

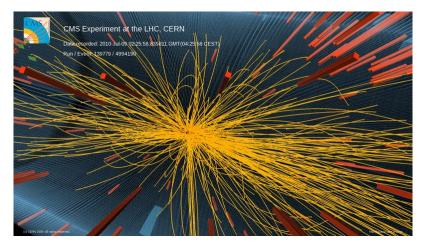
Modelling of minimum bias and underlying events

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IPMU-YITP Workshop, Kyoto, 9 September 2011

Event topologies

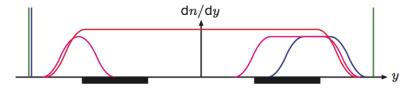


Expect and observe high multiplicities at the LHC. What are production mechanisms behind this?

What is minimum bias (MB)?

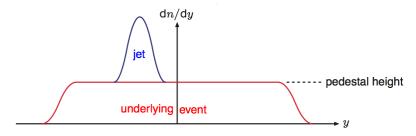
 $MB \approx$ "all events, with no bias from restricted trigger conditions" $\sigma_{tot} =$

 $\sigma_{\text{elastic}} + \sigma_{\text{single}-\text{diffractive}} + \sigma_{\text{double}-\text{diffractive}} + \dots + \sigma_{\text{non}-\text{diffractive}}$ Schematically:



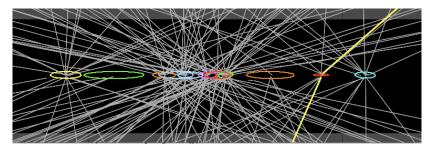
Reality: can only observe events with particles in central detector: no universally accepted, detector-independent definition $\sigma_{\rm min-bias} \approx \sigma_{\rm non-diffractive} + \sigma_{\rm double-diffractive} \approx 2/3 \times \sigma_{\rm tot}$

What is underlying event (UE)?



In an event containing a jet pair or another hard process, how much further activity is there, that does not have its origin in the hard process itself, but in other physics processes? Pedestal effect: the UE contains more activity than a normal MB event does (even discarding diffractive events). Trigger bias: a jet "trigger" criterion $E_{\perp jet} > E_{\perp min}$ is more easily fulfilled in events with upwards-fluctuating UE activity, since the UE E_{\perp} in the jet cone counts towards the $E_{\perp jet}$. Not enough!

What is pileup?

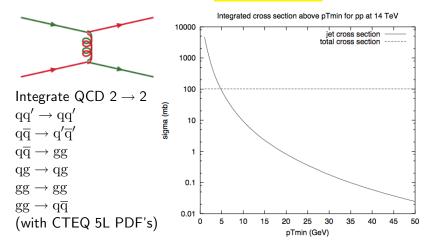


 $\langle n \rangle = \overline{\mathcal{L}} \, \sigma$

where $\overline{\mathcal{L}}$ is machine luminosity per bunch crossing, $\overline{\mathcal{L}} \sim n_1 n_2 / A$ and $\sigma \sim \sigma_{\text{tot}} \approx 100 \text{ mb.}$ Current LHC machine conditions $\Rightarrow \langle n \rangle$ approaching 10. Pileup introduces no new physics, and is thus not further considered here, but can be a nuisance. However, keep in mind concept of bunches of hadrons leading to multiple collisions.

The divergence of the QCD cross section

Cross section for $2 \rightarrow 2$ interactions is dominated by *t*-channel gluon exchange, so diverges like $d\hat{\sigma}/dp_{\perp}^2 \approx 1/p_{\perp}^4$ for $p_{\perp} \rightarrow 0$.



What is multiple partonic interactions (MPI)?

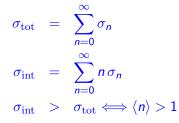
Note that $\sigma_{int}(p_{\perp min})$, the number of $(2 \rightarrow 2 \text{ QCD})$ interactions above $p_{\perp \min}$, involves integral over PDFs.

