

Electroweak Precision Physics at the LHC

Alexander Mück
RWTH Aachen University

Standard Model @ LHC
IPPP Durham, April 12, 2011

Outline

- EW precision physics

Where is EW precision **achievable** at the LHC?

Where are EW corrections **particularly important**?

- specific EW issues

How to treat **resonances**?

How to treat **photons**?

- Calculations + tools for EW precision

Which **calculations** are **available**?

Which **tools** are **available**?

- Summary and questions

Prerequisites

LHC is a discovery machine!

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 - Leading order (**LO**) up to 100% uncertainty
 - Next-to-leading order (**NLO**) needed everywhere
 - **NNLO** needed for high precision (some exceptions)

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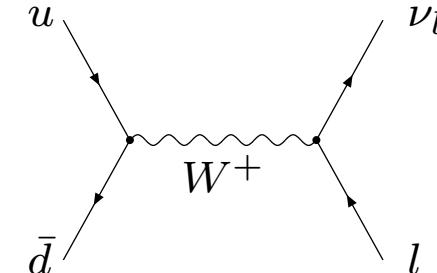
→ most of the talks at this workshop

Precision Channels

Charged-current Drell-Yan:

$$pp \rightarrow W^\pm \rightarrow l^\pm \nu_l$$

- clean signal: lepton + missing p_T
- huge cross section: $\sigma_{W^+ \rightarrow \mu^+ \nu_\mu} = 3 \text{ nb}$ (Atlas cuts at 7 TeV)

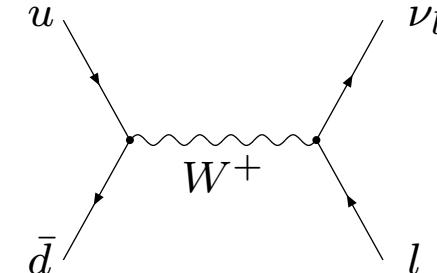


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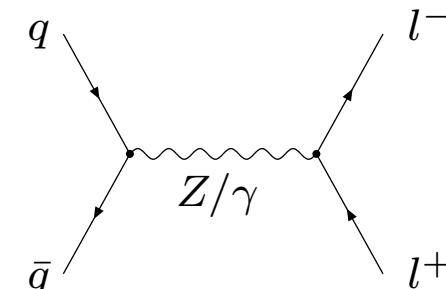
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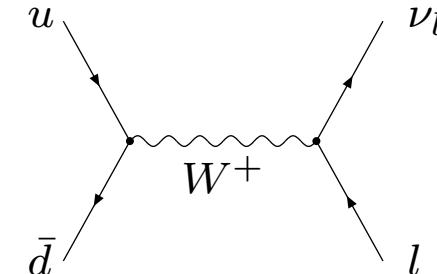


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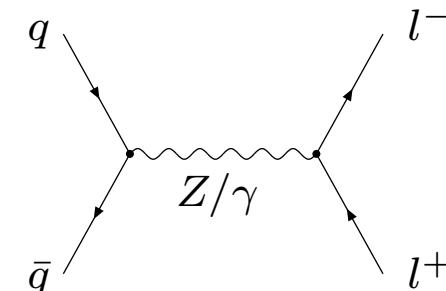
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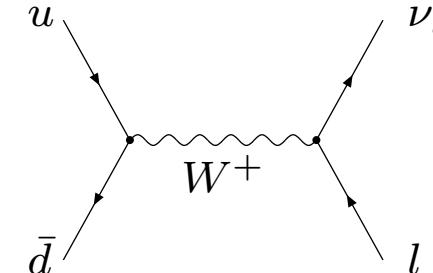
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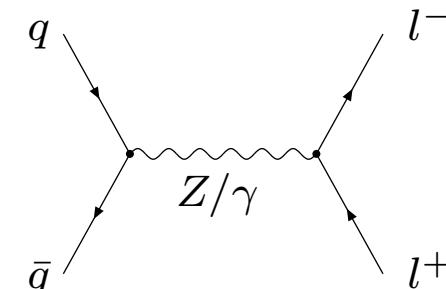
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Precision measurements: M_W , Γ_W , $\sin \theta_{\text{eff}}^{\text{lept}}$ (\leftrightarrow LEP)

QCD Predictions for DY

NNLO QCD:

- total cross section

v.Neerven, Zijlstra [NPB 382 (1992) 11]

Harlander, Kilgore [hep-ph/0201206]

- rapidity distributions

Anastasiou et al. [hep-ph/0312266]

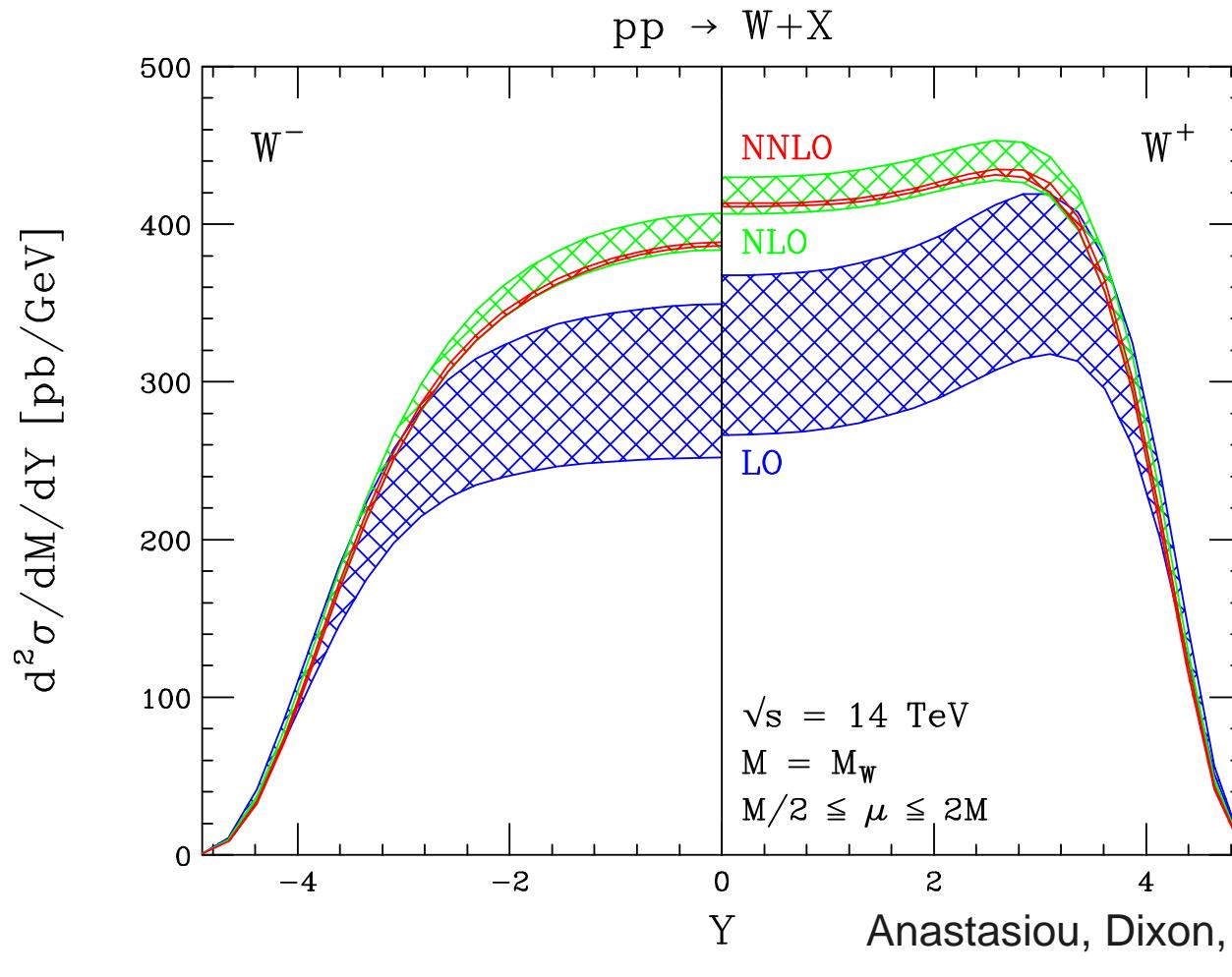
- fully differential cross sections

Melnikov, Petriello [hep-ph/0609070]

Catani et al. [arXiv:0903.2120]

QCD Predictions for DY

Rapidity distribution: 1% uncertainty at NNLO



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further QCD improvements:

- NNNLO in soft + virtual approximation Moch, Vogt [hep-ph/0508265]
- soft gluon resummation for $p_{T,W}$ distribution (Resbos)
Balasz, Yuan [hep-ph/9704258]
Ellis, Veseli [hep-ph/9706526]
Cao, Yuan [hep-ph/0401026]
- NLO plus parton shower (MC@NLO, Powheg)
Frixione, Nason, Webber [hep-ph/0305252]
Alioli, Nason, Oleari, Re [arXiv:0805.4802]

EW corrections

generic size:

- expect **percent level** corrections
- naive comparison with QCD: $\mathcal{O}(\alpha) \sim \mathcal{O}(\alpha_s^2)$
⇒ needed for **high precision observables** (like Drell-Yan)
- choose α appropriately (G_μ scheme for Drell-Yan)

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(logarithmically) enhanced EW corrections:

- at high energies: Sudakov logs $\propto \alpha \rightarrow \alpha \log^2(Q/M_W)$
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enhanced EW corrections in BSM models:

- e.g. in $b\bar{b} \rightarrow H$

Sudakov logs

interesting observables at $\sqrt{s} \gg M_{W,Z}$ at the LHC

- Z'/W' searches in invariant mass tails
- Z/W at high p_T in $Z/W + \text{jet}$

Sudakov logs

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- **leading two-loop** corrections important
 - Fadin et al. [hep-ph/9910338]
 - Ciafaloni, Cornelli [hep-ph/0001142]
 - Hori et al. [hep-ph/0007329]
 - Melles [hep-ph/0108221]
 - Beenakker, Werthenbach [hep-ph/0112030]
 - Denner, Melles, Pozzorini [hep-ph/0301241]
 - Jantzen, Kühn, Penin, Smirnov [hep-ph/0504111]
[hep-ph/0509157]
 - Denner, Jantzen, Pozzorini [hep-ph/0608326]

Sudakov logs

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- partial compensation from **real W and Z emission**

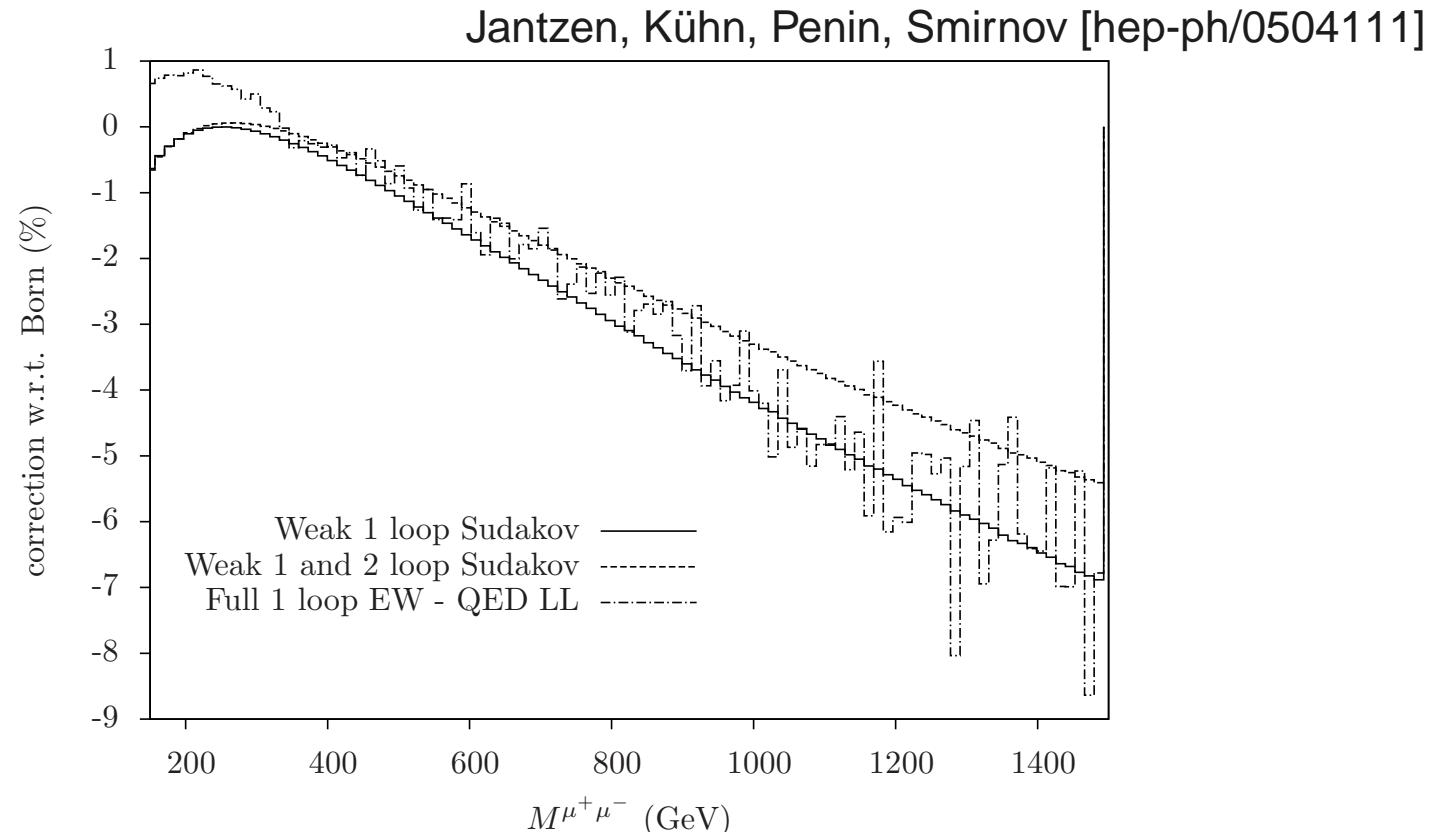
Ciafaloni, Cornelli [hep-ph/0604070]

Baur [hep-ph/0611241]

Sudakov logs

example 1: dimuon invariant mass tail

- full one-loop EW corrections from HORACE
- Sudakov logs in analytic form



Les Houches 2007 [arXiv:0803.0678]

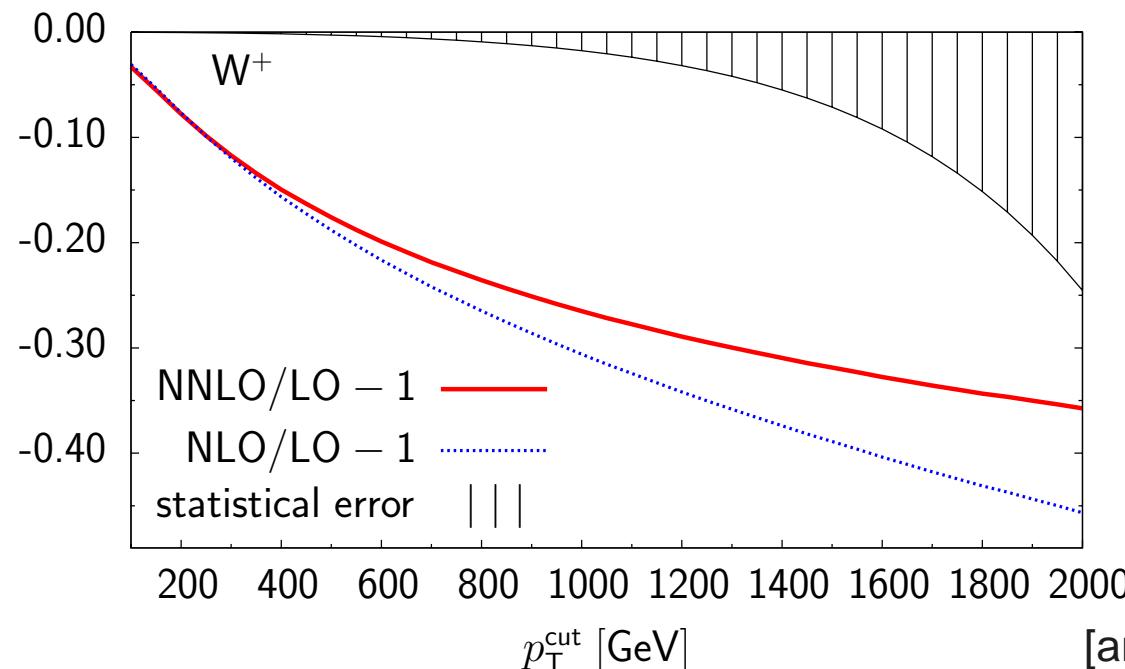
Sudakov logs

example 2: W bosons at **high p_T**

- full NLO EW and NLL 2-loop result

Kühn, Kulesza, Pozzorini, Schulze [arXiv:0708.0476]

