

CP-sensitive observables in MSSM at one loop

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Outline

- 1 Introduction
- 2 CP-even observables
- 3 CP-odd observables
- 4 Summary

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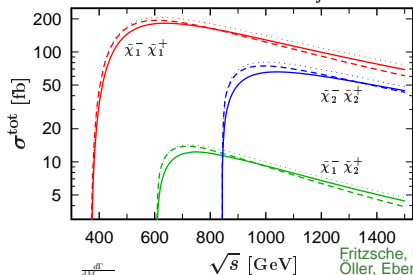
Motivation

- radiative corrections in MSSM could be of order 10%
- so far only CP-conserving case at one loop thoroughly examined
- MSSM with CP violating phases:

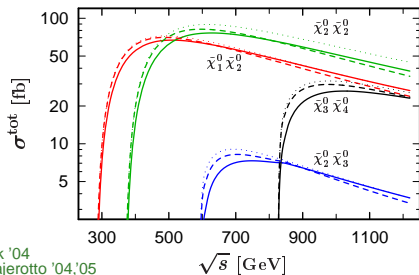
$$M_1 = |M_1|e^{i\Phi_1}, \mu = |\mu|e^{i\Phi_\mu}, A_f = |A_f|e^{i\Phi_f}$$
 - strong bounds on these phases from EDMs exist, however
 - large phases possible if accidental cancelations occur
 - or 1st and 2nd generation of squarks are heavy
 - Φ_1 poorly constrained
- calculation of radiative corrections to CP violating observables, e.g. asymmetries in sparticles production, asymmetries of triple products of momenta and/or spins, asymmetries in decay widths
 - such observables provide unambiguous way of detecting CP violating phases
- here we analyze gaugino/higgsino sector of complex MSSM at one-loop level

Motivation

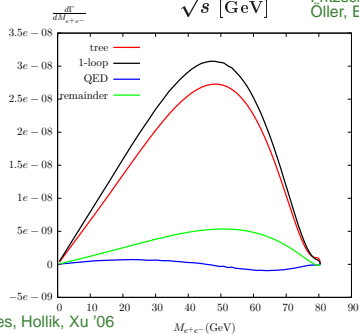
$$e^-e^+ \rightarrow \tilde{\chi}_i^- \tilde{\chi}_j^+$$



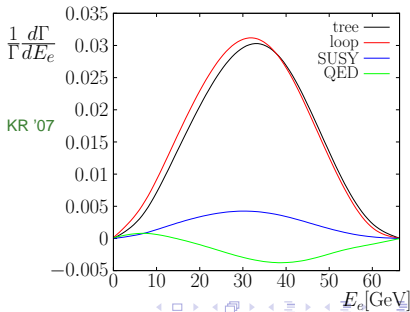
$$e^-e^+ \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0$$



Fritzsche, Hollik '04
 Oller, Eberl, Majerotto '04,'05



Drees, Hollik, Xu '06



KR '07

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 - such observables provide unambiguous way of detecting CP violating phases
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Minimal Supersymmetric Standard Model

particles		spin 0	spin 1/2	$SU(3)_c, SU(2)_L, U(1)_Y$
squarks and quarks (3 flavors)	Q	$\begin{pmatrix} \tilde{u}_L \\ \tilde{d}_L \end{pmatrix}$	$\begin{pmatrix} u \\ d \end{pmatrix}_L$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
	U	\tilde{u}_R^*	u_R^\dagger	$(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$
	D	\tilde{d}_R^*	d_R^\dagger	$(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3})$
sleptons and leptons (3 flavors)	L	$\begin{pmatrix} \tilde{\nu} \\ \tilde{e}_L \end{pmatrix}$	$\begin{pmatrix} \nu \\ e \end{pmatrix}_L$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$
	E	\tilde{e}_R^*	e_R^\dagger	$(\mathbf{1}, \mathbf{1}, 1)$
Higgs bosons and higgsinos	H_u	$\begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}$	$\begin{pmatrix} \tilde{H}_u^+ \\ \tilde{H}_u^0 \end{pmatrix}$	$(\mathbf{1}, \mathbf{2}, \frac{1}{2})$
	H_d	$\begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}$	$\begin{pmatrix} \tilde{H}_d^0 \\ \tilde{H}_d^- \end{pmatrix}$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$

particles	spin $\frac{1}{2}$	spin 1	$SU(3)_c, SU(2)_L, U(1)_Y$
gluino, gluon	\tilde{g}	g	$(\mathbf{8}, \mathbf{1}, 0)$
winos, W bosons	$\tilde{W}^\pm \tilde{W}^0$	$W^\pm W^0$	$(\mathbf{1}, \mathbf{3}, 0)$
bino, B boson	\tilde{B}^0	B^0	$(\mathbf{1}, \mathbf{1}, 0)$

Chargino sector of the MSSM

- chargino mass matrix in gauge eigenstate basis (\tilde{W}^- , \tilde{H}^-)

$$M_{\tilde{\chi}^\pm} = \begin{pmatrix} M_2 & \sqrt{2}m_W \cos \beta \\ \sqrt{2}m_W \sin \beta & \mu \end{pmatrix}$$

- diagonalization using unitary matrices U and V

$$V^* M_{\tilde{\chi}^\pm} U^\dagger = \begin{pmatrix} m_{\tilde{\chi}_1^\pm} & 0 \\ 0 & m_{\tilde{\chi}_2^\pm} \end{pmatrix}$$

- mass eigenstates in Weyl representation

$$U \begin{pmatrix} \tilde{W}_L^- \\ \tilde{H}_d^- \end{pmatrix} = \begin{pmatrix} \chi_{1L}^- \\ \chi_{2L}^- \end{pmatrix} \quad V \begin{pmatrix} \tilde{W}_R^+ \\ \tilde{H}_u^+ \end{pmatrix} = \begin{pmatrix} \chi_{1R}^+ \\ \chi_{2R}^+ \end{pmatrix}$$

