

Triboson production and interplay with associated Higgs production

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THE
ROYAL
SOCIETY

Outline

- ① Introduction
- ② The trilepton channel
- ③ The $e^+\mu^+jj$ channel
- ④ Conclusions

Introduction

① Introduction

② The trilepton channel

③ The $e^+\mu^+jj$ channel

④ Conclusions

Triboson production

Current status

- **NLO QCD** corrections known for all on-/off-shell processes
Binoth, Ossola, Papadopoulos, Pittau '08
Campanario, Hankele, Oleari, Prestel, Zeppenfeld '09
- **NLO QCD** on-shell $WWW + 0, 1j$ multijet merged
Höche, Krauss, Pozzorini, MS, Thompson, Zapp '14
- **NNLO QCD** for $\gamma\gamma\gamma$
Chawdhry, Czakon, Mitov, Poncelet '19
Kallweit, Sotnikov, Wieseemann '20
- corrections are typically large due to gluon-induced channels opening
- beware of single-top topologies in some channels in 5F

Triboson production

Current status

- **NLO EW** corrections known for all on-shell processes
Nhung et.al '13, Yong-Bai et.al '15, '16; Hong et.al '16
Dittmaier, Huss, Knippen '17
- **NLO EW** corrections for off-shell WWW in all trilepton channels
MS '18
- **NLO EW** corrections for off-shell WWW in triple pole approx.
Dittmaier, Knippen, Schwan '19
- large photon-induced corrections,
can compensate EW Sudakov corrections (depending on jet veto)

The trilepton channel

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- 4 Conclusions

The trilepton channel

MS '18

- contrihs from 0 SFOS ($e^-\mu^+\mu^+\bar{\nu}_e\nu_\mu\nu_\mu$), 1 SFOS ($e^-e^+\mu^+\bar{\nu}_e\nu_\mu\nu_\mu$) and 2 SFOS ($e^-e^+e^+\bar{\nu}_e\nu_\mu\nu_\mu$) processes, and $e \leftrightarrow \mu$

0 SFOS $e^-\mu^+\mu^+\bar{\nu}_e\nu_\mu\nu_\mu$

WWW

WH[$\rightarrow 2\ell 2\nu$]

WZ

1 SFOS $e^-e^+\mu^+\bar{\nu}_e\nu_\mu\nu_\mu$

WWW + WZZ

WH[$\rightarrow 2\ell 2\nu$]

WZ

 $e^-e^+\mu^+\bar{\nu}_\mu\nu_\mu\nu_\mu$

WZZ

WH[$\rightarrow 2\ell 2\nu$]

WZ

 $e^-e^+\mu^+\bar{\nu}_\tau\nu_\tau\nu_\mu$

WZZ

WH[$\rightarrow 2\ell 2\nu$]

WZ

2 SFOS $e^-e^+e^+\bar{\nu}_e\nu_e\nu_e$

WWW + WZZ

WH[$\rightarrow 2\ell 2\nu$]

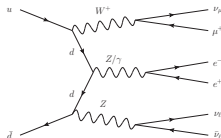
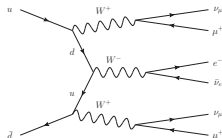
WZ

 $e^-e^+e^+\bar{\nu}_\mu/\tau\nu_\mu/\tau\nu_e$

WZZ

WH[$\rightarrow 2\ell 2\nu$]

WZ

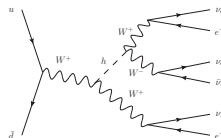
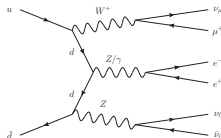
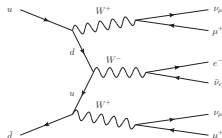


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	$e^-e^+\mu^+\bar{\nu}_\mu\nu_\mu\nu_\mu$	WZZ	$WH[\rightarrow 2\ell 2\nu]$	WZ
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2 SFOS	$e^-e^+e^+\bar{\nu}_e\nu_e\nu_e$	WWW + WZZ	$WH[\rightarrow 2\ell 2\nu]$	WZ
	$e^-e^+e^+\bar{\nu}_\mu/\tau\nu_\mu/\tau\nu_e$	WZZ	$WH[\rightarrow 2\ell 2\nu]$	WZ

