The background of the slide is a complex, artistic illustration. It features numerous small, colorful spheres (red, blue, orange, and grey) of varying sizes, some of which are connected to larger spheres by thin, vertical lines. These elements are set against a backdrop of swirling, wavy patterns in shades of brown, gold, and blue, suggesting a dynamic, perhaps quantum or particle physics, environment.

Overview of (some UK) Neutrino Theory

ECFA-UK Meeting on UK studies for the European Strategy
Particle Physics Update
Jessica Turner, IPPP, Durham University
26 September 2024

Neutrinos: what we know

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{atmospheric}} \cdot \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix}}_{\text{reactor}} \cdot \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{solar}} \cdot \begin{pmatrix} e^{i\frac{\alpha_{21}}{2}} & 0 & 0 \\ 0 & e^{i\frac{\alpha_{31}}{2}} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

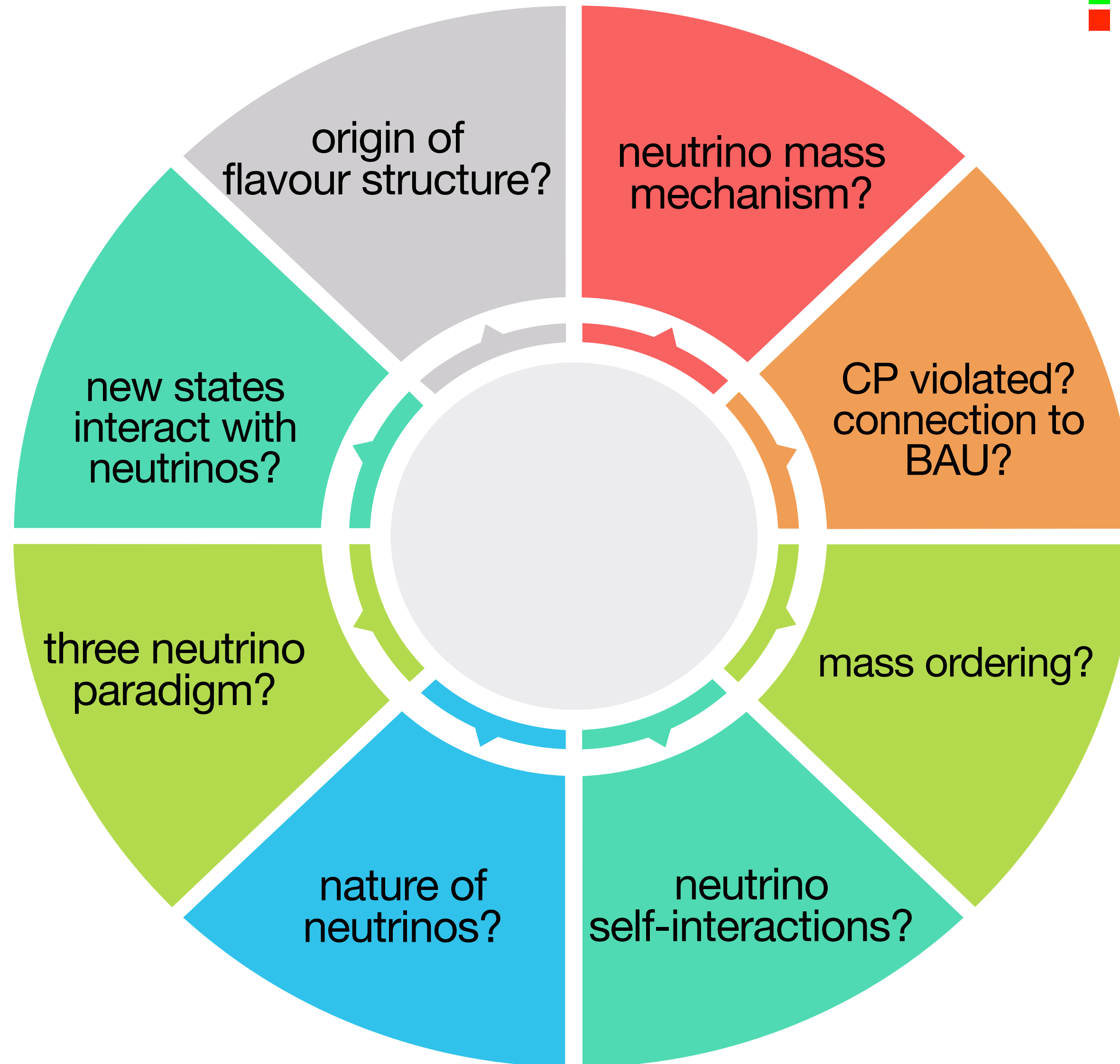
$$s_{ij} = \sin(\theta_{ij})$$

$$c_{ij} = \cos(\theta_{ij})$$

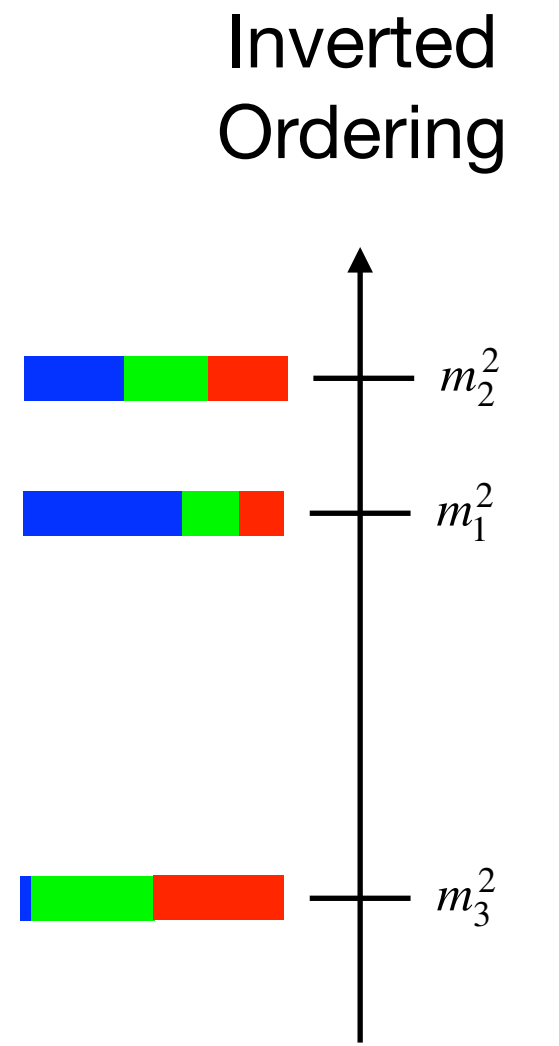
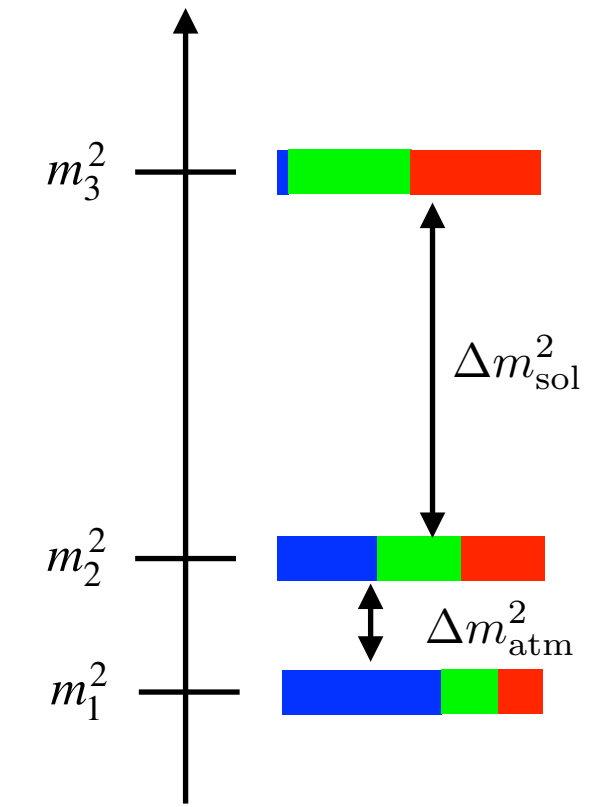
NuFIT 5.2

mixing parameter	central value	relative uncertainty (3σ)	
θ_{13} ($^\circ$)	8.6	4.7%	4.0%
θ_{23} ($^\circ$)	42.2	22%	5.2%
θ_{12} ($^\circ$)	33.4	7.3%	0.3%
δ_{CP} ($^\circ$)	232	100%	Quark sector

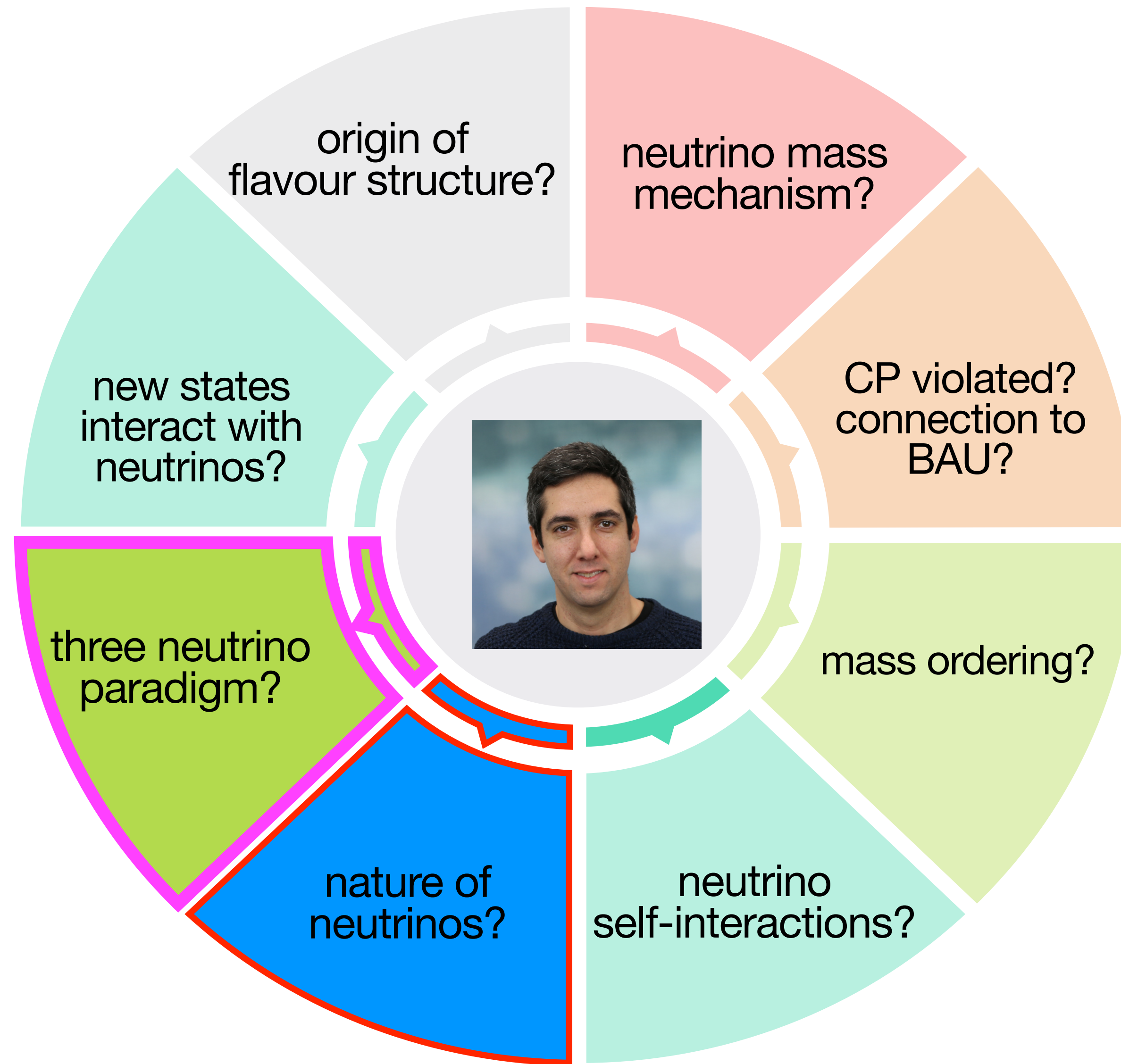
Neutrinos: what we don't know



ν_e
 ν_μ
 ν_τ



Neutrinos: what we don't know



PseudoDirac Neutrinos

$$\mathcal{L} = Y_\nu \bar{L} N \tilde{H} + \frac{1}{2} \overline{N^C} M_N N$$

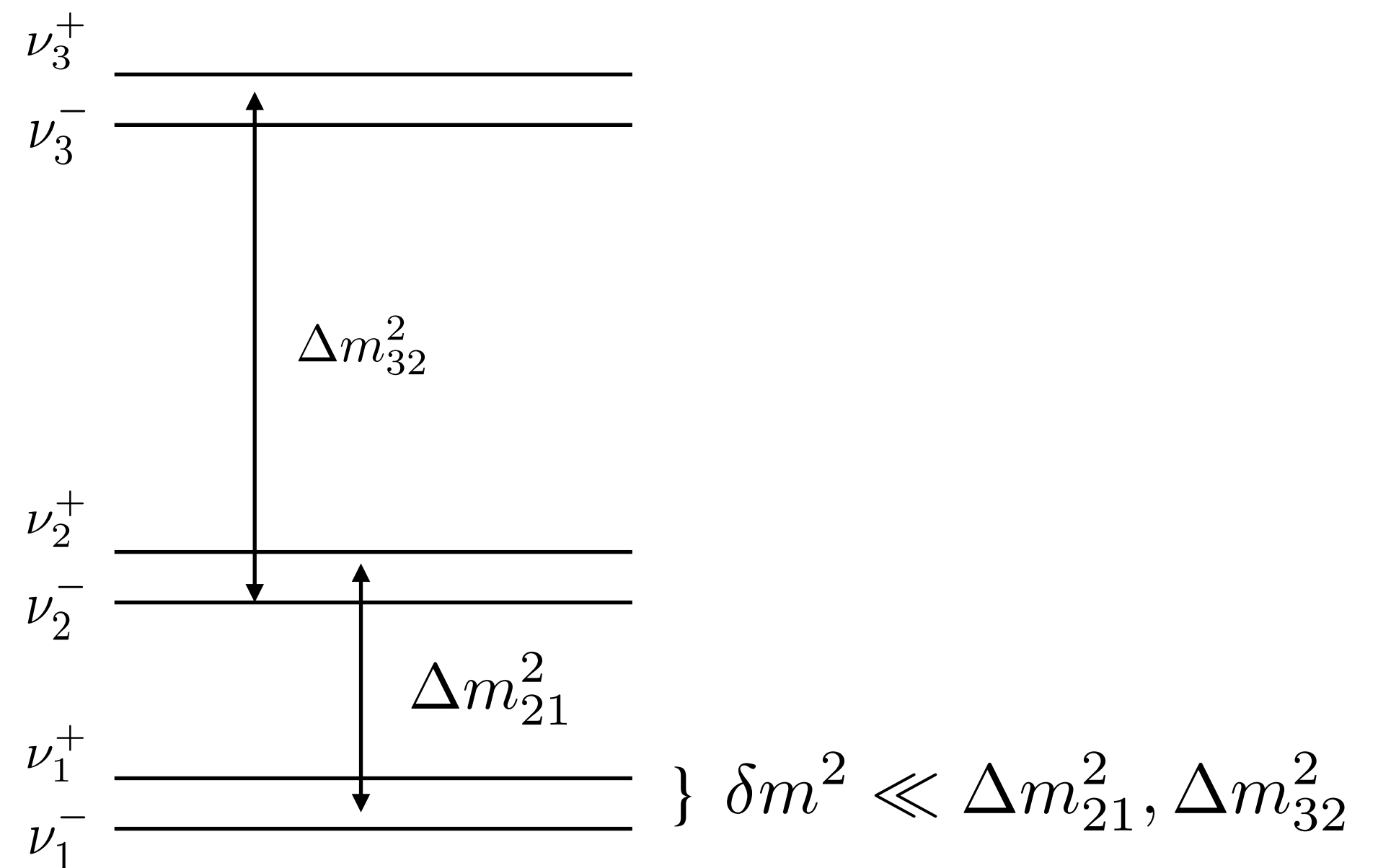
$$M = \begin{pmatrix} 0_3 & m_D \\ m_D & M_N \end{pmatrix}$$

- $M_N = 0 \rightarrow$ Dirac neutrinos
- $M_N \gg m_D \rightarrow$ Usual type I seesaw
- $M_N \ll m_D \rightarrow$ PseudoDirac neutrinos

