

CKM unitarity and lepton universality tests with kaons

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Outline:

- 1) Semileptonic K decays and CKM unitarity;
- 2) Leptonic K decays and lepton universality tests;
- 3) The future: ultra-rare decays $K \rightarrow \pi \nu \bar{\nu}$.



*Lattice meets Phenomenology • IPPP, Durham
17 September 2010*

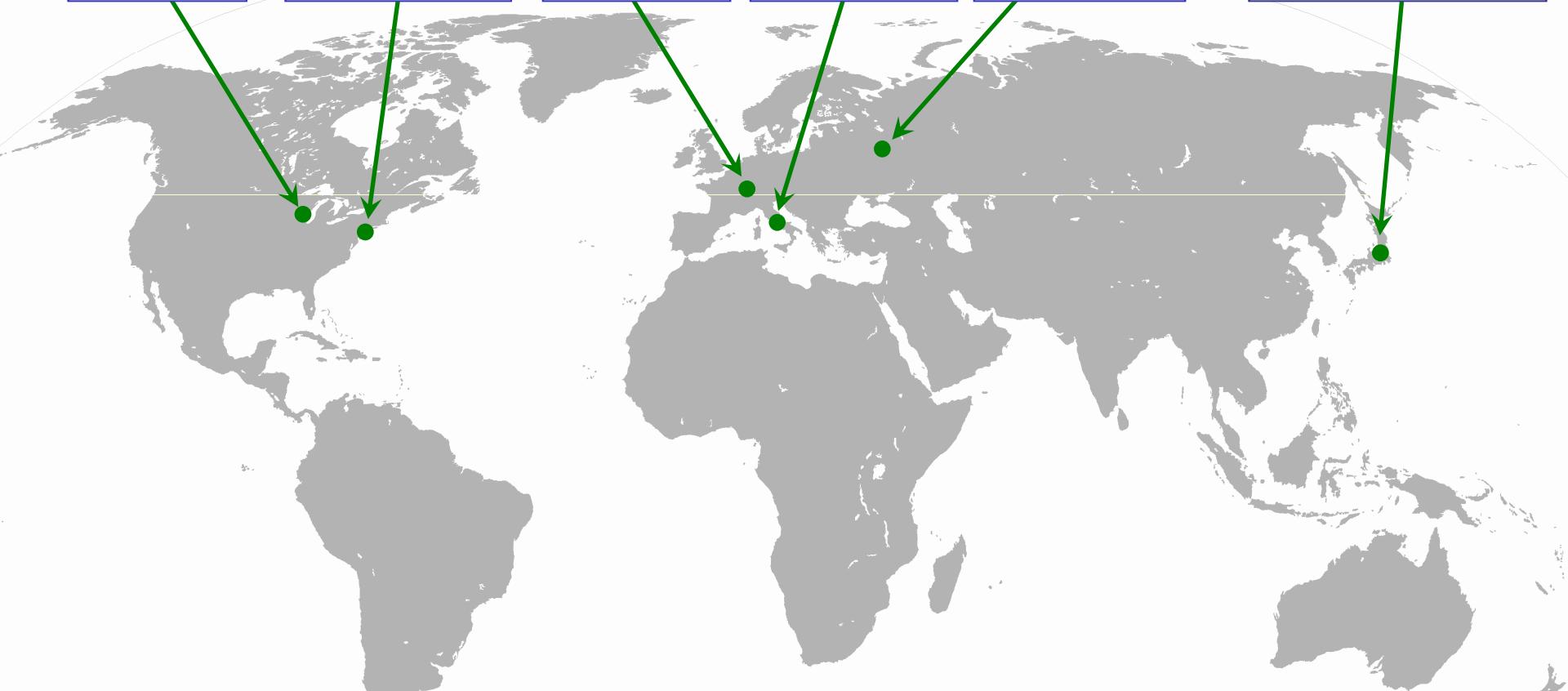


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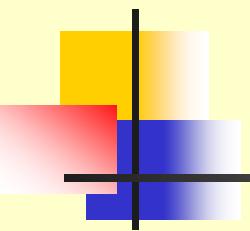


Major recent & future K experiments

<u>FNAL</u> KTeV, P996	<u>BNL</u> E865, 787, 949	<u>CERN</u> NA48, NA62	<u>LNF</u> KLOE, KLOE2	<u>IHEP</u> ISTRAP+, OKA	<u>KEK/J-PARC</u> E391a, KOTO, TREK
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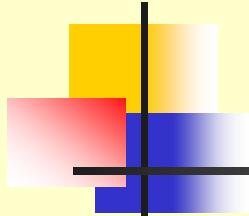


Variety of experimental techniques used:
decay-in-flight, decay-at-rest, ϕ factory (tagged decays).



Semileptonic kaon decays $(K \rightarrow \pi l \nu)$

→ Precise CKM unitarity test by measurement of $|V_{us}|$



$|V_{us}|$ with K_{l3} decays

$K \rightarrow \pi l\nu$ (K_{l3}) decays: ideal channels for $|V_{us}|$ determination

$$\Gamma(K_{l3(\gamma)}) = \frac{C_K^2 G_F^2 M_K^5}{192\pi^3} S_{EW} |V_{us}|^2 |f_+^{K^0\pi^-}(0)|^2 I_{kl}(\lambda) (1 + 2\Delta_K^{SU(2)} + 2\Delta_{kl}^{EM})$$

(with $K=K_S, K_L, K^+$; $l=e,\mu$; $C_K^2 = 1/2$ for K^+ , $C_K^2 = 1$ for K^0)

Inputs from experiment

$\Gamma(K_{l3(\gamma)})$:

radiation-inclusive decay rates;
in practice, branching ratios & lifetimes.

$I_{kl}(\lambda)$:

phase space integrals;
 λ s parameterize form factor dependence
on momentum transfer $t=(P_K-P_\pi)^2$.

E.g. Taylor expansion parameterization:
 $(\lambda_+', \lambda_+'')$ for K_{e3} , $(\lambda_+', \lambda_+'', \lambda_0')$ for $K_{\mu 3}$.

Inputs from theory

$S_{EW}=1.0232(3)$:

short-distance EW correction

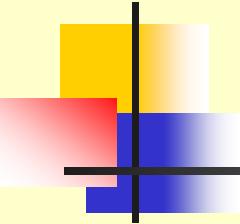
$f_+(0)$:

P.A.Boyle et al.,
arXiv:1004.0886

vector form factor at zero
momentum transfer ($t=0$)

$\Delta^{SU(2)}$ and Δ^{EM} :

channel-dependent isospin breaking
and long-distance EM corrections



$|V_{us}|$ from K_{l3} : recent history

2002: $|V_{ud}|^2 + |V_{us}|^2 - 1 = -0.0035(15)$.

(PDG 2004) A 2.3σ hint for CKM unitarity violation.

2003: BNL E865 measured a higher $\text{BR}(K^+ \rightarrow e^+ \nu_e) = 0.0513(10)$. ← 1.9%

Start of the $|V_{us}|$ revolution:
first modern measurement, consistent with unitarity.

2004-present: Many new measurements (ISTRA+, KLOE, KTeV, NA48)

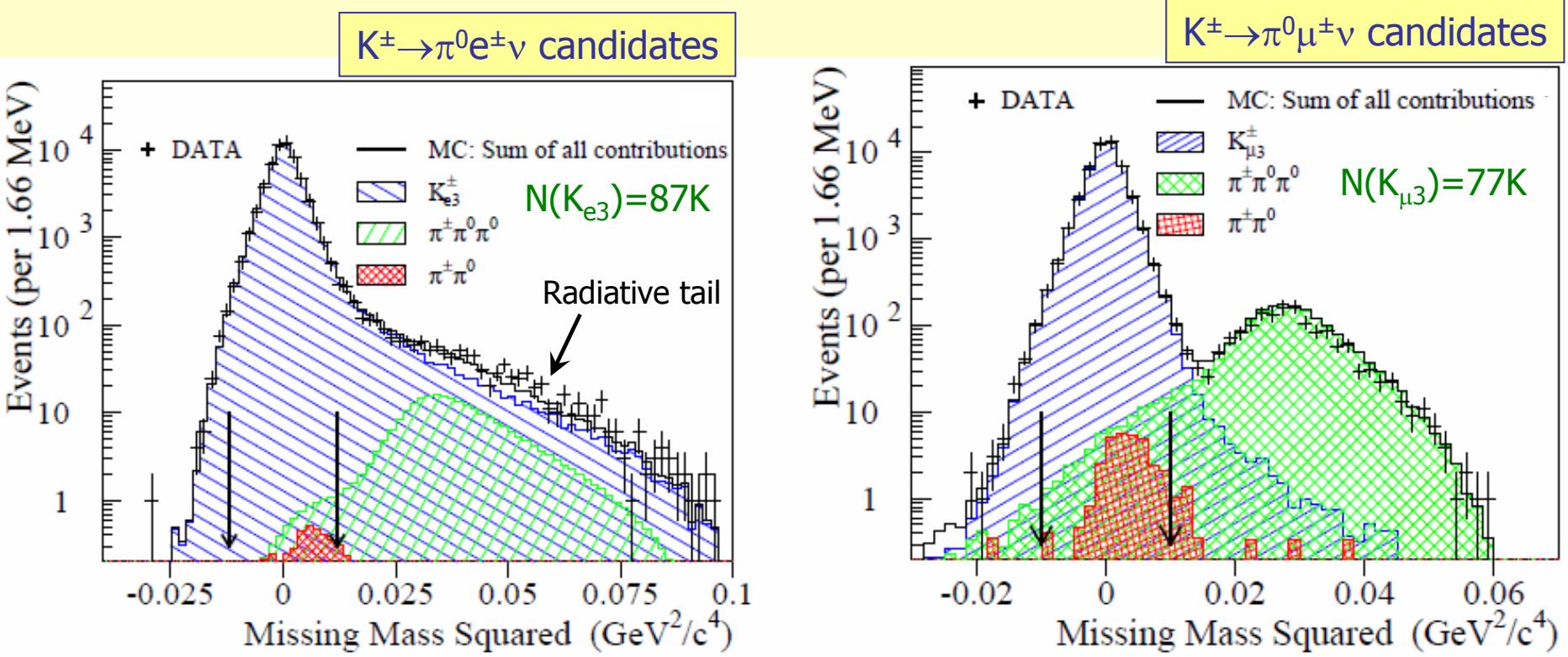
- BRs, lifetimes, form factor shapes;
- Much higher statistical precision than early measurements;
- Adequate treatment of radiative corrections;
- Correlations between measurements properly reported.

2008-beyond: Value of $|V_{us}|$ used for precision tests of the SM

FlaviaNet Kaon WG [www.lnf.infn.it/wg/vus]
arXiv:0801.1817 + update arXiv:1005.2323

Example: K^\pm from CERN NA48/2

Short special run in 2003: EPJ C50 (2007) 329



BR & τ measurements: K_L

FlaviaNet'10 fit: 21 input measurements
(published final results, mostly 2003-06)

KLOE: 4 absolute BRs, $BR(\pi^+\pi^-)/BR(K_{l3})$,
 $BR(\gamma\gamma)/BR(3\pi^0)$,

$\tau_{KL}=50.92(30)\text{ns}$ [2001/02 $K_L \rightarrow 3\pi^0$ sample]

$\tau_{KL}=50.56(25)\text{ns}$ [2004/05 preliminary/not used]

KTeV: 5 ratios of BRs, $BR(\pi^+\pi^-\gamma)/BR(\pi^+\pi^-)$
2 meas. of $BR(\pi^+\pi^-\gamma_{DE})/BR(\pi^+\pi^-)$

NA48: $BR(K_{e3})/BR(2\text{-track})$,
 $BR(\pi^+\pi^-)/BR(K_{l3})$, $BR(\gamma\gamma)/BR(3\pi^0)$

PDG: $BR(\pi^0\pi^0)/BR(\pi^+\pi^-)$

E731: $BR(\pi^+\pi^-\gamma_{DE})/BR(\pi^+\pi^-)$

Vosburgh (1972): τ_{KL}

Free parameters: 9 main BRs, lifetime τ_{KL} .

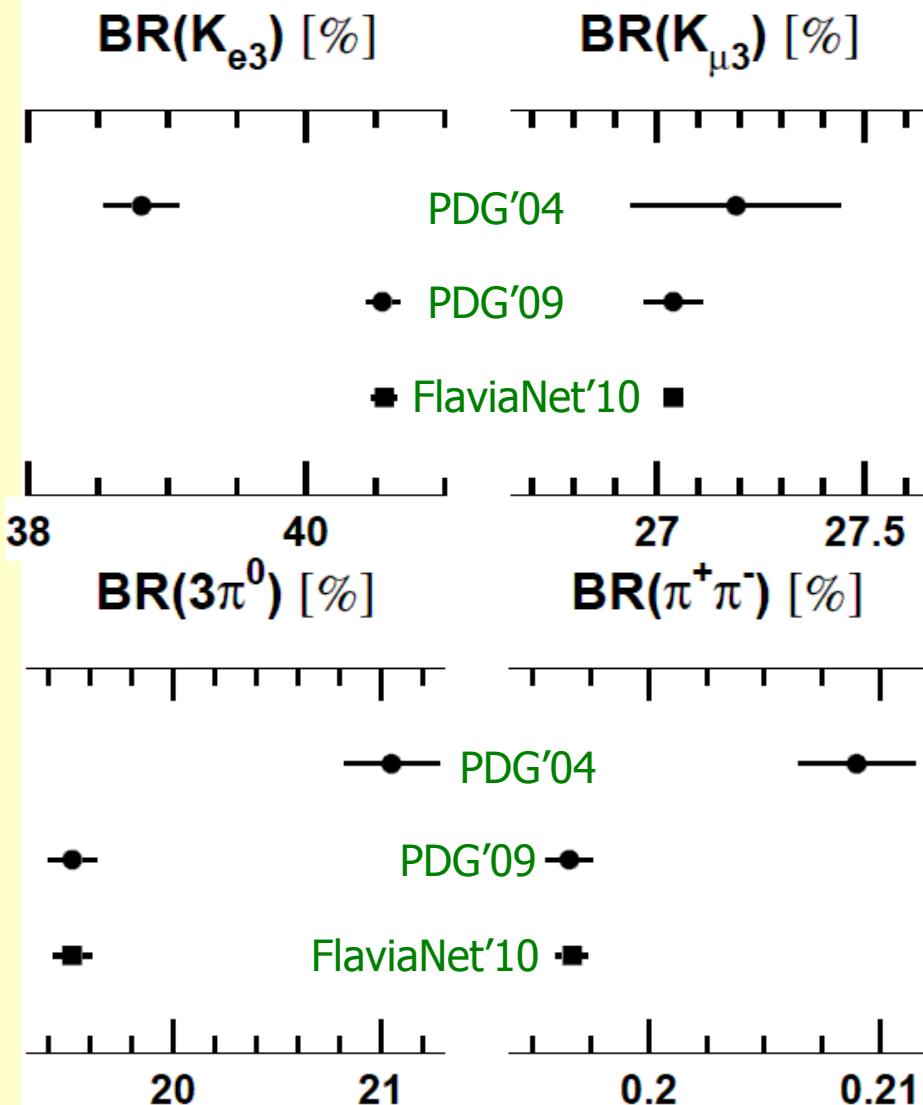
Constraint: $\sum BR_i = 1$.

Fit quality: $\chi^2/\text{ndf} = 19.8/12$ ($P=7.1\%$).

Cf. PDG'09: $\chi^2/\text{ndf} = 35.7/17$ ($P=0.5\%$).

~5 σ shifts wrt PDG'04: many new results,
elimination of old results with no radiative
corrections or not reporting correlations.

Evolution of main K_L BRs



BR & τ measurements: K^\pm

FlaviaNet'10 fit: 17 input measurements
 (mostly 2000s, but also earlier results)

KLOE: 5 absolute BRs, τ_K with $K^\pm \rightarrow \mu^\pm \nu$
 $[K^\pm \rightarrow 3\pi^\pm$ missing: analysis in progress]

NA48/2: $BR(K_{e3})/BR(\pi^\pm\pi^0)$, $BR(K_{\mu3})/BR(\pi^\pm\pi^0)$

E865: $BR(K_{e3})/BR(\pi^\pm\pi^0 + K_{\mu3} + K_{3\pi})$, π^0 Dalitz

KEK246: $BR(K_{e3})/BR(K_{\mu3})$

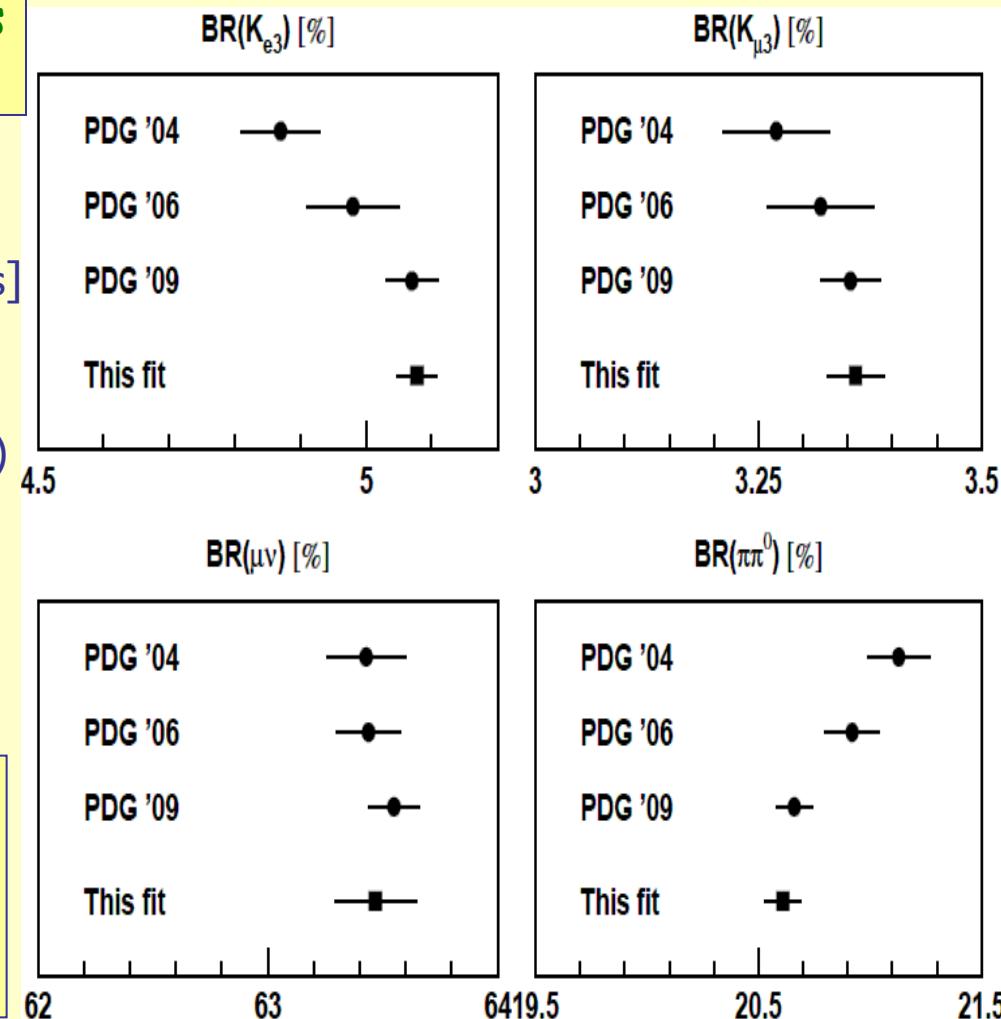
Earlier: $BR(K_{3\pi})$, 3 meas. of τ_K ,
 3 meas. of $BR(K \rightarrow \mu\nu)/BR(\pi^\pm\pi^0)$

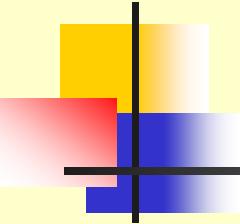
Free parameters: 6 main BRs, lifetime τ_K .
 Constraint: $\sum BR_i = 1$.

