Cosmological Stasis and Its Observational Signatures



Based on work done in collaboration with:

- K. R. Dienes, F. Huang, L. Heurtier, D. Kim, and T. M. P. Tait [2111.04753, 2212.01369]
- K. R. Dienes, F. Huang, L. Heurtier, and T. M. P. Tait [2309.10345, 2406.06830]
- K. R. Dienes, F. Huang, L. Heurtier, D. Hoover, and A. Paulsen [2503.19959]

PASCOS 2025, Durham University, July 22nd, 2025

Towers of Unstable States

- A wide variety of scenarios for new-physics predict **towers of massive**, **unstable states** with a broad spectrum of masses, cosmological abundances, and lifetimes.
- Such towers are a generic feature of, for example,...
 - String theory (string moduli, axions, etc.)
 - Theories with extra spacetime dimensions (KK towers)
 - Scenarios with confining dark/hidden-sector gauge groups (boundstate resonances)
 - Scenarios which lead to the production of primordial black holes with an extended mass spectrum (the black holes themselves)
- In some cases, such states can give rise to astrophysical signals, signals at colliders, etc.; in others, they are too heavy/short-lived.



Cosmological Consequences

• The presence of such towers can have a significant impact on earlyuniverse cosmology – even if the tower states are too heavy/short-lived to be accessible.



- Indeed, such towers can give rise to epochs of <u>cosmic stasis</u>: epochs wherein the abundances of multiple cosmological energy components (matter, radiation, etc.) remain effectively constant over an extended period. [Dienes, Huang, Heurtier, Kim, Tait, BT '21]
- These epochs are often **<u>global attractors</u>**: if the basic conditions under which they arise are satisfied, the universe will evolve toward them.

- Cosmological stasis is a phenomenon in which the abundances of multiple cosmological energy components (matter, radiation, etc.) remain <u>effectively constant</u> over an extended period.
- In order to see how this phenomenon can arise, let's consider a universe consisting only of massive matter (w = 0) and radiation (w = 1/3).

- Cosmological stasis is a phenomenon in which the abundances of multiple cosmological energy components (matter, radiation, etc.) remain <u>effectively constant</u> over an extended period.
- In order to see how this phenomenon can arise, let's consider a universe consisting only of massive matter (w = 0) and radiation (w = 1/3).



- Cosmological stasis is a phenomenon in which the abundances of multiple cosmological energy components (matter, radiation, etc.) remain <u>effectively constant</u> over an extended period.
- In order to see how this phenomenon can arise, let's consider a universe consisting only of massive matter (w = 0) and radiation (w = 1/3).



Boltzmann Equations

$$\frac{d\Omega_M}{dt} = H\Omega_M\Omega_\gamma$$
$$\frac{d\Omega_\gamma}{dt} = -H\Omega_M\Omega_\gamma$$

• Expansion drives Ω_M upward, Ω_γ downward.

- Cosmological stasis is a phenomenon in which the abundances of multiple cosmological energy components (matter, radiation, etc.) remain <u>effectively constant</u> over an extended period.
- In order to see how this phenomenon can arise, let's consider a universe consisting only of massive matter (w = 0) and radiation (w = 1/3).



Boltzmann Equations

$$\frac{d\Omega_M}{dt} = H\Omega_M\Omega_\gamma$$
$$\frac{d\Omega_\gamma}{dt} = -H\Omega_M\Omega_\gamma$$

- Expansion drives Ω_M upward, Ω_γ downward.
- However, in the presence of additional dynamics, the situation changes.

- Cosmological stasis is a phenomenon in which the abundances of multiple cosmological energy components (matter, radiation, etc.) remain <u>effectively constant</u> over an extended period.
- In order to see how this phenomenon can arise, let's consider a universe consisting only of massive matter (w = 0) and radiation (w = 1/3).



Boltzmann Equations

$$\frac{d\Omega_M}{dt} = H\Omega_M\Omega_\gamma - P(t)$$
$$\frac{d\Omega_\gamma}{dt} = -H\Omega_M\Omega_\gamma + P(t)$$

"Pump" from component with higher to lower w.

- Expansion drives Ω_M upward, Ω_γ downward.
- However, in the presence of additional dynamics, the situation changes.
- If some process "pumps" energy density from matter to radiation at a rate P(t) ∝ t⁻¹, it can <u>counteract</u> the effect of expansion.

• We've seen that stasis arises when source and sink tems in the Boltzmann equations "pump" energy density from one component to another at a rate that compensates for Hubble expansion.



So how can such a "pump" arise in practice?

 ϕ

• We've seen that stasis arises when source and sink tems in the Boltzmann equations "pump" energy density from one component to another at a rate that compensates for Hubble expansion.



