



Science and  
Technology  
Facilities Council

# B decays as probes of New Physics

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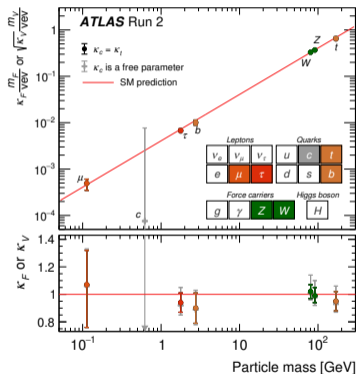
Internal Seminar, Oct 11th 2024

# Motivation

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# The Standard Model is great

## Higgs boson



[from ATLAS, 2024]

## Top quark

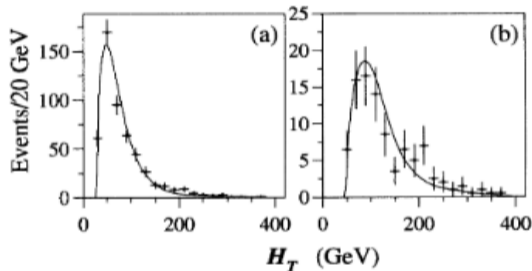


FIG. 2. Observed  $H_T$  distributions (points) compared to the distributions expected from background (line) for  $\cancel{E}_T > 25$  GeV/ $c$  and (a)  $e+ \geq 2$  jets and (b)  $e+ \geq 3$  jets.

[D0 collaboration, 1995]

## Electroweak force

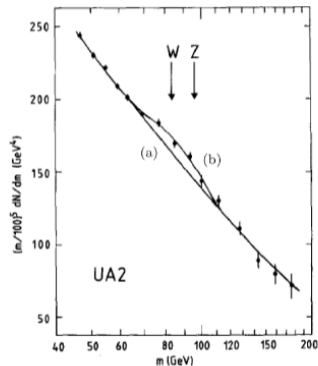
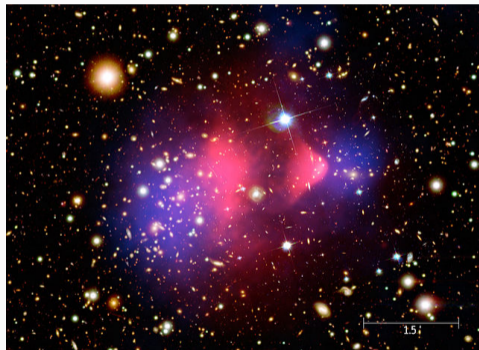


Fig. 24. Two-jet invariant mass distribution, as measured in the UA2 central calorimeter. Curve (a) is a best fit to the data excluding the mass interval  $65 < m < 105$  GeV. Curve (b) is a fit to all data points with the addition of two Gaussians centred at the nominal W and Z mass values.

But...

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- ▶ Can't describe dark matter



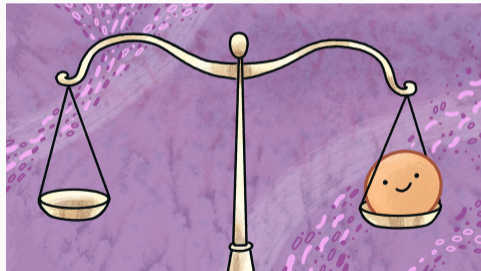
[Bullet Cluster]



- ▶ Can't describe dark matter
- ▶ Can't explain baryon asymmetry



- ▶ Can't describe dark matter
- ▶ Can't explain baryon asymmetry
- ▶ Can't explain neutrino masses