- Dirac spinors

$$\tilde{\chi}_1^- = \begin{pmatrix} \chi_{1L}^- \\ \chi_{1R}^- \end{pmatrix}, \quad \tilde{\chi}_2^- = \begin{pmatrix} \chi_{2L}^- \\ \chi_{2R}^- \end{pmatrix}$$

Neutralino sector of MSSM

- neutralino mass matrix in gauge eigenstate basis $(\tilde{B}, \tilde{W}^0, \tilde{H}_d^0, \tilde{H}_u^0)$

$$M_{\tilde{\chi}^0} = \begin{pmatrix} M_1 & 0 & -m_Z c_\beta s_W & m_Z s_\beta s_W \\ 0 & M_2 & m_Z c_\beta c_W & -m_Z s_\beta c_W \\ -m_Z c_\beta s_W & m_Z c_\beta c_W & 0 & -\mu \\ m_Z s_\beta s_W & -m_Z s_\beta c_W & -\mu & 0 \end{pmatrix}$$

- diagonalization of mass matrix

$$\text{diag}(m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_4^0}) = N^* M_{\tilde{\chi}^0} N^{-1}$$

- we obtain 4 mass eigenstates – Majorana fermions
- in the CP-conserving case:
 - \Rightarrow elements of matrix N are either purely real or purely imaginary
 - \Rightarrow neutralinos have intrinsic CP parity $\eta = \pm i$

Renormalization scheme

We work in the on-shell scheme:

- regularization by dimensional reduction
- physical masses are input parameters
- renormalization conditions defined at the pole masses
- renormalization is performed after rotation of fields to mass eigenstate basis
- introduce renormalization constants for fields and mixing matrices
- attention needed: the number of observable masses exceeds the number of free parameters
 - ⇒ e.g. in chargino/neutralino sector in the CP conserving case we have 4 parameters (M_1 , M_2 , μ , $\tan\beta$) and 6 masses
- counter terms added to *FeynArts* model file

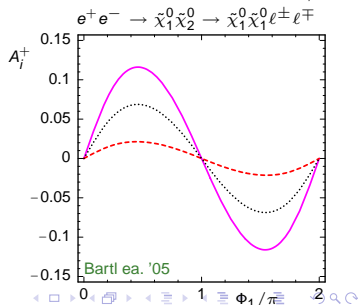
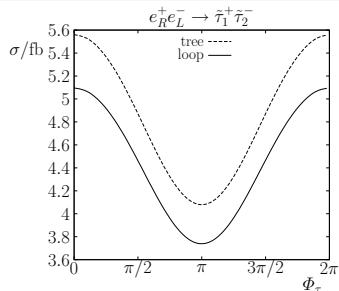
CP-sensitive observables

CP-even:

- U-shape dependence on complex phase
- cross-sections, decay rates or branching ratios
- threshold behavior of cross section or decay distribution

CP-odd:

- sinusoidal dependence on the phase
- asymmetries in production cross sections in CP-conjugated modes
- asymmetries in decay rates of particle and antiparticle
- triple products of momenta and/or spins
- angular distributions in production+decay



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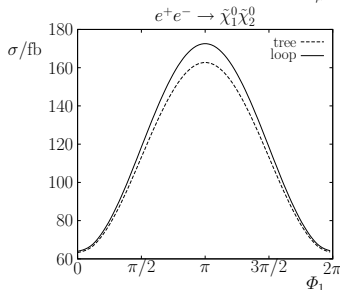
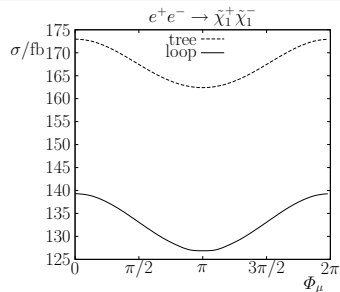
Cross sections dependence

chargino production:

- a few % sensitivity to the phase of μ parameter
- large radiative corrections

neutralino production:

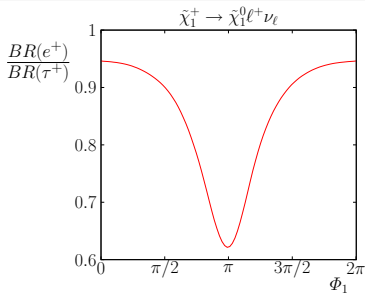
- strong dependence on the phase of M_1 parameter
- relative size of corrections strongly depends on Φ_1



Decay widths

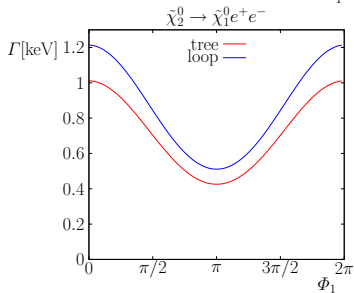
chargino decays:

- branching ratios for $\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 e^+ \nu_e$ and $\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 \tau^+ \nu_\tau$
- sensitive to the phase of M_1 and μ parameters



neutralino decays:

- decay width for $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 e^+ e^-$
- strong dependence on the phase of M_1 parameter

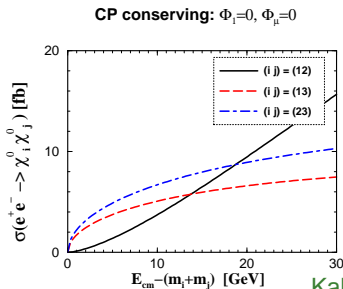


Threshold behavior in neutralino production

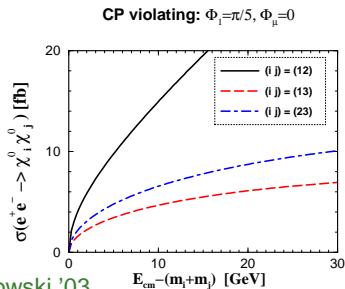
- orbital momentum L selection rule at the threshold for pair production of neutralinos $\{ij\}$ with CP parities η_i and η_j

$$1 = \eta_i \eta_j (-1)^L$$

- in the CP-conserving theory same (opposite) parities give P (S) wave excitation
- in the CP-violating theory there is always S-wave excitation



