# Resonant di-Higgs production as a probe of the NMSSM

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# Motivation

- Higgs pair production is our most direct probe of Higgs self-interactions
- HL-LHC should be able to discover di-Higgs production, but with somewhat large error bars
- Several types BSM effects can enter, so the usual coupling modifier framework is insufficient
- In fact, a clear deviation from SM predictions will require rather light BSM particles, so that also an EFT approach might be limited to the lower end of the  $m_{hh}$  distribution

Together with Stefano Moretti, Luca Panizzi, Jörgen Sjölin we have been developing ideas on how to interpret deviations from the SM. These results have been published in [2302.03401] and [2506.09006].

# Outline

I'll breafly discuss some of the directions we are investigating

- First a brief intro to di-Higgs in general
- Oeconstruction of BSM effects in terms of different diagrammatic contributions
- Resonant di-Higgs the significance of interferences and what they tell about the NMSSM?

Notice: We are working at one-loop (LO), we have not yet decided what to do for two-loop corrections (NLO). For SM diagrams differential K-factors available, but not for a generic BSM diagram. If you multiply everything with 1.8 you are reasonably close.

# Higgs pair production in the SM

Higgs pair production is dominated by gluon fusion  $gg \rightarrow hh$ . In the SM the process arises (mainly) through two diagrams (triangle and box), which interfere destructively.



- The top box amplitude is larger, hence it is more difficult to exclude large upward deviations of λ<sub>hhh</sub> (Run 2: -1.5 < λ<sub>hhh</sub>/λ<sub>hhh,SM</sub> < 6.7)</li>
- The destructive interference makes this process a very difficult one to detect

# Higgs pair production beyond the SM

There can be deviations to Higgs pair production, if

- the top Yukawa coupling deviates from its SM value
  - somewhat constrained by  $t\overline{t}h$  production rate
  - enters quadratically to the amplitude, so small deviations can have a large impact

Ithe trilinear Higgs self coupling deviated from its SM value

- very mildly constrained by experiments
- some models have intrinsic constraints that allow only small deviations, some others are more flexible
- there are light BSM particles coupling strongly to gluons/tops and Higgs bosons
  - top partners (stops in SUSY, fermionic partners in composite models) in non-resonant production, new neutral scalars in resonant production

#### Experimental landscape



- Sensitivity driven by three channels  $bb\gamma\gamma$  at low  $m_{hh}$ ,  $bb\tau\tau$  at intermediate  $m_{hh}$  and bbbb at high  $m_{hh}$
- For type-II 2HDM heavy Higgses excluded especially at high tan  $\beta$ , mostly singlet Higgses can evade the limits

# Model setup

Currently we have a SUSY-inspired model setup, in addition to the SM particle content we have

- additive coupling modifiers for the top Yukawa and the triple Higgs coupling
- up to four colored scalars in the fundamental representation (stops, sbottoms but need not to have SUSY couplings)
- up to two additional CP-even scalars (heavy Higgses) for resonant di-Higgs (UFO model in Github)

We use a private modification of SPheno to calculate the couplings and the spectra. Models for fermionic top partners not validated yet.

