

Cosmological Quasiparticles and the Cosmological Collider



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In collaboration with

Jay Hubisz, He Li, and Bharath Sambasivam: *ArXiv:2408.08951*
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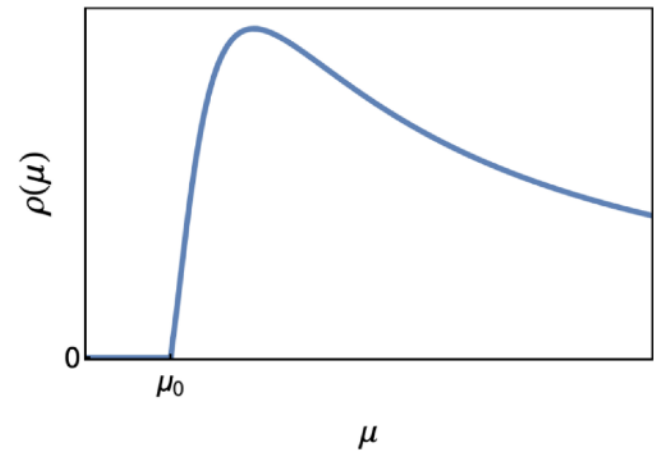
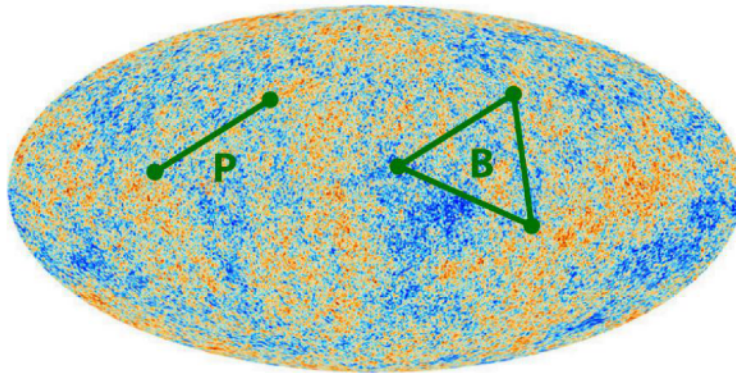
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- We can consider, for example, a CFT operator O with scaling dimension Δ , and ask what sort of contribution it gives to the power spectrum as a function of its boundary conditions and Δ .
- We can utilize the AdS/CFT dictionary, and study the quantum fluctuations of a 5D scalar field in AdS-dS

Elevator Pitch

The spectrum of a scalar operator in a large N CFT in an inflationary background is characterized by a **gapped continuum**, with the gap set by the Hubble rate of inflation.

In this work, we investigate the **non-Gaussian** signatures in the **CMB bispectrum** caused by the interaction of such an operator with the inflaton using Holographic principles.



Holography

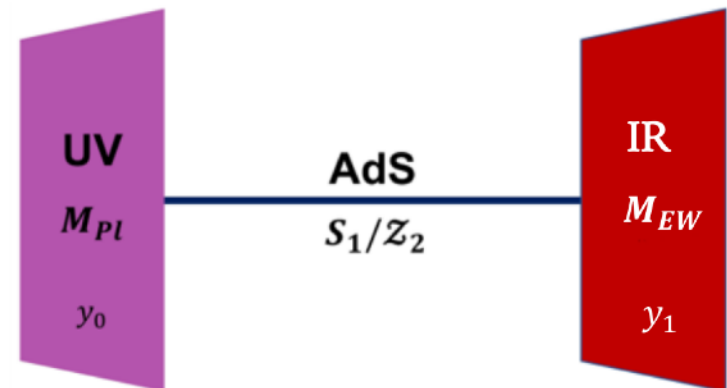
Hierarchy problem: Large hierarchy of scales in the standard model ($M_{EW} \sim 10^3 GeV$, $M_{Pl} \sim 10^{19} GeV$); Smallness of Higgs mass ($126 GeV$)

- Randall-Sundrum models- Elegant geometric solution

$$ds^2 = e^{-2A(y)} dx_4^2 - dy^2$$

- $A(y) = ky \equiv$ pure AdS; k is the inverse-curvature
- **Goldberger-Wise:** Size of extra dimension stabilized by scalar gaining a $\langle \phi \rangle(y)$, deforming AdS geometry
- Spectrum- discrete tower of KK modes with $m \sim f$

Spontaneously broken CFT on boundary



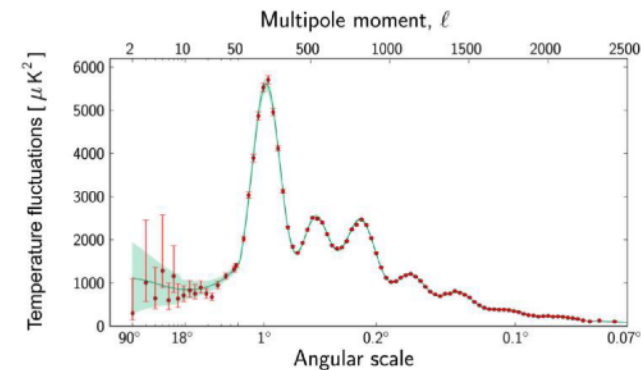
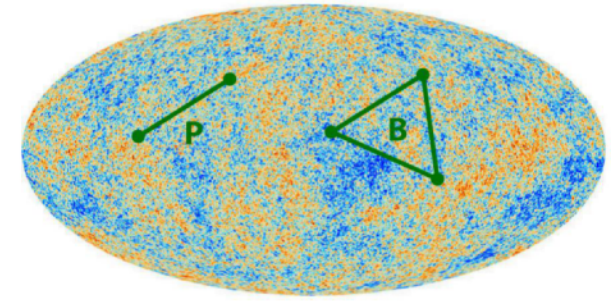
- AdS/CFT: 5D gravity \leftrightarrow 4D conformal gauge theory.
- RS1 and RS2 models as duals of large-N CFTs.
- Conformal symmetry breaking is essential for phenomenology.

Inflation

Epoch of dark energy domination leading to exponential expansion of the universe for ~ 60 efolds

- Inflation solves the flatness, homogenous & isotropy problems,
 - Curvature and inhomogeneities get stretched away
 - Quantum fluctuations of (ϕ, σ, \dots) get stretched, imprinted on superhorizon scales, and reenter horizon to seed fluctuations of CMB and large scale structure formation
- Fluctuations are primordial, approximately scale-invariant, and Gaussian