Kalinowski '03

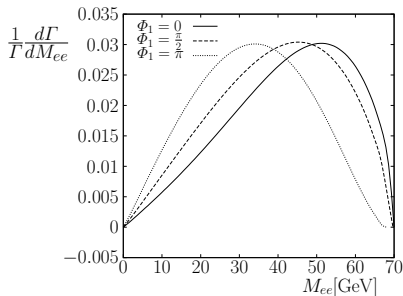


Threshold behavior in neutralino three-body decay

- consider 3-body neutralino decay $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \ell^+ \ell^-$
- orbital momentum L selection rule at the threshold for neutralino $\tilde{\chi}_1^0$ and lepton pair with neutralino CP parities η_2 and η_1

$$1 = -\eta_2 \eta_1 (-1)^L$$

- in the CP-conserving theory same (opposite) parities give S (P) wave excitation; in the CP-violating theory we have S-wave excitation



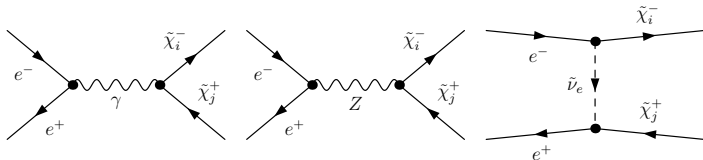
- note: if both decay and production of $\tilde{\chi}_2^0 \tilde{\chi}_1^0$ exhibit S-wave excitation \Rightarrow CPV phases are present

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Chargino production

- chargino production at the tree-level in e^+e^- collisions



- for non-diagonal pair $\tilde{\chi}_1^\pm \tilde{\chi}_2^\mp$ no contribution from photon exchange
- production amplitude after Fierz transformation

$$\mathcal{A}[e^+e^- \rightarrow \tilde{\chi}_i^- \tilde{\chi}_j^+] = \frac{e^2}{s} Q_{\alpha\beta}^{ij} \left(\bar{v}(e^+) \gamma_\mu P_\alpha u(e^-) \right) \left(\bar{u}(\tilde{\chi}_i^-) \gamma^\mu P_\beta v(\tilde{\chi}_j^+) \right)$$

- four bilinear couplings Q_{LL} , Q_{RL} , Q_{LR} , Q_{RR} depend on mixing angles of matrices U , V

Amplitude structure

- unpolarized differential cross-section

$$\frac{d\sigma^{\{ij\}}}{d\cos\theta d\phi} = \frac{\alpha^2}{4s} \lambda^{1/2} \left((1 - (\mu_i^2 - \mu_j^2)^2 + \lambda \cos^2 \theta) Q_1 + 4\mu_i\mu_j Q_2 + 2\lambda^{1/2} Q_3 \cos \theta \right)$$

P	CP	Quartic charges
even	even	$Q_1 = \frac{1}{4} (Q_{RR} ^2 + Q_{LL} ^2 + Q_{RL} ^2 + Q_{LR} ^2)$ $Q_2 = \frac{1}{2} \text{Re} (Q_{RR} Q_{RL}^* + Q_{LL} Q_{LR}^*)$ $Q_3 = \frac{1}{4} (Q_{RR} ^2 + Q_{LL} ^2 - Q_{RL} ^2 - Q_{LR} ^2)$
	odd	$Q_4 = \frac{1}{2} \text{Im} (Q_{RR} Q_{RL}^* + Q_{LL} Q_{LR}^*)$

- Q_4 can be probed by observables sensitive to chargino polarization component normal to the production plane

CP transformation in chargino production

- S matrix element for chargino production

$$\langle \tilde{\chi}_i^+(\mathbf{k}_1), \tilde{\chi}_j^-(\mathbf{k}_2) | S | e^+(\mathbf{p}_1), e^-(\mathbf{p}_2) \rangle$$

- P transformation: $\mathbf{p}_{1,2} \leftrightarrow -\mathbf{p}_{1,2}$, $\mathbf{k}_{1,2} \leftrightarrow -\mathbf{k}_{1,2}$

$$\langle \tilde{\chi}_i^+(-\mathbf{k}_1), \tilde{\chi}_j^-(-\mathbf{k}_2) | S | e^+(-\mathbf{p}_1), e^-(-\mathbf{p}_2) \rangle$$

- C transformation

$$\langle \tilde{\chi}_i^-(\mathbf{k}_1), \tilde{\chi}_j^+(\mathbf{k}_2) | S | e^-(\mathbf{p}_1), e^+(\mathbf{p}_2) \rangle$$

- CP transformation

$$\langle \tilde{\chi}_j^+(-\mathbf{k}_2), \tilde{\chi}_i^-(-\mathbf{k}_1) | S | e^+(-\mathbf{p}_2), e^-(-\mathbf{p}_1) \rangle$$

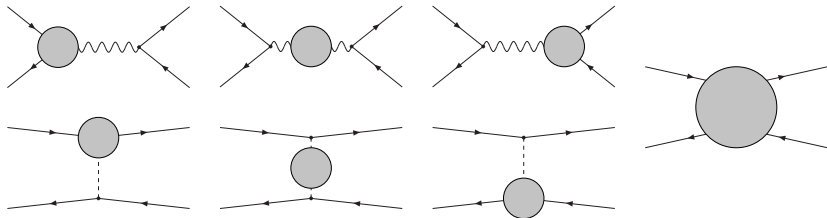
- in center of mass frame: $\mathbf{p}_1 = -\mathbf{p}_2$ and $\mathbf{k}_1 = -\mathbf{k}_2$

$$\langle \tilde{\chi}_j^+(\mathbf{k}_1), \tilde{\chi}_i^-(\mathbf{k}_2) | S | e^+(\mathbf{p}_1), e^-(\mathbf{p}_2) \rangle$$