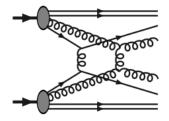
$$\sigma_{\rm int}(\boldsymbol{p}_{\perp\rm min}) = \iiint_{\boldsymbol{p}_{\perp\rm min}} \mathrm{d}x_1 \, \mathrm{d}x_2 \, \mathrm{d}\boldsymbol{p}_{\perp}^2 \, f_1(x_1, \boldsymbol{p}_{\perp}^2) \, f_2(x_2, \boldsymbol{p}_{\perp}^2) \, \frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}\boldsymbol{p}_{\perp}^2}$$

with $\int dx f(x, p_{\perp}^2) = \infty$, i.e. infinitely many partons.

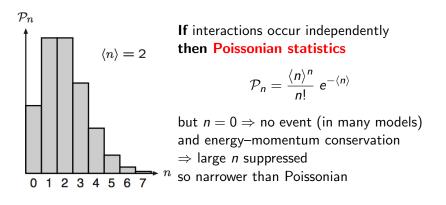
So half a solution to $\sigma_{int}(p_{\perp min}) > \sigma_{tot}$ is

many interactions per event: MPI (historically MI or MPPI)





Poissonian statistics



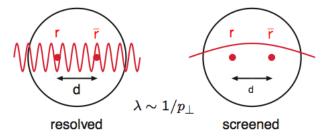
MPI is a logical consequence of the composite nature of protons, $n_{\text{parton}} \sim \sum_{q,\overline{q},g} \int f(x) \, dx > 3$, which allows $\sigma_{\text{int}}(p_{\perp \min}) > \sigma_{\text{tot}}$, but what about the limit $p_{\perp \min} \rightarrow 0$?

Colour screening

Other half of solution is that perturbative QCD is not valid at small p_{\perp} since q, g are not asymptotic states (confinement!). Naively breakdown at

$$p_{\perp \min} \simeq \frac{\hbar}{r_{\rm p}} \approx \frac{0.2 \ {
m GeV} \cdot {
m fm}}{0.7 \ {
m fm}} \approx 0.3 \ {
m GeV} \simeq \Lambda_{
m QCD}$$

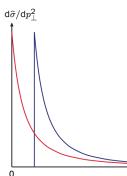
... but better replace r_p by (unknown) colour screening length d in hadron:



Regularization of low- p_{\perp} divergence

so need **nonperturbative regularization for** $p_{\perp} \rightarrow 0$, e.g.

$$\frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}p_{\perp}^2} \propto \frac{\alpha_{\mathrm{s}}^2(p_{\perp}^2)}{p_{\perp}^4} \rightarrow \frac{\alpha_{\mathrm{s}}^2(p_{\perp}^2)}{p_{\perp}^4} \theta\left(p_{\perp} - p_{\perp \mathrm{min}}\right) \quad \text{(simpler)}$$
or $\rightarrow \frac{\alpha_{\mathrm{s}}^2(p_{\perp 0}^2 + p_{\perp}^2)}{(p_{\perp 0}^2 + p_{\perp}^2)^2} \quad \text{(more physical)}$



where $p_{\perp \min}$ or $p_{\perp 0}$ are free parameters, empirically of order **2 GeV**.

Typically 2 – 3 interactions/event at the Tevatron, 4 – 5 at the LHC, but may be more in "interesting" high- p_{\perp} ones.

 p^2

Indirect evidence for multiple interactions -1

without MPI:

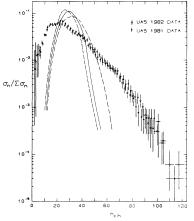


FIG. 3. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs simple models: dashed low p_T only, full including hard scatterings, dash-dotted also including initial- and final-state radiation.

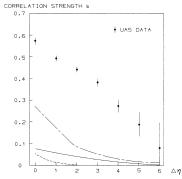


FIG. 4. Forward-backward multiplicity correlation at 540 GeV, UA5 results (Ref. 33) vs simple models; the latter models with notation as in Fig. 3.

with MPI included:

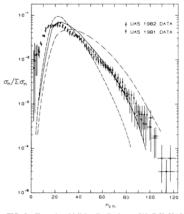


FIG. 5. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs impact-parameter-independent multipleinteraction model: dashed line, $p_{Tmin} = 1.0$ GeV; solid line, $p_{Tmin} = 1.6$ GeV; dashed-dotted line, $p_{Tmin} = 1.2$ GeV.