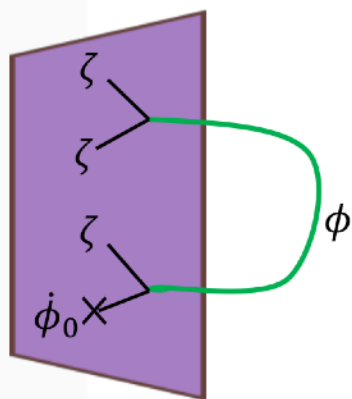
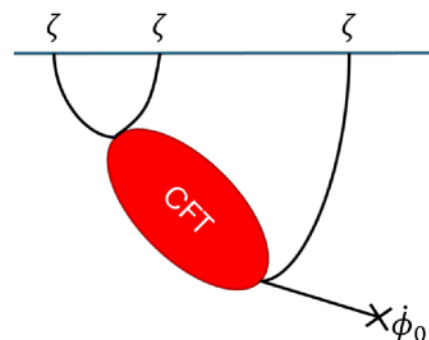
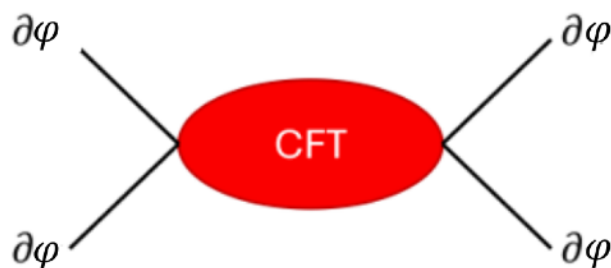
Non-Gaussianities and beyond the power spectrum?



$$n_s = 0.9649 \pm 0.0042$$
$$\Delta T/T \sim 10^{-5}$$

- Inflaton localized on UV brane.
- Bulk scalar coupled to inflaton field.
- AdS-dS geometry: Hubble scale introduces IR cutoff.

Our Model of Inflation and Spectral Density



ζ : Inflaton on the brane

ϕ : Bulk scalar field

ϕ_0 : background field

m : Bulk scalar mass

$\nu = \sqrt{4 + m^2}$: Eff mass of bulk scalar

m_0 : Brane mass

$$\mathcal{L}_{4D} = \mathcal{L}_{inf} + \mathcal{L}_{CFT} + \sum_{i,j} g_{i,j} \mathcal{O}_{inf}^i \mathcal{O}_{CFT}^j$$

Coupling term: $\lambda\phi(\nabla\zeta)^2$

$$\langle \phi(x)\phi(x') \rangle \propto \int \frac{d^4p}{(2\pi)^4} e^{ip(x-x')} \frac{i}{(p^2 + i\epsilon)^{2-\Delta}} = i \int \frac{d^4p}{(2\pi)^4} e^{ip(x-x')} \int_0^\infty d(\mu^2) \frac{\rho(\mu^2)}{(p^2 - \mu^2 + i\epsilon)};$$

$$\rho(\mu^2) = \frac{C(\Delta)}{(\mu^2)^{2-\Delta}}$$

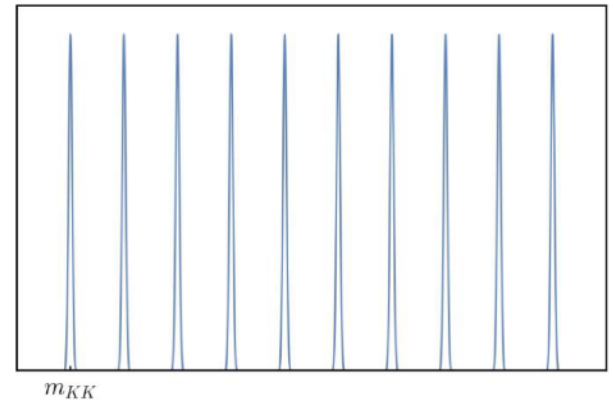
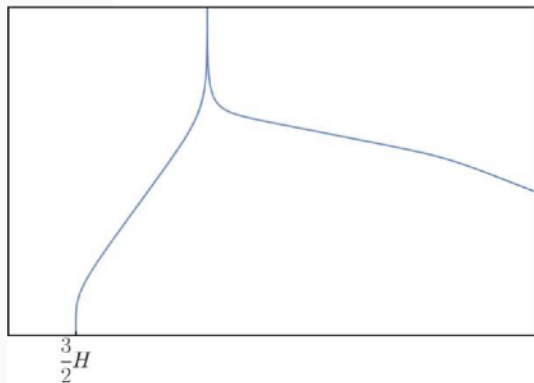
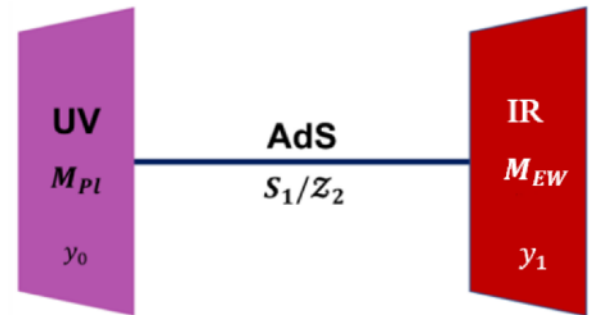
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$$ds^2 = e^{-2A(w)}(dt^2 - e^{2Ht}dx^2 - dw^2)$$

$$e^{-A(w)} = \frac{H}{k \sinh Hw}$$



Late Time



Note: the gap is not robust. Coupling with

curvature $\xi R \phi^2$ can shift it to $H \sqrt{\frac{9}{4} + 12\xi}$

~~CFT~~

5D inflationary set-up

$$\mathcal{L} = \mathcal{L}_{\text{inf}} + \mathcal{L}_{\text{CFT}} + \sum_{ij} g_{ij} \mathcal{O}_{\text{inf}}^i \mathcal{O}_{\text{CFT}}^j$$

5D Einstein-Hilbert action on a space with one brane, and a scalar field action on UV brane:

$$S = - \int d^5x \sqrt{g} \left[\Lambda + \frac{1}{2\kappa^2} R \right] + \int d^4x \sqrt{g_0} \left[\frac{1}{2} (\partial\varphi)^2 - \lambda(\varphi) \right] \quad \Lambda = -\frac{6k^2}{\kappa^2}$$

$$\ddot{\varphi} + 3H\dot{\varphi} + \frac{\partial\lambda(\varphi)}{\partial\varphi} = 0,$$

FLRW equation on the UV brane:

$$H^2 + \frac{1}{2}\dot{H} = \frac{\kappa^4}{36} \lambda^2(\varphi) \left(1 - \frac{\dot{\varphi}^2}{\lambda(\varphi)} \right) \left(1 + \frac{\dot{\varphi}^2}{2\lambda(\varphi)} \right) + \frac{\kappa^2}{6} \Lambda. \quad H^2 \approx \frac{\kappa^4}{36} \lambda^2(\varphi) - k^2.$$

5D metric:

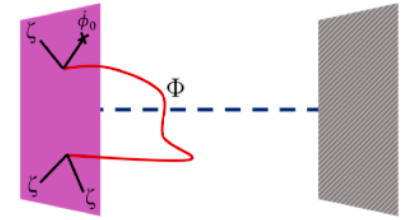
$$ds^2 = \frac{1}{(kz)^2} \left(dt^2 - e^{2Ht} d\vec{x}^2 - \frac{dz^2}{G^2(z)} \right) \quad G(z) = \sqrt{1 + H^2 z^2}.$$

The metric has a singularity at $z \rightarrow \infty$, corresponding to a horizon, and the length of the extra dimension is

$$L = \int_{1/k}^{\infty} \frac{1}{kzG} dz = k^{-1} \sinh^{-1} \frac{k}{H} \approx k^{-1} \log \frac{2k}{H}.$$

The finite size of the observable universe, H^{-1} , acts as an infrared cutoff for the geometry

