

# MEASURING STOP MIXING ANGLE AT THE LHC

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# Motivation

- stops play an important role in the mechanism of radiative electroweak symmetry breaking
- CP-violating phase in stop sector can have a large impact on the Higgs sector of MSSM and play significant role in baryogenesis
- can be inaccessible at the linear collider (at least at the first stage)
  - ⇒ extract as much information as possible from LHC
  - ⇒ for what can be done at the ILC see:  
Bartl ea. '95-'99, '04, Kraml '99
- here we propose a new method to determine properties of the stop sector at the LHC

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- 1 Introduction
- 2 Parameter determination
- 3 Conclusions

# Stop sector of the MSSM

- defined by soft SUSY breaking masses for squarks  $\widetilde{M}_Q$ ,  $\widetilde{M}_U$ , soft trilinear coupling  $A_t$ ,  $\tan \beta$  and  $\mu$  parameter
- mass matrix for scalar top quarks in gauge eigenstate basis  $\tilde{t}_L, \tilde{t}_R$

$$\mathcal{M}_{\tilde{t}}^2 = \begin{pmatrix} m_t^2 + m_{LL}^2 & m_{LR}^* m_t \\ m_{LR} m_t & m_t^2 + m_{RR}^2 \end{pmatrix}$$

with

$$m_{LL}^2 = \widetilde{M}_Q^2 + m_Z^2 \cos 2\beta \left( \frac{1}{2} - \frac{2}{3} s_W^2 \right)$$

$$m_{RR}^2 = \widetilde{M}_U^2 + \frac{2}{3} m_Z^2 \cos 2\beta s_W^2$$

$$m_{LR} = A_t - \mu^* (\cot \beta)$$

# Stop sector of the MSSM

- diagonalize mass matrix with unitary matrix  $U_{\tilde{t}}$

$$U_{\tilde{t}} \mathcal{M}_{\tilde{t}}^2 U_{\tilde{t}}^\dagger = \text{diag}(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2)$$

- obtain mass matrix eigenstates  $\tilde{t}_1$  and  $\tilde{t}_2$

$$\begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} = U_{\tilde{t}} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} = \begin{pmatrix} \cos \theta_{\tilde{t}} & \sin \theta_{\tilde{t}} e^{-i\phi_{\tilde{t}}} \\ -\sin \theta_{\tilde{t}} e^{i\phi_{\tilde{t}}} & \cos \theta_{\tilde{t}} \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

- stops interactions can be parametrized in terms of  $\cos \theta_{\tilde{t}}$  and  $\phi_{\tilde{t}}$

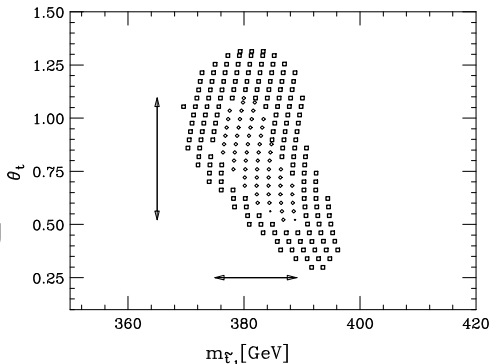
# Methods to determine $\cos \theta_{\tilde{t}}$

- take stops from gluino decays  
 $\tilde{g} \rightarrow t\tilde{t} \rightarrow tb\tilde{\chi}_1^+$   
 $\tilde{g} \rightarrow b\tilde{b}_i \rightarrow tb\tilde{\chi}_1^+$
- combine the analysis of sbottom and stop sectors
- fit to stop mass and mixing angle gives:

$$\Delta m_{\tilde{t}_1} = 7 \text{ GeV}$$

$$\Delta \theta_{\tilde{t}} = 0.29$$

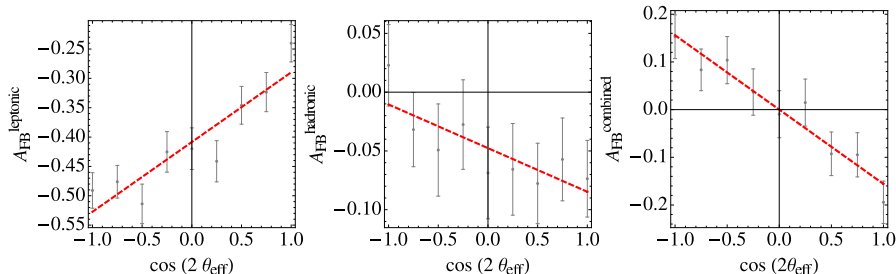
Hisano, Kawagoe, Nojiri '03



# Methods to determine $\cos \theta_{\tilde{t}}$

- measurement of top polarization in the decay  $\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t$
- use hadronic and semileptonic top decays and forward-backward asymmetries of decay products
- asymmetries have linear dependence on **effective** stop mixing angle

Perelstein, Weiler '08



# New method proposal

- $\cos \theta_{\tilde{t}}$  gives content of  $\tilde{t}_L$  and  $\tilde{t}_R$  states in  $\tilde{t}_1$  and  $\tilde{t}_2$   
⇒ measuring relative strength of the coupling to charginos and neutralinos gives information on the structure of stop sector
- take light stops from a direct pair production process to avoid background from sbottoms
- absolute measurement of branching ratios difficult  
⇒ look at the relative number of stops decaying to different charginos and neutralinos
- depending on the realized model one can get information on stop mixing (including phase) and mass  
⇒ can be combined with information from other methods



# Parameter point – SPS1a'

- masses:

$$m_{\tilde{t}_1} = 366 \text{ GeV}$$

$$m_{\tilde{\chi}_1^\pm} = 184 \text{ GeV}$$

$$m_{\tilde{\chi}_1^0} = 98 \text{ GeV}$$

$$m_{\tilde{\chi}_2^0} = 184 \text{ GeV}$$

- mixing angle:  $\cos \theta_{\tilde{t}} = 0.56$ ,  
 $\phi_{\tilde{t}} = 0$

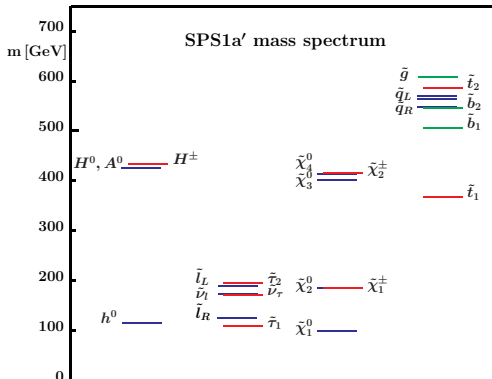
- decay modes:

$$BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^+ b) = 72\%$$

$$BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t) = 22\%$$

$$BR(\tilde{t}_1 \rightarrow \tilde{\chi}_2^0 t) = 7\%$$

- $\sigma^{14 \text{ TeV}}(pp \rightarrow \tilde{t}_1 \tilde{t}_1^*) = 3.4 \text{ pb}$

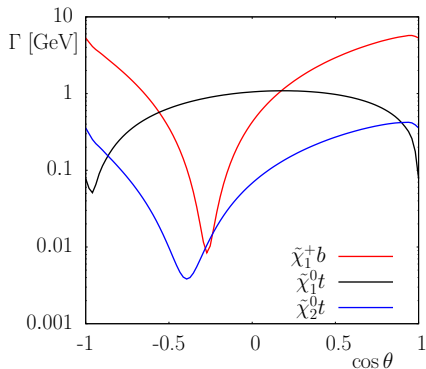


# Possible final states

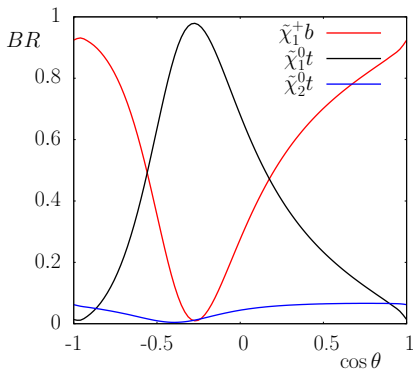
- for decay modes with  $t$  quark require top reconstruction
- neutralino decay modes include tau leptons
- number of events for integrated luminosity  $\mathcal{L} = 100 \text{ fb}^{-1}$