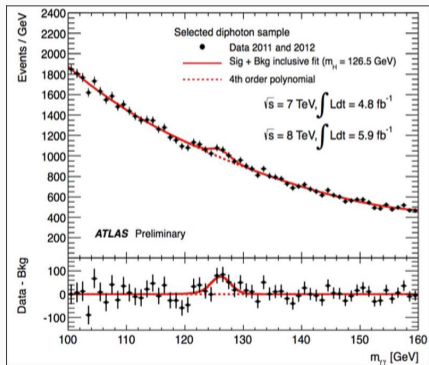


Search Directly

Search Indirectly

## Search Directly

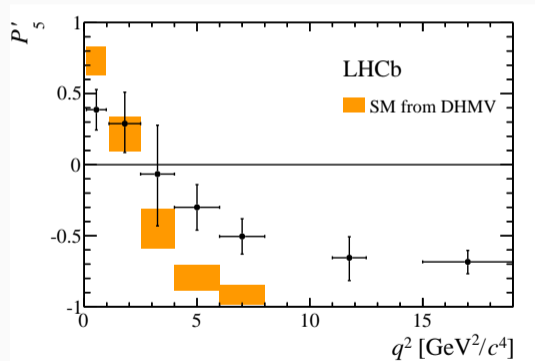
## Search Indirectly



[ATLAS collaboration, 2013]

Search Directly

Search Indirectly



Combine at low energy:

- ▶ Precise measurements
- ▶ Precise predictions

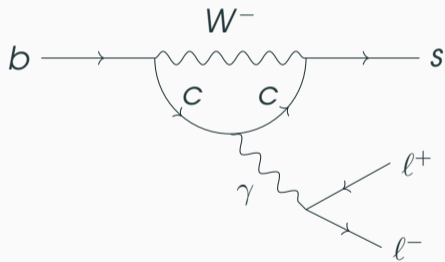
Combine at low energy:


$$\Lambda_{hadronic} \ll m_b^2 \ll m_W^2$$

- ▶ Precise measurements
- ▶ Precise predictions

# Which b decays?

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Flavour changing neutral currents  
only emerge at 1 loop level



Precise measurements

Precise measurements

- ▶ dedicated experiments e.g. LHCb, Belle II

## Precise measurements

- ▶ dedicated experiments e.g. LHCb, Belle II
  - ▶ dedicated components
    - ▶ to differentiate  $\rho, \pi, K, \mu$
    - ▶ to locate vertices



Precise predictions

Precise predictions

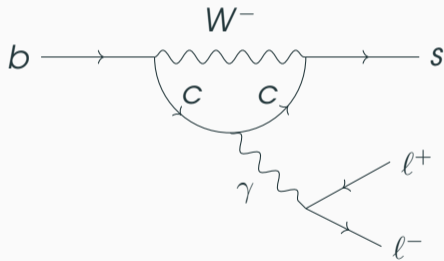
- ▶ multi-scale problem

## Precise predictions

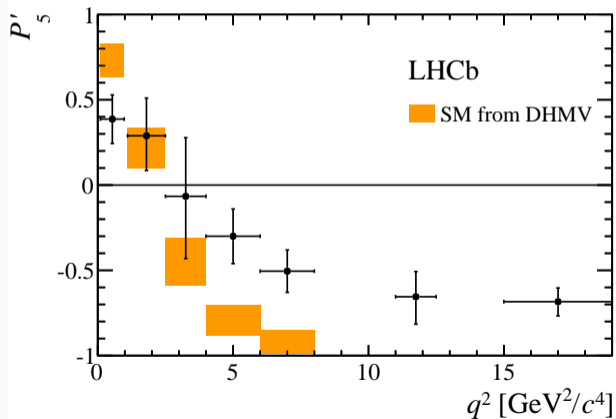
- ▶ multi-scale problem
- ▶ hadronic matrix elements

## Precise predictions

- ▶ multi-scale problem
- ▶ hadronic matrix elements
- ▶ perturbation theory



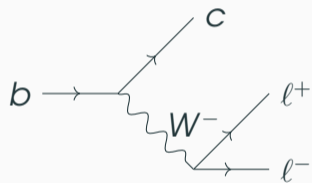
$$B^0 \rightarrow K^{*0} \mu^+ \mu^-$$





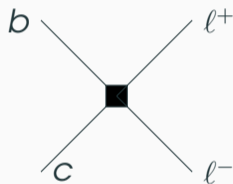
# Effective Field Theory tangent

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An electroweak interaction

→



A Four Fermi theory interaction

$$\mathcal{L}_{WET} \supset \mathcal{L}_{\text{QCD+QED}}^{\{\text{all fermions, top}\}} + \frac{1}{\Lambda^2} \sum_i c_i^{(6)} \mathcal{O}_i^{(6)}$$