Continuum in Inflationary 5D geometry

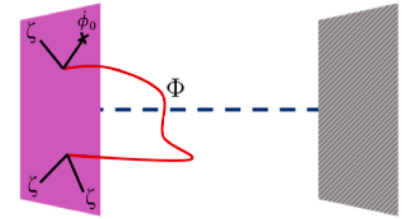


- Switch to a convenient conformal coordinate:

$$ds^2 = e^{-2A(w)} [dt^2 - e^{2Ht} - dw^2], \text{ with } e^{-A(w)} = \frac{H}{k \sinh Hw}$$

Bulk scalar eom: $-\phi'' + 3A'\phi' + m^2 e^{-2A(w)} \phi = -\square_{dS_4} \phi \equiv \mu^2 \phi.$

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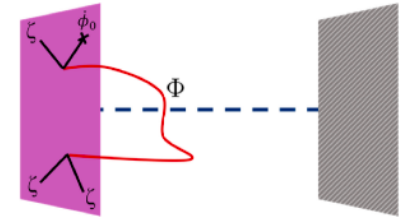
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Bulk Scalar eom after field rescaling ($\phi = \tilde{\phi} e^{3/2 A(w)}$): $-\tilde{\phi}'' + \left[m^2 e^{-2A} + \frac{9}{4} A'^2 - \frac{3}{2} A'' \right] \tilde{\phi} = \mu^2 \tilde{\phi},$

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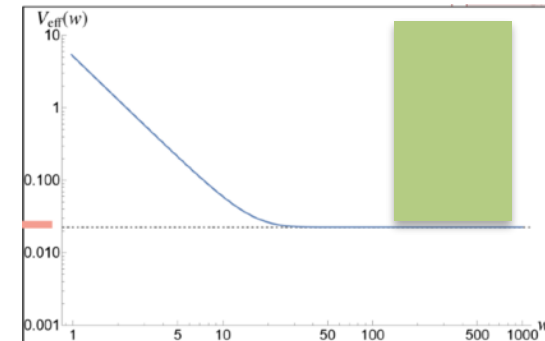
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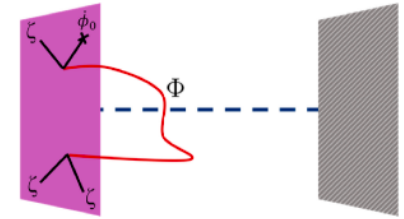
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“Schrödinger Eqn”.: $-\tilde{\phi}'' + \underbrace{H^2 \left[\frac{9}{4} \coth^2(Hw) + \frac{3 + 2m^2}{2 \sinh^2(Hw)} \right]}_{V(w)} \tilde{\phi} = \mu^2 \tilde{\phi}$



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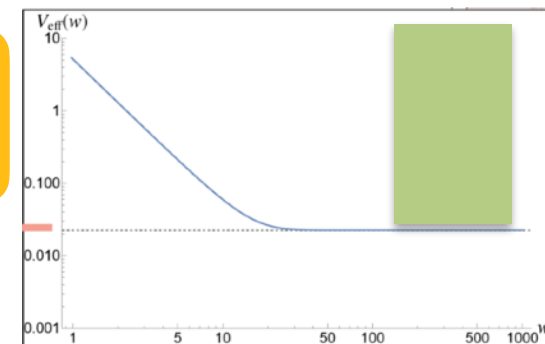
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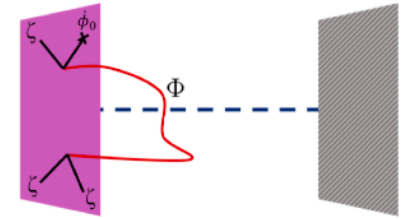
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\Rightarrow Continuum with
Mass Gap!

1D QM
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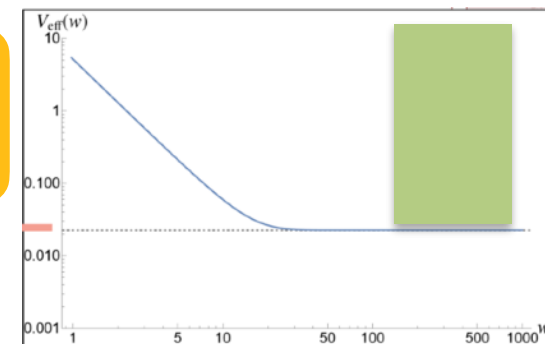
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if $V \xrightarrow{w \rightarrow \infty} \mu_0^2 = \text{finite} \Rightarrow$ Continuum with Mass Gap! 1D QM problem

$$V(w) \rightarrow \frac{9}{4} H^2 \text{ as } w \rightarrow \infty,$$

\Rightarrow continuum begins at: $\mu_0 = (3/2) * H$ for $\xi=0$



Correlation functions and the Spectral Density (From AdS/CFT)

$$\rho(\mu^2) = C(\Delta)(\mu^2)^{\Delta-2}$$

$$\Delta_{\pm} = 2 \pm \sqrt{4 + m^2}$$

unitarity bound, $\Delta \geq 1$

- For CFT (UV brane at the AdS boundary):

both Δ_{\pm} solution works for: $-4 \leq m^2 \leq -3$

describes two CFT's, with each of them associated with a different choice of boundary action for the scalar field