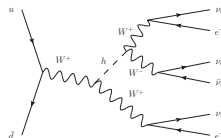
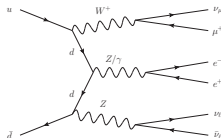
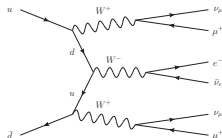


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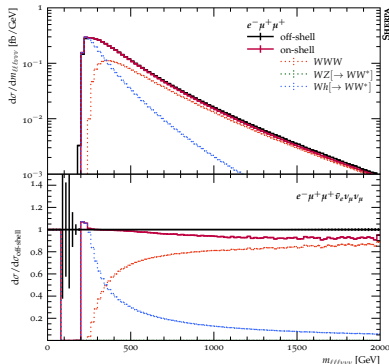


The trilepton channel

Selection	Cut	Value	
general	$p_T(\ell)$	$[20 \text{ GeV}, \infty)$	lepton acceptance
	$y(\ell)$	$[-2.5, 2.5]$	
	$\Delta R(\ell, \ell)$	$[0.2, \infty)$	
$\cancel{p}_T > 20 \text{ GeV}$	$\Delta\phi(\cancel{p}_T, \ell\ell\ell)$	$[\frac{5}{6}\pi, \pi]$	jet veto
1, 2 SFOS	$\cancel{p}_T$	$[50 \text{ GeV}, \infty)$	WZ veto
	$m_{\ell\ell}^{\text{SFOS}}$	$[0, 70 \text{ GeV}] \wedge [100 \text{ GeV}, \infty)$	

- cuts idealised from WWW [ATLAS '16](#)
- scale choice: $\mu = \sum m_{T,i}^W$ ambiguous in all channels, EW corrections largely scale independent: choose $\mu_R = \mu_F = 3 m_W$
- use NNPDF31_nlo_as_0118_luxqed for reliable γ PDF

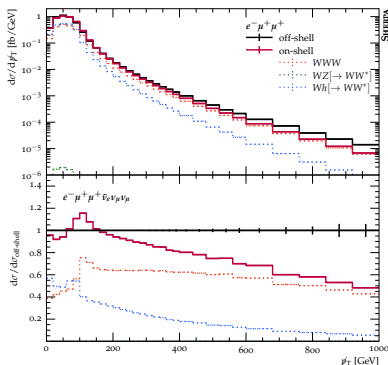
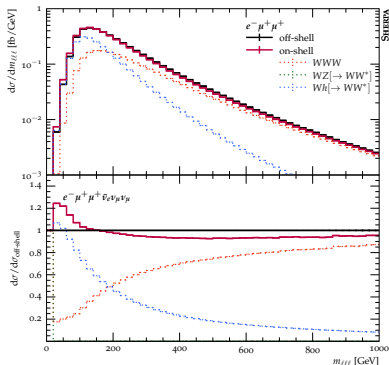
The trilepton channel – on-shell decomposition



$$m_{\ell\ell\ell\nu\nu} = m_{WWW}$$

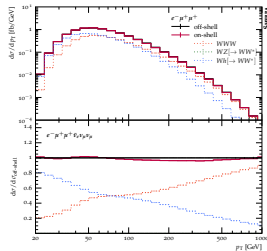
- due to presence of 3ν no W forced on-shell
- on-shell WWW not dominating for incl. xsec
- large cross section from WH , WZ negligible
- at larger m_{WWW} contribs from double (single) resonant

The trilepton channel – on-shell decomposition

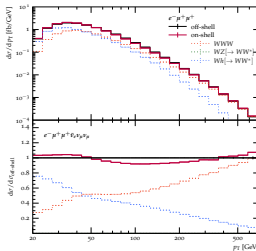


- on-shell approximation reasonable for $m_{\ell\ell}$
- large single and double resonant contris for MET

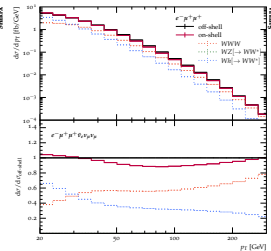
The trilepton channel – on-shell decomposition



