

SUSY Seesaw and LFV in the Era of the LHC

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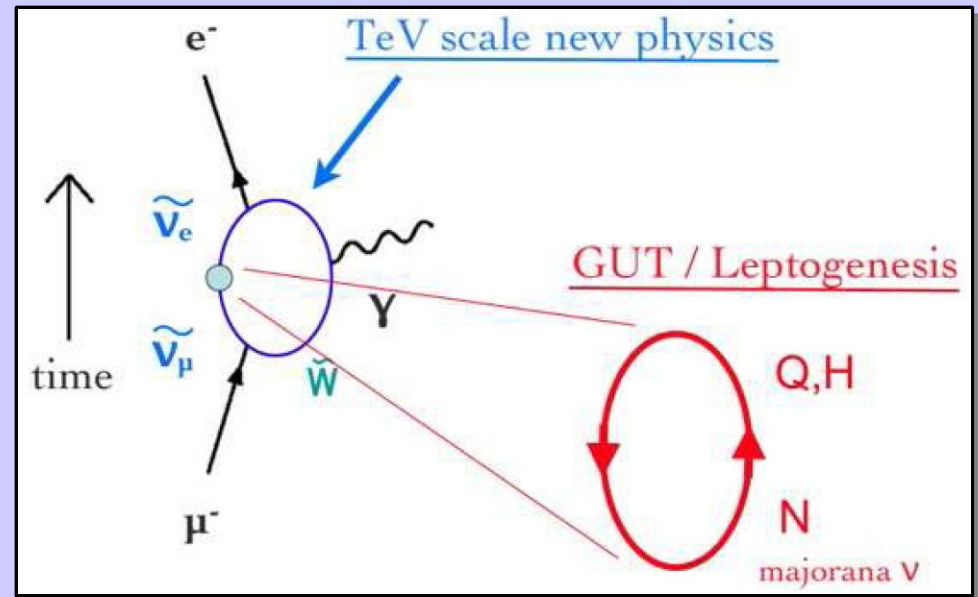
IPPP Seminar
Durham, December 4, 2008

Overview

- **Introduction**
 - Lepton Flavor Violation
 - Supersymmetry
 - Neutrino Physics
- **SUSY Seesaw**
 - Mechanism
 - Rare LFV Processes
- **LFV Signals at LHC**
- **Precision Slepton Mass Measurements**
- **Conclusion**

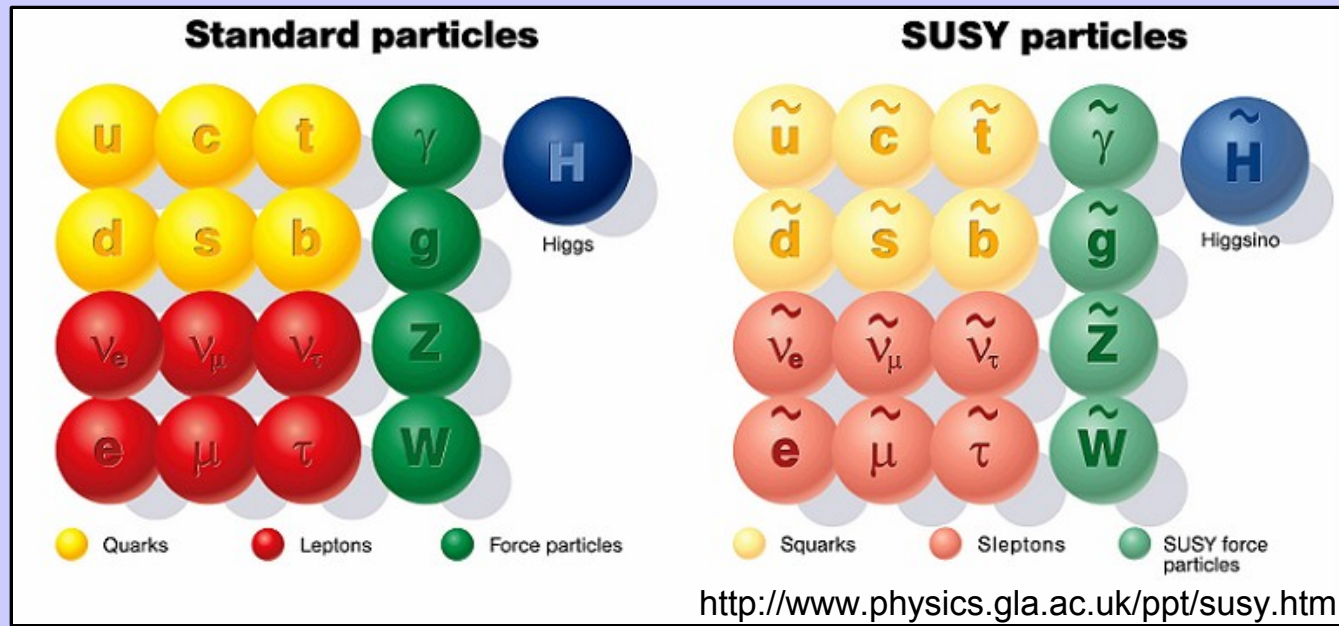
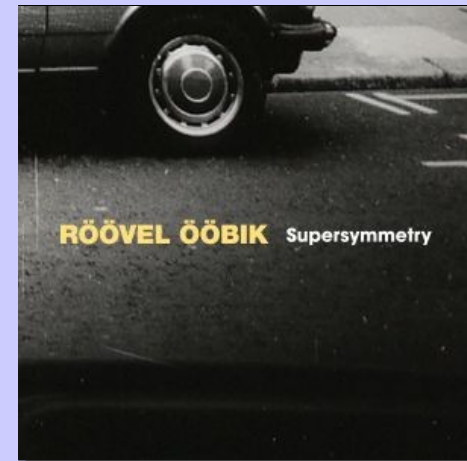
Lepton Flavor Violation

- **Lepton Flavor conserved in the Standard Model**
⇒ LFV is clear sign for BSM physics
- **Flavor Violation in quark and neutrino sector**
⇒ Strong case to look for charged LFV
- **LFV can shed light on**
 - Grand Unification Models, Connection to quark flavor violation
 - Flavor Symmetries
 - Origin of Flavor
- **Existing experimental bounds are stringent and will be improved in the near future**



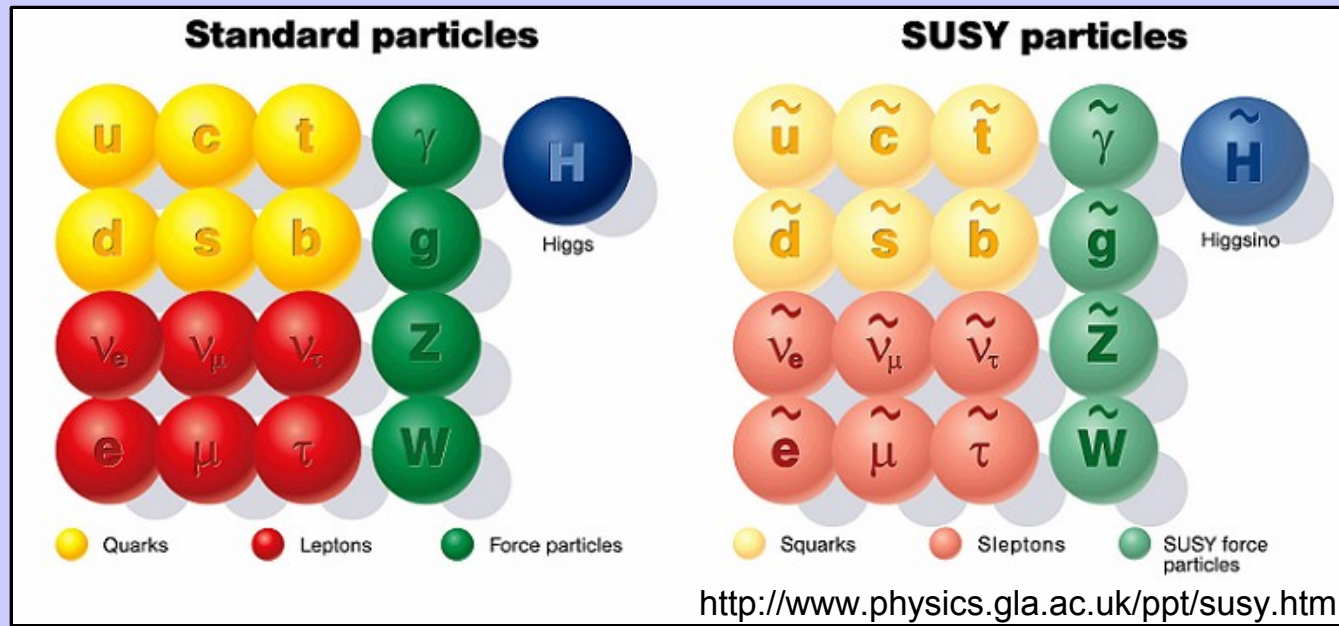
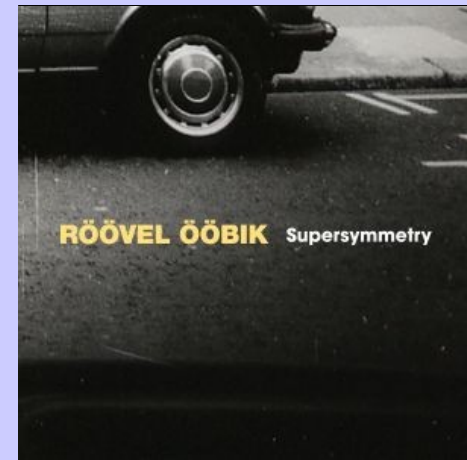
Supersymmetry

