



University
of Glasgow

BSM MULTI-HIGGS: IMPLICATIONS IN EWPT AND COLLIDERS

Wrishik Naskar

(based on L. Biermann, C. Borschensky, C. Englert, M. Mühlleitner, **WN** 2408.08043)

18th Dec. 2024 — **Young Theorists' Forum 2024**

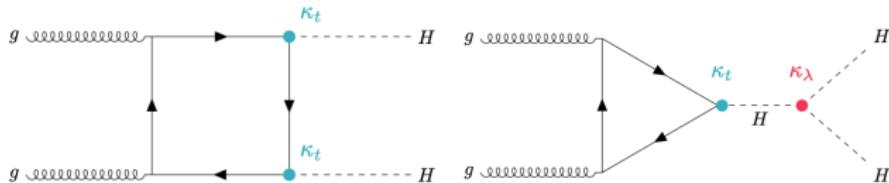
IPPP, Durham

INTRODUCTION

MULTI-HIGGS PROCESSES

- **hh** has been a cornerstone for physics Beyond the Standard Model (BSM) at the LHC.

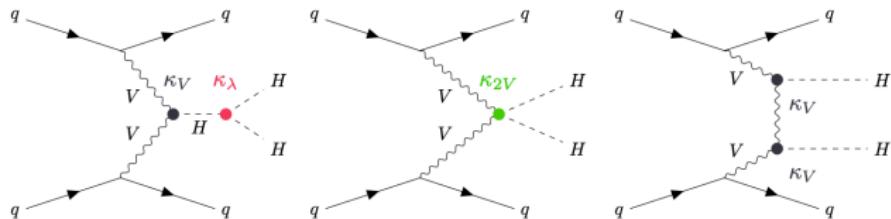
(ATLAS 2023; CMS 2023)



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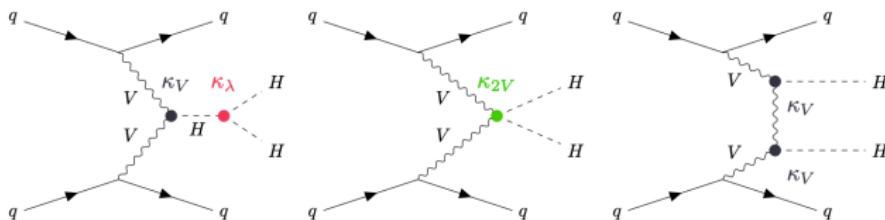
(ATLAS 2023; CMS 2023)



MULTI-HIGGS PROCESSES

- **hh** has been a cornerstone for physics Beyond the Standard Model (BSM) at the LHC.

(ATLAS 2023; CMS 2023)



- **hhh** is gradually gaining more focus.

(Papaefstathiou et al. 2016; Fuks et al. 2016; Chen et al. 2016; Robens et al. 2020; Papaefstathiou et al. 2019; Papaefstathiou et al. 2021; Florian et al. 2020; Papaefstathiou and Tetlalmatzi-Xolocotzi 2023; Stylianou et al. 2023; Delgado et al. 2023; Anisha et al. 2024; Brigljevic et al. 2024; Karkout et al. 2024; ATLAS 2024)

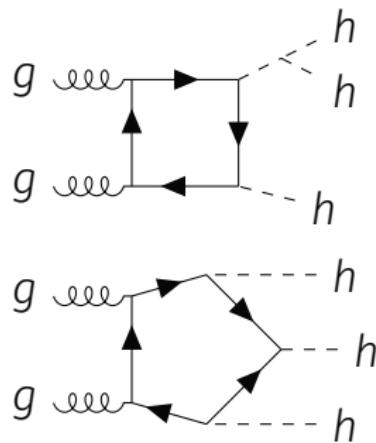
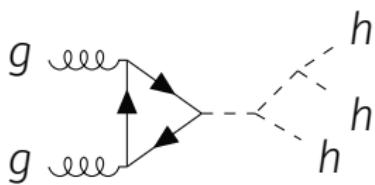
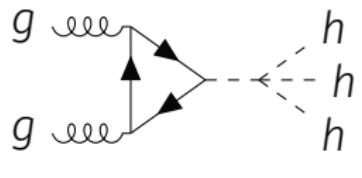
⇒ Crucial for future collider search strategies.

THE MORE, THE MERRIER?

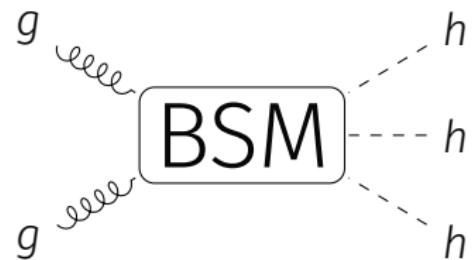
- SM cross-section for hhh (LO)

$$\boxed{\sigma_{hhh}^{ggF} = \mathcal{O}(50 \text{ ab})} \sim \textcolor{red}{4 \text{ (10) events}} \text{ (HL-LHC)}$$

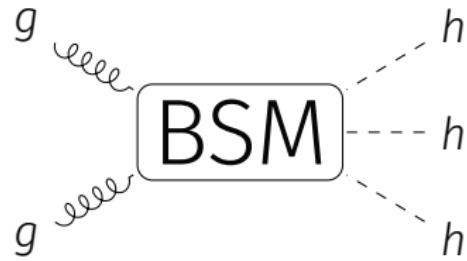
(Florian et al. 2020)



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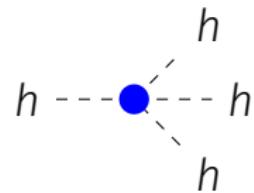
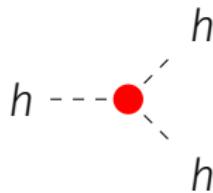
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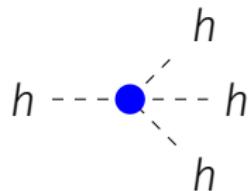
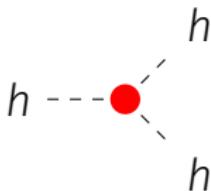
- SMEFT vs HEFT.