decay mode	# events
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_2^0 + \bar{t} \tilde{\chi}_2^0 \rightarrow t \bar{t} \ell \bar{\ell} \tilde{\chi}_1^0 + \bar{t} \ell \bar{\ell} \tilde{\chi}_1^0 \rightarrow 4\ell \ 4j \ 2b + E_{\text{miss}}$	225
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_2^0 + \bar{t} \tilde{\chi}_1^0 \rightarrow t \bar{t} \ell \bar{\ell} \tilde{\chi}_1^0 + \bar{t} \tilde{\chi}_1^0 \rightarrow 2\ell \ 4j \ 2b + E_{\text{miss}}$	1270
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_2^0 + b \tilde{\chi}_1^+ \rightarrow t \bar{t} \ell \bar{\ell} \tilde{\chi}_1^0 + b \bar{\ell} \nu_e \tilde{\chi}_1^0 \rightarrow 3\ell \ 2j \ 2b + E_{\text{miss}}$	6230
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_1^0 + \bar{t} \tilde{\chi}_1^0 \rightarrow 4j \ 2b + E_{\text{miss}}$	7100
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_1^0 + b \tilde{\chi}_1^+ \rightarrow t \tilde{\chi}_1^0 + b \bar{\ell} \nu_e \tilde{\chi}_1^0 \rightarrow \ell \ 2j \ 2b + E_{\text{miss}}$	35000
$\tilde{t}_1 \tilde{t}_1^* \rightarrow \bar{b} \tilde{\chi}_1^- + b \tilde{\chi}_1^+ \rightarrow \bar{b} \ell \bar{\nu}_e \tilde{\chi}_1^0 + b \bar{\ell} \nu_e \tilde{\chi}_1^0 \rightarrow 2\ell \ 2b + E_{\text{miss}}$	170000

# Stop decays



widths for different decay modes  
of  $\tilde{t}_1$  as a function of  $\cos \theta_{\tilde{t}}$



BRs for different decay modes  
as a function of  $\cos \theta_{\tilde{t}}$

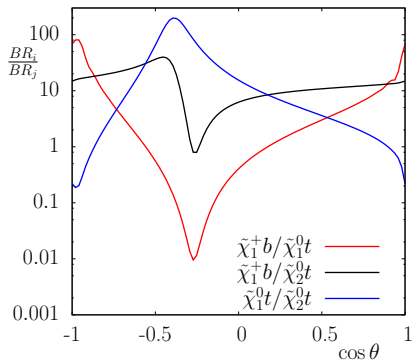
# Ratios of branching ratios

- define the following quantities in  $\tilde{t}_1$  decay modes:

$$R_1 = \frac{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^+ b)}{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t)}$$

$$R_2 = \frac{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^+ b)}{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_2^0 t)}$$

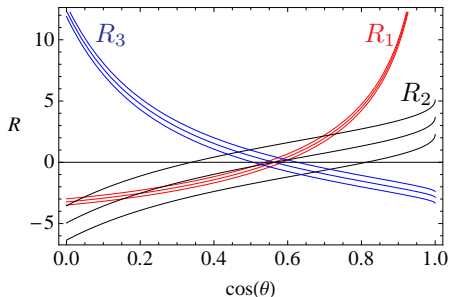
$$R_3 = \frac{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t)}{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_2^0 t)}$$



ratios of BRs for different decay modes as a function of  $\cos \theta_{\tilde{t}}$

# Determination of stop mixing angle

- number of events for any two decay modes give one of the ratios  $R_i$ 
  - $\Rightarrow$  best constraints from  $R_1$  and  $R_3$
  - $\Rightarrow$  no information on other decay modes required



- here ratios are normalized to their nominal values with  $1-\sigma$  statistical error bands

