

Recent results for dimension-eight SMEFT

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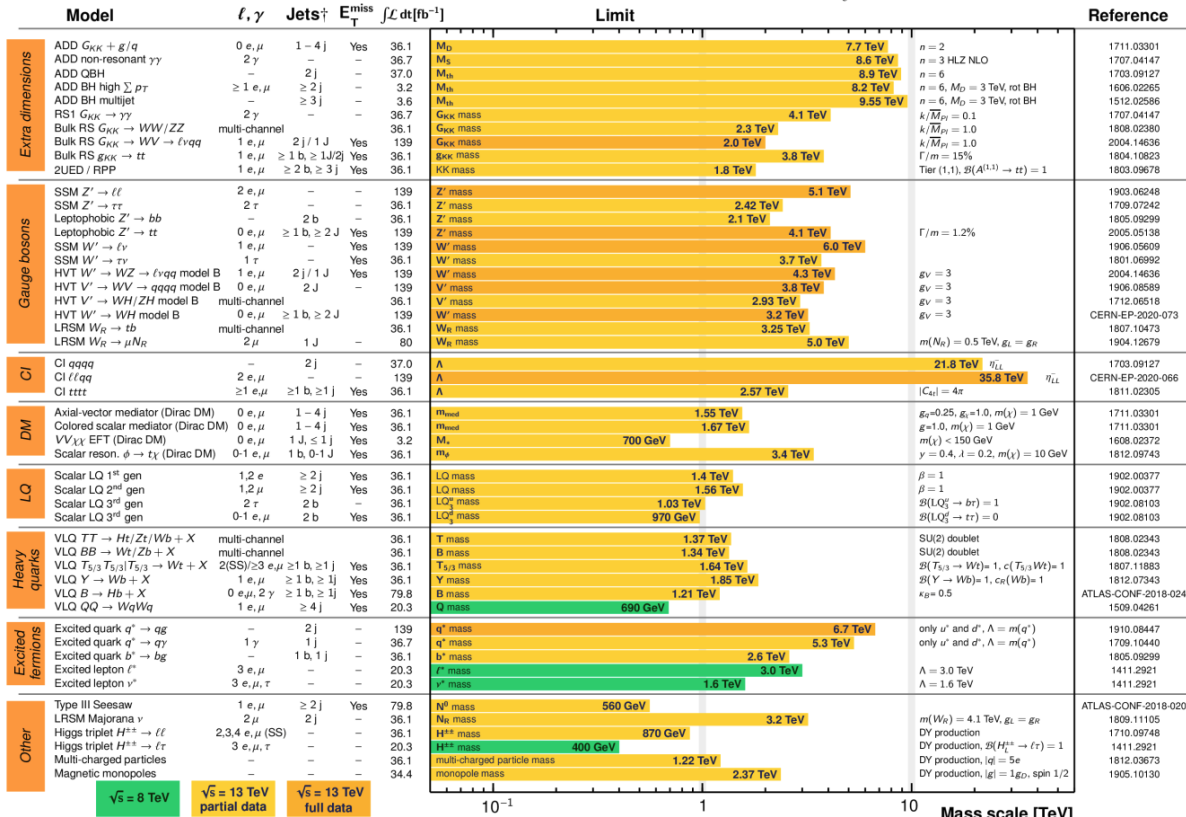
ATLAS Exotics Searches* - 95% CL Upper Exclusion Limits

Status: May 2020

ATLAS Preliminary

$$\int \mathcal{L} dt = (3.2 - 139) \text{ fb}^{-1}$$

$$\sqrt{s} = 8, 13 \text{ TeV}$$



*Only a selection of the available mass limits on new states or phenomena is shown.

† Small-radius (large-radius) jets are denoted by the letter j (J).

$\sqrt{s} = 8 \text{ TeV}$

$\sqrt{s} = 13 \text{ TeV}$

partial data

full data

10^{-1}

1

10

Mass scale [TeV]

10

10

10

10

10

10

10

10

10

10

10

10

10

10

10

The SMEFT

$$\mathcal{L}_d = c_i \mathcal{O}_i$$
$$[\mathcal{O}_i] = d$$

$$\Lambda \gg p$$

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{\mathcal{L}_6}{\Lambda^2} + \frac{\mathcal{L}_8}{\Lambda^4} + \mathcal{O}(1/\Lambda^6)$$

UV physics



p

EFT
Accessible scale



Bottom up: Write observables in terms of Wilson coeff; Global fits, etc with no mention of the UV



Top down: Calculate coefficients from a UV, translate EFT bounds into UV constraints

When does dimension-eight matter?

