

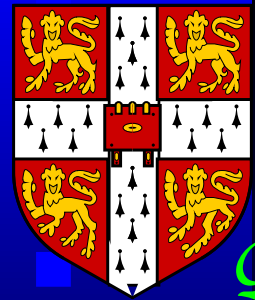
# Phenomenology of SUSY Breaking

by

Ben Allanach (University of Cambridge)

## Talk outline

- Current constraints on SUSY breaking
- Flavour violation
- R-parity violation
- LHC constraints on SUSY breaking



# Global SUSY Fits

Q: Why perform global fits to SUSY using DM+indirect data?

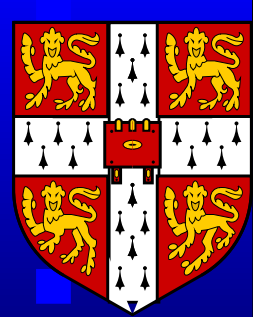




# Global SUSY Fits

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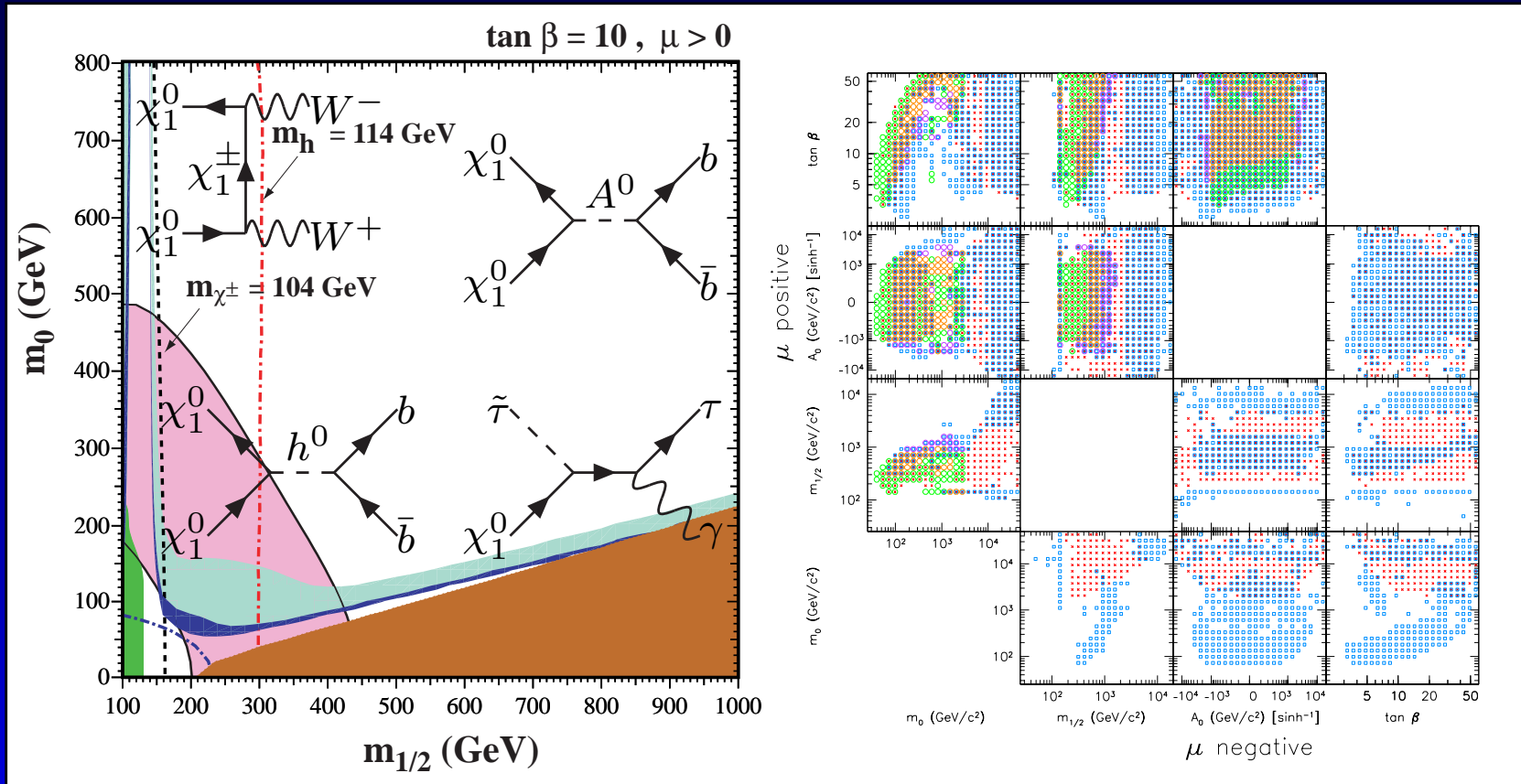




# Constraints on SUSY Models

CMSSM well-studied in literature: eg Ellis, Olive *et al* PLB565

(2003) 176; Roszkowski *et al* JHEP 0108 (2001) 024; Baltz, Gondolo, JHEP 0410 (2004) 052;...



# Implementation

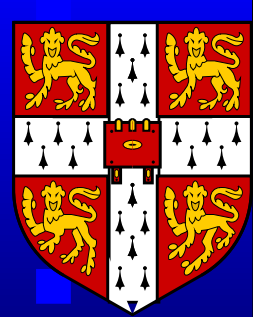
25 pMSSM input parameters are:  $M_{1,2,3}$ ,  $A_{t,b,\tau,\mu}$ ,  $m_{H_{1,2}}$ ,  $\tan \beta$ ,

$m_{\tilde{d}_{R,L}} = m_{\tilde{s}_{R,L}}$ ,  $m_{\tilde{u}_{R,L}} = m_{\tilde{c}_{R,L}}$ ,  $m_{\tilde{e}_{R,L}} = m_{\tilde{\mu}_{R,L}}$ ,  $m_{\tilde{t},\tilde{b},\tilde{\tau}_{R,L}}$

$m_t, m_b(m_b) \alpha_s(M_Z)^{\overline{MS}}$ ,  $\alpha^{-1}(M_Z)^{\overline{MS}}$ ,  $M_Z$ . We use

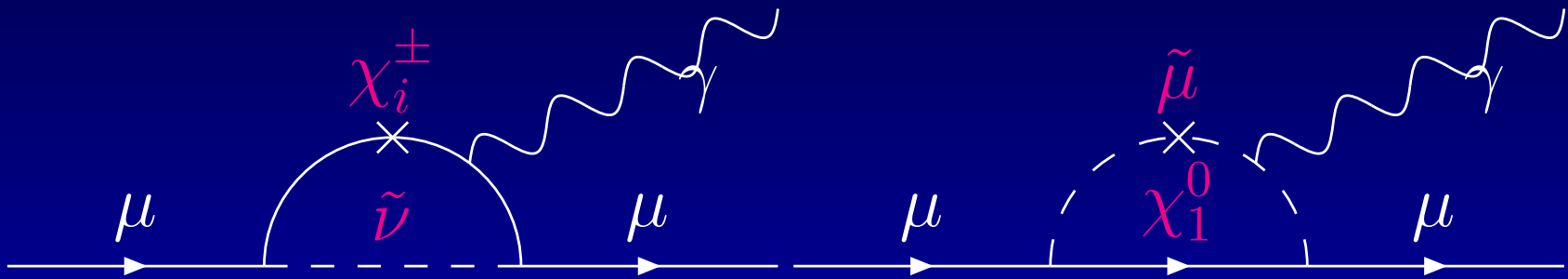
- 95% C.L. direct search constraints
- $\Omega_{DM} h^2 = 0.1143 \pm 0.02$  Boudjema *et al*
- $\delta(g - 2)_\mu/2 = (29.5 \pm 8.8) \times 10^{-10}$  Stöckinger *et al*
- $B$ -physics observables including  
 $BR[b \rightarrow s\gamma]_{E_\gamma > 1.6 \text{ GeV}} = (3.52 \pm 0.38) \times 10^{-4}$
- Electroweak data W Hollik, A Weber *et al*

$$2 \ln \mathcal{L} = - \sum_i \chi_i^2 + c = \sum_i \frac{(p_i - e_i)^2}{\sigma_i^2} + c$$

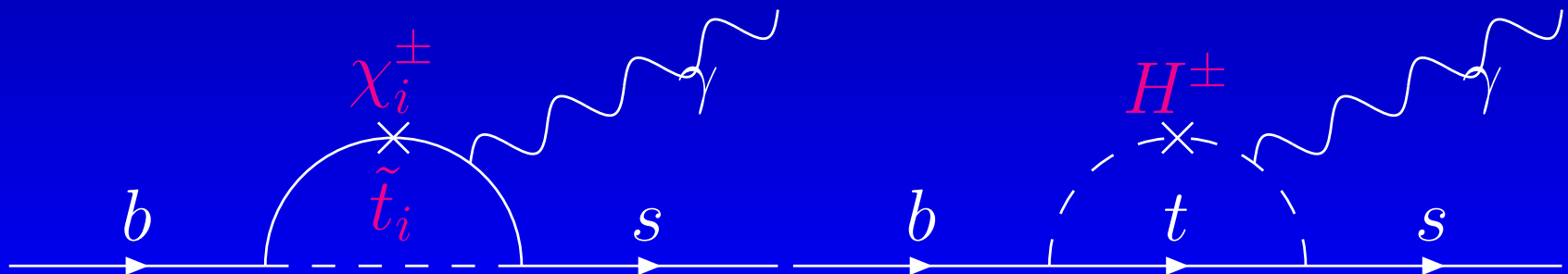


# Additional observables

$$\delta \frac{(g-2)_\mu}{2} \sim 13 \times 10^{-10} \left( \frac{100 \text{ GeV}}{M_{SUSY}} \right)^2 \tan \beta$$



$$BR[b \rightarrow s\gamma] \propto \tan \beta (M_W/M_{SUSY})^2$$





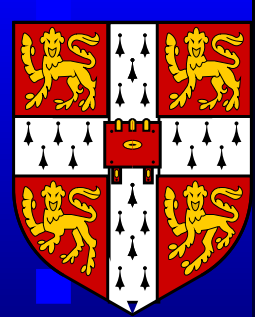
# Application of Bayes'

$\mathcal{L} \equiv p(\underline{d}|\underline{m}, H)$  is pdf of reproducing data  $\underline{d}$  assuming pMSSM hypothesis  $H$  and model parameters  $\underline{m}$

$$p(\underline{m}|\underline{d}, H) = p(\underline{d}|\underline{m}, H) \frac{p(\underline{m}, H)}{p(\underline{d}, H)}$$

$p(\underline{m}|\underline{d}, H)$  is called the **posterior** pdf. We will compare  $p(\underline{m}, H) = c$  with a **different** prior.

$$p(m_0, M_{1/2}|\underline{d}, H) = \int d\underline{o} p(m_0, M_{1/2}, \underline{o}|\underline{d}, H)$$



# Likelihood and Posterior

Q: What's the chance of observing someone to be pregnant, given that they are female?



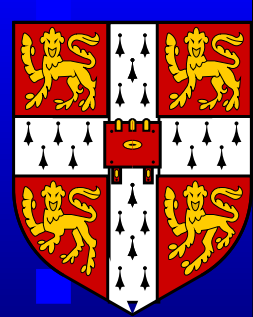
Likelihood

$$p(\text{pregnant} \mid \text{female, human}) = 0.01$$

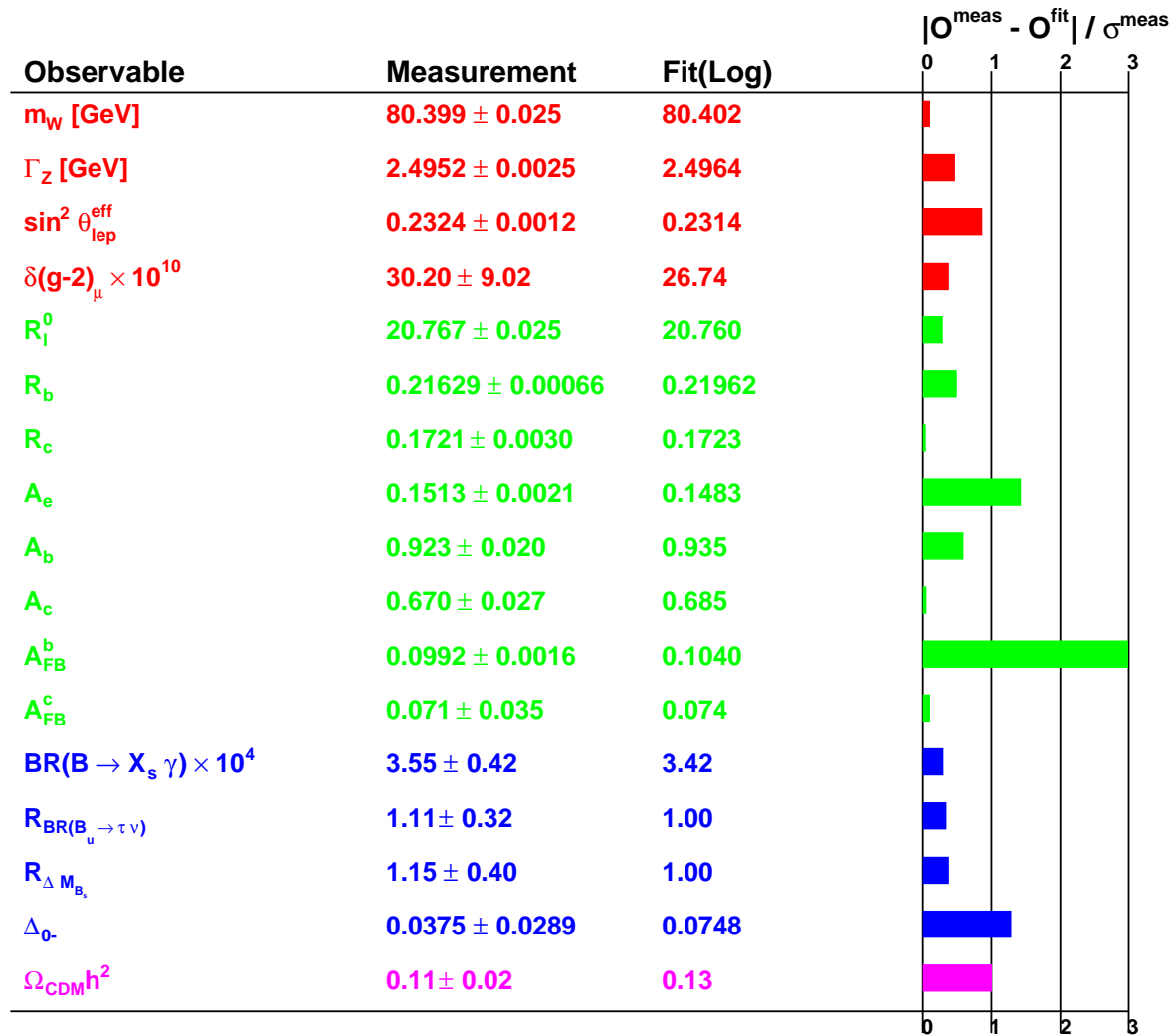
Posterior

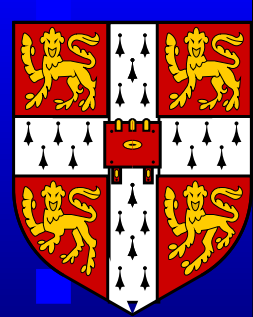
$$p(\text{female} \mid \text{pregnant, human}) = 1.00$$