MSSM: Minimal extension of the Standard Model with two Higgs doublets and conserved R-parity



Supersymmetry

MSSM: Minimal extension of the Standard Model with two Higgs doublets and conserved R-parity



SUSY must be broken

⇒ In general: Introduction of more than 100 free parameters

⇒ Required: Theoretical framework for SUSY breaking

⇒ **Minimal Supergravity (mSUGRA), Universality at GUT Scale**

Neutrinos

Oscillations

- **Standard Model: neutrinos are massless**
- **Neutrino Oscillations**
 \Rightarrow Neutrinos have masses and flavors mix

$$U^T m_\nu U = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3})$$

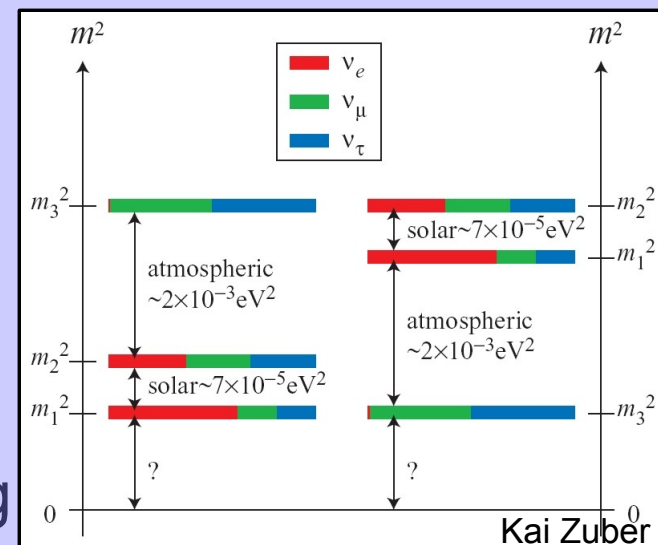
$$U = \begin{pmatrix} c_{13}c_{12} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - s_{23}s_{13}c_{12} & c_{23}c_{12} - s_{23}s_{13}s_{12} & s_{23}c_{13} \\ s_{23}s_{12} - s_{13}c_{23}c_{12} & -s_{23}c_{12} - s_{13}s_{12}c_{23} & c_{23}c_{13} \end{pmatrix} \times \text{diag}(e^{i\phi_1}, e^{i\phi_2}, 1)$$

- **Mixing angles and mass differences**

$$\sin^2 \theta_{12} = 0.30^{+0.04}_{-0.05}, \quad \sin^2 \theta_{23} = 0.50^{+0.14}_{-0.12}, \quad \sin^2 \theta_{13} < 0.028$$

$$\Delta m_{12}^2 = (8.1^{+0.6}_{-0.6}) \cdot 10^{-5} \text{ eV}^2, \quad \Delta m_{13}^2 = \pm (2.2^{+0.7}_{-0.5}) \cdot 10^{-3} \text{ eV}^2$$

\Rightarrow Nearly bi-maximal mixing \neq Quark mixing



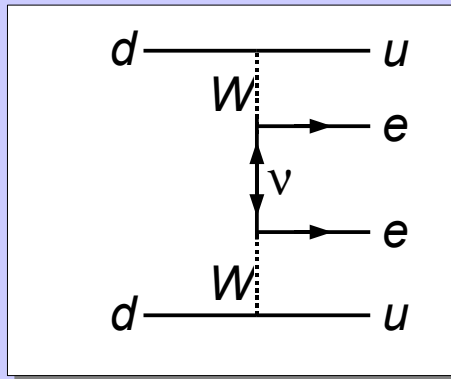
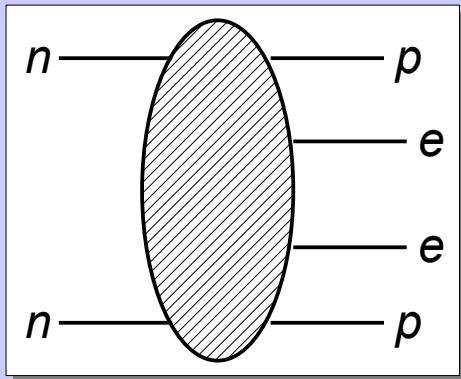
Neutrinos

Absolute Mass Scale

- Oscillation experiments can not determine absolute neutrino masses

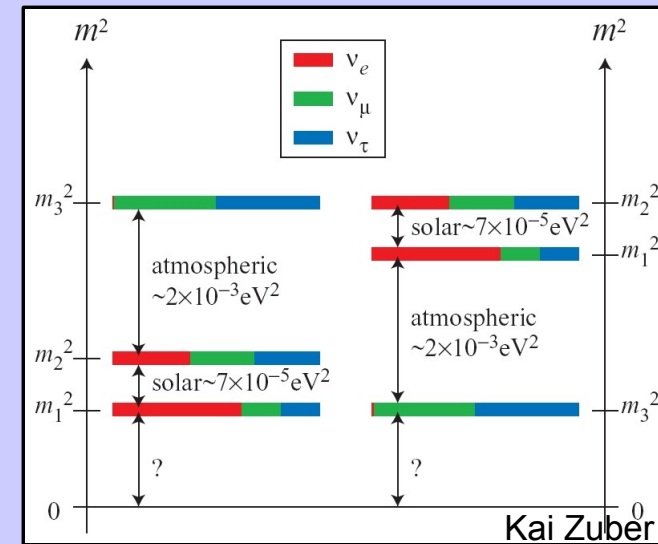
- Bounds from

- Cosmology (WMAP) $\sum m_{\nu_i} < 2 \text{ eV}$
- Tritium-Decay Endpoint (KATRIN)
- Neutrinoless double beta decay (Heidelberg-Moscow, Evidence?)



$$m_{ee} = \sum U_{ei}^2 m_{\nu_i} = (0.24 - 0.58) \text{ eV}$$

- Absolute mass scale $m_{\nu_1} = 0 \dots 0.5 \text{ eV}$



SUSY Seesaw

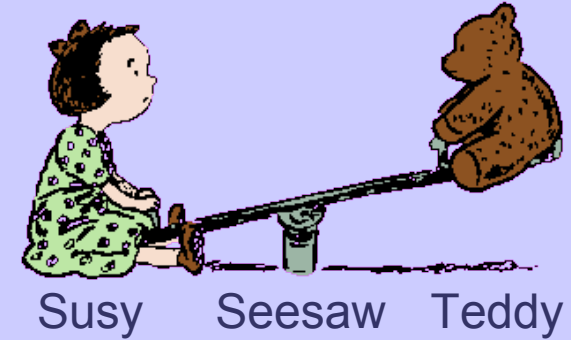
Collaboration with **H. Päs, A. Redelbach, R. Rückl**
Phys. Rev. D73 (2006) 033004 (hep-ph/0511062)
Phys. Rev. D69 (2004) 054014 (hep-ph/0310053)
Eur. Phys. J. C28 (2003) 365-374 (hep-ph/0206122)

SUSY Seesaw

Mechanism

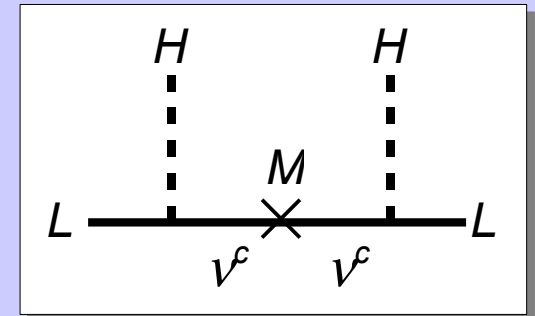
- Add right-handed neutrinos to (MS)SM particle content, Seesaw Type I

$$W = W_{\text{MSSM}} - \frac{1}{2} \hat{\nu}_R^{cT} M_R \hat{\nu}_R^c + \hat{\nu}_R^{cT} Y_\nu \hat{L} \cdot \hat{H}_u$$



- Diagonalize seesaw matrix assuming super-heavy right-handed neutrinos

$$\begin{pmatrix} 0 & m_D^T \\ m_D & M_R \end{pmatrix} \quad \text{with} \quad m_D = Y_\nu \langle H_u^0 \rangle \ll M_R$$



- Effective light neutrino mass matrix at low energies

$$m_\nu = m_D^T M^{-1} m_D \quad \text{for} \quad m_D \ll M_R \quad m_\nu \approx 0.1 \text{eV} \left(\frac{m_D}{100 \text{GeV}} \right)^2 \left(\frac{M_R}{10^{14} \text{GeV}} \right)^{-1}$$

Seesaw Mechanism

Variations

Seesaw I

$$\begin{pmatrix} \nu_i \\ e_i \end{pmatrix}, e_i^c, \nu_i^c$$

$$\begin{pmatrix} 0 & m_D^T \\ m_D & M_R \end{pmatrix}$$

$$m_D \ll M_R \Rightarrow m_\nu = m_D^T M^{-1} m_D$$

$$\frac{m_\nu}{0.1\text{eV}} = \frac{m_D^2}{(100\text{GeV})^2} \frac{10^{14}\text{GeV}}{M_R}$$