1st lepton



2nd lepton

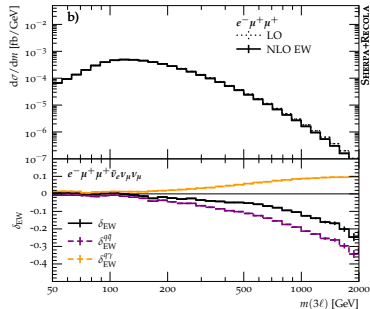
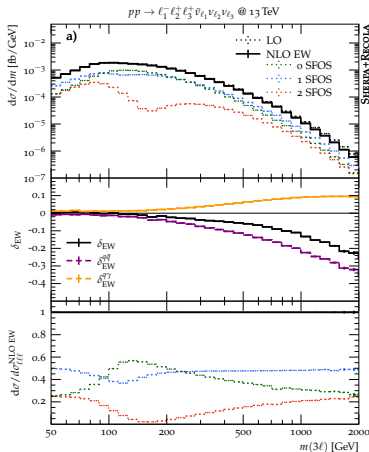


3rd lepton

- on-shell approximation reasonable for lepton p_T
- moderate impact of double (single) resonant contris

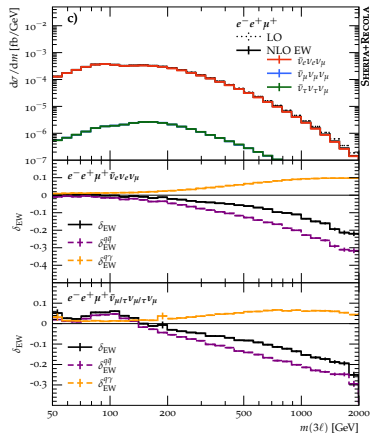
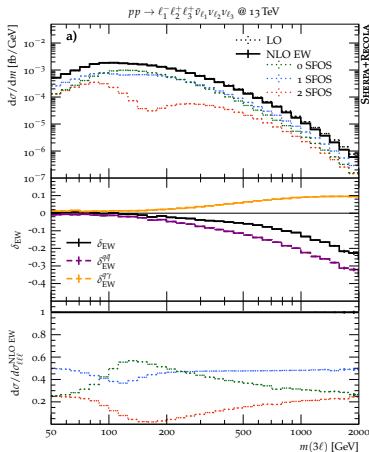
The trilepton channel – 0, 1, 2 SFOS decomposition

MS arXiv:1806.00307



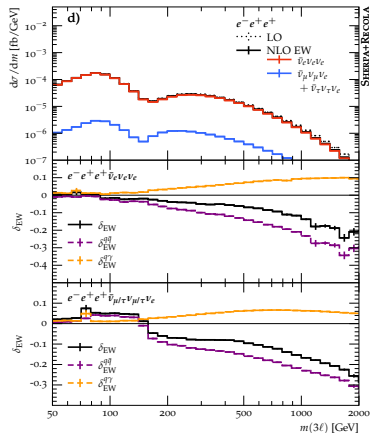
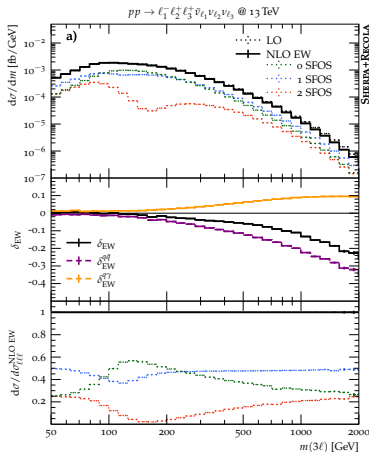
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The $e^+\mu^+jj$ channel

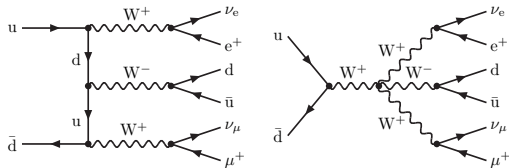
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The $e^+\mu^+jj$ channel

Denner, Pellen, MS, Schumann '24

$$pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj + X$$

- LO contributions
@ $\mathcal{O}(\alpha^6)$, $\mathcal{O}(\alpha_s \alpha^5)$,
and $\mathcal{O}(\alpha_s^2 \alpha^4)$