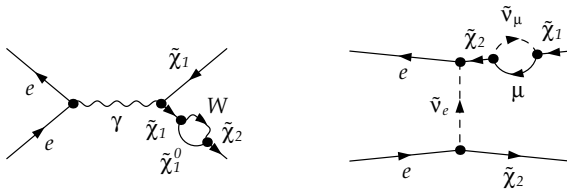
- no CP violation in diagonal chargino final states $\tilde{\chi}_1^- \tilde{\chi}_1^+$, $\tilde{\chi}_2^- \tilde{\chi}_2^+$
- at tree level for non-diagonal chargino pair production

$$\sigma(\tilde{\chi}_1^- \tilde{\chi}_2^+) - \sigma(\tilde{\chi}_1^+ \tilde{\chi}_2^-) = 0$$

Structure of corrections



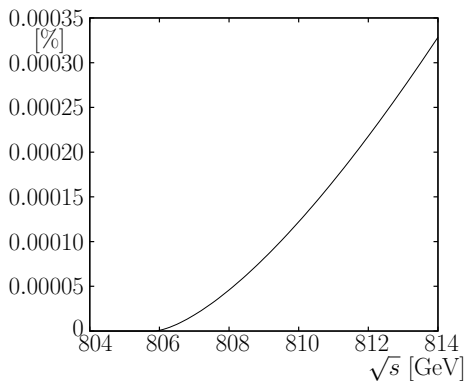
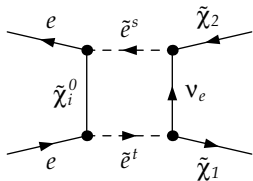
- three types of one-loop contributions: vertex diagrams, self-energy diagrams and box diagrams \Rightarrow use *FeynArts/FormCalc/LoopTools*
- inclusion of corrections on external charged lines necessary



Source of CP asymmetries

- CP violating effects appear due to interference between complex couplings and absorptive parts of loop integrals

- example: box diagram with selectron exchange
- asymmetry appears above selectron production threshold



CP asymmetry in $e^+ e^- \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_2^\mp$

- matrix element squared at one loop

$$|\mathcal{M}_{\text{loop}}|^2 = |\mathcal{M}_{\text{tree}}|^2 + 2 \operatorname{Re}(\mathcal{M}_{\text{tree}}^* \mathcal{M}_{\text{loop}})$$

- asymmetry in production cross section of non-diagonal chargino pairs induced by radiative corrections

$$A_{12} = \frac{\sigma^{\text{loop}}(e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_2^-) - \sigma^{\text{loop}}(e^+ e^- \rightarrow \tilde{\chi}_2^+ \tilde{\chi}_1^-)}{\sigma^{\text{tree}}(e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_2^-) + \sigma^{\text{tree}}(e^+ e^- \rightarrow \tilde{\chi}_2^+ \tilde{\chi}_1^-)}$$

- asymmetry vanishes at the tree level \Rightarrow it is finite at one loop
- soft and hard QED corrections cancel in the numerator
- A_{12} can be sensitive to the phases of μ , A_t , M_1 , A_b , A_τ

Chosen parameters

- gaugino mass parameters

$$|M_1| = 100 \text{ GeV}, M_2 = 200 \text{ GeV}, |\mu| = 400 \text{ GeV}, \tan \beta = 10$$

- sfermion parameters

$$m_{\tilde{q}} \equiv M_{\tilde{Q}_{1,2}} = M_{\tilde{U}_{1,2}} = M_{\tilde{D}_{1,2}} = 450 \text{ GeV}$$

$$M_{\tilde{Q}} \equiv M_{\tilde{Q}_3} = M_{\tilde{U}_3} = M_{\tilde{D}_3} = 300 \text{ GeV}$$

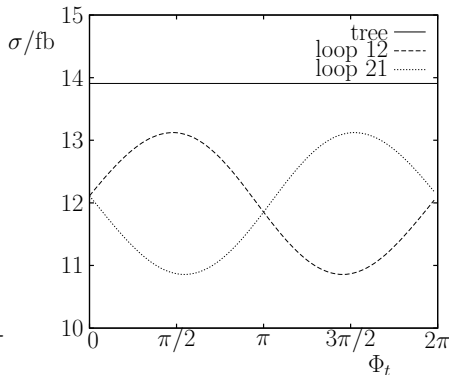
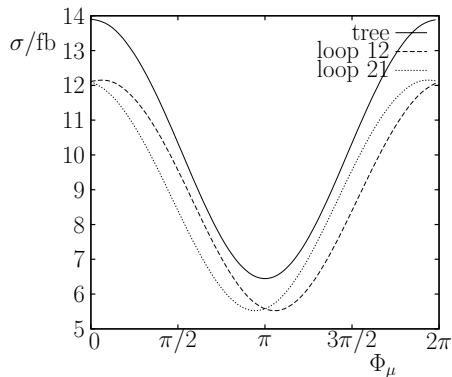
$$m_{\tilde{l}} \equiv M_{\tilde{L}_{1,2,3}} = M_{\tilde{E}_{1,2,3}} = 150 \text{ GeV}$$

$$A \equiv |A_t| = |A_b| = |A_\tau| = 400 \text{ GeV}$$

- resulting masses:

$m_{\tilde{\chi}_1^\pm}$	$m_{\tilde{\chi}_2^\pm}$	$m_{\tilde{\chi}_1^0}$	$m_{\tilde{\chi}_2^0}$	$m_{\tilde{\chi}_3^0}$	$m_{\tilde{\chi}_4^0}$	$m_{\tilde{t}_1}$	$m_{\tilde{t}_2}$
186.7	421.8	97.5	187.0	405.8	421.2	204.9	438.6