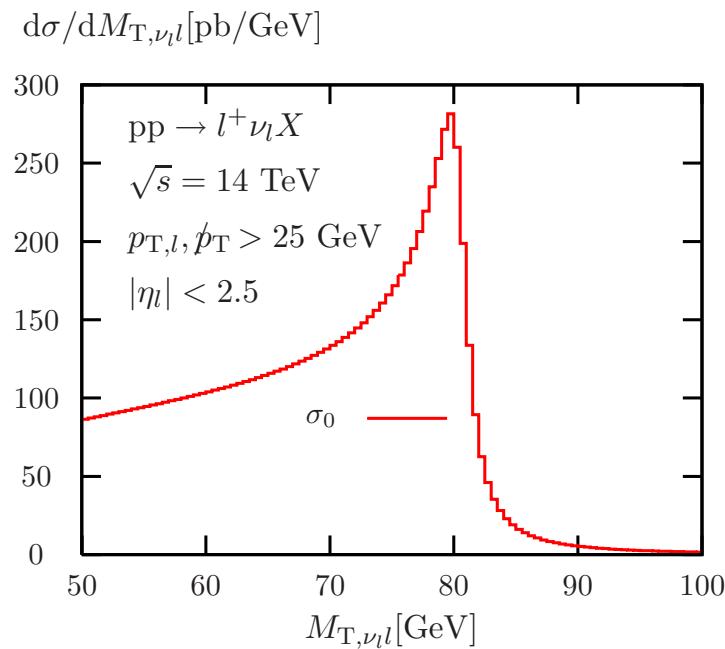
- compared to statistical LHC error ($300 \text{ fb}^{-1}, \sqrt{s} = 14 \text{ TeV}$)



Precision measurement M_W

W mass M_W from fit to distributions

- transverse mass: $M_T = \sqrt{2 p_{T,l} p_T^{\text{miss}} (1 - \cos \phi_{\nu l})}$
- transverse momentum: $p_{T,l}$



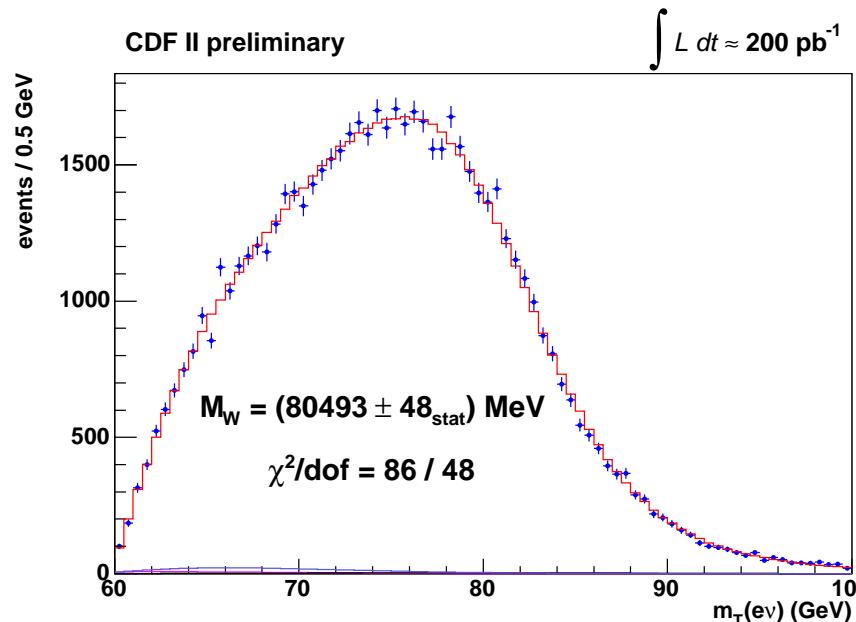
Jacobian peak at $M_T = M_W$

$d\sigma/dM_T$ and $d\sigma/dp_{T,l}$
equivalent at tree-level

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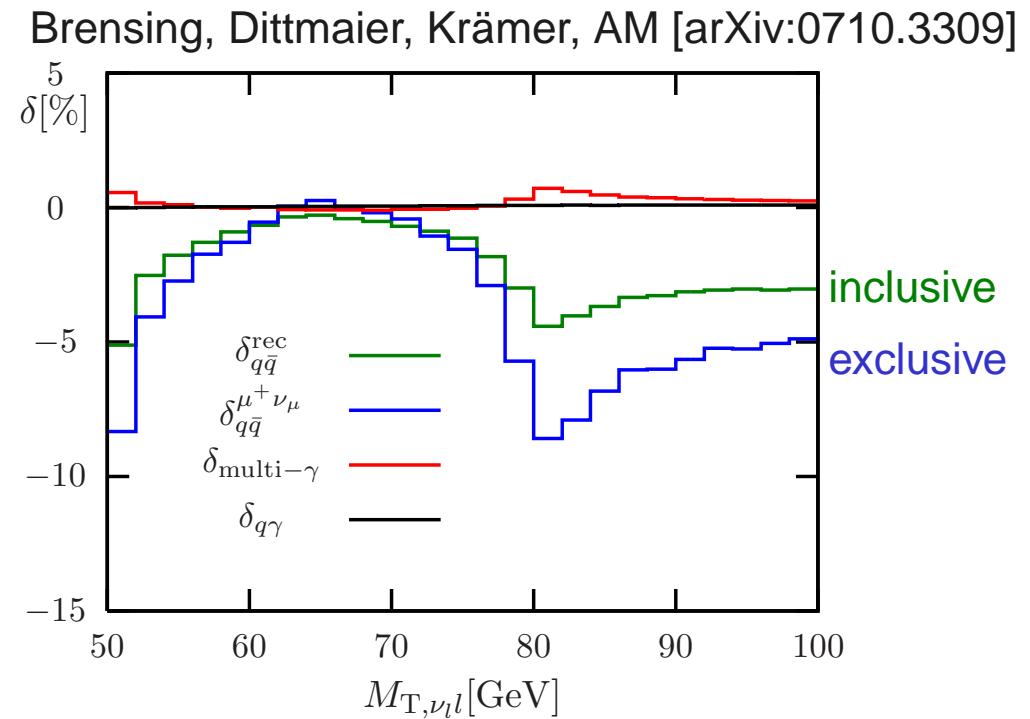
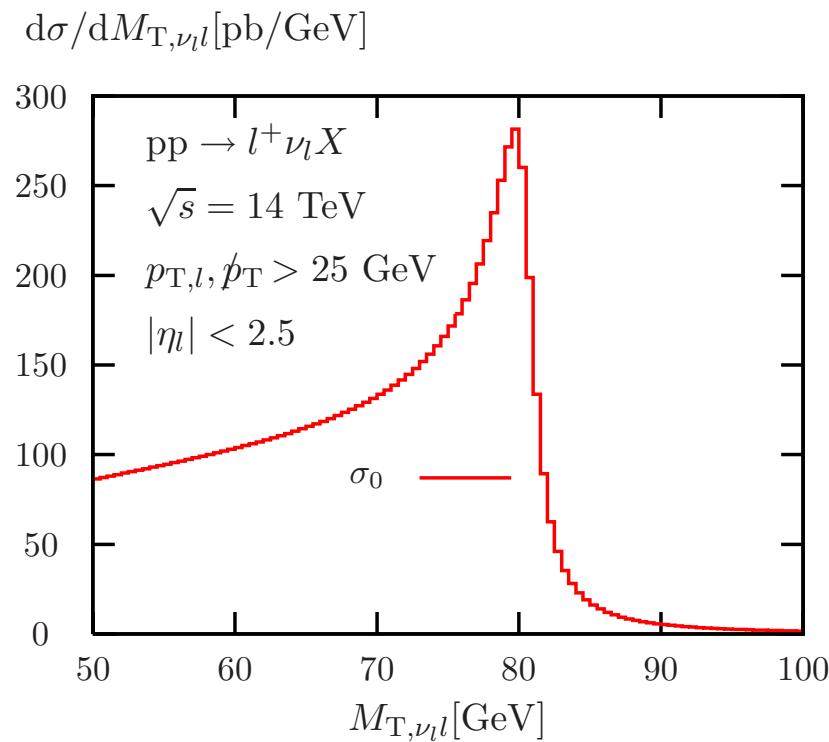


- combined Tevatron:
 $M_W = 80.420 \pm 0.031 \text{ GeV}$
 (already beats LEP)

- Ultimate LHC goal: 10 MeV error
 (use data from $pp \rightarrow Z \rightarrow l^+l^-$)

EW corrections: distributions

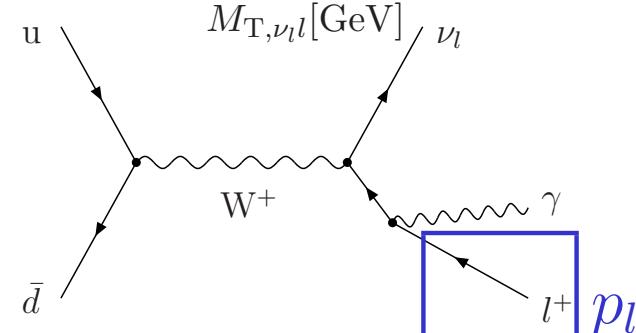
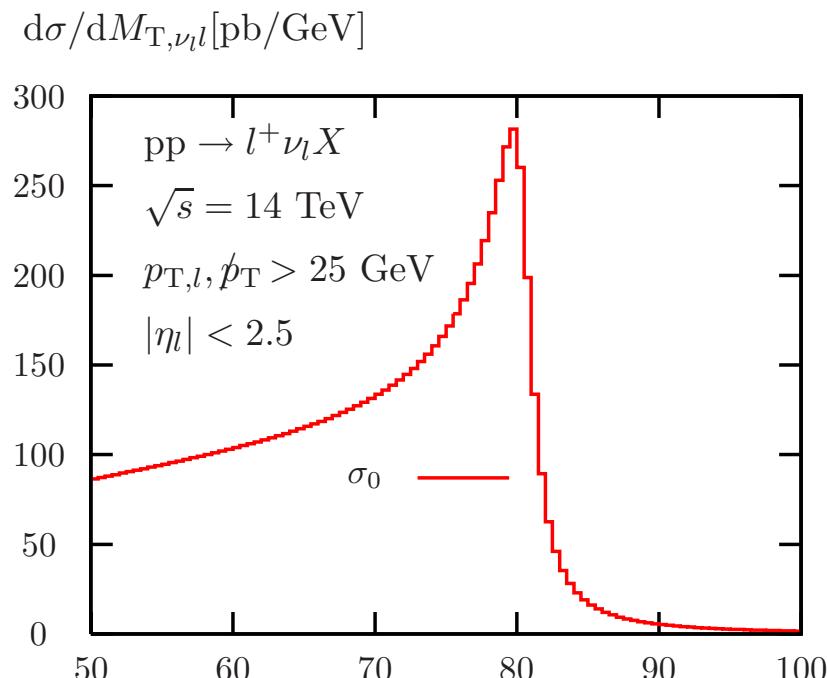
The transverse-mass distribution:



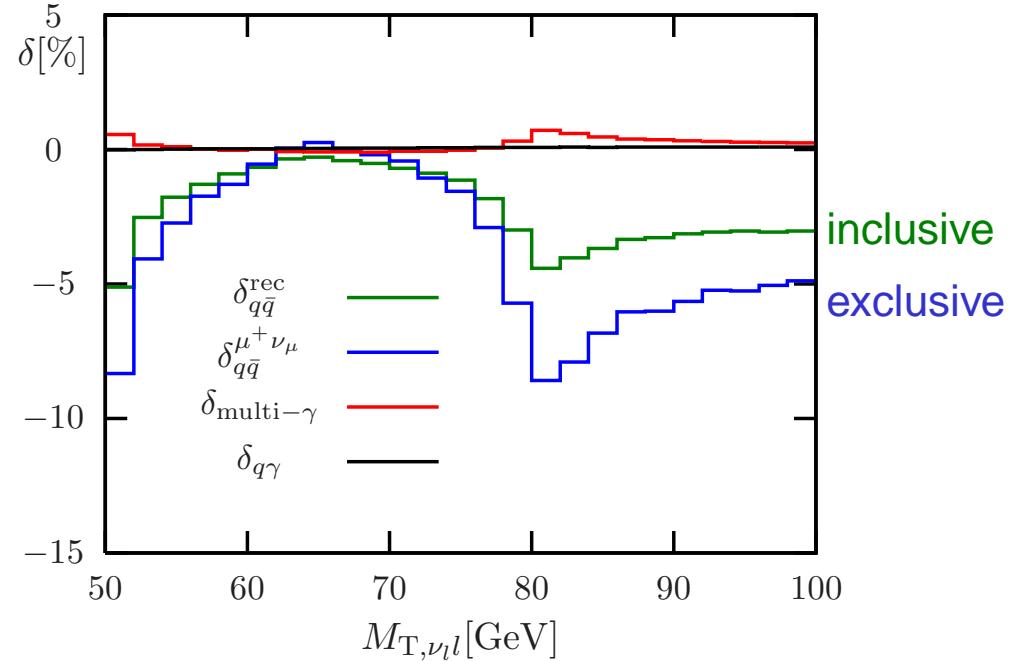
How to treat final state photons?

EW corrections: distributions

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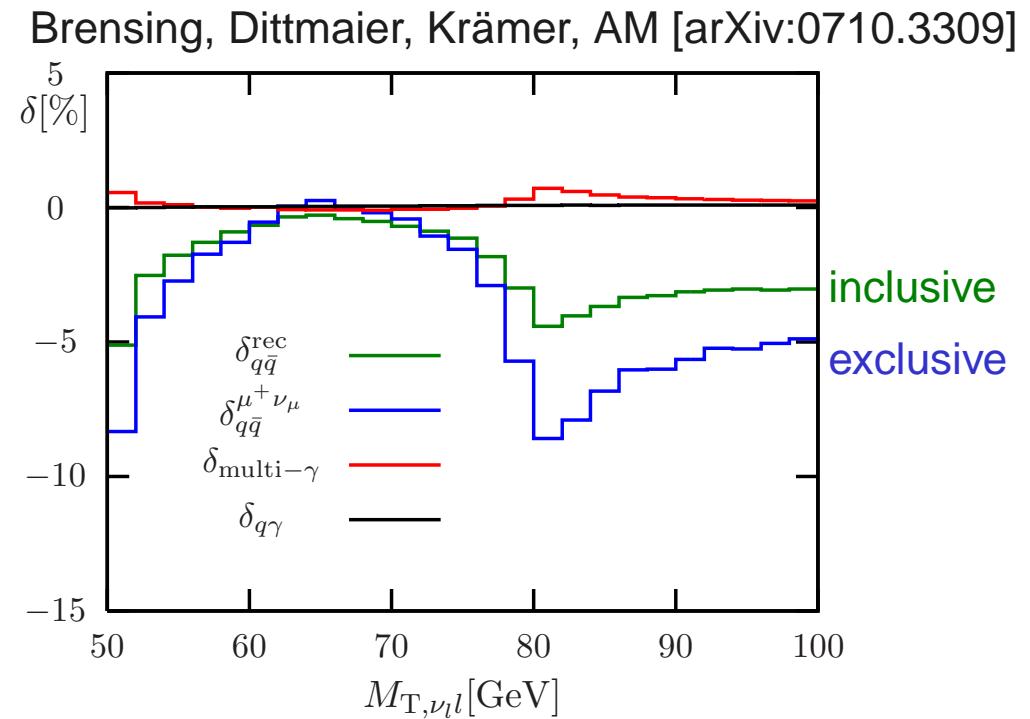
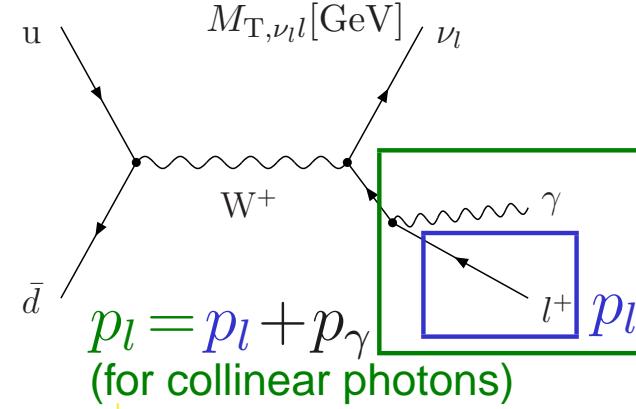
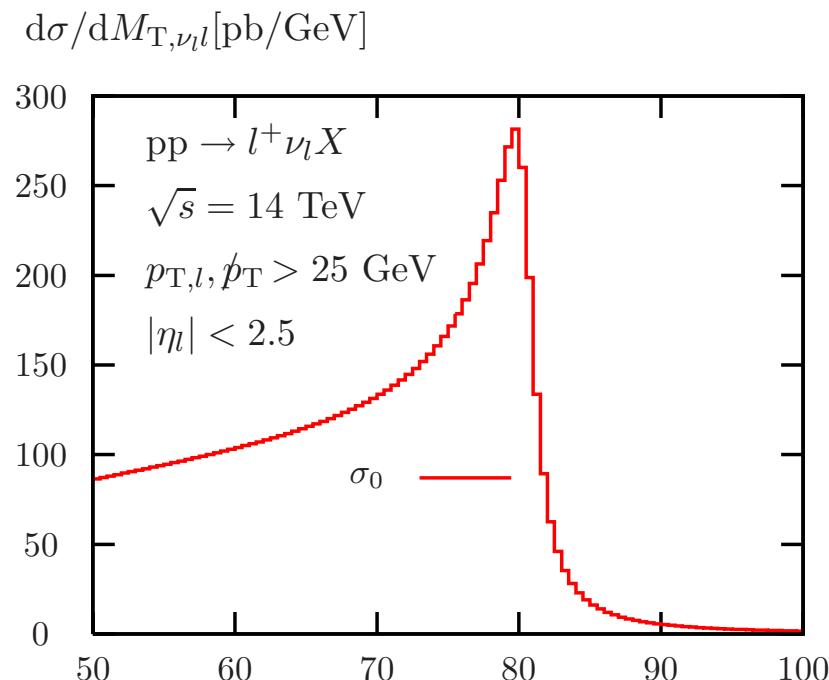
Brensing, Dittmaier, Krämer, AM [arXiv:0710.3309]



exclusive (bare) leptons (muons)
 $\Rightarrow \alpha \log(M_W^2/M_l^2)$ corrections