Fit quality: $\chi^2/ndf = 25.8/11$ ($P=0.7\%$).

Cf. PDG'09: $\chi^2/ndf = 52/24$ ($P=0.1\%$).

Evolution of main K^\pm BRs





BR & τ measurements: K_S

The most recent development: $|V_{us}|$ from K_S decays

KLOE (2006): PLB636 (2006) 173, EPJC48 (2006) 767

$$\begin{aligned} \text{BR}(K_S \rightarrow \pi^+ e^- \nu_e) / \text{BR}(K_S \rightarrow \pi^+ \pi^-) &= 10.19(13) \times 10^{-4} \\ \text{BR}(K_S \rightarrow \pi^+ \pi^-) / \text{BR}(K_S \rightarrow \pi^0 \pi^0) &= 2.2459(54) \end{aligned}$$

Rare decay!
13K candidates.
Error dominated
by statistics.

NA48 (2007): PLB653 (2007) 145

$$\text{BR}(K_S \rightarrow \pi^+ e^- \nu_e) / \text{BR}(K_L \rightarrow \pi^+ e^- \nu_e) = 0.993(34)$$

Lifetime from $K_S \rightarrow \pi^+ \pi^-$ decays

KTeV: PRD67 (2003) 012005 $\tau_{KS} = 89.580(130)$ ps

NA48: PLB537 (2008) 28 $\tau_{KS} = 89.598(70)$ ps

KLOE M.Antonelli, BEACH2010 $\tau_{KS} = 89.562(52)$ ps \leftarrow new! not used

Additional constraint:
assuming lepton universality
and using the measured form factors,
 $\text{BR}(K_{e3}) / \text{BR}(K_{\mu 3}) = 0.6655(15)$.

FlaviaNet'10 fit: 5 inputs.

Free parameters:

4 BRs ($\pi^+ \pi^-$, $\pi^0 \pi^0$, K_{e3} , $K_{\mu 3}$) + lifetime.

Constraint: $\sum \text{BR}_i = 1$.

$\chi^2/\text{ndf} = 0.015/1$ (P=90%)

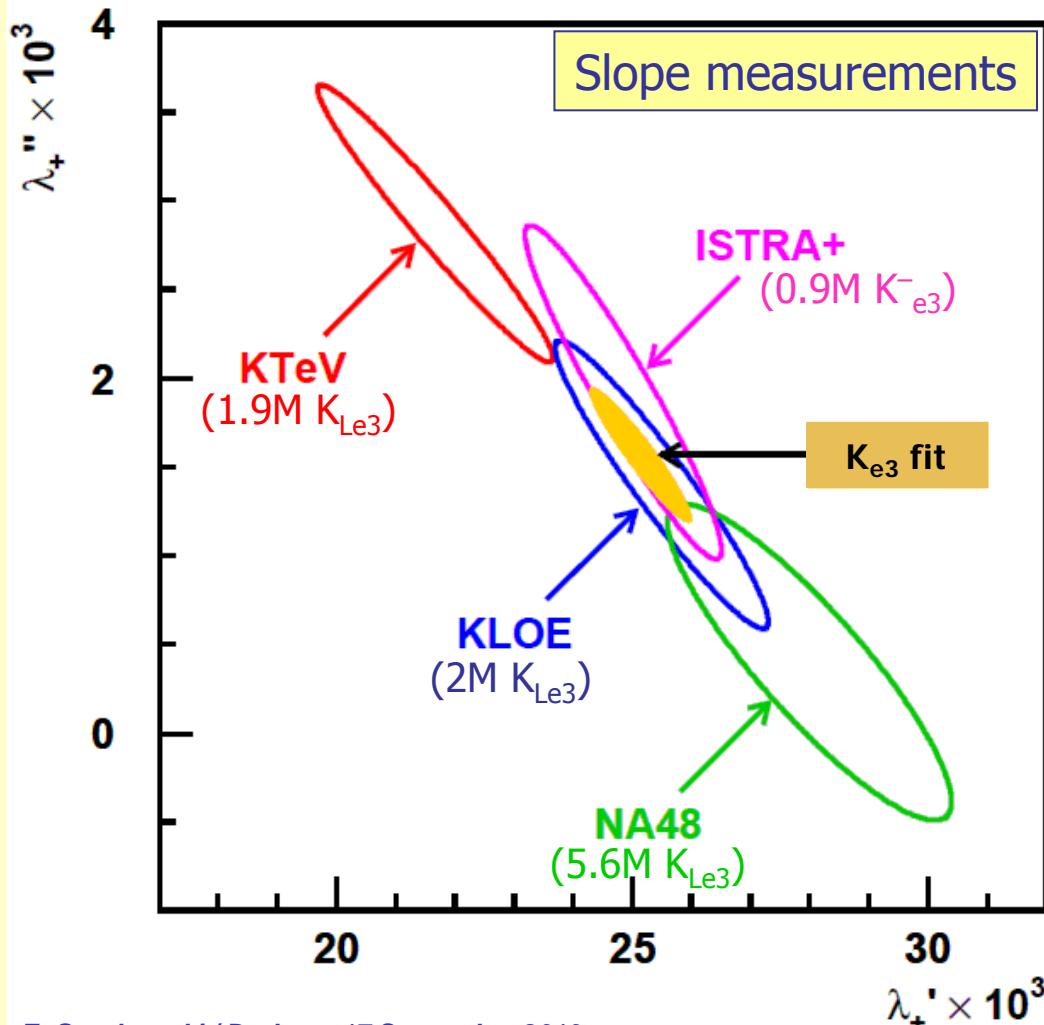
Fit result: $\text{BR}(K_{e3}) = 7.05(8) \times 10^{-4}$

$\leftarrow 1.1\%$

Form factors with K_{e3} : $(\lambda'_+, \lambda''_+)$

Polynomial parameterization:

$$f_+(t)/f_+(0) = 1 + \lambda'(t/m_\pi^2) + \frac{1}{2}\lambda''(t/m_\pi^2)^2 + \dots$$



Slope parameters $\times 10^3$

$$\lambda' = 25.1 \pm 0.9$$

$$\lambda'' = 1.6 \pm 0.4$$

$$\rho(\lambda', \lambda'') = -0.94$$

$$\chi^2/\text{ndf} = 3.5/6 \quad (\text{P}=51\%)$$

Phase Space Integrals:

$$I(K_{e3}^0) = 0.15463(21)$$

$$I(K_{e3}^\pm) = 0.15900(22)$$

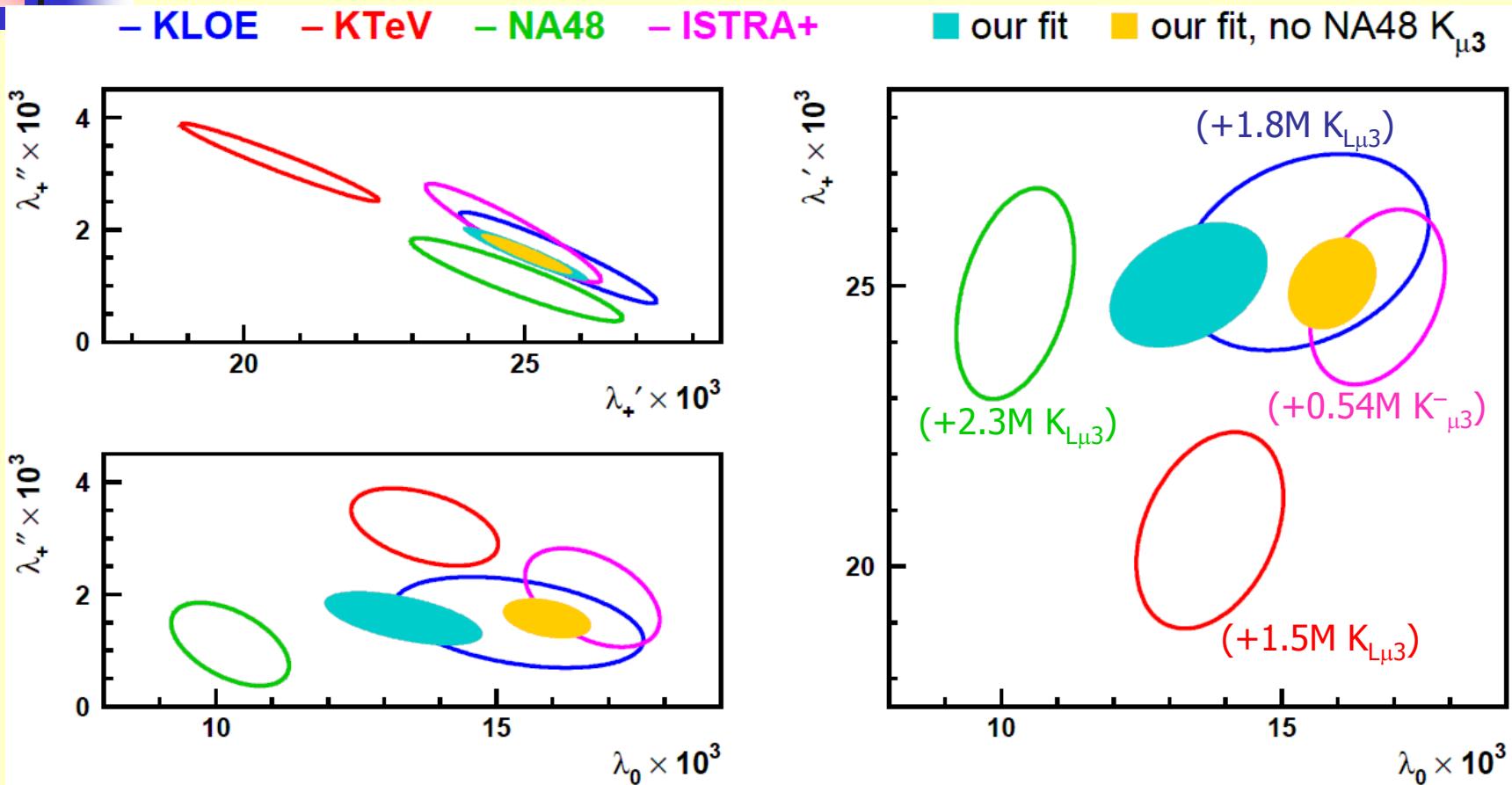
← 0.14%

Significance of λ'' slope: 4σ

Fits to pole and dispersive parameterizations lead to similar PSIs within 0.1%

Similar averaging is done for combined $K_{e3} + K_{\mu 3}$

Form factors, $K_{e3} + K_{\mu 3}$: $(\lambda'_+, \lambda''_+, \lambda_0)$



NA48 $K_{\mu 3}$ measurement is inconsistent and has been excluded

$\chi^2/\text{ndf}=5.6/5$ ($P=34\%$)

Phase Space Integrals:

$$I(K^0_{e3}) = 0.15457(20)$$

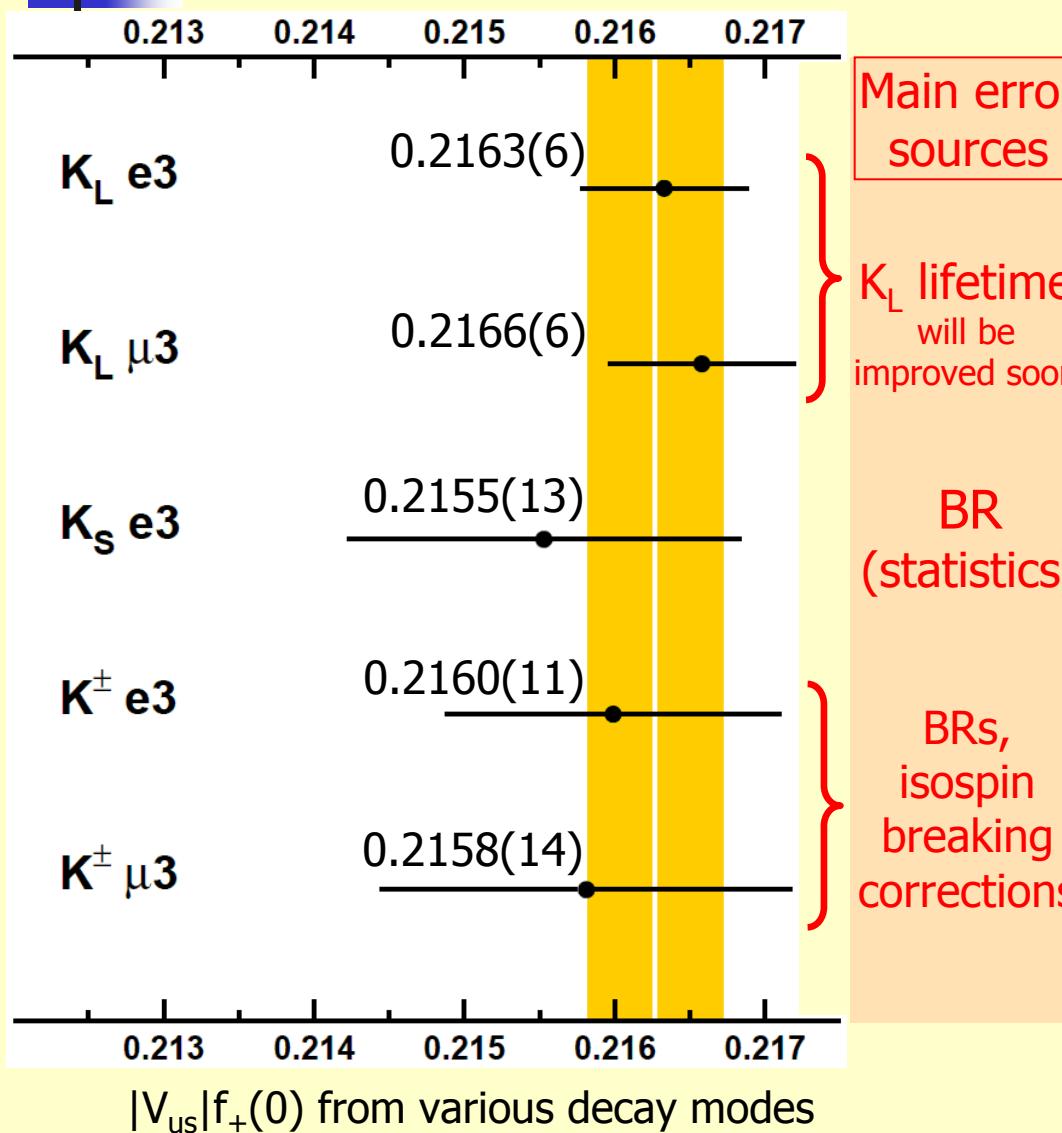
$$I(K^\pm_{e3}) = 0.15894(21)$$

$$I(K^0_{\mu 3}) = 0.10266(20)$$

$$I(K^\pm_{\mu 3}) = 0.12564(20)$$

+New NA48/2 $K^\pm_{\mu 3}$ result: M.Veltri, CKM2010

$|V_{us}|f_+(0)$ measurements with K_{l3}



Global fit result:
 $|V_{us}|f_+(0) = 0.2163(5)$

$\chi^2/ndf = 0.77/4$
 $(P=94\%)$

0.23% relative precision

Prospects:
KLOE-2/step-0 alone expect 0.14% precision on $|V_{us}|f_+(0)$ by improving on $BR(K_{Se3})$ and K_L, K^\pm lifetimes.
(arXiv:1003.3868)

NA48/NA62: improvements on K^+ BRs and FFs.