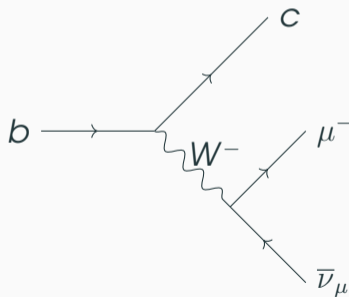
$$\mathcal{L}_{WET} \supset \mathcal{L}_{\text{QCD+QED}}^{\{\text{all fermions, top}\}} + \frac{1}{\Lambda^2} \sum_i c_i^{(6)} \mathcal{O}_i^{(6)}$$

$$\mathcal{O}_i^{(6)} \supset [c \gamma_\mu P_L b][l^+ \gamma^\mu P_L l^-]$$

Sector: Complete set of operators so that at leading order in  $G_F$  they can only mix into each other

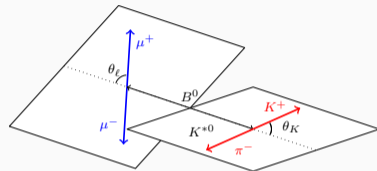
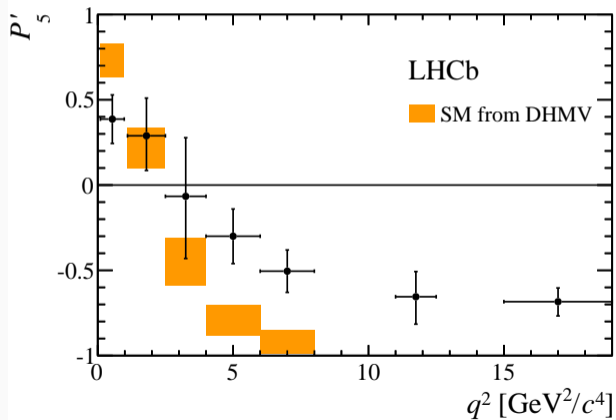
Sector: Complete set of operators so that at leading order in  $G_F$  they can only mix into each other

e.g.  $cb_{\mu\nu\mu}$ .



# My work

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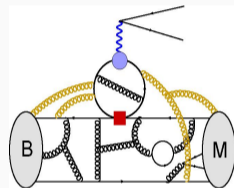
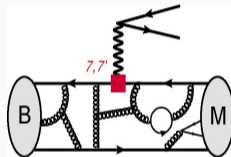
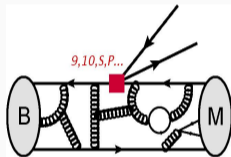
(a)  $\theta_K$  and  $\theta_\ell$  definitions for the  $B^0$  decay

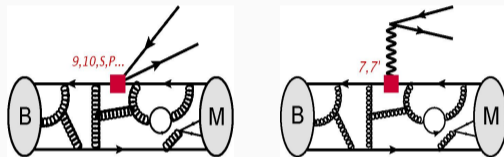


- ▶ Issues with measurement?

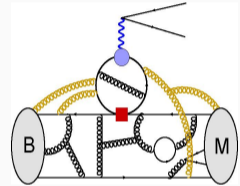
- ▶ Issues with measurement?
- ▶ Issues with hadronic form factors (local and non-local)?

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- ▶ Issues with hadronic form factors (local and non-local)?
- ▶ New physics in  $sb\{\gamma, ll, qq\}$  sector?





- ▶ Local  $\mathcal{P}_\mu \langle \bar{M}(k) | \bar{s} \Gamma^\mu b | \bar{B}(k+q) \rangle$



- ▶ Non-local  $iP_\mu \int d^4x e^{iq \cdot x} \langle \bar{M}(k) | T \{ J_{em}^\mu(x), C_i^{sbcc} O_i^{sbcc} \} | B(k+q) \rangle$

►  $sb\{\gamma, ll, qq\}$

- ▶  $sb\{\gamma, ll, qq\}$
- ▶ Prevailing assumption is that  $sbqq$  operators are SM-like
  - ▶ We're going to test this



*sbqq* mixes into *sbll* through non-local operator.