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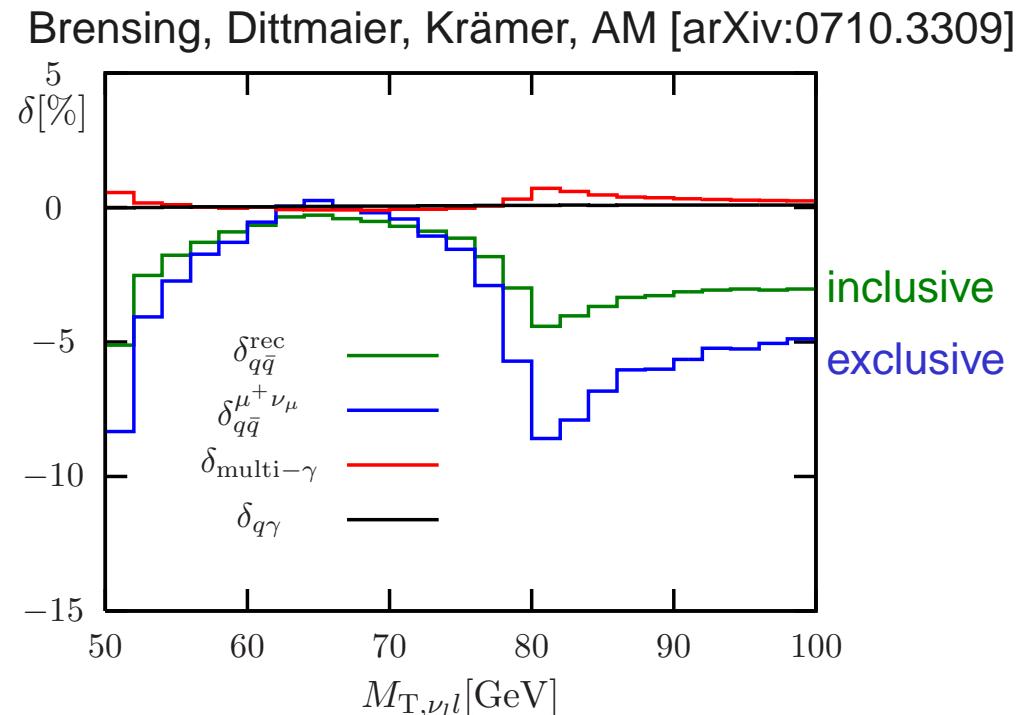
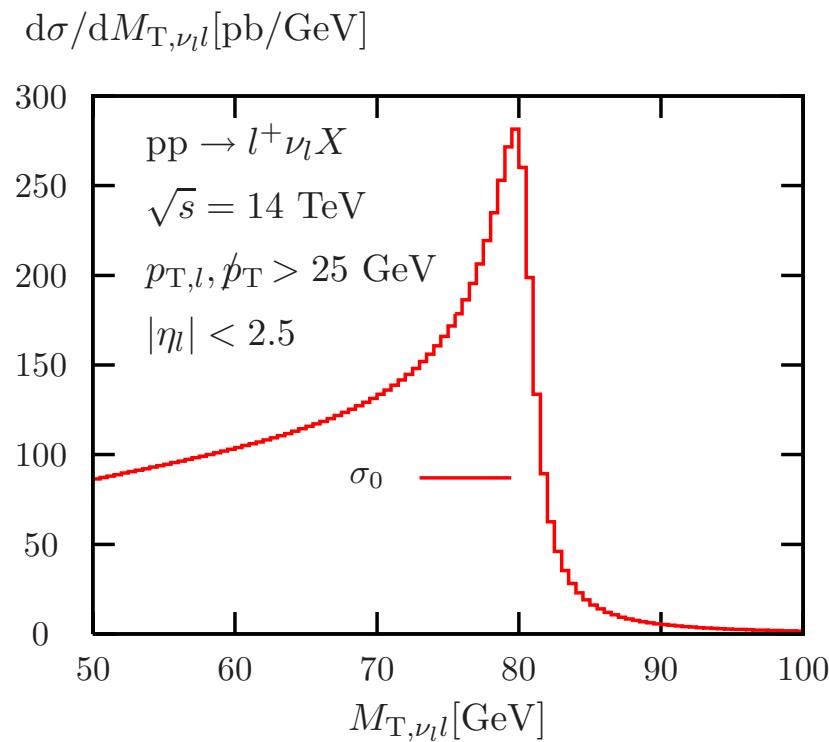
inclusive leptons (electrons)

\Rightarrow no mass logs (KLN theorem)



EW corrections: distributions

The transverse-mass distribution:



$\Rightarrow \sim 170$ (65) MeV shift for M_W for μ^\pm (e^\pm) channel
CDF [hep-ex/0007044]

$\Rightarrow \sim 10$ MeV shift for M_W from multi- γ final state radiation

Tools for Drell-Yan

Full NLO EW corrections available

Charged-Current DY:

Zykunov [hep-ph/0107059]

Dittmaier, Krämer [hep-ph/0109062]

Baur, Wackerlo [hep-ph/0405191]

Arbuzov et al. [hep-ph/0506110]

Carloni Calame et al. [hep-ph/0609170]

Baur et al. [hep-ph/0108274]

Zykunov [hep-ph/0509315]

Carloni Calame, Montagna, Nicrosini, Vicini [arXiv:0710.1722]

Arbuzov et al. [arXiv:0711.0625]

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Public codes for NLO EW corrections:

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- WGRAD/ZGRAD2

Baur, Wackerth [hep-ph/0405191]

Baur, Brein, Hollik, Schappacher, Wackerth [hep-ph/0108274]

- SANC

Arbuzov, et al. [arXiv:0711.0625]

Arbuzov, et al. [hep-ph/05061101]

Richardson, Sadykov, Sapronov, Seymour, Skands [arXiv:1011.5444]

→ interface with Herwig++ and Pythia8

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Multi-photon emission:

- HORACE NLO EW **matched** with QED parton shower
Carloni Calame, Montagna, Nicrosini, Treccani [hep-ph/0303102]
- WINHAC YFS exp., NLO EW from SANC for CC-DY
Placzek, Jadach [hep-ph/0302065]
Bardin, Bondarenko, Jadach, Kalinovskaya, Placzek [arXiv:0806.3822]
- W/ZGRAD Structure function approach+NLO EW
see also: Brensing, Dittmaier, Krämer, AM [arXiv:0710.3309]
Dittmaier, Huber [arXiv:0911.2329]

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Multi-purpose tools with/for FSR:

- PHOTOS Golonka, Was [hep-ph/0506026]
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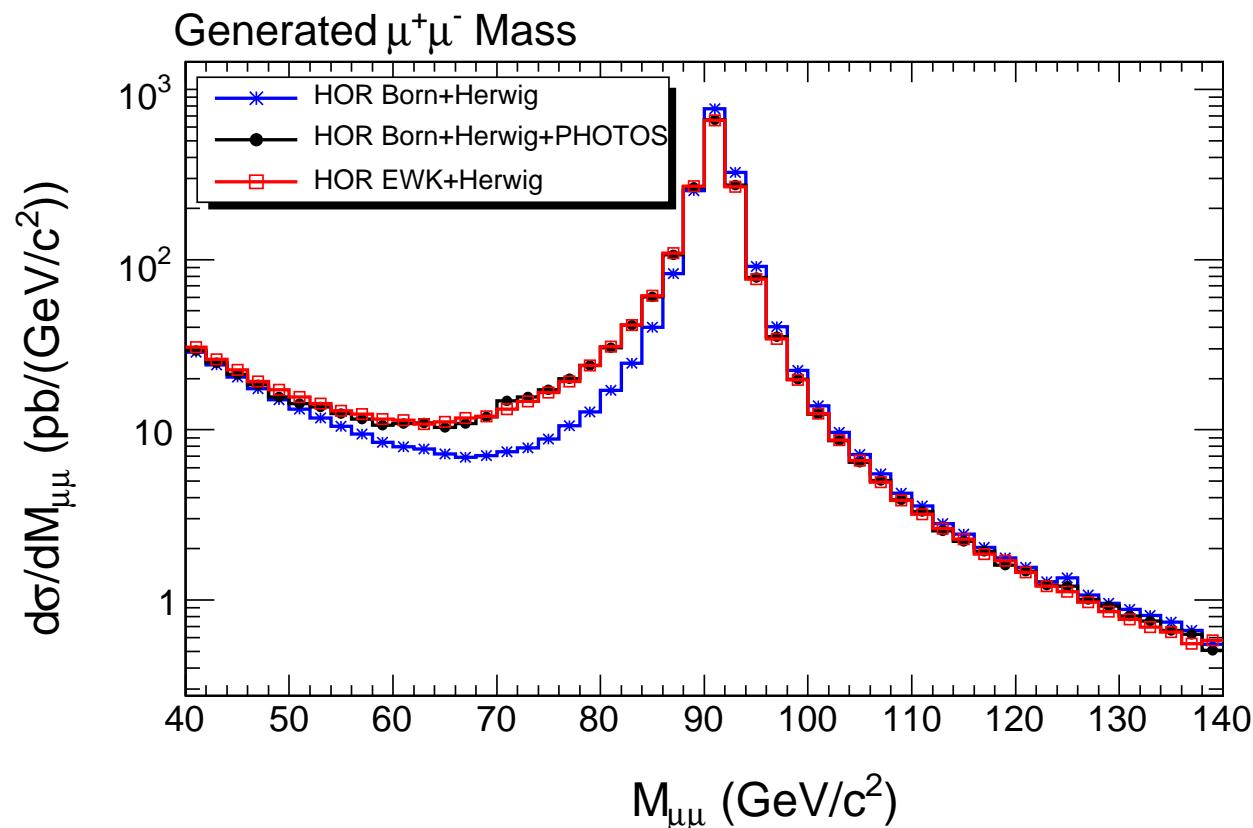
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easy to use ↔ precision



Z-boson lineshape

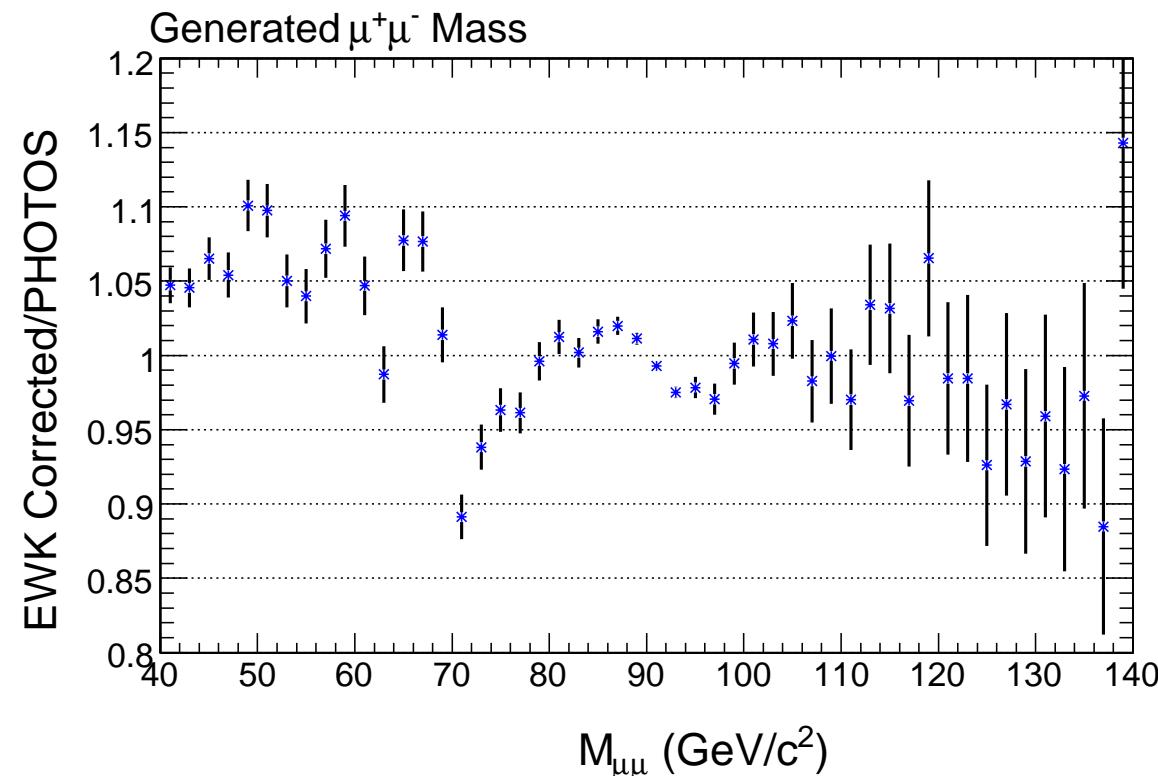
- Z lineshape for **calibration** (LEP as reference)



Z-boson lineshape

- Z lineshape for **calibration** (LEP as reference)
- How **precise** does the prediction have to be?

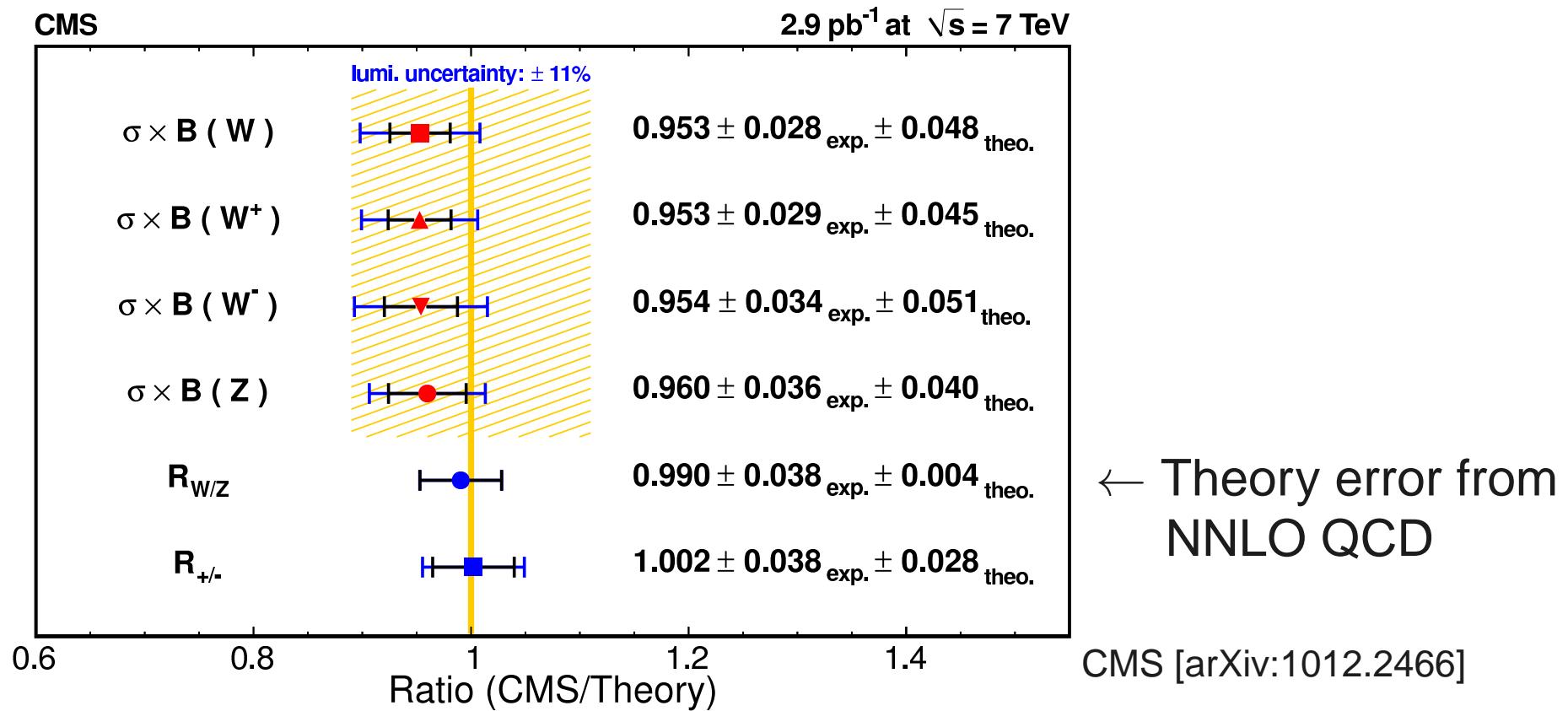
PHOTOS \leftrightarrow HORACE (NLO EW matched to parton shower)