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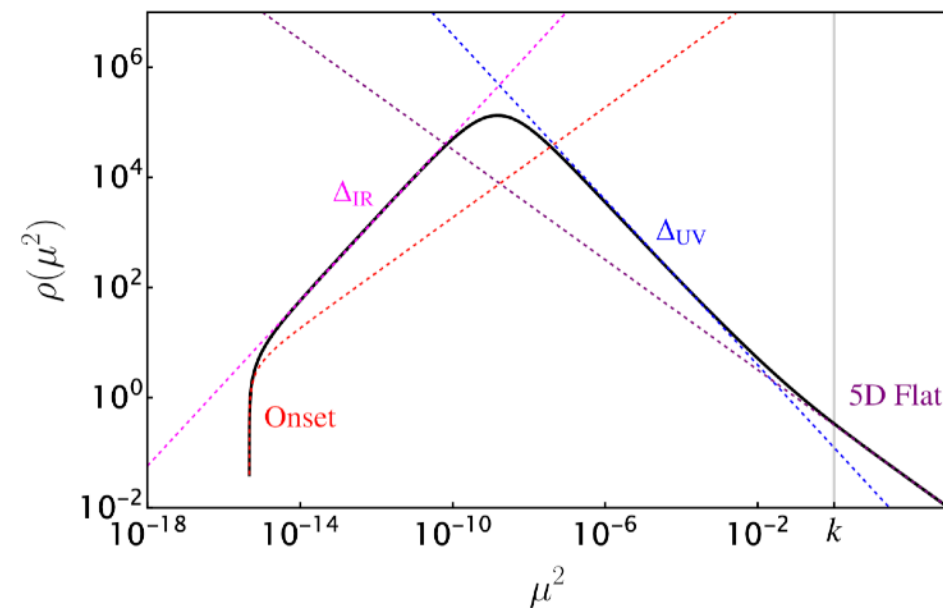
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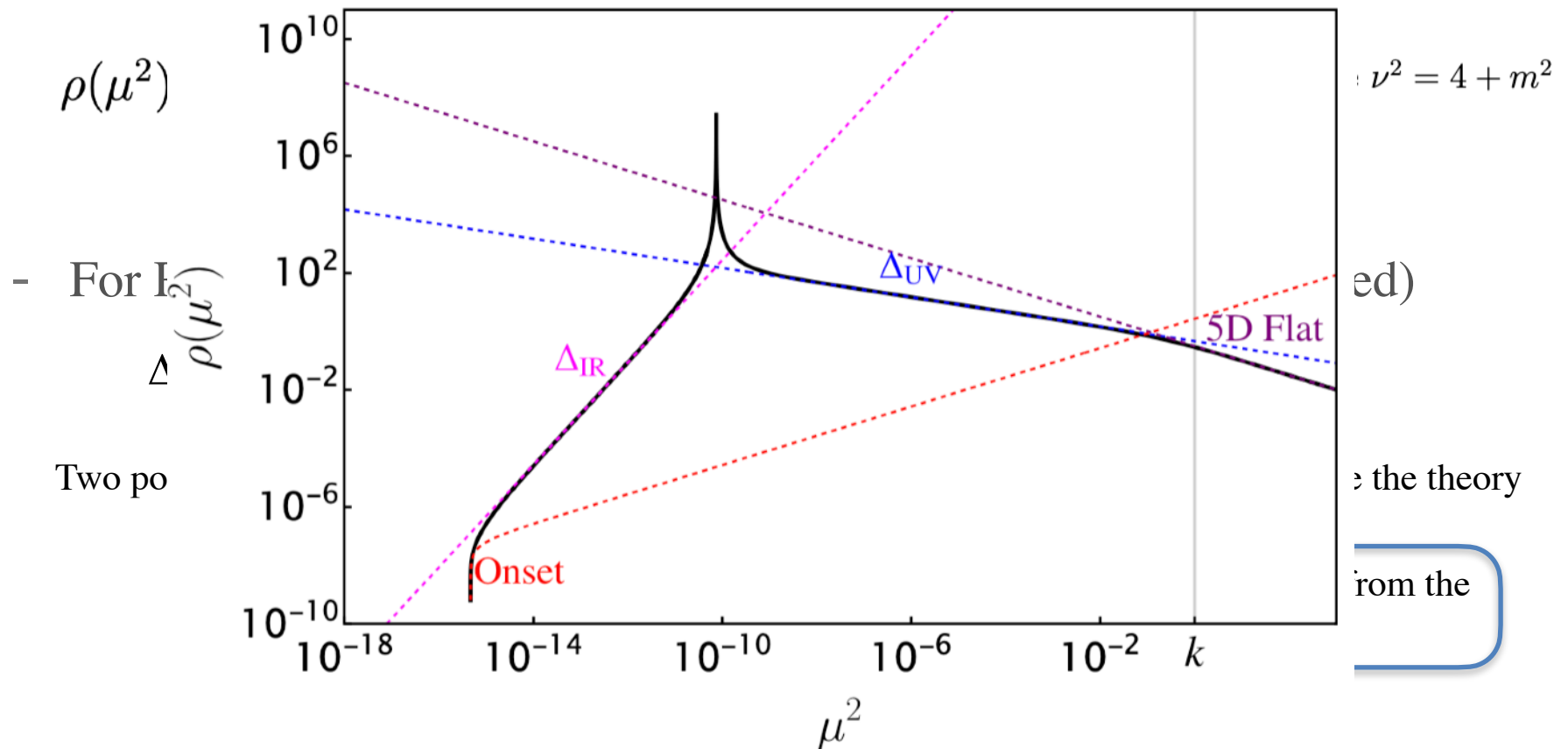
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As the theory transitions between the usual IR scaling, $\Delta_{IR} = \Delta_+$, and $\Delta_{UV} = \nu$ there is typically a sharp particle-like feature in the spectral density separating the two regions of distinct scalings

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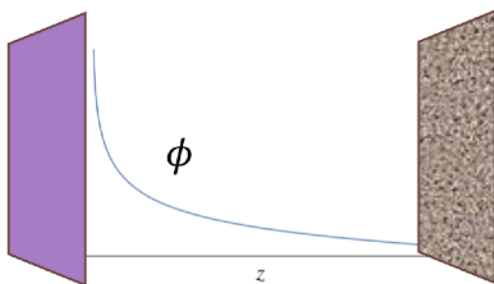
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UV / IR localized light mode

$$\nu^2 = 4 + m^2$$

Light mode: discrete mode below the gap



$\nu > 1$, UV localized, exist when $H=0$

$$\mu^2 = (\nu - 1) \left(m_0^2 - 2(2 - \nu) \right) + 2(2 - \nu)H^2 + \mathcal{O}(H^4)$$

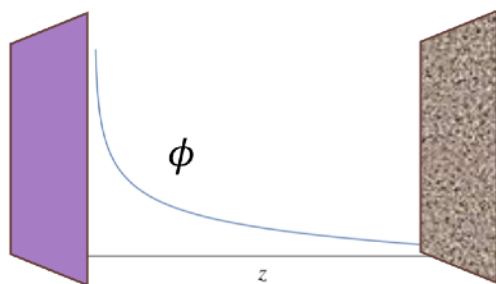
- Tune brane mass $m_0^2 \approx 2(2 - \nu)$
- CFT language: Fundamental bound state in the spectrum mixing with the CFT states; CFT deformation by H backreacts to modify the mass of the particle eigenstate

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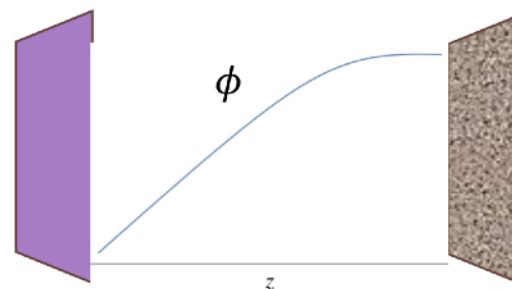


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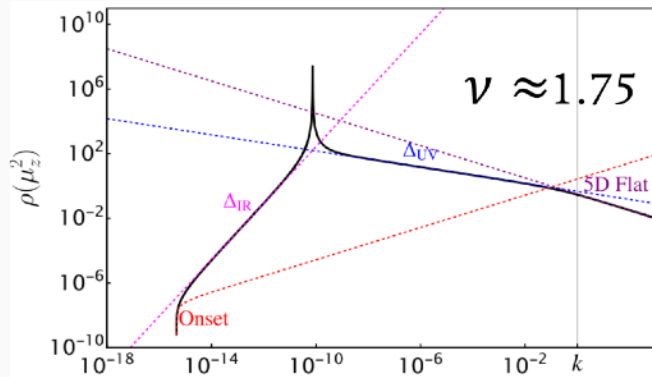
$$\mu^2 \equiv \text{UV}_{\text{mistune}} + \text{IR piece}(H)$$

- Analogous to the horizon localized solutions in Schwarzschild geometries for light scalar fields
- CFT language: Mostly composite modes of the near-conformal dynamics. They only exist during the inflationary epoch