(Delgado et al. 2023; Anisha et al. 2024)

SMEFT VS HEFT



SMEFT VS HEFT

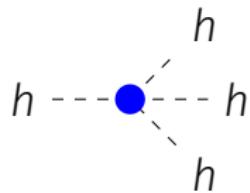
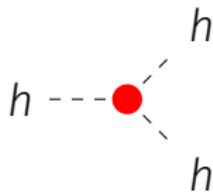


- SMEFT is a linear extension around the SM point.

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}}^{d \leq 4} + \sum_{i,d=5,6,\dots} \frac{C_i^{(d)} \mathcal{O}_i^{(d)}}{\Lambda^{d-4}}.$$

(Henning et al. 2016; Ilaria Brivio et al. 2019) ...

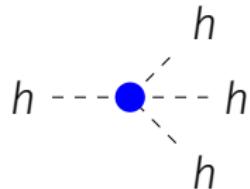
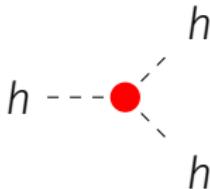
SMEFT VS HEFT



- SMEFT is a **linear** extension around the SM point.

$$\mathcal{L}_{\text{SMEFT}}^{\text{Higgs}, d \geq 6} \supset \frac{1}{\Lambda^2} C_6 |\Phi|^6 + \frac{1}{\Lambda^4} C_8 |\Phi|^8, \quad \Phi = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix}$$

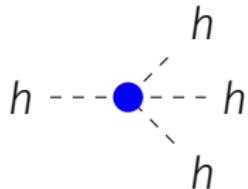
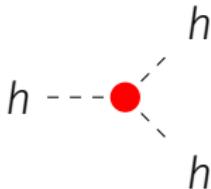
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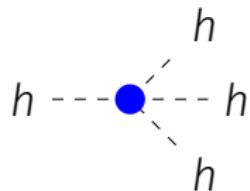
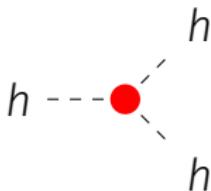
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- HEFT is a **non-linear** realisation of EWSB.

$$\Phi \rightarrow \frac{v + h}{\sqrt{2}} \mathbf{U} \begin{pmatrix} 0 \\ 1 \end{pmatrix}, \quad \mathbf{U} = \exp \left(\frac{i\sigma^j \pi_j}{v} \right)$$

(Alonso et al. 2013; I. Brivio et al. 2014; Gerhard Buchalla et al. 2014; G. Buchalla et al. 2016)

SMEFT VS HEFT



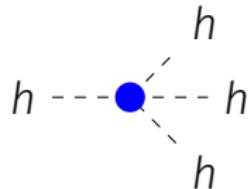
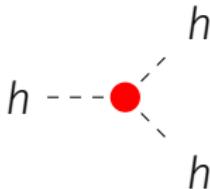
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$$\mathcal{L}_{\text{HEFT}}^{\text{Higgs}} \supset - \left(\frac{1}{2} m_h^2 h^2 + \frac{1}{2} \kappa_3 \frac{m_h^2}{v} h^3 + \frac{1}{2} \kappa_4 \frac{m_h^2}{v^2} h^4 \right)$$

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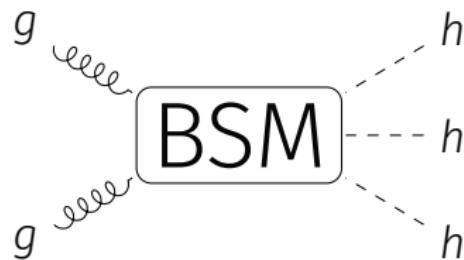
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⇒ HEFT can effectively capture any **decorrelated** new physics effects in **hhh** that is absent in di-/single Higgs.

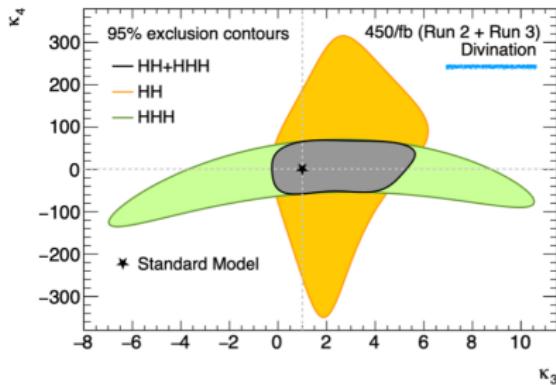
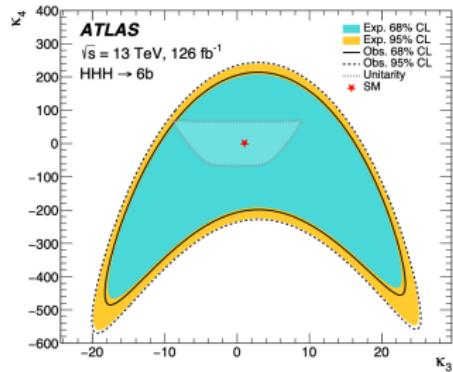
THE MORE, THE MERRIER?