$$\nu_{\alpha L} = \frac{1}{\sqrt{2}} U_{\alpha j} (\nu_j^+ + i \nu_j^-)$$

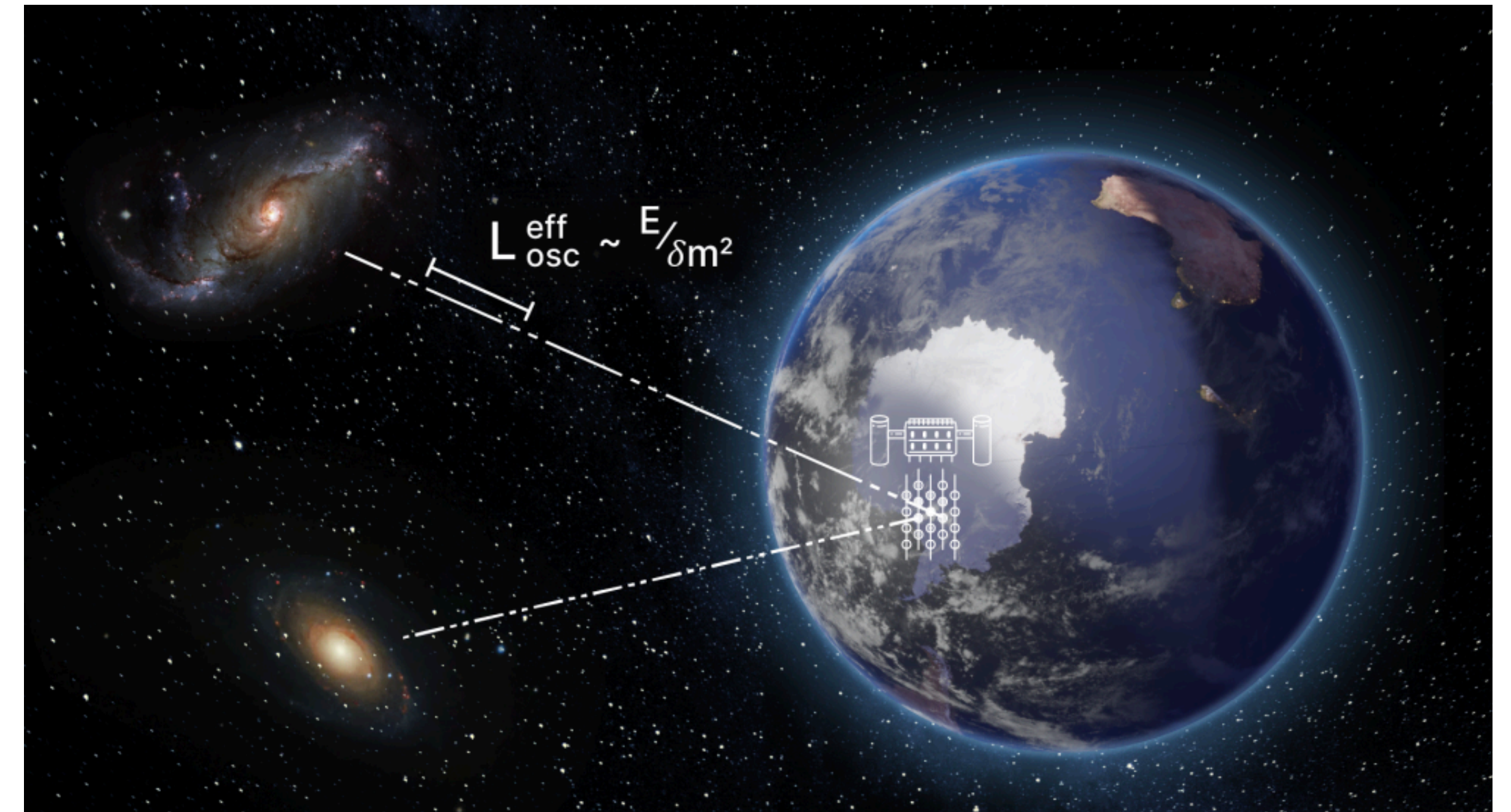
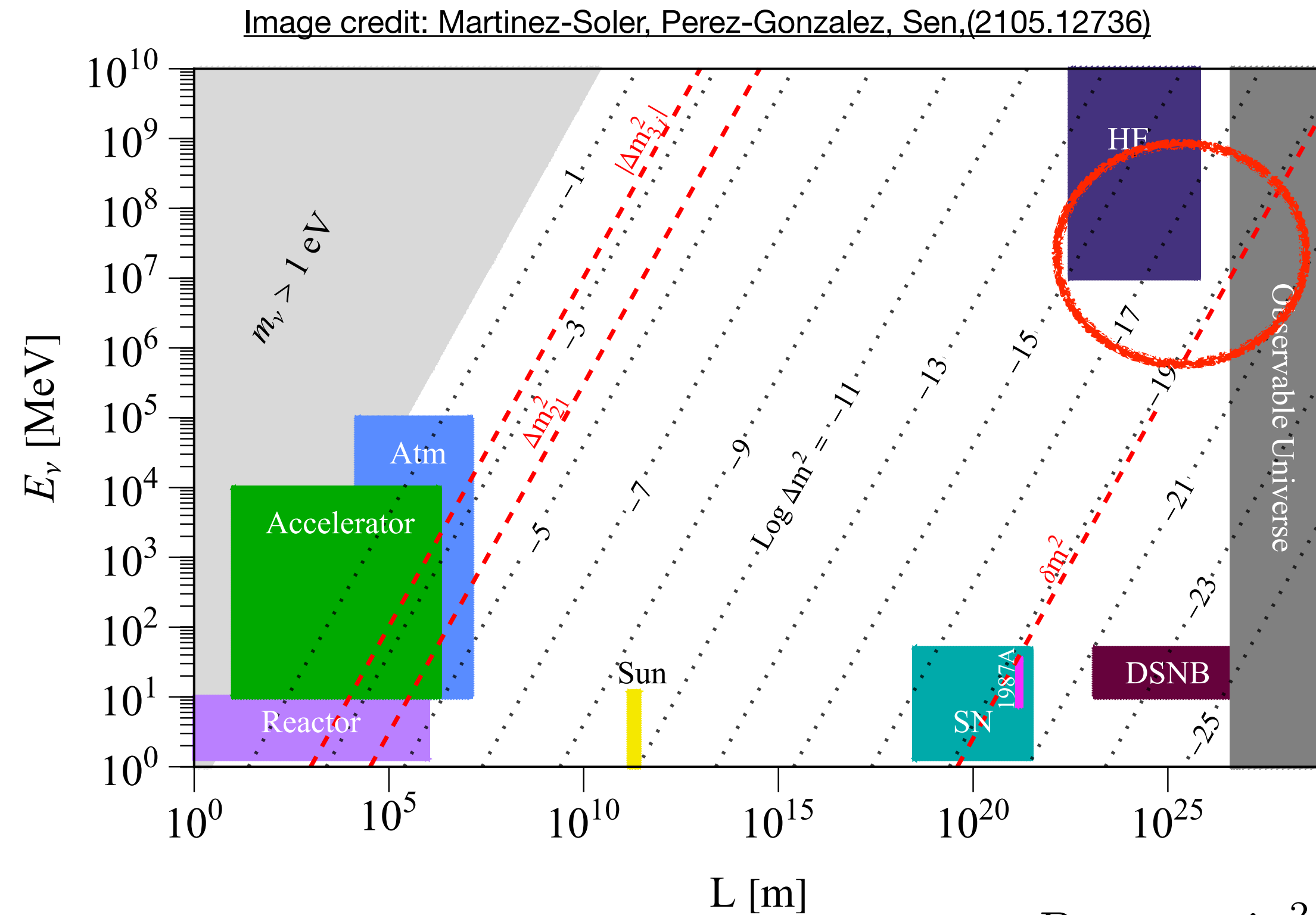
Flavour $\nu_{\alpha L}$ (indicated by a red arrow pointing to the left-hand side)

Mass $(\nu_j^+ + i \nu_j^-)$ (indicated by a blue arrow pointing to the right-hand side)





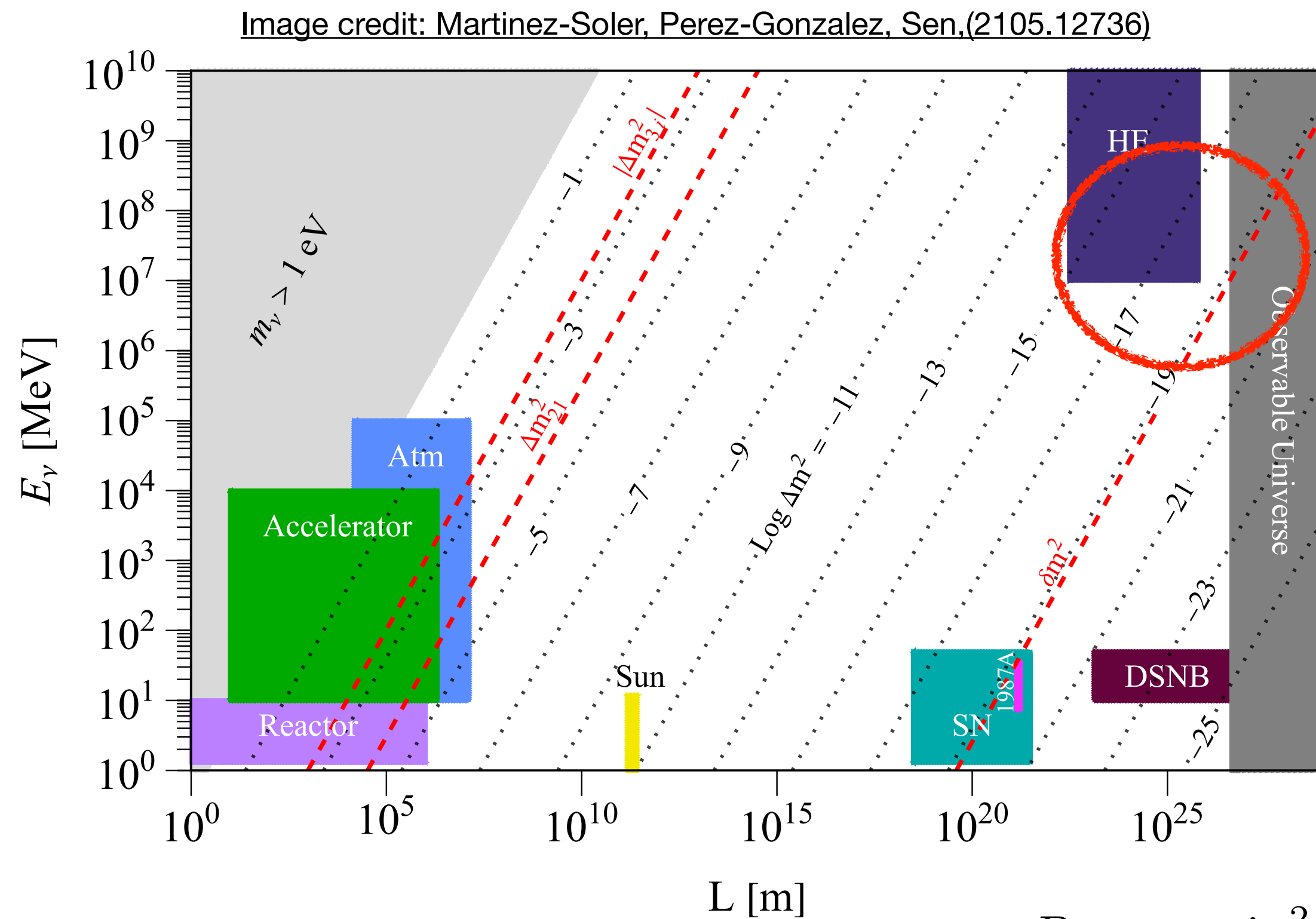
- [2212.00737](#) explore how the pseudo-Dirac neutrino scenario could be probed by observations of extragalactic neutrinos at IceCube
- Perform joint fit of NGC 1068 (14.4 MPc, 4.4×10^{20} km), PKS 1424+240 (1.4 Gpc) and TXS 0506+056 (1.16 Gpc)



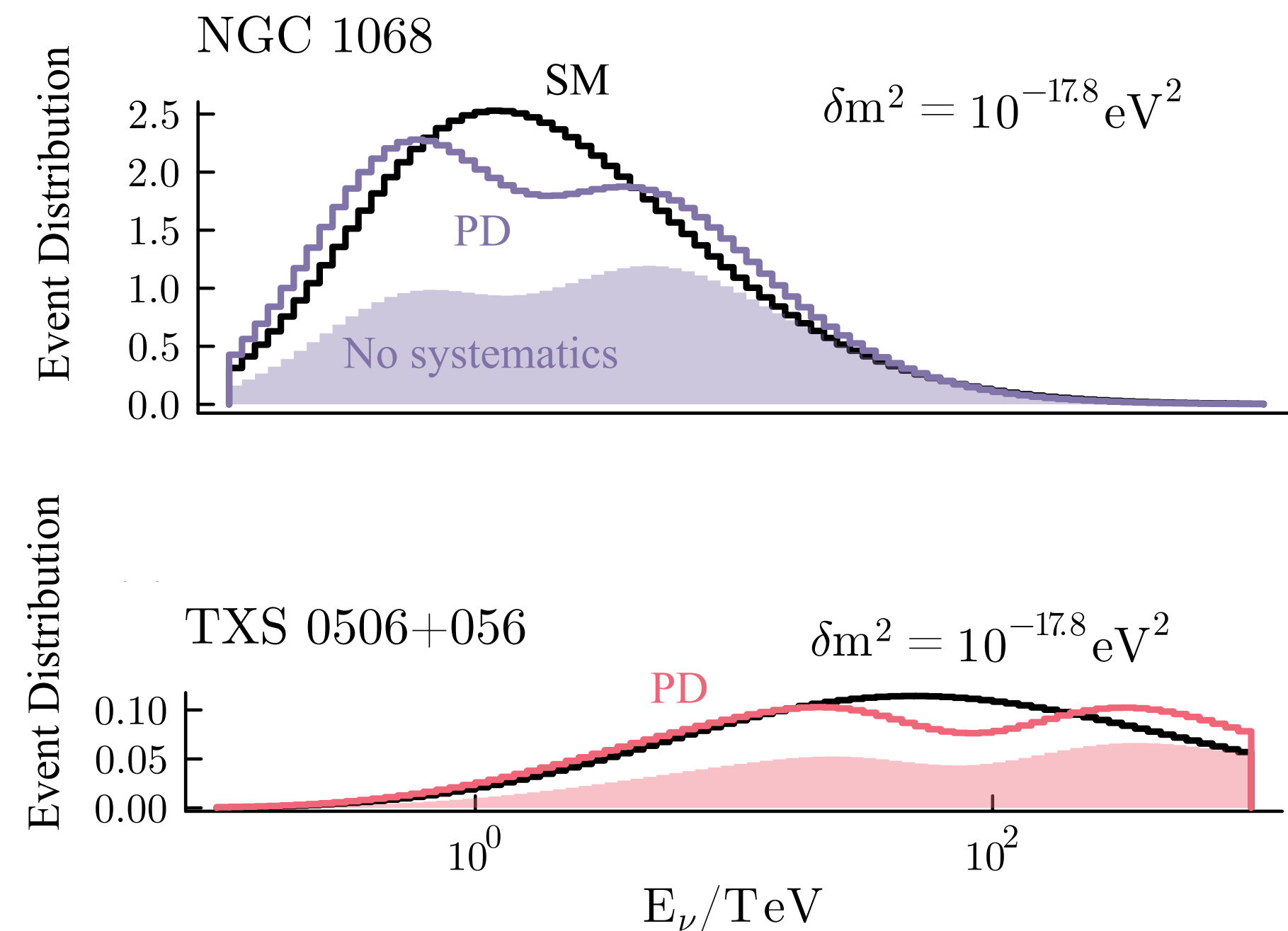
$$P_{\alpha \rightarrow \beta} = \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)$$



- [2212.00737](#) explore how the pseudo-Dirac neutrino scenario could be probed by observations of extragalactic neutrinos at IceCube
- Perform joint fit of NGC 1068 (14.4 Mpc, 4.4×10^{20} km), PKS 1424+240 (1.4 Gpc) and TXS 0506+056 (1.16 Gpc)

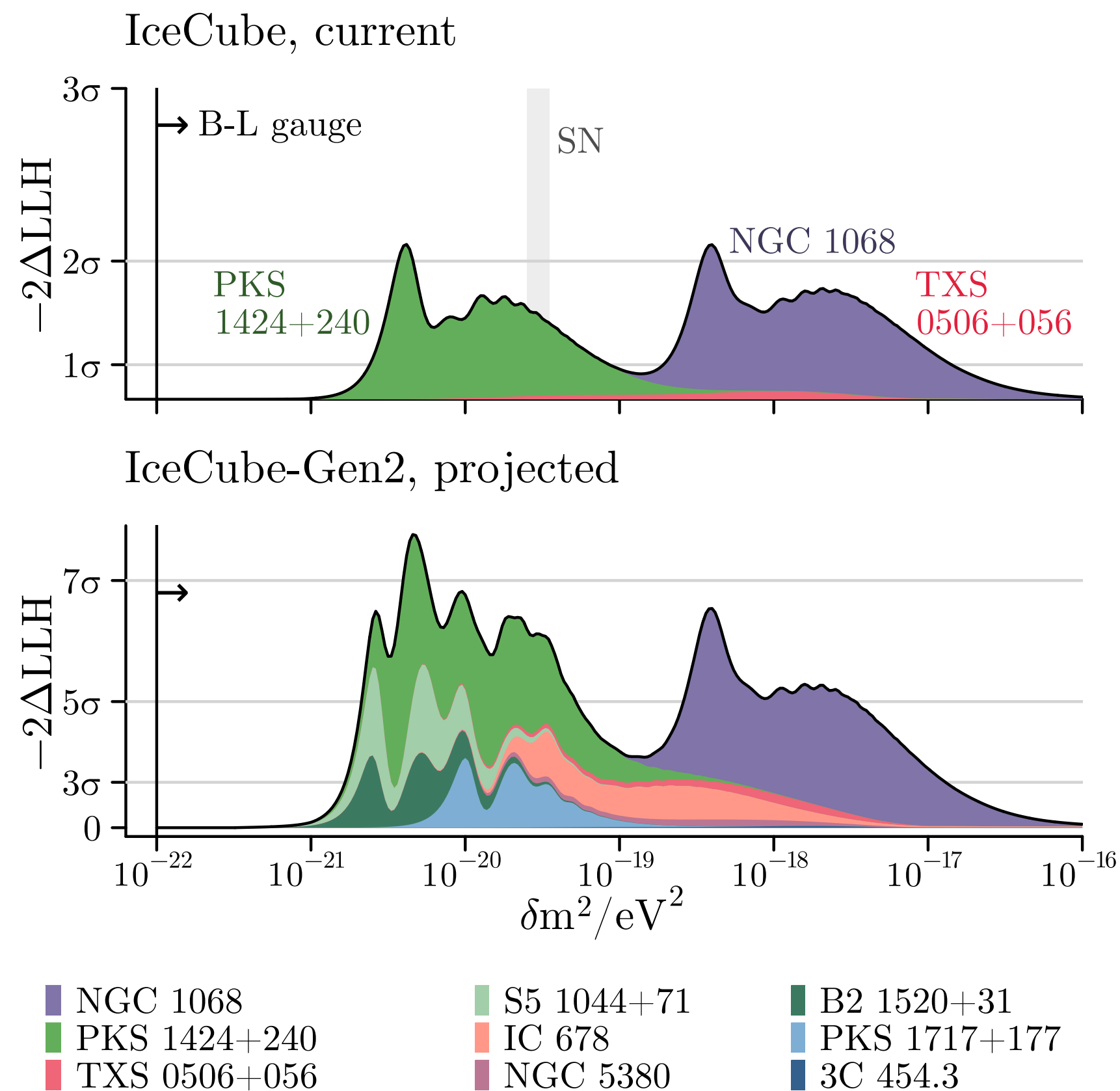


$$P_{\alpha \rightarrow \beta} = \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)$$



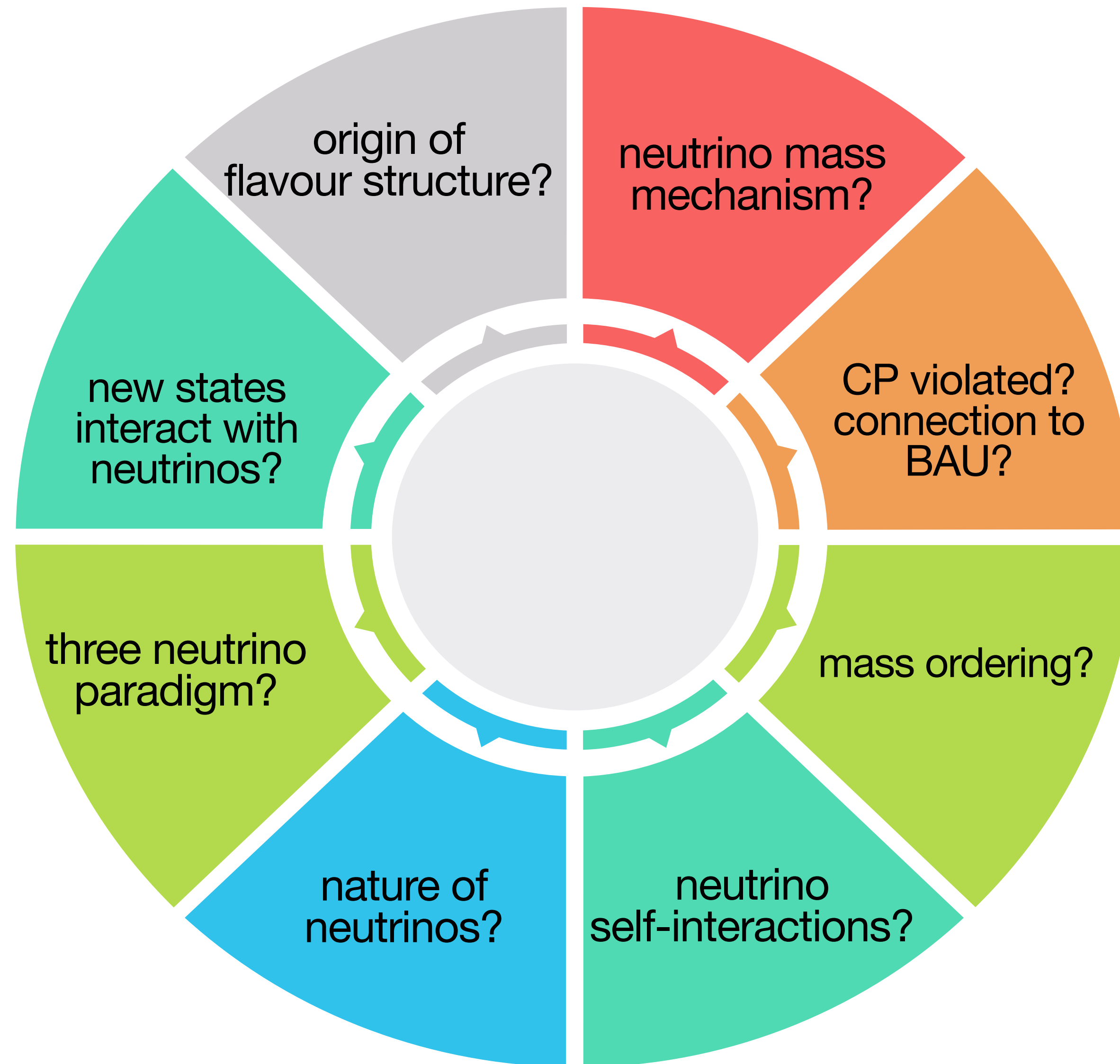


- 2212.00737 explore how the pseudo-Dirac neutrino scenario could be probed by observations of extragalactic neutrinos at IceCube
- Perform joint fit of NGC 1068 (14.4 MPc, 4.4×10^{20} km), PKS 1424+240 (1.4 Gpc) and TXS 0506+056 (1.16 Gpc)

