TeV Scale B-L extension of the Standard Model

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Introduction

• The SM, based on the gauge symmetry $SU(3)_C \times SU(2)_L \times U(1)_Y$, is in excellent agreement with experimental results.

• Three firm observational evidences of new physics beyond the Standard Model :

- 1. Neutrino Masses.
- 2. Dark Matter.
- 3. Baryon Asymmetry.

• These three problems may be solved by introducing right-handed neutrinos.

TeV Scale B-L

- The tremendous success of gauge symmetry in describing the SM indicates that any extension of the SM should be through the extension of its gauge symmetry.
- The minimal extension is based on the gauge group

 $G_{B-L} \equiv SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_{B-L}$

- This model accounts for the exp. results of the light neutrino masses
- New particles are predicted:
 - Three SM singlet fermions (right handed neutrinos) (cancellation of gauge anomalies)
 - Extra gauge boson corresponding to B–L gauge symmetry
 - Extra SM singlet scalar (heavy Higgs)
- These new particles have Interesting signatures at the LHC

$U(1)_{B-L}$ Model

- Under $U(1)_{B-L}$ we demand: $\psi_L \to e^{iY_{B-L}\theta(x)}\psi_L$, $\psi_R \to e^{iY_{B-L}\theta(x)}\psi_R$,
- Derivatives are covariant if a new gauge field C_{μ} is introduced:

Lagrangian: fermionic and kinetic sectors

$$L_{B-L} = i\bar{l}D_{\mu}\gamma^{\mu}l + i\bar{e}_{R}D_{\mu}e_{R} + i\bar{\nu}_{R}D_{\mu}\gamma^{\mu}\nu_{R} - \frac{1}{4}W_{\mu\nu}^{r}W^{r\mu\nu} - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}C_{\mu\nu}C^{\mu\nu}$$

Lagrangian: Higgs and Yukawa sectors

$$L_{\text{Higgs+Yukawa}} = (D_{\mu}\phi)(D^{\mu}\phi) + (D_{\mu}\chi)(D^{\mu}\chi) - V(\phi,\chi) - (\lambda_{e}\bar{l}\phi e_{R} + \lambda_{v}\bar{l}\phi\bar{v}_{R} + \frac{1}{2}\lambda_{v_{R}}\bar{v}_{R}^{c}\chi v_{R} + h.c.)$$

	l	V _R	e_R	q	u _R	d _R	ϕ	X
SU(1) _L x U(1) _Y	(2,-1/2)	(1,0)	(1,-1)	(2,1/6)	(1,2/3)	(1,1/3)	(2,1/2)	(1,0)
U(1) _{B-L}	-1	-1	-1	1/3	1/3	1/3	0	2

U(1)_{*B-L*} Symmetry Breaking

The U(1)_{B-L} gauge symmetry can be spontaneously broken by a SM singlet complex scalar field x:

$$\left|\left\langle \chi\right\rangle\right|=v'/\sqrt{2}$$

 The SU(2)_L×U(1)_Y gauge symmetry is broken by a complex SU(2) doublet of scalar field φ:

$$\left|\left\langle\phi\right\rangle\right| = v/\sqrt{2}$$

Most general Higgs potential:

$$V(\phi,\chi) = m_1^2 \phi^+ \phi + m_2^2 \chi^+ \chi + \lambda_1 (\phi^+ \phi)^2 + \lambda_2 (\chi^+ \chi)^2 + \lambda_3 (\phi^+ \phi) (\chi^+ \chi)$$

• For $V(\varphi, \chi)$ bounded from below, we require:

$$\lambda_3 > -2\sqrt{\lambda_1\lambda_2}, \quad \lambda_2, \lambda_1 \ge 0$$

• For non-zero local minimum, we require

 $\lambda_3^2 < 4\lambda_1\lambda_2$

U(1)_{*B-L*} Symmetry Breaking (Cont.)

Non-zero minimum:



- Interesting scale: $0 > \lambda_3 > -2\sqrt{\lambda_1 \lambda_2}$
- After the *B*-*L* gauge symmetry breaking, the gauge field C_{μ} acquires mass:

$$M_{z'}^2 = 4g''^2 v'^2$$

• Strongest Limit comes from LEP II: $\frac{M_{z'}}{g''} \approx O(TeV), \ g'' \approx O(1) \Rightarrow v' > O(TeV)$

B-L symmetry breaking scale.