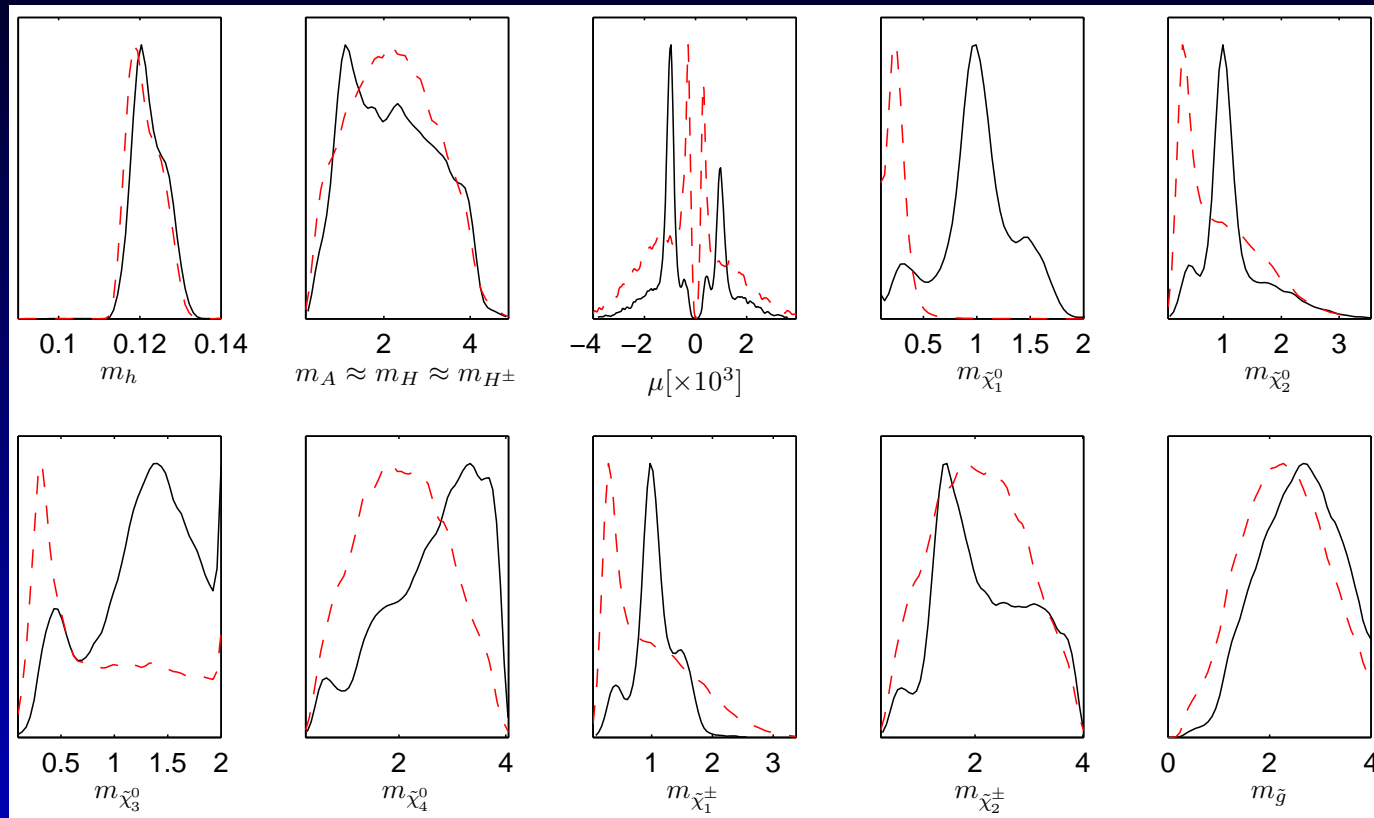


# Best-Fit Point



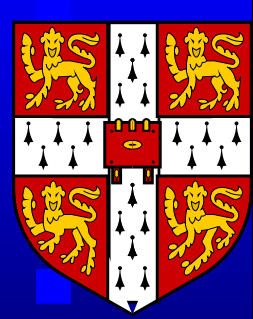


# Spectrum

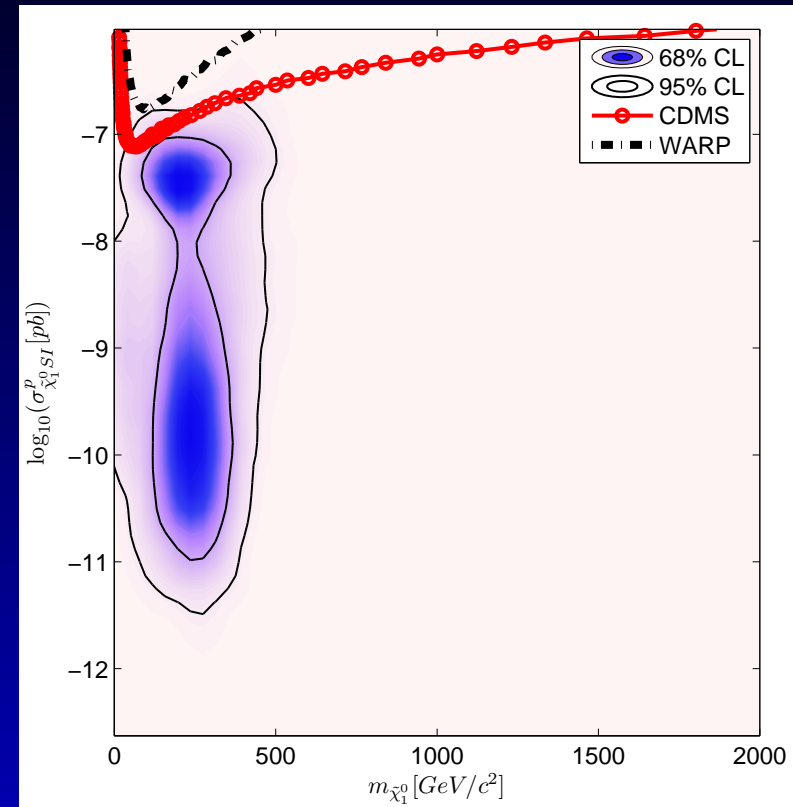
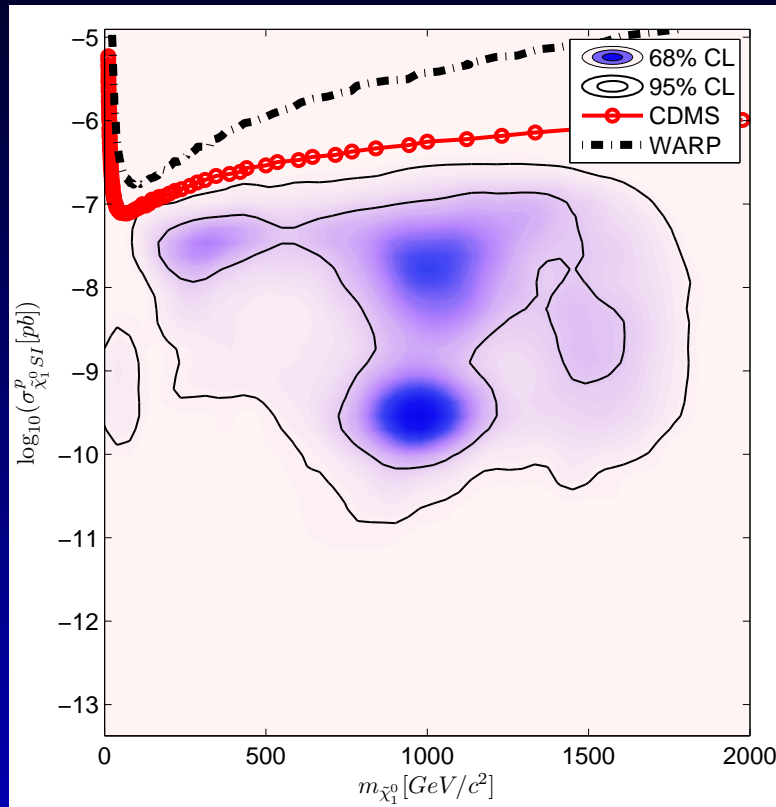


Obtained with MultiNest<sup>a</sup> algorithm in 16 CPU years. Prior dependence is *useful*: which predictions are **robust**?

<sup>a</sup>Feroz, Hobson [arxiv:0704.3704](https://arxiv.org/abs/0704.3704)

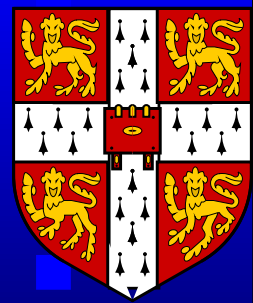


# Dark matter detection



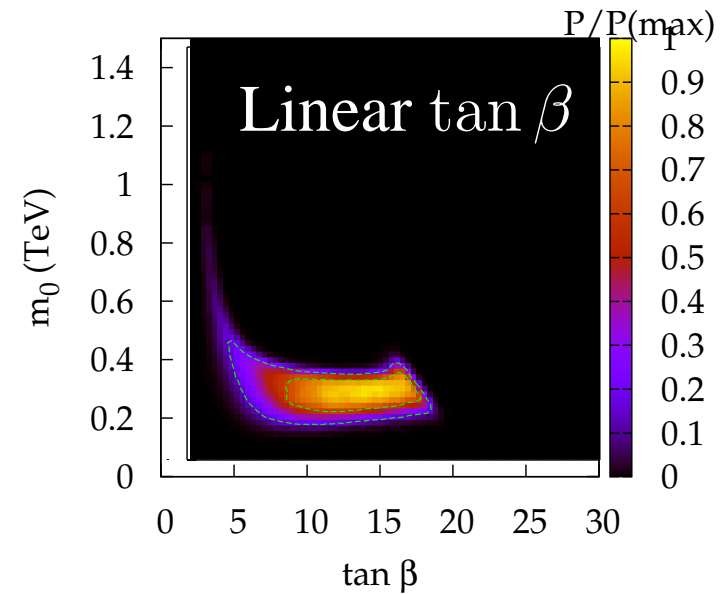
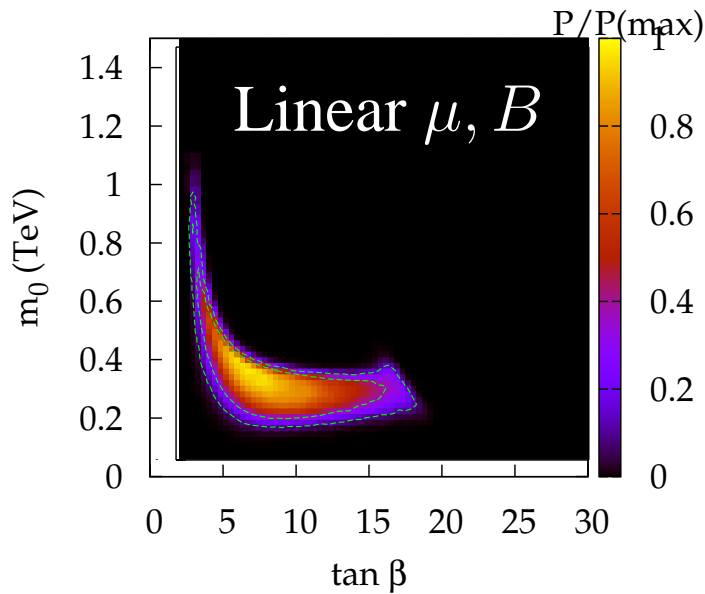
DM properties look too prior dependent to say anything concrete





# Large Volume String Models

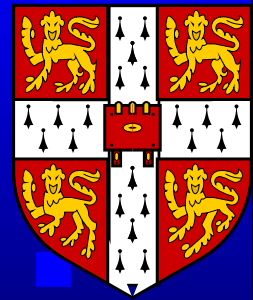
BCA, Dolan, JHEP08 (2008) 015, arXiv:0806.1184



$$M_{1/2} = -A_0 = m_0/\sqrt{3}$$

$$M_X = 10^{11} \text{ GeV}$$

Two constraints almost enough



# Model Comparison

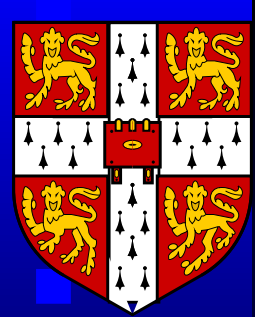
Calculate the *Bayesian evidence* of each model

$$\mathcal{Z}_i = \int p(\underline{d}|\underline{m}, H_i) p(\underline{m}|H_i) d\underline{m}$$

$$\frac{p(H_1|\underline{d})}{p(H_0|\underline{d})} = \frac{p(\underline{d}|H_1)p(H_1)}{p(\underline{d}|H_0)p(H_0)} = \frac{\mathcal{Z}_1 p(H_1)}{\mathcal{Z}_0 p(H_0)},$$

$p_i/p_{\text{mSUGRA}}^{\text{lin}}$	asymmetric <sup>a</sup> $\mathcal{L}_{\text{DM}}$		
Model/Prior	linear	log	flat $\mu, B$
mSUGRA	1	3	4
mAMSB	164	403	148
LVS	18	20	22

# Any Questions?





# Flavour Violating SUSY

In the MSSM, we additionally have soft mass terms like

$$V_2 = \tilde{Q}_{iLa}^* (m_{\tilde{Q}}^2)_{ij} \tilde{Q}_{jL}^a + \tilde{u}_{iR} (m_{\tilde{u}}^2)_{ij} \tilde{u}_{jR}^* + \tilde{d}_{iR} (m_{\tilde{d}}^2)_{ij} \tilde{d}_{jR}^*.$$

SUSY flavour problem: *Nearly all of this parameter space is ruled out by flavour constraints.*

There is clearly a need for some organising principle from symmetry and/or additional dynamics.