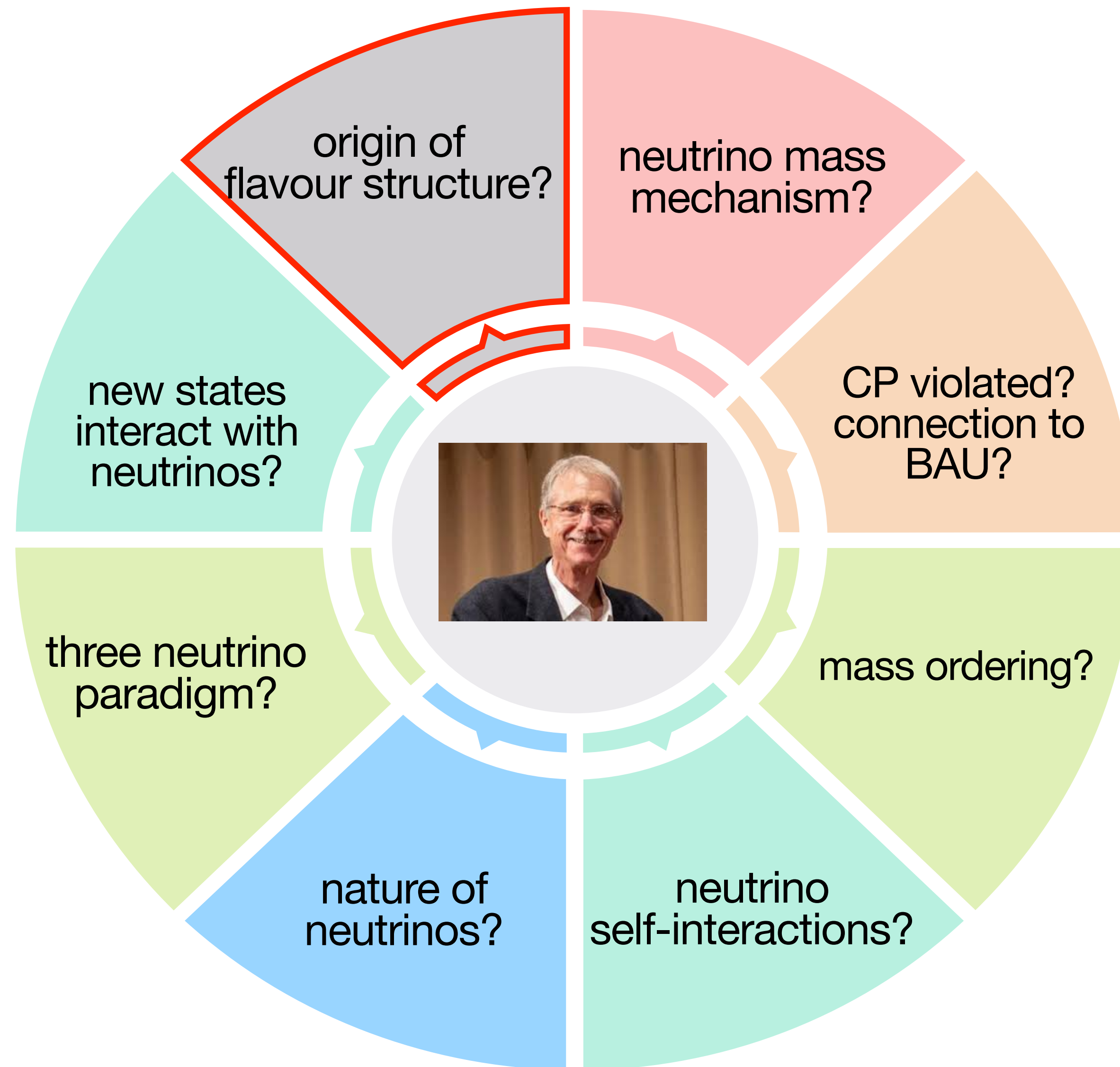


- IceCube probes Pseudo-Dirac neutrinos but limited low statistics & energy resolution
- Gen 2: more sources and 8× higher statistics, achieve 5σ $10^{-21} < \delta m^2 (eV^2) < 10^{-18}$
- IceCube's discovery of astrophysical neutrinos opens new avenues for exploring neutrino physics

Neutrinos: what we don't know



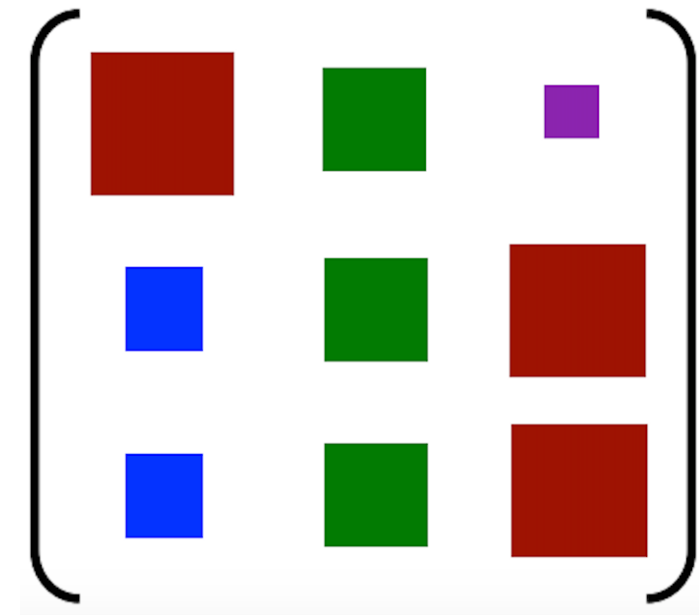
Neutrinos: what we don't know



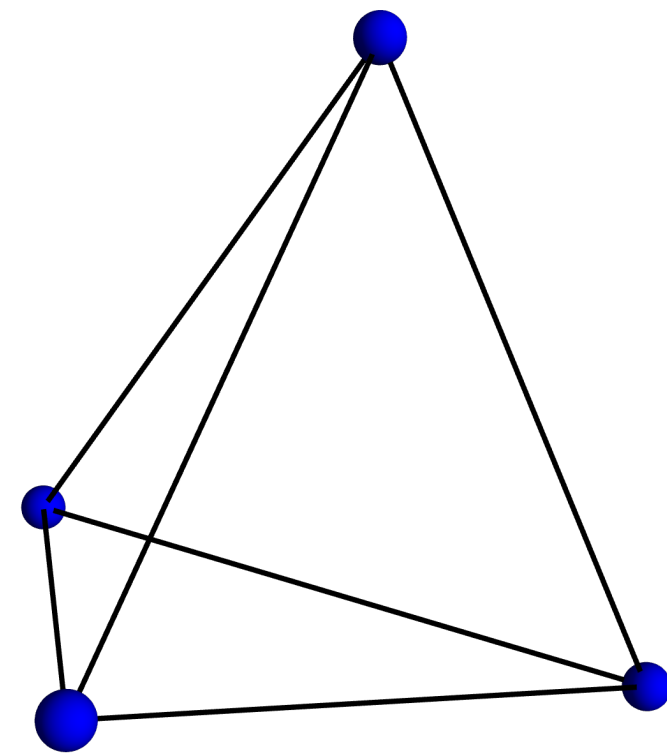
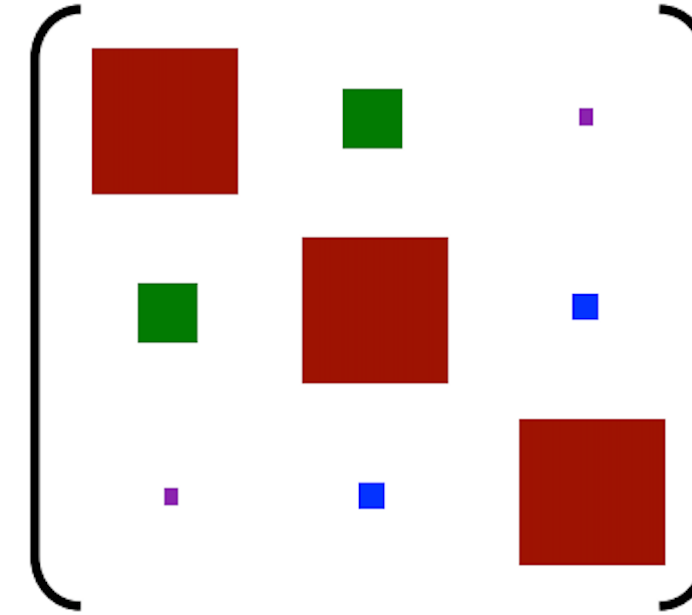


- 2307.13895 studies of neutrino mixing sum rules from discrete symmetries and Littlest Seesaw (LS) models.

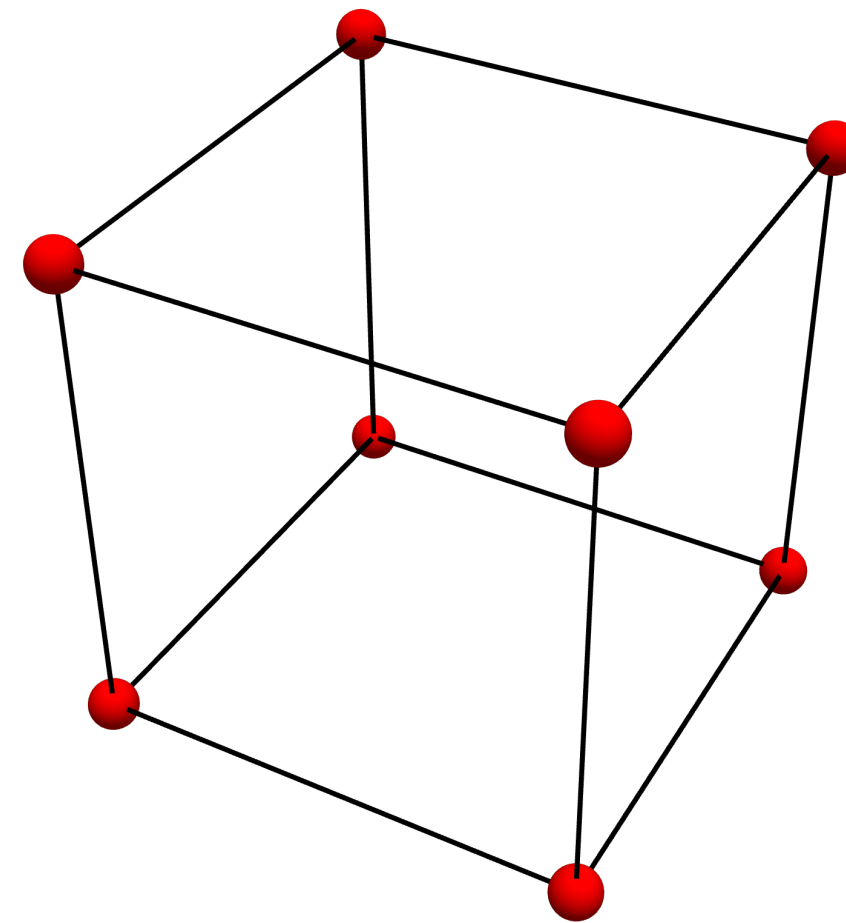
leptonic mixing



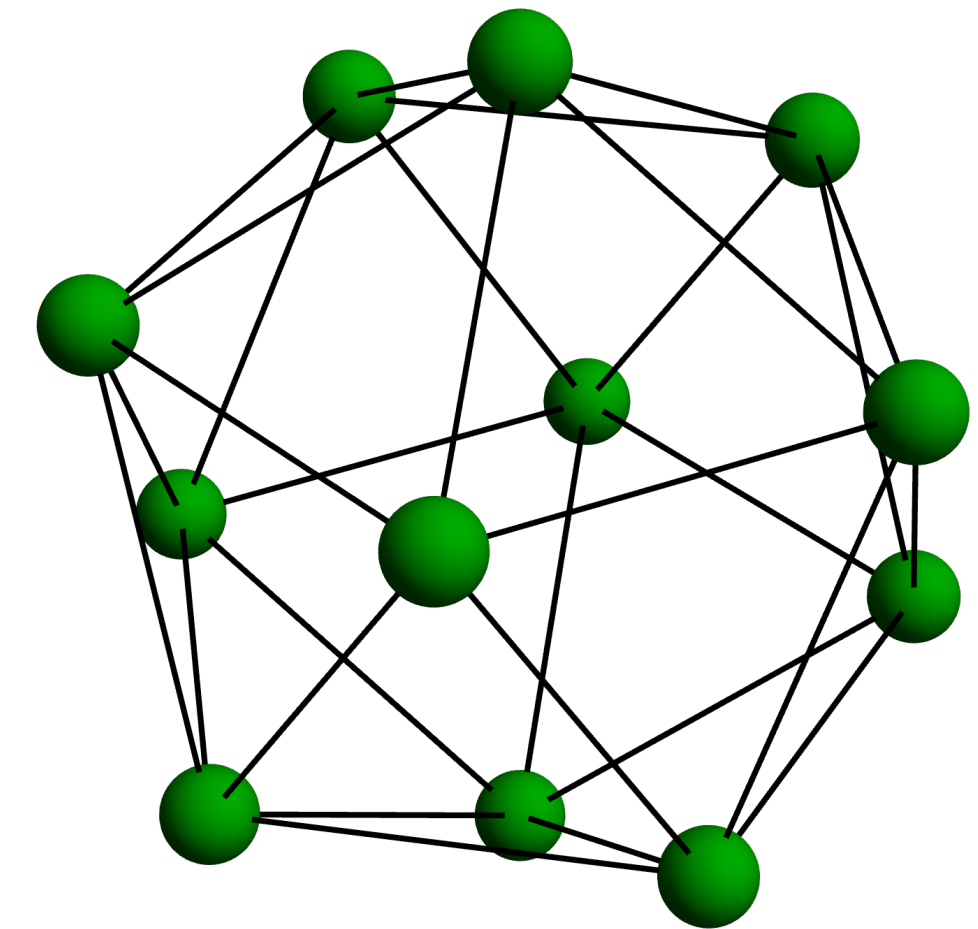
quark mixing



A_4



S_4

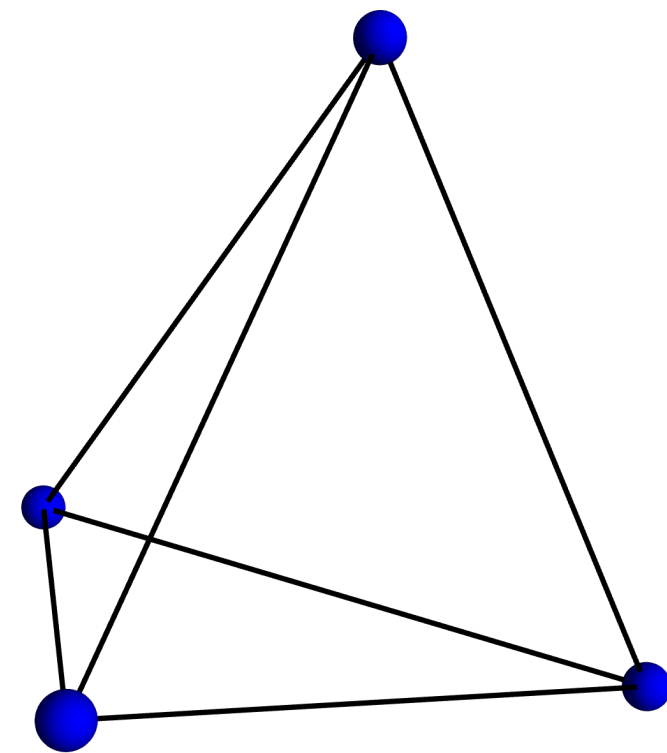
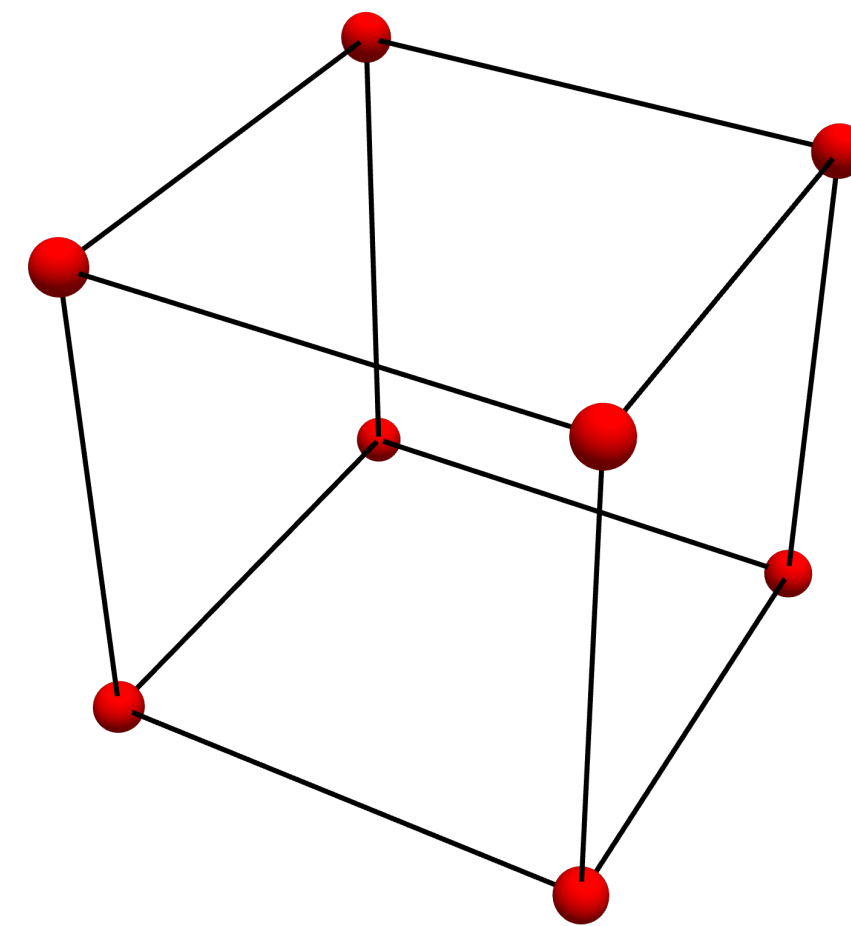
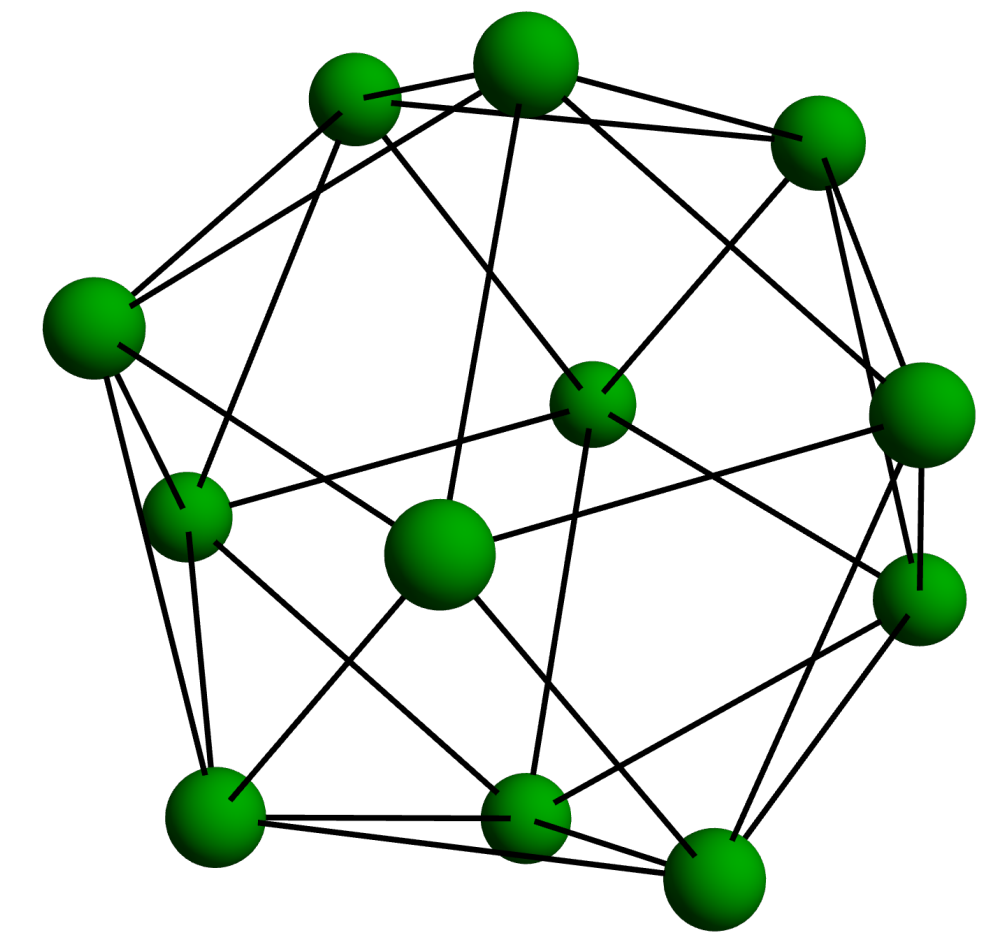


A_5



- 2307.13895 studies of neutrino mixing sum rules from discrete symmetries and Littlest Seesaw (LS) models.