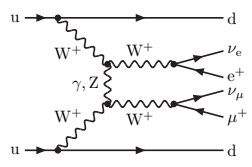
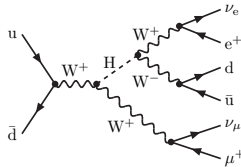
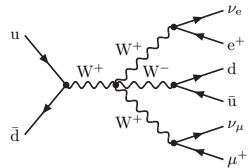
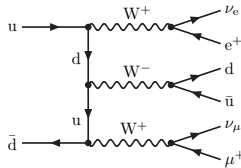


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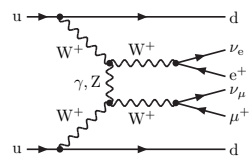
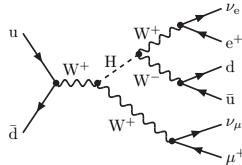
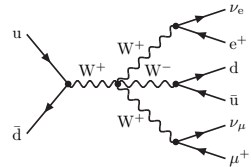
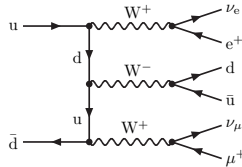
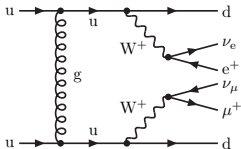


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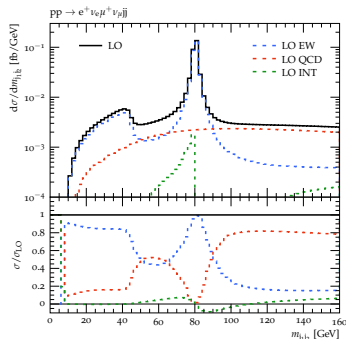
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The $e^+\mu^+jj$ channel @ LO

Fiducial phase space

- contribution of individual topologies varies throughout phase space, follow *WWW ATLAS '22*
- $p_{T,\ell} > 20 \text{ GeV}$, $|y_\ell| < 2.5$
 $m_{\ell\ell} \in [40, 400] \text{ GeV}$
- $p_{T,j} > 20 \text{ GeV}$, $|y_j| < 4.5$
 $m_{jj} \in [0, 160] \text{ GeV}$, $|\Delta y_{jj}| < 1.5$



	$\mathcal{O}(\alpha^6)$	$\mathcal{O}(\alpha_s\alpha^5)$	$\mathcal{O}(\alpha_s^2\alpha^4)$	sum
$\sigma_{LO} [\text{fb}]$	0.78549(9)	0.00732(1)	0.25925(3)	1.05206(9)
$\sigma/\sigma_{LO}^{\text{sum}} [\%]$	74.7	0.7	24.6	100

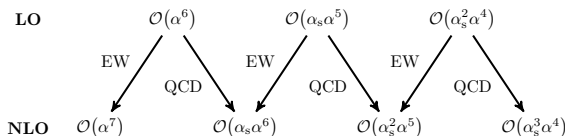
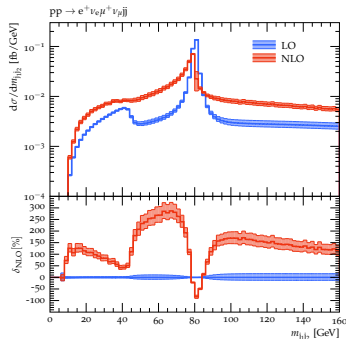
The $e^+\mu^+jj$ channel @ NLO

NLO corrections

- $\mathcal{O}(\alpha_s^3\alpha^4)$ pure QCD corr.
- $\mathcal{O}(\alpha_s^2\alpha^5)$ both EW and QCD corr.
- $\mathcal{O}(\alpha_s\alpha^6)$ both QCD and EW corr.
- $\mathcal{O}(\alpha^7)$ pure EW corr.

