



Euroflavour 2008, Durham

WG6: Review of MC tools

H. CZYŻ, IF, UŚ, Katowice

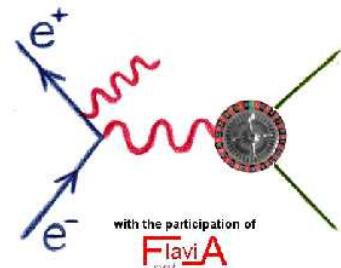
WG6 - Radiative Return and MC Tools



Group coordinators: H. Czyż, J.H. Kühn

wider structure:

Working Group on Rad. Corrections and MC Generators for Low Energies



with the participation of
FlaviA
net

Group coordinators: H. Czyż, G. Venanzoni (Frascati,KLOE)

Meetings:

- * Frascati, 16-17 October 2006
- * Frascati, 25-26 June 2007
- * Frascati, 11 April 2008
- * Beijing, 9-11 October 2008

The subjects covered:

- ▶ Monte Carlo generators for Luminosity
- ▶ Monte Carlo generators for e^+e^- annihilation into leptons and hadrons 
- ▶ Monte Carlo generators for e^+e^- annihilation into hadrons plus an energetic photon from initial state radiation (ISR) 
- ▶ Monte Carlo generators for τ production and decays 

People involved

Beijing: Wang, Zhang

Berlin: Jegerlehner

Bologna: Caffo, Remiddi

Cracov: Grzelińska, Jadach, Wąs

Dubna: Arbuzov, Kuraev

Frascati: Isidori, Mueller, Pacetti, Pancheri, Shekhovtsova, Venanzoni

Karlsruhe: Beltrame, Kluge, Kühn,

Katowice: Czyż, Gluza, Kołodziej

Mainz: Denig

Novosibirsk: Eidelman, Fedotovich, Sibidanov, Solodov

Padova: Passera

Parma: Trentadue

Pavia: Carloni-Calame, Montagna, Piccinini

Rome: Baldini, Bini, Greco, Nguyen

Valencia: Rodrigo

Zeuthen: Riemann

Experiments involved

BaBar

BELLE

BES-III

CMD2

KLOE

SND

MC generators

BABAYAGA

KKMC 

MCGPJ

PHOKHARA 

PHOTOS 

TAUOLA 

Why Beijing...by Wang Ping



BES-III will take data
from June 23rd.

BELLE will start
upgrade from 2009.

Best time to have our
meeting
in Beijing.

Luminosity

BabaYaga and its theoretical accuracy

Carlo M. Carloni Calame

INFN, Sezione di Pavia

Working Group on Radiative corrections and generators for low energy hadronic cross section and luminosity

based on [hep-ph/0607181](#) (accepted by [NPB](#))

in collaboration with G. Balossini, G. Montagna, O. Nicrosini,
F. Piccinini



Luminosity

Estimate of the theoretical accuracy

- switching off VP, tuned comparisons with independent calculations/approaches ([Labspv](#), [Bhwidē](#))
 - ★ $\Delta\sigma/\sigma < 0.03\%$ on cross sections
 - ★ up-to-0.5% differences between BabaYaga and Bhwidē in distribution tails
- comparison with existing perturbative 2-loop calculations
 - ★ currently available
 1. [Penin](#): complete virtual 2-loop photonic corrections (for $Q^2 \gg m_e^2$) plus real radiation in the soft limit
 2. [Bonciani et al.](#): virtual $N_F = 1$ [only electron in the loops] fermionic contributions plus real radiation in the soft limit
 - ★ the photonic and $N_F = 1$ $\mathcal{O}(\alpha^2)$ content of the S+V part in the BabaYaga matched formula can be easily extracted. The terms to be directly compared to 1. and 2. can be read out!
 - ★ the impact of the missing $\mathcal{O}(\alpha^2)$ S+V corrections can be quantified within realistic setup

Luminosity

Summary of theoretical errors

- for **Bhabha cross section**, within realistic setup for luminometry, the theoretical errors of **the new BabaYaga** are summarized

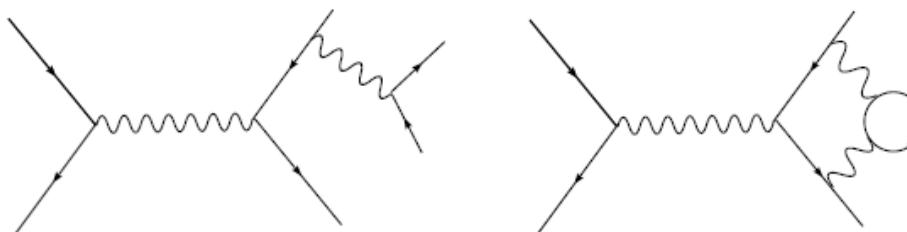
$ \delta^{err} $ (%)	(a)	(b)	(c)	(d)
$ \delta_{VP}^{err} $	0.01	0.00	0.02	0.04
$ \delta_{pairs}^{err} $	0.02	0.03	0.03	0.04
$ \delta_{H,H}^{err} $	0.00	0.00	0.00	0.00
$ \delta_{phot+N_f=1}^{err} $	0.01	0.01	0.00	0.01
$ \delta_{SV,H}^{err} $	0.05	0.05	0.05	0.05
$ \delta_{total}^{err} $	0.09	0.09	0.10	0.14

Table: LABS (a) (c), VLabs (b) (d), 1.02 GeV (a) (b), 10 GeV (c) (d)

Luminosity

Light-pair corrections (real & virtual)

- They contribute at $\mathcal{O}(\alpha^2)$, VPC (part of 2-loop $N_F = 1$) and RPC largely cancel. Not included in BabaYaga.



- To estimate the impact, VPC evaluated as in Jadach et al. ('97); Kniehl ('90); Burgers ('85); Barbieri et al. ('72); RPC evaluated in soft approximation as in Arbuzov et al. ('97)
- the correction does not exceed 0.05% in LABS¹ and VLABS² at 1 and 10 GeV (see hep-ph/0607181)

¹ $20^\circ < \vartheta_\pm < 160^\circ$

² $55^\circ < \vartheta_\pm < 125^\circ$

Luminosity

Hadronic corrections to Bhabha scattering

Tord Riemann, DESY, Zeuthen

based on work with:

S. Actis (RWTH Aachen), M. Czakon (U. Würzburg)
and J. Gluza (Silesian U. Katowice)



Working Group on Radiative Corrections and Generators for Low

Energy Hadronic Cross Section and Luminosity

11 April 2008, Frascati

- **Introduction: Two-loop corrections to Bhabha Scattering**
- **Leptonic contributions with $m_e^2 \ll m_f^2 \ll s, t$**
ACGR: NPB 786 (2007) [[arXiv:0704.2400](#)]
- **Leptonic contributions with $m_e^2 \ll m_f^2, s, t$**
ACGR: APP B38 (2007) [[arXiv:0710.5111](#)] → see also talk by Roberto Bonziani
- **Hadronic contributions**
ACGR: PRL 100 (2008) [[arXiv:0711.53847](#)]
- **Summary**

Luminosity

Summary

- We determine the $N_f = 2$ contributions to 2-loop Bhabha scattering, including the hadronic corrections
- They are small, but non-negligible at the scale 10^{-3} (\rightarrow No LEP influencing)
- Agreement for $m_e^2 \ll m_l^2 \ll s, t, u$ with:
"Two-loop QED corrections to Bhabha scattering"
Thomas Becher, Kirill Melnikov, arXiv:0704.3582 [hep-ph], JHEP
- Agreement for $m_e^2 \ll m_l^2, s, t, u$ with:
"Two-Loop Heavy-Flavor Contribution to Bhabha Scattering",
Roberto Bonciani, Andrea Ferroglio, Sacha Penin, arXiv:0710.4775v3 [hep-ph]
- To be evaluated yet:
 \longrightarrow 1-loop diagrams with real photon emission, interfering with real (Born) radiation, including 5-point functions
- Also: \longrightarrow Real pair production
- Both items were studied already by Andrei Arbuzov, Kuraev, Shaitchatdenov (1998, small photon mass)

PHOTOS

1

PHOTOS Monte Carlo – its phase-space and benchmarks

Z. Was

Institute of Nuclear Physics, Krakow *and* CERN-PH, Geneva

talk include contributions of:

P. Golonka

CERN IT/CO-BE , Geneva, Institute of Nuclear Physics, Krakow

G. Nanava

JINR, Dubna, Russia, Institute of Nuclear Physics, Krakow

PHOTOS

2

Purpose of the talk

Because QED corrections affect interpretation of measured quantities: cut off induced corrections to the rates, to parity sensitive asymmetries, CKM ...

PHOTOS was used for many years in low precision regime for that purpose by practically all experiments.

Precision requirements increased; responsibility on the project grows.

We have completed re-analysis of program content in some of its aspects:

- 1- matrix elements for $Z \rightarrow l\bar{l}$; QED.
- 2- matrix elements for $B \rightarrow K\bar{\pi}$; scalar QED.
- 3- phase space of no approximations, also for multiple photon radiation! On mass-shell iterative relations are attracting attention, technique used in PHOTOS may become useful outside QED?

Z. Was

Precision simulations with TAUOLA

Z. Wąs

Institute of Nuclear Physics, PAN, Kraków, Poland

Main messages:

- What is new or important for the users of our package TAUOLA
- Different perspectives:
 - TAUOLA decays into 5 scalars with full ME now, not real progress yet.
 - MC-TESTER for automated comparisons and benchmark database.
 - universal interface of TAUOLA, bridge between medium and high energy
 - Practical problems of encapsulation. C or not to C: coordination
- Summary

My web page is at <http://home.cern.ch/wasm>

Z. Was

Frascati, April 11, 2008

TAUOLA

TAUOLA

2

TAUOLA: basic structure these assumptions remain!

- Phase space.
- Matrix elements
- Leptonic decays: $\tau \rightarrow e(\mu)\nu_\tau\nu(\gamma)$.
- Electroweak vertex is clear and universal up to 0.1 % precision level..
- Semileptonic decays are different : Hadronic current need to remain experiments' property, in cases experiment wish so.
- The last point enforces constraint for program organization and requests good communication between experimentalists, model builders and TAUOLA authors.
- Also points to low energy e^+e^- data and models. Presence/absence of isospin symmetry need to be adressed.

