

Hybrid inflation and baryogenesis

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- 1 **Baryogenesis**
Observational constraints
Sakharov's conditions
- 2 **Complex hybrid inflation**
Proposal
General dynamics
- 3 **Asymmetrical charge**
Quantum perturbations
- 4 **Conclusions**

Matter vs anti-Matter

- Protons vs anti-protons

$$\frac{n_{\bar{p}}}{n_p} \sim 10^{-4} \quad (1)$$

- Helium vs anti-Helium

$$\frac{n_{\bar{He}}}{n_{He}} \sim 10^{-4} \quad (2)$$

- Nucleosynthesis: baryon to photon ratio η

$$5.92 \times 10^{-10} < \eta \equiv \frac{n_b - n_{\bar{b}}}{n_\gamma} < 6.28 \times 10^{-10} \quad (3)$$

- Baryon number: B

$$8 \times 10^{-11} < B \equiv \frac{n_b - n_{\bar{b}}}{s} < 9 \times 10^{-11} \quad (4)$$

General conditions

- Baryon number violation: B is not a conserved quantity
- C and CP violation (separate matter from anti-matter)
 - C(harge conjugation):

$$\Gamma(q_i \rightarrow q_f) = \Gamma(\bar{q}_i \rightarrow \bar{q}_f) \quad (5)$$

- C(harge conjugation)P(arity): No handedness asymmetry!
- Loss of thermal equilibrium: Stop reactions!

$$\Gamma < H \quad (6)$$

Ingredients and symmetries

- Inflaton field ϕ ; Complex rainfall field a
- **Symmetric potential**

$$V(\phi, a) = \frac{M^4}{4\lambda^2} \left(1 - \frac{\lambda^2}{M^2} |a|^2 \right)^2 + \left(\frac{m^2}{2} + \frac{g^2}{2} |a|^2 \right) \phi^2 \quad (7)$$

- C-invariant, $U(1)$ -invariant, ($a \rightarrow -a$)-invariant
- CP -preserving

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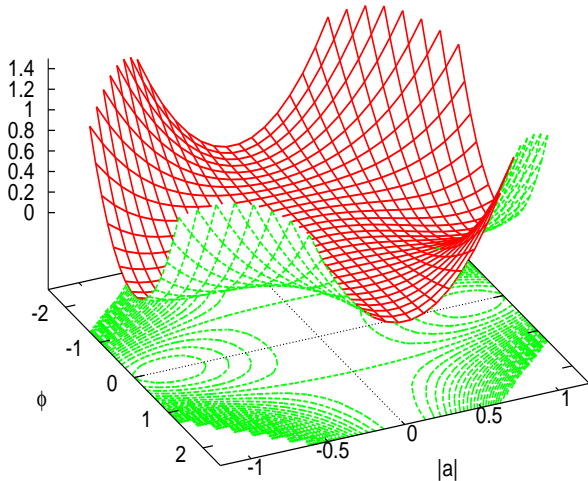
- C-invariant, $U(1)$ -invariant, $(a \rightarrow -a)$ -invariant
- CP -preserving
- **Asymmetric part**

$$\dots + \frac{\delta^2}{4} (a^2 + a^{*2}) \phi^2 \quad (8)$$

- C-invariant, $U(1)$ -broken, $(a \rightarrow -a)$ -invariant
- *Potentially* CP violating (!)

Inflationary dynamics (typical)

Standard hybrid inflation



Inflationary dynamics (typical)

- Set conditions for **vacuum (dominated) inflation**

$$V(\phi, \mathbf{a}) \simeq \frac{M^4}{4\lambda^2} \quad (9)$$

- Inflaton perturbations enhanced (effectively **massless**)
- Rainfall perturbations suppressed (**massive**)
- **Boltzmann equation: $n_a = \text{Im}(a^* \dot{a})$**

$$\dot{n}_a + 3Hn_a = -\delta^2 |a|^2 \phi^2 \sin(2\theta_a) \rightarrow 0 \quad (10)$$

- **No a -charge production, but a -charge dilution**

End of inflation (double)

- *Instability* induced by the rainfall field

$$\phi_- = M/\sqrt{g^2 - \delta^2} \quad (11)$$

$$\phi_+ = M/\sqrt{g^2 + \delta^2} \quad (12)$$

- Rainfall fields *become massless*

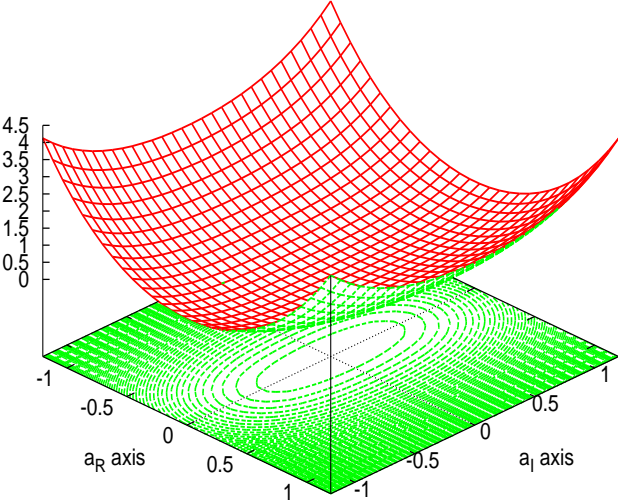
$$\delta a_I \simeq \frac{H_0}{2\pi} \Big|_{\phi=\phi_-}, \quad \delta a_R \simeq \frac{H_0}{2\pi} \Big|_{\phi=\phi_+} \quad (13)$$