- SMEFT vs HEFT.
(Delgado et al. 2023; Anisha et al. 2024)
- $hhh \Rightarrow$ Higgs potential (κ_3, κ_4)

COUPLING CONSTRAINTS

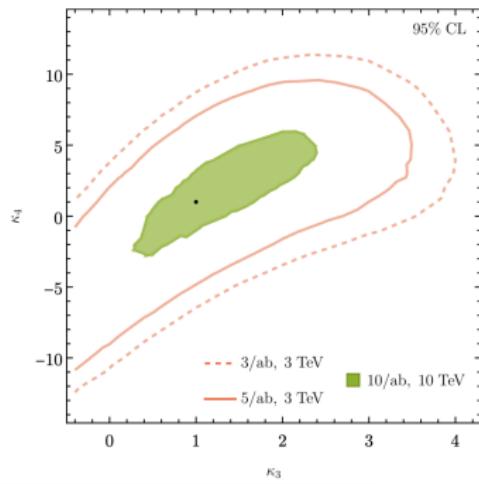
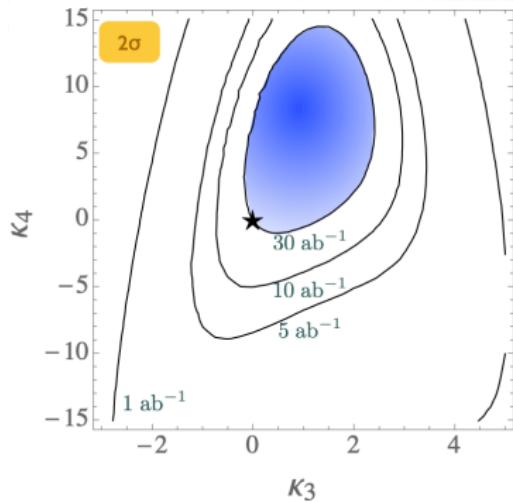
- hhh significantly improves constraints on κ_4 .



(ATLAS 2024; Fuks et al. 2016)

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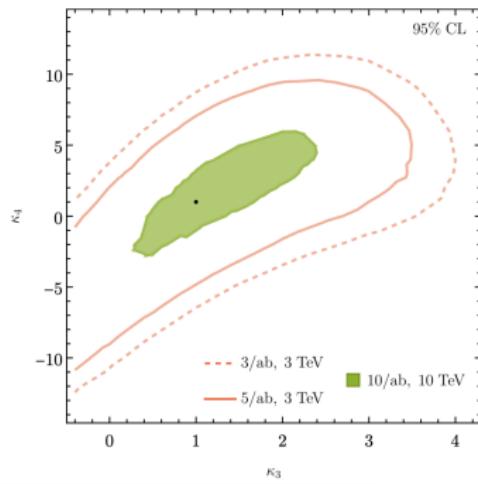
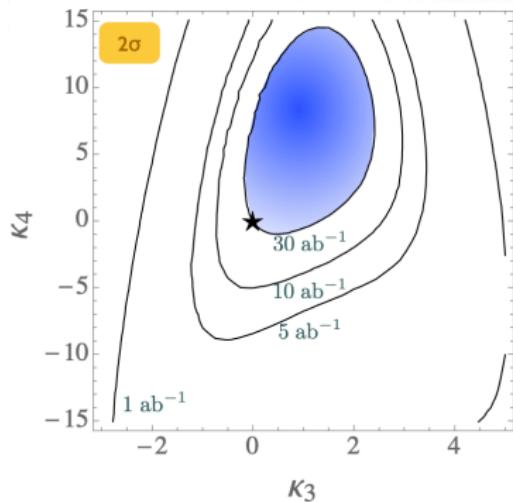
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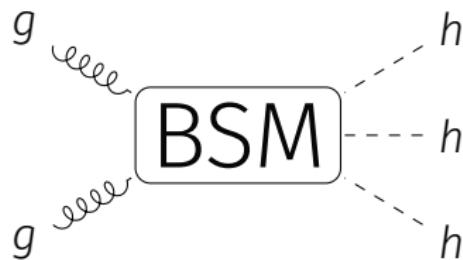
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(Fuks et al. 2016; Stylianou et al. 2023)

- Order of magnitude improvement in precision at FCC-hh and high energy lepton colliders.

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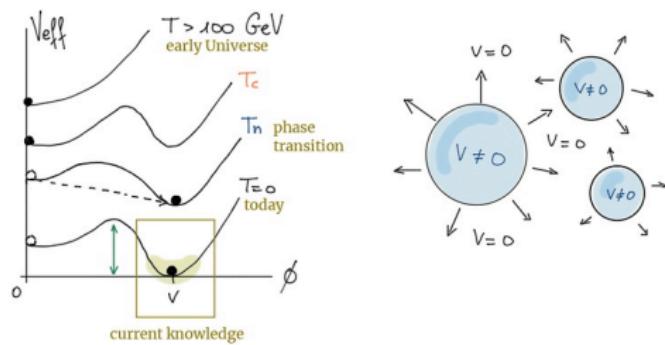
(Delgado et al. 2023; Anisha et al. 2024)

- hhh** \Rightarrow Higgs potential \Rightarrow EW vacuum structure \Rightarrow EWPTs, baryogenesis, stability of the universe, etc.