There are many approaches to the flavour problem in SUSY breaking (eg mSUGRA, GMSB,  $\tilde{g}$ MSSB, MRSSM<sup>a</sup> etc)

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<sup>a</sup>Kribs, Poppitz, Weiner, arXiv:0712.2039

# Anomaly Mediated SUSY Breaking

Loop suppressed soft masses<sup>a</sup>

$$M_\alpha = m_{3/2} \beta_{g_\alpha} / g_\alpha,$$

$$(m^2)^i_j = \frac{1}{2} m_{3/2}^2 \mu \frac{d}{d\mu} \gamma^i_j,$$

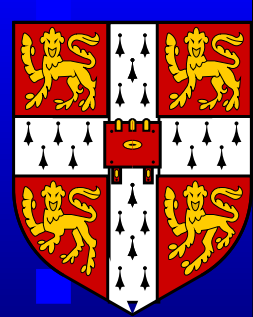
$$\gamma^i_j = \frac{1}{2} Y^{ikl} Y_{jkl} - 2 \sum_\alpha g_\alpha^2 [C(R_\alpha)]^i_j.$$

- Always present for a **hidden sector**
- **Dominant** in brane set-up:

$$\mathcal{L} = \mathcal{L}_{vis} + \mathcal{L}_{hid}$$

- **SUSY Flavour problem ameliorated**





# SUSY Breaking Terms

Scale **invariant** expressions<sup>a</sup> in terms of SUSY couplings and **gravitino mass**  $m_{3/2}$ .

$$M_i = \beta_i \frac{g_i^2}{16\pi^2} m_{3/2}, \quad \beta_i = (33/5, 1, -3)$$

$$m_{\tilde{u}_R, \tilde{c}_R}^2 = \frac{m_{3/2}^2}{(16\pi^2)^2} \left( -\frac{88}{25} g_1^4 + 8g_3^4 \right)$$

$$m_{\tilde{e}_R}^2 = -\frac{198}{25} \frac{m_{3/2}^2 g_1^4}{(16\pi^2)^2}$$

**Q:** What makes the slepton mass squared values positive?

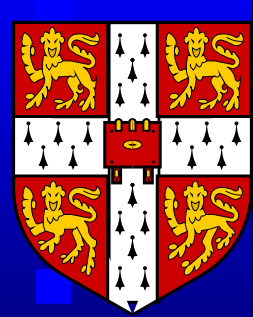
<sup>a</sup>[Gherghetta, Giudice and Wells, hep-ph/9904378](#)



# Solving Tachyonic Sleptons

- Bulk singlet contributions  $m_0$ : mAMSB
- Non-decoupling effects:
  - Katz, Shadmi, Shirman
  - Pomarol, Rattazzi
- Extra D-terms from additional U(1): Jack, Jones
- Extra (heavy) leptons: Chacko *et al*
- $R_p$  Violation: BCA, Dedes

Here, we shall consider the squark mixings, and therefore only the models which leave the squarks' AMSB terms untouched (in some cases, approximately and in some exactly).



# Flavoured AMSB

Previous literature only considers (33) entries to Yukawas. We include flavour corrections, e.g.

$$\frac{(16\pi^2)^2 (m_{\tilde{Q}}^2)^T}{m_{3/2}^2} = \left( -\frac{11}{50}g_1^4 - \frac{3}{2}g_2^4 + 8g_3^4 \right) \cdot 1 +$$
$$(Y_U Y_U^\dagger) \left( 3\text{Tr}(Y_U Y_U^\dagger) - \frac{13}{15}g_1^2 - 3g_2^2 - \frac{16}{3}g_3^2 \right) +$$
$$(Y_D Y_D^\dagger) \left( 3\text{Tr}(Y_D Y_D^\dagger) + \text{Tr}(Y_E Y_E^\dagger) - \frac{7}{15}g_1^2 - 3g_2^2 - \frac{16}{3}g_3^2 \right)$$
$$+ Y_U Y_U^\dagger Y_D Y_D^\dagger + Y_D Y_D^\dagger Y_U Y_U^\dagger + 3(Y_U Y_U^\dagger)^2 + 3(Y_D Y_D^\dagger)^2.$$

NB *Extremely predictive*. We'll use this to predict squark mixing

# Dominant Third Family Ap- proximation

$$\left(m_{\tilde{U}_L}^2\right)_{ij} = \frac{m_{3/2}^2}{(16\pi^2)^2} \left[ \delta_{ij} \left( -\frac{11}{50}g_1^4 - \frac{3}{2}g_2^4 + 8g_3^4 \right) \right.$$

$$+ \delta_{i3}\delta_{j3}\lambda_t^2(\hat{\beta}_{\lambda_t} - \lambda_b^2)$$

$$+ V_{ib}V_{jb}^*\lambda_b^2(\hat{\beta}_{\lambda_b} - \lambda_t^2)$$

$$+ \lambda_t^2\lambda_b^2(\delta_{i3}V_{jb}^*V_{tb} + \delta_{j3}V_{ib}V_{tb}^*) \Big],$$

$$\hat{\beta}_{\lambda_t} = 6\lambda_t^2 + \lambda_b^2 - \left( \frac{13}{15}g_1^2 + 3g_2^2 + \frac{16}{3}g_3^2 \right),$$

$$\hat{\beta}_{\lambda_b} = 6\lambda_b^2 + \lambda_\tau^2 + \lambda_t^2 - \left( \frac{7}{15}g_1^2 + 3g_2^2 + \frac{16}{3}g_3^2 \right).$$

in the super-CKM basis.  $\beta_i < 0$ . **NB at low**  
 $\tan\beta, \hat{\beta}_{\lambda_t}, \lambda_b \rightarrow 0$  : **AMSB is flavour conserving.**

$$(\delta_{ij}^u)_{LL} \equiv m_{\tilde{u}_{Lij}}^2 / \sqrt{m_{\tilde{u}_{Lii}}^2 + m_{\tilde{u}_{Ljj}}^2}$$

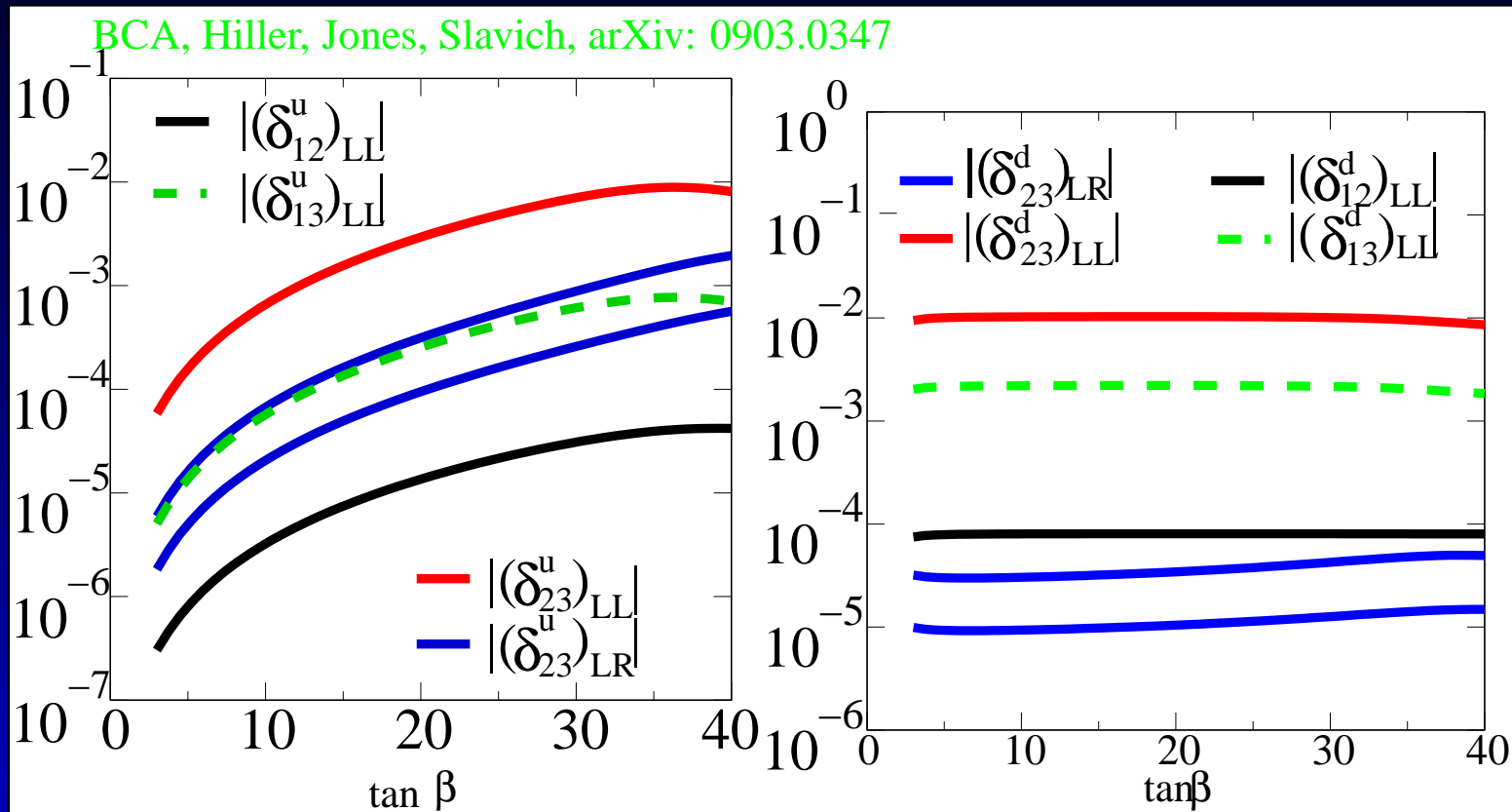
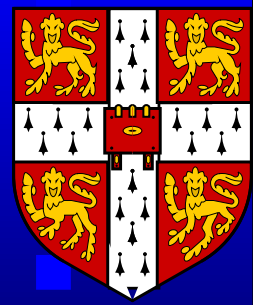


Figure 1: Largest flavour violating parameters for  $m_{3/2} = 40 - 140$  TeV. Note that  $\delta_{23}^d$  can affect  $b \rightarrow s$ .

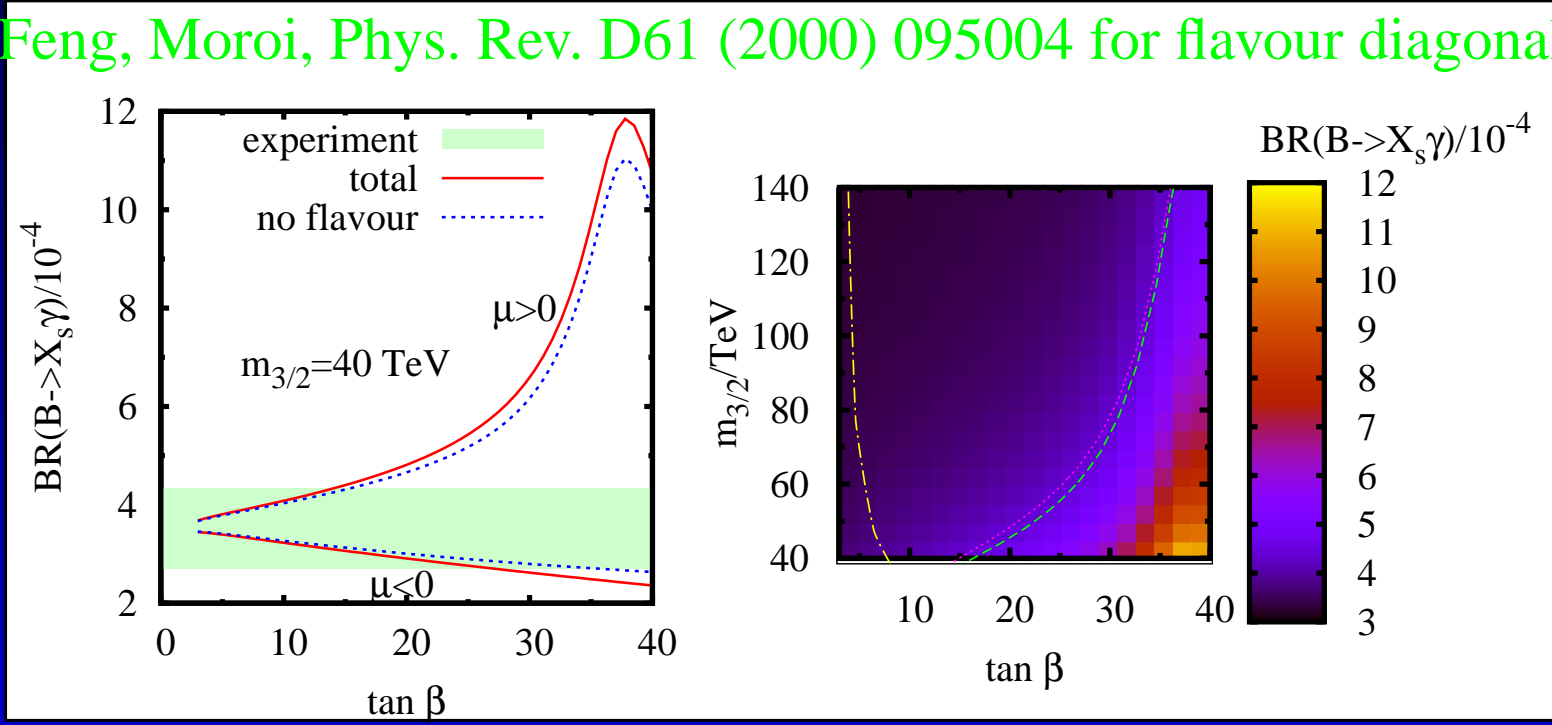


# $BR(B \rightarrow X_s \gamma)$

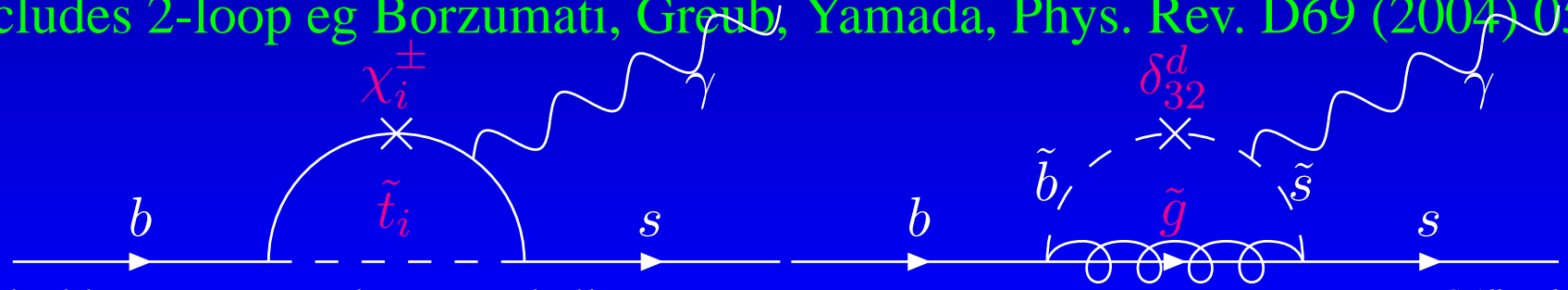
$m_{3/2} = 40$  TeV. **SOFTSUSY3.0** and **SusyBSG1.2**.