$|V_{us}|/|V_{ud}|$ from $K^+/\pi^+ \rightarrow \mu^+\nu$

SM ratio of radiation-inclusive leptonic decay widths:

$$\frac{\Gamma_{K\ell 2}}{\Gamma_{\pi\ell 2}} = \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{f_K^2}{f_\pi^2} \frac{m_K(1 - m_\ell^2/m_K^2)^2}{m_\pi(1 - m_\ell^2/m_\pi^2)^2} (1 + \delta_{EM})$$

Extracted

Lattice QCD input:

average of BMW, MILC'09, HPQCD/UKQCD

$f_K/f_\pi = 1.193(6)$ ← 0.5%

Experimental input

(1) from K^\pm BR fit

$\text{BR}(K_{\mu 2}) = 0.6347(18)$ ← 0.28%

$\tau(K^\pm) = 12.384(15)$ ns

(2) pion measurements (PDG 2009)

$\Gamma(\pi^\pm \rightarrow \mu^\pm \nu) = 38.408(7) \mu\text{s}^{-1}$

Experimental result:

$|V_{us}/V_{ud}| f_K/f_\pi = 0.2758(5) \leftarrow 0.18\%$

Long-distance EW correction

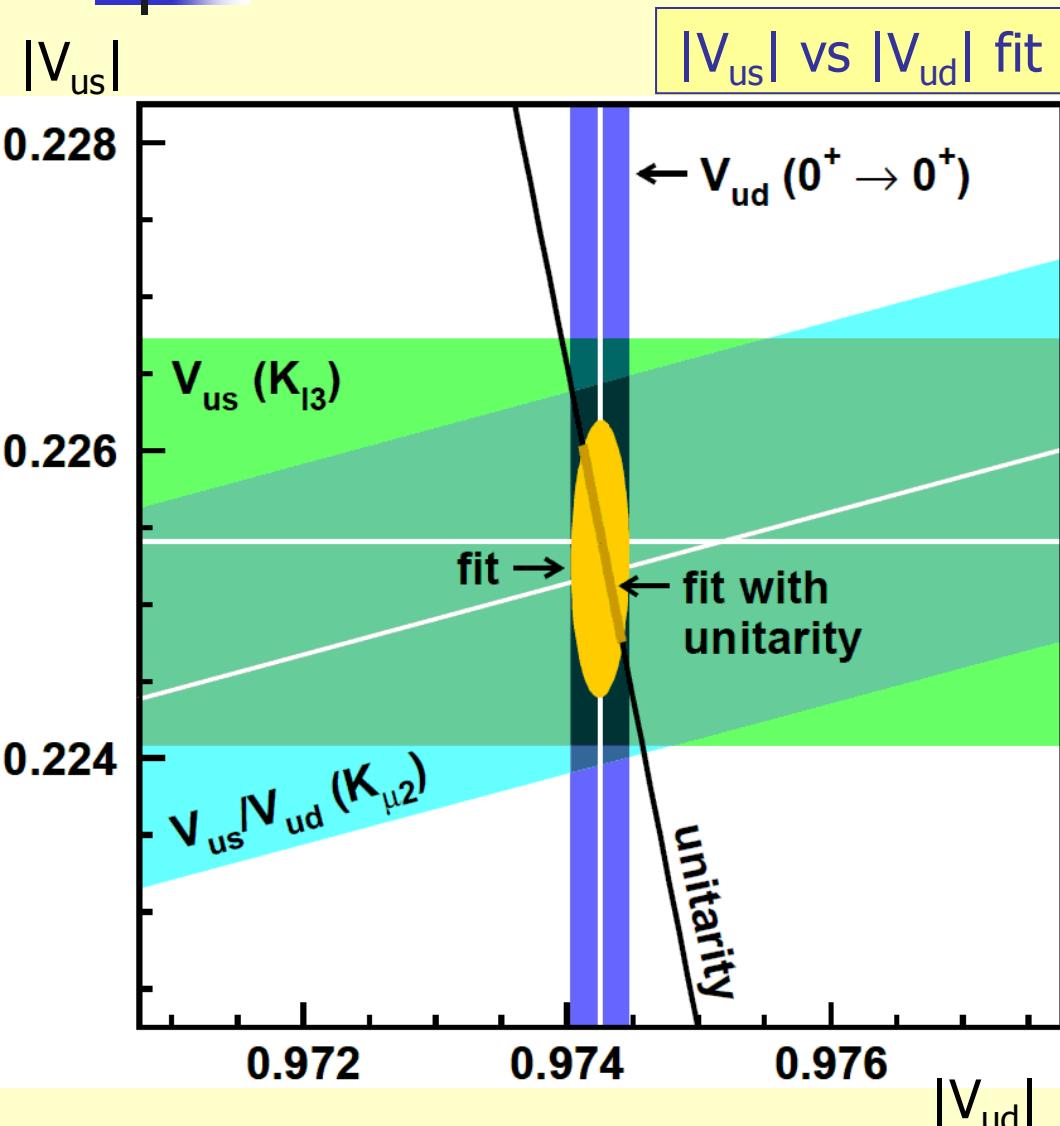
$\delta_{EM} = -0.0070(35)$

Dominant short-distance radiative effects are universal and cancel out:

$2\alpha/\pi \ln(M_Z/M_p) \sim 2.4\%$.

(Marciano, PRL 93 (2004) 231803)

CKM unitarity test (1)



Experimental input:

$$\begin{aligned} |V_{us}| f_+(0) &= 0.2163(5) \\ |V_{us}/V_{ud}| f_K/f_\pi &= 0.2758(5) \\ |V_{ud}| &= 0.97425(22) \end{aligned}$$

(average from 20 nuclear beta decays, Hardy & Towner, PRC79 (2009) 055502)

$\sim 0.2\%$

Lattice input:

$$\begin{aligned} f_+(0) &= 0.959(6) \quad 0.6\% \\ f_K/f_\pi &= 1.193(6) \end{aligned}$$

Fit result: 0.4% error dominated by theory

$$|V_{us}| = 0.2253(9)$$

Fit imposing unitarity:

$$|V_{us}| = 0.2254(6)$$

CKM unitarity test:

$$|V_{us}|^2 + |V_{ud}|^2 - 1 = -0.0001(6)$$

$|V_{us}|$ from τ decays

[BaBar, N.Gagliardi, BEACH2010]:

$\text{BR}(\tau \rightarrow K\nu)/\text{BR}(\tau \rightarrow \pi\nu): |V_{us}| = 0.2255(23)$.

Inclusive $\tau \rightarrow s$: $|V_{us}| = 0.2151(26)$,

3.7σ below the $K+\pi$ result.

CKM unitarity test (2)

Another view on the unitarity test:
comparison of weak couplings
from K decay and muon decay.

$$G_\mu = G_{CKM} = G_\mu (|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2)^{1/2} = 1.166371(6) \times 10^{-5} \text{ GeV}^{-2}$$

$$1.16633(35) \times 10^{-5} \text{ GeV}^{-2}$$

From muon lifetime: $\tau_\mu \sim 1/G_F^2$.
MuLan collaboration,
PRL 99 (2007) 032001

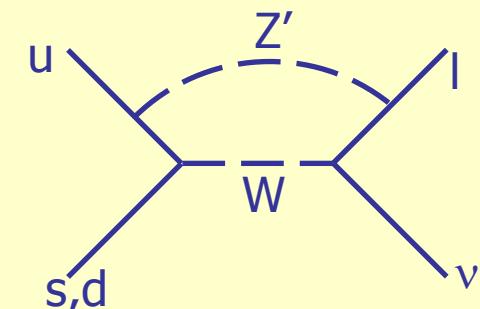
Example: additional Z' gauge bosons

W. J. Marciano, A. Sirlin, PRD 35 (1987) 1672

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \approx 1 + 0.005 \ln(M^2(Z')/(M^2(Z') - M^2(W)))$$

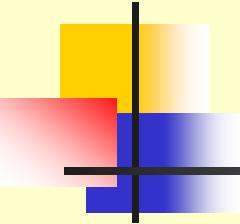
$\rightarrow M(Z') > \sim 400 \text{ GeV} @ 90\% \text{ CL}$

Other implications (exotic μ decays, heavy quarks and leptons)
are discussed in arXiv:0907.5386



Model-independent constraint on the effective scale of NP operators:
Cirigliano, Jenkins, González-Alonso, NPB 830 (2010) 95

$$\Delta_{CKM} = |V_{us}|^2 + |V_{ud}|^2 - 1 = -0.0001(6) \rightarrow \Lambda > 11 \text{ TeV} (90\% \text{ CL})$$



K_{l3} : lepton universality test

Comparison of $|V_{us}|$ determined from
 K_{e3} vs $K_{\mu 3}$ decays

$$r_{\mu e} = \frac{[|V_{us}|f_+(0)]_{\mu 3, \text{ exp}}^2}{[|V_{us}|f_+(0)]_{e3, \text{ exp}}^2} = \frac{\Gamma_{K\mu 3}}{\Gamma_{Ke3}} \frac{I_{e3} (1 + 2\delta_{\text{EM}}^{K_e})}{I_{\mu 3} (1 + 2\delta_{\text{EM}}^{K_\mu})} = (g_\mu/g_e)^2 = 1$$

SM
↓
↑

Experimental results

$$K^\pm: \quad r_{\mu e} = 0.998(9)$$

$$K^0: \quad r_{\mu e} = 1.003(5)$$

$$\rightarrow r_{\mu e} = 1.002(4)$$

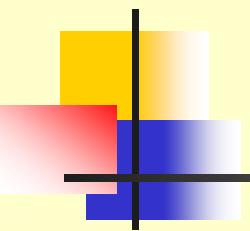
lepton coupling
at the $W \rightarrow l\nu$ vertex

Cf. other measurements:

$$\pi \rightarrow l\nu: \quad r_{\mu e} = 1.0042(33) \quad (\text{PRD } 76 (2007) 095017)$$

$$\tau \rightarrow l\nu\nu: \quad r_{\mu e} = 1.000(4) \quad (\text{Rev.Mod.Phys. } 78 (2006) 1043)$$

The sensitivity in kaon sector approaches those of the other measurements.



Leptonic kaon decays

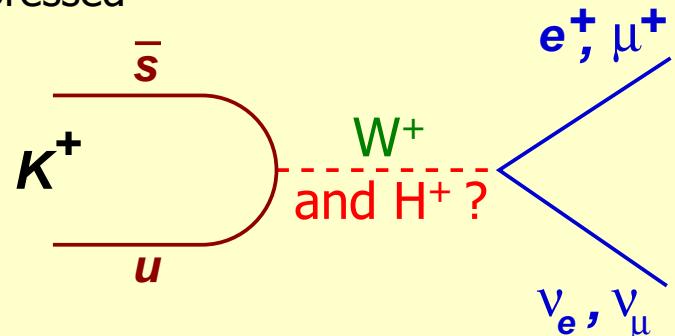
$$(K^+ \rightarrow l^+ \nu)$$

- Test of SM with $\Gamma(K_{\mu 2})/\Gamma(\pi_{\mu 2})$:
NP contributions to charged weak currents;
charged Higgs boson exchange in SM extensions with 2 Higgs doublets.
- Lepton flavour violation test in loop amplitude: $\Gamma(K_{e 2})/\Gamma(K_{\mu 2})$.

Leptonic meson decays: $P^+ \rightarrow l^+ \nu$

Angular momentum conservation \rightarrow SM contribution is suppressed

$$\Gamma(P^+ \rightarrow l^+ \nu) = \frac{G_F^2 M_P M_l^2}{8\pi} \left(1 - \frac{M_l^2}{M_P^2}\right)^2 f_P^2 |V_{qq'}|^2$$



Models with 2 Higgs doublets (2HDM-II including SUSY):
sizeable charged Higgs (H^\pm) exchange contributions

PRD48 (1993) 2342; Prog.Theor.Phys. 111 (2004) 295

(numerical examples for $M_H=500\text{GeV}/c^2$, $\tan\beta = 40$)

$\pi^+ \rightarrow l\nu$:	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_\pi/m_H)^2 m_d/(m_u+m_d)$	$\tan^2\beta \approx -2 \times 10^{-4}$
$K^+ \rightarrow l\nu$:	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_K/m_H)^2 \tan^2\beta$	$\approx -0.3\%$
$D_s^+ \rightarrow l\nu$:	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_D/m_H)^2 (m_s/m_c) \tan^2\beta$	$\approx -0.4\%$
$B^+ \rightarrow l\nu$:	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_B/m_H)^2 \tan^2\beta$	$\approx -30\%$

H^\pm exchange in $B^+ \rightarrow \tau^+ \nu$: (R.Barlow, CKM 2010)

BaBar+Belle: $\text{Br}_{\text{exp}}(B \rightarrow \tau \nu) = (1.64 \pm 0.34) \times 10^{-4}$
(HFAG)

Standard Model: $\text{Br}_{\text{SM}}(B \rightarrow \tau \nu) = (1.20 \pm 0.25) \times 10^{-4}$
(f_B from HPQCD, $|V_{ub}|$ from HFAG)

$$\Rightarrow \Delta\Gamma/\Gamma_{\text{SM}} = 0.37 \pm 0.35$$

$K_{\mu 2}$: sensitivity to new physics

Comparison of $|V_{us}|$ determined from helicity-suppressed $K_{\mu 2}$ decays vs helicity allowed K_{l3} decays

To reduce uncertainties of hadronic and EM corrections to $K_{\mu 2}$:

average from nuclear β decays,
PRC79 (2009) 055502

$$R_{\mu 23} = \left(\frac{f_K/f_\pi}{f_+(0)} \right)^{-1} \left(\left| \frac{V_{us}}{V_{ud}} \right| \frac{f_K}{f_\pi} \right)_{\mu 2} \frac{\left| V_{ud} \right|_{0^+ \rightarrow 0^+}}{\left[|V_{us}| f_+(0) \right]_{\ell 3}}$$

Lattice QCD input
Measured with $K_{\mu 2}/\pi_{\mu 2}$
Measured with $K \rightarrow \pi \mu \nu$

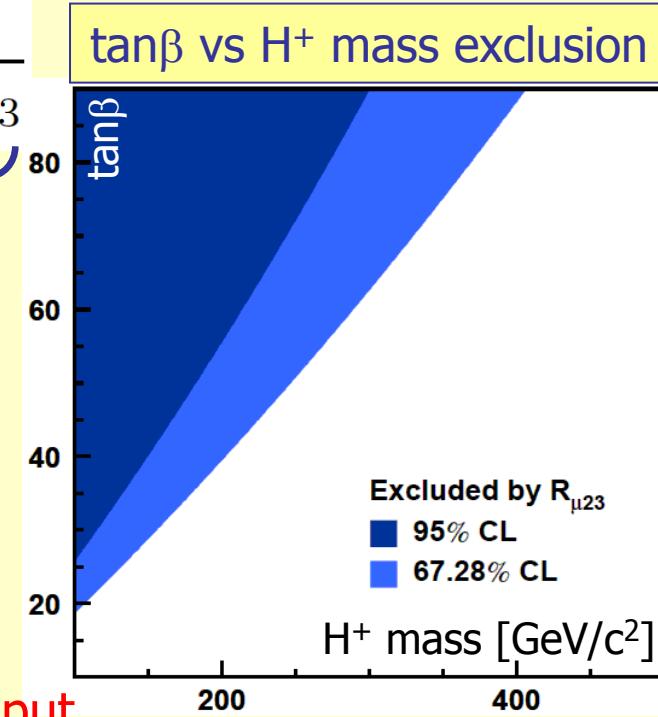
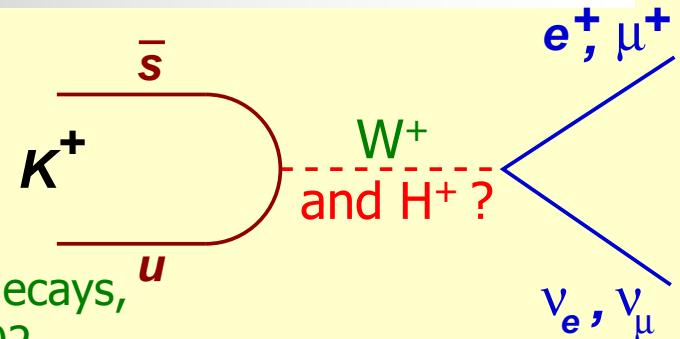
SM expectation: $R_{\mu 23} = 1$.

Charged Higgs mediated currents lead to

$$R_{\mu 23} \approx \left| 1 - \frac{m_{K^+}^2}{m_{H^+}^2} \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|$$

Experiment: $R_{\mu 23} = 0.999(7)$, limited by lattice QCD input.

(Flavianet Kaon WG, arXiv:1005.2323)

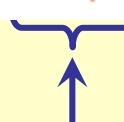


$R_K = K_{e2}/K_{\mu 2}$ in the SM

Observable sensitive to Lepton Flavour Violation and its SM expectation:

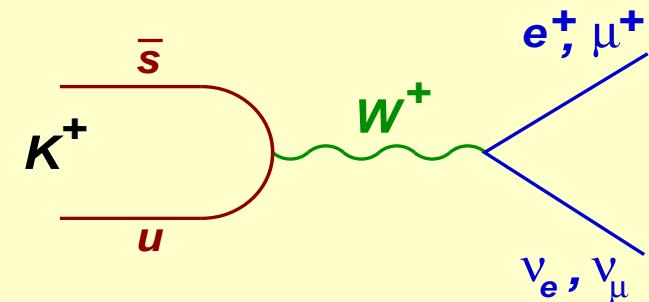
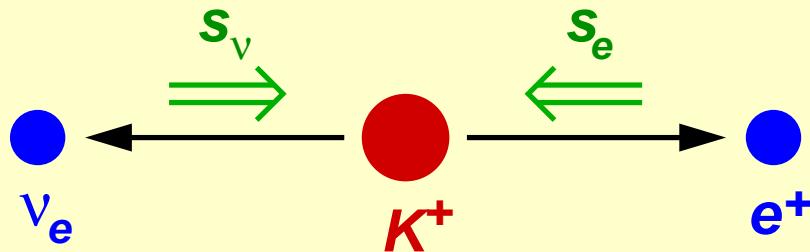
$$R_K = \frac{\Gamma(K^\pm \rightarrow e^\pm \nu)}{\Gamma(K^\pm \rightarrow \mu^\pm \nu)} = \frac{m_e^2}{m_\mu^2} \cdot \left(\frac{m_K^2 - m_e^2}{m_K^2 - m_\mu^2} \right)^2 \cdot (1 + \delta R_K^{\text{rad.corr.}})$$

(similarly, R_π in the pion sector)



Helicity suppression: $f \sim 10^{-5}$

Radiative correction (few %)
due to $K^+ \rightarrow e^+ \nu \gamma$ (IB) process,
by definition included into R_K



- SM prediction: excellent sub-permille accuracy:
not obstructed by hadronic uncertainties.
- Measurements of R_K and R_π have long been considered as tests of lepton universality.
- Understood recently: helicity suppression of R_K might enhance sensitivity to non-SM effects to an experimentally accessible level.

$$R_K^{\text{SM}} = (2.477 \pm 0.001) \times 10^{-5}$$

$$R_\pi^{\text{SM}} = (12.352 \pm 0.001) \times 10^{-5}$$

Phys. Lett. 99 (2007) 231801

$R_K = K_{e2}/K_{\mu 2}$ beyond the SM

2HDM – tree level

(including SUSY)

K_{l2} can proceed via exchange of charged Higgs H^\pm instead of W^\pm
 \rightarrow Does not affect the ratio R_K

2HDM – one-loop level

Dominant contribution to R_K : H^\pm mediated LFV (rather than LFC) with emission of ν_τ
 $\rightarrow R_K$ enhancement can be experimentally accessible

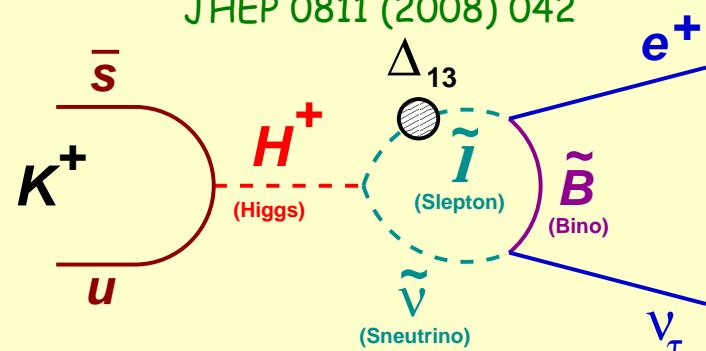
$$R_K^{\text{LFV}} \approx R_K^{\text{SM}} \left[1 + \left(\frac{m_K^4}{M_{H^\pm}^4} \right) \left(\frac{m_\tau^2}{M_e^2} \right) |\Delta_{13}|^2 \tan^6 \beta \right]$$

Up to $\sim 1\%$ effect in large (but not extreme) $\tan\beta$ regime with a massive H^\pm

Example:

$(\Delta_{13}=5\times 10^{-4}, \tan\beta=40, M_H=500 \text{ GeV}/c^2)$
lead to $R_K^{\text{MSSM}} = R_K^{\text{SM}}(1+0.013)$.