• The scale of B- L symmetry breaking is unknown, ranging from TeV to much higher scales (GUT or Planck NP).

• In SUSY, the electroweak and SUSY breaking scale are nicely correlated through the mechanism of radiative breaking of the EW symmetry.

• Radiative corrections may drive the squared Higgs mass from positive initial values at the GUT scale to negative values at the EW scale.

• The size of the Higgs VEV responsible for the EW breaking is determined by the size of the top Yukawa coupling and of the soft SUSY breaking terms.

Analogously, in a SUSY see-saw scheme it is possible to radiatively induce the breaking of B-L having the scale of such breaking directly linked to the soft SUSY breaking scale.

SUSY and B-L radiative symmetry breaking. S.K., A. Masiero, 2007

$$W = (h_U)_{ij}Q_iH_2U_j^c + (h_D)_{ij}Q_iH_1D_j^c + (h_L)_{ij}L_iH_1E_j^c + (h_\nu)_{ij}L_iH_2N_j^c + (h_N)_{ij}N_i^cN_j^c\chi_1 + \mu H_1H_2 + \mu'\chi_1\chi_2.$$

$$\frac{dm_{\chi_1}^2}{dt} = 6\tilde{\alpha}_{B-L}M_{B-L}^2 - 2\tilde{Y}_{N_3}\left(m_{\chi_1}^2 + 2m_{N_3}^2 + A_{N_3}^2\right),$$

$$\frac{dm_{N_3}^2}{dt} = \frac{3}{2}\tilde{\alpha}_{B-L}M_{B-L}^2 - \tilde{Y}_{N_3}\left(m_{\chi_1}^2 + 2m_{N_3}^2 + A_{N_3}^2\right).$$

$$\mu'^2 = \frac{m_{\chi_2}^2 - m_{\chi_1}^2 \tan^2\theta}{\tan^2\theta - 1} - \frac{1}{4}M_{Z_{B-L}}^2.$$

$$\sin 2\theta = \frac{2\mu_3^2}{\mu_1^2 + \mu_2^2}.$$

TeV scale B-L from GUT

• **G**_{B-L} can be obtained from SO(10) in the following branching rule:

SO(10)↓ $SU(4)_{C} \times SU(2)_{L} \times SU(2)_{R}$ ↓ $SU(3)_{C} \times SU(2)_{L} \times U(1)_{Y} \times U(1)_{B-L}$ ↓ $SU(3)_{C} \times SU(2)_{L} \times U(1)_{Y} \times U(1)_{B-L}$ ↓ At TeV scale via (1,1,0,2) Higgs $SU(3)_{C} \times SU(2)_{L} \times U(1)_{Y}$

TeV scale B-L through SU(5)

 Another way to get (modified) G_{B-L} is to have the following breaking of SO(10) :

> SO(10) ↓ SU(5) × U(1)_{χ} ↓ SU(5) × U(1)_{χ} ↓ SU(3)_C × SU(2)_L × U(1)_Y× U(1)_{χ} ↓ SU(3)_C × SU(2)_L × U(1)_Y× U(1)_{χ} At TeV scale via (1,1) in 24_H At TeV scale via (1,1,0,2) Higgs

Neutrino masses and mixing

• Left and right-handed neutrino form 2x2 mass matrix:

$$\begin{pmatrix} 0 & m_D \\ m_D & M_R \end{pmatrix}$$

• M_R Majorana mass ($U(1)_{B-L}$ symmetry breaking)

$$M_R = \lambda_{\nu_R} \nu'$$
 $\nu' \sim O(TeV), \ \lambda_{\nu_R} \sim O(1) \Rightarrow M_R \approx O(TeV)$

□ *m_D* Dirac mass (Electroweak symmetry breaking)

$$m_D = h_v v$$

 $h_{\nu} \sim O(1) \Rightarrow m_D \approx O(100) GeV, h_{\nu} \sim h_e \Rightarrow m_D \approx O(10^{-4}) GeV$