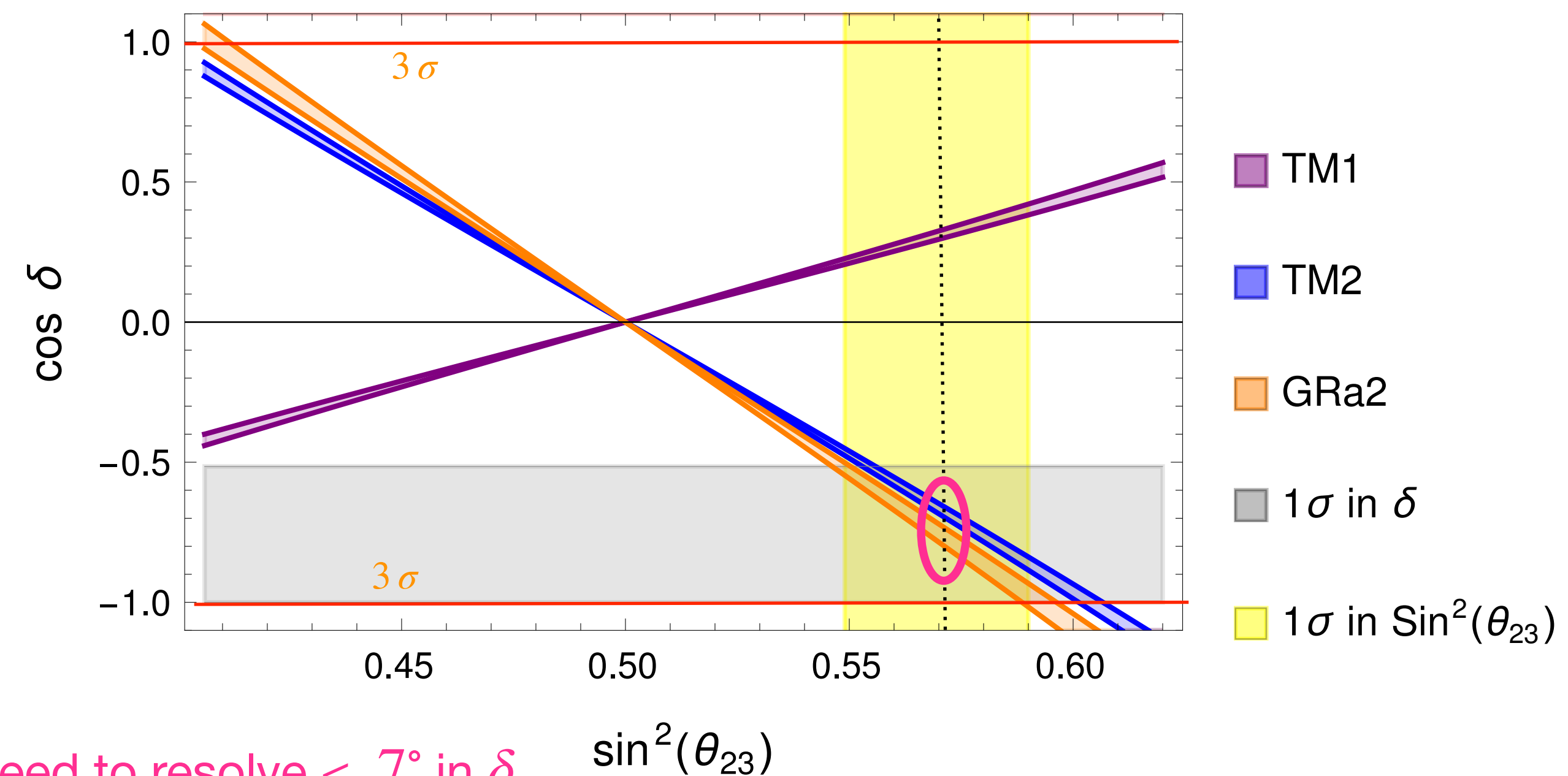
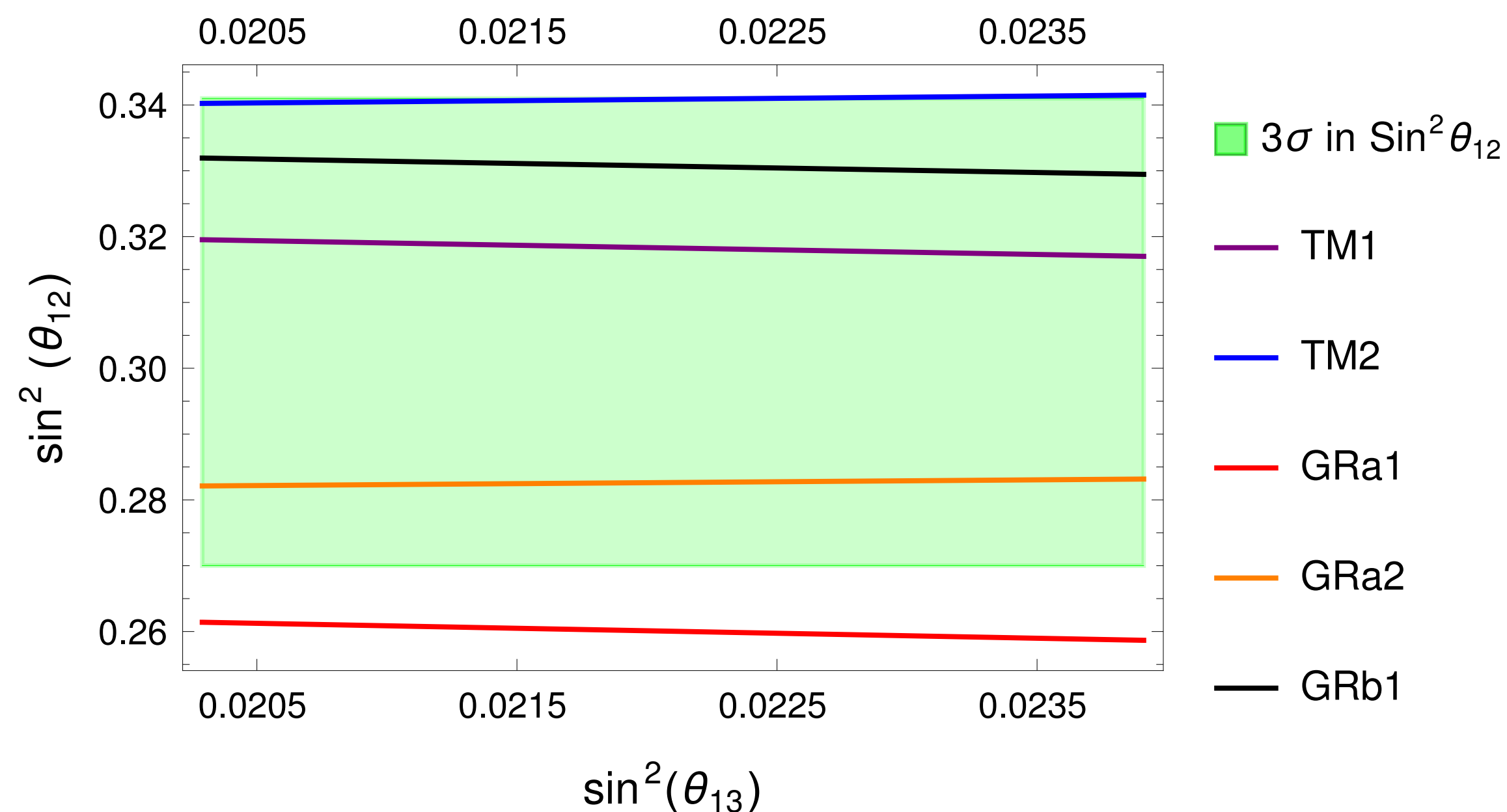
TM1	$\cos \theta_{12} = \sqrt{\frac{2}{3}} \frac{1}{\cos \theta_{13}}$	TM2	$\sin \theta_{12} = \frac{1}{\sqrt{3} \cos \theta_{13}}$
BM1	$\cos \theta_{12} = \frac{1}{\sqrt{2} \cos \theta_{13}}$	BM2	$\cos \theta_{12} = \frac{1}{\sqrt{2} \cos \theta_{13}}$
GRa1	$\cos \theta_{12} = \frac{\cos \theta}{\cos \theta_{13}}$	GRa2	$\cos \theta_{12} = \frac{\sin \theta}{\cos \theta_{13}}$
GRb1	$\cos \theta_{12} = \frac{1+\sqrt{5}}{4 \cos \theta_{13}}$	GRb2	$\sin \theta_{12} = \frac{\sqrt{5+\sqrt{5}}}{4 \cos \theta_{13}}$
GRc1	$\cos \theta_{12} = \frac{1+\sqrt{5}}{2\sqrt{3} \cos \theta_{13}}$	GRc2	$\sin \theta_{12} = \frac{1+\sqrt{5}}{2\sqrt{3} \cos \theta_{13}}$
HEX1	$\cos \theta_{12} = \frac{\sqrt{3}}{2 \cos \theta_{13}}$	HEX2	$\sin \theta_{12} = \frac{1}{2\sqrt{2} \cos \theta_{13}}$

 A_4  S_4  A_5



- 2307.13895 studies of neutrino mixing sum rules from discrete symmetries and Littlest Seesaw (LS) models.

TM1	$\cos \theta_{12} = \sqrt{\frac{2}{3}} \frac{1}{\cos \theta_{13}}$	TM2	$\sin \theta_{12} = \frac{1}{\sqrt{3} \cos \theta_{13}}$
BM1	$\cos \theta_{12} = \frac{1}{\sqrt{2} \cos \theta_{13}}$	BM2	$\cos \theta_{12} = \frac{1}{\sqrt{2} \cos \theta_{13}}$
GRa1	$\cos \theta_{12} = \frac{\cos \theta}{\cos \theta_{13}}$	GRa2	$\cos \theta_{12} = \frac{\sin \theta}{\cos \theta_{13}}$
GRb1	$\cos \theta_{12} = \frac{1+\sqrt{5}}{4 \cos \theta_{13}}$	GRb2	$\sin \theta_{12} = \frac{\sqrt{5+\sqrt{5}}}{4 \cos \theta_{13}}$
GRc1	$\cos \theta_{12} = \frac{1+\sqrt{5}}{2\sqrt{3} \cos \theta_{13}}$	GRc2	$\sin \theta_{12} = \frac{1+\sqrt{5}}{2\sqrt{3} \cos \theta_{13}}$
HEX1	$\cos \theta_{12} = \frac{\sqrt{3}}{2 \cos \theta_{13}}$	HEX2	$\sin \theta_{12} = \frac{1}{2\sqrt{2} \cos \theta_{13}}$



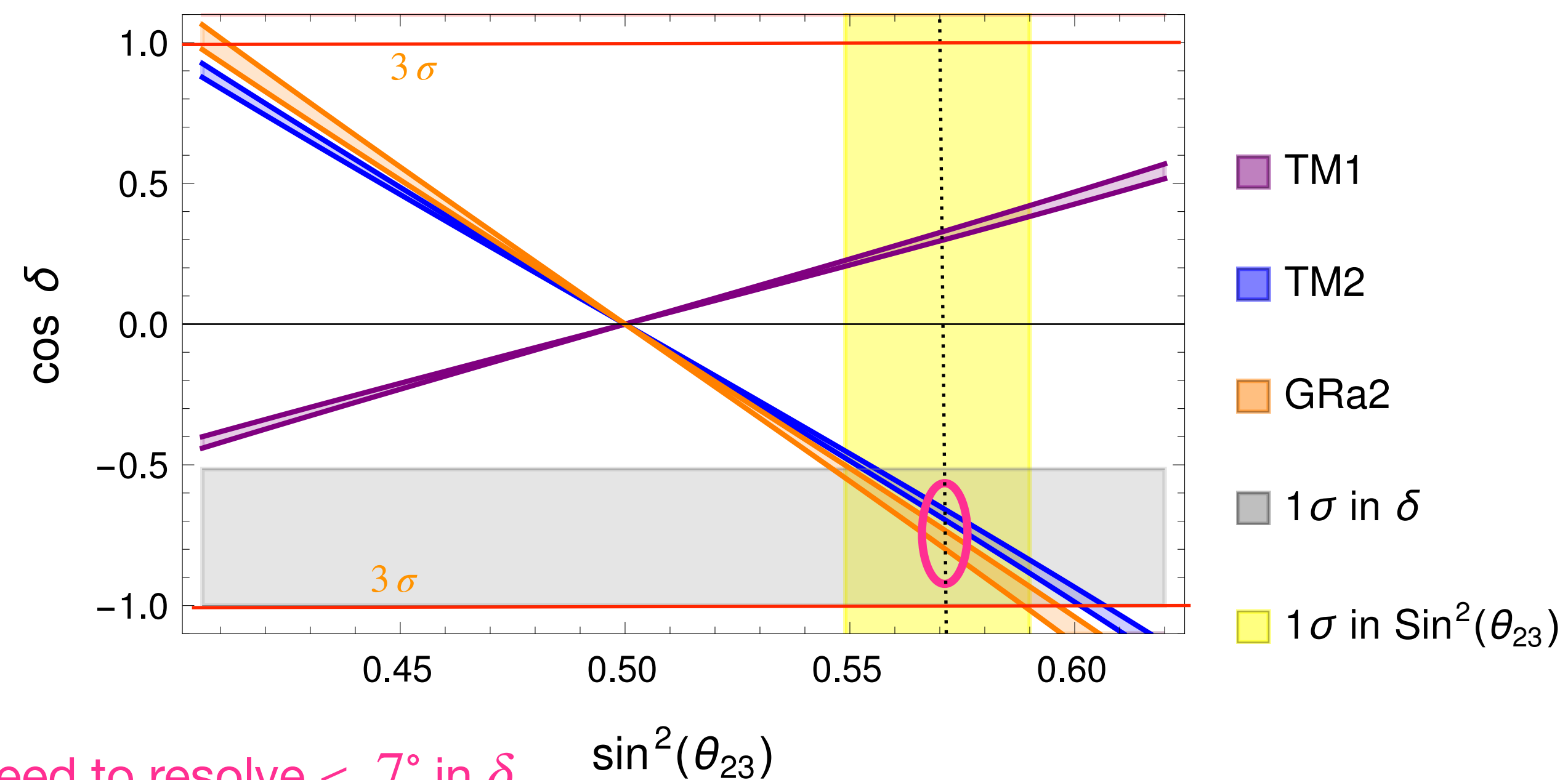
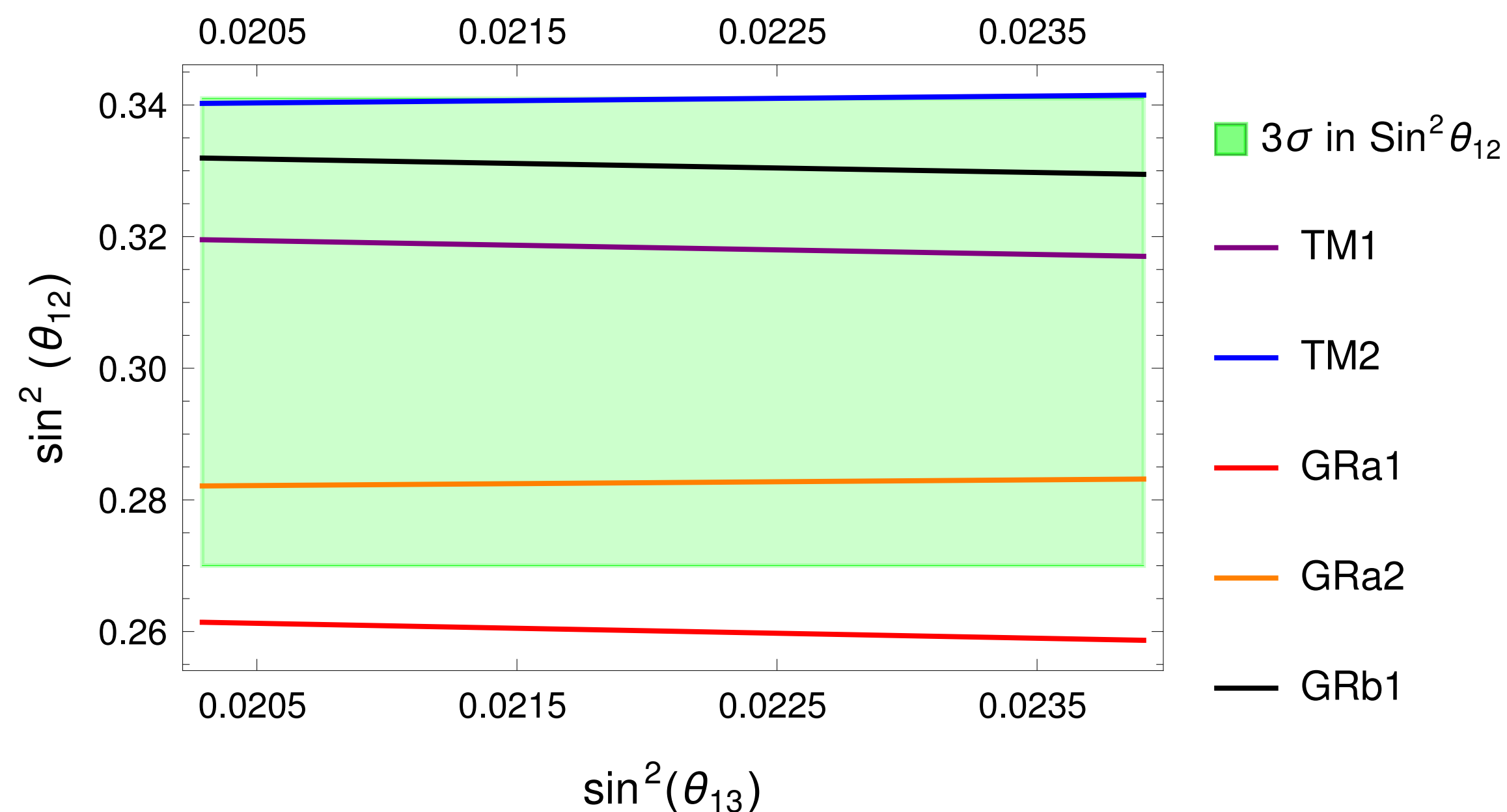
Need to resolve $< 7^\circ$ in δ



- 2307.13895 studies of neutrino mixing sum rules from discrete symmetries and Littlest Seesaw (LS) models.

