \quad (5)$$

$$aH \frac{dN_{N_3}}{da} = -\Gamma_{D_3}(z_{N_3}) (N_{N_3} - N_{N_3}^{\text{eq}}), \quad (6)$$

$$\frac{dT_{SM}}{da} = \left( \frac{ds_{SM}}{dT_{SM}} \right)^{-1} \left( \frac{1}{a^3 T_{SM}} \frac{dQ}{da} - 3 \frac{s_{SM}}{a} \right), \quad (7)$$

The  $T_{SM}$  evolution is derived from the second law of thermodynamics.

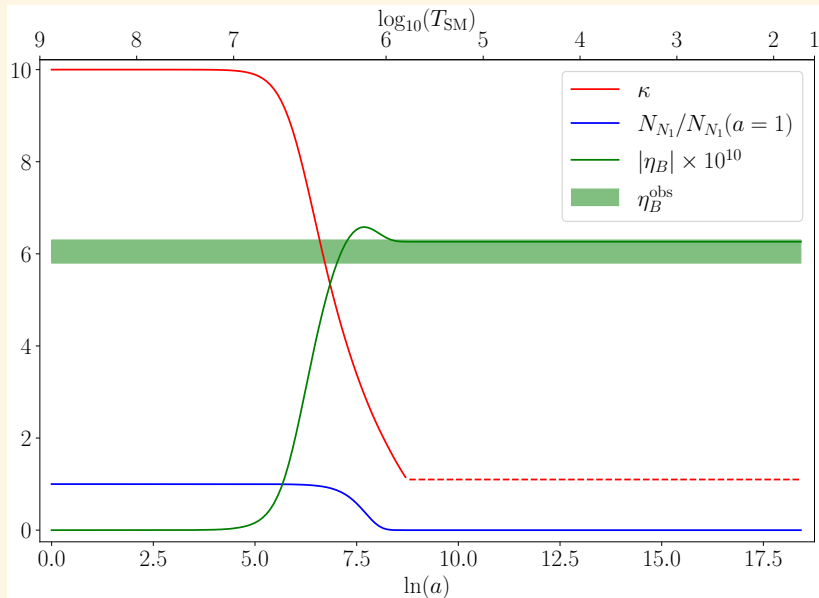
If chemical equilibrium holds,  $T_H$  is dictated by  $N_N = N_N^{\text{eq}}(z_H)$ , else the evolution of  $T_H$  can be derived from comoving energy density conservation.

# $N_{B-L}$ density matrix equation

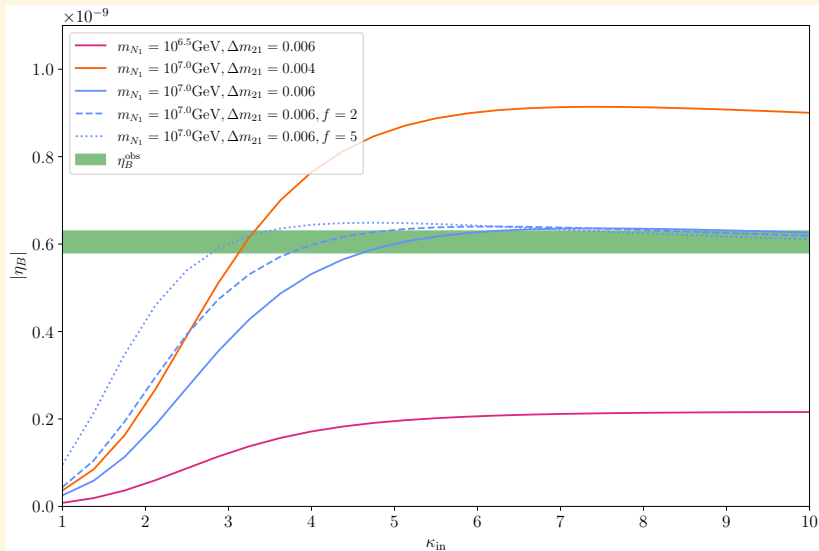
$$\begin{aligned}
 aH \frac{dN_{\alpha\beta}}{da} = & \epsilon_{\alpha\beta}^{(1)} \left( \Gamma_{D_1}(z_{N_1}) N_{N_1} - \Gamma_{D_1}(z_{SM}) N_{N_1}^{\text{eq}} \right) - \frac{1}{2} W_1 \left\{ P^{(1)}, N \right\}_{\alpha\beta} \\
 & + \sum_{i=2}^3 \epsilon_{\alpha\beta}^{(i)} \Gamma_{D_i}(z_{N_i}) \left( N_{N_i} - N_{N_i}^{\text{eq}} \right) - \frac{1}{2} W_i \left\{ P^{(i)}, N \right\}_{\alpha\beta} \\
 & - \mathcal{L}_\tau \left[ \left( \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right), \left[ \left( \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right), N \right] \right]_{\alpha\beta} \quad (8)
 \end{aligned}$$

$$- \mathcal{L}_\mu \left[ \left( \begin{array}{ccc} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{array} \right), \left[ \left( \begin{array}{ccc} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{array} \right), N \right] \right]_{\alpha\beta}, \quad (9)$$