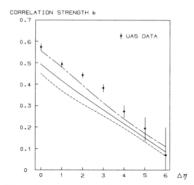


FIG. 6. Forward-backward multiplicity correlation at 540 GeV, UA5 results (Ref. 33) vs impact-parameter-independent multiple-interaction model; the latter with notation as in Fig. 5.

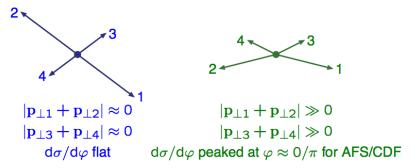
Direct observation of multiple interactions -1

Five pre-LHC studies: AFS (1987), UA2 (1991), CDF (1993, 1997), D0 (2009)

Order 4 jets $\mathbf{p}_{\perp 1} > \mathbf{p}_{\perp 2} > \mathbf{p}_{\perp 3} > \mathbf{p}_{\perp 4}$ and define φ as angle between $\mathbf{p}_{\perp 1} \mp \mathbf{p}_{\perp 2}$ and $\mathbf{p}_{\perp 3} \mp \mathbf{p}_{\perp 4}$ for AFS/CDF

Double Parton Scattering

Double BremsStrahlung



Direct observation of multiple interactions – 2

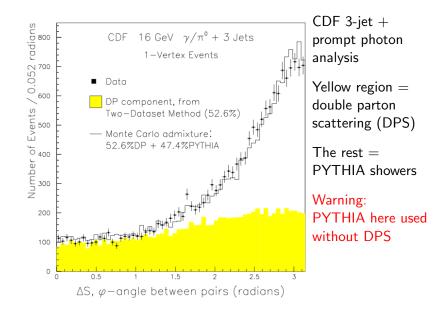
AFS 4-jet analysis (pp at 63 GeV; Copenhagen group): observe 6 times Poissonian prediction, with impact parameter expect 3.7 times Poissonian, but big errors \Rightarrow low acceptance, also UA2

CDF: 3-jet + prompt photon analysis (simplifies)

$$\sigma_{\rm DPS} = \frac{\sigma_A \sigma_B}{\sigma_{\rm eff}} \quad \text{for } A \neq B \implies \sigma_{\rm eff} = 14.5 \pm 1.7^{+1.7}_{-2.3} \text{ mb}$$

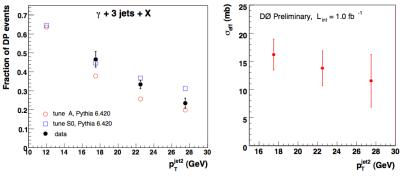
Note inverse relationship on $\sigma_{\rm eff}$. Natural scale is $\sigma_{\rm ND} \approx 40$ mb, so $\sigma_{\rm eff} \ll \sigma_{\rm ND}$ is strong enhancement relative to naive expectations! Consistent with (strongly) uneven matter distribution in proton.

Direct observation of multiple interactions - 3



Direct observation of multiple interactions - 4

D0 results:



 $\sigma_{\rm eff} = 15.1 \pm 1.9 \ {\rm mb}$

Agreement and precision "too good to be true"; tunes 8 and 4 years old, respectively, and not to this kind of data. More recent tunes have less matter fluctuations, i.e. higher $\sigma_{\rm eff}$, so likely to do worse.

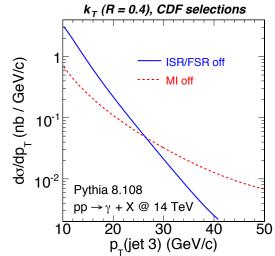
Torbjörn Sjöstrand

Same study also planned for LHC

Selection for DPS delicate balance:

showers dominate at large p_{\perp} \Rightarrow too large background

multiple interactions dominate at small p_{\perp} , but there jet identification difficult



All modern general-purpose generators are built on MPI concepts

but details differ, both physics and technology, e.g.