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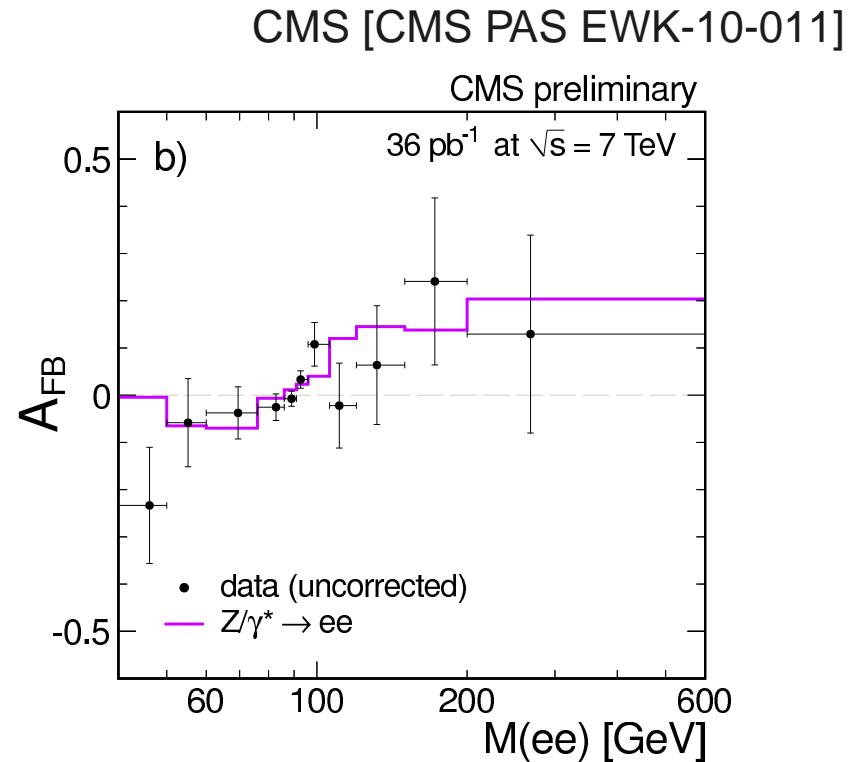
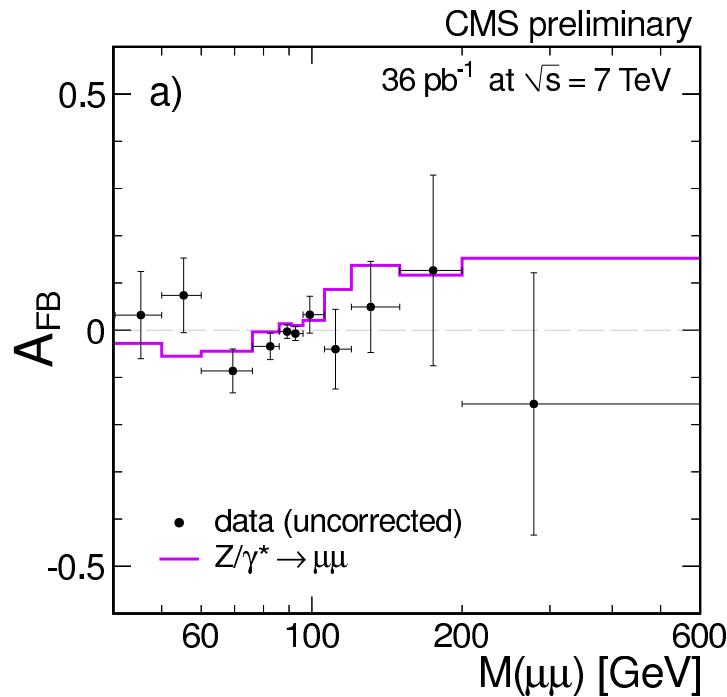
More precision observables

Cross section ratios



More precision observables

A_{FB} and $\sin^2 \theta_{\text{eff}}$



$$\Rightarrow \sin^2 \theta_{\text{eff}} = 0.2287 \pm 0.0077(\text{stat.}) \pm 0.0036(\text{syst.})$$

→ 0.0018 from FSR

⇒ room for improvement

(goal: $\delta \sin^2 \theta_{\text{eff}} = 0.0002$, LEP: $\sin^2 \theta_{\text{eff}} = 0.23153 \pm 0.00016$)

QCD \otimes EW corrections

Theory status:

- QCD: NNLO, resummation, parton shower matching
- EW: NLO, leading higher order contributions

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full (2-loop) $\mathcal{O}(\alpha\alpha_s)$ corrections not known

→ different possible choices for the combination:

Balossini et al. [arXiv:0907.0276]

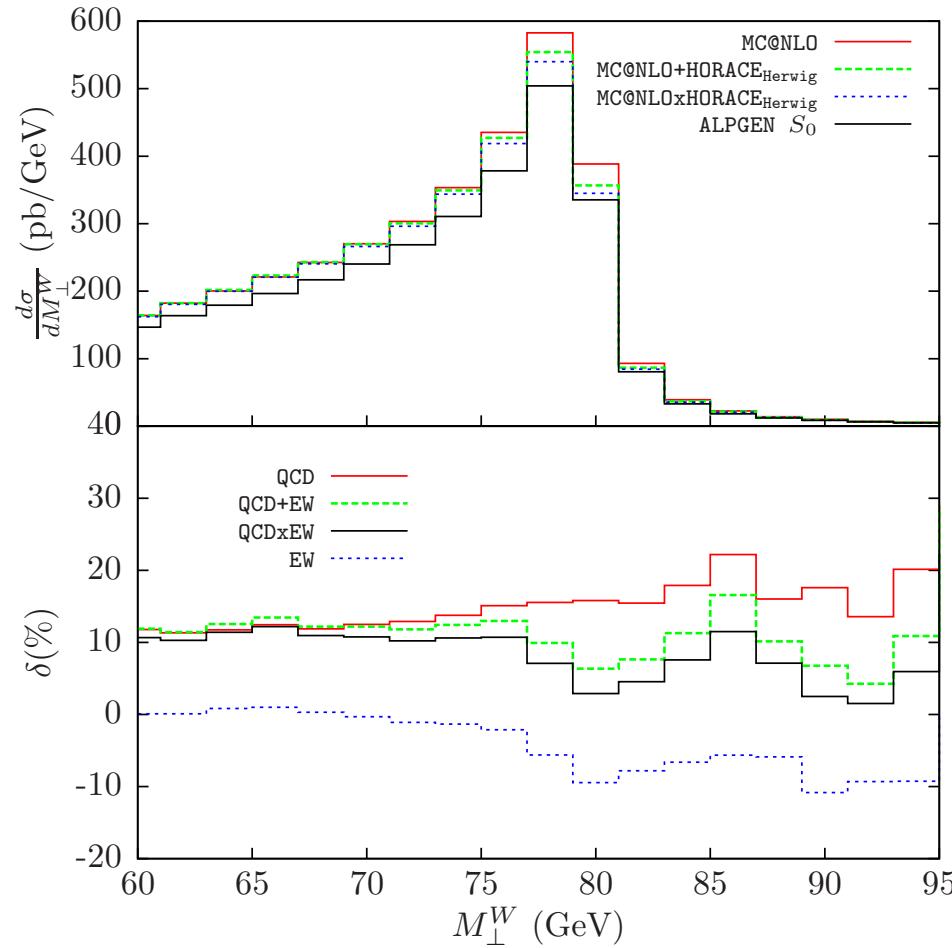
additive:

$$\left[\frac{d\sigma}{d\mathcal{O}} \right]_{\text{QCD+EW}} = \left\{ \frac{d\sigma}{d\mathcal{O}} \right\}_{\text{QCD}} + \left\{ \left[\frac{d\sigma}{d\mathcal{O}} \right]_{\text{EW}} - \left[\frac{d\sigma}{d\mathcal{O}} \right]_{\text{LO}} \right\}_{\text{HERWIG PS}}$$

factorized:

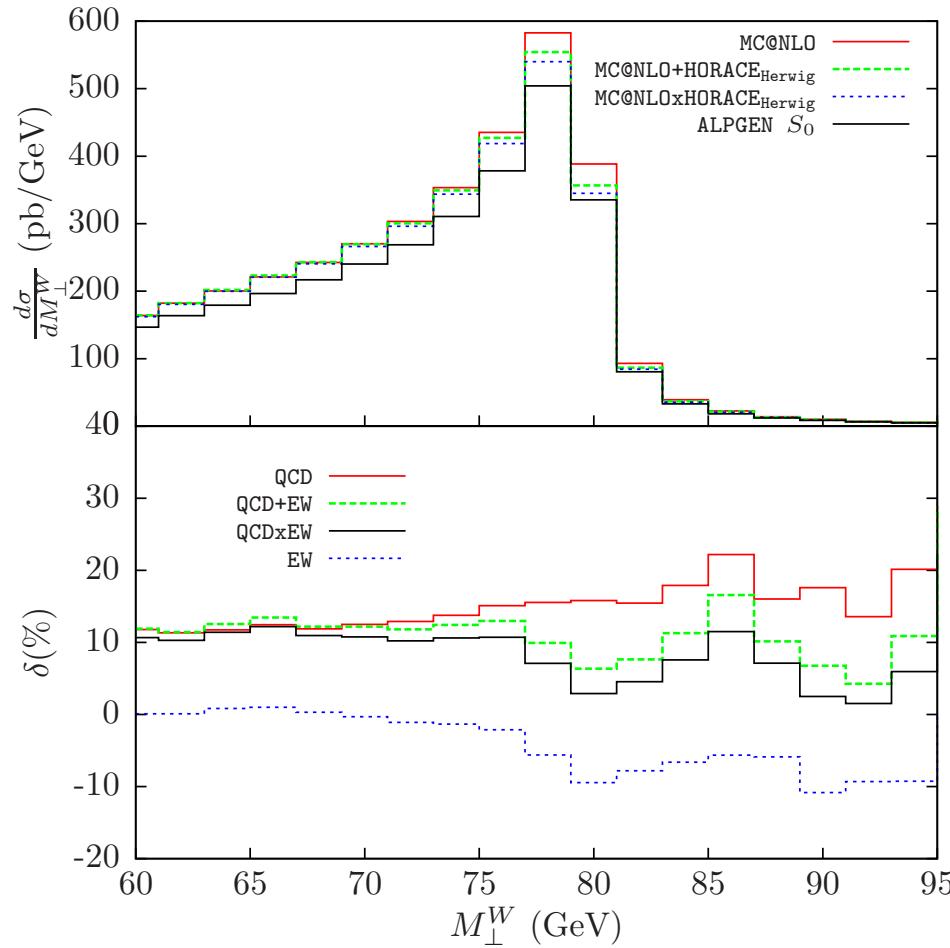
$$\left[\frac{d\sigma}{d\mathcal{O}} \right]_{\text{QCDxEW}} = \left(1 + \frac{\left[d\sigma/d\mathcal{O} \right]_{\text{MC@NLO}} - \left[d\sigma/d\mathcal{O} \right]_{\text{HERWIG PS}}}{\left[d\sigma/d\mathcal{O} \right]_{\text{LO/NLO}}} \right) \times \left\{ \frac{d\sigma}{d\mathcal{O}_{\text{EW}}} \right\}_{\text{HERWIG PS}}$$

Example: W production at the LHC:



QCD \otimes EW corrections

Example: W production at the LHC:



remaining ambiguity?

full $\mathcal{O}(\alpha\alpha_s)$:
→ work in progress

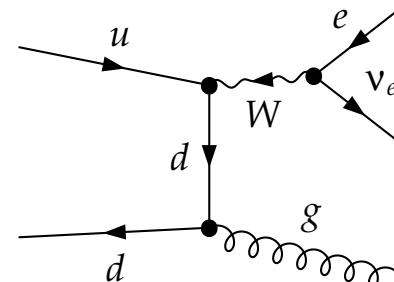
hard QCD radiation + EW
corrections:
→ W/Z+jet production

W/Z+jet production

$pp \rightarrow W + \text{jet} \rightarrow l\nu_l + \text{jet}$

$pp \rightarrow W + \text{jet} \rightarrow ll + \text{jet}$

- simple processes ...
... but leptons, p_T , miss, jet(s)

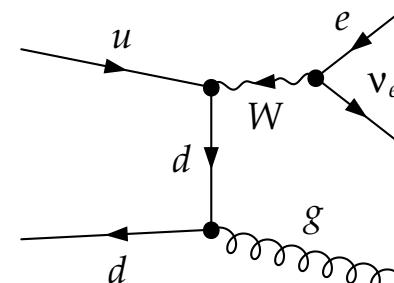


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Theoretical status:

- NLO QCD corrections known and available

DYRAD: Giele et al. [hep-ph/9302225]

MCFM: Campbell, Ellis [hep-ph/0202176]

and as part of NNLO single W: Melnikov, Petriello [hep-ph/0609070]

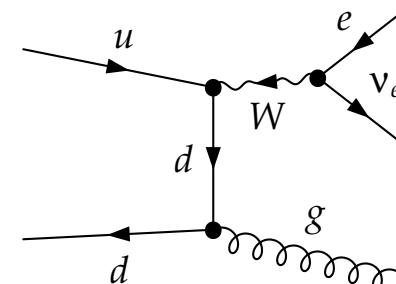
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Theoretical status:

- NLO QCD corrections known and available
- EW corrections for stable (on-shell) W bosons

Kühn, Kulesza, Pozzorini, Schulze [hep-ph/0703283], [arXiv:0708.0476]

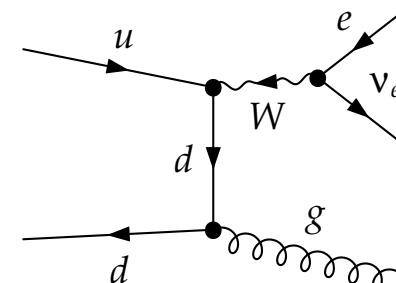
Hollik, Kasprzik, Kniehl [arXiv:0707.2553]

W/Z+jet production

$$pp \rightarrow W + \text{jet} \rightarrow l\nu_l + \text{jet}$$

$$pp \rightarrow W + \text{jet} \rightarrow ll + \text{jet}$$

- simple processes ...
... but leptons, $p_{\text{T, miss}}$, jet(s)



Theoretical status:

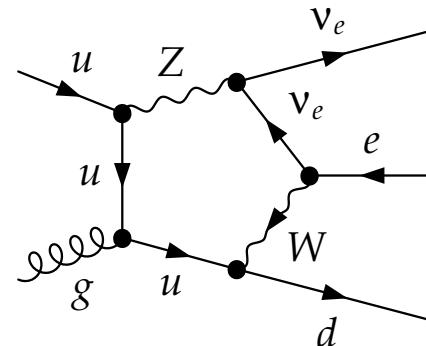
- NLO QCD corrections known and available
- EW corrections for stable (on-shell) W bosons
- Complete EW corrections available

W+jet: Denner, Dittmaier, Kasprzik, AM [arXiv:0906.1656]

Z+jet: Denner, Dittmaier, Kasprzik, AM [arXiv:1103.0914]

EW corrections

Complete EW corrections:



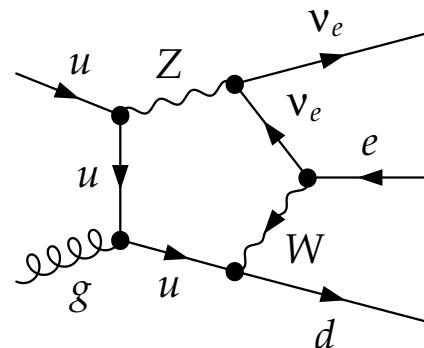
+

$\mathcal{O}(100)$ diagrams for W ,
 $\mathcal{O}(200)$ diagrams for Z
per partonic channel

- physical final state
- all off-shell effects included
- part of the $\mathcal{O}(\alpha\alpha_s)$ corrections for incl. W production

EW corrections

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per partonic channel

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Common issues for EW calculations:

- How to treat resonances?
- How to treat final-state photons?
- What about initial-state photons?

- naive **fixed-width** scheme
 - $\frac{1}{p^2 - M^2} \rightarrow \frac{1}{p^2 - M^2 + iM\Gamma}$
 - breaks gauge invariance (mildly?)
 - singularity structure at **NLO** screwed up

- naive **fixed-width** scheme
- **pole** expansions

Stuart [’91], Aeppli et al. [’93,’94], etc.

- gauge invariant
- not reliable at threshold or in off-shell tails

Resonances

- naive **fixed-width** scheme
- **pole** expansions
- **effective field theory** approach

Beneke, Chapovsky, Signer,Zanderighi [hep-ph/0312331,hep-ph/0401002]

Fleming, Hoang, Mantry, Stewart [hep-ph/0703207]

- gauge invariant
- valid at threshold
- framework for resummations
- for specific observables only (e.g. total cross section)

Resonances

- naive **fixed-width** scheme
- **pole** expansions
- **effective field theory** approach
- **complex mass scheme**

Denner, Dittmaier, Roth, Wieders [hep-ph/0505042]

- use complex W and Z masses everywhere by means of complex renormalization:

$$M_{V,0}^2 = \mu_V^2 + \delta\mu_V^2 \quad \text{with: } M_{V,0}^2 = \text{bare mass } (V = W, Z)$$

μ_V^2 = ren. complex mass

$\delta\mu_V^2$ = complex counterterm

- \Rightarrow complex $s_W^2 = 1 - \mu_W^2/\mu_Z^2$
- loop-integrals for complex masses needed
- unitarity-violating beyond NLO accuracy
- gauge invariant
- valid **everywhere in phase space**

How to deal with photon radiation from bare leptons?

- keep physical lepton mass in the amplitudes
 - ⇒ numerical integration of large logarithms necessary
- subtraction formalism also for non-collinear safe observables
 - ⇒ muon-mass logarithms extracted analytically

Dittmaier, Kabelschacht, Kasprzik [arXiv:0802.1405]

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- initial state photon emission ⇒ **collinear singularity**
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- additional $\mathcal{O}(\alpha)$ correction: photon-induced processes

Photons II

Treat final-state **photons** like another **parton**?