Seesaw II

$$\begin{pmatrix} \nu_i \\ e_i \end{pmatrix}, e_i^c, \nu_i^c$$

$$\begin{pmatrix} m_{LL} & m_D^T \\ m_D & M_R \end{pmatrix}$$

$$m_D \ll M_R \Rightarrow m_\nu = m_{LL} - m_D^T M^{-1} m_D$$

Seesaw III

$$\begin{pmatrix} \nu_i \\ e_i \end{pmatrix}, e_i^c, \nu_i^c, S_i$$

$$\begin{pmatrix} 0 & m_D^T & 0 \\ m_D & 0 & M_R^T \\ 0 & M_R & \mu \end{pmatrix}$$

$$\mu, m_D \ll M_R \Rightarrow m_\nu = m_D^T M_R^{T-1} \mu M_R^{-1} m_D$$

$$\frac{m_\nu}{0.1\text{eV}} = \frac{m_D^2}{(100\text{GeV})^2} \frac{\mu}{\text{keV}} \frac{(10^4\text{GeV})^2}{M_R^2}$$

- All three variations can emerge in SO(10) GUT models
- SUSY Seesaw as effective model of neutrino sector

SUSY Seesaw

Sleptons

Seesaw without SUSY

- Not testable, only effective light neutrino properties accessible (9 of 18 model parameters)
- Charged LFV is suppressed by tiny neutrino masses

SUSY Seesaw

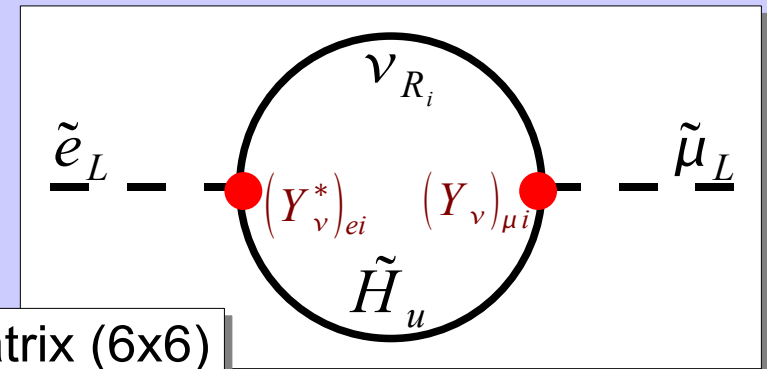
Sleptons

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SUSY Seesaw

- Neutrino flavor mixing radiatively induces slepton flavor mixing between M_{GUT} and the right-handed neutrino mass scale
(Masiero, Borzumati)



Slepton mass matrix (6x6)

$$m_{\tilde{l}}^2 = \begin{pmatrix} m_{\tilde{L}}^2 & (m_{\tilde{L}R}^2)^+ \\ m_{\tilde{L}R}^2 & m_{\tilde{R}}^2 \end{pmatrix}$$

SUSY Seesaw

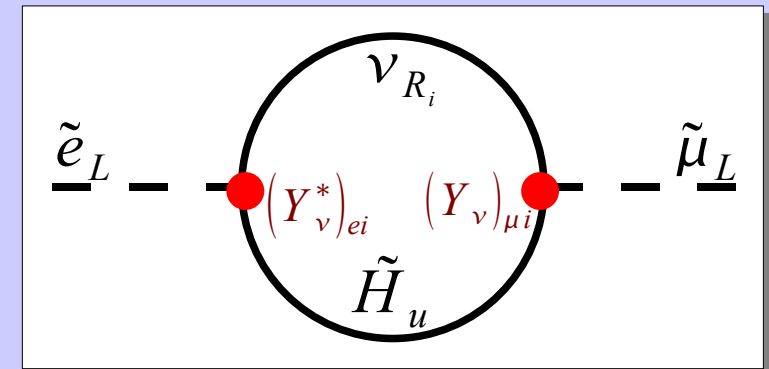
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SUSY Seesaw

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- Correlation between slepton and neutrino flavor mixing

$$\delta m_{\tilde{L}}^2 = \begin{pmatrix} \delta_{11} & \delta_{12} & \delta_{13} \\ \delta_{12}^* & \delta_{22} & \delta_{23} \\ \delta_{13}^* & \delta_{23}^* & \delta_{33} \end{pmatrix} = \frac{-1}{8\pi^2} (3m_0^2 + A_0^2) Y_\nu^+ \cdot Y_\nu \log\left(\frac{M_{\text{GUT}}}{M_R}\right)$$

$|\delta_{12}| \Rightarrow Br(\mu \rightarrow e \gamma), \text{ etc.}$

\Rightarrow 9 potential observables

\Rightarrow SUSY Seesaw testable (in principle)

$\Im(\delta_{ij}) \Rightarrow$ EDMs d_e, d_μ

Slepton mass differences (Colliders)

Rare LFV Processes

- **Current bounds** and **future sensitivities**
 - $\text{Br}(\mu \rightarrow e \gamma) < 1.2 \cdot 10^{-11}$ (MEGA) 10^{-13} (MEG, 2009)
 - $\text{Br}(\tau \rightarrow \mu \gamma) < 6.8 \cdot 10^{-8}$ (Belle) 10^{-8} (Super-B Factory, LHC?)
 - $\text{Br}(\tau \rightarrow e \gamma) < 3.7 \cdot 10^{-7}$ (BaBar) 10^{-8} (Super-B Factory)
 - $R(\mu N \rightarrow e N) < 7 \cdot 10^{-13}$ (Sindrum) 10^{-18} (PRIME), μ - e conversion in nuclei
 - $\mu \rightarrow 3e$, $\tau \rightarrow 3\mu$ (LHC), etc.

Rare LFV Processes

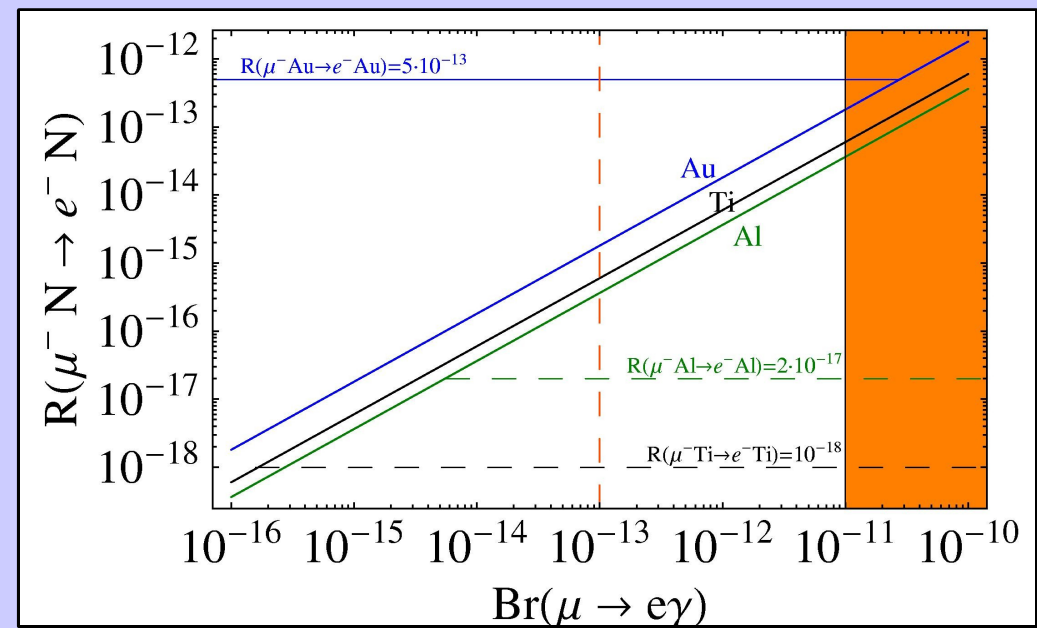
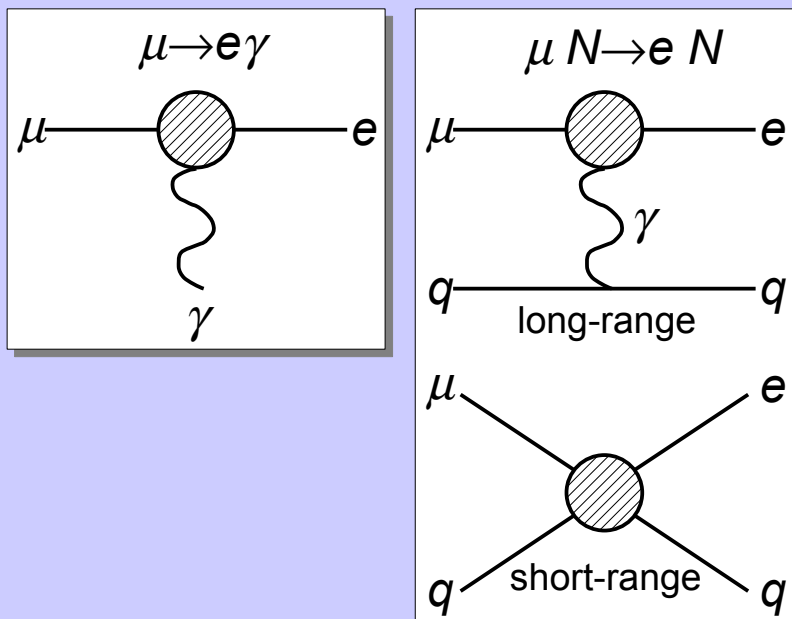
- **Current bounds**

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- $\mu \rightarrow 3e, \tau \rightarrow 3\mu$ (LHC), etc.