- Some observables are not captured by dimension-six operators:
 - Purely quartic anomalous gauge couplings;
 - Triple neutral gauge couplings;
 - Light-by-light scattering;
- Interpreting data in terms of models might necessitate dimension-eight corrections



Chala, Krause, Nardini 2018
Durieux, McCullough, Salvioni 2022

- No custodial breaking at tree and one-loop dim-6, but at one-loop dim-8

When does dimension-eight matter?

- Some observables are not captured by dimension-six operators:
 - Purely quartic anomalous gauge couplings;
 - Triple neutral gauge couplings;
 - Light-by-light scattering;
- Interpreting data in terms of models might necessitate dimension-eight corrections
- Theoretical considerations: positivity bounds, tree-loop mixing,...

Development at dimension-eight

- Physical and Green's basis developed

Murphy 2005.00059

Li, Ren, Shu, Xiao, Yu, Zheng 2005.00008

Chala, Carmona, GG, 2112.12724

- RGEs computed

Chala, GG, Ramos, Santiago 2106.05291

Huber, De Angelis 2108.03669

Bakshi, Chala, Diaz-Carmona, GG 2205.03301

Helset, Jenkins, Manohar; 2212.03253

Assi, Helset, Manohar, Pagès, Shen 2307.03187

Boughezal, Huang, Petriello 2408.15378

Bakshi, Chala, Diaz-Carmona, Ren, Vilches

2409.15408

- Observables

Kim, Martin, 2203.11976

Ellis, He, Xiao 2206.11676

Degrande, Li 2303.10493

Corbett, Desai, Eboli, Gonzalez-Garcia, Martines, Reimitz 2304.03305

- Matching of models:

Carmona, Lazopoulos, Olgoso, Santiago 2112.10787

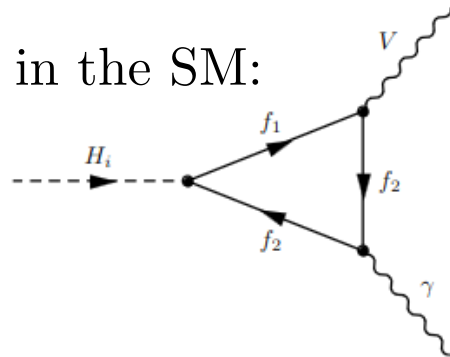
Fuentes-Martín, König, Pagès, Thomsen, Wilsch 2212.04510

Dawson, Forsslund, Schnubel 2404.01375

Adhikary, Biswas, Chakraborty, Englert, Spannowsky 2501.12160

Higgs decays in the SMEFT

Loop in the SM:



- Warsaw basis:

$$C_{h\gamma\gamma} = e^2 \left(\frac{C_{\phi W}}{g_2^2} + \frac{C_{\phi B}}{g_1^2} - \frac{C_{\phi WB}}{g_1 g_2} \right)$$

$$\mathcal{O}_{\phi X X'} = (\phi^\dagger \phi) X_{\mu\nu} X^{\mu\nu}$$

- Every dim-6 operator with a field-strength tensor is **necessarily generated at loop-level.**
 - *As it should, Higgs diphoton decay is loop-level in the SMEFT*

Higgs decays in the SMEFT

$$\mathcal{L}_{\text{SMEFT}} \supset C_{h\gamma\gamma} \frac{v}{\Lambda^2} h F_{\mu\nu} F^{\mu\nu}$$

$$C_{h\gamma\gamma}(m) = C_{h\gamma\gamma}(\Lambda) + \frac{\gamma_i C_i}{16\pi^2} \log\left(\frac{m}{\Lambda}\right)$$