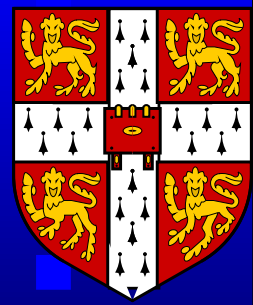
$$BR^{exp} = (3.52 \pm 0.23 \pm 0.09) \times 10^{-4},$$

See Feng, Moroi, Phys. Rev. D61 (2000) 095004 for flavour diagonal AMSB



Includes 2-loop eg Borzumati, Greub, Yamada, Phys. Rev. D69 (2004) 055005



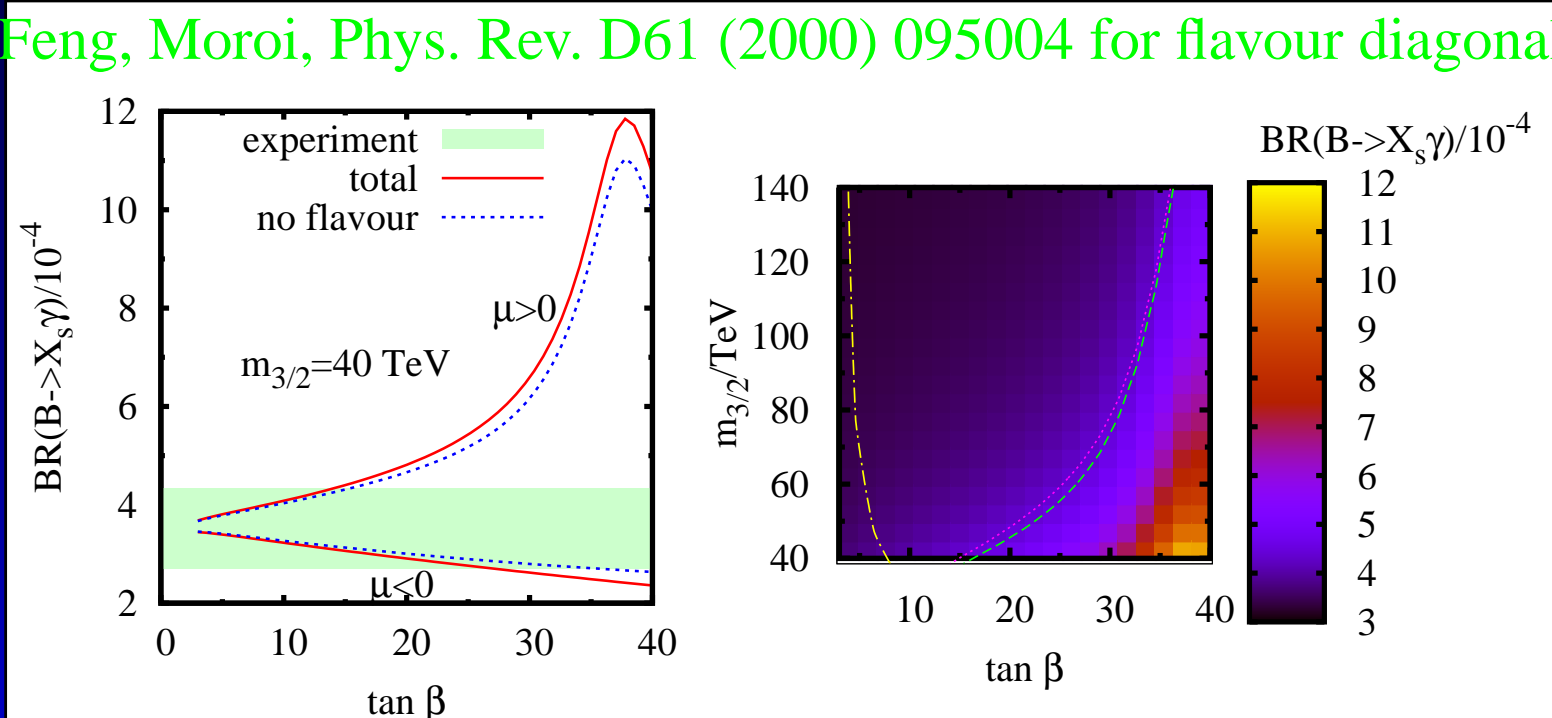


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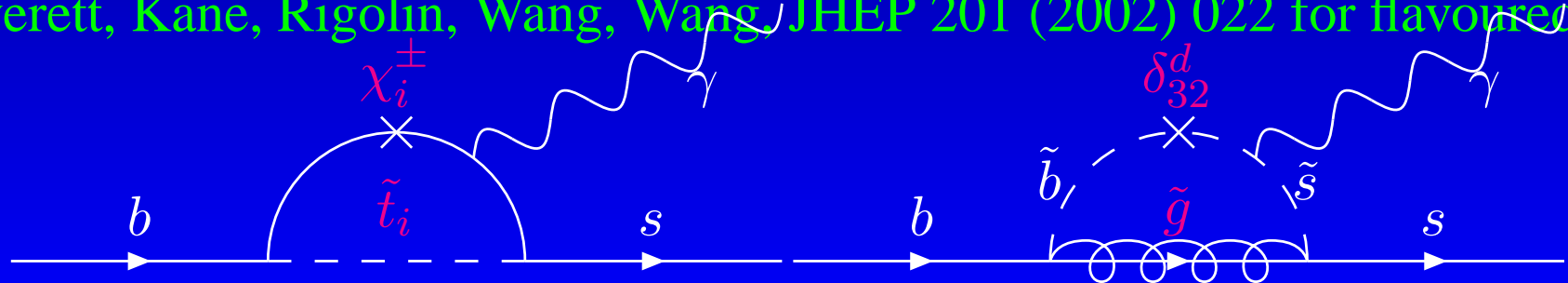
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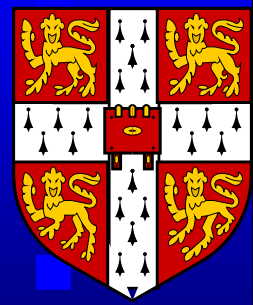
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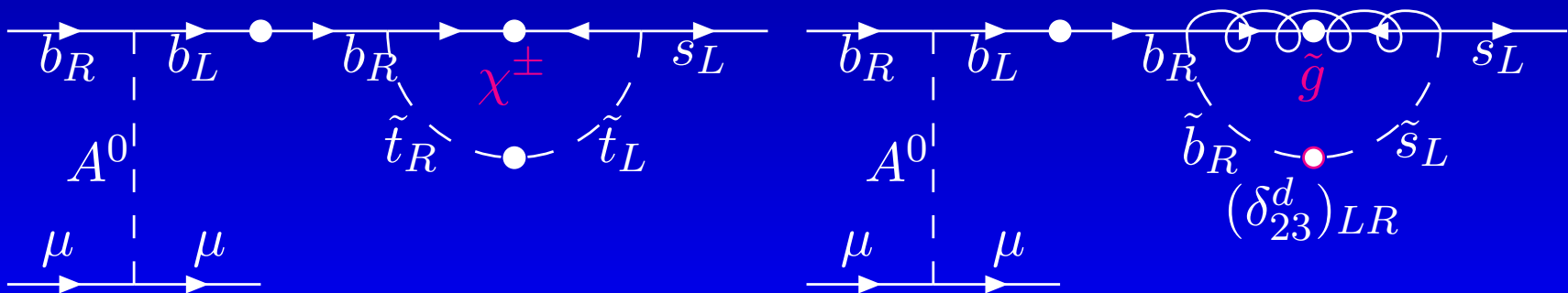
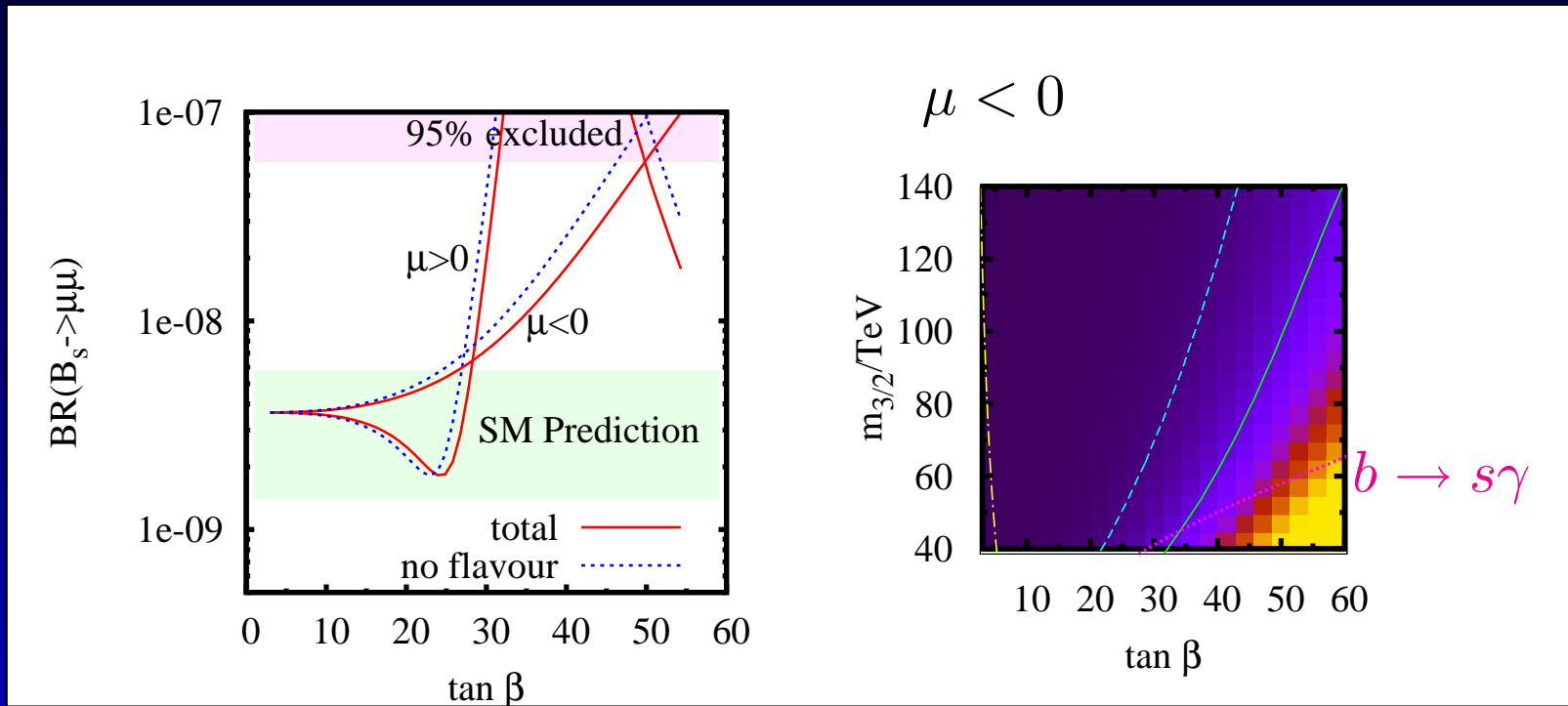
Everett, Kane, Rigolin, Wang, Wang, JHEP 201 (2002) 022 for flavoured MSSM





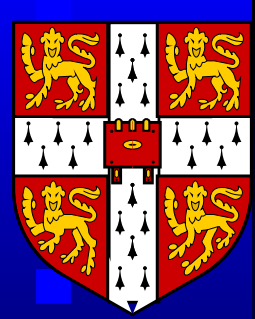
# $BR(B_s \rightarrow \mu^+ \mu^-)$ : LHCb

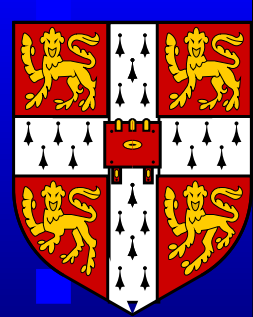
SOFTSUSY3.0.  $BR^{exp} < 58 \times 10^{-9}$ ,





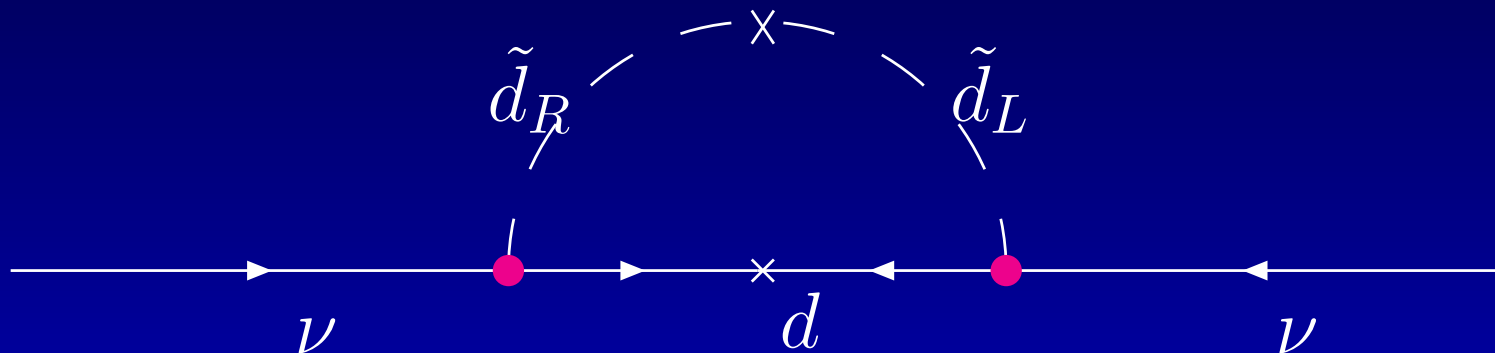
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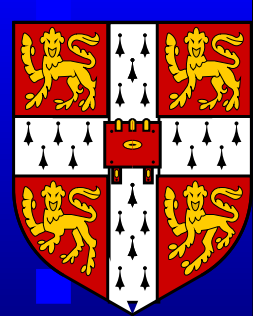


# Motivation for $\mathbb{R}_p$

- It has additional search possibilities.
- Neutrino masses and mixings testable at LHC

