

# Radiative Lifting of Flat Directions of the MSSM during Inflation

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BG, Phys. Rev. D **74** (2006) 043507, [arXiv:hep-th/0604166]

BG, Nucl. Phys. B. (in press), [arXiv:hep-ph/0612011]

BG, C. Pallis and A. Pilaftsis, JHEP **0612** (2006) 038, [arXiv:hep-ph/0605264]

# Outline

- Flat directions of the **MSSM** are lifted during inflation.
- Usually considered origins of lifting:
  - SUGRA corrections
  - nonrenormalizable superpotential terms
  - both contributions in general unknown or arbitrary

## In this talk:

There are **calculable** corrections of competitive magnitude to the aforementioned ones.

Two types of radiative corrections:

- a **generic** in the **curved de Sitter background**
- a **particular** one, arising in  **$F$ -term hybrid inflation**

# MSSM Flat Directions

- Combination of Higgs, squark and slepton scalar fields which
  - are gauge invariant ( $D$ -flat).
  - have vanishing potential arising from superpotential ( $F$ -flat).
- For example  $u\bar{d}\bar{d}$  may contain

$$\tilde{t}_R = \begin{pmatrix} \varphi \\ 0 \\ 0 \end{pmatrix}, \quad \tilde{s}_R^* = \begin{pmatrix} 0 \\ \varphi^* \\ 0 \end{pmatrix}, \quad \tilde{d}_R^* = \begin{pmatrix} 0 \\ 0 \\ \varphi^* \end{pmatrix}.$$

These compose a massless scalar field as

$$\Phi = \frac{1}{\sqrt{3}} (\tilde{t}_R + \tilde{s}_R^* + \tilde{d}_R^*).$$

- $\phi = |\varphi|$  is the canonically normalized modulus field and  $V(\phi) \equiv 0$ .

# Flat Directions in Cosmology

- There is a large number of flat directions, giving rise to exhaustively studied scenarios.
  - Affleck-Dine baryogenesis (Affleck & Dine (1985)).
  - Baryonic isocurvature perturbations (Enqvist & McDonald (1999)).
  - $Q$ -balls (Coleman (1985)).
  - Curvaton Scenario (Enqvist & Sloth; Lyth & Wands (2002)).
  - Thermal history of the Universe (Mazumdar, Allahverdi (2005)).
- During inflation, they can acquire large VEVs.
- VEV is determined by lifting contributions that break the flatness.
- Critical mass for overdamped regime:  $m^2 = \frac{9}{16}H^2$ .

# Non-calculable contributions to the lifting

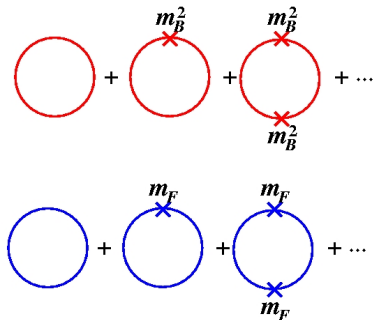
## SUGRA (Dine, Randall, Thomas (1995))

- For  $F \neq 0$ , typical mass terms of order  $H^2$ .
- Depend on the unknown Kähler potential.
- These corrections are absent or highly suppressed when imposing certain symmetries on the Kähler potential. (Gaillard, Murayama & Olive (1995))
- Also absent in  $D$ -term inflation.

## Nonrenormalizable superpotential terms (see e.g. Ghergetta, Kolda, Martin (1996))

- Higher dimensional, Planck scale suppressed superpotential terms.
- Purpose: Stabilizing the potential for VEVs towards the Planck scale.

# One-Loop Effective Potentials



- Sum of all mass insertions.
- VEV  $\phi$  of the flat direction generates masses
  - *via* the Yukawa couplings  $h$  from the superpotential.
  - *via* the gauge coupling  $g$  (super-Higgs mechanism).
- NB: These corrections vanish when SUSY exact (nonrenormalization).