$$\int d^4x e^{iq \cdot x} T \{ J_{em}^\mu(x-y), C_i^{sbcc} O_i^{sbcc}(y) \}$$

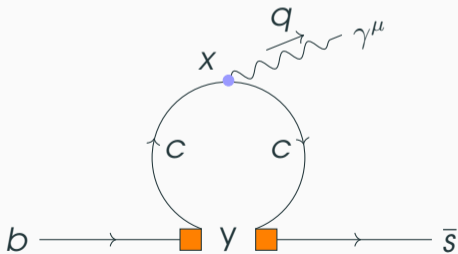
$sbqq$  mixes into  $sbll$  through non-local operator.

$$\int d^4x e^{iq \cdot x} T \{ J_{em}^\mu(x - y), \mathcal{O}_i^{sbcc} \}$$

for example:

▶  $J^\mu = Q_c \bar{c} \gamma^\mu c$

▶  $\mathcal{O}_2^{sbcc} = [\bar{s} \gamma_\nu P_L c][\bar{c} \gamma^\nu P_L b]$



Technical point:

「**Perturbation constraints:**  $|q^2 - 4m_c^2| > \Lambda_{hadronic}^2$ 」

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$$\int d^4x e^{iq \cdot x} T \{ J_{em}^\mu(x), c_i^{sbcc} O_i^{sbcc} \}$$

$$= \sum F_{ij} c_i^{sbcc} [\bar{s} \Gamma_j^\mu b]$$

$$F_{29} C_2^{\text{sbcc}} [\bar{s}\Gamma_9^\mu b]$$

$$= \frac{2}{9} (4\pi e^{-\gamma})^\epsilon \left[ \frac{12m_c^2}{q^2} + \left( 2 + \frac{3}{\epsilon} + 3 \log \frac{\mu^2}{m_c^2} \right) + 3 \text{DiscB}(q^2, m_c, m_c) \frac{(2m_c^2 + q^2)}{q^2} \right] \\ \times C_2^{\text{sbcc}} (q^2 g^{\mu\nu} - q^\mu q^\nu) [\bar{s}\gamma_\nu P_L b]$$

- ▶ I've done  $F_{1\dots 10,j}$  (all c quarks operators) to 1 loop (LO)

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- ▶  $F_{1\dots 10,j}$  to 2 loops (NLO)



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Next tasks:

- ▶  $F_{1\dots 10,j}$  to 2 loops (NLO)
- ▶  $F_{i>10,j}$  at 1 and 2 loop level ( $u, d$ ; (hopefully)  $s, b$ )

- ▶ Reduce to minimum number of independent propagators (solve algebraic equations)
- ▶ Reduce to scalar integrals (Passarino-Veltman)
- ▶ Reduce to minimum number of master integrals (Integration by parts identities)

$$\int d^d k_1 \dots d^d k_L \left[ \frac{\partial}{\partial k_i^\mu} \left( \frac{N^\mu}{P_1 P_2 \dots} \right) \right] = 0$$

- ▶ B decays are an important and interesting area of work
- ▶ There are some interesting challenges involved in the work
- ▶ I'm looking at 1 and 2 loop calculations (where SM is not assumed)

# Backup Slides

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The angular distribution of  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  decay is given by

$$\begin{aligned} \frac{1}{d(\Gamma + \bar{\Gamma}) dq} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}} \Big|_P = & \frac{9}{32\pi} \left[ \frac{3}{4} (1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ & + \frac{1}{4} (1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \\ & + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + \frac{4}{3} A_{\text{FB}} \sin^2 \theta_K \cos \theta_\ell \\ & \left. + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right] \end{aligned}$$

$F_L$  is a fraction of longitudinal polarization of  $K^{*0}$ ;

$$P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}$$

$sb\{\gamma, ll\}$  basis

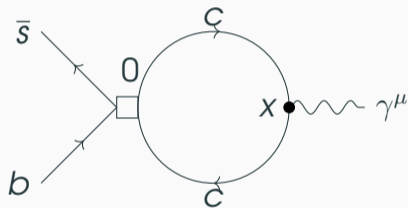
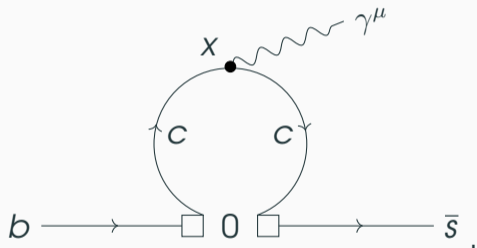
$$J_7 = 2im_b q_\nu [\bar{s}\sigma^{\mu\nu} P_R b]$$

