

Non-decoupling scalars at future detectors

[arXiv:2409.18177 w/ Dave Sutherland]

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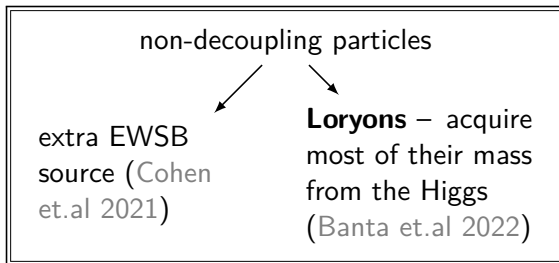
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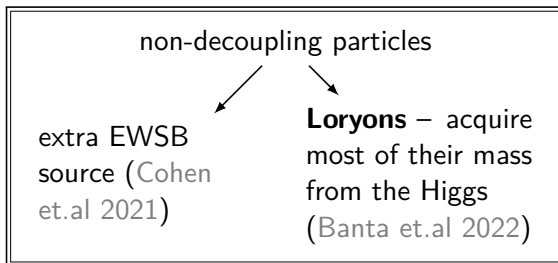
What is the nature of electroweak symmetry breaking?

Models vastly different from SM prediction remain viable ...



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Loryons {
are capped at the TeV scale by unitarity
can be scalars or vector-like fermions
are a finite target for future lepton colliders

The Loryon mass spectrum

$$\mathcal{L}_{\text{mass}} = - \underbrace{(m_{\text{ex}}^2 + \lambda_{h\phi} |H|^2)}_{M^2} |\Phi|^2 - \lambda'_{h\phi} (H^\dagger T^a H) (\Phi^\dagger T^a \Phi) - \lambda''_{h\phi} (\tilde{\Phi}^\dagger T^a \Phi) (H^\dagger T^a \tilde{H} + \text{h.c.})$$

- $M^2 = m_{\text{ex}}^2 + \frac{1}{2} \lambda_{h\phi} v^2$ Common mass of each component
- $f = \frac{\lambda_{h\phi} v^2}{2M^2}$ Fraction of mass obtained from Higgs
- $r_1 = \frac{\lambda'_{h\phi} v^2}{4M^2}$ Mass splitting parameter
- $r_2 = \frac{\lambda''_{h\phi} v^2}{4M^2}$ Additional mass splitting for $|Y| = \frac{1}{2}$ irreps

m_{ex} is an explicit mass term

Non-decoupling theories require HEFT

$$\text{SM} \subset \text{SMEFT} \subset \text{HEFT}$$

SMEFT \Rightarrow Expand about $|\Phi| = 0$

HEFT \Rightarrow Expand about $|\Phi| = v$

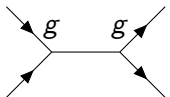
Integrate out a singlet S at tree-level,

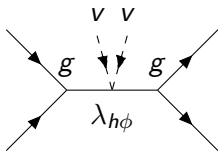
$$\mathcal{L}_{\text{UV}} = \frac{1}{2}(\partial S)^2 - gSJ - \frac{1}{2}M^2(|\Phi|^2)S^2.$$

Non-decoupling theories require HEFT

Integrate out a singlet S at tree-level,

$$\mathcal{L}_{UV} = \frac{1}{2}(\partial S)^2 - gSJ - \frac{1}{2}M^2(|\Phi|^2)S^2.$$


$$= \frac{g^2 J^2}{M^2(|\Phi|^2)}$$


$$= \frac{-g^2 J^2}{M^2(|\Phi|^2)} \left(\frac{\lambda_{h\phi} v^2}{M^2(|\Phi|^2)} \right)$$

Non-decoupling theories require HEFT

The top diagram shows a tree-level exchange between two pairs of external lines. Each pair of lines meets at a vertex labeled g . A horizontal line connects the two vertices. This is equated to the expression $\frac{g^2 J^2}{M^2(|\Phi|^2)}$.

The bottom diagram shows a similar tree-level exchange, but with a loop correction. Two dashed lines labeled v form a loop on the horizontal exchange line. A vertex labeled $\lambda_{h\phi}$ is attached to the loop. This is equated to the expression $\frac{-g^2 J^2}{M^2(|\Phi|^2)} \left(\frac{\lambda_{h\phi} v^2}{M^2(|\Phi|^2)} \right)$.