# Classification of topologies by coupling structure

	Topology type	Feynman diagrams	Amplitude		
1	Modified hhh coupling	$g_{g}_{g}_{g}_{g}_{g}_{g}_{g}_{g}_{g}_{g$	$A_i \propto \kappa_{hhh}$		
2	One modified <i>hff</i> coupling	$\begin{array}{c} g \\ g \\ t, b \\ g \\ g \\ \hline g \hline \hline g \\ \hline g \\ \hline g \\ \hline g \hline \hline $	$A_i \propto \kappa_{hff}$		
3	Modified <i>hhh</i> coupling and modified <i>hff</i> coupling	$g_{\sigma\sigma\sigma\sigma}^{g} \underbrace{\overset{t,b}{\overset{t,b}{\overset{t}}{\overset{t}}}}_{g \sigma\sigma\sigma\sigma} \underbrace{\overset{t,b}{\overset{t}}}_{t,b} \underbrace{\overset{h}{\overset{h}}}_{h} \underbrace{\overset{h}{\overset{h}}}_{h}$	$A_i \propto \kappa_{hhh} \kappa_{hff}$		
4	Two modified hff couplings	$g \underbrace{\overset{g \text{coss}}{\overset{t,b}}{\overset{t,b}}{\overset{t,b}}{\overset{t,b}}{\overset{t,b}}{\overset{t,b}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}$	$\mathcal{A}_i \propto \kappa_{hff}^2$		
5	Scalar bubble and triangle with $h\bar{s}\bar{s}$ couplings	$g^{g} \xrightarrow{\tilde{s}_{i}} h \xrightarrow{f} h \xrightarrow{g} g^{\tilde{s}_{i}} h \xrightarrow{\tilde{s}_{i}} h \xrightarrow{\tilde{s}_{i}} h$	$\mathcal{A}_i \propto \kappa_{h\bar{s}\bar{s}}^{ii}$		
6	$\begin{array}{l} \mbox{Modified $hhh$ coupling + $Scalar$ bubble and triangle $with $h\bar{s}\bar{s}$ coupling $ \end{array}$	$g^{g} \underbrace{\tilde{s}_{i}}_{g^{g}} \underbrace{h}_{\tilde{s}_{i}} \underbrace{h}_{h} \underbrace{g^{g}}_{h} \underbrace{h}_{h} \underbrace{g^{g}}_{h} \underbrace{h}_{h} \underbrace{g^{g}}_{h} \underbrace{h}_{h} \underbrace{g^{g}}_{h} \underbrace{h}_{h} \underbrace{h}_{h} \underbrace{g^{g}}_{h} \underbrace{h}_{h} \underbrace{h} \underbrace{h} \underbrace{h}_{h} \underbrace{h}_{h} \underbrace{h} \underbrace{h} \underbrace{h}_{h} \underbrace{h} \underbrace{h}$	$A_i \propto \kappa_{hhh} \kappa_{h\bar{a}\bar{a}}^{ii}$		
7	Scalar triangle and box with two $h\bar{s}\bar{s}$ couplings	$\begin{array}{c}g \operatorname{coss} \tilde{\underline{s}}_i \\ g \operatorname{coss} \tilde{\underline{s}}_i \\ g \operatorname{coss} \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \end{array} - h g \operatorname{coss} \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \end{array} - h g \operatorname{coss} \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \end{array} - h g \operatorname{coss} \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \\ \tilde{\underline{s}}_i \end{array}$	$\mathcal{A}_i \propto  \kappa_{h\bar{z}\bar{z}}^{ij} ^2$		
8	Scalar bubble and triangle with hhss coupling	$g^{g} \xrightarrow{\tilde{s}_{i}}_{\tilde{s}_{i}} \xrightarrow{h \ g} \xrightarrow{\tilde{s}_{i}}_{\tilde{s}_{i}} \xrightarrow{h \ g} \xrightarrow{\tilde{s}_{i}}_{\tilde{s}_{i}} \xrightarrow{\tilde{s}_{i}}_{h}$	$\mathcal{A}_i \propto \kappa_{hh\bar{s}\bar{s}}^{ii}$		
9	Neutral scalar	$g_{\mathfrak{sss}}^{g_{\mathfrak{sss}}} \overset{\mathfrak{sss}}{\underset{t,b}{\overset{t,b}{\overset{t}{\overset{t}{\overset{t}{\overset{t}{\overset{t}{\overset{t}{\overset{t}{$	$A_i \propto \kappa^I_{Shh} \kappa^I_{Sff}$		
10	Neutral scalar + coloured scalar	$g^{g} \xrightarrow{\tilde{s}_{i}}_{g} S^{g} \xrightarrow{\tilde{s}_{i}}_{h} h g^{g} \xrightarrow{\tilde{s}_{i}}_{g \text{ ord}} \frac{\tilde{s}_{i}}{\tilde{s}_{i}} S^{g} \xrightarrow{\tilde{s}_{i}}_{h}$	$\mathcal{A}_i \propto \kappa^l_{Shh} \kappa^{li}_{S\bar{s}\bar{s}}$		_
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## We speed up differential simulations by reweighting



- The amplitude from a diagram depends on couplings, masses and Higgs decay widths
- We factorise out the coupling dependence and simulate the cross section per each coupling combination on a grid of mass values
- We can then quickly calculate the full cross section by weighting the results with the corresponding coupling values
- Contributions from individual diagrams and their intereferences can be easily extracted

# Our approach allows to see individual contributions clearly

One of our benchmark points with various effects and interferences



Limitation: You can only have masses on the pre-simulated grid or need to simulate new samples

# Triple Higgs couplings

In the alignment limit of the NMSSM the triple Higgs couplings needed for di-Higgs production are

$$\begin{split} \lambda_{hhh} &= \left(\frac{g^2 + g'^2 \cos^2 2\beta}{8} + \frac{\lambda^2 \sin^2 2\beta}{4} + 4\delta \sin^4 \beta\right) v \\ \lambda_{Hhh} &= \left(\frac{3(g^2 + 2\lambda^2)}{16} \sin 4\beta + 12\delta \sin^3 \beta \cos \beta\right) v \end{split}$$

Here  $\delta$  represents leading one-loop corrections to the Higgs potential.

- $\lambda_{hhh}$  always positive but  $\lambda_{Hhh}$  can be positive or negative depending on tan  $\beta$  and the relative sizes of  $\lambda$  and  $\delta$
- $\lambda_{Hhh}$  tends towards zero at large tan  $\beta$
- $\lambda_{Hhh}$  negative if  $\lambda$  is large and  $\tan \beta \sim 2 \dots 3 \Rightarrow$  the conditions for tree-level enhancement of Higgs mass in the NMSSM

# Interference effects lead to large peaks and dips

The interference of the resonant part with the non-resonant continuum creates a peak-dip structure as the propagator changes sign:



- ullet on left a 800 GeV doublet Higgs and a 1200 GeV singlet, large  $\lambda$
- ullet on right a 800 GeV doublet Higgs (and a 100 GeV singlet), small  $\lambda$
- notice the difference in interference patterns between the 800 GeV Higgses, dip before the peak if Higgs mass from tree-level, after if from top-stop loops

