

# Measurements on jet substructure at the LHC

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Toni Mlinarević (UCL) on behalf of the  
ATLAS and CMS collaborations

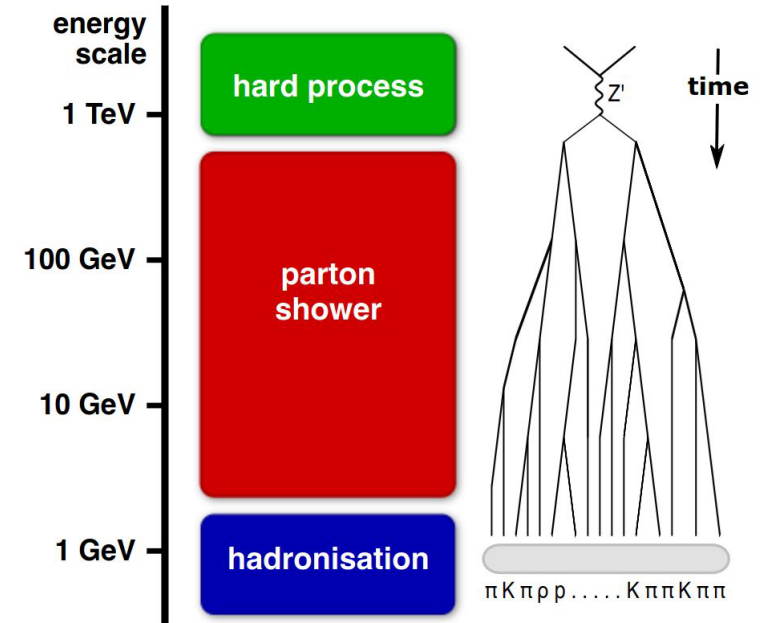
Standard Model at the LHC 2025, Durham

7 April – 10 April



# Jet substructure measurements

- probe of perturbative and non-perturbative QCD regimes (resummation methods, parton showers, hadronization, underlying event)
- can be used for tagging objects, mitigating effects of pile-up and underlying events



G. Salam's sketch

- This presentation focuses on 4 recent measurements:
  - Measurement of the primary **Lund jet plane** density in proton-proton collisions at  $\sqrt{s} = 13\text{TeV}$  (CMS, [JHEP 05 \(2024\) 116](#))
  - Measurement of the **Lund jet plane** in hadronic decays of **top quarks and W bosons** with the ATLAS detector ([arXiv:2407.10879](#), submitted to EPJC)
  - Measurement of **jet track functions** in  $pp$  collisions at  $\sqrt{s} = 13\text{ TeV}$  with the ATLAS detector ([arXiv:2502.02062](#), submitted to Physics Letters B)
  - Measurement of **event shape variables** using charged particles inside jets in proton-proton collisions at  $\sqrt{s} = 13\text{ TeV}$  ([CMS-PAS-SMP-22-004](#))

# The Lund jet plane (LJP)

F. Dreyer, G. Salam, G. Soyez, [JHEP12\(2018\)064](#)

- 2D representation of the phase space of splittings (emissions) within a jet
- Constructed by following the Cambridge–Aachen clustering tree in reverse; at each step we can calculate kinematic variables describing the branching:
  - emission opening angle:

$$\Delta R = \sqrt{(y^{\text{softer}} - y^{\text{harder}})^2 + (\phi^{\text{softer}} - \phi^{\text{harder}})^2}$$

- momentum fraction of the emitted particle:

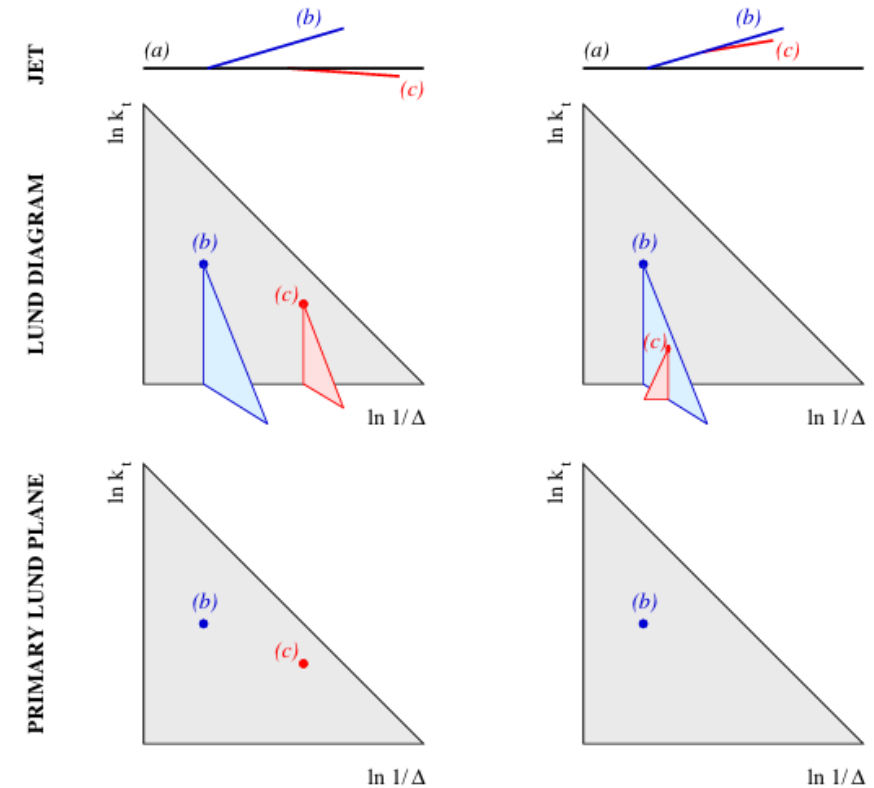
$$z = \frac{p_T^{\text{softer}}}{p_T^{\text{harder}} + p_T^{\text{softer}}}$$

- transverse momentum of emitted particle relative to the emitter:

$$k_t = \Delta R p_T^{\text{softer}}$$

(in the limit  $p_T^{\text{softer}} \ll p_T^{\text{harder}}$  and  $\Delta R \ll 1$ )

- The **primary** LJP is constructed only from the emissions along the hardest branch