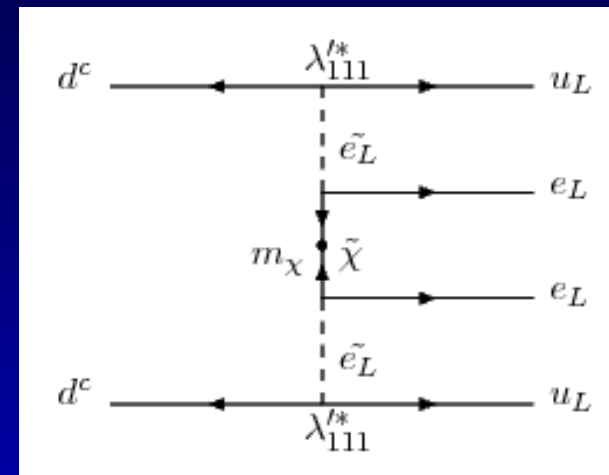
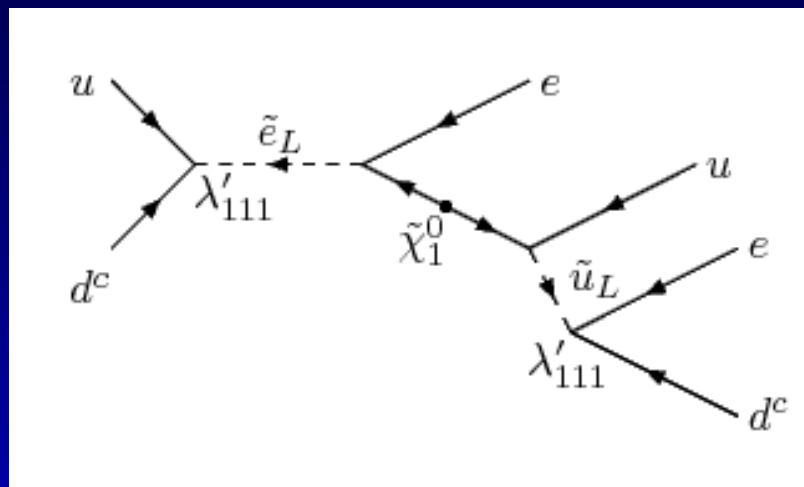


$$(m_\nu)_{11} = \frac{3}{32\pi^2} m_d \lambda'_{111}{}^2 \sin 2\theta_d \ln \frac{m_{\tilde{d}_L}^2}{m_{\tilde{d}_R}^2}$$



# LHC Single Selectron Production

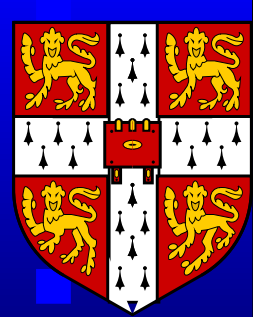
Like-sign dielectrons and two hard jets connects with neutrinoless double beta decay:



$$\sigma(pp \rightarrow \tilde{l}) \propto \frac{|\lambda'_{111}|^2}{m_{\tilde{e}_L}^3} \quad [T_{1/2}^{0\nu\beta\beta}(\text{Ge})]^{-1} \propto \frac{|\lambda'_{111}|^4}{M_{susy}^{10}}$$

So, there is an interesting interplay between the two<sup>a</sup>

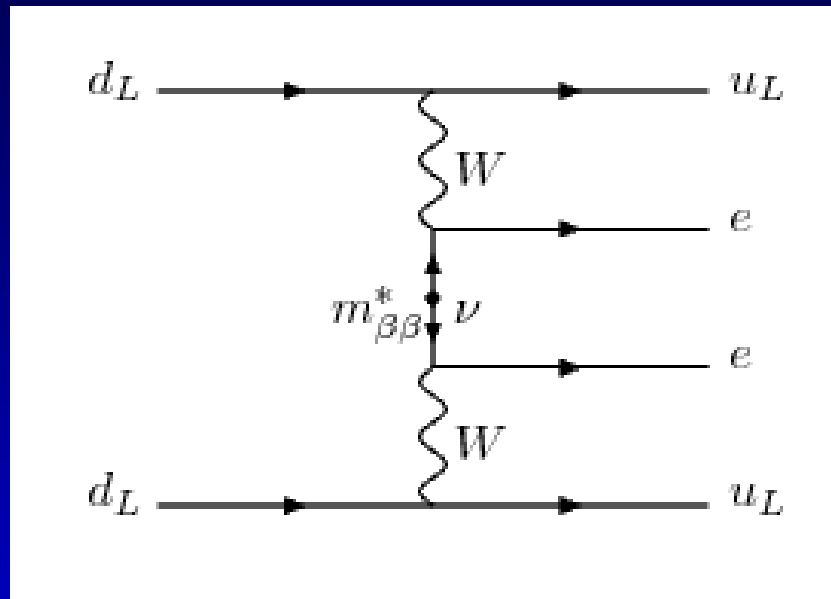
<sup>a</sup>BCA Kom Päs arXiv:0902.4697



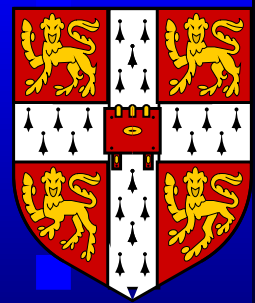
# Neutrinoless Double Beta Decay

Heidelberg-Moscow limit:

$$T_{1/2}^{0\nu\beta\beta}(\text{Ge}) \geq 1.9 \cdot 10^{25} \text{ yrs} \Rightarrow m_\nu < 0.46 \text{ eV}.$$

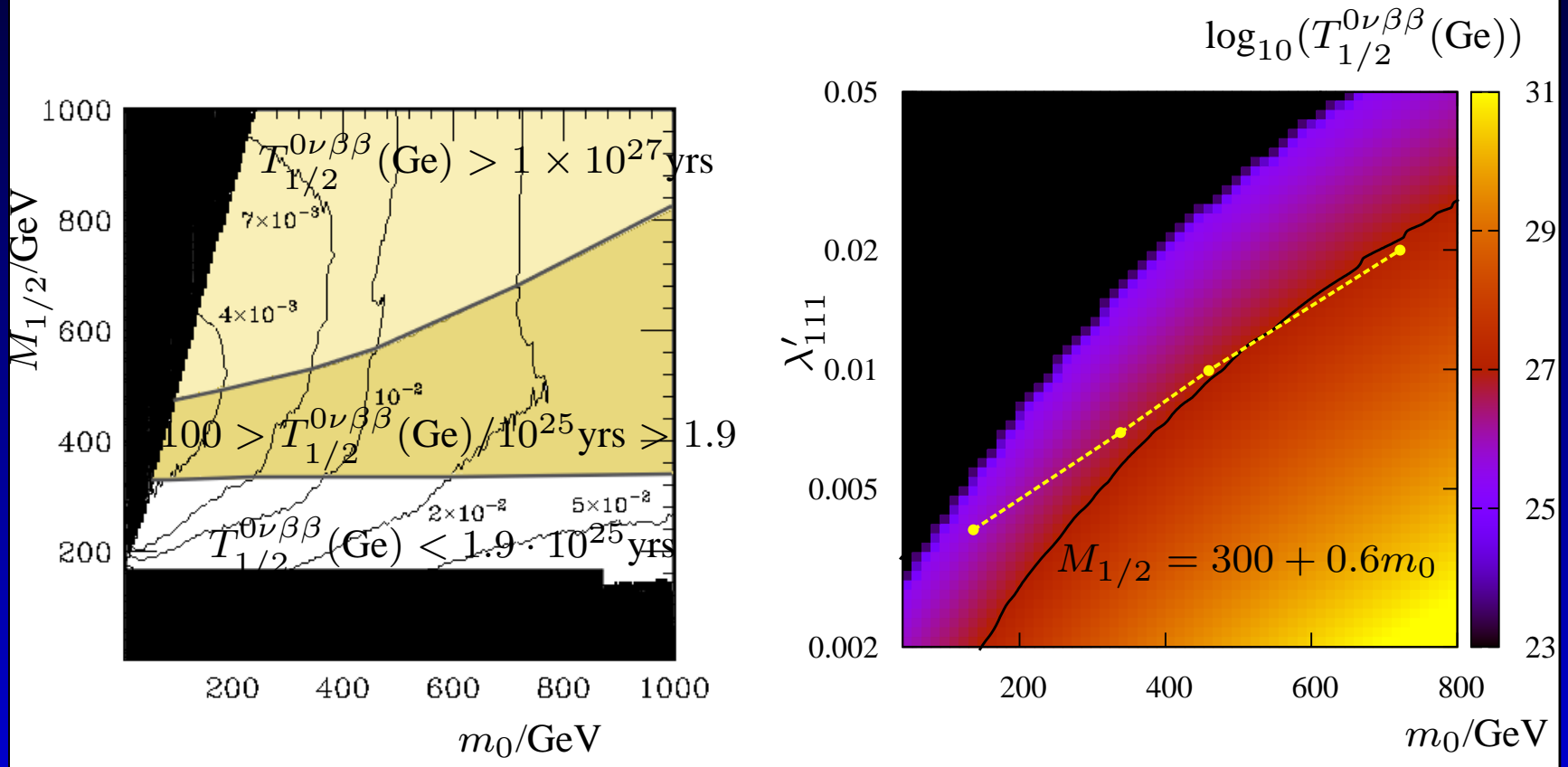


*Next round of experiments are going to improve the  $T_{1/2}^{0\nu\beta\beta}(\text{Ge})$  bound by a couple of orders of magnitude*

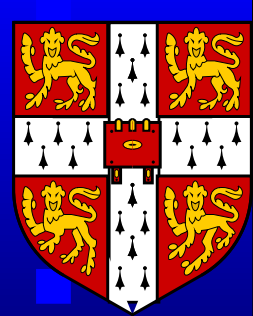


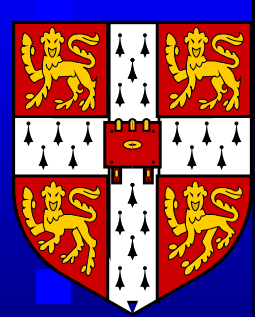
# Neutrinoless-LHC Interplay

Used Dreiner, Richardson, Seymour, PRD63 (2001) 055008 for reach  $10 \text{ fb}^{-1}$ ,  $\tan \beta = 10$ ,  $5\sigma$  discovery of  $\tilde{e}$



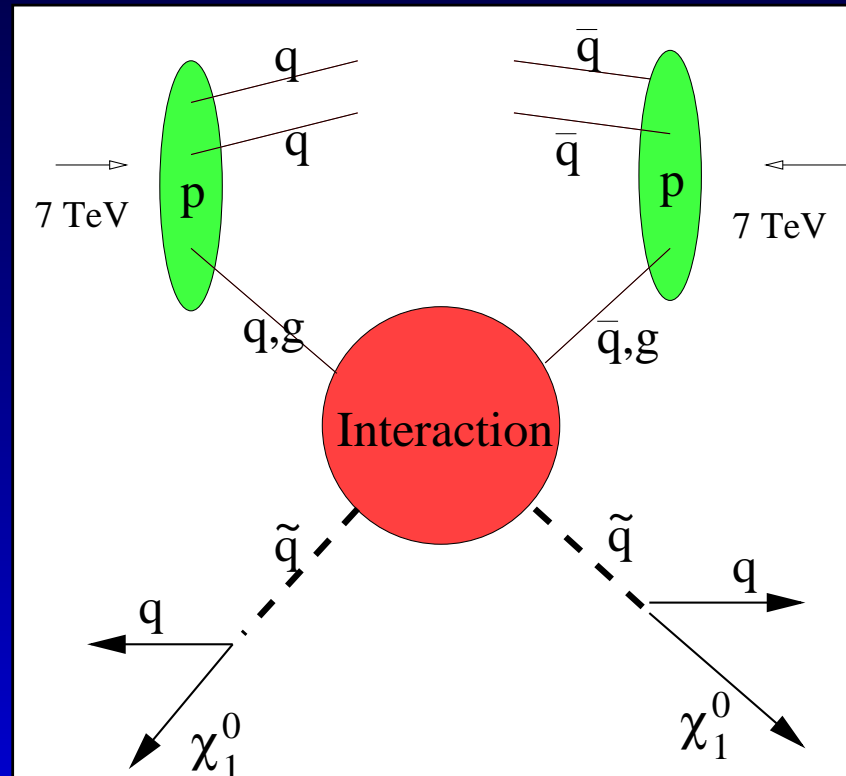
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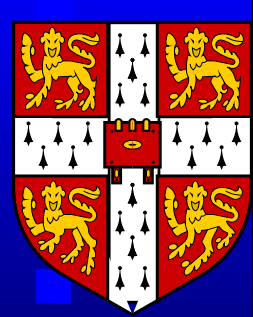


# Collider Sparticle Production

Strong sparticle production and decay to dark matter particles.