- Real and imaginary follow *different* evolutionary paths
- Dynamical *charge* production
- End of inflation: $\phi_+ = \phi_{end}$

$$\ln \left(\frac{\phi_-}{\phi_{end}} \right) \simeq \ln \left(\frac{\sqrt{\pi} \phi_-}{2 m_{Pl}} \right) \simeq \frac{\delta^2}{g^2} \quad (14)$$

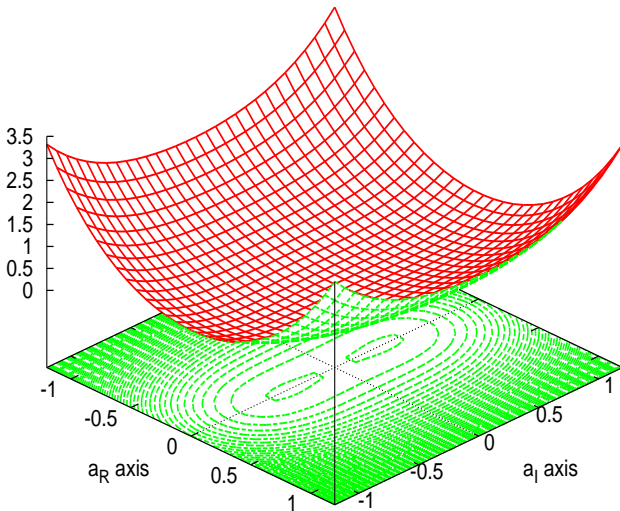
End of inflation (snapshots)

Before: $\phi > \phi_-$



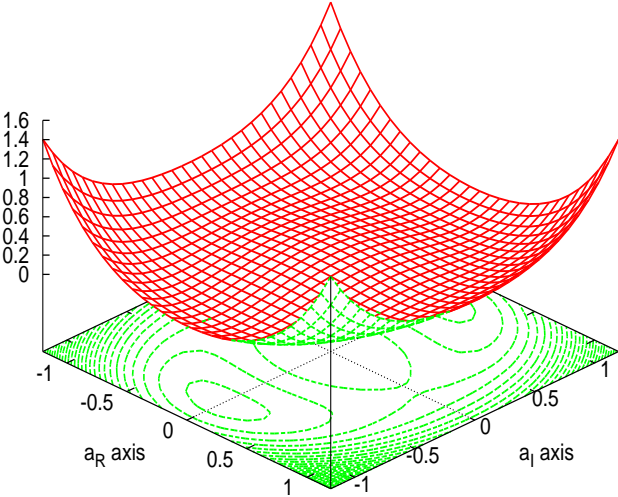
End of inflation (snapshots)

In between: $\phi_- > \phi > \phi_+$



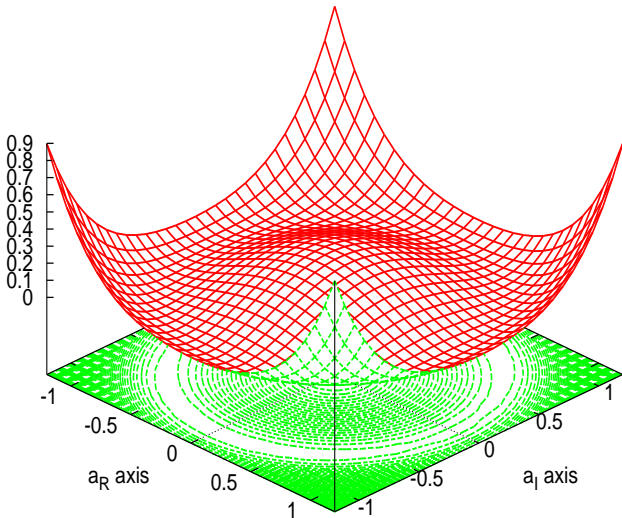
End of inflation (snapshots)

After: $\phi_+ > \phi$



End of inflation (snapshots)

Symmetry restored: $|\phi| \ll \phi_+$



Main results

- (Baryonic) Charge asymmetry (prompt reheating)

$$\left| \frac{n_a}{s} \right| \simeq \frac{g_*^{3/4}}{q_*} \frac{M^2}{m_{Pl}^2} \left(\frac{3H_0}{\sqrt{2}m} \frac{\delta}{g} \right) \exp \left(-\frac{9H_0^2}{2m^2} \frac{\delta^2}{g^2} \right) \quad (15)$$

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- CMB primordial amplitude δ_H constraint

$$\frac{9H_0^2}{2m^2} \frac{\delta^2}{g^2} = \frac{3\pi^{3/2}}{2\lambda^2 g} \frac{(M/m_{Pl})^5}{(m/m_{Pl})^2} \simeq 3 \times 10^{-4} \frac{\lambda}{g^2} \quad (16)$$

- + Spectral index n_s constraint

$$(M/\lambda m_{Pl}) < 5 \times 10^{-5}/g \quad (17)$$

- + Cosmic strings

$$G\mu \simeq (M/\lambda m_{Pl})^2 < 10^{-6} \quad (18)$$

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- Reheating: Translation to baryonic asymmetry (!)

$$\left| \frac{n_B}{s} \right| \simeq \kappa_{inf} \Delta B \frac{\Gamma_{\Delta B}}{\Gamma_a} \left| \frac{n_a}{s} \right| \quad (20)$$

- Inflaton channels are suppressed

$$\begin{cases} \Gamma(a \rightarrow 2\phi) & \sim g^4/\lambda^2 \\ \Gamma(a + a \rightarrow \phi + \phi) & \sim \delta^2 \end{cases} \quad (21)$$