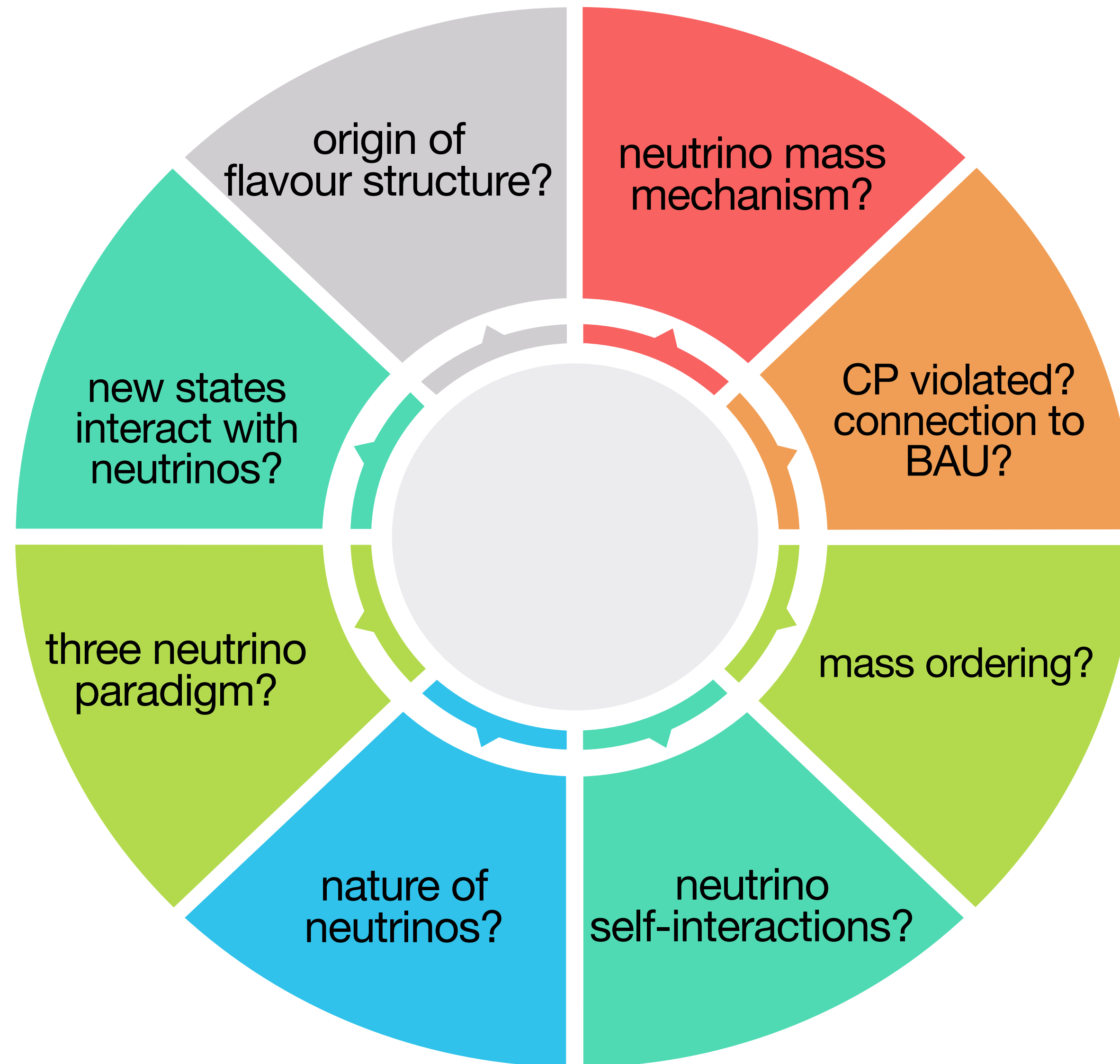
TM1	$\cos \theta_{12} = \sqrt{\frac{2}{3}} \frac{1}{\cos \theta_{13}}$	TM2	$\sin \theta_{12} = \frac{1}{\sqrt{3} \cos \theta_{13}}$
BM1	$\cos \theta_{12} = \frac{1}{\sqrt{2} \cos \theta_{13}}$	BM2	$\cos \theta_{12} = \frac{1}{\sqrt{2} \cos \theta_{13}}$
GRa1	$\cos \theta_{12} = \frac{\cos \theta}{\cos \theta_{13}}$	GRa2	$\cos \theta_{12} = \frac{\sin \theta}{\cos \theta_{13}}$
GRb1	$\cos \theta_{12} = \frac{1+\sqrt{5}}{4 \cos \theta_{13}}$	GRb2	$\sin \theta_{12} = \frac{\sqrt{5+\sqrt{5}}}{4 \cos \theta_{13}}$
GRc1	$\cos \theta_{12} = \frac{1+\sqrt{5}}{2\sqrt{3} \cos \theta_{13}}$	GRc2	$\sin \theta_{12} = \frac{1+\sqrt{5}}{2\sqrt{3} \cos \theta_{13}}$
HEX1	$\cos \theta_{12} = \frac{\sqrt{3}}{2 \cos \theta_{13}}$	HEX2	$\sin \theta_{12} = \frac{1}{2\sqrt{2} \cos \theta_{13}}$

- Future data, especially improved measurements δ & θ_{23} , will reduce # viable flavour models & lead to a deeper understanding of the flavour problem

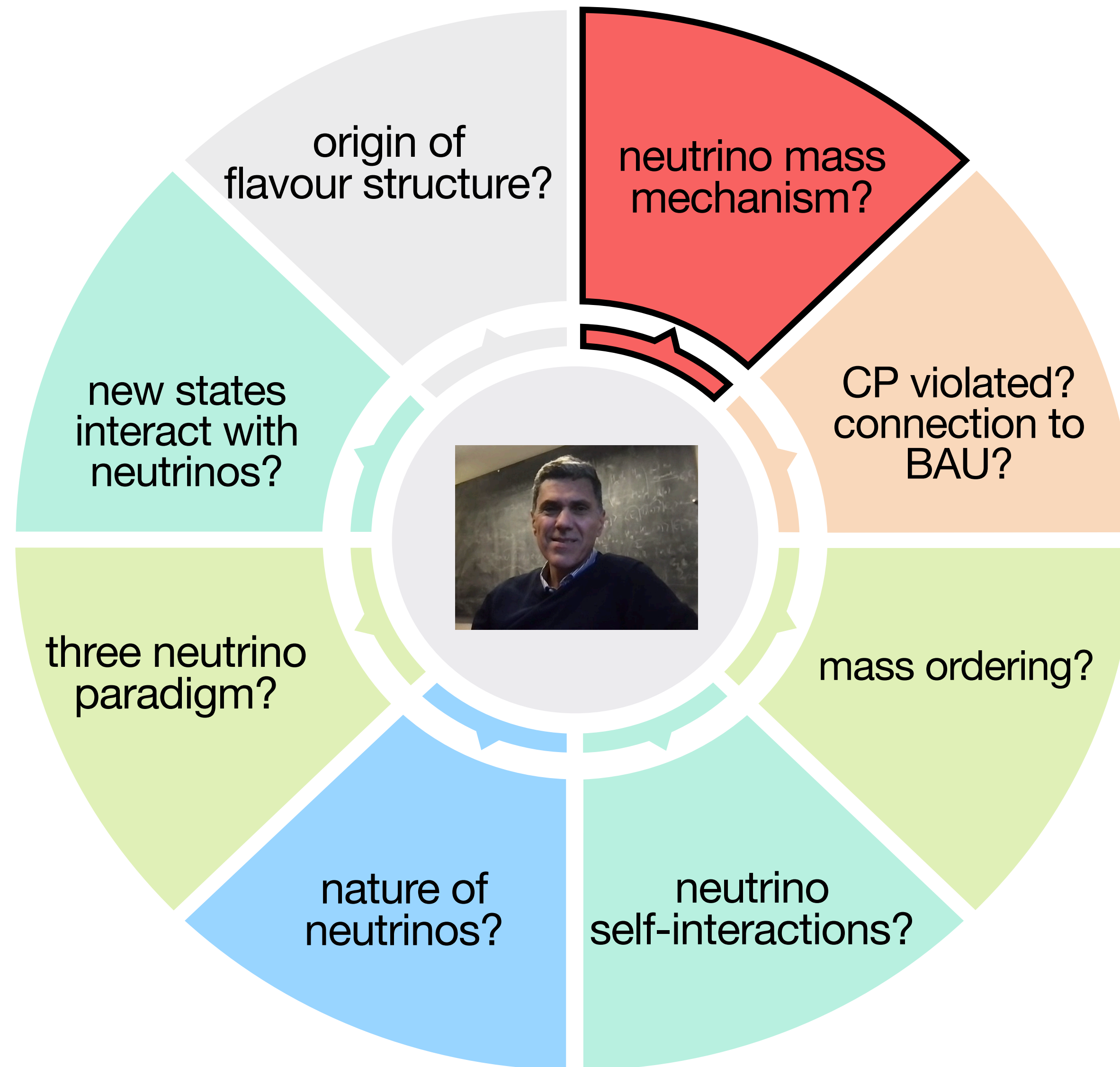


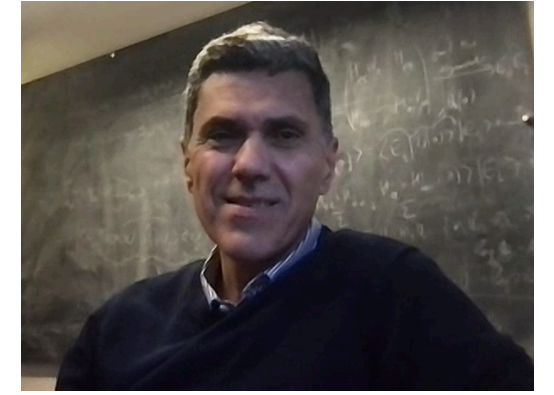
Need to resolve $< 7^\circ$ in δ

Neutrinos: what we don't know



Neutrinos: what we don't know





- 2307.03184 investigates how majoron model can alleviate cosmological tensions and help explain the PTA signal

- RHNs acquire mass from majoron getting a VEV. In multiple majoron model each RHN generation associated with majoron

$$\mathcal{L} = Y_{\alpha I} \overline{L}_{\alpha} N_I \tilde{\Phi} + Y_{\alpha I'} \overline{L}_{\alpha} N_{I'} \tilde{\Phi} + \frac{\lambda_I}{2} \phi \overline{N}_I^c N_I + \frac{\lambda_{I'}}{2} \phi' \overline{N}_{I'}^c N_{I'} \quad \xrightarrow{\text{Seesaw mechanism}} \quad m_{\nu} = \frac{v_{\text{ew}}^2}{2} \frac{Y_{\alpha I} Y_{\beta I}}{M_I}$$

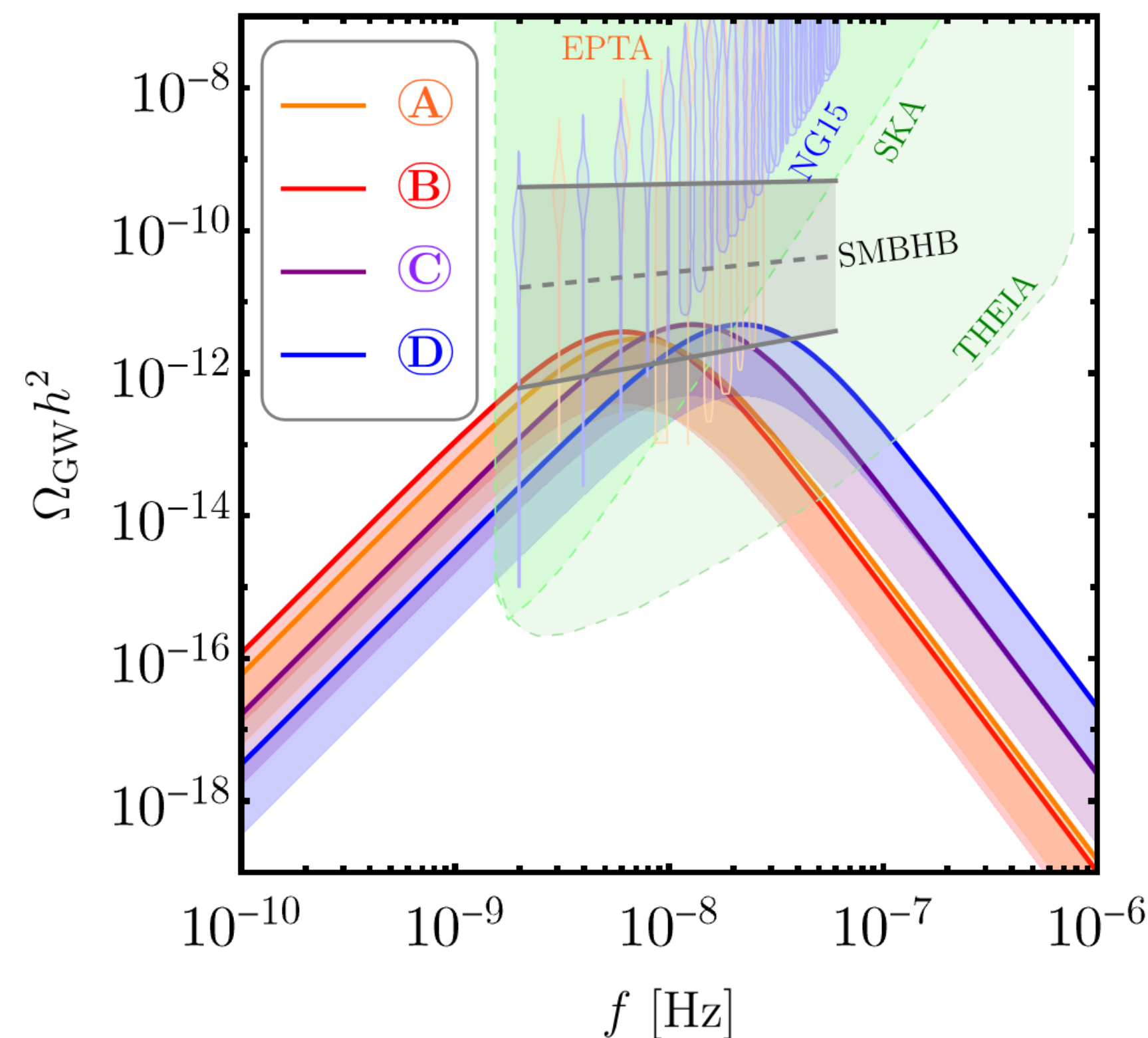
- RHNs acquire mass from majoron getting a VEV. In multiple majoron model each RHN generation associated with majoron



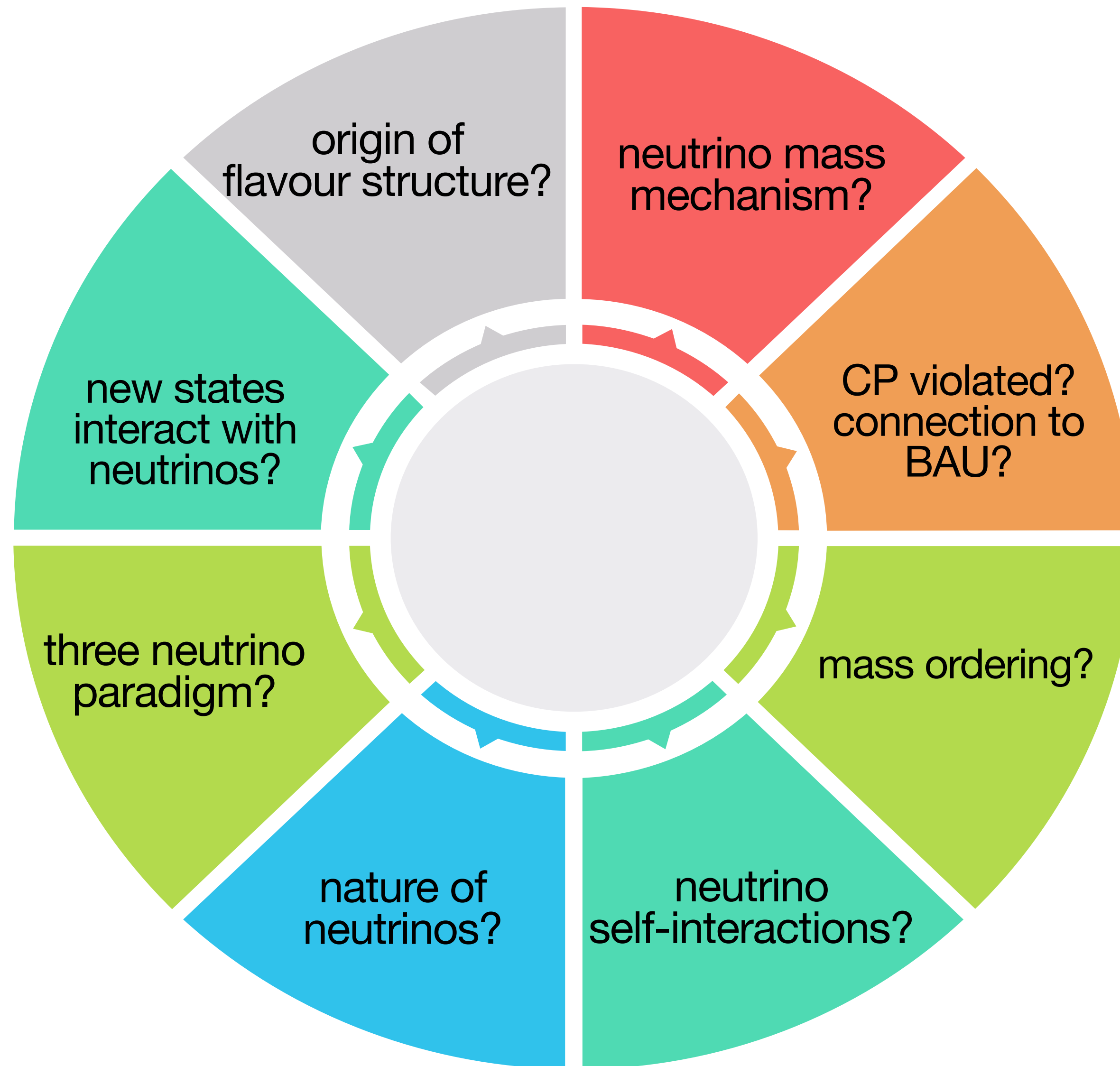
- [2307.03184](#) investigates how majoron model can alleviate cosmological tensions and help explain the PTA signal
- Cosmological tensions: Hubble tension & Deuterium problem can be Alleviated by present of majorons after neutrino decoupling