Expand around $|\Phi| = 0$, à la SMEFT;

$$\Rightarrow \mathcal{L}_{\text{EFT}} = \frac{g^2 J^2}{M^2(|\Phi|^2)} \left(1 - \frac{\lambda_{h\phi} v^2}{M^2(|\Phi|^2)} + \left(\frac{\lambda_{h\phi} v^2}{M^2(|\Phi|^2)} \right)^2 - \dots \right)$$

$$\Rightarrow 2f = \frac{\lambda_{h\phi} v^2}{M^2(|\Phi|^2)} < 1$$

Mass spectrum of charged multiplets

Real triplet ($Y = 0$)

$$\begin{pmatrix} H^+ \\ H^0 \\ H^- \end{pmatrix}$$

Inert 2HDM ($Y = \frac{1}{2}$)

$$\begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(H + iA) \end{pmatrix}$$

Masses

$$m_{H^+}^2 = M^2(1 - r_1)$$

$$m_{H^0}^2 = M^2$$

$$m_{H^-}^2 = M^2(1 + r_1)$$

$$m_{H^\pm}^2 = M^2 \left(1 - \frac{1}{2}r_1 \right)$$

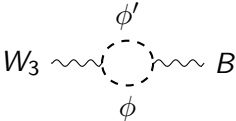
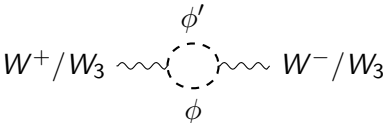
$$m_H^2 = M^2 \left(1 + \frac{1}{2}r_1 + 2r_2 \right)$$

$$m_A^2 = M^2 \left(1 + \frac{1}{2}r_1 - 2r_2 \right)$$

Neutral singlet: $m_S^2 = M^2$

Oblique parameters measure mass splittings

$$M^2 = m_{\text{ex}}^2 + \frac{1}{2} \lambda_{h\phi} v^2 \quad r_1 = \frac{\lambda'_{h\phi} v^2}{4M^2} \quad r_2 = \frac{\lambda''_{h\phi} v^2}{4M^2}$$

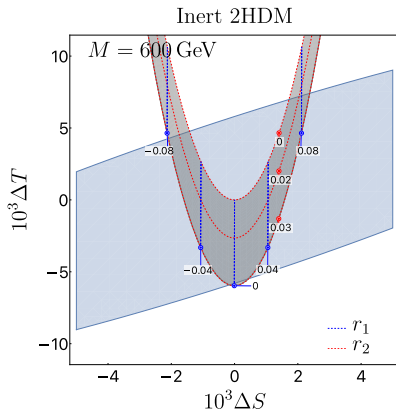
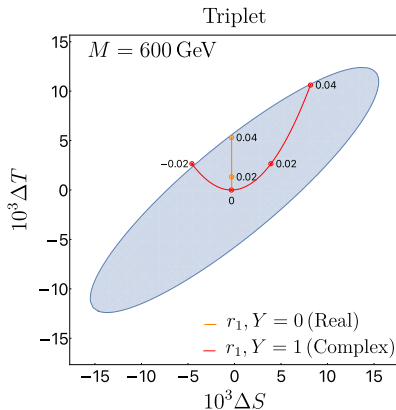
Observable	Representative diagram	Scaling
S		$r_1 YC(j)$ or $r_2^2 YC(j)$
T		$M^2 r_1^2 C(j)$ or $M^2 r_2^2 C(j)$

Impose \mathbb{Z}_2 symmetry: study deviations to gauge 2-pt functions at 1-loop.

$$C(j) = [(T^3)^2] = \frac{2}{3} j(j + \frac{1}{2})(j + 1)$$

Constraining r_1 and r_2 at FCC-ee

$$r_1 = \frac{\lambda'_{h\phi} v^2}{4M^2} \quad r_2 = \frac{\lambda''_{h\phi} v^2}{4M^2}$$

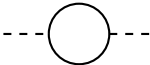
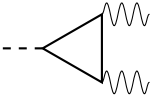
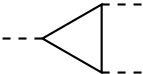


FCC-ee ellipse: (de Blas et.al 2021)

$\Rightarrow \sim 10\%$ sensitivity for 2HDM splittings, smaller for triplets.