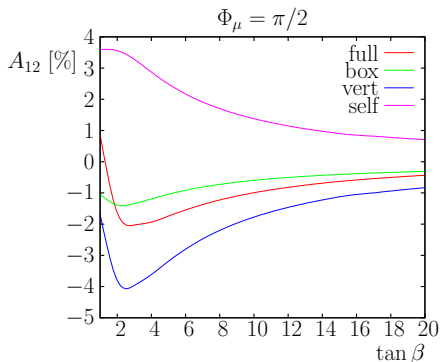
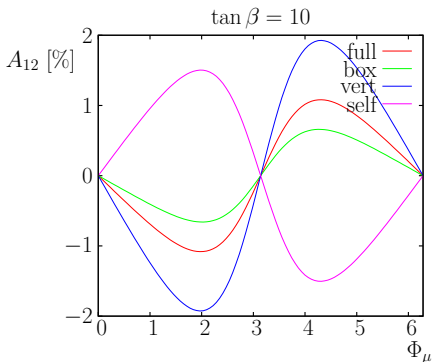
Cross section at one loop



- significant difference between corrections in two production channels \Rightarrow asymmetry can be observed

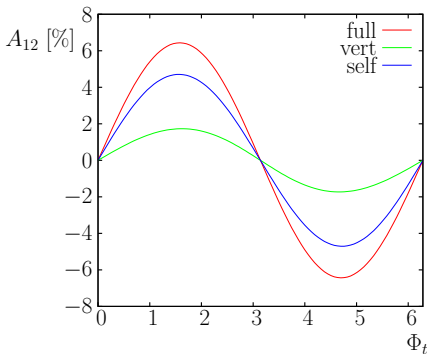
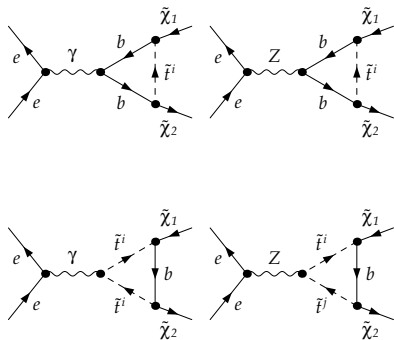
Asymmetry for $\Phi_\mu \neq 0$

- dependence of asymmetry on the phase of μ parameter
- large cancelations between different contributions
- for low and high $\tan\beta$, asymmetry small due to small value of imaginary parts of couplings



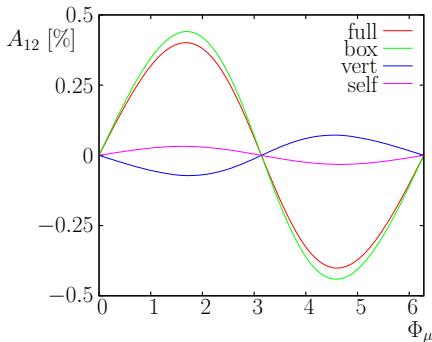
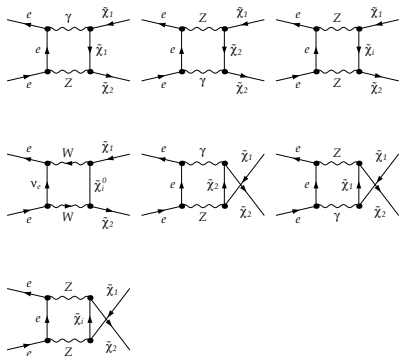
Asymmetry for $A_t \neq 0$

- only contributions from diagrams with stop exchange enter
- asymmetry can reach 6%
- gives access to CP violation in stop sector



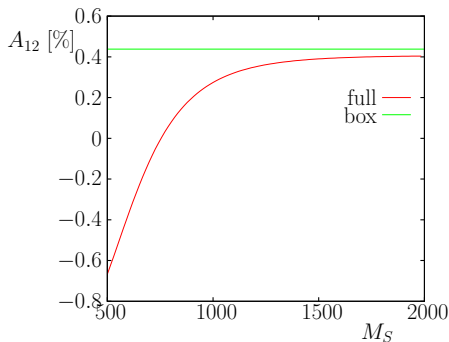
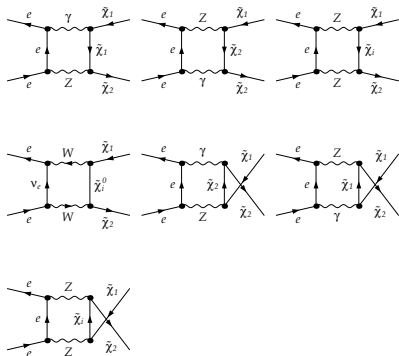
Case of heavy sfermions

- take heavy sfermions with masses 10 TeV - sfermion contributions can be neglected
- only gauge boson exchange contributes to asymmetry
- dominant contribution from box diagrams

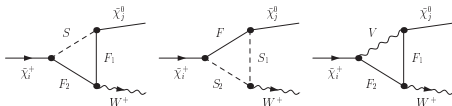


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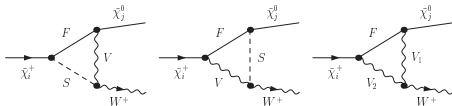
Loop corrections to $\tilde{\chi}_i^\pm \rightarrow W^\pm \tilde{\chi}_1^0$



SF_1F_2 :
 $\tilde{f}\tilde{f}', \phi^0\tilde{\chi}^+\tilde{\chi}^+, \phi^+\tilde{\chi}^+\tilde{\chi}^0$

FS_1S_2 :
 $\tilde{f}\tilde{f}', \tilde{\chi}^0\phi^0\phi^+, \tilde{\chi}^+\phi^+\phi^0$