- ϕ undergoes first-order PT at $T > T_{ew}$ & ϕ' at $T \sim \text{MeV}$

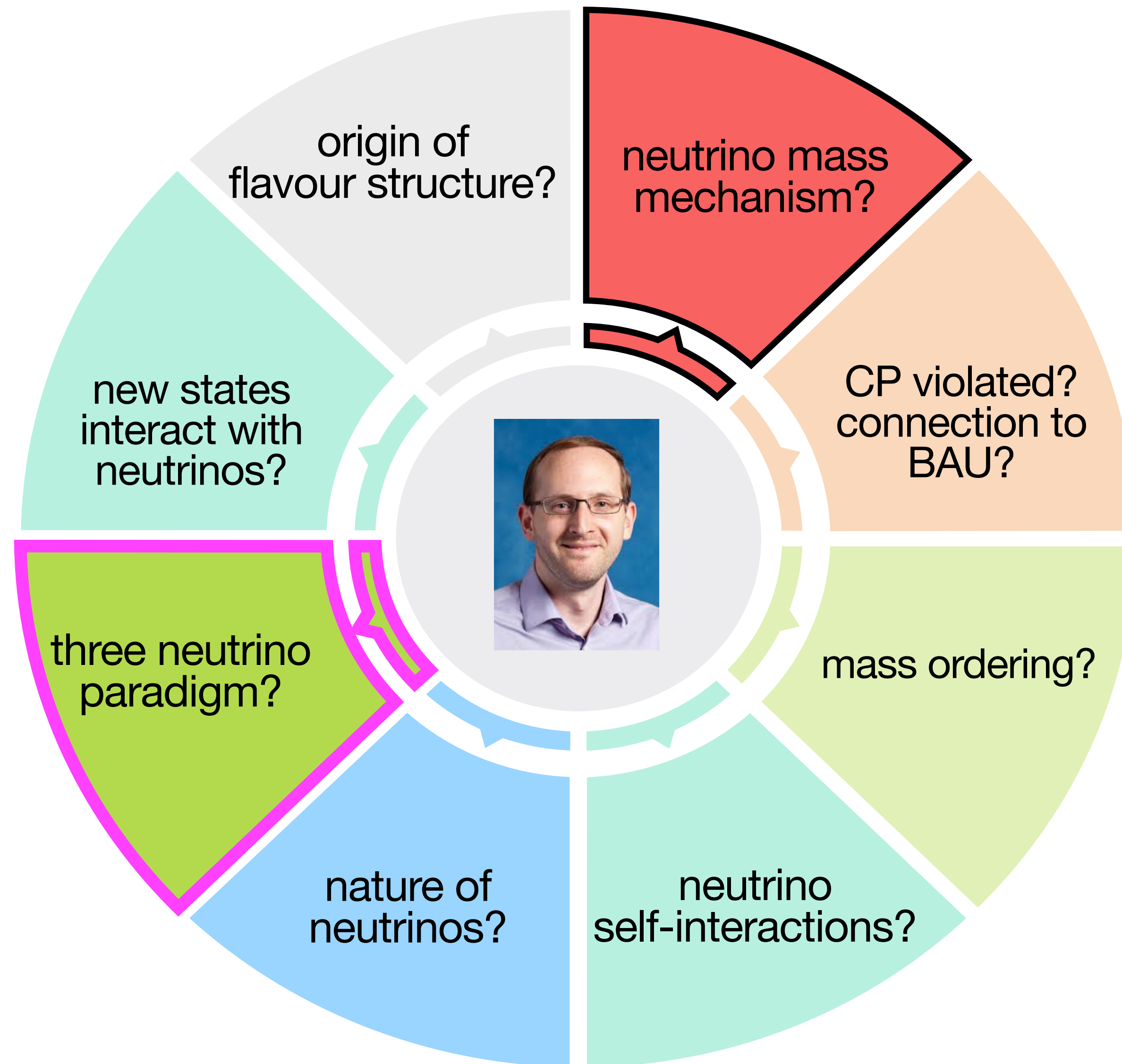
- MeV scale PT \rightarrow nano-Hertz GW signal which can help (in addition to mergers of SMBH) explain PTA signal



Neutrinos: what we don't know

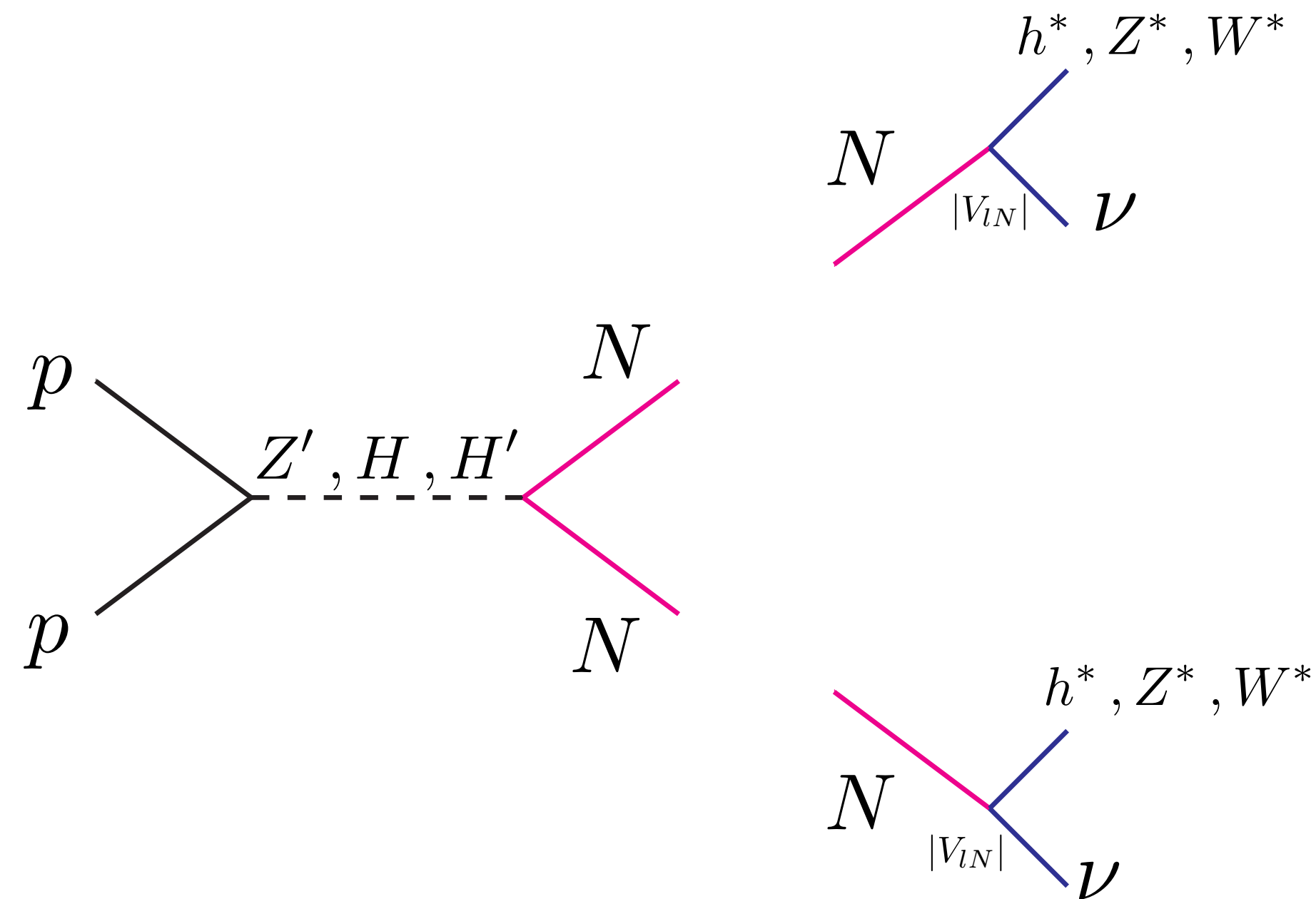


Neutrinos: what we don't know

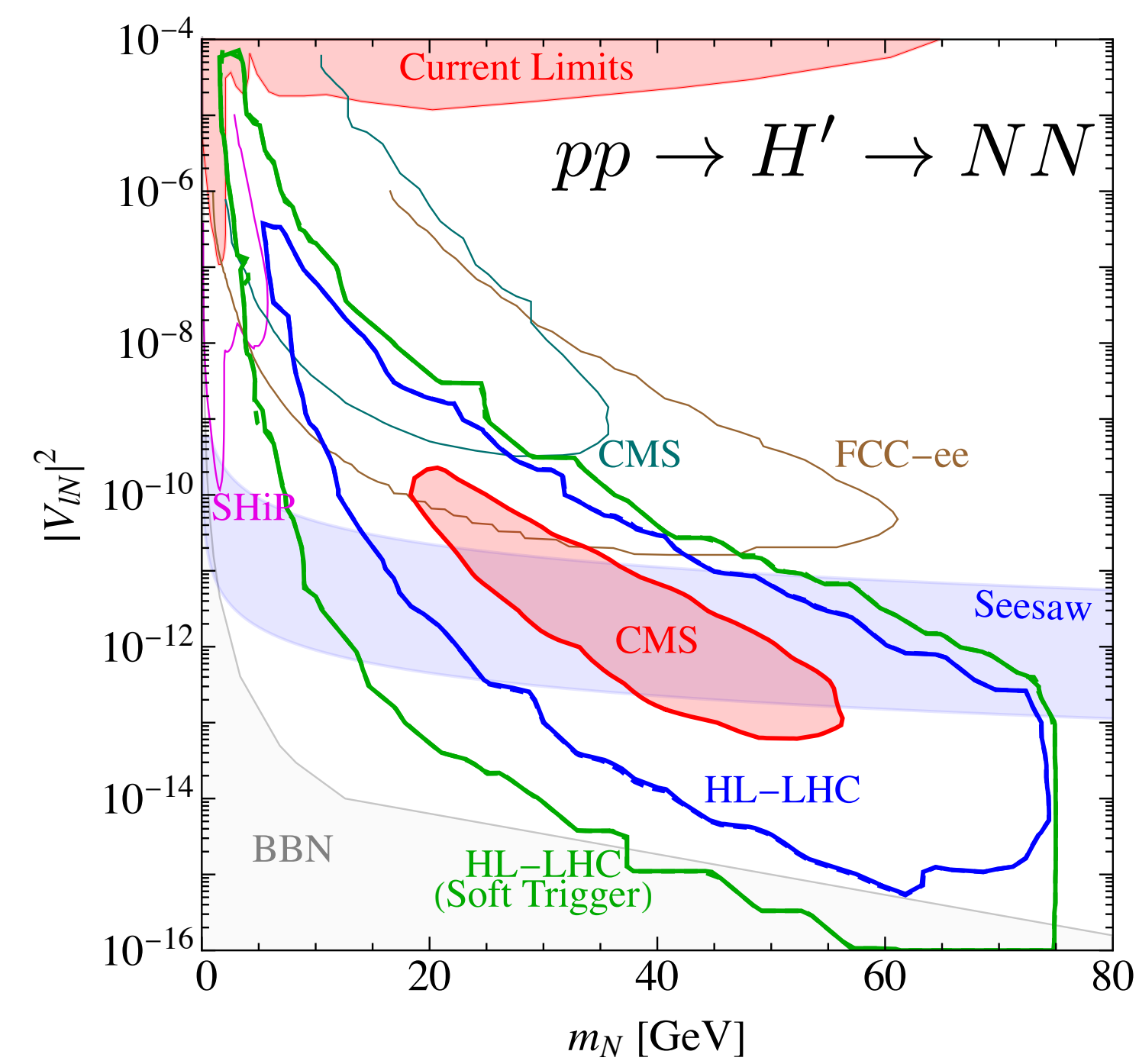
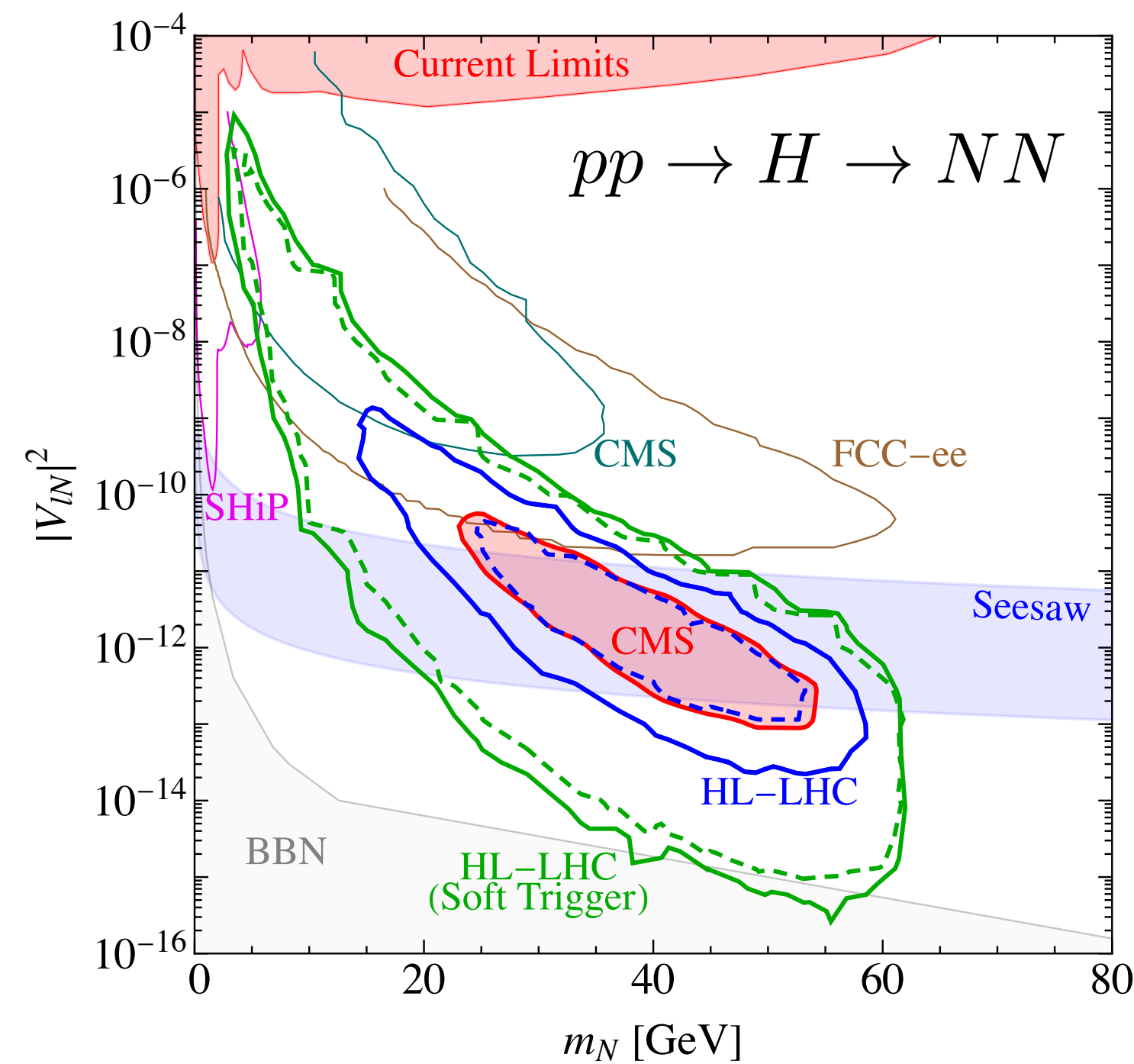




- 2407.20676 investigated breaking of gauge $B - L$ theory lead to GeV-scale RHNs along with exotic Higgs & Z'

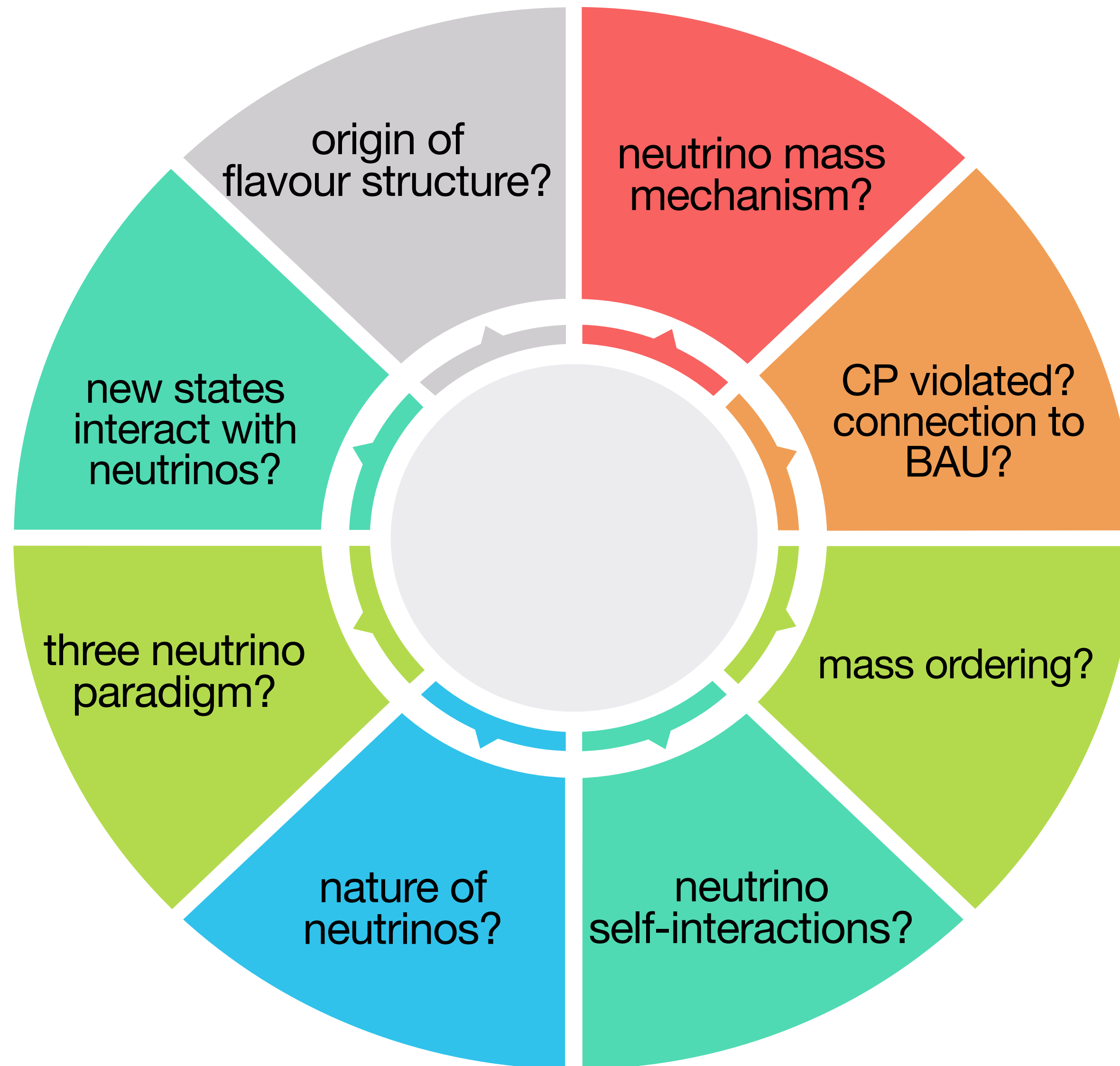


- RHNs produced via pp collision and because mixing to active neutrinos is small \implies displaced vertices (\sim meter scale).
- Focus on a search for displaced showers in the CMS muon system

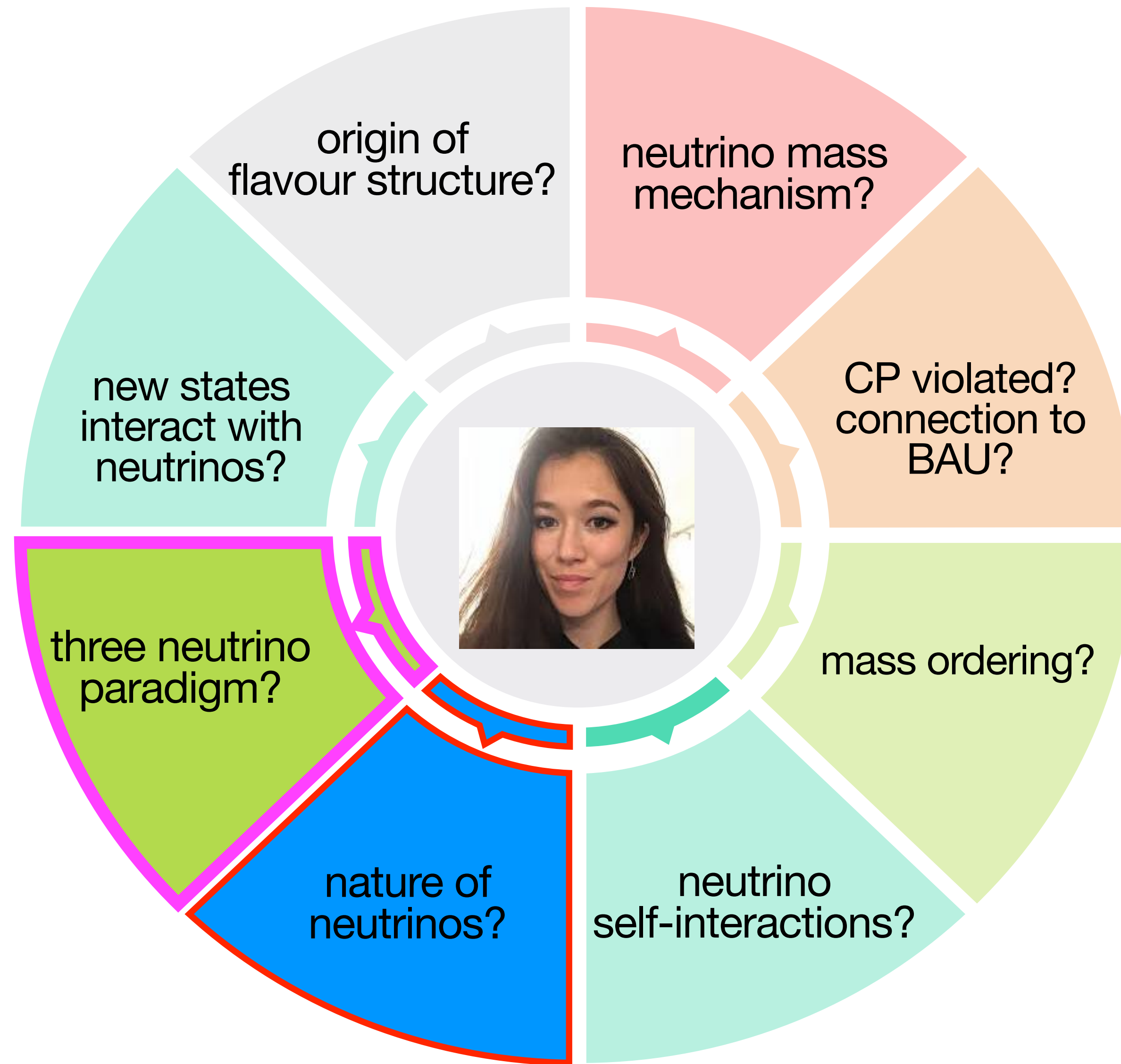


- CMS search for long-lived particles reinterpreted to explore RHNs via Higgs & exotic Higgs portals \implies potential to probe RHN masses around 40 GeV with existing data.
- Current CMS data is already excluding unexplored parameter space in the $B - L$ gauge model, motivating further searches for displaced showers in the muon system to better probe RHN signatures.