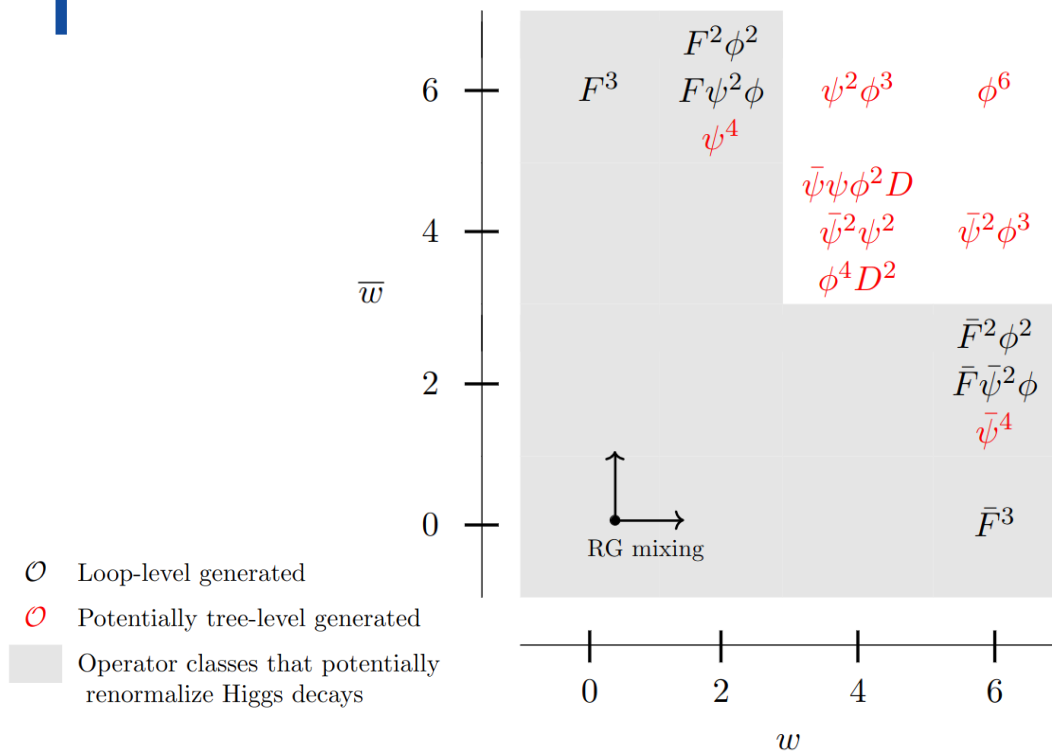
- If **tree-level operator mixes into loop**, RGE is of the same order (with a log-enhancement)
- Does not happen in Higgs decays at dimension-six SMEFT

Grojean, Jenkins, Manohar and Trott, 1711.10391

Elias-Miro, Espinosa, Masso and Pomarol 1302.5661

Alonso, Jenkins, Manohar and Trott 1308.2627, 1310.4838, 1312.2014

RG mixing structure of EFTs

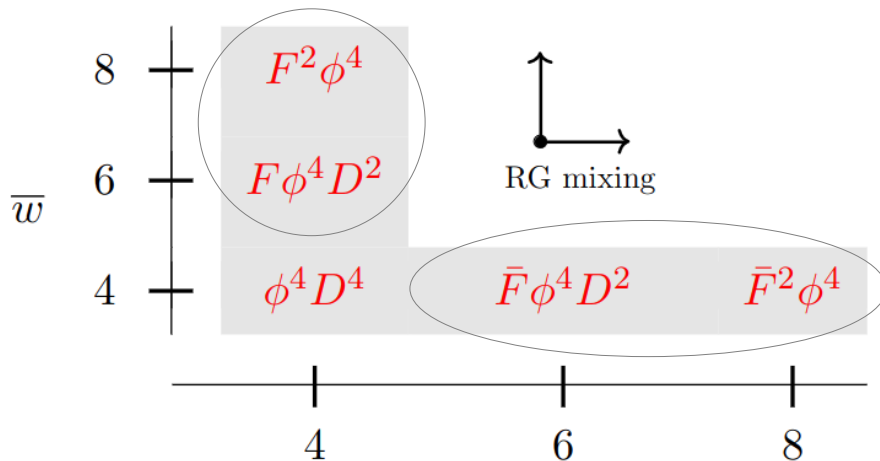


- RGE structure almost aligns with perturbative generation
- Explained by non-renormalization theorem:

$$\gamma_{ij} = 0 \quad \text{if} \quad \omega(\mathcal{O}_i) < \omega(\mathcal{O}_j) \\ \text{or} \quad \bar{\omega}(\mathcal{O}_i) < \bar{\omega}(\mathcal{O}_j)$$

Cheung and Shen 1505.01844

RG mixing structure of EFTs – dim eight



- $\mathcal{O}$ Loop-level generated
- $\textcolor{red}{\mathcal{O}}$ Potentially tree-level generated
- Operator classes that potentially renormalize Higgs decays

$$\mathcal{O}_{F^2\phi^4} = (\phi^\dagger\phi)^2 F_{\mu\nu}F^{\mu\nu}$$

$$\mathcal{O}_{F\phi^4 D^2} = (\phi^\dagger\phi)(D_\mu\phi^\dagger D_\nu\phi)F_{\mu\nu}$$

$$\mathcal{O}_{\phi^4 D^4} = (D_\mu\phi^\dagger D_\nu\phi)(D^\nu\phi^\dagger D^\mu\phi)$$