- a single regularized hard component or separate hard + soft components
- MPIs generated ordered in p_{\perp} or not
- energy/momentum/flavour conservation
- impact-parameter profile
- colour connection & reconnection strategies
- energy dependence
- . . .

In the following PYTHIA, Herwig++, Phojet; current Sherpa \approx PYTHIA; tomorrow future Sherpa

Reminder: the Sudakov form factor

A Poissonian process is one where "events" (e.g. radioactive decays) can occur uncorrelated in "time" t (or other ordering variable). If the probability for an "event" to occur at "time" t is P(t) then the probability for a *first* "event" after $t_0 = 0$ at t_1 is

$$\mathcal{P}(t_1) = \mathcal{P}(t_1) \exp\left(-\int_0^{t_1} \mathcal{P}(t) \,\mathrm{d}t\right)$$

and for an i'th at t_i is

$$\mathcal{P}(t_i) = \mathcal{P}(t_i) \exp\left(-\int_{t_{i-1}}^{t_i} \mathcal{P}(t) \, \mathrm{d}t\right)$$

Example: Sudakov form factor for parton showers, where increasing $t \rightarrow$ decreasing evolution variable Q and "event" \rightarrow parton branchings ... but relevant for MPIs as well ...

Basic generation of MPI - 1

- For now exclude diffractive (and elastic) topologies, i.e. only model nondiffractive events, with $\sigma_{\rm nd} \simeq 0.6 \times \sigma_{\rm tot}$
- Differential probability for interaction at p_{\perp} is

d P	_	1	$\mathrm{d}\sigma$
$\mathrm{d} \pmb{p}_{\perp}$	_	$\overline{\sigma_{ m nd}}$	$\overline{\mathrm{d} \pmb{p}_{\perp}}$

• Average number of interactions naively

$$\langle n
angle = rac{1}{\sigma_{
m nd}} \int_0^{E_{
m cm}/2} rac{{
m d}\sigma}{{
m d} p_\perp} \, {
m d} p_\perp$$

 Require ≥ 1 interaction in an event or else pass through without anything happening

$$P_{\geq 1} = 1 - P_0 = 1 - \exp(-\langle n \rangle)$$

(Alternatively: allow soft nonperturbative interactions even if no perturbative ones.)

Basic generation of MPI – 2

Can pick *n* from Poissonian and then generate *n* independent interactions according to $d\sigma/dp_{\perp}$ (so long as energy left), or better...

generate interactions in ordered sequence $p_{\perp 1} > p_{\perp 2} > p_{\perp 3} > \dots$

• Apply to ordered sequence of decreasing p_{\perp} , starting from $E_{\rm cm}/2$

$$\mathcal{P}(p_{\perp} = p_{\perp i}) = rac{1}{\sigma_{\mathrm{nd}}} rac{\mathrm{d}\sigma}{\mathrm{d}p_{\perp}} \exp\left[-\int_{p_{\perp}}^{p_{\perp}(i-1)} rac{1}{\sigma_{\mathrm{nd}}} rac{\mathrm{d}\sigma}{\mathrm{d}p'_{\perp}} \mathrm{d}p'_{\perp}
ight]$$

 Use rescaled PDF's taking into account already used momentum and flavours
 ⇒ n_{int} narrower than Poissonian

Impact parameter dependence – 1

So far assumed that all collisions have equivalent initial conditions, but hadrons are extended, e.g. empirical double Gaussian:

$$\rho_{\text{matter}}(r) = N_1 \exp\left(-\frac{r^2}{r_1^2}\right) + N_2 \exp\left(-\frac{r^2}{r_2^2}\right)$$

where $r_2 \neq r_1$ represents "hot spots", and overlap of hadrons during collision is

$$\mathcal{O}(b) = \int \mathrm{d}^3 \mathbf{x} \, \mathrm{d}t \;
ho_{1,\mathrm{matter}}^{\mathrm{boosted}}(\mathbf{x},t)
ho_{2,\mathrm{matter}}^{\mathrm{boosted}}(\mathbf{x},t)$$