# Leptogenesis evolution



# Increasing the temperature





# Casas-Ibarra Parametrisation

For the seesaw mechanism, the Yukawa matrix can be written as,

$$Y = \frac{1}{v} U \sqrt{\widehat{m}_\nu} R^T \sqrt{M_R}. \quad (10)$$

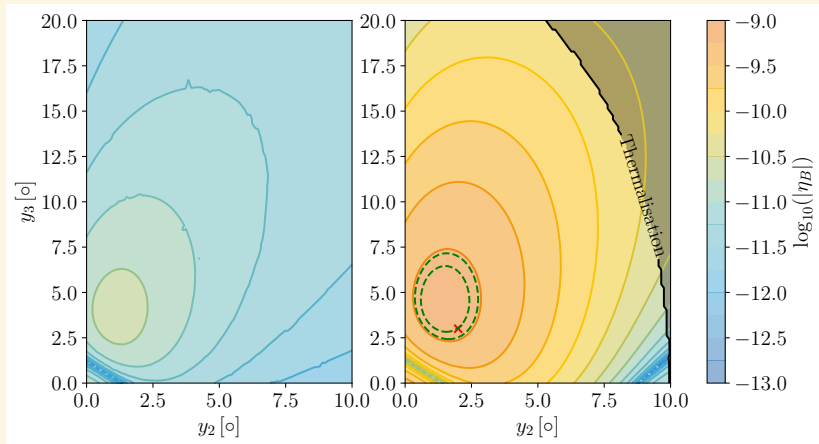
$R$  is given by

$$R = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{\omega_1} & s_{\omega_1} \\ 0 & -s_{\omega_1} & c_{\omega_1} \end{pmatrix} \begin{pmatrix} c_{\omega_2} & 0 & s_{\omega_2} \\ 0 & 1 & 0 \\ -s_{\omega_2} & 0 & c_{\omega_2} \end{pmatrix} \begin{pmatrix} c_{\omega_3} & s_{\omega_3} & 0 \\ -s_{\omega_3} & c_{\omega_3} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad (11)$$

where the complex angle  $\omega_i = x_i + iy_i$ .

# Scan of Casas-Ibarra parameters

We calculate  $\eta_B$  in vanilla leptogenesis and in hot leptogenesis for varying  $y_2$  (x-axis) and  $y_3$  (y-axis).



# Benchmark fine-tuning comparison<sup>4</sup>

$$\Delta_v = \frac{\sum_{i=1}^3 \text{SVD}[M_v]_i}{\sum_{i=1}^3 \text{SVD}[M_v^{1\text{-loop}}]_i}, \quad (12)$$

$$|\delta\mu^2| \approx \frac{1}{4\pi^2} \text{Tr} \left[ Y M_N^2 Y^\dagger \right]. \quad (13)$$

$$\Delta_H = \sqrt{\frac{(\mu_H^{\text{tree}})^2 - |\delta\mu^2|}{\frac{1}{2}((\mu_H^{\text{tree}})^2 + |\delta\mu^2|)}}} \approx \sqrt{\frac{\mu_H^2}{|\delta\mu^2|}}, \quad (14)$$

Benchmark	$S_1$	$S_2$	$S_3$	$\bar{S}_1$	$\bar{S}_2$	$\bar{S}_3$	Our Benchmark
$\Delta_v$ [%]	0.2	0.3	0.2	0.6	0.7	0.4	855
$\Delta_H$ [%]	0.08	0.02	0.004	0.3	0.06	0.1	10.4

<sup>4</sup>[Moffat et al., 2018]

# Conclusions

Hot leptogenesis is possible under two scenarios; a hot sector in kinetic equilibrium, or thermal equilibrium.

A hot RHN sector can resolve the tension between the Davidson-Ibarra bound and the Vissani bound.

***Thanks for listening!***

Any questions?

# References

- ☰ Bernal, N. and Fong, C. S. (2017).  
Hot Leptogenesis from Thermal Dark Matter.  
*JCAP*, 10:042.
- ☰ Davidson, S. and Ibarra, A. (2002).  
A Lower bound on the right-handed neutrino mass from leptogenesis.  
*Phys. Lett. B*, 535:25–32.
- ☰ Fukugita, M. and Yanagida, T. (1986).  
Baryogenesis Without Grand Unification.  
*Phys. Lett. B*, 174:45–47.
- ☰ Moffat, K., Pascoli, S., Petcov, S. T., Schulz, H., and Turner, J. (2018).  
Three-flavored nonresonant leptogenesis at intermediate scales.  
*Phys. Rev. D*, 98(1):015036.
- ☰ Vissani F (1998)