$$\mu_R = \mu_F = \sum m_T^W$$

NNPDF31_nlo_as_0118_luxqed



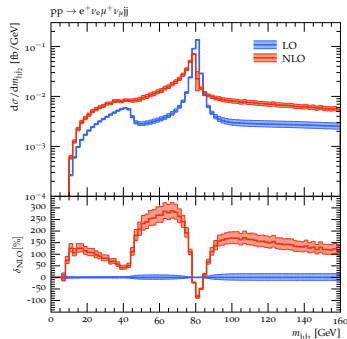
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	$\mathcal{O}(\alpha^7)$	$\mathcal{O}(\alpha_s\alpha^6)$	$\mathcal{O}(\alpha_s^2\alpha^5)$	$\mathcal{O}(\alpha_s^3\alpha^4)$	sum
$\delta\sigma[\text{fb}]$	-0.035(1)	0.305(1)	-0.0032(3)	0.2260(3)	0.493(2)
$\delta\sigma/\sigma_{\text{LO}}^{\text{sum}} [\%]$	-3.4	29.0	-0.30	21.5	46.9

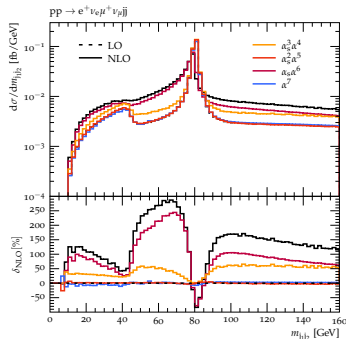
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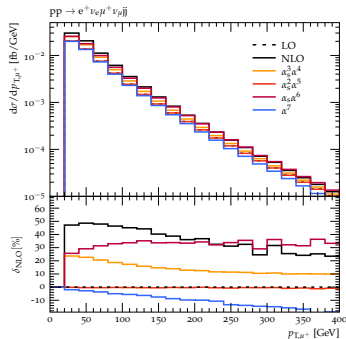
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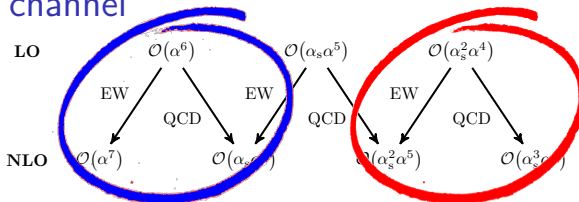
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The $e^+\mu^+jj$ channel



Decompose full result

- LO interference $\mathcal{O}(\alpha_s \alpha^5)$ (mostly) negligible, define

EW production $\mathcal{O}(\alpha^6) + \mathcal{O}(\alpha_s \alpha^6) + \mathcal{O}(\alpha^7)$

QCD production $\mathcal{O}(\alpha_s^2 \alpha^4) + \mathcal{O}(\alpha_s^3 \alpha^4) + \mathcal{O}(\alpha_s^2 \alpha^5)$

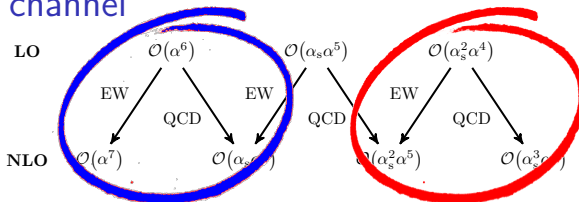
- caveat:

$\mathcal{O}(\alpha_s^2 \alpha^5)$ is still partially QCD corr. to LO interference $\rightarrow$ neglect

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$\rightarrow$ decompose further

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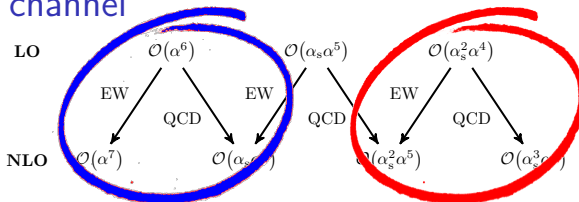
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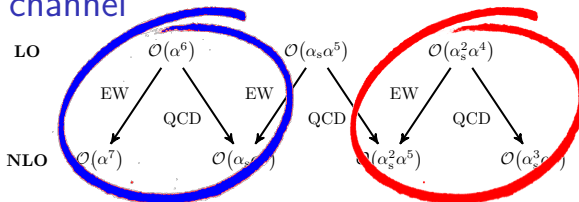
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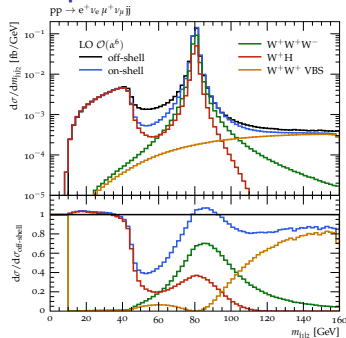
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The $e^+\mu^+jj$ channel – on-shell decomposition @ LO