- **and future sensitivities**

- 10^{-13} (MEG, 2009)
- 10^{-8} (Super-B Factory, LHC?)
- 10^{-8} (Super-B Factory)
- 10^{-18} (PRIME), μ - e conversion in nuclei

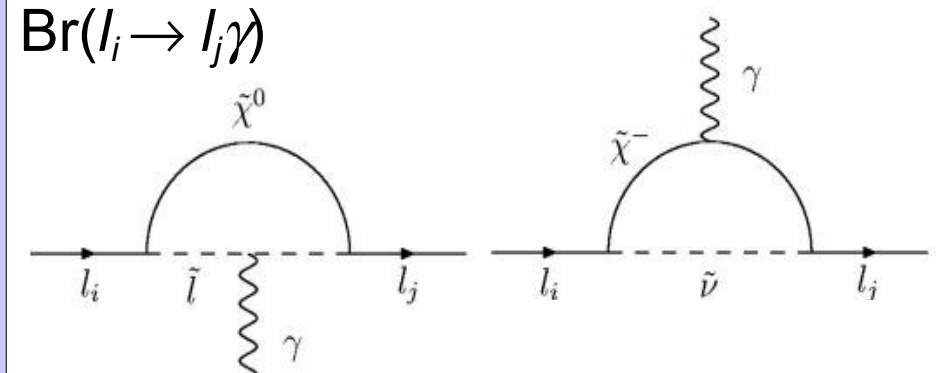
- **SUSY Seesaw: Correlation between processes of same flavor transition**



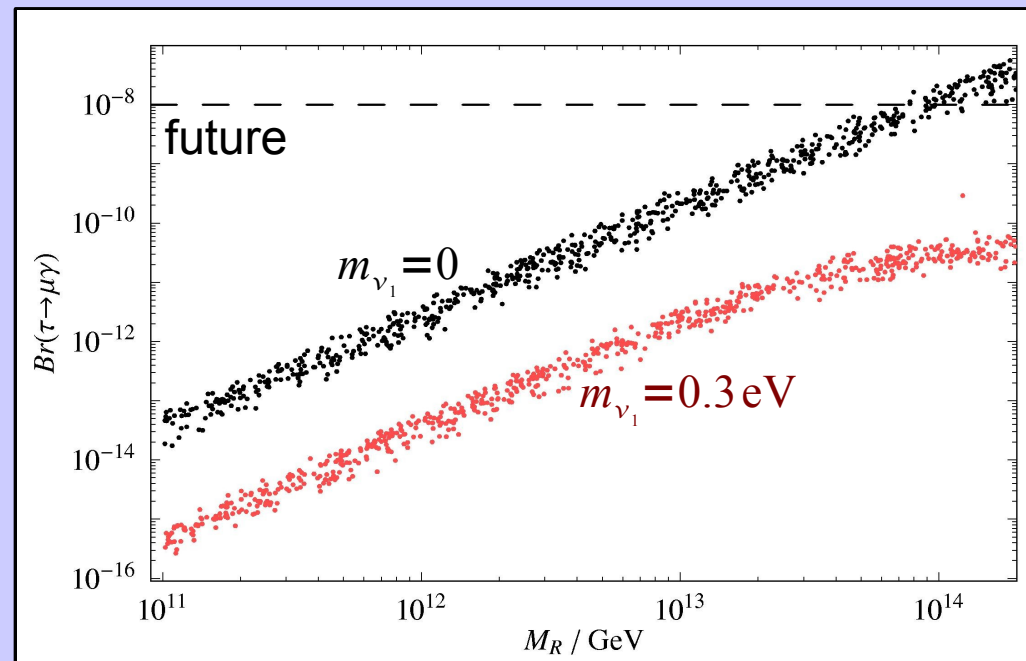
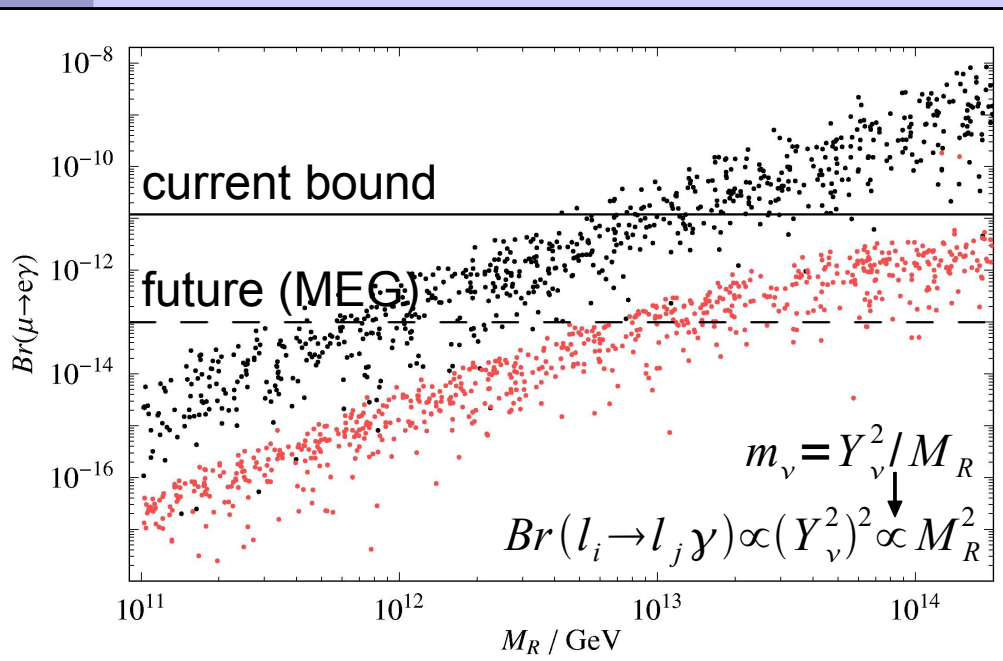
Rare LFV Decays

SUSY Seesaw

- Scattering of neutrino parameters
- Fixed SUSY scenario SPS1a
- Hierarchical (**Degenerate**) light neutrinos
- Degenerate heavy neutrinos $M_{\nu_i} = M_R$
- Strong dependence with M_R



$$Br(l_i \rightarrow l_j \gamma) \approx \frac{\alpha^3 \tan^2 \beta}{\tilde{m}^8} \frac{m_{l_i}^5}{\Gamma_{l_i}} \left| (\delta m_L^2)_{ij} \right|^2 \propto (Y_\nu^+ L Y_\nu)^2_{ij}$$



LFV Signals at LHC

Collaboration with **S. Albino, D. Ghosh, R. Rückl**

Report of WG3 CERN Workshop 'Flavor in the era of the LHC' (arXiv:0801.1826)

Eur. Phys. J. C46 (2006) 43-60 (hep-ph/0511344)

Phys. Rept. 426 (2006) 47-358 (hep-ph/0410364)

LFV at LHC

LFV Neutralino and Slepton Decays

- Squark and gluino production

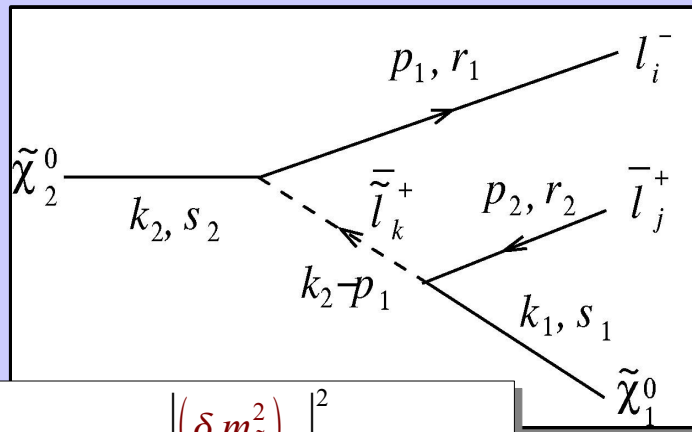
$$pp \rightarrow \tilde{q} \tilde{q}, \tilde{g} \tilde{q}, \tilde{g} \tilde{g}$$

- ... followed by cascade decays via second lightest neutralino

$$\tilde{q}(\tilde{g}) \rightarrow \tilde{\chi}_2^0 q(g)$$

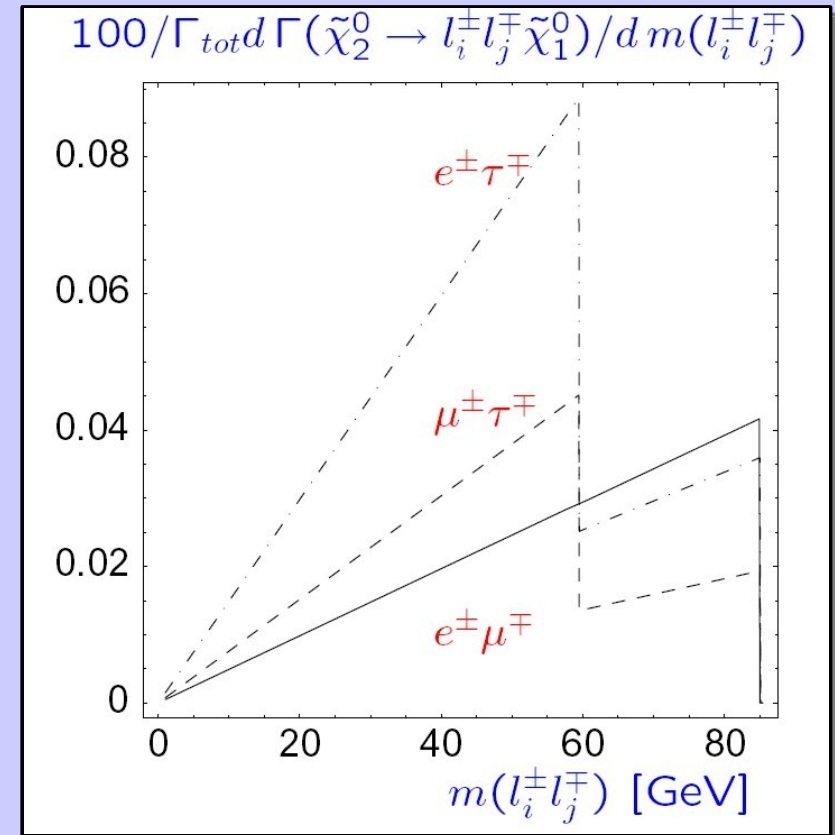
- ... followed by LFV decay via sleptons