(Papaefstathiou and Tetlalimatzi-Xolocotzi 2023; Stylianou et al. 2023; Karkout et al. 2024)

ELECTROWEAK PHASE TRANSITIONS

- EW symmetry breaking in the Early Universe at $T \sim \mathcal{O}(100)$ GeV \Rightarrow activation of the Higgs Mechanism.

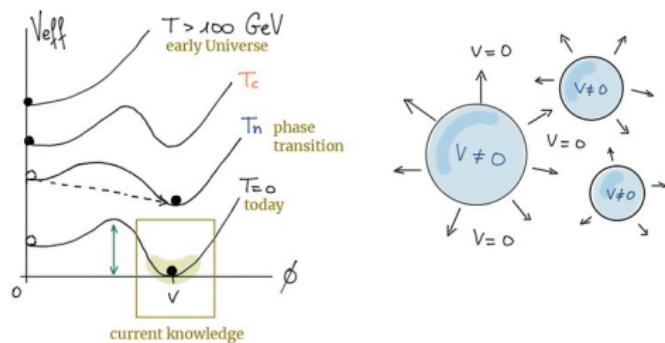


(Credits: Lisa Biermann)

(Sakharov 1967)

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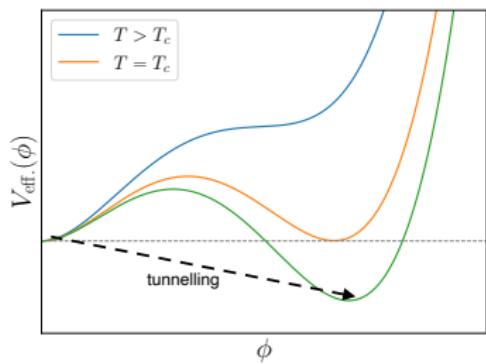
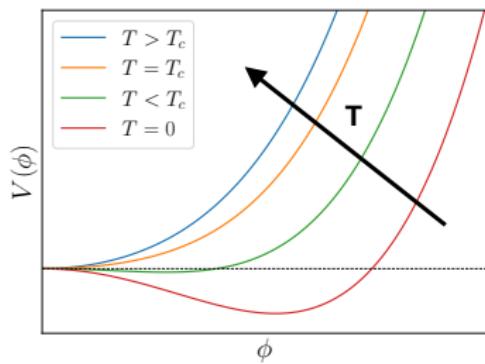
(Credits: Lisa Biermann)

- Strong First Order PTs required to explain EW Baryogenesis
 \Rightarrow Matter-antimatter asymmetry.

(Sakharov 1967)

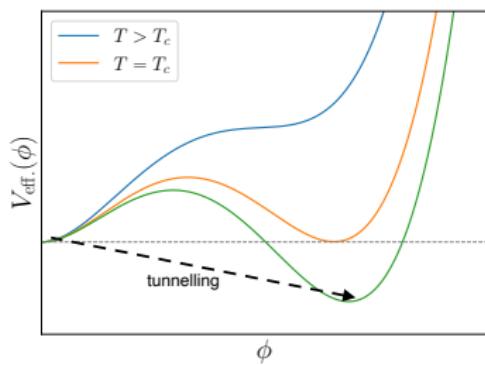
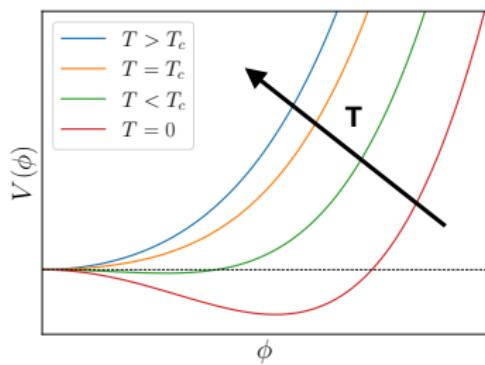
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- SM predicts smooth crossover for the Higgs mass, **NO FOPTs!**
⇒ **insufficient** for the required baryogenesis.



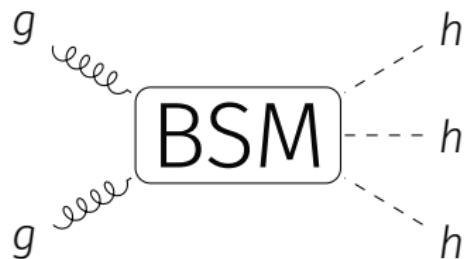
ELECTROWEAK PHASE TRANSITIONS

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⇒ insufficient for the required baryogenesis.



- Modifications to the scalar potential / couplings ⇒ modified EW vacuum structure ⇒ Strong FOPTs.

THE MORE, THE MERRIER?



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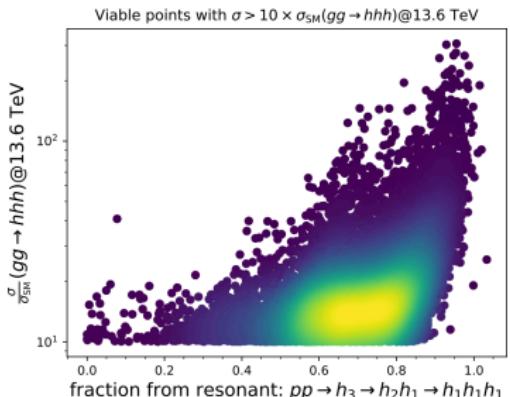
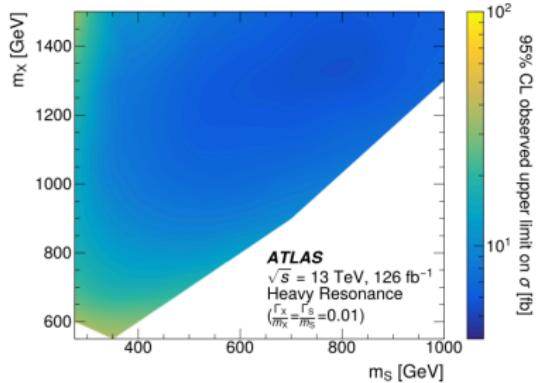
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- Enhancements in σ_{hhh}^{ggF}