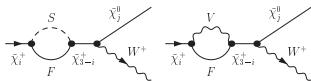
VF_1F_2 :
 $Z^0\tilde{\chi}^0\tilde{\chi}^+, W^+\tilde{\chi}^+\tilde{\chi}^0$



FVS :
 $\tilde{\chi}^0 Z^0 G^+, \tilde{\chi}^+ W^+ H_u^0$

FSV :
 $\tilde{\chi}^0 H_u^0 W^+, \tilde{\chi}^+ G^+ Z^0$

FV_1V_2 :
 $\tilde{\chi}^0 Z^0 W^+, \tilde{\chi}^+ W^+ Z^0$



SF :
 $\tilde{f}\tilde{f}', \tilde{\chi}^+\phi^0, \tilde{\chi}^0\phi^+$

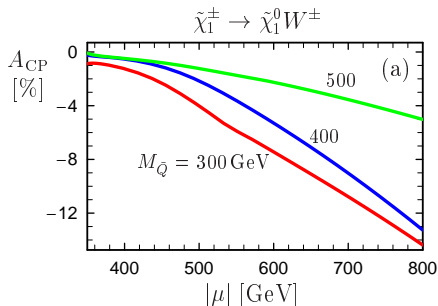
VF :
 $Z^0\tilde{\chi}^+, W^+\tilde{\chi}^0$

[Eberl, Gajdosik, Majerotto, Schrausser; Yang, Du]

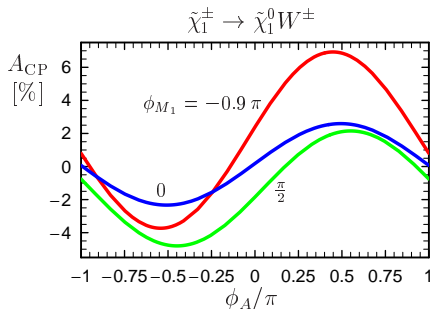
- branching ratios $\sim 5\%$
- possible detection at LHC - charginos from decay chains of \tilde{g} and \tilde{q}
- asymmetry

$$A_{CP} = \frac{\Gamma(\tilde{\chi}_i^+ \rightarrow W^+ \tilde{\chi}_1^0) - \Gamma(\tilde{\chi}_i^- \rightarrow W^- \tilde{\chi}_1^0)}{\Gamma(\tilde{\chi}_i^+ \rightarrow W^+ \tilde{\chi}_1^0) + \Gamma(\tilde{\chi}_i^- \rightarrow W^- \tilde{\chi}_1^0)}$$

CP asymmetries in $\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$



$M_2 = 500 \text{ GeV}, |A| = 400 \text{ GeV},$
 $\Phi_t = -\pi/4, \Phi_1 = 3\pi/4$



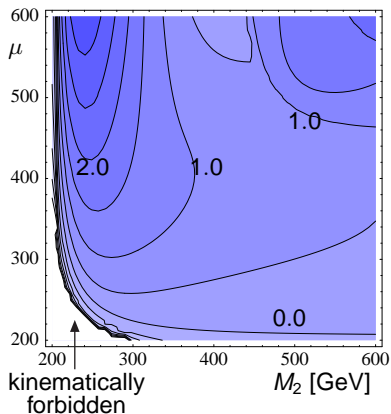
$M_2 = 500 \text{ GeV}, |A| = 400 \text{ GeV},$
 $\mu = 600 \text{ GeV}, M_{\tilde{Q}} = 400 \text{ GeV}$

- asymmetry sensitive to the phases of stop trilinear coupling A_t and bino mass M_1
- can be of the order of $\sim 10\%$

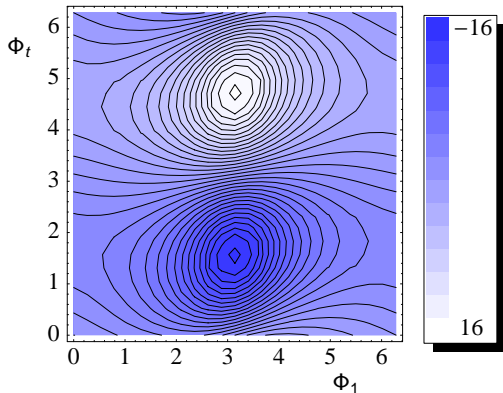
[Eberl, Gajdosik, Majerotto, Schrausser]

$$A_{CP}(\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0)$$

$$M_1 = 100 \text{ GeV}, \Phi_1 = \pi/2$$

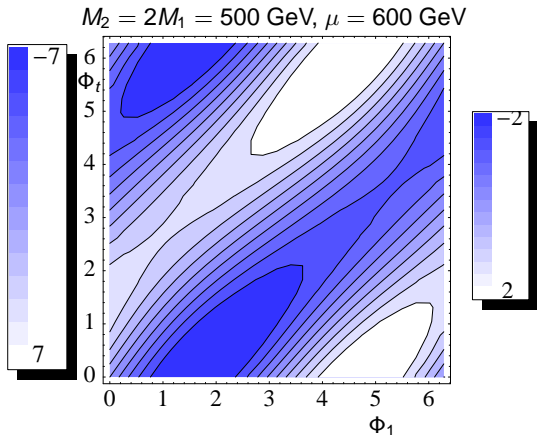
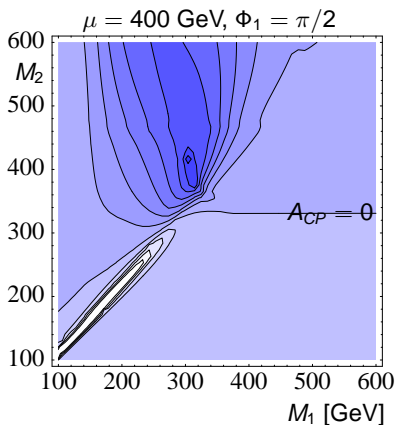