Z. Was

Frascati, April 11, 2008

H. Czyż, IF, UŚ, Katowice,



WG6: Review of MC tools

17

Systematic treatment of second order NLO QED radiative corrections to exclusive observables

Andrej Arbuzov

Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Dubna, Russia

**Talk at the Radio MontecarLow workshop, Frascati,
11th April 2008**

MCGPJ: A. Arbuzov

Outlook

- ▶ The **ansatz** for the treatment of $\mathcal{O}(\alpha^2 L^1)$ QED radiative corrections to exclusive observables is described
 - ▶ The ansatz is suited for MC simulations
 - ▶ Many processes can be treated in this way
 - ▶ $\mathcal{O}(\alpha^2 L^0)$ contributions can be put into the same structure
 - ▶ MCGPJ can be upgraded
 - ▶ MC integrator and generator for Bhabha scattering is under development (upgrade of SAMBHA MC)

The reason we need $R(s)$

$$a_\mu^{\text{had,LO}} = \frac{\alpha^2}{3\pi^2} \int_{4m_\pi^2}^\infty \frac{ds}{s} K(s) R(s)$$

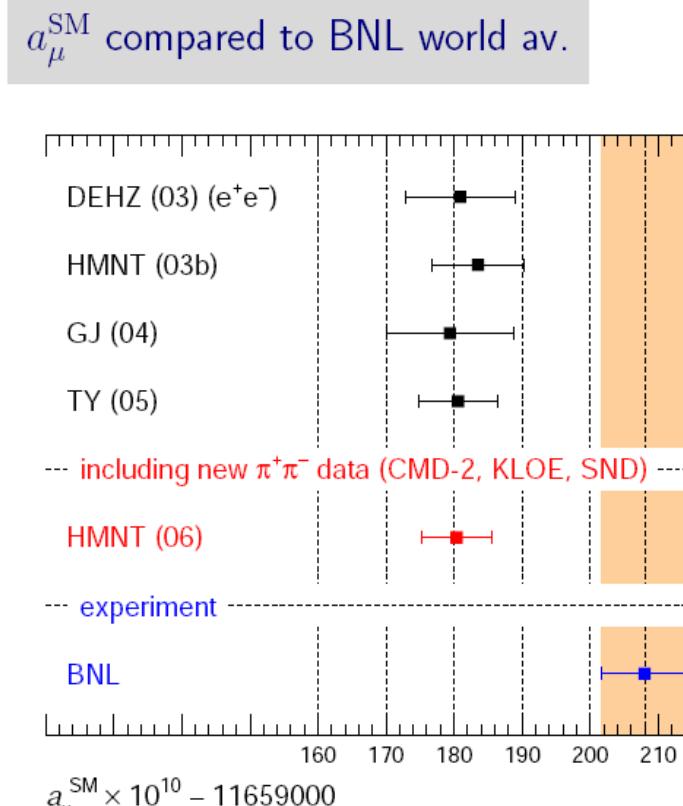
$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma_{\text{point}}}$$

One has to measure :

$$\sigma(e^+e^- \rightarrow \text{hadrons})$$

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a_μ , T. Teubner, Liverpool



DEHZ 06: 180.5 ± 5.6 [3.3 σ]
 Jegerlehner 06: 179.3 ± 6.8 [3.2 σ]

.. Discrepancy increased .. still not fully conclusive .. constrain SUSY ..

Recent changes

TH: Update of QED, up to 5-loop, new α :

was: $(116\ 584\ 719.35 \pm 1.43) \cdot 10^{-11}$

→ is now: $(116\ 584\ 718.09 \pm 0.16) \cdot 10^{-11}$

TH: Improved LO hadr. (from e^+e^-):

Now, with new CMD-2, SND, KLOE:

$(6924 \pm 64) \cdot 10^{-11}$ → $(6894 \pm 46) \cdot 10^{-11}$

EXP: BNL's '01 μ^- data [PRL92(2004)161802]:

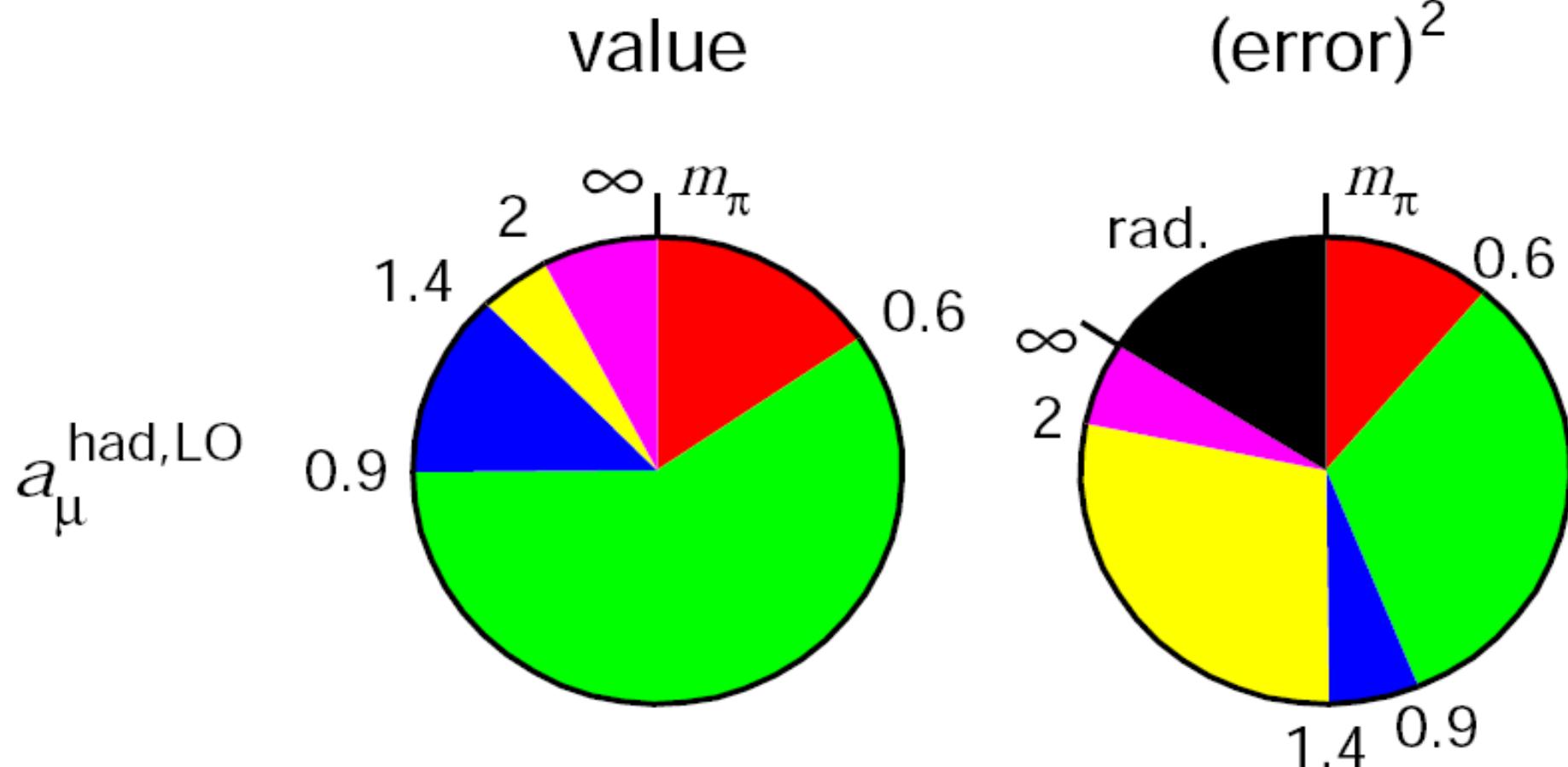
$a_{\mu^-} = 11\ 659\ 214(8)(3) \times 10^{-10}$ (0.7 ppm)

→ $a_\mu = 116\ 592\ 080(63) \times 10^{-11}$ (0.5 ppm)

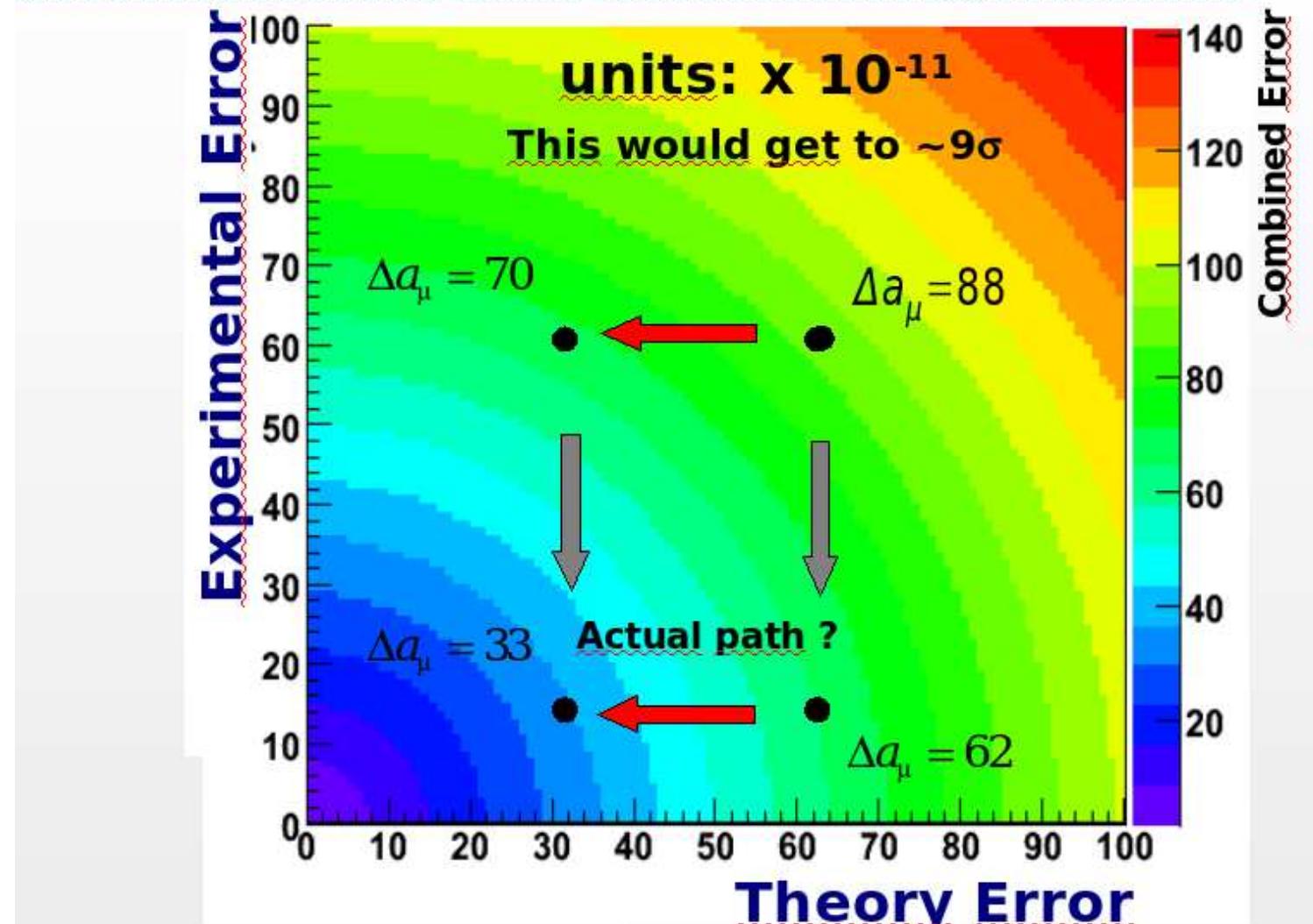
► With this input HMNT get:

$$a_\mu^{\text{EXP}} - a_\mu^{\text{TH}} = (27.6 \pm 8.1) \cdot 10^{-10}, \sim 3.4\sigma$$

a_μ , T. Teubner, Liverpool



Δa_μ improvement requires both experimental and theoretical progress



Conclusions and Prospects

At present, large N_c results agree within $1\ \sigma$ ✓

$$a_\mu^{\text{lbl}} = (11.0 \pm 4.0) \times 10^{-10}$$

More work needed to have the hadronic light-by-light contribution to muon $g - 2$ with reduced uncertainty •

Goal: To have under control model dependences •

a_μ , BaBar preliminary

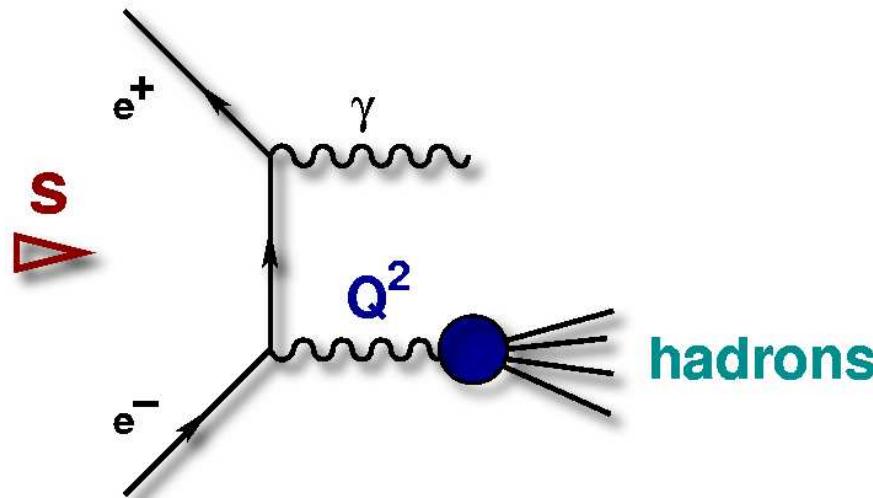
Conclusions

- BaBar analysis of $\pi\pi$ and $\mu\mu$ ISR processes completed
- Precision goal has been achieved: 0.6% in ρ region (0.6-0.9 GeV)
- Absolute $\mu\mu$ cross section agrees with NLO QED within 1.2%
- Preliminary results available for $\pi\pi$ in the range 0.5-3 GeV
- Structures observed in pion form factor at large masses
- Comparison with results from earlier experiments
 - discrepancy with CMD-2 and SND mostly below ρ
 - large disagreement with KLOE
 - better agreement with τ results, especially Belle
- Contribution to a_μ from BaBar agrees better with τ results
- Deviation between BNL measurement and theory prediction significantly reduced using BaBar $\pi\pi$ data
- $a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (27.5 \pm 8.4) \times 10^{-10} \Rightarrow (14.0 \pm 8.4) \times 10^{-10}$
- Wait for final results and contributions of multi-hadronic modes

THE RADIATIVE RETURN METHOD

$$d\sigma(e^+e^- \rightarrow \text{hadrons} + \gamma(\text{ISR})) =$$

$$H(Q^2, \theta_\gamma) d\sigma(e^+e^- \rightarrow \text{hadrons})(s = Q^2)$$



- ▶ measurement of $R(s)$ over the full range of energies, from threshold up to \sqrt{s}
- ▶ large luminosities of factories compensate α/π from photon radiation
- ▶ radiative corrections essential (NLO,...)

High precision measurement of the hadronic cross-section
at meson-factories

From EVA to PHOKHARA

EVA: $e^+e^- \rightarrow \pi^+\pi^-\gamma$

- tagged photon ($\theta_\gamma > \theta_{cut}$)
- ISR at LO + Structure Function
- FSR: point-like pions

[Binner et al.]

$e^+e^- \rightarrow 4\pi + \gamma$

- ISR at LO + Structure Function

[Czyż, Kühn, 2000]

H.C., A. Grzelinska,

J. H. Kühn, E. Nowak-Kubat,

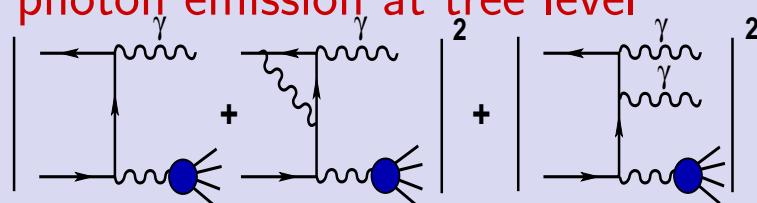
G. Rodrigo, A. Wapienik

PHOKHARA 6.0: $\pi^+\pi^-$,
 $\mu^+\mu^-$, 4π , $\bar{N}N$, 3π , KK ,
 $\Lambda(\rightarrow \dots) \bar{\Lambda}(\rightarrow \dots)$

- **ISR at NLO:** virtual corrections

to one photon events and two

photon emission at tree level



- FSR at NLO: $\pi^+\pi^-$, $\mu^+\mu^-$, K^+K^-
- tagged or untagged photons
- Modular structure

<http://ific.uv.es/~rodrigo/phokhara/>

From EVA to ...

$$e^+ e^- \rightarrow 4\pi + \gamma$$

- ISR at LO + Structure Function

[Czyż, Kühn]

$$e^+ e^- \rightarrow hadrons + \gamma$$

- upgraded by BaBar - not public (?)
- PHOTOS [Barberio et al.] for FSR

$$\text{EVA: } e^+ e^- \rightarrow \pi^+ \pi^- \gamma$$

- tagged photon ($\theta_\gamma > \theta_{cut}$)
- ISR at LO + Structure Function
- FSR: point-like pions

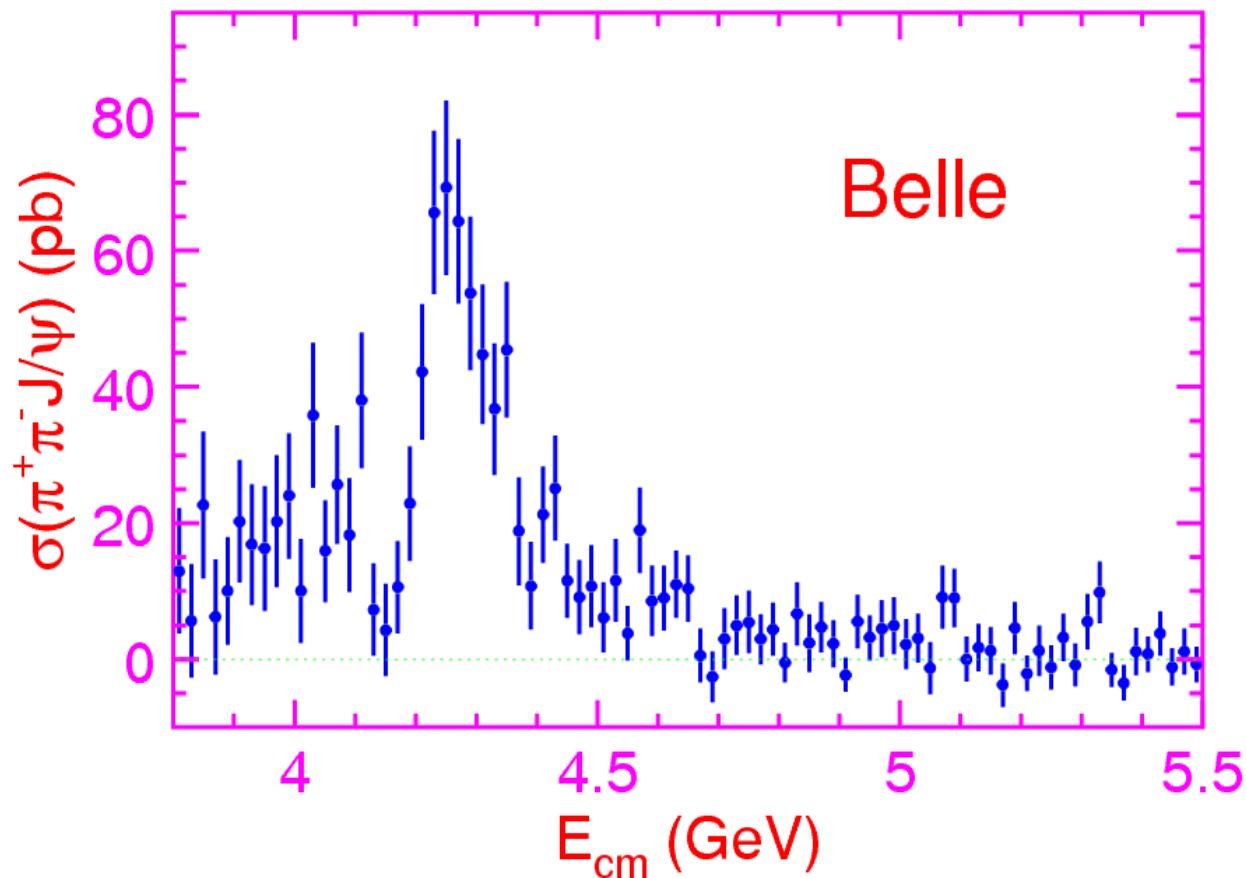
[Binner et al.]

$$e^+ e^- \rightarrow \pi^+ \pi^- + \gamma$$

- FSR studies

[Pancheri, Shekhovtsova, Venanzoni]

$\Upsilon(4260)$ via radiative return



BELLE: Phys.Rev.Lett.99:182004,2007.