Sample decomposition

- approximate off-shell result with incoherent sum of on-shell channels using spin-correlated decays in NWA Höche et.al '14
- different on-shell channels dominant in different regions,
- WWW nowhere $\gtrsim 70\%$

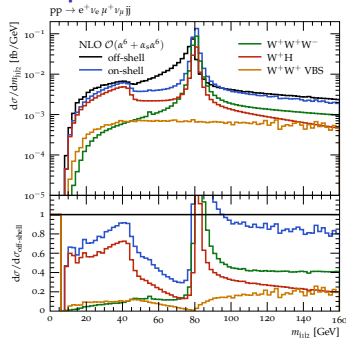


$\mathcal{O}(\alpha^6)$	off shell	on shell	on-shell subprocess			
Process		sum	WWW	WH	WZ	VBS
$\sigma_{\text{LO}}[\text{fb}]$	0.7917	0.7738	0.4207	0.3265	$5 \cdot 10^{-7}$	0.0266
$\sigma/\sigma_{\text{LO}}^{\text{off shell}}[\%]$	100	97.7	53.1	41.2	$7 \cdot 10^{-5}$	3.3

The $e^+\mu^+jj$ channel – on-shell decomposition @ NLO

Sample composition

- WWW contrib reduced by 4.8%
- VBS contrib increased by 4.4%, large K -factor driven by collinear radiation off forward jet forming new low- m_{jj} pair
- note: QCD corrections to $W \rightarrow q\bar{q}'$ decay not included here

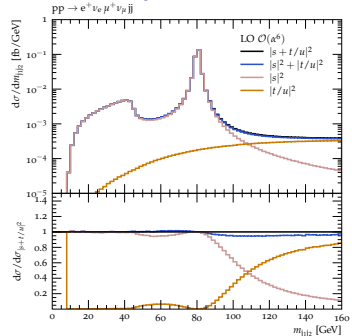


$\mathcal{O}(\alpha^6 + \alpha_s\alpha^6)$	off shell	on shell	on-shell subprocess			
Process		sum	WWW	WH	WZ	VBS
K_{NLO}	1.42	1.40	1.29	1.38	2.21	3.25
$\sigma/\sigma_{\text{NLO}}^{\text{off shell}} [\%]$	100	96.2	48.3	40.2	$2 \cdot 10^{-6}$	7.7

The $e^+\mu^+jj$ channel – s/t -channel decomposition

Sample composition

- decompose according to s or t/u -channel jet production
 - s $WWW + WH + WZ$ (coherent)
 - t/u VBS
- otherwise completely off-shell



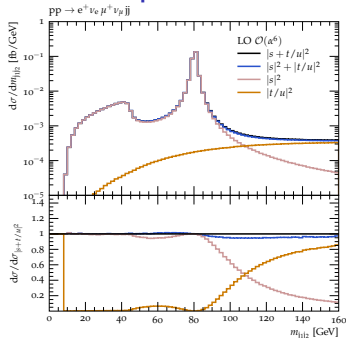
most partonic channels either s , t , or u ,
decompose remaining into incoherent sum, e.g.

$$\underbrace{ud \rightarrow e^+ \bar{\nu}_e \mu^+ \nu_\mu d \bar{u}}_{|s+t|^2} \longrightarrow \underbrace{ud \rightarrow e^+ \bar{\nu}_e \mu^+ \nu_\mu s \bar{c}}_{|s|^2} + \underbrace{us \rightarrow e^+ \bar{\nu}_e \mu^+ \nu_\mu d \bar{c}}_{|t|^2}$$

The $e^+\mu^+jj$ channel – s/t -channel decomposition

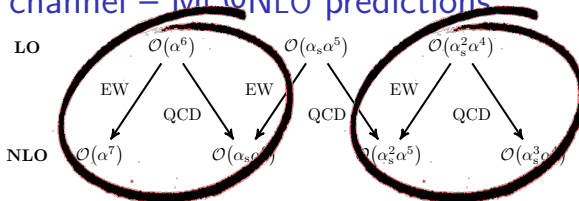
Sample composition

- decompose according to s or t/u -channel jet production
 - s $WWW + WH + WZ$ (coherent)
 - t/u VBS
- otherwise completely off-shell