$$J_9 = (q^\mu q^\nu - q^2 g^{\mu\nu}) [\bar{s}\gamma_\nu P_L b]$$

# sbcc operators

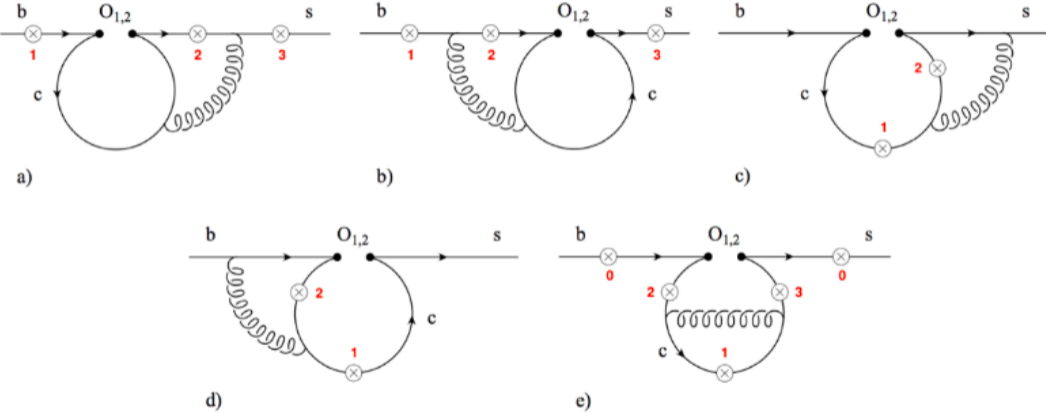
$$\begin{aligned} \mathcal{O}_1^{\text{sbcc}} &= [\bar{s}\gamma_\mu t^a P_L c][\bar{c}\gamma^\mu t^a P_L b] & \mathcal{O}_6^{\text{sbcc}} &= [\bar{s}\gamma_{\mu\nu\rho} t^a P_L b][\bar{c}\gamma^{\mu\nu\rho} t^a c] \\ \mathcal{O}_2^{\text{sbcc}} &= [\bar{s}\gamma_\mu P_L c][\bar{c}\gamma^\mu P_L b] & \mathcal{O}_7^{\text{sbcc}} &= [\bar{s}\gamma_\mu P_L b]Q_c[\bar{c}\gamma^\mu c] \\ \mathcal{O}_3^{\text{sbcc}} &= [\bar{s}\gamma_\mu P_L b][\bar{c}\gamma^\mu c] & \mathcal{O}_8^{\text{sbcc}} &= [\bar{s}\gamma_\mu t^a P_L b]Q_c[\bar{c}\gamma^\mu t^a c] \\ \mathcal{O}_4^{\text{sbcc}} &= [\bar{s}\gamma_\mu t^a P_L b][\bar{c}\gamma^\mu t^a c] & \mathcal{O}_9^{\text{sbcc}} &= [\bar{s}\gamma_{\mu\nu\rho} P_L b]Q_c[\bar{c}\gamma^{\mu\nu\rho} c] \\ \mathcal{O}_5^{\text{sbcc}} &= [\bar{s}\gamma_{\mu\nu\rho} P_L b][\bar{c}\gamma^{\mu\nu\rho} c] & \mathcal{O}_{10}^{\text{sbcc}} &= [\bar{s}\gamma_{\mu\nu\rho} t^a P_L b]Q_c[\bar{q}\gamma^{\mu\nu\rho} t^a q]. \end{aligned}$$

# 1 loop diagrams





# 2 loop diagrams



# Vertex Locator (VELO)

VELO is extremely close to beams to allow precision measurement of b quark location ( $10^{-5}\text{m}$ ).

It is mechanically moved into place once the beams have been stabilised so that they are not damaged when the beams are injected

$$\text{DiscB}(q^2, m_c, m_c) = \frac{\sqrt{q^2(q^2 - 4m_c^2)}}{q^2} \log\left(\frac{2m_c^2 - q^2 \sqrt{q^2(q^2 - 4m_c^2)}}{2m_c^2}\right)$$