# Primary LJP density

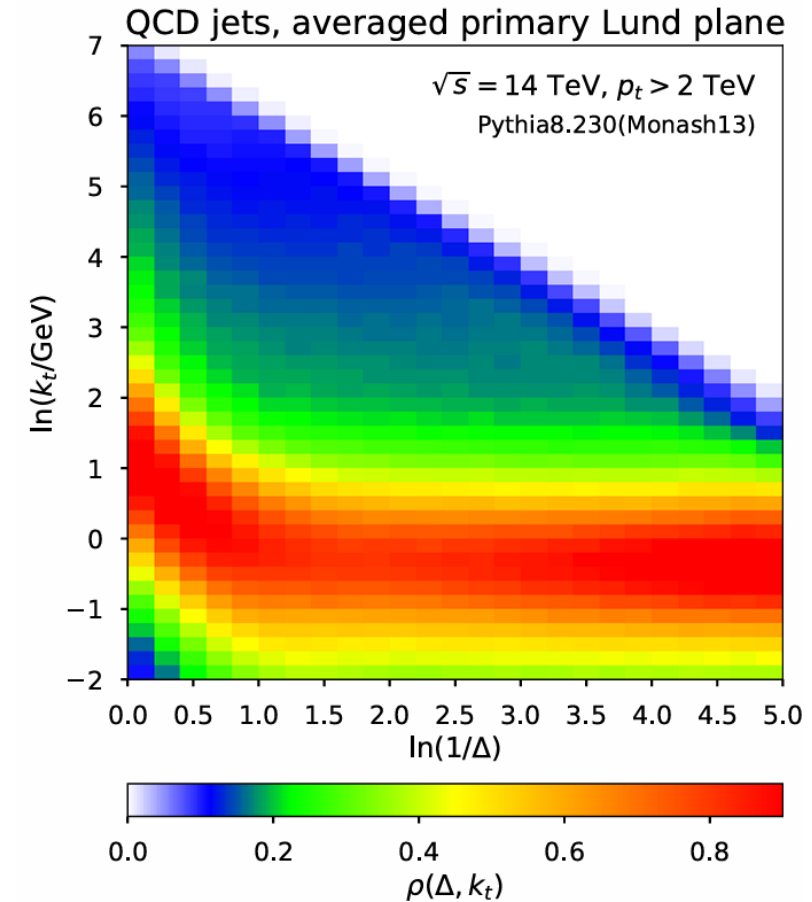
- Average density of emissions per jet and per unit area:

$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln \left( \frac{k_T}{\text{GeV}} \right) d \ln \left( \frac{R}{\Delta R} \right)}$$

- At leading order and for  $\Delta R \ll 1$ ,  $\frac{k_T}{p_{T,\text{jet}} \Delta R} \ll 1$ ,

$$\rho(k_T, \Delta R) \simeq \frac{2}{\pi} C_R \alpha_s(k_T) \quad \text{where } C_R = 3 \text{ for } g \rightarrow gg \text{ or } C_R = 4/3 \text{ for } q \rightarrow qg$$

F. Dreyer, G. Salam, G. Soyez, [JHEP12\(2018\)064](#)

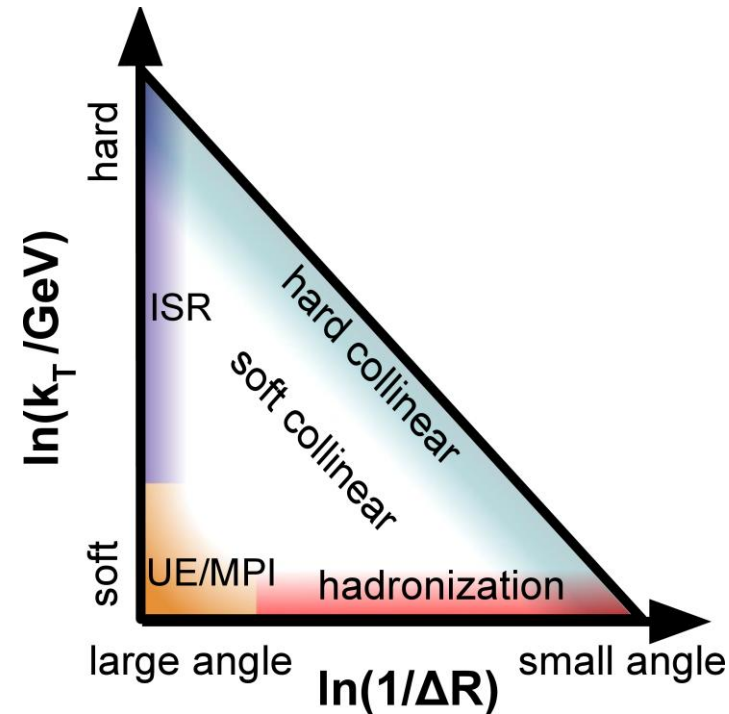


# Factorisation of physical effects

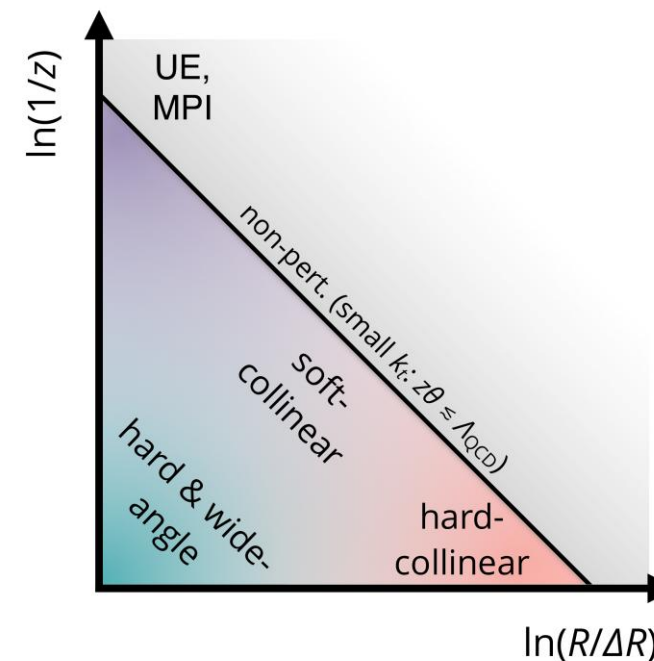
- Different regions of the LJP are dominated by QCD emissions of different physical origins
- Measurements of the LJP are useful tools for providing MC generator tunes

CMS:  $k_T$  vs  $\Delta R$

- shower and hadronization regions more clearly separated (by cutting on  $k_T$ )
- more sensitive to detector smearing effects



CMS, [JHEP 05 \(2024\) 116](#)



ATLAS, [PRL 124, 222002 \(2020\)](#)

ATLAS:  $z$  vs  $\Delta R$

- more resilient to smearing effects (cancel in  $z$  since it's a ratio)

# LJP measurements at the LHC

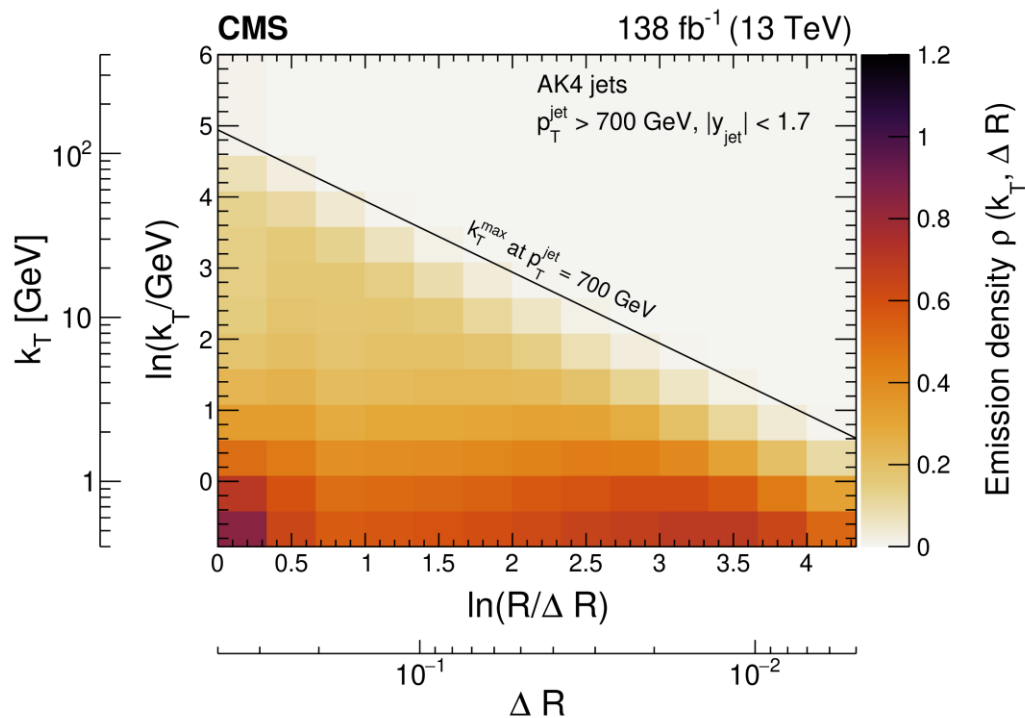
- Primary LJP densities:
  - ATLAS in dijet events: [PRL 124, 222002 \(2020\)](#)
  - ALICE in inclusive low-pT jets: [ALICE-PUBLIC-2021-002](#)
  - **CMS in inclusive jets: [JHEP 05 \(2024\) 116](#)**
  - **ATLAS in top and W jets: [arXiv:2407.10879](#), submitted to EPJC**
- ALICE dead-cone effect observation: [Nature 605 \(2022\) 440-446](#)
- ATLAS Lund subjet multiplicities ([PLB 859 \(2024\) 139090](#))