So how can such a "pump" arise in practice?



One natural mechanism via which energy density can be transferred from matter to radiation is **particle decay**.

• We've seen that stasis arises when source and sink tems in the Boltzmann equations "pump" energy density from one component to another at a rate that compensates for Hubble expansion.



So how can such a "pump" arise in practice?



One natural mechanism via which energy density can be transferred from matter to radiation is **particle decay**.

• The exponential decay of a single matter species, which occurs over a relatively short time period, is insufficient for achieving stasis.

• We've seen that stasis arises when source and sink tems in the Boltzmann equations "pump" energy density from one component to another at a rate that compensates for Hubble expansion.



So how can such a "pump" arise in practice?



One natural mechanism via which energy density can be transferred from matter to radiation is **particle decay**.

- The exponential decay of a single matter species, which occurs over a relatively short time period, is insufficient for achieving stasis.
- However, a <u>tower of matter states</u> ϕ_{ℓ} , where $\ell = 0, 1, 2, ..., N 1$, whose decay widths Γ_{ℓ} and initial abundances $\Omega_{\ell}^{(0)}$ scale across the tower as a function of their mass m_{ℓ} can indeed give rise to a pump that compensate for the effect of cosmic expansion over a extended period.

• We've seen that stasis arises when source and sink tems in the Boltzmann equations "pump" energy density from one component to another at a rate that compensates for Hubble expansion.



So how can such a "pump" arise in practice?



One natural mechanism via which energy density can be transferred from matter to radiation is **particle decay**.

- The exponential decay of a single matter species, which occurs over a relatively short time period, is insufficient for achieving stasis.
- However, a <u>tower of matter states</u> ϕ_{ℓ} , where $\ell = 0, 1, 2, ..., N 1$, whose decay widths Γ_{ℓ} and initial abundances $\Omega_{\ell}^{(0)}$ scale across the tower as a function of their mass m_{ℓ} can indeed give rise to a pump that compensate for the effect of cosmic expansion over a extended period.

<u>This</u> is why we expect stasis to be a fairly common feature in BSM cosmologies. As discussed earlier, towers of massive, unstable states are a generic feature of many well-motivated extensions of the SM!

A Concrete Realization

[Dienes, Huang, Heurtier, Kim, Tait, BT '21]

• Let's consider a tower of N such matter states ($w_M = 0$) with...

Masses

Decay Widths

Initial Abundances

$$m_{\ell} = m_0 + (\Delta m) \ell^{\delta}$$

$$\Gamma_{\ell} = \Gamma_0 \left(\frac{m_{\ell}}{m_0}\right)^{\gamma}$$

$$\Omega_{\ell}^{(0)} = \Omega_0^{(0)} \left(\frac{m_{\ell}}{m_0}\right)^{\alpha}$$

A Concrete Realization

[Dienes, Huang, Heurtier, Kim, Tait, BT '21]

• Let's consider a tower of N such matter states ($w_M = 0$) with...

Masses

Decay Widths

Initial Abundances

$$m_{\ell} = m_0 + (\Delta m) \ell^{\delta}$$

$$\Gamma_{\ell} = \Gamma_0 \left(\frac{m_{\ell}}{m_0}\right)^{\gamma}$$

$$\Omega_{\ell}^{(0)} = \Omega_0^{(0)} \left(\frac{m_{\ell}}{m_0}\right)^{\alpha}$$

- Towers of states with mass spectra of this form arise naturally in many extensions of the Standard Model.
 - KK excitations of a 5D scalar:
 - Bound states of a stronglycoupled gauge theory:
- Decay to radiation ($w_{\gamma} = 1/3$) through <u>contact operators</u> of dimension *d* implies a scaling:

$$\begin{cases} mR \ll 1 \longrightarrow \delta \sim 1 \\ mR \gg 1 \longrightarrow \delta \sim 2 \\ \delta \sim \frac{1}{2} \\ \mathcal{O}_{\ell} \sim \frac{c_{\ell}}{\Lambda^{d-4}} \phi_{\ell} \mathcal{F} \longrightarrow \gamma = 2d - 7 \end{cases}$$

A Concrete Realization

[Dienes, Huang, Heurtier, Kim, Tait, BT '21]

• Let's consider a tower of N such matter states ($w_M = 0$) with...