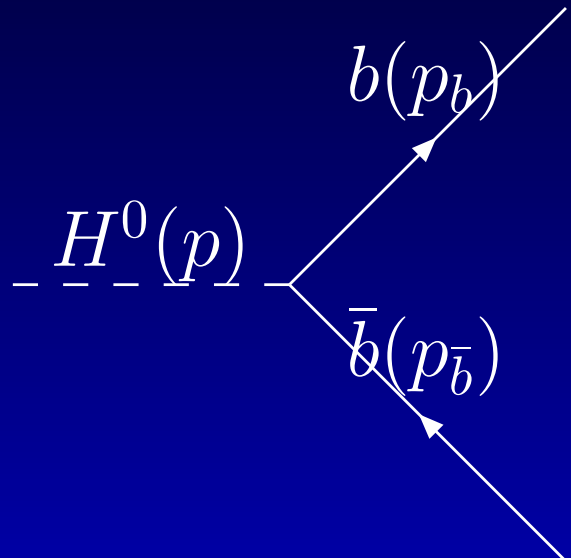


*Any (light enough) dark matter candidate that couples to hadrons can be produced at the LHC*



# SUSY Kinematics: a Reminder

Take a particle decaying into 2 particles, eg  $H^0 \rightarrow b\bar{b}$ .  
We define the **invariant mass** of the  $b\bar{b}$  pair such that:



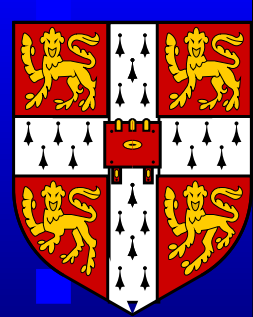
The diagram shows a horizontal dashed line on the left labeled  $H^0(p)$ . Two solid lines branch out to the right. The upper line is labeled  $b(p_b)$  and the lower line is labeled  $\bar{b}(p_{\bar{b}})$ . Both lines have arrows pointing to the right.

$$p^\mu = (\sqrt{m_H^2 + p^2}, \underline{p}) = p_b^\mu + p_{\bar{b}}^\mu$$
$$\Rightarrow p^2 = m_H^2 = (p_b + p_{\bar{b}})^2$$

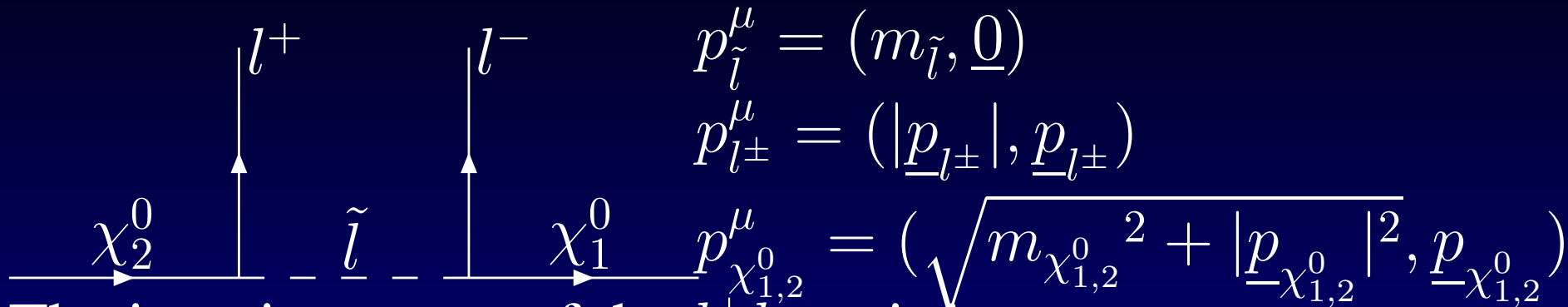
Is *invariant* in boosted frames

**Question:** What happens to invariant mass in SUSY cascade decays, where we miss the final particle?





# Cascade Decay



The invariant mass of the  $l^+l^-$  pair is

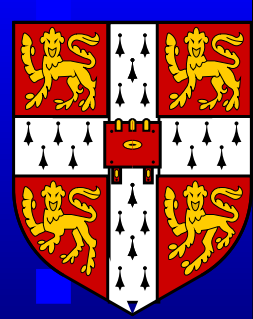
$$m_{ll}^2 = (p_{l^+} + p_{l^-})^\mu (p_{l^+} + p_{l^-})_\mu = p_{l^+}^2 + p_{l^-}^2 + 2p_{l^+} \cdot p_{l^-} \\ = 2|\underline{p}_{l^+}||\underline{p}_{l^-}|(1 - \cos \theta) \leq 4|\underline{p}_{l^+}||\underline{p}_{l^-}|.$$

**Momentum conservation:**

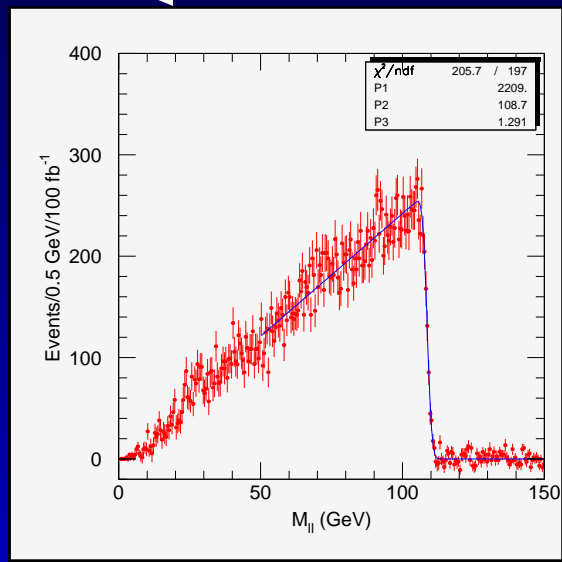
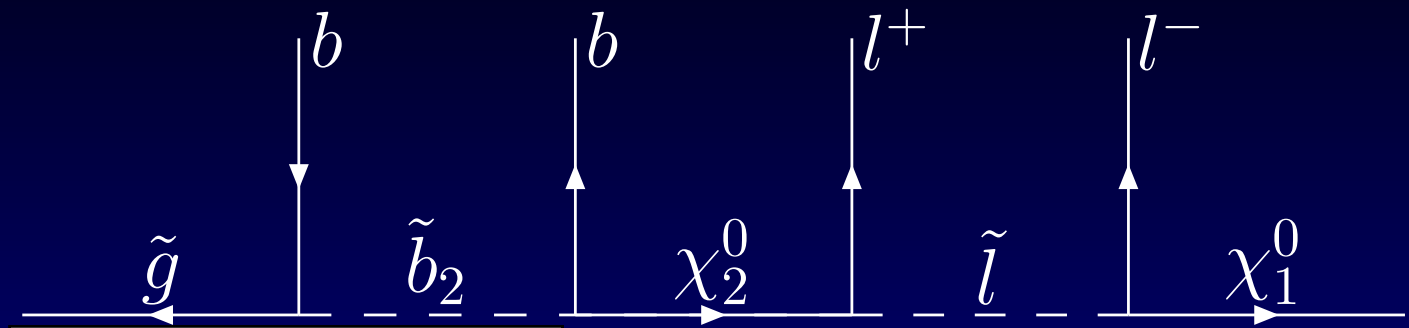
$$\Rightarrow \underline{p}_{\chi_2^0} + \underline{p}_{l^+} = \underline{0}, \quad \underline{p}_{l^-} + \underline{p}_{\chi_1^0} = \underline{0}.$$

**Energy conservation:**  $\sqrt{m_{\chi_2^0}^2 + |\underline{p}_{l^+}|^2} = m_{\tilde{l}} + |\underline{p}_{l^+}|,$

$$\Rightarrow |\underline{p}_{l^+}| = \frac{m_{\chi_2^0}^2 - m_{\tilde{l}}^2}{2m_{\tilde{l}}}. \quad \text{Similarly } |\underline{p}_{l^-}| = \frac{m_{\tilde{l}}^2 - m_{\chi_1^0}^2}{2m_{\tilde{l}}}.$$



# LHC SUSY Measurements



$$m_{ll}^2 = \frac{(m_{\chi_2^0}^2 - m_{\tilde{l}}^2)(m_{\tilde{l}}^2 - m_{\chi_1^0}^2)}{m_{\tilde{l}}^2}$$

**Q:** Can we measure enough of these to pin SUSY<sup>a</sup> down?

<sup>a</sup>BCA, Lester, Parker, Webber, JHEP 0009 (2000) 004





# Selectron-Smuon Splitting

In GUT-scale models,

$$\begin{aligned} \Delta m^2(M_Z) = & \Delta m^2(M_X) + \frac{8m_\mu^2}{16\pi^2\nu^2} \left[ m_{\tilde{\mu}_R}^2(M_X) \right. \\ & + m_{\tilde{\mu}_L}^2(M_X) + m_{H_1}^2(M_X) + \\ & \left. A_\mu^2(M_X) \right] \tan^2 \beta \ln \left( \frac{M_X}{M_Z} \right). \end{aligned}$$

In AMSB, we have

$$\begin{aligned} \frac{(16\pi^2)^2(m_{\tilde{e}_R}^2)}{m_{3/2}^2} = & \left( -\frac{198}{25}g_1^4 \right) \cdot 1 + 6(Y_E^\dagger Y_E)^2 + \\ & (Y_E^\dagger Y_E) \left( \text{Tr}(2Y_E Y_E^\dagger + 6Y_D Y_D^\dagger) - \frac{18}{5}g_1^2 - 6g_2^2 \right) \end{aligned}$$

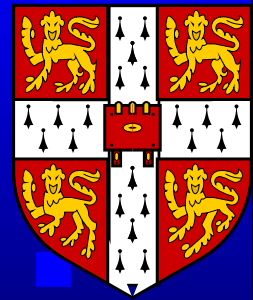
# Selectron-smuon mass splitting

In AMSB,

$$\frac{\Delta m^2}{m_{3/2}^2} = \frac{2m_\mu^2 \tan^4 \beta}{(16\pi^2)^2 v^2} \left[ \frac{12m_b^2 + 4m_\tau^2}{v^2} - \frac{1}{\tan^2 \beta} \left( \frac{18}{5} g_1^2 + 6g_2^2 \right) \right]$$

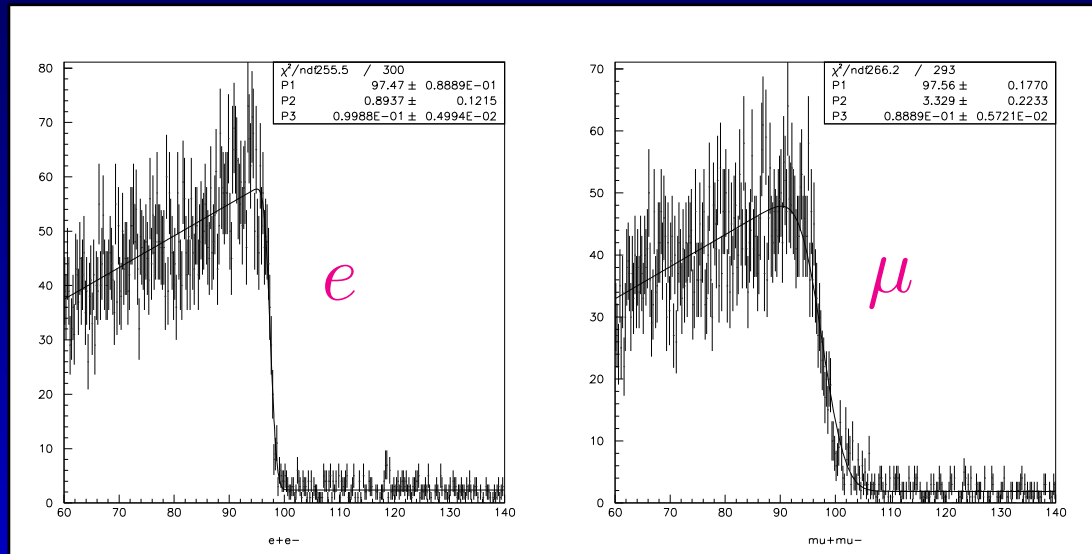
Dilepton edge at  $m_{ll}^2(\max) = \frac{(m_{\chi_2^0}^2 - m_{\tilde{l}}^2)(m_{\tilde{l}}^2 - m_{\chi_1^0}^2)}{m_{\tilde{l}}^2}$

$$\Rightarrow \frac{\Delta m_{ll}}{m_{ll}} = \frac{\Delta m_{\tilde{l}}}{m_{\tilde{l}}} \left( \frac{m_{\chi_1^0}^2 m_{\chi_2^0}^2 - m_{\tilde{l}}^4}{(m_{\chi_2^0}^2 - m_{\tilde{l}}^2)(m_{\tilde{l}}^2 - m_{\chi_1^0}^2)} \right),$$

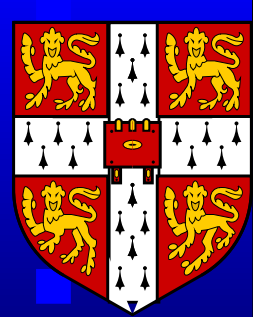


# Experimental Precision

SUGRA point 5:  $m_0 = 100$  GeV,  $m_{1/2} = 300$  GeV,  $A_0 = 300$  GeV,  $\tan \beta = 2.1$ . Total SUSY cross-section from HERWIG6 .510 is 24 pb. Pass through AcerDet minimal rough detector sim,



$16 \text{ fb}^{-1}$ . Require 2 OSSF isolated leptons with  $p_T > 10$  GeV, missing  $E_T > 100$  GeV. Perform  $\log L$  fit to Gaussian-smeared  $\Delta$  and number of events.



# Background Subtraction

We can still subtract<sup>a</sup> SM backgrounds like those from  $t\bar{t}$  or  $W^+W^-$  by (eg)

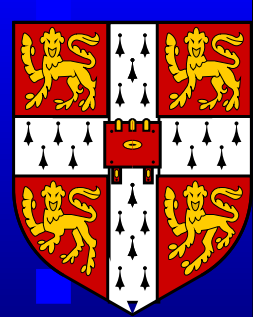
$$N_{e^+e^-} - \frac{1}{2} (N_{e^+\mu^-} + N_{e^-\mu^+}),$$

but we'll have to know the efficiencies of  $es$  and  $\mu s$  well.

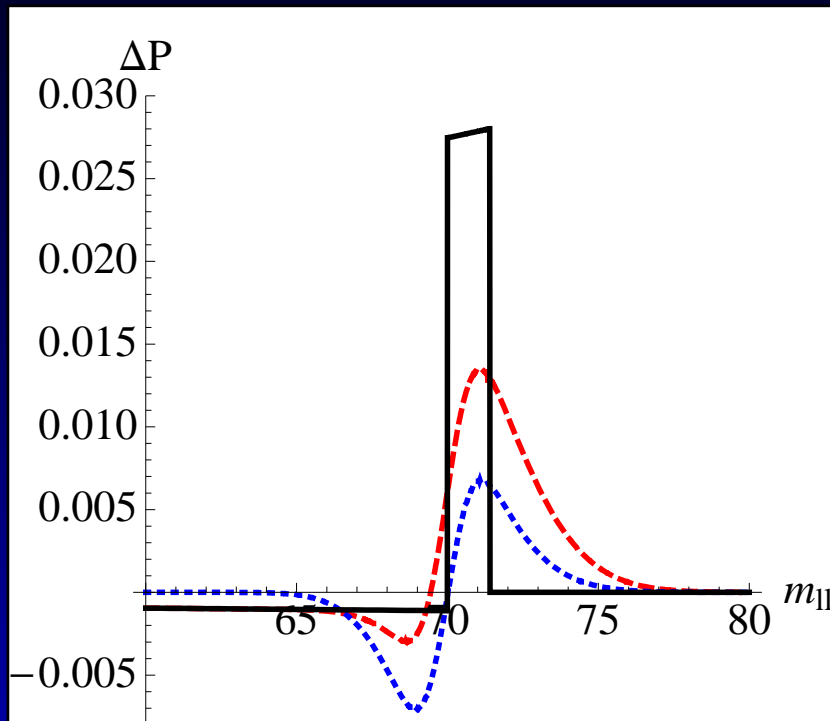
Use muons/electrons from  $Z^0$  pole to calibrate energies/efficiencies by extrapolation: for SPS1a,3,5,9  
 $m_{ll} = 80, 118, 99, 122, 343$  GeV. Best guess

$$\Delta E/E = 0.1\%$$

<sup>a</sup>See [Goto, Kawagoe, Nojiri, Phys. Rev. D70 \(2004\) 075016](#) for BRs/charge asymmetries sensitive to  $\tilde{\mu}_L - \tilde{\mu}_R$  mixing



# Difference in mass distributions



$\Delta m/m = 2\%$  and  
(black) no energy resolution

Red: Energy resolution

Blue:  $\Delta m/m = 0$  with  
energy resolution

Thus we could be fooled by the difference.