# Fit results for $\cos \theta_{\tilde{t}}$ and $m_{\tilde{t}_1}$

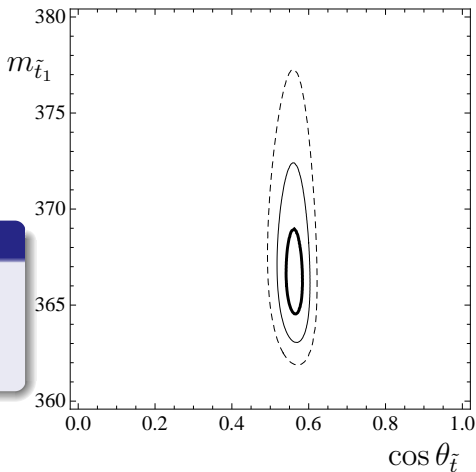
- 1000 events of stop production
- $\chi^2$  fit to all 3 ratios
- error = statistical only

## Results

$$\cos \theta_{\tilde{t}} = 0.56 \pm 0.03$$

$$\theta_{\tilde{t}} = 0.98 \pm 0.05$$

$$m_{\tilde{t}_1} = 366_{-2}^{+3} \text{ GeV}$$



# SM Backgrounds

- Standard Model background:

$$t\bar{t} \rightarrow 4j\ 2b, \quad 2j\ 2b\ \ell + E_{miss}, \quad 2b\ 2\ell + E_{miss}$$

- cuts proposed by **Perelstein, Weiler '08**

- ⇒ large missing transverse energy  $E_{miss} > 125\text{ GeV}$
- ⇒ semileptonic top veto (using neutrino momentum reconstruction)
- ⇒ hadronic top reconstruction to eliminate  $W$ +jets background
- ⇒ angular and separation cuts

# SUSY Backgrounds

- gluino pairs decaying to:

$$\tilde{g}\tilde{g} \rightarrow \tilde{b}_i b + \tilde{b}_j b, \quad \tilde{b}_i b + \tilde{t}_1 t, \quad \tilde{t}_1 t + \tilde{t}_1 t$$

⇒ good  $b$  tagging efficiency needed to reject these

- production of  $\tilde{b}_i \tilde{b}_j^*$  and  $\tilde{t}_2 \tilde{t}_2^*$  is order of magnitude smaller than the signal

- different final states within the signal may fake each other when top decays leptonically:

$$\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0 \rightarrow b \ell + E_{miss} \quad \text{and} \quad \tilde{t}_1 \rightarrow b \tilde{\chi}_1^+ \rightarrow b \ell + E_{miss}$$

⇒ needs further study

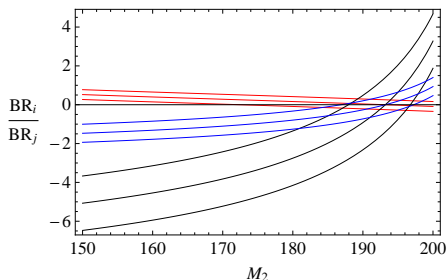
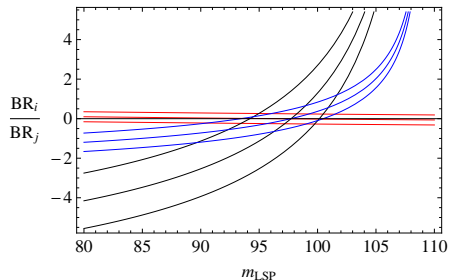


# Conclusions

- if stops are too heavy for ILC we have to use maximum information from LHC
- proposed method can give useful constraints on parameters of stop sector
- additional information on gaugino/higgsino sector may be required from the linear collider  
⇒ example of LHC-ILC interplay
- combination with CP-odd observables can resolve CP properties of top squarks
- more detailed experimental study needed to assess viability of this method

# Dependence on gaugino parameters

ratios of BRs show only moderate dependence on LSP mass  
 (keeping  $m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}$  fixed) and wino mass parameter  $M_2$   
 $\Rightarrow$  no precise knowledge needed to get useful constraints



$\Rightarrow$  stronger dependence only for decay to  $\tilde{\chi}_2^0 t$  which is close to kinematic limit