Neutrinos: what we don't know

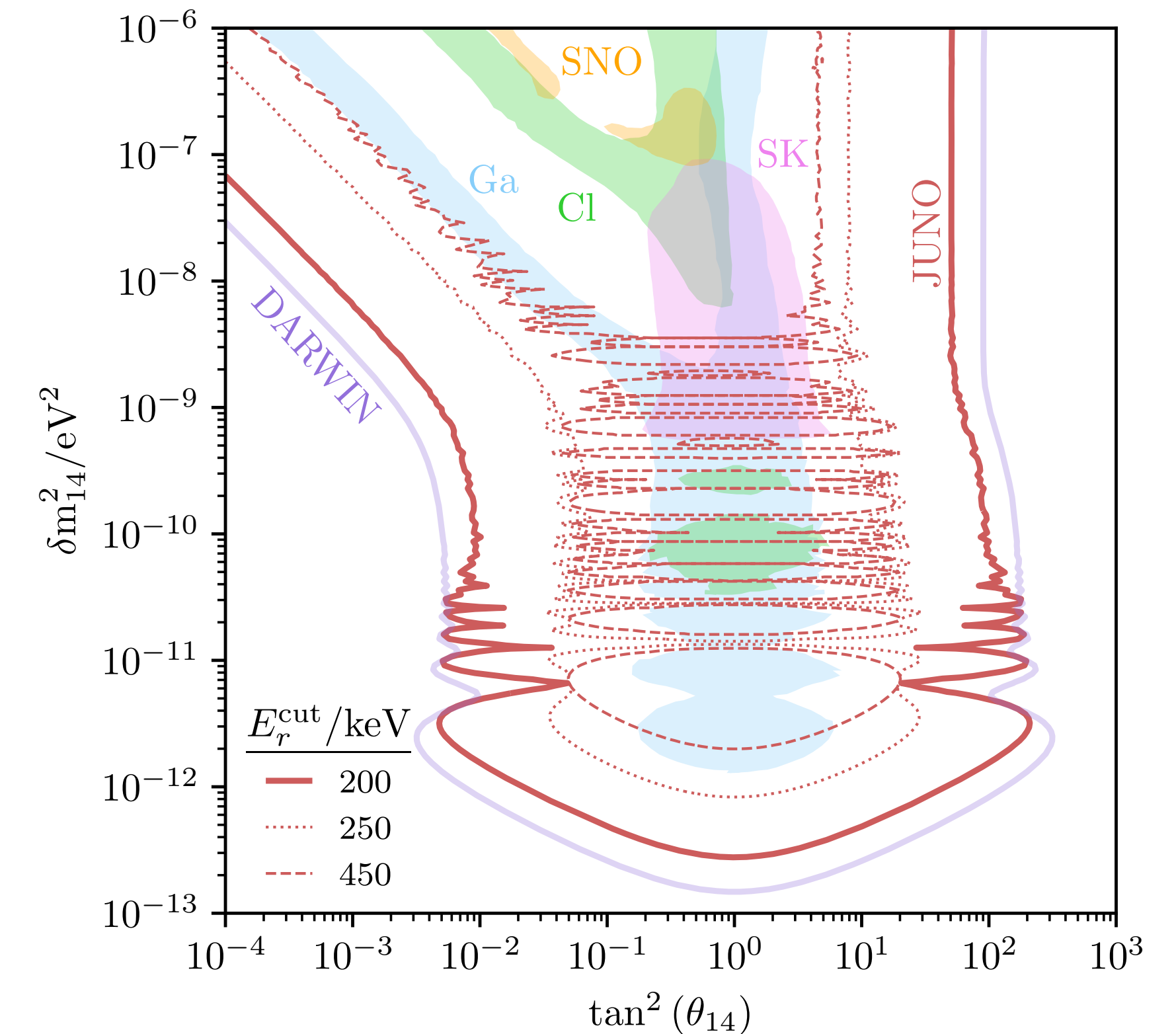
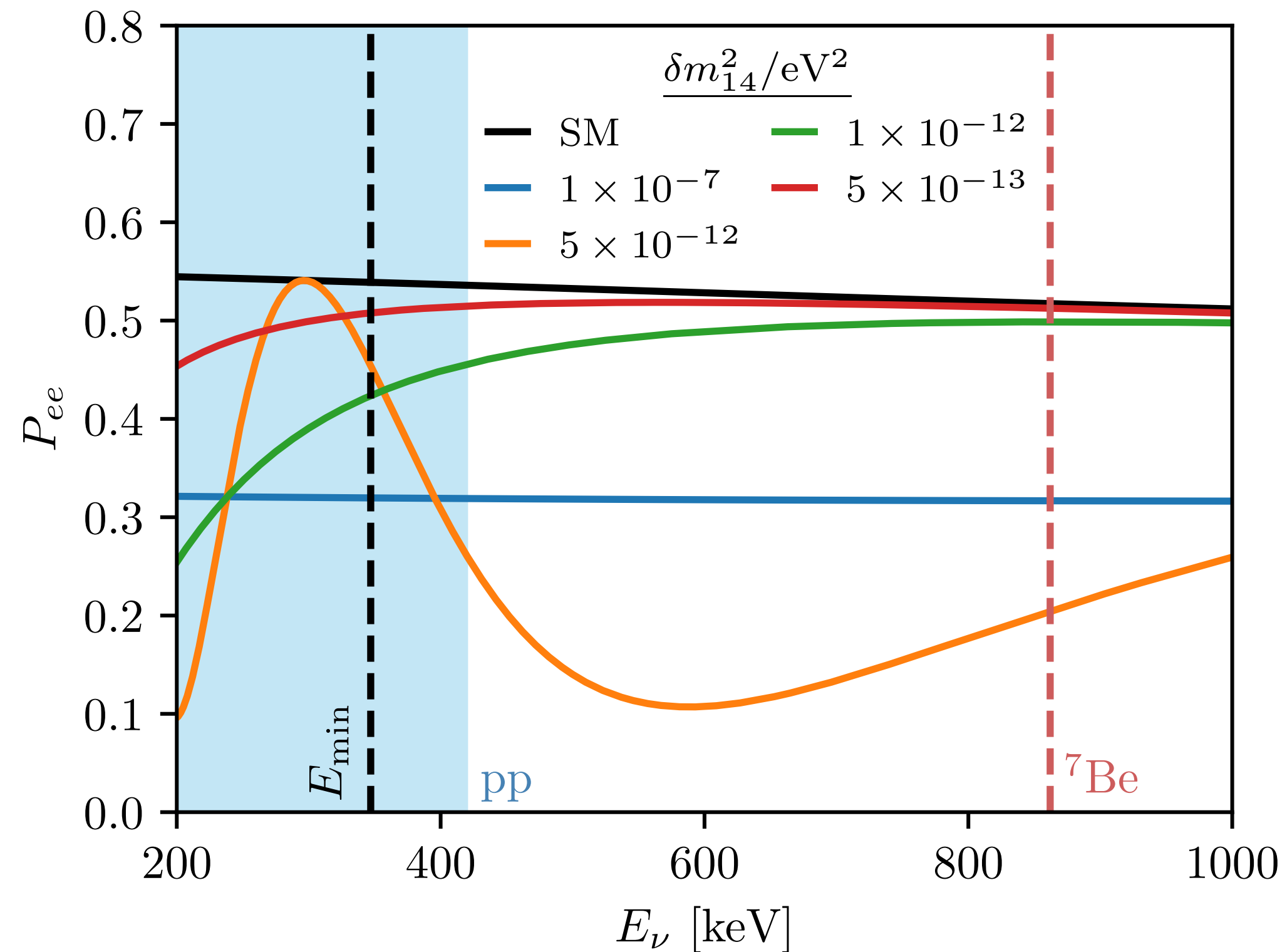


Neutrinos: what we don't know



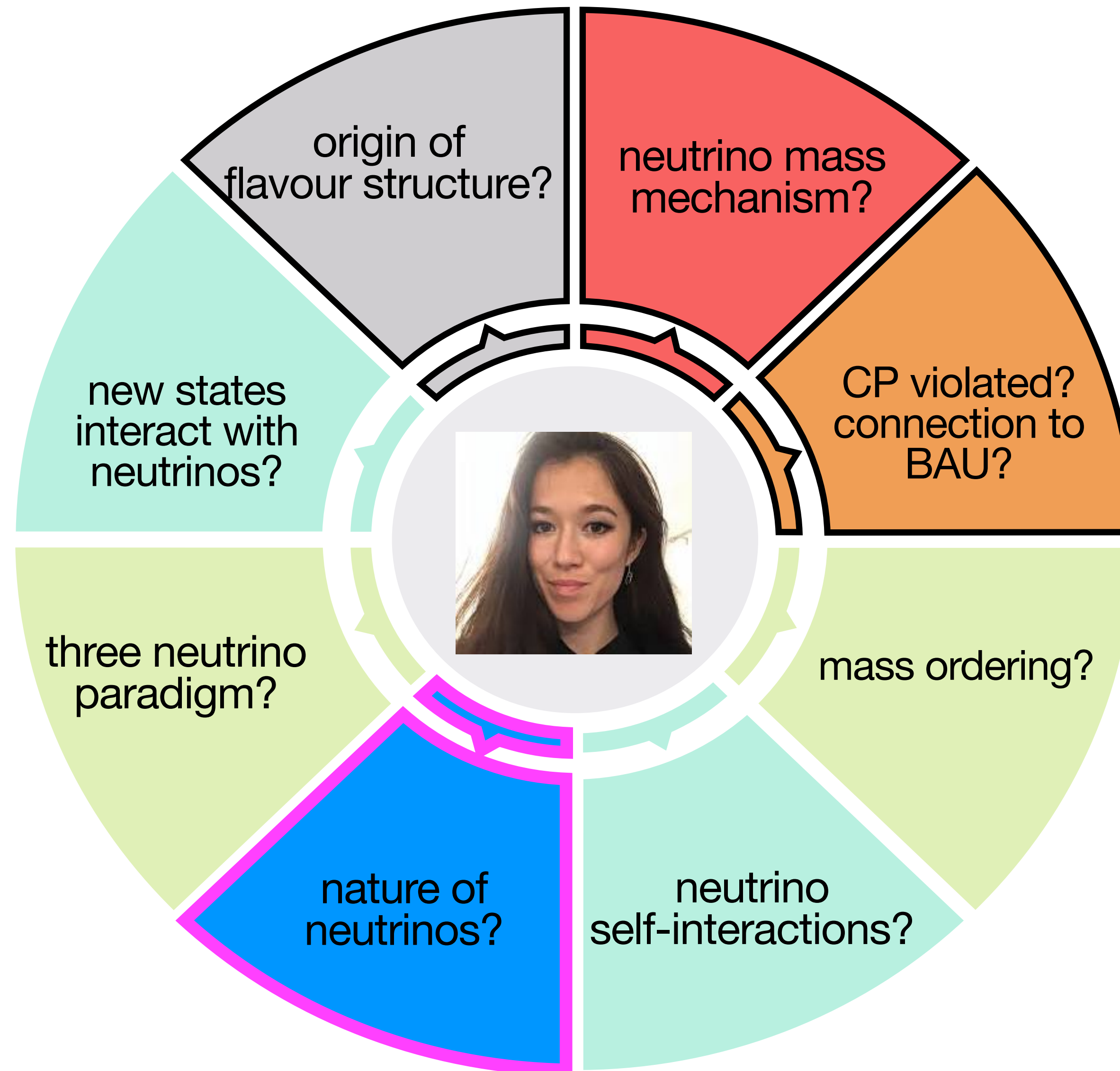


- [2304.05418](#) investigates JUNO's potential to investigate possible pseudo-Dirac nature of neutrinos using solar neutrinos



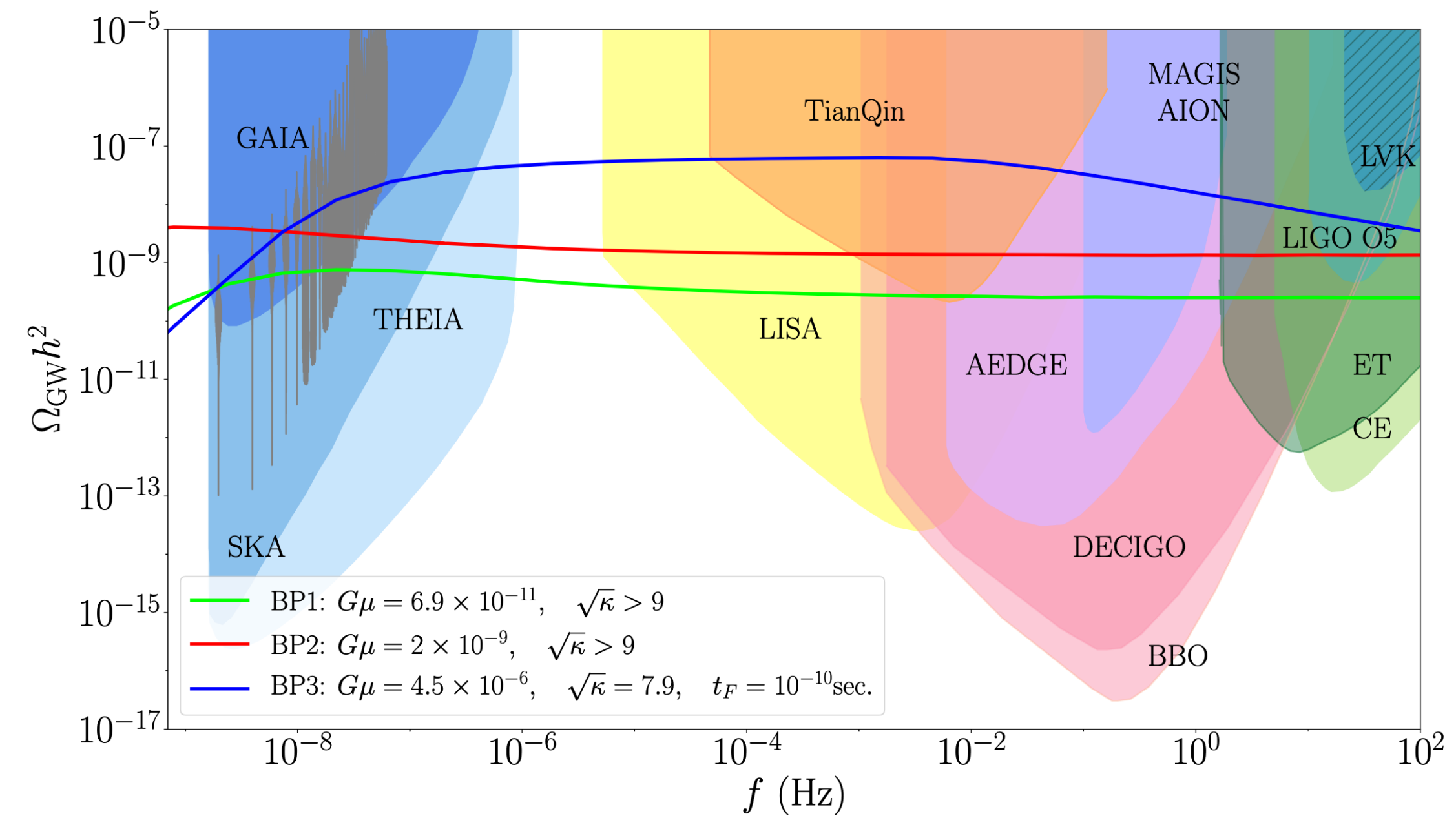
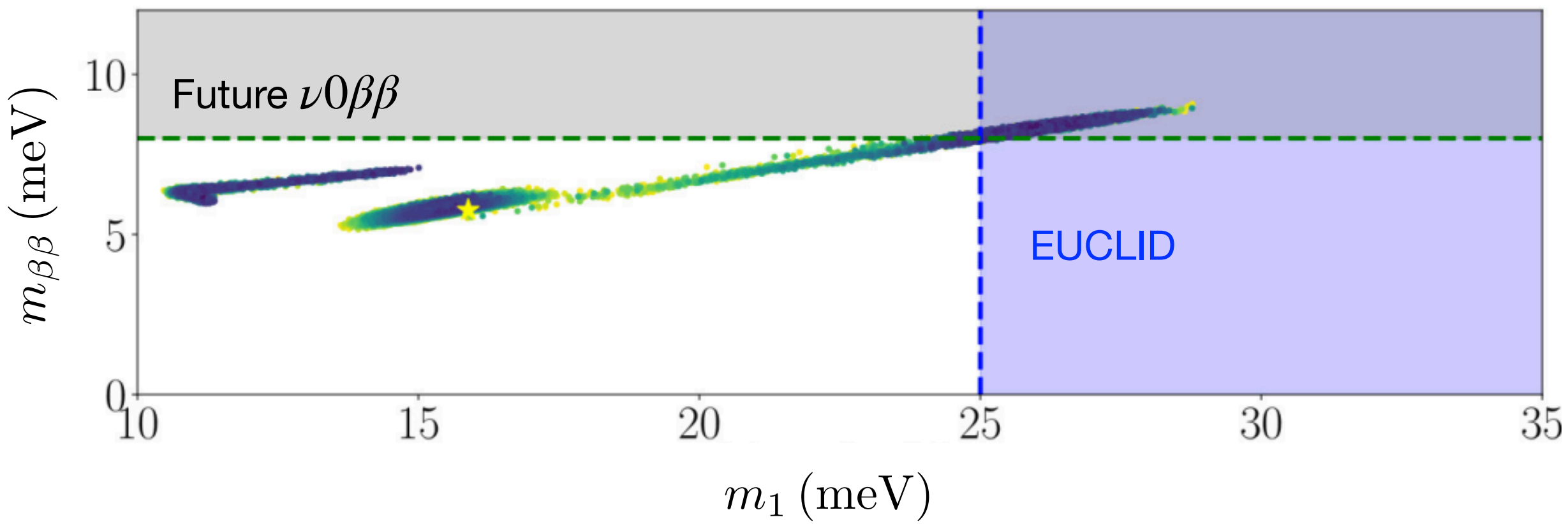
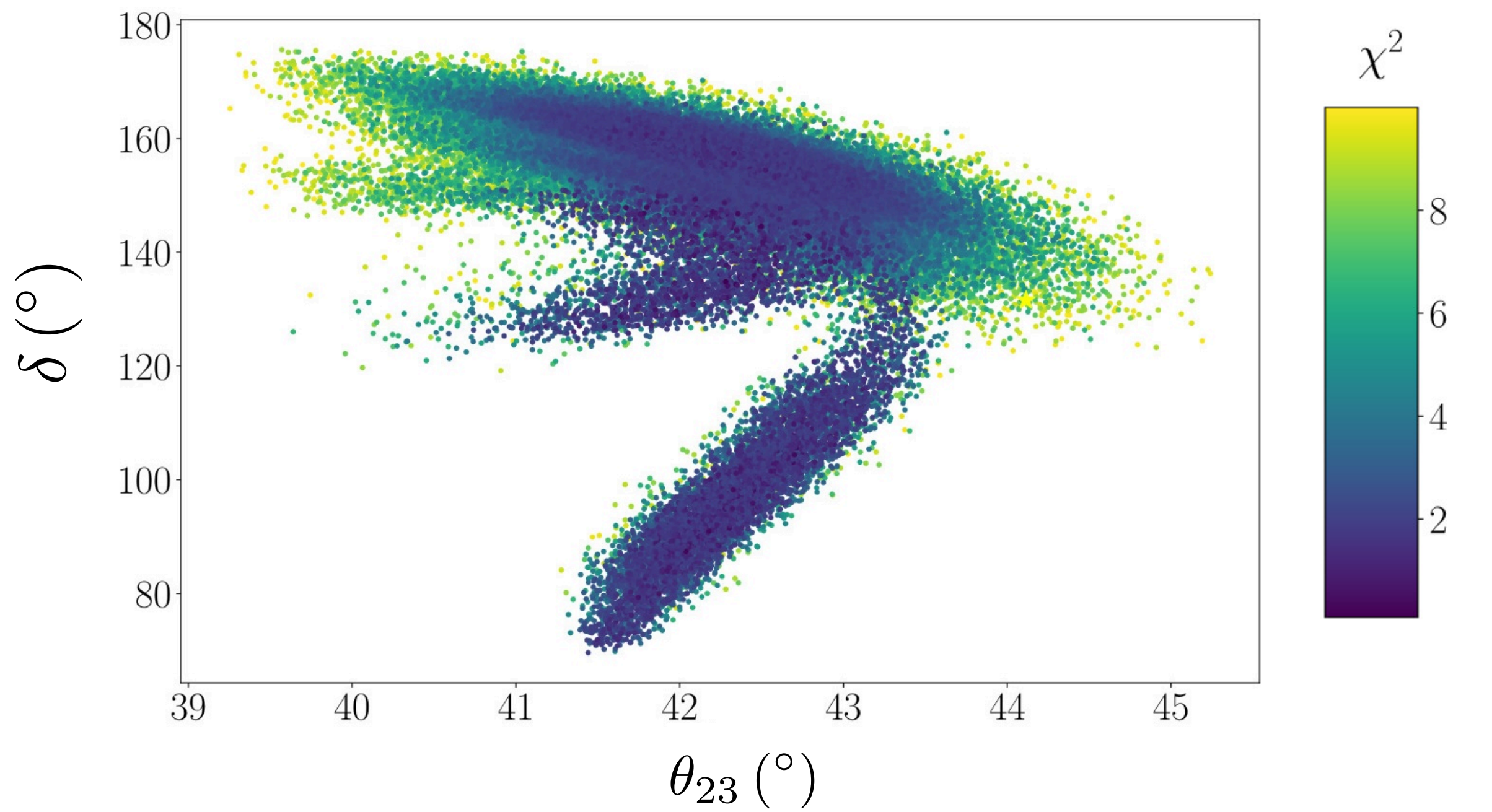
- JUNO competitive with DARWIN in probing nature of neutrinos.