Neutrino Masses (Cont.)

 we adopt the basis where the charged lepton mass matrix and the Majorana mass matrix *MR* are both diagonal.

$$M_R = M_{R_3} \begin{pmatrix} r_1 & 0 & 0 \\ 0 & r_2 & 0 \\ 0 & 0 & 1 \end{pmatrix},$$

Where

$$M_{R_3} = |\lambda_{\nu_{R_3}}| \frac{v'}{\sqrt{2}}$$

And

$$r_{1,2} = \frac{M_{R_{1,2}}}{M_{R_3}} = \left| \frac{\lambda_{\nu_{R_{1,2}}}}{\lambda_{\nu_{R_3}}} \right|.$$

 M_R is parameterized by 3 parameters ($v' \sim \text{TeV}$,) & m_D is given by 9 parameters.

 $U(1)_{B-L}$ can not impose any constraint to reduce the number of these parameters

Neutrino Masses (Cont.)

□ The solar & atmospheric neutrino oscillation experiments imply at the 3³/₄ level:

$$\Delta m_{12}^2 = (7.9 \pm 0.4) \times 10^{-5} \text{eV}^2,$$

$$|\Delta m_{32}^2| = (2.4 + 0.3) \times 10^{-3} \text{eV}^2,$$

$$\theta_{12} = 33.9^\circ \pm 1.6^\circ,$$

$$\theta_{23} = 45^\circ,$$

$$\sin^2 \theta_{13} \leq 0.048.$$

□ An interesting parameterization for the m_D is: $m_D = U_{MNS} \sqrt{m_{\nu}^{diag}} R \sqrt{M_R}$,

□ In order to fix the angles of R, one needs a favor symmetry.

Neutrino Masses (Cont.)

From the measured values of the quark and lepton masses:

$$\frac{m_u}{m_c} \sim \frac{m_e}{m_\mu} \sim O(10^{-3}), \qquad \qquad \frac{m_c}{m_t} \sim \frac{m_\mu^2}{m_\tau^2} \sim O(10^{-3})$$

In the event of a favor symmetry that explains these ratios, the down quark and neutrino sectors may also be subjected to this symmetry.

If the scale of this favor symmetry breaking (v_F) is below seesaw scale

$$\frac{m_d}{m_s} \sim \frac{m_{\nu_1}}{m_{\nu_2}} \sim O(10^{-2}) \qquad \qquad \frac{m_s}{m_b} \sim \frac{m_{\nu_2}^2}{m_{\nu_3}^2} \sim O(10^{-2}).$$

If the scale of the favor symmetry breaking is above the seesaw mechanism scale

$$\frac{m_d}{m_s} \sim \frac{m_{D_1}}{m_{D_2}} \sim O(10^{-2}) \qquad \qquad \frac{m_s}{m_b} \sim \frac{m_{D_2}^2}{m_{D_3}^2} \sim O(10^{-2})$$

In case v_F <v'

$$m_{\nu} \simeq 0.05 \ eV \left(\begin{array}{ccc} 10^{-3} & 0 & 0 \\ 0 & 0.16 & 0 \\ 0 & 0 & 1 \end{array} \right)$$

Consistent with the hierarch

0

Consistent with the hierarchal ansatz with $m_{\gamma 1} \sim 10^{-4}$

The Dirac neutrino mass matrix (for $r_1 \sim r_2 \sim 0.1$, $M_{R3} = 5$ TeV, and order one angles/phases of *R*-matrix) is given by:

•

$$m_D \simeq 10^{-3} \begin{pmatrix} 0.16 + 0.23 \ i & -0.25 + 0.16 \ i & -0.19 - 0.26 \ i \\ -0.22 - 0.34 \ i & 0.37 - 0.24 \ i & 0.30 + 0.38 \ i \\ -0.14 + 0.47 \ i & -0.53 - 0.15 \ i & 0.16 - 0.68 \ i \end{pmatrix}$$

$Z_{R,I}$ Decay

The interactions of the Z' boson with the SM fermions are described by \triangleright



 $Z' \rightarrow q\bar{q} BR = 10\%$

- Branching ratios of $Z' \rightarrow /''$ are relatively high compared to $Z' \rightarrow qq$. \triangleright
- Search for Z' at LHC via dilepton channels are \triangleright accessible at LHC.