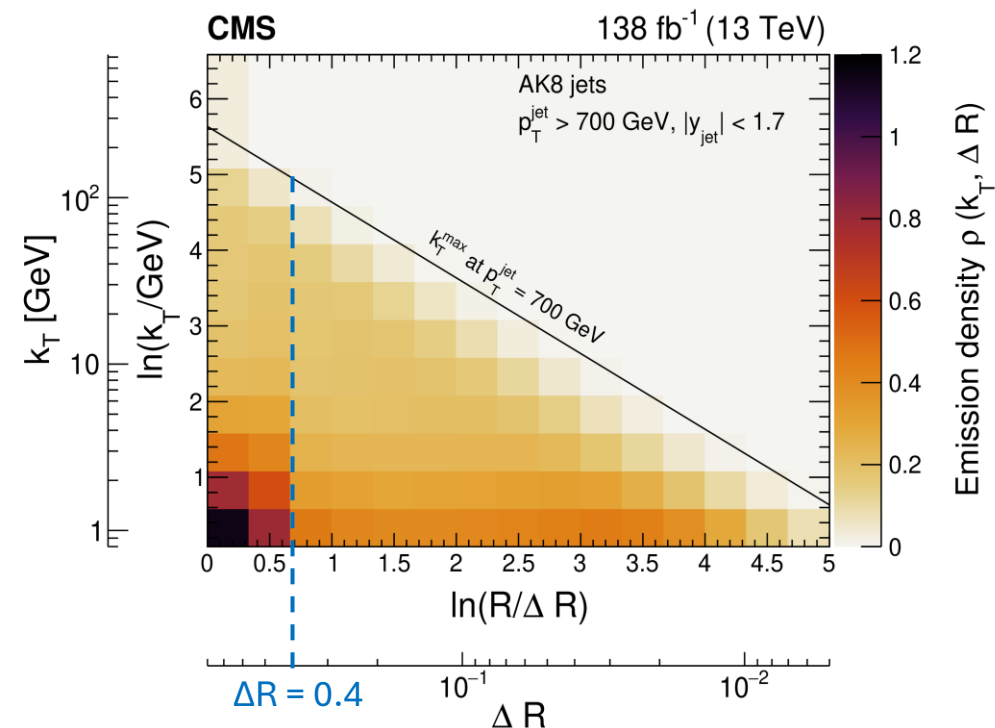
# CMS primary LJP density measurement in inclusive jet production

- $p_T > 700$  GeV
- charged particle tracks used for substructure
- first measurements in large-radius jets  $\rightarrow$  mitigates clustering effects
- multidimensional unfolding

$R = 0.4$  (standard for Run 2)



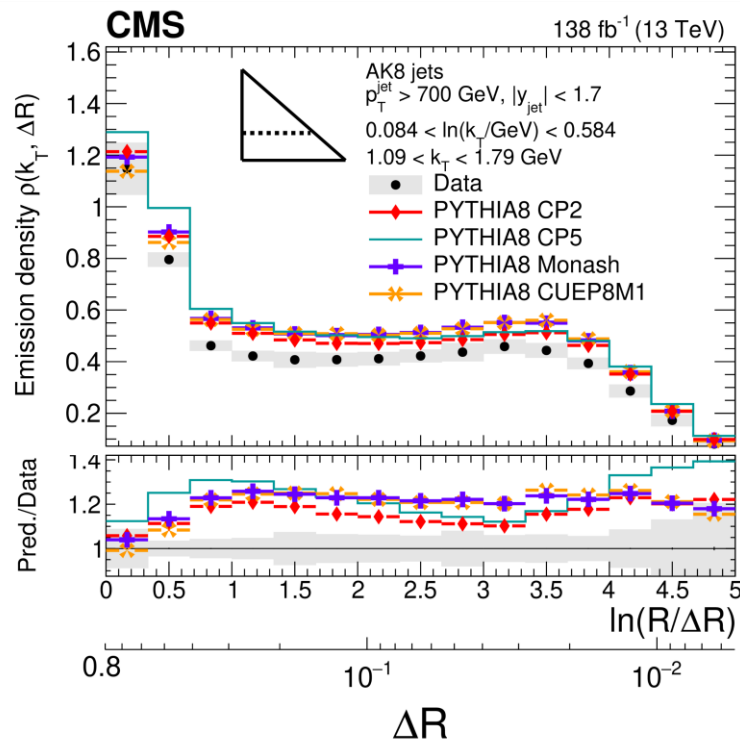
$R = 0.8$  (access to large  $\Delta R$  and high  $k_T$ )





# CMS Lund plane slices

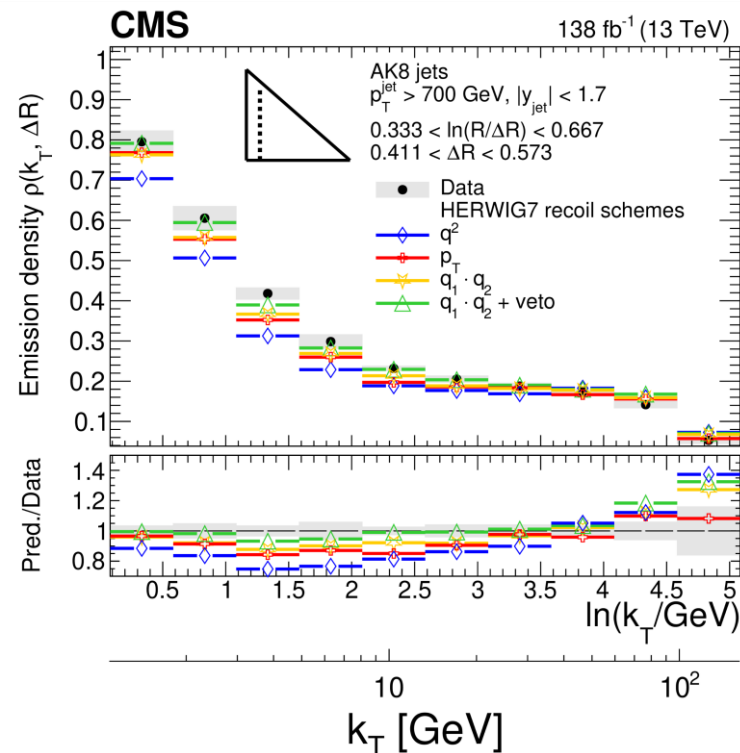
Low  $k_T$  ( $\sim 1$  GeV) - hadronization region, comparison to several Pythia8 tunes