## Yukawa Contributions

Bosons:

Higgs/squark/sfermion mixing state

Fermions:

higgsino/quark/lepton mixing state

$$\text{tr } m_B^2 = \text{tr } m_F^2 \propto h^2 \phi^2$$

## Gauge Contributions

Bosons:

gauge bosons,

$D$ -term scalars

Fermions:

gaugino/higgsino mixing state

$$\text{tr } m_B^2 = \text{tr } m_F^2 \propto g^2 \phi^2$$

# SUSY breaking during inflation

- Breaking through the **curved de Sitter background**.  
BG, Phys. Rev. D **74** (2006) 043507, [arXiv:hep-th/0604166]  
BG, Nucl. Phys. B. (in press), [arXiv:hep-ph/0612011]
- The usual mechanism of **spontaneous SUSY breaking**:  
For certain models, the MSSM fields couple via loops to the vacuum energy driving inflation.  **$F$ -term hybrid inflation**.  
BG, C. Pallis and A. Pilaftsis, JHEP **0612** (2006) 038,  
[arXiv:hep-ph/0605264]

# Effective Potentials for Fermions & Scalars in de Sitter

- Effective potentials in curved spacetime are generalizations of the Coleman Weinberg potential.
- Additional corrections of order  $H^2$ .
- Calculable by using **position space** techniques.
- UV cutoff length  $\varrho$ , de Sitter invariant.
- Dirac fermion contribution:

$$V_\psi = -\frac{m^2}{2\pi^2} \frac{1}{\varrho^2} + \frac{1}{16\pi^2} \left\{ -m^4 \log(\varrho^2 m^2) - 2H^2 m^2 \log(\varrho^2 m^2) \right\}$$

Candelas, Raine (1975); corrected form in BG (2006) and Miao, Woodard (2006)

- Real scalar contribution:

$$V_\phi = \frac{m_\phi^2}{8\pi^2 \varrho^2} + \frac{1}{16\pi^2} \left\{ \frac{1}{4} m_\phi^4 \log(\varrho^2 m_\phi^2) - H^2 m_\phi^2 \log(\varrho^2 m_\phi^2) \right\}$$

Candelas, Raine (1982)



# Effective Potential for Chiral Multiplets

- Within supersymmetry, **one** massive Dirac fermion is accompanied by **four** real scalars of the same mass.
- These can be constructed from two chiral multiplets.

## Two-Chiral Multiplet Effective Potential

$$V_{\text{chiral}} = 4V_{\phi} + V_{\psi} = -\frac{3}{8\pi^2} H^2 m^2 \log(\varrho^2 m^2)$$

- Flat space contributions cancel, as they should.
- Non-vanishing contribution  $\propto H^2$  due to the curvature.

# Example

- Consider again  $t\bar{s}\bar{d}$ .
- Superpotential  $W$  contains  $W \supset h_t\bar{t}tH_u^0$ .
- Neglect other Yukawa couplings,  $h_t \gg h_s \gg h_d$ .
- Four real scalars from  $H_u^0$  and  $\tilde{t}_L$ .
- One Dirac fermion  $\begin{pmatrix} t_L \\ \tilde{H}_u^0 \end{pmatrix}$ .
- All these particles have the mass square  $|h_t\phi|^2$ .

## Lifting Potential

$$V_{\text{chiral}} = -\frac{3}{8\pi^2}H^2|h_t\phi|^2 \log(\varrho^2|h_t\phi|^2)$$

- $\varrho$  needs to be fixed by renormalization condition.
- Need to check whether also the gauge coupling  $g$  mediates lifting.

# Effective Potential for the Higgs Mechanism

- Need to add gauge boson  $A$ , Goldstone  $G$  and ghost  $\eta$  contributions. Gauge-fixing parameter  $\xi$ .

$$V_A = \text{tr} \left[ \frac{M^2}{8\pi^2 \varrho^2} (3 + \xi) + \frac{1}{64\pi^2} (3M^4 + 12H^2 M^2 + \xi^2 M^4 - 4H^2 \xi M^2) \log(\varrho^2 M^2) \right],$$

$$V_G = \text{tr} \left[ \frac{M_G^2}{8\pi^2 \varrho^2} \xi + \frac{1}{64\pi^2} (\xi^2 M_G^4 - 4H^2 \xi M_G^2) \log(\varrho^2 M_G^2) \right],$$

$$V_\eta = \text{tr} \left[ -\frac{M^2}{4\pi^2 \varrho^2} \xi - \frac{1}{64\pi^2} (2\xi^2 M^4 - 8H^2 \xi M^2) \log(\varrho^2 M^2) \right].$$

Using  $\text{tr} M_G^2 = \text{tr} M^2$ , we find the net result, which is independent of  $\xi$ :

$$V_{\text{gauge}} = V_A + V_G + V_\eta = \text{tr} \left[ \frac{3M^2}{8\pi^2 \varrho^2} + \frac{1}{64\pi^2} (3M^4 + 12H^2 M^2) \log(\varrho^2 M^2) \right]$$

First derived in Landau gauge,  $\xi = 0$ , by Allen (1982); Ishikawa (1982).