PRD 74 (2006) 011701,
JHEP 0811 (2008) 042



Analogous SUSY effect
in pion decay is suppressed
by a factor $(M_\pi/M_K)^4 \approx 6 \times 10^{-3}$
(see also PRD76 (007) 095017)

Large effects in B decays
due to $(M_B/M_K)^4 \sim 10^4$:

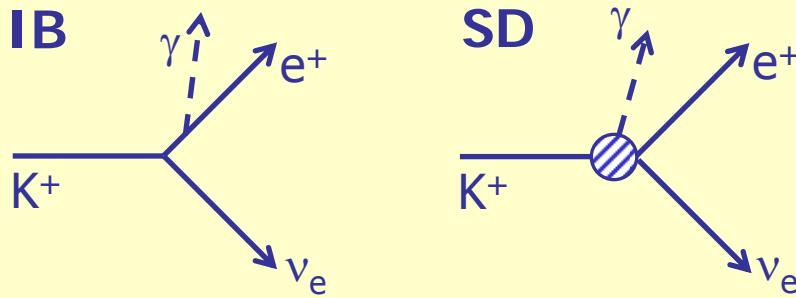
$B_{\mu\nu}/B_{\tau\nu} \rightarrow \sim 50\%$ enhancement;

$B_{ev}/B_{\tau\nu} \rightarrow$ enhanced by
 \sim one order of magnitude.

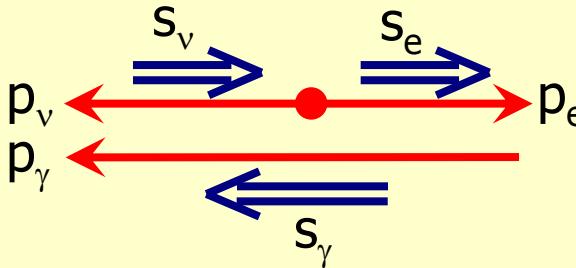
Out of reach: $\text{Br}^{\text{SM}}(B_{ev}) \approx 10^{-11}$

Radiative $K^+ \rightarrow e^+ \nu \gamma$ process

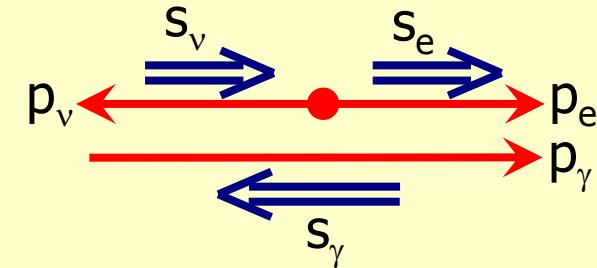
R_K is inclusive of IB radiation by definition.
SD radiation is a background. INT is negligible.



SD⁺: positive γ helicity

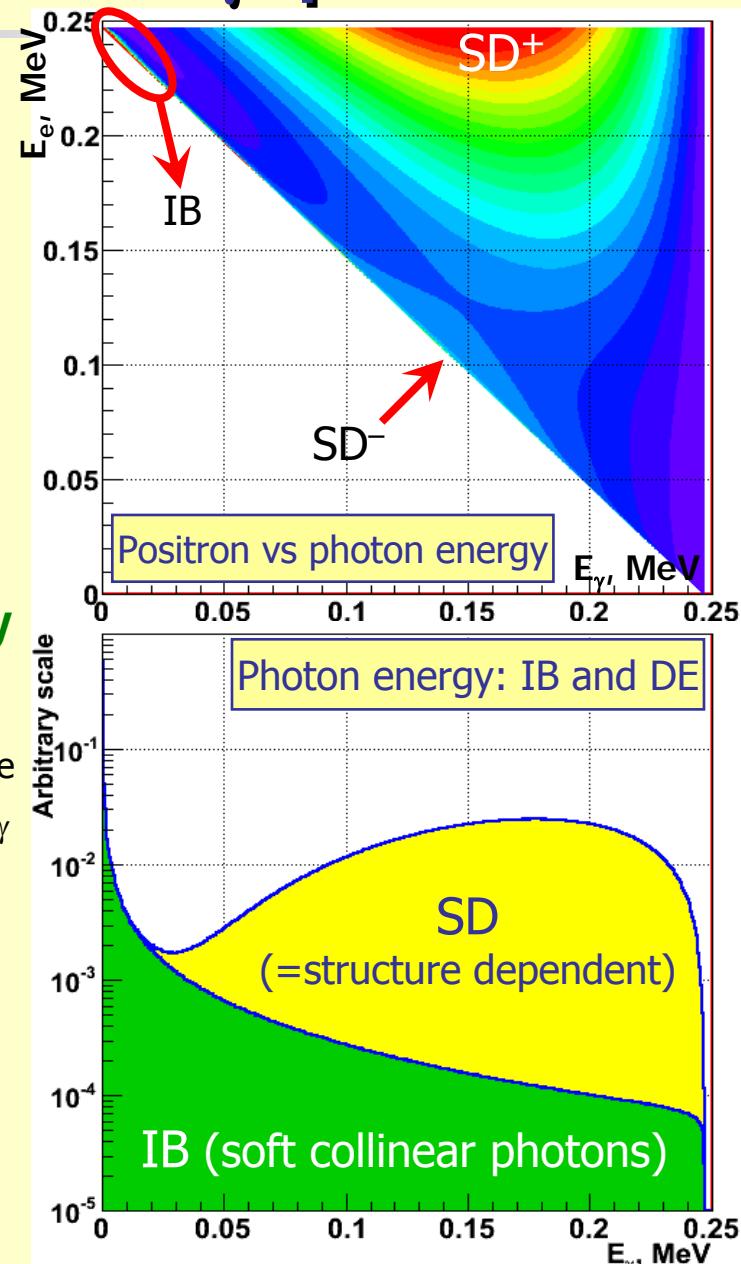


SD⁻: negative γ helicity



SD radiation is not helicity suppressed.

KLOE measurement of the form factor leads to
 $BR(SD^+, \text{full phase space}) = (1.37 \pm 0.06) \times 10^{-5}$.
 (EPJC64 (2009) 627)



NA62: decay-in-flight technique

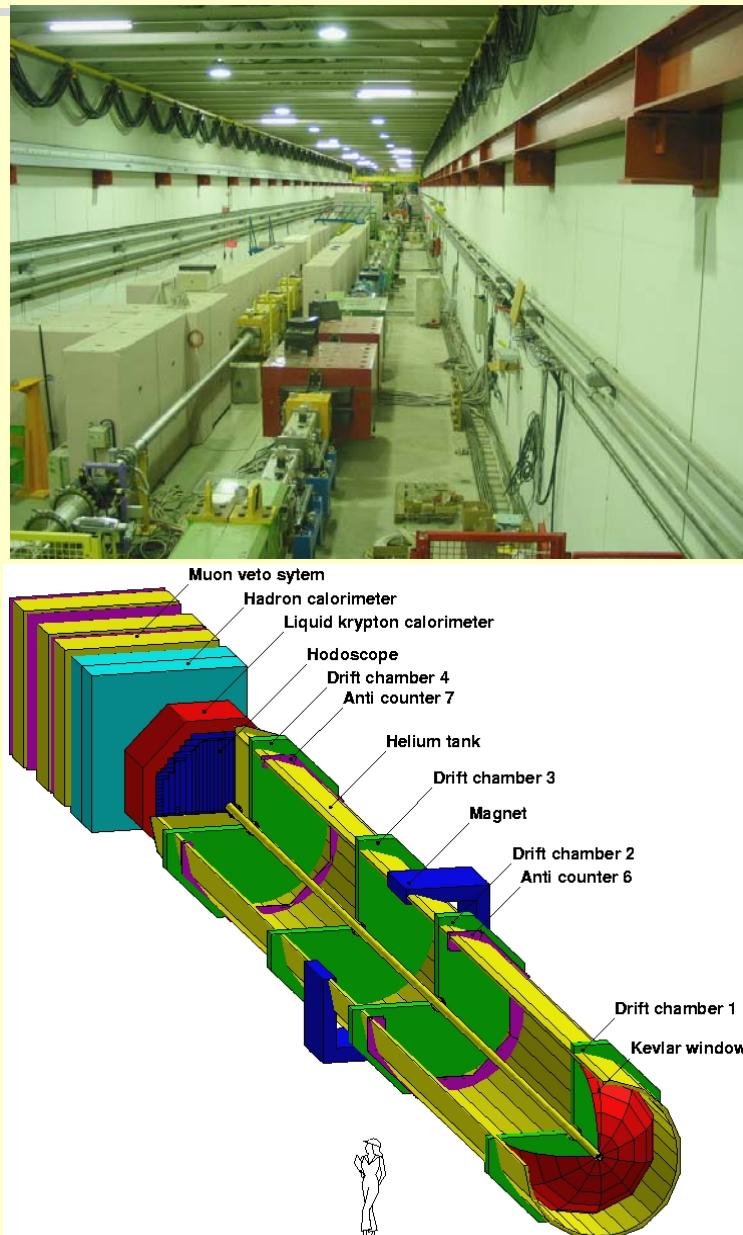
Narrow momentum band K^+ beam:

$$P_K = (74.0 \pm 1.6) \text{ GeV/c}$$

- Four months in 2007 (23/06–22/10):
 $\sim 4 \times 10^5$ SPS spills,
 $\sim 5 \times 10^{10} K^+$ decays in 114m long vacuum tank

Principal subdetectors:

- Magnetic spectrometer (4 DCHs):
4 views/DCH: redundancy \Rightarrow efficiency;
 $\Delta p/p = 0.47\% + 0.020\% * p$ [GeV/c]
- Hodoscope
fast trigger, precise time measurement (150ps).
- Liquid Krypton EM calorimeter (LKr)
High granularity, quasi-homogeneous;
 $\sigma_E/E = 3.2\%/E^{1/2} + 9\%/E + 0.42\%$ [GeV];
 $\sigma_x = \sigma_y = 0.42/E^{1/2} + 0.6\text{mm}$ (1.5mm@10GeV).



NA62: K_{e2} vs $K_{\mu 2}$ selection

Large common part (topological similarity)

- one reconstructed track (lepton candidate);
- geometrical acceptance cuts;
- K decay vertex: closest approach of lepton track & nominal kaon axis;
- veto extra LKr energy deposition clusters;
- track momentum: $13\text{GeV}/c < p < 65\text{GeV}/c$.

Kinematic identification

missing mass $M_{miss}^2 = (P_K - P_l)^2$

P_K : average measured with $K_{3\pi}$ decays

→ Sufficient $K_{e2}/K_{\mu 2}$ separation at $p_{track} < 25\text{GeV}/c$

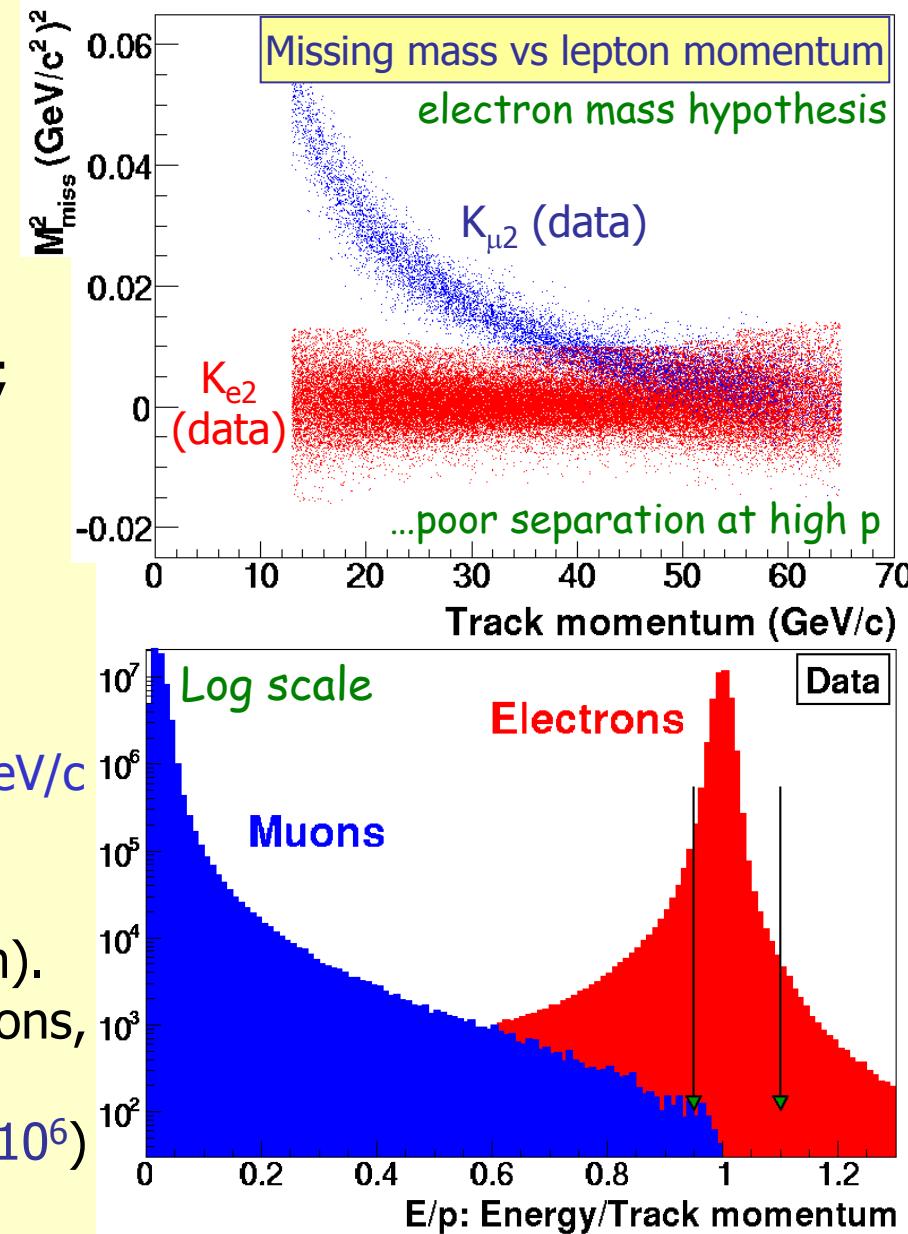
Lepton identification

$E/p = (\text{LKr energy deposit}/\text{track momentum})$.

(0.90 to 0.95) $< E/p < 1.10$ for electrons,

$E/p < 0.85$ for muons.

→ Powerful μ^\pm suppression in e^\pm sample ($\sim 10^6$)



NA62: $K_{\mu 2}$ background

Main background source

Muon “catastrophic” energy loss in LKr by emission of energetic bremsstrahlung photons.
 $P_{\mu e} \sim 3 \times 10^{-6}$ (and momentum-dependent).

$P_{\mu e} / R_K \sim 10\%$:
 $K_{\mu 2}$ decays represent a major background

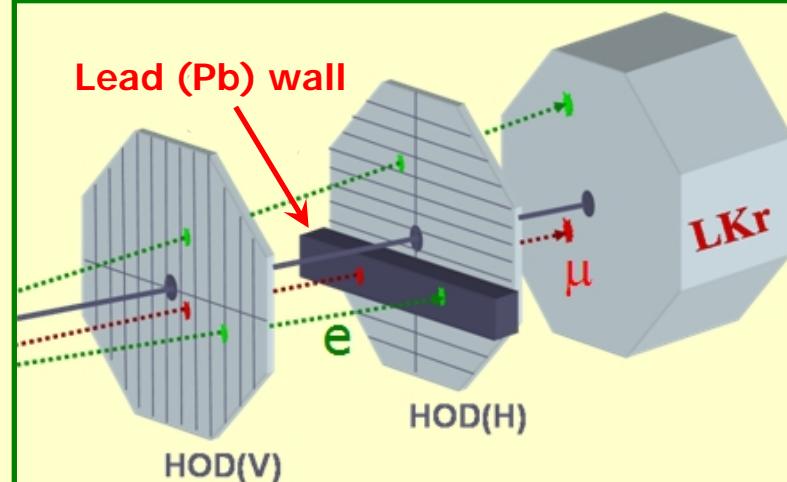
Direct measurement of $P_{\mu e}$

Pb wall ($9.2X_0$) in front of LKr: suppression of $\sim 10^{-4}$ positron contamination due to $\mu \rightarrow e$ decay.

$K_{\mu 2}$ candidates, track traversing Pb, $p > 30\text{GeV}/c$, $E/p > 0.95$: positron contamination $< 10^{-8}$.

$P_{\mu e}$ is modified by the Pb wall:

- ionization losses in Pb (low p);
- bremsstrahlung in Pb (high p).