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- \Rightarrow this is what we want; But: **not infrared safe**

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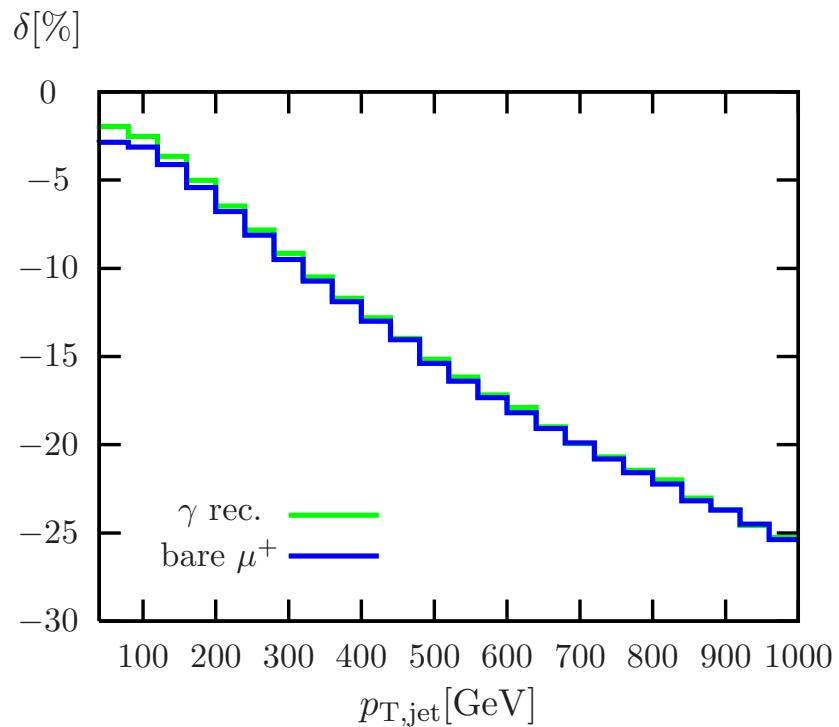
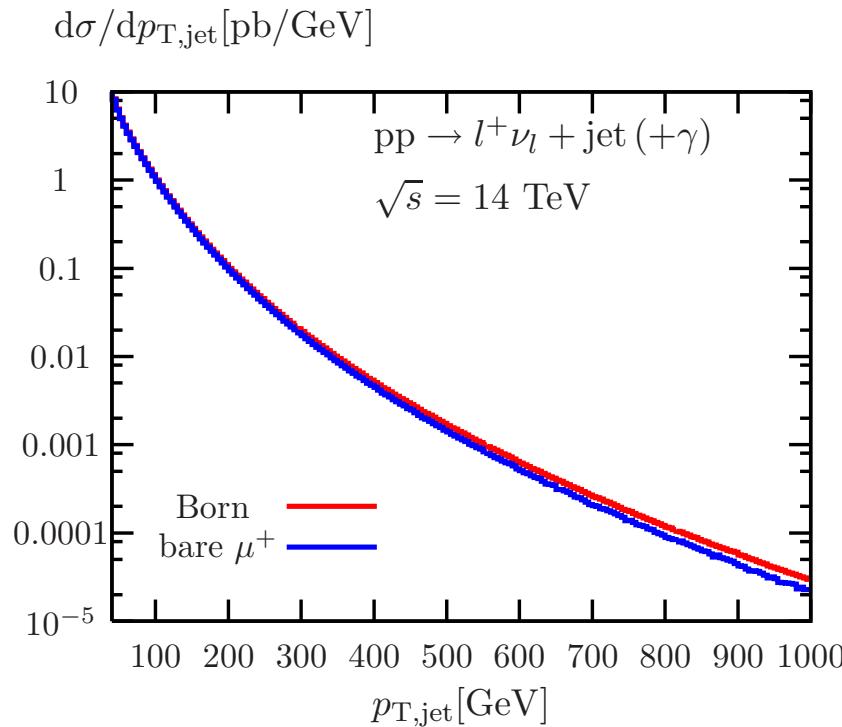
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- or **cut on photon energy fraction** z_γ inside a jet
 - \Rightarrow isolate singularity analytically (\rightarrow subtraction formalism)
 - \Rightarrow absorb singularity into measured **quark-to-photon fragmentation function**

selected W/Z+jet results

$p_{\text{T,jet}}$ distribution for W+jet at the LHC:

Denner, Dittmaier, Kasprzik, AM [arXiv:0906.1656]



large corrections at large energies (Sudakov logs)
(on-shell W good approximation)

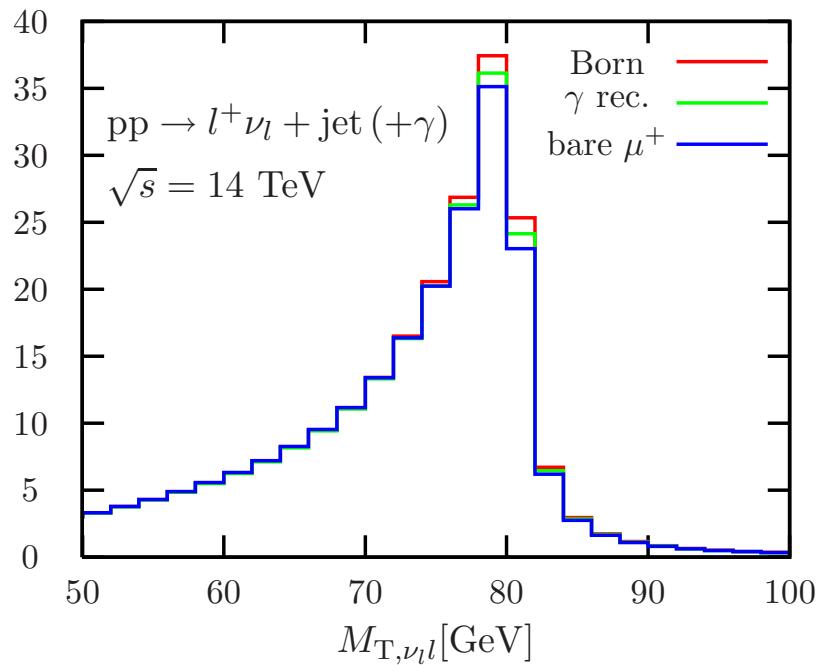
selected W/Z+jet results

M_T distribution for the LHC:

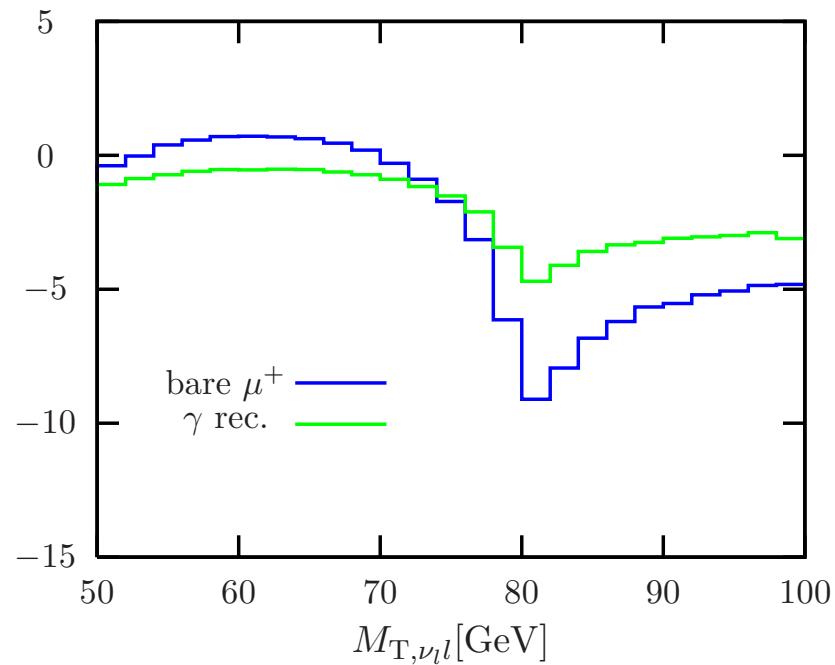
$$M_{T,\nu_l l} = \sqrt{2 p_{T,l} p_T^{\text{miss}} (1 - \cos \phi_{\nu_l l})}$$

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$d\sigma/dM_{T,\nu_l l} [\text{pb}/\text{GeV}]$



$\delta [\%]$



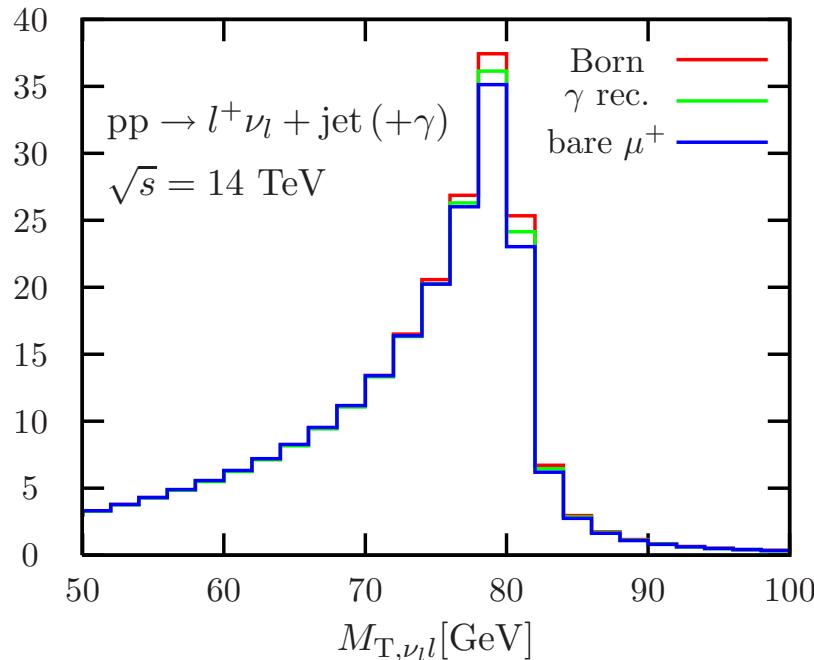
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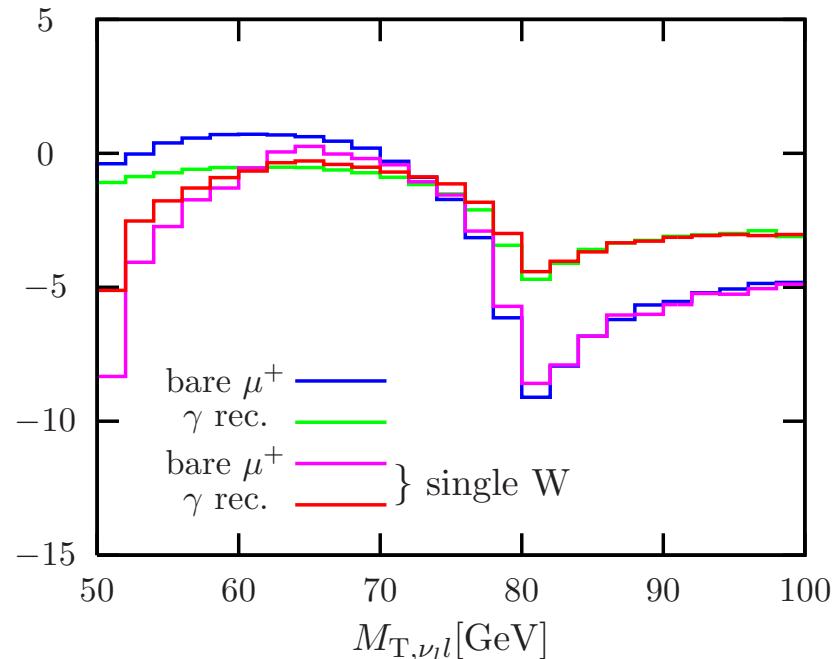
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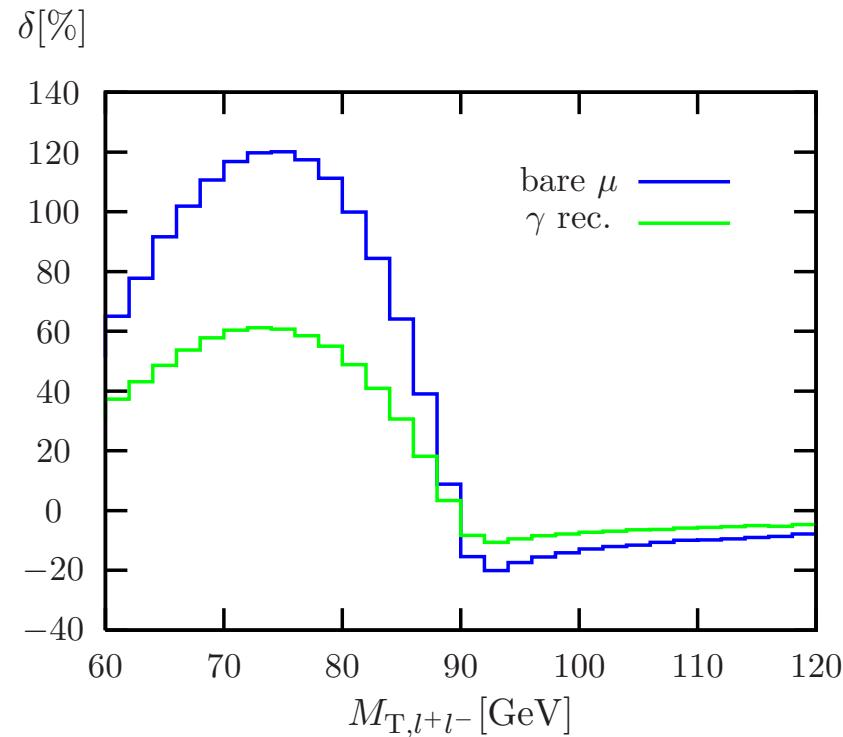
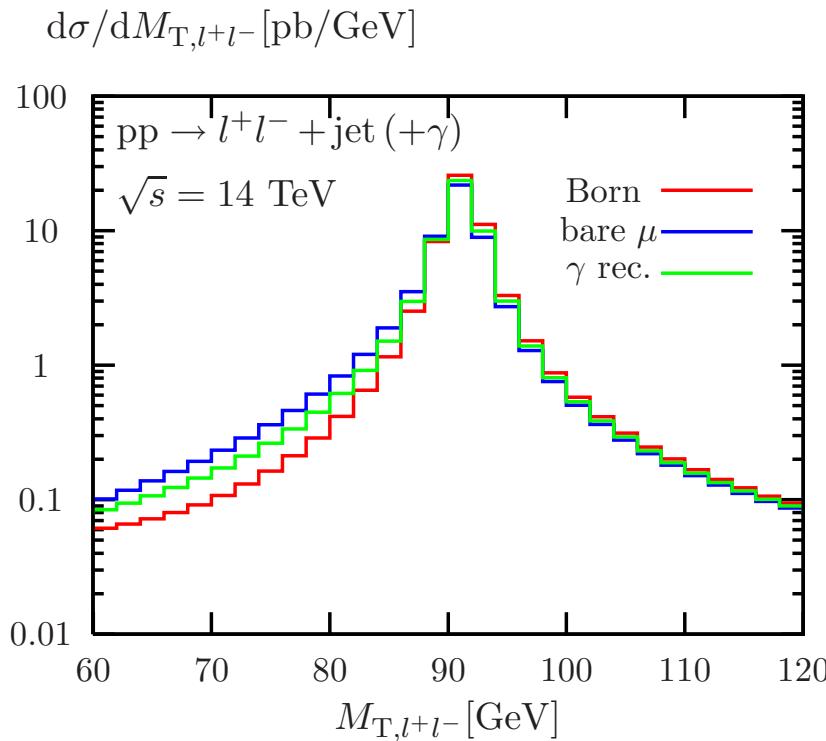
corrections very similar to single W production

⇒ supports **factorization** for QCD \otimes QED corrections

selected W/Z+jet results

Z lineshape in Z+jet events at the LHC:

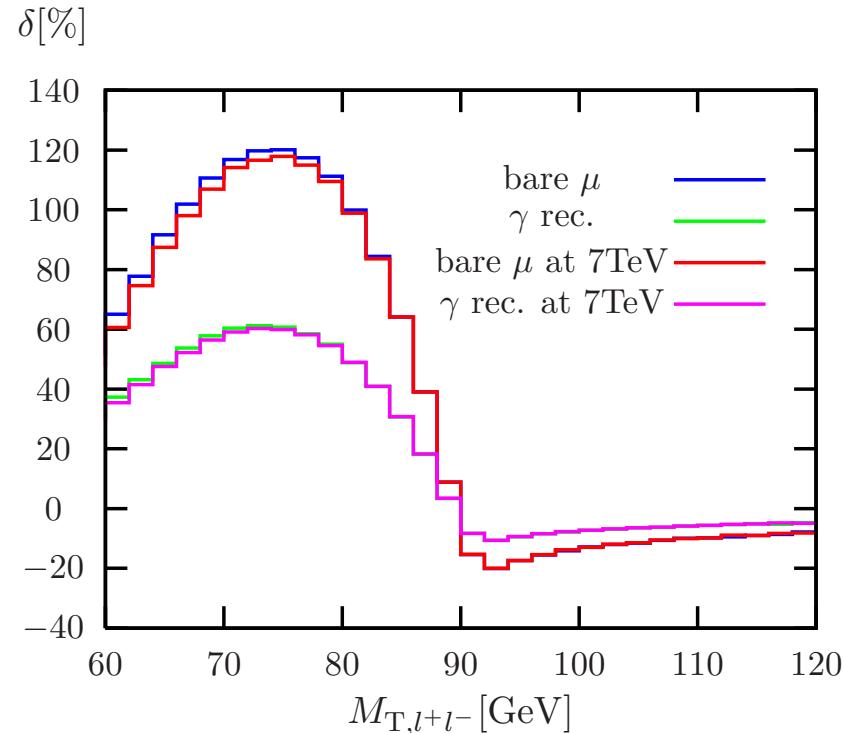
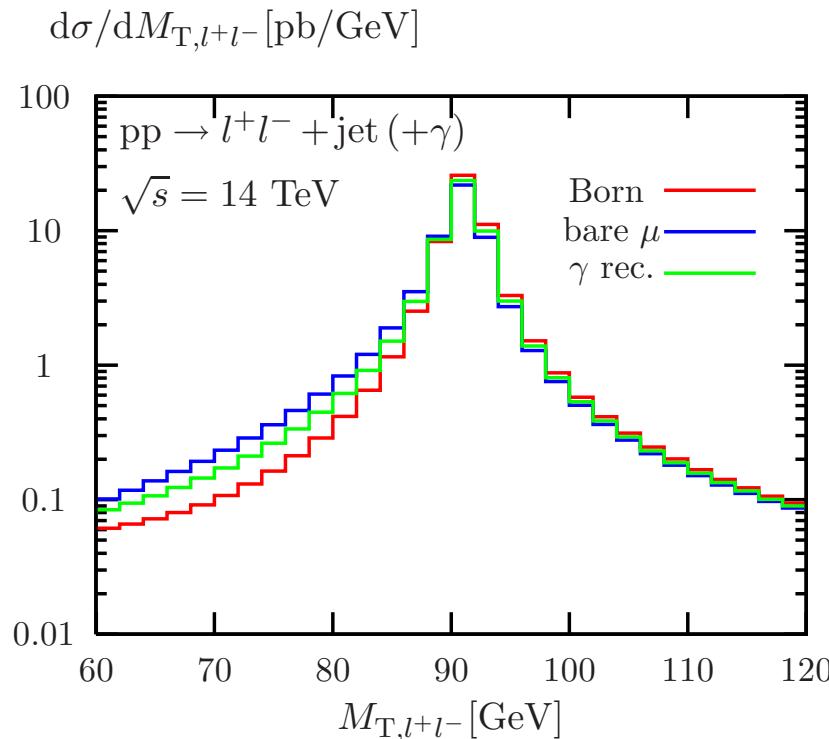
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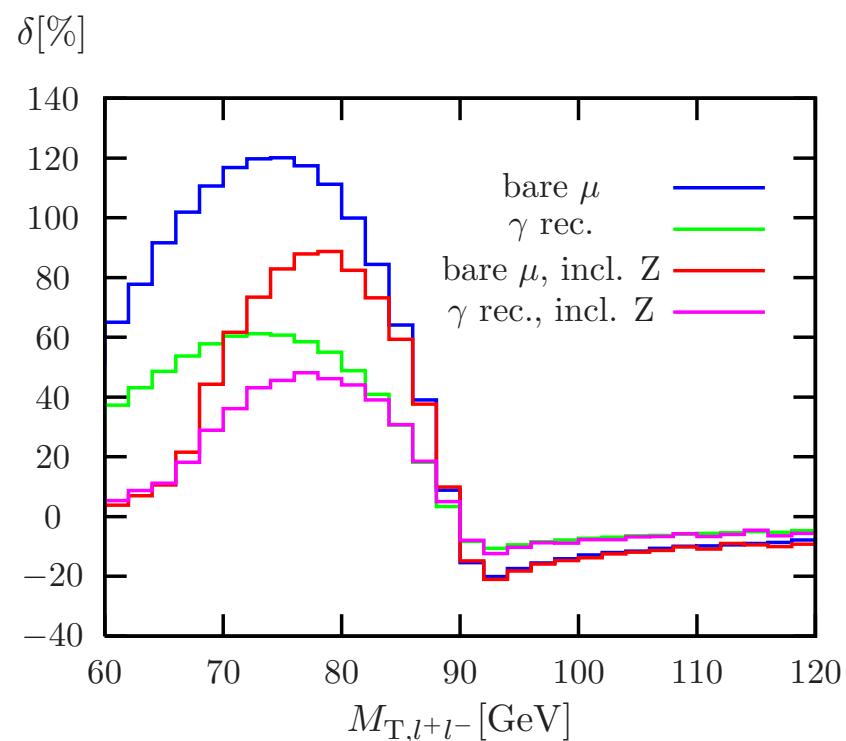
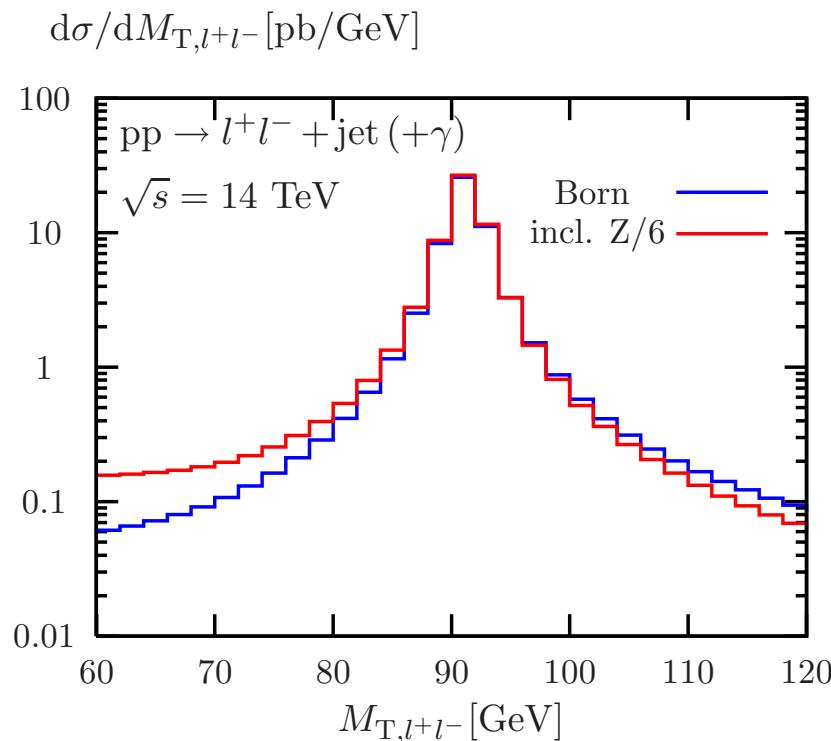
Denner, Dittmaier, Kasprzik, AM [arXiv:1103.0914]



corrections hardly differ at 7 TeV

selected W/Z+jet results

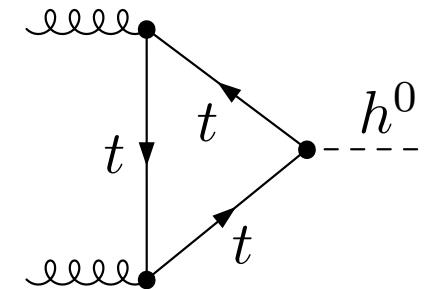
comparison with inclusive Z production:



lineshape (and corrections) depends on $p_{T,Z}$ in the tail

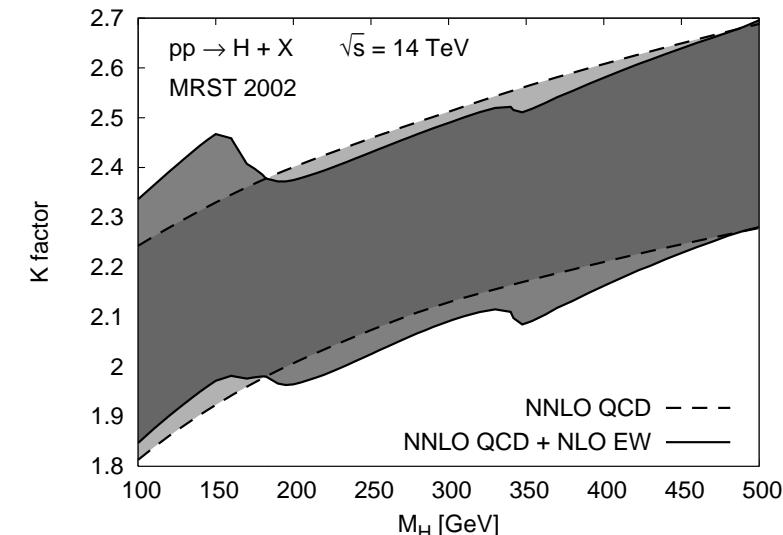
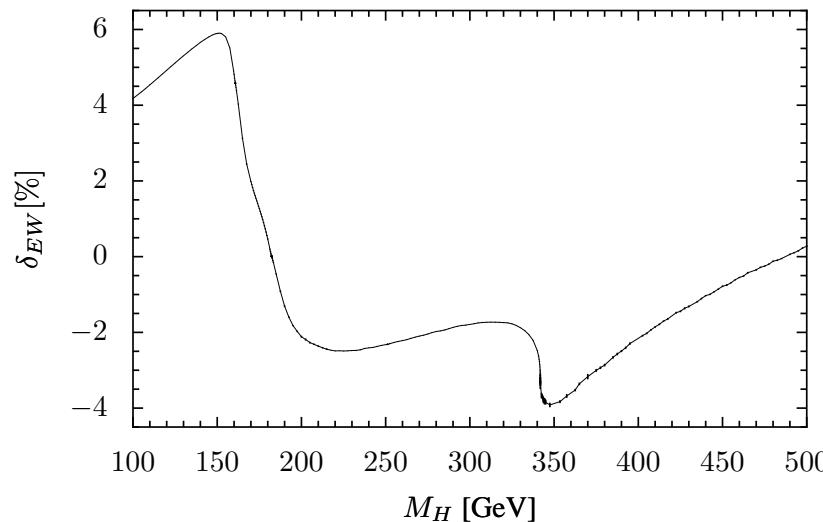
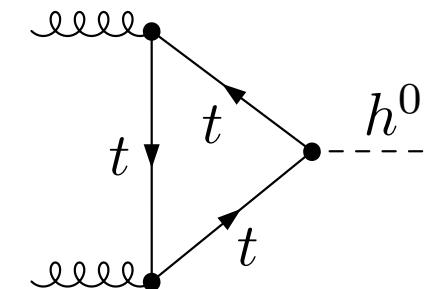
Higgs in Gluon-Fusion

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- enormous efforts for the QCD prediction



Higgs in Gluon-Fusion

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- enormous efforts for the QCD prediction
- full NLO (2-loop) EW corrections

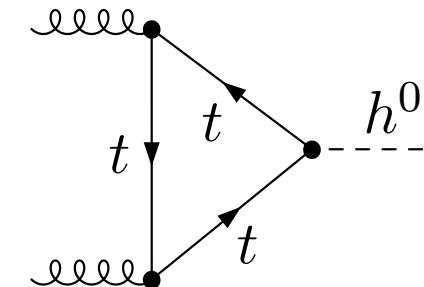


Actis, Passarino, Sturm, Uccirati [arXiv:0809.1301]

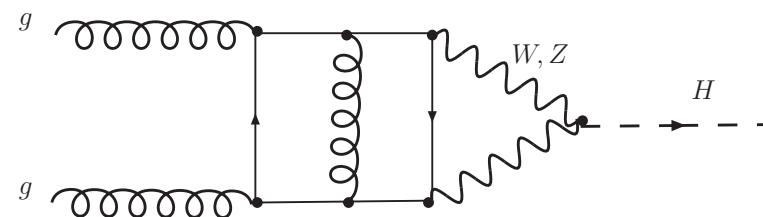
- non-trivial threshold behaviour inside loops (WW,ZZ, $t\bar{t}$)
 \Rightarrow complex-mass scheme at two loops

Higgs in Gluon-Fusion

- dominant production process at LHC
- enormous efforts for the QCD prediction
- full NLO (2-loop) EW corrections
- mixed $\mathcal{O}(\alpha\alpha_s)$ corrections (light fermion loops)



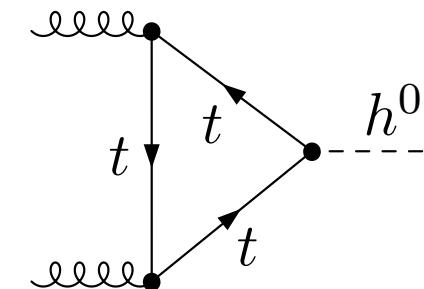
Anastasiou, Boughezal, Petriello [arXiv:0811.3458]



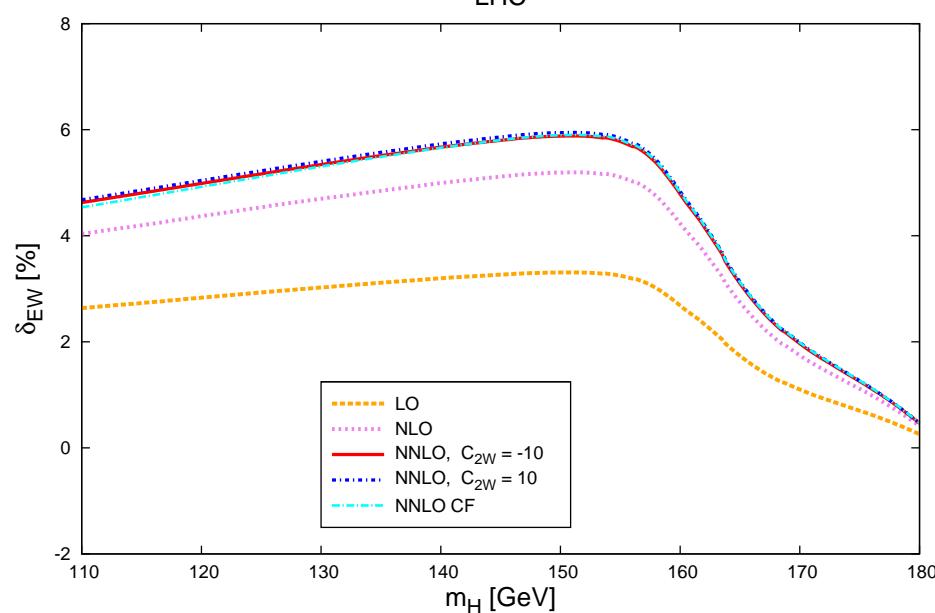
⇒ effective theory approach

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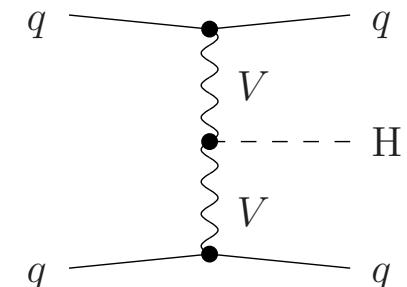
Anastasiou, Boughezal, Petriello [arXiv:0811.3458]



supports factorization
of EW and QCD corrections

Higgs in VBF

- important Higgs discovery channel
- measurement of HVV couplings
- powerful cuts for background suppression
- small QCD uncertainty: $\pm 4\%$ (DIS like process) \rightarrow VBFNLO



Figi, Oleari, Zeppenfeld [hep-ph/0306109]

Higgs in VBF

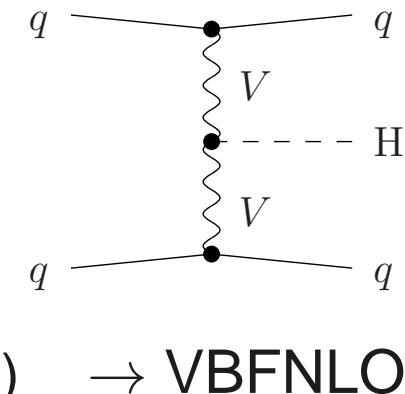
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Ciccolini, Denner, Dittmaier [arXiv:0710.4749]

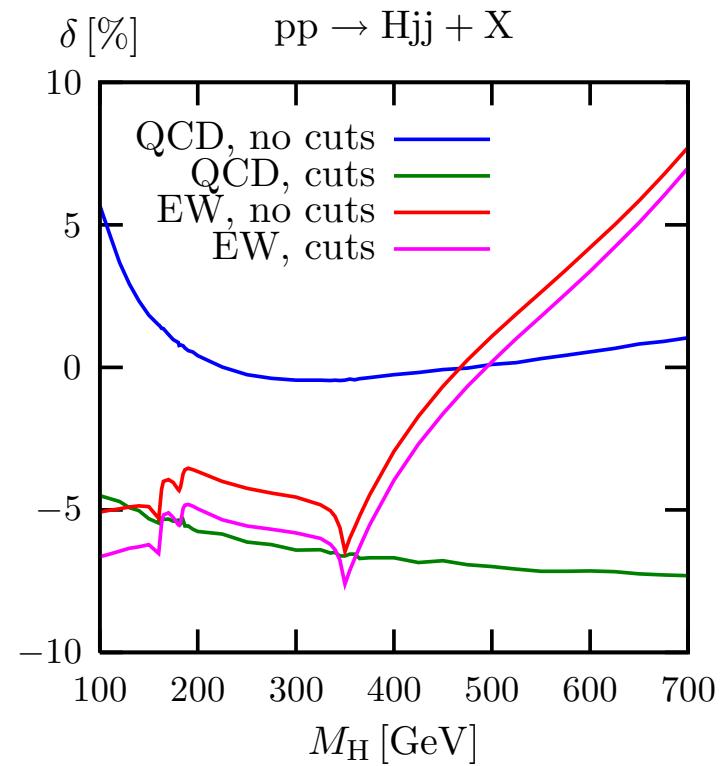
no VBF approximations

flexible tool: **HAWK**

Denner, Dittmaier, AM [<http://omnibus.uni-freiburg.de/~sd565/programs/hawk/hawk.html>]