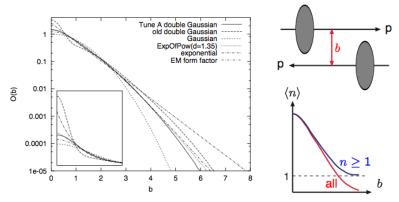
or electromagnetic form factor:

$$S_{
m p}(\mathbf{b}) = \int rac{{
m d}^2 \mathbf{k}}{2\pi} \, rac{\exp(i\mathbf{k}\cdot\mathbf{b})}{(1+\mathbf{k}^2/\mu^2)^2}$$

where $\mu = 0.71~{
m GeV}
ightarrow$ free parameter, which gives

$$\mathcal{O}(b) = \frac{\mu^2}{96\pi} \, (\mu b)^3 \, K_3(\mu b)$$

Impact parameter dependence – 2



• Events are distributed in impact parameter b

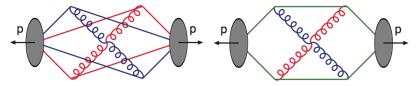
- Average activity at b proportional to $\mathcal{O}(b)$
 - \star central collisions more active $\Rightarrow \mathcal{P}_n$ broader than Poissonian
 - \star peripheral passages normally give no collisions \Rightarrow finite $\sigma_{
 m tot}$
- Also crucial for *pedestal effect* (more later)

(1) Colour connections:

Each interaction hooks up with colours from beam remnants, but how does the colours in the remnant hook up with each other?

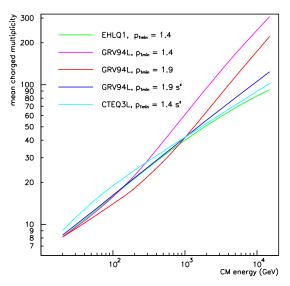
(2) Colour reconnections:

Many interaction "on top of" each other \Rightarrow tightly packed partons! Is there a strict colour memory when partons recede?



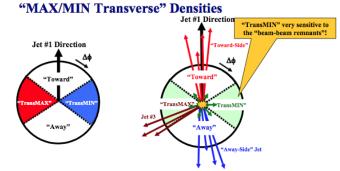
Recall: $N_C = 3$, not $N_C = \infty$!

Energy dependence of $p_{\perp \min}$ and $p_{\perp 0}$



Larger collision energy \Rightarrow probe parton (\approx gluon) density at smaller x \Rightarrow smaller colour screening length d \Rightarrow larger $p_{\perp \min}$ or $p_{\perp 0}$ \Rightarrow dampened multiplicity rise

Events with hard scale have more underlying activity! Trigger bias: hard scale ⇒ central collision ⇒ large UE. Studied in particular by Rick Field, comparing with CDF data: http://www.phys.ufl.edu/~rfield/cdf/rdf_talks.html)



• Define the MAX and MIN "transverse" regions on an event-by-event basis with MAX (MIN) having the largest (smallest) density.

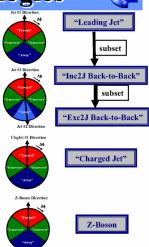
Jet pedestal effect - 2





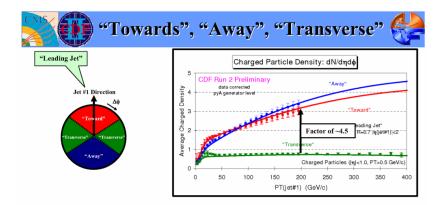
Event Topologies

- "Leading Jet" events correspond to the leading calorimeter jet (MidPoint R = 0.7) in the region |η| < 2 with no other conditions.
- → "Inclusive 2-Jet Back-to-Back" events are selected to have at least two jets with Jet#1 and Jet#2 nearly "backto-back" ($\Delta \phi_{12} > 150^{\circ}$) with almost equal transverse energies (P_T (jet#2)/ P_T (jet#1) > 0.8) with no other conditions.
- ⇒ "Exclusive 2-Jet Back-to-Back" events are selected to have at least two jets with Jet#1 and Jet#2 nearly "backto-back" ($\Delta \phi_{12} > 150^{\circ}$) with almost equal transverse energies (P_T (jet#2)/ P_T (jet#1) > 0.8) and P_T (jet#3) < 15 GeV/c.
- "Leading ChgJet" events correspond to the leading charged particle jet (R = 0.7) in the region |η| < 1 with no other conditions.
- "Z-Boson" events are Drell-Yan events with 70 < M(lepton-pair) < 110 GeV with no other conditions.