*Best to fit both  $\tilde{e}$ ,  $\tilde{\mu}$  endpoints separately.<sup>a</sup>*

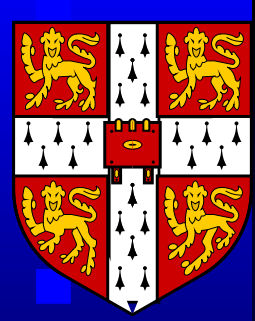
<sup>a</sup>BCA, Conlon, Lester, Phys. Rev. D77 (2008) 076006,  
arXiv:0801.366



# Summary

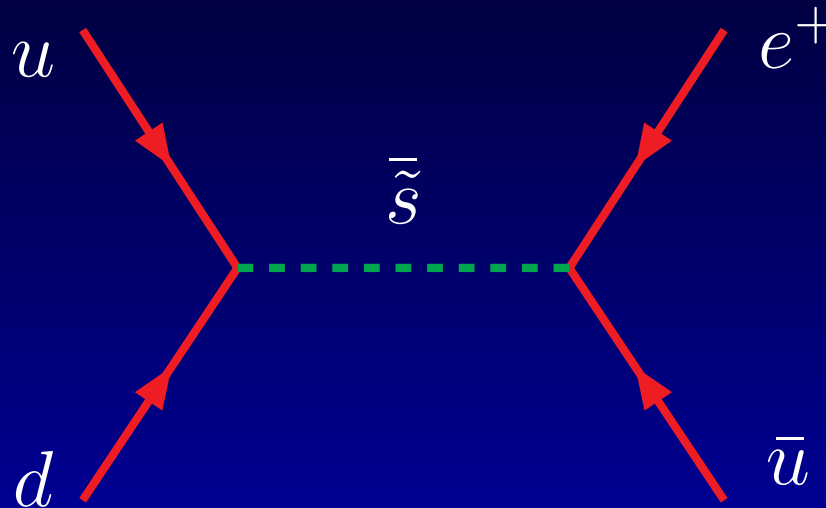
- Current indirect data are weak and only constrain models with a couple of extra parameters: LHC will change this situation
- Want **predictivity in flavour sector** eg AMSB. LHCb data going to provide  $BR(B_s \rightarrow \mu^+ \mu^-)$  for instance.
- SLHA2 compliant flavour tools developed in process SOFTSUSY3.0<sup>a</sup>., SUSYBSG1.3<sup>b</sup>
- Does your model violate  $R_p$ ? It could lead to interesting *detection possibilities*.
- Constrained models' useful predictions are *those that can be easily measured* - bear in mind





# Proton decay

$\mathcal{R}_p$  terms are lepton number  $L$ , or baryon number  $B$  violating.



$$\Gamma(p \rightarrow e^+ \pi^0) \approx \frac{\lambda'_{11k}{}^2 \lambda''_{11k}{}^2}{16\pi^2 \tilde{m}_{d_k}^4} M_{proton}^5.$$

$$\tau(p \rightarrow \nu K^+) > 7 \cdot 10^{32} \text{ yr} \Rightarrow \lambda'_{11k} \cdot \lambda''_{11k} \lesssim 10^{-27} \left( \frac{\tilde{m}_{d_k}}{100 \text{ GeV}} \right)^2.$$



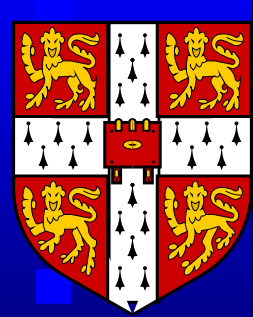


# Alternatives to $R_p$

All of the following stabilise the proton:

- **Matter Parity**  $M_p = (-1)^{3B+L}$ .  
Does exactly the same job as  $R_p$ .
- **Baryon Parity**  $B_p = (-1)^{3B}$ .  
Allows  $R_p$  terms  $\lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k$ .
- **Lepton Parity**  $L_p = (-1)^L$ .  
Allows  $R_p$  terms  $\lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k$ .

The second two alternatives allow for increased SUSY **detection** possibilities.



# Minimal Flavour Violation

In BSM models, MFV says that, essentially

SM Yukawa couplings contain *all* of the flavour violation in the model.

SM has a global

$U(3)_Q \times U(3)_L \times U(3)_e \times U(3)_d \times U(3)_u$  flavour symmetry where  $Q, L, e_R, u_R, d_R$  all transform as a fundamental representation under a  $U(3)$  and singlets under the rest, since terms like

$$\mathcal{L}_{kin} = \bar{Q}_i i \not{D} Q_i + \bar{L}_i i \not{D} L_i + \bar{e}_{Ri} i \not{D} e_{Ri} + \dots$$

are *invariant*.



# MFV and Yukawa Couplings

Even Yukawa couplings like

$$\mathcal{L}_{yuk} = \bar{Q}_i H (Y_U)_{ij} u_{Rj}$$

are invariant if we impose that, under  $U(3)^5$

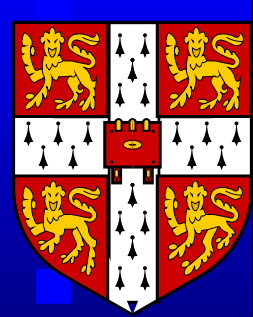
$$(Y_U)_{ij} \rightarrow U_Q (Y_U)_{ij} U_u^\dagger.$$

transforms as a spurion field<sup>a</sup>.

*These models are in general safer than non-MFV models from being ruled out by flavour constraints.*

---

<sup>a</sup>D'Ambrosio, Giudice, Isidori, Strumia, Nucl. Phys. B645 (2002)



# SUSY

which look like they **break** the symmetry. Suppose we can write, for some SUSY breaking scheme, e.g.

$$(m_{\tilde{u}}^2)_{ij} = z_1^u \delta_{ij} + z_2^u (Y_U^\dagger Y_U) + z_3^u Y_U^\dagger Y_D Y_D^\dagger Y_U + z_4^u (Y_U^\dagger Y_U)^2 + \dots$$

then MFV is **preserved** in the term

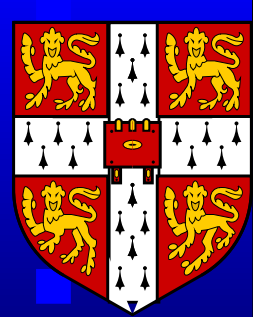
$$\tilde{u}_{iR} (m_{\tilde{u}}^2)_{ij} \tilde{u}_{jR}^*$$

In fact, such an expansion **spans all possible<sup>a</sup>**  $(m_{\tilde{u}}^2)_{ij}$  unless

$$\frac{z_{i>1}}{z_1} \leq \mathcal{O}(1) \Rightarrow \text{AMSB}$$

---

<sup>a</sup>Colangelo, Nikolidakis, Smith, Eur. Phys. J. C59 (2009) 75



# MSSM is MFV?

By use of Cayley-Hamilton identities<sup>a</sup>

$$0 = M^3 - [M]M^2 + \frac{1}{2}M([M]^2 - [M^2]) - |M|$$

$$|M| = \frac{1}{3}[M^3] - \frac{1}{2}[M][M^2] + \frac{1}{6}[M]^3,$$

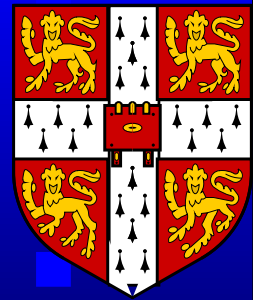
it can be shown that the MFV expansion terminates after 18 terms *for an arbitrary hermitian matrix*.

Thus, the MSSM *always* respects  $U(3)^5$ ! To make the definition of MFV meaningful, we add

$$\frac{z_{i>1}}{z_1} \leq \mathcal{O}(1) \Rightarrow \text{AMSB}$$

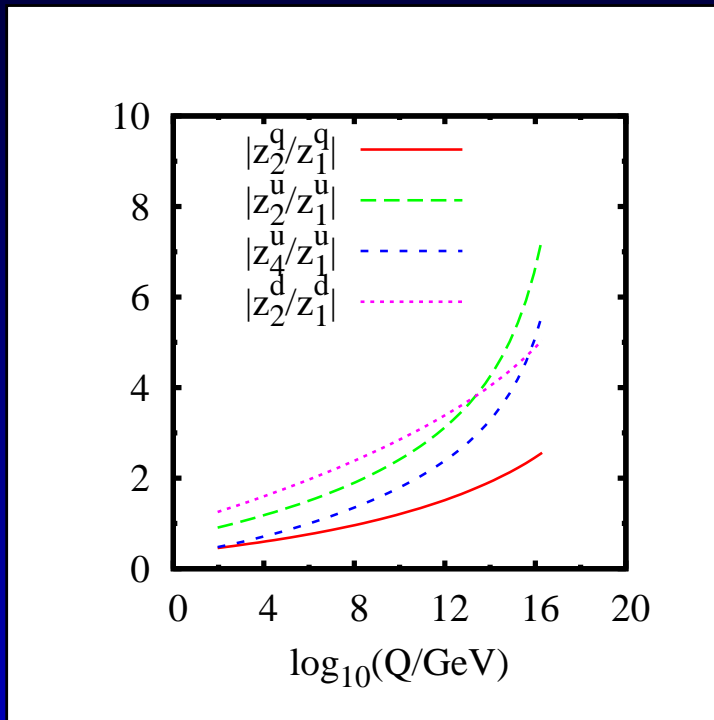


<sup>a</sup>Colangelo, Nikolidakis, Smith, Eur. Phys. J. C59 (2009) 75



# MFV Decomposition

$$\tan \beta = 10$$



$$z_1^u = m_{3/2}^2 \left( -\frac{88}{25} g_1^4 + 8g_3^4 \right) / (16\pi^2)$$

$$z_4^u = 6m_{3/2}^2 / (16\pi^2)$$

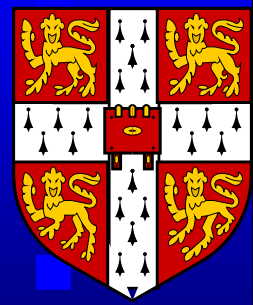
Nowhere flavour blind

MSUGRA/GMSB have small  $z_{i>1}$

**AMSB is MFV**

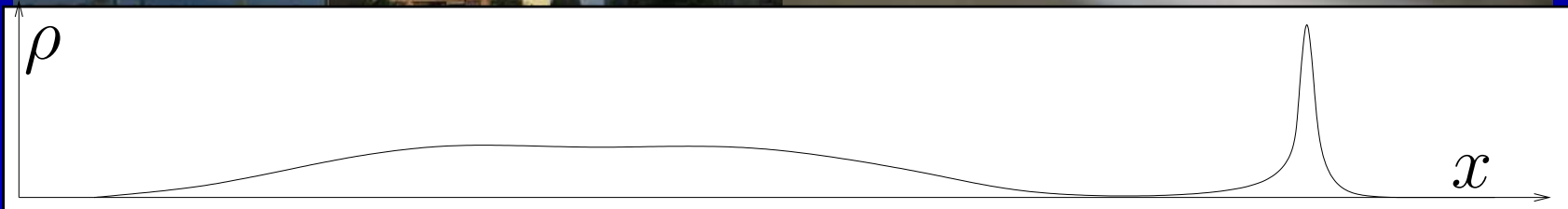
We'll predict  $\delta$ s, eg:

$$(1) \quad (\delta_{ij}^q)_{LL} = m_{\tilde{q}_{ij}}^2 / \sqrt{m_{\tilde{q}_{Li}}^2 m_{\tilde{q}_{Lj}}^2}.$$



# Volume Effects

*Can't rely on a good  $\chi^2$  in non-Gaussian situation*







# QIRFP of $\lambda_t$

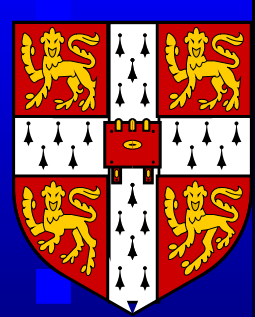
Neglecting electroweak gauge couplings, solve RGEs to obtain in IRQFP limit  $\lambda_t(M_X) \rightarrow \infty$

$$\frac{\lambda_t^2(m_t)}{g_3^2(m_t)} = \frac{7}{18} \left( 1 - \left( \frac{g_3^2(M_X)}{g_3^2(m_t)} \right)^{\frac{7}{9}} \right)^{-1}.$$

Putting in the electroweak corrections and  $M_X = M_{GUT}$ ,

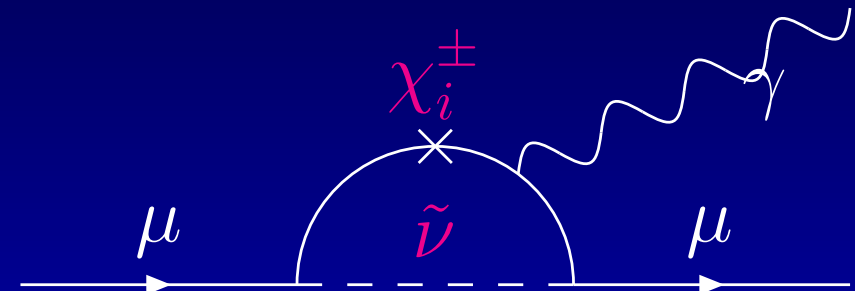
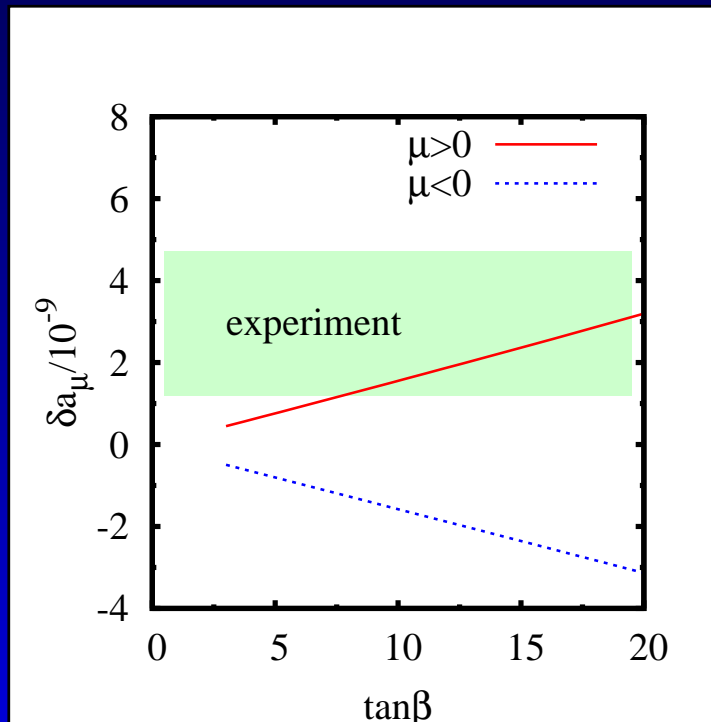
$$\lambda_t(m_t) = 1.1$$

whereas  $\hat{\beta}_t$  vanishes for  $\lambda_t = 1.2$ : **flavour violation at low  $\tan \beta$  has an additional suppression.**



# Anomalous mag. moment of $\mu$

$U(1)'$  solution to tachyonic sleptons<sup>a</sup>.  $m_{3/2} = 40$  TeV,  $\mu > 0$ , have a solution to  $\delta a_\mu = (29.5 \pm 8.8) \times 10^{-10}$ ,  $BR(B_s \rightarrow X_S \gamma)$  for  $8 < \tan \beta < 14$ :



$$a_\mu \propto \frac{\tan \beta}{M_{SUSY}^2}$$

Depends on slepton fix

<sup>a</sup>Hodgson, Jack, Jones, JHEP 0710 (2007) 070, arXiv:0709.2854



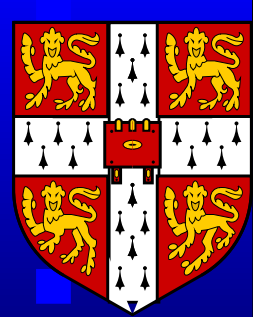
# Constraints

$\mathcal{L}_{MSSM}$  strongly constrained by absence of new physics contributions to FCNCs, eg

$BR(\mu \rightarrow e\gamma) < 1.2 \times 10^{-11}$  by MEGA. Constrains off-diagonal propagator mixing between selectron and smuon flavour eigenstates to

$$(2) \quad \frac{m_{\tilde{L}_{12}}^2}{m_{\tilde{L}_{11}}^2 + m_{\tilde{L}_{22}}^2} \lesssim 6 \times 10^{-4}.$$

$RR$  constraints similar over most of parameter space, but there are possible cancellations.