Thickness:

$\sim 10X_0$ (Pb+Fe)

Width:

240cm (=HOD size)

Height:

18cm (=3 counters)

Area:

$\sim 20\%$ of HOD area

Duration:

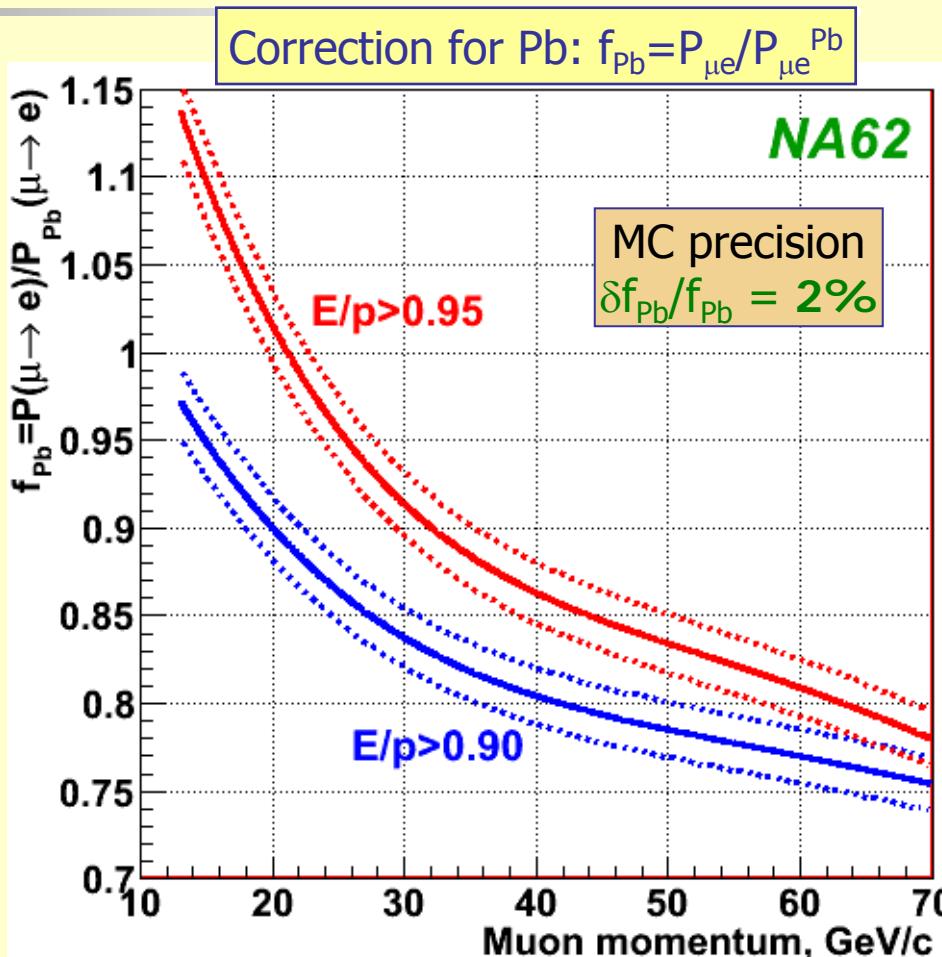
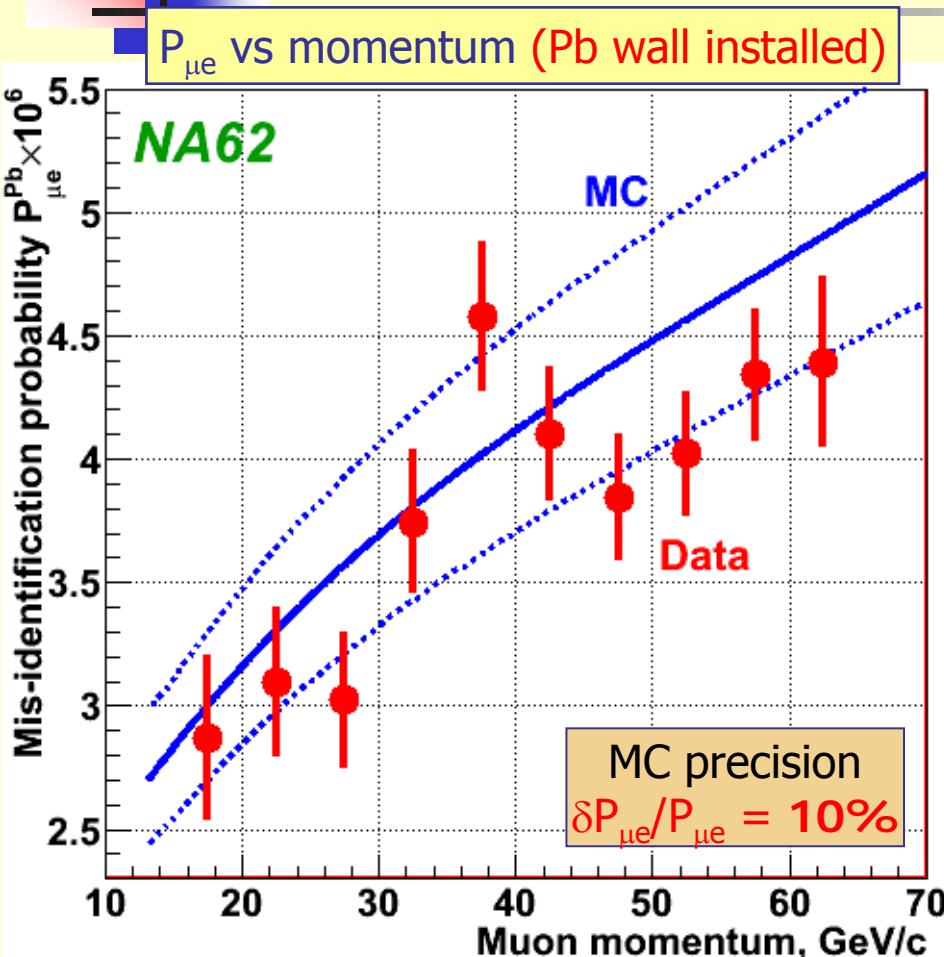
$\sim 50\%$ of R_K runs

+ special muon runs

The correction $f_{\text{Pb}} = P_{\mu e} / P_{\mu e}^{\text{Pb}}$ is evaluated with a dedicated simulation

[Muon bremsstrahlung:
 Phys. Atom. Nucl. 60 (1997) 576]

NA62: muon mis-identification

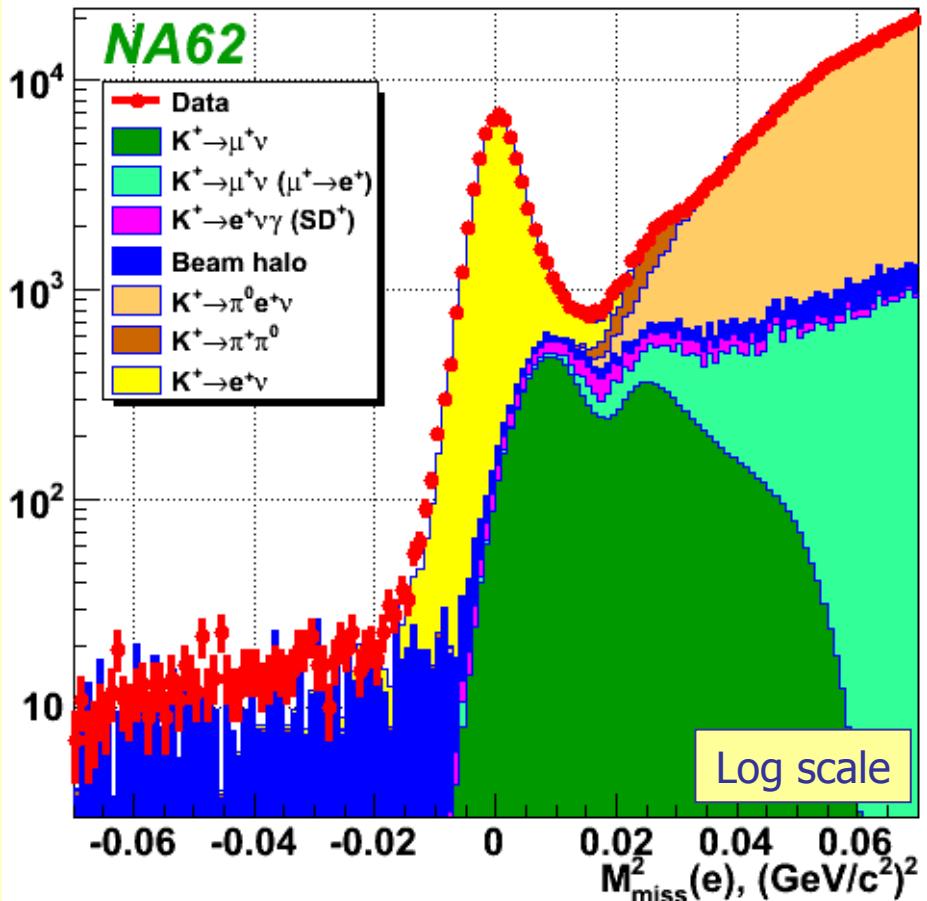
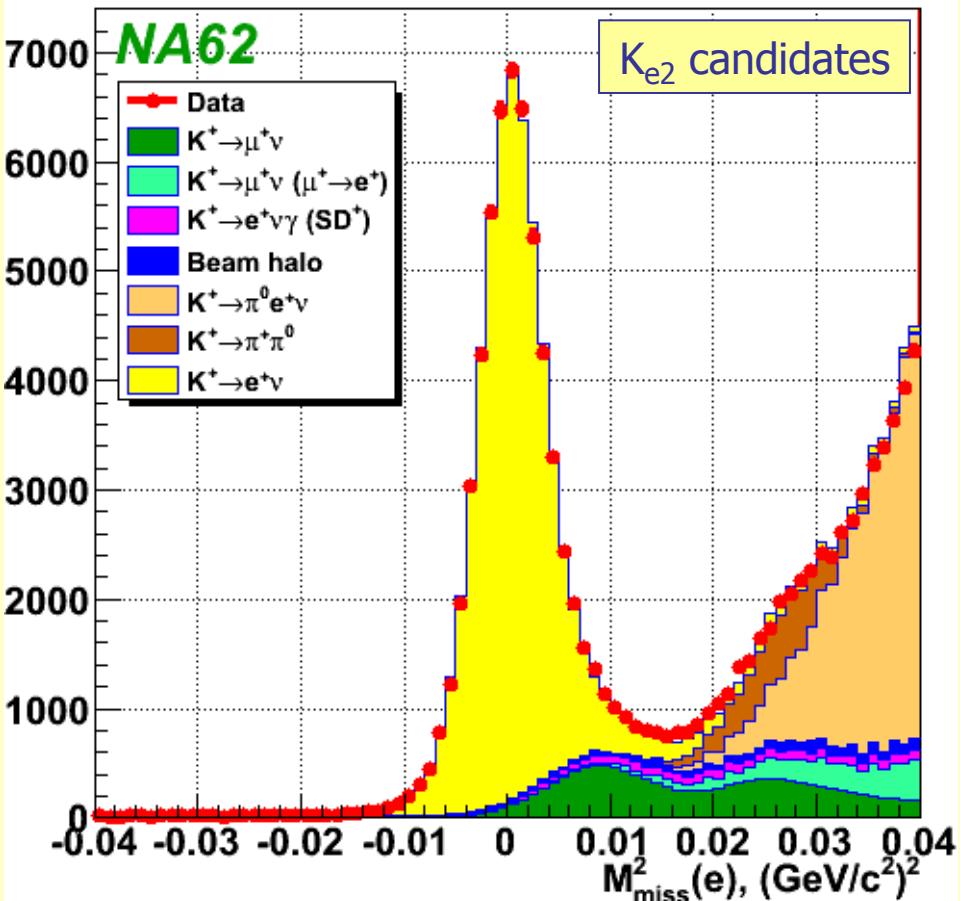


Result: $B/(S+B) = (6.10 \pm 0.22)\%$

Uncertainty is ~ 3 times smaller than the one obtained solely from simulation

Uncertainties
 Limited data sample (0.16%);
 MC correction (0.12%);
 M_{miss}^2 vs P_{track} correlation (0.08%).

NA62: 40% data set



59,963 $K^+ \rightarrow e^+\nu$ candidates.
 Positron ID efficiency: $(99.27 \pm 0.05)\%$.
 $B/(S+B) = (8.8 \pm 0.3)\%$.

cf. KLOE: 13.8K candidates (K^+ and K^-),
 ~90% electron ID efficiency, 16% background

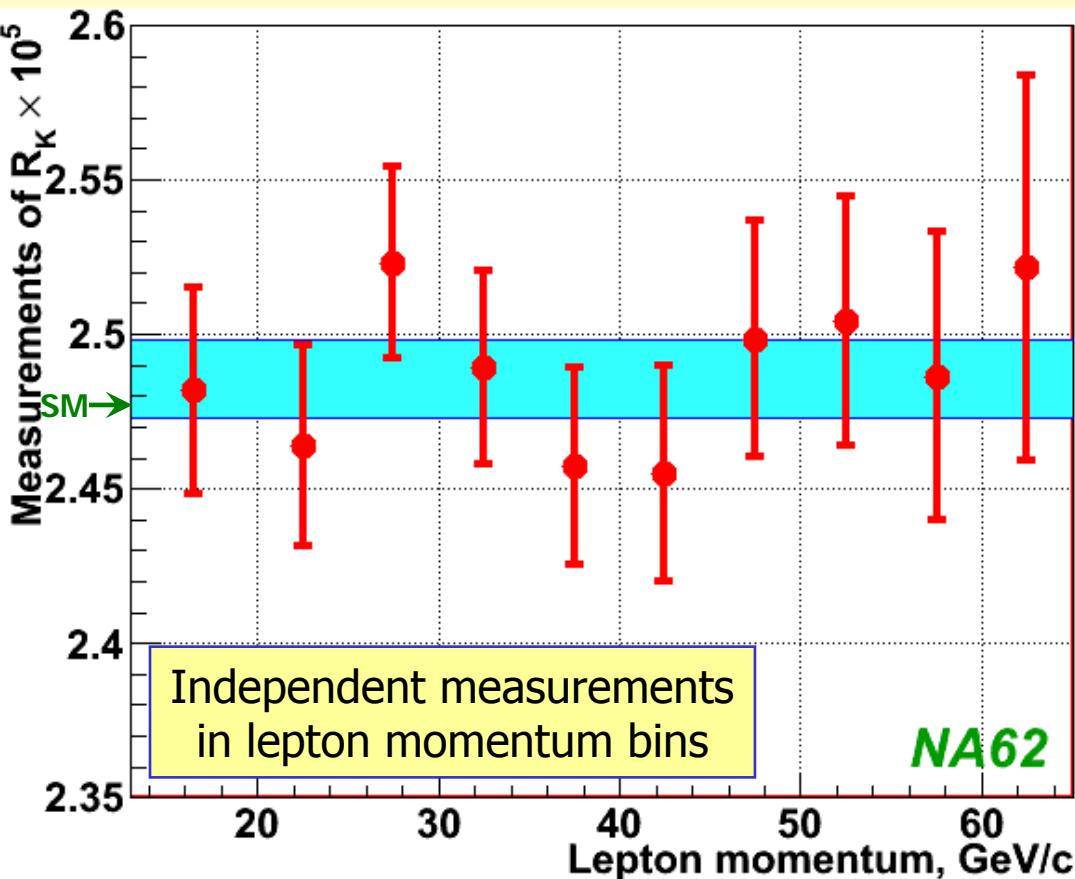
NA62 estimated total K_{e2} sample:
 ~130K K^+ & ~20K K^- candidates.
 Proposal (CERN-SPSC-2006-033):
 150K candidates

NA62 final result (40% data set)

(new: June 2010)

$$R_K = (2.486 \pm 0.011_{\text{stat}} \pm 0.007_{\text{syst}}) \times 10^{-5}$$

$$= (2.486 \pm 0.013) \times 10^{-5}$$



(systematic errors included, partially correlated)

Backgrounds

Source	$B/(S+B)$
$K_{\mu 2}$	$(6.10 \pm 0.22)\%$
$K_{\mu 2} (\mu \rightarrow e)$	$(0.27 \pm 0.04)\%$
$K_{e2\gamma} (\text{SD}^+)$	$(1.15 \pm 0.17)\%$
Beam halo	$(1.14 \pm 0.06)\%$
$K_{e3(D)}$	$(0.06 \pm 0.01)\%$
$K_{2\pi(D)}$	$(0.06 \pm 0.01)\%$
Total	$(8.78 \pm 0.29)\%$

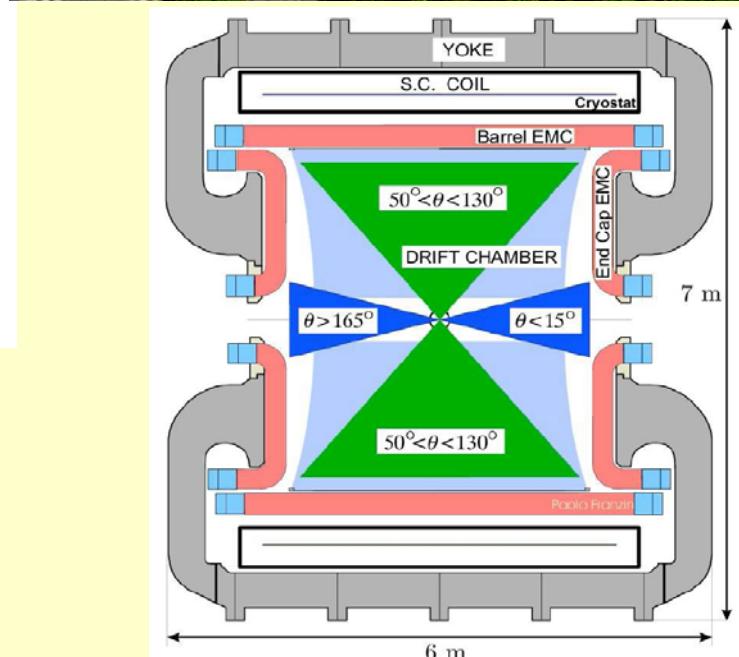
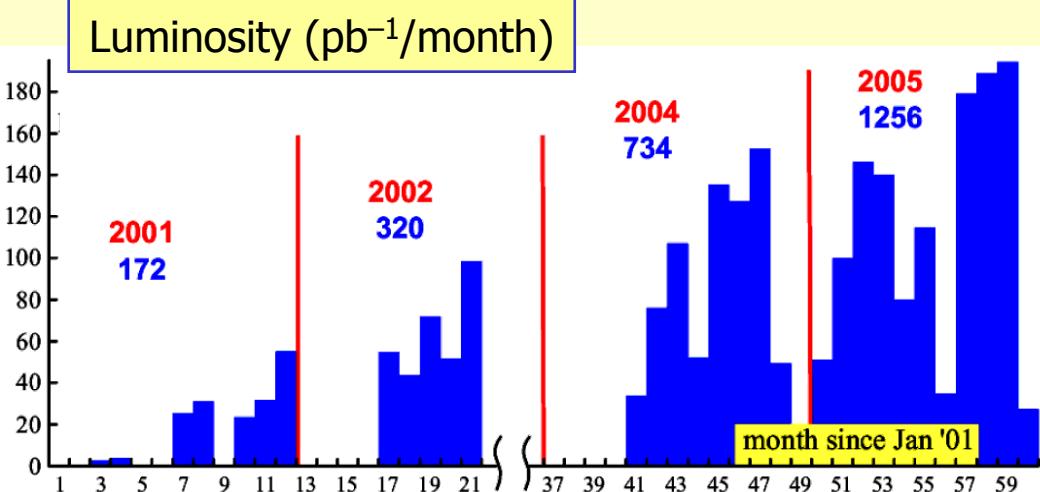
Uncertainties

Source	$\delta R_K \times 10^5$
Statistical	0.011
$K_{\mu 2}$	0.005
$\text{BR}(K_{e2\gamma} \text{ SD}^+)$	0.004
Beam halo	0.001
Acceptance corr.	0.002
DCH alignment	0.001
Positron ID	0.001
1-track trigger	0.002
Total	0.013

KLOE: ~ 110 MeV/c kaons

DAΦNE: e^+e^- collider at LNF Frascati

- CM energy $\sim m_\phi = 1.02$ GeV;
- $BR(\phi \rightarrow K^+K^-) = 49.2\%$;
- ϕ production cross-section $\sigma_\phi = 1.3 \mu b$;
- Residual momentum: $p_\phi \sim 13$ MeV/c;
- Data sample (2001–05): 2.5 fb^{-1} .