Masses

Decay Widths

Initial Abundances

$$m_{\ell} = m_0 + (\Delta m)\ell^{\delta}$$

$$\Gamma_{\ell} = \Gamma_0 \left(\frac{m_{\ell}}{m_0}\right)^{\gamma}$$

$$\Omega_{\ell}^{(0)} = \Omega_0^{(0)} \left(\frac{m_{\ell}}{m_0}\right)^{\alpha}$$

- Towers of states with mass spectra of this form arise naturally in many extensions of the Standard Model. $\begin{cases} mR \ll 1 \quad \longrightarrow \quad \delta \sim 1 \\ mR \gg 1 \quad \longrightarrow \quad \delta \sim 2 \end{cases}$
 - KK excitations of a 5D scalar:
 - Bound states of a stronglycoupled gauge theory:
- Decay to radiation ($w_{\gamma} = 1/3$) through *contact operators* of dimension *d* implies a scaling:
- Scaling of initial abundances depends on how they're generated:

 $\delta \sim \frac{1}{2}$ $\mathcal{O}_{\ell} \sim \frac{c_{\ell}}{\Lambda d - 4} \phi_{\ell} \mathcal{F} \longrightarrow \gamma = 2d - 7$ Misalignment production $\longrightarrow \alpha < 0$ Thermal freeze-out $\rightarrow \alpha < 0 \text{ or } \alpha > 0$ Universal inflaton decay $\longrightarrow \alpha \sim 1$ **PBH** evaporation $\longrightarrow \alpha \sim \pm 1$ Gravitational production $\longrightarrow \alpha \sim 0, 1/2, \text{ or } 2$

The Emergence of Stasis



• The matter and radiation abundances during stasis turn out to depend on the model parameters α , γ , and δ .

The Emergence of Stasis



 $\overline{w} = \Omega_M w_M + \Omega_\gamma w_\gamma$

• The <u>effective equation-of-state parameter</u> \overline{w} for the universe is constant during stasis – but takes a non-canonical value within the range $0 < \overline{w} < 1/3$.

Stasis as a Global Attractor

- Perhaps even more importantly, achieving cosmological stasis does not require a fine-tuning of the initial conditions for Ω_M and H – or, alternatively, for Ω_m and its time-average $\langle \Omega_M \rangle$ – or for the ratio $\Gamma_{N-1}/H^{(0)}$.
- In fact, stasis is a <u>global attractor</u> in the sense that Ω_M and Ω_γ will <u>evolve toward their stasis values</u> regardless of what these initial conditions are.



Other Realizations of Stasis

- While I'll be concentrating of stases that involve matter and radiation for the remainder of this talk, I want to emphasize that stasis is a very general phenomenon.
- For example, stasis can also involve <u>vacuum energy</u>. A natural realization of such a stasis involves a tower of oscillating scalar fields with a spectrum of masses m_ℓ which transition from overdamped behavior ($w_\ell \approx -1$) to underdamped ($\langle w \rangle \approx 0$) behavior when $3H(t) \approx 2m_\ell$. [Dienes, Heurtier, Huang, Tait, BT '23; Dienes, Heurtier, Huang, Tait, BT '24]
- It is also possible for a stasis to develop involves <u>more than</u> <u>two components</u>.

[Dienes, Heurtier, Huang, Tait, BT '23]

 In certain situations, stasis can also arise due to the <u>annihilation</u> of non-relativistic particles into radiation.

[Barber, Dienes, BT '24]



• In terms of the homogeneous background cosmology (the evolution of *a* and ρ_{crit}), a stasis epoch **mimics an epoch of perfect-fluid domination** (PFD) wherein the fluid has an equation-of-state parameter $w_{\text{PF}} = \overline{w}$.

• In terms of the homogeneous background cosmology (the evolution of *a* and ρ_{crit}), a stasis epoch **mimics an epoch of perfect-fluid domination** (PFD) wherein the fluid has an equation-of-state parameter $w_{\text{PF}} = \overline{w}$.



To what extent is this equivalence broken at the perturbation level?

• In terms of the homogeneous background cosmology (the evolution of *a* and ρ_{crit}), a stasis epoch **mimics an epoch of perfect-fluid domination** (PFD) wherein the fluid has an equation-of-state parameter $w_{\text{PF}} = \overline{w}$.



To what extent is this equivalence broken at the perturbation level?

- More specifically, let's consider a "<u>spectator"</u> <u>component</u> χ with the following properties:
 - Behaves like massive matter: $w_{\chi} = 0$.



- Has $\rho_{\chi} \ll \rho_{crit}$ during the epoch of interest and thus no appreciable impact on the background cosmology.
- Interacts with other components only through gravity.
- In other words, χ behaves like a population decoupled (e.g. frozen-out) **<u>dark-matter</u>** particles.