PYTHIA8 CP5 overestimates the number of emissions by 15-20% (default CMS PYTHIA8 underlying-event tune)

Possibility for improvement: include FSR cutoff  $k_T$  as a free parameter in future event generator tuning

Large-angles, comparison to different Herwig7 recoil schemes



best described by Herwig7 angle-ordered with  $q_1 \cdot q_2 + \text{veto}$





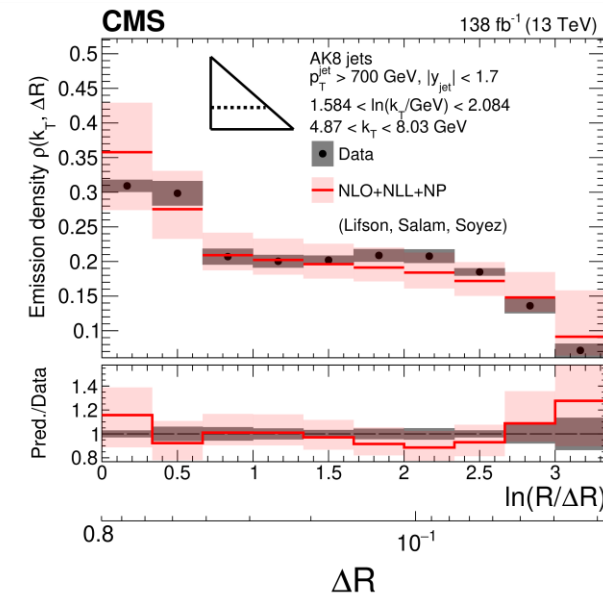
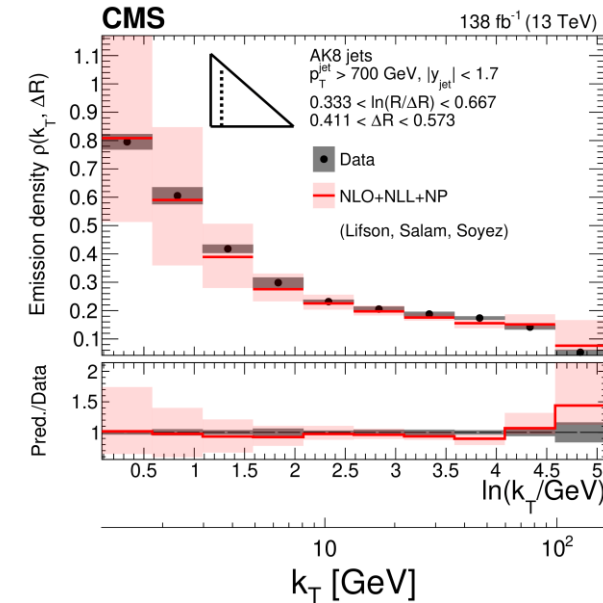
# Comparison to parton-level pQCD predictions

- NLL accuracy, matched to NLO, with non-perturbative corrections
- parton-level calculations corrected to the hadron level using bin-by-bin corrections derived from MC
- nonperturbative corrections mostly affect  $k_T < 5$  GeV

$4.87 < k_T < 8.03$  GeV – pQCD calculation reliable and hadronisation corrections not large

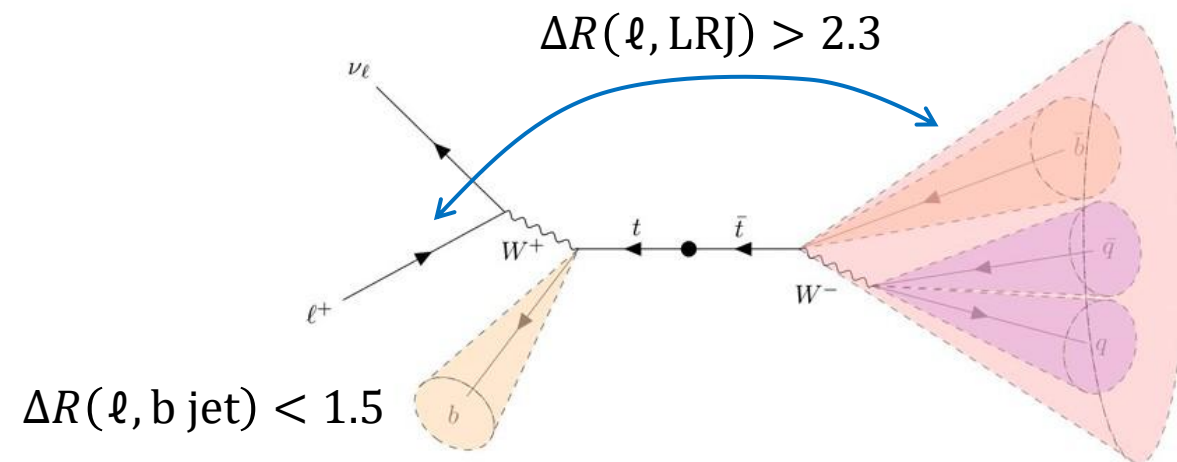
- resummation of nonglobal logarithms → increased density at large  $\Delta R$

- predictions consistent with unfolded data



# Lund plane from top and W jets

- The first measurement of the Lund jet plane in top-jets and W-jets
- First LJP study in large- $R$  jets in ATLAS and first with  $R = 1.0$