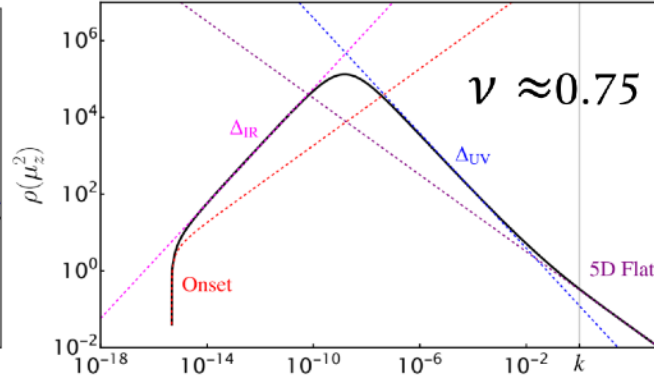
Cosmological Quasiparticles:

Anatomy of Spectral density and Scaling dimension

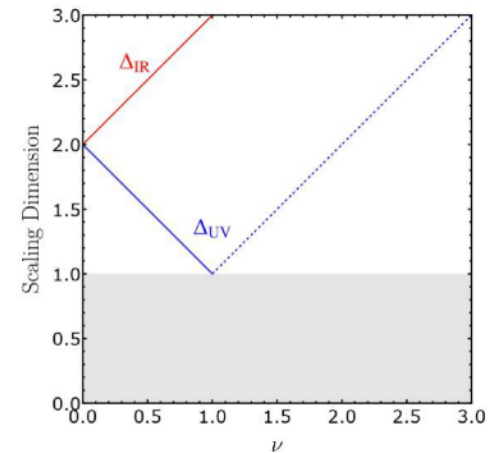
$$\rho(\mu^2) = C(\nu, H) \delta(\mu^2 - \mu_*^2) + \rho_c(\nu, m_0, \mu^2, H) \Theta\left(\mu^2 - \frac{9}{4}H^2\right)$$



$$\begin{aligned} \Delta_{IR} &= \Delta_+ = 2 + \nu \\ \Delta_{UV} &= 2 - \Delta_- = \nu \end{aligned}$$



$$\begin{aligned} \Delta_{IR} &= \Delta_+ = 2 + \nu \\ \Delta_{UV} &= \Delta_- = 2 - \nu \end{aligned}$$



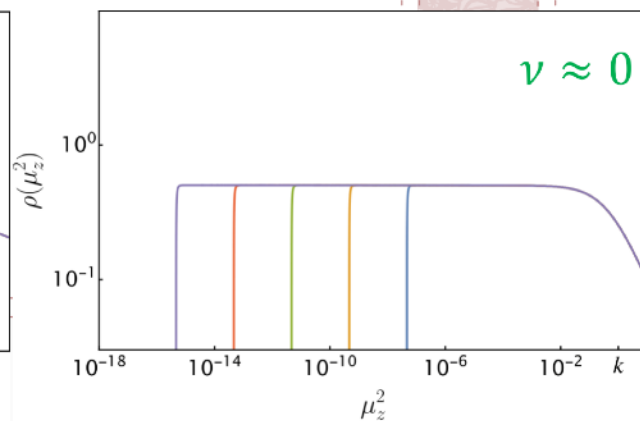
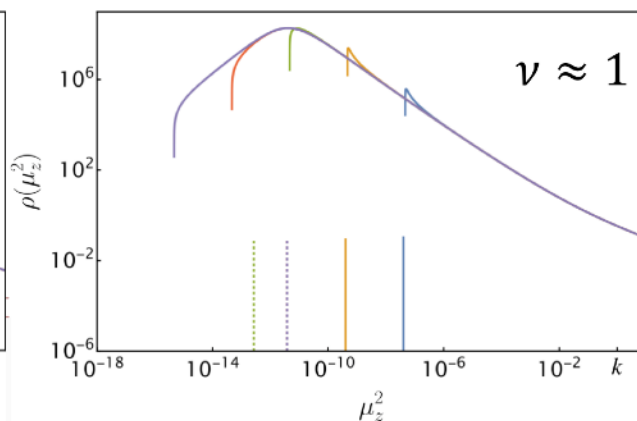
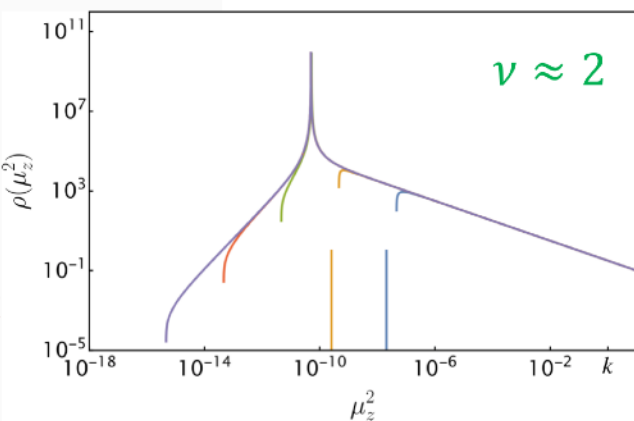
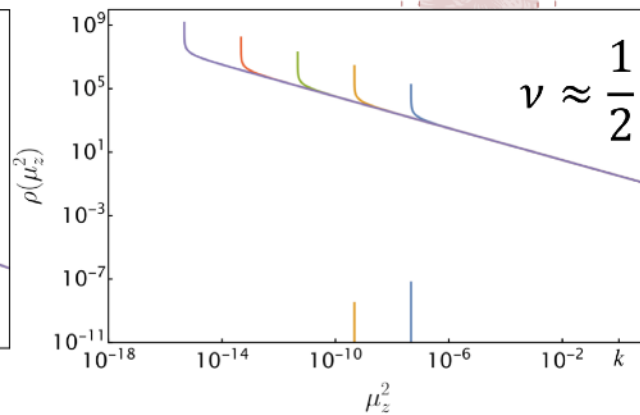
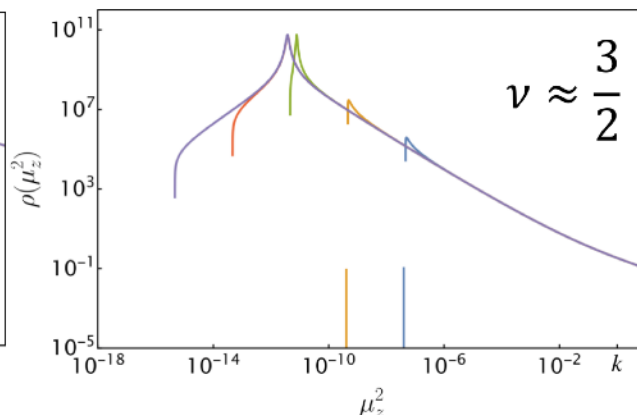
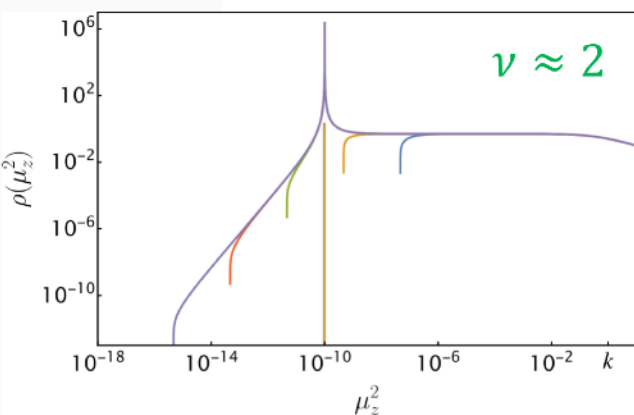
Solutions of 5D scalar equation yield two scaling dimensions:

$$\Delta_{\pm} = 2 \pm \nu = 2 \pm \sqrt{4 + m^2}$$

We have identified a new UV scaling dimension $\Delta_{UV} = 2 - \Delta_-$ when $\nu > 1$