Z_{B-L} Discovery at LHC

Emam, Mine, 2008

In case of g" ~ O(0.1) then M_{ZB-L} ~ O(600) GeV

In LHC, the neutral gauge boson Z_{B-L} can be produced through $q \overline{q} \rightarrow Z_{B-L}$

The SM background for this production consists mostly of the Drell-Yan process

$$q\overline{q} \rightarrow \gamma / Z^0 \rightarrow e^+ e^-$$

Therefore, one expects a clear peak at M_{ZB-L} boson in the M_{e+e-} distribution

 Z_{B-L} boson could be discovered in the e+e- decay channel in the mass region 800<M_z < 1000 GeV with an integrated luminosity of 10 fb⁻¹.



Higgs Sector

- One complex $SU(2)_L$ doublet and one complex scalar singlet
- Six scalar degrees of freedom
- **•** Four are eaten by *C*,*Z*⁰,*W*[±] after symmetry breaking
- Two physical degrees of freedom: φ , χ

Mass matrix:
$$\frac{1}{2}M^{2}(\phi,\chi) = \begin{pmatrix} \lambda_{1}v^{2} & \lambda_{3}vv'/2\\ \lambda_{3}vv'/2 & \lambda_{2}v'^{2} \end{pmatrix}$$

Mass eigenstates:

•

$$\begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \phi \\ \chi \end{pmatrix}, \quad \tan 2\theta = \frac{|\lambda_3|vv'}{\lambda_1 v^2 - \lambda_2 v'^2}$$

- Masses: $m_{1,2}^2 = \lambda_1 v^2 + \lambda_2 v'^2 \mp \sqrt{(\lambda_1 v^2 \lambda_2 v'^2)^2 + \lambda_3^2 v^2 v'^2}$
- Mixing is controlled by λ_3 : $\lambda_3 = 0 \rightarrow m_{\phi} = \sqrt{\lambda_1} v$, $m_{\psi} = \sqrt{\lambda_2} v'$

Higgs Sector (Cont.)

Couplings to fermions and gauge bosons



Higgs Sector (Cont.)

Self-couplings

$$\phi_{1} \qquad \phi_{1} \qquad g_{\phi_{1}^{3}} = 6i(\lambda_{1}v\cos^{3}\theta - \lambda_{3}v'\cos^{2}\theta\sin\theta/2) \qquad \phi_{1} \qquad g_{\phi_{1}^{4}} = 6i\lambda_{1}\cos^{4}\theta$$

$$\phi_{2} \qquad \phi_{2} \qquad g_{\phi_{2}^{3}} = 6i(\lambda_{2}v'\cos^{3}\theta + \lambda_{3}v\cos^{2}\theta\sin\theta/2) \qquad \phi_{2} \qquad \phi_{2} \qquad g_{\phi_{2}^{4}} = 6i\lambda_{2}\cos^{4}\theta$$

$$\phi_{1} \qquad \phi_{2} \qquad \phi_{2} \qquad g_{\phi_{1}^{2}} = 2i(\lambda_{3}v\cos^{3}\theta/2 + \lambda_{3}v'\cos^{2}\theta\sin\theta - 3\lambda_{2}v'\cos^{2}\theta\sin\theta)$$

$$\phi_{2} \qquad \phi_{2} \qquad g_{\phi_{1}^{2}\phi_{2}^{2}} = 2i(\lambda_{3}v'\cos^{3}\theta/2 - \lambda_{3}v\cos^{2}\theta\sin\theta + 3\lambda_{1}v\cos^{2}\theta\sin\theta)$$

$$\phi_{2} \qquad \phi_{3} \qquad g_{\phi_{1}^{2}\phi_{2}^{2}} = i\lambda_{3}\cos^{4}\theta$$





m_µ(GeV)

Signatures for $v_{\rm R}$ at the LHC

$$\mathcal{L}_{int.} \sim -g^{"}C_{\mu}[(\overline{\nu_{R}})_{i}\gamma^{\mu}(\nu_{R})_{i} + b_{ij}\overline{(\nu_{L})^{c}}_{i}\gamma^{\mu}(\nu_{R})_{j} + h.c.]$$

+ $\frac{g_{2}}{\sqrt{2}}[W_{\mu}^{-}l_{i}^{+}\gamma^{\mu}U_{ij}(\nu_{L})_{j} + b_{ij}W_{\mu}^{-}l_{i}^{+}\gamma^{\mu}(\nu_{R})_{j}^{c} + h.c.],$



These decays are very clean with four hard leptons in the final states and large missing energy due to the associated neutrinos.