## Top jet selection

$$m_{\text{LRJ}} > 140 \text{ GeV}$$

$$\Delta R(\text{b jet}, \text{LRJ}) < 1.0$$

## W jet selection

$$60 \text{ GeV} < m_{\text{LRJ}} < 100 \text{ GeV}$$

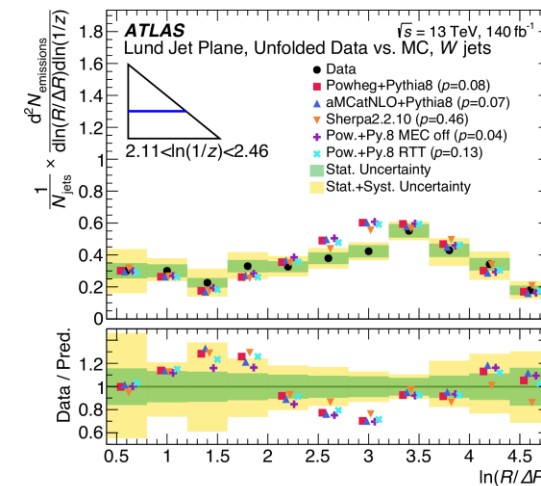
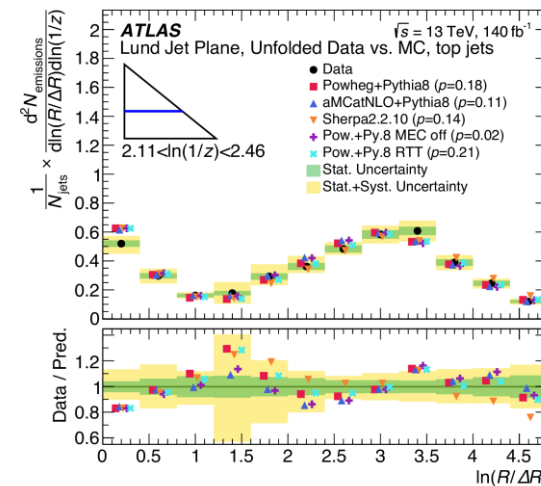
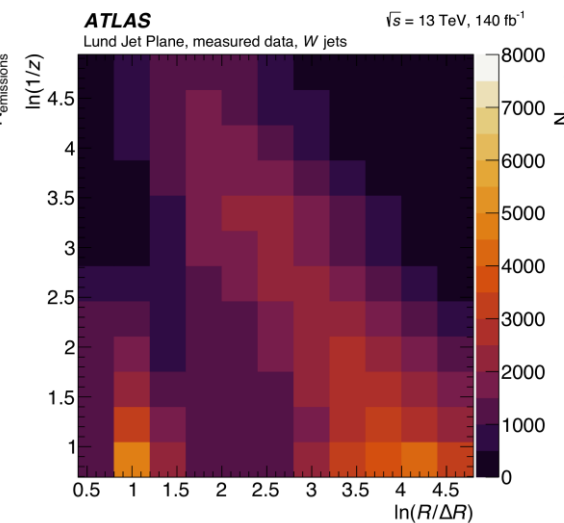
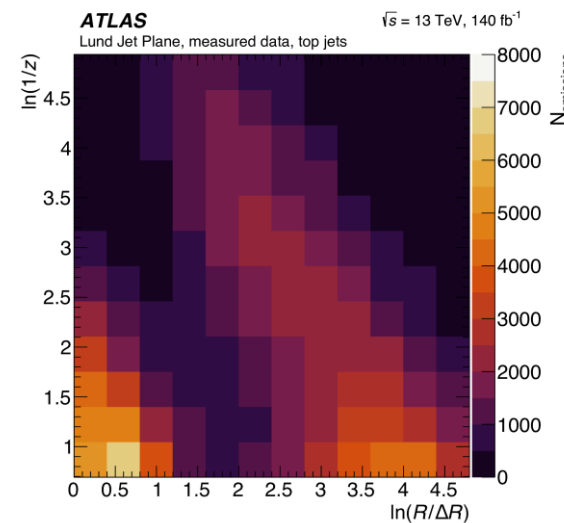
$$\Delta R(\text{b jet}, \text{LRJ}) > 1.0$$

# Lund plane from top and W jets

- Highest density for hard and wide-angle emissions
  - peak shifted towards wider angles for top jets due to higher mass
- Density of emissions unfolded using iterative Bayesian unfolding (IBU) and compared with predictions from other generators
  - Signal modelled with POWHEG+PYTHIA8
- Good agreement
  - But for W jets, no generator agrees with measurements across whole plane
  - For top jets, disagreements also observed for smaller subregions
- Large modelling uncertainties in the majority of the plane

top jets

W jets



# Measurement of jet track functions

- Track functions characterize the **transverse momentum fraction**

$$r_q = p_T^{\text{charged}} / p_T^{\text{all}}$$

carried by **charged hadrons** from a fragmenting quark or gluon

- Track functions are **non-perturbative** → must be measured
- $r_q$  distributions measured in high- $p_T$  jets in **dijet events**
- **Moments of  $r_q$**  as a function of  $p_T$  extracted
  - moment higher than first moment not previously measured
  - encode interesting correlations in the hadronization process
  - scale evolution provides a test of QCD beyond the DGLAP paradigm

# Extracting moments of distributions

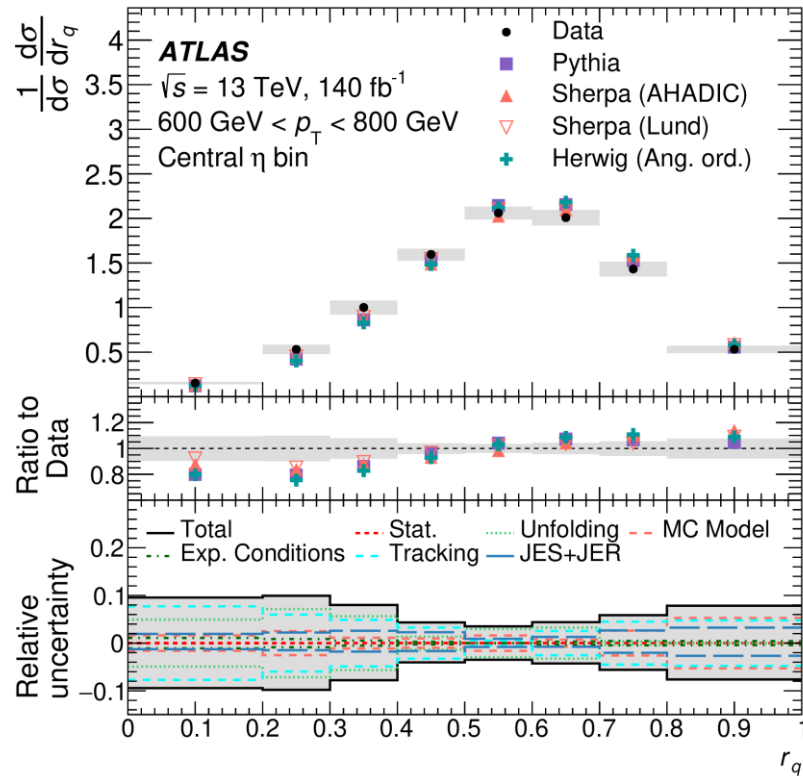
- $n$ th moment is expectation value of  $r_q^n$ , estimated using central bin values:

$$m_n = \sum_i r_{q_i}^n N_i$$

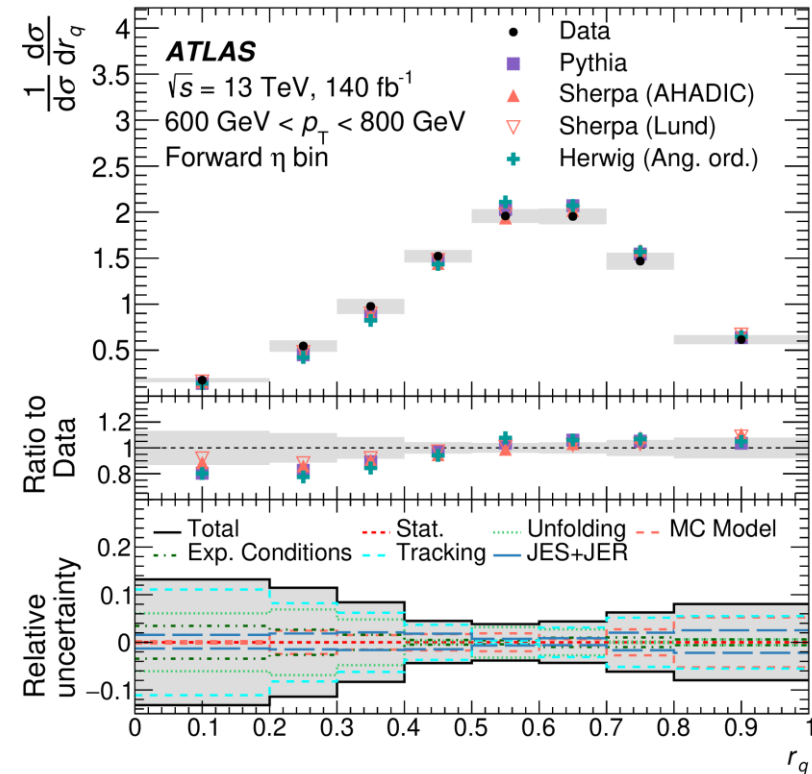
- The data are corrected for detector effects using **IBU**
- **OmniFold** used for **data-driven** correction for binning artifacts in the moment extractions