$$M_2 = 2M_1 = 500 \text{ GeV}, \mu = 600 \text{ GeV}$$



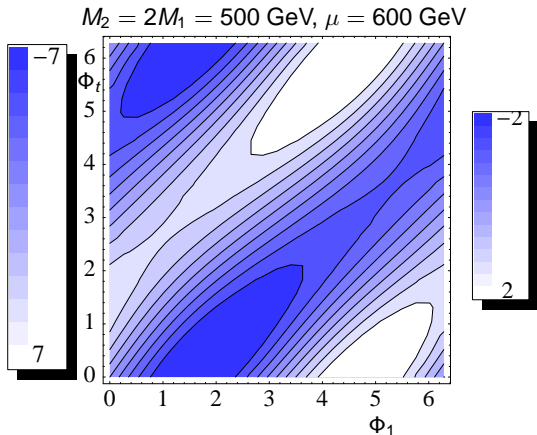
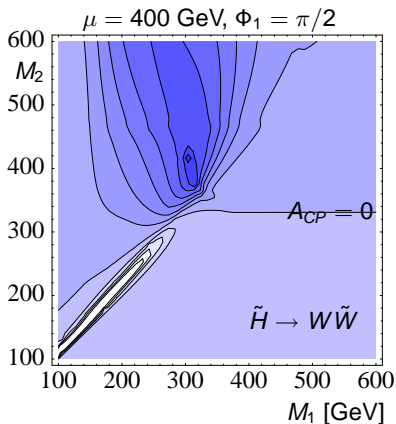
- stop parameters: $|A| = 400 \text{ GeV}$, $m_{\tilde{Q}} = 300 \text{ GeV}$
- maximal asymmetry $\sim 16\%$ for $\Phi_1 = \pi$

$$A_{CP}(\tilde{\chi}_2^\pm \rightarrow W^\pm \tilde{\chi}_1^0)$$



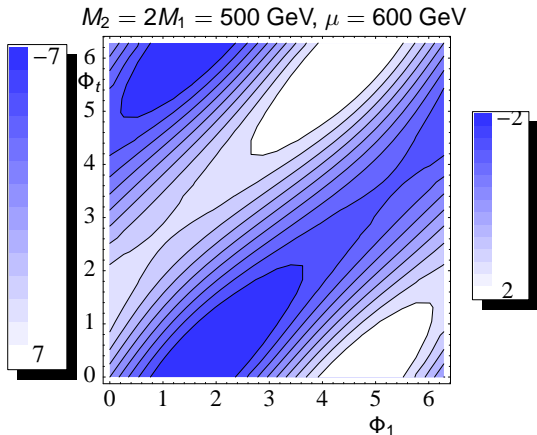
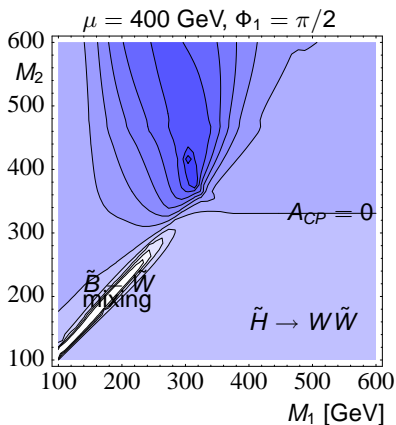
- stop parameters: $|A| = 400 \text{ GeV}, m_{\tilde{Q}} = 300 \text{ GeV}$
- Φ_1 and Φ_t effects correlated

$$A_{CP}(\tilde{\chi}_2^\pm \rightarrow W^\pm \tilde{\chi}_1^0)$$



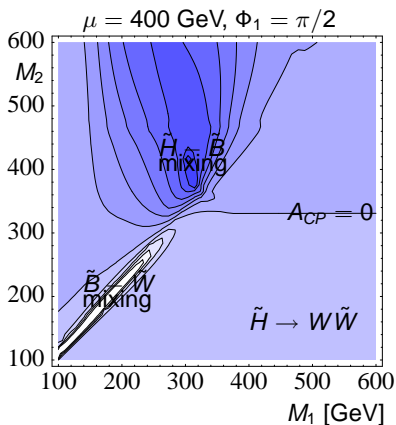
- stop parameters: $|A| = 400 \text{ GeV}, m_{\tilde{Q}} = 300 \text{ GeV}$
- Φ_1 and Φ_t effects correlated

$$A_{CP}(\tilde{\chi}_2^\pm \rightarrow W^\pm \tilde{\chi}_1^0)$$

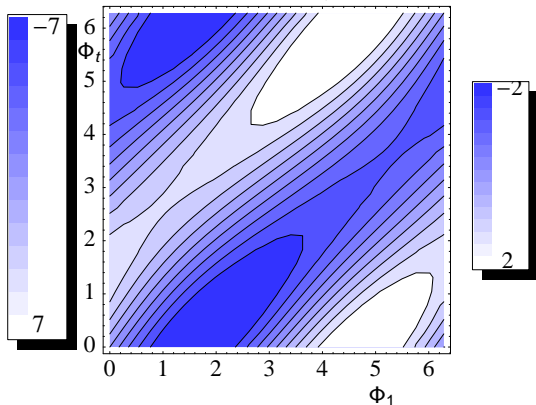


- stop parameters: $|A| = 400 \text{ GeV}, m_{\tilde{Q}} = 300 \text{ GeV}$
- Φ_1 and Φ_t effects correlated

$$A_{CP}(\tilde{\chi}_2^\pm \rightarrow W^\pm \tilde{\chi}_1^0)$$



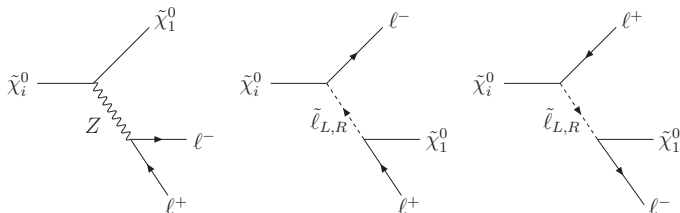
$$M_2 = 2M_1 = 500 \text{ GeV}, \mu = 600 \text{ GeV}$$