• In terms of the homogeneous background cosmology (the evolution of *a* and ρ_{crit}), a stasis epoch **mimics an epoch of perfect-fluid domination** (PFD) wherein the fluid has an equation-of-state parameter $w_{\text{PF}} = \overline{w}$.



To what extent is this equivalence broken at the perturbation level?

- More specifically, let's consider a "<u>spectator"</u> <u>component</u> χ with the following properties:
 - Behaves like massive matter: $w_{\chi} = 0$.



- Has $\rho_{\chi} \ll \rho_{crit}$ during the epoch of interest and thus no appreciable impact on the background cosmology.
- Interacts with other components only through gravity.
- In other words, χ behaves like a population decoupled (e.g. frozen-out) <u>dark-matter</u> particles.
- We'll now examine at how density perturbations for χ and in particular its density contrast $\delta_{\chi} \equiv \Delta \rho_{\chi} / \rho_{\chi}$ evolves during a <u>matter/radiation stasis</u> with $0 < \overline{w} < 1/3$. As we'll see, the results differ significantly from the corresponding results for PFD!



In order to answer this question, let's first begin by reviewing some general aspects of how δ_{χ} (or its Fourier transform $\delta_{k\chi}$) evolves.

• The spectator is decoupled (no source/sink terms):

$$\nabla_{\mu}(T_{\chi})^{\mu}{}_{\nu} = 0$$



In order to answer this question, let's first begin by reviewing some general aspects of how δ_{χ} (or its Fourier transform $\delta_{k\chi}$) evolves.

• The spectator is decoupled (no source/sink terms):

$$\nabla_{\mu}(T_{\chi})^{\mu}{}_{\nu} = 0$$

• This relation yields an equation of motion for $\delta_{k\chi}$:

$$\delta_{k\chi}^{\prime\prime} + \frac{3}{2a} \left(1 - \langle w \rangle \right) \delta_{k\chi}^{\prime} = \left[-3\Phi_{k}^{\prime\prime} - \frac{9}{2a} \left(1 - \langle w \rangle \right) \Phi_{k}^{\prime} + \tilde{k}^{2} a^{3\langle w \rangle - 1} \Phi_{k} \right]$$

$$S_{k\chi}$$



In order to answer this question, let's first begin by reviewing some general aspects of how δ_{χ} (or its Fourier transform $\delta_{k\chi}$) evolves.

• The spectator is decoupled (no source/sink terms):

$$\nabla_{\mu}(T_{\chi})^{\mu}{}_{\nu} = 0$$

• This relation yields an equation of motion for $\delta_{k\chi}$:

$$\delta_{k\chi}^{\prime\prime} + \frac{3}{2a} (1 - \langle w \rangle) \delta_{k\chi}^{\prime} = \begin{bmatrix} -3\Phi_{k}^{\prime\prime} - \frac{9}{2a} (1 - \langle w \rangle) \Phi_{k}^{\prime} + \tilde{k}^{2} a^{3\langle w \rangle - 1} \Phi_{k} \end{bmatrix}$$
• The solution (applying boundary conditions at early times) is:

$$\delta_{k\chi} = \frac{2\Phi_{k0}}{1 + \langle w \rangle} + \int_{0}^{a} db S_{k\chi} G_{k\chi}(a, b)$$
Green's Function



In order to answer this question, let's first begin by reviewing some general aspects of how δ_{χ} (or its Fourier transform $\delta_{k\chi}$) evolves.

• The spectator is decoupled (no source/sink terms):

$$\nabla_{\mu}(T_{\chi})^{\mu}{}_{\nu} = 0$$

• This relation yields an equation of motion for $\delta_{k\chi}$:

$$\delta_{k\chi}'' + \frac{3}{2a}(1 - \langle w \rangle)\delta_{k\chi}' = \begin{bmatrix} -3\Phi_k'' - \frac{9}{2a}(1 - \langle w \rangle)\Phi_k' + \tilde{k}^2 a^{3\langle w \rangle - 1}\Phi_k \end{bmatrix}$$
• The solution (applying boundary conditions at early times) is:
• The solution (applying boundary conditions at early times) is:
• The evolution of Φ_k follows from the Einstein equation:
Sum over cosmological components X
 $\Phi_k'' + \frac{(7 + 3\langle w \rangle)}{2a}\Phi_k' + \frac{\langle w \rangle k^2}{a^4 H^2}\Phi_k = \begin{bmatrix} 4\pi G \\ a^2 H^2 \sum_X \bar{\rho}_X \delta_{kX}(\langle w \rangle - c_{sX}^2) \end{bmatrix}$
• Source Term
Effective equation-
of-state parameter $\langle w \rangle = \sum_X \Omega_X w_X$
Effective sound speed of X
 $c_{sX} \equiv \sqrt{\Delta p_X / \Delta \rho_X}$

X

Perfect-Fluid Domination

- First, let's consider a PFD epoch in which the equation of state for the perfect fluid is $p = w_{\text{PF}}\rho$, where w_{PF} is a constant. [Redmond, Trezza, Erickcek '18]
- In this case, $\langle w
 angle pprox w_{
 m PF}\,$ and $\,c_{s
 m PF}^2 = w_{
 m PF}$.