Jet pedestal effect – 3

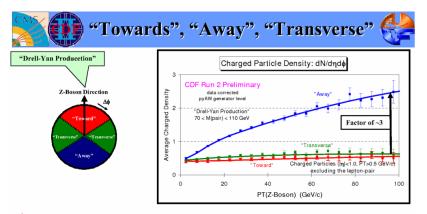
(Rick Field)



Data at 1.96 TeV on the density of charged particles, dN/dŋdø, with p_T > 0.5 GeV/c and |η| < 1 for "leading jet" events as a function of the leading jet p_T for the "toward", "away", and "transverse" regions. The data are corrected to the particle level (with errors that include both the statistical error and the systematic uncertainty) and are compared with PYTHIA Tune A at the particle level (i.e. generator level).

Jet pedestal effect - 4

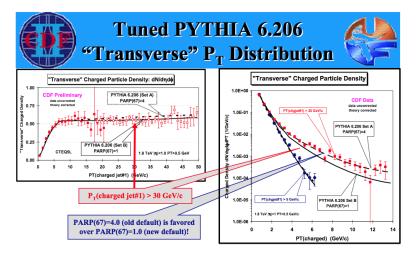
(Rick Field)



Data at 1.96 TeV on the density of charged particles, dN/dndø, with p_T > 0.5 GeV/c and |n| < 1 for "Z-Boson" events as a function of the leading jet p_T for the "toward", "away", and "transverse" regions. The data are corrected to the particle level (with errors that include both the statistical error and the systematic uncertainty) and are compared with PYTHIA Tune AW at the particle level (*i.e.* generator level).



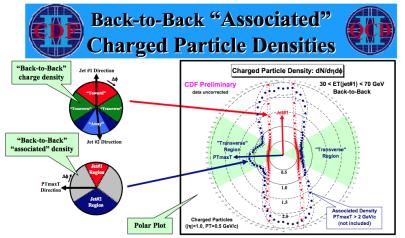
(Rick Field)



Compares the average "transverse" charge particle density ($|\eta| < 1$, $P_T > 0.5$ GeV) versus P_T (charged jet#1) and the P_T distribution of the "transverse" density, $dN_{chg}/d\eta d\phi dP_T$ with the QCD Monte-Carlo predictions of two tuned versions of PYTHIA 6.206 (P_T (hard) > 0, CTEQ5L, Set B (PARP(67)=1) and Set A (PARP(67)=4)).

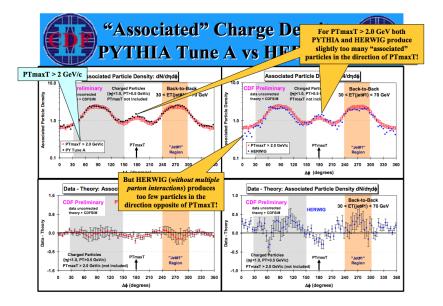
Jet pedestal effect - 6

(Rick Field)



Shows the Δφ dependence of the "associated" charged particle density, dN_{chg}/dηdφ, p_T > 0.5 GeV/c, |η| < 1, PTmaxT > 2.0 GeV/c (*not including PTmaxT*) relative to PTmaxT (rotated to 180°) and the charged particle density, dN_{chg}/dηdφ, p_T > 0.5 GeV/c, |η| < 1, relative to jet#1 (rotated to 270°) for "back-to-back events" with 30 < E_T(jet#1) < 70 GeV.</p>

(Rick Field)



Has gradually evolved from the MPI start in 1985; still older versions in use.

Current version involves (among others):

- MPI ordered in p_{\perp} , and also
- transverse-momentum-ordered parton showers for ISR and FSR.