(Agashe/Graesser, Hisano et al., Bartl et al., Hinchliffe/Paige, Carvalho et al., Andreev et al.)



$$Br(\tilde{\chi}_2^0 \rightarrow \mu^- e^+ \tilde{\chi}_1^0) \propto \frac{|\left(\delta m_L^2\right)_{12}|^2}{m_i^2 \Gamma_i^2} Br(LFC)$$

- Edge structure of di-lepton invariant mass distribution



- Reach

$$Br(\tilde{\chi}_2^0 \rightarrow \mu e \tilde{\chi}_1^0) = 2 - 4\%, L = 30 \text{ fb}^{-1}$$

LFV at the LHC

Signals and Background

- Possible signal signatures

$$pp \rightarrow l_i l_j + 2 j + E_T^{\text{miss}}$$

$$l_i l_j + 3 j + E_T^{\text{miss}}$$

$$l_i l_j l_k l_k + 2 j + E_T^{\text{miss}}$$

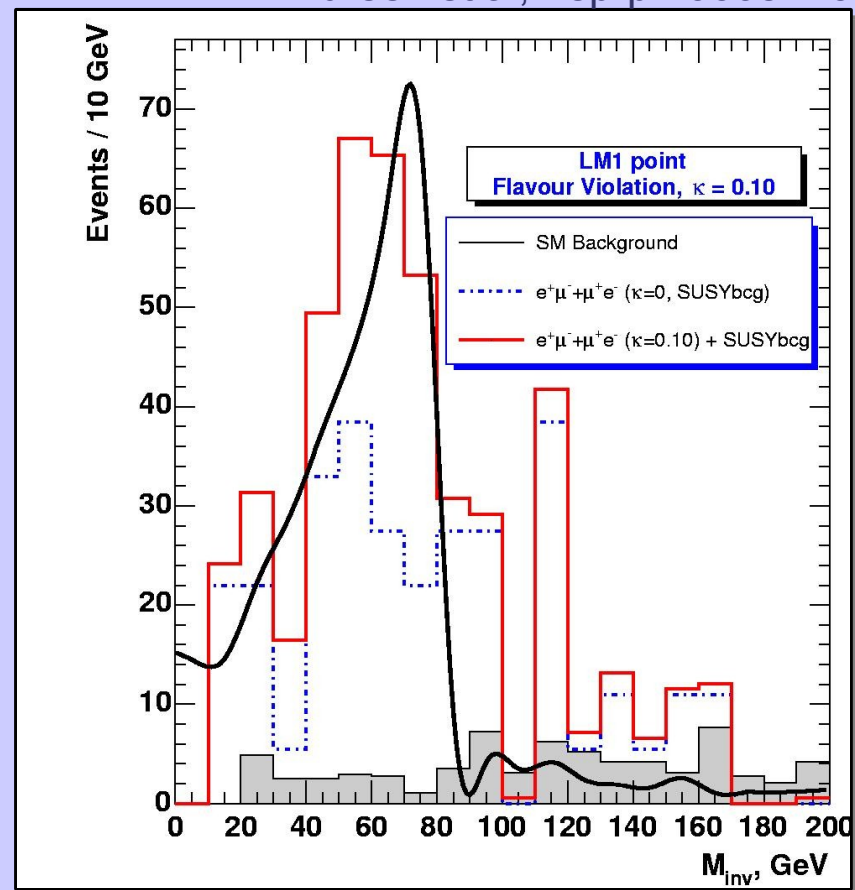
- Exploit edge structure of signal invariant mass distribution

$$\left(m_{\text{inv}}^{\text{max}}(l_i^- l_j^+)\right)^2 = m_{\tilde{\chi}_2^0}^2 \left(1 - \frac{m_{\tilde{l}}^2}{m_{\tilde{\chi}_2^0}^2}\right) \left(1 - \frac{m_{\tilde{\chi}_1^0}^2}{m_{\tilde{l}}^2}\right)$$

- Sensitivity estimate

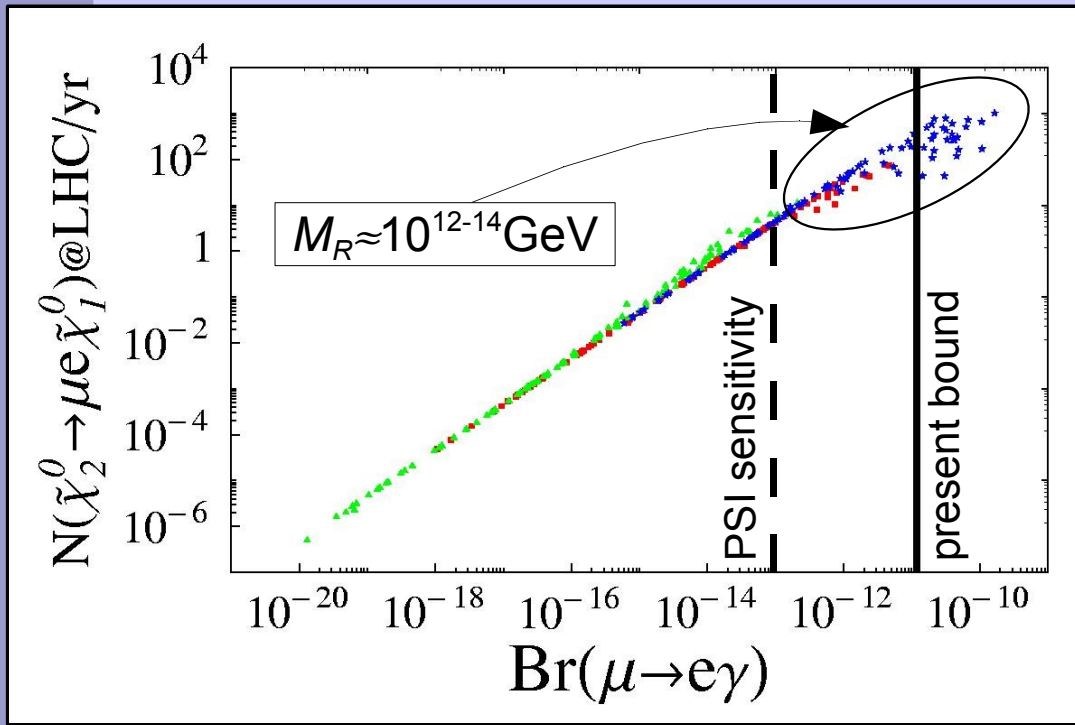
$$N(\tilde{\chi}_2^0 \rightarrow \mu e \tilde{\chi}_1^0) = 200 \Rightarrow 5\sigma @ L = 100 \text{ fb}^{-1}$$

Andreev et al, hep-ph/0608176



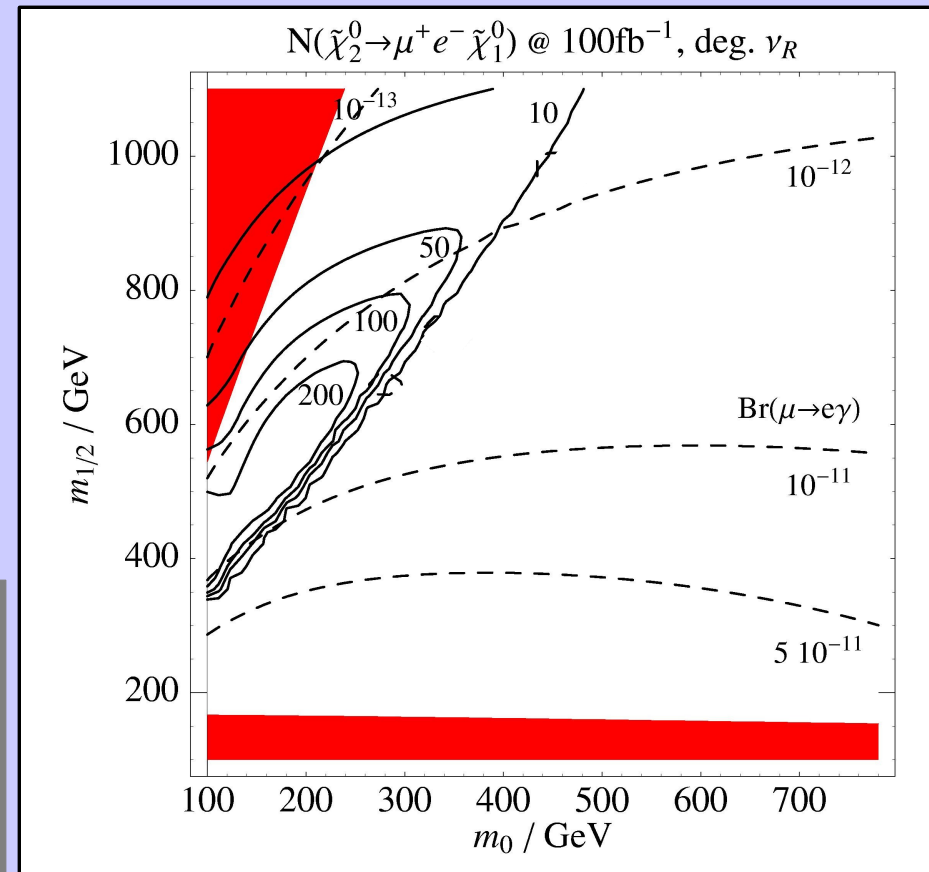
LFV at the LHC

SUSY Seesaw



Correlation with $\text{Br}(\mu \rightarrow e\gamma)$

- Fixed mSUGRA scenario: SPS1a
- Variation of neutrino parameters, **deg L/R**, **hier L/R** and **hier R/deg R** neutrinos