Integrated luminosity ~ 300 fb⁻¹ gives 71 events for the right handed neutrino mass of 200 GeV while it gives 46 events for the right handed neutrino mass of 400 GeV.

Leptogenesis in B-L Extension

□ The recent observations lead to the following baryon asymmetry in the Universe

$$Y_B = \frac{n_B - n_{\bar{B}}}{s} = \frac{n_B}{s} = (6.3 \pm 0.3) \times 10^{-10},$$

□ This asymmetry may be originate through the CP violating decay of the heavy right-handed neutrino is an interesting mechanism known as Leptogenesis

$$u_{R_i}
ightarrow \phi + l_lpha$$

 \Box The lepton asymmetry is usually dominated by v_{R1}

$$\varepsilon_{1} = \frac{\sum_{\alpha} \left(\left| A(\nu_{R_{1}} \to \phi \ l_{\alpha}) \right|^{2} - \left| A(\nu_{R_{1}} \to \bar{\phi} \ \bar{l}_{\alpha}) \right|^{2} \right)}{\sum_{\alpha} \left(\left| A(\nu_{R_{1}} \to \phi \ l_{\alpha}) \right|^{2} + \left| A(\nu_{R_{1}} \to \bar{\phi} \ \bar{l}_{\alpha}) \right|^{2} \right),$$



SM like right-handed neutrino decay through tree, vertex, and self-energy diagrams



B-L new contributions through diagrams mediated by extra Higgs and extra gauge boson.

The tree level contribution is given by

$$A_0(\nu_{R_1} \to \phi \ l_\alpha) = -i(\lambda_\nu)_{\alpha 1} \Big(\bar{u}(p) \ P_R \ u^c(q) \Big),$$

The contribution to the decay amplitude from the vertex correction is given by

$$A_V(\nu_{R_1} \to \phi \ l_\alpha) = \frac{i}{16\pi^2} \sum_i (\lambda_\nu)_{\alpha i} (\lambda_\nu^\dagger \lambda_\nu)_{1i} \Big(\bar{u}(p) \ P_R \ u^c(q) \Big) \ F_V \left(\frac{M_{R_i}^2}{M_{R_1}^2} \right).$$

The self-energy diagram leads to the following contribution:

$$A_S(\nu_{R_1} \to \phi \ l_\alpha) = \frac{i}{16\pi^2} \sum_i (\lambda_\nu)_{\alpha i} (\lambda_\nu^\dagger \lambda_\nu)_{1i} \Big(\bar{u}(p) \ P_R \ u^c(q) \Big) \ F_S\left(\frac{M_i^2}{M_{R_1}^2}\right),$$

The extra Higgs contribution is given by

$$A_{\chi}(\nu_{R_1} \to \phi \ l_{\alpha}) = \frac{1}{16\pi^2 M_{R_1}} (\lambda_{\nu_R})_{11} (\lambda_{\nu})_{1\alpha} \ g_{\phi^2 \chi} \ (\bar{u}(p) \ P_R \ u^c(q)) \ F_{\chi}\left(\frac{M_{\chi}^2}{M_{R_1}^2}\right).$$

Finally, the extra gauge boson contribution is

$$A_{Z'}(\nu_{R_1} \to \phi \ l_{\alpha}) = \frac{1}{4\pi^2} g''^2(\lambda_{\nu})_{\alpha 1} \left(\bar{u}(p) P_R u^c(q)\right) \ F_{Z'}\left(\frac{M_{z'}^2}{M_{R_1}^2}\right),$$

Some Remarks:

1- The loop functions $F_V \& F_s$ are complex while $F_\chi \& F_{Z'}$ are real. New Contributions interface with SM one loop amplitudes only, so their impacts are small.

$$Im \ F_S(x) = \frac{\sqrt{x}}{1-x}.$$

In the limit of quasi-degenerate right-handed neutrinos, $x \sim 1$, a resonant enhancement for the lepton asymmetry is obtained.