Status of PHOKHARA

in collaboration with

A. Grzelińska, J. H. Kühn, E. Nowak-Kubat and A. Wapienik

4π revisited

- ▶ experimental situation: τ vs. e^+e^- data
- ▶ new model predictions

Narrow resonances - FSR

Conclusions

Isospin relations: 4π

$$\langle \pi^+ \pi^- \pi_1^0 \pi_2^0 | J_\mu^3 | 0 \rangle = \textcolor{red}{J}_\mu(p_1, p_2, p^+, p^-)$$

$$\begin{aligned} \langle \pi_1^+ \pi_2^+ \pi_1^- \pi_2^- | J_\mu^3 | 0 \rangle = \\ \textcolor{red}{J}_\mu(p_2^+, p_2^-, p_1^+, p_1^-) + \textcolor{red}{J}_\mu(p_1^+, p_2^-, p_2^+, p_1^-) \\ + \textcolor{red}{J}_\mu(p_2^+, p_1^-, p_1^+, p_2^-) + \textcolor{red}{J}_\mu(p_1^+, p_1^-, p_2^+, p_2^-) \end{aligned}$$

$$\begin{aligned} \langle \pi^- \pi_1^0 \pi_2^0 \pi_3^0 | J_\mu^- | 0 \rangle = \\ \textcolor{red}{J}_\mu(p_2, p_3, p^-, p_1) + \textcolor{red}{J}_\mu(p_1, p_3, p^-, p_2) + \textcolor{red}{J}_\mu(p_1, p_2, p^-, p_3) \end{aligned}$$

$$\begin{aligned} \langle \pi_1^- \pi_2^- \pi^+ \pi^0 | J_\mu^- | 0 \rangle = \\ \textcolor{red}{J}_\mu(p^+, p_2, p_1, p^0) + \textcolor{red}{J}_\mu(p^+, p_1, p_2, p^0) \end{aligned}$$

J. H. Kühn (1999)
H. Czyż, IF, UŚ, Katowice,



Isospin relations: 4π

$$\int J_\mu^{em} (J_\nu^{em})^* d\Phi_n(Q; q_1, \dots, q_n) \\ = \frac{1}{6\pi} (Q_\mu Q_\nu - g_{\mu\nu} Q^2) R(Q^2)$$

$$R(Q^2) = \sigma(e^+e^- \rightarrow hadrons)(Q^2)/\sigma_{point}$$

Isospin relations: 4π

$$\frac{d\Gamma_{\tau \rightarrow \nu + hadrons}}{dQ^2} = 2 \Gamma_e \frac{|V_{ud}|^2 S_{EW}}{m_\tau^2} \left(1 - \frac{Q^2}{m_\tau^2}\right)^2 \left(1 + 2\frac{Q^2}{m_\tau^2}\right) R^\tau(Q^2)$$

$$\int J_\mu^- J_\nu^{-*} d\Phi_n(Q; q_1, \dots, q_n) = \frac{1}{3\pi} (Q_\mu Q_\nu - g_{\mu\nu} Q^2) R^\tau(Q^2)$$

Isospin relations: 4π

$$R^\tau (- \ 0 \ 0 \ 0) = \frac{1}{2} R (+ \ + \ - \ -)$$

$$R^\tau (- \ - \ + \ 0) = \frac{1}{2} R (+ \ + \ - \ -) + R (+ \ - \ 0 \ 0)$$

Isospin relations: 4π ; exp. situation

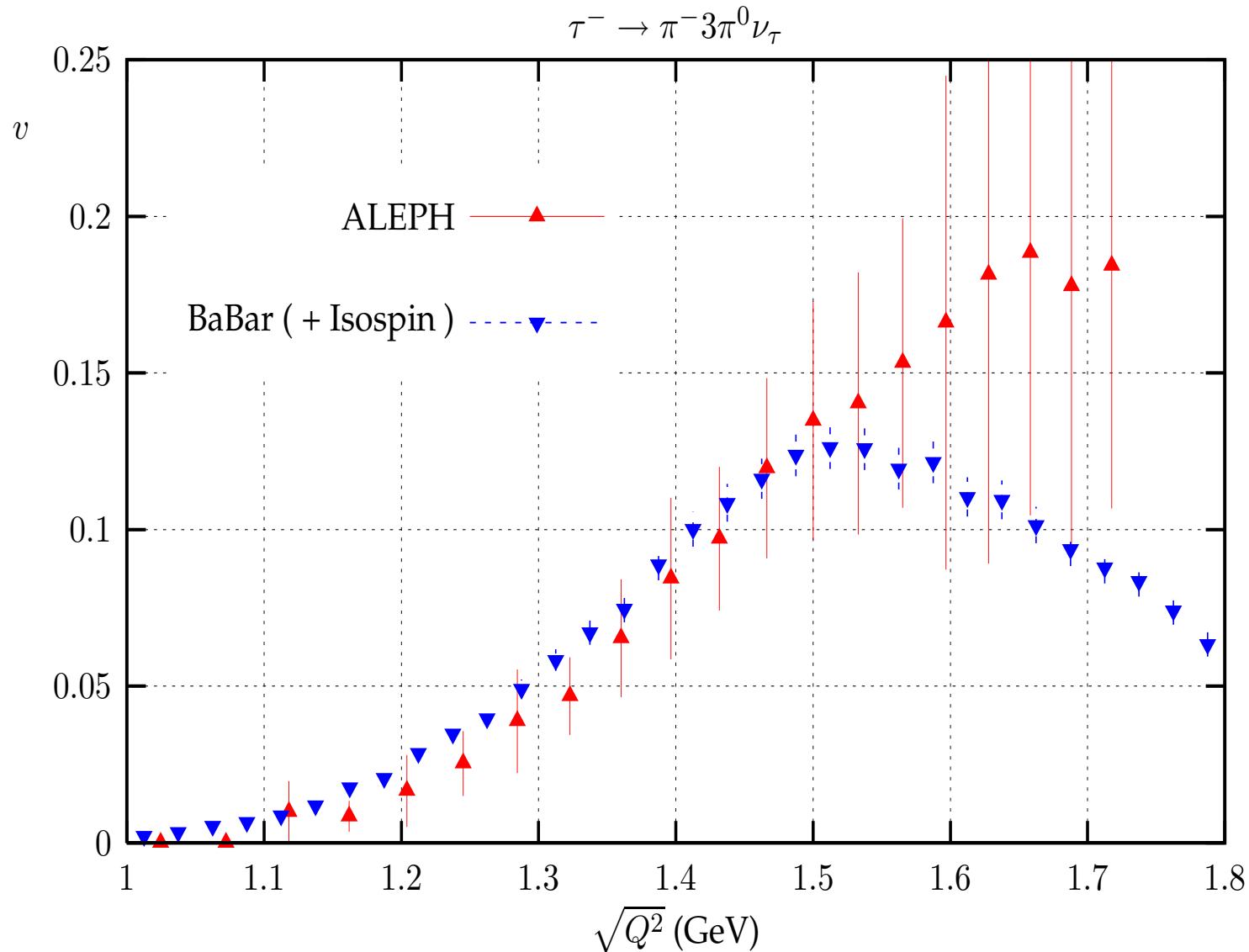
$e^+e^- \rightarrow 2\pi^+2\pi^-$: BaBar, CMD2, SND

$e^+e^- \rightarrow 2\pi^0\pi^+\pi^-$: BaBar(preliminary), CMD2, SND

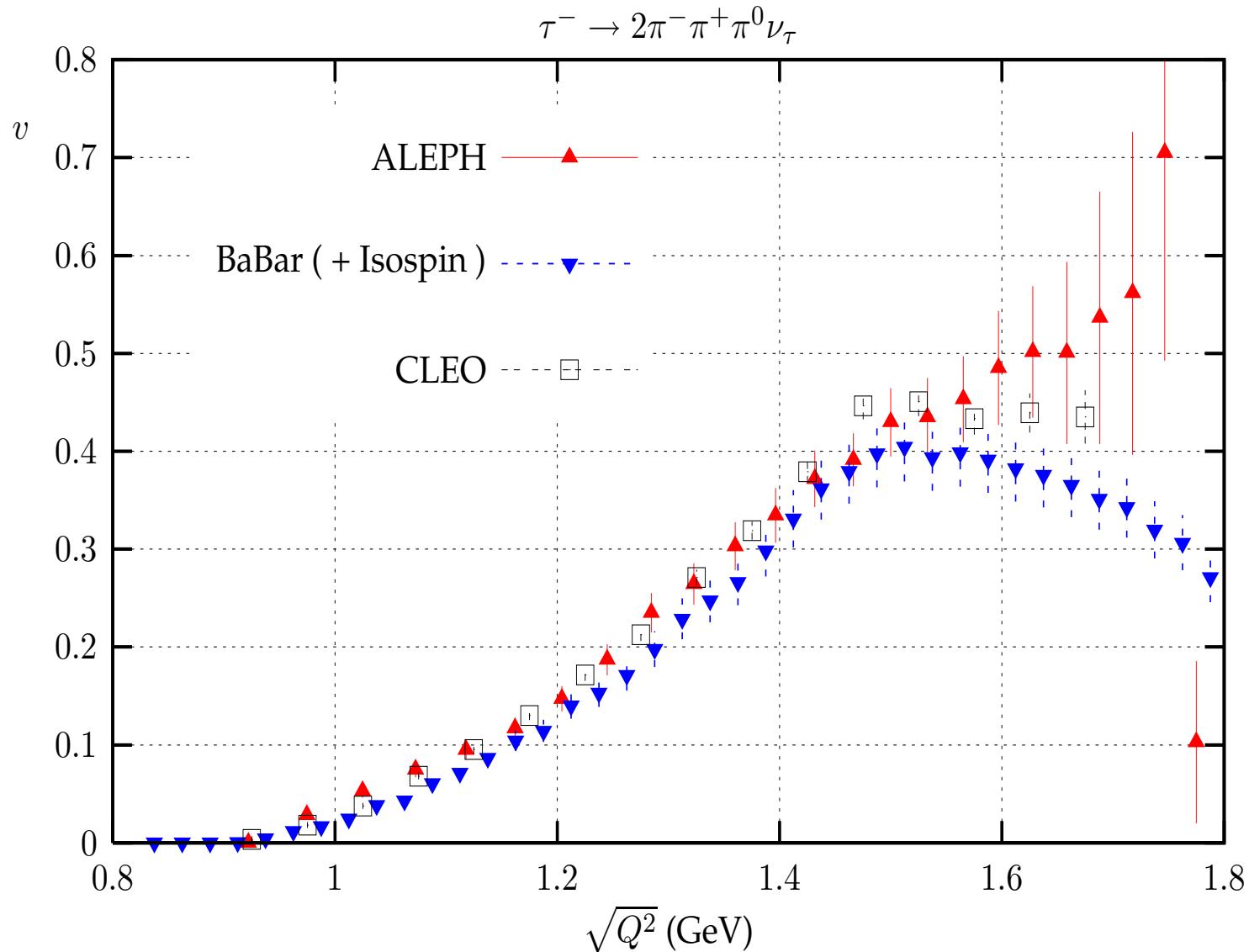
$\tau^- \rightarrow \nu 3\pi^0\pi^-$: ALEPH