Higgs coupling modifiers provide indirect bounds

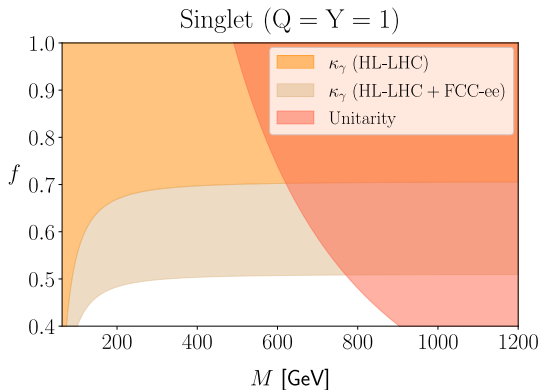
$$f = \frac{\lambda_{h\phi} v^2}{2M^2} > 0.5 \quad M^2 = m_{\text{ex}}^2 + \frac{1}{2} \lambda_{h\phi} v^2$$

Observable	Representative diagram	Scaling
κ_h		$M^2 f^2 d(j)$
κ_γ		$f (C(j) + Y^2 d(j))$
κ_λ		$M^4 f^3 d(j)$

$$C(j) = [(T^3)^2] = \frac{2}{3} j(j + \frac{1}{2})(j + 1),$$

$$d(j) = 2j + 1$$

κ_γ – Any charged Loryon can be found at FCC-ee ¹

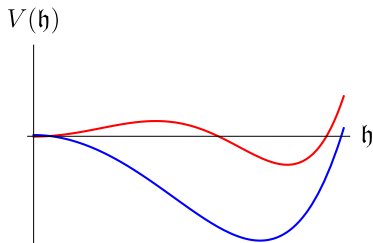


Using 2σ projected κ_γ sensitivities from (Tab. 4.2, Abada et.al 2022).
 \Rightarrow sensitive to everything above $f > 0.5$.

¹or similar machine

Electroweak Baryogenesis

- Baryogenesis could be explained by a strong first order phase transition (SFOPT) in the early Universe (see Quiros 1999, Croon 2023 for reviews).
- Not possible in SM, but adding scalars induces potential barrier (enhances h^3 term).



SFOPT:

$$v_{\text{nuc}}/T_{\text{nuc}} \gtrsim 1,$$
$$100 < S_3/T_{\text{nuc}} < 200,$$
$$S_3 \equiv \text{bounce action}.$$

strong transition ensures baryon asymmetry not washed out at later time. ▶

Gravitational wave production

- During transition, bubbles of the new phase collide
⇒ produce gravitational wave (GW) background.
- Determined by the energy released (α) and the duration of the phase transition ($\sim \beta$),

$$\alpha = \left(\Delta V - \frac{T_{\text{nuc}}}{4} \Delta \frac{dV}{dT} \right) / \frac{g_{\text{eff}} \pi^2 T_{\text{nuc}}^4}{30},$$

$$\beta/H_* = \left. \frac{dS_3}{dT} \right|_{T_{\text{nuc}}} - \frac{S_3}{T_{\text{nuc}}}.$$

(Caprini et.al 2016, 2020)

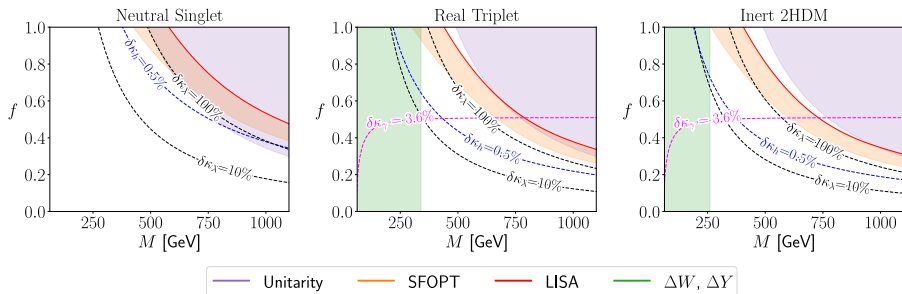
- Approx bounds for LISA: $\log(\beta/H_*) - 1.2 \log(\alpha) < 8.8$