# Effective Potential for the Super-Higgs Mechanism

- Within SUSY, have additional fermionic contributions from Higgsinos/Gauginos.
  - One set of Dirac fermions with mass matrix  $M_\psi$  satisfying  $\text{tr}M_\psi^2 = \text{tr}M^2$ . Effective potential contribution  $V_\psi$ .
- And one set of real scalars with mass matrix  $M^2$  arising from the  $D$ -terms, yielding contribution  $V_D$ .

## Effective Potential for the Super-Higgs Mechanism

$$V_{\text{SH}} = V_{\text{gauge}} + V_D + V_\psi = 0$$

(disappointingly, up to possible corrections of order  $H^4$ )

- This completes the possible contributions to curvature-induced lifting.

# Spontaneous SUSY-breaking in $F$ -term inflation

- Superpotential

$$\kappa SX\bar{X} - \kappa SM^2 + \lambda SH_u H_d$$

During inflation  $\langle S \rangle \neq 0$ .

- For definiteness, calculate corrections due to  $H_u$  &  $H_d$ .
- In general,  $X$  and  $\bar{X}$  break a GUT-symmetry and also couple to the MSSM-fields.
- Higgs Bosons and Higgsinos, squarks and quarks acquire different masses.
- To be specific, we again consider the  $u\bar{d}\bar{d}$ -direction.  
Assume that  $\tilde{u}_R$  corresponds to the right handed stop  $\tilde{t}_R$ .  
Can then expand in terms of the top-quark Yukawa coupling  $h = h_t$ .

## Effective potential for the stop

$$\begin{aligned}
 V^{(1)}(\tilde{u}_R) = & \frac{\kappa^2 \lambda^2 M^4}{8\pi^2} \left[ \ln \left( \frac{\lambda^2 |S|^2}{Q^2} \right) - \frac{3}{2} \right] - \frac{1}{48\pi^2} \frac{h^2 \kappa^4 M^8}{\lambda^2 |S|^6} |\tilde{u}_R|^2 + \frac{1}{16\pi^2} \frac{h^4 \kappa^2 M^4}{\lambda^2 |S|^4} |\tilde{u}_R|^4 \\
 & + \frac{1}{16\pi^2} \left( \frac{h^2 \kappa^2 M^4}{\lambda^2 |S|^4} |\tilde{u}_R|^2 \right)^2 \ln \left( \frac{h^2 \kappa^2 M^4}{\lambda^4 |S|^6} |\tilde{u}_R|^2 \right) + \mathcal{O}(h^6 |\tilde{u}_R|^6)
 \end{aligned}$$

- The  $\tilde{u}_R$ -dependent terms are **independent of the renormalization scale  $Q$** .
- Unique vacuum expectation value

$$\langle \tilde{u}_R \rangle = \frac{\kappa}{\sqrt{6} h} M$$

- Unique mass term

$$M_{\tilde{u}_R}^2 = \frac{1}{24\pi^2} \frac{h^2 \kappa^4}{\lambda^2} M^2$$

# Summary

## Lifting induced by the curved background

- Mediated by Yukawa couplings.
- Typical lifting mass square term  $\sim h^2 H^2$ , where  $h$  is the largest Yukawa coupling of the constituents of the flat direction.
- First calculation of an effective potential in curved space, which is explicitly **independent of the gauge-fixing  $\xi$** .
- Within SUSY, no lifting mediated by the gauge coupling  $g$  to order  $H^2$ .
- Dependence on renormalization constant  $\rho$ .
- Leading correction in  $D$ -term models.

# Summary

## Lifting in $F$ -term hybrid inflation

- Unique minimum of the potential and mass  $\sim \frac{1}{24\pi^2} h^2 M^2 \gg H^2$ , where  $M$  is a GUT-scale mass.
- Independent on the renormalization scale  $Q$ .
- Dominant contribution within  $F$ -term hybrid inflation.