- Richer structure at dimension-eight
- Theorem allows for more **trees mixing into loops**

Craig, Jiang, Li and Sutherland, 2001.00017
Murphy, 2005.00059

Matching at tree-level

Consider all (scalar) extensions coupling to two Higgs:

		$S \sim (1, 1, 0)$	$\Xi \sim (1, 3, 0)$	$\Xi_1 \sim (1, 3, 1)$
$\phi^4 D^4$	$\mathcal{O}_{\phi^4}^{(1)}$		4	
	$\mathcal{O}_{\phi^4}^{(2)}$			8
	$\mathcal{O}_{\phi^4}^{(3)}$	2	-2	
$X \phi^4 D^2$	$g \mathcal{O}_{W \phi^4 D^2}^{(1)}$	0		
	$g' \mathcal{O}_{B \phi^4 D^2}^{(1)}$			
$X^2 \phi^4$	$g^2 \mathcal{O}_{\phi^4 W^2}^{(1)}$			
	$g^2 \mathcal{O}_{\phi^4 W^2}^{(3)}$			
	$g' g \mathcal{O}_{\phi^4 W B}^{(1)}$			
	$g'^2 \mathcal{O}_{\phi^4 B^2}^{(1)}$			

$$\mathcal{L}_{\Xi} = \frac{1}{2} D_{\mu} \Xi^a D^{\mu} \Xi^a - \frac{1}{2} M^2 \Xi^a \Xi^a - \kappa_{\Xi} \Xi^a \phi^{\dagger} \sigma^a \phi$$

- Results presented in dim 8
Green's basis

Chala, Carmona and G. G., 2112.12724

- Scalar extensions do not generate** the operator classes responsible for the Higgs decays

Corbett, Helset, Martin and Trott 2102.02819

Chala and Santiago 2110.01624

Banerjee, Chakraborty, Englert, Rahaman and Spannowsky 2210.14761

Ellis, Mimasu and Zampedri, 2304.06663

Matching at tree-level

Criado and Perez-Victoria, 1811.09413
 Hays, Helset, Martin and Trott 2007.00565
 Chala, Carmona and G. G., 2112.12724
 Dawson, Forsslund, Schnubel, 2404.01375

Consider all (vector) extensions coupling to two Higgs:

	$\mathcal{B}^\mu \sim (1, 1, 0)$	$\mathcal{B}_1^\mu \sim (1, 1, 1)$	$\mathcal{W}^\mu \sim (1, 3, 0)$	$\mathcal{W}_1^\mu \sim (1, 3, 1)$
$\phi^4 D^4$	$\mathcal{O}_{\phi^4}^{(1)}$	-2	2	$\frac{1}{2}$
	$\mathcal{O}_{\phi^4}^{(2)}$	2	$\frac{1}{2}$	
	$\mathcal{O}_{\phi^4}^{(3)}$		-2	-1
$X \phi^4 D^2$	$g \mathcal{O}_{W \phi^4 D^2}^{(1)}$	2	2	$-\frac{1}{2}(1 + 2k_W)$
	$g' \mathcal{O}_{B \phi^4 D^2}^{(1)}$	-2	$-2k_{B_1}$	$\frac{3}{2}$
$X^2 \phi^4$	$g^2 \mathcal{O}_{\phi^4 W^2}^{(1)}$	$\frac{1}{4}$	$\frac{1}{4}$	$-\frac{1}{16}(1 + 2k_W)$
	$g^2 \mathcal{O}_{\phi^4 W^2}^{(3)}$			$\frac{1}{32}(k_{W_1,2} - 1)$
	$g' g \mathcal{O}_{\phi^4 W B}^{(1)}$		$\frac{1}{4}(1 - k_{B_1})$	$\frac{1}{8}(1 - k_W)$
	$g'^2 \mathcal{O}_{\phi^4 B^2}^{(1)}$	$-\frac{1}{4}$	$-\frac{1}{4}k_{B_1}$	$\frac{1}{16}(k_{W_1,1} + k_{W_1,2} - 2)$
			$\frac{3}{16}$	$\frac{1}{16}(k_{W_1,1} - 1)$