$\tau^- \rightarrow \nu 2\pi^-\pi^+\pi^0$: ALEPH, CLEO

Isospin relations: 4π ; exp. situation



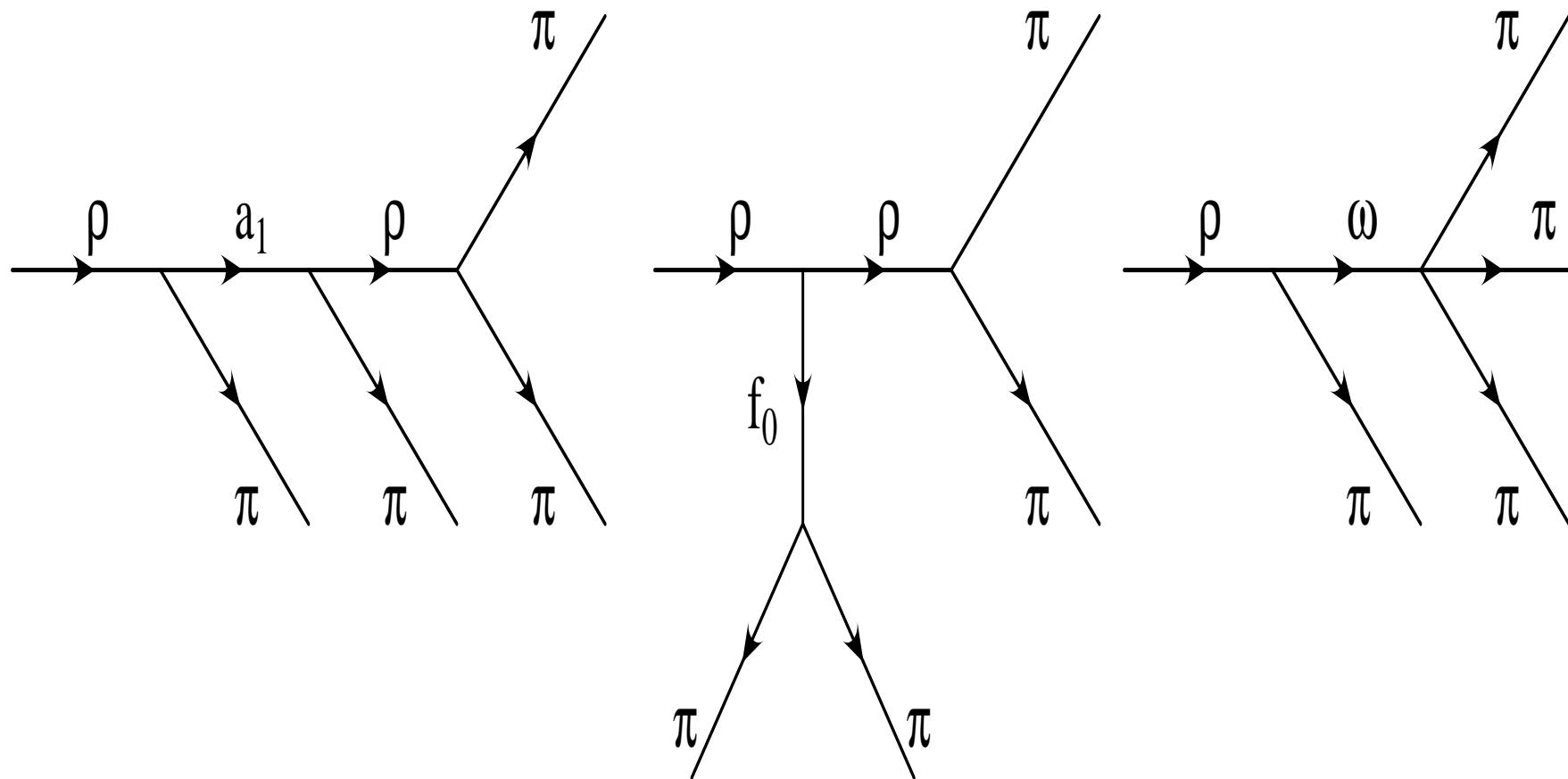
Isospin relations: 4π ; exp. situation



4π : exp. situation

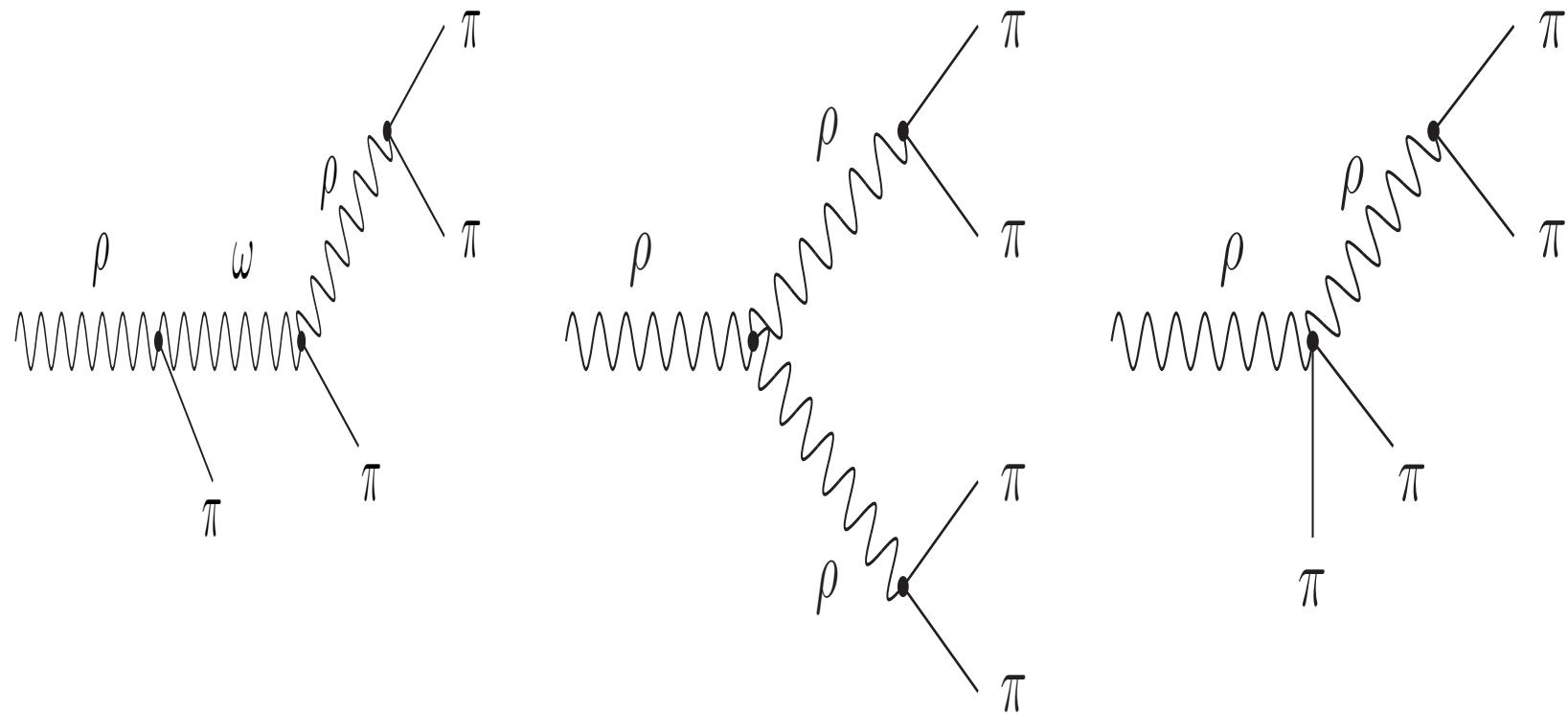
- ▶ $\pi\omega(\rightarrow \pi^+\pi^-\pi^0)$: CLEO, BaBar(prel.)
- ▶ $\rho \rightarrow \rho(\rightarrow \pi\pi)\rho(\rightarrow \pi\pi)$: BaBar(prel.)

The model



H.C., J.H. Kühn (2000)

The model



H.C., J.H. Kühn, A. Wapienik (2008)

H.C., A. Grzelińska, J.H. Kühn, G. Rodrigo(2006)

The model

$$\mathcal{L}_\rho = \frac{1}{4} \vec{F}_{\mu\nu} \cdot \vec{F}^{\mu\nu} + \frac{1}{2} (\vec{D}^\mu \phi) \cdot (\vec{D}_\mu \phi)$$

$$+ \frac{1}{2} m_\pi^2 \vec{\phi} \cdot \vec{\phi} + \frac{1}{2} m_\rho^2 \vec{\rho}_\mu \cdot \vec{\rho}^\mu$$

$$\vec{D}_\mu \phi = \partial_\mu \vec{\phi} + g \left(\vec{\rho}_\mu \times \vec{\phi} \right)$$

$$\vec{F}_{\mu\nu} = \partial_\mu \vec{\rho}_\nu - \partial_\nu \vec{\rho}_\mu - g \vec{\rho}_\mu \times \vec{\rho}_\nu$$

The fit

$$m_{\rho'}, m_{\rho''}, m_{\rho'''}, \Gamma_{\rho'}, \Gamma_{\rho''}, \Gamma_{\rho'''}$$