$\mathcal{O}\alpha^6 + \alpha_s\alpha^6$	coherent	incoherent	subchannels	
Process	$ s + t/u ^2$	$ s ^2 + t/u ^2$	$ s ^2$	$ t/u ^2$
$\sigma_{\text{NLO}}[\text{fb}]$	1.091	1.084	0.998	0.086
$\sigma/\sigma_{\text{NLO}}^{\text{off shell}}[\%]$	100	99.4	91.5	7.9

The $e^+\mu^+jj$ channel – Mc@NLO predictions



Building an event generator

- separate into QCD and EW production
- build on s - t -channel decomposition in EW production, removes EW divergences from $\mathcal{O}(\alpha_s \alpha^6)$ QCD corr. to EW prod.
→ can use traditional Mc@NLO QCD as implemented in SHERPA for parton-shower matching, include EW corrections through EW_{virt} approximation

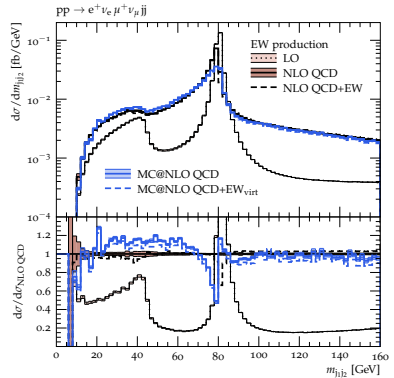
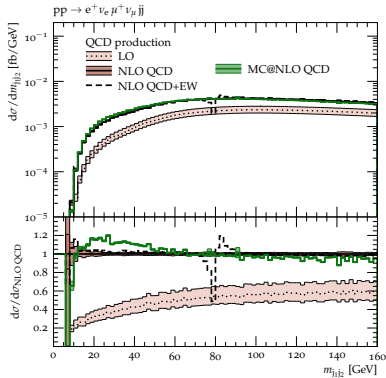
Höche, Krauss, MS, Siebert '11

Kallweit, Lindert, Pozzorini, MS '15

Three generators: ① QCD prod., ② s -ch. EW prod., ③ t -ch. EW prod.

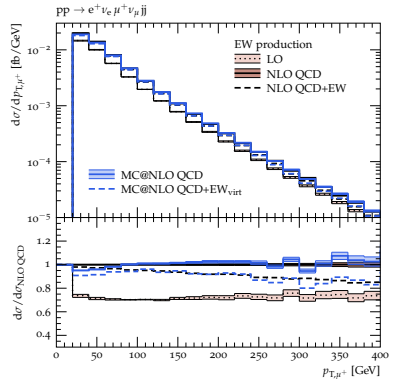
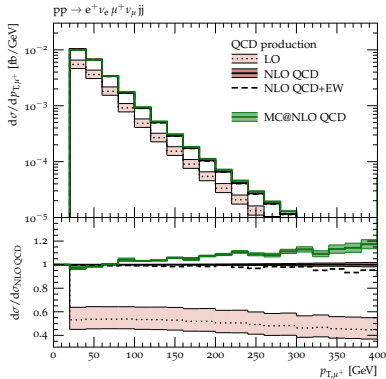
Denner, Pellen, MS, Schumann '24

The $e^+\mu^+jj$ channel – MC@NLO predictions



- large beyond-NLO corrections around W resonance
- $\mathcal{O}(\alpha_s^2 \alpha^5)$ has s -channel W/g interference, spurious shape feature

The $e^+\mu^+jj$ channel – MC@NLO predictions



- EW Sudakov correction for EW production well reproduced
- small corrections beyond NLO

Conclusions

- triboson signatures have to be computed off-shell due to their rich internal structure
- various resonant configurations present in (almost) all channels
 - always WWW and WH (WZ)
 - VBS in hadronic channels
 - WZZ in ≥ 1 OSSF channels
- a number of precision Monte-Carlo simulations for off-shell production exist and should be used for a reliable description
- QCD corrections are large, EW corrections are sizeable

Thank you!