Allows interleaved evolution for MPI, ISR and FSR:

$$\begin{array}{ll} \frac{\mathrm{d}\mathcal{P}}{\mathrm{d}p_{\perp}} & = & \left(\frac{\mathrm{d}\mathcal{P}_{\mathrm{MPI}}}{\mathrm{d}p_{\perp}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathrm{ISR}}}{\mathrm{d}p_{\perp}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathrm{FSR}}}{\mathrm{d}p_{\perp}}\right) \\ & \times & \exp\left(-\int_{p_{\perp}}^{p_{\perp}\max} \left(\frac{\mathrm{d}\mathcal{P}_{\mathrm{MPI}}}{\mathrm{d}p'_{\perp}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathrm{ISR}}}{\mathrm{d}p'_{\perp}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathrm{FSR}}}{\mathrm{d}p'_{\perp}}\right) \mathrm{d}p'_{\perp}\right) \end{array}$$

ordered in decreasing p_{\perp} using "Sudakov" trick.

Corresponds to increasing "resolution" of partonic final state: smaller p_{\perp} fill in details of the basic picture set at larger p_{\perp} .

PYTHIA implementation – 2

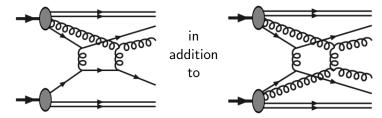
Other aspects in line with previous discussions:

- smooth dampening $d\hat{\sigma}/dp_{\perp}^2 \propto 1/(p_{\perp 0}^2 + p_{\perp}^2)^2$ \Rightarrow all interactions belong to same "hard" kind
- energy-dependent $p_{\perp 0}$

$$egin{split}
olimits
ho_{ot 0}(E_{
m cm}) &=
olimits
ho_{ot 0}(E_{
m cm,ref}) \, \left(rac{E_{
m cm}}{E_{
m cm,ref}}
ight)^k \end{split}$$

- matter profile flexible, Gaussian or more spiked
- PDF rescaling for energy/momentum/flavour conservation
- colour connection/reconnection important component
- drift of baryon number by junction topology

• Rescattering (optional since 2009)



Same order in α_s , \sim same propagators, but one PDF weight less \Rightarrow smaller σ , and one jet less $\Rightarrow 2 \rightarrow 3$ QCD radiation background larger • An x-dependent proton size (optional since 2011)

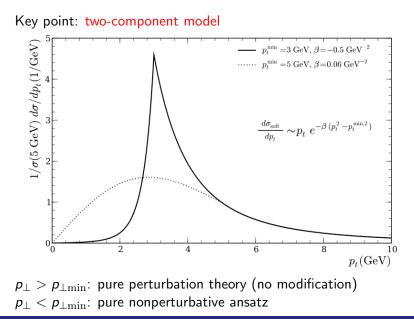
$$\rho(r, x) \propto \frac{1}{a^3(x)} \exp\left(-\frac{r^2}{a^2(x)}\right) \text{ with } a(x) = a_0 \left(1 + a_1 \ln \frac{1}{x}\right)$$

 $a_1 \approx 0.15 \text{ tuned to rise of } \sigma_{\text{ND}}$
 $a_0 \text{ tuned to value of } \sigma_{\text{ND}}, \text{ given PDF, } p_{\perp 0}, \dots$

Old non-MPI Soft Underlying Event thoroughly killed. Jimmy add-on to HERWIG does UE, but not MB.

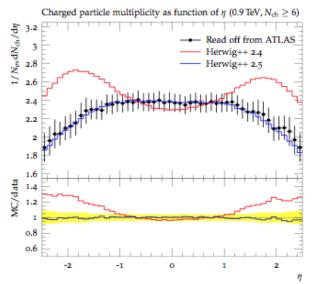
- \Rightarrow Herwig++ first complete alternative:
 - number of interactions first picked; thereafter generated unordered in p_⊥
 - interactions uncorrelated, up until energy used up
 - force ISR to reconstruct back to gluon after first interaction
 - impact parameter by electromagnetic form factor shape, but with tunable width (\sim factor 3 different from em width)
 - $p_{\perp \min}$ scale to be tuned energy-by-energy