Spectral Density Plots

10^{-4} 10^{-5} 10^{-6} 10^{-7} 10^{-8}

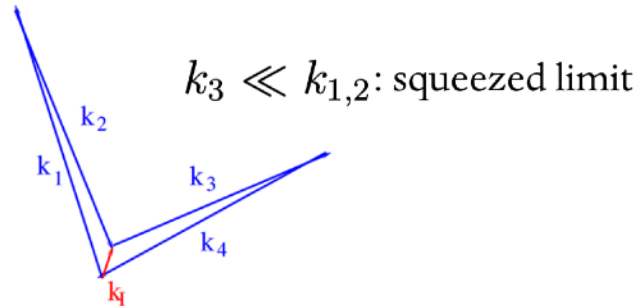
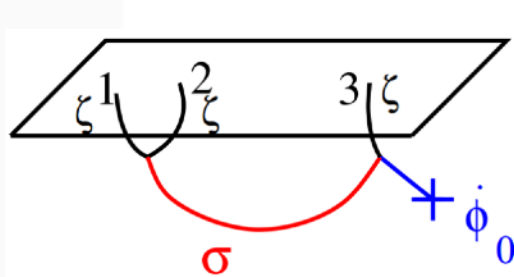


Cosmological Collider Physics

Higher energy physics \longrightarrow Higher energy collider \longrightarrow Higher cost of money

What about nature's cosmological collider?

Primordial quantum fluctuations(fields interact with inflatons) \longrightarrow Non-Gaussianity from CMB bispectrum(fnl)



UV brane localized

scalar inflaton

$$\phi(t, x) = \phi_0(t) + \xi(t, x)$$

$$\zeta = -\frac{H}{\dot{\phi}_0} \xi$$

$$f_{NL} = \frac{5}{3} \left(\frac{\langle \vec{\zeta}_{\vec{k}_1} \vec{\zeta}_{\vec{k}_2} \vec{\zeta}_{\vec{k}_3} \rangle}{4 \langle \vec{\zeta}_{\vec{k}_1} \vec{\zeta}_{-\vec{k}_1} \rangle \langle \vec{\zeta}_{\vec{k}_3} \vec{\zeta}_{-\vec{k}_3} \rangle} \right)_{k_3 \rightarrow 0} = -\frac{\epsilon M_{Pl}^2 \lambda^2}{4\sqrt{\pi}} \frac{\pi^2}{\cosh^2 \pi \gamma} \left(\frac{k_3}{k_1} \right)^{\frac{3}{2}} \times \left[A(\gamma) \left(\frac{k_3}{4k_1} \right)^{-i\gamma} + A^*(\gamma) \left(\frac{k_3}{4k_1} \right)^{i\gamma} \right]$$

Bispectrum

Goal: To find the bispectrum due to an interaction of the inflaton and a massive scalar field of the form $\lambda \int (\nabla \phi)^2 \sigma$

- Currently, let us focus on the non-local contributions in position space, i.e., terms that are non-analytic in k

$$\langle \phi_{\vec{k}}(\eta) \phi_{-\vec{k}}(\eta') \rangle \supset \frac{(\eta \eta')^{\frac{3}{2}}}{4\pi} \left[\Gamma(-i\gamma)^2 \left(\frac{k^2 \eta \eta'}{4} \right)^{i\gamma} + \Gamma(i\gamma)^2 \left(\frac{k^2 \eta \eta'}{4} \right)^{-i\gamma} \right]$$

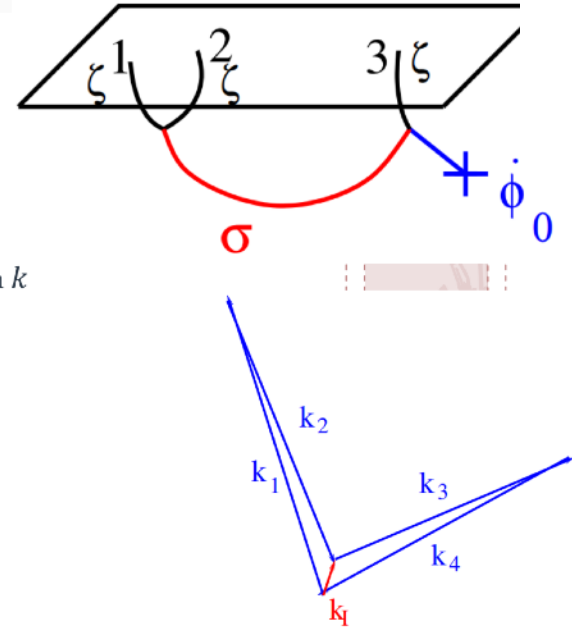
- To find the bispectrum, we find the 4-point correlator and set one of the legs to the background

$$\begin{aligned} \langle \phi_{\vec{k}_1}(\eta_0) \cdots \phi_{\vec{k}_4}(\eta_0) \rangle &\supset \frac{\eta_0^4 2^2 \lambda^2}{16 k_1 k_2 k_3 k_4} (I_{++} + I_{+-} + I_{-+} + I_{--}) \\ I_{\pm\pm} &= (\pm i)(\pm i) \int_{-\infty}^0 \frac{d\eta}{\eta^2} e^{\pm i k_{12} \eta} \int_{-\infty}^0 \frac{d\eta'}{\eta'^2} e^{\pm i k_{34} \eta'} \langle \sigma_{\vec{k}_1}(\eta) \sigma_{-\vec{k}_1}(\eta') \rangle_{\pm\pm} \end{aligned}$$