4 couplings in a_1 - part

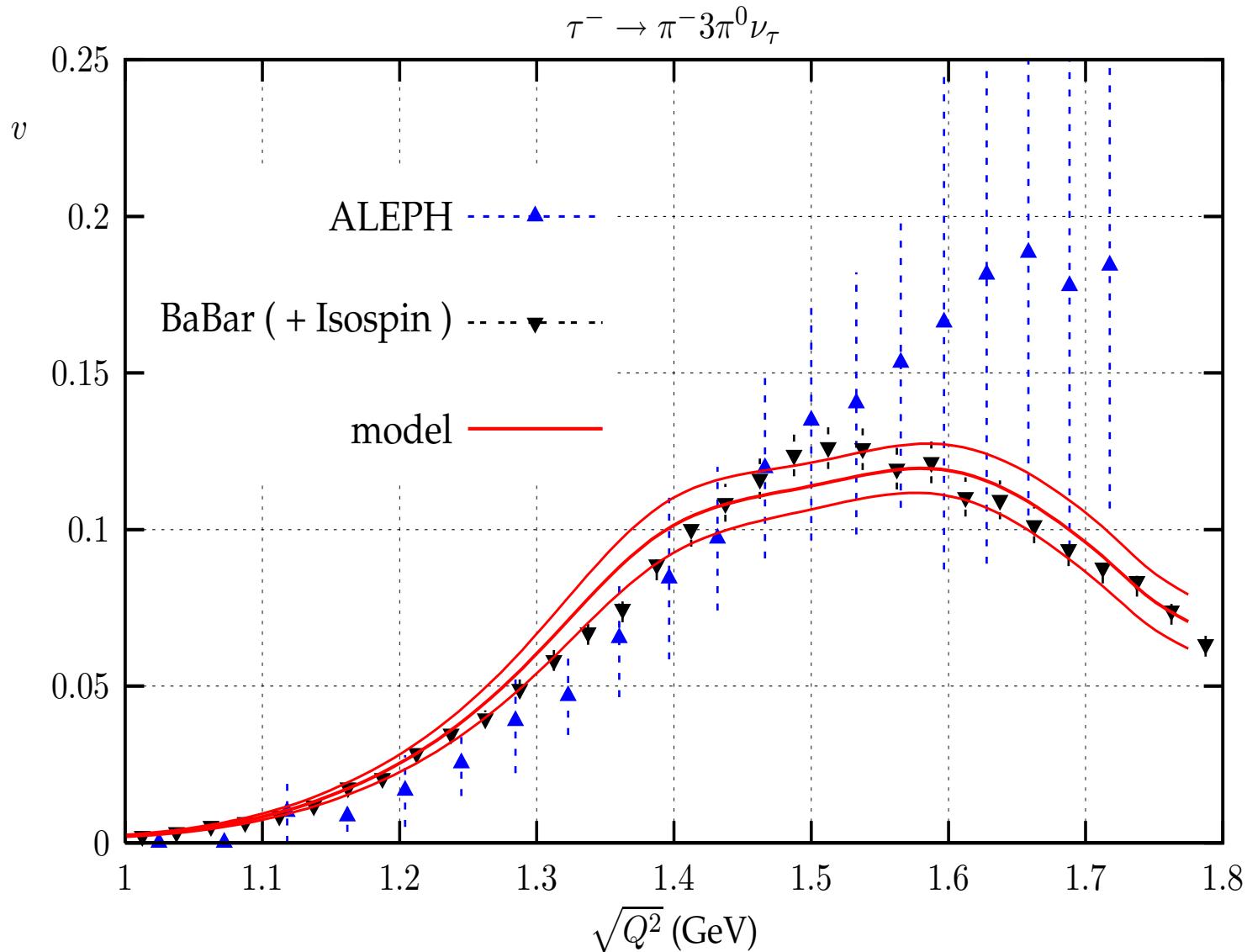
4 couplings in f_0 - part

4 couplings in ω - part

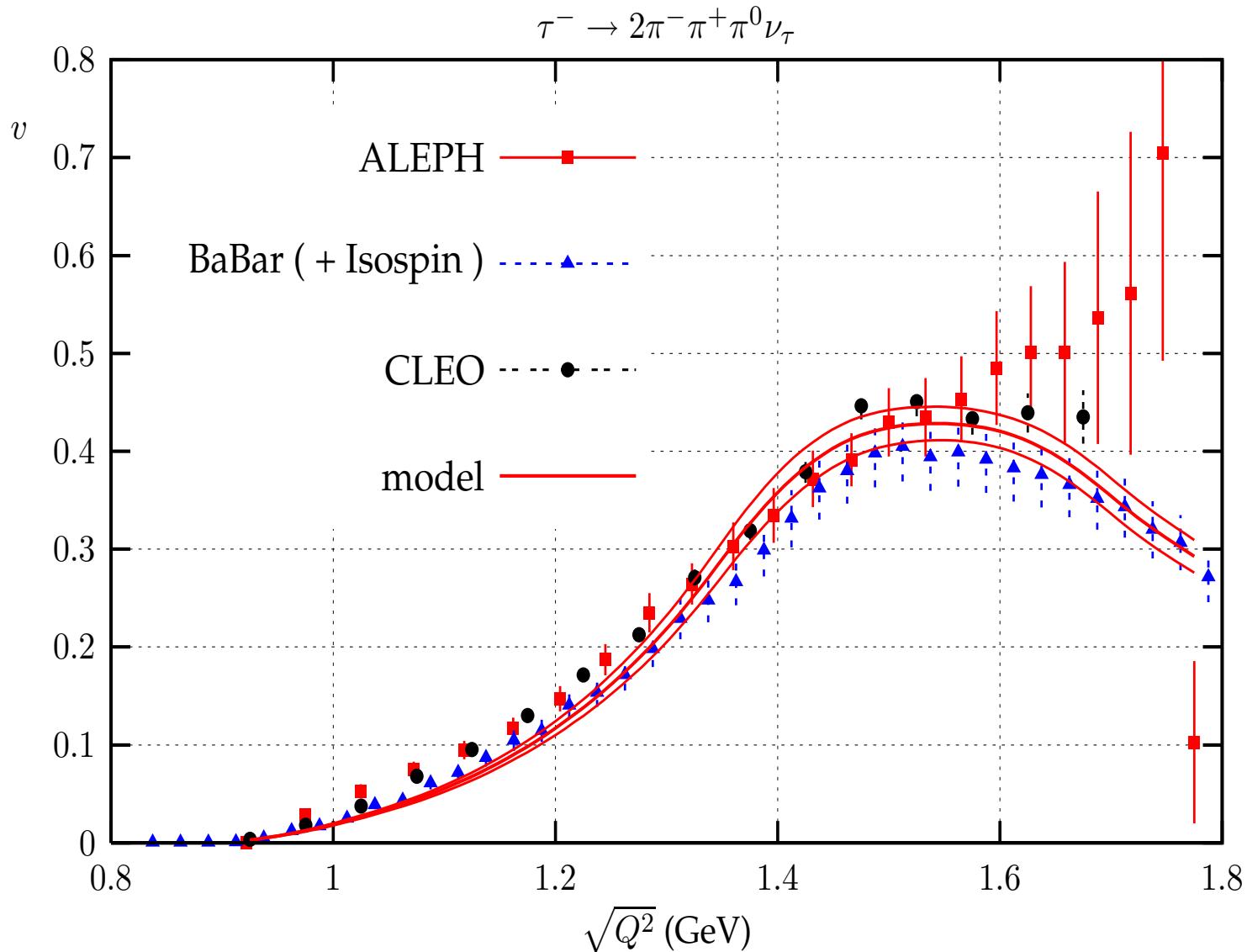
1 coupling in ρ - part

$$\chi^2 = 275 , \quad n_{d.o.f} = 287$$

Comparing with τ data



Comparing with τ data



Comparing with τ data

$$\text{Br}(\tau^- \rightarrow \nu_\tau 2\pi^-\pi^+\pi^0)$$

PDG06 $(4.46 \pm 0.06)\%$

model $(4.12 \pm 0.21)\%$

BaBar (CVC) $(3.98 \pm 0.30)\%$

$$\text{Br}(\tau^- \rightarrow \nu_\tau \pi^- \omega (\pi^-\pi^+\pi^0))$$

PDG06 $(1.77 \pm 0.1)\%$

model $(1.60 \pm 0.13)\%$

BaBar (CVC) $(1.57 \pm 0.31)\%$

Comparing with τ data

$$\text{Br}(\tau^- \rightarrow \nu_\tau \pi^- 3\pi^0)$$