Matching at tree-level

Consider all (vector) extensions coupling to two Higgs:

$$\mathcal{L}_{\mathcal{B}_1} \supset -i g' k_{\mathcal{B}_1} \mathcal{B}_1^{\dagger\mu} \mathcal{B}_1^\nu B_{\mu\nu} ,$$

$$\mathcal{L}_{\mathcal{W}} \supset -\frac{1}{2} g k_{\mathcal{W}} \epsilon^{abc} \mathcal{W}^{\mu a} \mathcal{W}^{\nu a} W_{\mu\nu}^c ,$$

$$\mathcal{L}_{\mathcal{W}_1} \supset -i g' k_{\mathcal{W}_1,1} \mathcal{W}_{1\mu}^{\dagger a} \mathcal{W}_{1\nu}^a B^{\mu\nu} - g k_{\mathcal{W}_1,2} \epsilon^{abc} \mathcal{W}_{1\mu}^{\dagger a} \mathcal{W}_{1\nu}^b W^{\mu\nu c}$$

- **Tree-level perturbative unitarity** in the UV entails $k_{\mathcal{X}} = 1$

Ferrara, Porrati and Telegdi (1992)

Henning, Lu and Murayama, 1412.1837

Feuillat, Lucio and Pestieau hep-ph/0010145

Djukanovic, Schindler, Gegelia and Scherer hep-ph/0505180

Barbieri, Isidori, Pattori and Senia 1512.01560

Biggio, Bordone, Di Luzio and Ridolfi 1607.07621

**When this is imposed,
generation of Higgs decays
vanishes at tree-level**

Renormalization group equations

Using dimension-eight RGEs

$$\begin{aligned}
 16\pi^2\mu\frac{d}{d\mu}\left(\frac{\mathcal{A}[h\gamma\gamma]}{v^3/\Lambda^4}\right) = & -3e^2g'^2\left(\frac{C_{\phi^4W^2}^{(1)}}{g^2} + \frac{C_{\phi^4W^2}^{(3)}}{g^2} - \frac{C_{\phi^4WB}^{(1)}}{g'g} + \frac{C_{\phi^4B^2}^{(1)}}{g'^2}\right) \\
 & + e^2g^2\left(-9\frac{C_{\phi^4W^2}^{(1)}}{g^2} + 3\frac{C_{\phi^4W^2}^{(3)}}{g^2} + 3\frac{C_{\phi^4WB}^{(1)}}{g'g}\right. \\
 & \quad \left.- 9\frac{C_{\phi^4B^2}^{(1)}}{g'^2} + \frac{3}{2}\frac{C_{W\phi^4D^2}^{(1)}}{g} + \frac{3}{2}\frac{C_{B\phi^4D^2}^{(1)}}{g'}\right) \\
 & + e^2\lambda\left(36\frac{C_{\phi^4W^2}^{(1)}}{g^2} + 28\frac{C_{\phi^4W^2}^{(3)}}{g^2} - 32\frac{C_{\phi^4WB}^{(1)}}{g'g}\right. \\
 & \quad \left.+ 36\frac{C_{\phi^4B^2}^{(1)}}{g'^2} - \frac{C_{W\phi^4D^2}^{(1)}}{g} - \frac{C_{B\phi^4D^2}^{(1)}}{g'}\right),
 \end{aligned}$$

Chala, G. G., Ramos and Santiago, 2106.05291

Huber and De Angelis, 2108.03669

Das Bakshi, Chala, Carmona and G. G., 2205.03301

- Triggered by operators in potentially tree-level generated classes
- But are these **linear combinations actually generated?**

Renormalization group equations

$$16\pi^2\mu\frac{d}{d\mu}\left(\frac{\mathcal{A}[h\gamma\gamma]}{v^3/\Lambda^4}\right) = e^2 \begin{cases} g_{\mathcal{B}_1}^2(\lambda - \frac{3}{2}g^2)(k_{\mathcal{B}_1} - 1), & \mathcal{B}_1 \sim (1, 1, 1) \\ \frac{1}{2}g_{\mathcal{W}}^2(\lambda - \frac{3}{2}g^2)(k_{\mathcal{W}} - 1), & \mathcal{W} \sim (1, 3, 0) \\ \frac{1}{4}g_{\mathcal{W}_1}^2(\lambda - \frac{3}{2}g^2)(k_{\mathcal{W}_1,1} - 1), & \mathcal{W}_1 \sim (1, 3, 1) \end{cases}$$