Vanishes

• The resulting sourceless equation yields:



Matter/Radiation Stasis

- Now let's consider the situation during an epoch of matter/radiation stasis epoch.
- In this case, there are <u>two</u> components with non-negligible Ω_X . Matter with $c_{sM}^2 = w_M = 0$ and radiation with $c_{s\gamma}^2 = w_\gamma = 1/3$.

Doesn't generally vanish

$$\Phi_k'' + \frac{(7+3\langle w \rangle)}{2a} \Phi_k' + \frac{\langle w \rangle k^2}{a^4 H^2} \Phi_k = \left[\frac{4\pi G}{a^2 H^2} \sum_X \overline{\rho}_X \delta_{kX} \left(\langle w \rangle - c_{sX}^2 \right) \right]$$

- The equations of motion for Φ_k and the perturbations in the stasis sector are therefore non-trivially **coupled** during stasis.
- These effects can dramatically impact on how $\delta_{k\chi}$ evolves!



Growth Through Stasis

 We find that after entering the horizon (when k ~ aH), modes experience enhanced, power-law growth until stasis ends.



• During an EMDE, $\delta_{k\chi}$ grows linearly with a_{\perp}

[Erickcek, Sigurdson '11; Fan, Ozsoy, Watson '14; Erickcek '15]

 Thus, even at the perturbation level, stasis interpolates between radiation and matter domination!

Why All This Matters

• Small primordial inhomogeneities in the matter density provide the seeds for the formation of structure at later times.







- Enhancements or suppressions in the linear matter power spectrum $P(k) = |\delta_{km}|^2$ relative to the standard cosmology across different ranges of k can have a observational consequences for cosmic structure.
- In the stasis case, they could lead to the formation of <u>microhalos</u> – small, dense clumps of matter.



Why All This Matters

• Small primordial inhomogeneities in the matter density provide the seeds for the formation of structure at later times.



- Enhancements or suppressions in the <u>linear matter power</u> <u>spectrum</u> $P(k) = |\delta_{km}|^2$ relative to the standard cosmology across different ranges of k can have a observational consequences for <u>cosmic structure</u>.
- In the stasis case, they could lead to the formation of <u>microhalos</u> – small, dense clumps of matter.



Why All This Matters

• Small primordial inhomogeneities in the matter density provide the seeds for the formation of structure at later times.



- Enhancements or suppressions in the <u>linear matter power</u> <u>spectrum</u> $P(k) = |\delta_{km}|^2$ relative to the standard cosmology across different ranges of k can have a observational consequences for <u>cosmic structure</u>.
- In the stasis case, they could lead to the formation of <u>microhalos</u> – small, dense clumps of matter.



Other Observational Signatures of Stasis

- In addition to its effect on the matter power specturm, stasis can also have a number of additional potentially observable consequences.
 - Stasis modifies the predictions for the <u>CMB observables</u> r and n_s that follow from a given inflationary model. [Dienes, Huang, Heurtier, Kim, Tait, BT '22]
 - Stasis can modify the spectrum of the <u>stochastic gravitational-</u> <u>wave background</u> in characteristic ways. [Dienes, Huang, Heurtier, Kim, Tait, BT '22]
 - A stasis involving vacuum energy and matter can lead to accelerated expansion – and potentially even to phenomenologically viable models of <u>cosmic inflation</u>.

[Dienes, Heurtier, Huang, Tait, BT '24]

See Lucien Heurtier's plenary talk from Monday.





Summary

- <u>Stable, mixed-component cosmological eras</u> *i.e.* <u>stasis eras</u> can have a variety of implications for observational cosmology.
- The evolution of density perturbations is modified during stasis. For example, we've seen that the density contrast $\delta_{k\chi}$ for a spectator matter component grows like a power law with an exponent $0 < q(\overline{w}) < 1$.
- In this way, this power-law growth <u>interpolates</u> between the behaviors that $\delta_{k\chi}$ exhibits during matter domination and radiation domination.
- This power-law growth can lead to <u>enhanced structure on small</u> <u>scales</u>, including potentially the formation of microhalos.
- Stasis can give rise to a variety of other observational signatures as well.