- stop parameters: $|A| = 400 \text{ GeV}, m_{\tilde{Q}} = 300 \text{ GeV}$
- Φ_1 and Φ_t effects correlated

Three-body neutralino decay

- 3-body decay of polarized $\tilde{\chi}_2^0(\hat{n}) \rightarrow \tilde{\chi}_1^0(\mathbf{p}) + \ell^+(\mathbf{q}_+) + \ell^-(\mathbf{q}_-)$



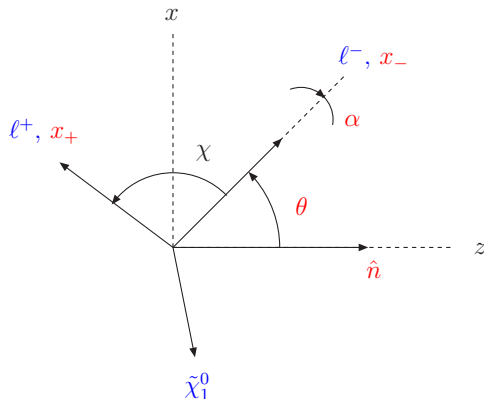
- differential decay rate at tree level

Choi, Chung, Kalinowski, Kim, KR '05

$$\frac{d^4\Gamma}{dx_- dx_+ d\cos\theta d\varphi} = \frac{\alpha^2 m_2}{16\pi^2} \left[F_0(x_-, x_+) + (\hat{q}_- \cdot \hat{n}) F_1(x_-, x_+) \right. \\ \left. + (\hat{q}_+ \cdot \hat{n}) F_2(x_-, x_+) + \hat{n} \cdot (\hat{q}_- \times \hat{q}_+) F_3(x_-, x_+) \right]$$

- with kinematic functions $F_i(x_-, x_+)$ and $x_{\pm} = 2E_{\ell^{\pm}}/m_2$
- Majorana nature of neutralinos leads to $F_3(x_-, x_+) \xrightarrow{CP} -F_3(x_+, x_-)$

Kinematical configuration



CP transformation:

$$\begin{aligned}
 \mathbf{x}_{\pm} &\xrightarrow{CP} +\mathbf{x}_{\mp}, & \vec{\mathbf{q}}_{\pm} &\xrightarrow{CP} -\vec{\mathbf{q}}_{\mp}, \\
 \hat{\mathbf{q}}_{\pm} \cdot \hat{\mathbf{n}} &\xrightarrow{CP} -\hat{\mathbf{q}}_{\mp} \cdot \hat{\mathbf{n}}, \\
 \hat{\mathbf{n}} \cdot (\hat{\mathbf{q}}_{-} \times \hat{\mathbf{q}}_{+}) &\xrightarrow{CP} -\hat{\mathbf{n}} \cdot (\hat{\mathbf{q}}_{-} \times \hat{\mathbf{q}}_{+})
 \end{aligned}$$

CPT transformation:

$$\begin{aligned}
 \mathbf{x}_{\pm} &\xrightarrow{CPT} +\mathbf{x}_{\mp}, & \vec{\mathbf{q}}_{\pm} &\xrightarrow{CPT} +\vec{\mathbf{q}}_{\mp}, \\
 \hat{\mathbf{q}}_{\pm} \cdot \hat{\mathbf{n}} &\xrightarrow{CPT} -\hat{\mathbf{q}}_{\mp} \cdot \hat{\mathbf{n}}, \\
 \hat{\mathbf{n}} \cdot (\hat{\mathbf{q}}_{-} \times \hat{\mathbf{q}}_{+}) &\xrightarrow{CPT} +\hat{\mathbf{n}} \cdot (\hat{\mathbf{q}}_{-} \times \hat{\mathbf{q}}_{+})
 \end{aligned}$$

CP asymmetry in the neutralino decay

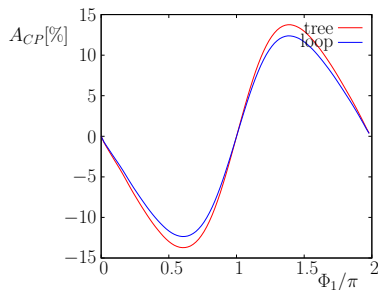
- a CP-odd and CPT-even distribution

$$F_{\text{CP}}(x_-, x_+) = \frac{1}{2} [F_3(x_-, x_+) + F_3(x_+, x_-)]$$

- a CP-odd quantity related to the above CP-odd distribution

$$O_{\text{CP}} = \hat{n} \cdot (\hat{q}_+ \times \hat{q}_-)$$

$$A_{\text{CP}} \equiv \frac{N(O_{\text{CP}} > 0) - N(O_{\text{CP}} < 0)}{N(O_{\text{CP}} > 0) + N(O_{\text{CP}} < 0)} = \frac{\int_{\mathcal{D}} \frac{1}{2} \sin \chi F_{\text{CP}}(x_-, x_+) dx_- dx_+}{\int_{\mathcal{D}} F_0(x_-, x_+) dx_- dx_+}$$



Outline

- 1 Introduction
- 2 CP-even observables
- 3 CP-odd observables
- 4 Summary**

Summary

- many possible CP-even and CP-odd observables can give information about complex phases of μ , M_1 , A_t , A_τ
- unambiguous detection will require combining data from different channels/sectors
- some asymmetries are induced by loop effects
- could be of the order of a few % for phases of μ , M_1 , A_t
⇒ access to CP properties of chargino, neutralino and stop sectors
- Outlook:
full analysis of production+decay required at one loop for precision physics at the ILC