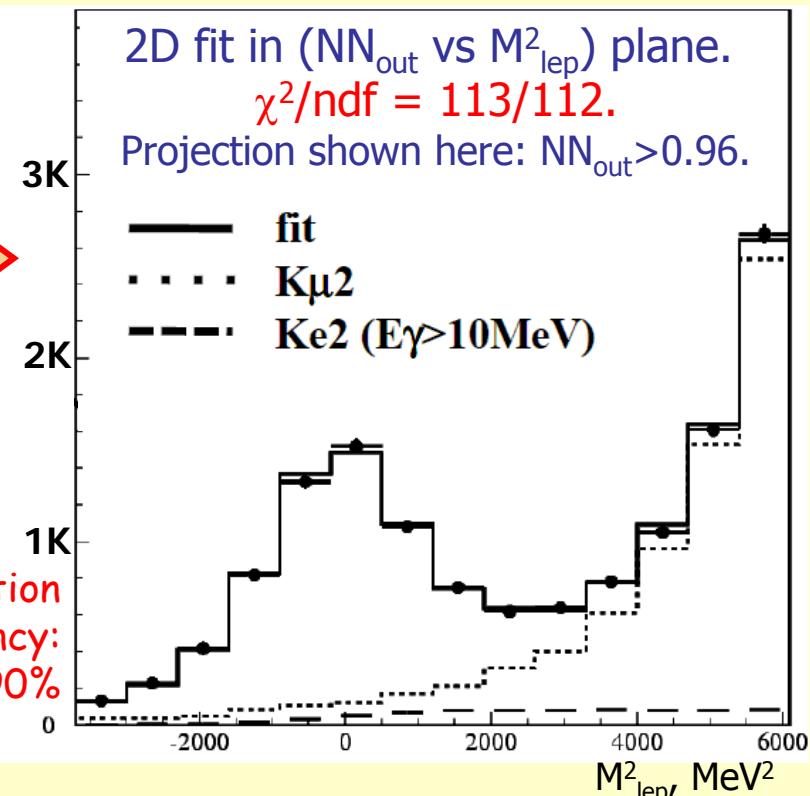
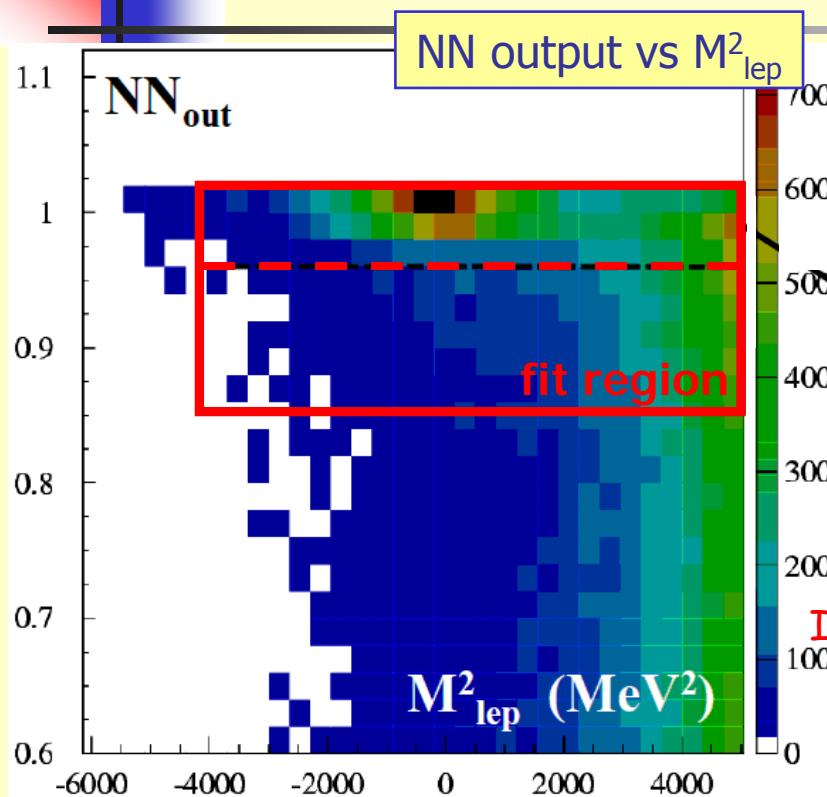


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$K_{e2}/K_{\mu 2}$ selection technique (vs NA62):

- Kinematics: by M_{lept}^2 (equivalent to M_{miss}^2);
- PID: neural network with 12 input parameters (vs E/p for NA62).

KLOE K_{e2} measurement



Uncertainties	$\delta R_K/R_K (\%)$
Statistical	1.0
$K\mu 2$ subtraction	0.3
$Ke2\gamma$ (SD ⁺)	0.2
Reconstruction efficiency	0.6
Trigger efficiency	0.4
Total	1.3

Final result [EPJ C64 (2009) 627]

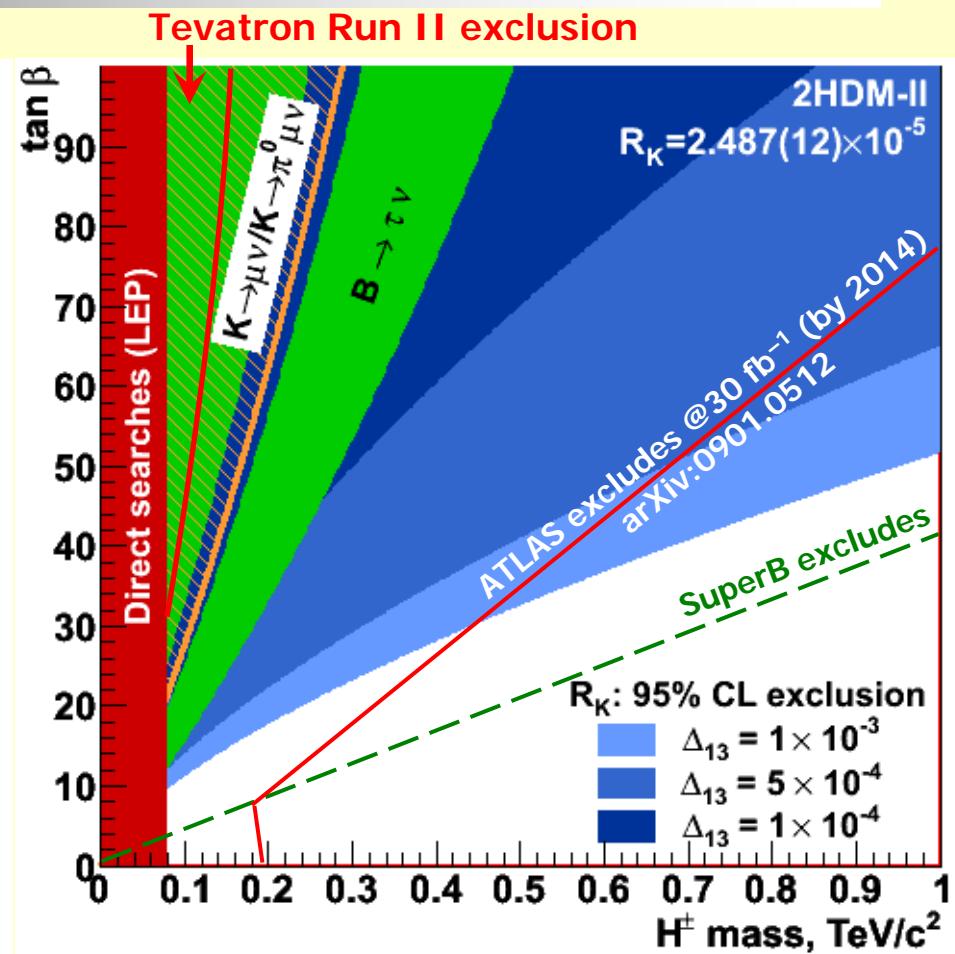
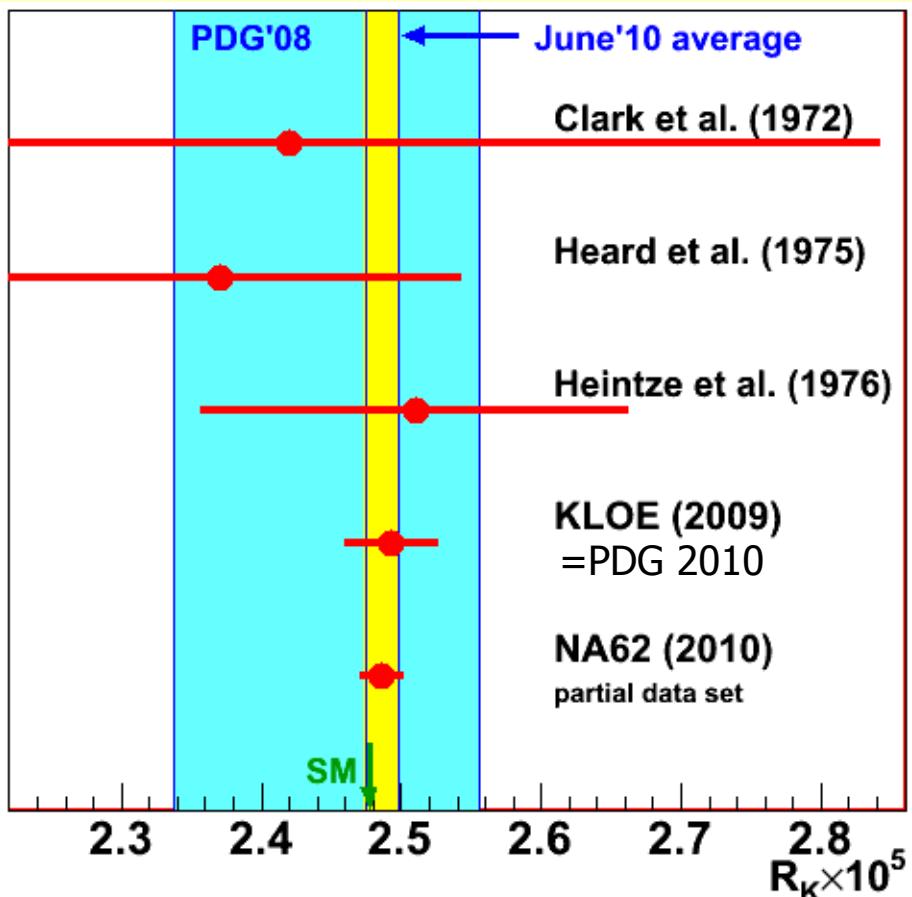
13.8K K_{e2} candidates, 16% background

$$R_K = (2.493 \pm 0.025_{\text{stat}} \pm 0.019_{\text{syst}}) \times 10^{-5}$$

$$= (2.493 \pm 0.031) \times 10^{-5}$$

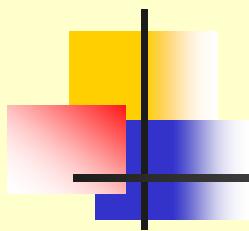
KLOE-2: starting in 2010, expect $\delta R_K/R_K = 0.4\%$. 30
[arXiv:1003.3862]

R_K : world average



World average	$\delta R_K \times 10^5$	Precision
March 2009	2.467 ± 0.024	0.97%
June 2010	2.487 ± 0.012	0.48%

For non-tiny values of the LFV slepton mixing Δ_{13} , sensitivity to H^\pm in $R_K = K_{e2}/K_{\mu 2}$ is better than in $B \rightarrow \tau \nu$



Ultra-rare kaon decays

$(K \rightarrow \pi \nu \bar{\nu})$

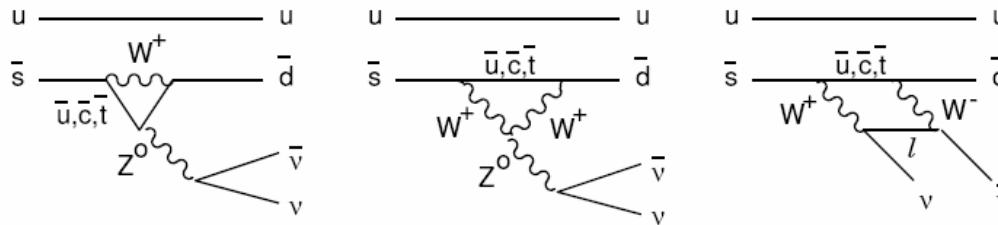
$K_{\pi VV}$: motivation

$K \rightarrow \pi VV$: theoretically clean, sensitive to NP, almost unexplored

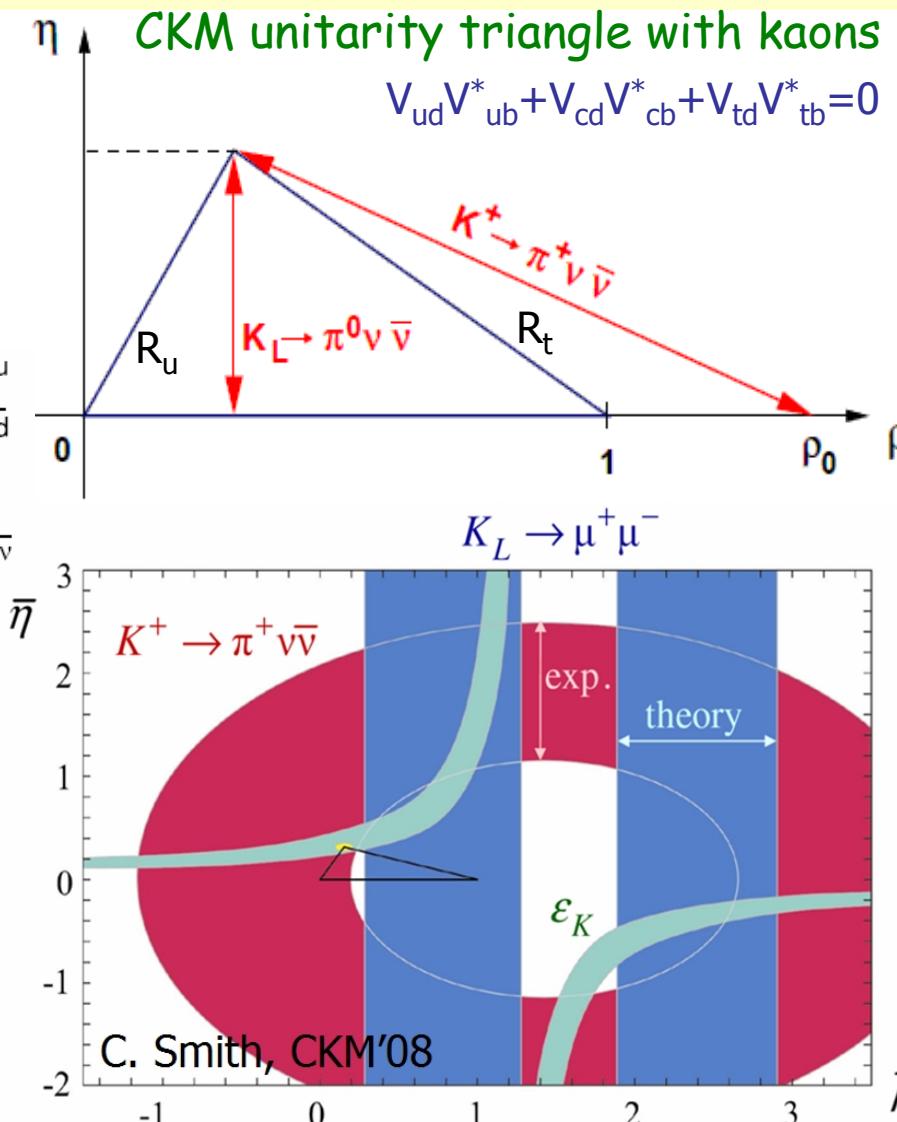
SM branching ratio $\times 10^{10}$

(FlaviaNet Kaon WG)

Mode	BR(SM)
$K^+ \rightarrow \pi^+ VV(\gamma)$	0.822 ± 0.084
$K_L \rightarrow \pi^0 VV$	0.276 ± 0.040



- Ultra-rare FCNC processes, proceed via Z-penguin and W-box diagrams.
- Hadronic matrix element extracted from precise $K \rightarrow \pi e \nu$ measurements.
- Exceptional SM precision not matched by any other loop-induced meson decay.
- Main SM uncertainty: CKM parametric.



BNL E787/E949: $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

Technique: K^+ decay at rest.

Data taking: E787(1995–98), E949(2002).

Spill: $65 \times 10^{12} \text{ pot} \times (2.2\text{s}/5.4\text{s})$.

PID: range (entire $\pi/\mu/e$ decay chain).