3- The coupling $g_{\phi^2\chi}$ is real since $g_{\phi^2\chi} = \sqrt{2}v'\lambda_3$. However, $(\lambda_{\nu_R})_{11} = \frac{2\sqrt{2}M_{R_1}}{v'} e^{i\phi_1}$.

4- Since the coupling g' is real the Z' contribution can be considered as correction to the tree level contribution.

If the new contributions are neglected, the lepton asymmetry is given by

$$\varepsilon_1^{\rm SM} \simeq \frac{1}{8\pi} \frac{1}{(\lambda_\nu^\dagger \lambda_\nu)_{11}} \sum_{i=2,3} \operatorname{Im}\left\{ (\lambda_\nu^\dagger \lambda_\nu)_{1i}^2 \right\} \left[\operatorname{Im} F_V\left(\frac{M_{R_i}^2}{M_{R_1}^2}\right) + \operatorname{Im} F_S\left(\frac{M_{R_i}^2}{M_{R_1}^2}\right) \right].$$

> Therefore, the necessary condition for leptogenesis is

$$\operatorname{Im}\left(\lambda_{\nu}^{\dagger}\lambda_{\nu}\right)_{1i} \neq 0 \Rightarrow \operatorname{Im}\left(\sqrt{M_{R}} \ R \ m_{\nu}^{\operatorname{diag}}R^{+}\sqrt{M_{R}}\right) \neq 0, \ i=2,3.$$

 \geq Due to the unitarity of U_{MNS}, leptogenesis does not depend on low energy phase appears in the leptonic mixing matrix.

> If the matrices R and M_R are real the $\epsilon_1 = 0$

In B-L extension of the SM, the lepton asymmetry is given by

$$\varepsilon_{1} \simeq \frac{1}{8\pi (\lambda_{\nu}^{\dagger} \lambda_{\nu})_{11}} \sum_{i=2,3} \left[\frac{\operatorname{Im}\{(\lambda_{\nu}^{\dagger} \lambda_{\nu})_{1i}^{2}\}}{\left(1 - \frac{1}{4\pi^{2}} g''^{2} F_{Z'} \left(\frac{M_{z'}^{2}}{M_{R_{1}}^{2}}\right) - \frac{1}{4\pi^{2}} \lambda_{3} F_{\chi} \left(\frac{M_{\chi}^{2}}{M_{R_{1}}^{2}}\right)\right)} \right] \\ \left[\operatorname{Im} F_{V} \left(\frac{M_{R_{i}}^{2}}{M_{R_{1}}^{2}}\right) + \operatorname{Im} F_{S} \left(\frac{M_{R_{i}}^{2}}{M_{R_{1}}^{2}}\right) \right].$$

Thermal leptogenesis is realized by the out of equilibrium of v_{R1} at temperature below its mass scale.

To avoid washing out the asymmetry ϵ_1 by inverse decay and scattering processes, the total width of ν_{R1} decay should be smaller than the expansion rate of the universe at temperature T = M_{R1}.



Summary

- The SM gauge group can be minimally extended by adding $U(1)_{B-L}$
- G_{B-L} contains three right handed neutrinos, extra gauge boson, and extra scalar Higgs.
- Neutrino masses and mixing can be accommodate in this type of models.
- Search for Z' at LHC via dilepton channels is promising.
- Extra Higgs phenomenology at LHC has been studied.
 - Only production is affected, cross-sections are reduced by about 25-40 % at the interesting mass range of $100 < m_H < 250$.
 - Decay Branching ratios are not affected.
- We explore the signature for a right handed neutrino at the LHC.
- We computed the new contributions to the CP violating decay of right handed neutrino to Higgs and leptons, due to the extra Higgs and extra gauge boson.
- Successful baryogenesis can be obtained by resonance leptogenesis.