No trees mixing into loops for

$$h \rightarrow \gamma\gamma \quad \text{for} \quad k_{\mathcal{X}} = 1$$

Renormalization group equations

$$16\pi^2\mu\frac{d}{d\mu}\left(\frac{\mathcal{A}[h\gamma Z]}{v^3/\Lambda^4}\right)=g'g^3\begin{cases}\frac{3}{2}\frac{\kappa_{\Xi}^2}{M^2}, & \Xi\sim(1,3,0), \\ -3\frac{|\kappa_{\Xi_1}|^2}{M^2}, & \Xi_1\sim(1,3,1), \\ \frac{9}{4}g_{\mathcal{B}_1}^2, & \mathcal{B}_1\sim(1,1,1),\ k_{\mathcal{B}_1}=1, \\ -\frac{9}{8}g_{\mathcal{W}}^2, & \mathcal{W}\sim(1,3,0),\ k_{\mathcal{W}}=1\end{cases}$$

Trees mix into operators responsible
for $h\rightarrow\gamma Z$ at dimension-eight

A new basis

	Scalar extensions			Vector extensions			
	S (1, 1, 0)	Ξ (1, 3, 0)	Ξ_1 (1, 3, 1)	$\mathcal{B}^\mu$ (1, 1, 0)	$\mathcal{B}_1^\mu$ (1, 1, 1)	$\mathcal{W}^\mu$ (1, 3, 0)	$\mathcal{W}_1^\mu$ (1, 3, 1)
$\mathcal{O}_{\phi^4}^{(1)}$		4		-2	2	1/2	
$\mathcal{O}_{\phi^4}^{(2)}$			8	2		1/2	
$\mathcal{O}_{\phi^4}^{(3)}$	2	-2			-2	-1	
$C_{h\gamma\gamma}$	0						
$C_{h\gamma Z}$							
C_3							
C_4							
C_5							
C_{TLO}				$\frac{1}{4}$	$\frac{1}{4}$	-3/16	

$$\frac{\mathcal{A}[h\gamma\gamma]^{(8)}}{v^3/\Lambda^4} = 2e^2 C_{h\gamma\gamma},$$

$$\frac{\mathcal{A}[h\gamma Z]^{(8)}}{v^3/\Lambda^4} = 2e^2 \frac{g^2 - g'^2}{g'g} C_{h\gamma\gamma} + 2g'g C_{h\gamma Z}$$