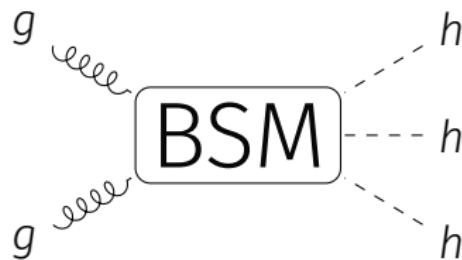
hhh ENHANCEMENTS



(ATLAS 2024; Karkout et al. 2024)

- Upper limit on SM **hhh** cross-section = **59 fb**.

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(Delgado et al. 2023; Anisha et al. 2024)

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- Enhancements in $\sigma_{hhh}^{ggF} \sim \mathcal{O}(100)$ events at HL-LHC, can be relevant at FCC- hh .

(Papaefstathiou et al. 2019; Papaefstathiou et al. 2021; Papaefstathiou et al. 2016; Fuks et al. 2016; ATLAS 2024)

METHODOLOGY

THE SCALAR EXTENSIONS

$$\begin{aligned} V_{\text{2HDM}} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \cancel{m_{12}^2} (\Phi_1^\dagger \Phi_2 + \text{h.c.}) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 \\ & + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \frac{\lambda_5}{2} \left[(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.} \right] \end{aligned} \quad (\text{softly broken } \mathbb{Z}_2 \text{ symmetry})$$

R2HDM : $m_{11}^2, m_{22}^2, \cancel{m_{12}^2}, \lambda_{1,\dots,4}, \lambda_5 \in \mathbb{R}$ (CP-Conserving)

C2HDM : $m_{11}^2, m_{22}^2, \lambda_{1,\dots,4} \in \mathbb{R}, \cancel{m_{12}^2}, \lambda_5 \in \mathbb{C}$ (CP-Violating)

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Next-to-Minimal 2HDM (**N2HDM**): R2HDM + $\boxed{\Phi_S} \leftarrow \text{Singlet}$

$$V_{\text{N2HDM}} = V_{\text{R2HDM}} + \frac{1}{2} m_S^2 \Phi_S^2 + \frac{\lambda_6}{8} \Phi_S^4 + \frac{\lambda_7}{2} (\Phi_1^\dagger \Phi_1) \Phi_S^2 + \frac{\lambda_8}{2} (\Phi_2^\dagger \Phi_2) \Phi_S^2$$

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- **R2HDM:** 2 CP-Even neutral mass eigenstates (h, H)

$$m_h \approx 125 \text{ GeV} < m_H$$

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- **C2HDM** and **N2HDM** : 3 neutral mass eigenstates (H_1, H_2, H_3).

$$m_{H_1} \cong m_h \approx 125 \text{ GeV} < m_{H_2} < m_{H_3}$$

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- Parameter scans:

⇒ **ScannerS**: Vary exotic Higgs masses, mixing angles.

⇒ **HiggsTools**: Apply theoretical, experimental constraints

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THE SCALAR EXTENSIONS

- **R2HDM:** 2 CP-Even neutral mass eigenstates (h, H).

$$m_h \approx 125 \text{ GeV} < m_H$$

- **C2HDM** and **N2HDM** : 3 neutral mass eigenstates (H_1, H_2, H_3).

$$m_{H_1} \cong m_h \approx 125 \text{ GeV} < m_{H_2} < m_{H_3}$$

- Parameter scans:

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- **FeynRules** ⇒ **MadGraph_aMC@NLO**: Model implementations, generate $hh(h)$ cross-sections.

(Alloul et al. 2014; Degrande et al. 2012; Darmé et al. 2023; Alwall et al. 2014)

PHASE TRANSITIONS WITH BSMPT

- Model-independent implementation of the one-loop daisy-resummed effective potential at finite temperature.

$$V_{\text{eff.}}(T) = \underbrace{V_0}_{\text{tree-level}} + \underbrace{V_{\text{CW}}}_{\text{One-loop potential} \\ \textit{Coleman-Weinberg}} + \underbrace{V_{\text{CT}}}_{\text{Counter-term} \\ \text{potential}} + \underbrace{V_T(T) + V_{\text{daisy}}(T)}_{T-\text{dependent}}$$

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$$\xi(T) = \frac{v_{\text{EW}}(T)}{T}$$