# $r_q$ distributions

## Central $\eta$ bin



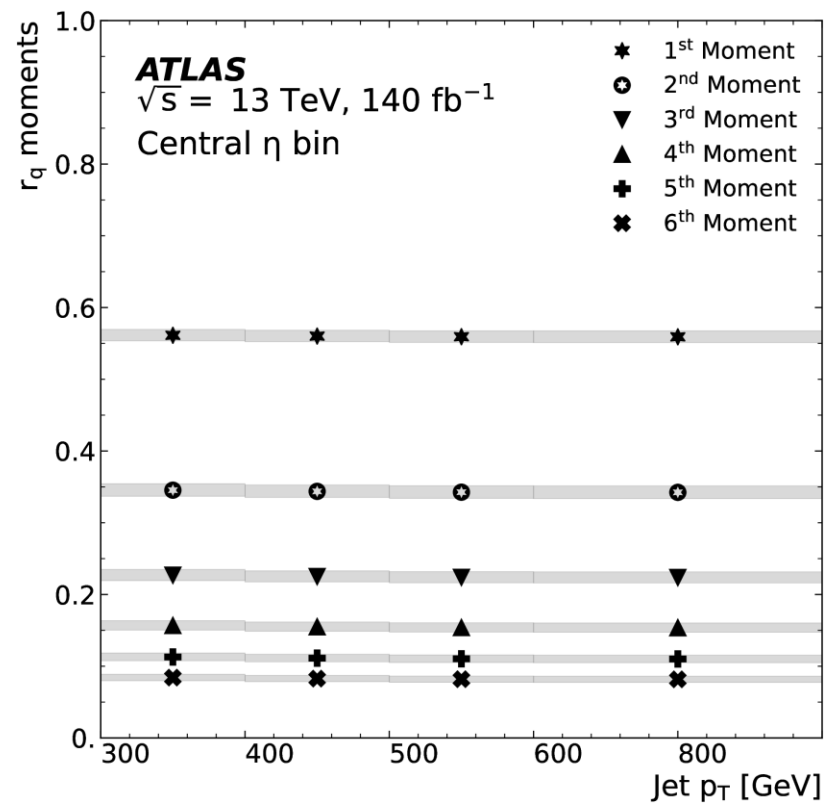
## Forward $\eta$ bin



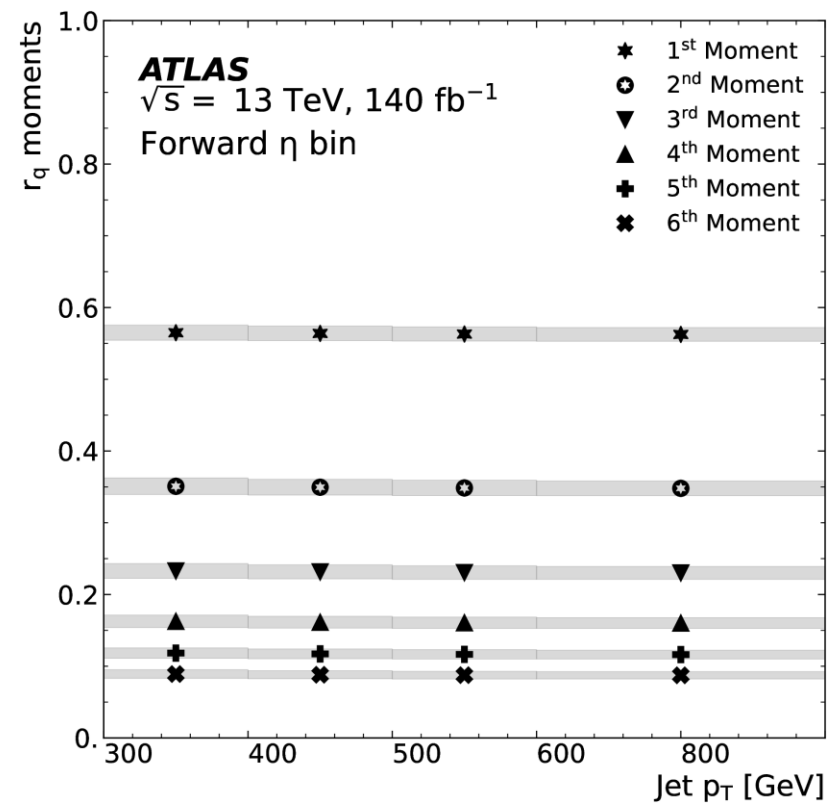
- Agree with MC within uncertainties, but underestimated at low  $r_q$  and overestimated at high  $r_q$