### At decay level the features become somewhat smeared

#### SM + Signal (or × BR = 0.074 fb) SSIB 1025, × BR = 0.000 fto SM + Signal (ct x BR = 41.475 fb) 5 (ct x BR = 25.384 fb) StiR off, x 88 - 0.009 fb) Signal (0 × 88 = 0.041 fb) 5x (a<sub>10</sub> × 8R = 0.000 fs) $M_{\rm [H}^2 + M_{\rm [}^2 S + M_{\rm [}^2 S_{\rm H}^2 + m_{\rm (D}^2 + M_{\rm (D)}^2 \times {\rm IIR} = 0.000~{\rm fb})$ Signel (7 x 0R = 22 234 fb) CTT 55 (5to × 8R = 0.005 th) M|s+N|S+N|S 18<sup>1</sup><sub>0</sub> + 101 + 101 + 00 = 0.034 fb) 5M (of × 8R = 0.033 fb) MIM + MIB (*q*Cl<sub>14 + MR</sub> × 8R = -0.003 fb) S|S+S|SS+S|SS (0<sup>1</sup>/<sub>2</sub>) + g|S + S|S = 0.000 fb) 5N (2 × 5R = 19 245 PM M(rs, x 55 = 0.000 ft) s(x + x)B (C<sup>10</sup><sub>101 + 101</sub> × BR = 0.000 fb) $(1) = (1 + 1) P (\sigma_{11}^{(1)} + m \times RR = 0.136 \text{ fb})$ 516, × 88 = 0.000 ft) THE REPORT OF THE PROPERTY AND ADDRESS OF THE PROPERTY ADDRESS SIR (eff. x RR = -0.003 fb) \$ \$5, × 8R = 0.002 fto 5|8 14(1 × 8R = -1.428 fto NMSSM BP1 NMSSM BP1 m. = 1400 GeV m. = 1400 GeV my = 2000 GeV mu = 2000 GeV 10 m5 = 2000 GeV mi, = 2000 GeV ms, = 2000 GeV mi. = 2000 GeV 3000 fb<sup>-1</sup>) 10 Events ( $\mathcal{L}_{int} = 300 \text{ fb}^{-1}$ ) 102 (F/m)<sub>67</sub> = 1.57 × 10<sup>-1</sup> mat = 2000 GeV mel = 2000 GeV $(\Gamma/m)_{S7} = 1.54 \times 10^{-1}$ (F/m)<sub>st</sub> = 1.54 × 10 10 Ξ. Events ( $\mathcal{L}_{\text{int}}$ = $\frac{1}{1}$ o $\frac{1}{1}$ -10 $-10^{2}$ 250 250 500 750 1000 1250 1500 1750 2000 500 750 1000 1250 1500 1750 2000 M [h\_h\_] (GeV/c<sup>2</sup>) M [a1a2bb1bb2] (GeV/c2)

#### An example of a singlet Higgs at 350 GeV:

- peak very sharp at parton level, lot wider even in the  $bb\gamma\gamma$  channel
- $\bullet$  interference pattern hard to see experimentally, even though the dip above 350 GeV at parton level is  $\sim 30\%$

#### It is easier to see, on which side the excess is



- here again the two benchmarks with 800 GeV Higgses, now in the bb au au channel
- peak gets smeared out, but does not look like a Breit-Wigner distribution
- destructive interference gets washed out almost completely, constructive one survives better

# Summary

- We have developed a framework, where one may compute differential distributions efficiently by reweighting the individual contributions
- This approach allows one to analyse processes at given benchmark points and to understand, which processess contribute to a given feature
- Interference effects in di-Higgs can be large in SUSY models and cannot be neglected
- The interference pattern in NMSSM tells us where the Higgs mass comes from tree-level contributions or top-stop loops

Future work:

- using the deconstructed data sets to extract couplings from (simulated) data and mapping it onto parameters of a fundamental theory
- investigating if one can interpolate between grid points somehow
- introduce fermionic particles in the loop, NLO corrections...

# Details on the deconstruction

- In the UFO model each BSM coupling has its own coupling order, dimensionful couplings are divided by v to make them dimensionless
- For a given set of masses and  $\Gamma_H/m_H$  events are simulated in MadGraph5 setting all couplings to 0.01, simulations are run for all combinations of UFO coupling orders that exist in the differential cross sections
- For a given point this leads to  $\sim$  700 different unweighted contributions, which are then reweighted with the couplings fed into the code
- A script does the reweighting and then plots distributions (distributions are obtained from real events, one could make this faster by just stroring distributions, but one would be constrained to one binning choice)
- Some SPheno code examples can be obtained from the authors

# Impact of a 95 GeV Higgs?



- one of the benchmarks contains a 100 GeV singlet Higgs and the intention was to see, what the impact would be
- no fit to the excesses was made, but the typical effects are not too dependent on the details
- the largest effect is the reduced top Yukawa, which reduces the overall cross section (mimics  $\kappa_{\lambda} > 1$ )
- the interference between the singlet diagram and the continuum is destructive, this is subleading and most visible at the lowest values of  $m_{hh}$