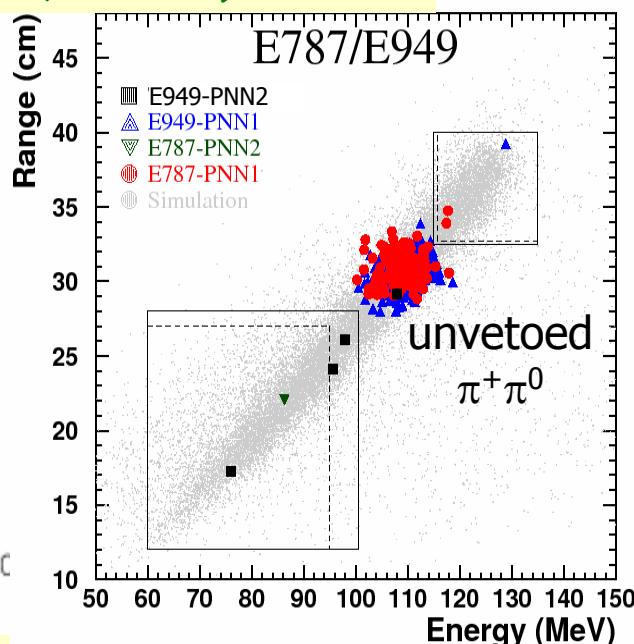
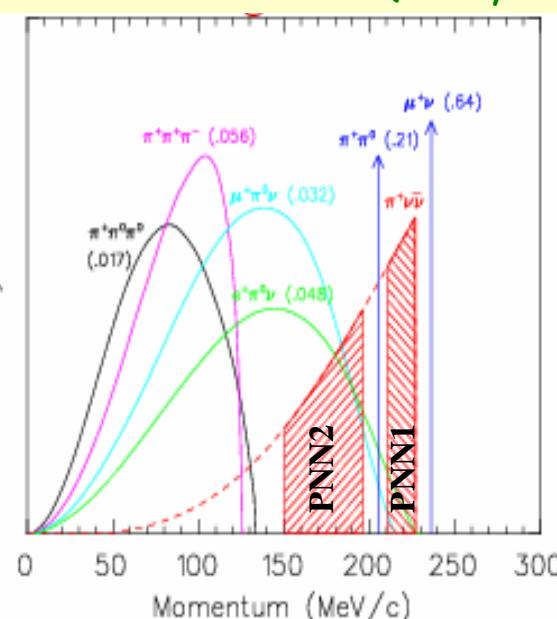
Observed events: 7

Expected background: 2.6

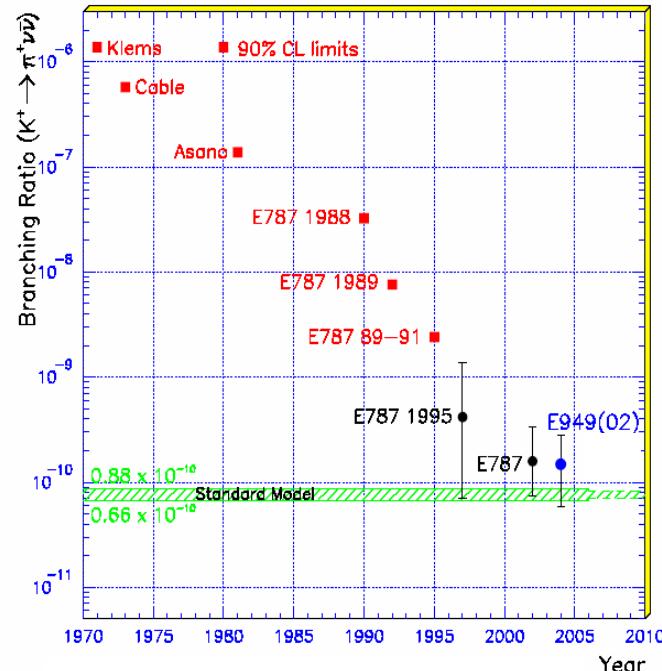
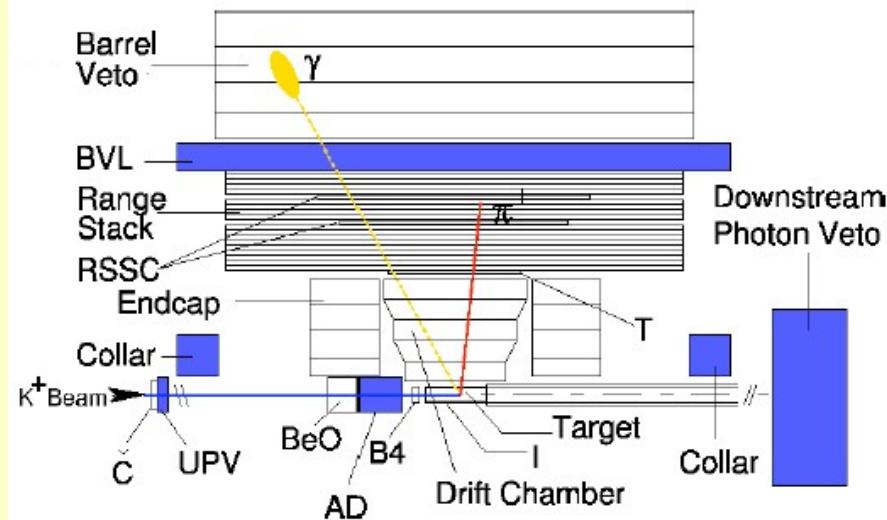
Final result: $\text{BR} = (1.73^{+1.15}_{-1.05}) \times 10^{-10}$

PRL 101 (2008) 191802, PRD 79 (2009) 092004

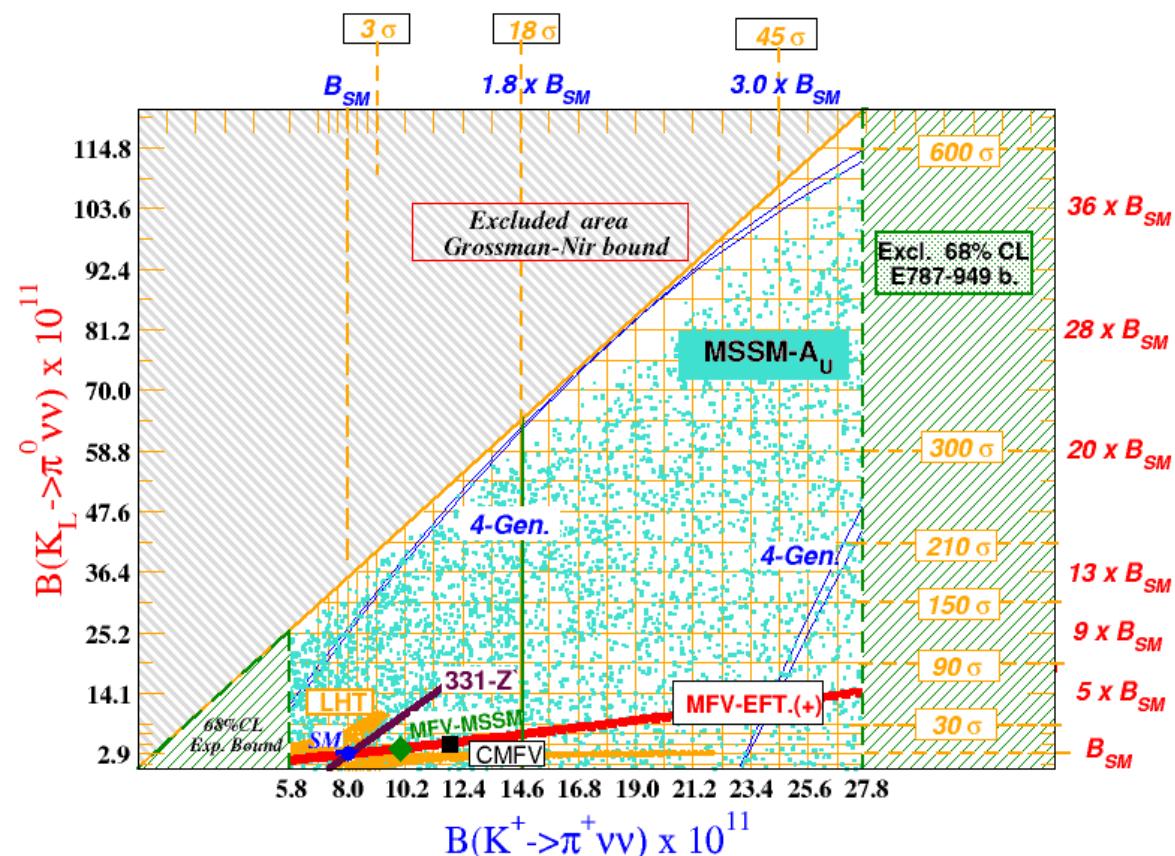
Future: $\sim 10^3$ SM events with stopped kaons
@FNAL? (D.Bryman, Kaon'09)



Barrel detector: 1T solenoid field



$K_{\pi VV}$: situation after E949



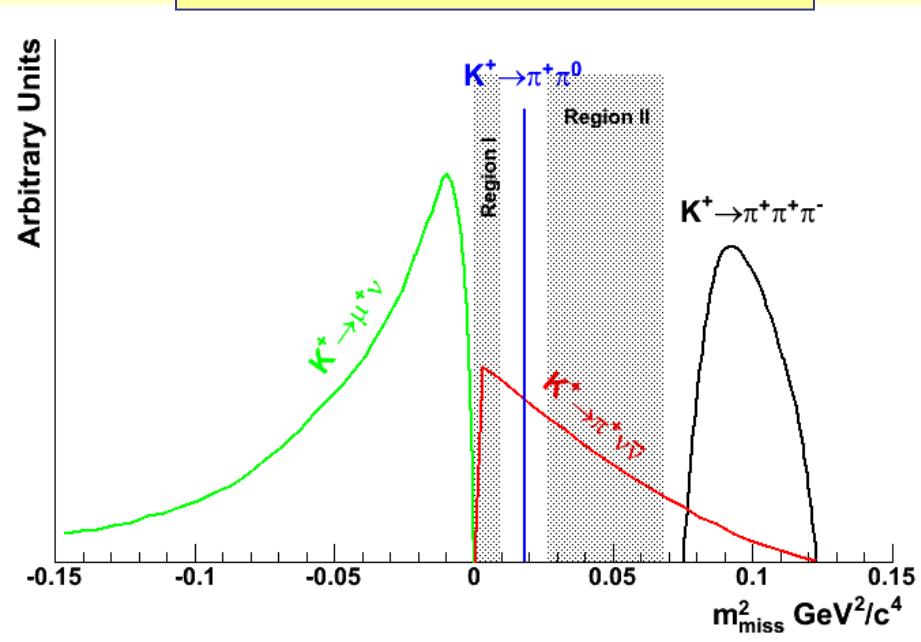
BR($K^+ \rightarrow \pi^+ VV$) $\times 10^{10}$: selected models	
SM	0.82 ± 0.08
MFV (hep-ph/0310208)	1.91
EEWP (NPB697 (2004) 133, hep-ph/0402112)	0.75 ± 0.21
EDSQ (PRD70 (2004) 093003, hep-ph/0407021)	up to 1.5
MSSM (NPB713 (2005) 103, hep-ph/0408142)	up to 4.0

- Large variations in predictions for new physics.
- A 10% precision measurement will provide a stringent SM test.

The NA62 collaboration at CERN aims to measure $O(100)$ $K^+ \rightarrow \pi^+ VV$ candidates with $\sim 10\%$ background in 2-3 years of data taking

CERN NA62: signal region

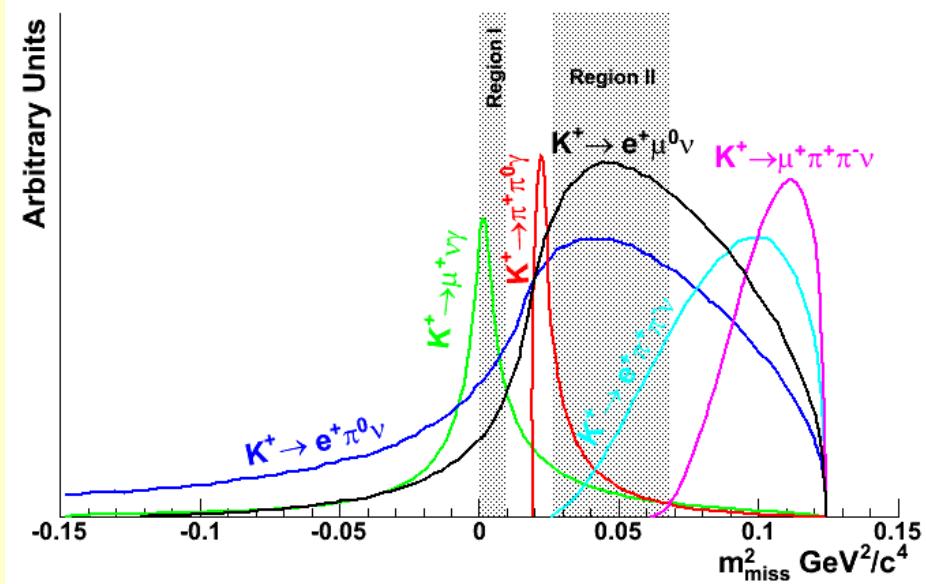
Kinematically constrained



92% of total background

- ▶ Definition of the signal region
- ▶ $K^+ \rightarrow \pi^+ \pi^0$ forces us to split it into two parts (Region I and Region II)

NOT kinematically constrained



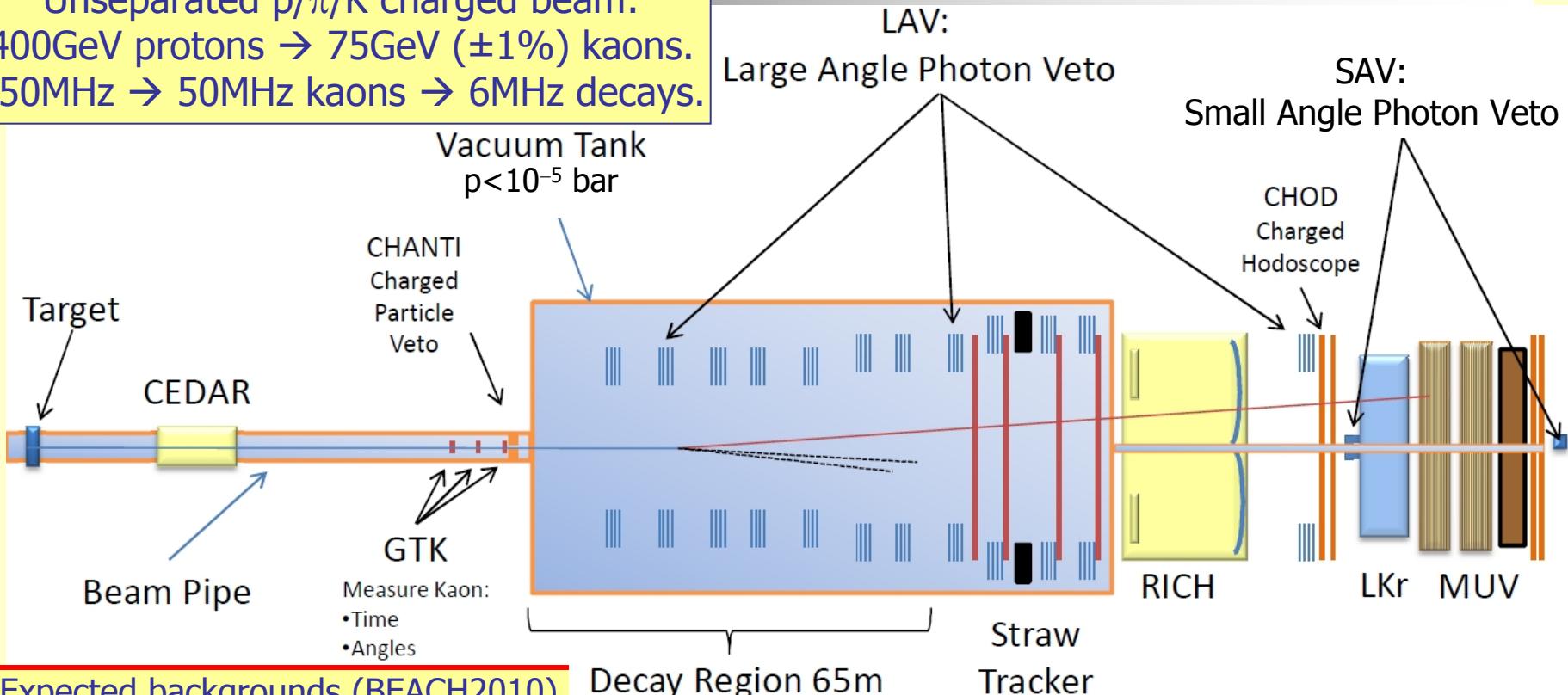
8% of total background

- ▶ Span across the signal region
- ▶ Rejection relies on vetoes/PID

Kinematic rejection power: 10^4 ($K^+ \rightarrow \pi^+ \pi^0$), 10^5 ($K^+ \rightarrow \mu^+ \nu_\mu$)
 Sources of inefficiency: non-Gaussian MS tails; K/π mismatch.

CERN NA62: sensitivity

Unseparated p/ π /K charged beam:
 400GeV protons \rightarrow 75GeV ($\pm 1\%$) kaons.
 750MHz \rightarrow 50MHz kaons \rightarrow 6MHz decays.

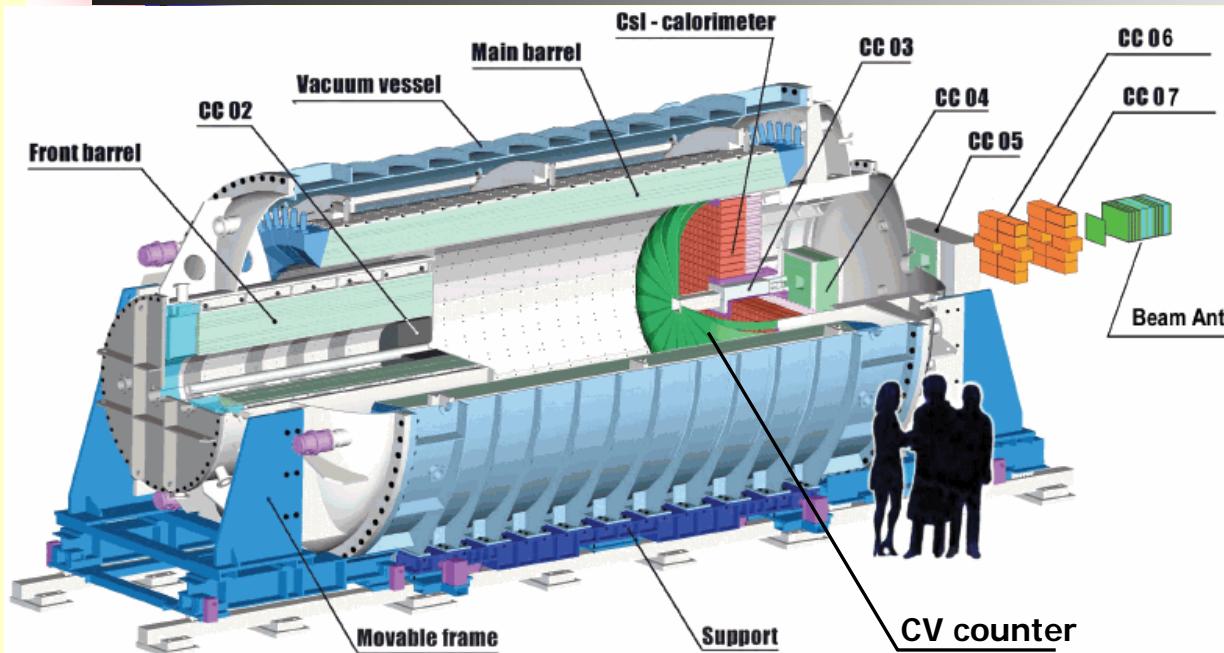


Expected backgrounds (BEACH2010)

Signal	45 evt/year
$K^+ \rightarrow \pi^+ \pi^0$	4.3%
$K^+ \rightarrow \mu^+ \nu$	2.2%
$K^+ \rightarrow 3$ charged tracks	<4.5%
$K^+ \rightarrow \pi^+ \pi^0 \gamma$	~2%
$K^+ \rightarrow \mu^+ \nu \gamma$	~0.7%
Total background	<13.5%

- 4.8×10^{12} K^+ decays/year \rightarrow record SES of $\sim 10^{-12}$;
- Hermetic veto & redundant kinematics measurements;
- R&D finishing, detector construction has started;
- Physics runs are to start in 2013.

KEK E391a: $K_L \rightarrow \pi^0 \nu \bar{\nu}$



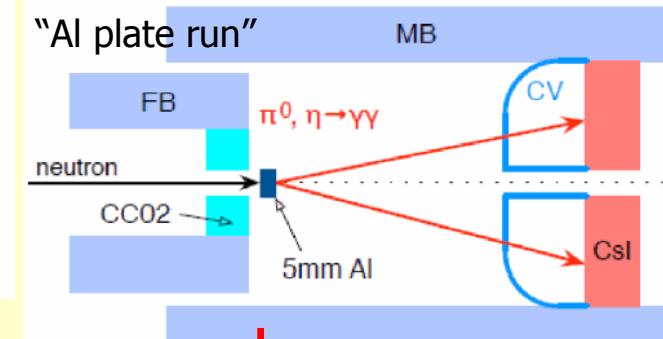
Good physics runs (Runs 2,3):
Feb-Dec 2005

Pencil K_L beam, 2.5×10^{18} PoT.