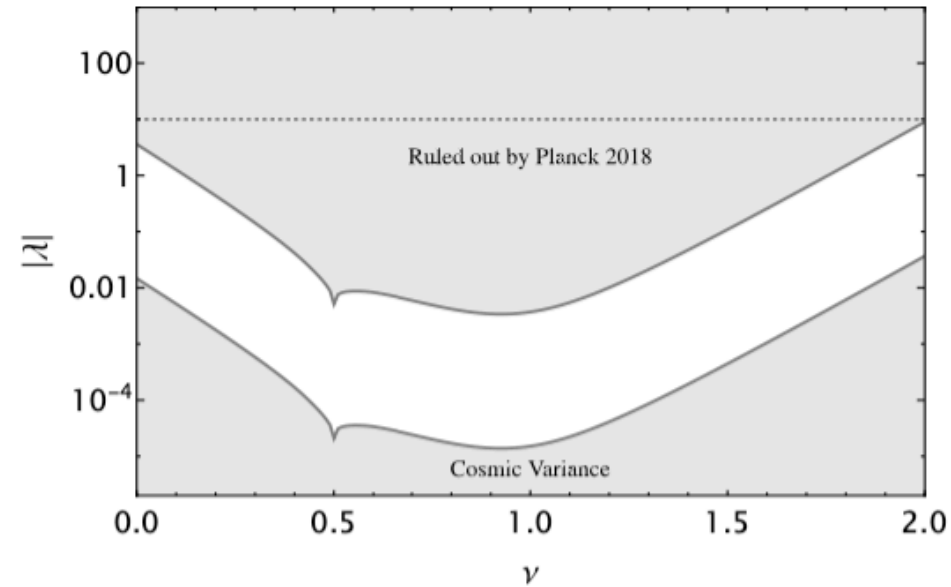
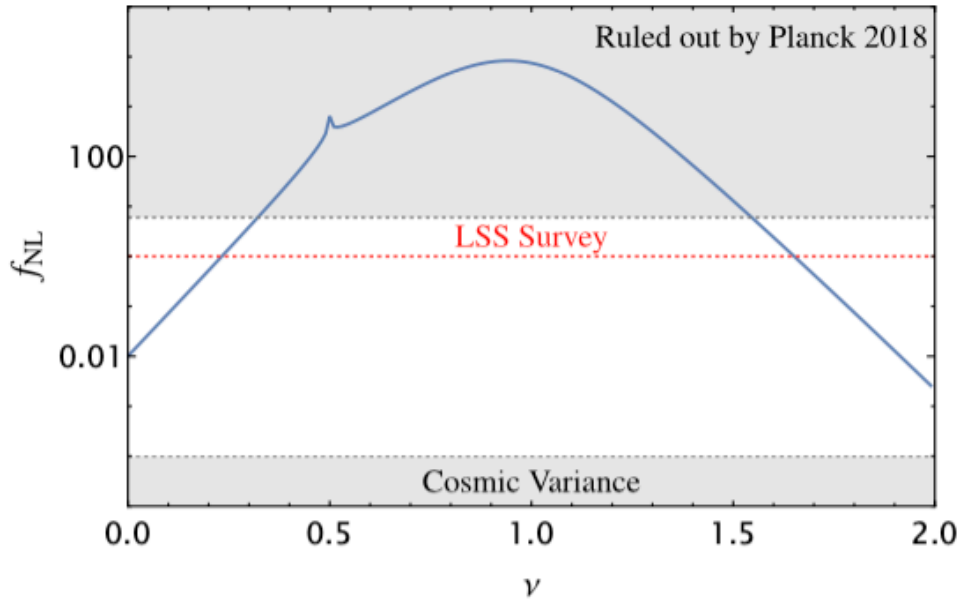
- Fluctuations of the inflaton $\phi(t, x) = \phi_0(t) + \xi(t, x)$ can be related to the curvature fluctuation

$$\zeta = -\frac{H}{\dot{\phi}_0} \xi$$

$$f_{NL} = \frac{5}{3} \left(\frac{\langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \zeta_{\vec{k}_3} \rangle}{4 \langle \zeta_{\vec{k}_1} \zeta_{-\vec{k}_1} \rangle \langle \zeta_{\vec{k}_3} \zeta_{-\vec{k}_3} \rangle} \right)_{k_3 \rightarrow 0} = -\frac{\epsilon M_{Pl}^2 \lambda^2}{4\sqrt{\pi}} \frac{\pi^2}{\cosh^2 \pi \gamma} \left(\frac{k_3}{k_1} \right)^{\frac{3}{2}} \times \left[A(\gamma) \left(\frac{k_3}{4k_1} \right)^{-i\gamma} + A^*(\gamma) \left(\frac{k_3}{4k_1} \right)^{i\gamma} \right]$$



Results of non-Gaussianity



$\lambda=1$ (in unit of k , the AdS curvature)

$H=10^{13}$ GeV

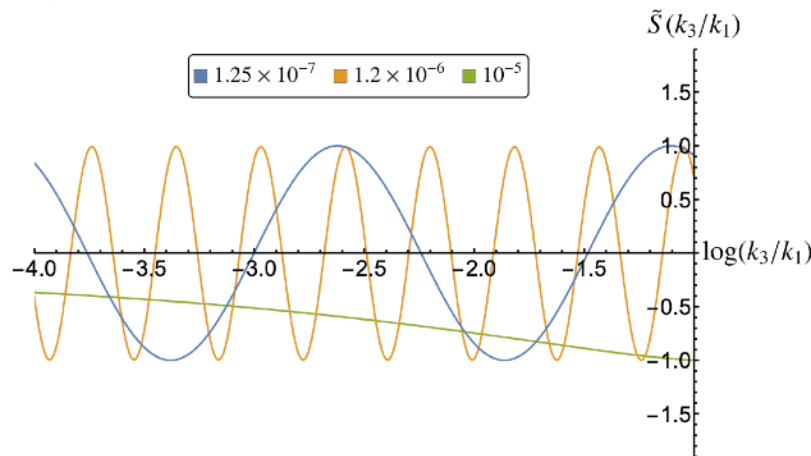
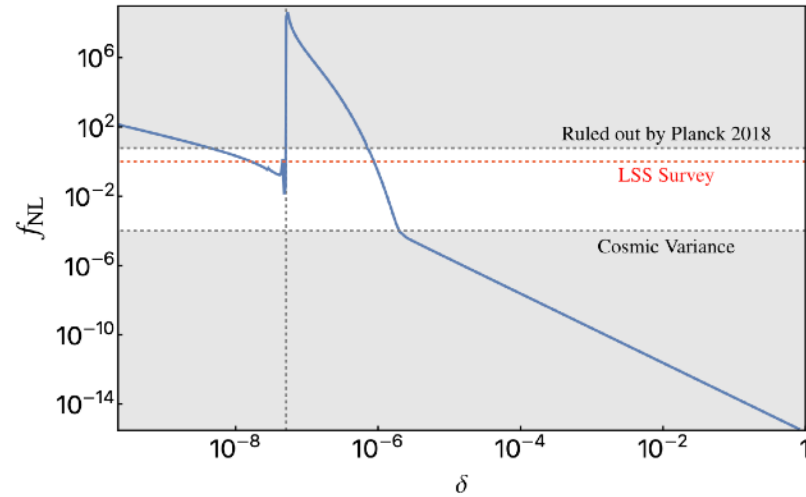
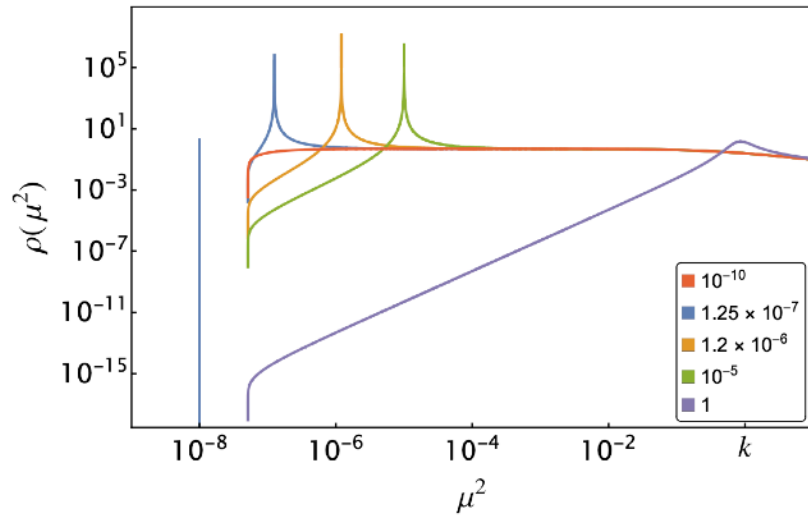
$\frac{k_3}{k_1} = 0.1$