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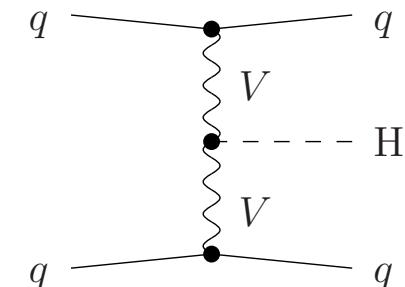
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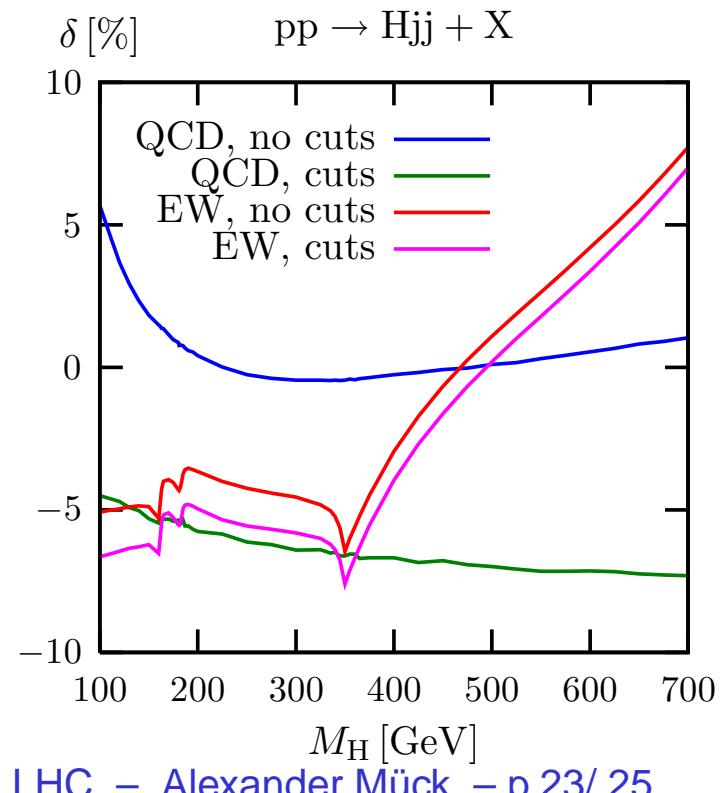
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⇒ Higgsstrahlung included
(leptonic V decays: available soon)



→ VBFNLO



Higgs Decays

NLO EW corrections to Higgs boson decays:

- $H \rightarrow f\bar{f}$

Bardin, Vilensky, Khristova
[Sov.J.Nucl.Phys. 53 (1991) 152]
Dabelstein, Hollik
[Z.Phys. C53 (1992) 507]
Kniehl
[Nucl.Phys. B376 (1992) 3]

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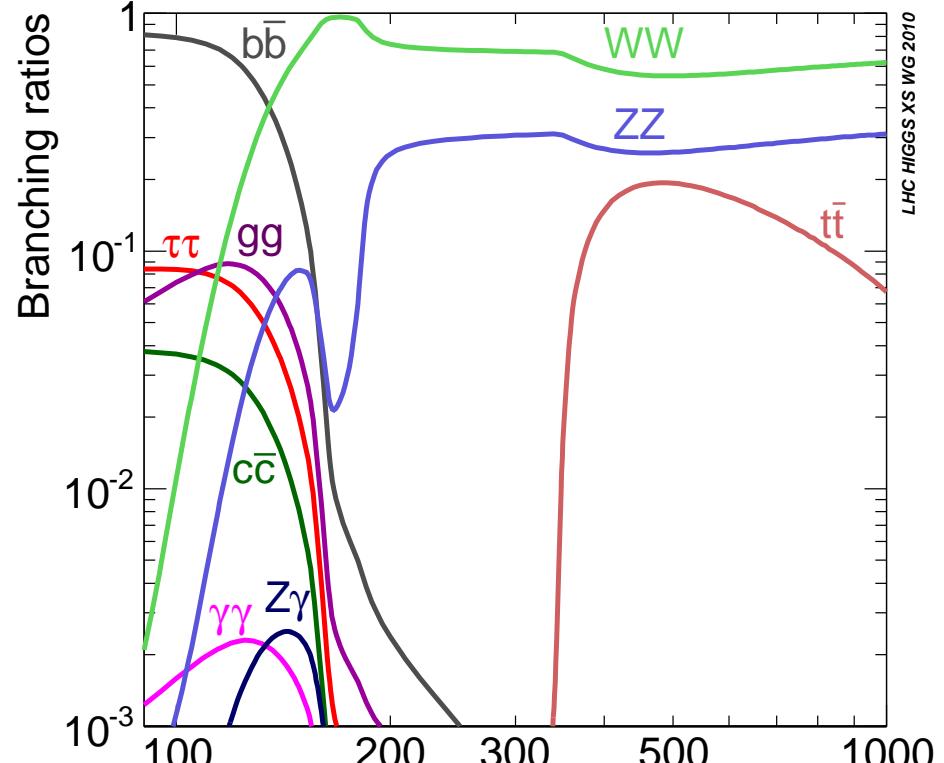
- $H \rightarrow gg$

Actis, Passarino, Sturm, Uccirati
[arXiv:0809.1301]

all included in **HDECAY**

(together with QCD corrections)

Djouadi, Kalinowski, Spira [hep-ph/9704448]



M_H [GeV]
LHC Higgs Cross Section
Working Group
[arXiv:1101.0593]

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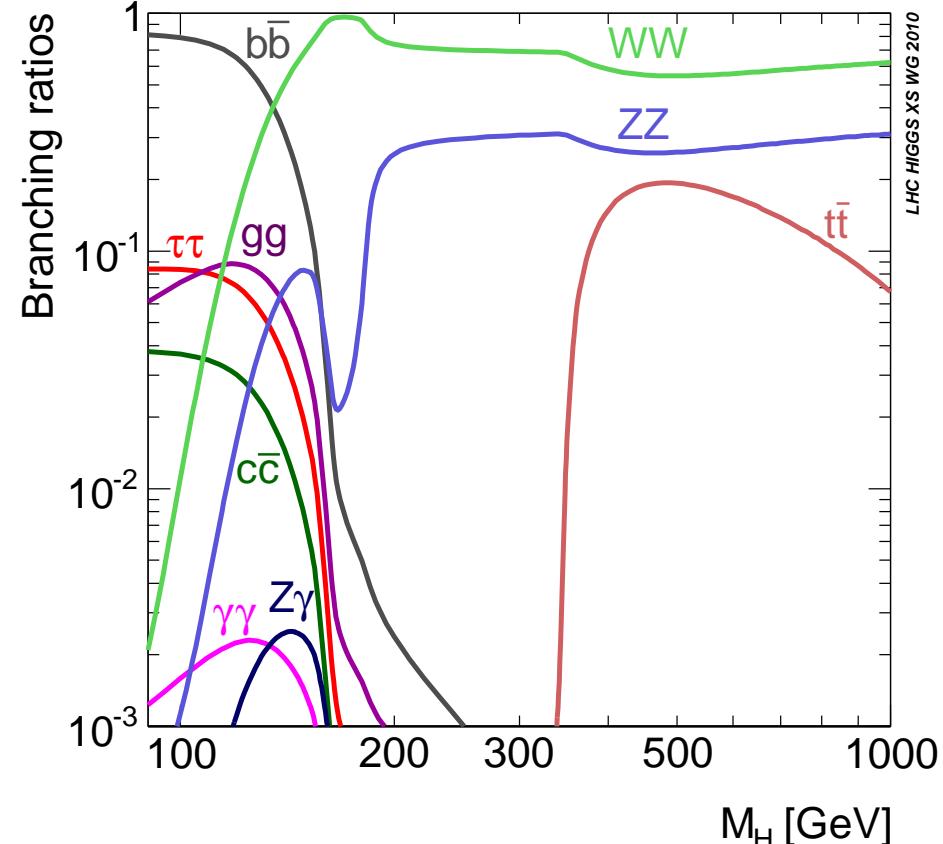
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[arXiv:0809.1301]

- $H \rightarrow WW/ZZ \rightarrow 4f$

for off-shell/decaying W/Z bosons

Bredenstein, Denner, Dittmaier, Weber [hep-ph/0611234]



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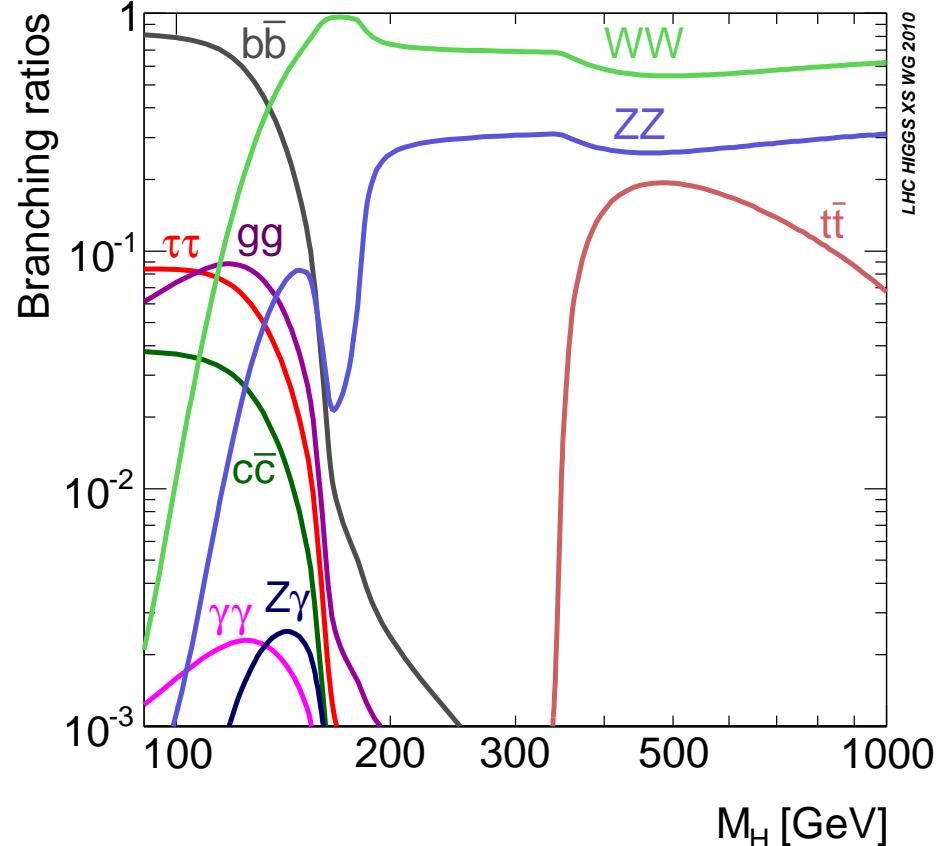
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[arXiv:0809.1301]

- $H \rightarrow WW/ZZ \rightarrow 4f$

⇒ **Prophecy4f** MC generator



Bredenstein, Denner, Dittmaier, AM, Weber

[<http://omnibus.uni-freiburg.de/~sd565/programs/prophecy4f/prophecy4f.html>]

Summary

LHC is a tool for precision physics (e.g. M_W , Γ_W , $\sin \theta_{\text{eff}}^{\text{lept}}$, ...)

Electroweak corrections at the LHC:

- important for any precision measurement (percent level)
- enhancements in specific cases
 - collinear photon radiation
 - Sudakov Logs at high energies
- many calculations are available
- Tools are available (in particular for Drell-Yan)

Outlook/Questions:

- Theory: more on $\mathcal{O}(\alpha\alpha_s)$?
missing calculations? missing observables?
- Analysis: efficiency \leftrightarrow accuracy? missing observables?

Back-up slides

non collinear-safe subtract.

- usual subtraction procedure:

$$\int d\Phi_{n+1} |\mathcal{M}|^2 = \int d\Phi_{n+1} \left(|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2 \right) + \int d\Phi_n \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$$

- clever choice of $|\mathcal{M}_{\text{Sub}}|^2$
 - $\Rightarrow (|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2)$ is integrable
 - $\Rightarrow \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$ can be done analytically

non collinear-safe subtract.

- usual subtraction procedure:

$$\int d\Phi_{n+1} |\mathcal{M}|^2 = \int d\Phi_{n+1} \left(|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2 \right) + \int d\Phi_n \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$$

- $\mathcal{M}_{\text{Sub}} = \sum_f \mathcal{M}_{\text{Sub}}(p_{\text{jet}}, z_f)$ where $z_f \rightarrow p_f^0/(p_f^0 + p_\gamma^0)$, $p_{\text{jet}} \rightarrow p_f^0 + p_\gamma^0$
for collinear events
- only cuts on p_{jet} , no cuts on $p_f \Rightarrow$ cuts independent of z_f
 $\Rightarrow z_f$ integration can be done analytically

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for collinear events
- only cuts on p_{jet} , no cuts on $p_f \Rightarrow$ cuts independent of z_f
 $\Rightarrow z_f$ integration can be done analytically

- non-collinear safe implementation:

- no recombination: cuts on p_f allowed
- cut on z_f in \mathcal{M}_{Sub} to ensure cancellation of singularities
- integrate over z_f in dk_γ numerically

(soft divergence treated via Plus-distribution
in analogy to treatment of initial-state emitters/spectators)

photon–jet recombination

What does z_γ cut imply?

- sensitivity to $q \rightarrow q\gamma$ splitting
- non-perturbative corrections to be included

photon-jet recombination

What does z_γ cut imply?

- sensitivity to $q \rightarrow q\gamma$ splitting
- non-perturbative corrections to be included
- introduce quark-to-photon fragmentation function $D_{q \rightarrow \gamma}(z_\gamma, \mu_F)$
 - measured in hadronic Z decays at LEP ($Z \rightarrow q\bar{q} \rightarrow q\bar{q}\gamma$)
 - using ALEPH fit:

$$D_{q \rightarrow \gamma}(z_\gamma, \mu_F) = \frac{\alpha Q_q^2}{2\pi} P_{q \rightarrow \gamma}(z_\gamma) \left(\ln \frac{m_q^2}{\mu_F^2} + 2 \ln z_\gamma + 1 \right) + D_{q \rightarrow \gamma}^{\text{ALEPH}}(z_\gamma, \mu_F),$$

where

$$D_{q \rightarrow \gamma}^{\text{ALEPH}}(z_\gamma, \mu_F) = \frac{\alpha Q_q^2}{2\pi} \left(P_{q \rightarrow \gamma}(z_\gamma) \ln \frac{\mu_F^2}{(1 - z_\gamma)^2 \mu_0^2} + C \right)$$

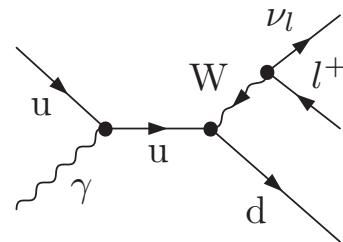
$$P_{q \rightarrow \gamma}(z_\gamma) = \frac{1 + (1 - z_\gamma)^2}{z_\gamma}$$

up to $\mathcal{O}(\alpha^3 \alpha_s)$ in W/Z+jet

- also full NLO QCD corrections
 - variable (phase-space dependent) scale supported

up to $\mathcal{O}(\alpha^3 \alpha_s)$ in W/Z+jet

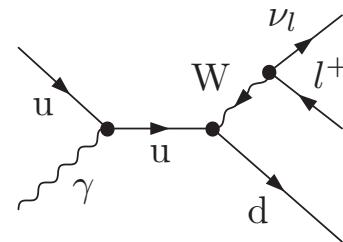
- also full NLO QCD corrections
 - variable (phase-space dependent) scale supported
- photon-induced processes



at NLO QCD
(phenomenologically irrelevant)

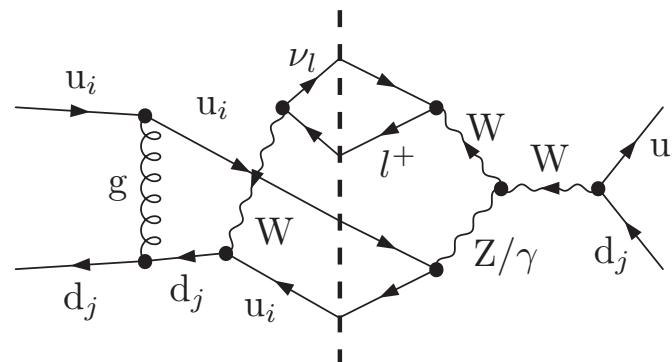
up to $\mathcal{O}(\alpha^3 \alpha_s)$ in W/Z+jet

- also full NLO QCD corrections
 - variable (phase-space dependent) scale supported
- photon-induced processes



at NLO QCD
(phenomenologically irrelevant)

- QCD-EW interference terms in 4-quark processes



(phenomenologically irrelevant,
dropped for Z+jet)

MC programs for W/Z+jet

two completely independent calculations

- in mutual agreement
- FeynArts 1.0 [Böhm, Denner, Küblbeck]
 - in-house Mathematica Routines
 - loop integral library: DD [Dittmaier]
 - Vegas integration
- FeynArts 3.2, FormCalc 3.1 [Hahn]
 - loop integral library: Coli [Denner]
 - Pole [Meier, AM]
 - using Weyl-van der Waerden formalism Dittmaier [hep-ph/9805445]
 - automatic generation of subtraction/slicing terms
 - automatic multi-channeling using Lusifer Dittmaier, Roth [hep-ph/0206070]