Comparing sensitivity reach

- Fixed neutrino parameters: hierarchical light, degenerate heavy: $M_R = 10^{14} \text{ GeV}$
- Variation of $m_{1/2}$, m_0 ($A_0 = 0$, $\tan\beta = 10$, $\text{sign}\mu = +$)

Precision Slepton Mass Measurements

Collaboration with **A. Freitas, W. Porod, P. Zerwas**
Phys. Rev. D77 (2008) 075009 (arXiv:0712.0361)

Precision Mass Measurements

SO(10) GUT Model

- **SO(10)**
 - Favoured GUT group
 - Incorporates Seesaw

$$\mathbf{16}_F = (u_c, d_c, e, L, Q_c, \nu_R)$$

Precision Mass Measurements

SO(10) GUT Model

- **SO(10)**

- Favoured GUT group
- Incorporates Seesaw

- **Generic SO(10) Model**

- Top unification $Y_\nu = Y_u$ (3rd gen.)
- Two Higgs **10**-plets to avoid large $\tan\beta$
- Dominance of $M^1_{126} \rightarrow$ **Seesaw Type I**
- Realistic mass relations for all fermions are not our goal

$$\mathbf{16}_F = (u_c, d_c, e, L, Q_c, \nu_R)$$

$$W = Y_d^{10} \mathbf{16}_F \cdot \mathbf{16}_F \cdot \mathbf{10}_{H_1} \\ + Y_u^{10} \mathbf{16}_F \cdot \mathbf{16}_F \cdot \mathbf{10}_{H_2} \\ + Y^{126} \mathbf{16}_F \cdot \mathbf{16}_F \cdot \mathbf{126}_H$$

Breaking to SM

$$M^u = M^5_{10_2} + M^5_{126} \\ M^{\nu}_{LR} = M^5_{10_2} - 3 M^5_{126} \\ M^d = M^5_{10_1} + M^{45}_{126} \\ M^e = M^5_{10_1} - 3 M^{45}_{126} \\ M^{\nu}_{LL} = M^{15}_{126} \\ M^{\nu}_{RR} = M^1_{126}$$

Precision Mass Measurements

SO(10) GUT Model

- **SO(10)**

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- Incorporates Seesaw

- **Generic SO(10) Model**

- Top unification $Y_v = Y_u$ (3rd gen.)
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- **SO(10) Symmetry Breaking**

- Direct: **SO(10) \rightarrow SM**
- Two-Step: **SO(10) \rightarrow SU(5) \rightarrow SM**

$$\mathbf{16}_F = (u_c, d_c, e, L, Q_c, \nu_R)$$

$$W = Y_d^{10} \mathbf{16}_F \cdot \mathbf{16}_F \cdot \mathbf{10}_{H_1} + Y_u^{10} \mathbf{16}_F \cdot \mathbf{16}_F \cdot \mathbf{10}_{H_2} + Y^{126} \mathbf{16}_F \cdot \mathbf{16}_F \cdot \mathbf{126}_H$$

Breaking to SM

$$\begin{aligned} M^u &= M^5_{10_2} + M^5_{126} \\ M^{\nu}_{LR} &= M^5_{10_2} - 3 M^5_{126} \\ M^d &= M^5_{10_1} + M^{45}_{126} \\ M^e &= M^5_{10_1} - 3 M^{45}_{126} \\ M^{\nu}_{LL} &= M^{15}_{126} \\ M^{\nu}_{RR} &= M^1_{126} \end{aligned}$$

Precision Mass Measurements

Heavy Neutrino Mass Spectrum

- **Seesaw relation**

$Y_\nu = Y_u$ Yukawa unification (neglect small quark mixing)

$$M_{\nu_R} = Y_\nu \cdot m_\nu^{-1} \cdot Y_\nu^T \nu_u^2 \approx \text{diag}(m_{u_i}) \cdot U_\nu \cdot \text{diag}(m_{\nu_i}^{-1}) \cdot U_\nu^T \cdot \text{diag}(m_{u_i})$$

- **Strongly hierarchical masses**

$$M_{\nu_{R1}} : M_{\nu_{R2}} : M_{\nu_{R3}} \approx m_u^2 : m_c^2 : m_t^2$$

Precision Mass Measurements

Heavy Neutrino Mass Spectrum

- **Seesaw relation**

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- **Strongly hierarchical masses**

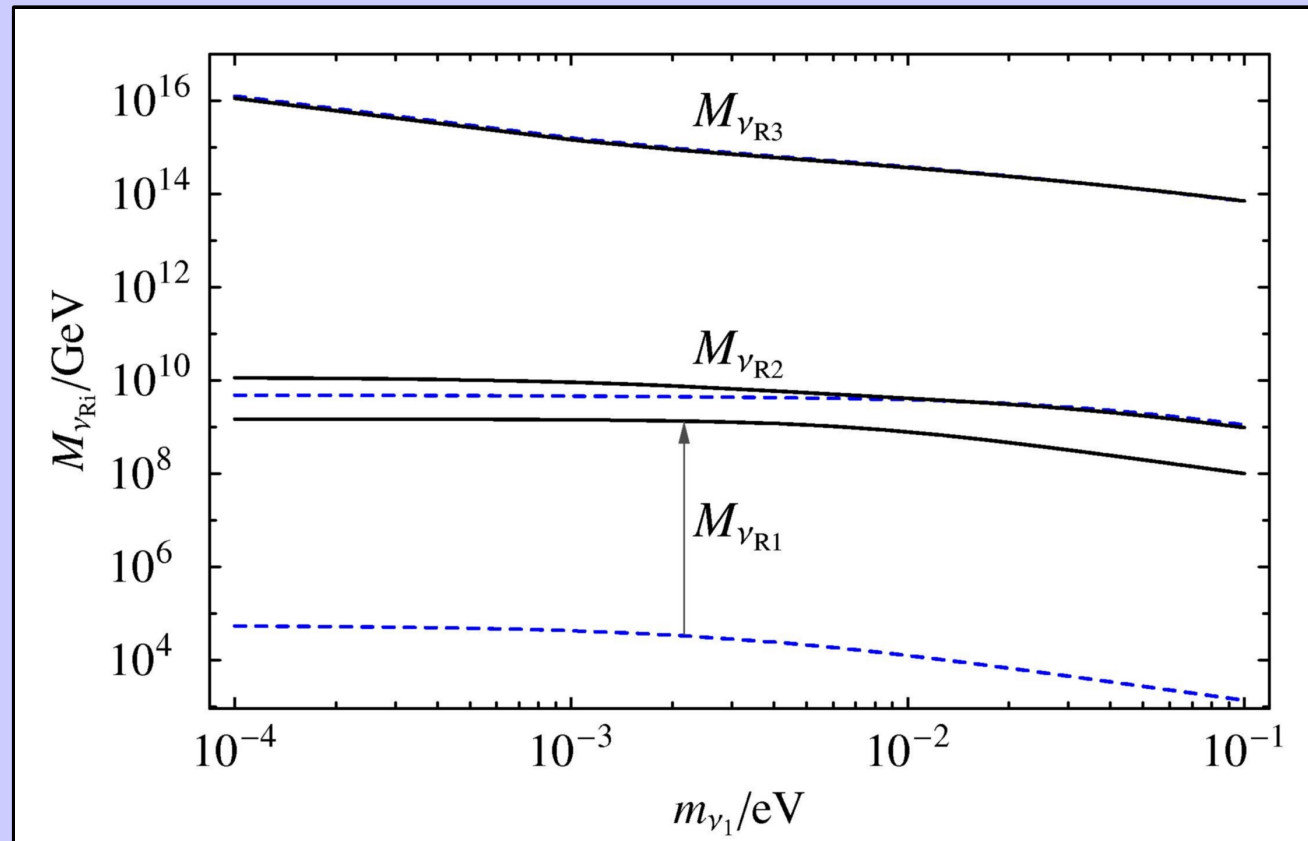
$$M_{\nu_{R1}} : M_{\nu_{R2}} : M_{\nu_{R3}} \approx m_u^2 : m_c^2 : m_t^2$$