Calorimeter:

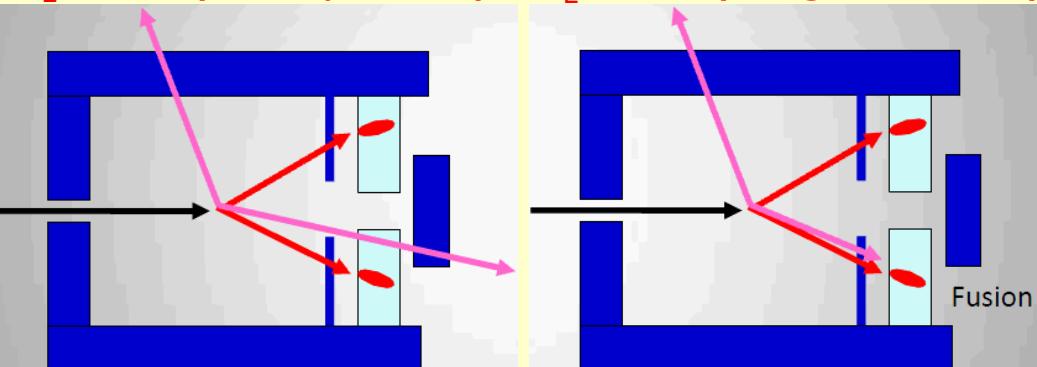
496 ($7 \times 7 \times 30$) cm³ CsI crystals

Veto: Pb+scintillator+WLS fibers



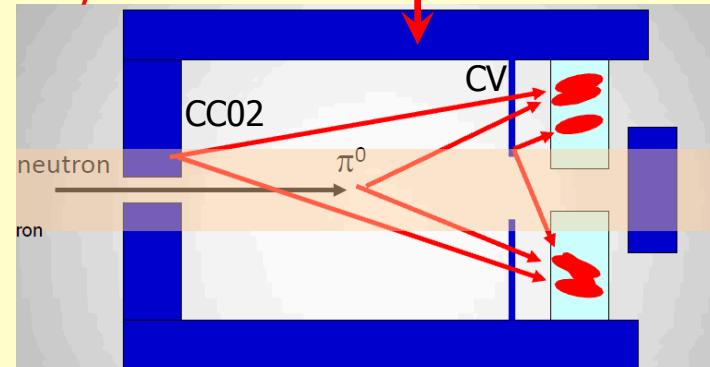
Principal backgrounds:

$K_L \rightarrow \pi^0 \pi^0$ (2 lost photons) $K_L \rightarrow \pi^0 \pi^0$ (merged clusters)



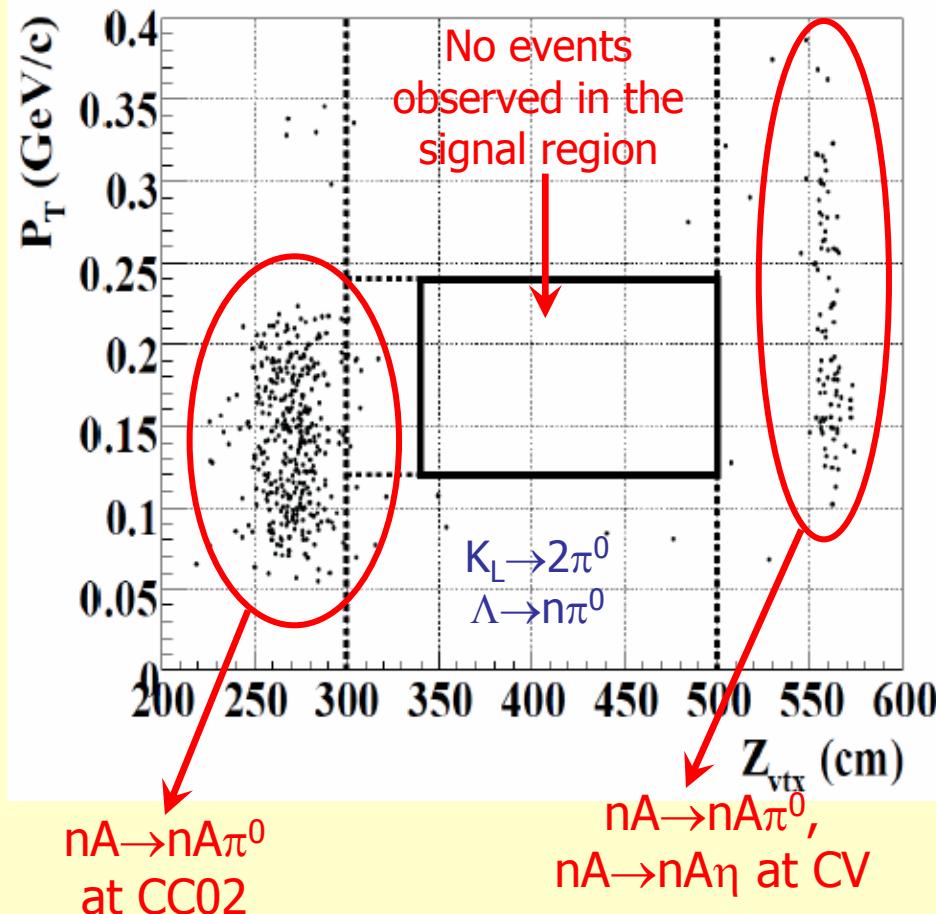
π^0/η production
by halo neutrons

FLUKA simulation
validated with data



KEK E391a: final result

Signature: a high- p_T π^0 + nothing
Blind analysis technique employed.



Background source	Estimated number of BG
halo neutron BG	0.66 ± 0.39
CC02- π^0	< 0.36
CV- π^0	
CV- η	0.19 ± 0.13
K_L^0 decay BG	$(2.4 \pm 1.8) \times 10^{-2}$
$K_L^0 \rightarrow \pi^0\pi^0$	
$K_L^0 \rightarrow \gamma\gamma$	negligible
charged modes	negligible ($\mathcal{O}(10^{-4})$)
other BG	
backward π^0	< 0.05
residual gas	negligible ($\mathcal{O}(10^{-4})$)
total	0.87 ± 0.41

Background is dominated by beam interactions

Number of K_L decays:

$$N = (8.70 \pm 0.17_{\text{stat}} \pm 0.59_{\text{syst}}) \times 10^9$$

Signal acceptance: $\sim 1\%$

$$\text{SES: } (1.11 \pm 0.02_{\text{stat}} \pm 0.10_{\text{syst}}) \times 10^{-8}$$

Final result:

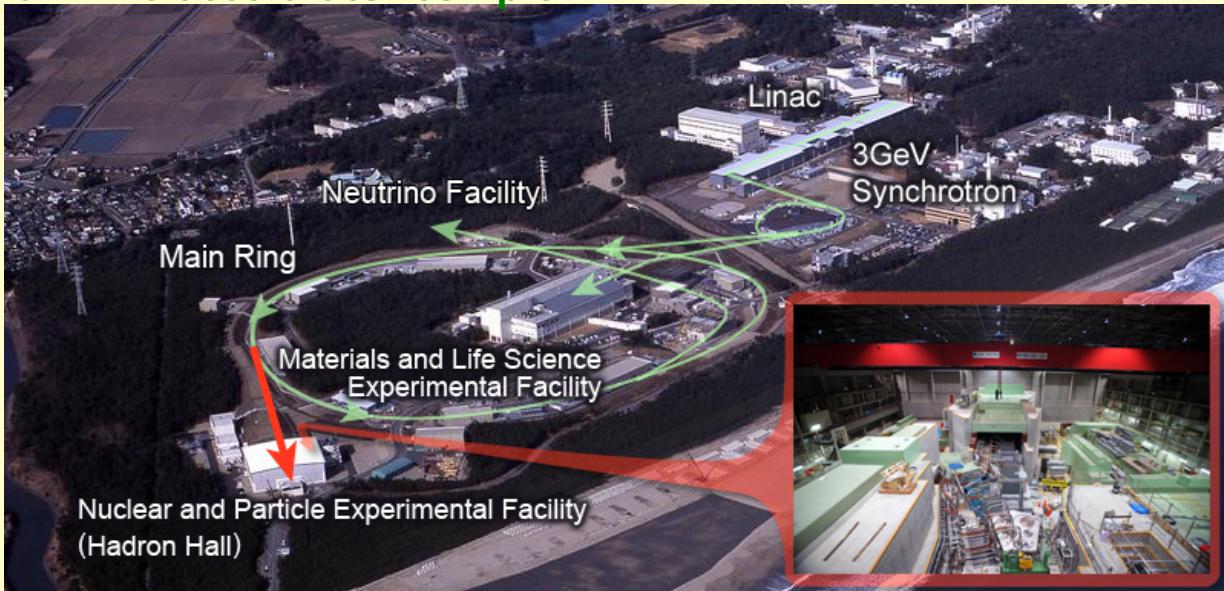
$$\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 2.6 \times 10^{-8} \text{ @90% CL}$$

PRD81 (2010) 072004

Order of magnitude above the GN limit;
seen as preparation for JPARC E14 39

Next step: JPARC E14 (K⁰TO)

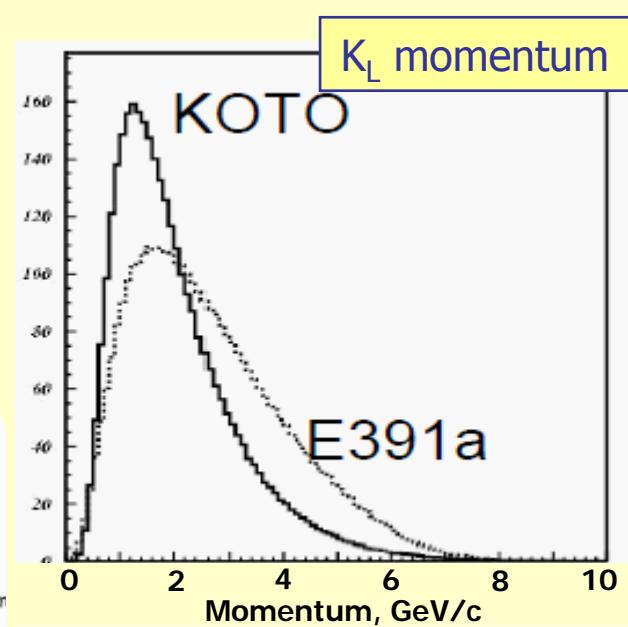
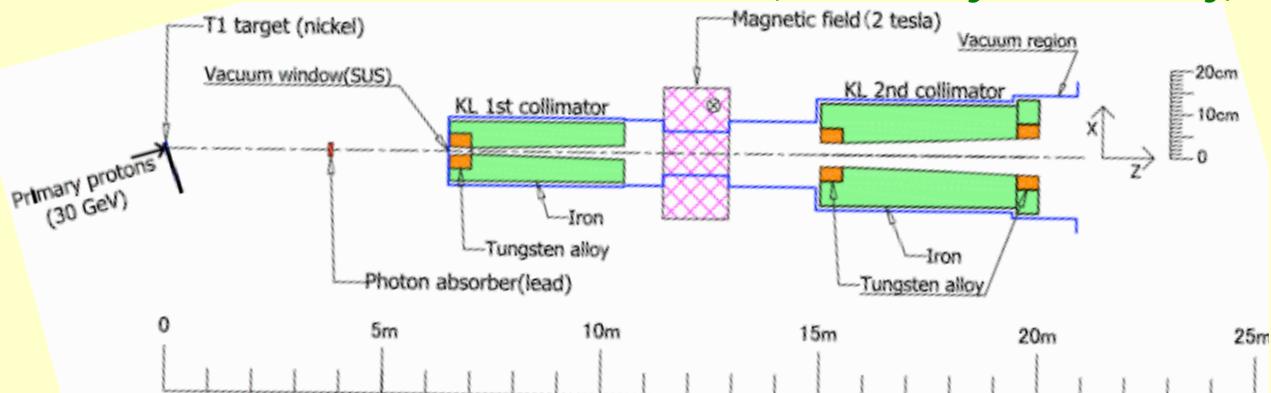
J-PARC accelerator complex



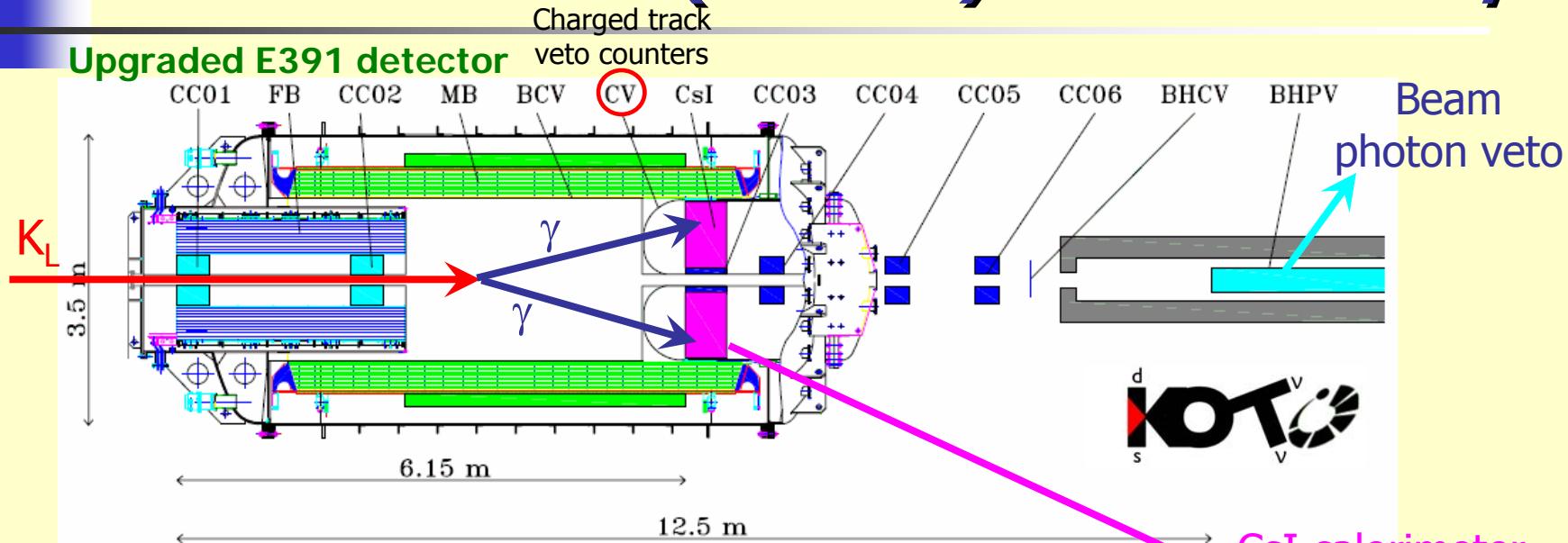
- Proton energy: 30 GeV
- Intensity: 2×10^{14} PoT/spill
- Spill duration: 0.7s/3.3s
- Solid angle: 9 μ Str
- K_L/spill: 7.8×10^6
- Decay probability: 4%

Physics runs planned: 2011-2013
(12 months in total)

K_L beam: suppression of halo neutrons to $\sim 10^{-3}/K_L$.
Flux * RunTime * Acc = 3000 \times E391a (=discovery of SM decay).



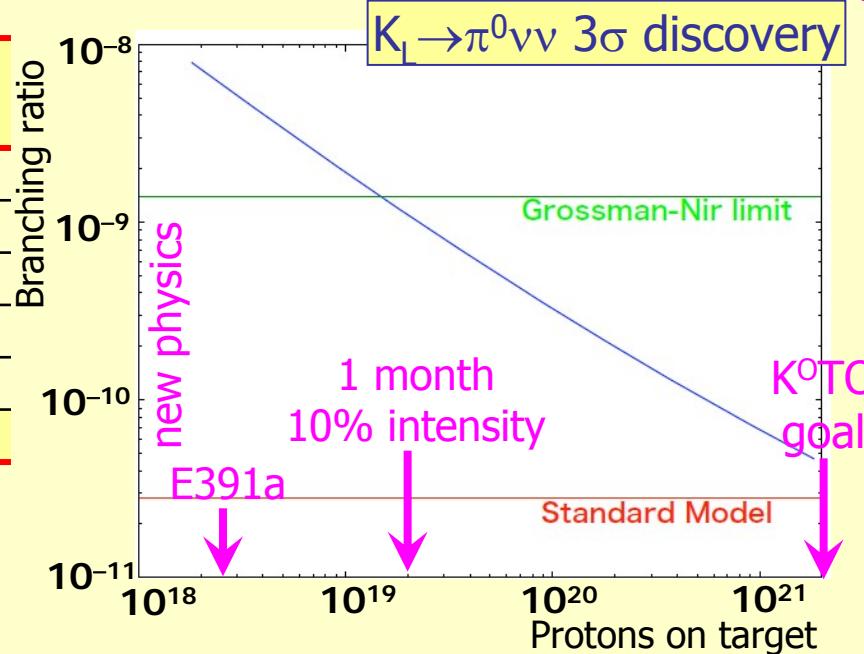
JPARC E14 (K⁰TO): sensitivity

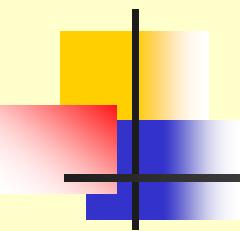


Signal & background (3 years)
PoS(KAON09)047

Signal	2.7
$K_L \rightarrow \pi^0 \pi^0$	1.7
Halo neutron: CC02	0.01
Halo neutron: CV- π^0	0.08
Halo neutron: CV- η	0.3
Total background	2.1

Possible K⁰TO upgrade aims at collecting ~100 SM events





Summary

- Tremendous progress in measurements and interpretation of semileptonic kaon decays: $|V_{us}| f_+(0)$ measured to 0.23% precision, $|V_{us}|$ extracted with 0.4% precision.
- CKM unitarity with $|V_{ud}|^2 + |V_{us}|^2$ tested at 0.06% precision:
→ O(10 TeV) lower bound on the scale of new physics.
- Precision measurements of leptonic decays $K \rightarrow l\nu$ place non-trivial bounds on the 2HDM parameters.
- Most future K experiments aim at $K \rightarrow \pi \nu \bar{\nu}$; still significant experimental improvements in both K_{l3} and K_{l2} are expected in the medium-term (KLOE, NA48/NA62).

Data interpretation (except $K_{e2}/K_{\mu 2}$) is limited by lattice QCD input