# Moments of $r_q$ as function of jet $p_T$

## Central $\eta$ bin



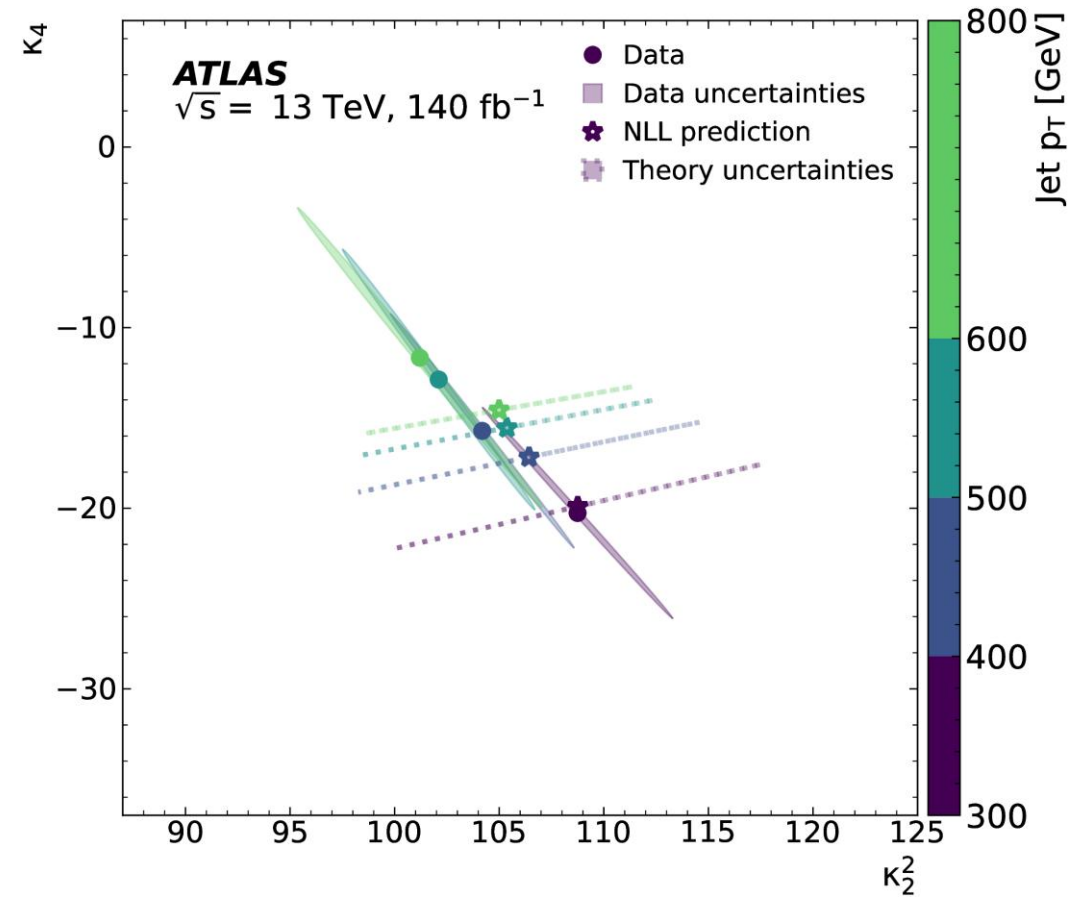
## Forward $\eta$ bin



# Renormalization group flows

- Cumulants  $\kappa_n$  can be expressed in terms of central moments, e.g.  

$$\kappa_2 = \mu_2, \kappa_4 = \mu_4 - 3\mu_2^2, \dots$$
- Energy dependence of the relationship between pairs of these cumulants is theoretically determined by renormalization group flows
- Good data-theory agreement







# Measurement of event shape variables using charged particles inside jets

- First CMS study that uses charged particles inside jets to evaluate event shape variables
- Event shape variables:
  - constructed from four-momenta of final-state objects (charged particles in this case)
  - sensitive to QCD predictions in multijet production
  - minimal impact of systematic uncertainties
- Multijet events selected using dijet triggers



# Event shape variables

- Complement of transverse thrust:

$$\tau_{\perp} \equiv 1 - T_{\perp}, \quad T_{\perp} \equiv \max_{\vec{n}_T} \frac{\sum_i |\vec{p}_{T,i} \cdot \vec{n}_T|}{\sum_i p_{T,i}}$$

maximizes  $T_{\perp}$ , defines the thrust direction

- more dependent on initial hard scattering

- Third-jet resolution parameter:

$$Y_{23} \equiv \frac{\max \left( p_{T,3}^2, \left[ \min(p_{T,i}, p_{T,j})^2 \frac{(\Delta R_{i,j})^2}{R^2} \right] \right)}{P_{12}^2}$$

- If more than three final-state particles, they are recombined with the distance parameter  $R = 0.4$  until only 3 particles pseudo-particles left in the final state
- sensitive to clustering and substructure

- designed to have higher values for multijet, spherical events and lower values for back-to-back two-jet events
- $P$  denotes scalar sums

- Jet broadening:

$$B_X \equiv \frac{1}{2P_T} \sum_{i \in C_X} p_{T,i} \sqrt{(\eta_i - \eta_X)^2 + (\phi_i - \phi_X)^2}$$

$X$  refers to upper part of the event  $U$  where all particles have  $\vec{p}_T \cdot \vec{n}_T > 0$  or lower part  $L$  where  $\vec{p}_T \cdot \vec{n}_T < 0$

$$B_T = B_U + B_L$$

- Jet masses: normalized squared invariant mass of the jets in the upper and lower regions

$$\rho_X \equiv \frac{M_X^2}{P^2}$$

$$\rho_{\text{Tot}} = \rho_U + \rho_L$$

Corresponding quantity in transverse plane:  $\rho_{\text{Tot}}^T$

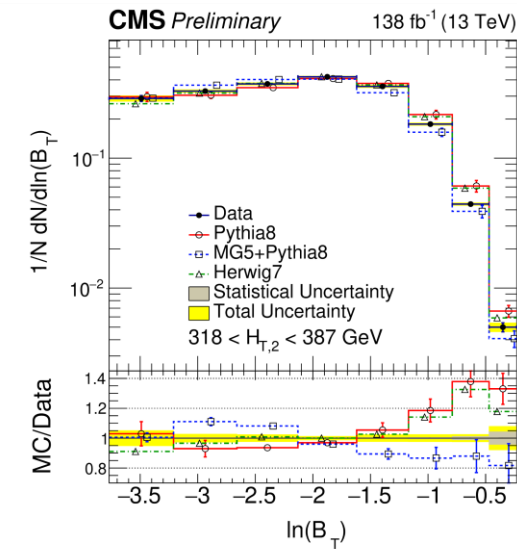
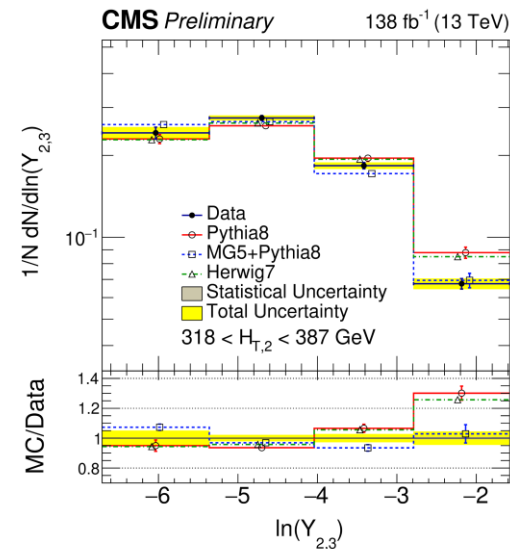
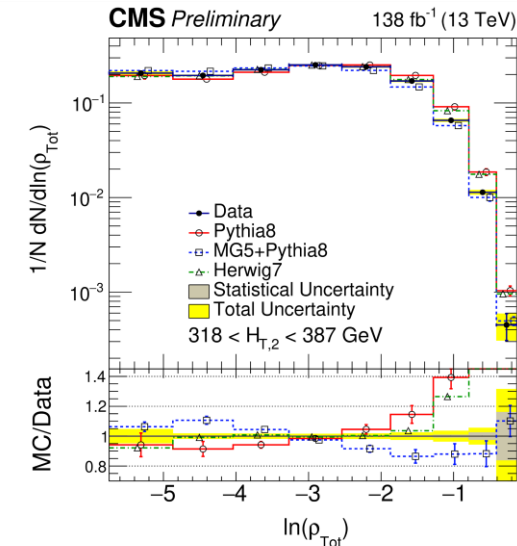
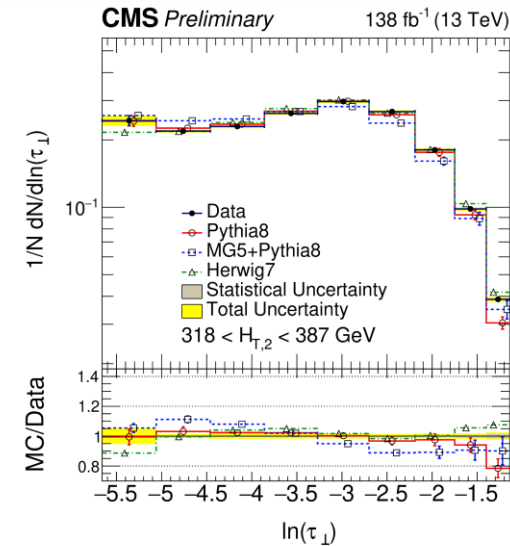
Jet masses and jet broadening depend more on nonperturbative QCD.