- **Small violation of Yukawa unification**

$$Y_v = Y_u + O\left(\frac{m_c}{M_Z}\right)$$

→ Lifting of 1st and 2nd mass

- Realistic fermion mass relations
- Leptogenesis
- Does not affect our analysis



Precision Mass Measurements

Direct Breaking $SO(10) \rightarrow SM$

Boundary Conditions at GUT scale Λ_U

$$m_{16} = m_{10_1} = m_{10_2} \equiv M_0$$

$$M_{1/2}, A_0, \tan \beta, \text{sign } \mu$$

D_U

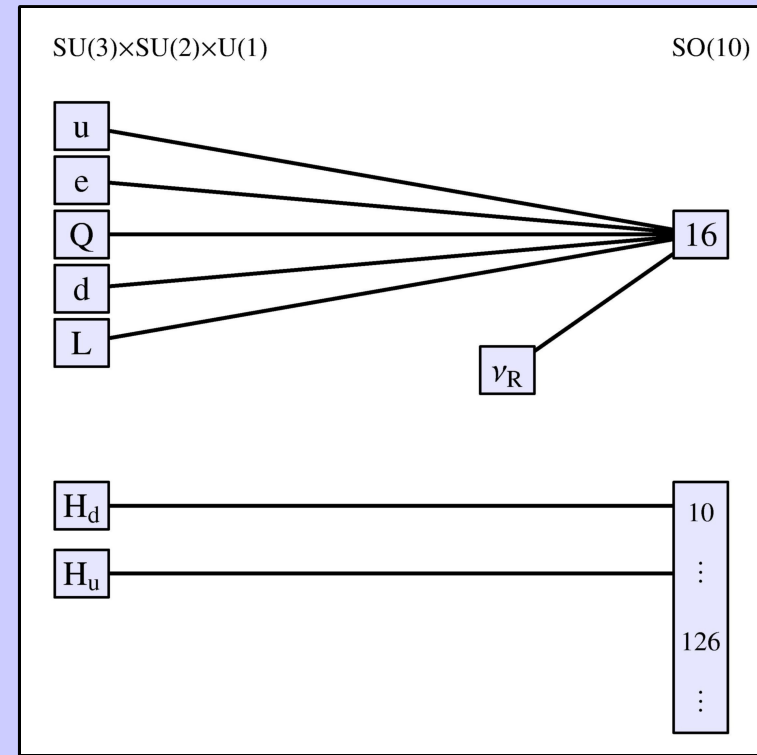
SSB masses at Λ_U

$$m_L^2 = m_{16}^2 - 3D_U$$

$$m_E^2 = m_{16}^2 + D_U$$

D -term associated with breaking rank-5 $SO(10)$ to rank-4 SM

$$D_U \simeq g_U^2 O(m_{16}^2)$$



Precision Mass Measurements

Direct Breaking $SO(10) \rightarrow SM$

Boundary Conditions at GUT scale Λ_U

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D_U

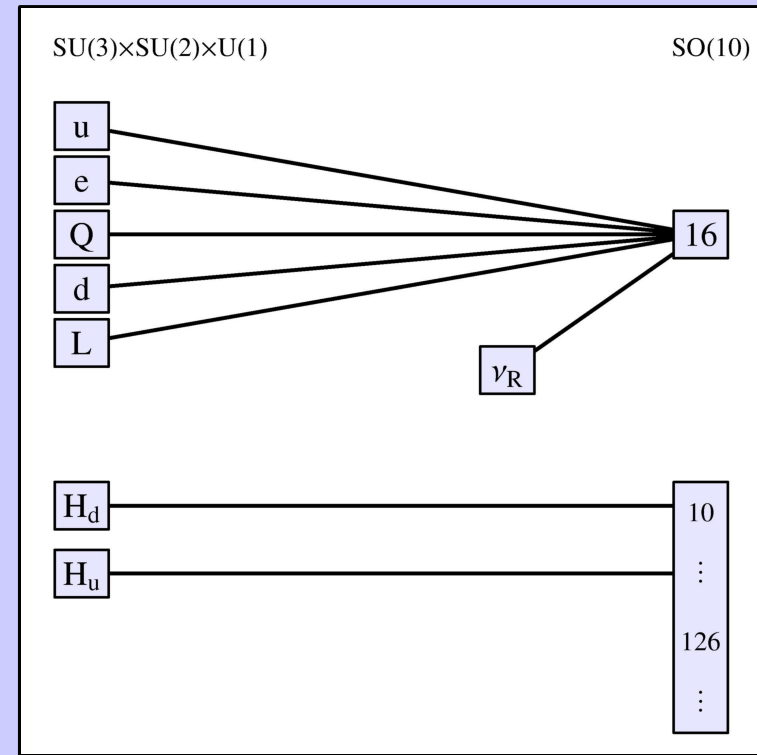
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Solution to MSSM RGEs from Λ_U to M_Z

1st and 2nd generation

$$m_{\tilde{e}_L}^2 = m_{16}^2 + 3D_U + \alpha_L M_{1/2}^2 - (1 - 2s_W^2) D_{EW}$$

$$m_{\tilde{\nu}_{eL}}^2 = m_{16}^2 + 3D_U + \alpha_L M_{1/2}^2 + D_{EW}$$

$$m_{\tilde{e}_R}^2 = m_{16}^2 + D_U + \alpha_R M_{1/2}^2 - 2s_W^2 D_{EW}$$

3rd gen. shifted due to strong Yukawa coupling

$$m_{\tilde{t}_L}^2 = m_{\tilde{e}_L}^2 + m_{\tau}^2 - \Delta_{\tau} - \Delta_{\nu_{\tau}}$$

$$m_{\tilde{\nu}_{\tau L}}^2 = m_{\tilde{\nu}_{eL}}^2 - \Delta_{\tau} - \Delta_{\nu_{\tau}}$$

$$m_{\tilde{t}_R}^2 = m_{\tilde{e}_R}^2 + m_{\tau}^2 - 2\Delta_{\tau}$$

$$\Delta_{\nu_{\tau}} \approx \frac{m_t^2(\Lambda_U)}{4\pi^2 v_u^2} (3m_{16}^2 + A_0^2) \log \frac{\Lambda_U^2}{M_{\nu_{R3}}^2}$$

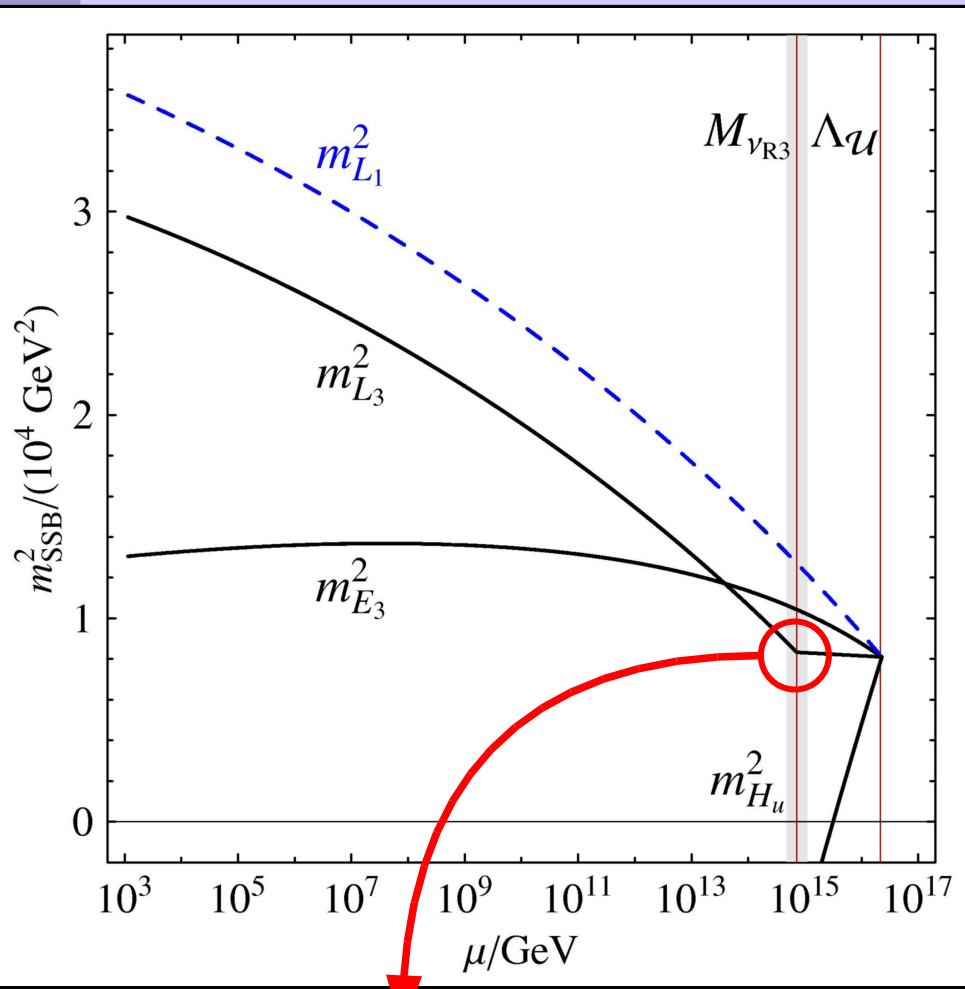
Precision Mass Measurements

Slepton Mass Evolution

SUSY parameter measurements (combined LHC+ILC sensitivity)

Parameter	Value	Error	Parameter	Value	Error
$m_{\tilde{e}_R}$	140.9 GeV	0.05 GeV	μ	481.1 GeV	4.5 GeV
$m_{\tilde{e}_L}$	190.4 GeV	0.4 GeV	$\tan\beta$	10.0	1.0
$m_{\tilde{\nu}_e}$	173.4 GeV	1.3 GeV	$M_{1/2}$	250.0 GeV	0.4 GeV
$m_{\tilde{\tau}_1}$	104.2 GeV	0.3 GeV	A_0	-640.0 GeV	13 GeV
$m_{\tilde{\tau}_2}$	187.8 GeV	1.1 GeV			
$m_{\tilde{\nu}_\tau}$	154.7 GeV	1.6 GeV			