PDG06 $(1.04 \pm 0.08)\%$

model $(1.06 \pm 0.09)\%$

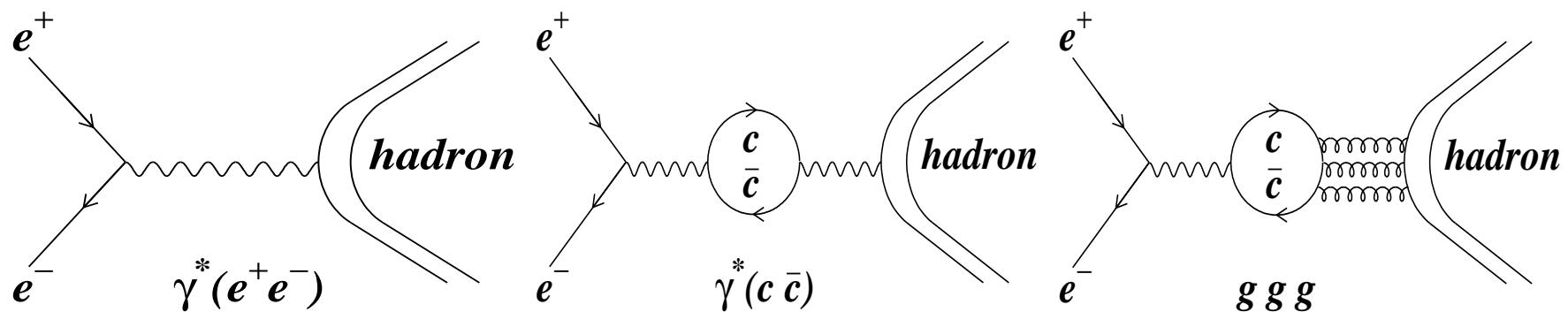
BaBar (CVC) $(1.02 \pm 0.05)\%$

Narrow Resonances

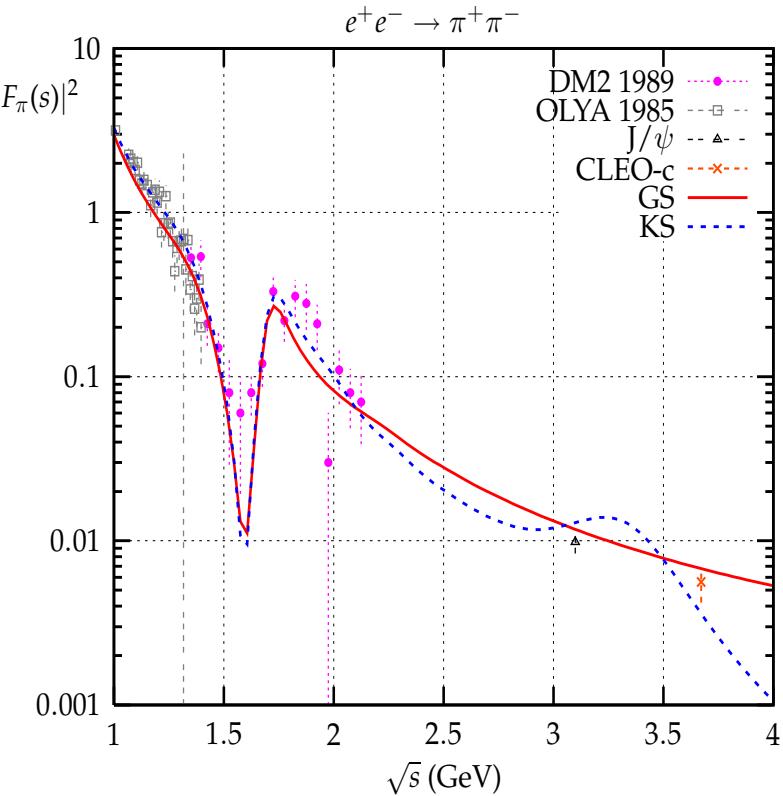
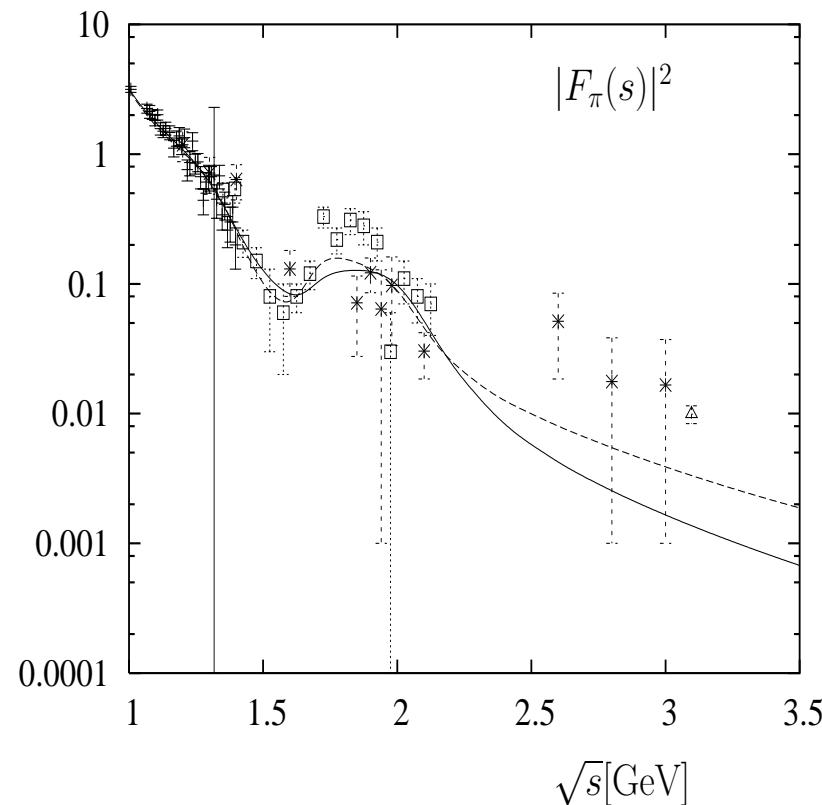
$$e^+ e^- \rightarrow J/\psi \ (\psi(2S))\gamma \rightarrow \pi^+ \pi^-, \mu^+ \mu^-, KK + \gamma(\gamma)$$

$$J/\psi \rightarrow M_{J/\psi} = 3096.916 \text{ MeV}, \quad \Gamma_{J/\psi} = 93.4 \text{ keV}$$

$$\psi(2S) \rightarrow M_{\psi(2S)} = 3686.093 \text{ MeV}, \quad \Gamma_{\psi(2S)} = 337 \text{ keV}$$



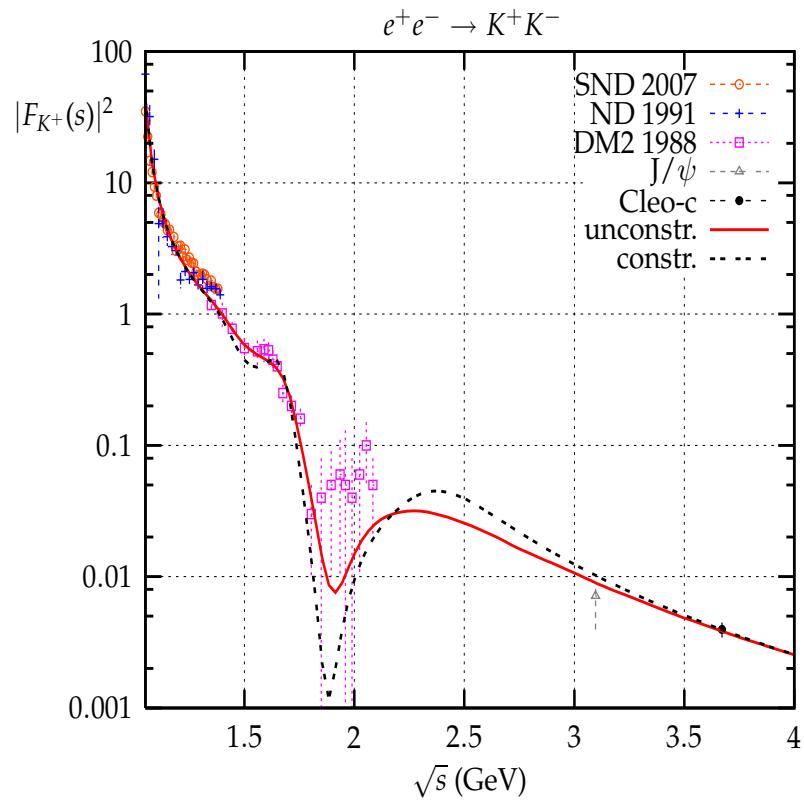
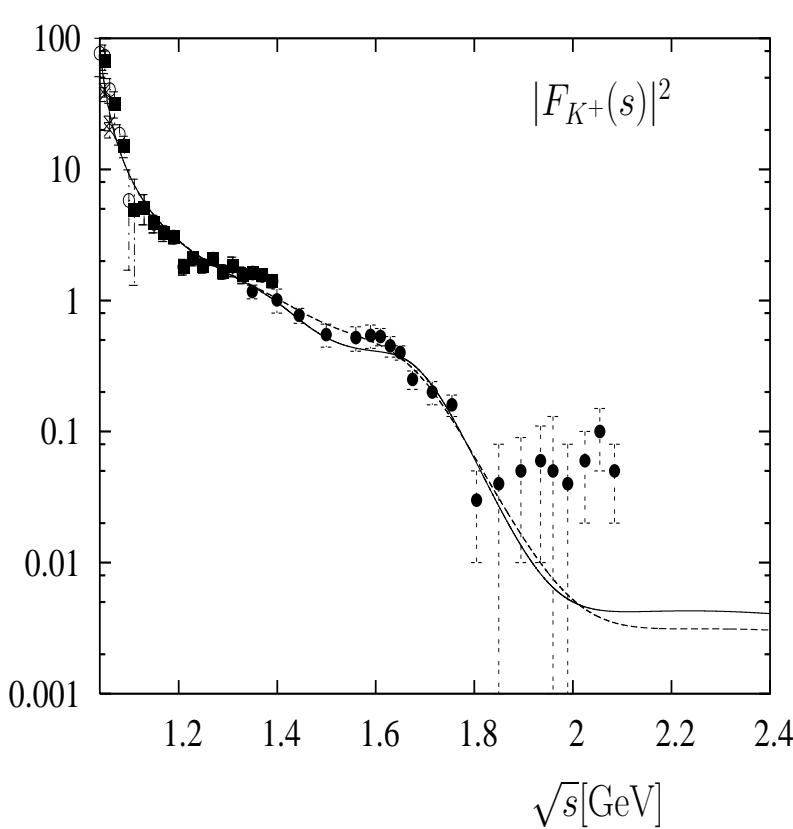
Pion form factor