Only one direction is
tree-level generated

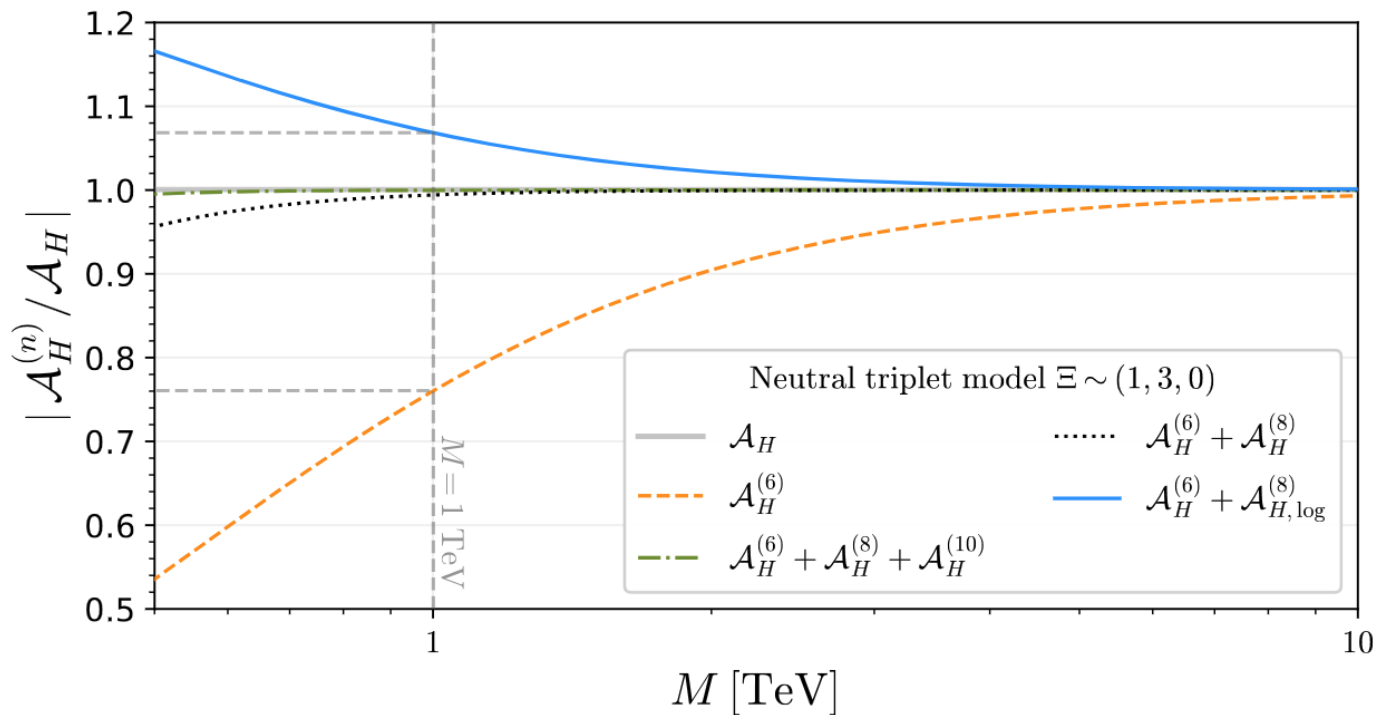


A full model

$$\mathcal{L}_\Xi = \frac{1}{2} D_\mu \Xi^a D^\mu \Xi^a - \frac{1}{2} M^2 \Xi^a \Xi^a - \kappa_\Xi \Xi^a \phi^\dagger \sigma^a \phi$$

■ Compared with full results in

Hue, Arbuzov, Hong, Nguyen, Si and Long, 1712.05234
 Degrande, Hartling and Logan, 1708.08753



Decay width

- Pheno estimate:

Dawson and Giardino, 1801.01136

Dedes, Suxho and Trifyllis, 1903.12046

Hays, Helset, Martin and Trott, 2007.00565

- Use numerical results from
- Include: dimension-six one-loop effects + dimension-eight RGE effects
- Not including: one-loop dimension-eight (non-RGE) terms

- Can the logarithm of dimension-eight important?

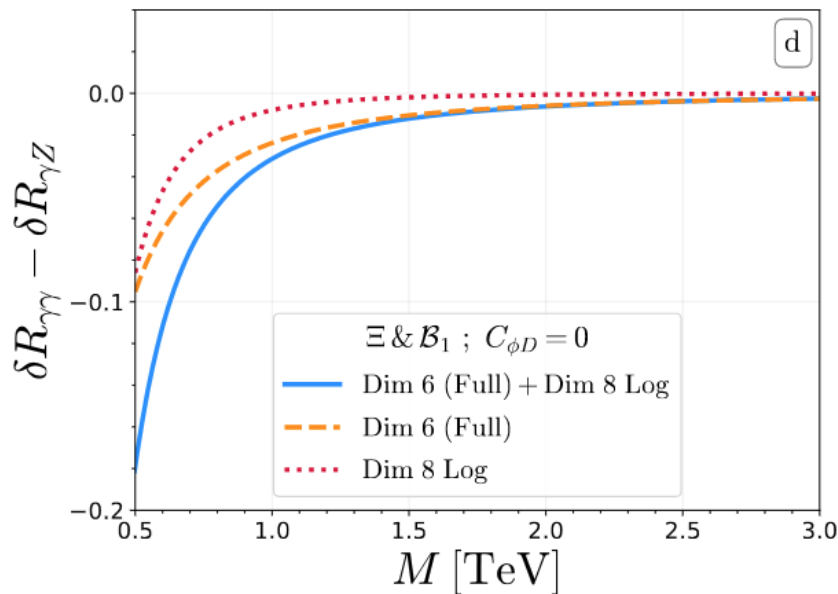
- The decay $h \rightarrow \gamma Z$ is dominated by indirect effects at dimension-six

Influence for the decay width – custodial symmetry?

$$\begin{aligned}\frac{1 + \delta\mathcal{R}_{\gamma\gamma}}{1 + \delta\mathcal{R}_{\gamma Z}} &= 1 + \delta\mathcal{R}_{\gamma\gamma} - \delta\mathcal{R}_{\gamma Z} + O(\delta\mathcal{R}^2) \\ &= 1 - \left(\frac{1 \text{ TeV}}{\Lambda}\right)^2 (0.12C_{\phi D} - 0.02C_{u\phi,33} + 0.049\bar{C}_{\phi B} - 0.002\bar{C}_{\phi W} - 0.024\bar{C}_{\phi WB}) \\ &\quad + 0.0007 \left(\frac{1 \text{ TeV}}{\Lambda}\right)^4 \left(6C_{\text{TLO}} + \frac{3}{8}C_{\phi^4}^{(1)} - \frac{3}{8}C_{\phi^4}^{(2)}\right) \log\left(\frac{m_h}{\Lambda}\right) + O(\delta\mathcal{R}^2), \quad (5.7)\end{aligned}$$

- Most indirect contributions cancelled. However the leading numerical term comes from custodial-symmetry breaking
 - In scalar scenarios **logarithm and custodial-symmetry are correlated!** Need vectors to break correlation

Influence at the observable level – custodial symmetry?