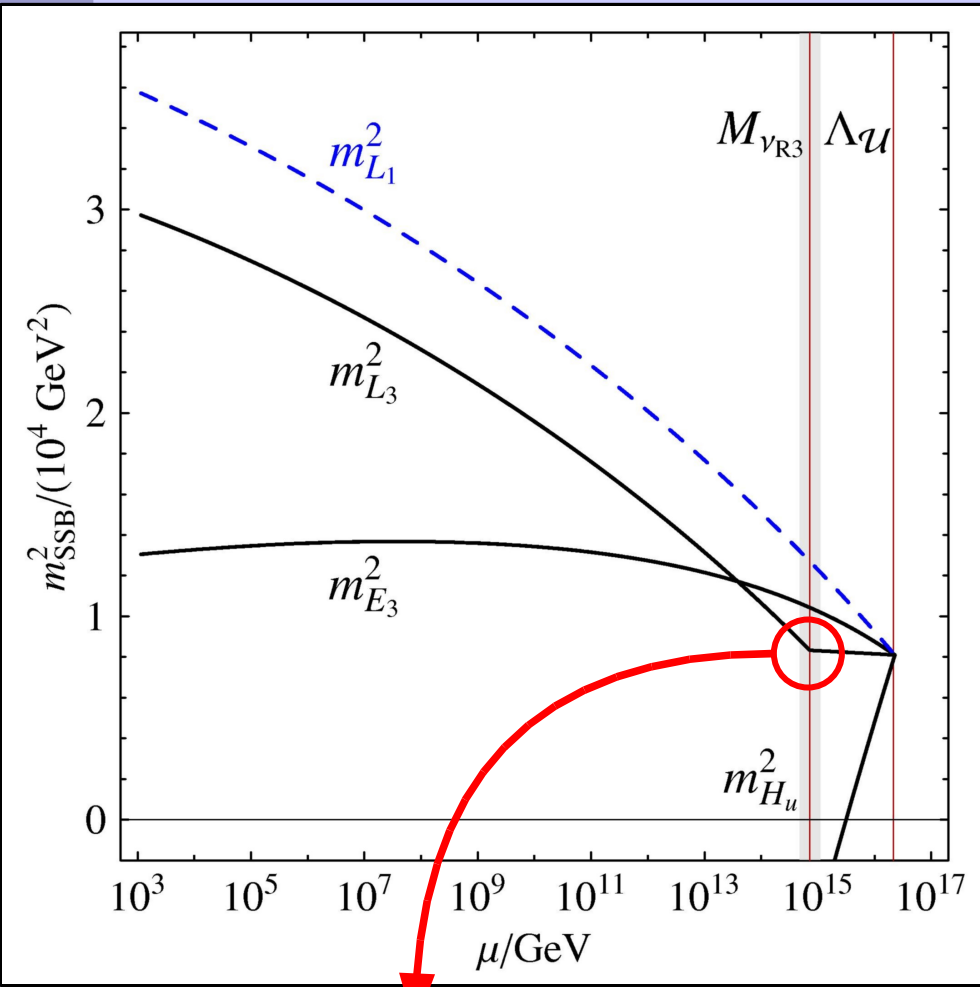
Aguilar-Saavedra et al., Weiglein et al.



Different running of left-stau mass above and below the heavy neutrino mass scale

Precision Mass Measurements

Slepton Mass Evolution



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Global Fit

Model input parameters

Parameters in SO(10) \rightarrow SM	Ideal	Error
unification scale Λ_U	$2.16 \cdot 10^{16}$ GeV	$0.02 \cdot 10^{16}$ GeV
matter scalar mass M_0	90 GeV	0.25 GeV
GUT D-term $\sqrt{-D_U}$	30 GeV	0.9 GeV
heaviest R-neutrino mass $M_{\nu R3}$	$7.2 \cdot 10^{14}$ GeV	$[4.8, 11] \cdot 10^{14}$ GeV
lightest neutrino mass m_{ν_1}	$3.5 \cdot 10^{-3}$ eV	$[1.6, 6.7] \cdot 10^{-3}$ eV

Precision Mass Measurements

Determination of Neutrino Mass Scales

- Theory: RG evolution**

$$\Delta_{\nu_\tau} \approx \frac{m_t^2(\Lambda_U)}{4\pi^2 v_u^2} (3m_{16}^2 + A_0^2) \log \frac{\Lambda_U^2}{M_{\nu_{R3}}^2}$$

- Experiment: Slepton mass measurements (ILC sensitivity)**

$$\Delta_{\nu_\tau} = (4.7 \pm 0.5) \cdot 10^3 \text{ GeV}^2$$

Fit

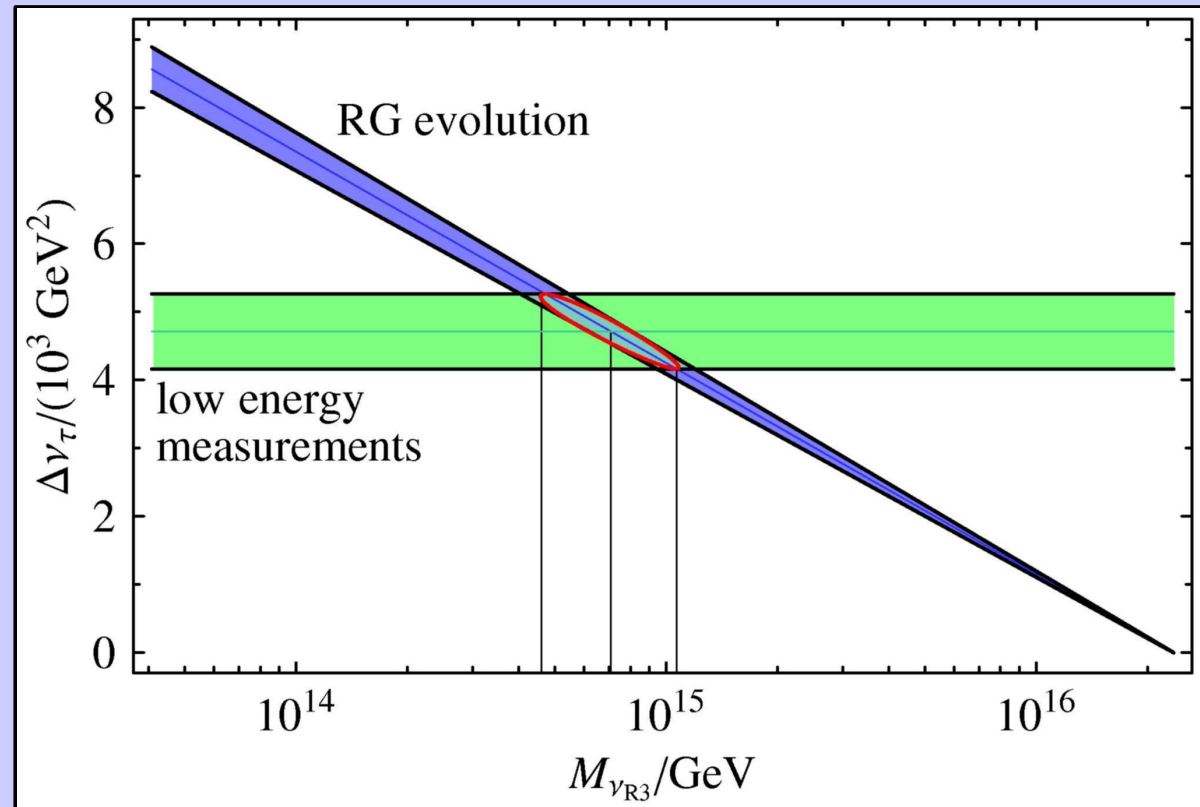
- Heavy neutrino mass**

$$M_{\nu_{R3}} = (7.2^{+4.0}_{-2.5}) \cdot 10^{14} \text{ GeV}$$

Seesaw

- Light neutrino mass**

$$m_{\nu_1} = (3.0^{+3.5}_{-1.5}) \cdot 10^{-3} \text{ eV}$$



Conclusion

- **SUSY Seesaw**
 - Effective Description emerging naturally from $SO(10)$
 - Connecting Neutrino, EW, SUSY and GUT Scale Physics
 - CP Violation Effects, Leptogenesis, EDMs
 - Charged Lepton Flavor Violation
- **Charged LFV Processes**
- **Reconstruction of Model Parameters**
- **Outlook**

Conclusion

- **SUSY Seesaw**
- **Charged LFV Processes**
 - Low Energy Processes such as $Br(\mu \rightarrow e \gamma)$
 - Decays of Second Lightest Neutralino at the LHC
 - Slepton Pair Production at the ILC
 - Correlations among Processes and Neutrino Parameters
- **Reconstruction of Model Parameters**
- **Outlook**

Conclusion

- **SUSY Seesaw**
- **Charged LFV Processes**
- **Reconstruction of Model Parameters**
 - LFV Processes probe Neutrino Yukawa Couplings
 - Synergy between Neutrino and Collider Physics
 - Example: Determination of Heaviest and Lightest Neutrino Mass in SO(10)
- **Outlook**

Conclusion

- **SUSY Seesaw**
- **Charged LFV Processes**
- **Reconstruction of Model Parameters**
- **Outlook**
 - Synergy and Interplay between Neutrino and Collider Physics
 - Systematic Study of Slepton Flavor Structure at LHC “Slepton Oscillations”
 - Application to realistic SO(10) GUT Models