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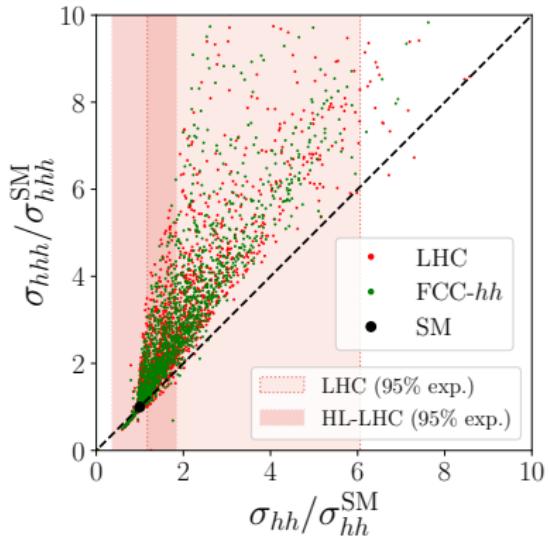
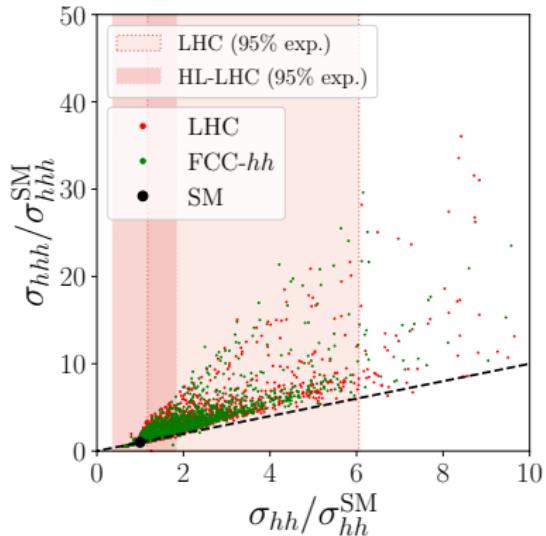
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- Minimising $V_{\text{eff.}}$ $\Rightarrow (g_{hhh}, g_{hhhh}, \dots) \Rightarrow \text{MadGraph}$

RESULTS

R2HDM AT THE LHC AND FCC- hh

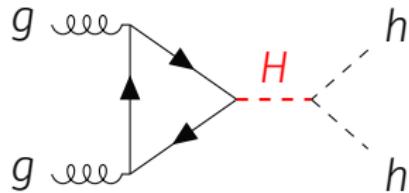


(CMS 2022)

- **hhh enhanced** compared to **hh**, although clearly correlated!
- Enhancements generalise to FCC- hh !

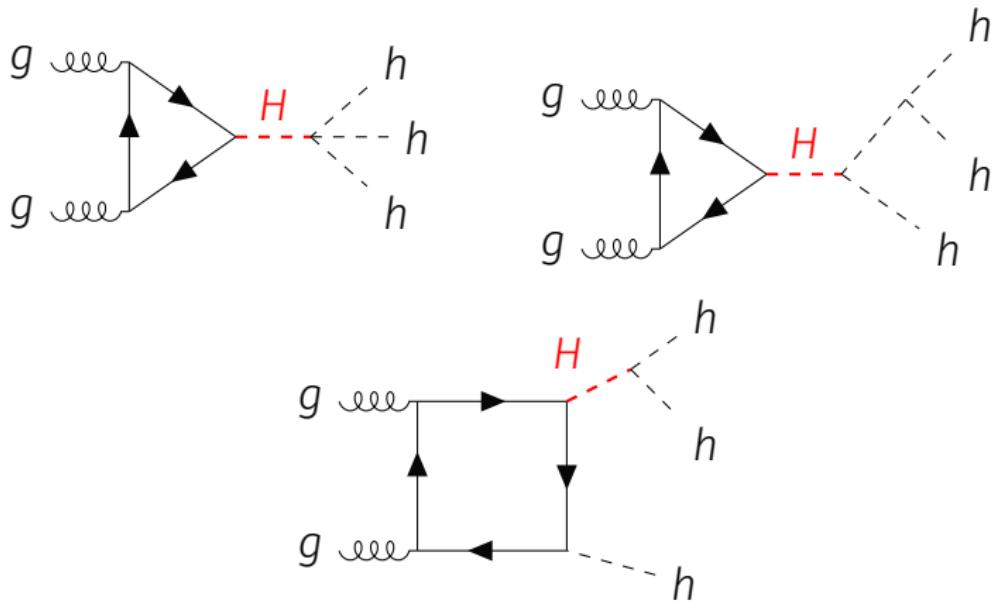
ENHANCING hh/hhh (R2HDM)