Herwig++ implementation -2



Herwig++ implementation -3

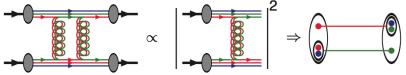
Colour reconnection essential to get $dn/d\eta$ correct:



PhoJet (& relatives) implementation

(1) Cut Pomeron (1982)

- \bullet Pomeron predates QCD; nowadays \sim glueball tower
- Optical theorem relates σ_{total} and $\sigma_{\mathrm{elastic}}$



- Unified framework of nondiffractive and diffractive interactions
- Purely low- p_{\perp} : only primordial k_{\perp} fluctuations
- Usually simple Gaussian matter distribution

(2) Extension to large p_{\perp} (1990)

• distinguish soft and hard Pomerons:

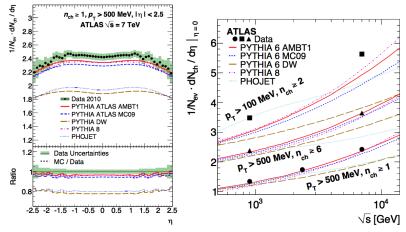
soft = nonperturbative, low- p_{\perp} , as above

hard = perturbative, "high" - p_{\perp}

• hard based on PYTHIA code, with lower cutoff in p_{\perp}

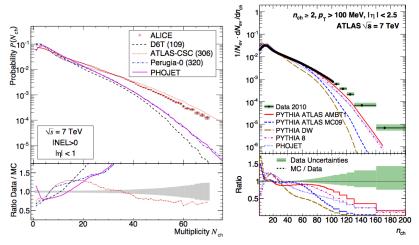
LHC outcome – 1

First/most LHC comparisons to old versions of generators, e.g.:



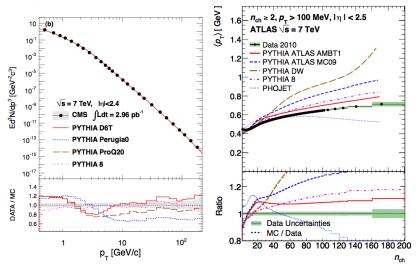
LHC outcome – 2

First/most LHC comparisons to old versions of generators, e.g.:



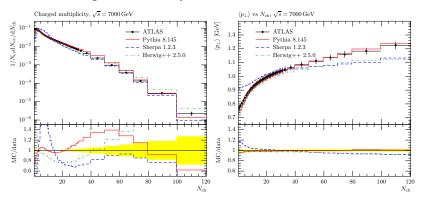
LHC outcome - 3

First/most LHC comparisons to old versions of generators, e.g.:



LHC outcome - 4

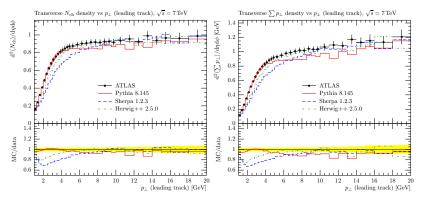
State of new generators early 2011:



A. Buckley et al., Phys. Rep. 504 (2011) 145 [arXiv:1101.2599[hep-ph]]

LHC outcome - 5

State of new generators early 2011:



A. Buckley et al., Phys. Rep. 504 (2011) 145 [arXiv:1101.2599[hep-ph]]

Summary

- MPI concept compelling; it has to exist at some level
- By now, strong direct evidence, overwhelming indirect
- Understanding of MPI crucial for LHC precision physics
- Many details uncertain:
 - \star physics and form of $p_{\perp \min}/p_{\perp 0}$ regularization
 - \star non-factorized impact parameter picture
 - * multiparton densities in incoming hadron
 - \star colour correlations between interactions
 - \star energy dependence \Rightarrow predictivity
 - * dense-packing of partons and hadrons \Rightarrow collective effects? * diffraction, forward physics, ...
- Above physics aspects must all be present, and more? If a model is simple, it is wrong!
- So stay tuned for ever more complicated models in the future!