# Unconstraints

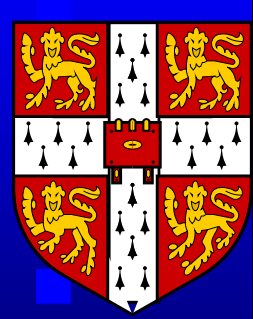
However, these constraints do *not* constrain selectron-smuon mass splitting

$$(3) \quad \Delta m^2 \equiv m_{\tilde{\mu}_R}^2 - m_{\tilde{e}_R}^2$$

in the absence of lepton flavour violation (**LFV**).

Some other work on SUSY **LFV** at LHC:

Agashe, Graesser hep-ph/9904422; Hinchliffe, Paige hep-ph/0010086;  
Hisano, Kitano, Nojiri hep-ph/0202129; Carvalho, Ellis, Gomez, Lola,  
Romao hep-ph/0206148; Bartl, Hidaka, Hohenwarter-Sodek,  
Kernreiter, Majerotto, Porod 0510074; Grossman, Nir, Thaler,  
Volansky, Zupan 0706.1845; Feng, Lester, Nir, Shadmi 0712.0674



# Enhancement Factor

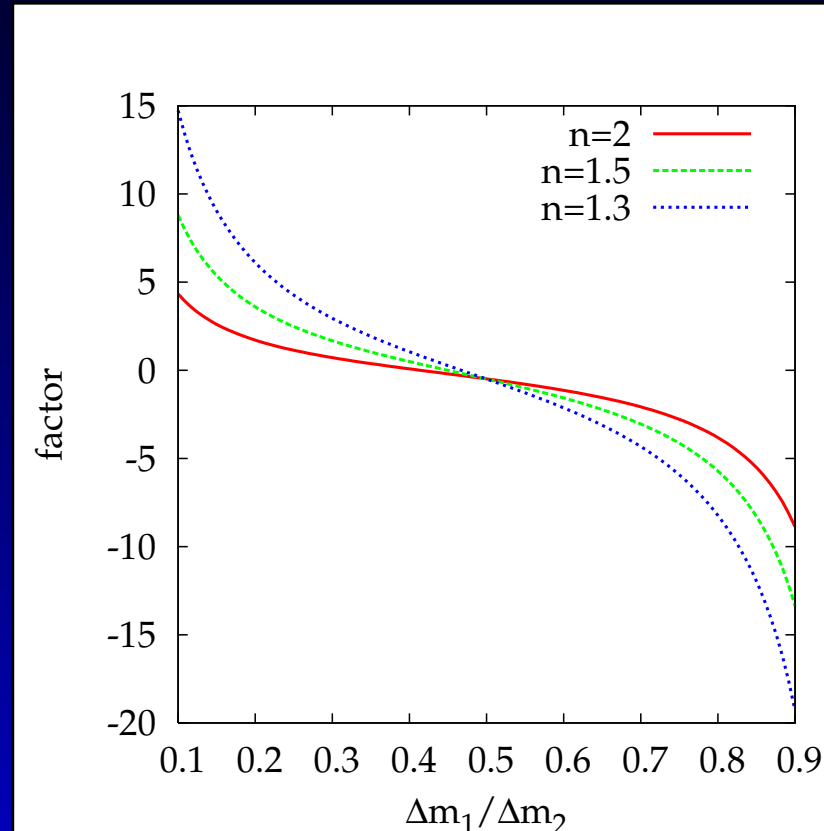


Figure 2:  $(\Delta m_{ll}/m_{ll})/(\Delta m_{\tilde{l}}/m_{\tilde{l}})$  as a function of  $\Delta m_1/\Delta m_2 \equiv (m_{\tilde{l}} - m_{\chi_1^0})/(m_{\chi_2^0} - m_{\chi_1^0})$  for three different values of  $n \equiv m_{\chi_2^0}/m_{\chi_1^0}$ .

# Luminosity Dependence

Integrated Luminosity ( $fb^{-1}$ )	Events below 100 GeV	Electron Endpoint (GeV)	Muon Endpoint (GeV)
16.0	22145	$97.47 \pm 0.09$	$97.56 \pm 0.18$
8.0	11131	$97.41 \pm 0.13$	$97.83 \pm 0.23$
4.0	5520	$97.54 \pm 0.19$	$97.63 \pm 0.35$
2.0	2707	$97.52 \pm 0.28$	$97.56 \pm 0.50$

Fractional fit error

$$\Sigma = \sqrt{(0.002 \sqrt{22145/N})^2 + 0.001^2} \text{ defined by } \Delta E/E \text{ and largest endpoint error.}$$



# Splitting Discovery

Define splitting discovery significance

$$S_1 = \left| \frac{\Delta m_{ll}}{m_{ll}} \right| \div \Sigma$$

In mSUGRA,  $S_1(\text{max}) = 0.5$ . If trigger and reconstruction efficiencies could be controlled, one could also use

(4) 
$$S_2 = \frac{N_{ee} - N_{\mu\mu}}{\sqrt{N}}.$$

*(we won't)*



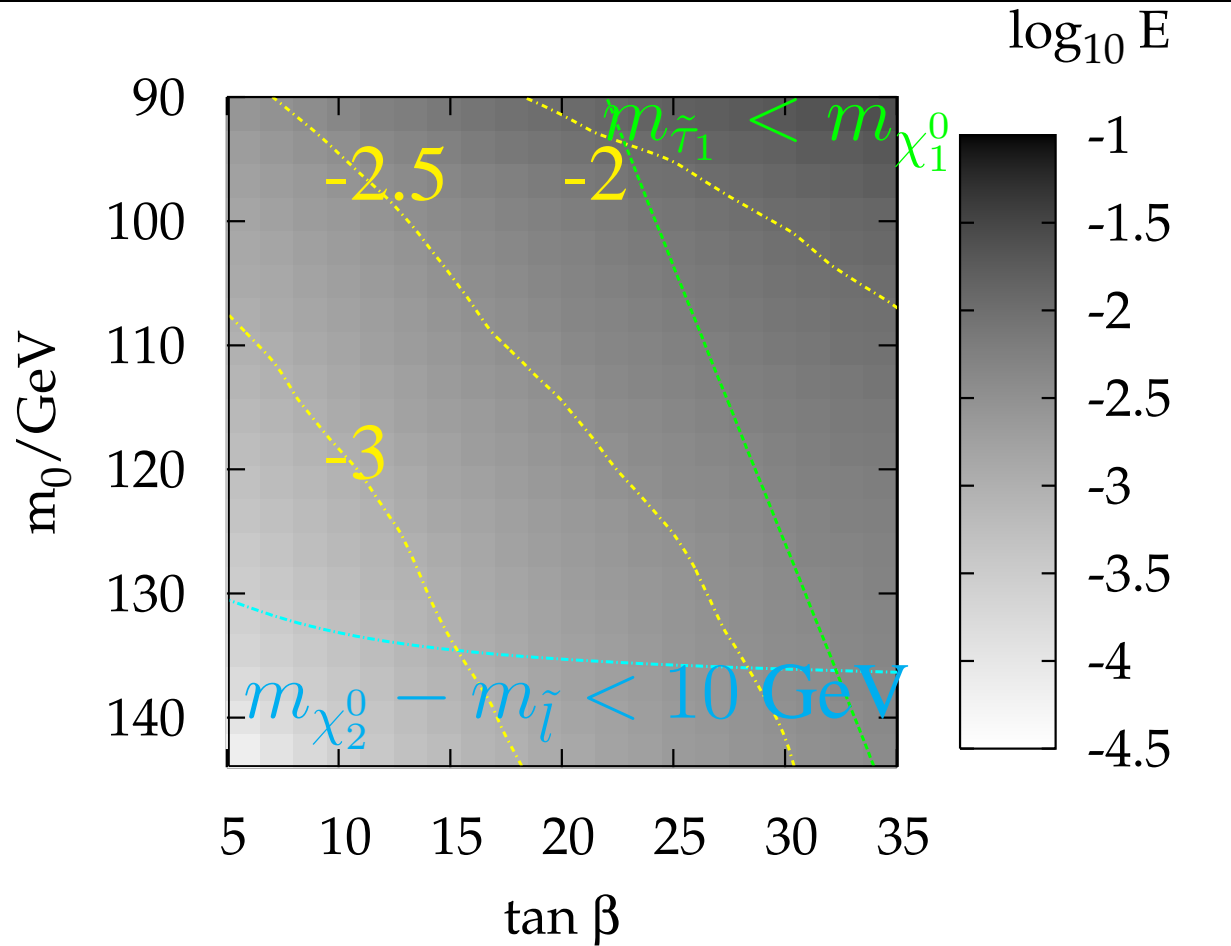
# mSUGRA Degeneracy

In fact, mSUGRA splittings at large  $\tan \beta$  can often be **several %**. But at large  $\tan \beta$ ,  $\tilde{\tau}_R$  is light and dominates decay modes with  $BR(\chi_2^0 \rightarrow \tilde{l}_R l) \ll 1$ ,  $BR(\chi_2^0 \rightarrow \tilde{\tau}_1 \tau) \approx 1$ .

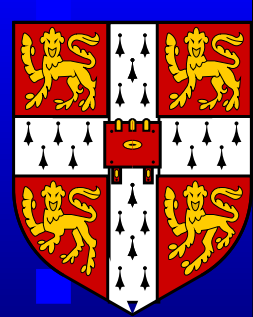
If we depart from mSUGRA by making  $\tilde{\tau}$ s heavy, one might easily discriminate from smuon-selectron universality:  $m_0 = 148$  GeV,  $m_{1/2} = 250$  GeV,  $A_0 = -600$  GeV,  $\tan \beta = 40$  but  $m_{\tilde{\tau}_{L,R}} = 950$  GeV:  $\Delta m_{\tilde{\tau}}/m_{\tilde{\tau}} = 2.3 \times 10^{-3}$  and  $\Delta m_{ll}/m_{ll} = 1.5\%$  whereas  $\Sigma = 0.27\%$ , **allowing an ( $S_1 > 5$ )-sigma discovery.**



# 1 $\sigma$ Sensitivity to $\tilde{e}$ - $\tilde{\mu}$ Universality



$$\mathcal{L} = 30 \text{ fb}^{-1} \text{ SPS1a. } E \equiv \left. \frac{\Delta m_{\tilde{l}}}{m_{\tilde{l}}} \right|_{S_1=1}.$$



# Extra Broken $U(1)$

$Q$	$\bar{U}$	$\bar{D}$	$H_1$	$H_2$	$\bar{\nu}$
$-\frac{1}{3}L$	$-e - \frac{2}{3}L$	$e + \frac{4}{3}L$	$-e - L$	$e + L$	$-2L - e$

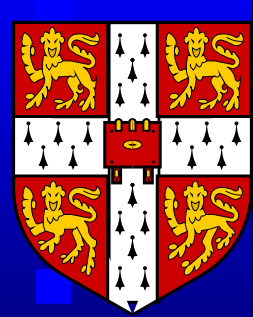
$$m_{\tilde{Q}}^2 \rightarrow m_{\tilde{Q}}^2 - \xi \frac{L}{3} \cdot \mathbf{1}, \quad m_{\tilde{u}}^2 \rightarrow m_{\tilde{u}}^2 - \xi \left( e + \frac{2}{3}L \right) \cdot \mathbf{1},$$

$$m_{\tilde{d}}^2 \rightarrow m_{\tilde{d}}^2 + \xi \left( e + \frac{4}{3}L \right) \cdot \mathbf{1}$$

*a*



*a* [Hodgson, Jack, Jones, JHEP 0710 \(2007\) 070, arXiv:0709.2854](#)



# Lepton number violation

Need to get all **six** slepton masses positive, while respecting bounds on couplings:  $W = \lambda_{ijk} L_i L_j E_k$

$$\lambda_{mni} \not\rightarrow \lambda_{mnj} \quad , \quad \lambda_{imn} \not\rightarrow \lambda_{jmn} \quad i \neq j,$$

$$\lambda_{123} \lesssim 0.49 \times \frac{m_{\tilde{\tau}_R}}{1 \text{ TeV}}$$

$$\lambda_{132} \lesssim 0.62 \times \frac{m_{\tilde{\mu}_R}}{1 \text{ TeV}}$$

$$\lambda_{231} \lesssim 0.70 \times \frac{m_{\tilde{e}_R}}{1 \text{ TeV}},$$

Search through **min** number of operators, and get **BCA**,  
Dedes, JHEP 06 (2000) 017, hep-ph/0003222

$$(m_E^2)_2^2 = \frac{M_{3/2}^2}{(16\pi^2)^2} \left[ \lambda_{231}^2 (4\lambda_{231}^2 + \lambda_{123}^2 + \lambda_{132}^2) - \frac{198}{25} g_1^4 \right]$$