Coupling term: $\lambda\phi(\nabla\zeta)^2$

Shaded area: Ruled out

Blank: Allowed according to current experiments

Small Bulk Mass: $m^2 \approx 0$ $L \ni \lambda O$ with $[O] \sim 4$



$$\delta \equiv m_0^2 - 2(2 - \nu)$$

$$F_{NL}(k_3/k_1) = f_{NL} \left(\frac{k_3}{k_1} \right)^{3/2} \tilde{S}(k_3/k_1).$$

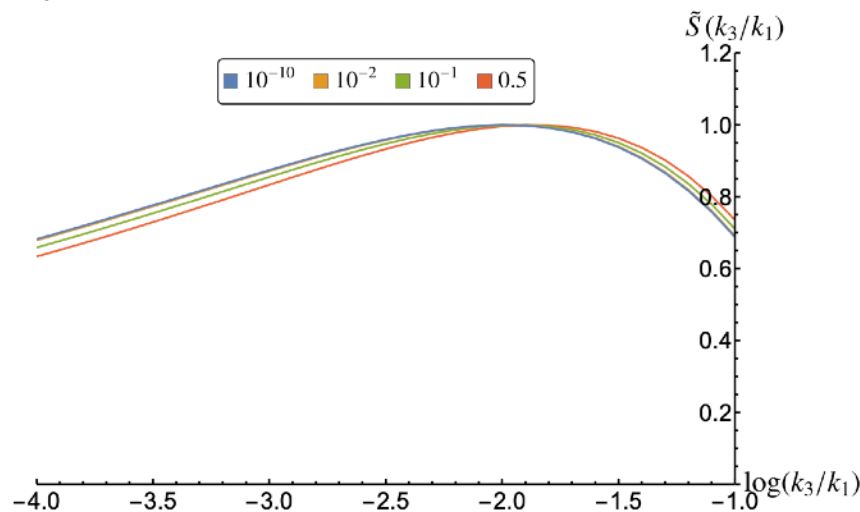
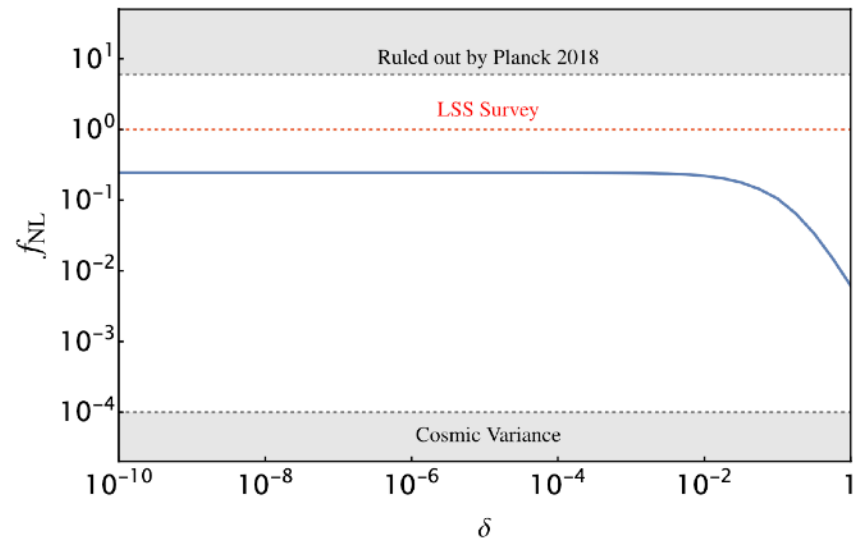
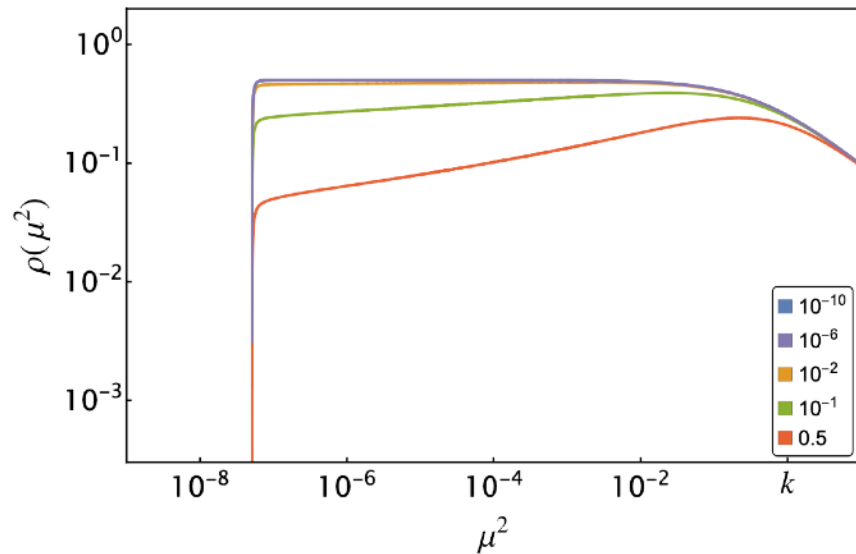
The spectral densities and f_{NL} when the scalar bulk mass $m^2 \sim 0$ for various values of UV brane mistunes, δ . We also show some of the shape functions, which exhibit clear oscillatory behavior when there is a particle slightly above the critical mass, $3/2H$.

Small Bulk Mass: $m^2 \approx -4$ $L \ni \lambda O^\dagger O$ with $[O] \sim 2$

$$\beta = -\lambda^2$$

$$\nu \approx 0 \quad \delta = 2(\nu - \lambda)$$

-can lead to an IR localized state that is near to the horizon, producing a “cosmological quasiparticle”



$$\delta \equiv m_\sigma^2 - 2(2 - \nu)$$

$$F_{\text{NL}}(k_3/k_1) = f_{\text{NL}} \left(\frac{k_3}{k_1} \right)^{3/2} \tilde{S}(k_3/k_1).$$

Conclusions and Outlook

- We considered a simple model of inflation in a holographic setup and found the spectrum of a scalar operator in the large N CFT- a **gapped continuum**
- We find a **UV localized light mode** when the UV boundary conditions are somewhat tuned
- We also find a normalizable transient cosmological **IR localized light mode** when $\nu < 1$ localized, that tracks the gap of the spectral density without fine-tuning
- We find a **novel scaling dimension** in the UV when $\nu > 1$.
- The non-analytic particle-like feature can rise above the continuum contributions, giving the “smoking gun” oscillatory features in the shape function for F_{NL}
- The continuum seems to generate non-Gaussian features that are detectable in future cosmological experiments!
- An extra coupling term $\xi R\phi^2$ of curvature and scalar field can shift the gap

Thank you!