Resonant contributions to $\textcolor{red}{hh}$

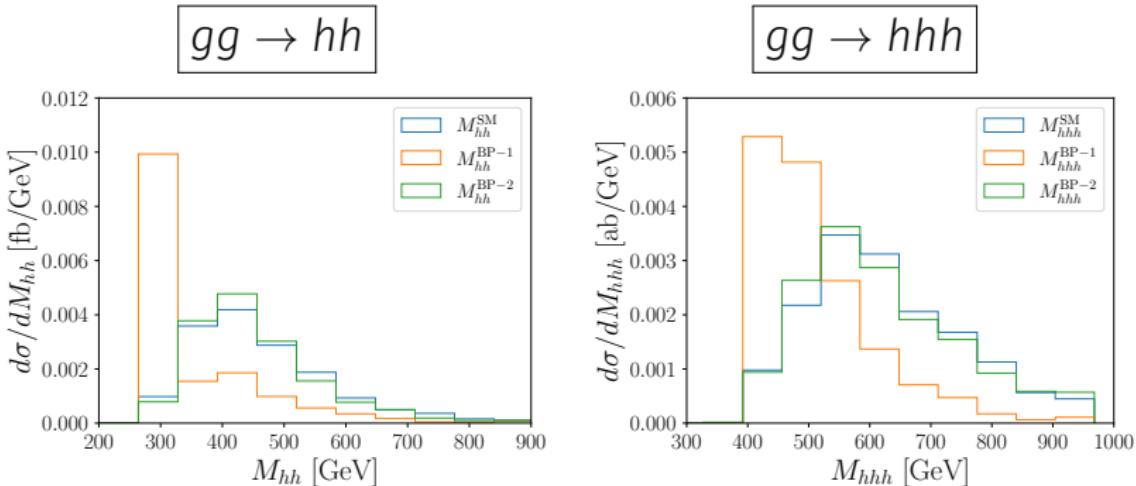


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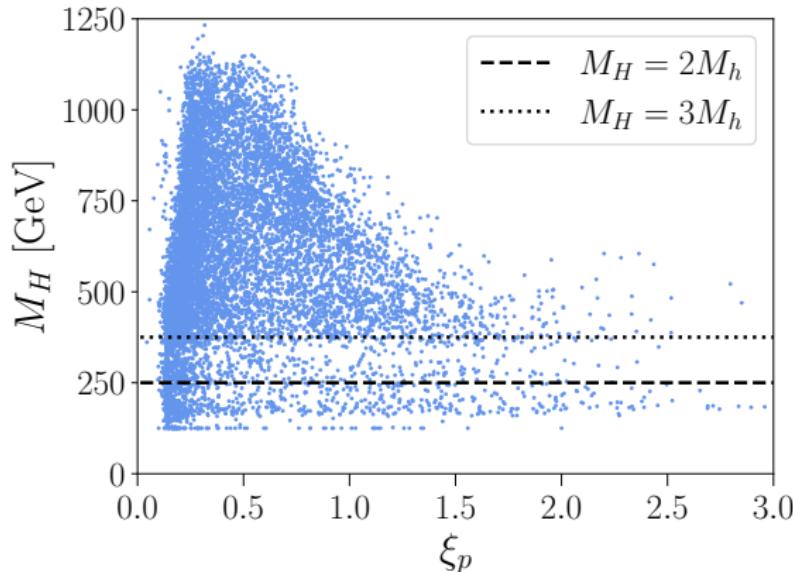
ENHANCEMENTS IN R2HDM



- BP-1: largely enhanced ($m_H \simeq 2m_h$).
- BP-2: SM-like.

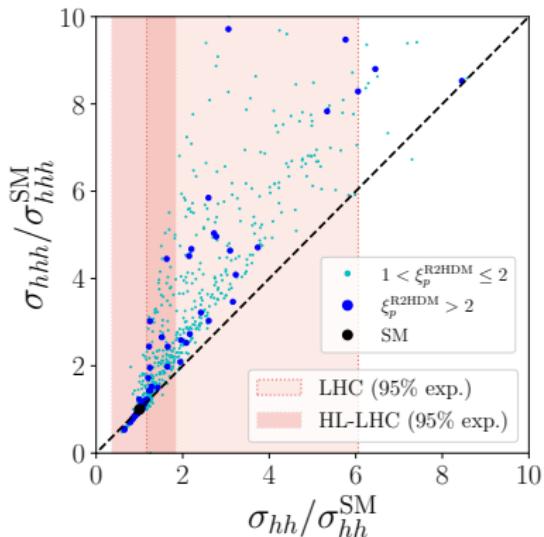
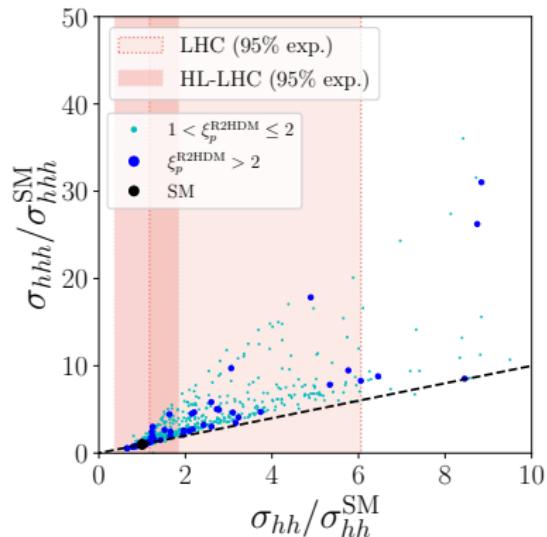
BP	$\sigma_{hh}/\sigma_{hh}^{\text{SM}}$	$\sigma_{hhh}/\sigma_{hhh}^{\text{SM}}$	M_H [GeV]	g_{hhH} [GeV]	g_{hhhH}
BP-1	3.24	15.26	274.29	75.28	0.203
BP-2	1.02	1.02	469.30	-7.11	-0.011

MASS SPECTRA OF R2HDM



- EWPTs driven by the physics of light dofs.
- ⇒ **Stronger** phase transitions proceed via **lighter** spectra!

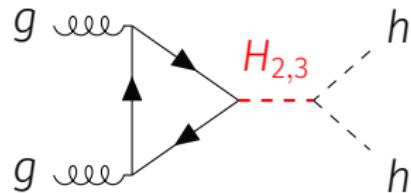
R2HDM ($\xi_p \geq 1$)



⇒ Neutral Higgs rates alone **NOT** indicative of the strength of EWPTs.