Neutrinos: what we don't know





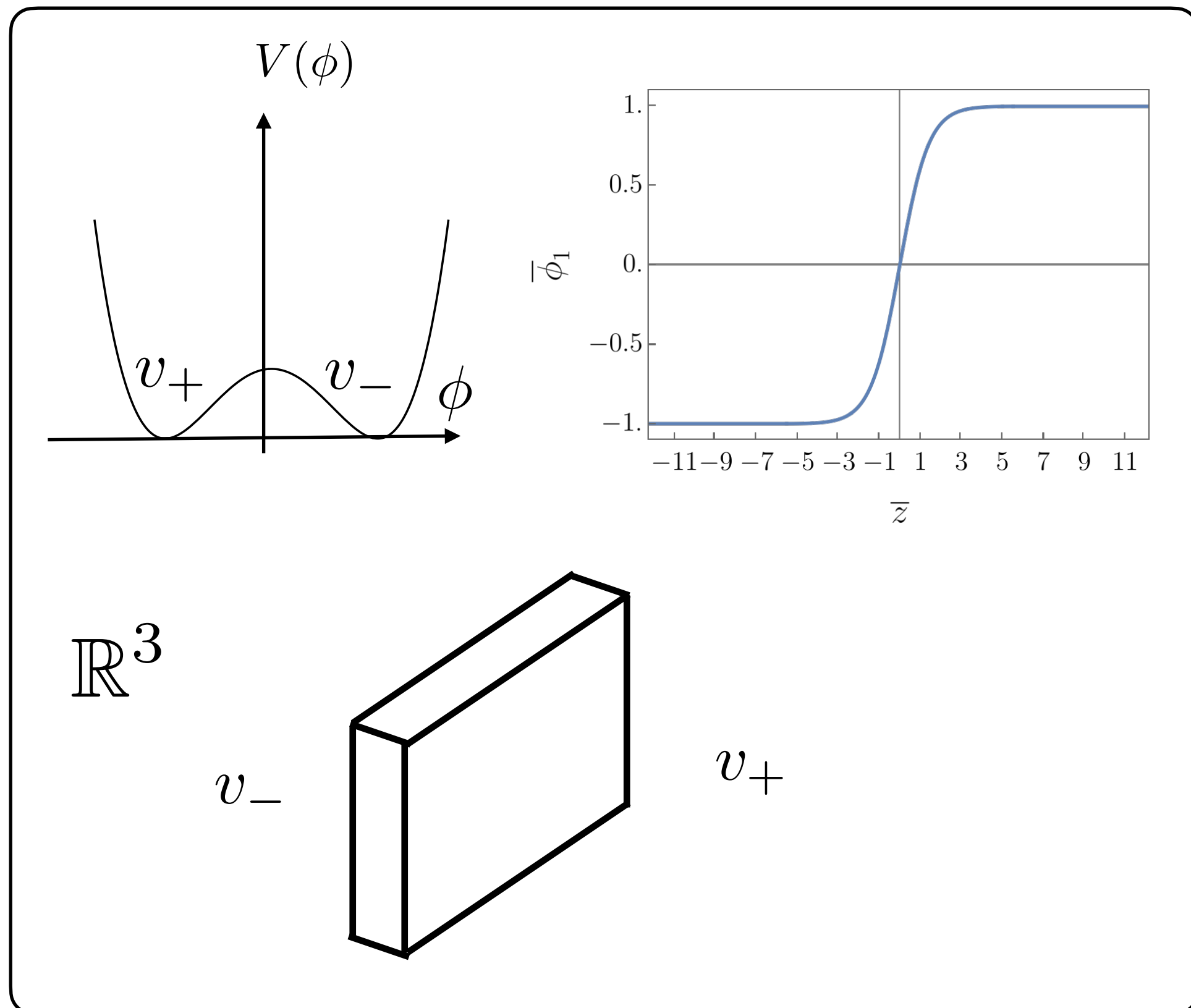
- 2308.05799 investigates how GUT model predicts correlations in flavour data, matter antimatter asymmetry, GW signal generated by cosmic strings & are testable at Hyper-K & DUNE via proton decay



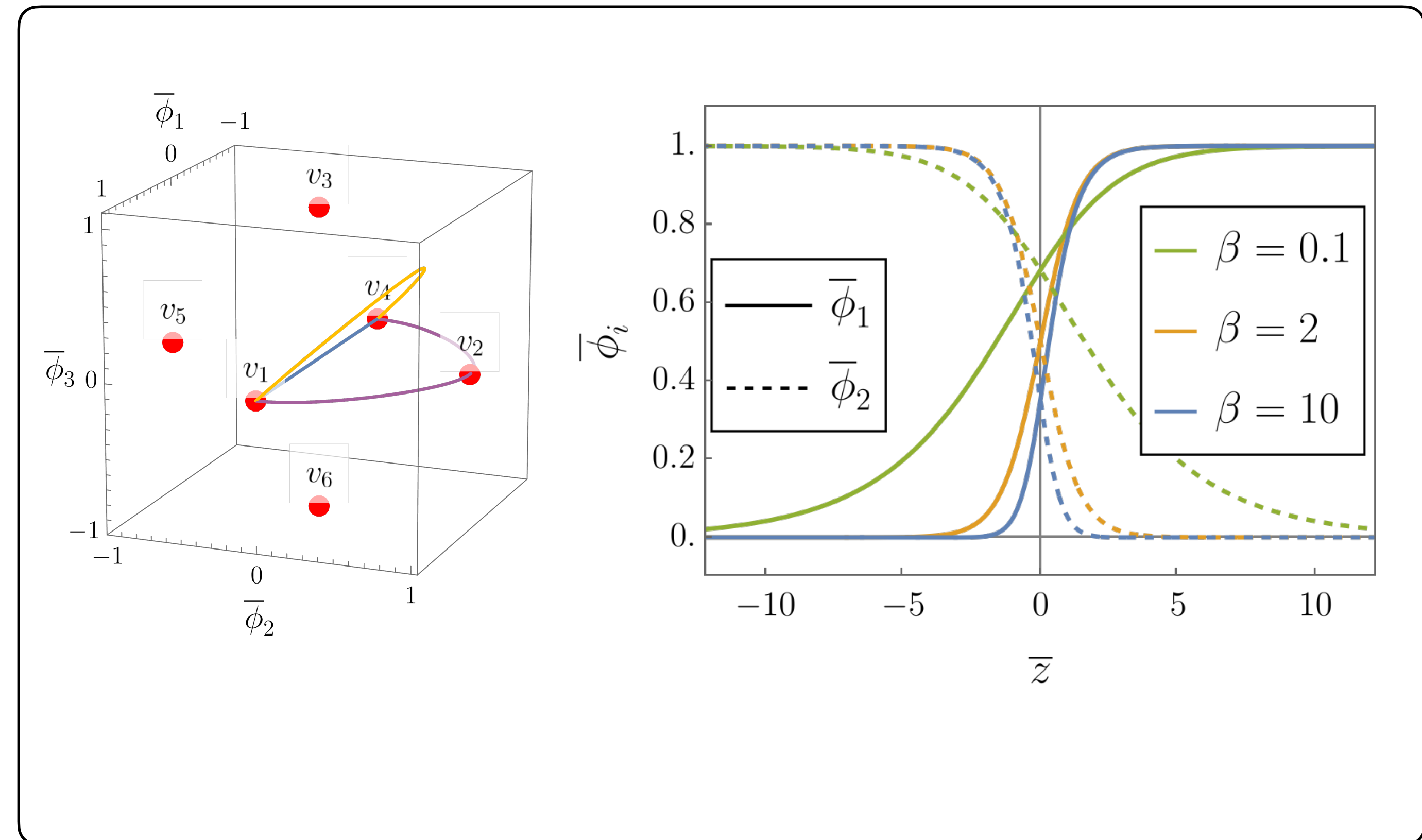


- 2409.16359 (today!) work on cosmological signatures of non-abelian flavour models with S. King. Upcoming flavour data complemented by GW data
- Vacuum manifold of most flavour models is rich and generate domain walls which are more complex than typical \mathbb{Z}_2 domain wall

Abelian Domain Wall

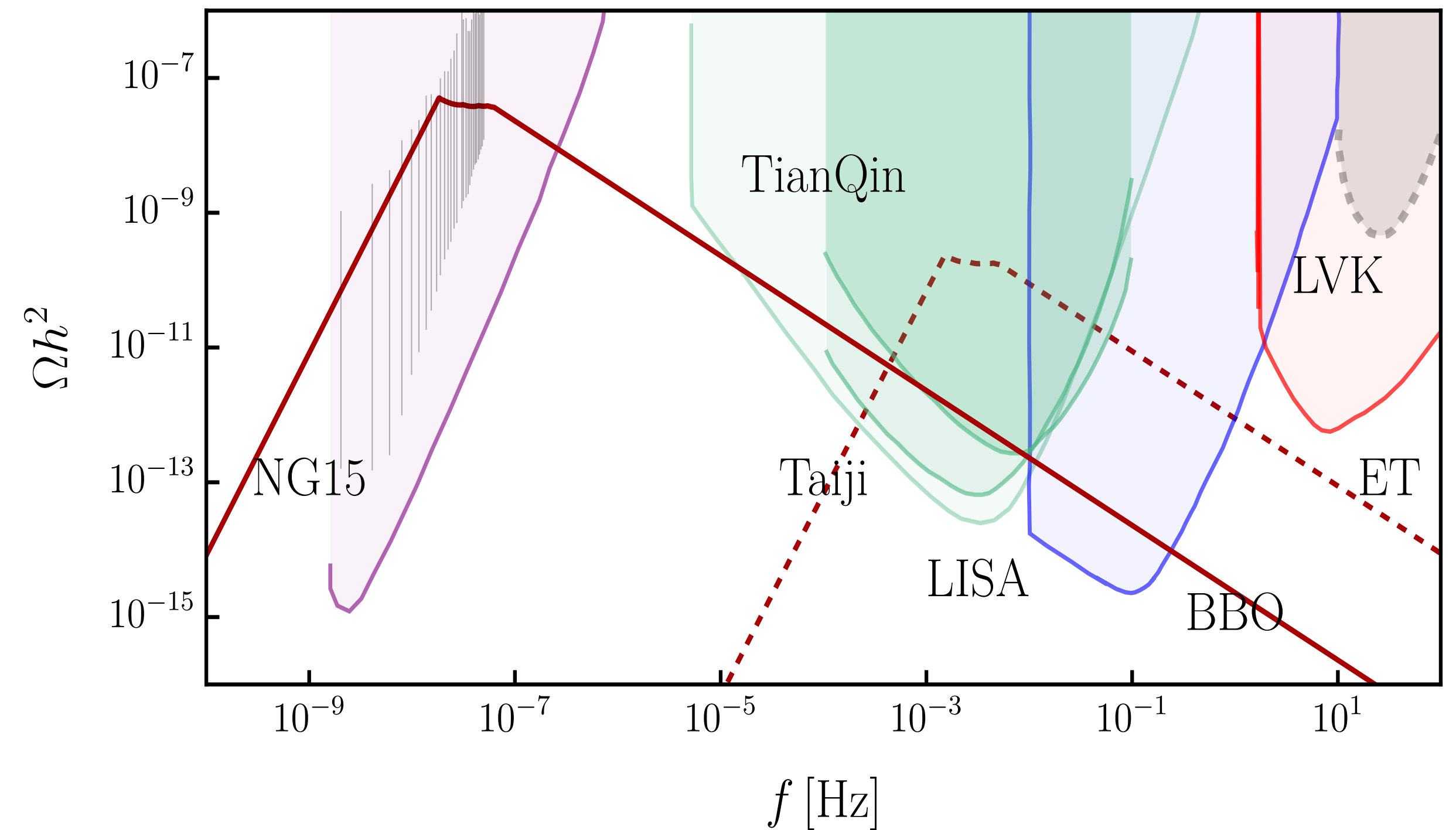
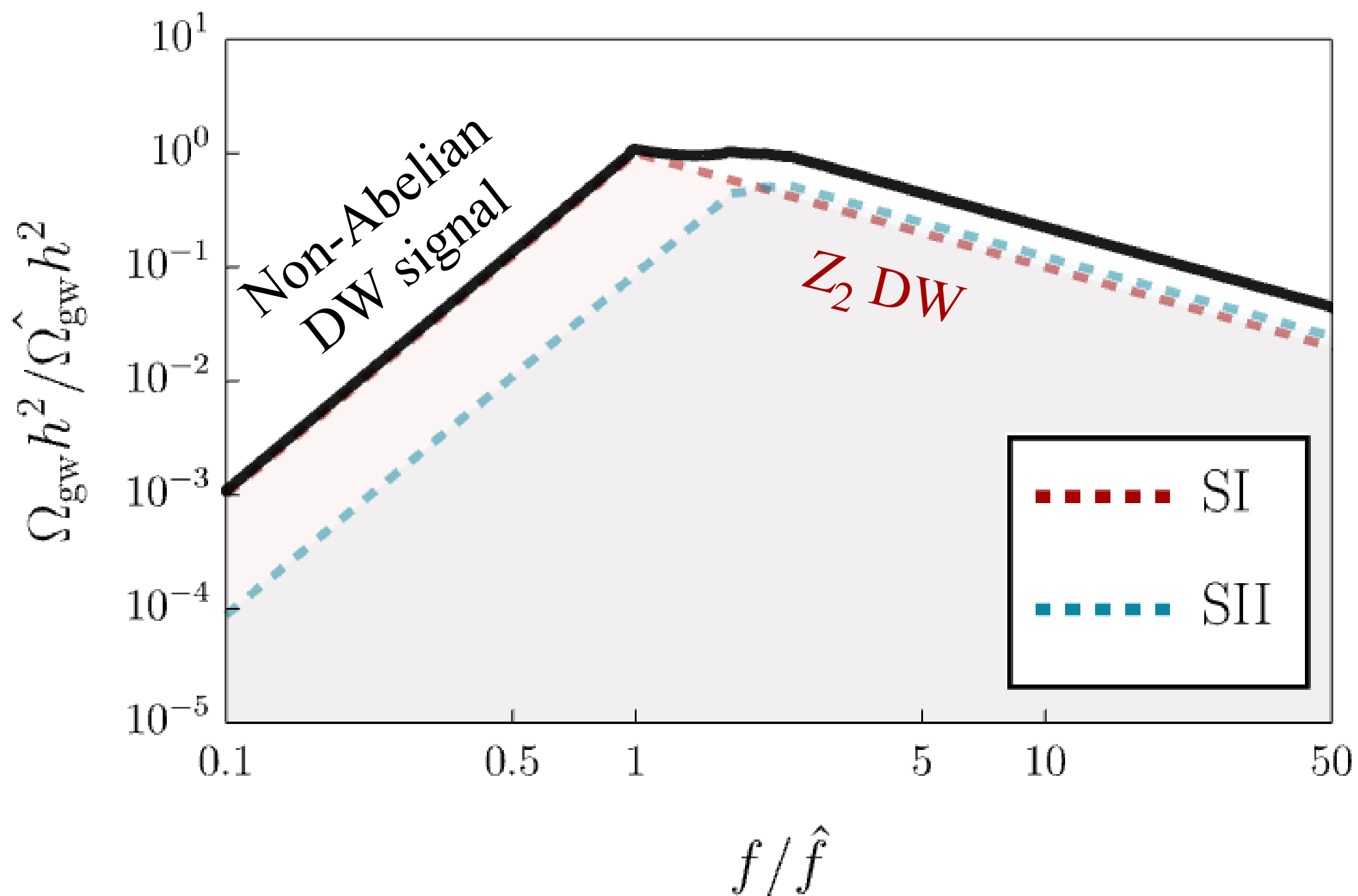


Non-Abelian Domain Wall





- 2409.16359 (today!) work on cosmological signatures of non-abelian flavour models with S. King. Upcoming flavour data complemented by GW data
- Vacuum manifold of most flavour models is rich and generate domain walls which are more complex than typical \mathbb{Z}_2 domain wall



Summary

- Neutrino theory in the UK is a small but vibrant community but covers a wide array of key open questions in neutrino physics
- Current & upcoming neutrino oscillation & $\nu 0\beta\beta$ exps will allow us to test many neutrino theories including flavour & GUTs. Complemented by GW exps
- Astrophysical neutrinos are playing an increasingly important role in understanding neutrinos, more data will come and this will complement accelerator & reactor neutrino experiments.
- Colliders & forward physics facilities (see S. Sarkar's talk) provide a complementary method of understanding neutrino mass (leptogenesis)
- Theoretical developments of neutrino cross section is a key area that requires more attention