# Event shape variables - results

$H_{T,2}$  = average  $p_T$  of the leading and sub-leading  $p_T$  jets

- Pythia 8 and Herwig 7 – good agreement with data for  $\tau_{\perp}$  and  $\rho_{T_{\text{Tot}}}^T$ , overestimate spherical, multijet events for  $\rho_{T_{\text{Tot}}}$ ,  $Y_{23}$ ,  $B_T$   
 $\Rightarrow$  improvements needed for modelling of fragmentation and hadronization
- For Pythia 8, agreement with data improves with  $H_{T,2}$ , but not for Herwig 7
- MG5+ Pythia 8 predictions underestimate spherical, multijet events for  $\tau_{\perp}$ ,  $\rho_{T_{\text{Tot}}}^T$ ,  $\rho_{T_{\text{Tot}}}$ ,  $B_T$ ; disagreement increases with  $H_{T,2}$ 
  - agreement only good for  $Y_{23}$ $\Rightarrow$  issues in the combination of matrix element calculations with the parton showers

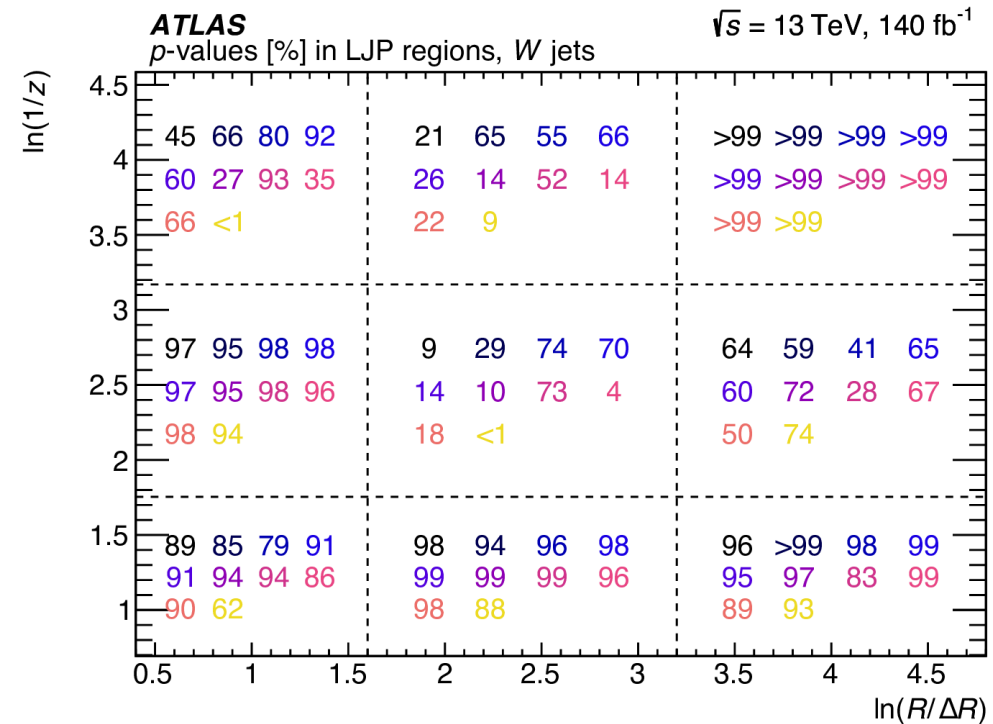
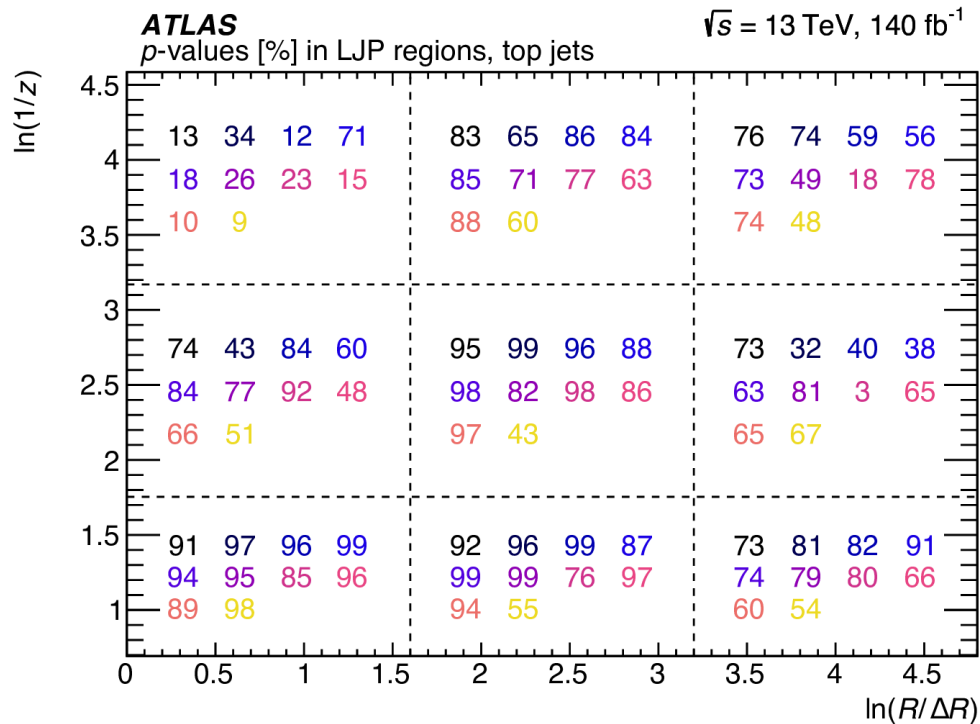


# Summary

- Jet track function analysis
  - provides results that, when incorporated into theoretical calculations, will enable precision comparisons between data and theory for track-based jet substructure observables
  - Provides a test of QCD **beyond the DGLAP paradigm**
- Event shape observables measurements indicate improvements needed for modelling of fragmentation and hadronization, and issues in the combination of ME calculations with the PS
- Lund jet plane measurements:
  - In  $W$  jets, all predictions are incompatible with the measurement
  - In top quark jets, disagreement with all predictions is observed in smaller subregions of the plane, and with a subset of the predictions across the fiducial plane
  - The ATLAS and CMS measurements could be used to improve different aspects of physics modeling in event generators (hadronization, parton showers, better modelling of hadronic decays of heavy quarks and bosons), or to improve the performance of jet taggers

# Backup

# Lund plane from top and W jets: Comparison with MC predictions



- Powheg+Pythia8
- Powheg+Herwig7.2
- Powheg+Herwig7.1
- Powheg+Herwig7.0
- Pow.+Py.8 RTT
- aMCatNLO+Pythia8
- Sherpa2.2.10
- Pow.+Py.8 MEC off
- Pow.+Py.8 FSR Up
- Pow.+Py.8 FSR Down