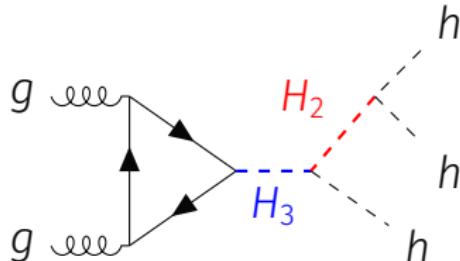
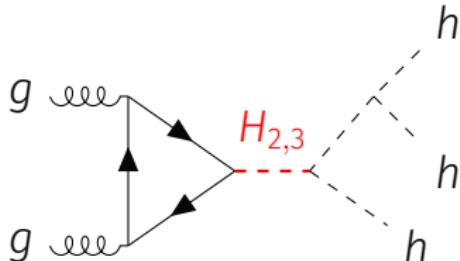
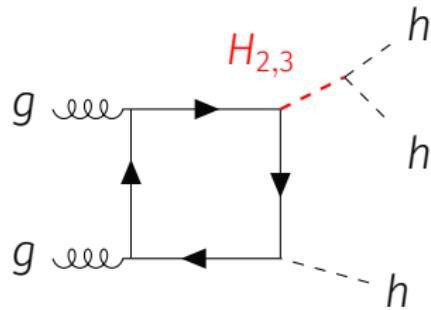
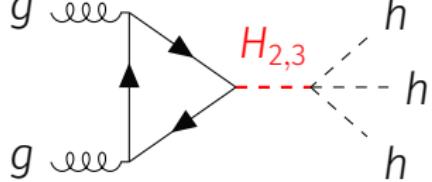
ENHANCING hh/hhh (3 DOFS)

Resonant contributions to **hh**

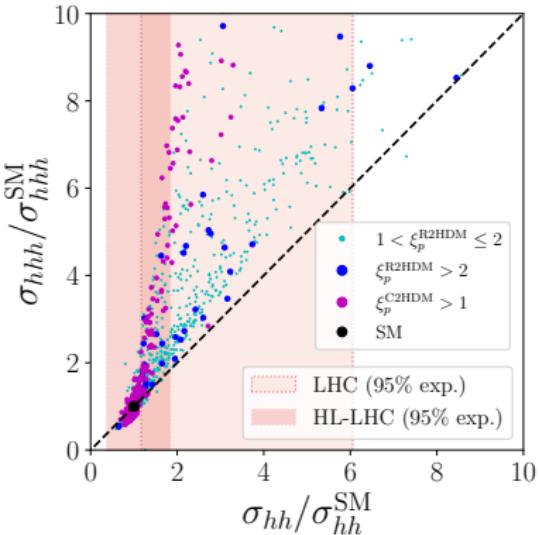
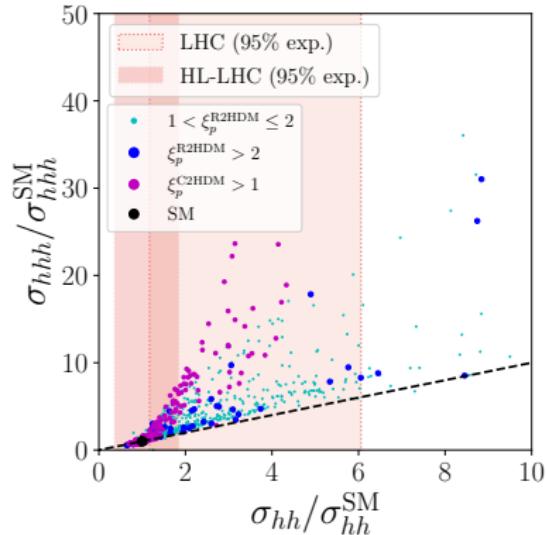


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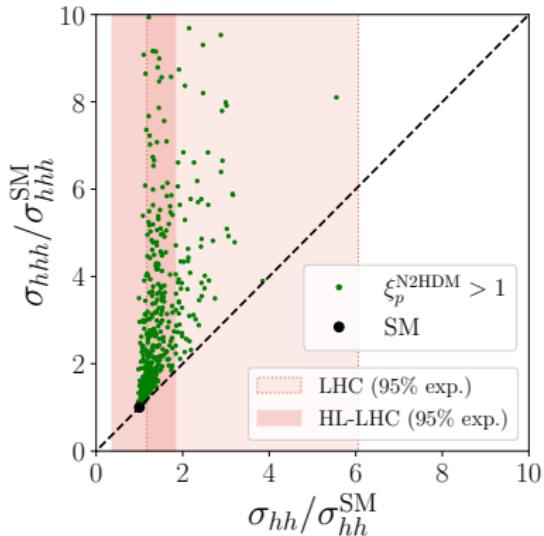
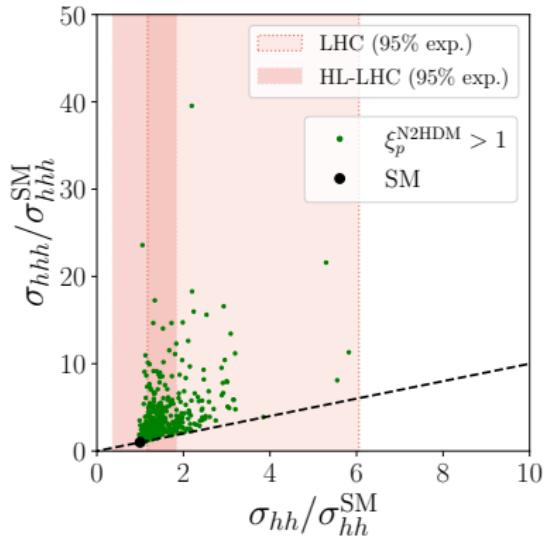
Resonant contributions to **hhh**



R2HDM + C2HDM



- Additional dof \Rightarrow hhh more enhanced.
- Stringent EDMs \Rightarrow Minimal CP admixture ($\lesssim 10\%$), thus no dramatic changes.



- The **additional dof** enhances **hhh** , like C2HDM.
- Enhancements $\sim 10 - 25$ in **hhh** , within HL-LHC **hh** sensitivity
 \Rightarrow can be accessible in FCC- **hh** !

SUMMARISING

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Thank you!