(Banta 2022)

$g_{\text{eff}} \equiv$ effective relativistic d.o.f

SFOPT/GW constraints

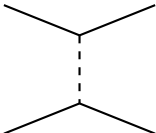
$$f = \frac{\lambda_{h\phi} v^2}{2M^2} > 0.5 \quad M^2 = m_{\text{ex}}^2 + \frac{1}{2} \lambda_{h\phi} v^2$$



Bounds for multiplets with larger d.o.f will move towards the bottom left.

following (Banta 2022)

- Motivation: non-decoupling physics may have important implications in understanding the **nature of EWSB**.
- Pheno: scalar Loryons can **induce a SFOPT** in the early Universe – potential source of baryogenesis – and a residual GW background.
- Search: present a **finite target for future colliders** – virtually all of the parameter space accessible by FCC-hh.

Observable	Representative diagram	Scaling
Unitarity	 A Feynman diagram representing a 2 to 2 scattering process. It consists of two incoming lines from the left and two outgoing lines to the right. A vertical dashed line connects the two vertices, representing the exchange of a Higgs boson.	$M^3 f^2$

Constraint dominated by $2 \rightarrow 2$ elastic scattering of Loryon with exchange of a Higgs – only tree-level diagram that grows as $\lambda_{h\phi}^2$.

Contributions of an arbitrary multiplet to the oblique parameters W and Y are given by;

$$\Delta W = \frac{1}{2\rho} \underbrace{\frac{43}{180} \frac{g^2}{(4\pi)^2} \frac{m_W^2}{M^2}}_{\simeq 1.2 \times 10^{-5} \left(\frac{600 \text{ GeV}}{M}\right)^2} \times j(j + \frac{1}{2})(j + 1),$$

$$\Delta Y = \frac{1}{2\rho} \underbrace{\frac{43}{60} \frac{g'^2}{(4\pi)^2} \frac{m_W^2}{M^2}}_{\simeq 1.0 \times 10^{-5} \left(\frac{600 \text{ GeV}}{M}\right)^2} \times Y^2(j + \frac{1}{2}).$$

A lower bound for the Real Triplet and Inert 2HDM models were found using 2d sensitivities for ΔW and ΔY (de Blas et.al 2016).

$$V_{\text{eff}}(\mathfrak{h}) = V_0(\mathfrak{h}) + \underbrace{\sum_i n_i V_{\text{CW,bos}}(m_i^2(\mathfrak{h})) + n_t V_{\text{CW,fer}}(m_t^2(\mathfrak{h})) + n_\Phi V_{\text{CW,bos}}(m_\Phi^2(\mathfrak{h}))}_{\text{zero temperature corrections}} + \underbrace{\sum_i n_i V_{\text{T,bos}}(m_i^2(\mathfrak{h}), T) + n_t V_{\text{T,fer}}(m_t^2(\mathfrak{h}), T) + n_\Phi V_{\text{T,bos}}(m_\Phi^2(\mathfrak{h}))}_{\text{finite temperature corrections}}$$

$$i = \{W_T, W_L, Z_T, Z_L, h, \chi, \gamma_L\}$$

$$n_i \text{ (degrees of freedom)} = \{4, 2, 2, 1, 1, 3, 1\}$$

$$v \rightarrow \mathfrak{h} \equiv v + h$$

Field-dependent masses are shifted by contributions of hard thermal loops;

$$\Pi_i = \frac{\partial^2 V_T}{\partial f_i^2},$$

e.g, the Higgs and Goldstones shift by,

$$\Pi_h = \Pi_\chi = \frac{1}{24} T^2 \left(\frac{3}{2} g'^2 + \frac{9}{2} g^2 + 12\lambda_{hh} + 6y_t^2 + n_{\text{Loryons}}\lambda \right).$$

We use the Parwani scheme, inserting $m_i^2(\mathfrak{h}) \rightarrow m_i^2(\mathfrak{h}) + \Pi_i(\mathfrak{h}, T)$ directly into $V_{\text{eff}}(\mathfrak{h})$ (Parwani 1991).