C. Bruch, A. Khodjamirian and J.H. Kühn, Eur. Phys. J. C39(2005)41

H. C., A. Grzelińska, E. Nowak-Kubat and J.H. Kühn, in preparation

Kaon form factor

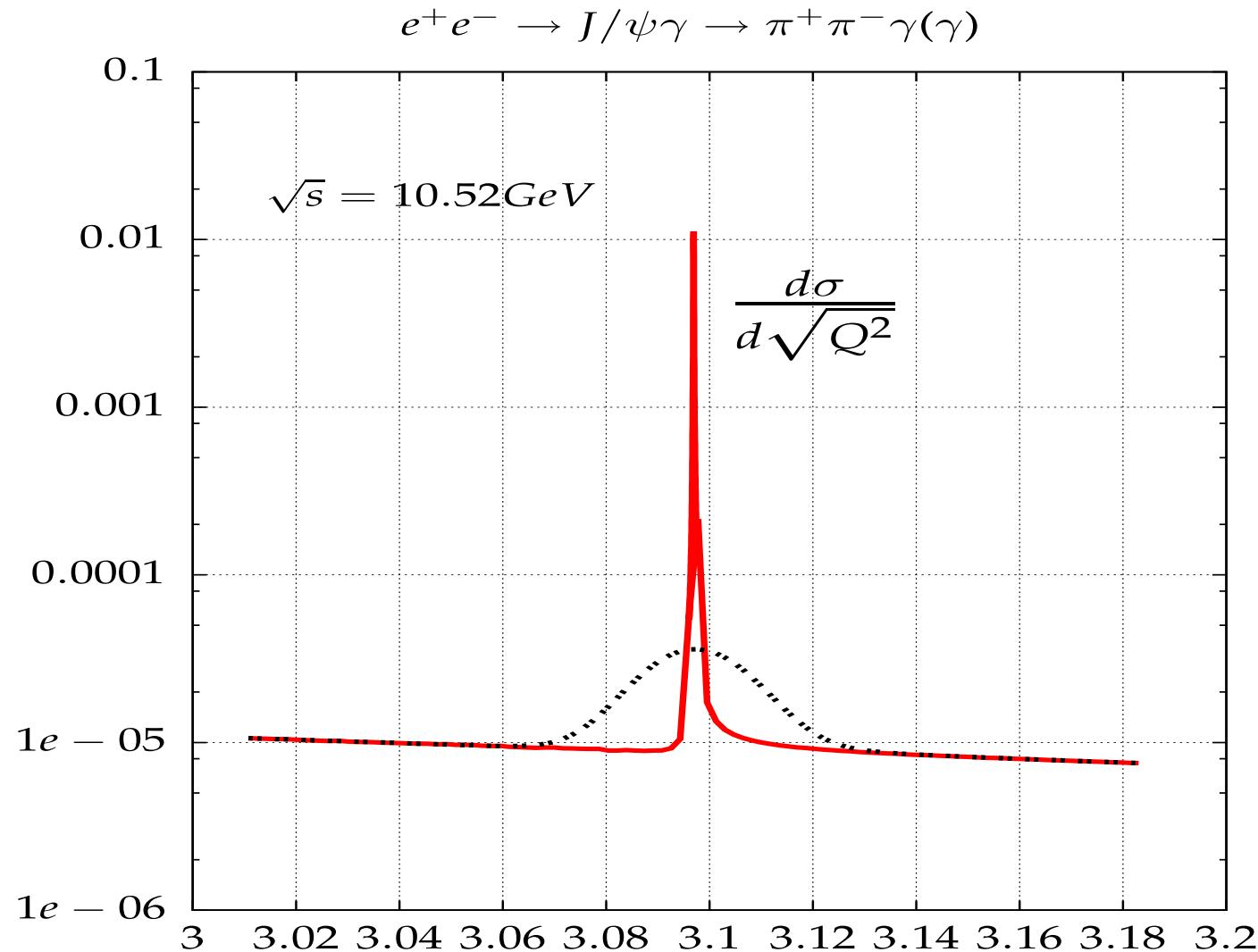


C. Bruch, A. Khodjamirian and J.H. Kühn, Eur. Phys. J. C39(2005)41

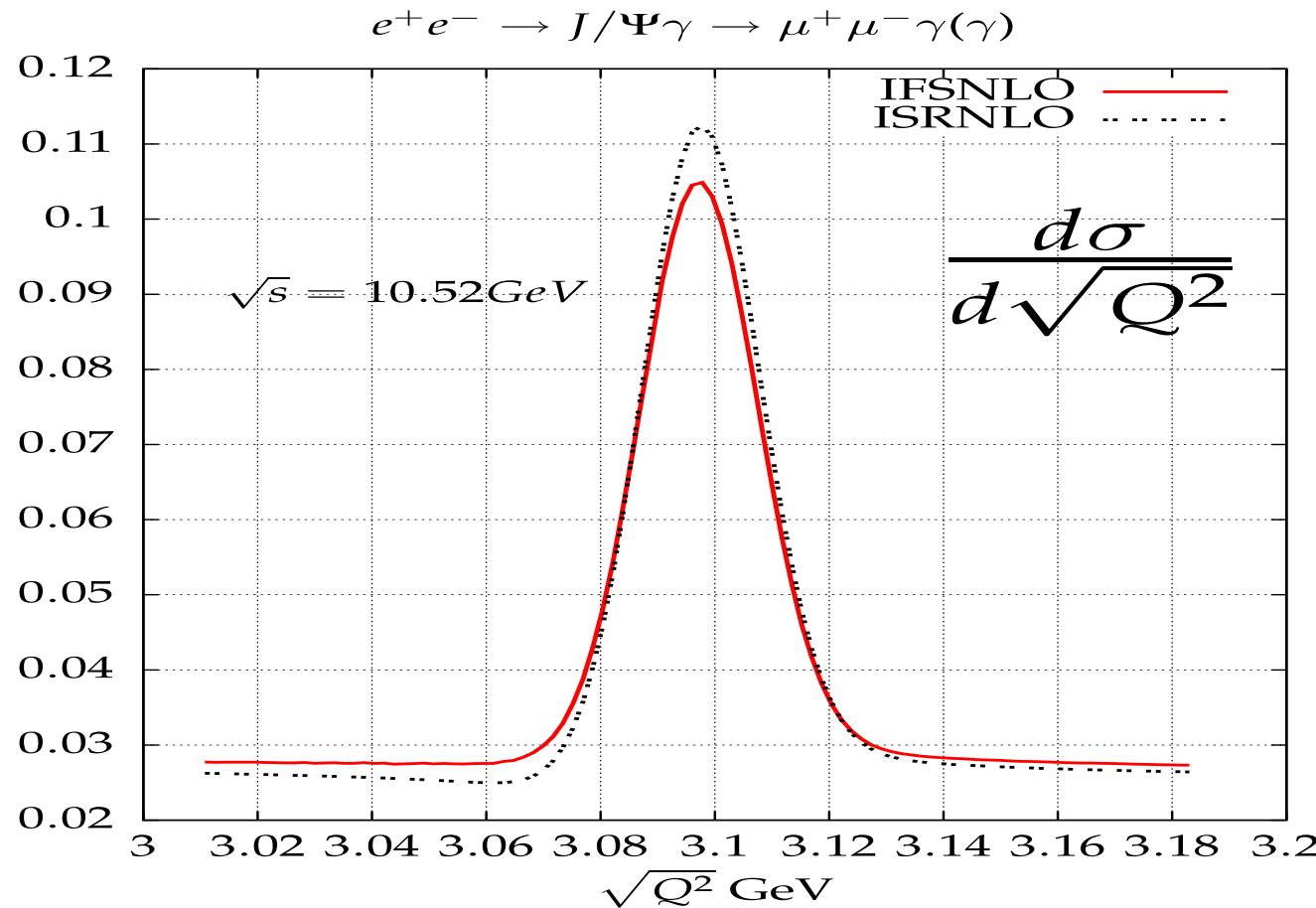
H. C., A. Grzelinska, E. Nowak-Kubat and J.H. Kühn, in preparation

Energy resolution

$\Delta q = 14.5 \text{ MeV}$



FSR - muons

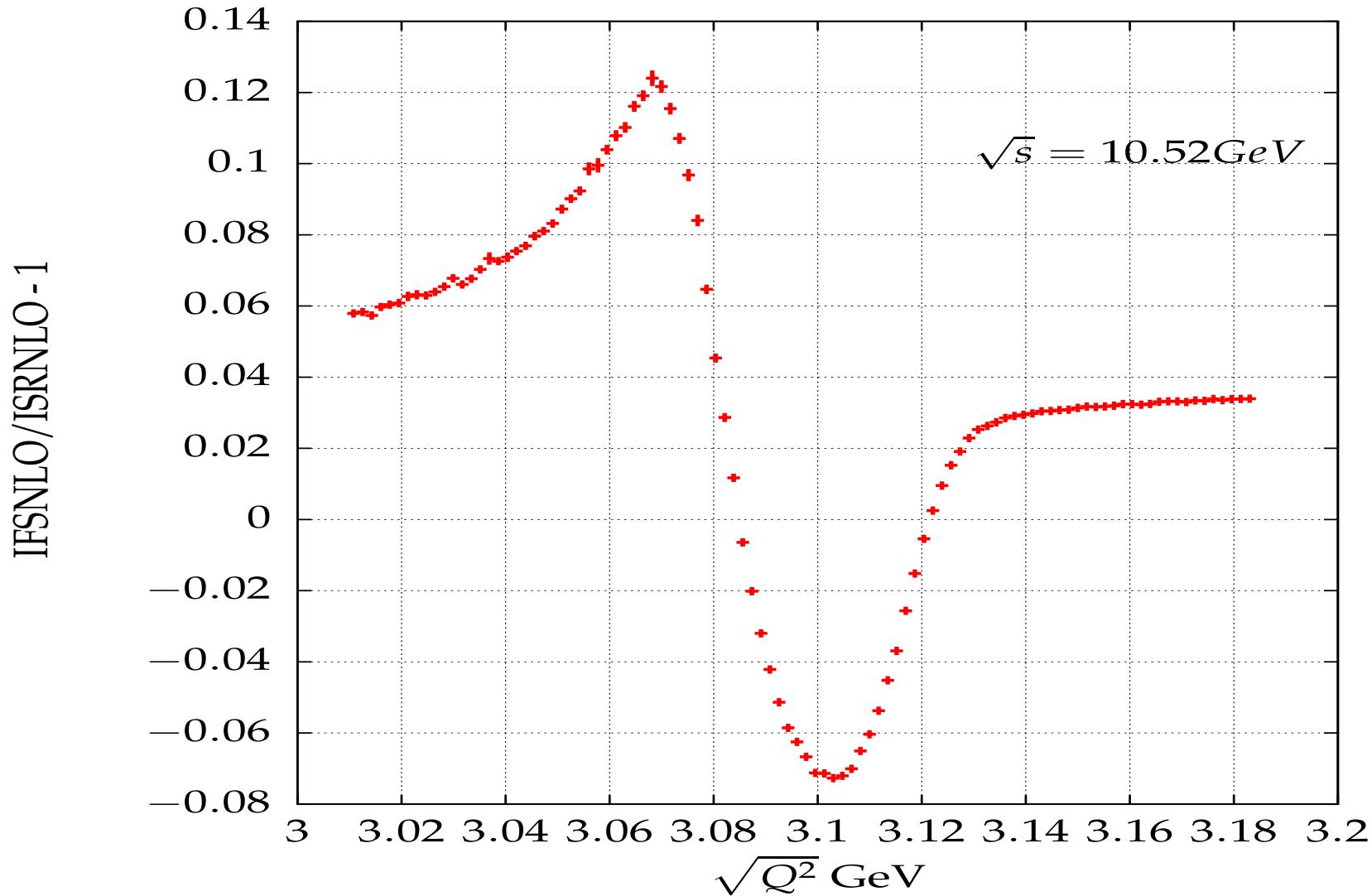


$$\sigma(\text{IFSNLO}) = (6.8527 \pm 0.0006) \text{ pb}$$

$$\sigma(\text{ISRNLO}) = (6.79862 \pm 0.00008) \text{ pb}$$

FSR - muons

$$e^+e^- \rightarrow J/\psi\gamma \rightarrow \mu^+\mu^-\gamma(\gamma)$$



Summary and plans

- 4π channels reanalysis was performed
 - isospin symmetry violation not seen
 - new model proposed and implemented in PHOKHARA

Summary and plans

- ▶ soon J/ψ and $\psi(2S)$ in PHOKHARA
 - ▶ with FSR corrections included
- ▶ PHOKHARA: ISR accuracy 0.5%
 - ▶ need for ISR accuracy $\sim 0.2\%$