Setup for W/Z+jet

basic cuts

- $p_{\text{T},l/\text{miss/jet}} > 25 \text{ GeV}$
- $|y_{l/\text{jet}}| < 2.5$
- lepton isolation: $R_{l,\text{jet}} > 0.5$
- photon-energy fraction inside jets: $z_\gamma < 0.7$

recombination

- do not recombine photons and muons (bare μ^+)
- photons and electrons: $R_{\gamma,l} < 0.1$ (γ rec.)
- photons and partons: $R_{\gamma,\text{jet}} < 0.5$

renormalization and factorization scale

- fixed scale ($\mu = M_{\text{W/Z}}$)
- variable scale: $\mu = \sqrt{M_{\text{W/Z}}^2 + p_{\text{T}}^{\text{had}}}$ (our default choice)

QCD corrections

$p_{T,\text{jet}}$ distribution for the LHC:

huge NLO QCD corrections:

new kinematical configuration:

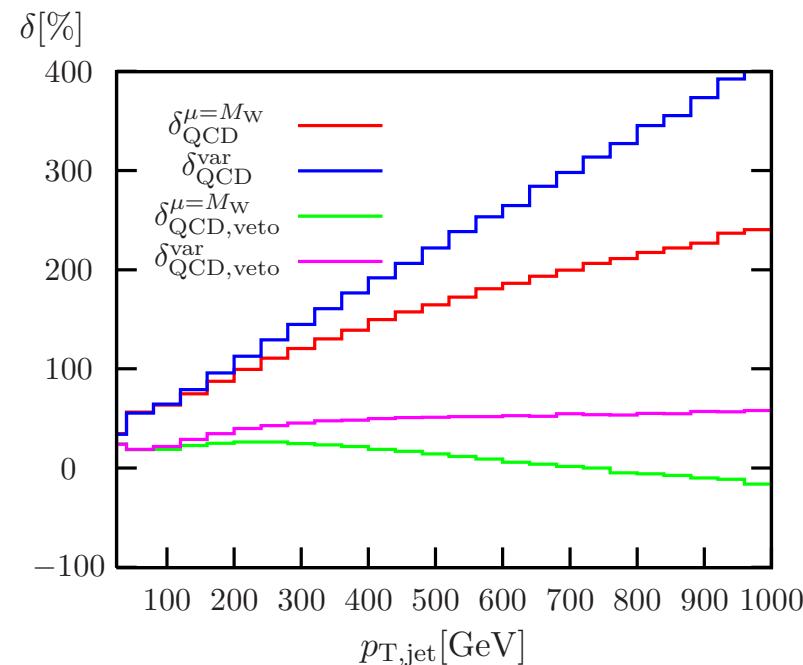
back-to-back jets balance p_T

⇒ 2 jet events with W emission

⇒ no genuine QCD correction
for W+jet

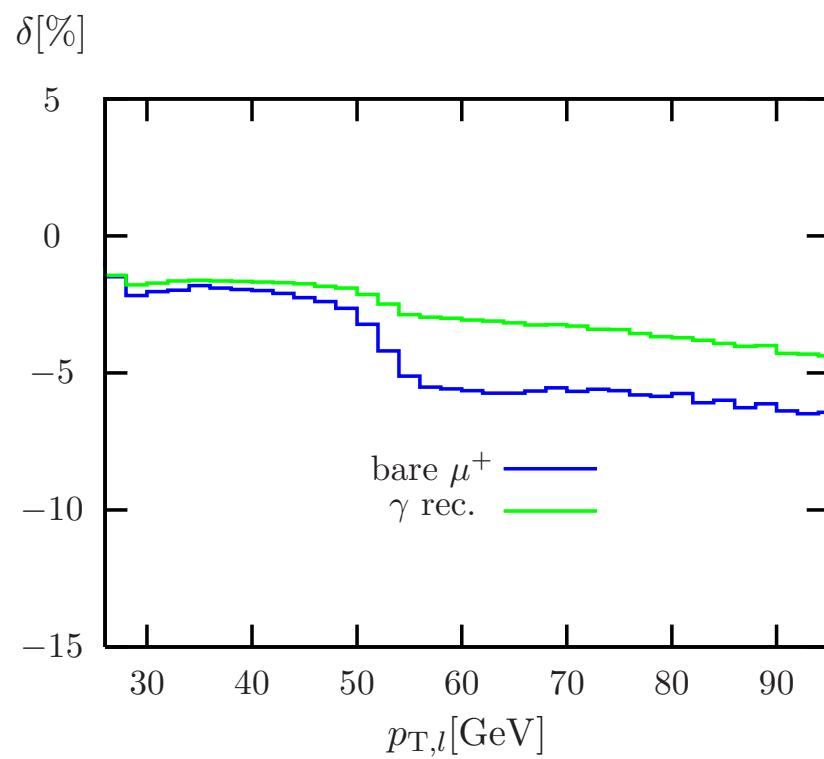
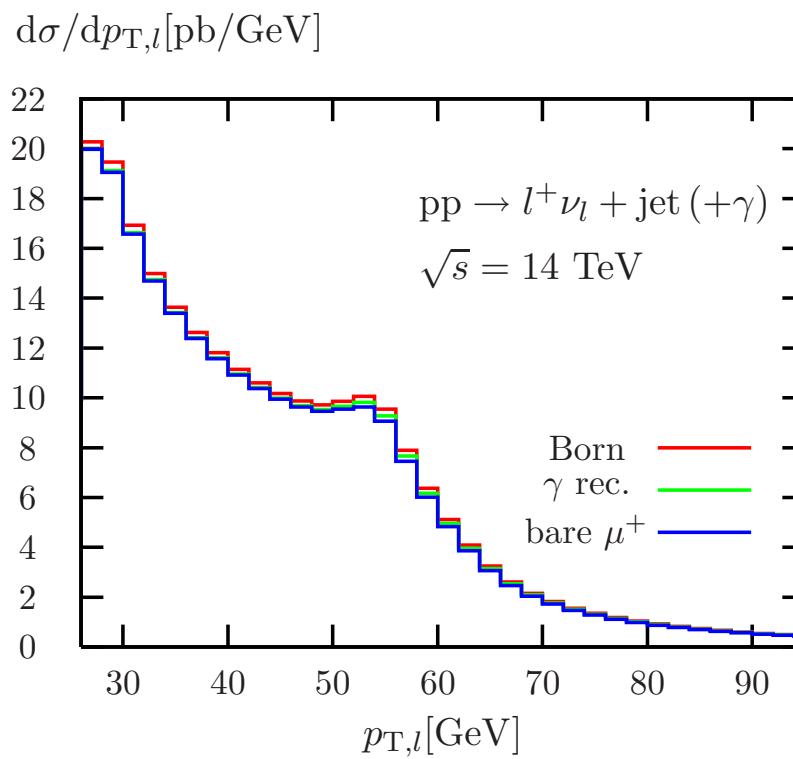
use simple jet veto:

veto second jet with $p_T > \frac{1}{2} p_T^{\text{lead}}$.



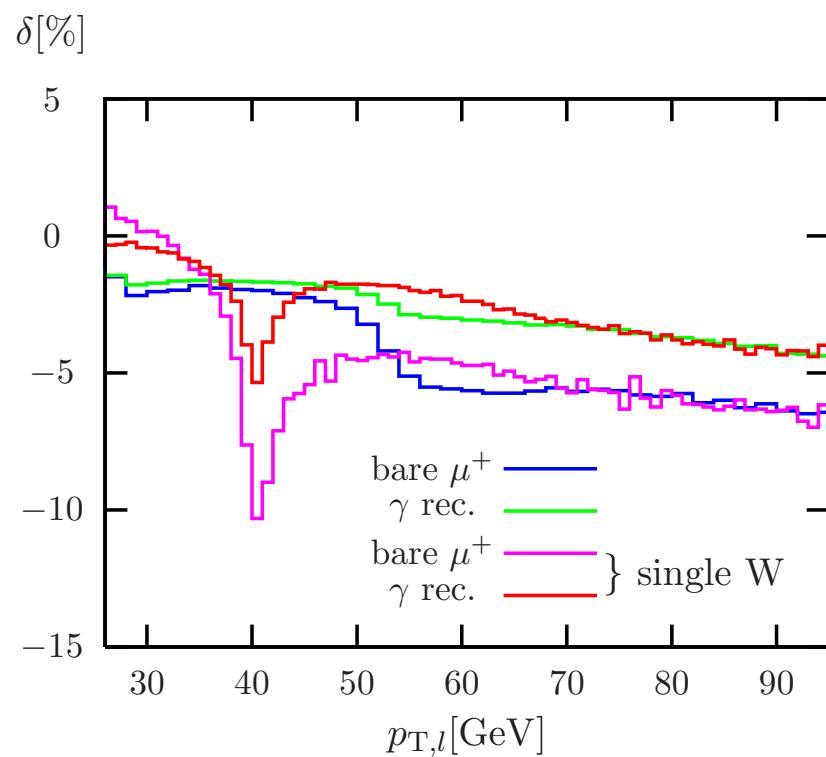
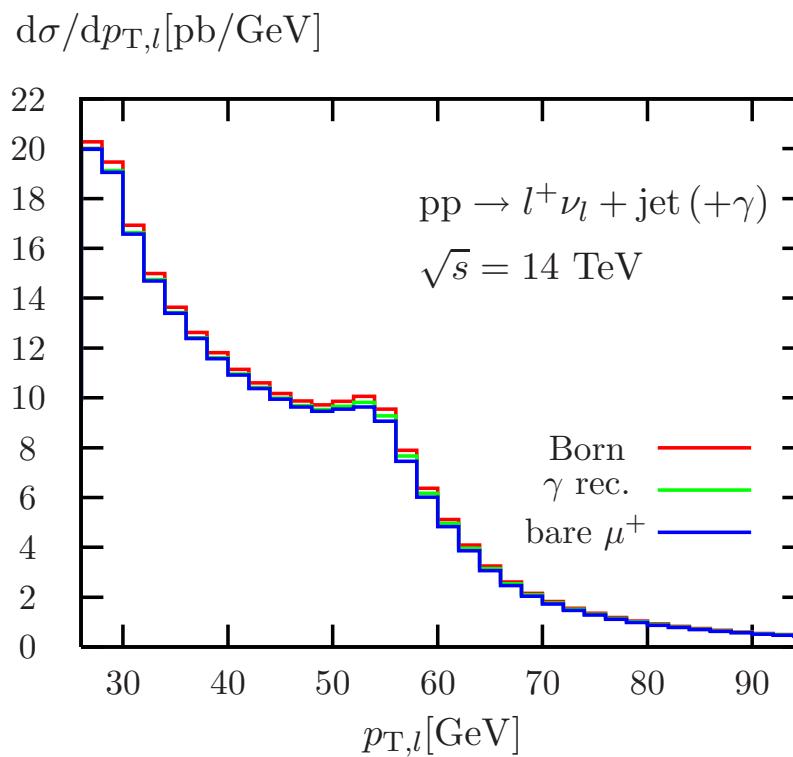
EW corrections

p_T distribution for the LHC:
(similar results for the Tevatron)



EW corrections

p_T distribution for the LHC:
(similar results for the Tevatron)



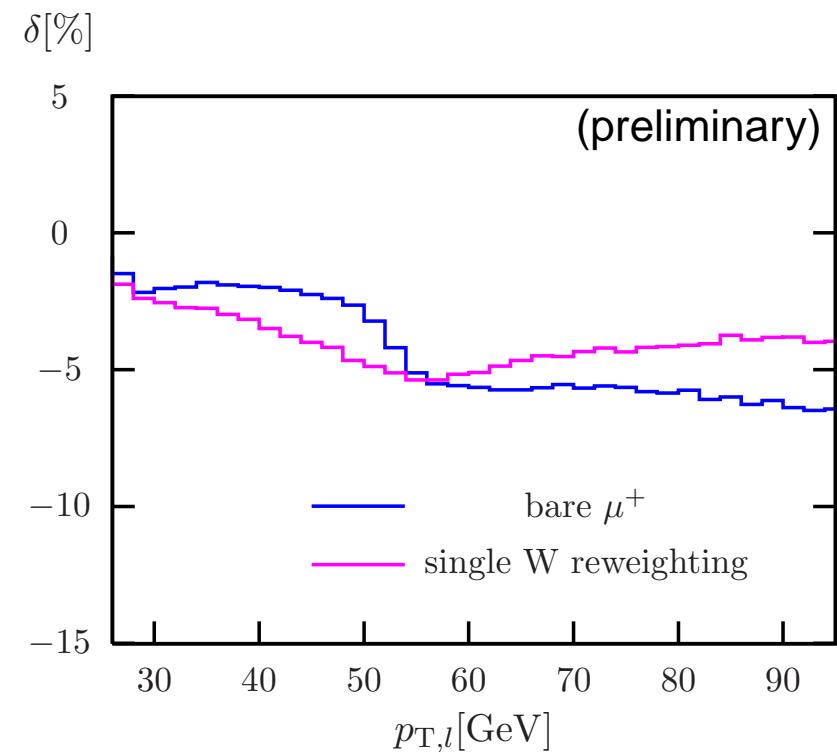
no similarity to single W production

single W vs. W+jet

p_T distribution for the LHC:

single W reweighting:

- boost W+jet event to W-boson **rest frame**
- reweight event with EW correction for single W in rest-frame $p_{T,l}$ bin

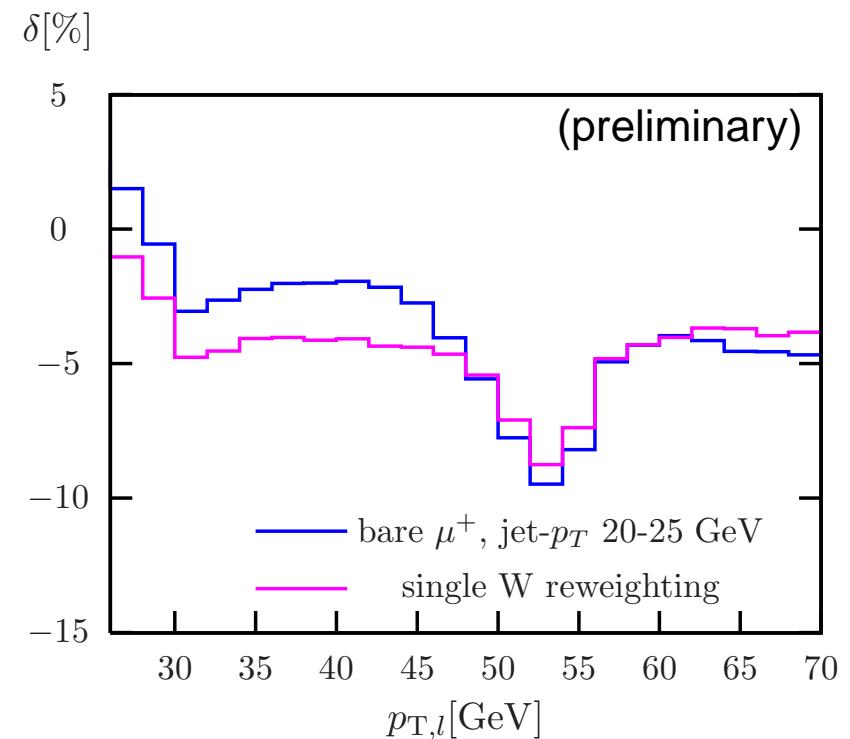


still big differences due to high- p_T jets

single W vs. W+jet

p_T distribution for the LHC:

- only look at jets with
 $p_{T,\text{jet}} = 20 - 25 \text{ GeV}$

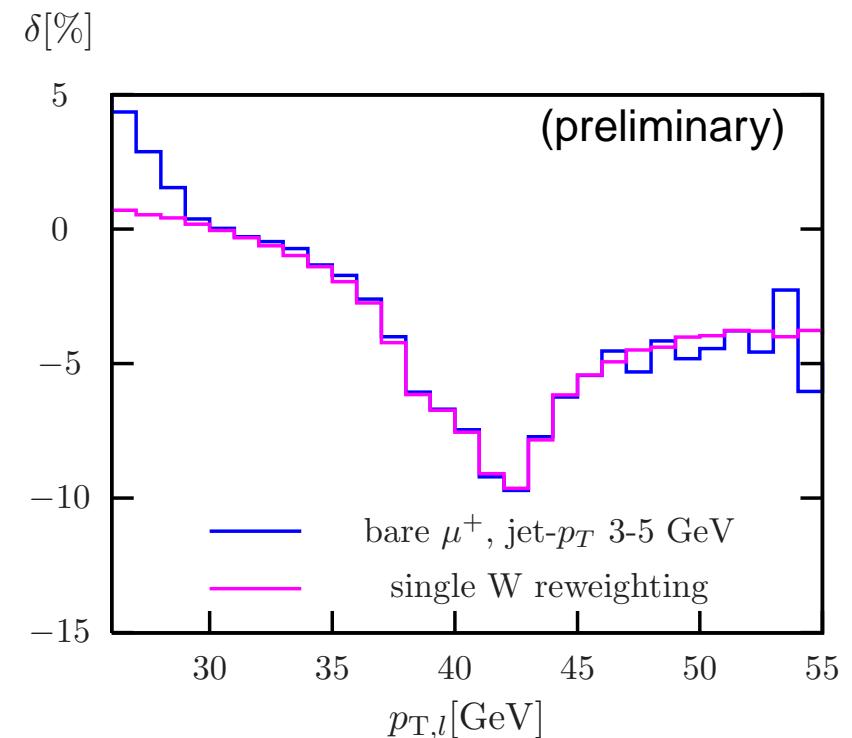


good but not perfect agreement

single W vs. W+jet

p_T distribution for the LHC:

- only look at jets with $p_{T,\text{jet}} = 3 - 5 \text{ GeV}$
- cross-section not reliably predicted in this region
- one can still estimate the EW corrections for the limited kinematical region



very good agreement