- Adding a heavy vector allows for the cancellation of tree-level $C_{\phi D}$, while maintaining a non-zero dimension-eight RGE.

- Matching with results from dictionaries

de Blas, Criado, Perez-Victoria and Santiago, 1711.10391
G. G., Olgoso and Santiago, 2303.16965

- Dimension-eight RGE corresponds to **25% of the full result**

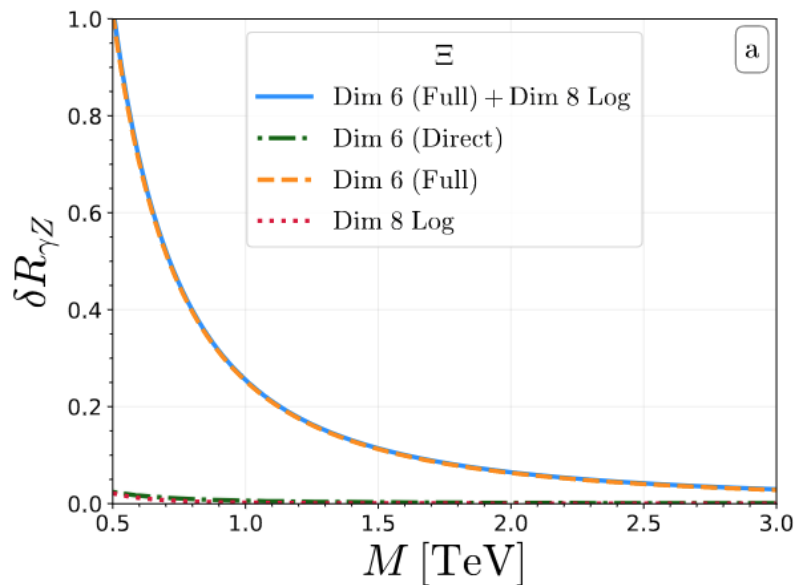
Conclusions

- Immense development of dimension-eight SMEFT
 - Basis construction, observable parameterization, renormalization group structure, etc.
- Certain scalings and/or kinematics are only captured by dimension-eight
- Trees renormalizing higgs decays arises at dimension-eight whereas it was absent at dimension-six – new qualitative behaviour at higher-order
- Relevance to these observations dependent on the model

Thanks

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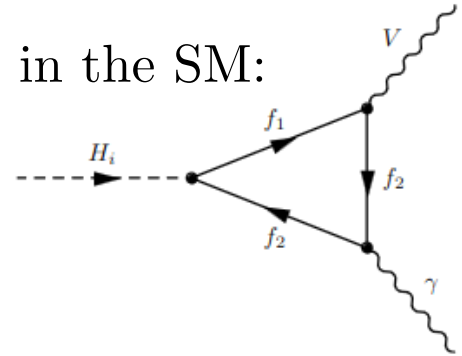
Influence for the decay width



- Indirect contributions at dimension-six completely dominate
- One could imagine more complicated models or ...

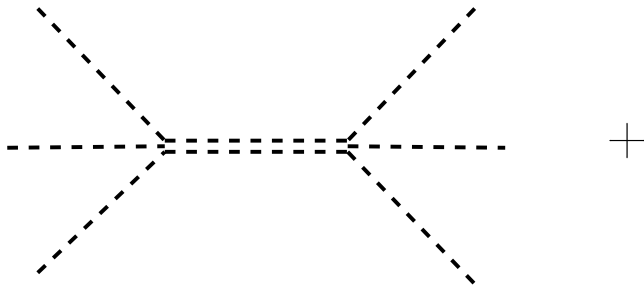
Higgs decays in the SMEFT

Loop in the SM:



$$\mathcal{L}_{\text{SMEFT}} \supset C_{h\gamma\gamma} \frac{v}{\Lambda^2} h F_{\mu\nu} F^{\mu\nu}$$

- For basis of operators with non-vanishing leading terms (non-zero amplitudes for the lowest field content):



Considering that UV respects SM gauge symmetries – gauge bosons couple diagonally:

- An operator must have at least 4 Higgses or fermions for it to be potentially tree-level generated